

Global Spin Alignment of ^4Li in Heavy-Ion Collisions

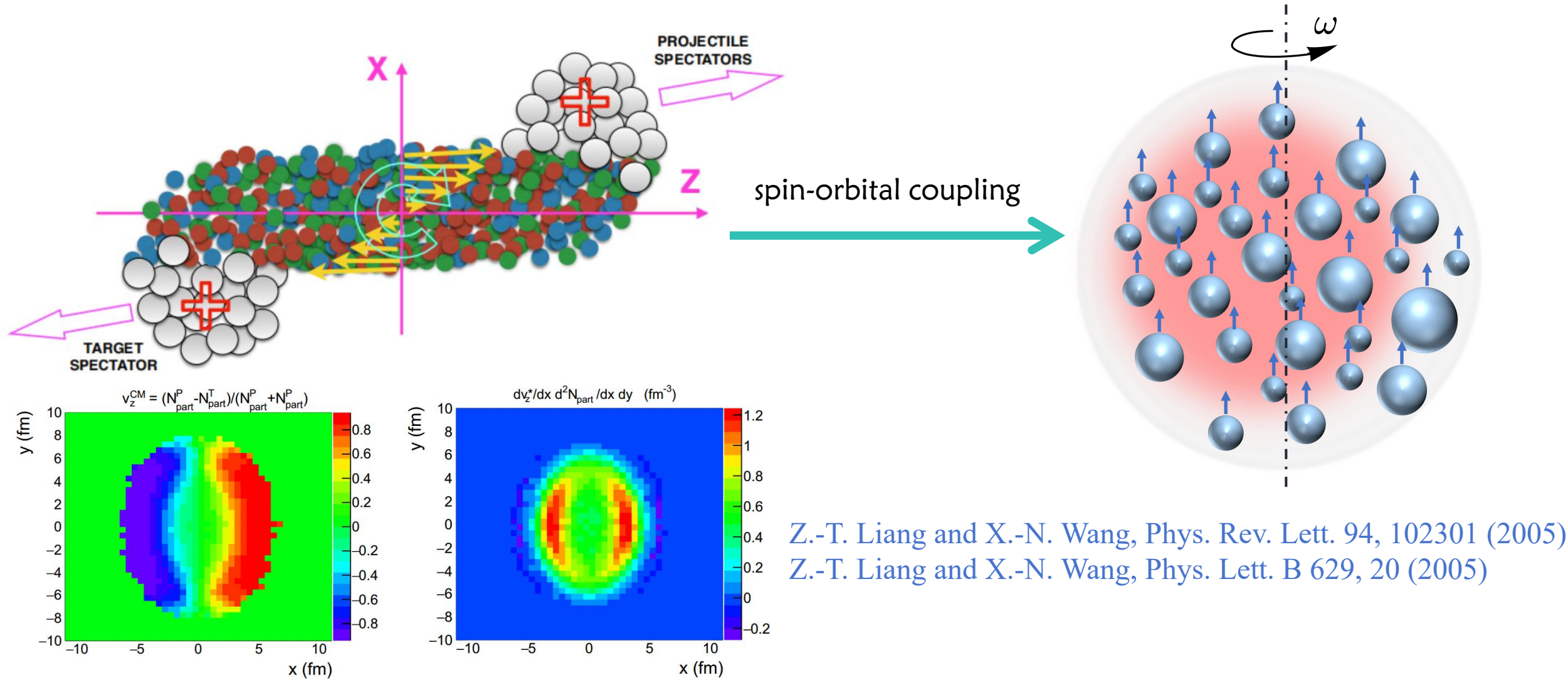
Yunpeng Zheng
Fudan university

In Collaborated with Dai-Neng Liu, Lie-Wen Chen,
Jin-Hui Chen, Che Ming Ko, Yu-Gang Ma, Kai-Jia
Sun, Jun Xu and Bo Zhou

