

Measurement of branching fractions of

$$D^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^- \text{ and } K_S^0 K^+ \pi^+ \pi^- \pi^0$$

Physics & Software Meeting

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- 1 Introduction
- 2 Analysis method
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- 4 Data analysis
- 5 Systematic uncertainties
- 6 IO check
- 7 Summary

- Since the discovery of D mesons in 1976, their decays have been extensively studied. However, many hadronic D decays remain unmeasured.
- The BFs of hadronic D decays provide important information for testing lepton flavor universality in B physics [PLB781,368].
- Combining measured BFs with partial wave analysis results helps study quark SU(3) symmetry and its breaking effects.
- CP violation in charm decays is crucial for understanding the universe's asymmetry. CP violation was observed in D decays at the LHCb in 2019 [PRL122,211803].
- Our goal is to measure the BFs of unknown hadronic D decays.

$$N_{tag}^{obs} = 2N_{D^+D^-} \mathcal{B}_{tag} \epsilon_{tag}$$

$$N_{sig}^{obs} = 2N_{D^+D^-} \mathcal{B}_{tag} \mathcal{B}_{sig} \epsilon_{tag,sig}$$

$$\mathcal{B}_{sig} = \frac{N_{sig}^{obs,\alpha}}{\sum_{\alpha} N_{tag}^{obs,\alpha} \epsilon_{tag,sig}^{\alpha} / \epsilon_{tag}^{\alpha}}$$

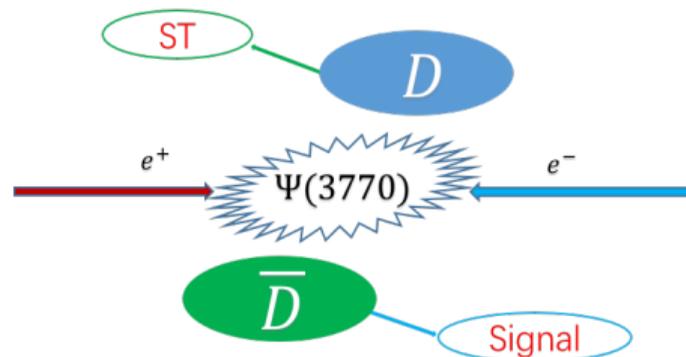
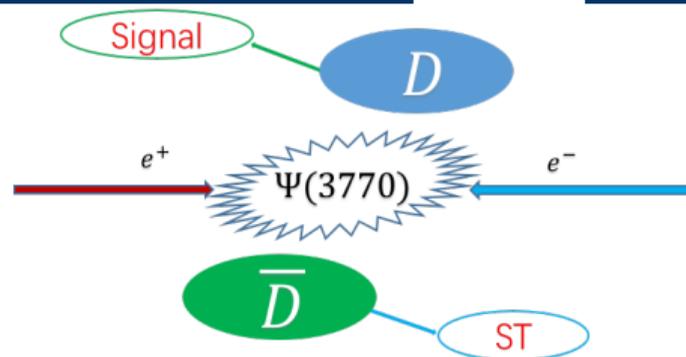
N_{sig}^{obs} : Signal yields

N_{tag}^{obs} : Single tag yields

$\epsilon_{tag,sig}$: Double tag efficiency

ϵ_{tag} : Single tag efficiency

α : Six single tag modes



Charge track : $|V_{xy}| < 1cm$ $|V_z| < 10cm$ $|\cos\theta| < 0.93$

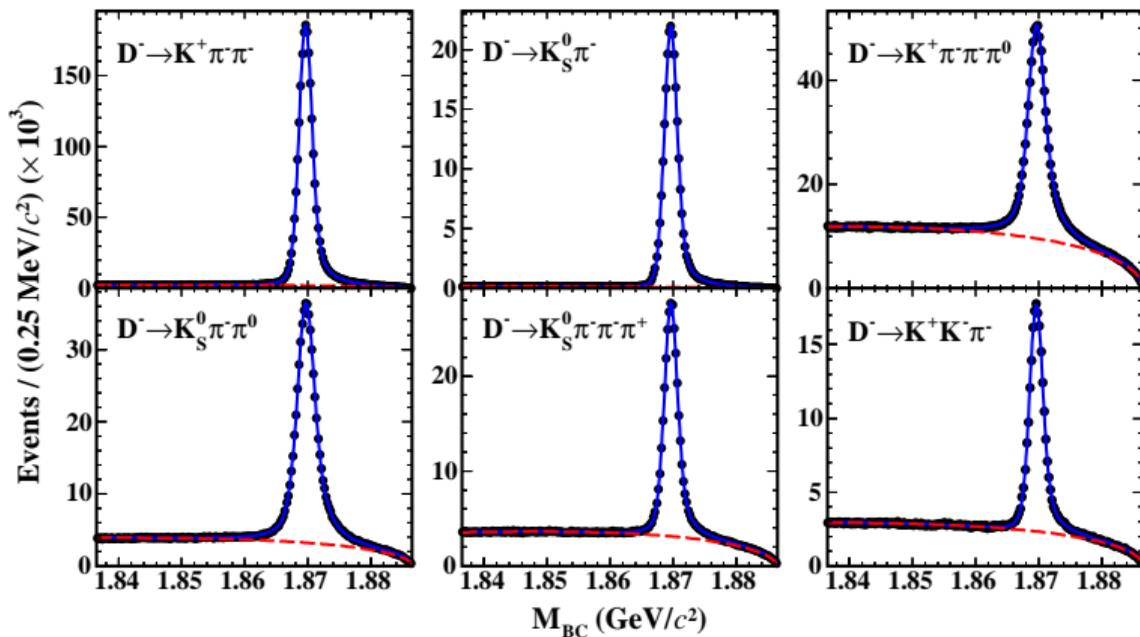
$K_S^0 \rightarrow \pi^+\pi^-$: no PID performed on π $|\cos\theta| < 0.93$
 $M_{\pi^+\pi^-} \in (0.4857, 0.5097) GeV/c^2$ $|R_z| < 20.0cm$
 Vertex fit: $\chi^2 < 100$ 2nd vertex fit: $L/\sigma > 2$

