



# Precision Predictions for Three-Dimensional Nucleon Tomography

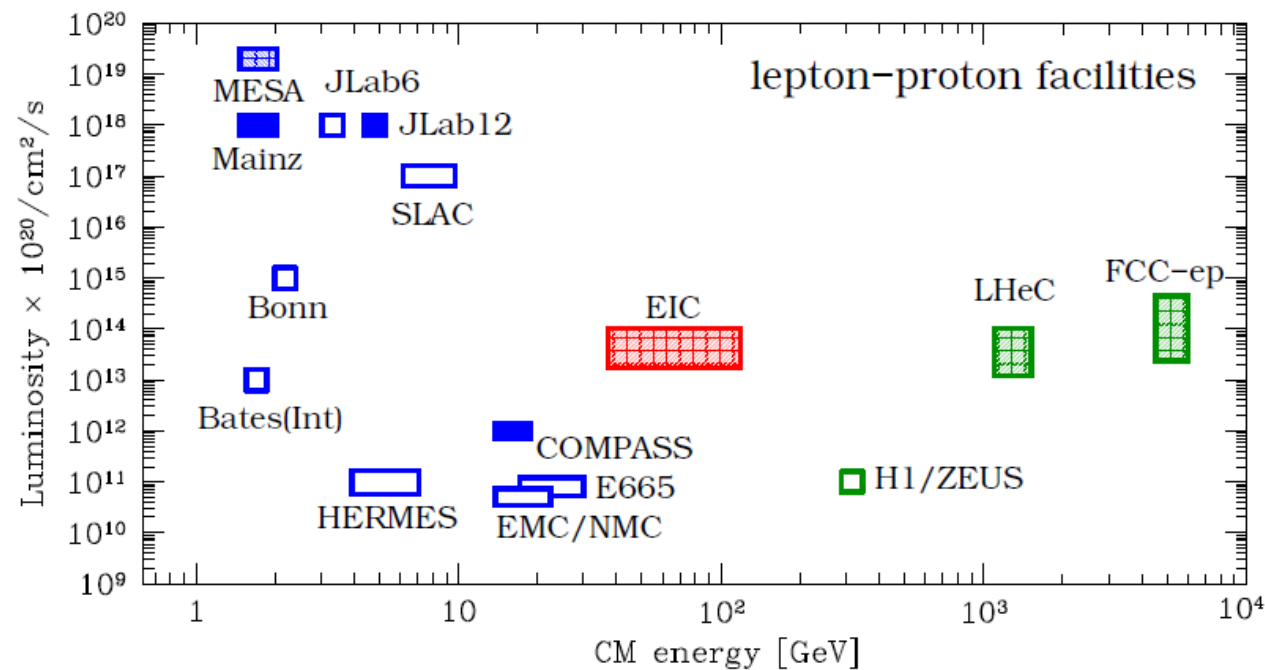
Shen Fang (方申)  
Fudan University

**The 26<sup>th</sup> international symposium on spin physics (SPIN2025)**  
**Qingdao Sep 23, 2025**

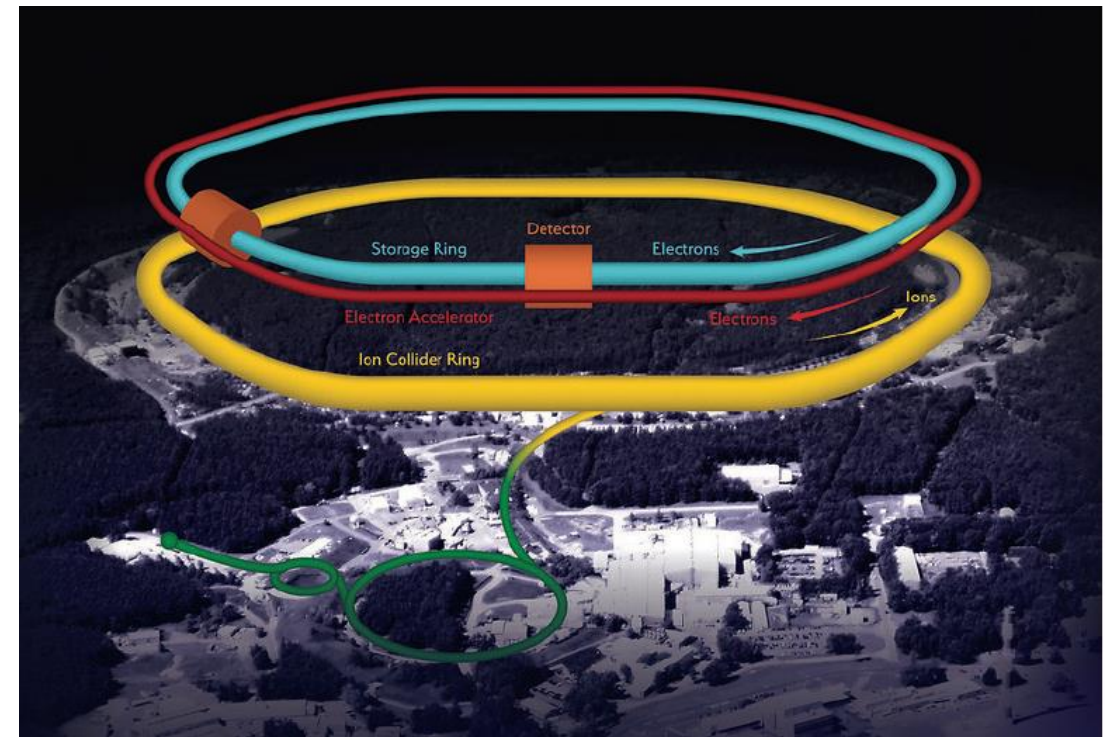
Collaborators: Dingyu Shao, Weiyao Ke, John Terry,  
Meisen Gao, Haitao Li, Zhongbo Kang

