

# Latest results from the Muon g-2 Experiment at Fermilab

26th international symposium on spin physics  
(**SPIN2025**)

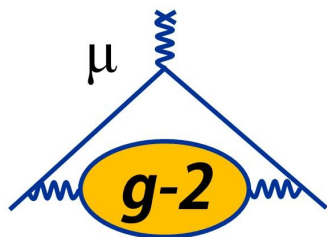
26 Sep 2025

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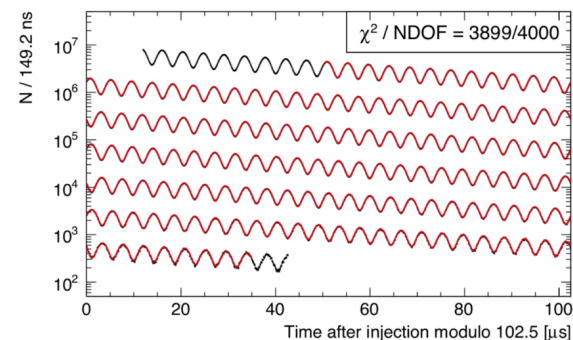
**Paolo Girotti** (INFN - LNF)  
on behalf of the Muon g-2 collaboration

# Overview

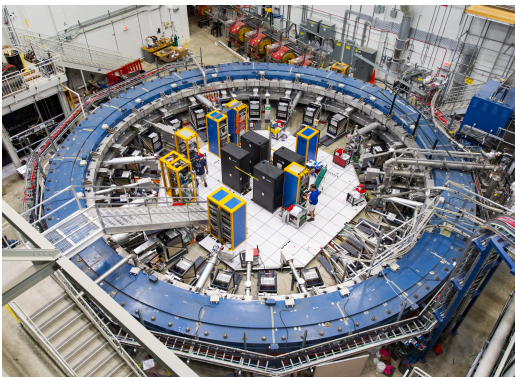
## The Muon g-2



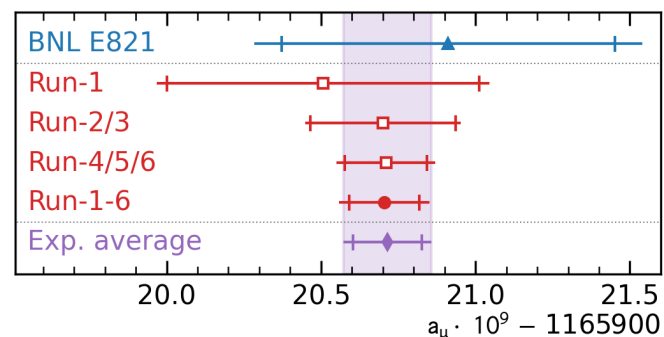
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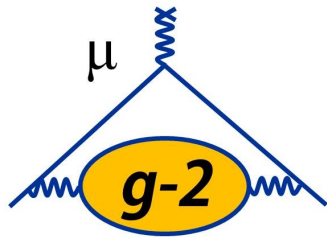
## Latest results and overlook



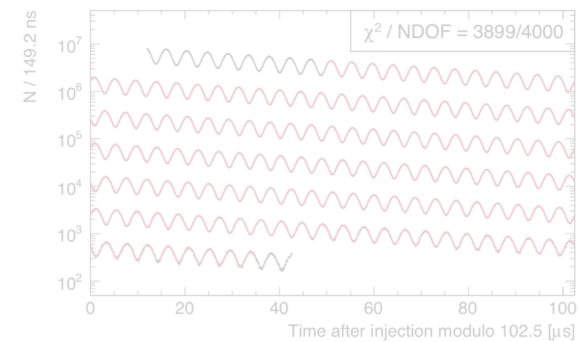


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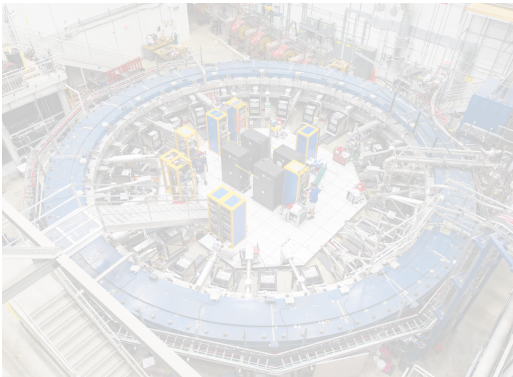
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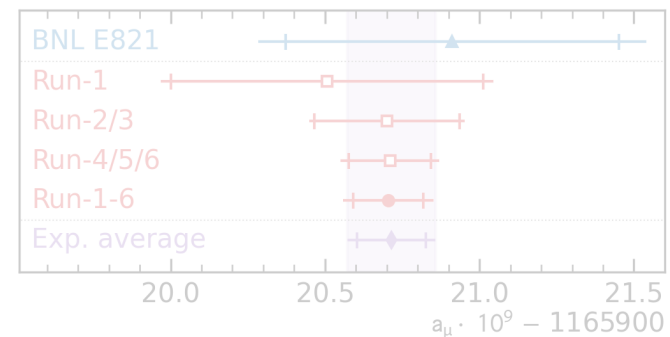
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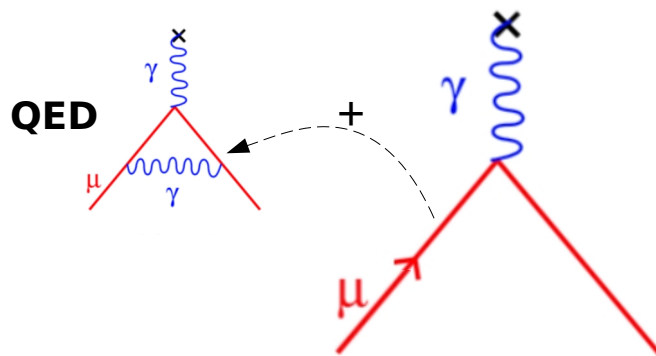




# The muon **g-2**

$$\vec{\mu} = \underset{\uparrow}{g} \frac{q}{2m} \vec{S}$$

- The magnetic moment of the muon is proportional to the **g**-factor
- g** encodes all the possible virtual interactions between the muon and the magnetic field
  - With no virtual quantum interactions, **g=2**
  - Considering the entire Standard Model, **g=2.002331...**



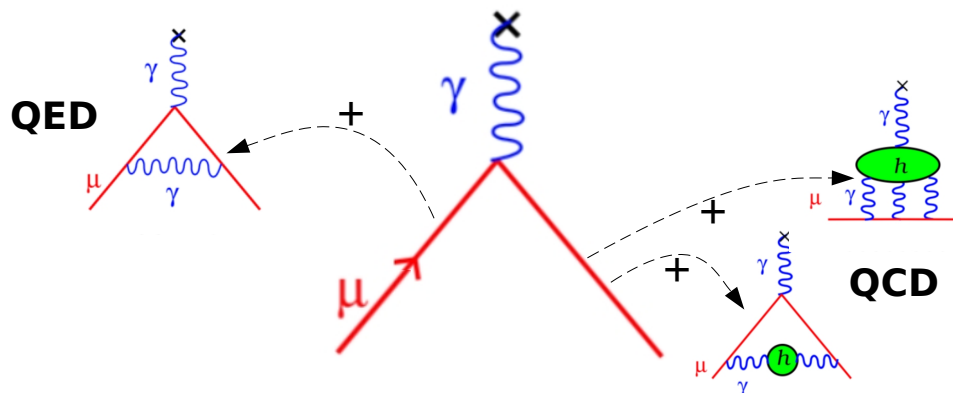
$\approx 2.4 \text{ MeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$  up	$\approx 1.275 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$  charm	$\approx 172.44 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$  top	$0$ $0$ $1$  gluon	$\approx 125.09 \text{ GeV}/c^2$ $0$ $0$ $0$  Higgs
$\approx 4.8 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$  down	$\approx 95 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$  strange	$\approx 4.18 \text{ GeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$  bottom	$0$ $0$ $1$  photon	SCALAR BOSONS
$\approx 0.511 \text{ MeV}/c^2$ $-1$ $\frac{1}{2}$  electron	$\approx 105.67 \text{ MeV}/c^2$ $-1$ $\frac{1}{2}$  muon	$\approx 1.7768 \text{ GeV}/c^2$ $-1$ $\frac{1}{2}$  tau	$\approx 91.19 \text{ GeV}/c^2$ $0$ $1$ $1$  Z boson	
$\approx 2.2 \text{ eV}/c^2$ $0$ $\frac{1}{2}$  electron neutrino	$\approx 1.7 \text{ MeV}/c^2$ $0$ $\frac{1}{2}$  muon neutrino	$\approx 15.5 \text{ MeV}/c^2$ $0$ $\frac{1}{2}$  tau neutrino	$\approx 80.39 \text{ GeV}/c^2$ $\pm 1$ $1$ $1$  W boson	

GAUGE BOSONS

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GAUGE BOSONS

SCALAR BOSONS



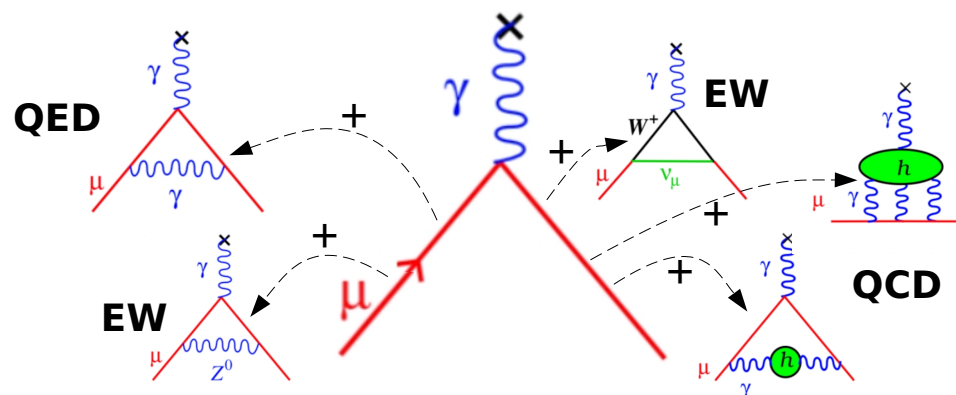
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Aoyama et al. (2020)

<https://doi.org/10.1016/j.physrep.2020.07.006>



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GAUGE BOSONS

SCALAR BOSONS

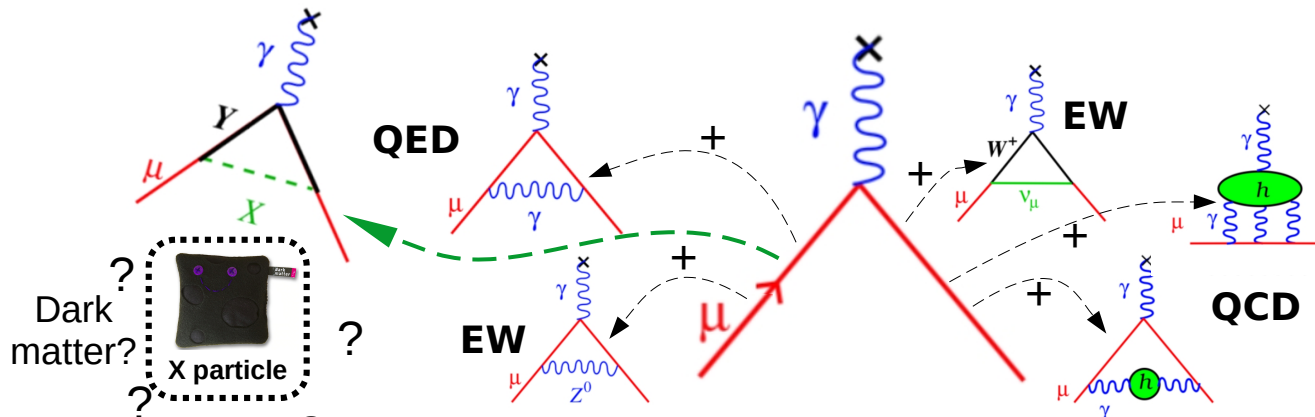
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  - Is there something else?

Aoyama et al. (2020)

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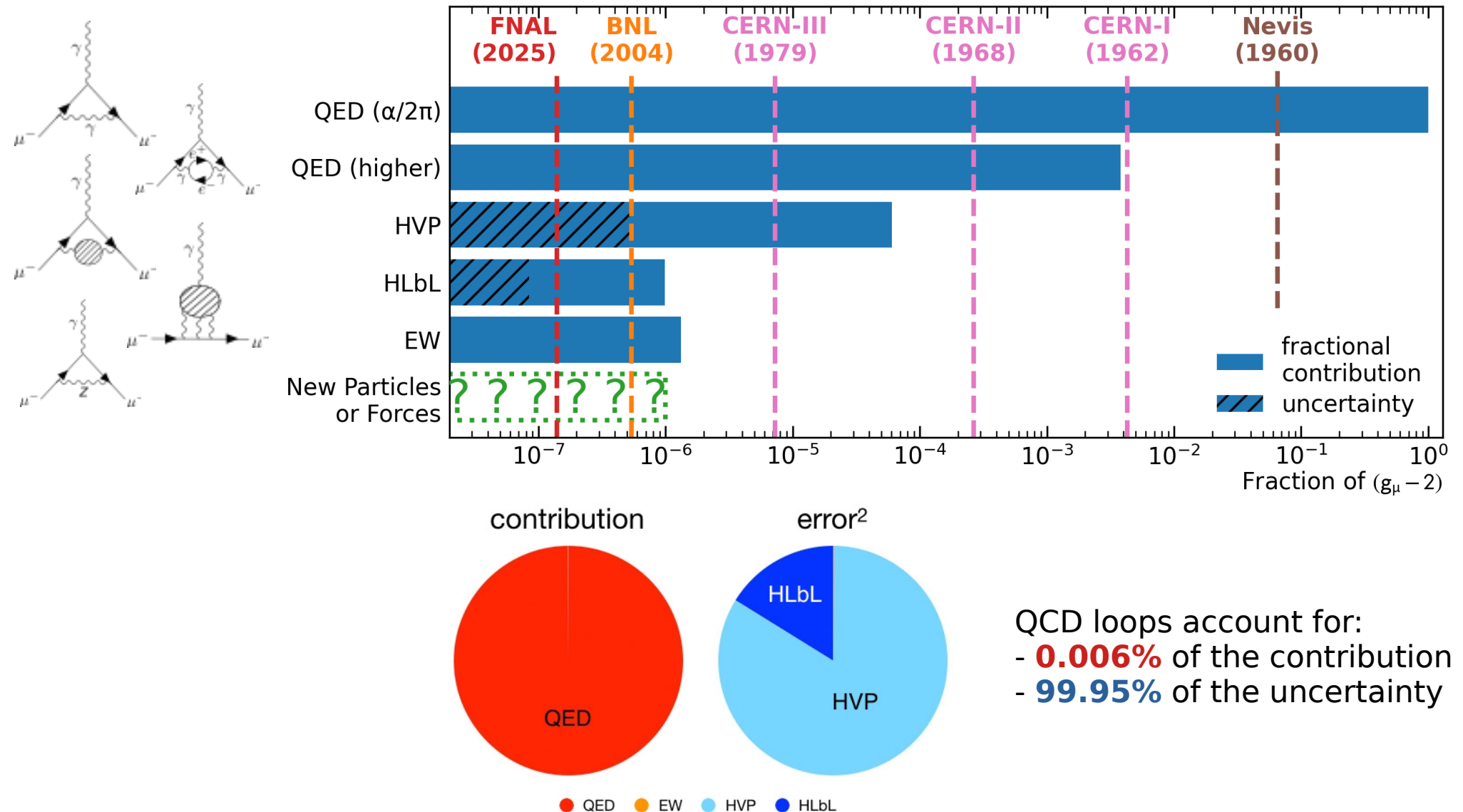
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SCALAR BOSONS

GAUGE BOSONS



# SM contributions



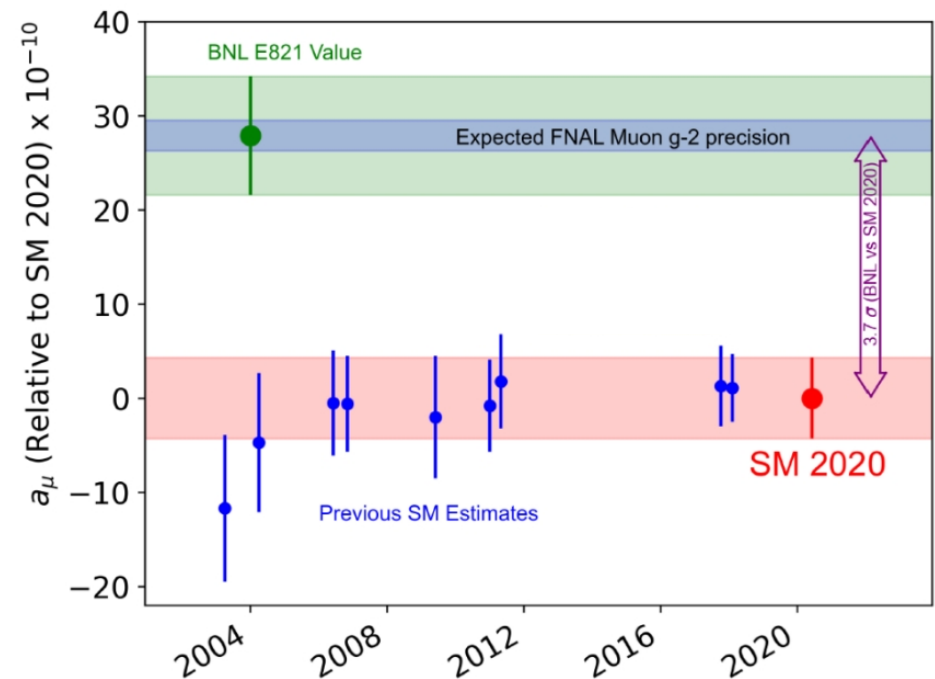
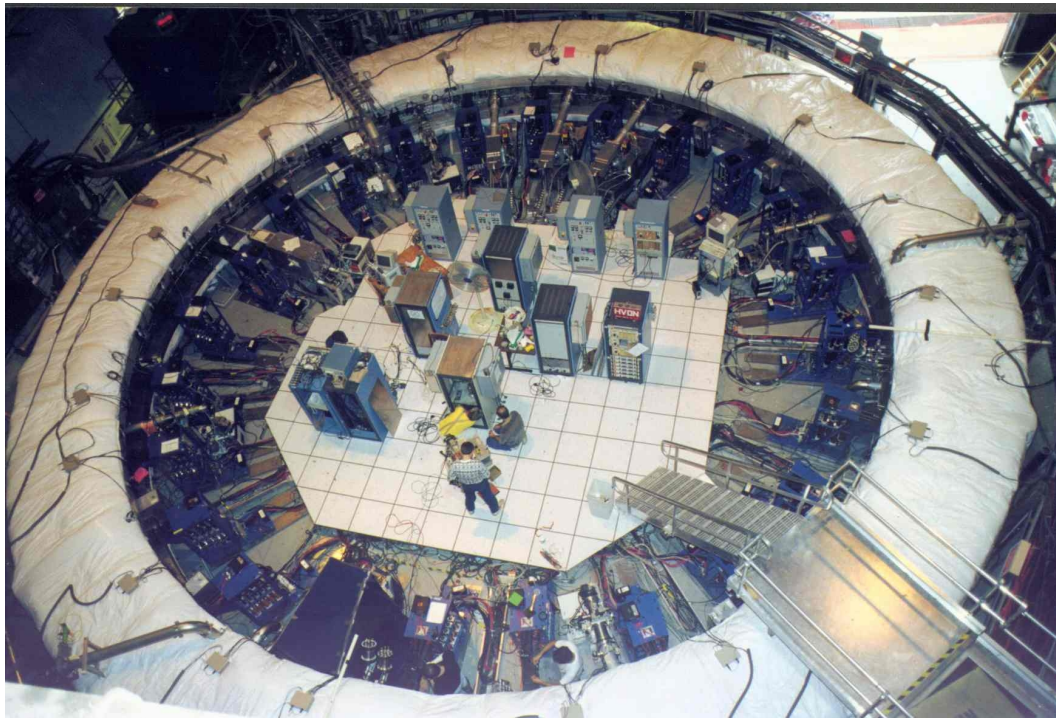
# Yes but why muons?

- Elementary fermion
  - Higher mass than electron  $\rightarrow$  enhanced sensitivity to new heavy particles
- Series of “gifts” from nature facilitate experiments:
  - Pion decay produces highly polarized muons  $\rightarrow$  **polarizer**
  - Decay  $e^{+/-}$  encodes the muon’s spin information  $\rightarrow$  **polarimeter**
  - Magic momentum of 3.1 GeV/c cancels effects from external electric fields
- Long enough lifetime to be stored and measured
- Many measurements and calculations since the ‘50s
  - Still a very active research topic



# BNL measurement

- 2006 → Tantalizing hint of new physics at  $3.7\sigma$
- 2009 → proposal to build new experiment at Fermilab by recycling BNL's magnet



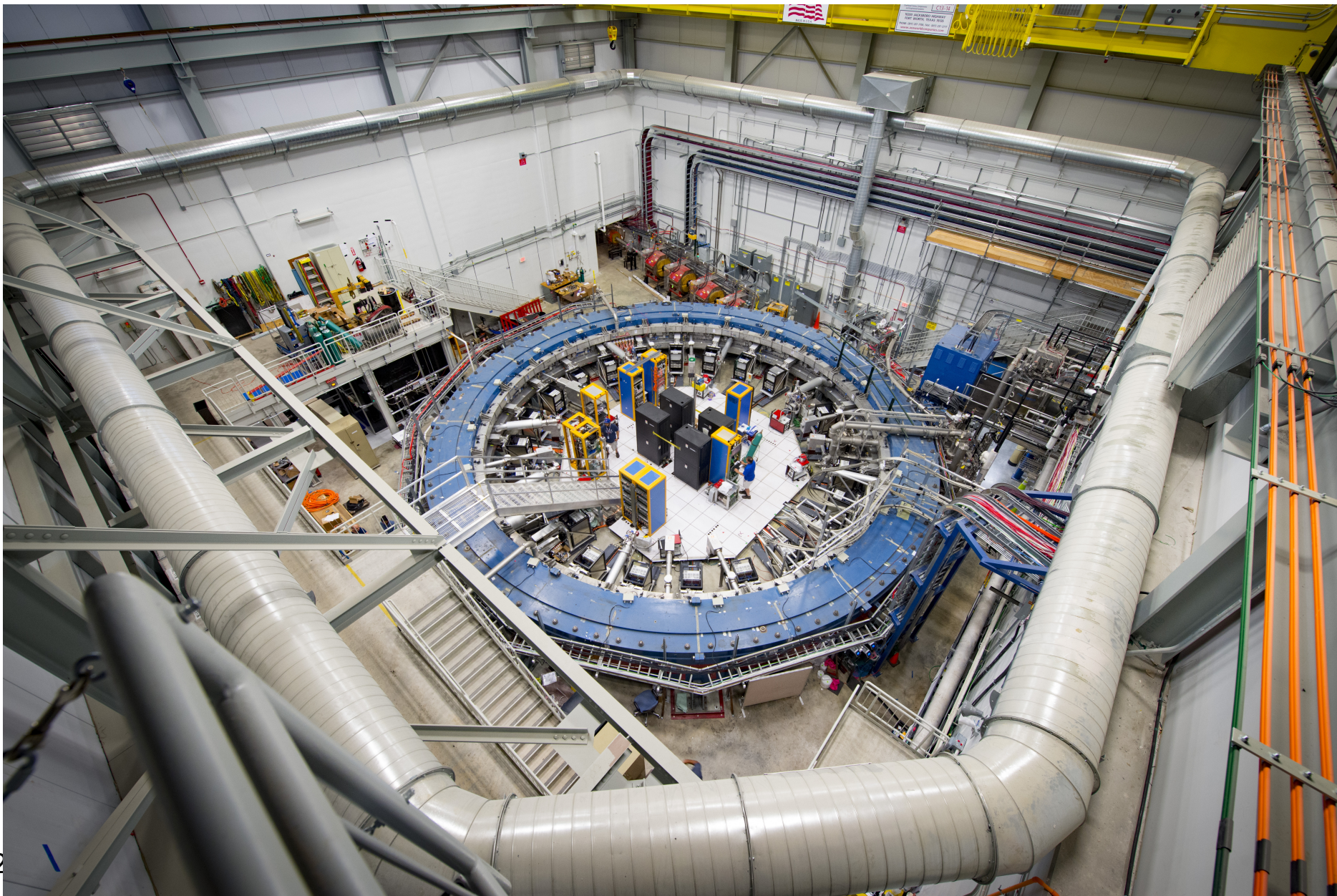
# The big move

- 50 ton package shipped from Brookhaven (BNL) to Fermilab (FNAL) on the summer of 2013
- **35 days** and 5000+ km on water and land



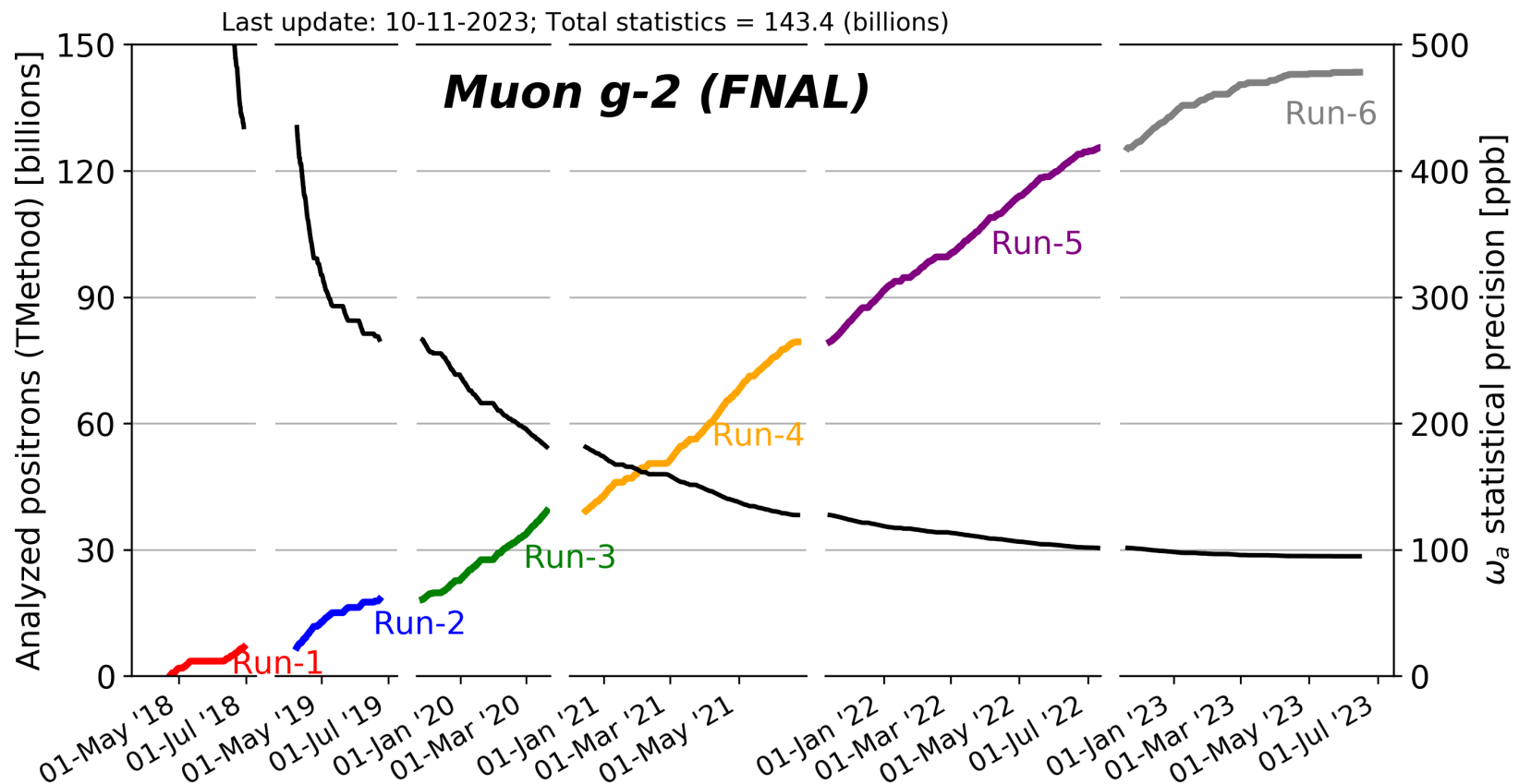
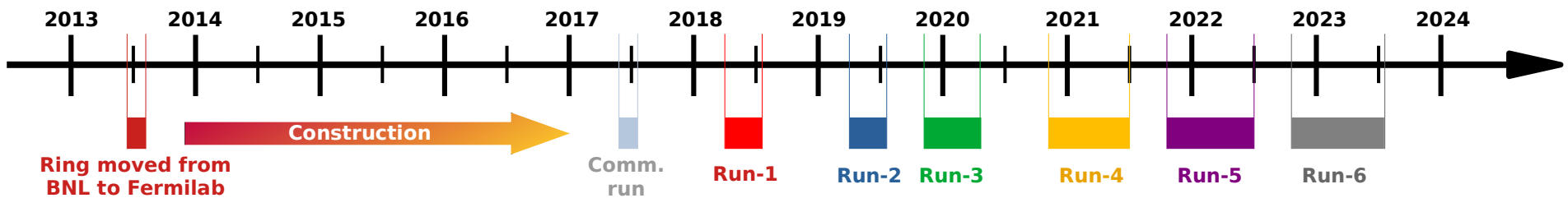


