



BESIII

Flavor physics at BESIII

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On behalf of the BESIII Collaboration

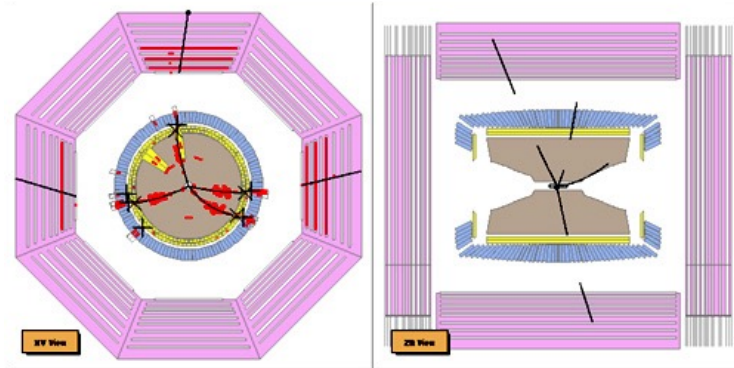
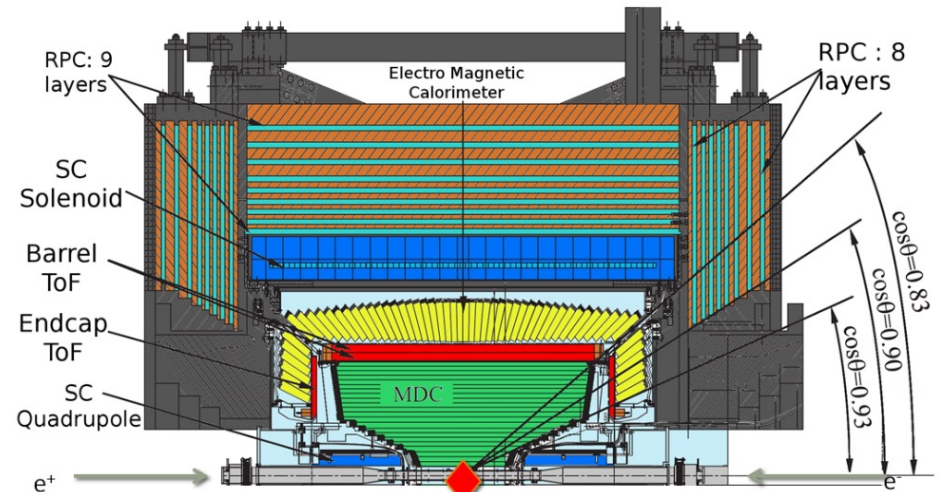
第4届LHCb前沿物理研讨会