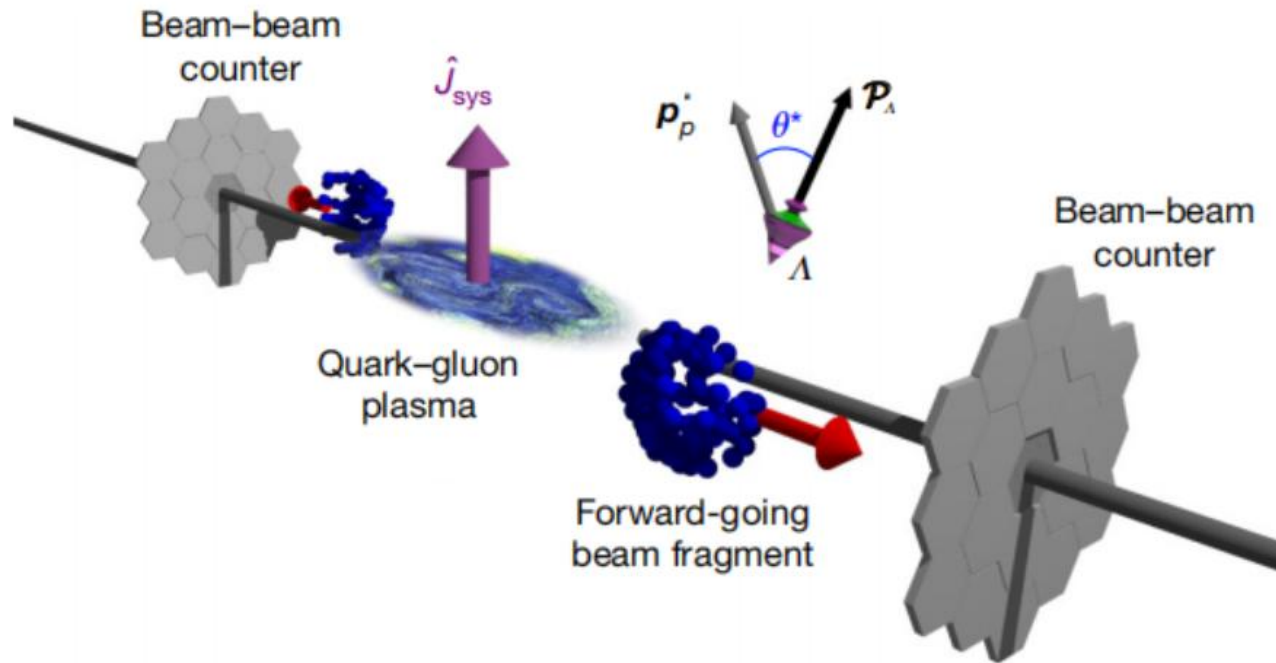


Qingdao, September. 24, 2025



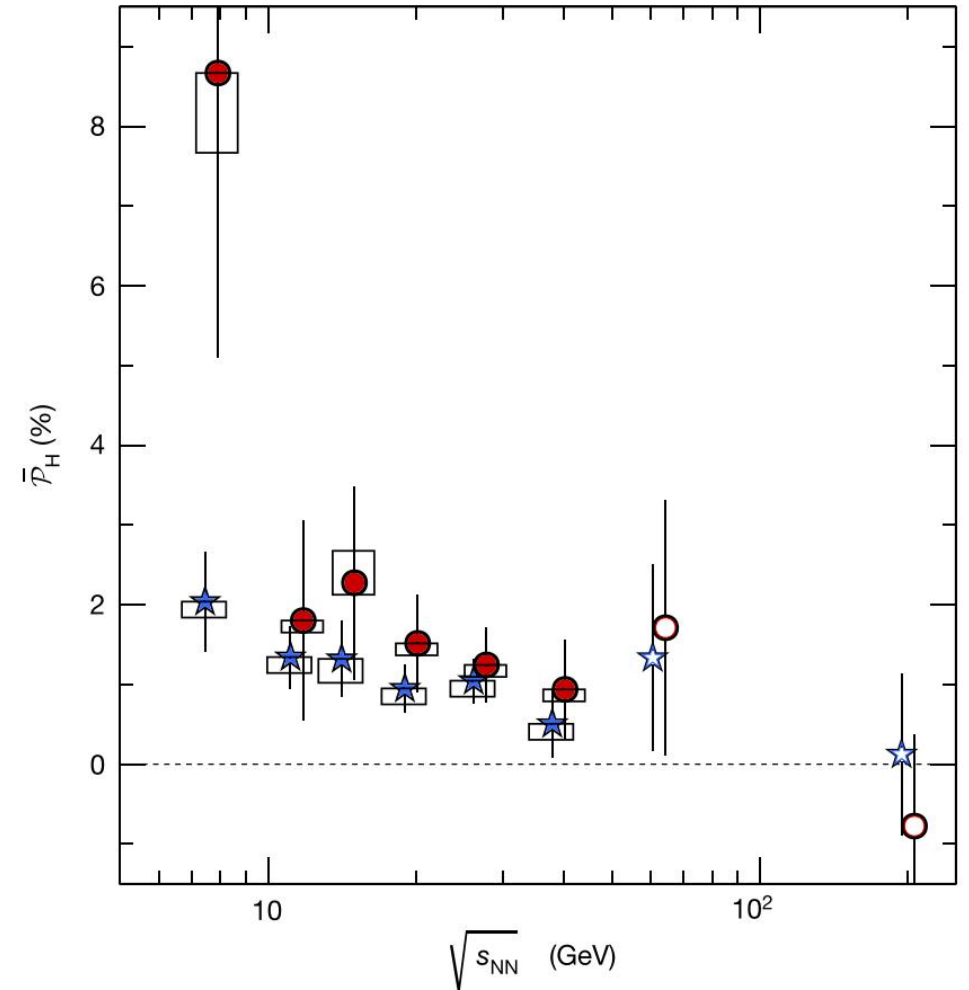


Z.-T. Liang and X.-N. Wang, Phys. Rev. Lett. 94, 102301 (2005)
 Z.-T. Liang and X.-N. Wang, Phys. Lett. B 629, 20 (2005)