PID : K : $CL_K > CL_\pi, CL_K > 0$ $dE/dx + TOF$
 π : $CL_\pi > CL_K, CL_\pi > 0$

Photon : $0 \leq t_{TDC} \leq 14(\times 50 ns)$
 Barrel : $|\cos\theta| < 0.8, E_{\gamma,EMC}^{Barrel} > 25 MeV$
 Endcap : $0.86 < |\cos\theta| < 0.92, E_{\gamma,EMC}^{Endcap} > 25 MeV$

π^0 : Mass constraint fit on $\pi^0(\gamma\gamma) : \chi^2 < 50$
 $\pi^0 \in (0.115, 0.150) GeV/c^2$

Double – Gaussian(signal) + ARGUS(BKG)



<https://docbes3.ihep.ac.cn/cgi-bin/DocDB/ShowDocument?docid=1289>

- common cut

- ▶ $|\Delta E_{tag}| \in 3.5\sigma$
- ▶ $|M_{\pi^+\pi^-}^{sig} - 0.4977| > 0.02\text{GeV}/c^2$
- ▶ $|M_{K_S^0} - 0.4977| < 0.012\text{GeV}/c^2$
- ▶ $\theta_{D\bar{D}} > 160^\circ$

- additional cut for fitting ΔE_{sig}

- ▶ $1.863\text{GeV}/c^2 < M_{BC}^{tag(sig)} < 1.877\text{GeV}/c^2$

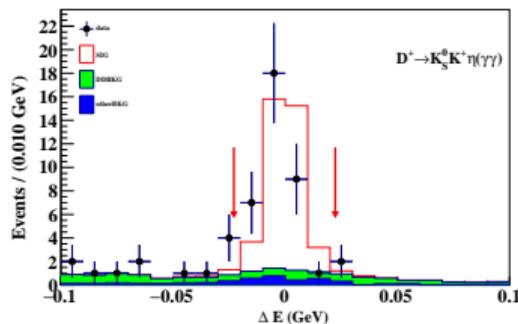
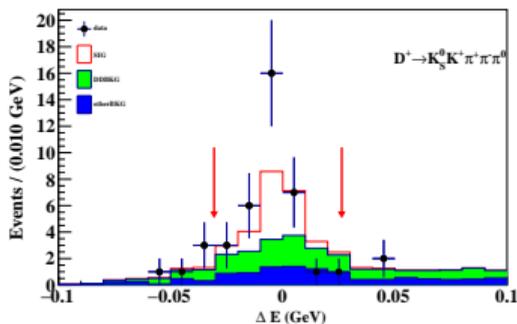
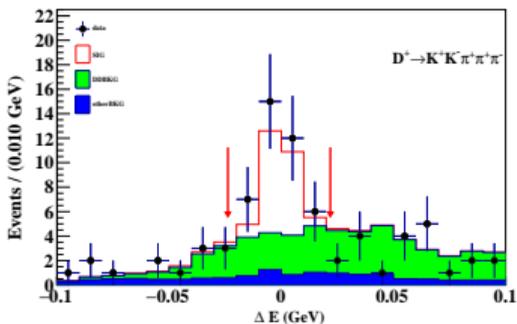
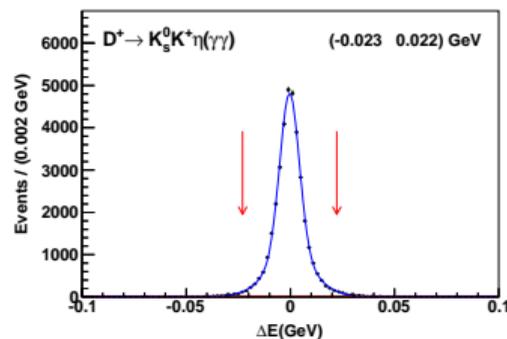
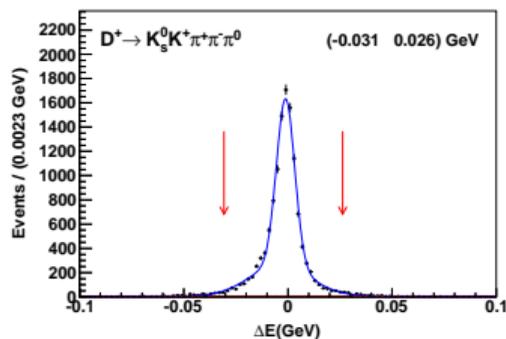
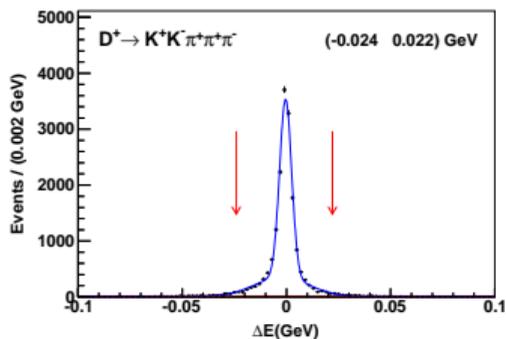
- additional cut for fitting M_{BC}^{sig}