2024.07.28 烟台

Outline

- BEPCII & BESIII
- Recent Highlights on Flavor Physics
- Summary & Prospect

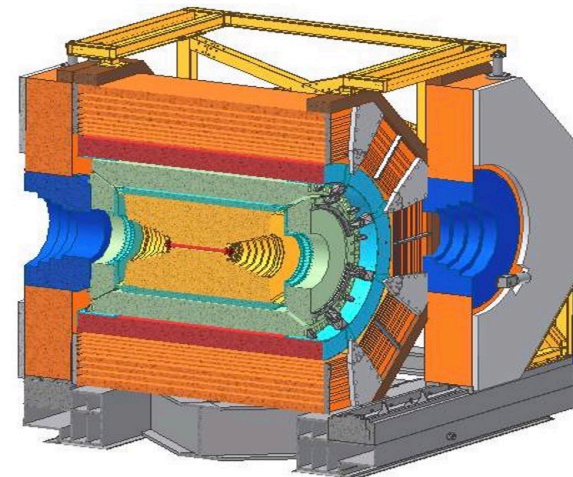
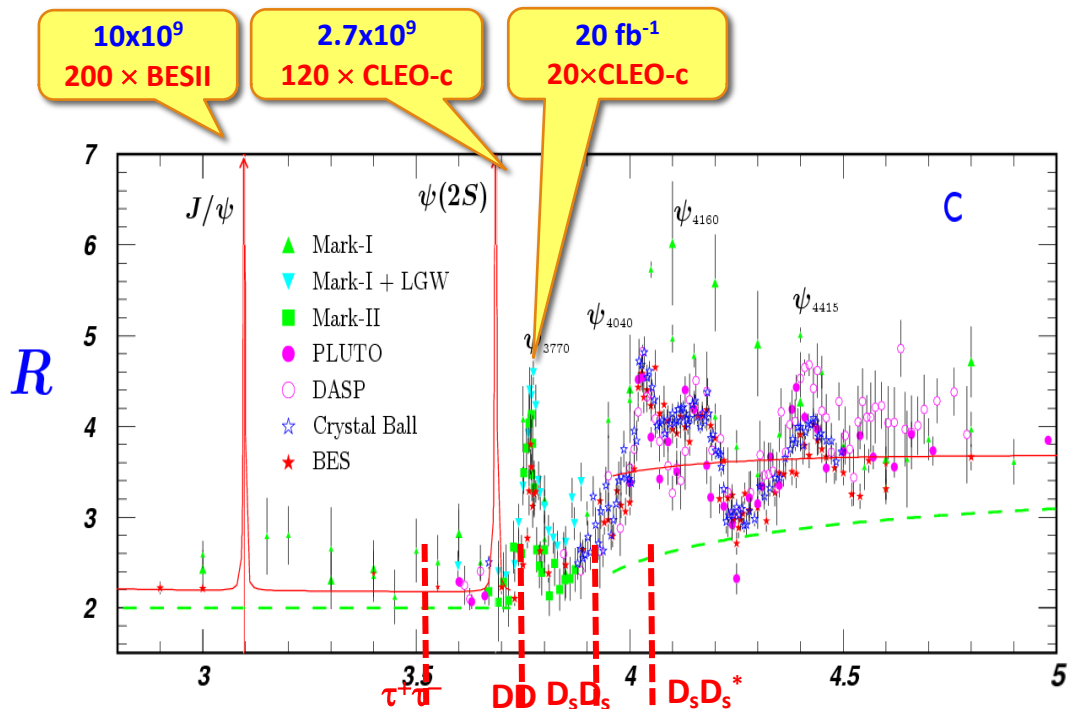
BEP CII & BES III



First HEP collider in China (1988)
 c.m.s energy: 2 ~ 4.95 GeV
 Max luminosity: $1 \times 10^{33} \text{cm}^{-2} \text{s}^{-1}$



