

BESIII上粲介子含轻衰变的研究

马海龙 (高能所)



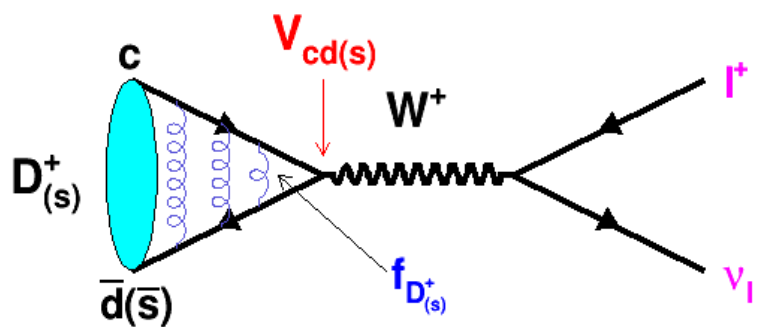
第四届中国格点量子色动力学会议，湖南省长沙市，
2024年10月11-15日

主要内容

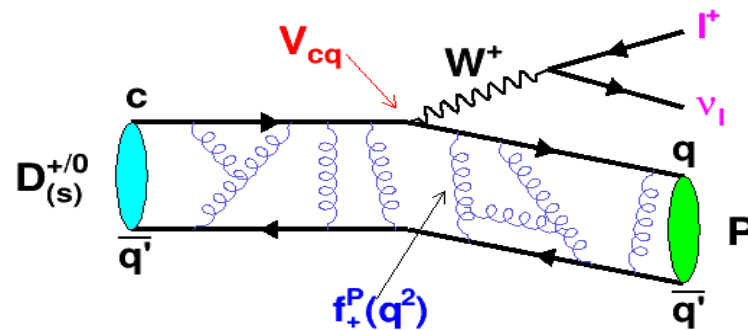
- 物理动机
- 数据样本
- 粲介子纯轻衰变研究
- 粲介子半轻衰变研究
- 总结

(Semi)leptonic D decays

探讨夸克和轻子相互作用的理想桥梁，检验标准模型的理想探针之一



$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_l^2 m_{D_{(s)}^+} \left(1 - \frac{m_l^2}{m_{D_{(s)}^+}^2}\right)^2$$



$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

- 衰变常数、半轻衰变形状因子
- CKM矩阵元 $|V_{cs}|$ 、 $|V_{cd}|$
- 分支比之比 $B_{\mu/e}$ 、 $B_{\tau/\mu}$
- 稀有含轻衰变

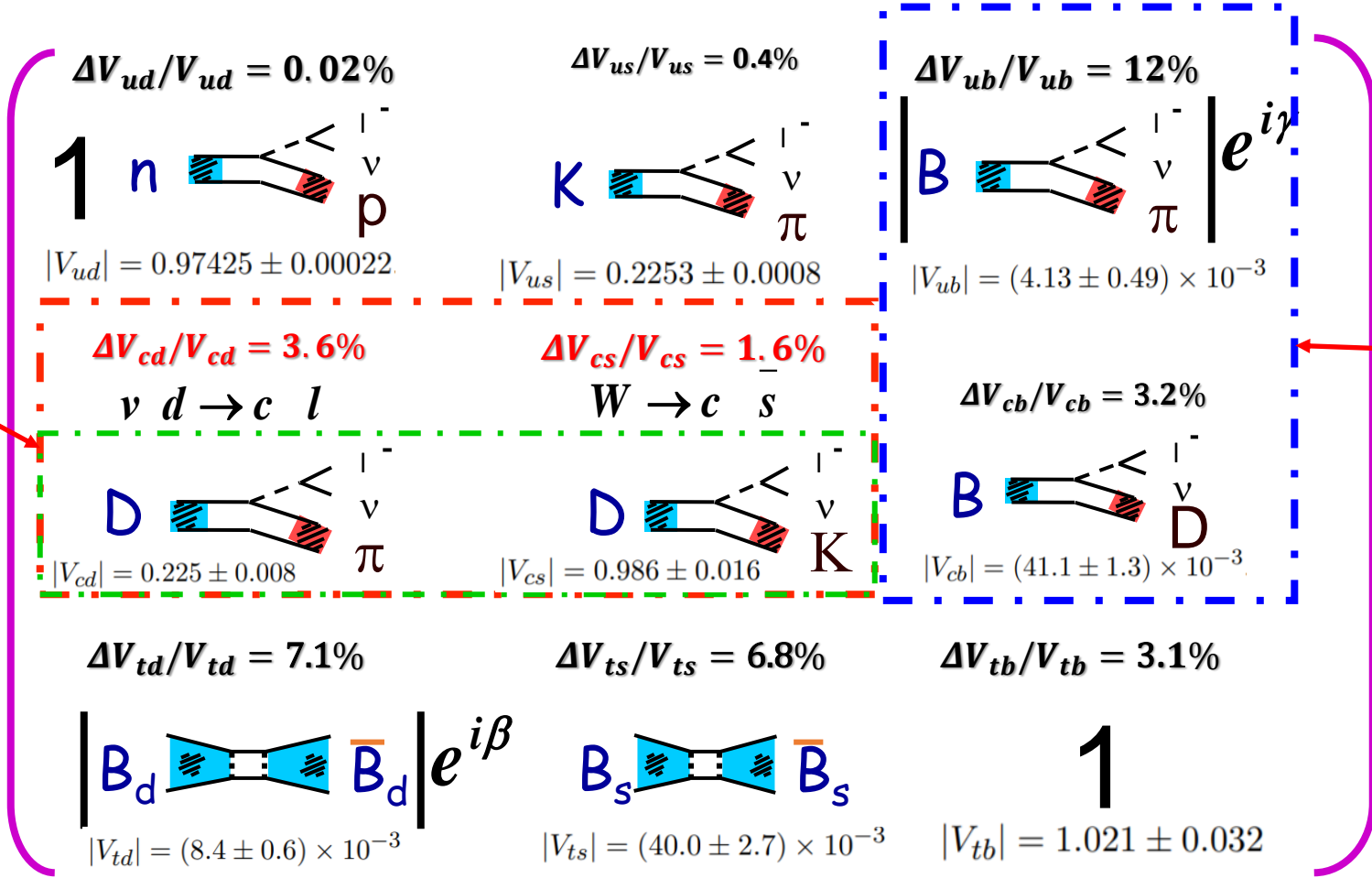
- 精密刻度格点QCD等计算
- 在更高精度下检验CKM矩阵的么正性
- 精确检验轻子普适性
- 寻找超出标准模型的新物理效应

BESIII之前 $|V_{cs(d)}|$ 的测量状态

PDG2014

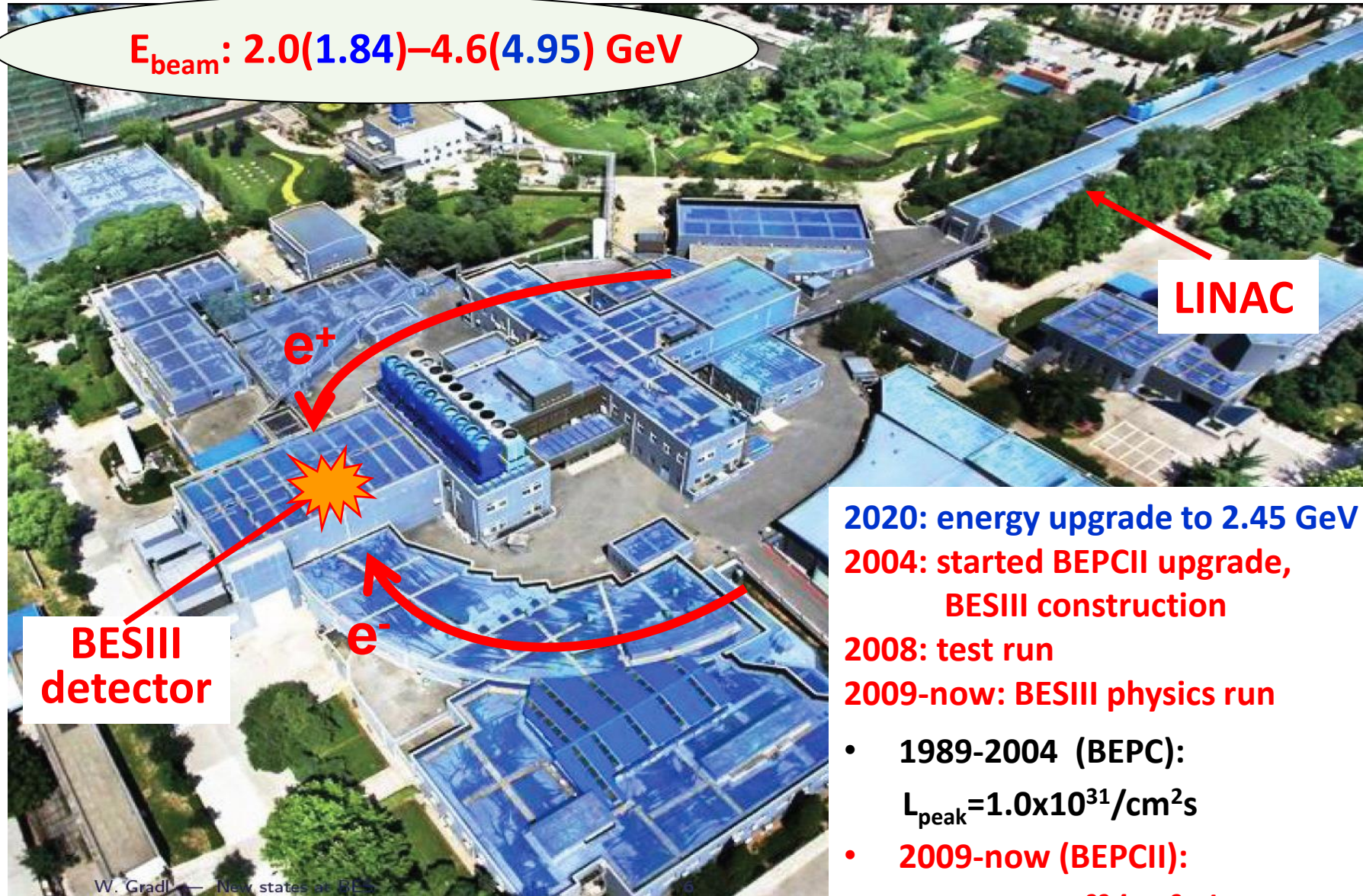
Direct measurement: (semi)leptonic c D decays

Indirect constraint: Hadronic D decays



V_{ud} , V_{us} and V_{cb} are the best determined due to flavor symmetries: I, SU(3), HQS. Charm (V_{cd} & V_{cs}) and rest of the beauty sector (V_{ub} , V_{td} , V_{ts}) are poorly determined. Theoretical errors on hadronic matrix element dominate.

北京正负电子对接机II (BEPCII)



$E_{\text{beam}}: 2.0(1.84) - 4.6(4.95) \text{ GeV}$

LINAC

BESIII
detector

2020: energy upgrade to 2.45 GeV

2004: started BEPCII upgrade,
BESIII construction

2008: test run

2009-now: BESIII physics run

- 1989-2004 (BEPC):

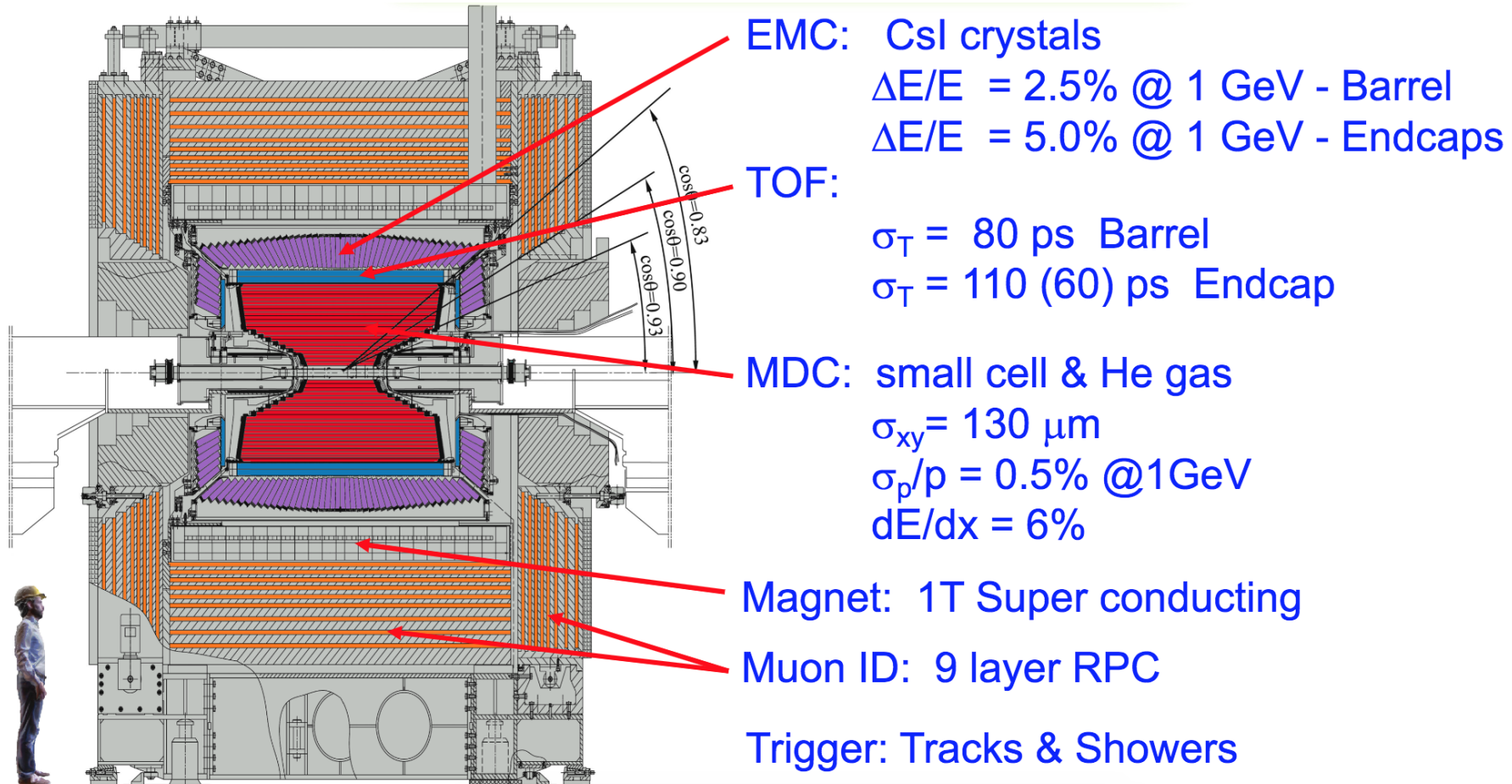
$$L_{\text{peak}} = 1.0 \times 10^{31} / \text{cm}^2 \text{s}$$

- 2009-now (BEPCII):

$$L_{\text{peak}} = 1.1 \times 10^{33} / \text{cm}^2 \text{s} \text{ (2022, 2023)}$$

北京谱仪III (BESIII)

NIMA614(2010)345



Excellent resolution, particle identification, and large coverage
for neutral and charged particles

BESII国际合作组

Europe (18)

Germany(6): Bochum University, GSI Darmstadt, Helmholtz Institute Mainz, Johannes Gutenberg University of Mainz, Universitaet Giessen, University of Münster
Italy(3): Ferrara University, INFN, University of Turin,
Netherlands(1): KVI/University of Groningen
Russia(2): Budker Institute of Nuclear Physics, Dubna JINR
Sweden(1): Uppsala University
Turkey (1): Turkish Accelerator Center Particle Factory Group
UK(3): University of Manchester, University of Oxford, University of Bristol
Poland(1): National Centre for Nuclear Research

Pakistan(2)
COMSATS Institute of Information Technology
University of the Punjab
India(1)
Indian Institute of Technology madras

China (54)

Beihang University, Central China Normal University, Central South University, China Center of Advanced Science and Technology, China University of Geosciences, Fudan University, Guangxi Normal University, Guangxi University, Hangzhou Normal University, Hebei University, Henan University, Henan Normal University, Henan University of Science and Technology, Henan University of Technology, Huangshan College, Hunan University, Hunan Normal University, Inner Mongolia University, Institute of High Energy Physics, Institute of Modern Physics, Jilin University, Lanzhou University, Liaoning Normal University, Liaoning University, Nanjing Normal University, Nanjing University, Nankai University, North China Electric Power University, Peking University, Qufu Normal University, Renmin University of China, Shanxi University, Shanxi Normal University, Sichuan University, Shandong Normal University, Shandong University, Shandong University of Technology, Shanghai Jiao Tong University, Soochow University, South China Normal University, Southeast University, Sun Yat-sen University, Tsinghua University, University of Chinese Academy of Sciences, University of Jinan, University of Science and Technology of China, University of Science and Technology Liaoning, University of South China, Wuhan University, Xinyang Normal University, Yantai University, Yunnan University, Zhejiang University, Zhengzhou University

Mongolia(1)

Institute of Physics and Technology

Korea(1)

Chung-Ang University

Thailand(1)

Suranaree University of Technology

USA(3)

Carnegie Mellon University
Indiana University
University of Hawaii

Chile(1)

University of Tarapaca

> 600 members

From 82 institutions

in 16 countries

- 1 RUSSIA
- 2 LUXEMBOURG
- 3 LIECHTENSTEIN
- 4 SWITZERLAND
- 5 AUSTRIA
- 6 SLOVAKIA
- 7 SLOVENIA
- 8 CROATIA
- 9 MONTENEGRO
- 10 SAN MARINO
- 11 BOSNIA AND HERZEGOVINA
- 12 SERBIA
- 13 MONTENEGRO
- 14 ANDORRA
- 15 VATICAN CITY
- 16 MALTA
- 17 NORTH MACEDONIA
- 18 MOLDOVA
- 19 ROMANIA
- 20 POLAND
- 21 HUNGARY
- 22 CZECH REPUBLIC
- 23 SLOVAKIA
- 24 SLOVENIA
- 25 UNITED ARAB EMIRATES
- 26 INDIA
- 27 KENYA

Data samples at BESIII

- 2009: 106M $\psi(3686)$
225M J/ψ
- 2010: 0.98 fb⁻¹ $\psi(3770)$
- 2011: 2.93 fb⁻¹ $\psi(3770)$ ($D^{0(+)}$), total
0.48 fb⁻¹ @4.01 GeV
- 2012: 0.45B $\psi(3686)$ (total)
1.30B J/ψ (total)
- 2013: 1.09 fb⁻¹ @4.23 GeV (XYZ& D_s^+)
0.83 fb⁻¹ @4.26 GeV
0.54 fb⁻¹ @4.36 GeV
10×0.05 fb⁻¹ XYZ scan@3.81-4.42 GeV
- 2014: 1.03 fb⁻¹ @4.42 GeV
0.11 fb⁻¹ @4.47 GeV
0.11 fb⁻¹ @4.53 GeV
0.05 fb⁻¹ @4.575 GeV
0.57 fb⁻¹ @4.60 GeV (XYZ& Λ_c^+)
0.80 fb⁻¹ R scan @3.85-4.59 GeV
- 2009: 106M $\psi(3686)$
- 2015: R-scan 2-3 GeV+2.175 GeV
- 2016: 3.20 fb⁻¹ @4.178 GeV (XYZ& D_s^+)
- 2017: 7×0.50 fb⁻¹ @4.19-4.22 GeV (XYZ& D_s^+),
@4.24-4.27 (XYZ)
- 2018: More J/ψ +tuning new RF cavity
- 2019: 10B J/ψ (total)
8×0.50 fb⁻¹ XYZ scan@4.13, 4.16 (XYZ& D_s^+),
4.29-4.44 GeV
- 2020: 3.8 fb⁻¹ @ 4.61-4.7 GeV (XYZ& Λ_c^+)
- 2021: 2.0 fb⁻¹ @ 4.74-4.946 GeV
2.7B $\psi(3686)$ (total)
- 2022:** 0.4 fb⁻¹ @3.650 GeV
0.4 fb⁻¹ @3.682 GeV
2.9→7.9 fb⁻¹ $\psi(3770)$ ($D^{0(+)}$), total)
- 2023-2024: 7.9→20.3 fb⁻¹ $\psi(3770)$ (for $D^{0(+)}$), total)
2×0.42 fb⁻¹ $\psi(3770)$ scan
0.14 fb⁻¹ @3.800-3.885 GeV
0.13 fb⁻¹ @3.554 GeV
0.025 fb⁻¹ @1.84-2.00 GeV

>50 fb⁻¹ at E_{cm} between 1.84 and 4.95 GeV in 15 year running

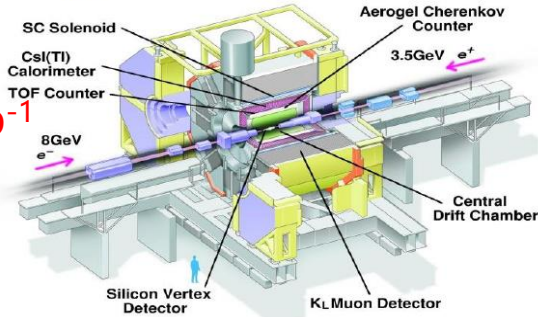
近年来开展粲强子研究的实验

Belle @ KEKB



$e^+e^- : \sim 10.6 \text{ GeV } (\Upsilon(4S))$
 $\sigma(e^+e^- \rightarrow cc) = 1.3 \text{ nb}$
 $L_{\text{peak}} = 2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

0.98 ab^{-1}

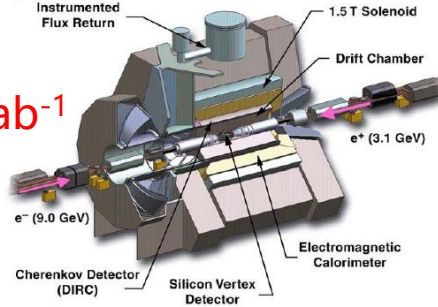


BaBar @ PEP-II

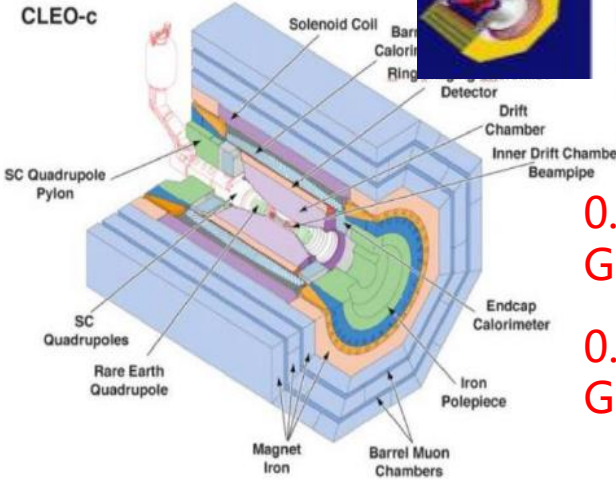


$e^+e^- : \sim 10.6 \text{ GeV } (\Upsilon(4S))$
 $\sigma(e^+e^- \rightarrow cc) = 1.3 \text{ nb}$
 $L_{\text{peak}} = 1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