Reference: JHEP05(2024)066, JHEP01(2025)029

# Electron-ion collider (EIC)

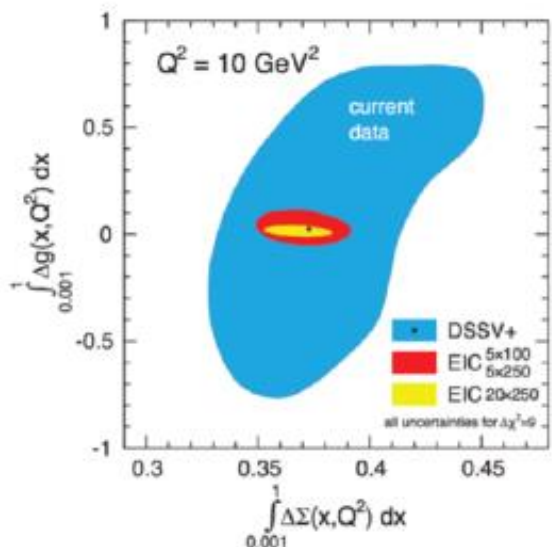


Abdul et al. '22

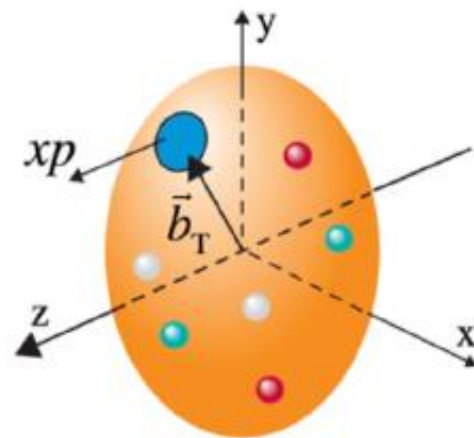


Abdul et al. '22

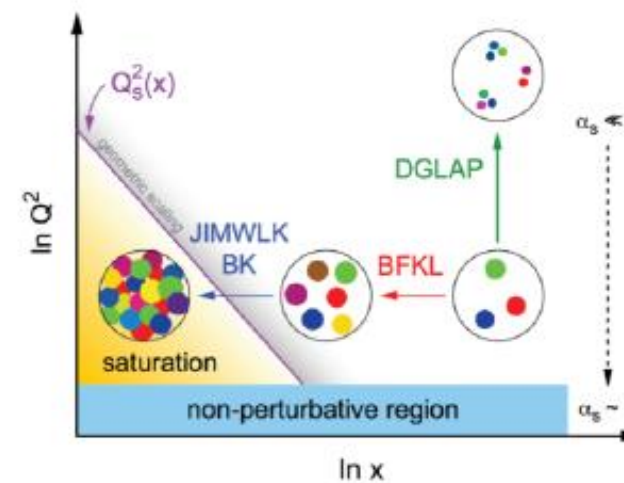
**Proton spin**



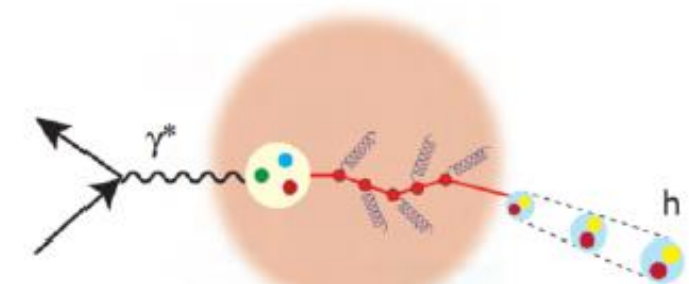
**3D nucleon tomography**



**Gluon saturation**



**Hadronization in the nucleus**

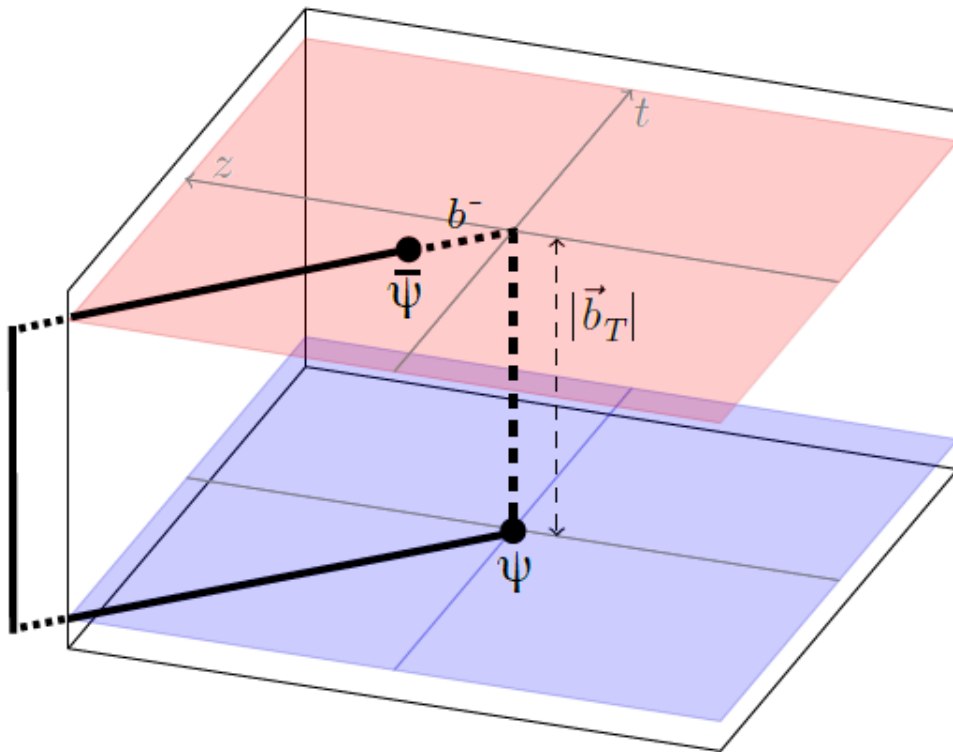


# 3D imaging of the nucleons

- Both longitudinal and transverse motion
- Correlation between nucleon spin with parton(quark, gluon) orbital angular momentum

$$\tilde{f}_{i/p_S}^{[\Gamma]0(u)}(x, \mathbf{b}_T, \epsilon, \tau, xP^+) = \int \frac{db^-}{2\pi} e^{-ib^-(xP^+)} \left\langle p(P, S) \left| \left[ \bar{\psi}^i(b^\mu) W_\square(b^\mu, 0) \frac{\Gamma}{2} \psi^i(0) \right]_\tau \right| p(P, S) \right\rangle$$

- Dirac structures  $\Gamma \in \{ \gamma^+, \gamma^+ \gamma_5, i\sigma^{\alpha+} \gamma_5 \}$



Boussarie et al. '23

Leading Quark TMDPDFs

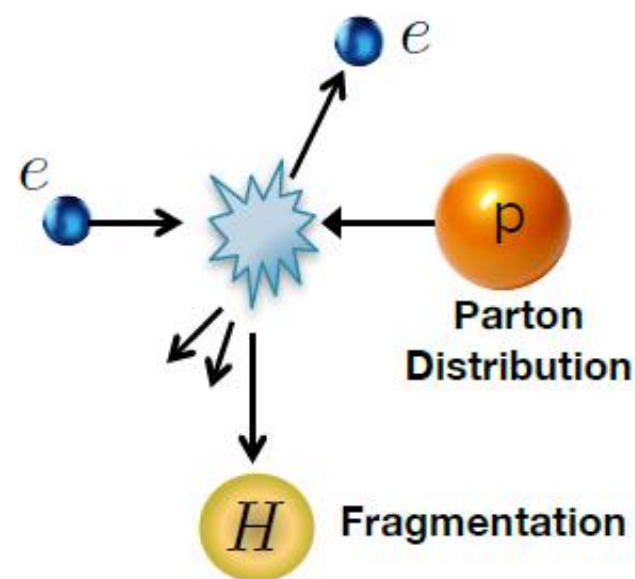
Nucleon Spin
 Quark Spin

		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \text{Unpolarized}$		$h_1^\perp = \text{Boer-Mulders}$
	L		$g_1 = \text{Helicity}$	$h_{1L}^\perp = \text{Worm-gear}$
	T	$f_{1T}^\perp = \text{Sivers}$	$g_{1T}^\perp = \text{Worm-gear}$	$h_1 = \text{Transversity}$ $h_{1T}^\perp = \text{Pretzelosity}$

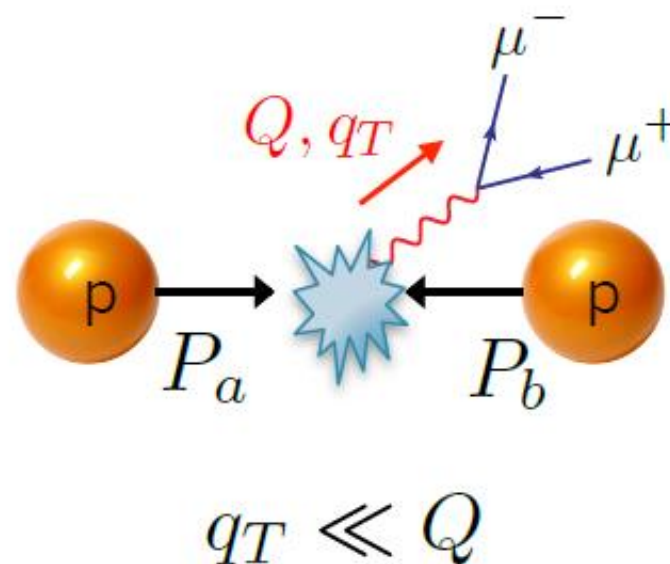
# Transverse momentum distributions of quarks