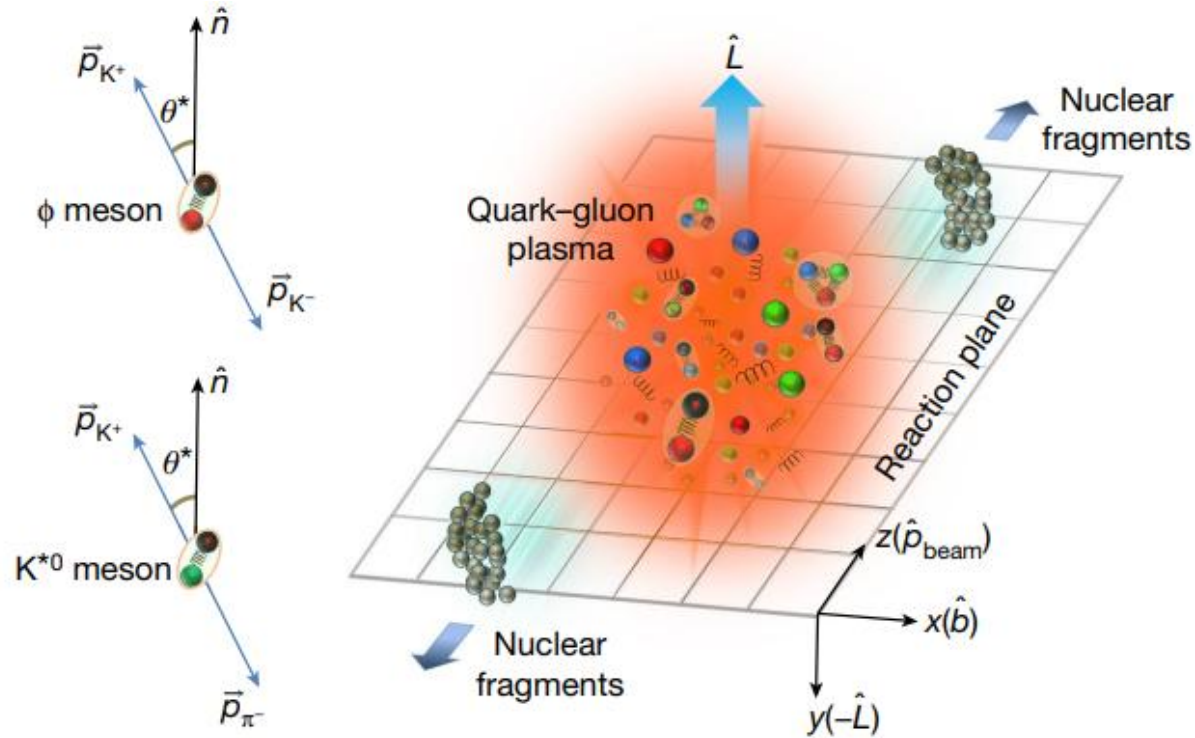


$$\Lambda \rightarrow p + \pi^-$$

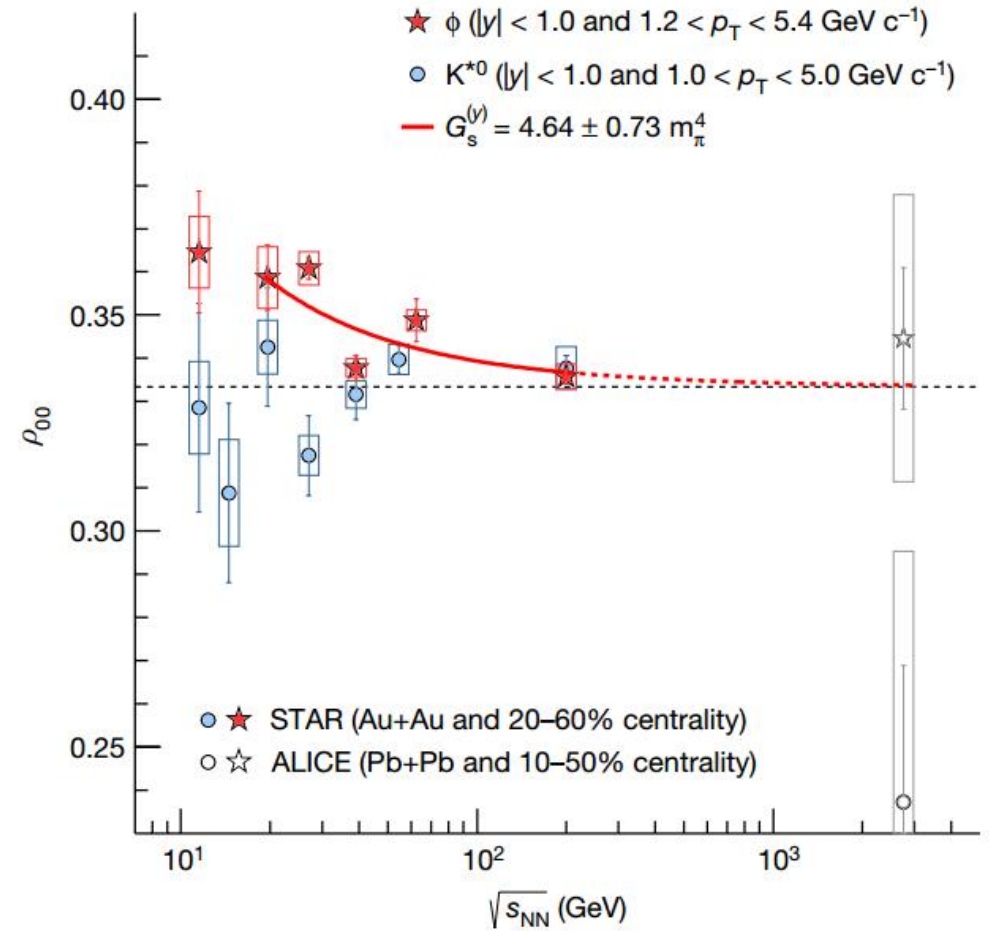
$$\frac{dN}{d\Omega} = \frac{1}{4\pi} (1 + \alpha_\Lambda |P_\Lambda| \cos \theta^*)$$

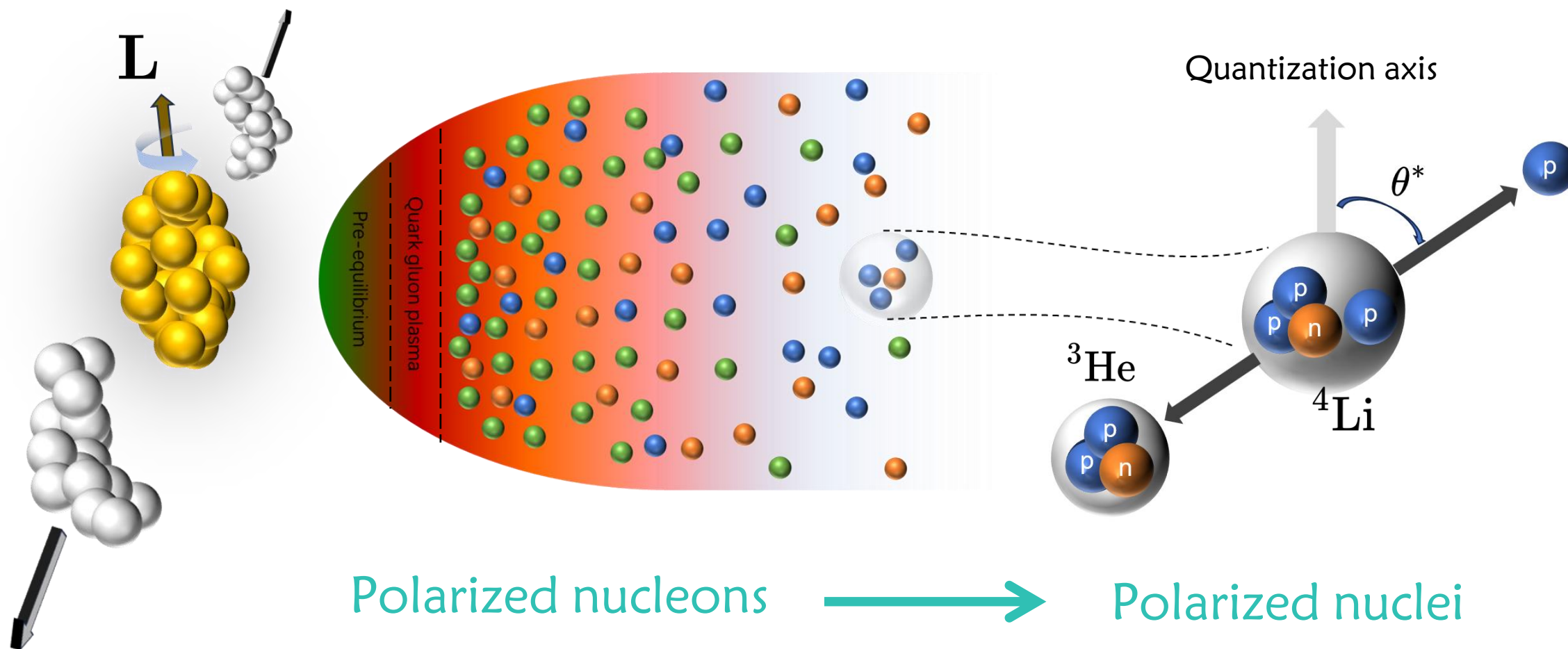


L. Adamczyk et al. (STAR), Nature 548, 62 (2017)



$$\frac{dN}{d(\cos\theta^*)} \propto (1 - \rho_{00}) + (3\rho_{00} - 1)\cos^2\theta^*$$