# FNAL (2013-2025)



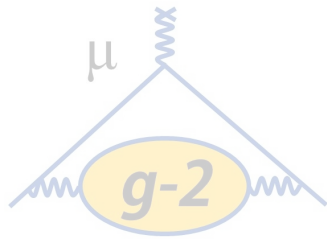


# Six years of beam data

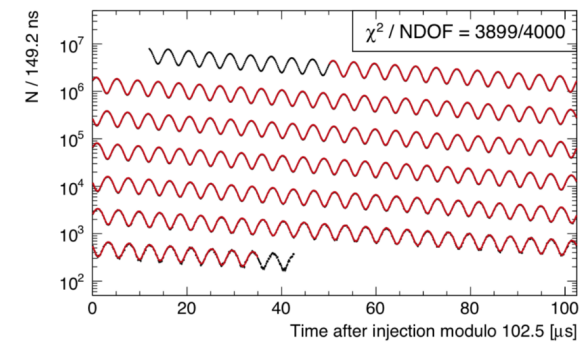


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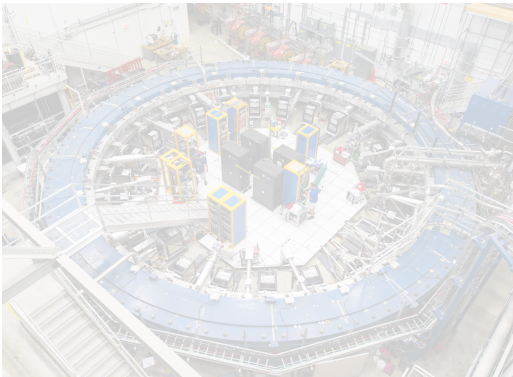
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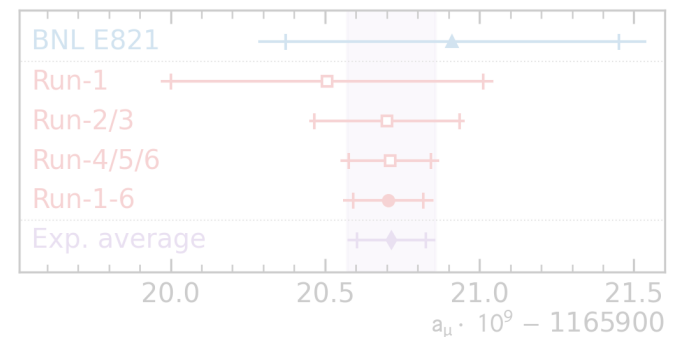
## Experimental principles



## The Muon g-2 Experiment at Fermilab

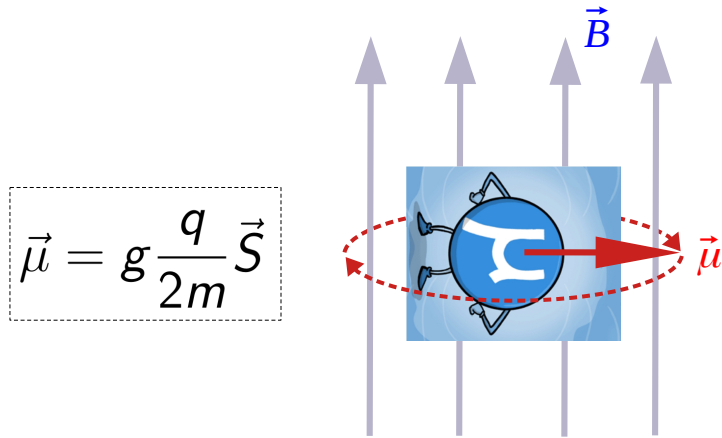


## Latest results and overlook





# Experimental principle

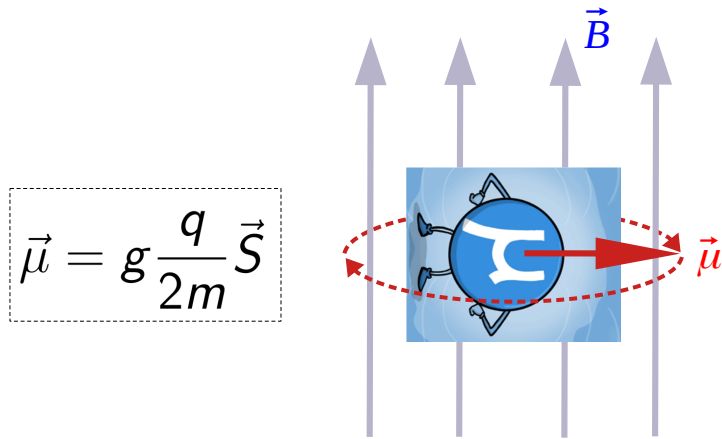


- In a magnetic storage ring, the muon spin **precesses** slightly faster than its **cyclotron** frequency

$$\underline{\vec{\omega}_s} = -\frac{ge\vec{B}}{2m} - (1 - \gamma)\frac{e\vec{B}}{m\gamma} \quad \underline{\vec{\omega}_c} = -\frac{e\vec{B}}{m\gamma}$$

- If we do the difference we get...

# Experimental principle



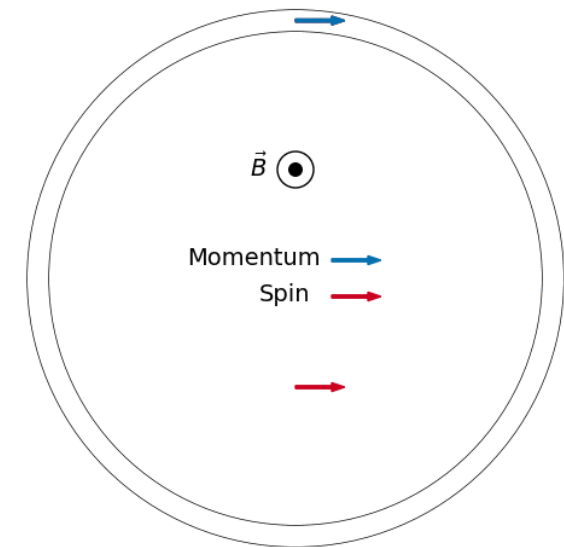
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- If we do the difference we get...

$$\vec{\omega}_a = \underline{\vec{\omega}_s} - \underline{\vec{\omega}_c} = -\left(\frac{g-2}{2}\right)\frac{e\vec{B}}{m} \equiv -\boxed{a_\mu}\frac{e\vec{B}}{m}$$

- This “anomalous” precession frequency is proportional to g-2 and to the magnetic field
- $\omega_a$  is entirely due to the virtual interactions between the muon and the field
- Measure  $\omega_a$  and  $\mathbf{B} \rightarrow$  obtain  $\boxed{\mathbf{a}_\mu}$



# Experimental principle

$$\vec{\omega}_a = -a_\mu \frac{e\vec{B}}{m}$$

In a real experiment:

- Electric fields needed for vertical focusing
- Muon's orbit can be slightly tilted

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$$\vec{\omega}_a = -\frac{e}{m} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} - a_\mu \frac{\gamma}{\gamma + 1} (\vec{\beta} \cdot \vec{B}) \vec{\beta} \right]$$

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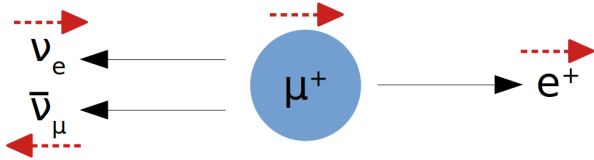
=0 for  
p = 3.094 GeV/c

=0 for  
planar orbits

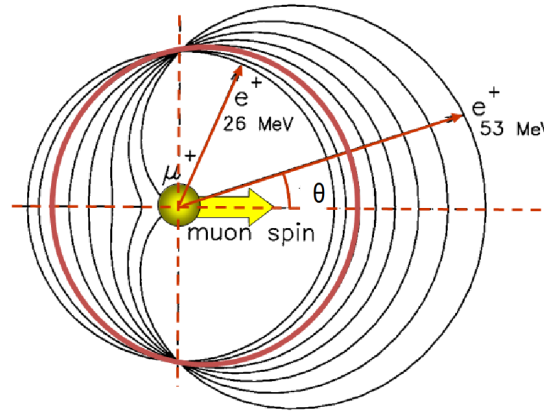
- Any small deviation from perfect momentum and orbit can be measured and corrected at analysis stage



# Parity violation

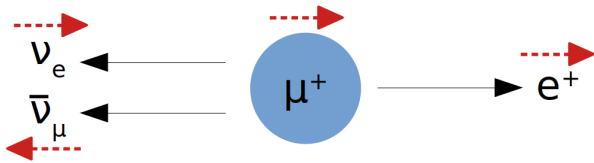


Muon decays in a positron and 2 neutrinos

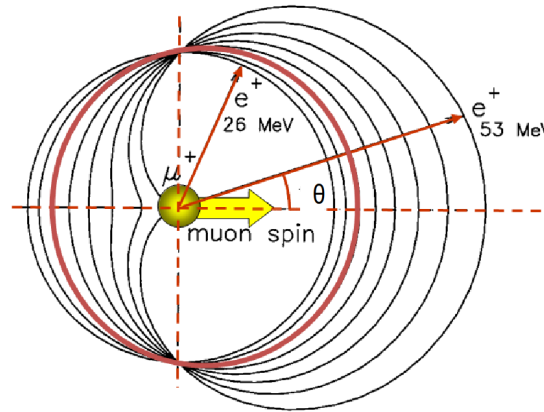


Parity violation  $\rightarrow$  positrons in CM preferably in the direction of the muon spin

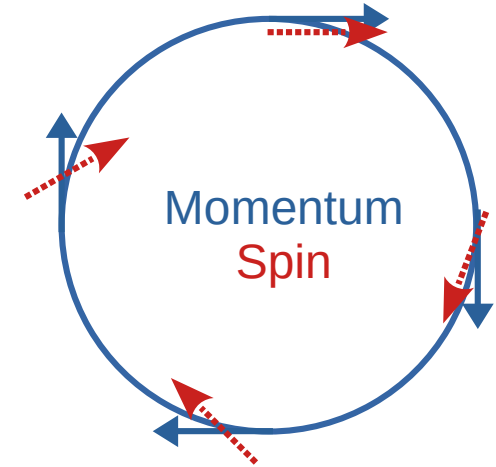
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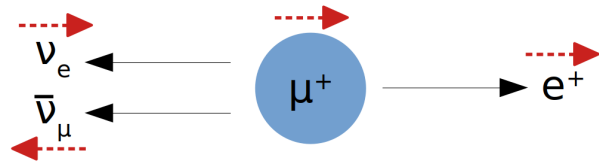


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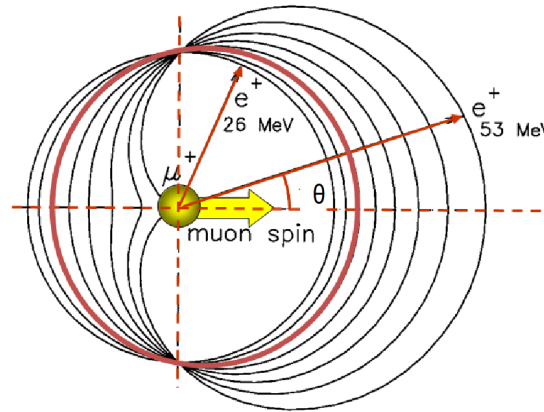


Spin precession  $\rightarrow$  the energy spectrum in the lab frame **oscillates** through time

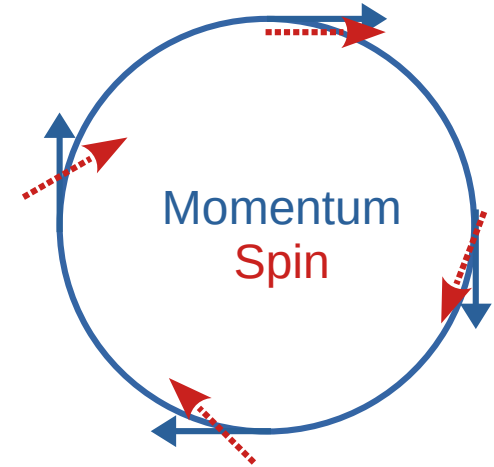
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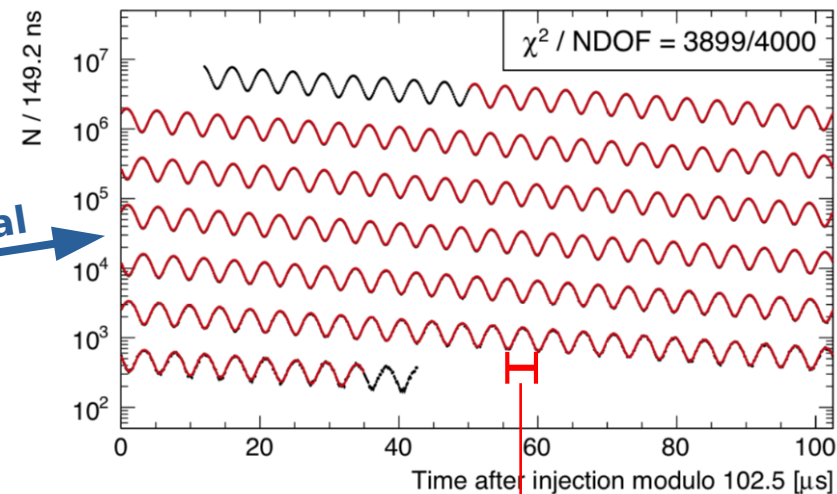
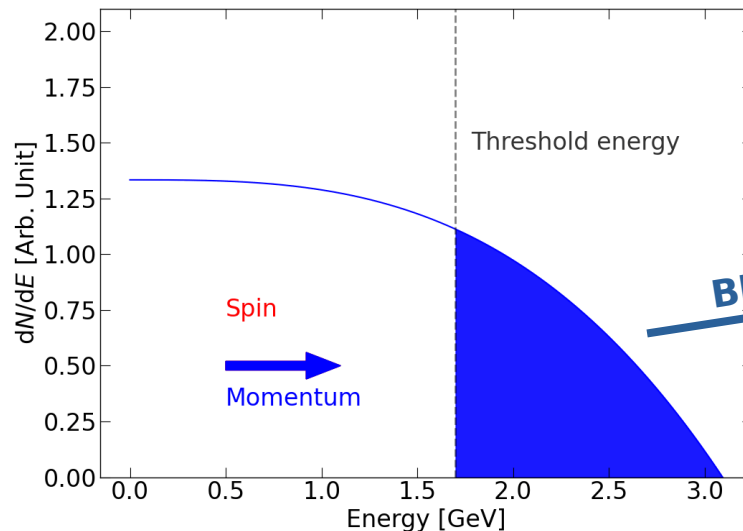
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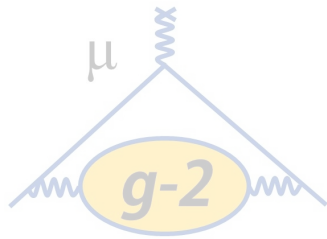


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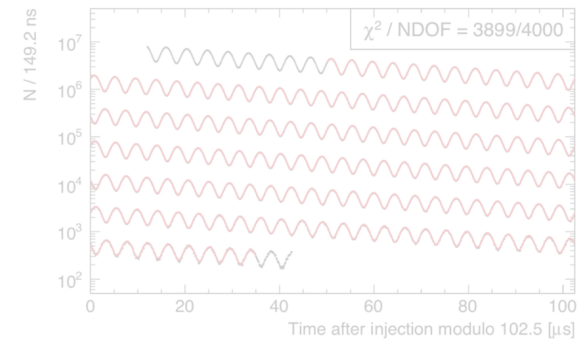


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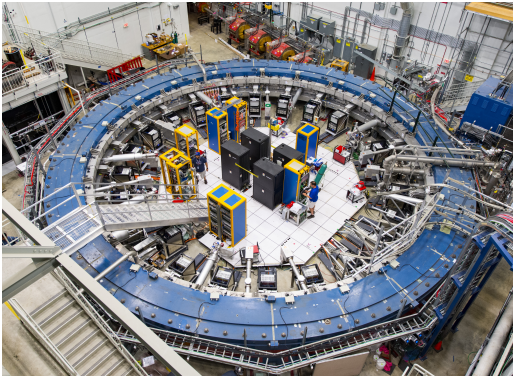
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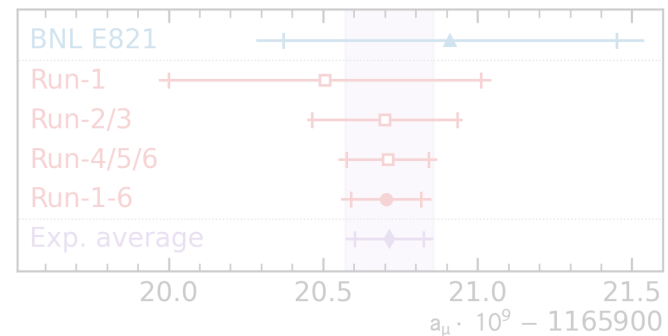
## Experimental principles



## The Muon g-2 Experiment at Fermilab



## Latest results and overlook

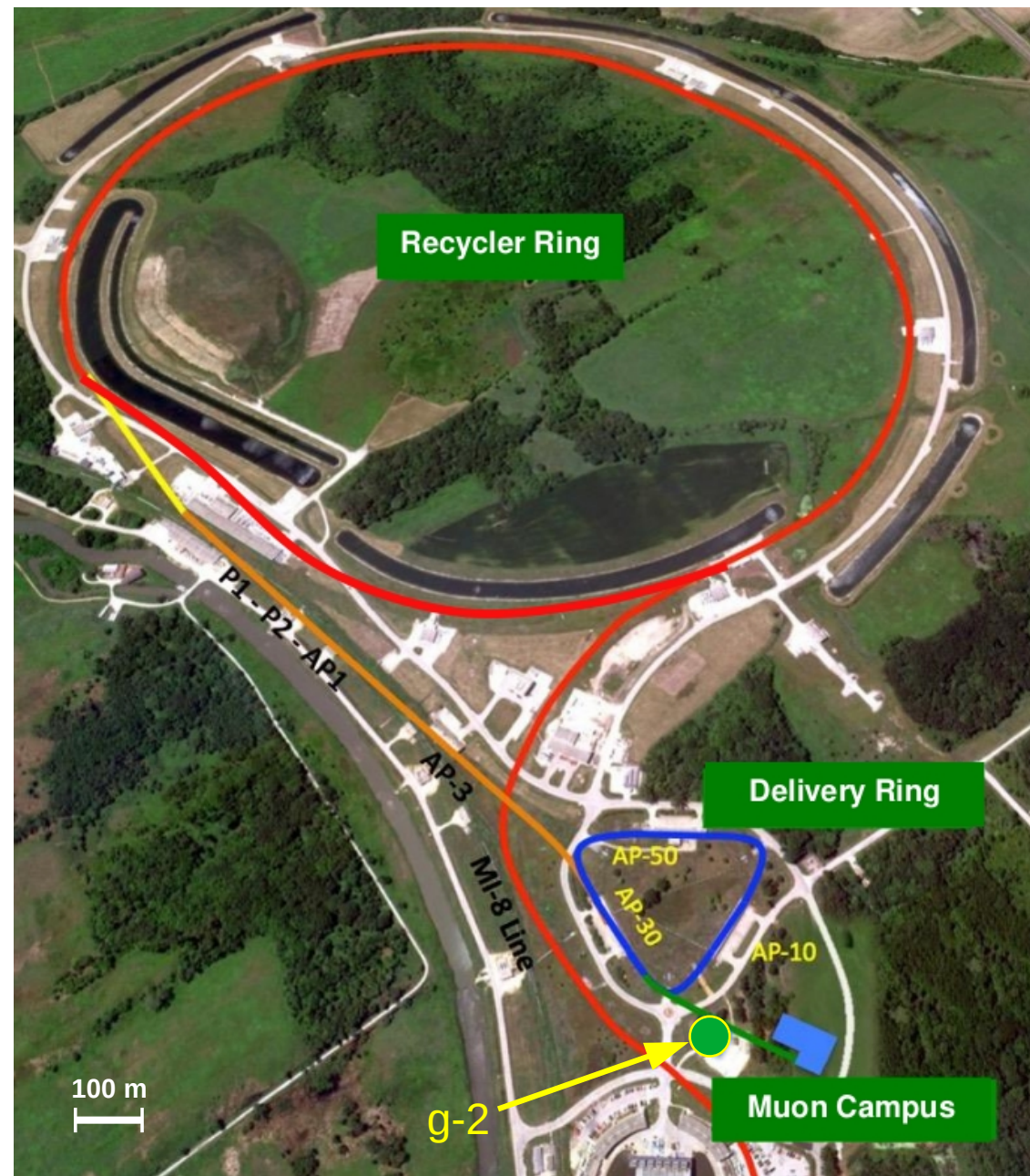




# Muon source

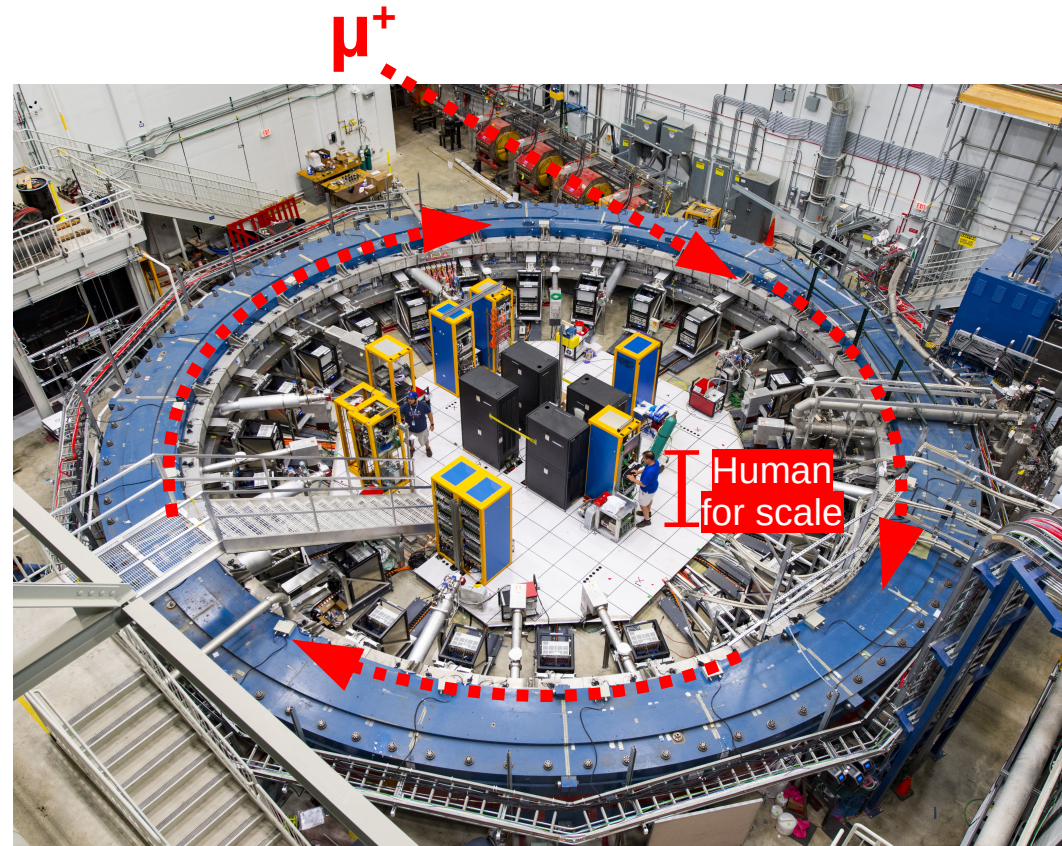
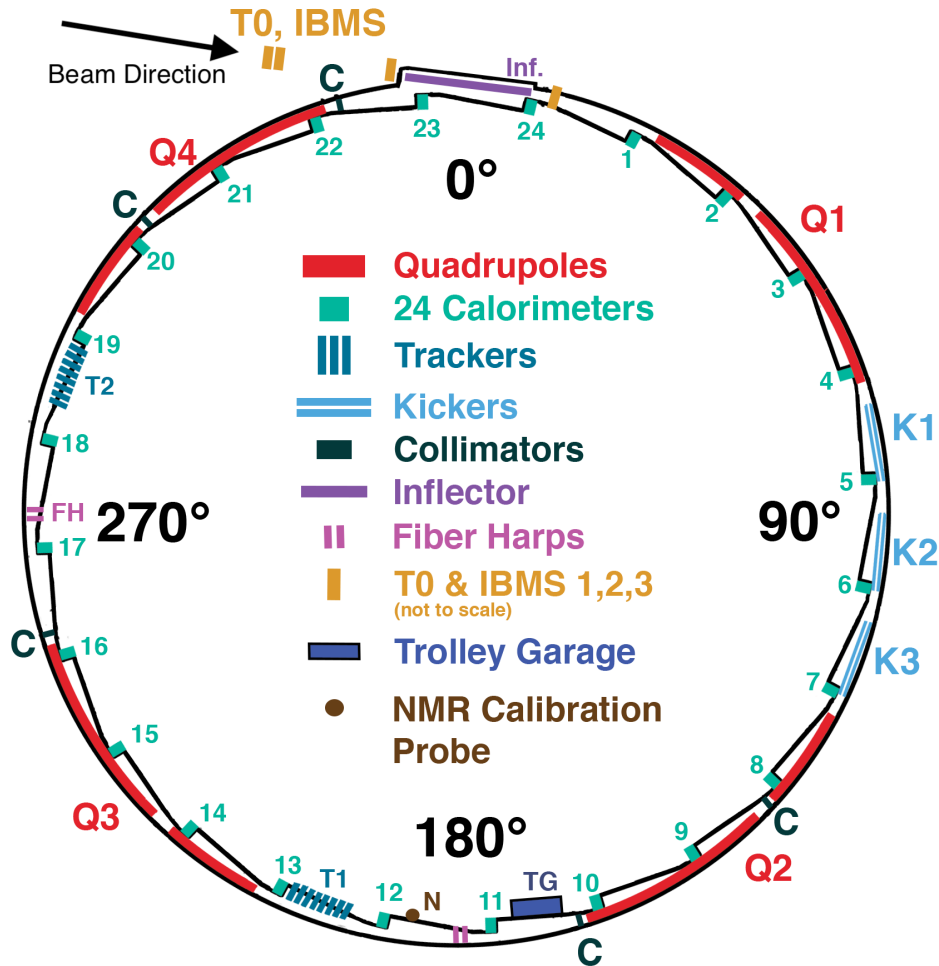
- 16 bunches of  $10^{12}$  protons @8 GeV get **boosted** and delivered via the **recycler ring** every 1.4 seconds
- Each bunch hits a fixed Inconel® (NiCrFe) **target**
- Positive pions from shower extracted and decay in **delivery ring**
- Pure and polarized muon beam enters **g-2 ring**

$$p \rightarrow \pi^+ \rightarrow \mu^+ \rightarrow e^+$$



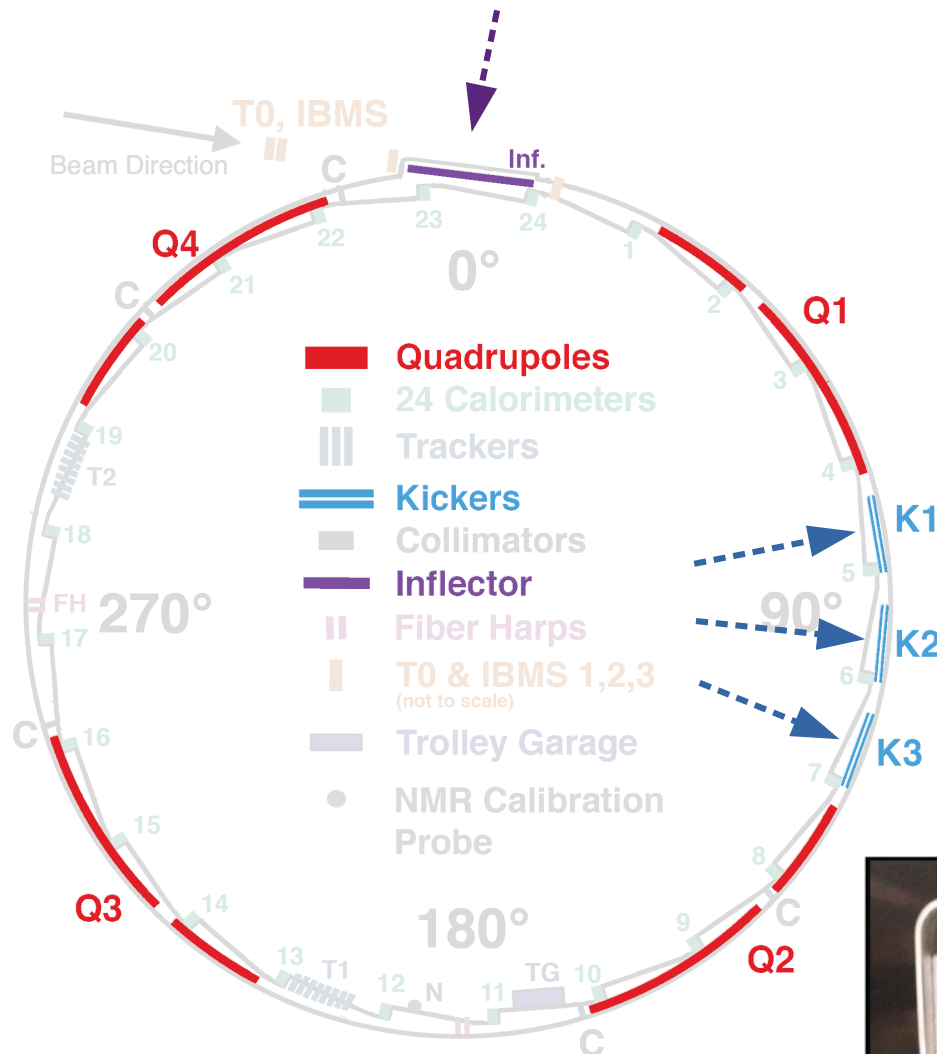


# Muon g-2 Experiment



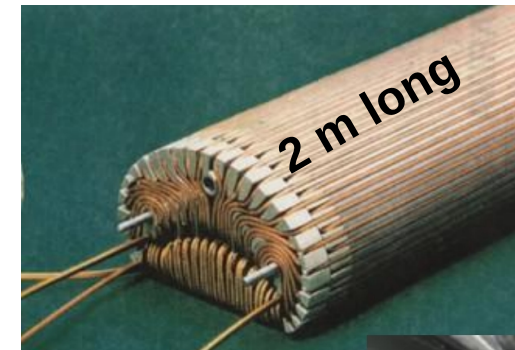
MC-1 building @Fermilab

# Beam injection & kick

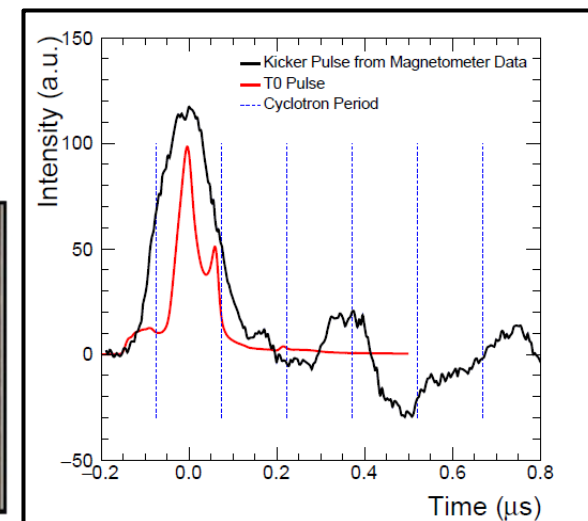
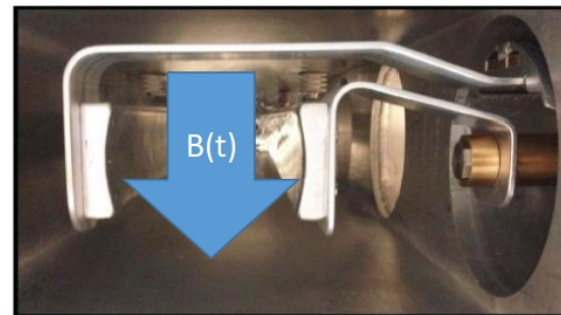