- Three classical processes used to probe quark TMDs:

## Semi-Inclusive DIS

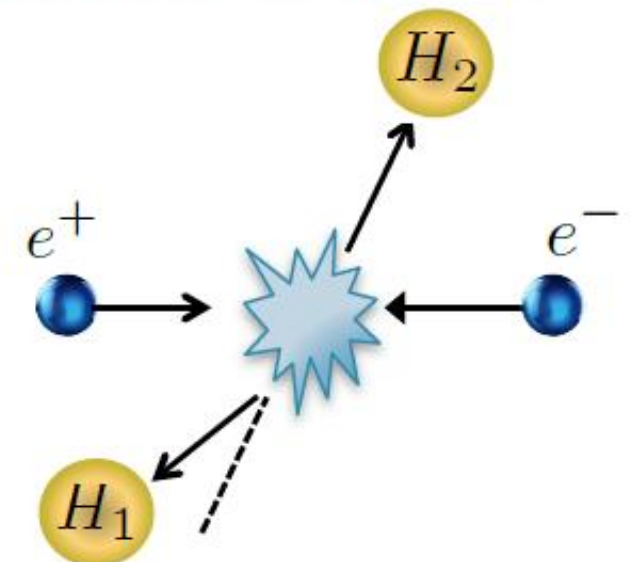


## Drell-Yan



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## Dihadron in $e^+e^-$



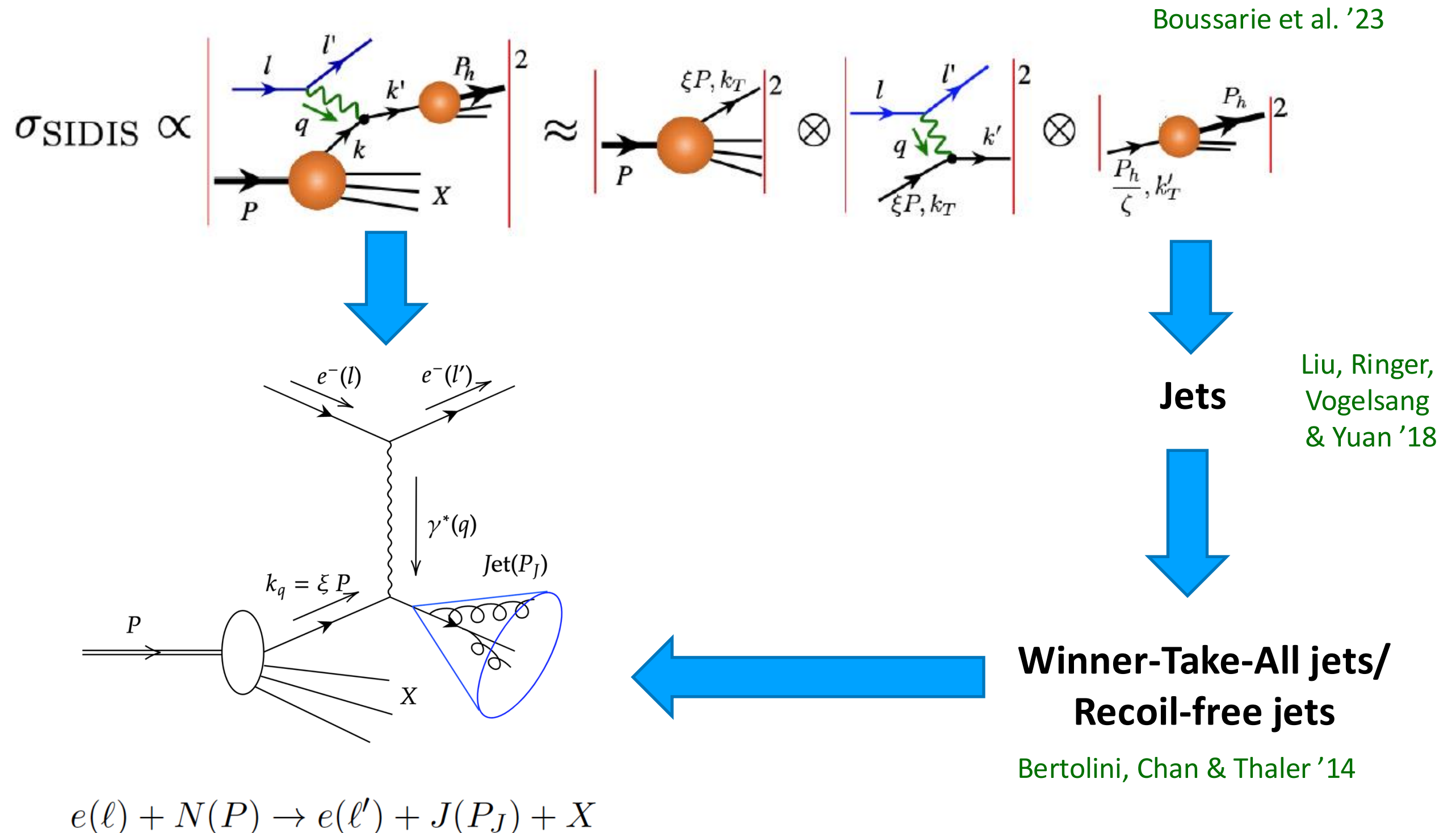
- Typical multi-scale problems
- Theory tools: TMD factorization

Collins, Soper & Sterman 1985  
Florian & Grazzini '01

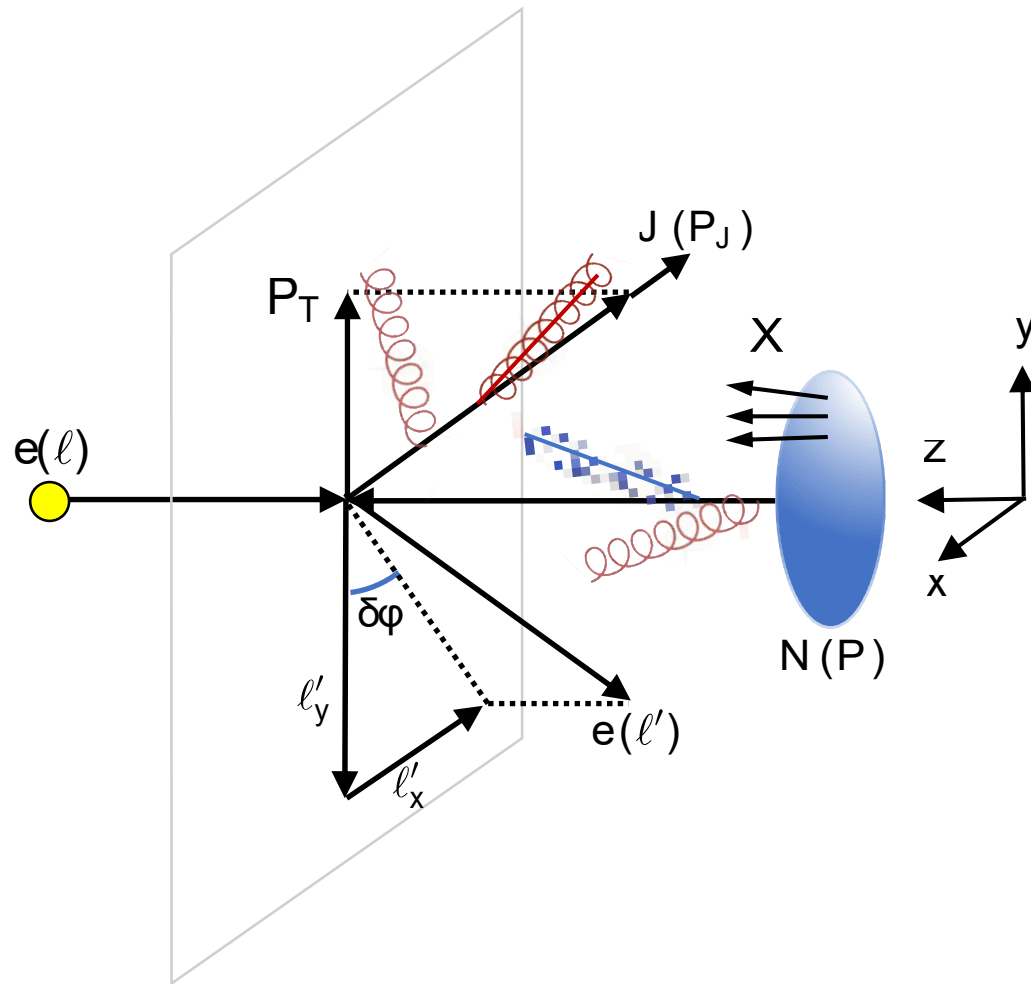


# Semi-inclusive deep inelastic scattering

Factorized SIDIS cross section in the parton model:



# QCD factorization



$$e(\ell) + N(P) \rightarrow e(\ell') + J(P_J) + X$$

- **Factorization formula :**

$$\frac{d\sigma}{d^2\ell'_T dy dq_x} = \frac{\sigma_0}{1-y} H(Q, \mu) \mathcal{C}[B \mathcal{J} S] ,$$

$$\mathcal{C}[B \mathcal{J} S] = \sum_q e_q^2 \int \frac{db}{2\pi} \cos(b q_x) B_{q/N}(x_B, b, \mu, \zeta_B/\nu^2)$$

$$\mathcal{J}_q(b, \mu, \zeta_{\mathcal{J}}/\nu^2) S(b, n \cdot n_J, \mu, \nu) .$$

- **EFT modes :**

$$\text{hard} : p_h^\mu \sim \ell'_T(1, 1, 1),$$

$$n\text{-collinear} : p_c^\mu \sim \ell'_T(\delta\phi^2, 1, \delta\phi),$$

$$\text{soft} : p_s^\mu \sim \ell'_T(\delta\phi, \delta\phi, \delta\phi),$$

$$n_J\text{-collinear} : p_J^\mu \sim \ell'_T(\delta\phi^2, 1, \delta\phi)_J ,$$

- **Observables:**

$$y = 1 - P \cdot \ell' / P \cdot l \quad q_x = \ell'_T \delta\phi$$

- **EFT parameters:**

$$\delta\phi \ll 1$$

# RG evolution

## Hierarchy Problem:

$$\mu_b = \frac{2e^{-\gamma_E}}{b} \ll Q \quad L = \ln \frac{Q^2}{\mu_b^2} \gg 1$$

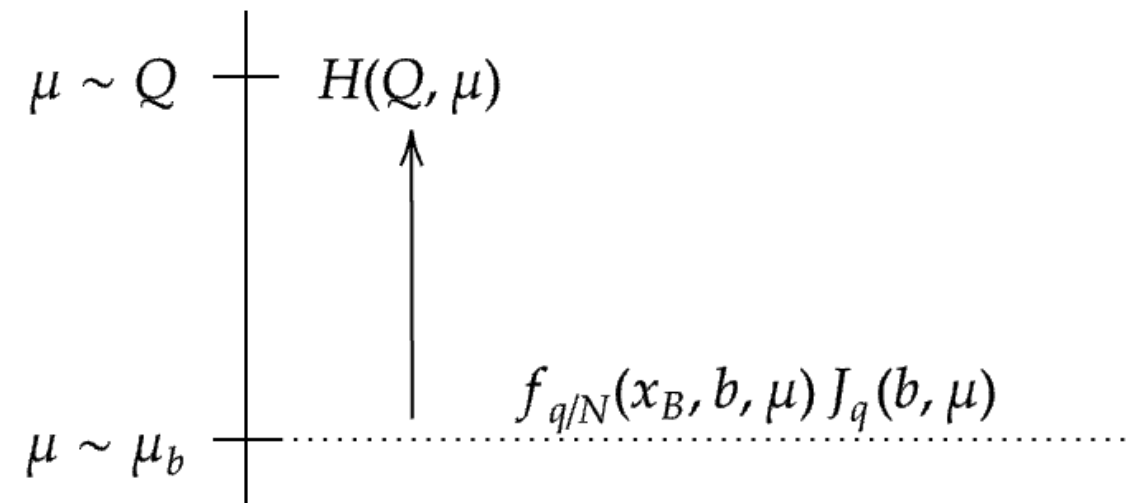
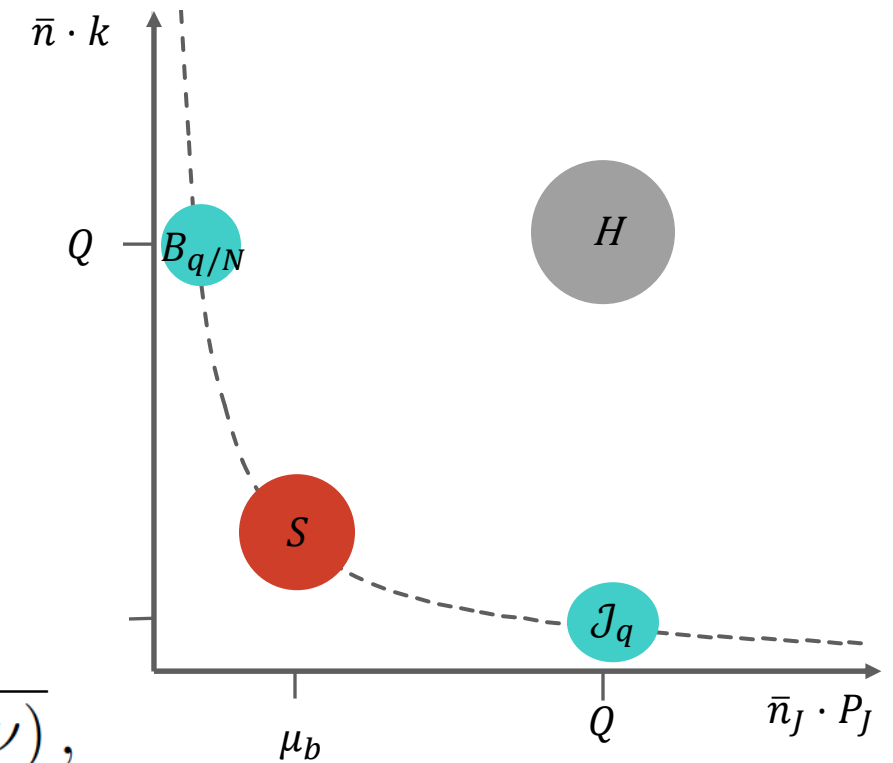
## Standard CSS formalism: Collins '13

$$f_{q/N}(x_B, b, \mu, \zeta_f) = B_{q/N}(x_B, b, \mu, \zeta_B/\nu^2) \sqrt{S_{n\bar{n}}(b, \mu, \nu)},$$

$$J_q(b, \mu, \zeta_J) = \mathcal{J}_q(b, \mu, \zeta_J/\nu^2) \frac{S(b, n \cdot n_J, \mu, \nu)}{\sqrt{S_{n\bar{n}}(b, \mu, \nu)}},$$

## Scale independence:

$$\frac{d}{d \ln \mu} \ln \sigma_{\text{phsy}}(Q, \mu_b, \mu) = 0$$



# Predictions in e-A

SF, Ke, Shao, Terry '23

## non-perturbative model

$$U_{\text{NP}}^f(x, b, A, Q_0, Q) = \exp \left[ -g_1^A b^2 - \frac{g_2}{2} \ln \frac{Q}{Q_0} \ln \frac{b}{b_*} \right],$$