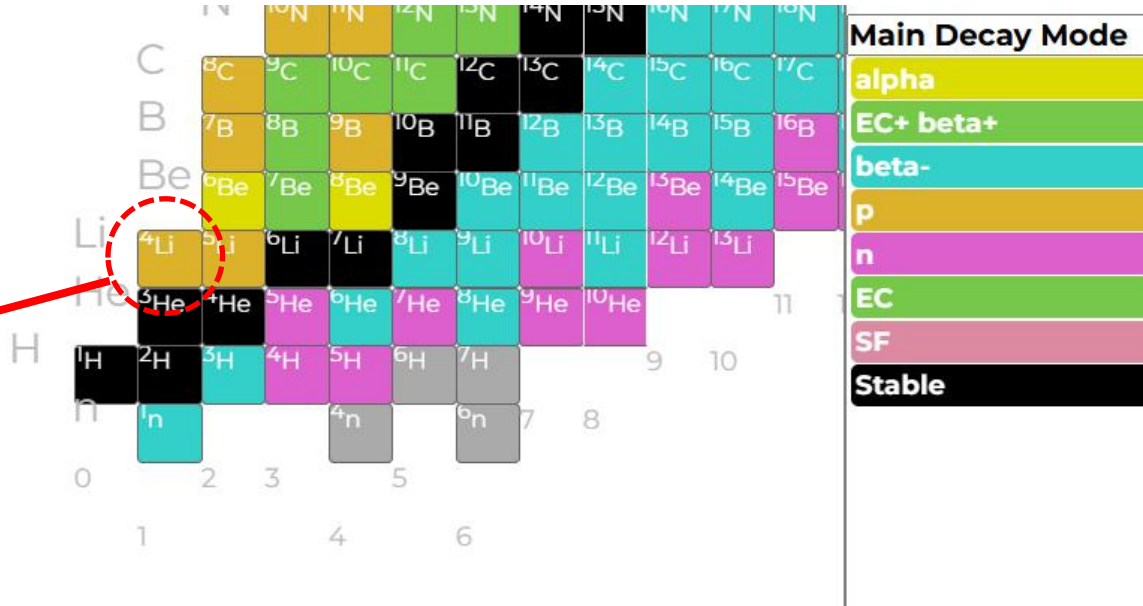
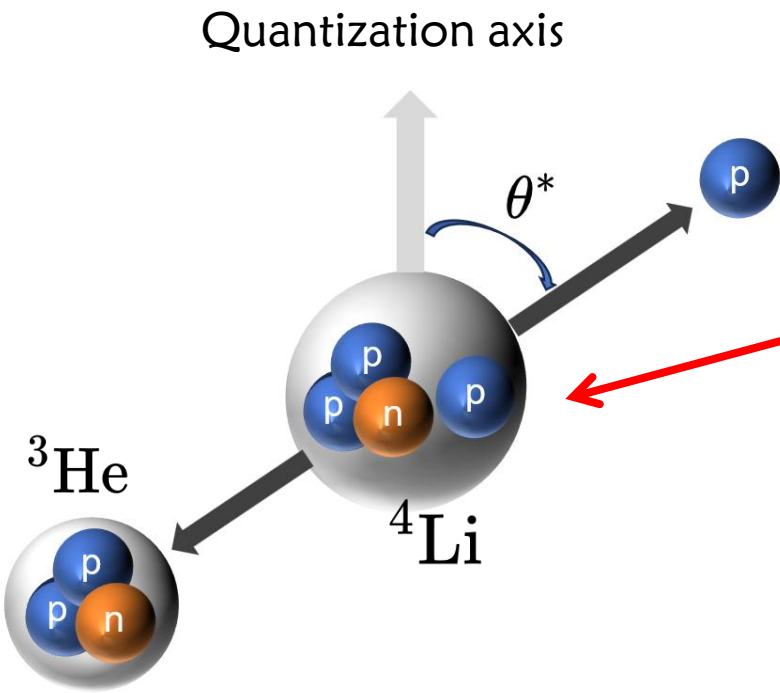




R.-J. Liu and J. Xu, Phys. Rev. C 109, 014615 (2024)

Kai-Jia Sun et al., Phys. Rev. Lett. 134, 022301 (2025)

Yun-Peng Zheng et al., arXiv:2509.15286 (2025)



Decay angular distribution :

$$\frac{dN}{d\Omega^*} = \frac{\text{Tr}[\hat{T}^\dagger \hat{\rho} \hat{T}]}{\int d\Omega^* \text{Tr}[\hat{T}^\dagger \hat{\rho} \hat{T}]} \longleftrightarrow \frac{dN}{\sin \theta^* d\theta^*} = 2\pi \frac{\text{Tr}[\hat{T}^\dagger \hat{\rho} \hat{T}]}{\int d\Omega^* \text{Tr}[\hat{T}^\dagger \hat{\rho} \hat{T}]}$$

$A = 4$	$E_x \text{ (MeV)}$	J^π	Decay channels
^4Li	g.s.	2^-	p(100%)
	0.32	1^-	p(100%)
	2.08	0^-	p(100%)
	2.85	1^-	p(100%)