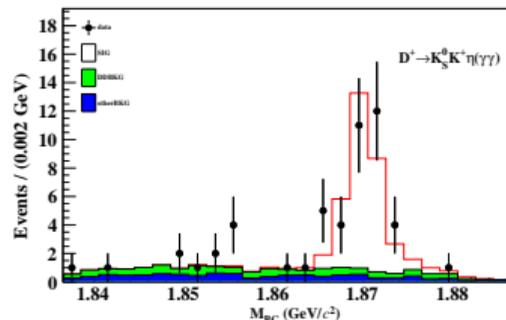
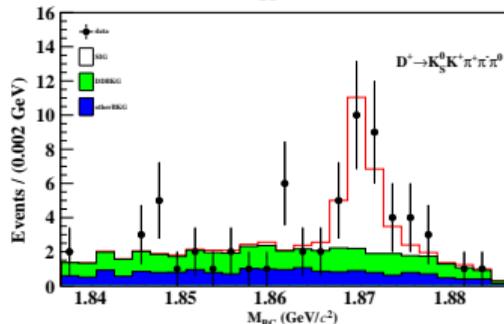
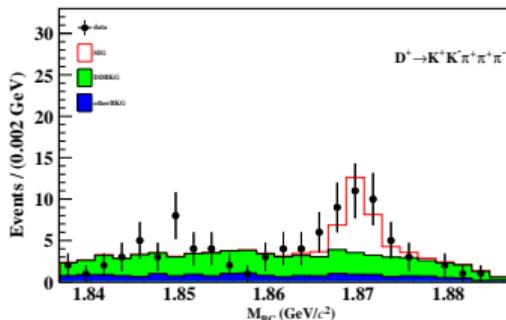
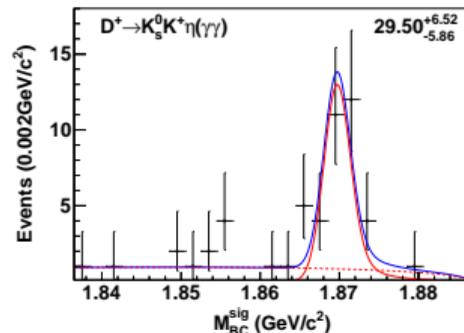
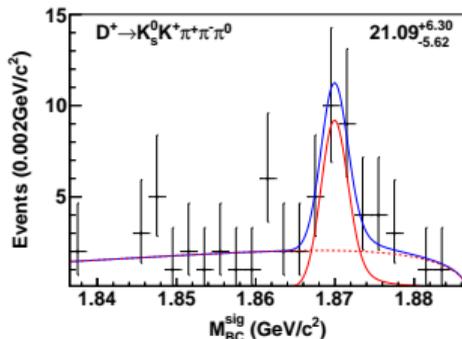
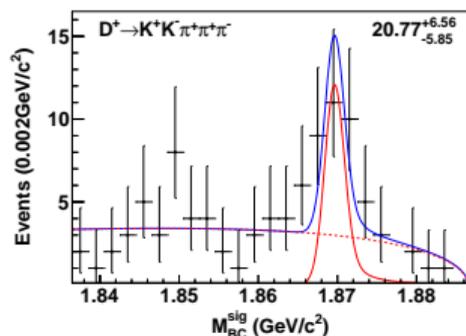
- ▶ $\Delta E_{sig} \in 3\sigma$

- additional cut for fitting others

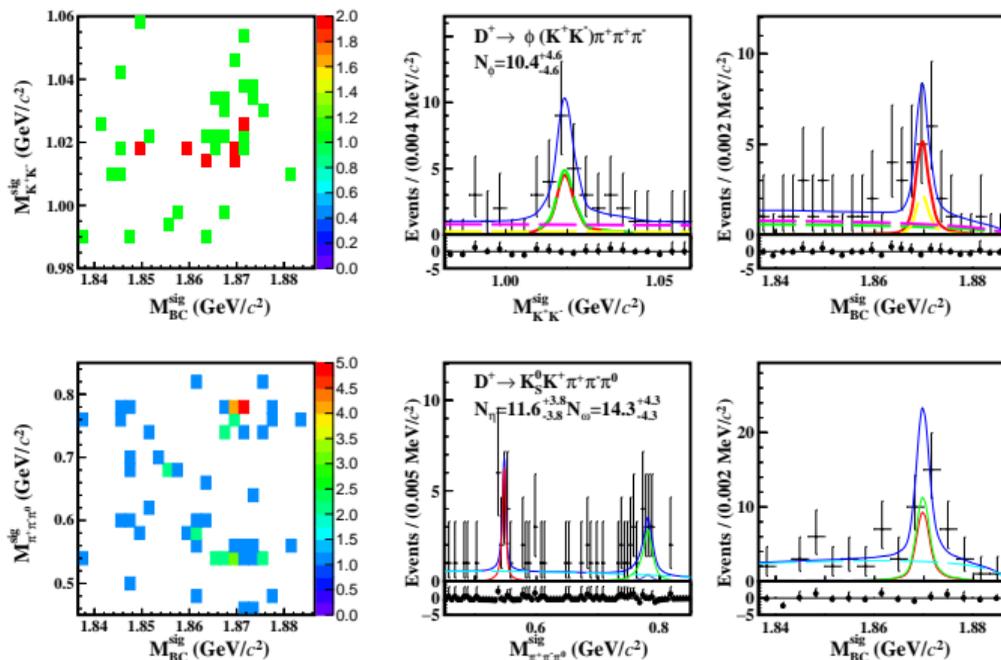
- ▶ $\Delta E_{sig} \in 3\sigma$
- ▶ $1.863\text{GeV}/c^2 < M_{BC}^{tag(sig)} < 1.877\text{GeV}/c^2$

FITTING ΔE_{sig} AT 3σ SIGNAL REGION

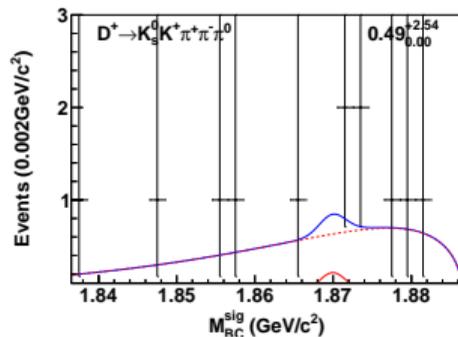
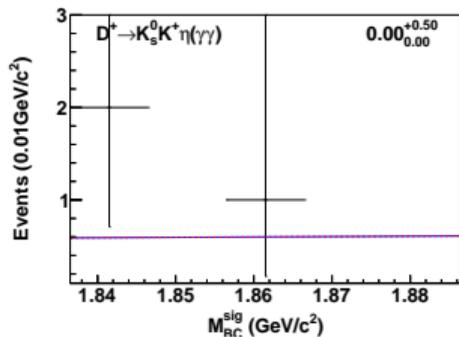
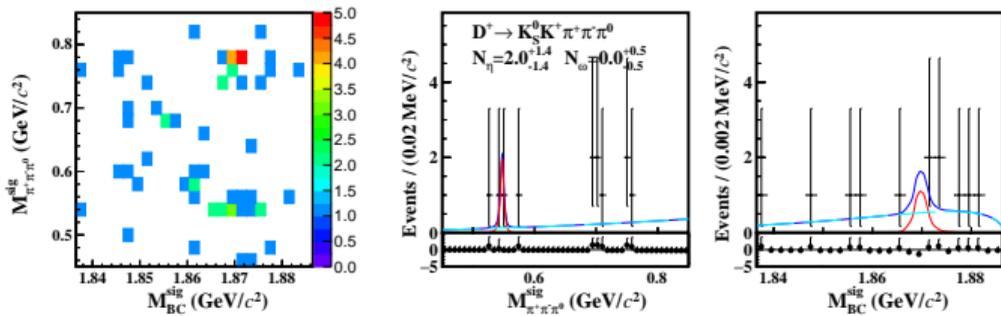