Sun, Isaacson, Yuan & Yuan '14

## We apply modified nuclear TMD PDFs

$$g_1^A = g_1^f + a_N(A^{1/3} - 1) \quad a_N = 0.016 \pm 0.003 \text{ GeV}^2$$

## Collinear dynamics using EPPS16

Alrashed, Anderle, Kang, Terry & Xing '22

## We include LO momentum broadening of the jet within SCET<sub>G</sub>

$$J_q^A(b, \mu, \zeta_J) = J_q(b, \mu, \zeta_J) e^{\chi[\xi b K_1(\xi b) - 1]}$$

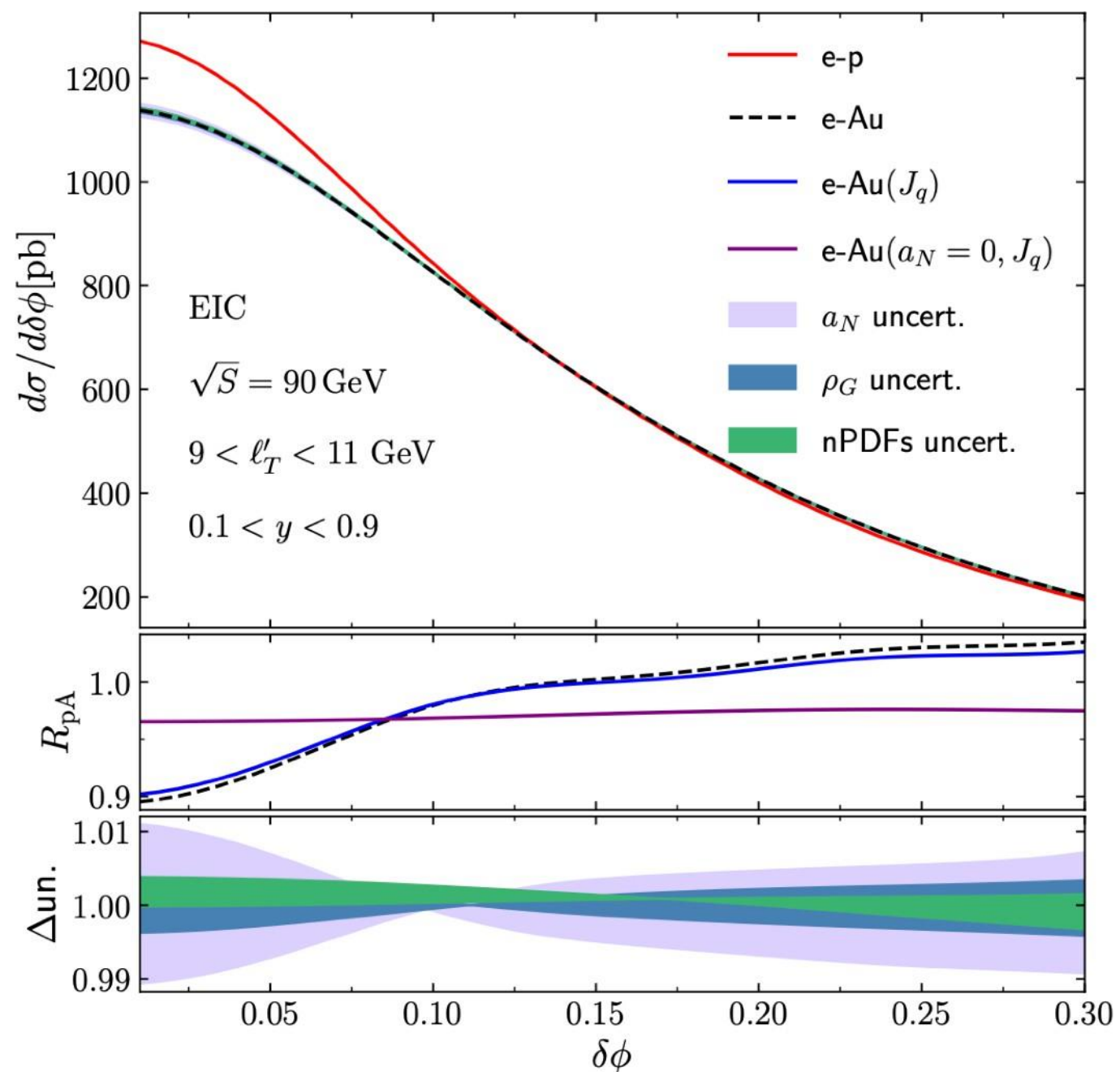
Opacity parameter  $\chi = \frac{\rho_G L}{\xi^2} \alpha_s(\mu_{b_*}) C_F$