T_{ij} : initial spin state i $\longrightarrow$ final spin state j

V. Vovchenko, B. D’onigus, B. Kardan, M. Lorenz, and H. Stoecker, Phys. Lett. B, 135746 (2020)

Productions of the ground states with different J_z

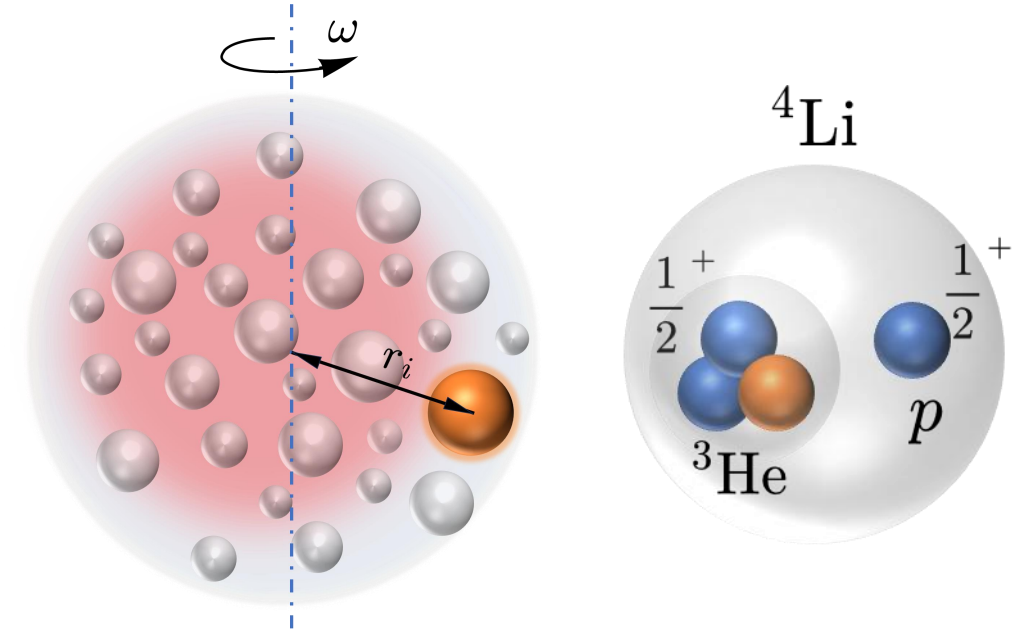
$$E \frac{d^3 N_{^4\text{Li}, J_z=m}}{d\mathbf{K}^3} = E \int \left[\prod_{i=1,2,3,4} k_i^\mu d^3 \sigma_\mu \frac{d^3 k_i}{E_i} \bar{f}_i(\mathbf{x}_i, \mathbf{k}_i) \right] \\ \times \text{Tr}_s[\hat{W}(\mathbf{r}'_1, \mathbf{k}'_1, \mathbf{r}'_2, \mathbf{k}'_2, \mathbf{r}'_3, \mathbf{k}'_3; J_z = m) \\ \times \hat{\sigma}_{p_1 p_2 p_3 n}] \times \delta(\mathbf{K} - \sum_i \mathbf{k}_i).$$

$$W_{\tilde{m}_1 \tilde{m}_2 \tilde{m}_3 \tilde{m}_4}^{m_1 m_2 m_3 m_4} = \int d\eta'_1 d\eta'_2 d\eta'_3 e^{-i(\eta'_1 \mathbf{k}'_1 + \eta'_2 \mathbf{k}'_2 + \eta'_3 \mathbf{k}'_3)} \\ \times \left\langle \mathbf{r}'_1 + \frac{\eta'_1}{2}, \mathbf{r}'_2 + \frac{\eta'_2}{2}, \mathbf{r}'_3 + \frac{\eta'_3}{2}; \tilde{m}_1 \dots \tilde{m}_4 | 2, m \right\rangle_{\text{rel}} \\ \times \left\langle 2, m | \mathbf{r}'_1 - \frac{\eta'_1}{2}, \mathbf{r}'_2 - \frac{\eta'_2}{2}, \mathbf{r}'_3 - \frac{\eta'_3}{2}; m_1 \dots m_4 \right\rangle_{\text{rel}}.$$

(without hadron spin correlation)

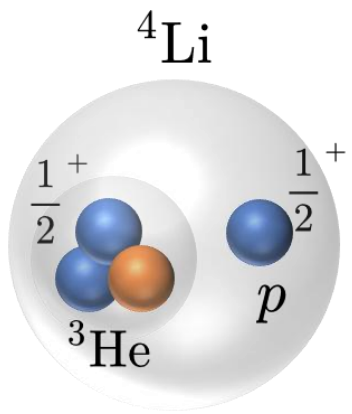
$$\hat{\sigma}_{p_1 p_2 p_3 n} = \hat{\sigma}_{p_1} \otimes \hat{\sigma}_{p_2} \otimes \hat{\sigma}_{p_3} \otimes \hat{\sigma}_n$$

$$\hat{\sigma}_j = \text{diag}\left[\frac{1 + \mathcal{P}_j}{2}, \frac{1 - \mathcal{P}_j}{2}\right]$$



Single particle distribution in a vortical fluid

$$f(\mathbf{r}_i, \mathbf{k}_i) = \frac{2\xi_i}{(2\pi)^3} e^{-\frac{(\mathbf{k}_i - m\omega \times \mathbf{r}_i)^2}{2mT}}$$



Wavefunctions of ${}^4\text{Li}$ ground state in shell model 7

$$V = \frac{1}{2}m_1\omega^2 r_1^2 + \frac{1}{2}m_2\omega^2 r_2^2 + \frac{1}{2}m_3\omega^2 r_3^2 + \frac{1}{2}m_4\omega^2 r_4^2$$

$$= \frac{1}{2}M\omega^2 R^2 + \frac{1}{2}\mu_1\omega^2 r_1'^2 + \frac{1}{2}\mu_2\omega^2 r_2'^2 + \frac{1}{2}\mu_3\omega^2 r_3'^2$$

One dimension harmonic oscillator wavefunction

$$\phi_0 = \frac{1}{\sqrt{b\sqrt{\pi}}} \exp\left[-\frac{x^2}{2b^2}\right]$$

$$\phi_1 = \sqrt{\frac{2}{b\sqrt{\pi}}} \frac{x}{b} \exp\left[-\frac{x^2}{2b^2}\right]$$