0.54 ab^{-1}



CLEO-c



0.8 fb^{-1} @ 3.774 GeV

0.6 fb^{-1} @ 4.170 GeV

BESIII @ BEPC II



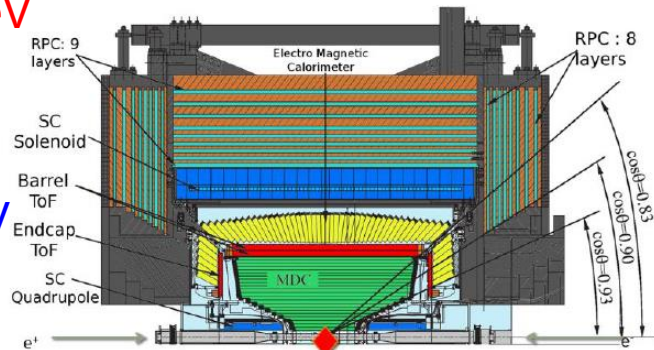
$e^+e^- : 2-4.6 \text{ GeV}$
 $\sigma(e^+e^- \rightarrow cc) = 3 \text{ nb}$
 $L_{\text{peak}} = 1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

2.9 → 20.3 fb^{-1} @ 3.773 GeV

7.33 fb^{-1} @ 4.13-4.23 GeV

4.50 fb^{-1} @ 4.6-4.7 GeV

10.6 fb^{-1} @ 4.23-4.7 GeV

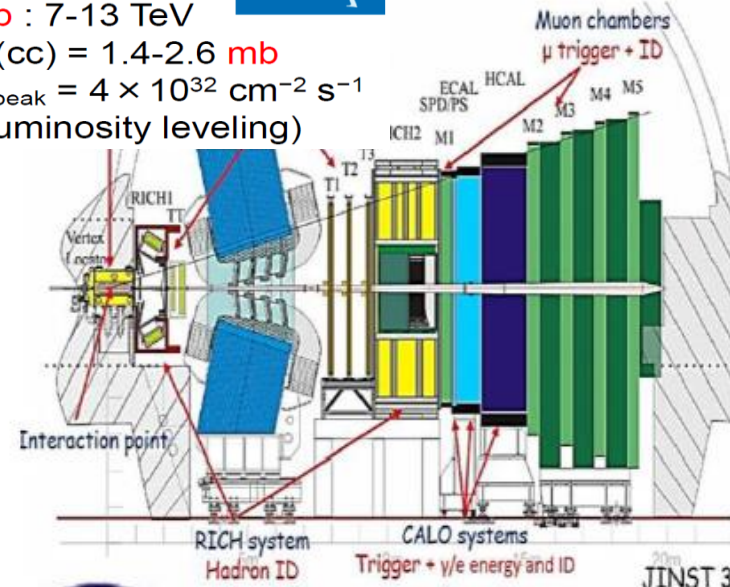


LHCb @ LHC

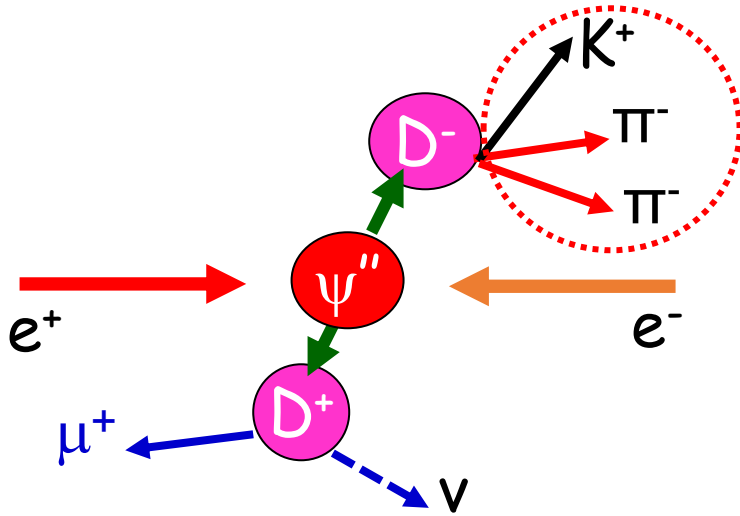


$pp : 7-13 \text{ TeV}$
 $\sigma(cc) = 1.4-2.6 \text{ mb}$
 $L_{\text{peak}} = 4 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
 (luminosity leveling)

9 fb^{-1}



The world largest threshold charmed hadrons at BESIII



Produced in pair \rightarrow Double tag method
 Low background \rightarrow low systematic uncertainties
 Quantum correlation for $\psi(3770) \rightarrow D^0\bar{D}^0$ pairs

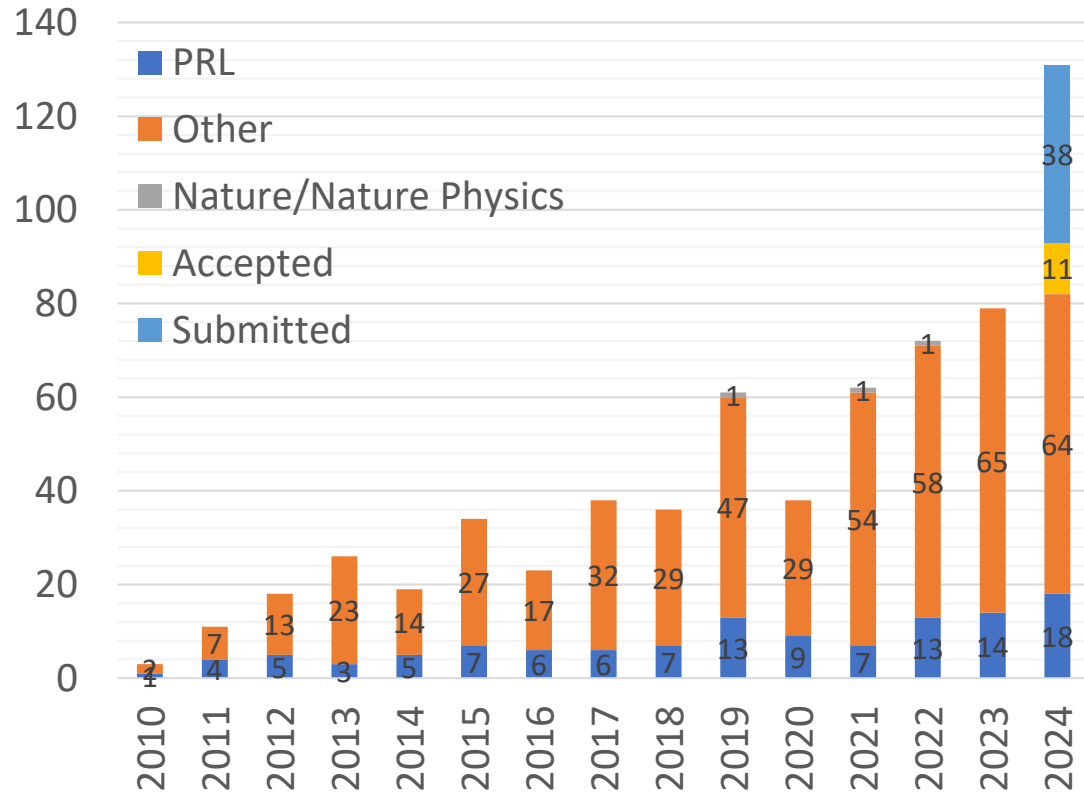
Yields of Singly Tagged (ST) charmed hadrons

E_{cm} (GeV)	Data taking year	L (fb^{-1})	ST D^0 yield	ST D^+ Yield	ST D_s^+ yield	ST Λ_c^+ yield
3.773	2010-11 (\rightarrow 2022-24)	2.93 \rightarrow 20.3	2.7M ($\sim 7\times$)	1.7M ($\sim 7\times$)		
4.009	2011	0.48			13K	
4.13-4.23	2016,2017,2012,2019	7.33			0.8M	
4.6-4.7	2014, 2020	4.5				0.12M

Total yields of various charmed hadrons at BESIII are lower than Belle and LHCb by 2-3 orders. However, BESIII, Belle and LHCb have complimentary advantages in various charm physics

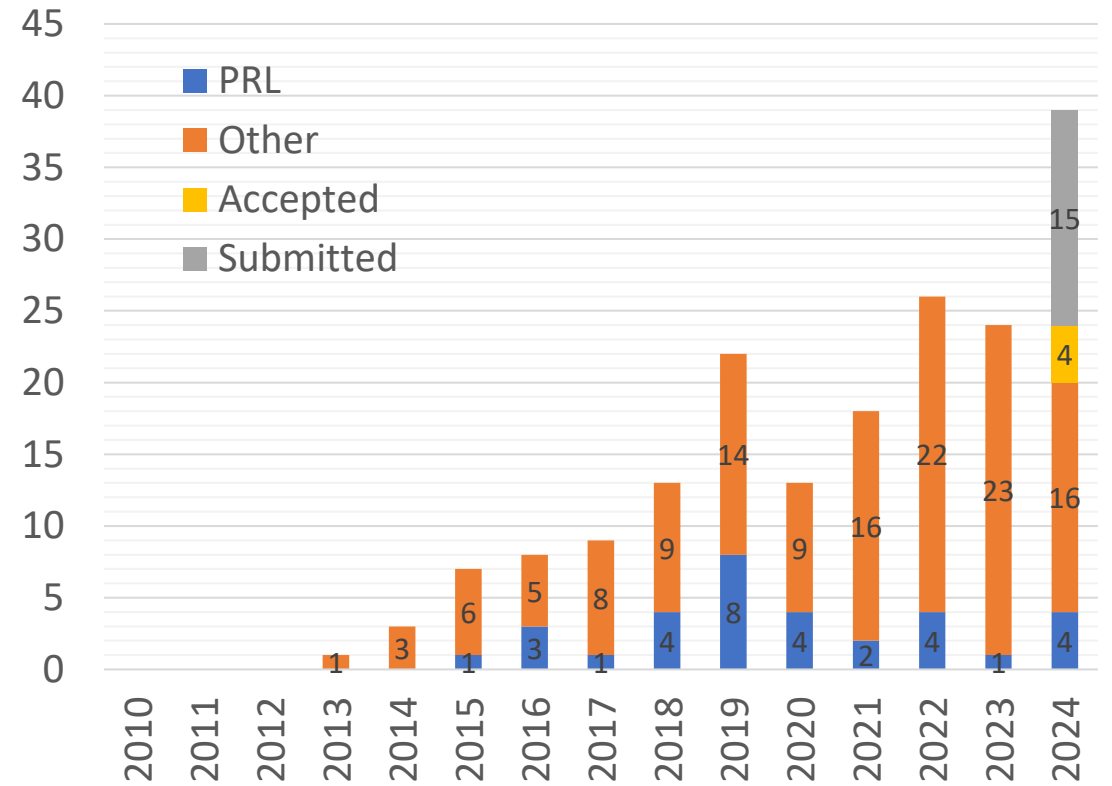
Publications of BESIII

BESIII physics



602 papers and 121 in PRL

Charm physics at BESIII



164 papers and 32 in PRL

粲介子含轻衰变: > 50篇文章 (15篇PRL)

粲介子纯轻衰变

Studies of $D^+ \rightarrow l^+ \nu_l$

PRD89(2014)051104

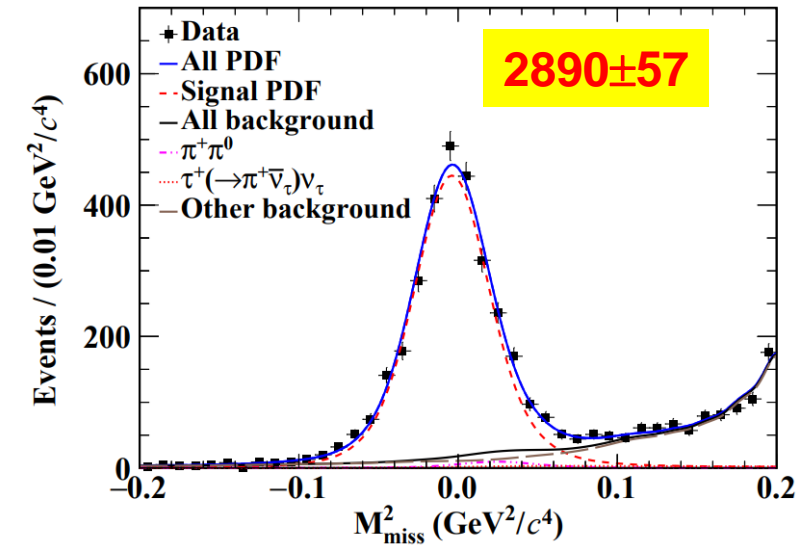
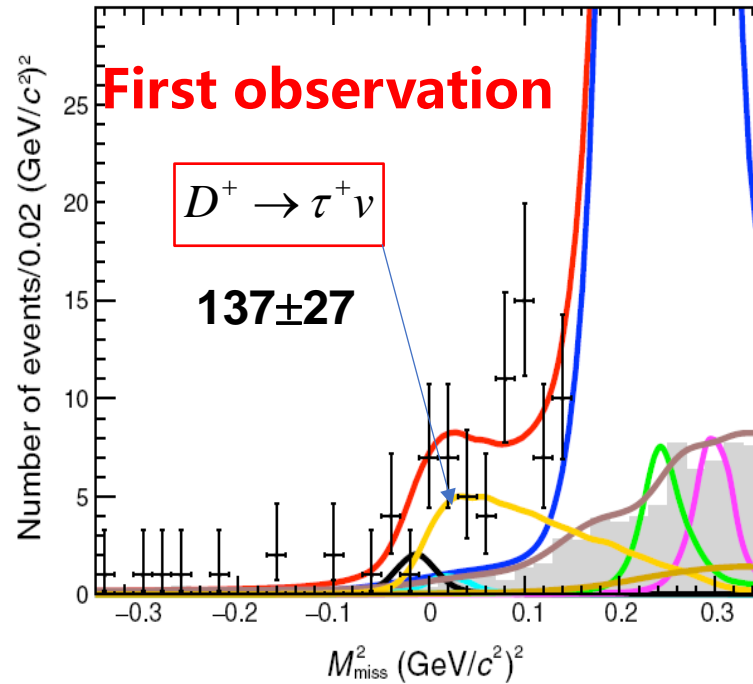
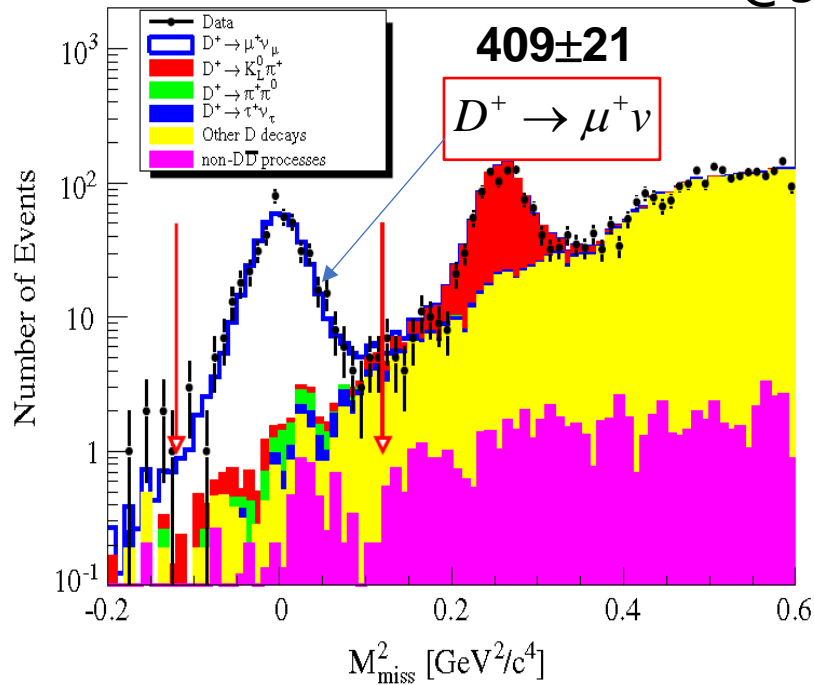
2.93 fb⁻¹

PRL123(2019)211802

@3.773 GeV

arXiv:2410.07626, 最新结果

20.3 fb⁻¹@3.773 GeV



The most precise to date

$$B[D^+ \rightarrow \mu^+ \nu] = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$B[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24 \pm 0.12) \times 10^{-3}$$

$$B[D^+ \rightarrow \mu^+ \nu] = (3.98 \pm 0.08 \pm 0.04) \times 10^{-4}$$

$$f_{D^+} |V_{cd}| = 46.7 \pm 1.2 \pm 0.4 \text{ MeV}$$

$$f_{D^+} |V_{cd}| = 50.4 \pm 5.0 \pm 2.5 \text{ MeV}$$

$$f_{D^+} |V_{cd}| = 47.53 \pm 0.48 \pm 0.27 \text{ MeV}$$

Precision ~2.7%

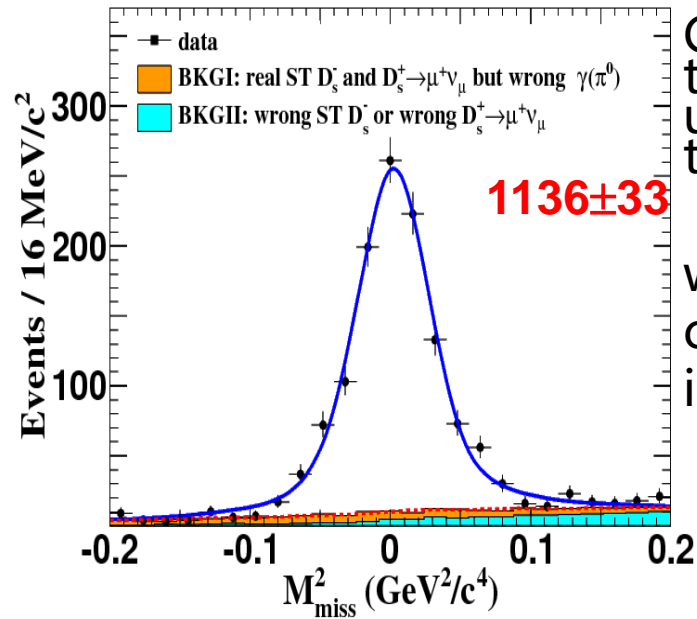
Precision ~11%

Precision ~1.2%

Studies of $D_s^+ \rightarrow \mu^+ \nu_\mu$

3.19 fb⁻¹@4.18 GeV

PRL122(2019)071802



Constrained fit to matched and un-matched transition $\gamma(\pi^0)$

with μ counter information

1136±33

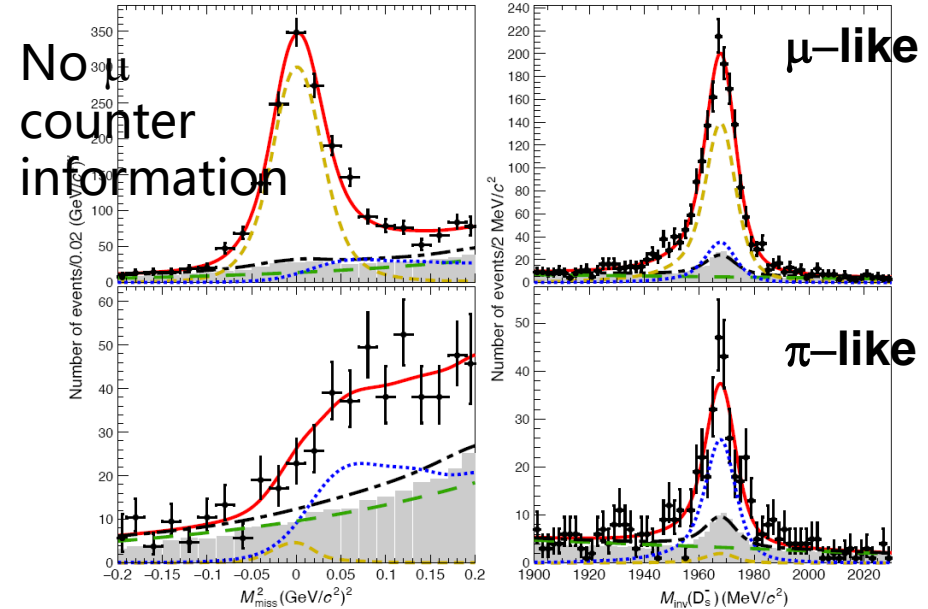
$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.49 \pm 0.16 \pm 0.15) \times 10^{-3}$$

$$f_{D_s^+} |V_{cs}| = (246.2 \pm 3.6 \pm 3.5) \text{ MeV}$$

Precision ~2.1%

6.3 fb⁻¹@4.18-4.23 GeV

PRD104(2021)052009



2198±55

$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.35 \pm 0.13 \pm 0.16) \times 10^{-3}$$

$$f_{D_s^+} |V_{cs}| = (243.1 \pm 3.0 \pm 3.7) \text{ MeV}$$

Precision ~2.0%

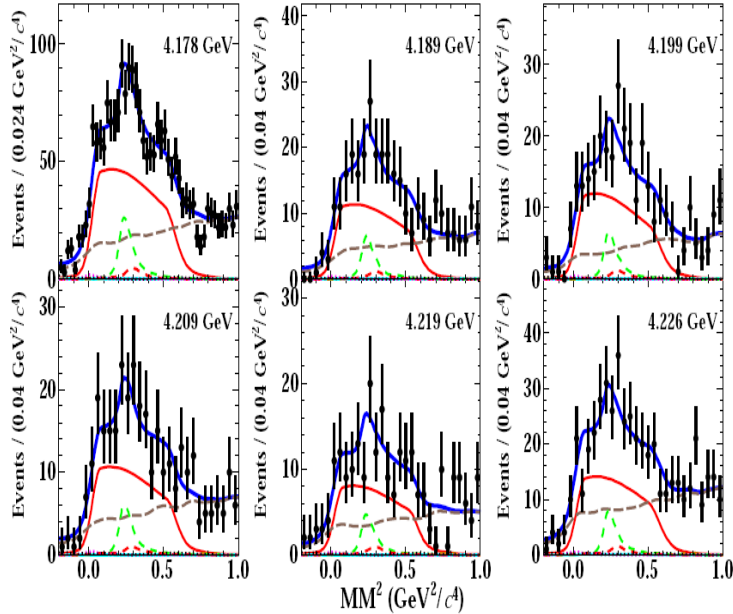
Studies of $D_s^+ \rightarrow \tau^+ \nu_\tau$