Gyulassy, Levai & Vitev '02

$\rho_G$  : density of the medium

$\xi$  : the screening mass

$L$  : the length of the medium

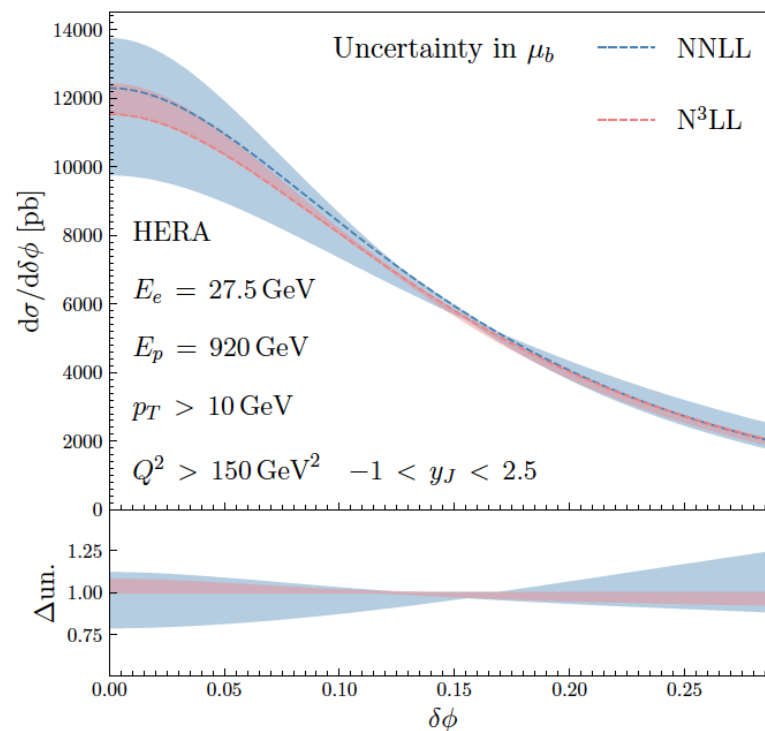
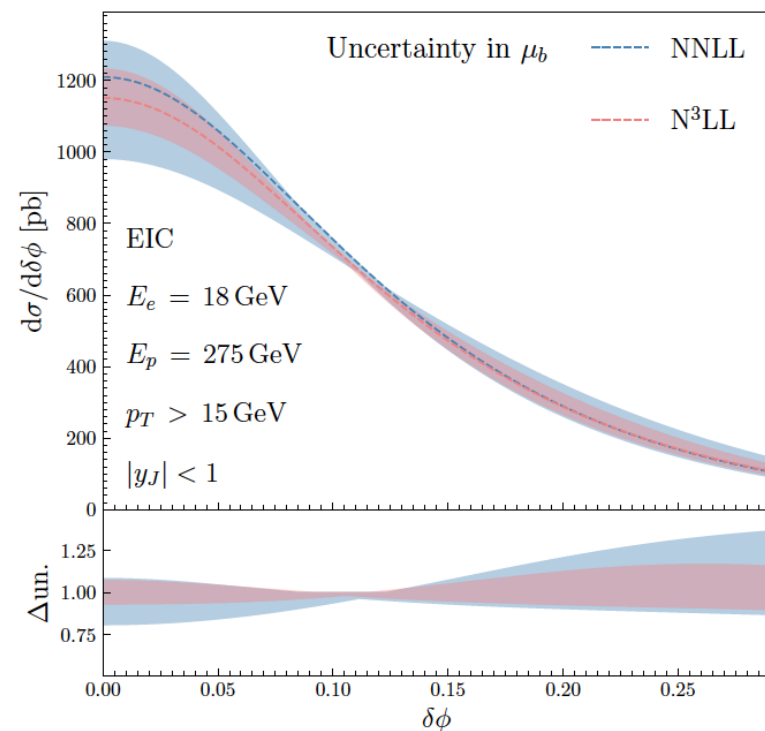
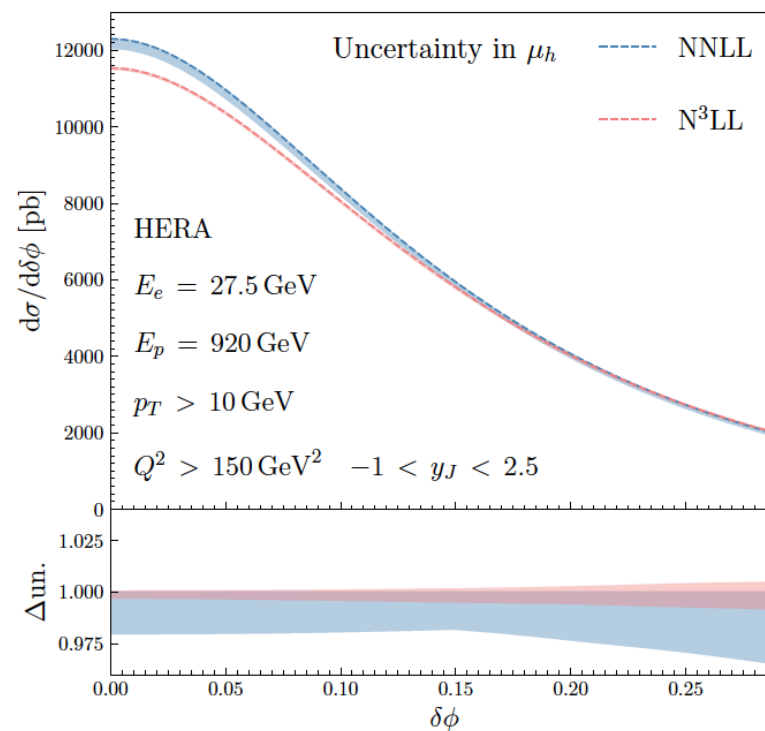
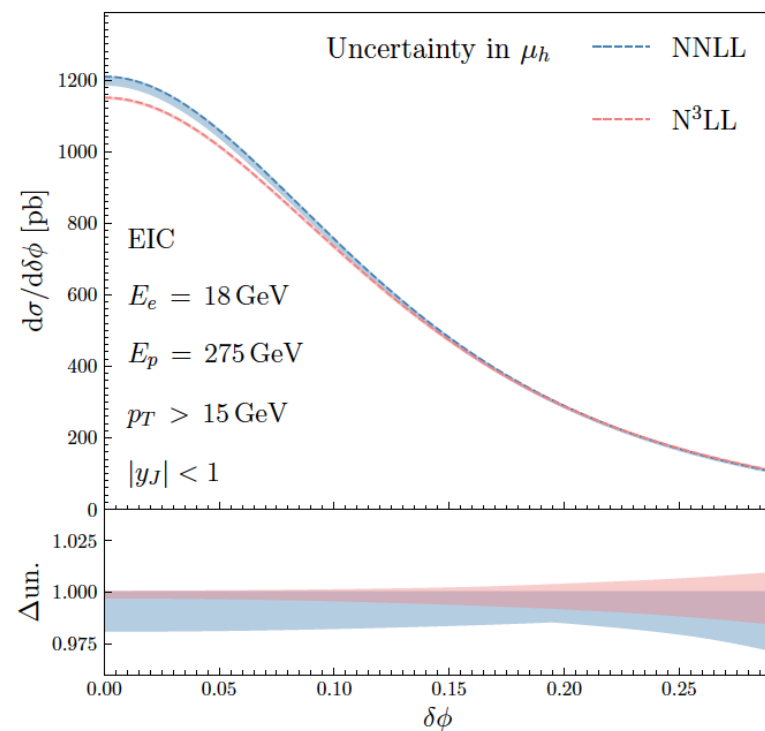


The process is primarily sensitive to the initial state's broadening effects, thereby serving as a clean probe of nTMD PDFs.



# Comparison of resummation results at NNLL and N<sup>3</sup>LL

SF, Gao, Li, Shao 24'



- The uncertainty bands are narrower at N<sup>3</sup>LL (red) compared to NNLL (blue)