Construct three dimension harmonic oscillator wavefunction

$$\phi_{M=1}^{L=1}(\mathbf{r}) = \frac{1}{\sqrt{2}}[\phi_1(x)\phi_0(y) + i\phi_0(x)\phi_1(y)]\phi_0(z)$$

$$\phi_{M=-1}^{L=1}(\mathbf{r}) = \phi_{M=1}^{L=1}(\mathbf{r})^*$$

$$\phi_{M=0}^{L=1}(\mathbf{r}) = \phi_0(x)\phi_0(y)\phi_1(z)$$

$$\langle \mathbf{r}_1, \dots, \mathbf{r}_4 | 2, 2 \rangle = \sqrt{\frac{1}{3!}} \begin{bmatrix} \phi_{M=1}^{L=1}(\mathbf{r}_1) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_1} & \phi_{M=1}^{L=1}(\mathbf{r}_2) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_2} & \phi_{M=1}^{L=1}(\mathbf{r}_3) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_3} \\ \phi_{M=0}^{L=0}(\mathbf{r}_1) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_1} & \phi_{M=0}^{L=0}(\mathbf{r}_2) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_2} & \phi_{M=0}^{L=0}(\mathbf{r}_3) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_3} \\ \phi_{M=0}^{L=0}(\mathbf{r}_1) \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_1} & \phi_{M=0}^{L=0}(\mathbf{r}_2) \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_2} & \phi_{M=0}^{L=0}(\mathbf{r}_3) \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_3} \end{bmatrix} \phi_{M=0}^{L=0}(\mathbf{r}_4) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_n$$

$$= \sqrt{\frac{1}{6}} (\phi_{M=1}^{L=1}(\mathbf{r}_1) \phi_{M=0}^{L=0}(\mathbf{r}_2) \phi_{M=0}^{L=0}(\mathbf{r}_3) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_1} \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_2} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_3}$$

$$- \phi_{M=1}^{L=1}(\mathbf{r}_1) \phi_{M=0}^{L=0}(\mathbf{r}_2) \phi_{M=0}^{L=0}(\mathbf{r}_3) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_1} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_2} \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_3}$$

$$+ \phi_{M=1}^{L=1}(\mathbf{r}_3) \phi_{M=0}^{L=0}(\mathbf{r}_1) \phi_{M=0}^{L=0}(\mathbf{r}_2) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_3} \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_1} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_2}$$

$$- \phi_{M=1}^{L=1}(\mathbf{r}_2) \phi_{M=0}^{L=0}(\mathbf{r}_1) \phi_{M=0}^{L=0}(\mathbf{r}_3) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_2} \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_1} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_3}$$

$$- \phi_{M=1}^{L=1}(\mathbf{r}_3) \phi_{M=0}^{L=0}(\mathbf{r}_2) \phi_{M=0}^{L=0}(\mathbf{r}_1) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_3} \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_2} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_1}$$

$$+ \phi_{M=1}^{L=1}(\mathbf{r}_2) \phi_{M=0}^{L=0}(\mathbf{r}_3) \phi_{M=0}^{L=0}(\mathbf{r}_1) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_2} \left| \frac{1}{2}, \frac{1}{2} \right\rangle_{p_3} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle_{p_1}) \phi_{M=0}^{L=0}(\mathbf{r}_n) \left| \frac{1}{2}, \frac{1}{2} \right\rangle_n$$

Productions of the ground states with different J_z

$$N_{{}^4\text{Li}, J_z=2} \approx 8 \frac{N_p^3 N_n}{V^3} \left(\frac{2\pi}{mT} \right)^{\frac{9}{2}} \frac{(1 + \mathcal{P}_N)^3 (1 - \mathcal{P}_N)}{16} (1 + 2\mathcal{P}_L + 2\mathcal{P}_L^2).$$

$$N_{{}^4\text{Li}, J_z=1} \approx 8 \frac{N_p^3 N_n}{V^3} \left(\frac{2\pi}{mT} \right)^{\frac{9}{2}} \left(\frac{1}{2} \frac{(1 + \mathcal{P}_N)^2 (1 - \mathcal{P}_N)^2}{16} (1 + 2\mathcal{P}_L + 2\mathcal{P}_L^2) + \frac{1}{2} \frac{(1 + \mathcal{P}_N)^3 (1 - \mathcal{P}_N)}{16} \right),$$

$$N_{{}^4\text{Li}, J_z=0} \approx 8 \frac{N_p^3 N_n}{V^3} \left(\frac{2\pi}{mT} \right)^{\frac{9}{2}} \left(\frac{1}{6} \frac{(1 + \mathcal{P}_N)^3 (1 - \mathcal{P}_N)}{16} (1 - 2\mathcal{P}_L + 2\mathcal{P}_L^2) + \frac{2}{3} \frac{(1 + \mathcal{P}_N)^2 (1 - \mathcal{P}_N)^2}{16} + \frac{1}{6} \frac{(1 + \mathcal{P}_N)(1 - \mathcal{P}_N)^3}{16} (1 + 2\mathcal{P}_L + 2\mathcal{P}_L^2) \right),$$

$$N_{{}^4\text{Li}, J_z=-1} \approx 8 \frac{N_p^3 N_n}{V^3} \left(\frac{2\pi}{mT} \right)^{\frac{9}{2}} \left(\frac{1}{2} \frac{(1 + \mathcal{P}_N)^2 (1 - \mathcal{P}_N)^2}{16} (1 - 2\mathcal{P}_L + 2\mathcal{P}_L^2) + \frac{1}{2} \frac{(1 + \mathcal{P}_N)(1 - \mathcal{P}_N)^3}{16} \right),$$

$$N_{{}^4\text{Li}, J_z=-2} \approx 8 \frac{N_p^3 N_n}{V^3} \left(\frac{2\pi}{mT} \right)^{\frac{9}{2}} \frac{(1 + \mathcal{P}_N)(1 - \mathcal{P}_N)^3}{16} (1 - 2\mathcal{P}_L + 2\mathcal{P}_L^2).$$