BESIII: τ -charm factory

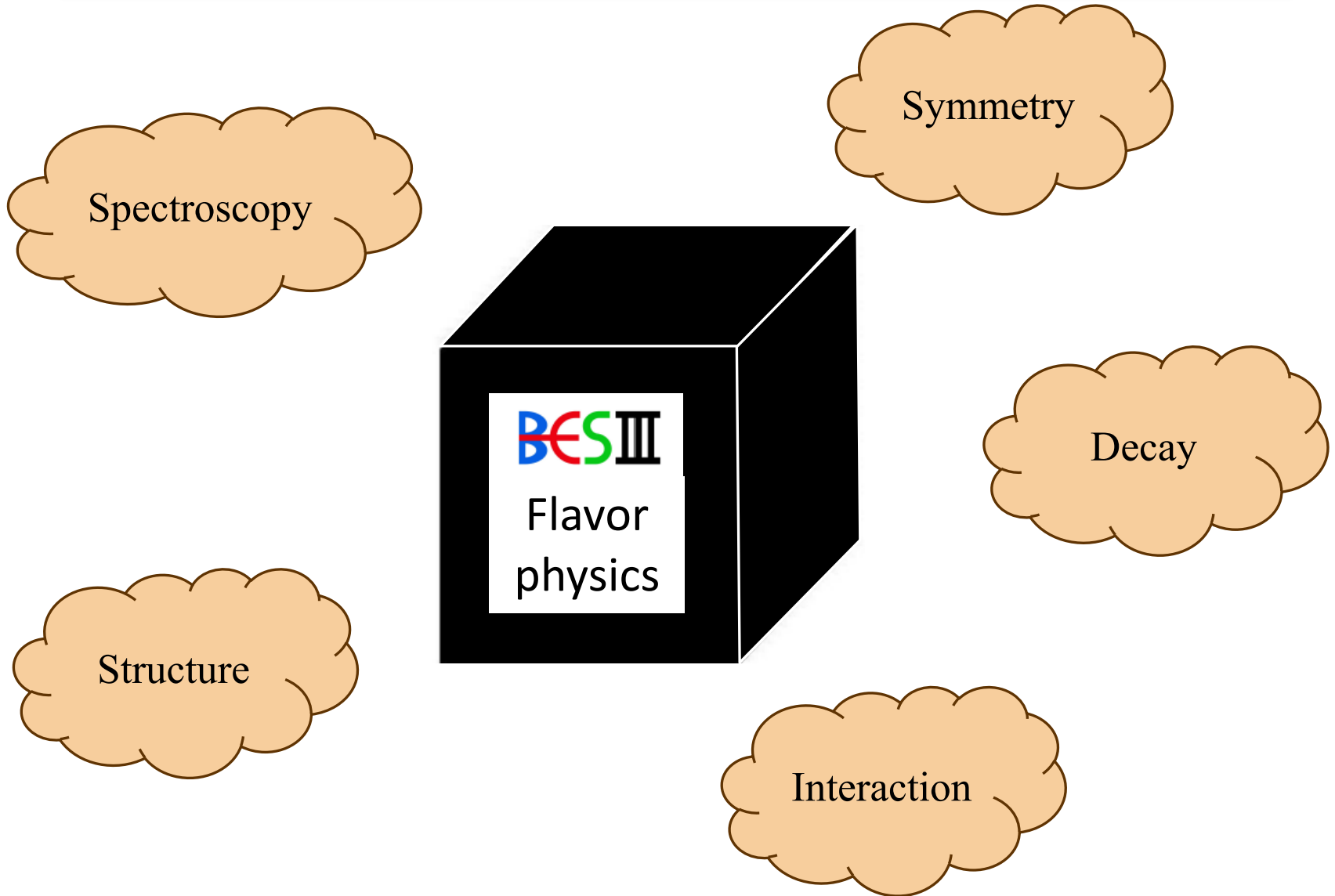


- Charmonium physics
- Light hadron physics
- Charm physics
- R-QCD physics
- New physics

BESIII: $\sim 55 \text{ fb}^{-1}$ data in $E_{\text{cm}} = 2 \sim 4.95 \text{ GeV}$

World largest data sample directly collected in the τ -charm region

BESIII flavor physics

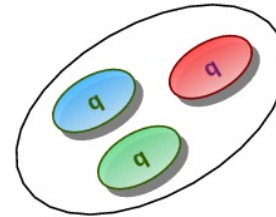


Spectroscopy

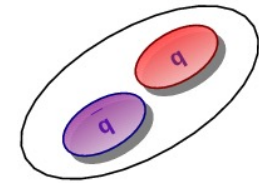
Ordinary vs exotic matter

- Conventional hadrons
- QCD allows for “exotics”