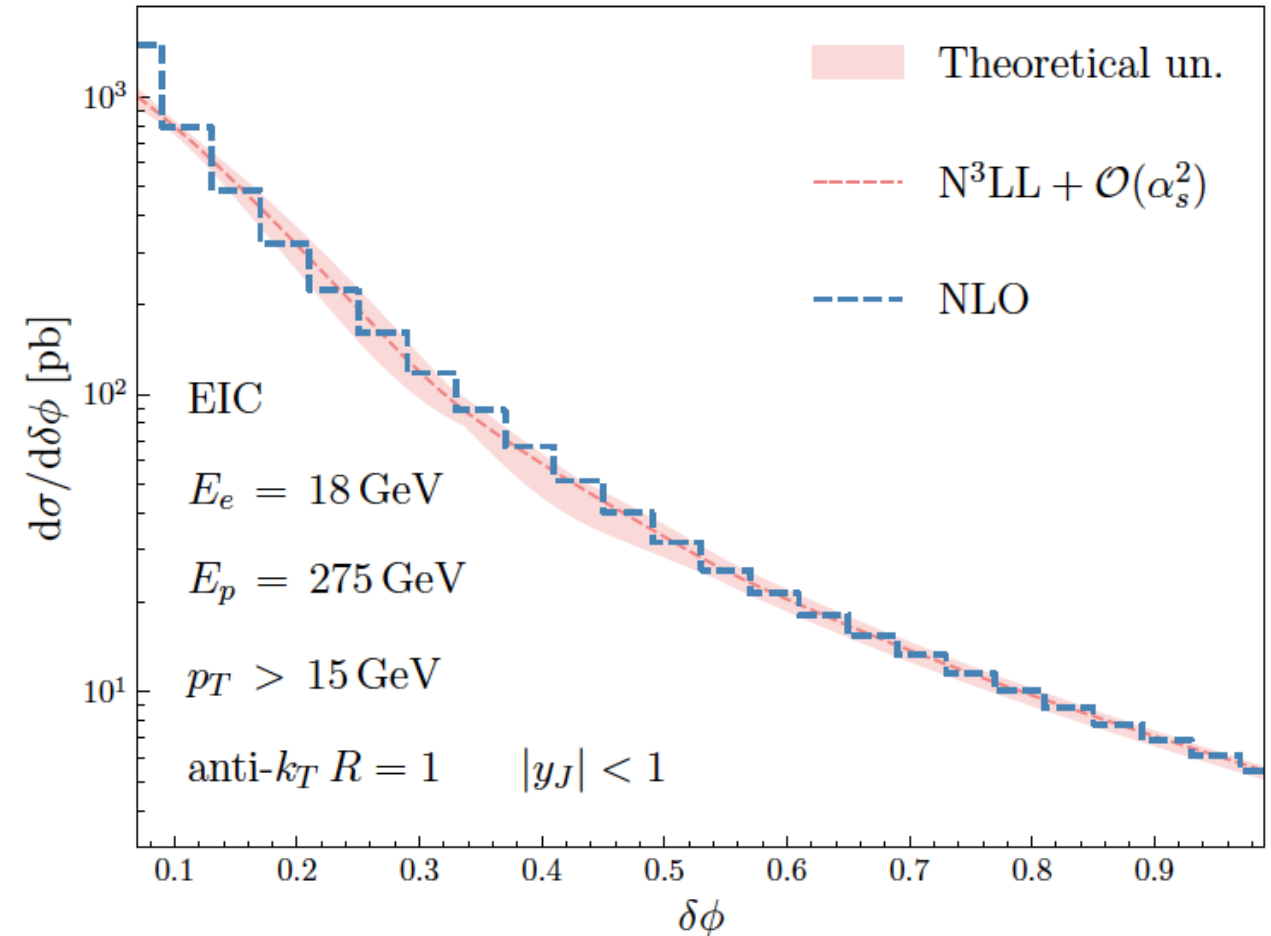
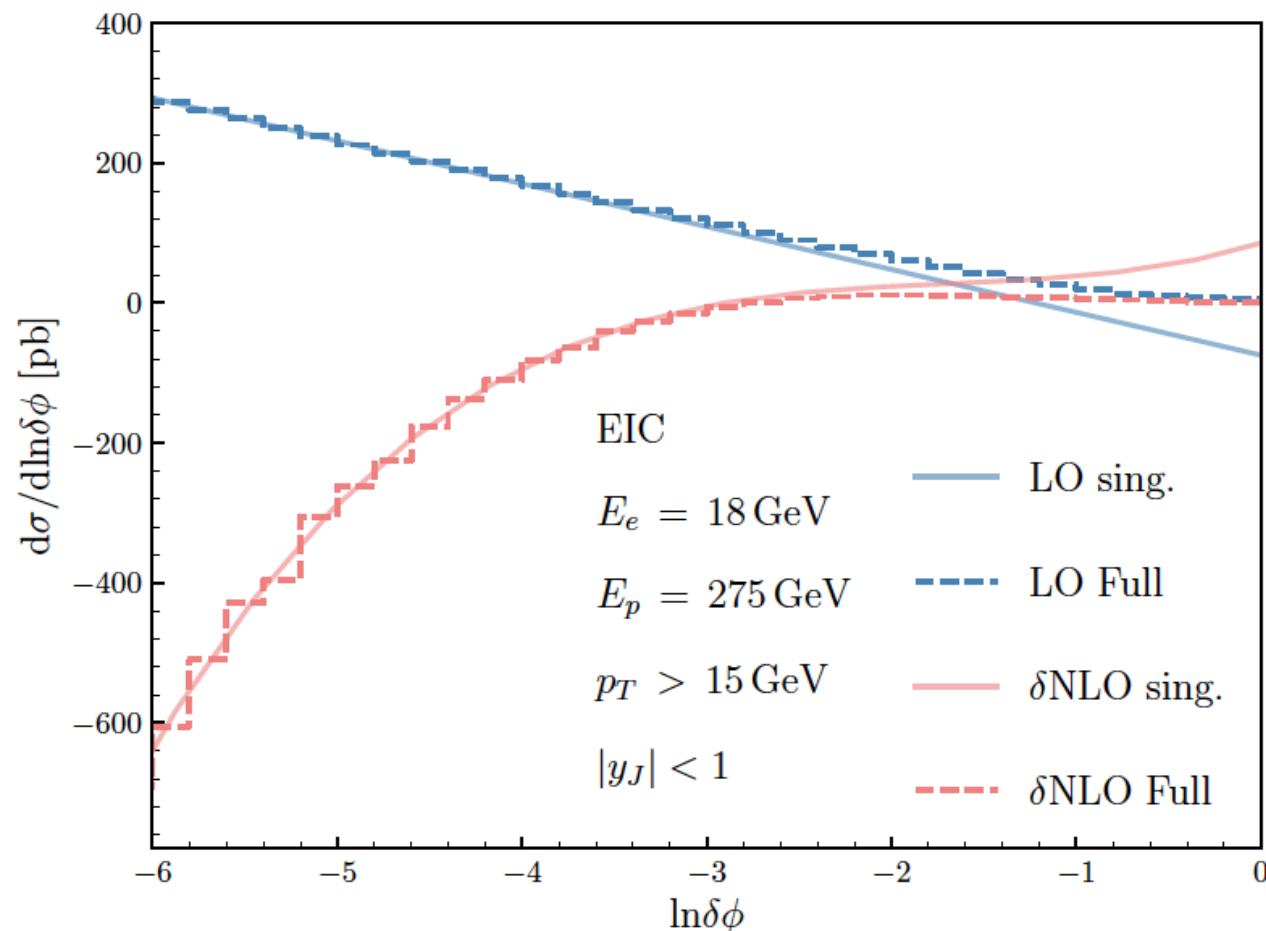
- At N<sup>3</sup>LL the dominant scale uncertainties are from  $\mu_b$  variation