- Superconducting **inflector** ~8 cm offset from nominal orbit
- 3 fast magnetic **kickers** operated at ~4 kA current for ~200 ns

Inflector

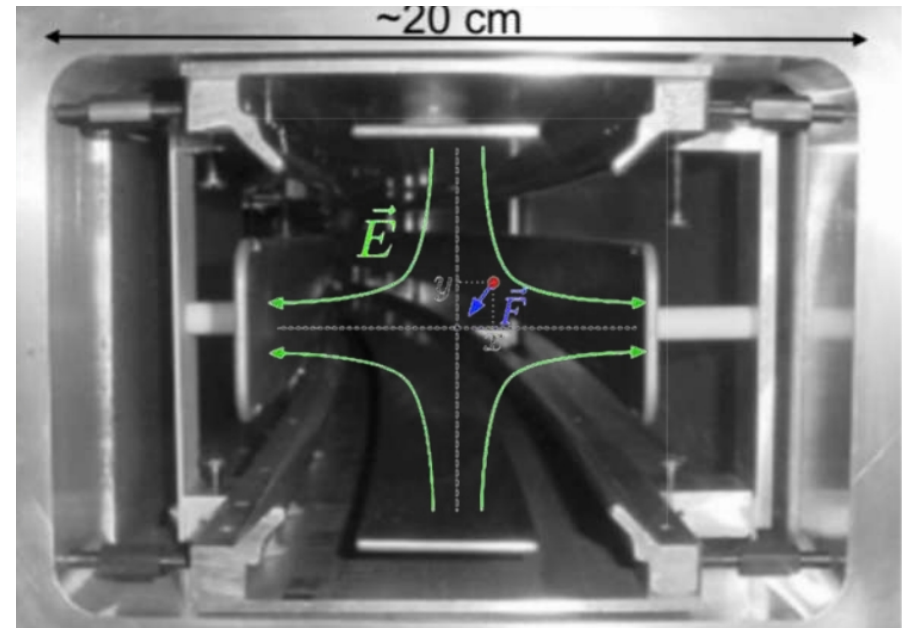
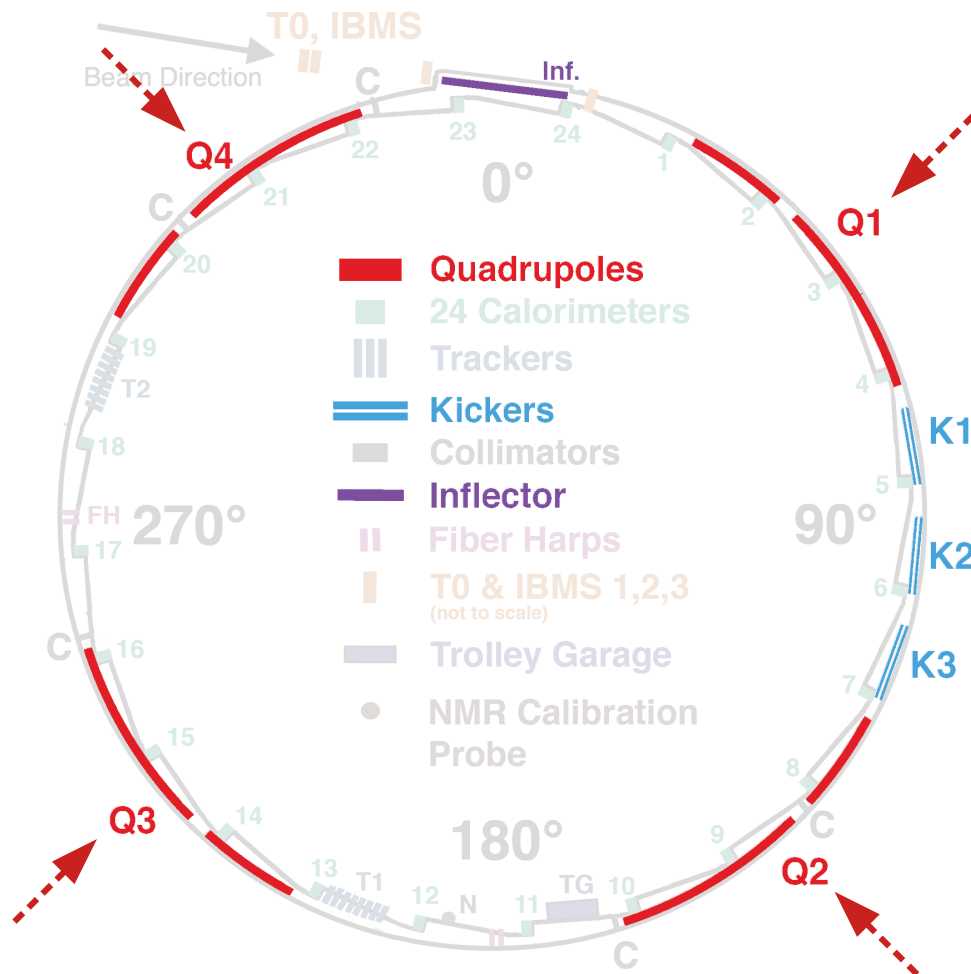


Kicker plates



# Electric quadrupoles

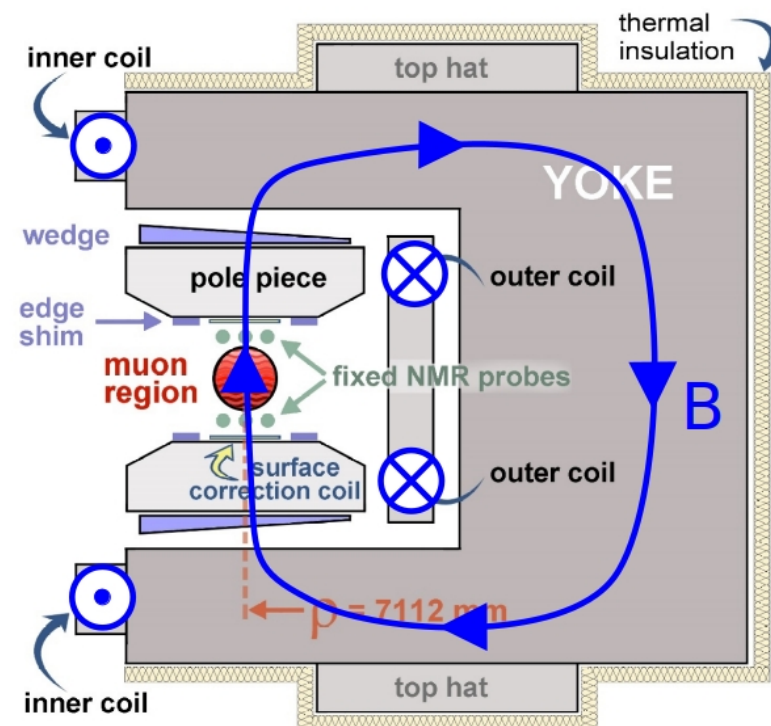
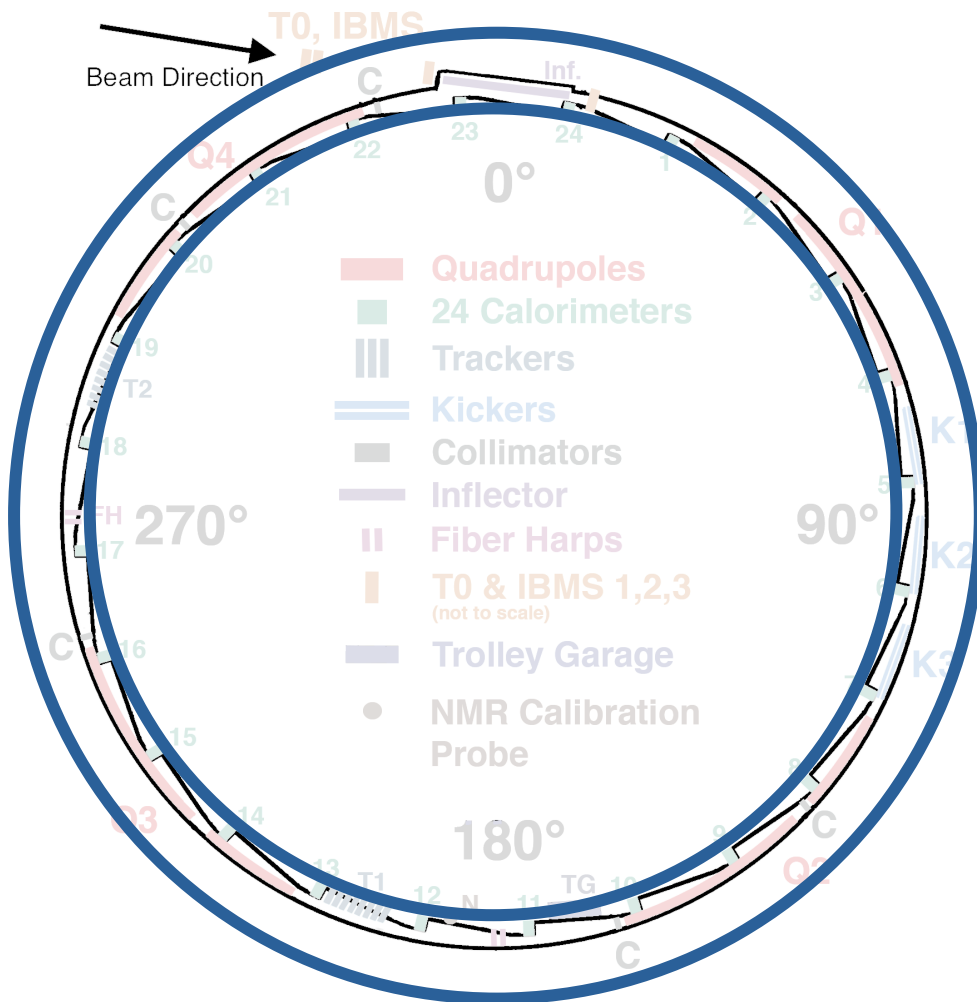
- 8 aluminum electrostatic **quadrupoles** at 13.8 kV to provide weak vertical focus





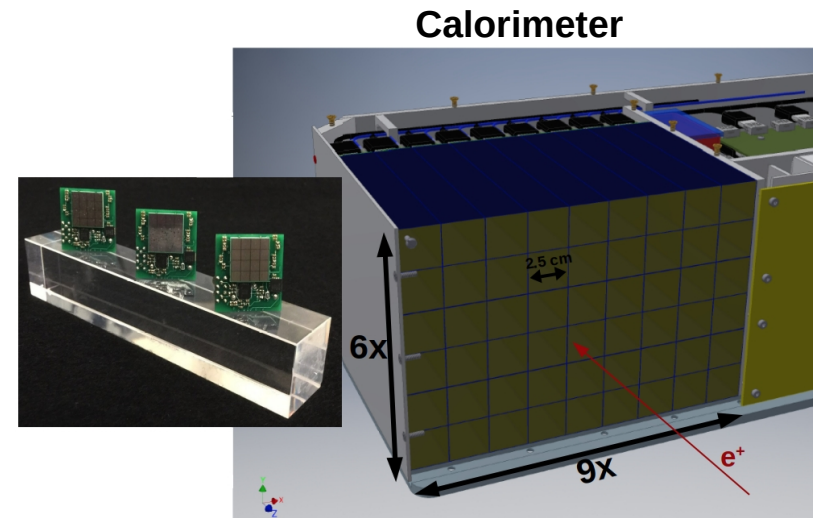
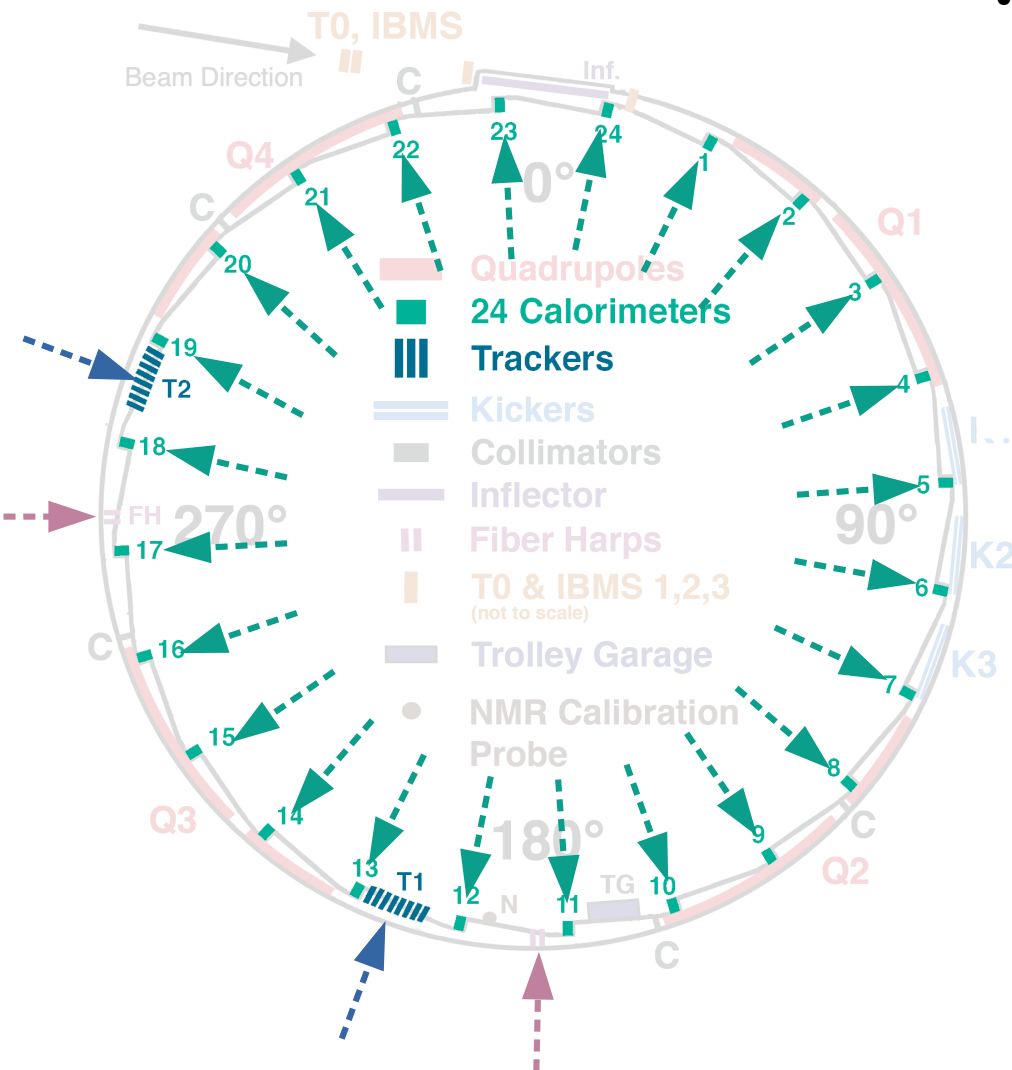
# Magnet

- Superconductive **magnet** cooled at  $\sim 5$  K with LHe
- 7.112 m radius, highly **uniform 1.45 T** vertical magnetic field
- Shimmed passively and actively stabilized. Better than 14 ppm RMS field homogeneity across the full azimuth

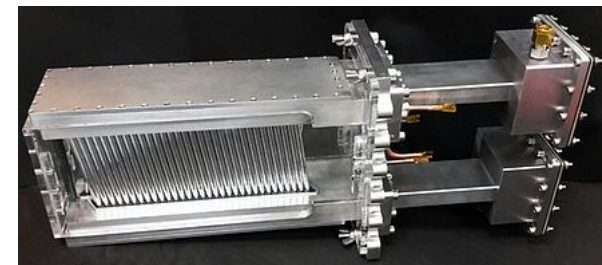


# Detectors

- 24 electromagnetic **calorimeters** for positron energy and time measurement
- 2 **tracker** stations to extrapolate decay vertex location and measure beam distribution

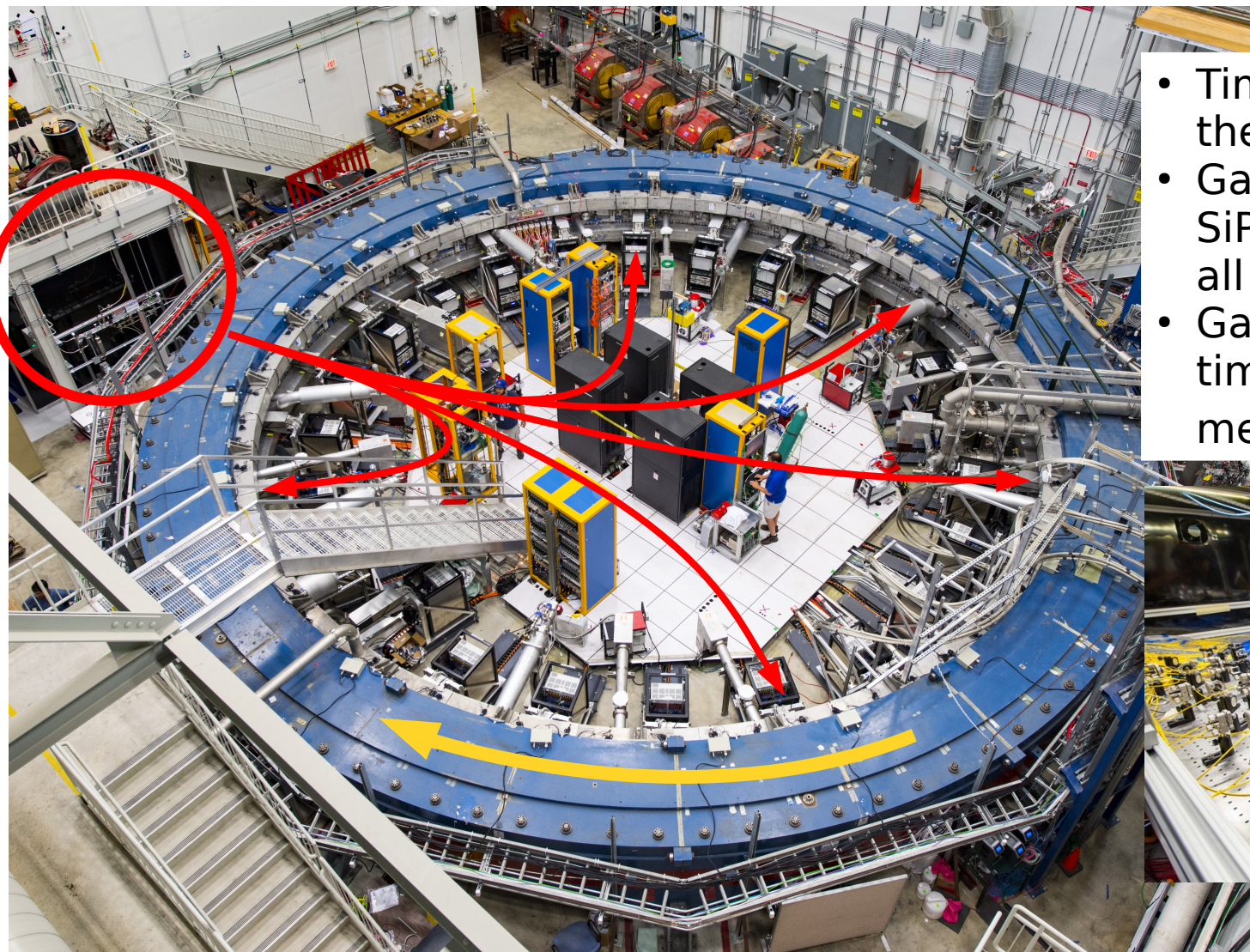


Tracker module

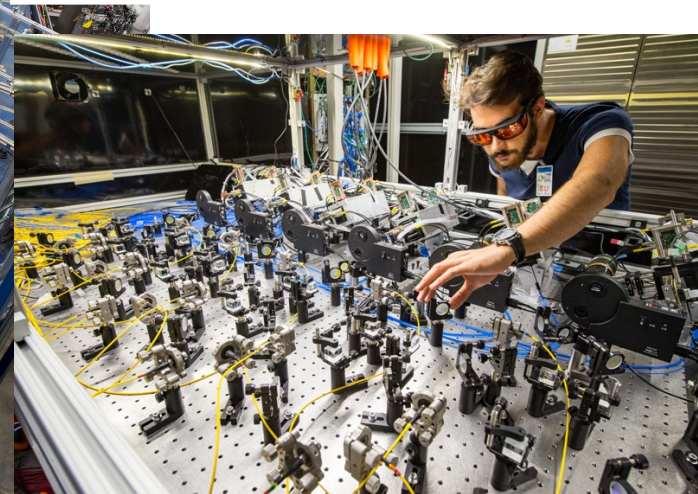




# Laser Calibration System



- Time synchronization at the  $\sim 50$  ps level
- Gain calibration of the SiPMs at the  $10^{-4}$  level at all timescales
- Gain stability through time is crucial for  $\omega_a$  measurement



# Master formula

$$\vec{\omega}_a = a_\mu \frac{e\vec{B}}{m} \longrightarrow a_\mu = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} \frac{\mu'_p(T_r)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}$$

Constants known from other experiments with high precision (25 ppb)



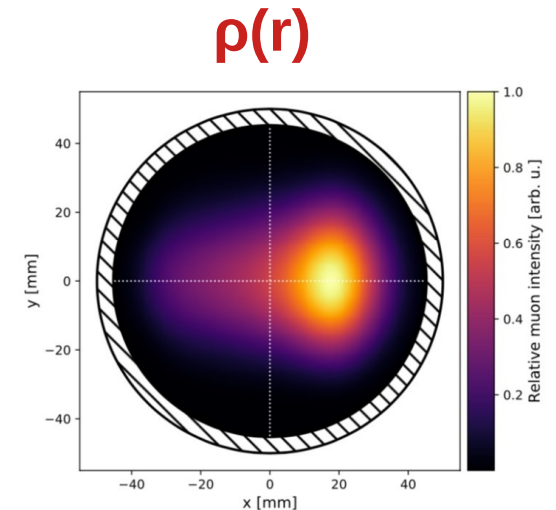
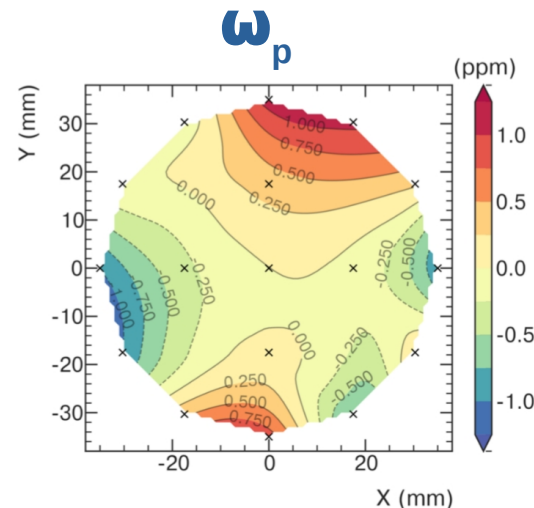
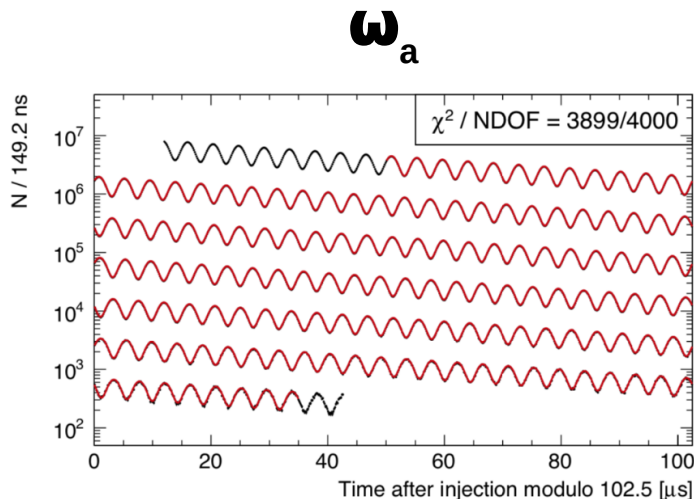
# Master formula

$$\vec{\omega}_a = a_\mu \frac{e\vec{B}}{m} \longrightarrow a_\mu = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} \underbrace{\frac{\mu'_p(T_r)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}}_{\text{Constants known from other experiments with high precision (25 ppb)}}$$

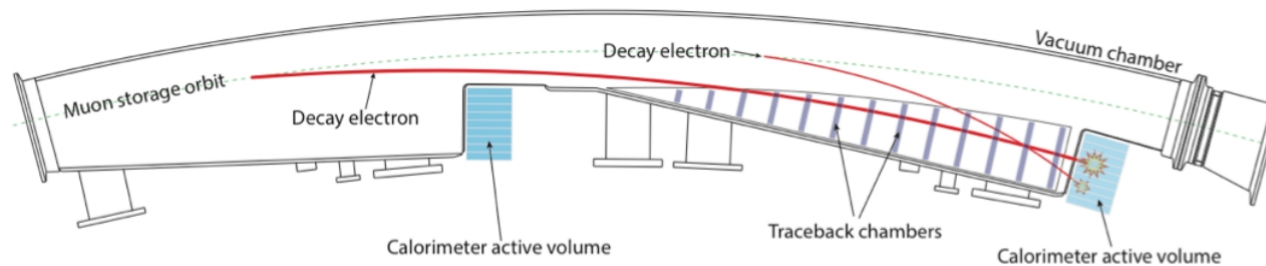
$$a_\mu \propto \frac{f_{\text{clock}} \omega_a^m (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle \omega'_p(x, y, \phi) \times \underline{M(x, y, \phi)} \rangle (1 + B_k + B_q)}$$