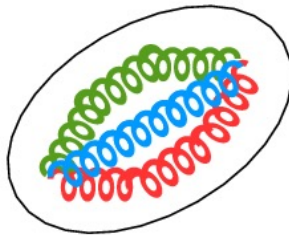
Baryon



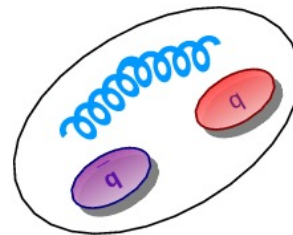
Meson



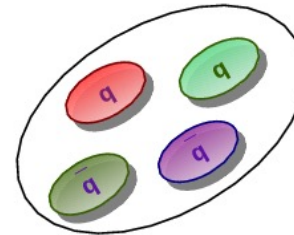
Glueball



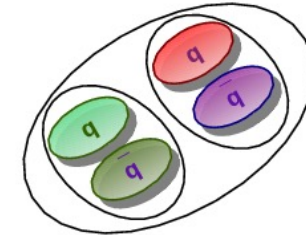
Hybrid



Tetraquark

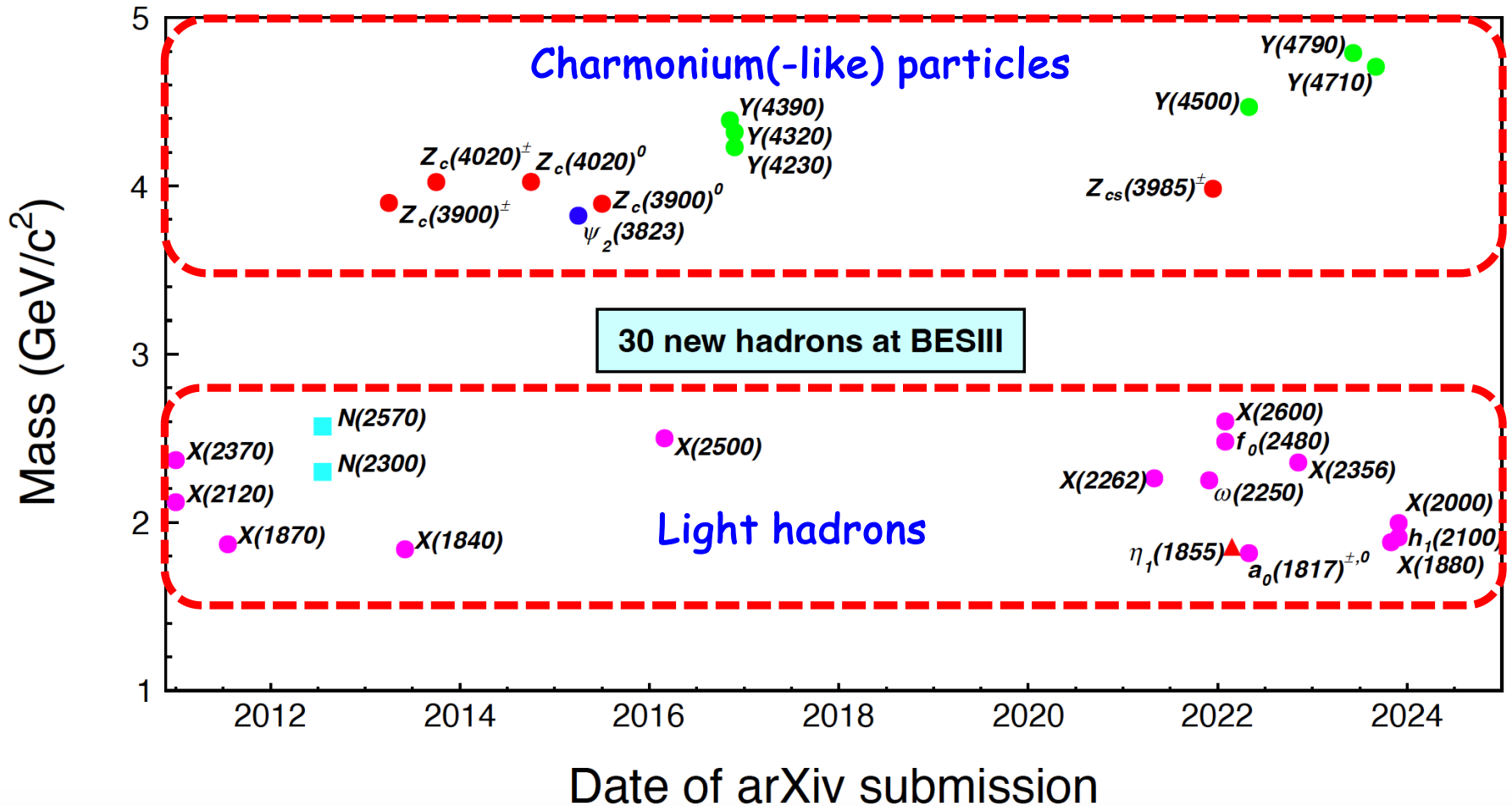


Hadronic Molecule



- Searching for those states provides test of QCD

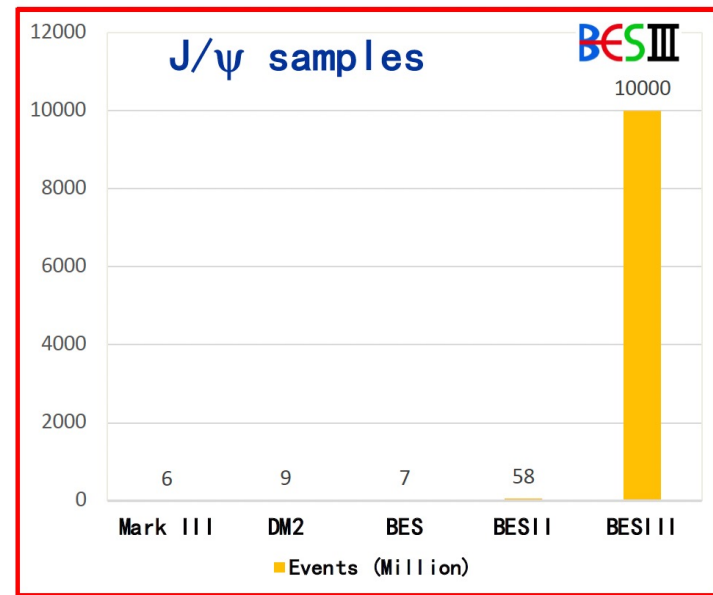
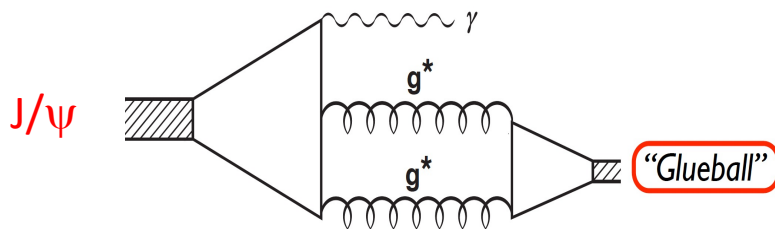
New resonant structures at BESIII



Glueball searches