PRD104(2021)032001

$D_s^+ \rightarrow \tau^+ (\rho^+ \nu) \nu$

6.3 fb⁻¹

1745±84



$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.29 \pm 0.25 \pm 0.20)\%$$

$$f_{D_s^+} |V_{cs}| = (244.8 \pm 5.8 \pm 4.8) \text{ MeV}$$

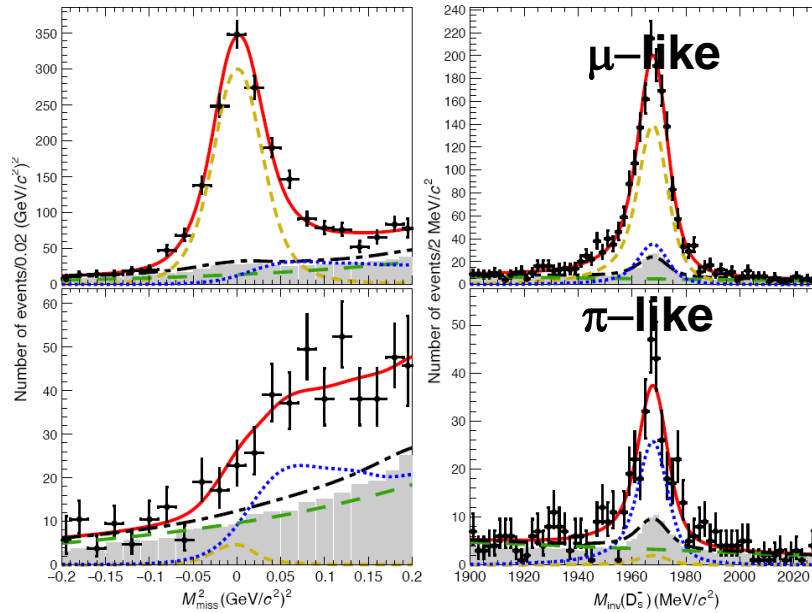
Precision ~ 3.1%

PRD104(2021)052009

$D_s^+ \rightarrow \tau^+ (\pi^+ \nu) \nu$

6.3 fb⁻¹

946±46



$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.21 \pm 0.25 \pm 0.17)\%$$

$$f_{D_s^+} |V_{cs}| = (243.0 \pm 5.8 \pm 4.0) \text{ MeV}$$

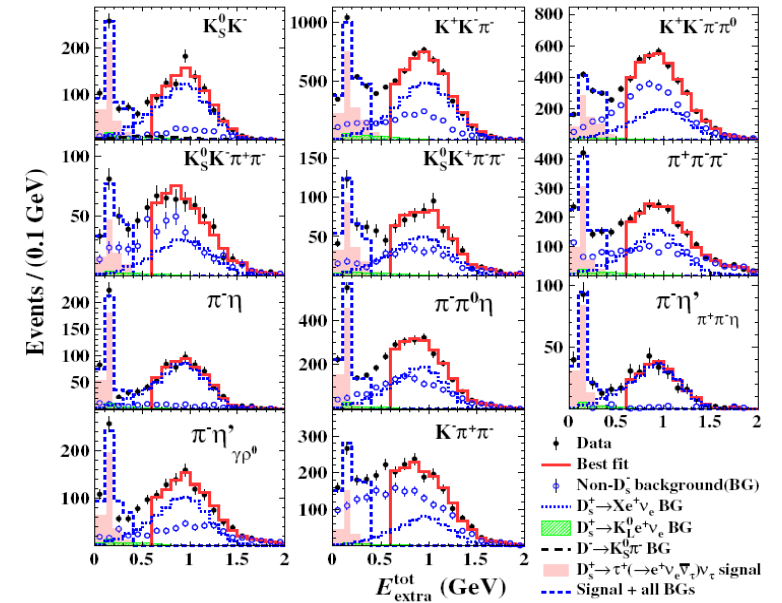
Precision ~ 2.9%

PRL127(2021)171801

$D_s^+ \rightarrow \tau^+ (e^+ \nu) \nu$

6.3 fb⁻¹

4940±97



$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.27 \pm 0.10 \pm 0.12)\%$$

$$f_{D_s^+} |V_{cs}| = (244.4 \pm 2.3 \pm 2.9) \text{ MeV}$$

Precision ~ 1.5%

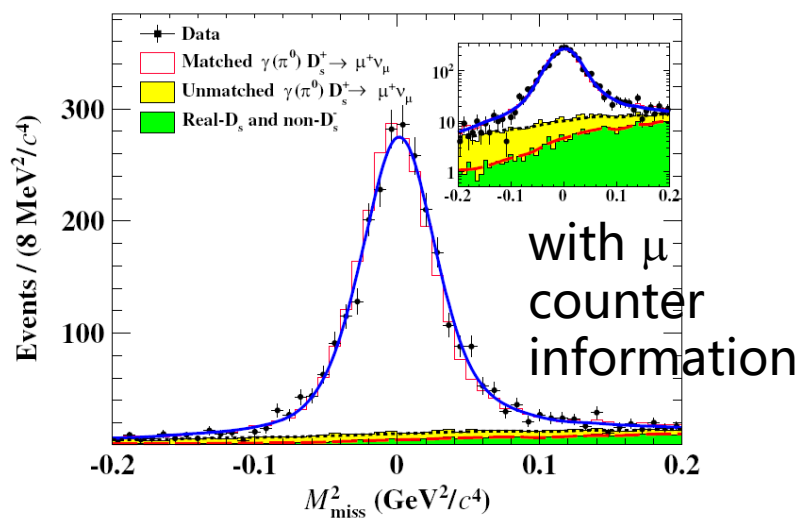
More measurements of $D_s^+ \rightarrow l^+ \nu_l$

PRD108(2023)112001

$$D_s^+ \rightarrow \mu^+ \nu$$

7.33 fb⁻¹

2515 ± 52

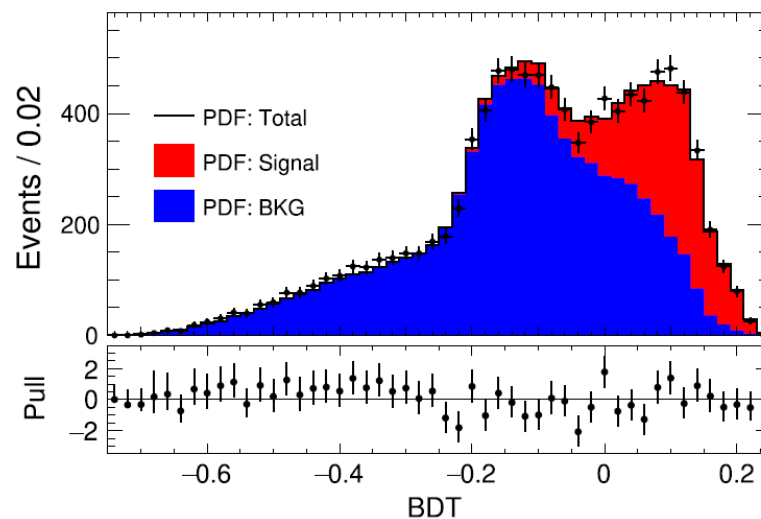


PRD108(2023)092014

$$D_s^+ \rightarrow \tau^+ (\pi^+ \nu) \nu \quad \text{BDT}$$

7.33 fb⁻¹

2411 ± 75

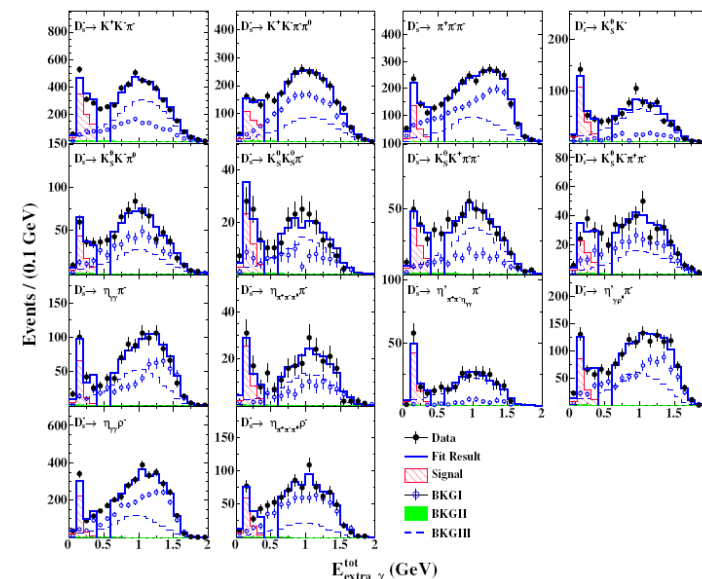


JHEP09(2023)124

$$D_s^+ \rightarrow \tau^+ (\mu^+ \nu \nu)$$

7.33 fb⁻¹

2281 ± 73



$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.29 \pm 0.11 \pm 0.09) \times 10^{-3} \quad ; [D_s^+ \rightarrow \tau^+ \nu] = (5.44 \pm 0.17 \pm 0.13)\%$$

$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.37 \pm 0.17 \pm 0.15)\%$$

$$f_{D_s^+} |V_{cs}| = (241.8 \pm 2.5 \pm 2.2) \text{ MeV}$$

$$f_{D_s^+} |V_{cs}| = (248.3 \pm 3.9 \pm 3.2) \text{ MeV}$$

$$f_{D_s^+} |V_{cs}| = (246.7 \pm 3.9 \pm 3.6) \text{ MeV}$$

Precision ~ 1.4%

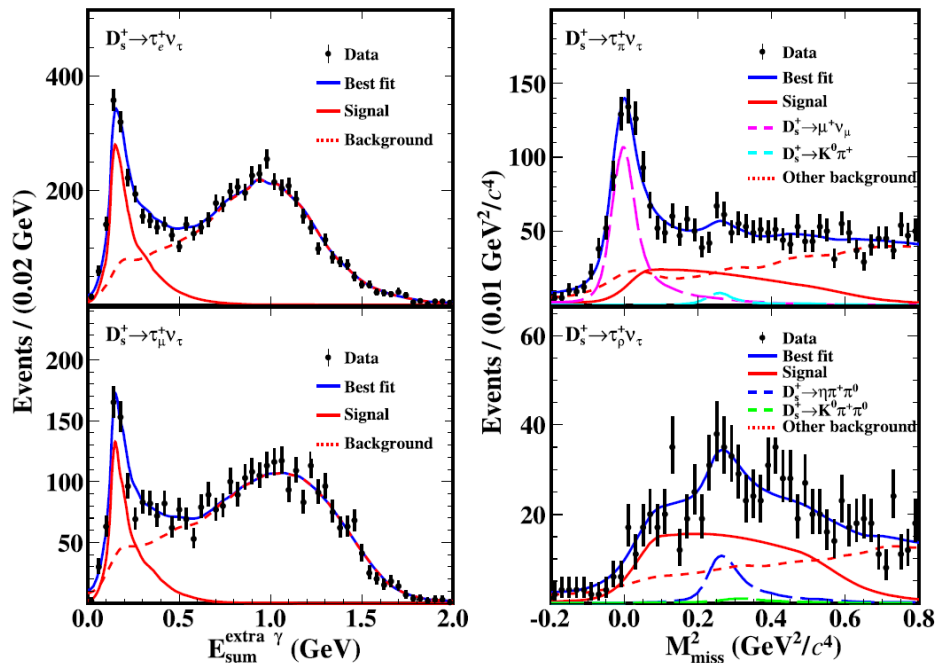
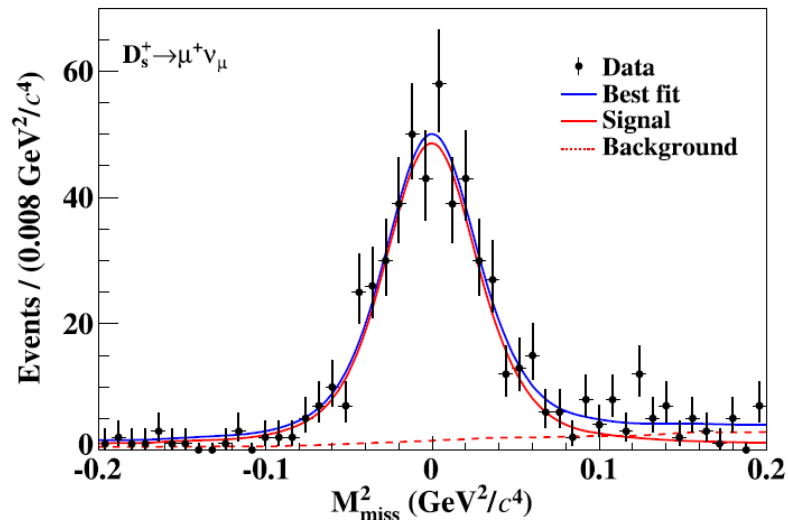
Precision ~ 2.0%

Precision ~ 2.2%

The most precise to date

基于 $e^+e^- \rightarrow D_s^+ D_s^-$ 研究 D_s^+ 纯轻衰变

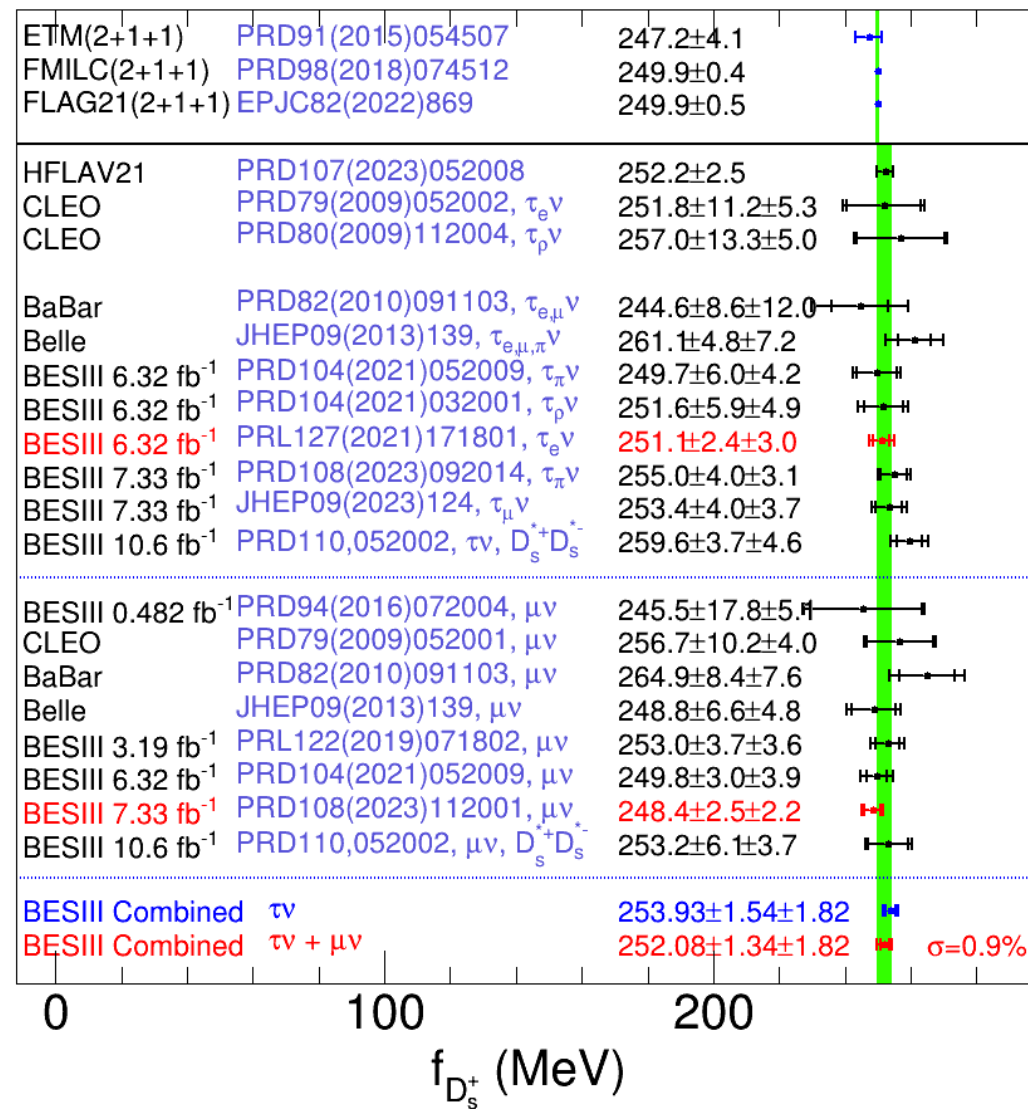
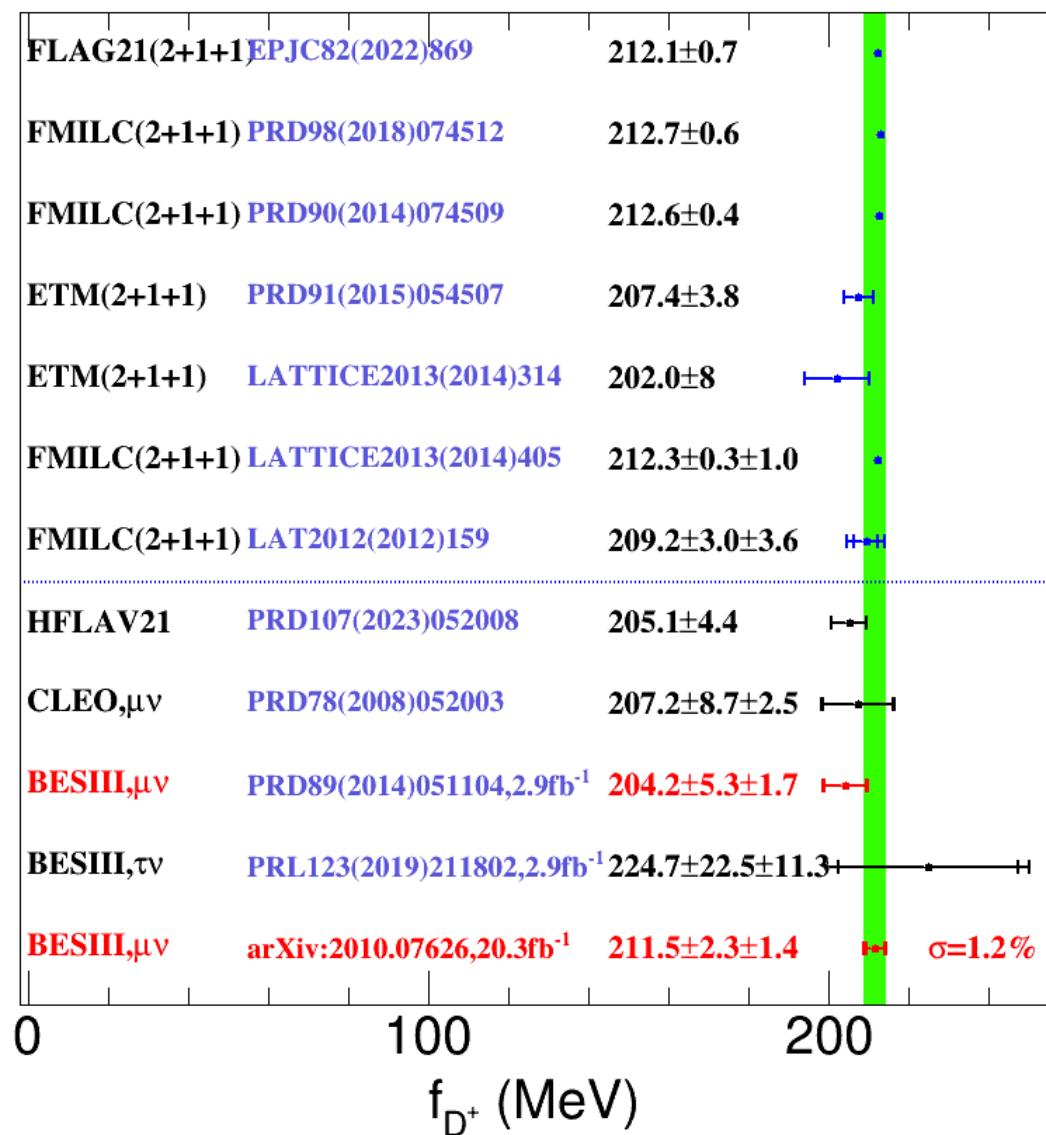
PRD110 (2024) 052002



基于4.23-4.7 GeV 10.6 fb⁻¹数据, 挖掘现有及未来BESIII数据潜力

Signal decay	$\bar{\epsilon}_{\text{sig}} (\%)$	No lepton universality constraint		Lepton universality constraint	
		N_{DT}	$\mathcal{B} (\%)$	$N_{\text{DT}}^{\text{SM}}$	$\mathcal{B}^{\text{SM}} (\%)$
$D_s^+ \rightarrow \tau_e^+ \nu_\tau$	7.81 ± 0.02				
$D_s^+ \rightarrow \tau_\mu^+ \nu_\tau$	18.57 ± 0.04	2845 ± 83	$5.60 \pm 0.16 \pm 0.20$	2754 ± 69	$5.39 \pm 0.14 \pm 0.20$
$D_s^+ \rightarrow \tau_\pi^+ \nu_\tau$	8.93 ± 0.02				
$D_s^+ \rightarrow \tau_\rho^+ \nu_\tau$	6.11 ± 0.02				
$D_s^+ \rightarrow \mu_b^+ \nu_\mu$	94.76 ± 0.20	579 ± 34	$0.491 \pm 0.029 \pm 0.020$	641 ± 16	$0.553 \pm 0.014 \pm 0.021$
$D_s^+ \rightarrow \mu_a^+ \nu_\mu$	74.67 ± 0.16	507 ± 26	$0.547 \pm 0.026 \pm 0.016$