## Three key measurements:

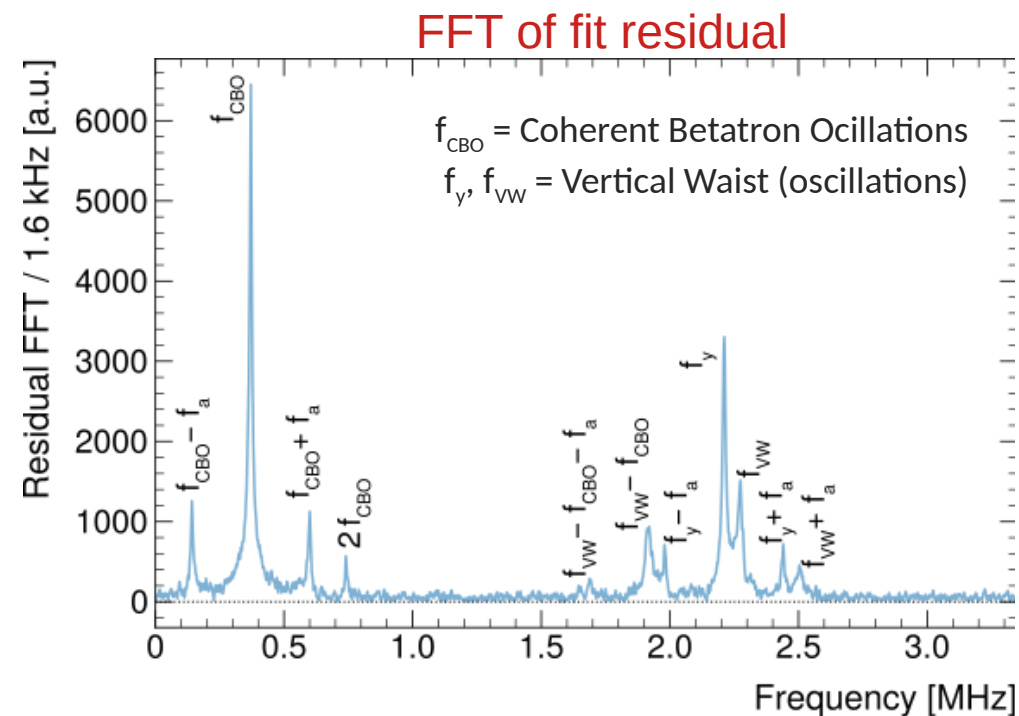
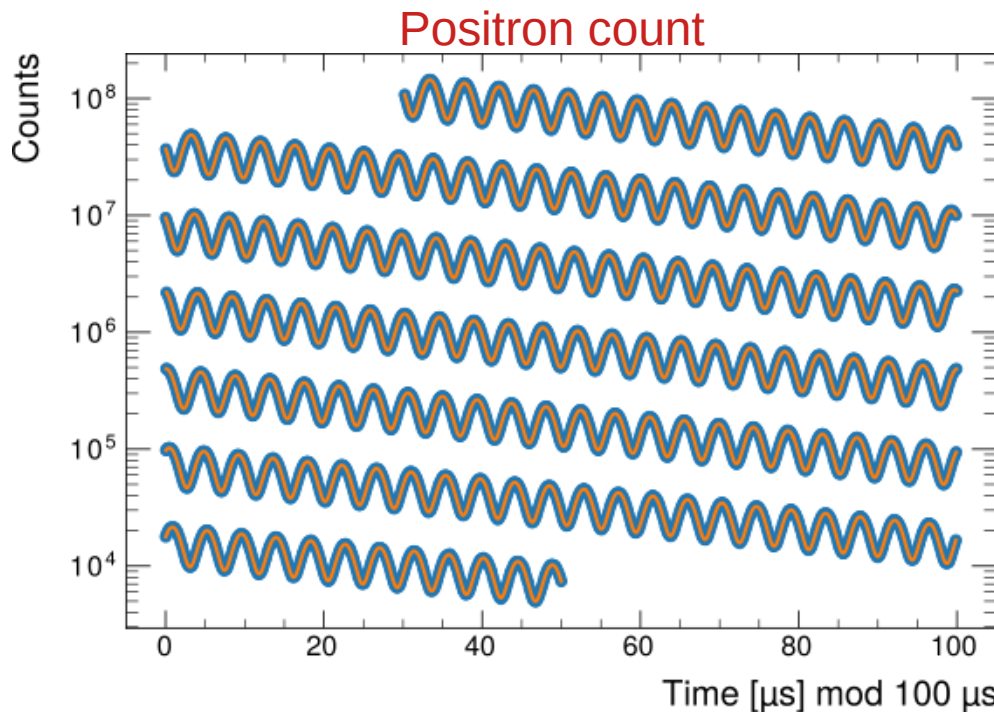
- $\omega_a$ : Muon anomalous precession frequency
- $\omega_p$ : Larmor precession frequency of protons (B field)
- $\rho_r$ : Muon distribution



# Measuring $\omega_a$



- Positrons above 1 GeV are counted vs time (weighted by their asymmetry)
- “Wiggle” plot fitted for exponential decay and  $\omega_a$  oscillation



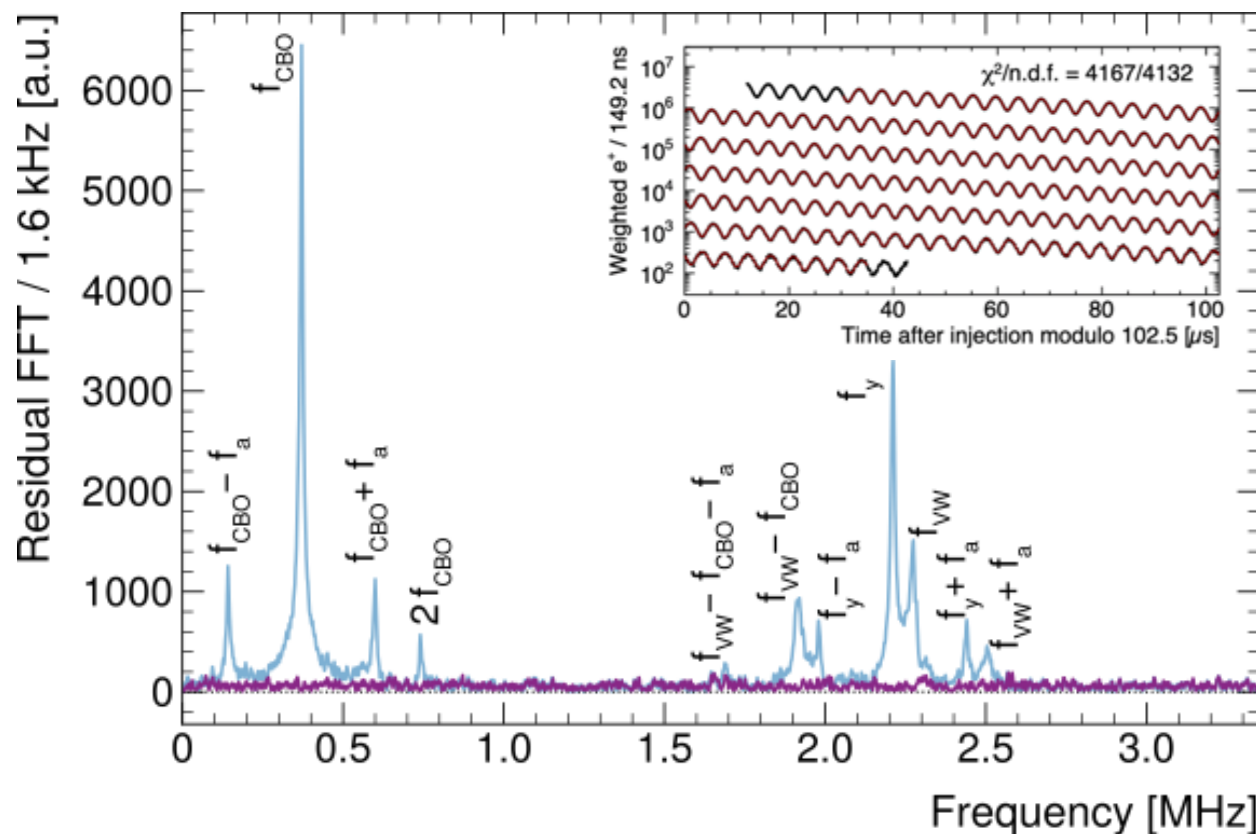
# Measuring $\omega_a$

- Must account for beam oscillations, muons losses, detector effects
- Complete fit has 27 or more free parameters
- 5 analysis groups, 8 hist/fit methods, 3 energy reconstructions

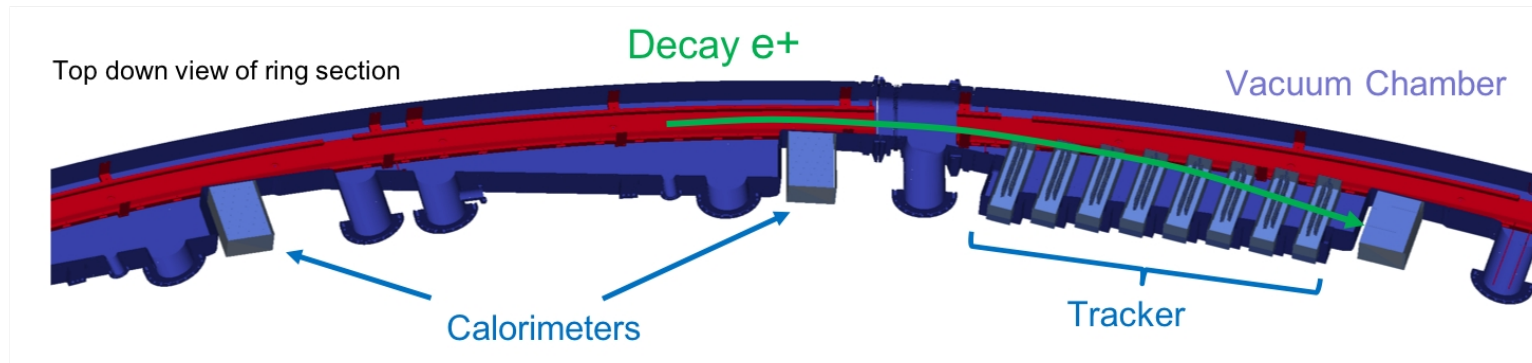
$$\begin{aligned}
 N(t) = & N e^{-t/\tau_\mu} [1 + A \cdot \cos(\omega_a t - \phi + \phi_{BO}(t))] \cdot \\
 & \cdot \left( 1 + A_{CBO} \cos(\omega_{CBO} t - \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}} \right) \cdot \\
 & \cdot \left( 1 + A_{VW} \cos(\omega_{VW} t - \phi_{VW}) e^{-\frac{t}{\tau_{VW}}} \right) \cdot \\
 & \cdot \left( 1 + A_{2CBO} \cos(\omega_{2CBO} t - \phi_{2CBO}) e^{-\frac{t}{\tau_{2CBO}}} \right) \cdot \\
 & \cdot \left( 1 + A_y \cos(\omega_y t - \phi_y) e^{-\frac{t}{\tau_y}} \right) \cdot \\
 & \cdot \left( 1 - k_{LM} \int_0^t L(t') e^{t'/\tau_\mu} dt' \right) \cdot \\
 & \cdot \left( 1 + [A_+ \cos(\omega_+(t)t - \phi_+) + A_- \cos(\omega_-(t)t - \phi_-)] e^{-\frac{t}{\tau_{CBOVW}}} \right)
 \end{aligned}$$

# Measuring $\omega_a$

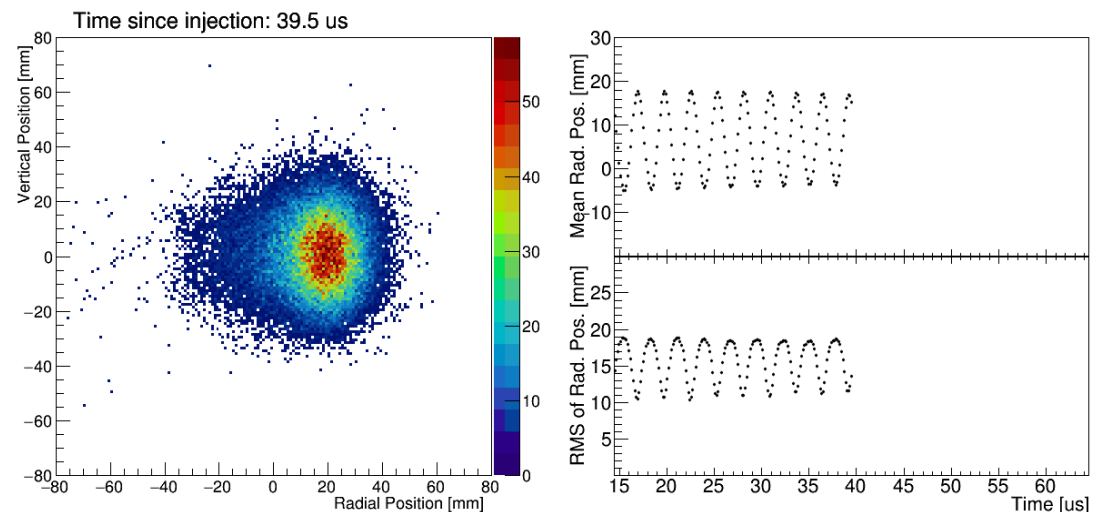
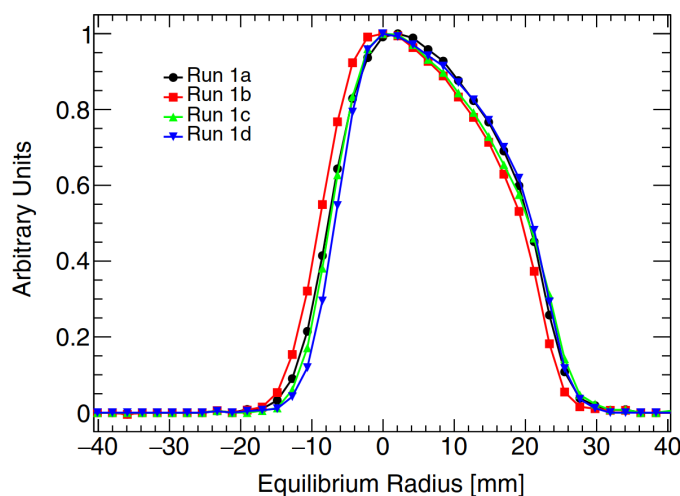
- Must account for beam oscillations, muons losses, detector effects
- Complete fit has 27 or more free parameters
- 5 analysis groups, 8 hist/fit methods, 3 energy reconstructions



# Measuring the beam



- Trackers at  $180^\circ$  and  $270^\circ$  reconstruct the positron trajectory to extrapolate the decay vertex in the storage region
- Muon distribution maps extrapolated to the entire ring azimuth with Geant4 simulation (gm2ringsim)
- Calorimeter hit energy matching to perform particle identification

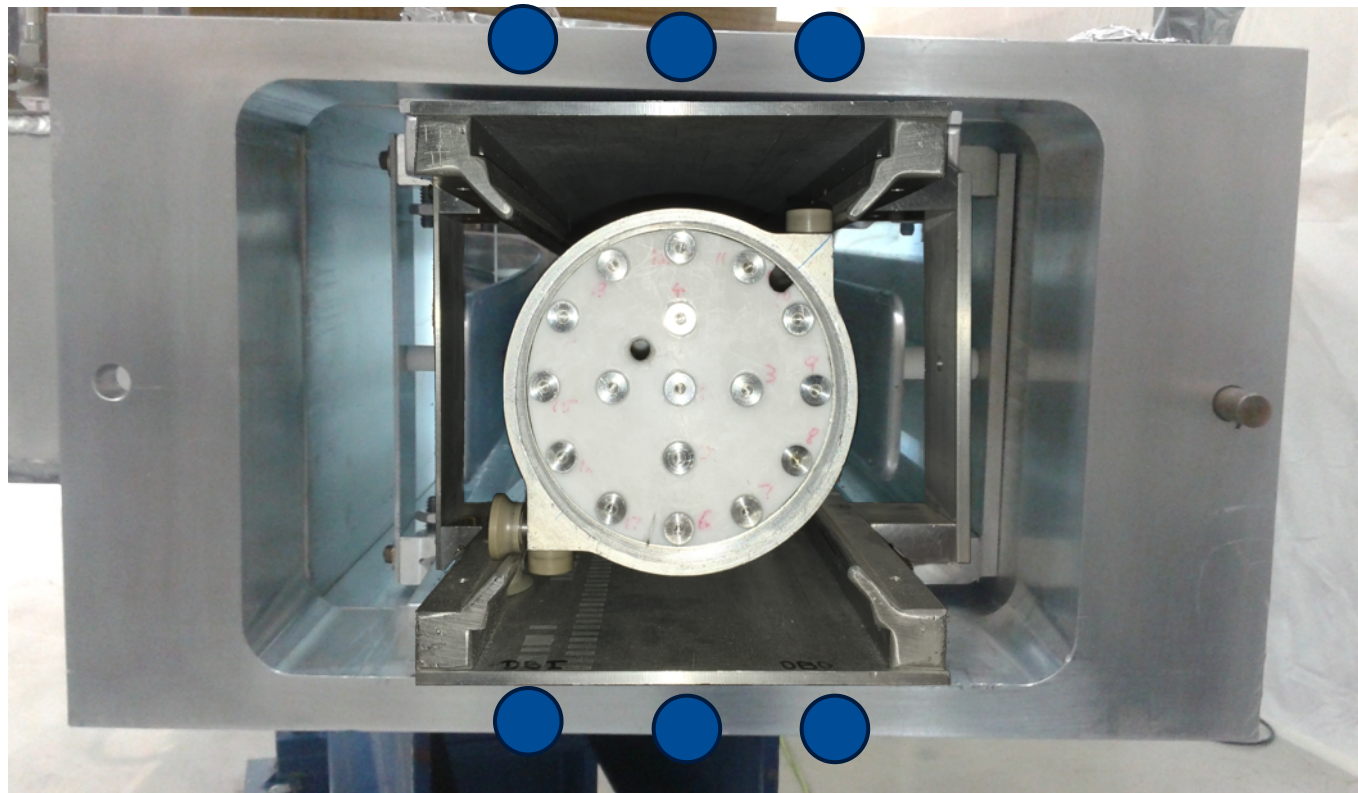
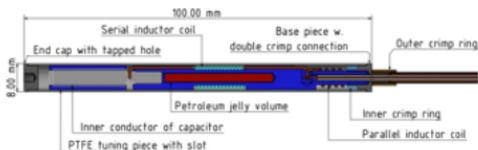




# Measuring the field

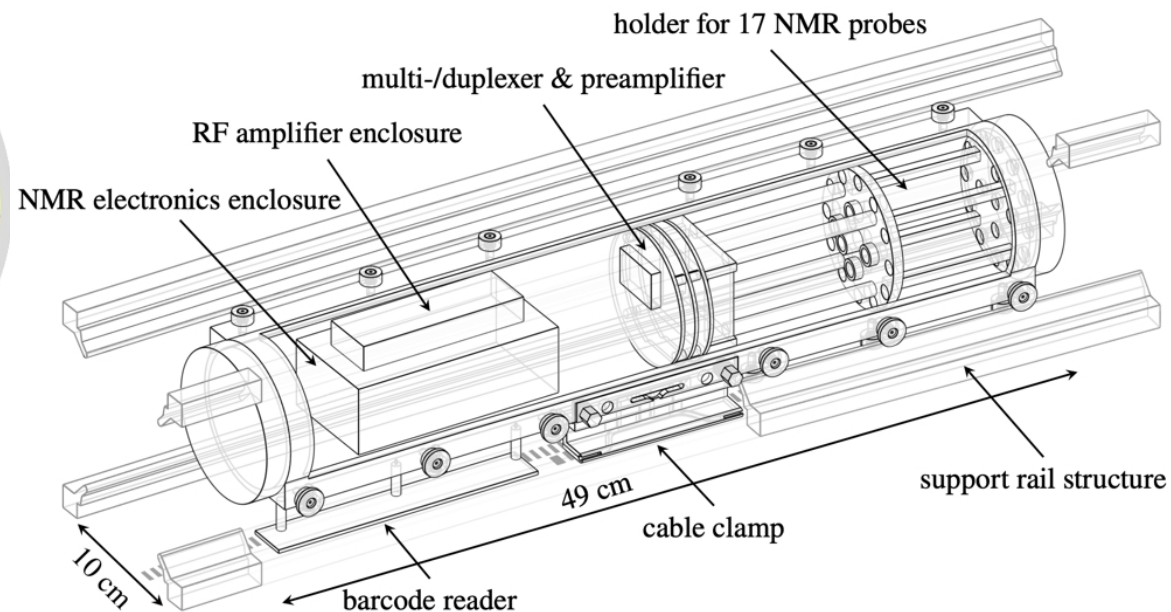
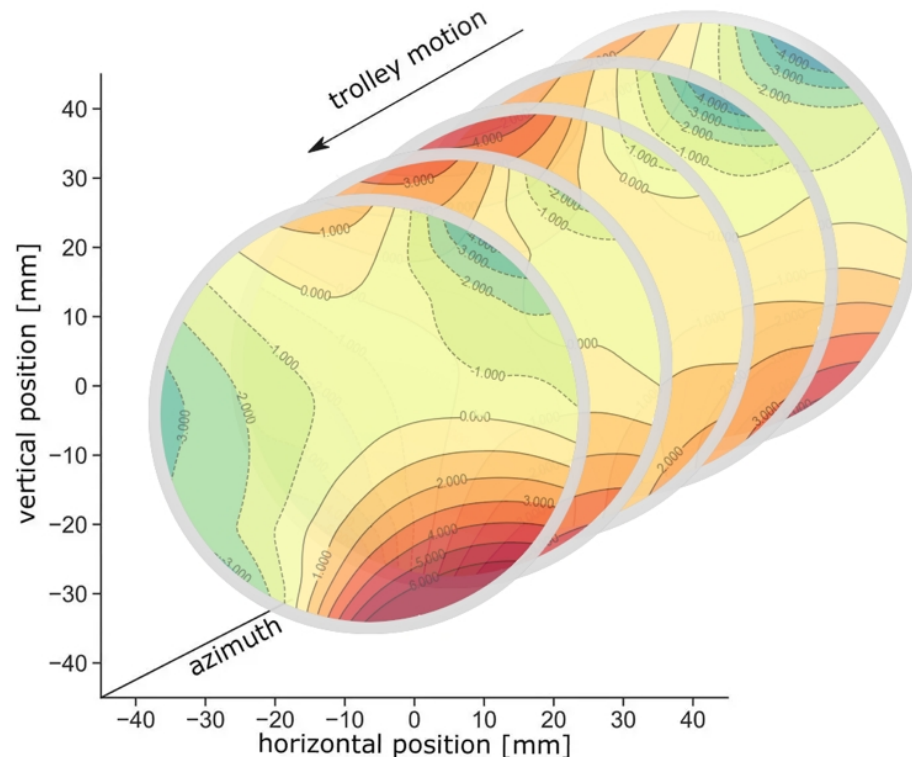
- Field intensity measured with Nuclear Magnetic Resonance (NMR) probes in terms of proton precession frequency  $\omega_p$
- Continuously monitored around the storage region and periodically measured inside the storage region

378 fixed probes  
continuous monitoring



# Measuring the field

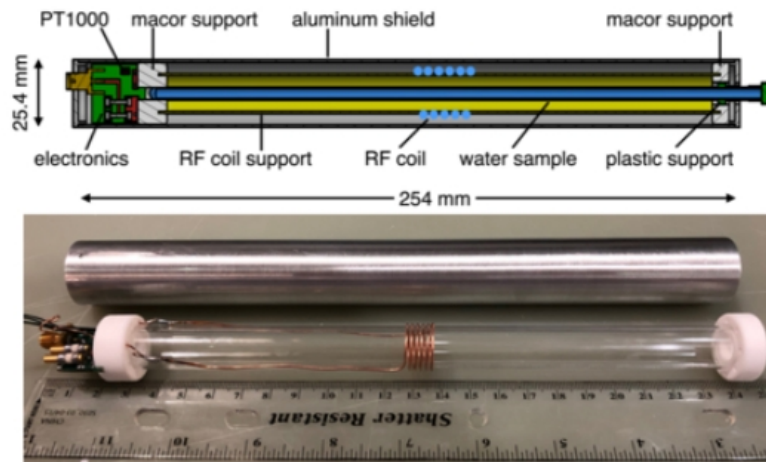
- Every  $\sim 3$  days, a trolley equipped with 17 probes runs through the storage region
- 9000 2D slices for complete magnetic field map





# Measuring the field

- Field measurements are calibrated in-situ with a water-based cylindrical Fixed Calibration Probe and externally with shielded protons in sperical sample

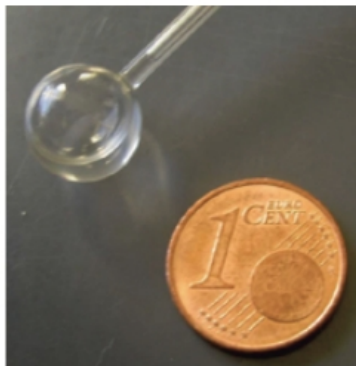
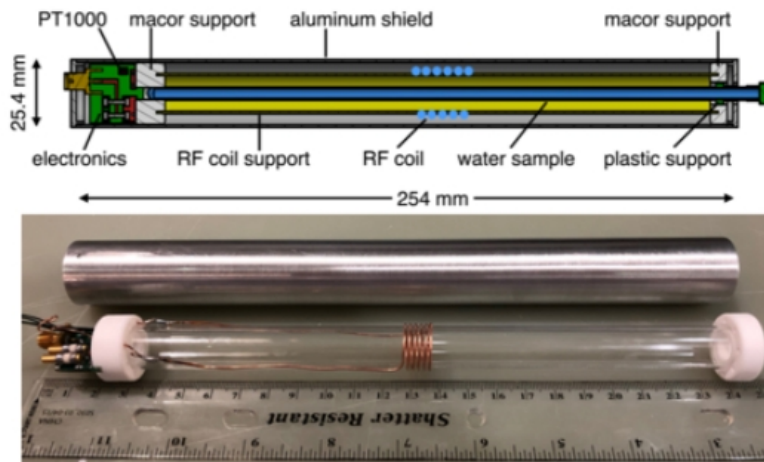


Cross-calibrations:

- $^3\text{He}$  magnetometer
- J-PARC Muon  $g-2$ /EDM continuous-wave based NMR calibration probe

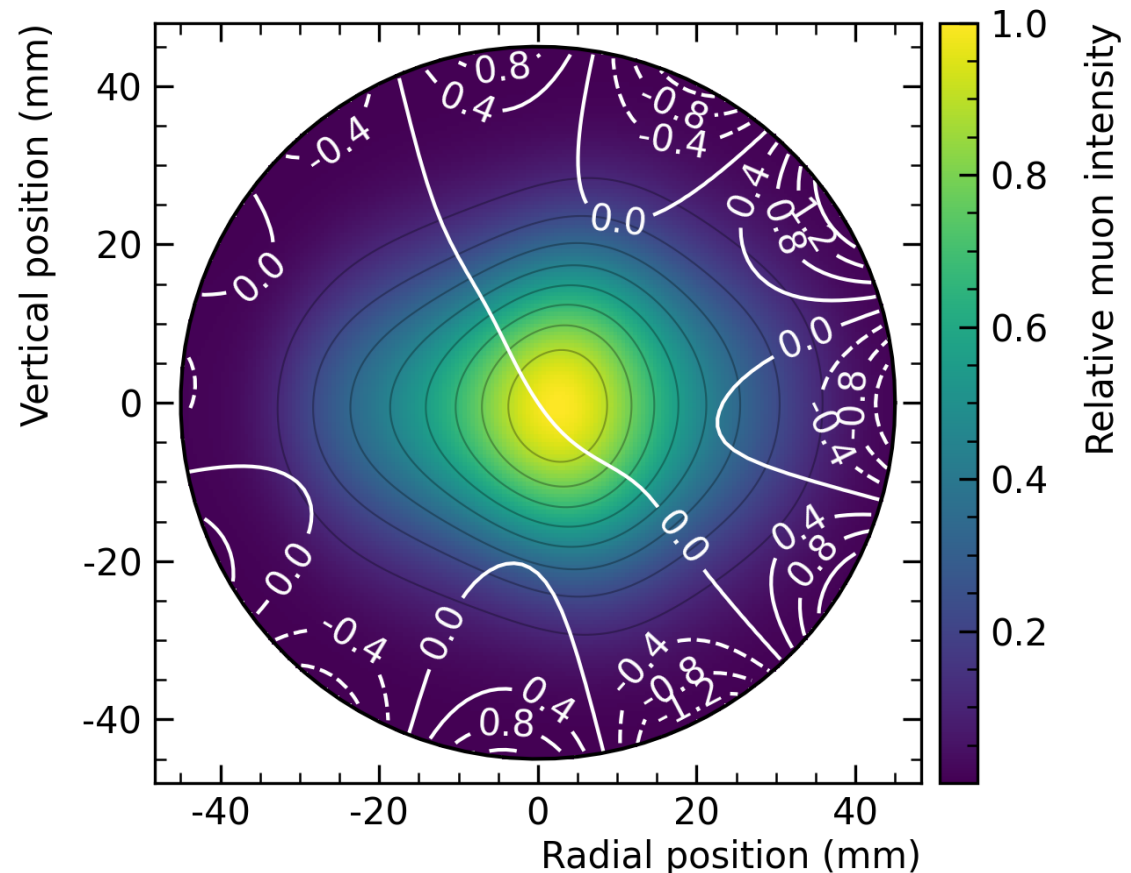
# Measuring the field

- Field measurements are calibrated in-situ with a water-based cylindrical Fixed Calibration Probe and externally with shielded protons in sperical sample
- Finally, magnetic field is weighted by the measured beam distribution



Cross-calibrations:

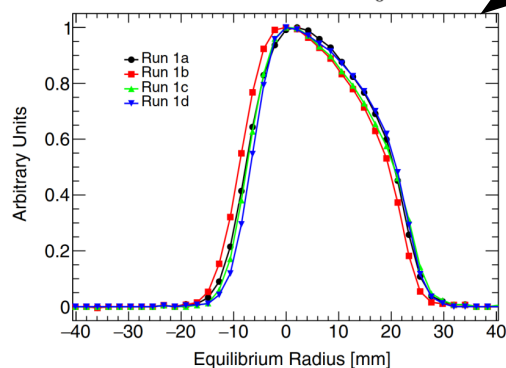
- $^3\text{He}$  magnetometer
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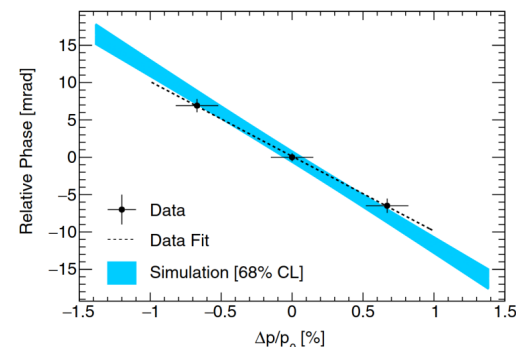
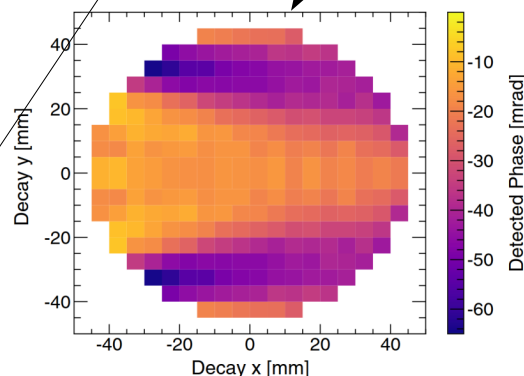
# Master formula

$$\frac{\omega_a}{\omega_p} = \frac{\omega_a^m}{\omega_p^m} \frac{1 + \boxed{C_e + C_p + C_{pa} + C_{dd} + C_{ml}}}{1 + B_k + B_q}$$

$$C_e \approx 2n(1-n)\beta_0 \frac{\langle x_e^2 \rangle}{R_0^2}$$

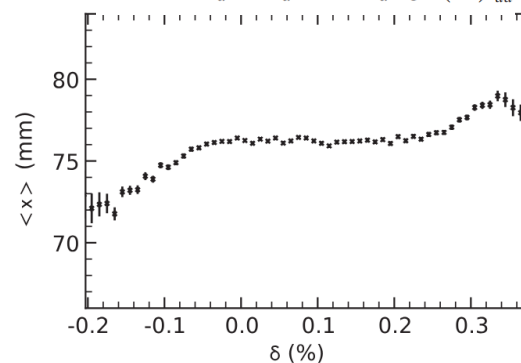


Phase-acceptance correction



Differential decay correction

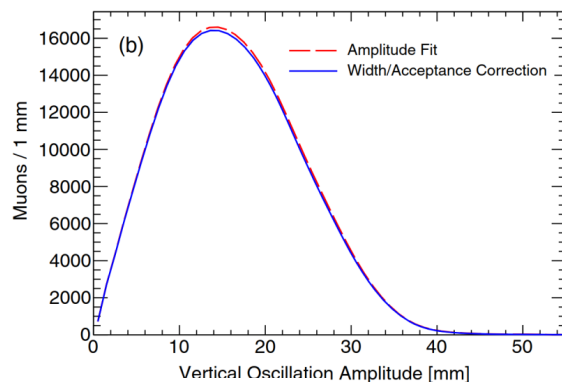
$$C_{dd} = -\frac{\Delta\omega_a}{\omega_a} = \frac{1}{\omega_a} \frac{d\phi_0}{dt} = \frac{1}{\omega_a} \frac{d\phi_0}{dp} \left( \frac{dp}{dt} \right)_{dd}$$



Lost muons momentum correlation

Electric field correction

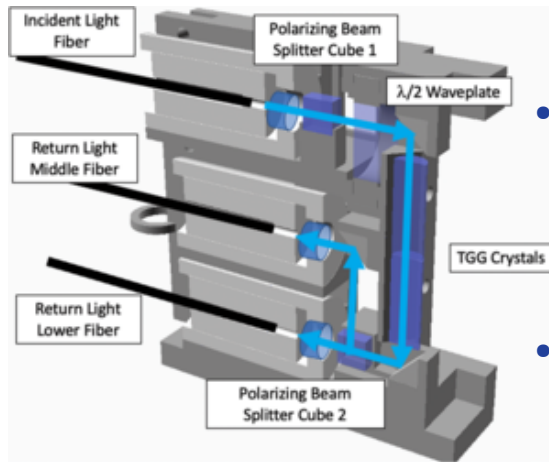
Pitch correction



$$C_p \approx \frac{n}{4} \frac{\langle A_y^2 \rangle}{R_0^2}$$

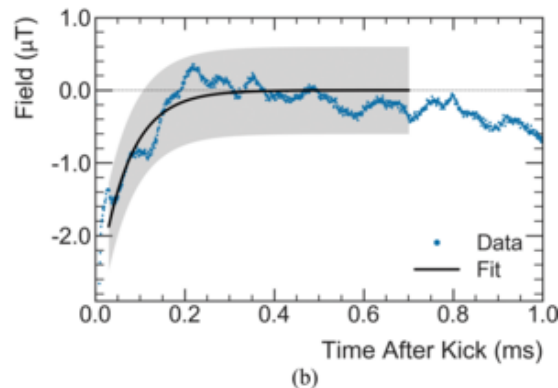
# Master formula

$$\frac{\omega_a}{\omega_p} = \frac{\omega_a^m}{\omega_p^m} \frac{1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml}}{1 + B_k + B_q}$$

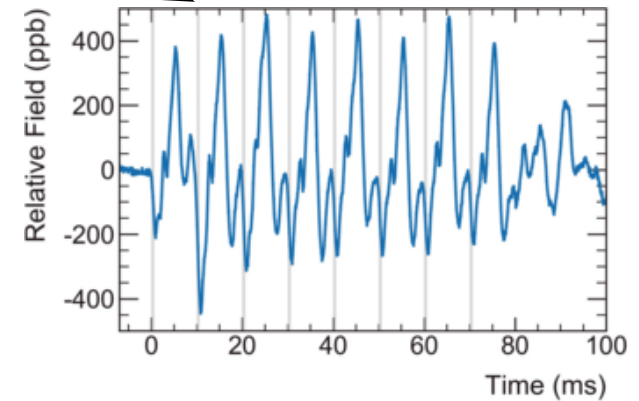


(a)

- Millisecond-long eddy currents induced by the kicker pulse
- Measured with dedicated Faraday magnetometers

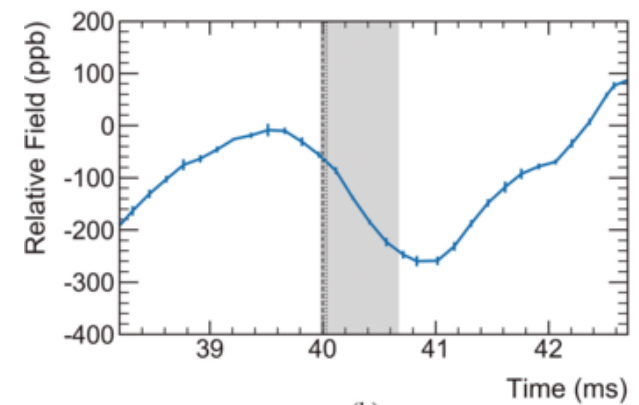


(b)



(a)

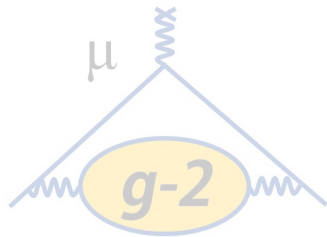
- Low-frequency oscillations of the electrostatic quadrupole plates
- Measured with dedicated probes



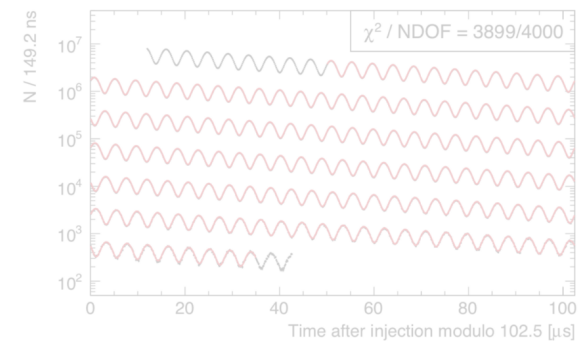
(b)

# Overview

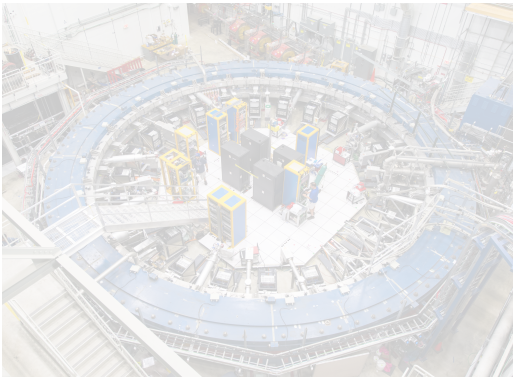
## The Muon g-2



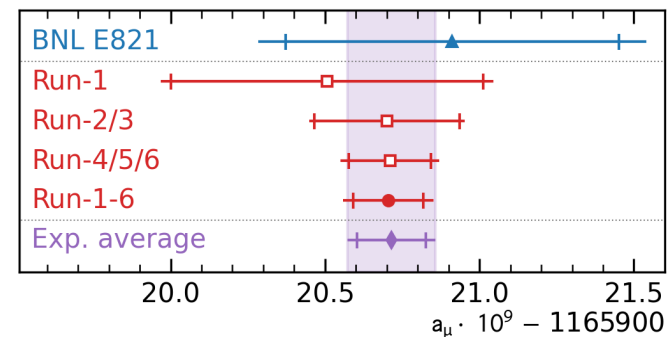
## Experimental principles



## The Muon g-2 Experiment at Fermilab

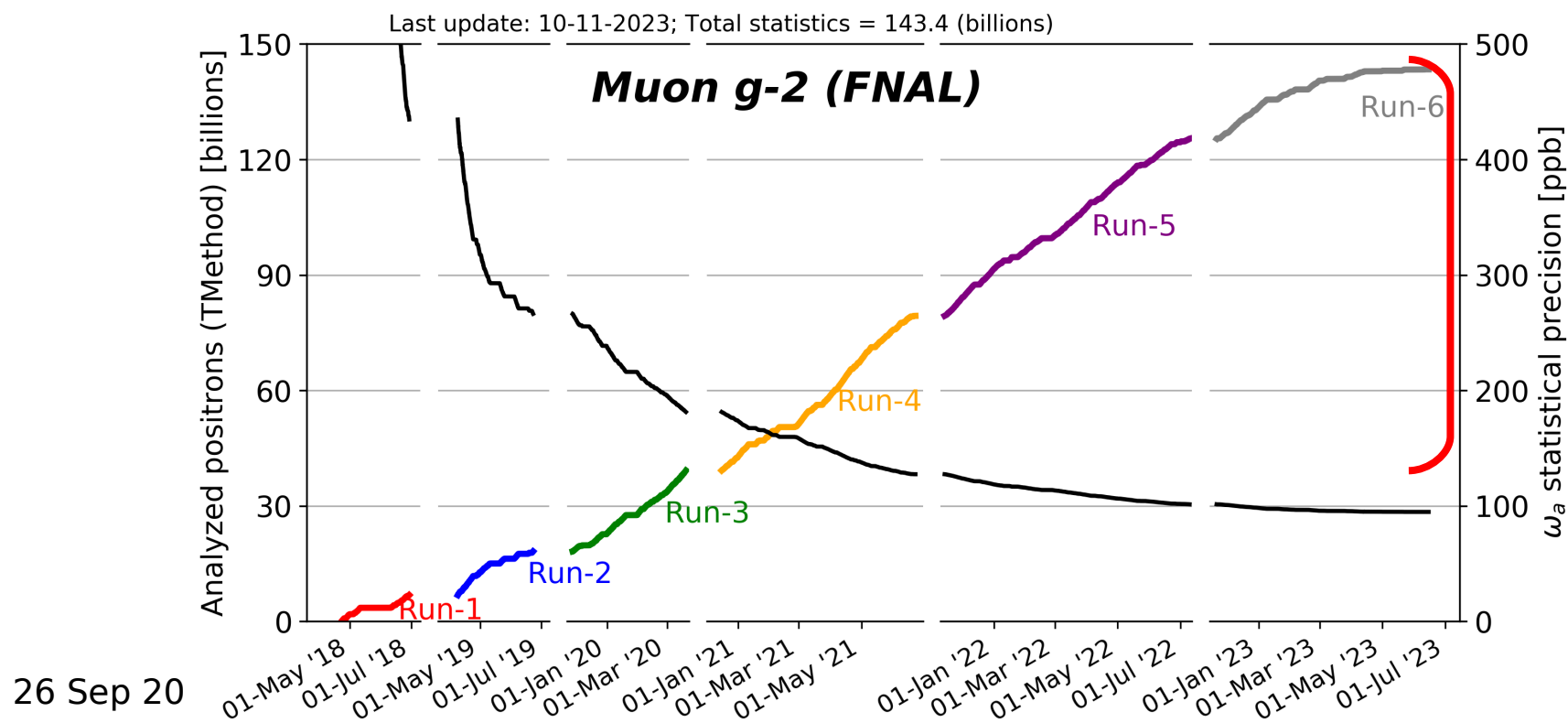


## Latest results and overlook



# Run-456 results

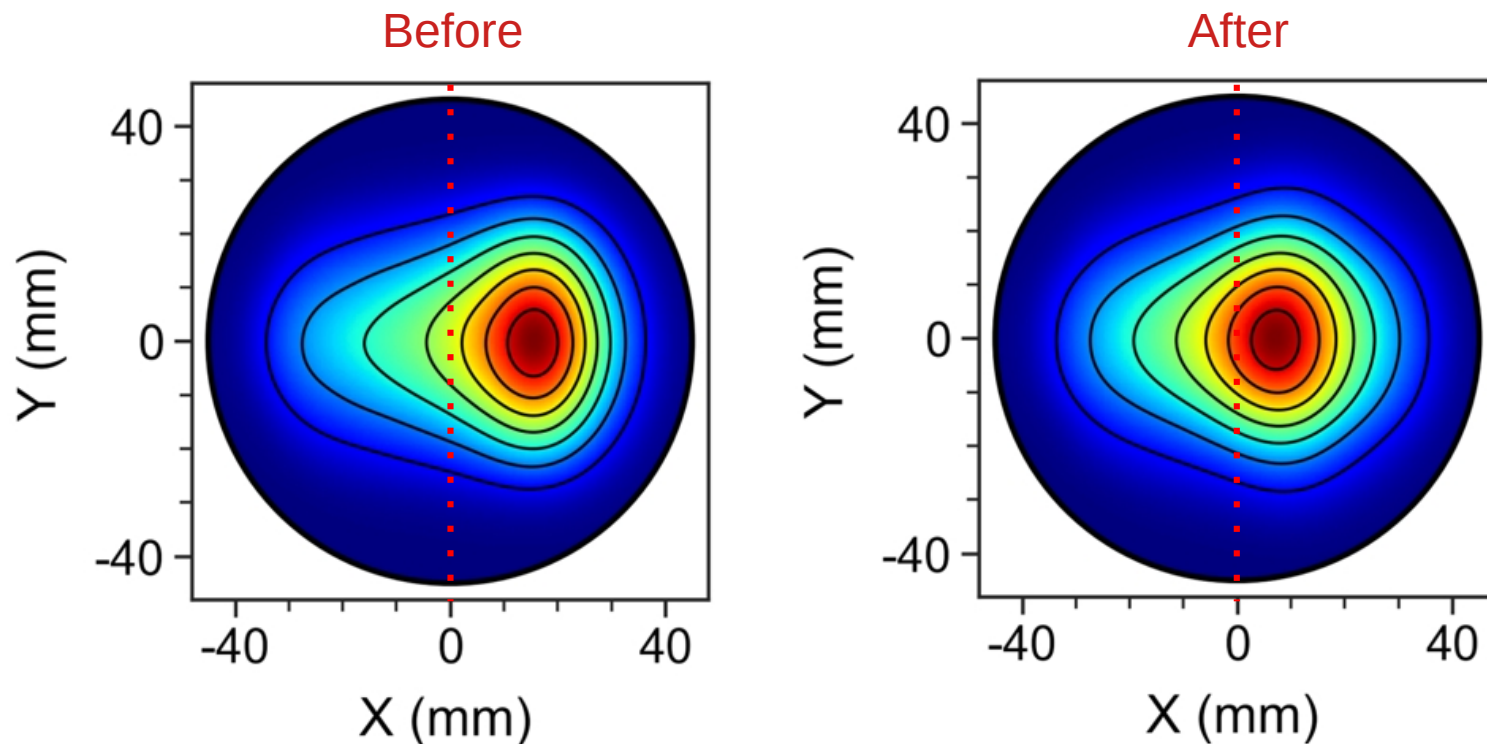
- Final three datasets taken from 2020 to 2023
- They account for  $\sim 70\%$  of total statistics
- Statistical design goal achieved in February 2023 and surpassed thereafter
- I will go through some of the most important improvements with respect to previous runs





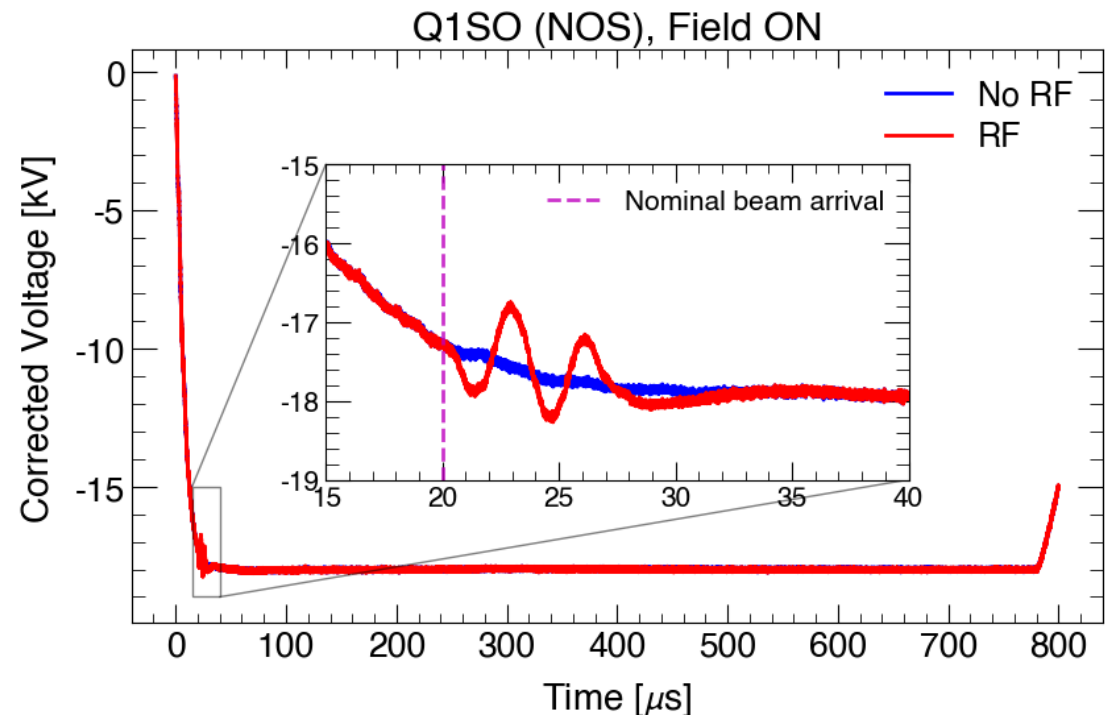
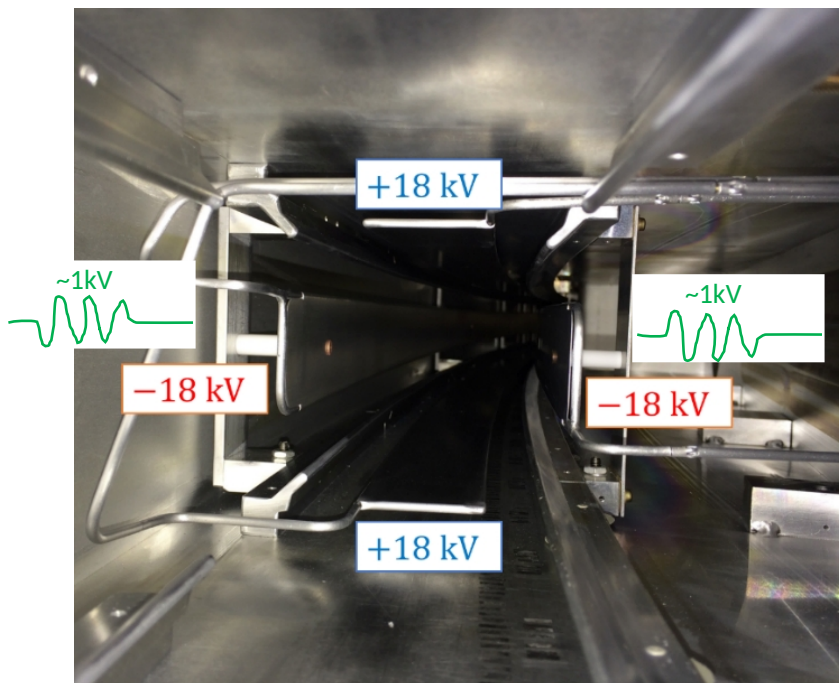
# Kicker performance

- Toward the end of Run-3, upgraded kicker cables and improved impedance matching: kick now at design specs
- Result: better centering of muon distribution



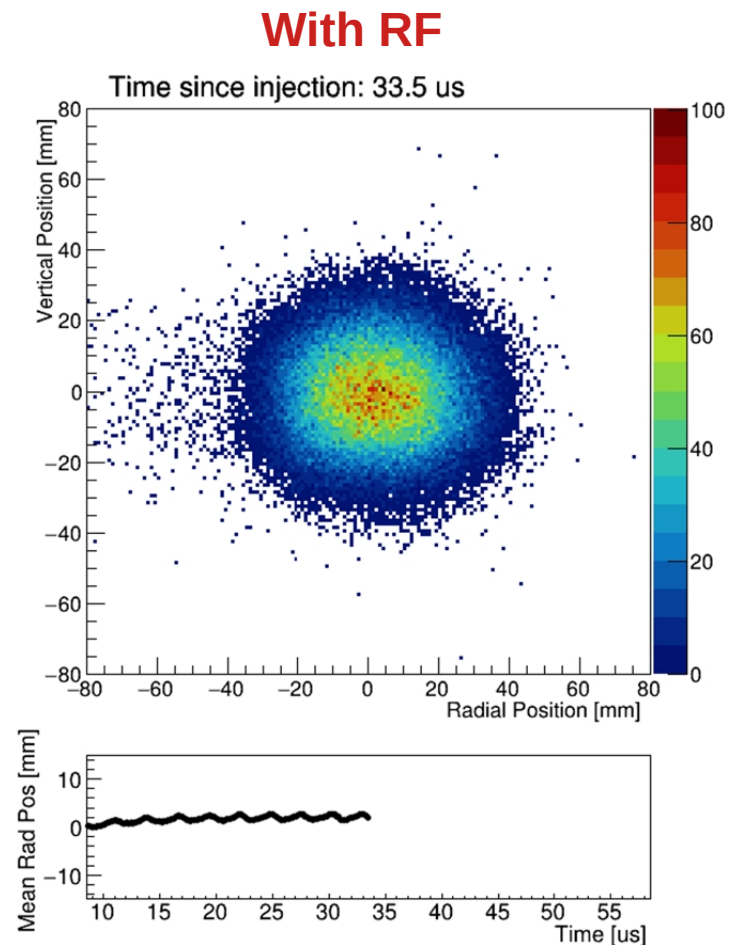
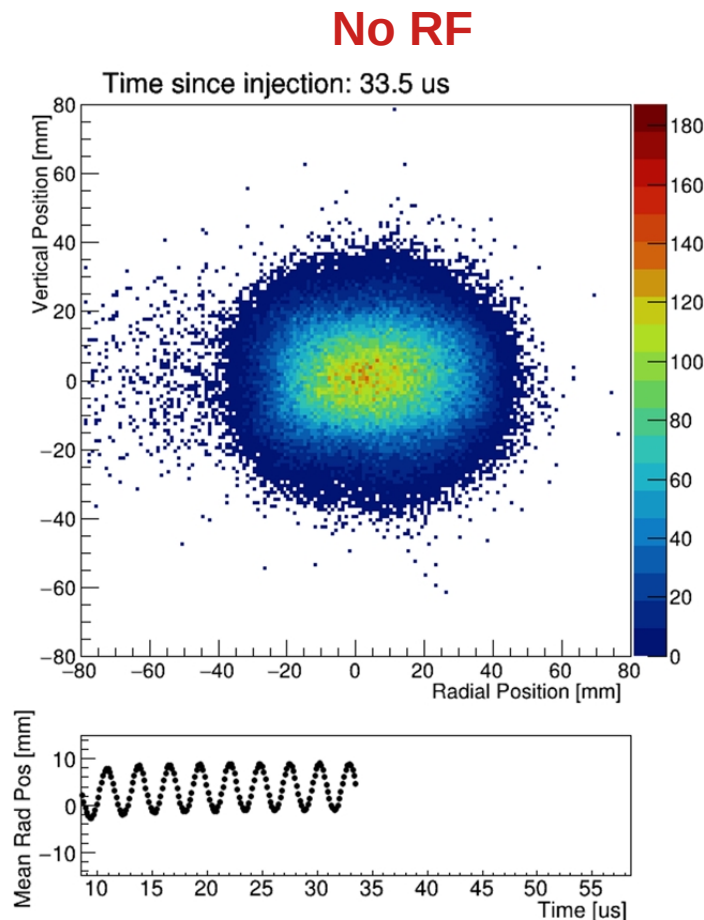
# Quadrupole RF

- A quadrupole radio-frequency dampening system has been installed at the end of Run-4
- The RF pulsing scheme generates a resonant kick within 10  $\mu\text{s}$  after the beam injection. This reduces the radial and vertical oscillations of the beam
- Turned on starting from Run-5



# Quadrupole RF

- Coherent Betatron Oscillation (CBO) amplitude decreased by factor  $\sim 9$
- Decreasing CBO systematic uncertainties, among the largest ones in Run-23



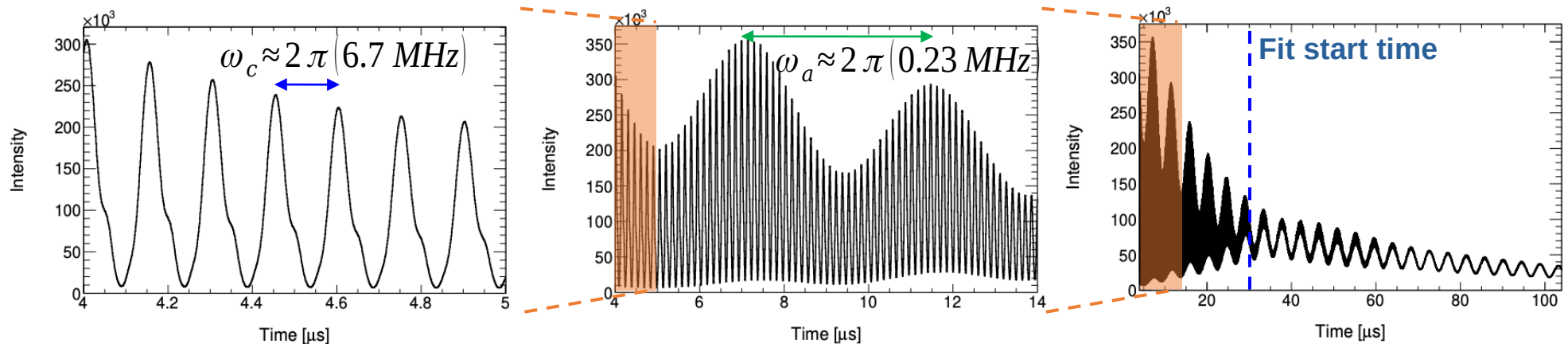
# E-field correction

$$\left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E}$$

=0 for  
p = 3.094 GeV/c

$$\frac{\omega_a}{\omega_p} = \frac{\omega_a^m}{\omega_p^m} \frac{1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml}}{1 + B_k + B_q}$$

- Not all muons have perfect magic momentum of 3.094 GeV/c
  - Higher momentum → larger orbit radius → longer period
  - Lower momentum → smaller orbit radius → shorter period
- Dephasing and radial position are used to extract the stored momentum spectrum