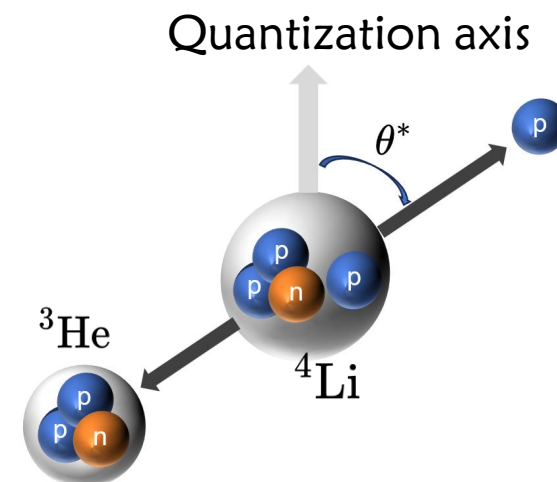
polarization of orbital motion $\mathcal{P}_L \approx \frac{\omega}{2T}$

$$\hat{\rho}({}^4\text{Li}(2^-)) = \text{diag} \left[\begin{array}{cc} \frac{3(\mathcal{P}_N + 1)^2 (2\mathcal{P}_L(\mathcal{P}_L + 1) + 1)}{4(2\mathcal{P}_N^2 + 5)\mathcal{P}_L^2 + 20\mathcal{P}_N\mathcal{P}_L + 5(\mathcal{P}_N^2 + 3)}, & \frac{3(-\mathcal{P}_L(\mathcal{P}_L + 1)\mathcal{P}_N^2 + \mathcal{P}_N + \mathcal{P}_L^2 + \mathcal{P}_L + 1)}{4(2\mathcal{P}_N^2 + 5)\mathcal{P}_L^2 + 20\mathcal{P}_N\mathcal{P}_L + 5(\mathcal{P}_N^2 + 3)}, \\ \frac{-\mathcal{P}_N^2 - 4\mathcal{P}_L\mathcal{P}_N + 2(\mathcal{P}_N^2 + 1)\mathcal{P}_L^2 + 3}{4(2\mathcal{P}_N^2 + 5)\mathcal{P}_L^2 + 20\mathcal{P}_N\mathcal{P}_L + 5(\mathcal{P}_N^2 + 3)}, & \frac{3(\mathcal{P}_N - 1)((\mathcal{P}_N + 1)(\mathcal{P}_L - 1)\mathcal{P}_L + 1)}{4(2\mathcal{P}_N^2 + 5)\mathcal{P}_L^2 + 20\mathcal{P}_N\mathcal{P}_L + 5(\mathcal{P}_N^2 + 3)}, \\ \frac{3(\mathcal{P}_N - 1)^2 (2(\mathcal{P}_L - 1)\mathcal{P}_L + 1)}{4(2\mathcal{P}_N^2 + 5)\mathcal{P}_L^2 + 20\mathcal{P}_N\mathcal{P}_L + 5(\mathcal{P}_N^2 + 3)}, & \end{array} \right],$$

$$T = \sqrt{\frac{3}{8\pi}} \begin{bmatrix} -\sin \theta^* e^{i\phi^*} & 0 & 0 & 0 \\ \cos \theta^* & -\frac{1}{2} \sin \theta^* e^{i\phi^*} & -\frac{1}{2} \sin \theta^* e^{i\phi^*} & 0 \\ \sqrt{\frac{1}{6}} \sin \theta^* e^{-i\phi^*} & \sqrt{\frac{2}{3}} \cos \theta^* & \sqrt{\frac{2}{3}} \cos \theta^* & -\sqrt{\frac{1}{6}} \sin \theta^* e^{i\phi^*} \\ 0 & \frac{1}{2} \sin \theta^* e^{-i\phi^*} & \frac{1}{2} \sin \theta^* e^{-i\phi^*} & \cos \theta^* \\ 0 & 0 & 0 & \sin \theta^* e^{-i\phi^*} \end{bmatrix},$$

$$\frac{dN}{\sin \theta^* d\theta^*} = \frac{1}{2} + \left(\frac{3}{8} \hat{\rho}_{1,1} + \frac{3}{8} \hat{\rho}_{-1,-1} + \frac{1}{2} \hat{\rho}_{0,0} - \frac{1}{4} \right) (3 \cos^2 \theta^* - 1)$$

$$\approx \frac{1}{2} \left[1 - \frac{7}{30} (\mathcal{P}_N^2 + 4\mathcal{P}_N\mathcal{P}_L + \mathcal{P}_L^2) (3 \cos^2 \theta^* - 1) \right].$$



Decay angular distribution for ${}^4\text{Li}({}^3P_1)$ state

$$\hat{\rho}({}^4\text{Li}({}^3P_1)) = \left[\frac{-\mathcal{P}_L(\mathcal{P}_L + 1)\mathcal{P}_N^2 + \mathcal{P}_N + \mathcal{P}_L^2 + \mathcal{P}_L + 1}{(\mathcal{P}_N - 2\mathcal{P}_L)^2 + 3}, \right. \\ \frac{\mathcal{P}_N^2 - 4\mathcal{P}_L\mathcal{P}_N + 2(\mathcal{P}_N^2 + 1)\mathcal{P}_L^2 + 1}{(\mathcal{P}_N - 2\mathcal{P}_L)^2 + 3}, \\ \left. - \frac{(\mathcal{P}_N - 1)((\mathcal{P}_N + 1)(\mathcal{P}_L - 1)\mathcal{P}_L + 1)}{(\mathcal{P}_N - 2\mathcal{P}_L)^2 + 3} \right].$$

$$\hat{T}({}^4\text{Li}({}^3P_1) \rightarrow {}^3\text{He} + p) \\ = \sqrt{\frac{3}{8\pi}} \begin{bmatrix} -\cos\theta^* & -\frac{1}{2}\sin\theta^*e^{i\phi^*} & -\frac{1}{2}\sin\theta^*e^{i\phi^*} & 0 \\ -\sqrt{\frac{1}{2}}\sin\theta^*e^{-i\phi^*} & 0 & 0 & -\sqrt{\frac{1}{2}}\sin\theta^*e^{i\phi^*} \\ 0 & -\frac{1}{2}\sin\theta^*e^{-i\phi^*} & -\frac{1}{2}\sin\theta^*e^{-i\phi^*} & \cos\theta^* \end{bmatrix}$$

$$\frac{dN}{\sin\theta^*d\theta^*} = \frac{1}{2} - \frac{3}{8}(\hat{\rho}_{0,0} - \frac{1}{3})(3\cos^2\theta^* - 1) \\ \approx \frac{1}{2} \left(1 - \frac{1}{6}(\mathcal{P}_N^2 - 4\mathcal{P}_N\mathcal{P}_L + \mathcal{P}_L^2)(3\cos^2\theta^* - 1) \right),$$