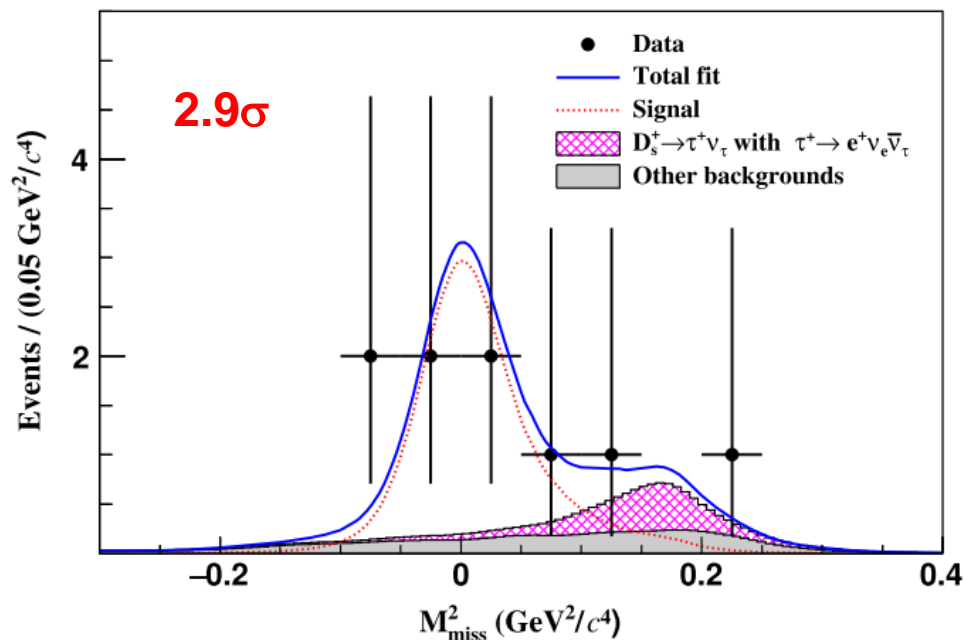
Comparisons of f_{D^+} and $f_{D_s^+}$



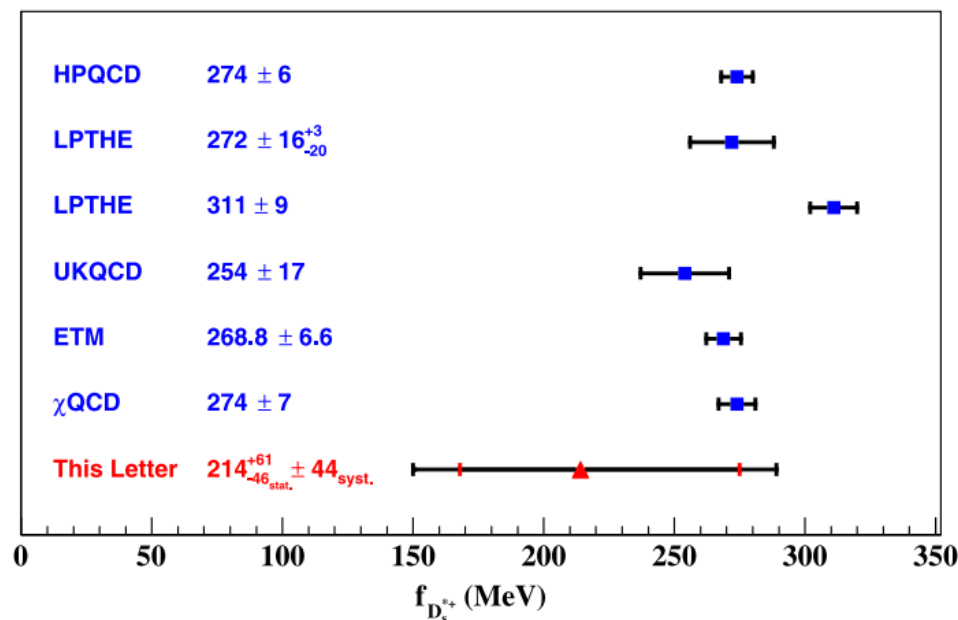
First experimental study of $D_s^{*+} \rightarrow e^+ \nu_e$

PRL131 (2023) 141802

7.33 fb⁻¹@4.13-4.23 GeV



联合格点QCD计算的 D_s^{*+} 总宽度,
首次抽取 D_s^{*+} 衰变常数



$$\mathcal{B}(D_s^{*+} \rightarrow e^+ \nu_e) = (2.1^{+1.2}_{-0.9 \text{ stat}} \pm 0.2_{\text{syst}}) \times 10^{-5}$$

$$\Gamma(D_s^{*+} \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2}{12\pi} |V_{cs}|^2 f_{D_s^{*+}}^2 m_{D_s^{*+}}^3 \left(1 - \frac{m_{\ell^+}^2}{m_{D_s^{*+}}^2}\right)^2 \times \left(1 + \frac{m_{\ell^+}^2}{2m_{D_s^{*+}}^2}\right),$$

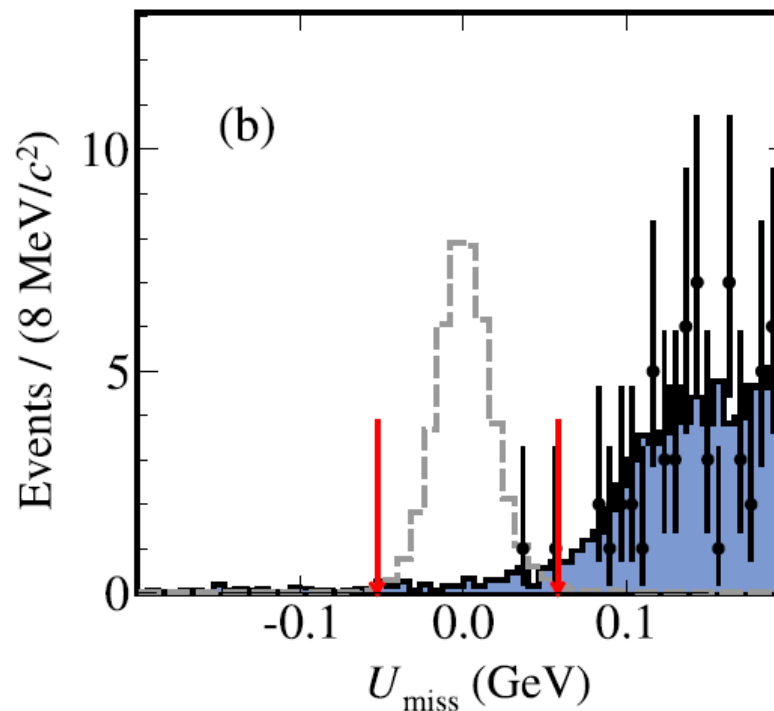
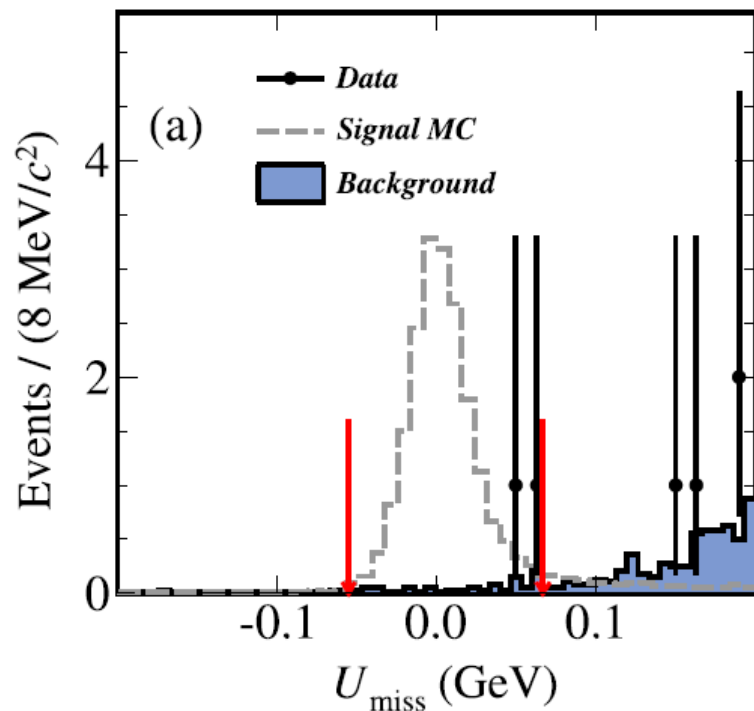
→ 为约束格点QCD计算的 D_s^{*+} 衰变常数首次提供实验依据

→ 对 D_s^{*+} 宽度上限的约束改进3个量级

Search for $D^{*+} \rightarrow l^+ \nu_l$

PRD110 (2024) 012003

6.3 fb⁻¹@4.18-4.23 GeV



Signal mode	N_{ST}^{tot}	N_{SR}^{data}	N_{SB}^{data}	N_{SR}^{MC}	N_{SB}^{MC}	$\bar{\epsilon}_{D^{*+} \rightarrow l^+ \nu_l}$ (%)	N_{UL}	\mathcal{B}_{UL}
$D^{*+} \rightarrow e^+ \nu_e$	516256 ± 1870	2	4	34	239	80.90 ± 1.46	5.9	1.1×10^{-5}
$D^{*+} \rightarrow \mu^+ \nu_\mu$		1	61	182	2872	68.86 ± 1.23	2.2	4.3×10^{-6}

分支比上限比标准模型预期高3个量级

粲介子半轻衰变

- $D \rightarrow Pe^+\nu_e$

- $D \rightarrow Ve^+\nu_e$

- $D \rightarrow Se^+\nu_e$

- $D \rightarrow Ae^+\nu_e$

- 其它衰变



见本次会议张书磊的报告

$D \rightarrow Pl^+ \nu_l$ 型半轻衰变

微分跃迁率测量

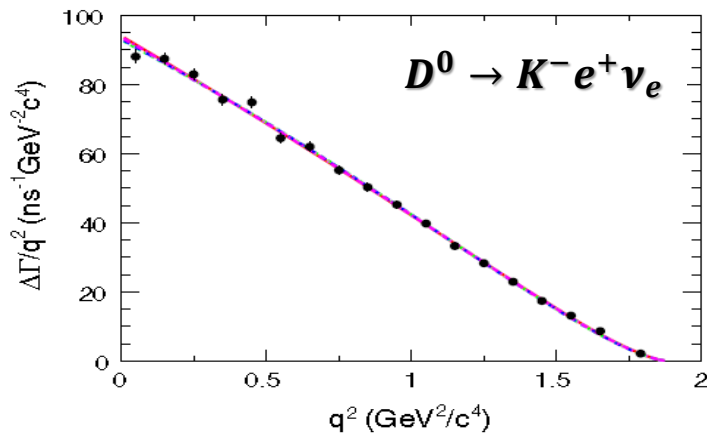
$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2 \longrightarrow \mathbf{f_+^{D \rightarrow P}(0) |V_{cs(d)}|}$$

Form factor parameterizations:

- Single pole form $f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$
- Modified pole $f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{M_{\text{pole}}^2}\right)\left(1 - \alpha \frac{q^2}{M_{\text{pole}}^2}\right)}$
- ISGW2 $f_+(q^2) = f_+(q_{\text{max}}^2) \left(1 + \frac{r_{\text{ISGW2}}^2}{12} (q_{\text{max}}^2 - q^2)\right)^{-2}$
- Series expansion $f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$

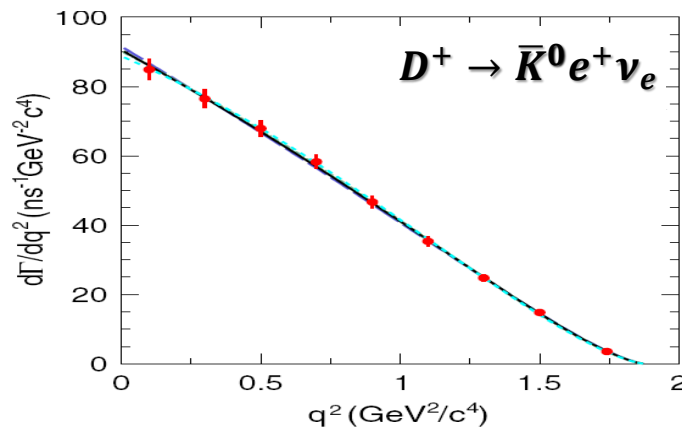
$c \rightarrow sl^+ \nu_l$ 型半轻衰变

PRD92(2015)072012



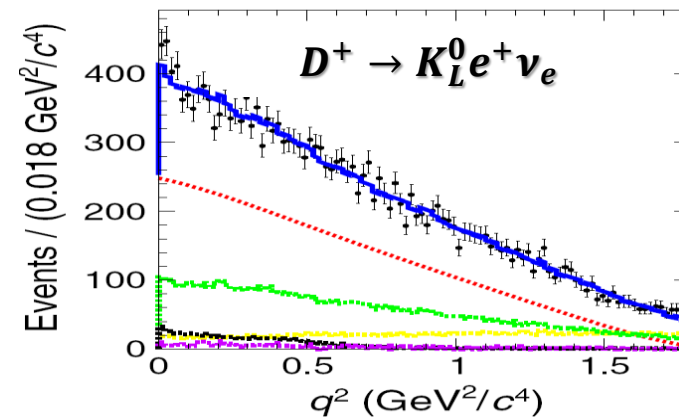
$$f_+^{D \rightarrow K}(0) |V_{cs}| = 0.717(03)(04)$$

PRD96(2017)012002



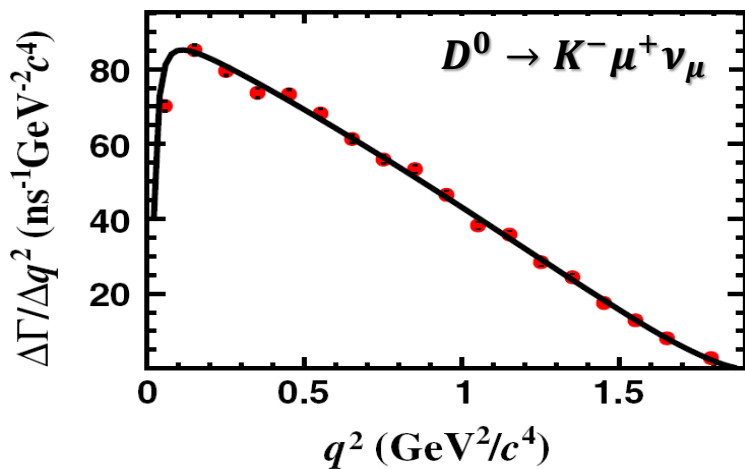
$$f_+^{D \rightarrow K}(0) |V_{cs}| = 0.705(04)(11)$$

PRD92(2015)112008



$$f_+^{D \rightarrow K}(0) |V_{cs}| = 0.728(06)(11)$$

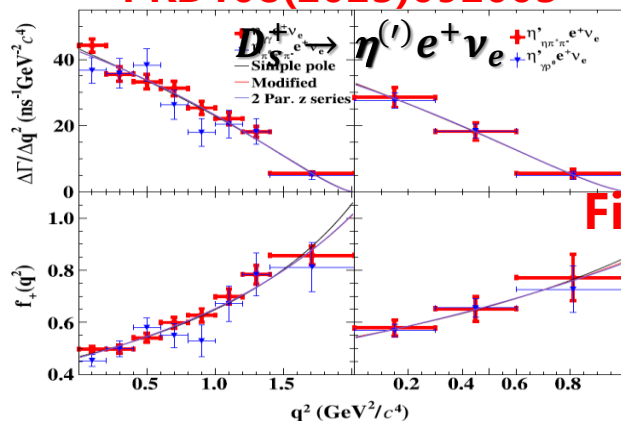
PRL122(2019)011804



$$f_+^{D \rightarrow K}(0) |V_{cs}| = 0.7148(38)(29)$$

PRL123(2019)121801 →

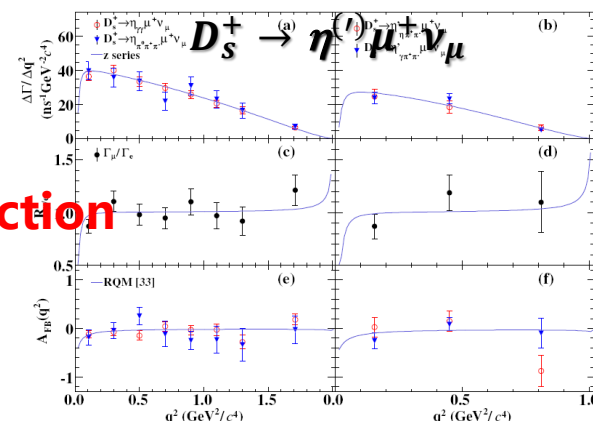
PRD108(2023)092003



$$f_+^{D_S \rightarrow \eta}(0) |V_{cs}| = 0.452(07)(07)$$

$$f_+^{D_S \rightarrow \eta'}(0) |V_{cs}| = 0.525(24)(09)$$

PRL132(2024)091802



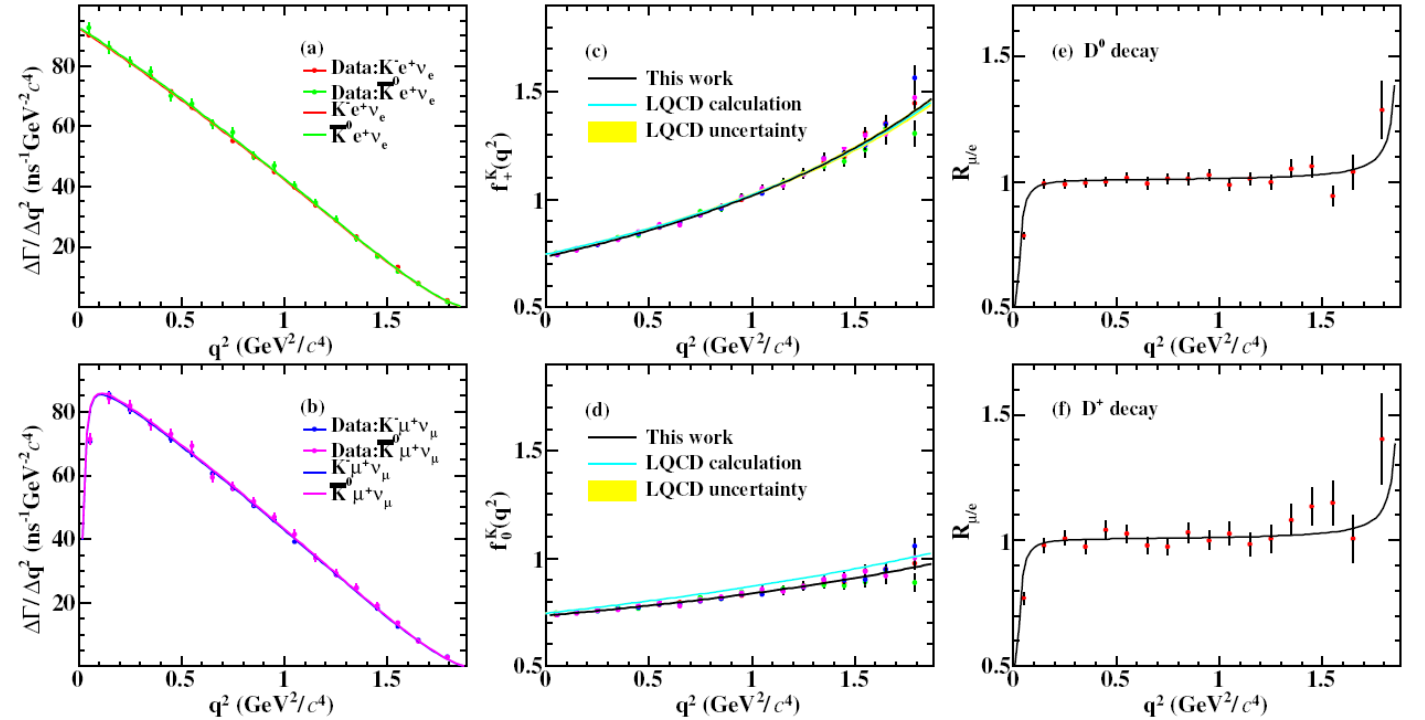
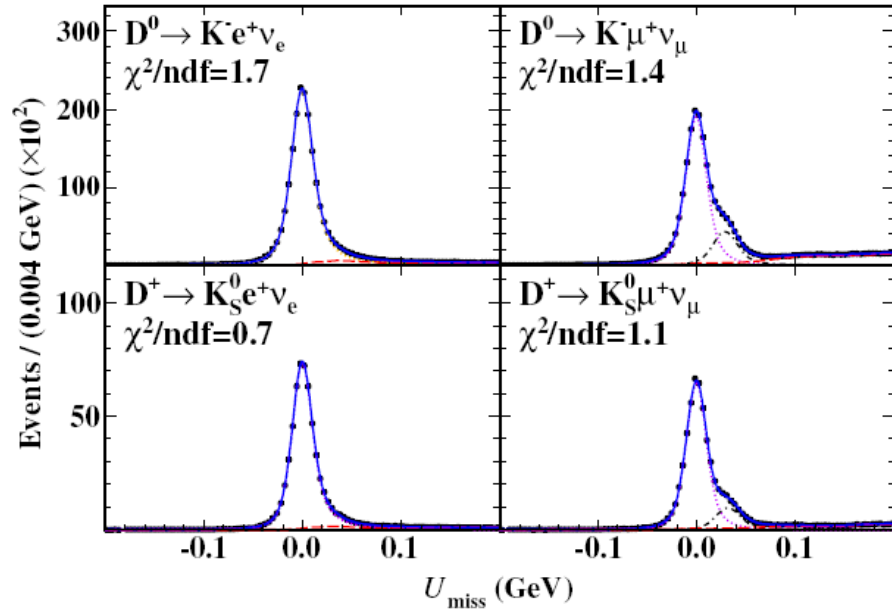
$$f_+^{D_S \rightarrow \eta}(0) |V_{cs}| = 0.451(10)(08)$$

$$f_+^{D_S \rightarrow \eta'}(0) |V_{cs}| = 0.506(37)(11)$$

Recent results of $D^{0(+)} \rightarrow \bar{K} \ell^+ \nu_\ell$ ($\ell = e$ or μ)

7.9 fb⁻¹ @3.773 GeV

arXiv:2408.09087

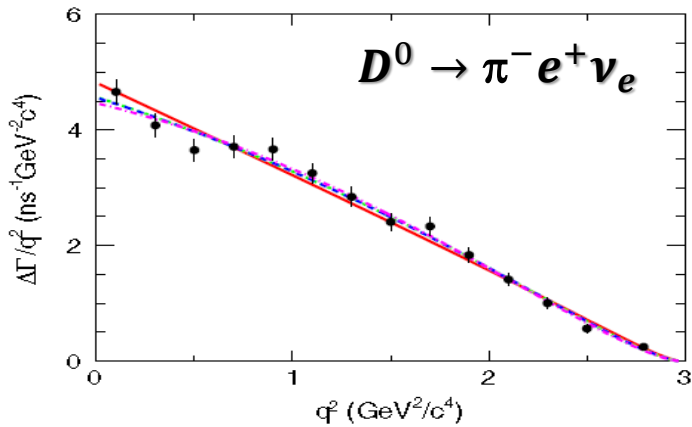


Decay	N_{DT}	$\bar{\epsilon}_{sig}$ (%)	\mathcal{B}_{sig} (%)
$D^0 \rightarrow K^- e^+ \nu_e$	190605 ± 471	68.79 ± 0.03	$3.509 \pm 0.009 \pm 0.013$
$D^0 \rightarrow K^- \mu^+ \nu_\mu$	147596 ± 488	54.85 ± 0.03	$3.408 \pm 0.011 \pm 0.013$
$D^+ \rightarrow \bar{K}^0 e^+ \nu_e$	57846 ± 256	15.74 ± 0.01	$8.856 \pm 0.039 \pm 0.078$
$D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu$	47229 ± 248	13.14 ± 0.01	$8.661 \pm 0.046 \pm 0.080$