$Truth\ shape \otimes Gaussian(signal) + ARGUS(background)$



SigMC shape(signal) + ARGUS(background)



$$\begin{aligned}
 D^+ &\rightarrow K^+ K^- \pi^+ \pi^+ \pi^- \\
 &\rightarrow \phi \pi^+ \pi^+ \pi^-, \phi \rightarrow K^+ K^- && (62\%) \\
 &\rightarrow K^+ K^- \pi^+ \pi^+ \pi^- && (38\%)
 \end{aligned}$$

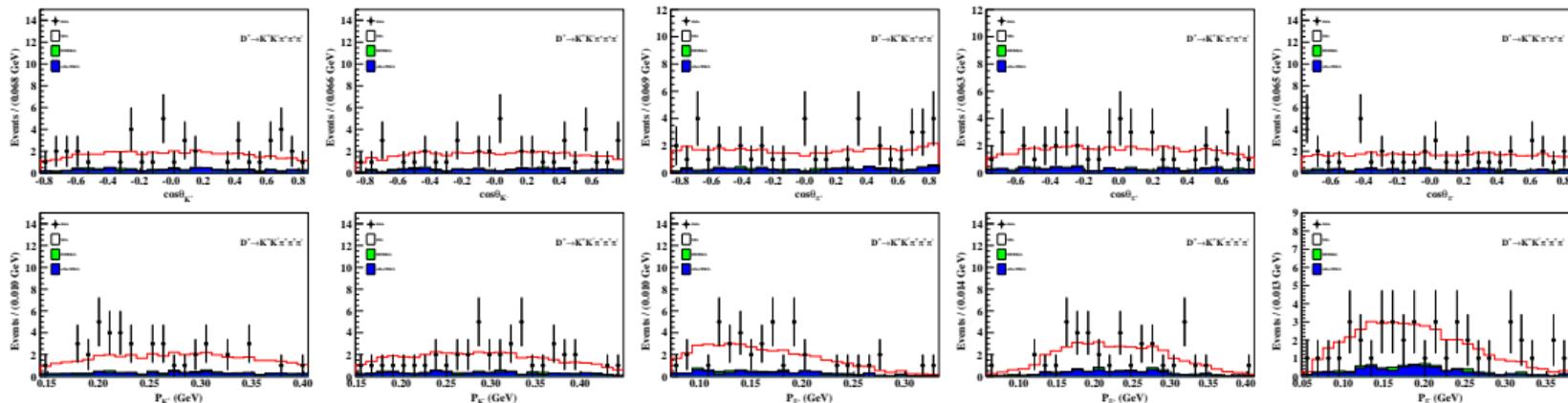
$$\begin{aligned}
 D^+ &\rightarrow K_S^0 K^+ \pi^+ \pi^- \pi^0 \\
 &\rightarrow \bar{K}_1^0 K^+, \bar{K}_1^0 \rightarrow \omega \bar{K}^0, \bar{K}^0 \rightarrow K_S^0, \omega \rightarrow \pi^- \pi^+ \pi^0 && (41.0\%) \\
 &\rightarrow \bar{K}_1^+ K_S^0, \bar{K}_1^+ \rightarrow \omega K^+, \omega \rightarrow \pi^- \pi^+ \pi^0 && (32.1\%) \\
 &\rightarrow K_S^0 K^+ \eta, \eta \rightarrow \pi^- \pi^+ \pi^0 && (26.9\%)
 \end{aligned}$$

$$D^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$$

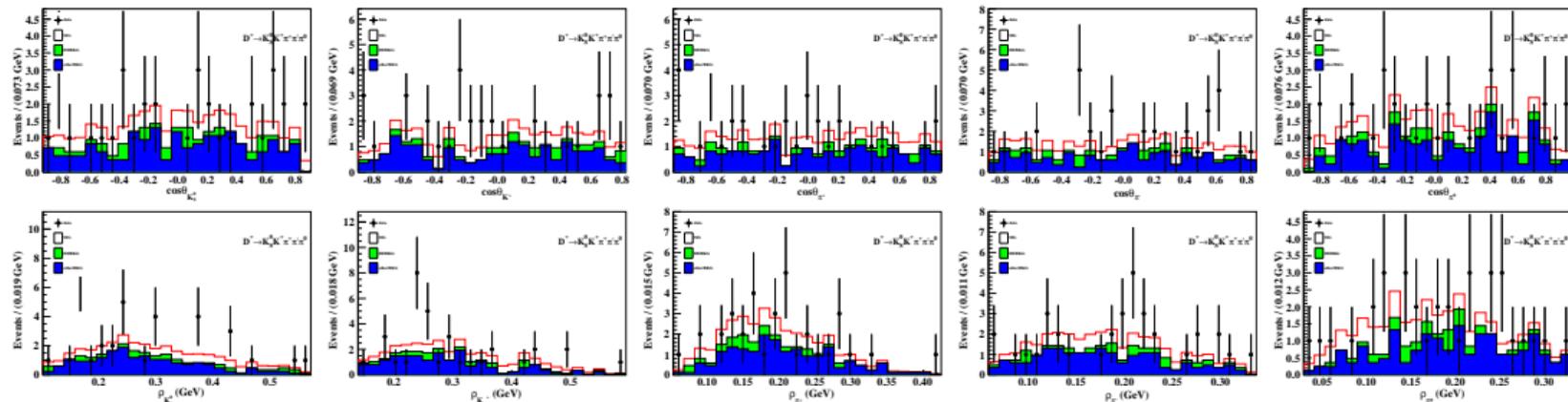
Tag modes	N_{gen}	$N_{\text{obs}}^{\text{sig}}$	$\epsilon_{\text{tag}}(\%)$	$\epsilon_{\text{tag,sig}}(\%)$	$\epsilon_{\text{sig}}(\%)$	Weight
$K^+ \pi^- \pi^-$	100000	4403 ± 68	52.44 ± 0.01	4.40 ± 0.09	8.40 ± 0.17	7.74 ± 0.11
$K_S^0 \pi^-$	100000	4174 ± 67	51.89 ± 0.02	4.17 ± 0.09	8.04 ± 0.17	
$K^+ \pi^- \pi^- \pi^0$	100000	1769 ± 45	27.19 ± 0.01	1.77 ± 0.08	6.51 ± 0.29	
$K_S^0 \pi^- \pi^0$	100000	1906 ± 45	27.57 ± 0.01	1.91 ± 0.08	6.91 ± 0.29	
$K_S^0 \pi^- \pi^- \pi^+$	100000	2093 ± 48	29.68 ± 0.01	2.09 ± 0.08	7.05 ± 0.27	
$K^+ K^- \pi^-$	100000	3380 ± 61	42.05 ± 0.02	3.38 ± 0.09	8.04 ± 0.20	