Decay angular distribution for ${}^4\text{Li}({}^1P_1)$ state

$$\hat{\rho}({}^4\text{Li}({}^1P_1)) = \begin{bmatrix} \frac{2\mathcal{P}_L(\mathcal{P}_L+1)+1}{4\mathcal{P}_L^2+3} & 0 & 0 \\ 0 & \frac{1}{4\mathcal{P}_L^2+3} & 0 \\ 0 & 0 & \frac{2(\mathcal{P}_L-1)\mathcal{P}_L+1}{4\mathcal{P}_L^2+3} \end{bmatrix}$$

$\hat{T}({}^4\text{Li}({}^1P_1) \rightarrow {}^3\text{He} + p)$

$$= \sqrt{\frac{3}{8\pi}} \begin{bmatrix} 0 & -\sqrt{\frac{1}{2}}\sin\theta^*e^{i\phi^*} & \sqrt{\frac{1}{2}}\sin\theta^*e^{i\phi^*} & 0 \\ 0 & \cos\theta^* & -\cos\theta^* & 0 \\ 0 & \sqrt{\frac{1}{2}}\sin\theta^*e^{-i\phi^*} & -\sqrt{\frac{1}{2}}\sin\theta^*e^{-i\phi^*} & 0 \end{bmatrix}$$

$$\frac{dN}{\sin\theta^*d\theta^*} = \frac{1}{2} + \frac{3}{4}(\hat{\rho}_{0,0} - \frac{1}{3})(3\cos^2\theta^* - 1) \\ \approx \frac{1}{2} \left(1 - \frac{2}{3}\mathcal{P}_L^2(3\cos^2\theta^* - 1) \right)$$

State	E (MeV)	Structure	L	Decay mode	Γ (MeV)	$\frac{dN}{\sin\theta^* d\theta^*}$
${}^4\text{Li}({}^3P_2)$	g.s.	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	6.03	$\frac{1}{2} \left(1 - \frac{7}{30} (\mathcal{P}_N^2 + 4\mathcal{P}_N\mathcal{P}_L + \mathcal{P}_L^2) (3\cos^2\theta^* - 1)\right)$
${}^4\text{Li}({}^3P_1)$	0.32	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	7.35	$\frac{1}{2} \left(1 - \frac{1}{6} (\mathcal{P}_N^2 - 4\mathcal{P}_N\mathcal{P}_L + \mathcal{P}_L^2) (3\cos^2\theta^* - 1)\right)$
${}^4\text{Li}({}^1P_0)$	2.08	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	9.35	$\frac{1}{2}$
${}^4\text{Li}({}^1P_1)$	2.85	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	13.51	$\frac{1}{2} \left(1 - \frac{2}{3} \mathcal{P}_L^2 (3\cos^2\theta^* - 1)\right)$

Averaged decay angular distribution : $\frac{dN}{\sin\theta d\theta} = \frac{1}{2} \left(1 - \frac{1}{36} (5\mathcal{P}_N^2 + 8\mathcal{P}_N\mathcal{P}_L + 11\mathcal{P}_L^2) (3\cos^2\theta - 1)\right)$

${}^4\text{Li}$ decay angular distribution within thermal model

$$\hat{\rho}({}^4\text{Li}(2^-)) = \frac{1}{1 + 2\cosh(\frac{\omega}{T}) + 2\cosh(\frac{2\omega}{T})} \begin{bmatrix} e^{\frac{2\omega}{T}} & 0 & 0 & 0 & 0 \\ 0 & e^{\frac{\omega}{T}} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & e^{-\frac{\omega}{T}} & 0 \\ 0 & 0 & 0 & 0 & e^{-\frac{2\omega}{T}} \end{bmatrix}, \hat{\rho}({}^4\text{Li}(1^-)) = \frac{1}{1 + 2\cosh(\frac{\omega}{T})} \begin{bmatrix} e^{\frac{\omega}{T}} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{-\frac{\omega}{T}} \end{bmatrix}, \hat{\rho}({}^4\text{Li}(0^-)) = 1.$$

Let $\mathcal{P} = \frac{\omega}{2T}$,

Averaged decay angular distribution from thermal model

$$\frac{dN}{\sin\theta d\theta} = \frac{1}{2} \left(1 - \frac{2}{3} \mathcal{P}^2 (3\cos^2\theta - 1)\right)$$

$\mathcal{P}_L = \mathcal{P}_N = \mathcal{P}$

1. The coalescence of polarized nucleons results in polarized light nuclei, the polarization of unstable nuclei can be measured.
2. We calculate the decay angular distribution of ${}^4\text{Li}$ which can be measured experimentally.
3. These results provide a viable probe to study nucleon polarization and the vortical structure of nuclear matter.

State	E (MeV)	Structure	L	Decay mode	Γ (MeV)	$\frac{dN}{\sin\theta^* d\theta^*}$
${}^4\text{Li}({}^3P_2)$	g.s.	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	6.03	$\frac{1}{2} \left(1 - \frac{7}{30} (\mathcal{P}_N^2 + 4\mathcal{P}_N\mathcal{P}_L + \mathcal{P}_L^2) (3\cos^2\theta^* - 1) \right)$
${}^4\text{Li}({}^3P_1)$	0.32	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	7.35	$\frac{1}{2} \left(1 - \frac{1}{6} (\mathcal{P}_N^2 - 4\mathcal{P}_N\mathcal{P}_L + \mathcal{P}_L^2) (3\cos^2\theta^* - 1) \right)$
${}^4\text{Li}({}^1P_0)$	2.08	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	9.35	$\frac{1}{2}$
${}^4\text{Li}({}^1P_1)$	2.85	${}^3\text{He}(\frac{1}{2}^+) - p(\frac{1}{2}^+)$	1	${}^4\text{Li} \rightarrow {}^3\text{He} + p$	13.51	$\frac{1}{2} \left(1 - \frac{2}{3} \mathcal{P}_L^2 (3\cos^2\theta^* - 1) \right)$

Averaged decay angular distribution :
$$\frac{dN}{\sin\theta d\theta} = \frac{1}{2} \left(1 - \frac{1}{36} (5\mathcal{P}_N^2 + 8\mathcal{P}_N\mathcal{P}_L + 11\mathcal{P}_L^2) (3\cos^2\theta - 1) \right)$$

Thanks for your attention !

$\mathcal{P}_N$: nucleon polarization

$\mathcal{P}_L = \frac{\omega}{2T}$: orbital motion polarization