Case	Decay	$f_+^K(0) V_{cs} $	$r_1(t_0)$	ρ_{2par}	χ^2/ndf
Individual fit	$D^0 \rightarrow K^- e^+ \nu_e$	$0.7168 \pm 0.0016 \pm 0.0014$	$-2.30 \pm 0.05 \pm 0.03$	0.53	16.3/16
	$D^0 \rightarrow K^- \mu^+ \nu_\mu$	$0.7150 \pm 0.0022 \pm 0.0016$	$-2.28 \pm 0.08 \pm 0.02$	0.67	17.2/16
	$D^+ \rightarrow \bar{K}^0 e^+ \nu_e$	$0.7204 \pm 0.0027 \pm 0.0033$	$-2.13 \pm 0.10 \pm 0.07$	0.30	13.1/16
	$D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu$	$0.7122 \pm 0.0035 \pm 0.0030$	$-2.41 \pm 0.12 \pm 0.08$	0.46	10.4/16
Simultaneous fit	$D \rightarrow \bar{K} \ell^+ \nu_\ell$	$0.7162 \pm 0.0011 \pm 0.0012$	$-2.28 \pm 0.04 \pm 0.02$	0.48	61.2/70

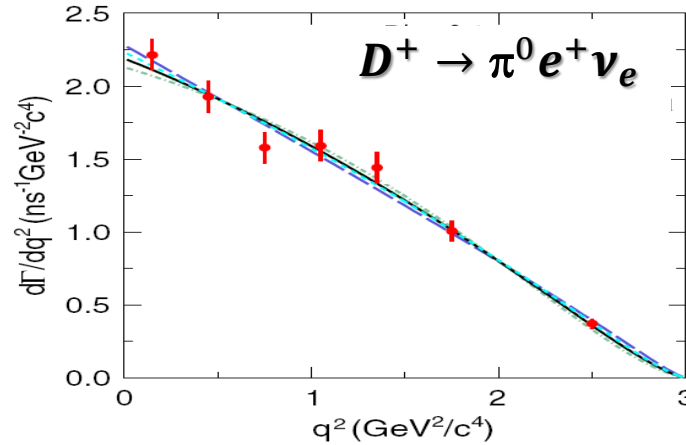
$c \rightarrow dl^+ \nu_l$ 型半轻衰变

PRD92(2015)072012



$$f_+^{D \rightarrow \pi}(0)|V_{cd}| = 0.144(02)(01)$$

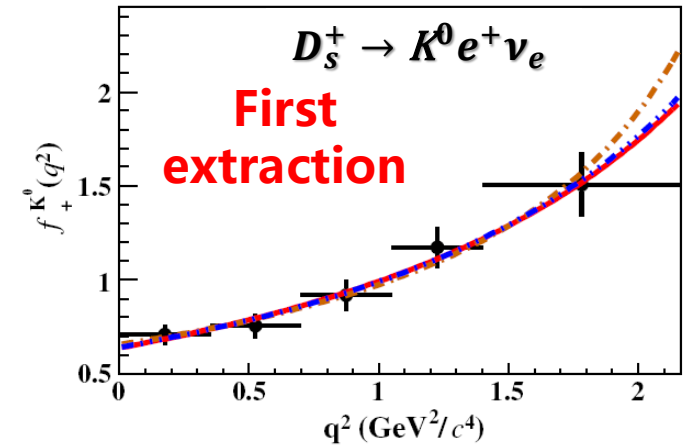
PRD96(2017)012002



$$f_+^{D \rightarrow \pi}(0)|V_{cd}| = 0.140(03)(01)$$

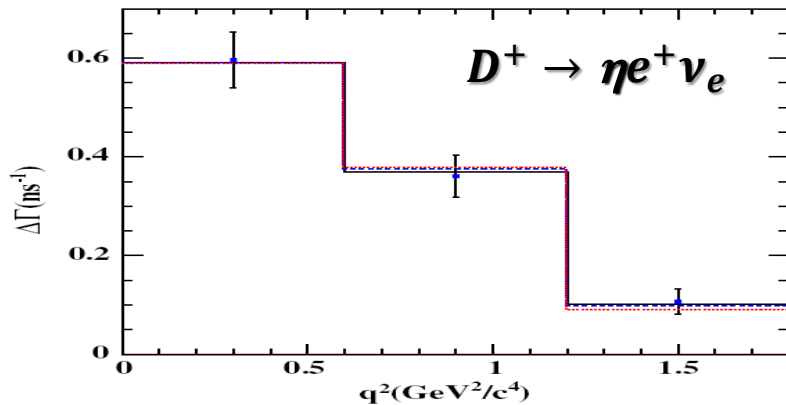
PRL122(2019)061801

→ arXiv:2406.19190



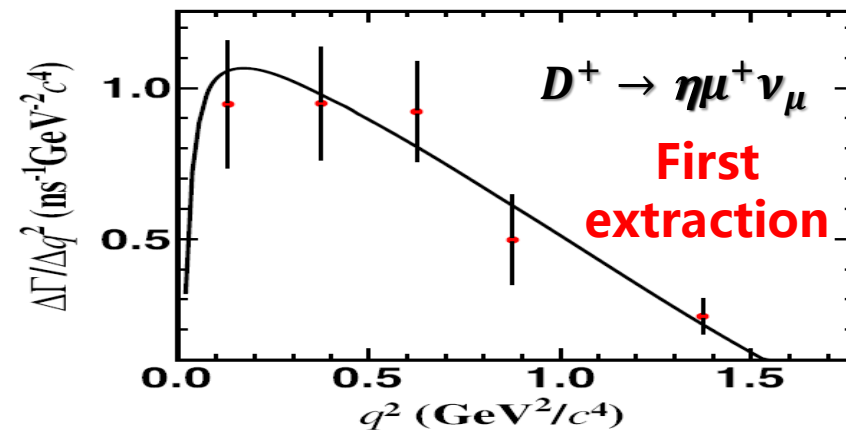
$$f_+^{\nu s \rightarrow \nu c}(0)|V_{cd}| = 0.143(11)(03)$$

PRD97(2018)092009



$$f_+^{D \rightarrow \eta}(0)|V_{cd}| = 0.079(06)(02)$$

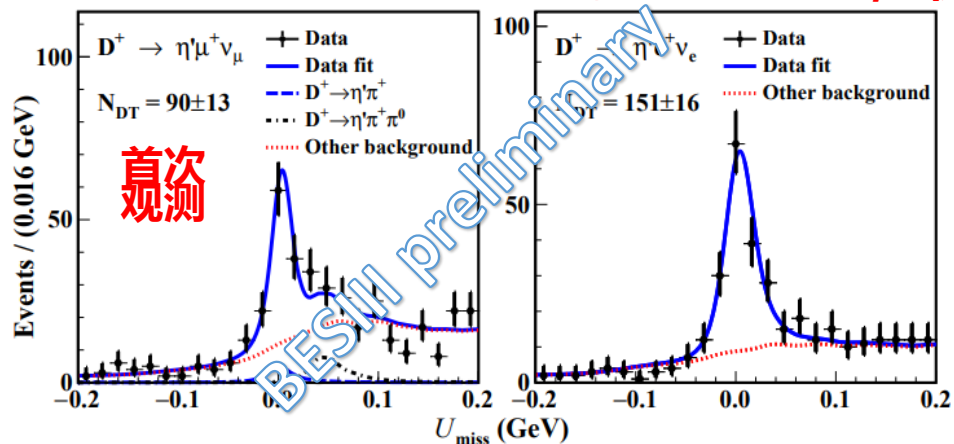
PRL124(2020)231801



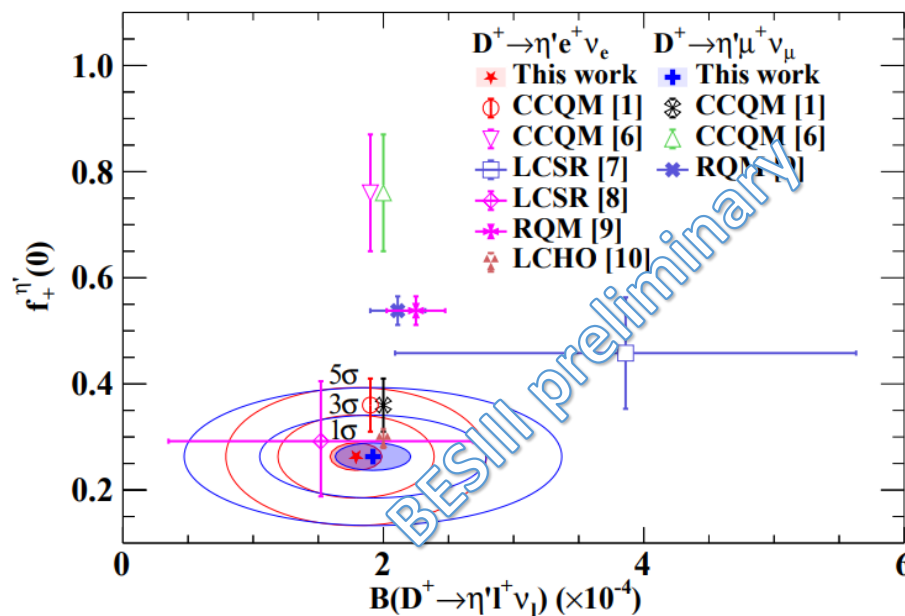
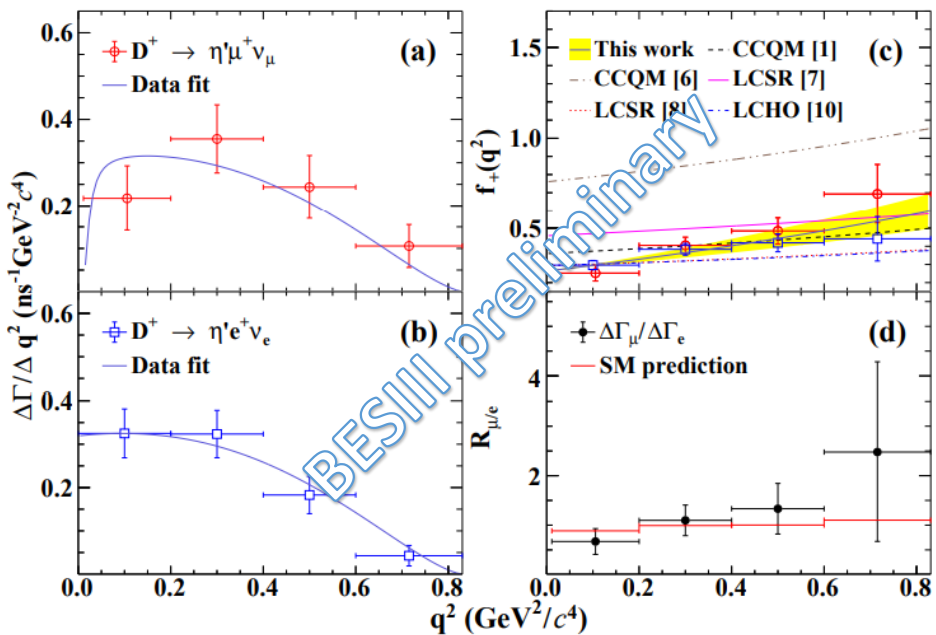
$$f_+^{D \rightarrow \eta}(0)|V_{cd}| = 0.087(08)(02)$$

Recent results of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$ ($\ell = e$ or μ)

20.3 fb⁻¹ @3.773 GeV, 最新结果, submitted to arXiv, no No. yet



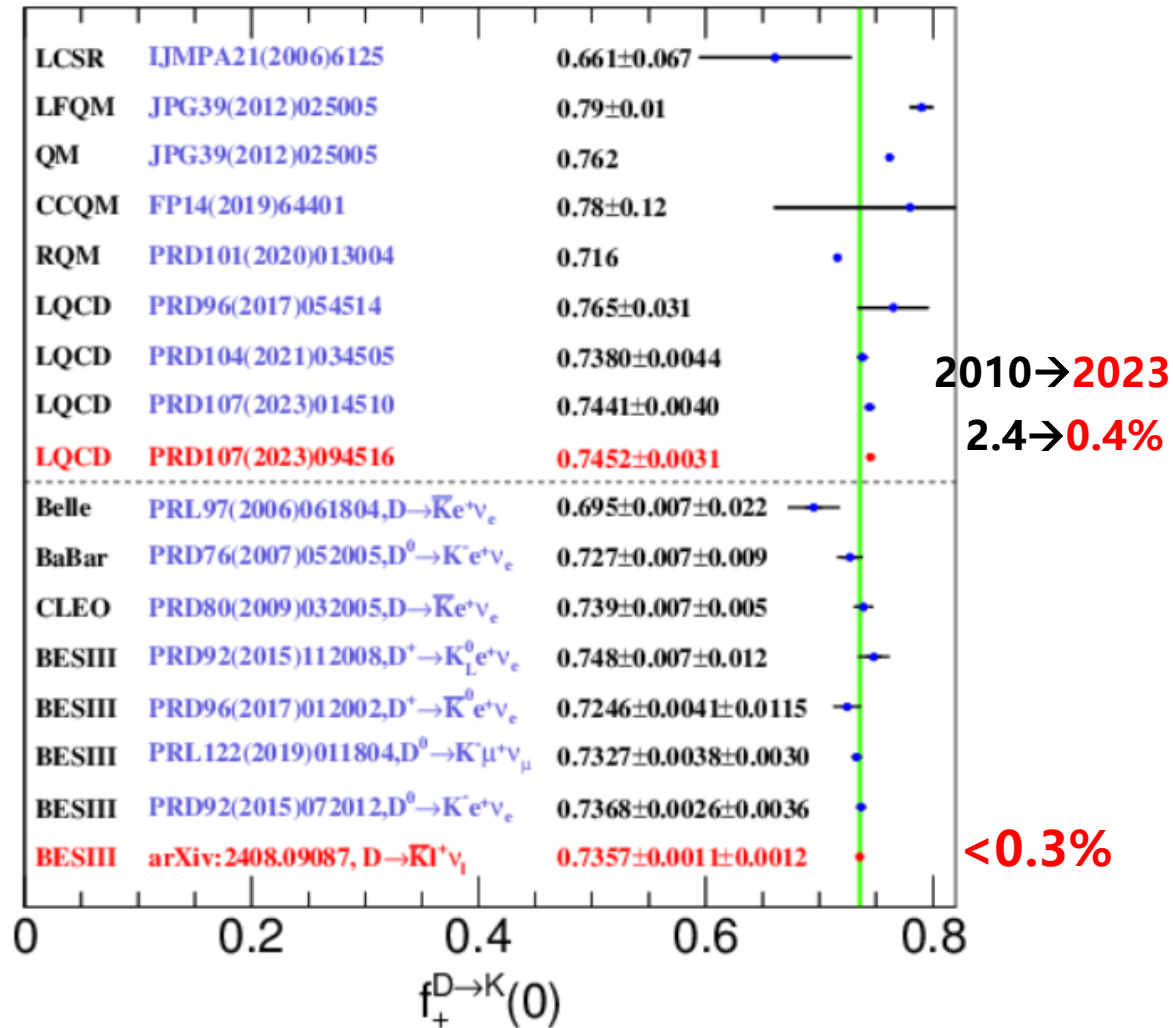
Decay	$\eta' \mu^+ \nu_\mu$		$\eta' e^+ \nu_e$	
	$\eta \pi^+ \pi^-$	$\gamma \pi^+ \pi^-$	$\eta \pi^+ \pi^-$	$\gamma \pi^+ \pi^-$
$\epsilon_{\text{sig}} (\%)$	1.77 ± 0.01	2.77 ± 0.01	5.70 ± 0.01	5.50 ± 0.01
N_{DT}	90 ± 13		151 ± 16	
Significance	8.6σ		12.9σ	
$\mathcal{B} (\times 10^{-4})$	1.92 ± 0.28	3.08	$1.79 \pm 0.19 \pm 0.07$	



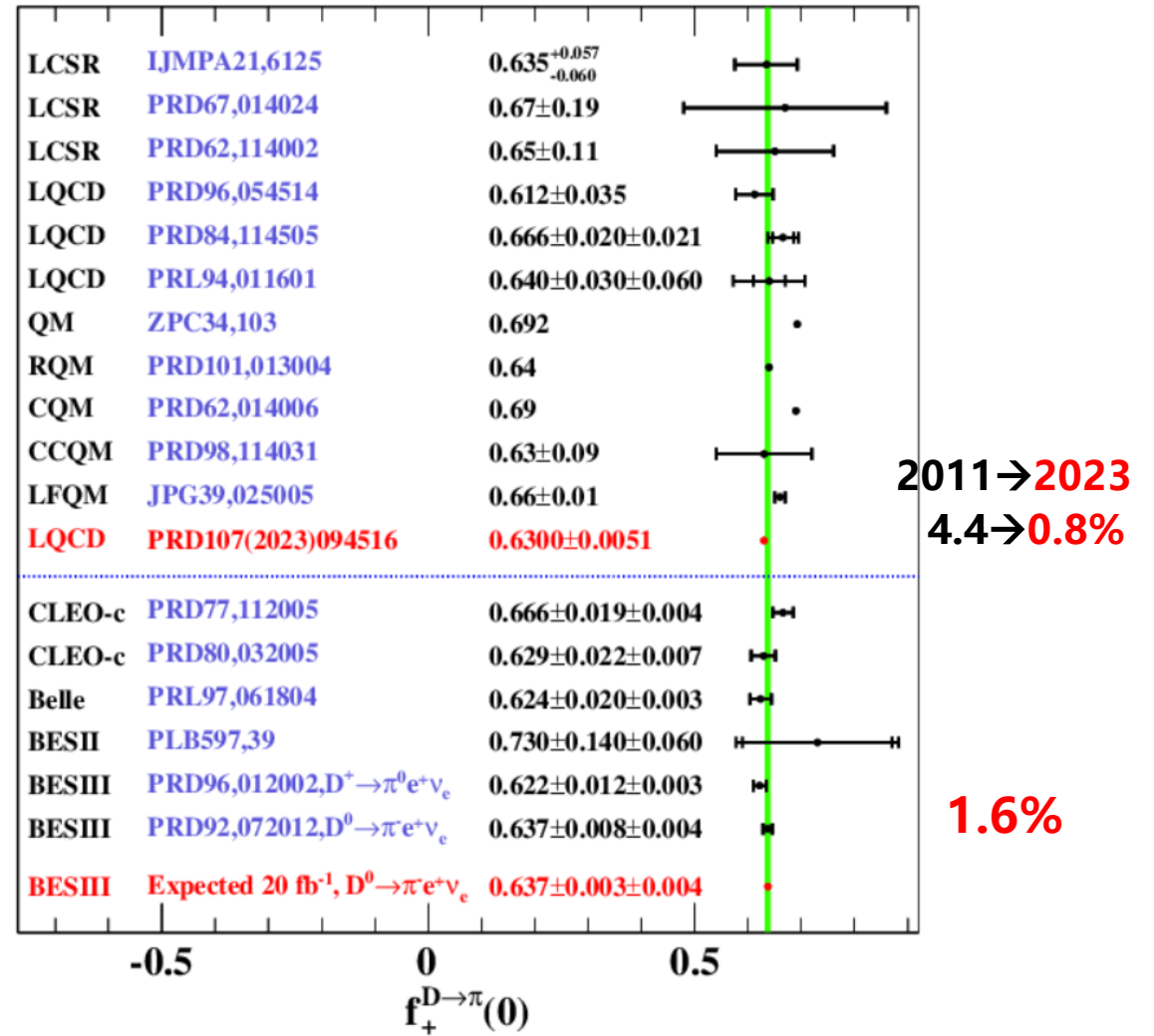
$$f_+^{D \rightarrow \eta'}(0) |V_{cd}| = (5.92 \pm 0.56 \pm 0.13)\%$$