In the case of the decay mentioned above,
the final efficiency is obtained by weighting through single-tag channels,
other decay channels can be found in the backup slides.

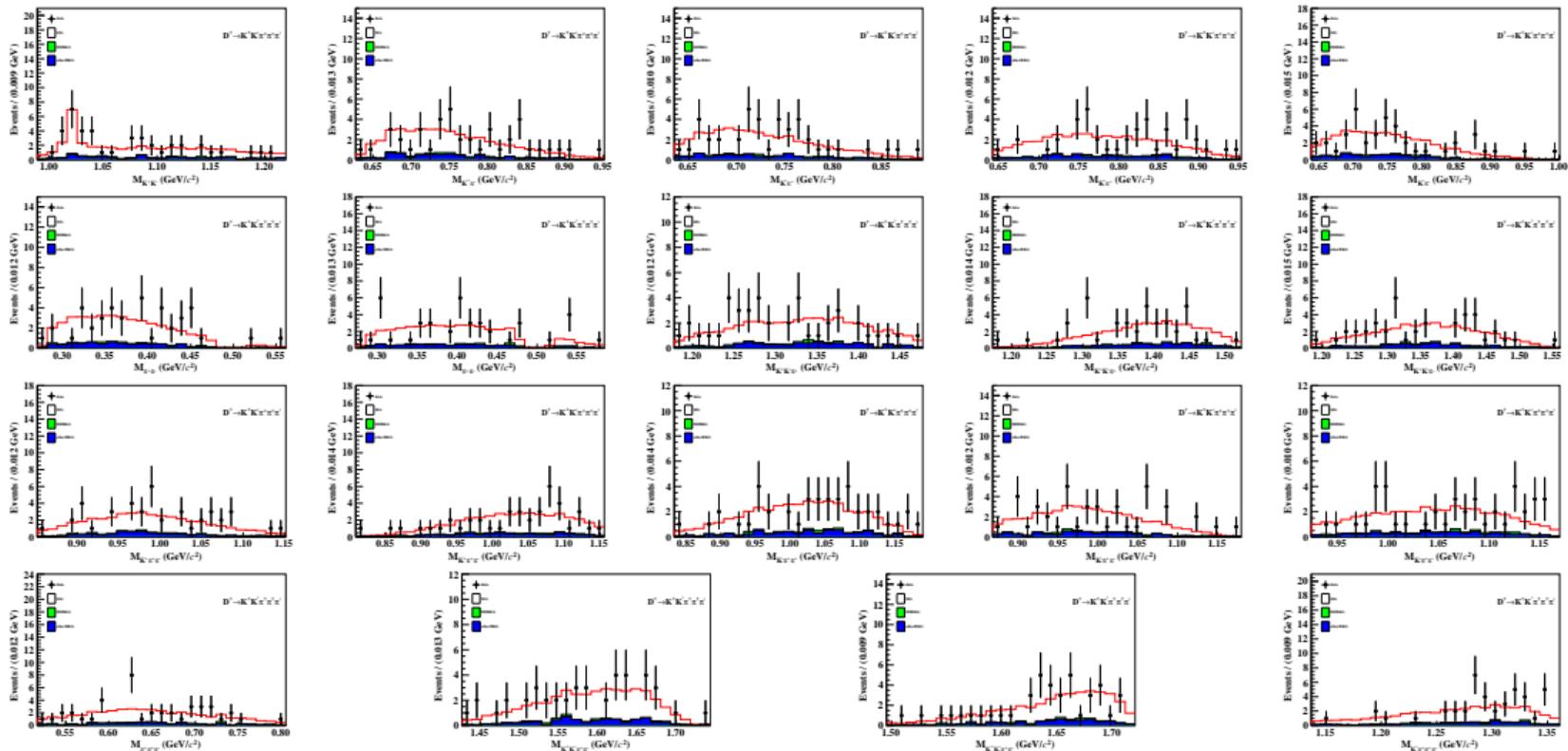
Angle and Momentum of $D^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$