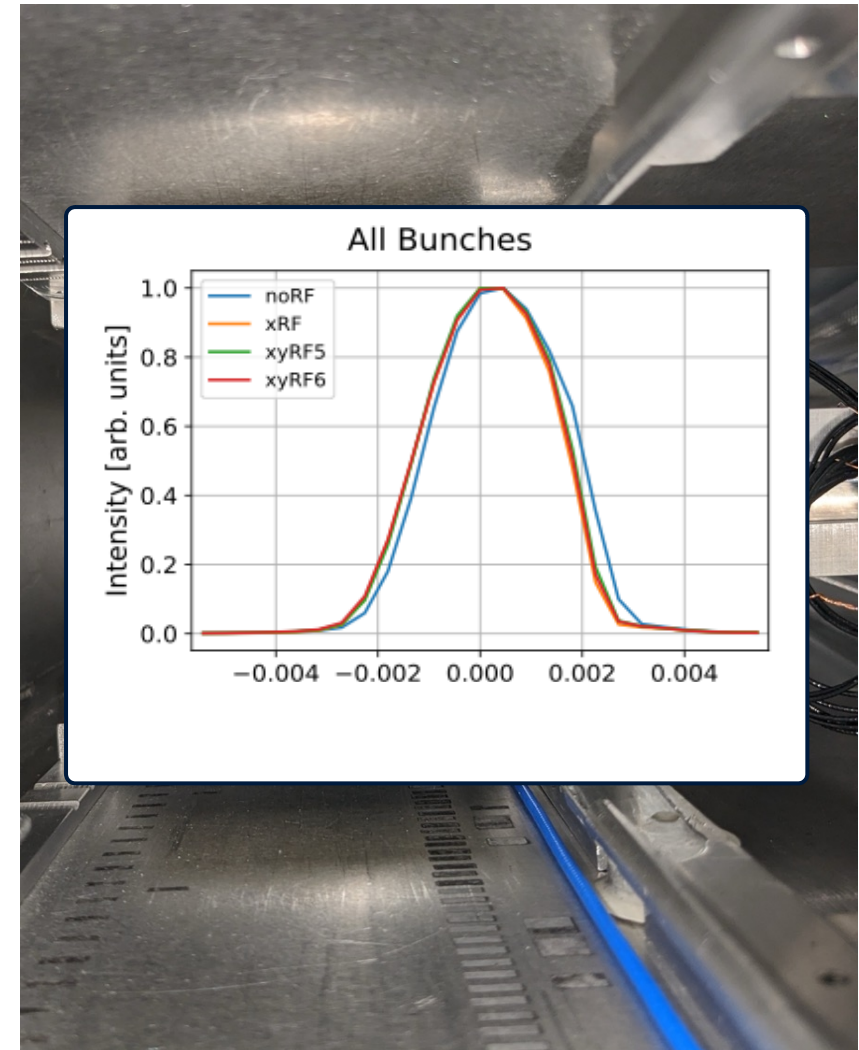
# Momentum distribution

- **Trackers**
  - Parasitic: measure muon dispersion from decay positrons and use beam dynamics
- **Calorimeters**
  - Parasitic: measure muon dephasing (how muons spread into the beam) to infer radial distribution
  - Improved robustness of method
- Two new **Minimally** intrusive **Scintillating Fiber** (Mini-SciFi) detectors installed before Run-6
  - Vertical and Horizontal versions
  - Destructive: Cross-checks and uncertainty determination (tracker)



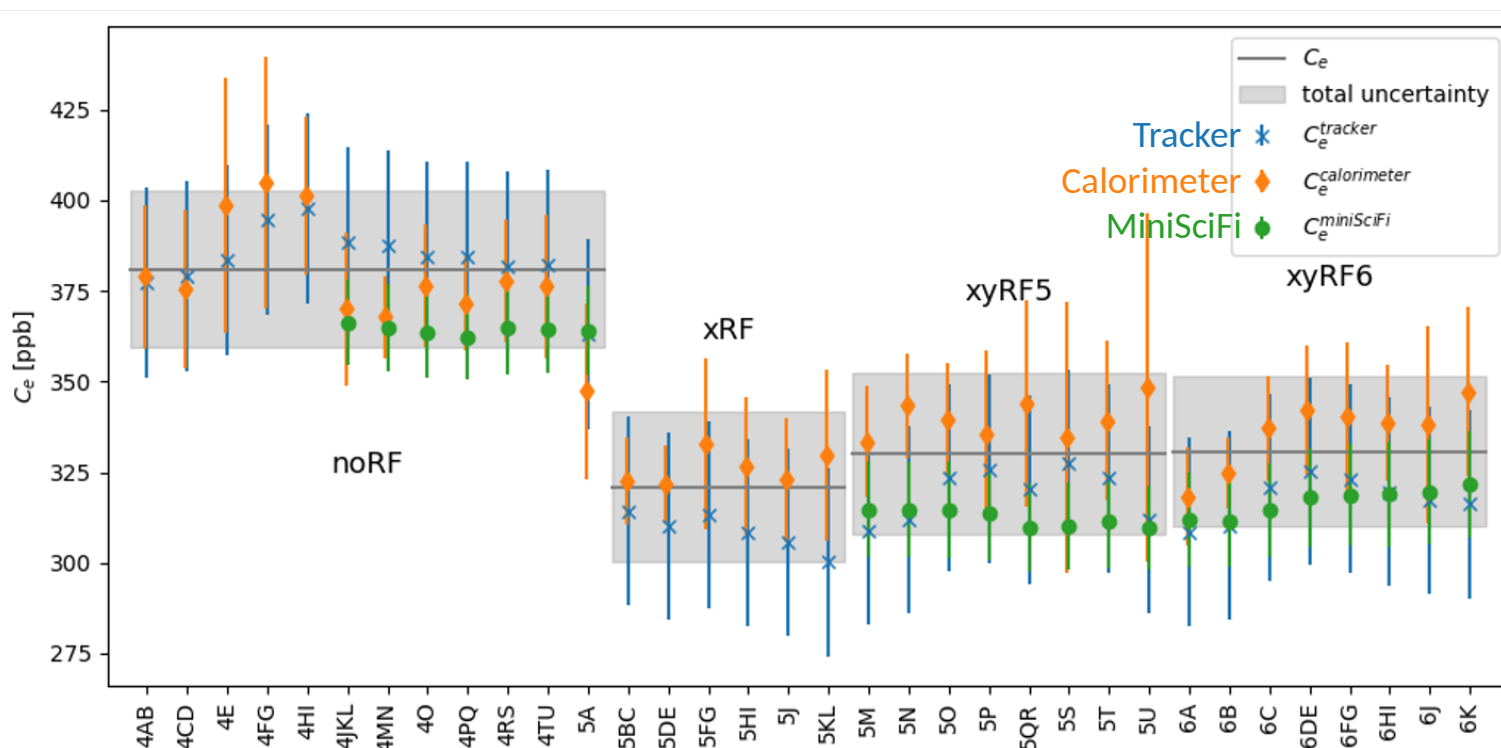
# Momentum distribution

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# E-field correction

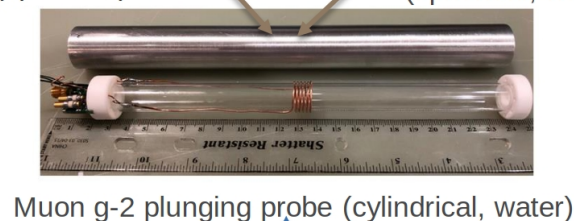
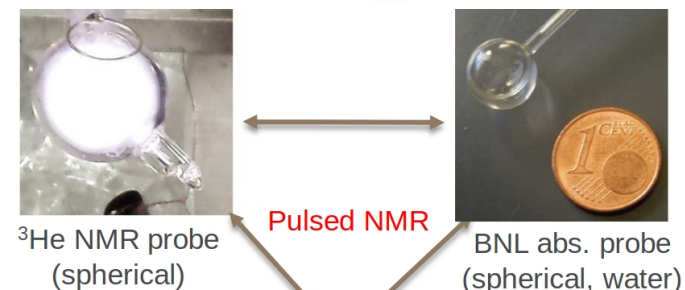
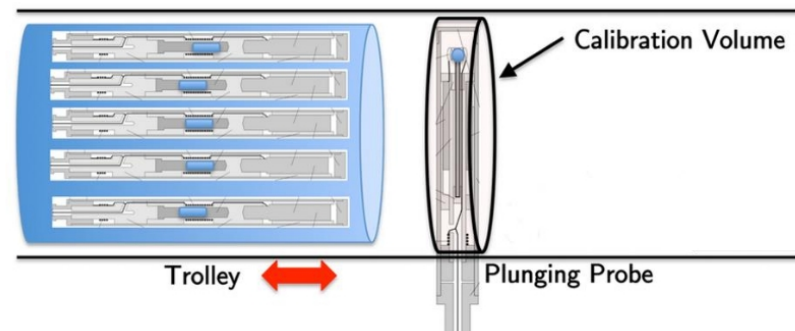
- The largest correction: 347 ppb
- The three different approaches increased confidence and resulted in small reduction of uncertainties to total of only 27 ppb



# Field calibrations

- Excellent performance of field determinations in Run-23, already exceeding TDR goals
- Some improvements and cross checks in Run-456 analysis to increase trust in methods
- New tests on absolute calibration with  $^3\text{He}$  probe
- Cross calibration measurements with Japan collaboration
- Improved trolley position algorithms

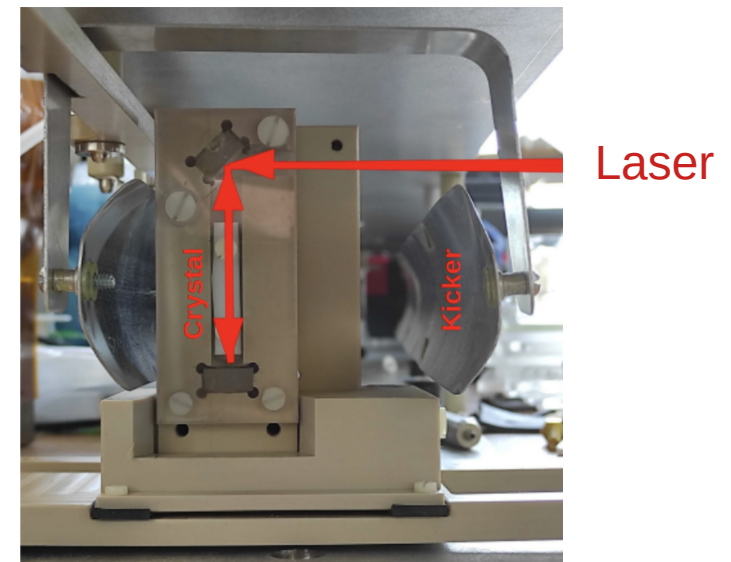
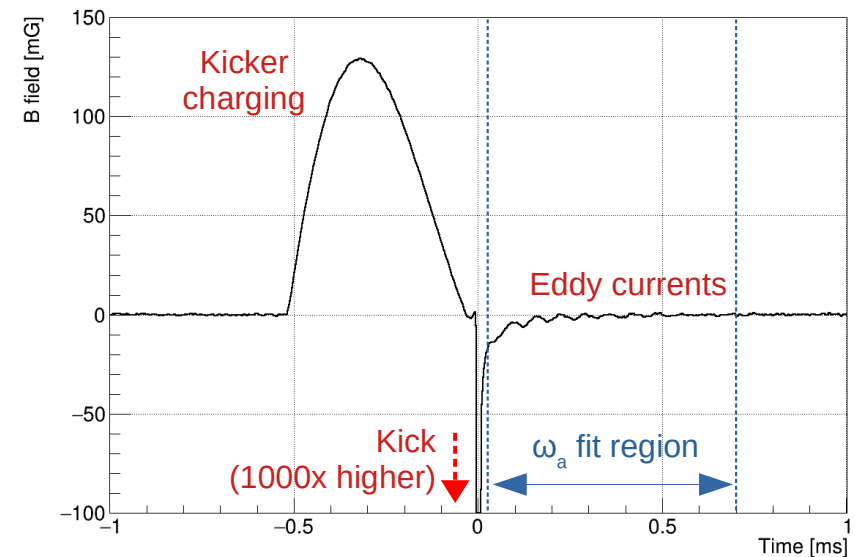
$$\frac{\omega_a}{\omega_p} = \frac{\omega_a^m}{\omega_p^m} \frac{1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml}}{1 + B_k + B_q}$$





# Kicker transient

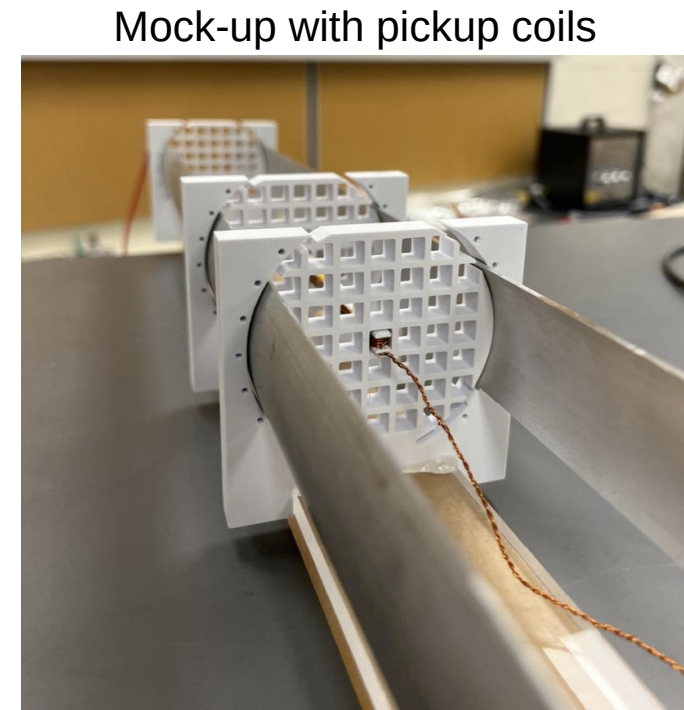
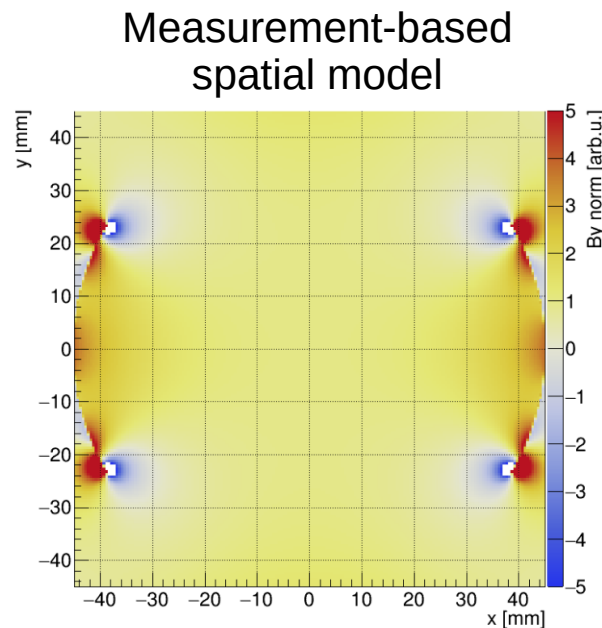
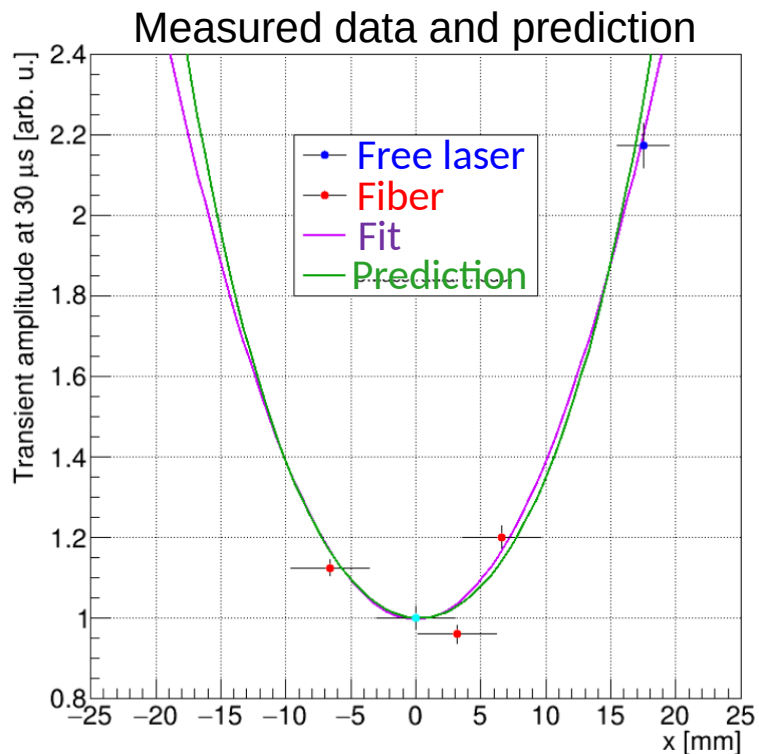
- Kickers induce slowly decaying eddy currents in the surrounding aluminum
- Two Faraday magnetometers to measure the effect: one with optic fibers and a new one with free-space laser since the end of Run-5
- Improved suppression of mechanical vibrations and multiple radial position measurements



$$\frac{\omega_a}{\omega_p} = \frac{\omega_a^m}{\omega_p^m} \frac{1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml}}{1 + B_k + B_q}$$

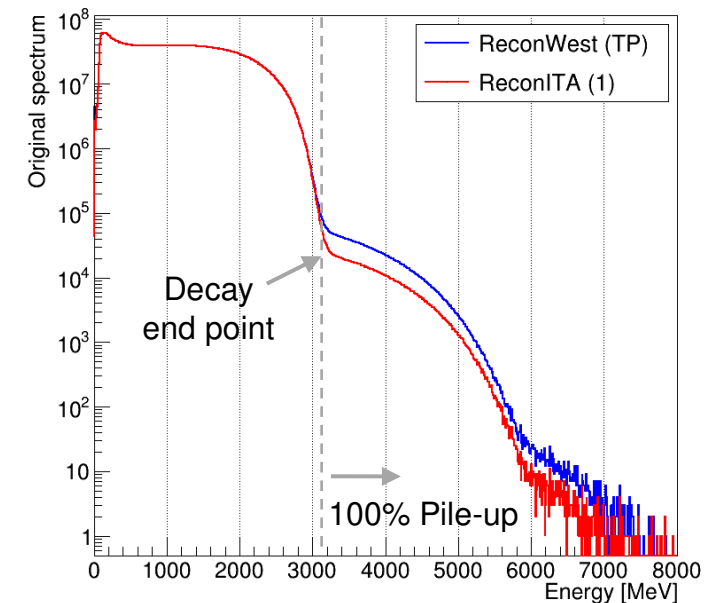
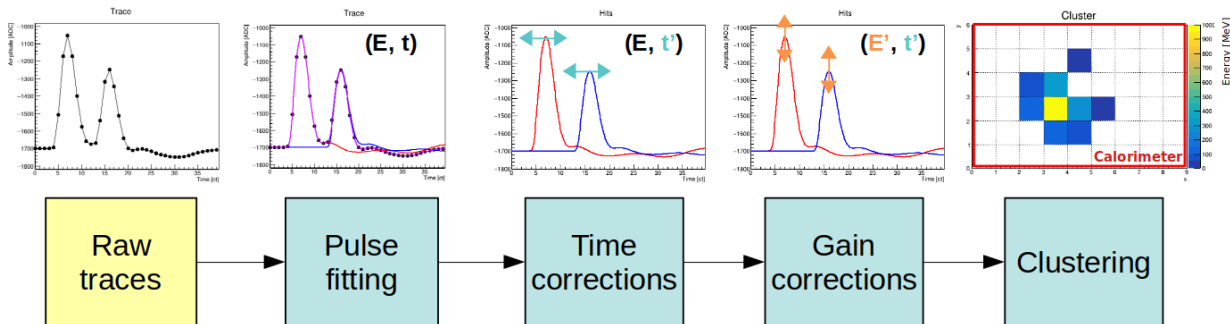
# Kicker transient

- We the new measurements we found that the effect from eddy currents has a radial position dependency
- Confirmed with independent laboratory mock-up measurements



# Positron reconstruction

- Three calorimeter positron reconstructions techniques, with a new one since Run-4
- All have been upgraded to further improve pulse fitting and positron cluster separation
- Pileup has been reduced by 2x or more, and is no longer a dominant systematic in  $\omega_a$  measurement
- Improved energy reconstruction accuracy



$$\frac{\omega_a}{\omega_p} = \frac{\omega_a^m}{\omega_p^m} \frac{1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml}}{1 + B_k + B_q}$$

# Uncertainties

	Statistical (ppb)	Systematic (ppb)	Total (ppb)
Run-1	434	159	462
Run-2/3	201	78	216
Run-4/5/6	114	76	137
Run-1-6	98	78	125

TDR goal:  
100 ppb ✓

TDR goal:  
100 ppb ✓

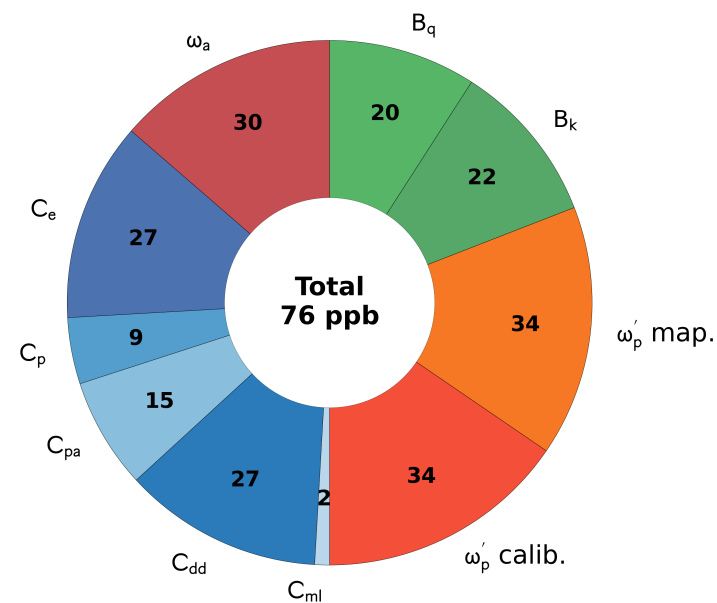
TDR goal:  
140 ppb ✓



# Systematic unc.

Run-4/5/6

Quantity	Correction (ppb)	Uncertainty (ppb)
$\omega_a^m$ (statistical)	...	114
$\omega_a^m$ (systematic)	...	30
$C_e$ Electric Field	347	27
$C_p$ Pitch	175	9
$C_{pa}$ Phase Acceptance	-33	15
$C_{dd}$ Differential Decay	26	27
$C_{ml}$ Muon Loss	0	2
$\langle \omega_p' \times M \rangle$ (mapping, tracking)	...	34
$\langle \omega_p' \times M \rangle$ (calibration)	...	34
$B_k$ Transient Kicker	-37	22
$B_q$ Transient ESQ	-21	20
$\mu_p' / \mu_B$	...	4
$m_\mu / m_e$	...	22
Total systematic for $\mathcal{R}'_\mu$	...	76
Total for $a_\mu$	572	139



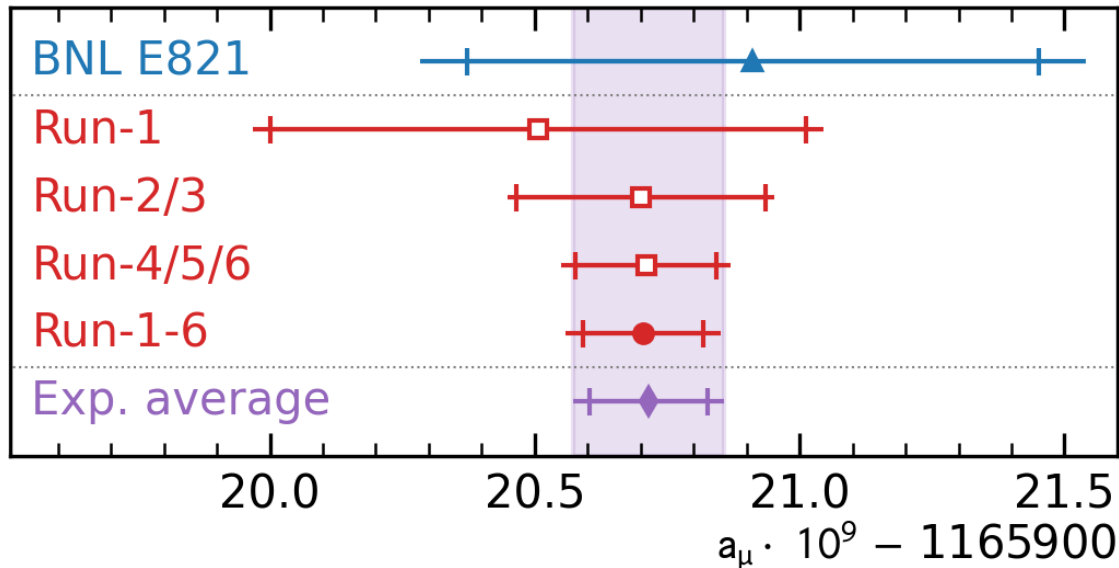
- TDR goal: 100 ppb ✓
- “evenly” distributed
  - No dominant source
  - Further improving would require to reduce in many categories

# Unblinding process

- Calorimeter digitization clocks are artificially de-tuned by a secret  $<40$  ppm amount by two individuals external to the Muon  $g-2$  collaboration
- Many review stages for all analyses. After the final global review, we unblind by revealing the secret offset
- The Run-4/5/6 unblinding took place on May 20th, 2025



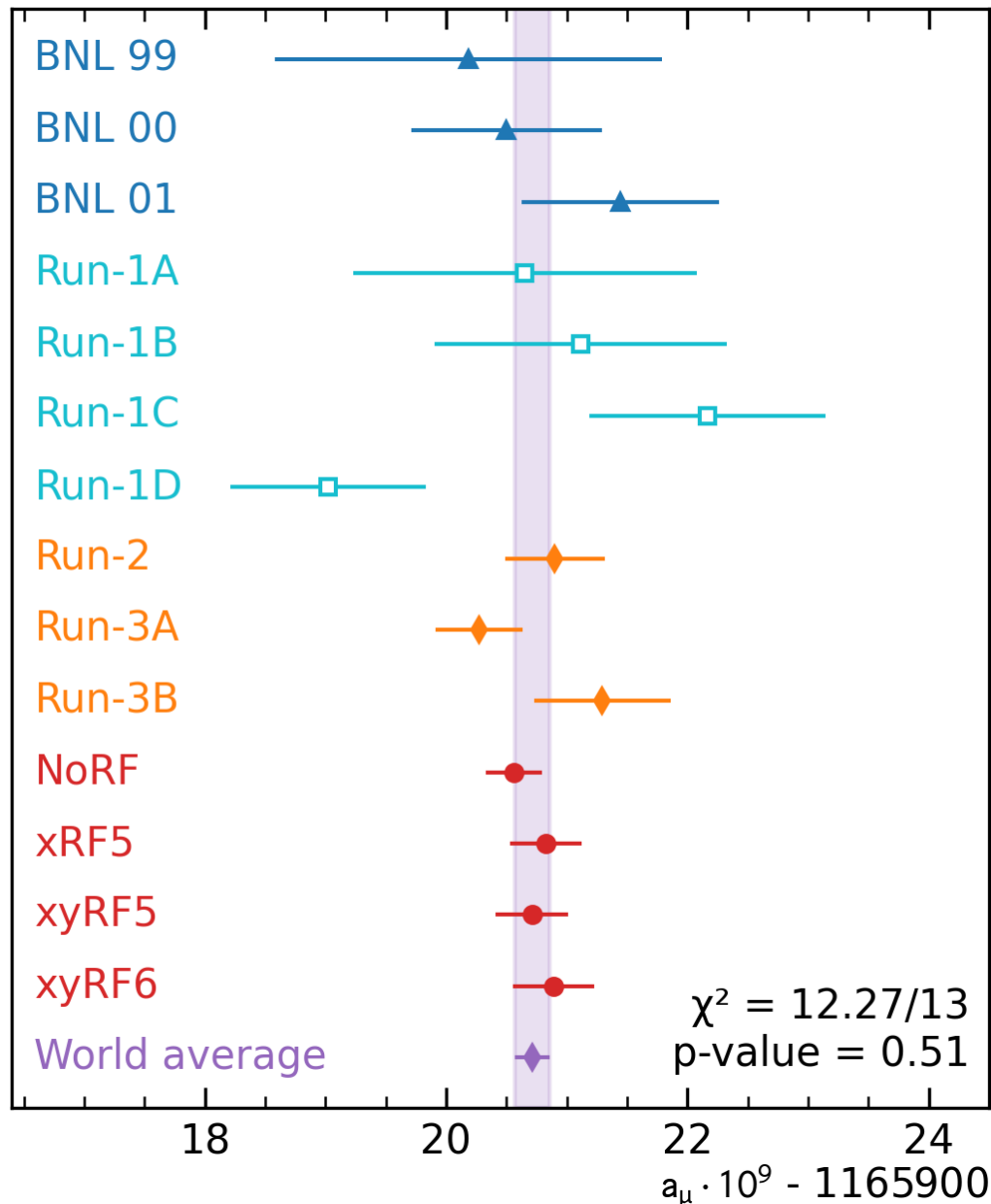
# Final results



- Fantastic agreement with previous runs and with BNL experiment
- World most precise measurement of the muon anomaly
- This measurement will remain a benchmark for many years to come