首次抽取 $D^+ \rightarrow \eta'$ 形状因子, 为检验理论计算提供了重要依据

Comparisons of $f_+^{D \rightarrow K}(0)$ and $f_+^{D \rightarrow \pi}(0)$

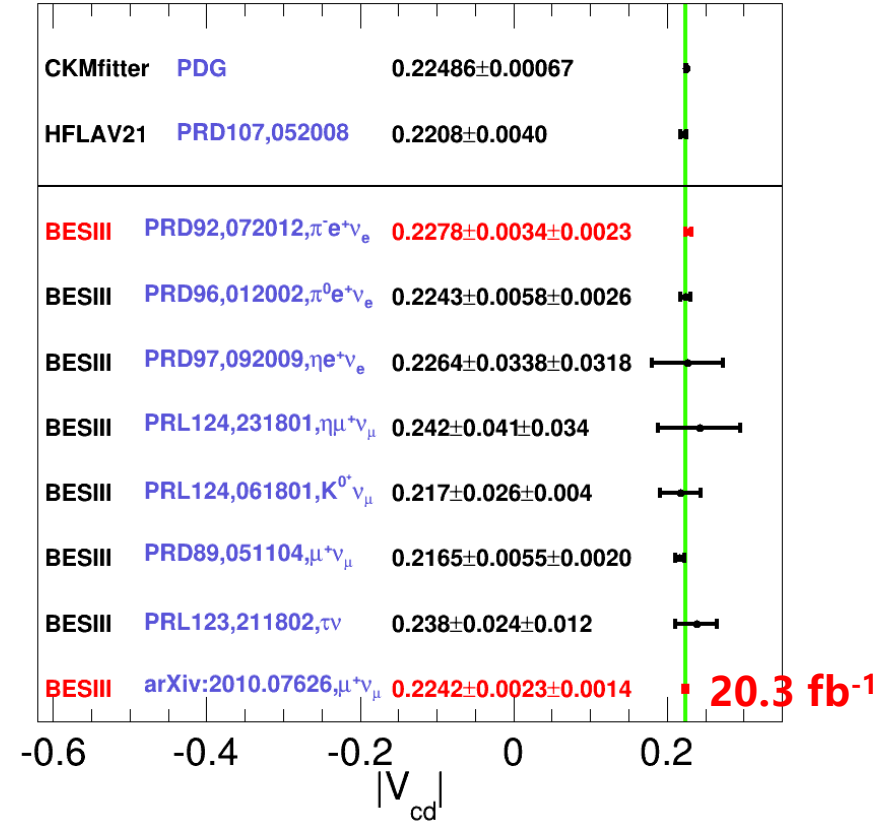
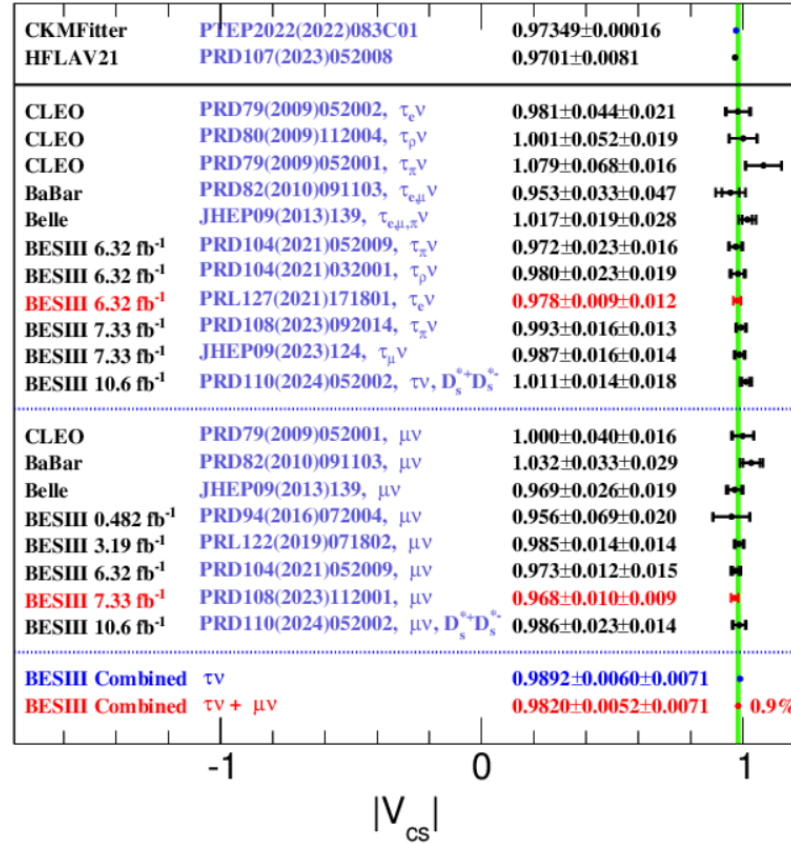
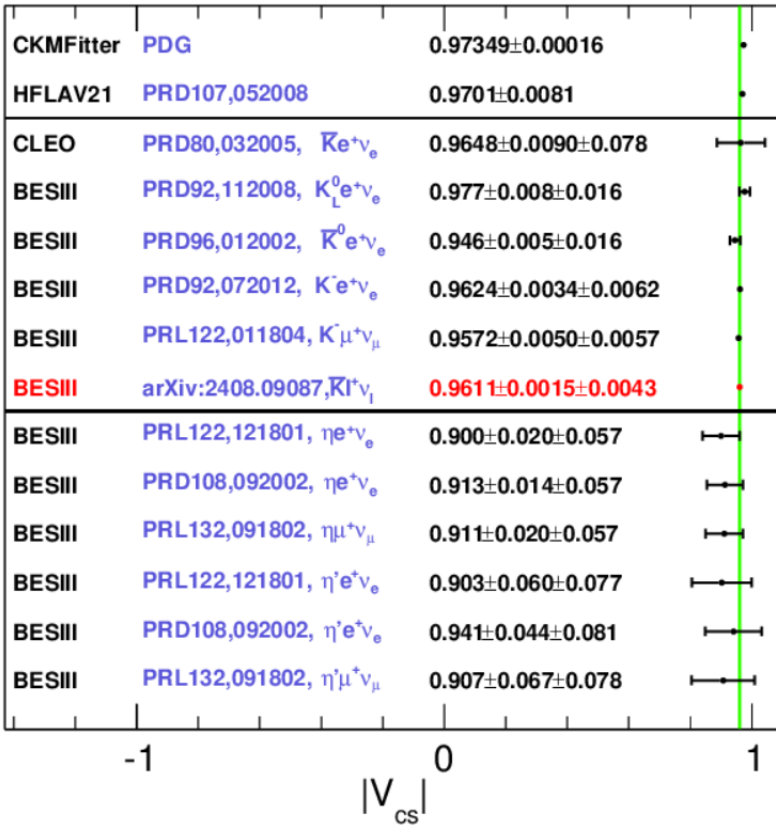


Experimental precision of $f_+^{D \rightarrow K}(0)$ is comparable to the latest LQCD precision



Experimental precision of $f_+^{D \rightarrow \pi}(0)$ is still dominated by statistical uncertainties

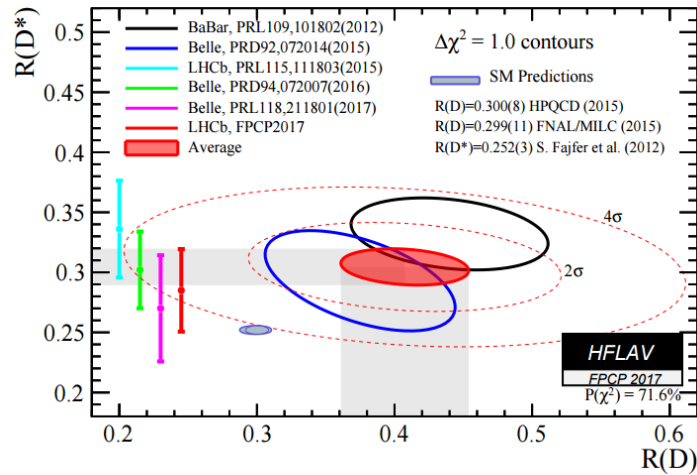
Comparisons of $|V_{cs}|$ and $|V_{cd}|$



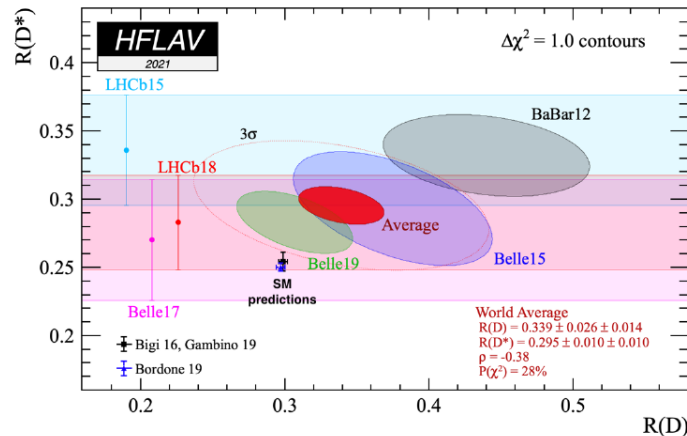
LFU tests in (semi)leptonic D decays before BESIII

Tension in B physics

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^{(*)} l \nu_l)}$$



3.9σ



3.3σ

Tension in D physics

$$\mathcal{B}^{\text{PDG18}}[D^0 \rightarrow \pi^- \mu^+ \nu] = (0.237 \pm 0.024)\%$$

$$\frac{\Gamma^{\text{PDG18}}[D^0 \rightarrow \pi^- \mu^+ \nu]}{\Gamma^{\text{PDG18}}[D^0 \rightarrow \pi^- e^+ \nu]} = 0.82 \pm 0.08 \quad \text{SM prediction: } 0.985$$

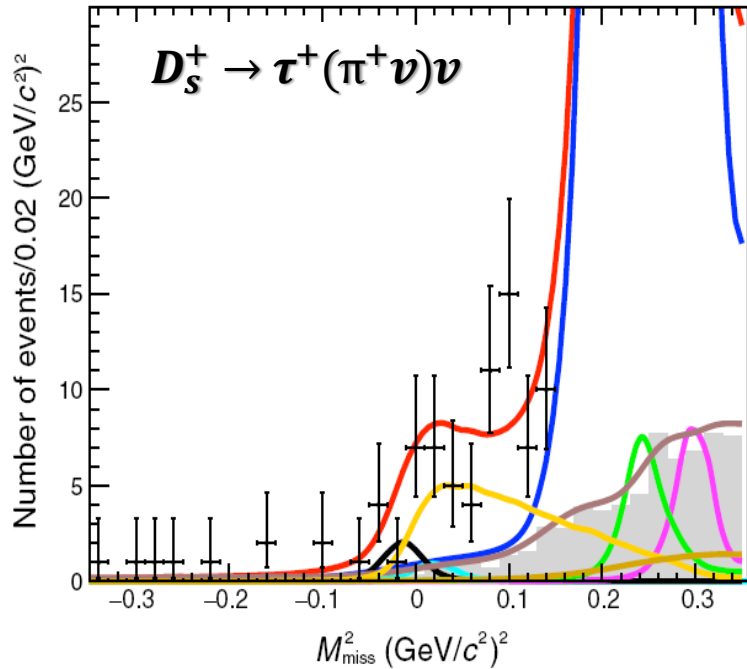
(2.1σ)

The knowledge of semimuonic charm meson decays is very poor

	D^0	D^+	D_s^+			
$c \rightarrow sl^+ \nu$	K^-	4% ^{Belle}	\bar{K}^0	7% ^{FOCUS}	η	NA
	K^{*-}	13% ^{FOCUS}	\bar{K}^{*0}	3% ^{CLEOc}	η'	NA
					ϕ	NA
					f_0	NA
$c \rightarrow dl^+ \nu$	π^-	10% ^{Belle}	π^0	NA	K^0	NA
	ρ^-	NA	ρ^0	17% ^{FOCUS}	K^{*0}	NA
			ω	NA		
			η	NA		
			η'	NA		

Tests of LFU in leptonic charm decays

PRL123(2019)211802



$$B^{\text{BESIII}}[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24 \pm 0.12) \times 10^{-3}$$

$$B^{\text{PDG}}[D^+ \rightarrow \mu^+ \nu] = (3.74 \pm 0.17) \times 10^{-4}$$

$$R_D = \frac{B[D^+ \rightarrow \tau^+ \nu]}{B[D^+ \rightarrow \mu^+ \nu]} = 3.21 \pm 0.64 \pm 0.43$$

SM prediction: 2.67

PRD108(2023)112001

PRL127(2021)171801,
PRD108(2023)092014,
PRD104(2021)032001,
JHEP09(2023)124

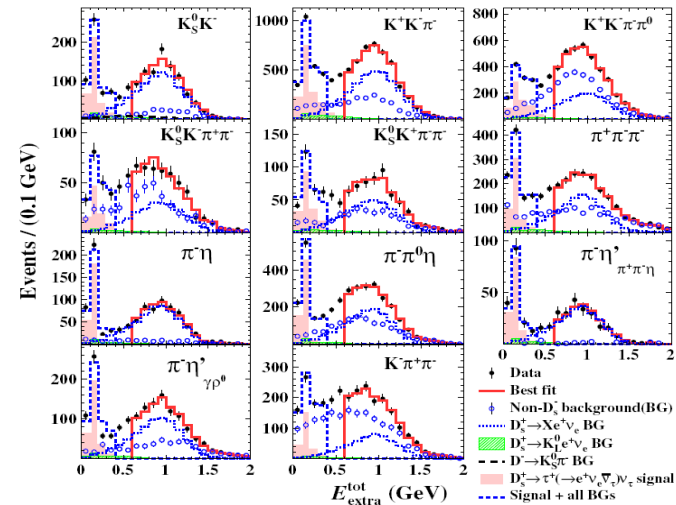
$D_s^+ \rightarrow \mu^+ \nu$

$D_s^+ \rightarrow \tau^+(e^+ \nu \nu) \nu$,

$D_s^+ \rightarrow \tau^+(\pi^+ \nu) \nu$,

$D_s^+ \rightarrow \tau^+(\rho^+ \nu) \nu$,

$D_s^+ \rightarrow \tau^+(\mu^+ \nu \nu) \nu$



$$B^{\text{BESIII}}[D_s^+ \rightarrow \mu^+ \nu] = (5.294 \pm 0.108 \pm 0.085) \times 10^{-3}$$

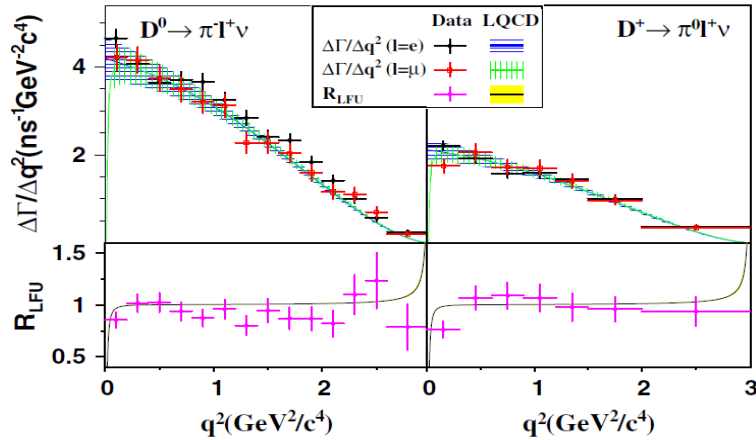
$$B^{\text{BESIII}}[D_s^+ \rightarrow \tau^+ \nu] = (5.32 \pm 0.07 \pm 0.07)\%$$

$$R_{D_s} = \frac{B[D_s^+ \rightarrow \tau^+ \nu]}{B[D_s^+ \rightarrow \mu^+ \nu]} = 10.05 \pm 0.35$$

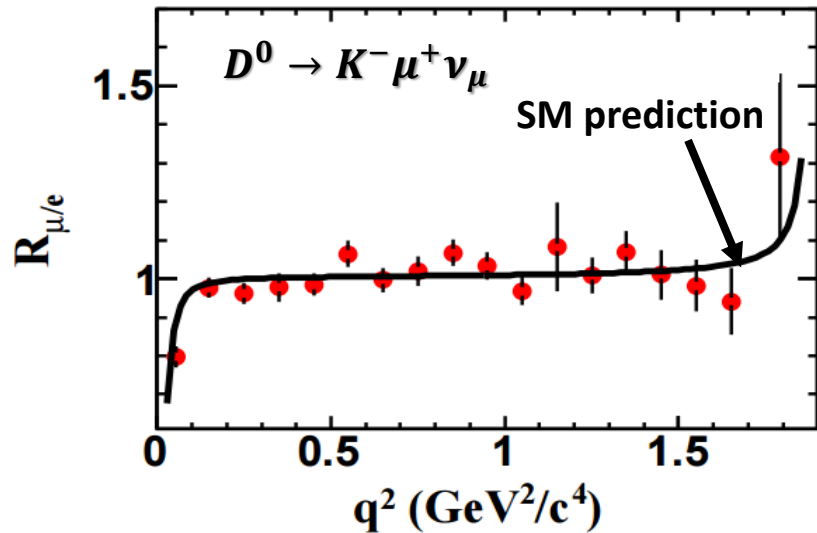
SM prediction: 9.75

Tests of LFU in semileptonic charm decays

PRL121(2018)171803



PRL122(2019)011804



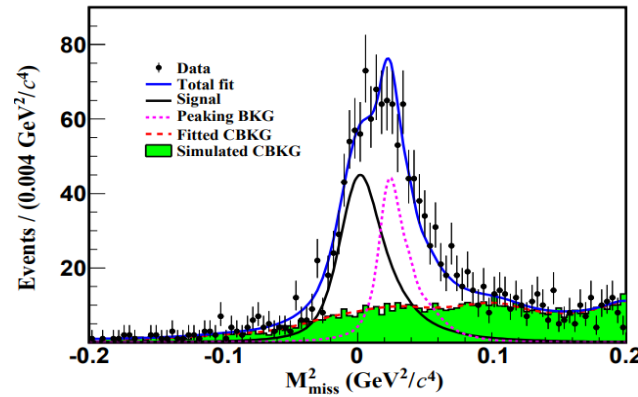
SM predictions: 0.93-0.99

$D^+ \rightarrow \eta \mu^+ \nu$ PRL124(2020)231801

$D^+ \rightarrow \omega \mu^+ \nu$ PRD101(2020)072005

$D^0 \rightarrow \rho^- \mu^+ \nu$ PRD104(2021)L091103

$D^+ \rightarrow \rho^0 \mu^+ \nu$ arXiv:2401.13225



$$R_{D^+ \eta} = \frac{\Gamma[D^+ \rightarrow \eta \mu^+ \nu]}{\Gamma[D^+ \rightarrow \eta e^+ \nu]} = 0.91 \pm 0.13$$

$$R_{D^+ \omega} = \frac{\Gamma[D^+ \rightarrow \omega \mu^+ \nu]}{\Gamma[D^+ \rightarrow \omega e^+ \nu]} = 1.05 \pm 0.14$$

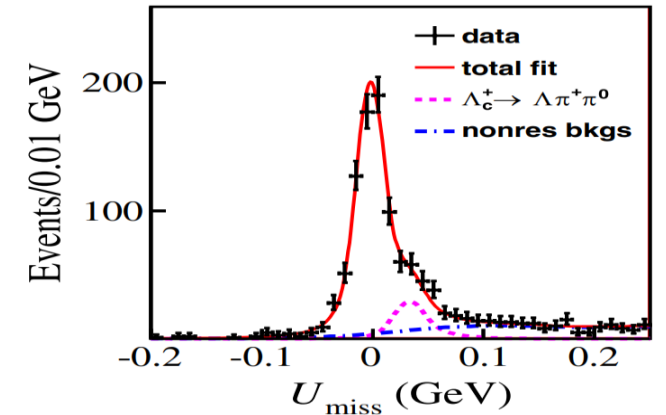
$$R_{D^0 \rho} = \frac{\Gamma[D^0 \rightarrow \rho^- \mu^+ \nu]}{\Gamma[D^0 \rightarrow \rho^- e^+ \nu]} = 0.90 \pm 0.11$$

$$R_{D^+ \rho} = \frac{\Gamma[D^+ \rightarrow \rho^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \rho^0 e^+ \nu]} = 0.88 \pm 0.10$$

$\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu$

PLB767(2017)42 →

PRD108(2023)L031105



$$R_{\Lambda_c^+ \Lambda} = \frac{\Gamma[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu]}{\Gamma[\Lambda_c^+ \rightarrow \Lambda e^+ \nu]} = 0.98 \pm 0.06$$

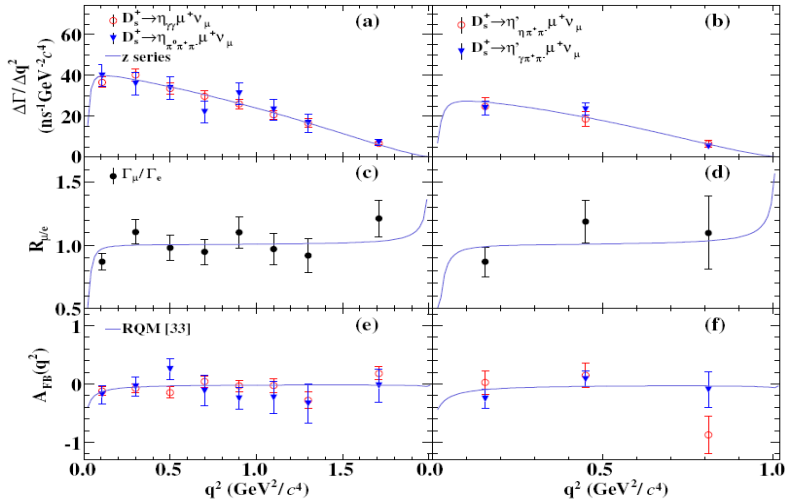
$D^0 \rightarrow K^{*-} \mu^+ \nu$ arXiv:2401.12927

$$R_{D^0 K^{*-}} = \frac{\Gamma[D^0 \rightarrow K^{*-} \mu^+ \nu]}{\Gamma[D^0 \rightarrow K^{*-} e^+ \nu]} = 0.96 \pm 0.08$$

Summary of LFU tests at BESIII

PRD97(2018)012006 →

$D_S^+ \rightarrow \eta^{(\prime)} \mu^+ \nu_\mu$ PRL132(2024)091802



$$R_{D_S^+ \eta} = \frac{\Gamma[D_S^+ \rightarrow \eta \mu^+ \nu]}{\Gamma[D_S^+ \rightarrow \eta e^+ \nu]} = 0.984 \pm 0.032$$

$$R_{D_S^+ \eta'} = \frac{\Gamma[D_S^+ \rightarrow \eta' \mu^+ \nu]}{\Gamma[D_S^+ \rightarrow \eta' e^+ \nu]} = 0.989 \pm 0.089$$

$D_S^+ \rightarrow \phi \mu^+ \nu_\mu$ JHEP12(2023)072

$$R_{D_S^+ \phi} = \frac{\Gamma[D_S^+ \rightarrow \phi \mu^+ \nu]}{\Gamma[D_S^+ \rightarrow \phi e^+ \nu]} = 0.94 \pm 0.08$$

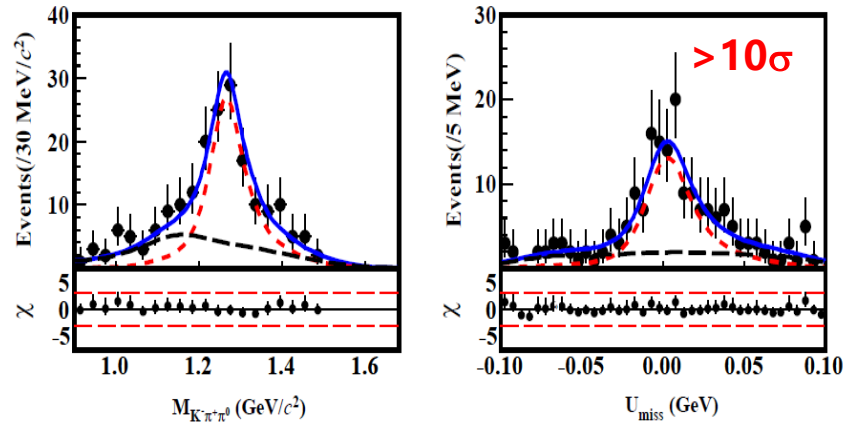
Eleven decays are observed for the first time, all other decays are measured with better precision

	BF ratios	References	
μ/e	$D^0 \rightarrow K^-$	$0.971 \pm 0.004 \pm 0.005$	arXiv:2408.090987
	$D^0 \rightarrow \pi^-$	$0.922 \pm 0.030 \pm 0.022$	PRL121(2018)171803
	$D^0 \rightarrow \rho^-$	0.90 ± 0.11	PRD104(2021)L091003
	$D^+ \rightarrow \bar{K}^0$	$0.978 \pm 0.007 \pm 0.012$	arXiv:2408.090987
	$D^+ \rightarrow \pi^0$	$0.964 \pm 0.037 \pm 0.026$	PRL121(2018)171803
	$D^+ \rightarrow \eta$	0.91 ± 0.13	PRL124(2020)231801
	$D^+ \rightarrow \eta'$	$1.07 \pm 0.19 \pm 0.03$	Submitted, no arXiv No.
	$D^0 \rightarrow K^{*-}$	0.96 ± 0.08	arXiv:2403.12927
	$D^+ \rightarrow \omega$	1.05 ± 0.14	PRD101(2020)072005
	$D^+ \rightarrow f_0$	1.14 ± 0.28	arXiv:2401.13225
	$D^+ \rightarrow \rho^0$	0.88 ± 0.10	arXiv:2401.13225
	$D_S^+ \rightarrow \eta$	$0.984 \pm 0.028 \pm 0.016$	PRL132(2024)091802
	$D_S^+ \rightarrow \eta'$	$0.989 \pm 0.082 \pm 0.034$	
		$D_S^+ \rightarrow \phi$	0.94 ± 0.08
	$\Lambda_c^+ \rightarrow \Lambda$	$0.98 \pm 0.05 \pm 0.03$	PRD108(2023)L031105
τ/μ	$D^+ \rightarrow t^+ \nu$	3.02 ± 0.68	BESIII arXiv
	$D_S^+ \rightarrow t^+ \nu$	10.05 ± 0.35	PRL127(2021)171801

No deviation greater than 1.7σ is found!