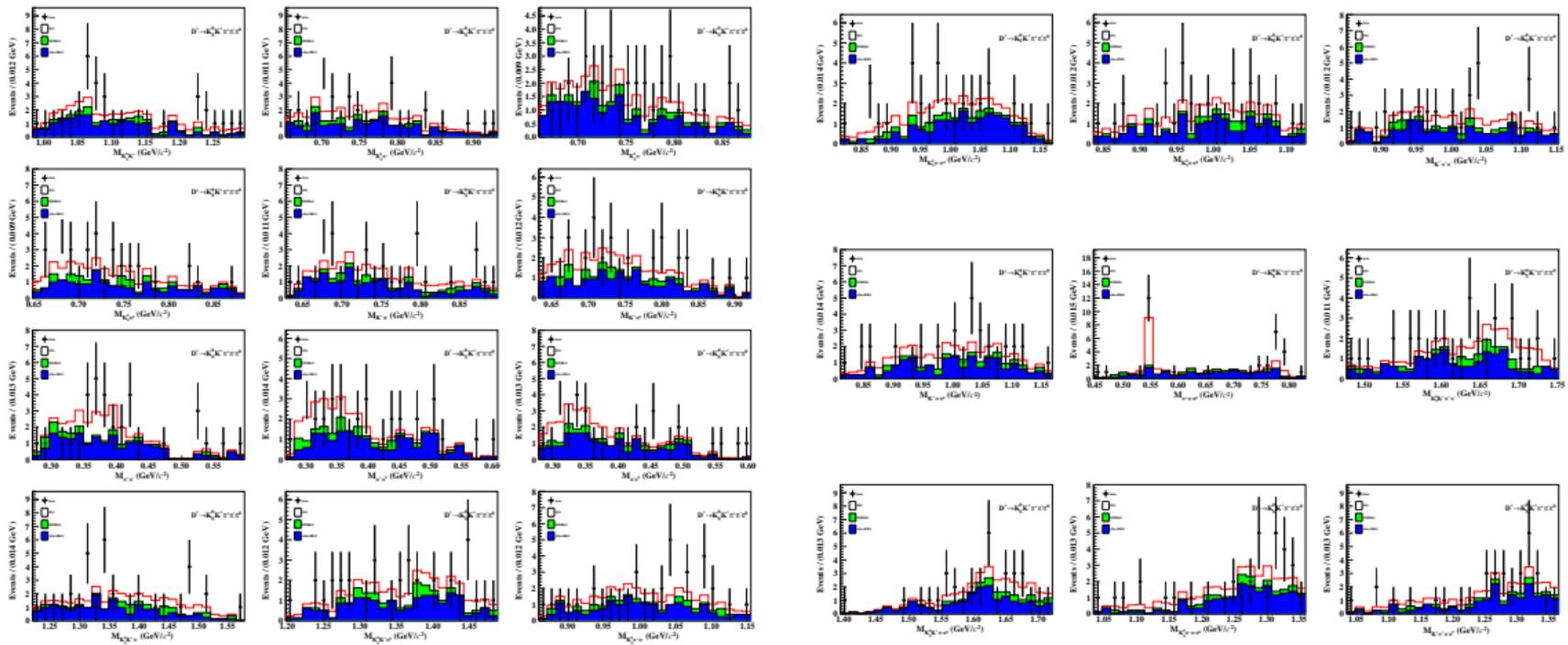
Angle and Momentum of $D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^- \pi^0$



INVARIANT MASS OF $D^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$



INVARIANT MASS OF $D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^- \pi^0$



Decay mode	$N_{\text{data,net}}$	N_{tag}	$\epsilon_{\text{sig}}(\%)$	$\mathcal{B}_{\text{sig}}(\times 10^{-4})$	Significance
$K^+K^-\pi^+\pi^+\pi^-$	$20.8^{+6.6}_{-5.9}$	4296647 ± 2438	7.74 ± 0.11	$0.62^{+0.20}_{-0.18}$	4.0
$K_S^0K^+\pi^+\pi^-\pi^0$	$21.1^{+6.3}_{-5.6}$		3.90 ± 0.08	$1.84^{+0.55}_{-0.49}$	4.4
$K_S^0K^+\eta(\gamma\gamma)$	$29.5^{+6.5}_{-5.9}$		15.10 ± 0.15	$1.68^{+0.37}_{-0.33}$	6.8
$K_S^0K^+\eta(\pi^+\pi^-\pi^0)$	$10.5^{+3.9}_{-3.9}$		6.49 ± 0.10	$2.41^{+0.87}_{-0.87}$	4.0
$K_S^0K^+\omega(\pi^+\pi^-\pi^0)$	$14.3^{+4.3}_{-4.3}$		3.23 ± 0.07	$1.69^{+0.51}_{-0.51}$	3.8
$\phi(K^+K^-\pi^+\pi^+\pi^-)$	$10.4^{+4.6}_{-4.6}$		6.34 ± 0.10	$0.77^{+0.35}_{-0.35}$	2.1

Decay mode	$\mathcal{B}(\times 10^{-4})$	$\mathcal{B}_{PDG}(\times 10^{-4})$
$D^+ \rightarrow K^+K^-\pi^+\pi^+\pi^-$	$0.62^{+0.20}_{-0.18}$	2.3 ± 1.2
$D^+ \rightarrow K_S^0K^+\eta(\gamma\gamma)$	$1.68^{+0.37}_{-0.33}$	1.8 ± 0.5
$D^+ \rightarrow K_S^0K^+\eta(\pi^+\pi^-\pi^0)$	$2.41^{+0.87}_{-0.87}$	

The top table shows the final results, the left table displaying the comparison between the results and the PDG values.

Decay modes	1	2	3	4	5	6
N_{tag}	0.1	0.1	0.1	0.1	0.1	0.1
$(K/\pi)^\pm$ tracking	3.0	5.0	1.0	3.0	3.0	5.0
$(K/\pi)^\pm$ PID	3.0	5.0	1.0	3.0	3.0	5.0
K_S^0 reconstruction	2.0	-	2.0	2.0	2.0	-
η & π^0 reconstruction	3.3	-	-	3.3	3.3	-
K_S^0 rejection	0.0	0.0	-	0.0	0.0	0.0
$\mathcal{B}_{\text{sub-decay}}$	0.08	-	0.5	1.2	0.8	1.0
ΔE_{sig} cut	1.6	0.2	0.0	1.6	1.6	0.2
Mass fit	6.3	1.6	9.0	3.8	3.7	4.0
MC generator	6.2	2.6	-	6.2	6.2	2.6
MC statistics	1.8	1.3	1.7	2.0	3.6	1.6
Total	10.6	7.8	9.5	9.5	9.7	8.6