# $N^3\text{LL} + \mathcal{O}(\alpha_s^2)$ predictions on lepton-jet azimuthal correlation

SF, Gao, Li, Shao '24

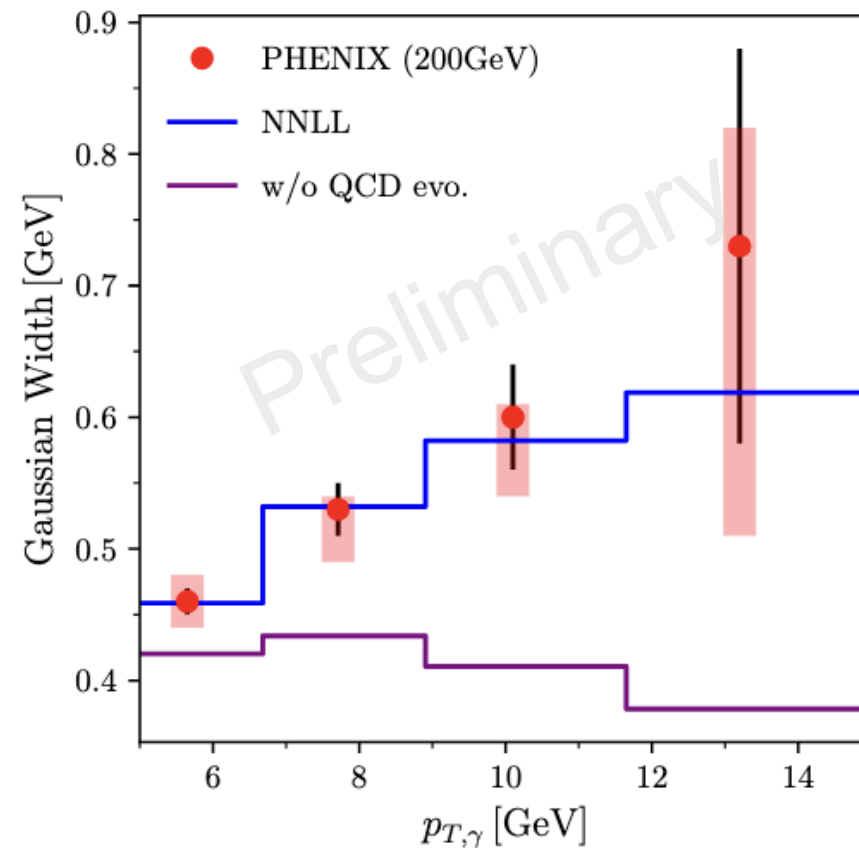
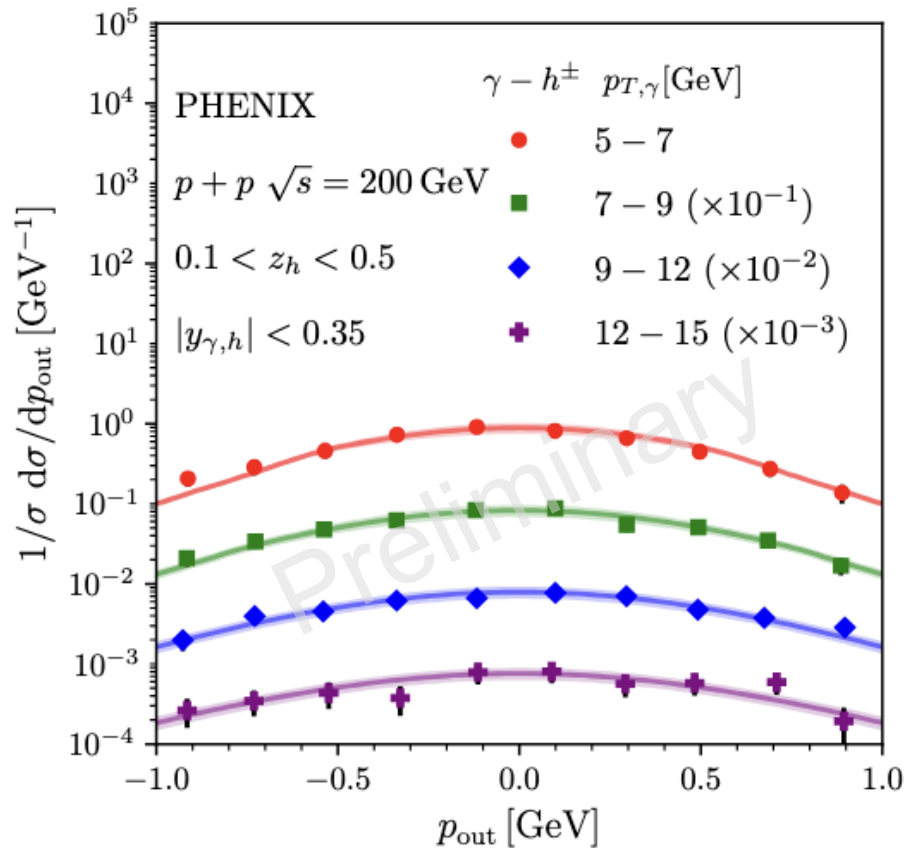
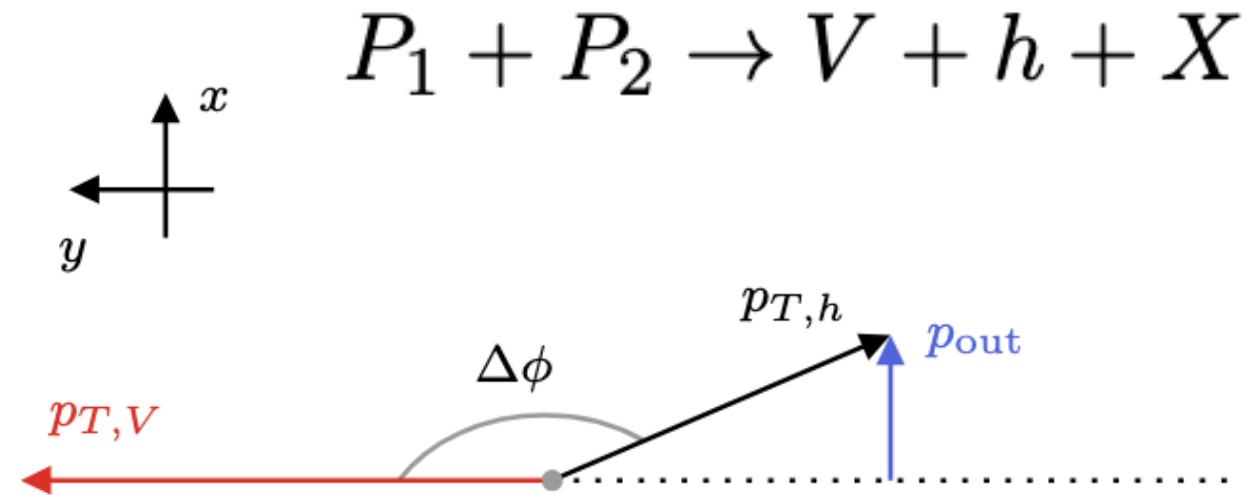
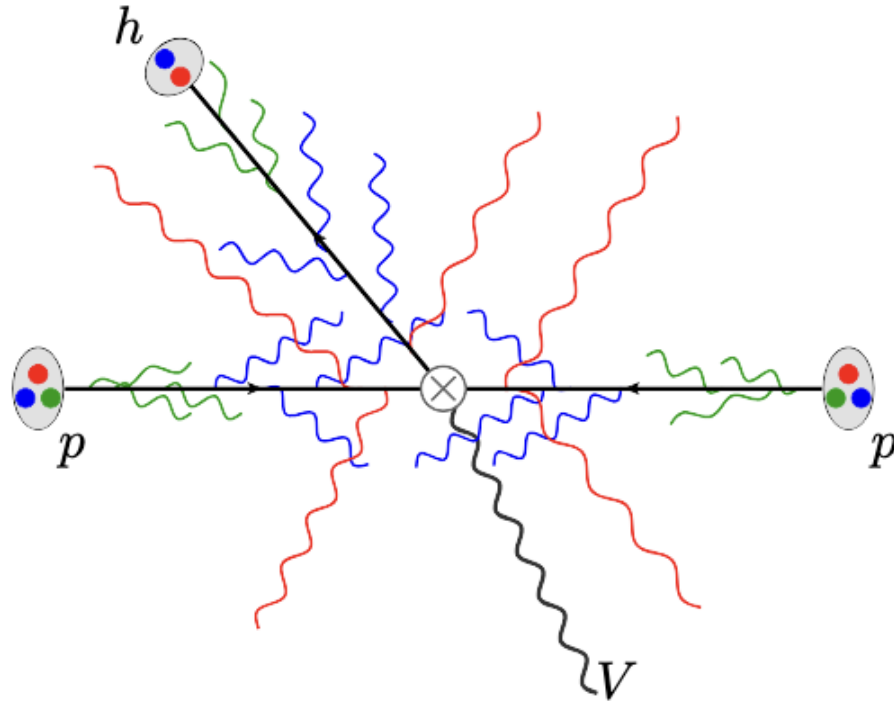
- In the back-to-back limit ( $\delta\phi \rightarrow 0$ ) the singular contributions in DIS are consistent with the fixed-order results from NLOJET++ up to  $\mathcal{O}(\alpha_s^2)$
- In the large  $\delta\phi$  region the resummation formula receives significant matching corrections
- It is necessary to switch off the resummation and instead employ fixed-order calculations

$$d\sigma_{\text{add}}(NNNLL + \mathcal{O}(\alpha_s^2)) \equiv d\sigma(NNNLL) + \underbrace{d\sigma(\text{NLO}) - d\sigma(\text{NLO singular})}_{d\sigma(\text{NLO non-singular})}$$



# NNLL predictions on photon-hadron azimuthal correlation

SF, Gao, Kang, Shao 2510.XXXXX



- The Gaussian widths (blue) are consistent with PHENIX results (red)
- Perturbative evolution also contributes to the Gaussian widths

# Summary

- We have studied on the lepton-jet correlation in both e-p and e-A collisions. Utilizing SCET, we derived a factorization theorem for back-to-back lepton-jet configurations.
- In e-A collisions, we discussed the utility of our approach in disentangling intrinsic non-perturbative contributions from nTMDs and dynamical medium effects in nuclear environments. We find the process is primarily sensitive to the initial state's broadening effects.
- TMD resummation accuracy has been improved to  $N^3\text{LL} + \mathcal{O}(\alpha_s^2)$  accuracy in e-p collisions. It is good to have the measurement at the HERA to make a comparison.
- In pp collisions, we find perturbative QCD dynamics contribute substantially to the TMD broadening effects.
- Our work sets the groundwork for spin-independent TMD effects in e-A and p-p collisions, offering a robust framework for measuring nTMDs.

# Thank you