# Consistency check

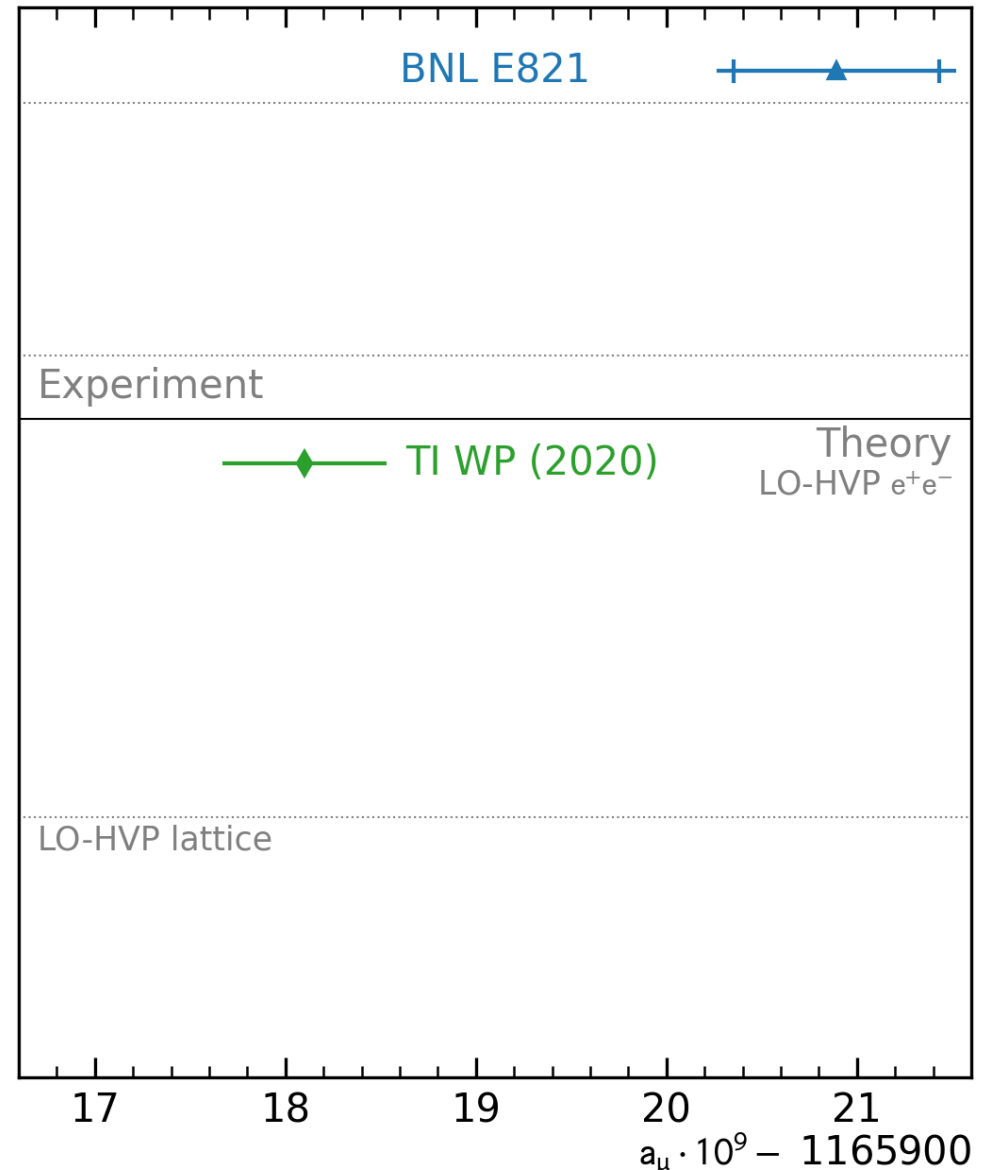


# History

## Before the Fermilab Muon $g-2$ Experiment

- 100+ theorist compile the theoretical input and provide recommendations
- [muon-gm2-theory.illinois.edu](http://muon-gm2-theory.illinois.edu)

- **TI White Paper 2020**  
Physics Reports 887 (2020) 1-166

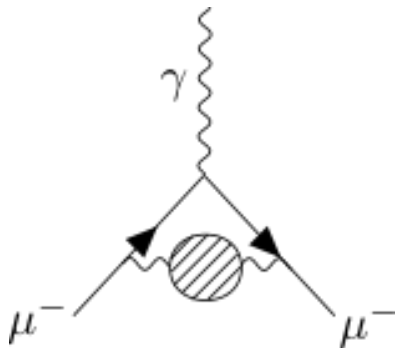




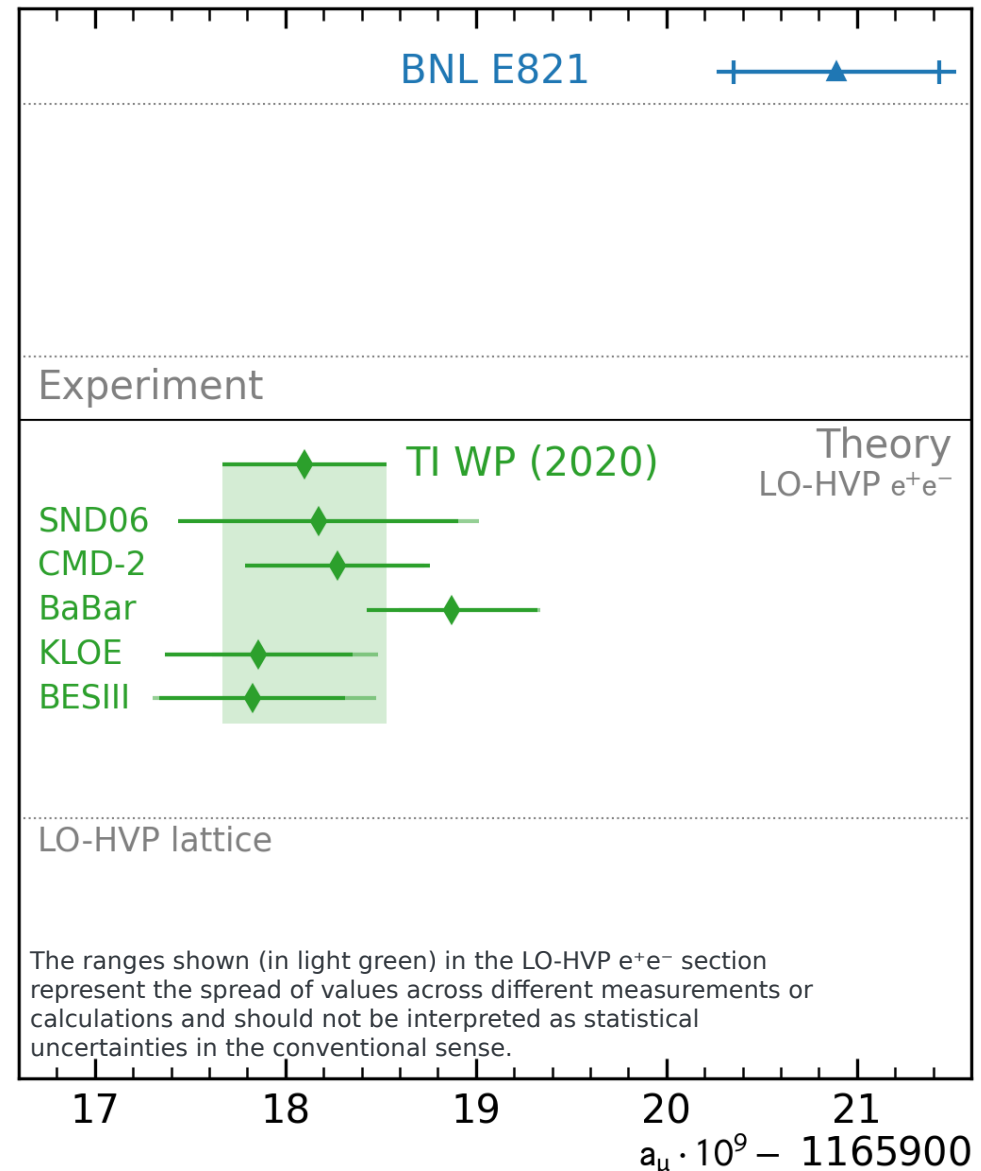
# History

## TI White Paper 2020

- Hadronic Vacuum Polarization (HVP)



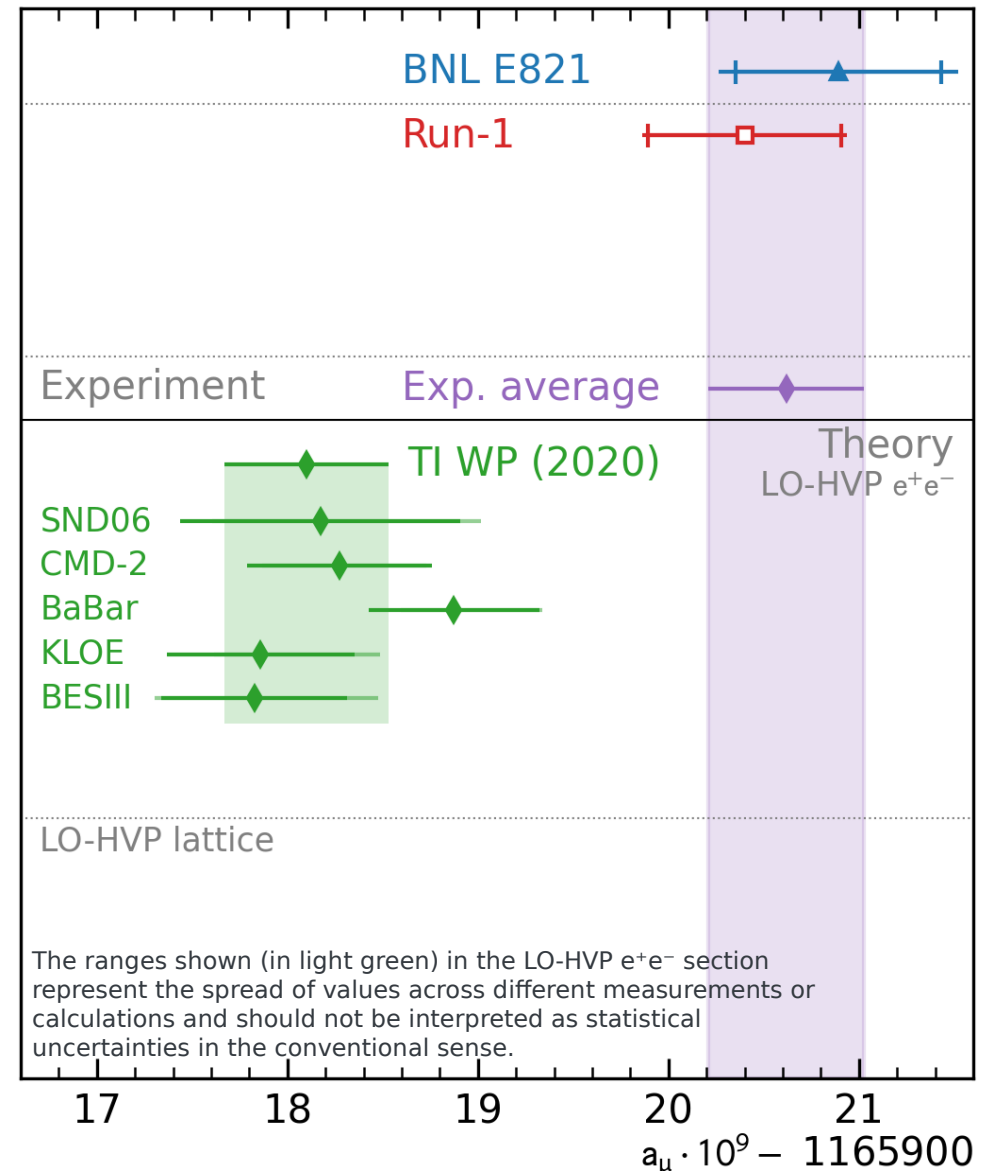
- data-driven dispersive approach from data from different experiments over 20+ years



# History

## April 2021: Fermilab Run-1

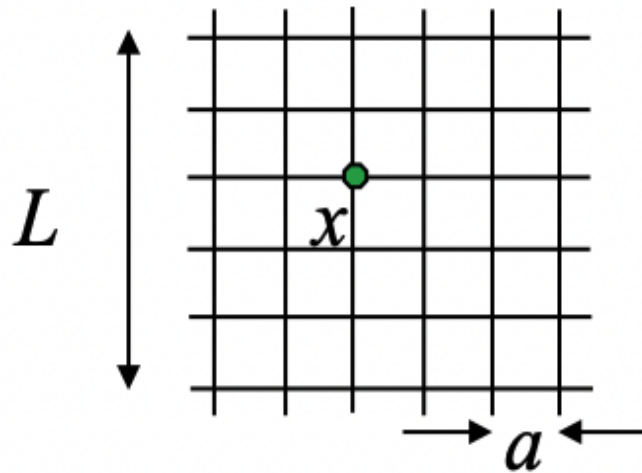
- 5% of our full dataset
- In good agreement with previous results



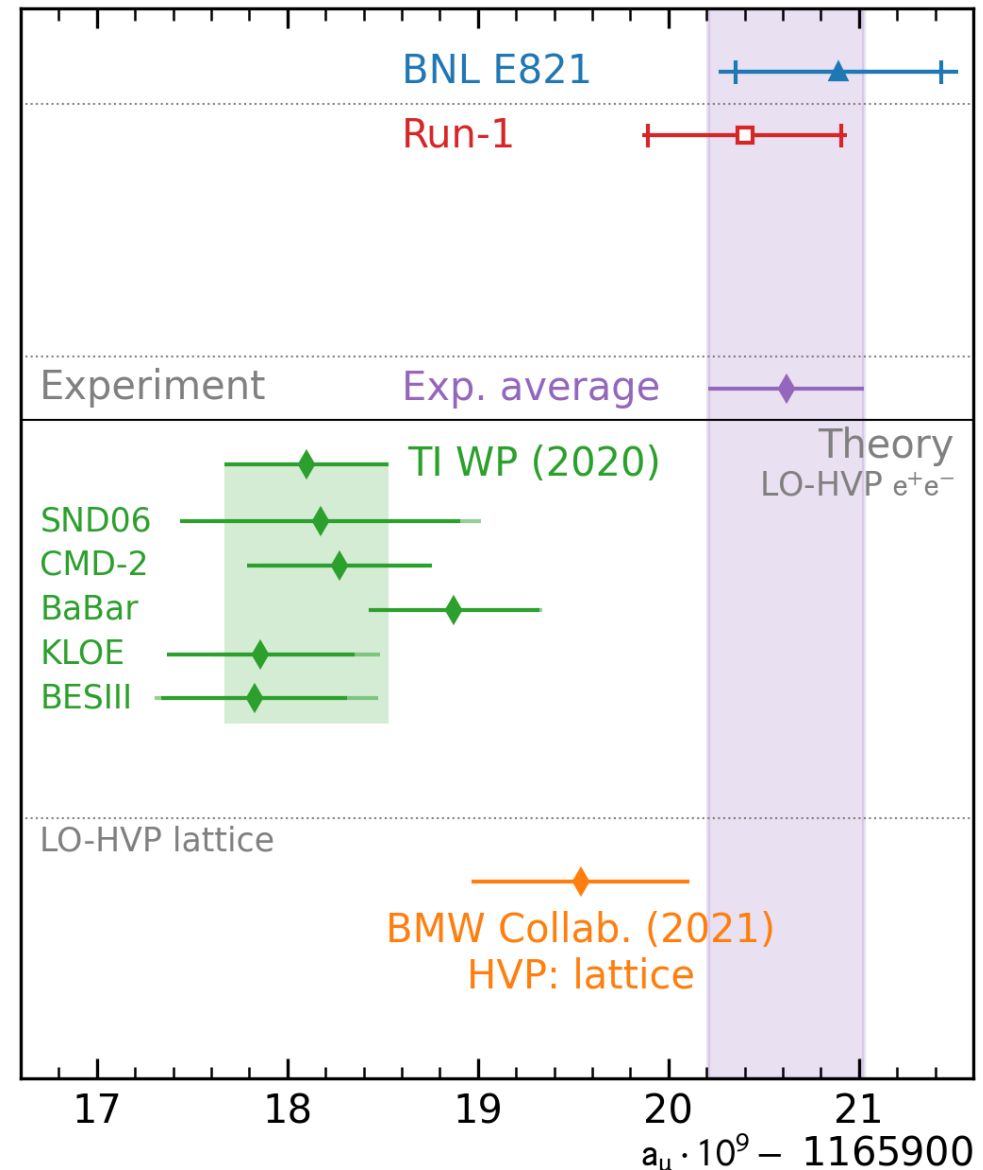
# History

## HVP lattice calculation

- First high-precision calculations of LO-HVP on lattice-QCD



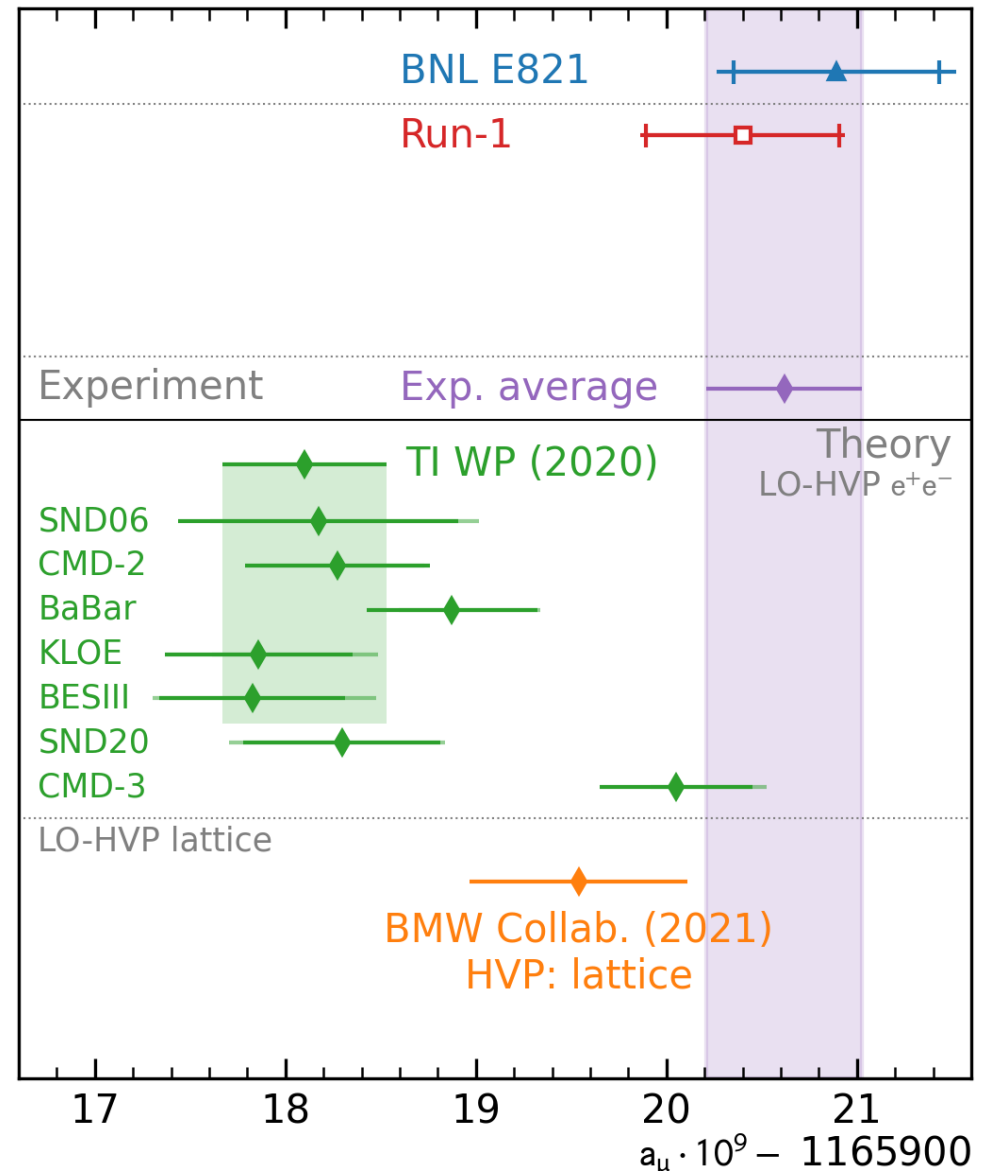
- in tension with the data-driven approach



# History

## New Input Data

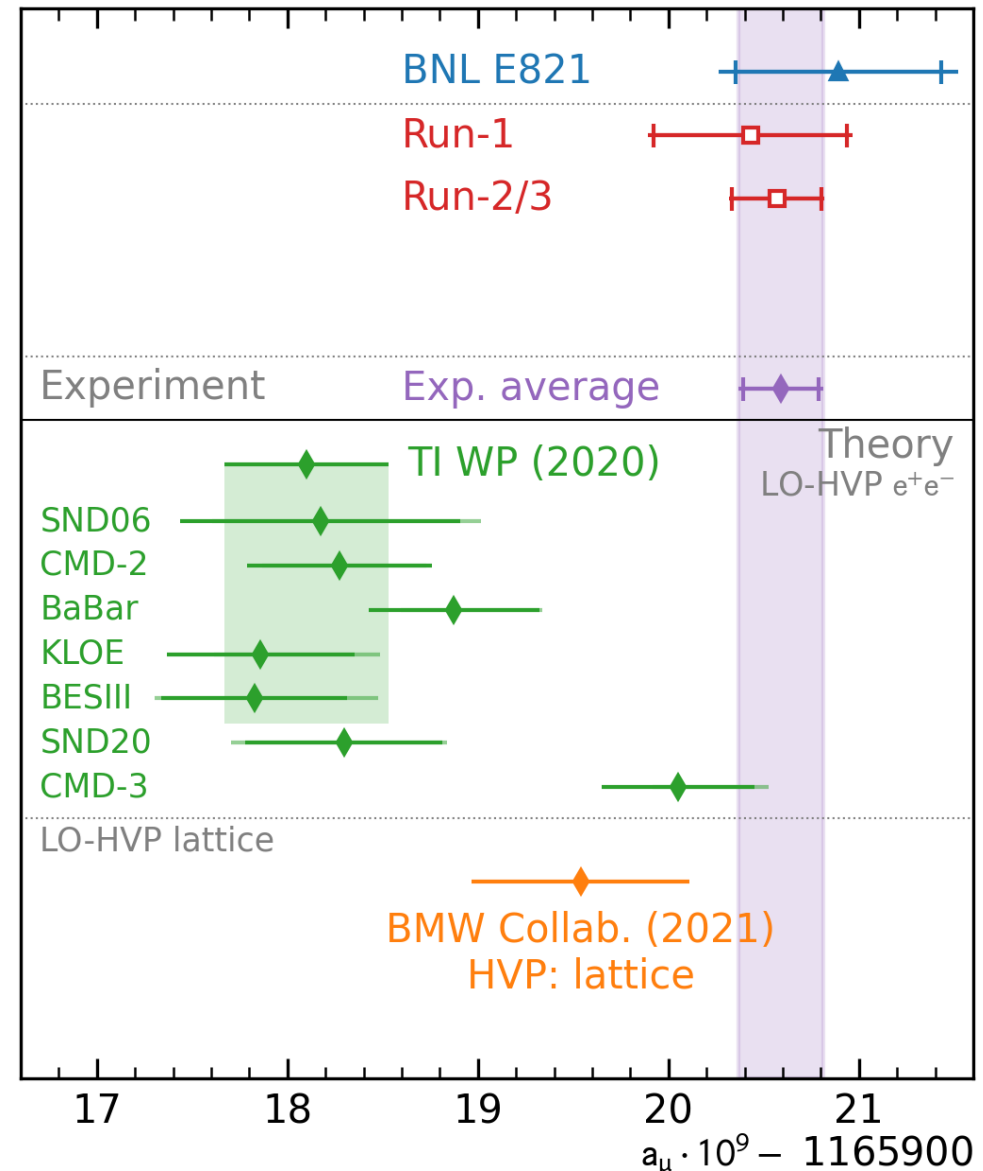
- New results from the CMD-3 experiment are in tension with WP (2020) input



# History

## August 2023: Fermilab Run-2/3

- 4.6 times more data
- More than a two-fold increase in precision

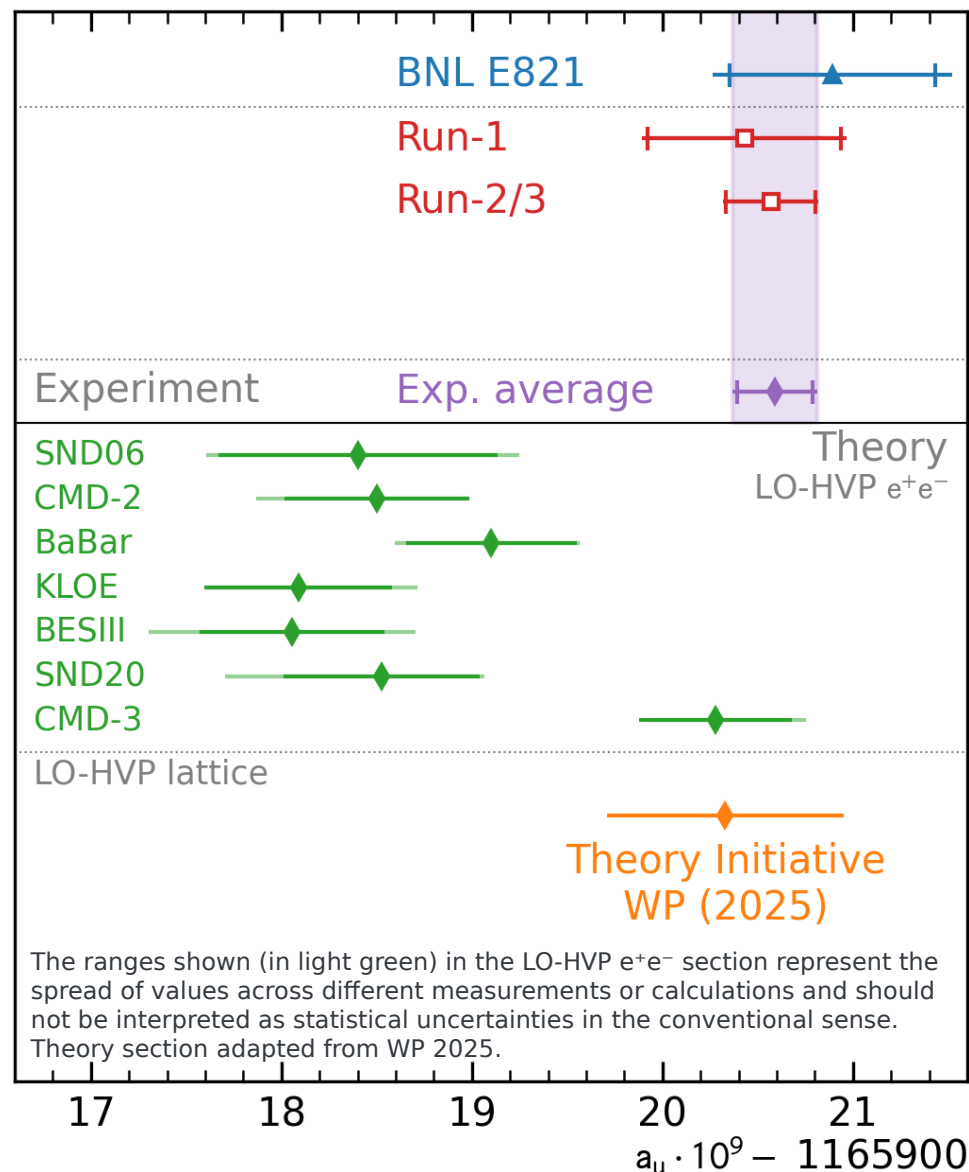




# History

## TI White Paper 2025

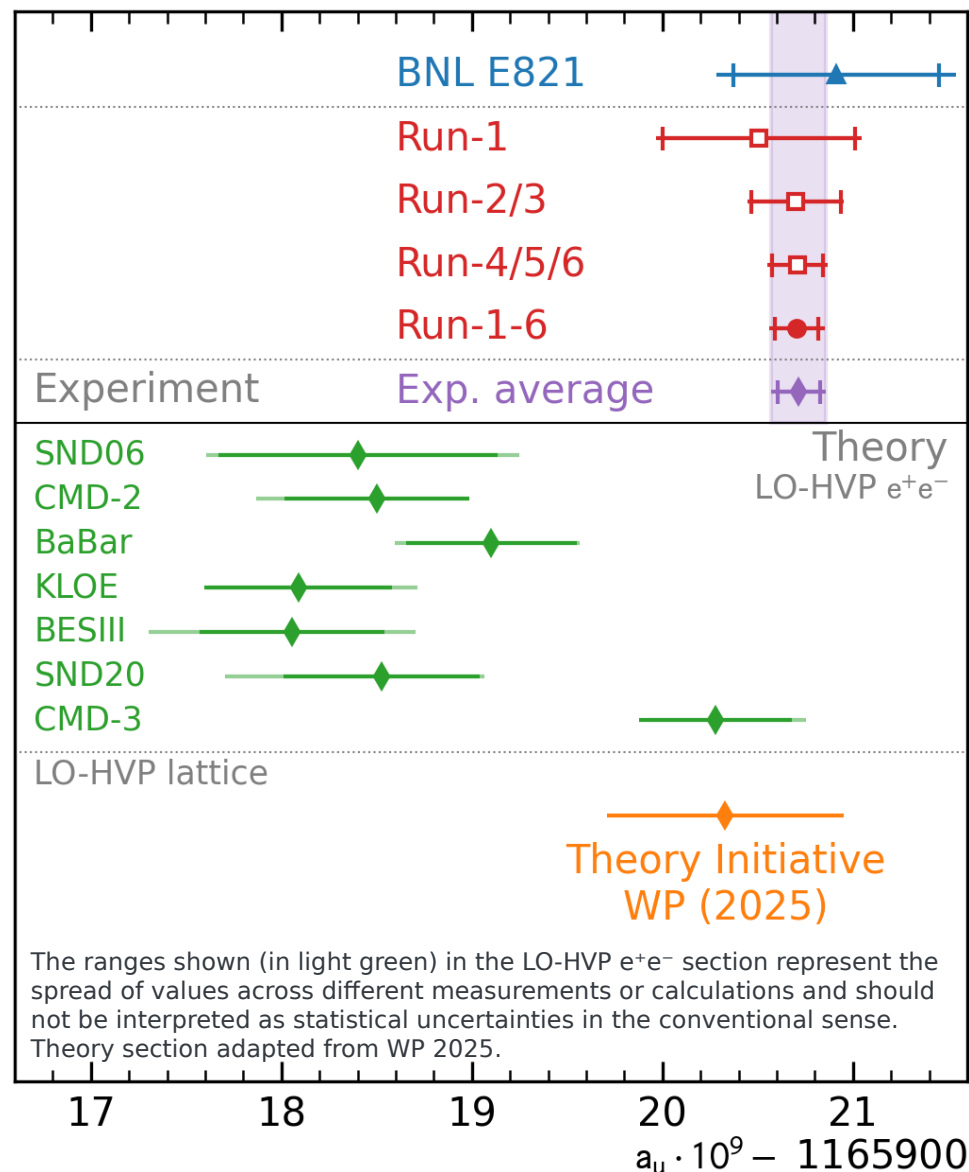
- New TI White Paper (2025) using only lattice-QCD based LO-HVP determination
- Uses input from several published lattice-QCD calculations to compile the WP (2025) value
- \*small changes in the points from other (not HVP-LO) contribution
- **TI White Paper 2025**  
arXiv:2505.21476