Relative systematic uncertainties (%)
in the measurements of the BFs of

$D^+ \rightarrow$

(1) $K_S^0 K^+ \pi^+ \pi^- \pi^0$,

(2) $K^+ K^- \pi^+ \pi^+ \pi^-$,

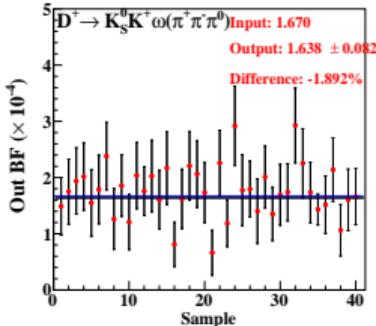
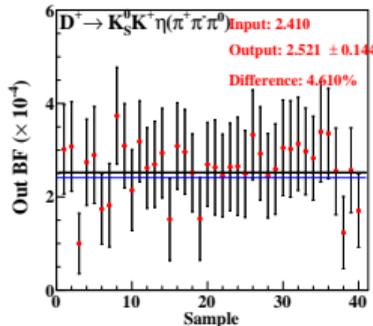
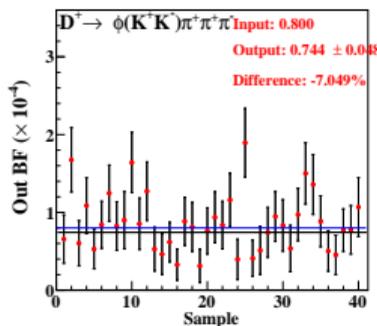
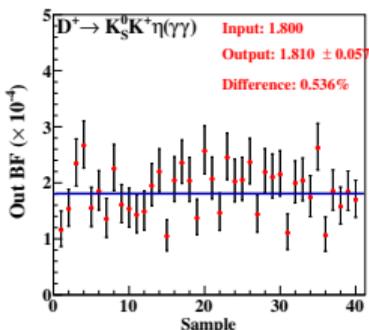
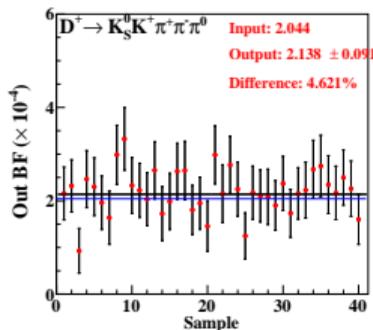
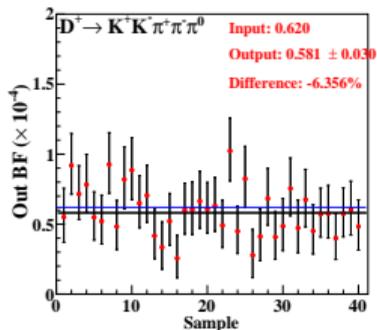
(3) $K_S^0 K^+ \eta(\gamma\gamma)$,

(4) $K_S^0 K^+ \eta(\pi^+ \pi^- \pi^0)$,

(5) $K_S^0 K^+ \omega(\pi^+ \pi^- \pi^0)$,

(6) $\phi(K^+ K^-) \pi^+ \pi^+ \pi^-$

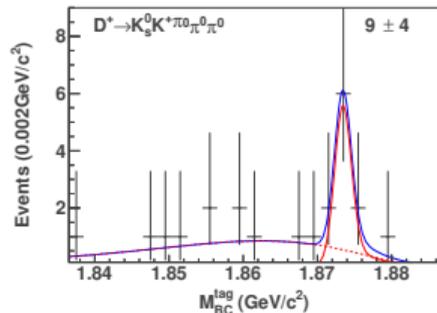
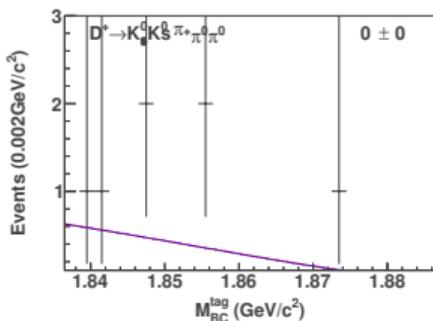
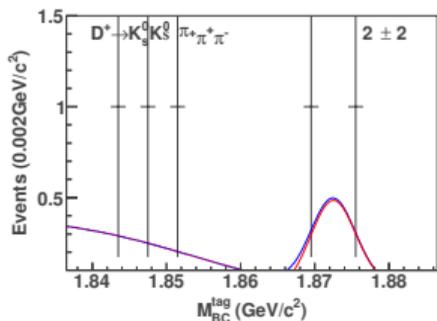
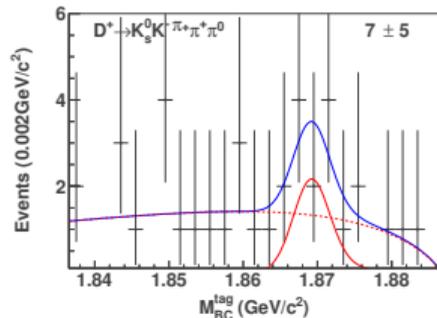
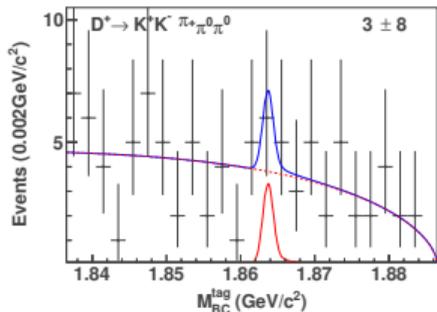
The leftmost column in the table
displays all the considered items.



The left displays the difference of the BFs between the input and output in the $40 \times \text{MC}$ sample.

- By analyzing an e^+e^- annihilation data of 7.9 fb^{-1} collected at $\sqrt{s} = 3.773 \text{ GeV}$ with the BESIII detector:
 - ▶ improved precision:
 - $D^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$
 - $D^+ \rightarrow K_S^0 K^+ \eta$
 - ▶ measured for the first time:
 - $D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^- \pi^0$
 - $D^+ \rightarrow \phi \pi^+ \pi^+ \pi^-$
 - $D^+ \rightarrow K_S^0 K^+ \omega$

Thank You!