$D \rightarrow Ae^+\nu_e$ 半轻衰变的研究

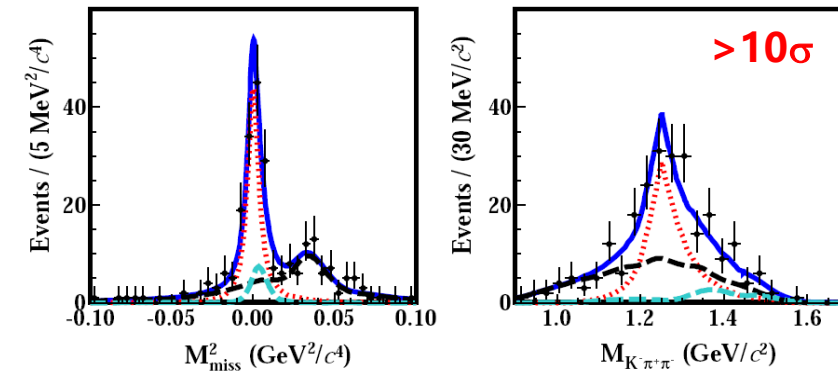
$D^+ \rightarrow \bar{K}_1^0(1270)e^+\nu_e$ PRL123(2019)231801



$$B_{D^+ \rightarrow \bar{K}_1^0(1270)e^+\nu_e} = (2.30 \pm 0.26 \pm 0.18 \pm 0.25) \times 10^{-3}$$

Helps to test various theoretical calculations which are sensitive to K_1 mixing angle

$D^0 \rightarrow K_1(1270)^-e^+\nu_e$ PRL127(2021)131801

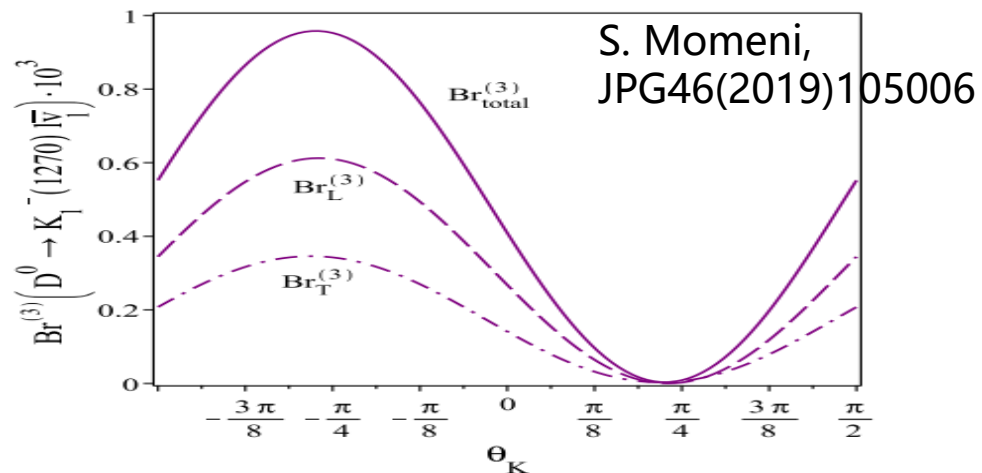


$$B_{D^0 \rightarrow K_1(1270)^-e^+\nu_e} = (1.09 \pm 0.13 \pm 0.13 \pm 0.12) \times 10^{-3}$$

New window to explore the property and nature of K_1 and K_1 mixing angle

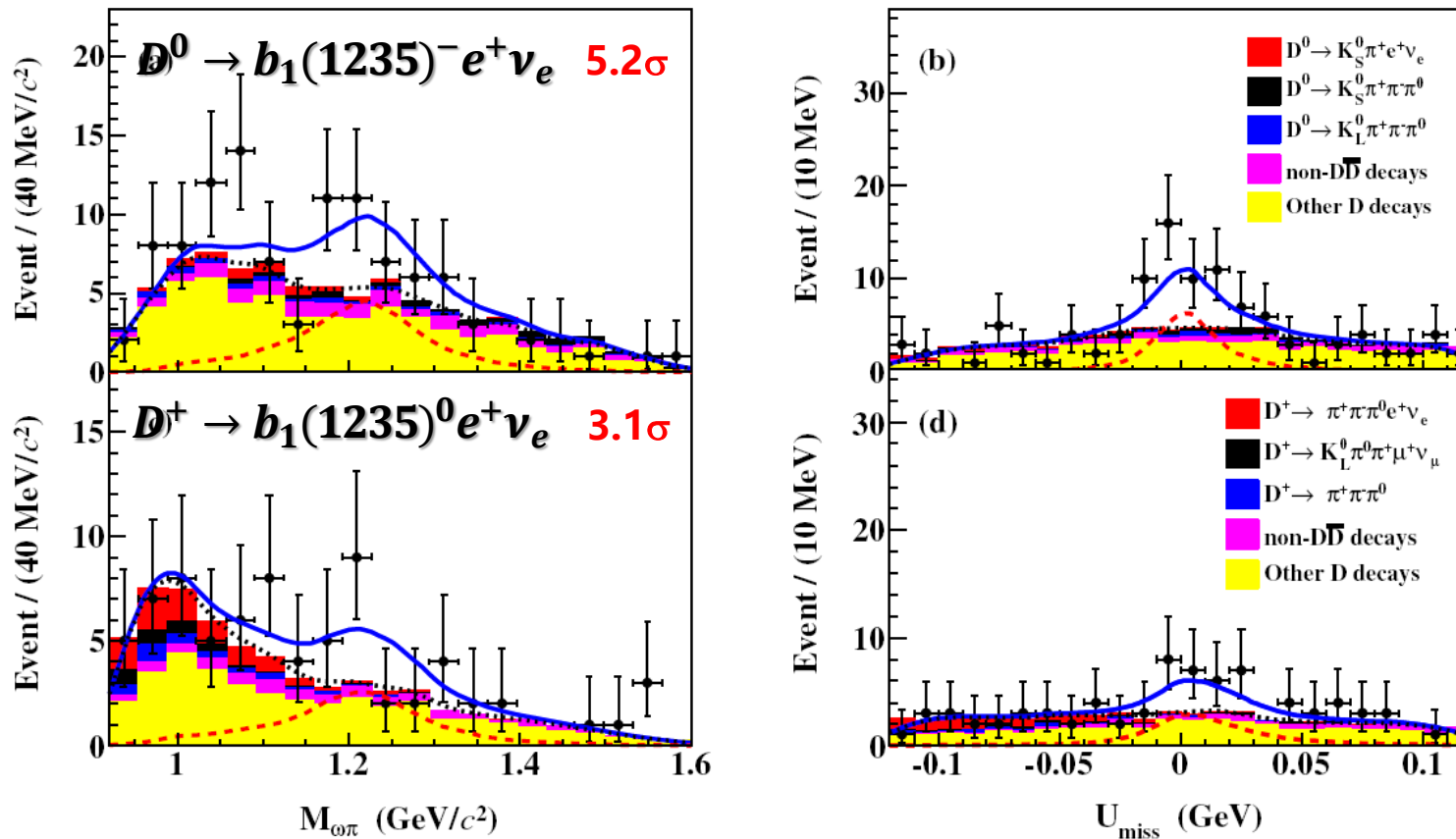
Combined analysis of $D \rightarrow \bar{K}_1 e^+ \nu$ and $B \rightarrow \gamma \bar{K}_1$ helps to constrain new physics effect in the studies of photon polarization in $b \rightarrow s \gamma$ process

Wei Wang et al. PRL125(2020)051802



Observation of $D \rightarrow Ae^+\nu_e$

arXiv:2407.20551



$$\mathcal{B}(D^0 \rightarrow b_1(1235)^- e^+ \nu_e) \times \mathcal{B}(b_1(1235)^- \rightarrow \omega \pi^-) = (0.72 \pm 0.18_{-0.08}^{+0.06}) \times 10^{-4}$$

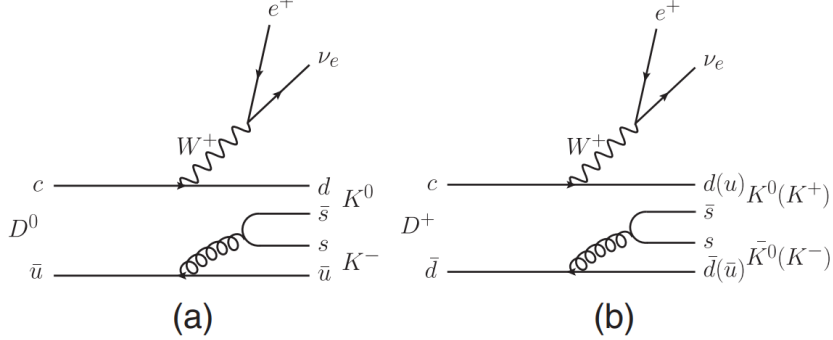
$$\mathcal{B}(D^+ \rightarrow b_1(1235)^0 e^+ \nu_e) \times \mathcal{B}(b_1(1235)^0 \rightarrow \omega \pi^0) = (1.16 \pm 0.44 \pm 0.16) \times 10^{-4}$$

支持 $\omega\pi$ 是 b_1 主导衰变模式

$$\frac{\Gamma(D^0 \rightarrow b_1^- e^+ \nu_e)}{2\Gamma(D^+ \rightarrow b_1^0 e^+ \nu_e)} = 0.78 \pm 0.19_{-0.05}^{+0.04}$$

$D \rightarrow KKe^+\nu_e$ 半轻衰变的寻找

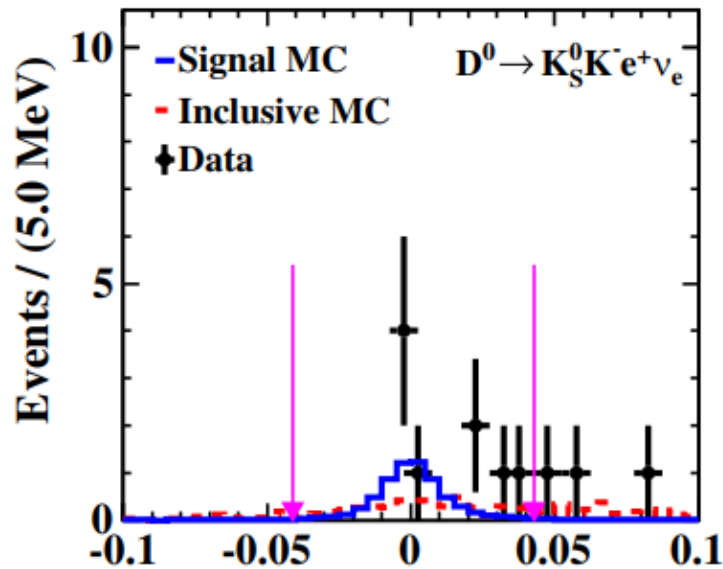
7.9 fb⁻¹ @3.773 GeV



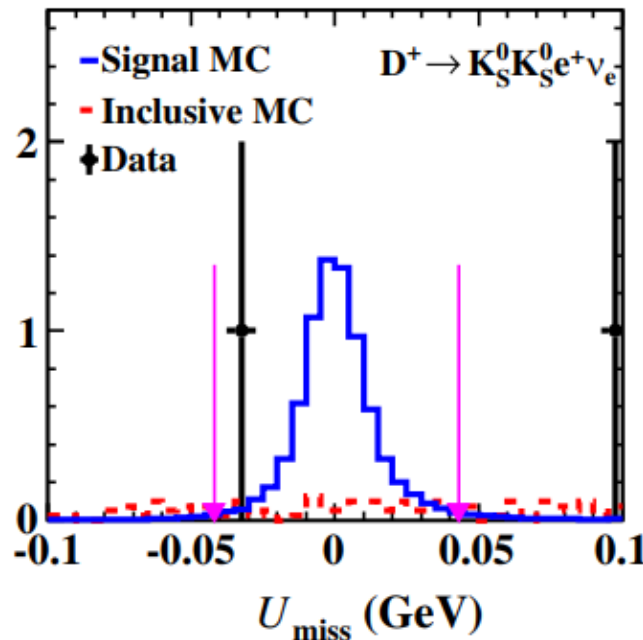
PRL121(2018)081802

BFs	$a_0(980)[\rightarrow \pi\eta]e^+\nu_e$ [7] ($\times 10^{-4}$)	$a_0(980)[\rightarrow K_S^0 K^-]e^+\nu_e$ ($\times 10^{-5}$)	$a_0(980)[\rightarrow K_S^0 K_S^0]e^+\nu_e$ ($\times 10^{-5}$)	$a_0(980)[\rightarrow K^+ K^-]e^+\nu_e$ ($\times 10^{-5}$)
D^0	$1.33^{+0.33}_{-0.29} \pm 0.09$	$1.14^{+0.28}_{-0.24} \pm 0.07$
D^+	$1.66^{+0.81}_{-0.66} \pm 0.11$...	$0.71^{+0.34}_{-0.28} \pm 0.05$	$2.86^{+1.39}_{-1.13} \pm 0.19$

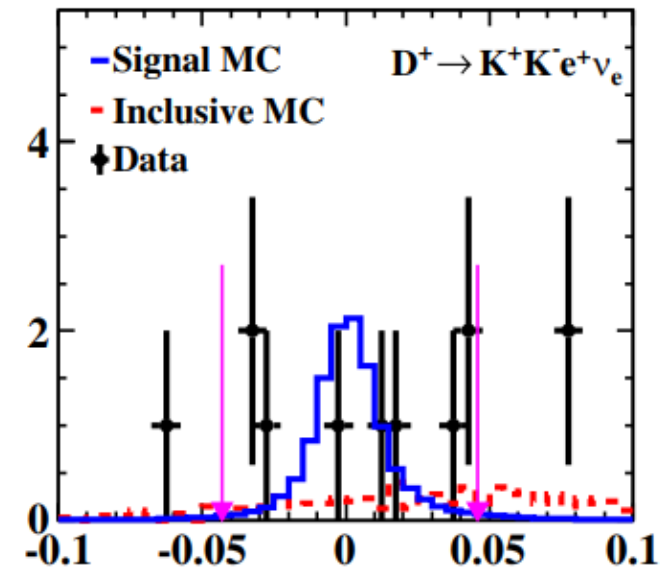
PRD109(2024)070032



$$B_{D^0 \rightarrow K_S^0 K^- e^+ \nu_e} < 2.13 \times 10^{-4}$$



$$B_{D^+ \rightarrow K_S^0 K_S^0 e^+ \nu_e} < 1.53 \times 10^{-4}$$



$$B_{D^+ \rightarrow K^+ K^- e^+ \nu_e} < 2.10 \times 10^{-4}$$

All @90% CL

$D \rightarrow K\eta e^+ \nu_e$ 和 $D \rightarrow \eta\eta e^+ \nu_e$ 的寻找

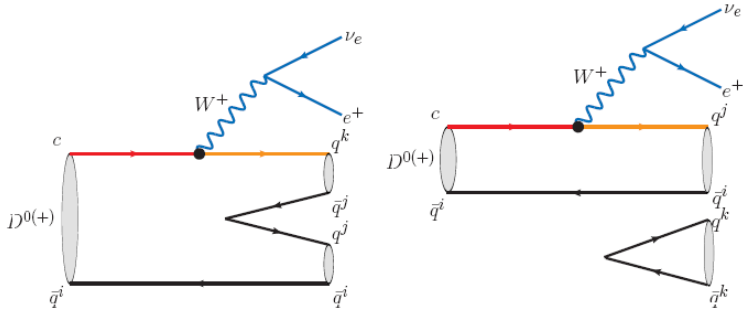
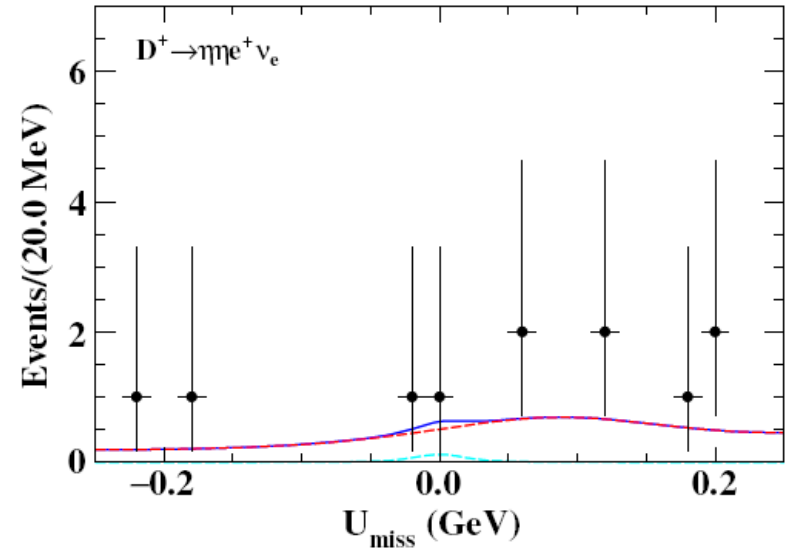
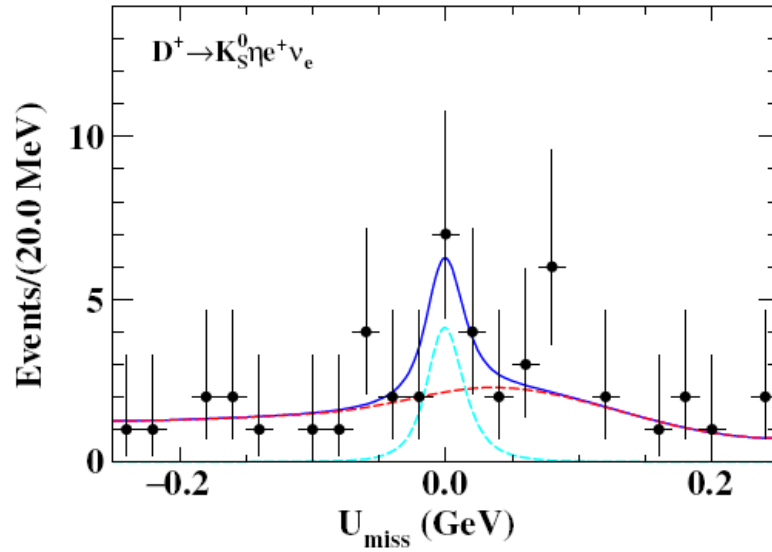
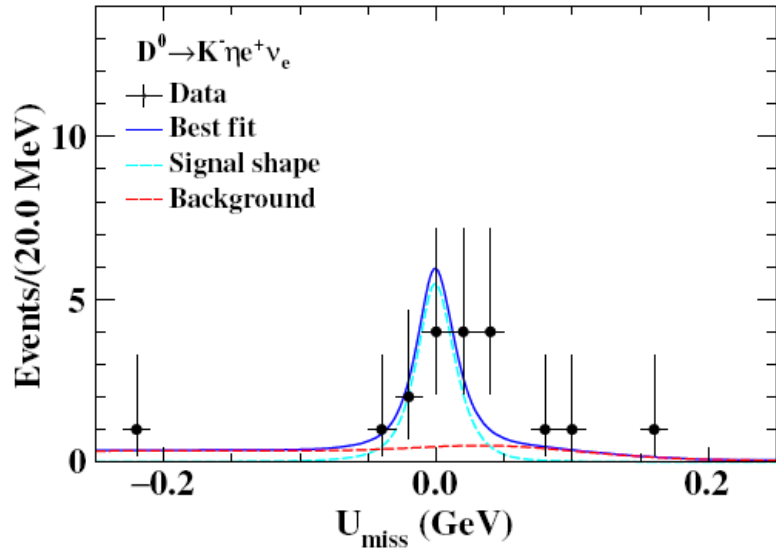


Table 1. The branching fractions of $D^0 \rightarrow K^- \eta e^+ \nu_e$, $D^+ \rightarrow \bar{K}^0 \eta e^+ \nu_e$ and $D^+ \rightarrow \eta \eta e^+ \nu_e$ predicted using SU(3) flavor symmetry [5].