# History

## June 2025: Run-4/5/6

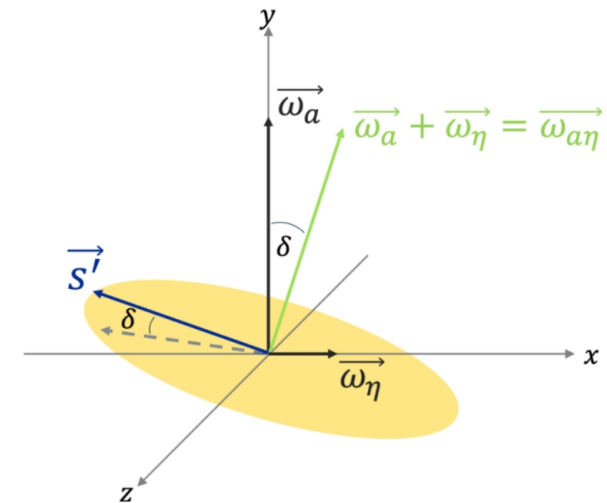
- 2.6 times more data
- Final precision of 127 ppb, more than a 4-fold improvement over the BNL result



# Not only $a_\mu$

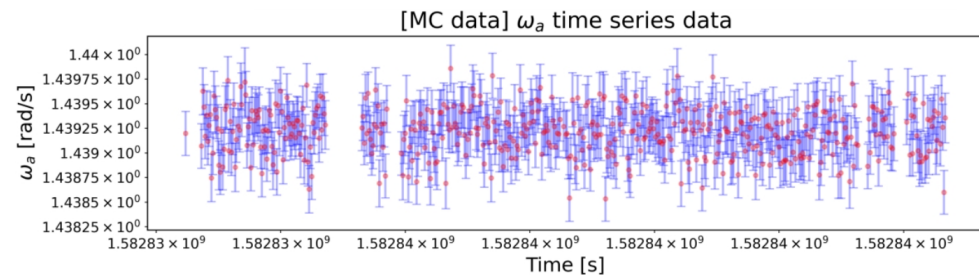
- Electric Dipole Moment (EDM)**

- If the muon has EDM, the spin precession plane will be tilted
- Run-1/2/3 results are expected soon
- Current limit (BNL):  $1.8 \times 10^{-19} \text{ e} \cdot \text{cm}$
- Projected limit:  $< 3 \times 10^{-20} \text{ e} \cdot \text{cm}$



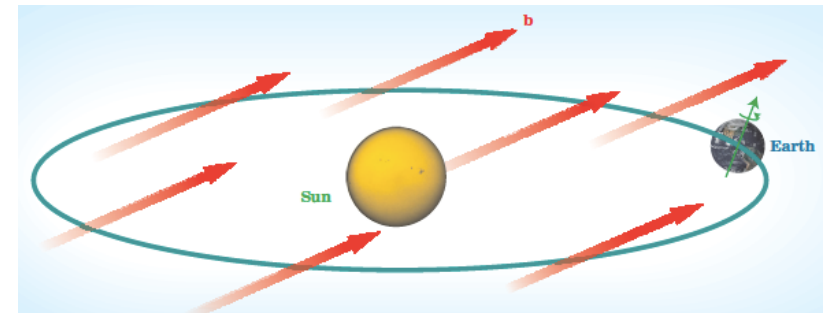
- CPT and Lorentz Invariance violation**

- Sidereal modulation of  $\omega_a$  frequency
- Run-2/3 in review
- Current limit (BNL):  $1.4 \times 10^{-24} \text{ GeV}$
- Projected limit:  $O(10^{-25}) \text{ GeV}$



- Ultralight Muonic Dark Matter (scalar)**

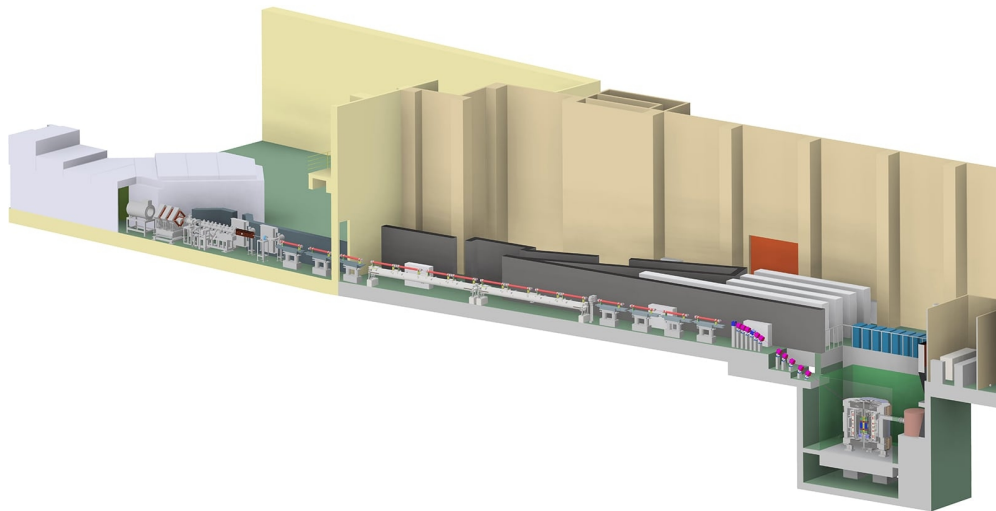
- $\omega_a$  modulated at the DM compton frequency
- Run-2/3 in progress



# Future experiments

- **Muon g-2/EDM Experiment @J-PARC**

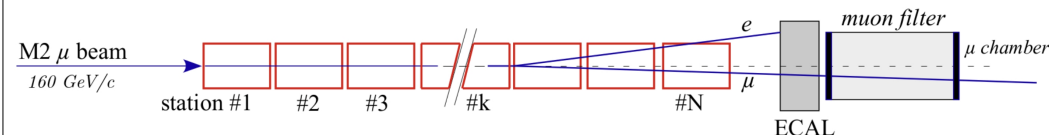
- Innovative novel techniques (muon acceleration, spiral injection, etc.)



- Proposed **MUonE @CERN**

$$a_{\mu}^{HLO} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{had}[t(x)]$$

- hadronic contribution to the running of  $\Delta\alpha_{had}$  in the space-like region
- can be extracted from the shape of differential cross section





# Future theory improvements

- Ongoing work in experimental inputs on  $\sigma(e^+e^- \rightarrow \text{hadrons})$
- Initial State Radiation technique:
  - BaBar: new analysis of large  $\pi\pi$  data set with better detector
  - KLOE: new analysis of 7x larger  $\pi\pi$  set
  - BESIII: new results for  $\pi\pi$  channel and  $\pi\pi\pi$
  - Belle II: larger statistics than BaBar or KLOE and similar or better systematics for low-energy cross sections
- Energy scan (VEPP-2000 machine in Novosibirsk)
  - SND: new results for  $\pi\pi$  channel
  - CMD-3: more channels to be analyzed
- The RadioMonteCarLow2 initiative is committed to improving the Monte Carlo event generators

# Summary

PHYSICAL REVIEW LETTERS **135**, 101802 (2025)

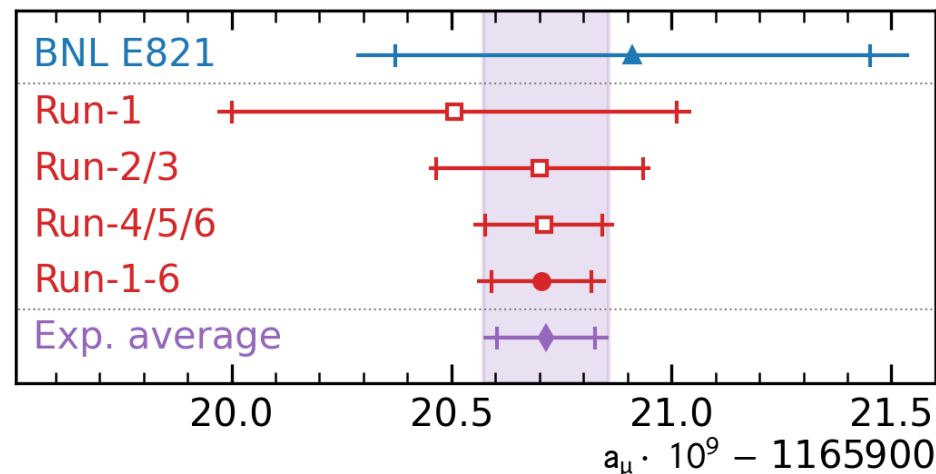
Editors' Suggestion

Featured in Physics

## Measurement of the Positive Muon Anomalous Magnetic Moment to 127 ppb

D. P. Aguillard<sup>33</sup>, T. Albahri<sup>30</sup>, D. Allsach<sup>7</sup>, J. Annala<sup>7</sup>, K. Badgley<sup>7</sup>, S. Baeßler<sup>35</sup>, I. Bailey<sup>16,a</sup>, L. Bailey<sup>27</sup>, E. Barlas-Yucel<sup>28,b</sup>, T. Barrett<sup>6</sup>, E. Barzi<sup>7</sup>, F. Bedeschi<sup>10</sup>, M. Berz<sup>17</sup>, M. Bhattacharya<sup>7</sup>, H. P. Binney<sup>36</sup>, P. Bloom<sup>18</sup>, J. Bono<sup>7</sup>, E. Bottalico<sup>30</sup>, T. Bowcock<sup>30</sup>, S. Braun<sup>36</sup>, M. Bressler<sup>32</sup>, G. Cantatore<sup>12,c</sup>, R. M. Carey<sup>2</sup>, B. C. K. Casey<sup>7</sup>, D. Cauz<sup>26,d</sup>, R. Chakraborty<sup>29</sup>, A. Chapelain<sup>6</sup>, S. Chappa<sup>7</sup>, S. Charity<sup>30</sup>, C. Chen<sup>22,21,e</sup>, M. Cheng<sup>28</sup>, R. Chislett<sup>27</sup>, Z. Chu<sup>21,e</sup>, T. E. Chupp<sup>33</sup>, C. Claessens<sup>36</sup>, F. Confortini<sup>9,f</sup>, M. E. Convery<sup>7</sup>, S. Corrodi<sup>1</sup>, L. Cotrozzi<sup>30</sup>, J. D. Crnkovic<sup>7</sup>, S. Dabagov<sup>8,g</sup>, P. T. Debevec<sup>28</sup>, S. Di Falco<sup>10</sup>, G. Di Sciascio<sup>11</sup>, S. Donati<sup>10,h</sup>, B. Drendel<sup>7</sup>, A. Driutti<sup>10,29</sup>, M. Eads<sup>19</sup>, A. Edmonds<sup>2,37</sup>, J. Esquivel<sup>7</sup>, M. Farooq<sup>33</sup>, R. Fatemi<sup>29</sup>, K. Ferraby<sup>30</sup>, C. Ferrari<sup>10,i</sup>, M. Ferli<sup>14</sup>, A. T. Fienberg<sup>36</sup>, A. Fioretti<sup>10,i</sup>, D. Flay<sup>32</sup>, S. B. Foster<sup>29,2</sup>, H. Friedsam<sup>7</sup>, N. S. Froemming<sup>19</sup>, C. Gabbanini<sup>10,i</sup>, I. Gaines<sup>7</sup>, S. Ganguly<sup>7</sup>, J. George<sup>32,j</sup>, L. K. Gibbons<sup>6</sup>, A. Gioiosa<sup>25,k</sup>, K. L. Giovanetti<sup>13</sup>, P. Girotti<sup>10,i</sup>, W. Gohn<sup>29</sup>, L. Goodenough<sup>7</sup>, T. Gorringer<sup>29</sup>, J. Grange<sup>33</sup>, S. Grant<sup>1,27</sup>, F. Gray<sup>20</sup>, S. Haciomeroglu<sup>5,m</sup>, T. Halewood-Leagas<sup>30</sup>, D. Hampai<sup>8</sup>, F. Han<sup>29</sup>, J. Hempstead<sup>36</sup>, D. W. Hertzog<sup>36</sup>, G. Hesketh<sup>27</sup>, E. Hess<sup>10</sup>, A. Hibbert<sup>30</sup>, Z. Hodge<sup>36</sup>, S. Y. Hoh<sup>22,21,e</sup>, K. W. Hong<sup>35</sup>, R. Hong<sup>1,29</sup>, T. Hu<sup>22,21,e</sup>, Y. Hu<sup>21,e</sup>, M. Iacovacci<sup>9,f</sup>, M. Incagli<sup>10</sup>, S. Israel<sup>2,32</sup>, P. Kammel<sup>36</sup>, M. Kargiantoulakis<sup>7</sup>, M. Karuza<sup>12,n</sup>, J. Kaspar<sup>36</sup>, D. Kawall<sup>32</sup>, L. Kelton<sup>29,23</sup>, A. Keshavarzi<sup>31</sup>, D. S. Kessler<sup>32</sup>, K. S. Khaw<sup>22,21,e</sup>, Z. Khechadorian<sup>6</sup>, B. Kiburg<sup>7</sup>, M. Kiburg<sup>7,18</sup>, O. Kim<sup>34</sup>, N. Kinnaird<sup>2</sup>, E. Kraegelloh<sup>4,q</sup>, K. R. Labe<sup>6</sup>, J. LaBounty<sup>36</sup>, M. Lancaster<sup>31</sup>, S. Lee<sup>5</sup>, B. Li<sup>21,o</sup>, D. Li<sup>21,p</sup>, L. Li<sup>21,e</sup>, I. Logashenko<sup>4,q</sup>, A. Lorente Campos<sup>29</sup>, Z. Lu<sup>21,e</sup>, A. Lucà<sup>7</sup>, G. Lukicov<sup>27</sup>, A. Lusiani<sup>10,r</sup>, A. L. Lyon<sup>7</sup>, B. MacCoy<sup>36</sup>, R. Madrak<sup>7</sup>, K. Makino<sup>17</sup>, S. Mastroianni<sup>9</sup>, R. McCarthy<sup>2,s</sup>, J. P. Miller<sup>2</sup>, S. Miozzi<sup>11</sup>, B. Mitra<sup>34</sup>, J. P. Morgan<sup>7</sup>, W. M. Morse<sup>3</sup>, J. Mott<sup>7</sup>, A. Nath<sup>9,f</sup>, J. K. Ng<sup>22,21,e</sup>, H. Nguyen<sup>7</sup>, Y. Oksuzian<sup>1</sup>, Z. Omarov<sup>15,5</sup>, W. Osar<sup>6</sup>, R. Osofsky<sup>36</sup>, S. Park<sup>5</sup>, G. Pauletta<sup>26,t,d</sup>, J. Peck<sup>29</sup>, G. M. Piacentino<sup>25,k</sup>, R. N. Pilato<sup>30</sup>, K. T. Pitts<sup>28,b</sup>, B. Plaster<sup>29</sup>, D. Počanić<sup>35</sup>, N. Pohlman<sup>19</sup>, C. C. Polly<sup>7</sup>, J. Price<sup>30</sup>, B. Quinn<sup>34</sup>, M. U. H. Qureshi<sup>14</sup>, G. Rakness<sup>7</sup>, S. Ramachandran<sup>1,j</sup>, E. Ramberg<sup>7</sup>, R. Reimann<sup>14</sup>, B. L. Roberts<sup>2</sup>, D. L. Rubin<sup>6</sup>, M. Sakurai<sup>27</sup>, L. Santi<sup>26,u,d</sup>, C. Schlesier<sup>28,i</sup>, A. Schreckenberger<sup>7</sup>, Y. K. Semertzidis<sup>5,15</sup>, A. K. Soha<sup>7</sup>, M. Sorbara<sup>11,u</sup>, J. Stapleton<sup>7</sup>, D. Still<sup>7</sup>, D. Stöckinger<sup>24</sup>, C. Stoughton<sup>7</sup>, D. Stratakis<sup>7</sup>, H. E. Swanson<sup>36</sup>, G. Sweetmore<sup>31</sup>, D. A. Sweigart<sup>6</sup>, M. J. Syphers<sup>19</sup>, Y. Takeuchi<sup>22,21,e</sup>, D. A. Tarazona<sup>6</sup>, T. Teubner<sup>30</sup>, A. E. Tewsley-Booth<sup>29,33</sup>, V. Tishchenko<sup>3</sup>, N. H. Tran<sup>2,v</sup>, W. Turner<sup>30</sup>, E. Valetov<sup>17</sup>, D. Vasilkova<sup>30</sup>, G. Venanzoni<sup>30,w</sup>, T. Walton<sup>7</sup>, A. Weisskopf<sup>17</sup>, L. Welty-Rieger<sup>7</sup>, P. Winter<sup>1</sup>, Y. Wu<sup>1</sup>, B. Yu<sup>34</sup>, M. Yucel<sup>7</sup>, E. Zaid<sup>30</sup>, Y. Zeng<sup>22,21,e</sup> and C. Zhang<sup>30</sup>

(Muon  $g-2$  Collaboration)



- Phys. Rev. Lett. **135**, 101802  
<https://doi.org/10.1103/7clf-sm2v>
- Release talk (June 3rd) and 8-minute explainer video at  
<https://www.youtube.com/@fermilab>
- Visit <https://muon-g-2.fnal.gov>

谢谢 for listening!



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- Department of Energy (USA)
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- Royal Society (UK)
- Leverhulme Trust (UK)
- European Union's Horizon 2020
- Strong 2020 (EU)
- German Research Foundation (DFG)
- National Natural Science Foundation of China
- MSIP, NRF and IBS-R017-D1 (Republic of Korea)



Science and  
Technology  
Facilities Council

LEVERHULME  
TRUST



Horizon 2020

**STRONG-2020**

**DFG** Deutsche  
Forschungsgemeinschaft



**国家自然科学基金委员会**  
National Natural Science Foundation of China



# Backup

# WP25 - dispersive

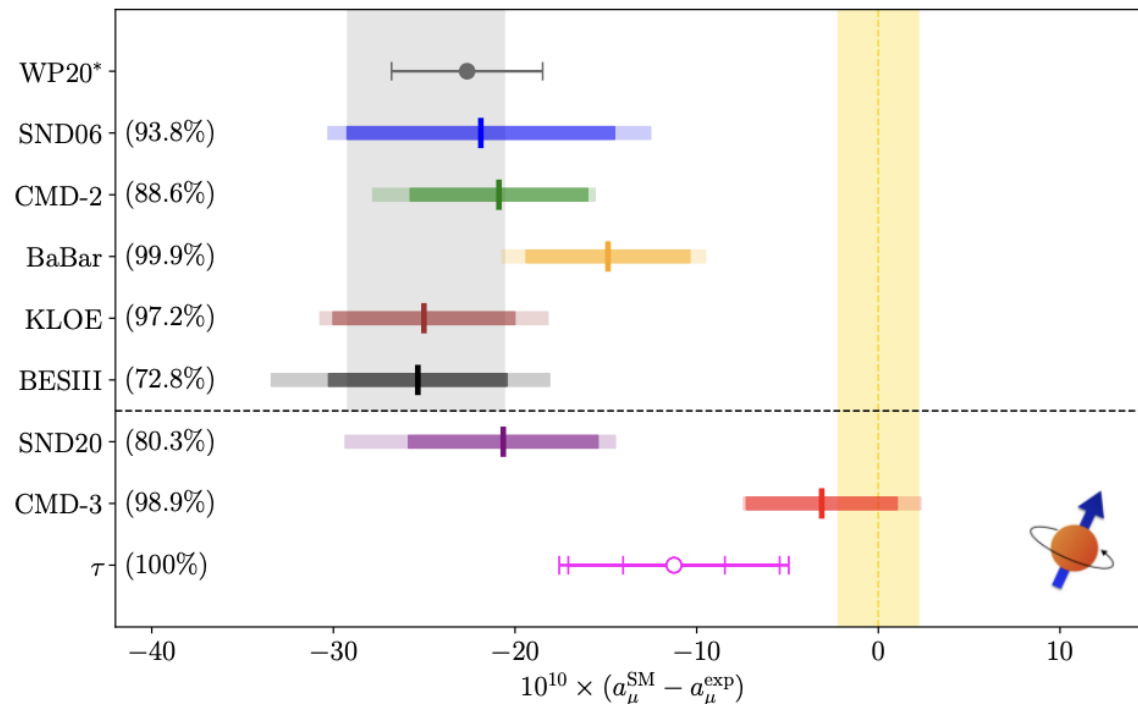
- Calculated from data for  $\sigma(e^+e^- \rightarrow \text{hadrons})$

$\text{Im} \text{ had.} \sim \left| \text{had.} \right|^2 \longrightarrow a_\mu^{\text{HVP,LO}} = \frac{\alpha^2}{3\pi^2} \int_{s_{th}}^{\infty} \frac{K(s)}{s} R(s) ds$

Analyticity & Unitarity

Hadronic R-ratio  
(Data Driven)

- Uses **data** from different experiments from **20+ years**
- 1/s weights low energy strongly: 73% from  **$\pi^+\pi^-$  channel**





# WP25 - dispersive

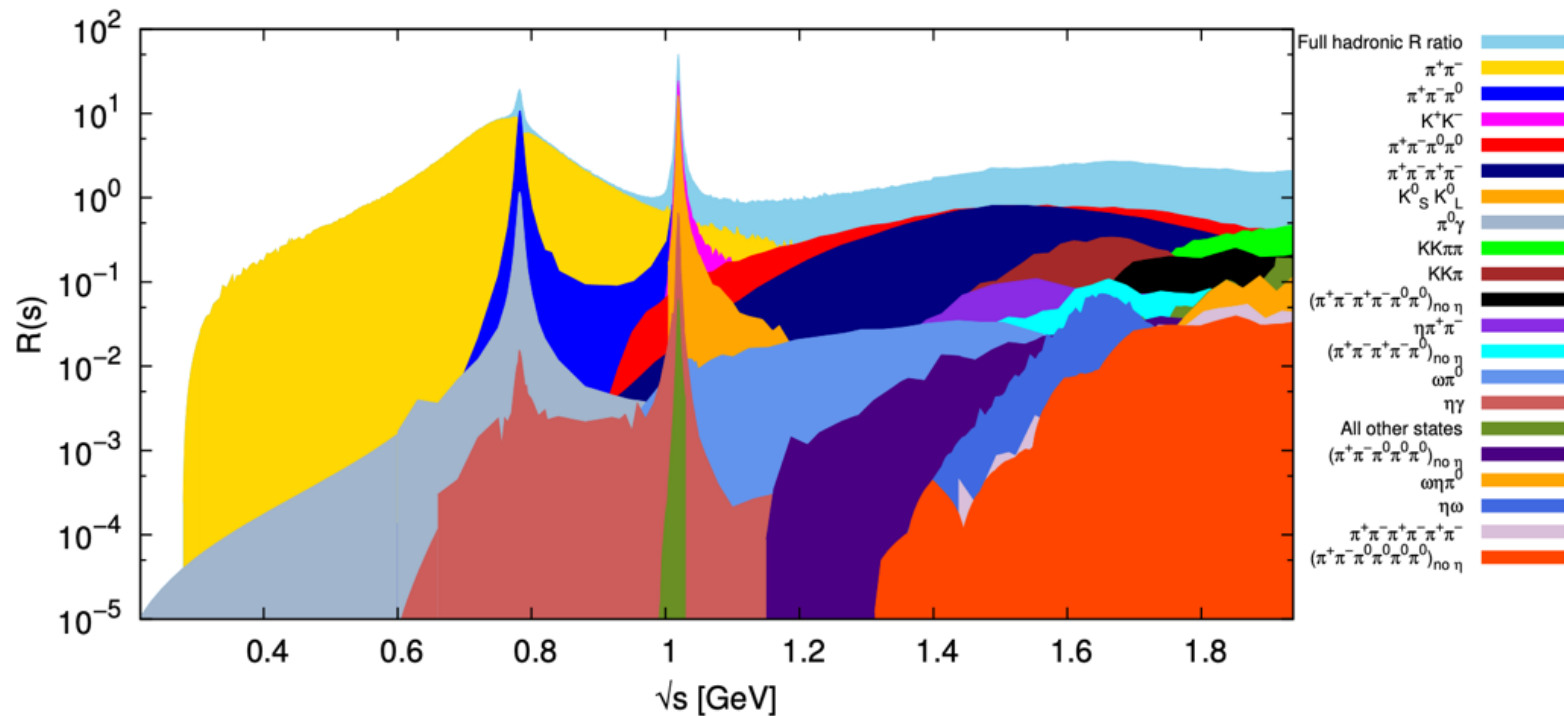


Figure 16: Contributions to the KNT data compilation of the total hadronic  $R$ -ratio from the different hadronic final states below 1.937 GeV [30, 265]. The full  $R$ -ratio is shown in light blue. Each final state is included as a new layer on top in decreasing order of the size of its contribution to  $a_\mu^{\text{HVP, LO}}$ .

# WP25 - lattice QCD

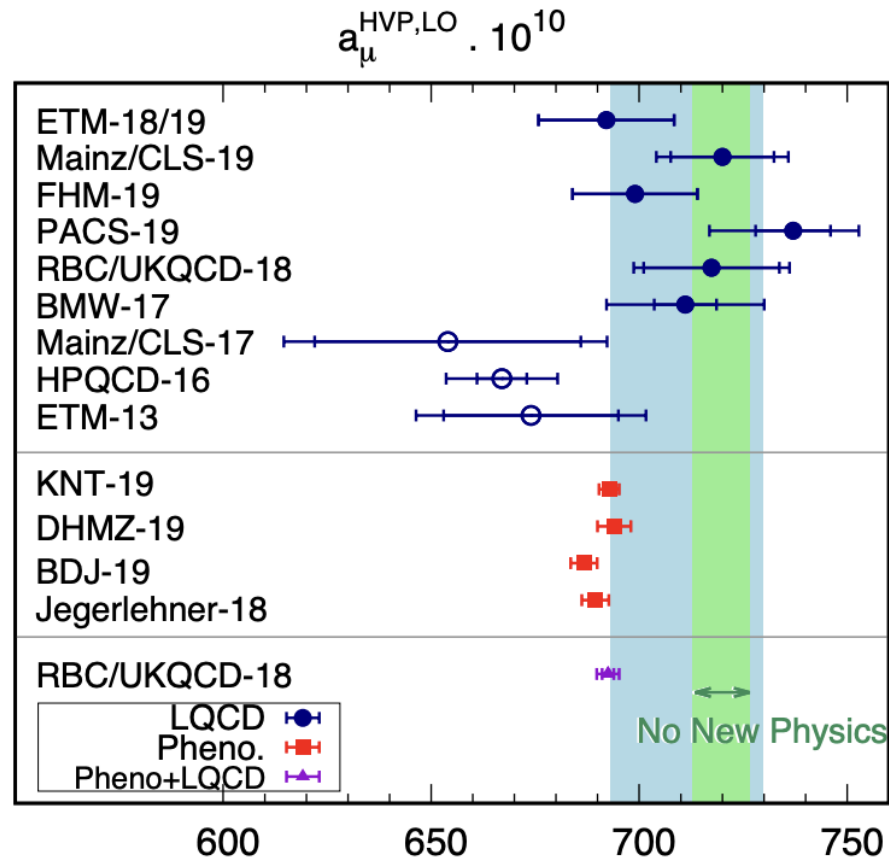


Figure 44: Compilation of recent results for  $a_\mu^{\text{HVP,LO}}$  in units of  $10^{-10}$ . The filled dark blue circles are lattice results that are included in the “lattice world average”. The average, which is obtained from a conservative averaging procedure in Sec. 3.5.1, is indicated by a light blue band, while the light-green band indicates the “no new physics” scenario, where  $a_\mu^{\text{HVP,LO}}$  results are large enough to bring the SM prediction of  $a_\mu$  into agreement with experiment. The unfilled dark blue circles are lattice results that are older or superseded by more recent calculations. The red squares indicate results obtained from the data-driven methods reviewed in Sec. 2. See Table 8 for more information on the results included in the plot. Adapted from Ref. [443].