$$D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^- \pi^0$$

Tag modes	N_{gen}	$N_{\text{obs}}^{\text{sig}}$	$\epsilon_{\text{tag}}(\%)$	$\epsilon_{\text{tag,sig}}(\%)$	$\epsilon_{\text{sig}}(\%)$	Weight
$K^+ \pi^- \pi^-$	100000	2286 ± 51	52.44 ± 0.01	2.29 ± 0.06	4.36 ± 0.12	3.90 ± 0.08
$K_S^0 \pi^-$	100000	2322 ± 51	51.89 ± 0.02	2.32 ± 0.07	4.47 ± 0.13	
$K^+ \pi^- \pi^- \pi^0$	100000	788 ± 31	27.19 ± 0.01	0.79 ± 0.05	2.90 ± 0.20	
$K_S^0 \pi^- \pi^0$	100000	939 ± 33	27.57 ± 0.01	0.94 ± 0.06	3.40 ± 0.21	
$K_S^0 \pi^- \pi^- \pi^+$	100000	979 ± 34	29.68 ± 0.01	0.98 ± 0.06	3.30 ± 0.19	
$K^+ K^- \pi^-$	100000	1737 ± 44	42.05 ± 0.02	1.74 ± 0.06	4.13 ± 0.15	

$$D^+ \rightarrow K_S^0 K^+ \omega (\pi^+ \pi^- \pi^0)$$

Tag modes	N_{gen}	$N_{\text{obs}}^{\text{sig}}$	$\epsilon_{\text{tag}}(\%)$	$\epsilon_{\text{tag,sig}}(\%)$	$\epsilon_{\text{sig}}(\%)$	Weight
$K^+ \pi^- \pi^-$	100000	1924 ± 45	52.44 ± 0.01	1.92 ± 0.06	3.67 ± 0.11	3.23 ± 0.07
$K_S^0 \pi^-$	100000	1854 ± 44	51.89 ± 0.02	1.85 ± 0.06	3.57 ± 0.11	
$K^+ \pi^- \pi^- \pi^0$	100000	638 ± 27	27.19 ± 0.01	0.64 ± 0.05	2.34 ± 0.18	
$K_S^0 \pi^- \pi^0$	100000	751 ± 21	27.57 ± 0.01	0.75 ± 0.05	2.72 ± 0.19	
$K_S^0 \pi^- \pi^- \pi^+$	100000	781 ± 29	29.68 ± 0.01	0.78 ± 0.05	2.63 ± 0.17	
$K^+ K^- \pi^-$	100000	1507 ± 40	42.05 ± 0.02	1.51 ± 0.06	3.58 ± 0.14	

$$D^+ \rightarrow K_S^0 K^+ \eta (\pi^+ \pi^- \pi^0)$$

Tag modes	N_{gen}	$N_{\text{obs}}^{\text{sig}}$	$\epsilon_{\text{tag}}(\%)$	$\epsilon_{\text{tag,sig}}(\%)$	$\epsilon_{\text{sig}}(\%)$	Weight
$K^+ \pi^- \pi^-$	100000	3768 ± 63	52.44 ± 0.01	3.77 ± 0.08	7.19 ± 0.16	6.49 ± 0.10
$K_S^0 \pi^-$	100000	3870 ± 64	51.89 ± 0.02	3.87 ± 0.08	7.46 ± 0.16	
$K^+ \pi^- \pi^- \pi^0$	100000	1374 ± 39	27.19 ± 0.01	1.37 ± 0.07	5.05 ± 0.25	
$K_S^0 \pi^- \pi^0$	100000	1539 ± 40	27.57 ± 0.01	1.54 ± 0.07	5.58 ± 0.26	
$K_S^0 \pi^- \pi^- \pi^+$	100000	1622 ± 42	29.68 ± 0.01	1.62 ± 0.07	5.46 ± 0.24	
$K^+ K^- \pi^-$	100000	2980 ± 56	42.05 ± 0.02	2.98 ± 0.08	7.09 ± 0.19	

$$D^+ \rightarrow K_S^0 K^+ \eta(\gamma\gamma)$$

Tag modes	N_{gen}	$N_{\text{obs}}^{\text{sig}}$	$\epsilon_{\text{tag}}(\%)$	$\epsilon_{\text{tag,sig}}(\%)$	$\epsilon_{\text{sig}}(\%)$	Weight
$K^+ \pi^- \pi^-$	100000	8497 ± 100	52.44 ± 0.01	8.50 ± 0.12	16.20 ± 0.22	15.10 ± 0.15
$K_S^0 \pi^-$	100000	8426 ± 100	51.89 ± 0.02	8.43 ± 0.12	16.24 ± 0.22	
$K^+ \pi^- \pi^- \pi^0$	100000	3422 ± 63	27.19 ± 0.01	3.42 ± 0.10	12.59 ± 0.39	
$K_S^0 \pi^- \pi^0$	100000	3802 ± 68	27.57 ± 0.01	3.80 ± 0.11	13.79 ± 0.40	
$K_S^0 \pi^- \pi^- \pi^+$	100000	4233 ± 71	29.68 ± 0.01	4.23 ± 0.11	14.26 ± 0.37	
$K^+ K^- \pi^-$	100000	6700 ± 90	42.05 ± 0.02	6.70 ± 0.12	15.93 ± 0.28	

$$D^+ \rightarrow \phi(K^+K^-)\pi^+\pi^+\pi^-$$

Tag modes	N_{gen}	$N_{\text{obs}}^{\text{sig}}$	$\epsilon_{\text{tag}}(\%)$	$\epsilon_{\text{tag,sig}}(\%)$	$\epsilon_{\text{sig}}(\%)$	Weight
$K^+\pi^-\pi^-$	100000	3556 ± 62	52.44 ± 0.01	3.56 ± 0.08	6.78 ± 0.15	6.34 ± 0.10
$K_S^0\pi^-$	100000	3472 ± 60	51.89 ± 0.02	3.47 ± 0.08	6.69 ± 0.15	
$K^+\pi^-\pi^-\pi^0$	100000	1438 ± 40	27.19 ± 0.01	1.44 ± 0.07	5.29 ± 0.26	
$K_S^0\pi^-\pi^0$	100000	1606 ± 206	27.57 ± 0.01	1.61 ± 0.07	5.83 ± 0.27	
$K_S^0\pi^-\pi^-\pi^+$	100000	1835 ± 20	29.68 ± 0.01	1.83 ± 0.08	6.18 ± 0.26	
$K^+K^-\pi^-$	100000	2796 ± 53	42.05 ± 0.02	2.80 ± 0.08	6.65 ± 0.19	