Decay	$D^0 \rightarrow K^- \eta e^+ \nu_e$	$D^+ \rightarrow \bar{K}^0 \eta e^+ \nu_e$	$D^+ \rightarrow \eta \eta e^+ \nu_e$
Value ($\times 10^{-6}$)	3.51 ± 3.51	8.9 ± 8.9	3.16 ± 2.26

7.9 fb⁻¹
@3.773 GeV

arXiv:2409.15044



Decay	$N_{\text{sig}}^{\text{fit}}$	Significance (σ)	$N_{\text{sig}}^{\text{up}}$	$\bar{\epsilon}_{\text{SL}}$ (%)	$\mathcal{B} (\times 10^{-4})$	$\mathcal{B}^{\text{up}} (\times 10^{-4})$
$D^0 \rightarrow K^- \eta e^+ \nu_e$	$11.1^{+4.5}_{-3.8}$	3.3	...	5.29 ± 0.05	$0.84^{+0.34}_{-0.29} \pm 0.22$...
$D^+ \rightarrow K_S^0 \eta e^+ \nu_e$	$8.4^{+4.7}_{-3.9}$	1.9	17.8	7.79 ± 0.05	...	< 2.0
$D^+ \rightarrow \eta \eta e^+ \nu_e$	$0.3^{+1.9}_{-1.2}$	0.0	4.8	7.52 ± 0.05	...	< 1.0

All @90% CL

总结

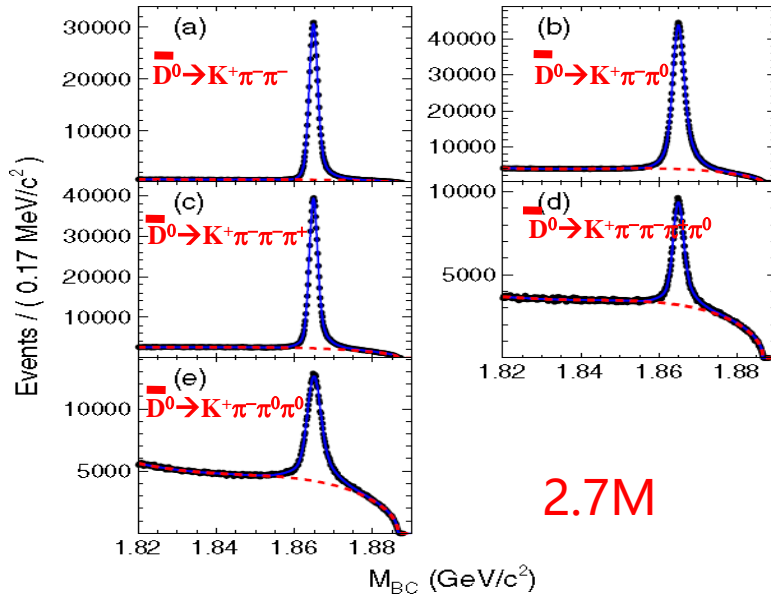
- 基于前期数据，BESIII粲介子含轻衰变的研究取得了一系列重要成果。
- BESIII上粲介子衰变常数、形状因子、 $|V_{cs}|$ 和 $|V_{cd}|$ 测量精度达到(0.3-1)%。
- 基于最新的、 20.3 fb^{-1} @3.773 GeV数据，第一批粲介子 $D^{0(+)}$ 重要的物理成果已于本周发布，更多结果将随后陆续推出。

谢谢!

Backup slides

Single-tag charmed hadrons at BESIII

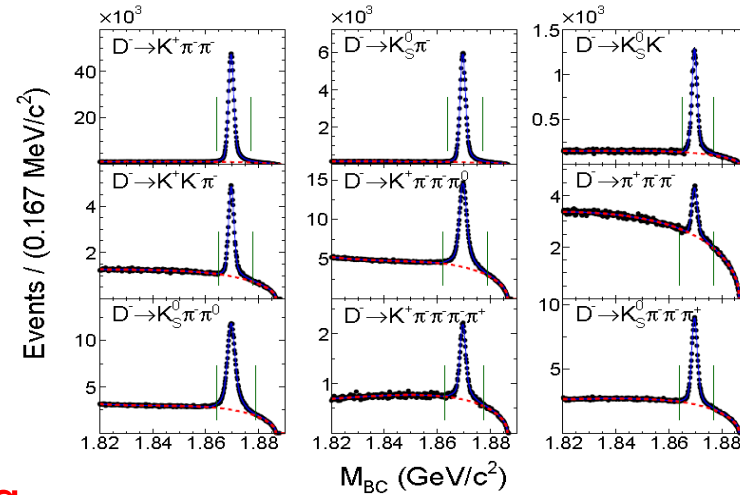
$$e^+e^- \rightarrow \psi(3770) \rightarrow D^0 \bar{D}^0$$



2.7M

2.93 → 20.3 fb⁻¹
@3.773 GeV

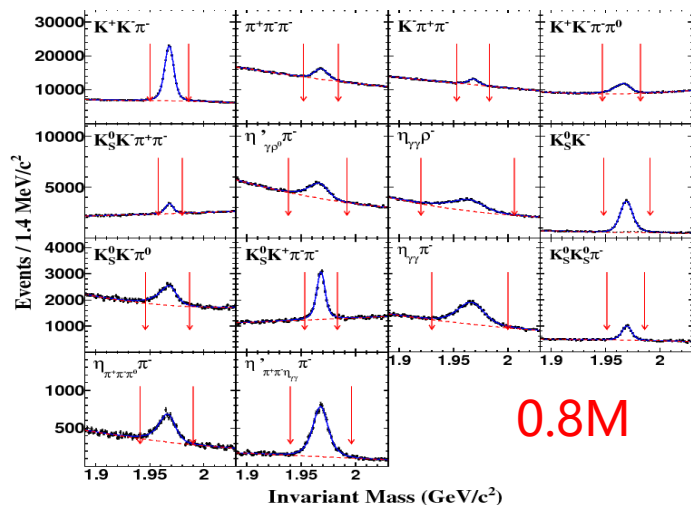
$$e^+e^- \rightarrow \psi(3770) \rightarrow D^+ D^-$$



2.93 → 20.3 fb⁻¹
@3.773 GeV

1.7M

$$e^+e^- \rightarrow \psi(4160) \rightarrow D_s^+ D_s^{*-} + c.c.$$

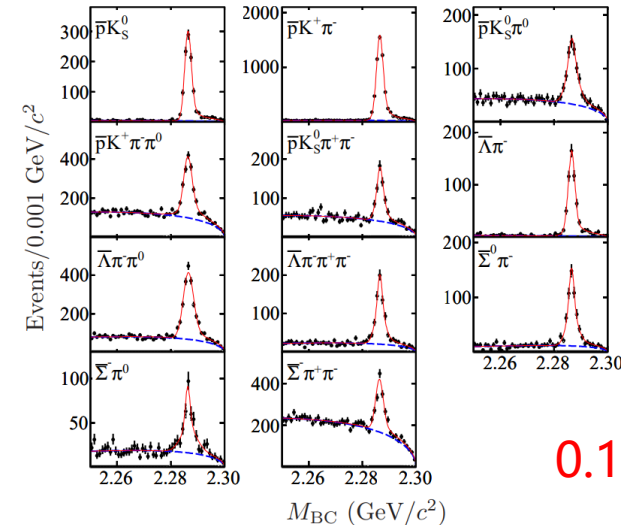


0.8M

7.33 fb⁻¹
@4.13-4.23 GeV

The single-tag yields of \bar{D}^0 , D^- , and D_s^- are 3.6, 3.6, and 9 times CLEO-c, respectively

$$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^- + c.c.$$

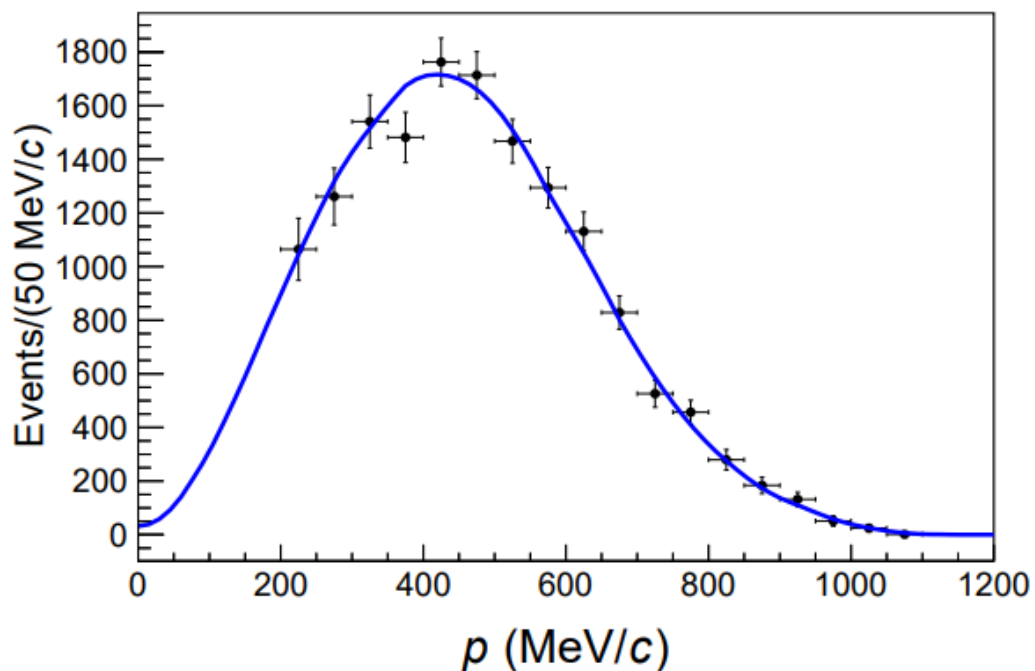


0.57 → 4.5 fb⁻¹
@4.6-4.7 GeV

0.12M

粲介子单举半轻衰变 $D_s^+ \rightarrow \nu_e e X$

PRD104(2021)012003



$$B_{D_s^+ \rightarrow \nu_e e X} = (6.30 \pm 0.13 \pm 0.10)\%$$

与此前最好精度的CLEO结果比, 统计误差改进3倍, 系统误差改进1.5倍

$$\Gamma_{D_s^+ \rightarrow \nu_e e X} / \Gamma_{D^0 \rightarrow \nu_e e X} = 0.790 \pm 0.016 \pm 0.020$$

与理论预期0.813 [J. L. Rosner PRD83(2011)034025]一致

已知遍举电子半轻衰变道的分支比[PDG2020]

$D_s^+ \rightarrow \phi e^+ \nu_e$	$(2.37 \pm 0.11)\%$
$D_s^+ \rightarrow \eta e^+ \nu_e$	$(2.32 \pm 0.08)\%$
$D_s^+ \rightarrow \eta' e^+ \nu_e$	$(0.80 \pm 0.07)\%$
$D_s^+ \rightarrow K^0 e^+ \nu_e$	$(0.34 \pm 0.04)\%$
$D_s^+ \rightarrow K^*(892)^0 e^+ \nu_e$	$(0.21 \pm 0.03)\%$
$D_s^+ \rightarrow f_0(980) e^+ \nu_e, f_0(980) \rightarrow \pi\pi$	$(0.30 \pm 0.05)\%$
Sum of semielectronic modes	$(6.34 \pm 0.17)\%$
$B(D_s^+ \rightarrow X e^+ \nu_e)$	$(6.52 \pm 0.42)\%$
$D_s^+ \rightarrow \tau^+ \nu_\tau \rightarrow e^+ \bar{\nu}_\tau \nu_e \nu_\tau$	$(0.96 \pm 0.04)\%$

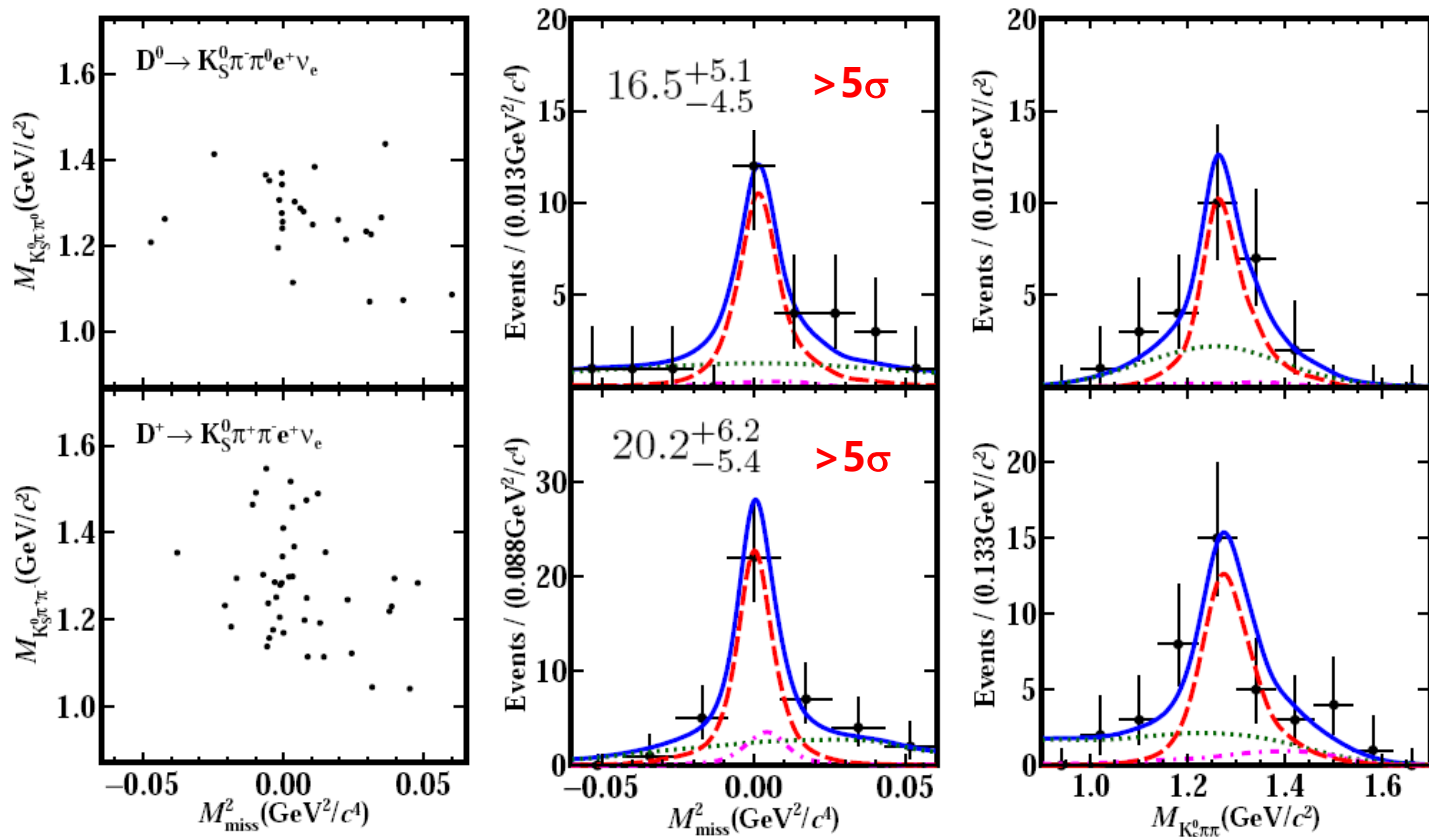
单举和遍举电子半轻衰变分支比之差:

$$\Delta B = (-0.04 \pm 0.23)\%$$

表明没有更多 D_s^+ 遍举电子半轻衰变

$D \rightarrow Ae^+\nu_e$ 半轻衰变的研究

arXiv:2403.19091

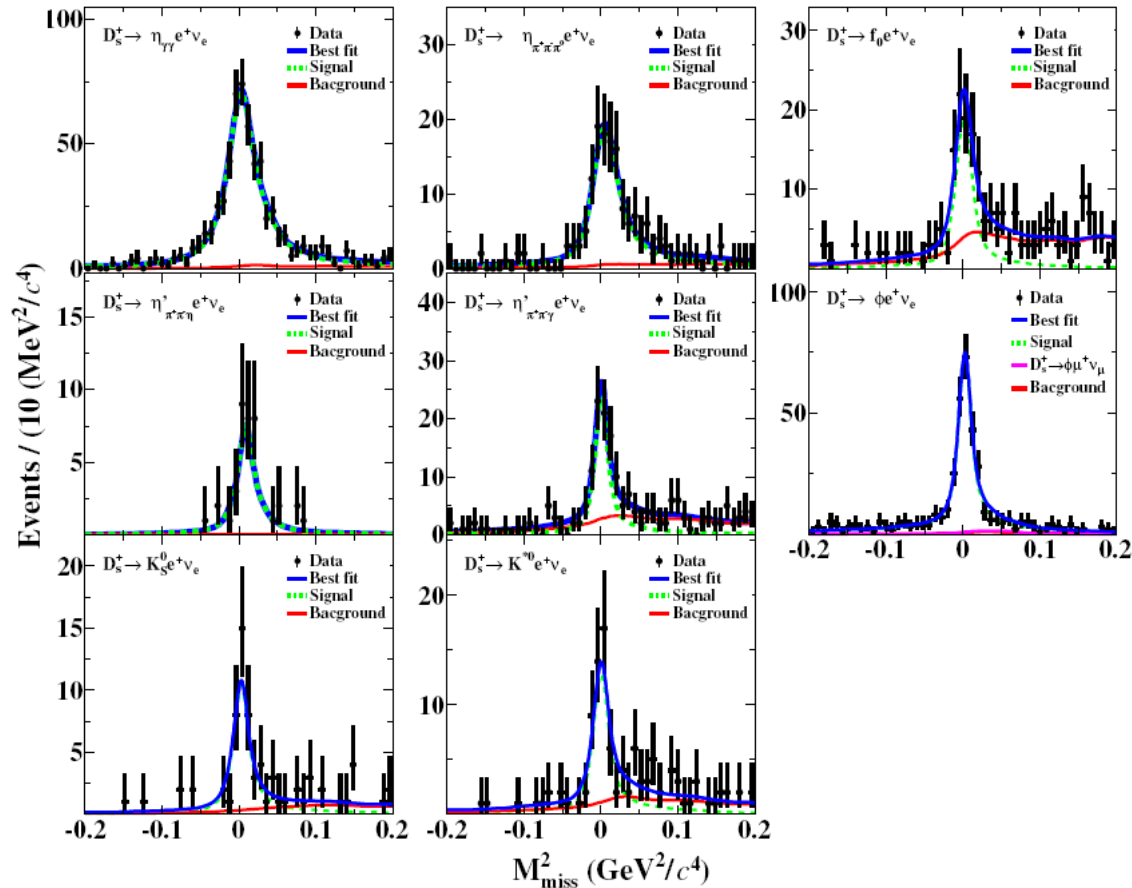


Decay mode	$\mathcal{B}_{\text{sig}} (\times 10^{-4})$	$\mathcal{B}_{\text{com}} (\times 10^{-4})$
$D^0 \rightarrow K_S^0 \pi^- \pi^0 e^+ \nu_e$	$(1.69^{+0.53}_{-0.46} \pm 0.18)$	/
$D^+ \rightarrow K_S^0 \pi^+ \pi^- e^+ \nu_e$	$(1.47^{+0.45}_{-0.40} \pm 0.20)$	/
$D^0 \rightarrow K_1(1270)^- e^+ \nu_e$	$(10.5^{+3.3}_{-2.8} \pm 1.2 \pm 1.2)$	$(10.8^{+1.3+0.8}_{-1.2-1.1} \pm 1.2)$
$D^+ \rightarrow \bar{K}_1(1270)^0 e^+ \nu_e$	$(12.9^{+4.0}_{-3.5} \pm 1.8 \pm 1.5)$	$(18.6^{+2.3}_{-2.2} \pm 1.3 \pm 2.1)$

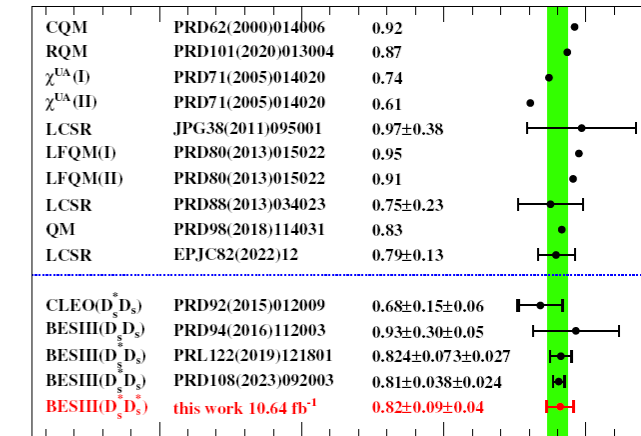
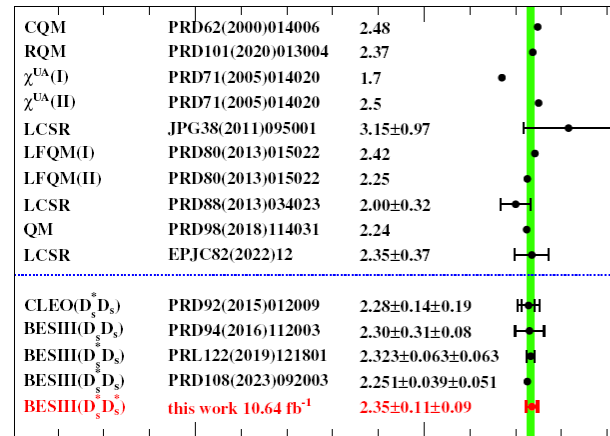
基于 $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$ 的 D_s^+ 半轻衰变的研究

基于4.23-4.7 GeV 10.6 fb^{-1} 数据, 挖掘现有及未来BESIII数据潜力

arXiv:2406.01332,
accepted by PRD



Decay	$\epsilon_{\text{sig}} (\%)$	N_{DT}	$\mathcal{B} (\%)$
$D_s^+ \rightarrow \eta_{\gamma\gamma} e^+ \nu_e$	50.78 ± 0.12	716.2 ± 33.8	$2.35 \pm 0.11 \pm 0.10$
$D_s^+ \rightarrow \eta_{\pi^+\pi^-\pi^0} e^+ \nu_e$	20.42 ± 0.08		
$D_s^+ \rightarrow \eta'_{\pi^+\pi^-\eta} e^+ \nu_e$	22.35 ± 0.07	133.7 ± 14.5	$0.82 \pm 0.09 \pm 0.04$
$D_s^+ \rightarrow \eta'_{\pi^+\pi^-\gamma} e^+ \nu_e$	32.48 ± 0.09		
$D_s^+ \rightarrow \phi_{K^+K^-} e^+ \nu_e$	25.48 ± 0.07	350.2 ± 24.5	$2.21 \pm 0.16 \pm 0.11$
$D_s^+ \rightarrow f_0 e^+ \nu_e$	46.24 ± 0.11	91.0 ± 14.1	$0.15 \pm 0.02 \pm 0.01$
$D_s^+ \rightarrow K^{\bar{0}} e^+ \nu_e$	46.21 ± 0.11	50.5 ± 8.4	$0.24 \pm 0.04 \pm 0.01$
$D_s^+ \rightarrow K^{0*} e^+ \nu_e$	41.78 ± 0.10	65.4 ± 10.9	$0.19 \pm 0.03 \pm 0.01$



$B(D_s^+ \rightarrow \eta e^+ \nu_e) (\%)$

$B(D_s^+ \rightarrow \eta' e^+ \nu_e) (\%)$