- **Two big issues**

- What is the production mechanism to utilize?
- What is the mixing with quark model mesons?



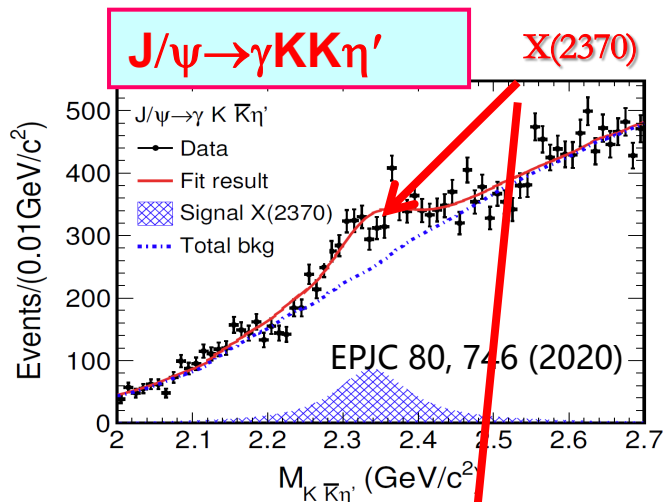
- Production rate could be calculable in LQCD, but the manifestation of a "glueball" can be tricky!

Chanowitz, Phys.Rev.Lett. 95(2005)172001

Systematic studies needed

- Outnumbering of conventional QM states
- Abnormal properties ? Eg., small production rate in two photon process

Glueball candidate



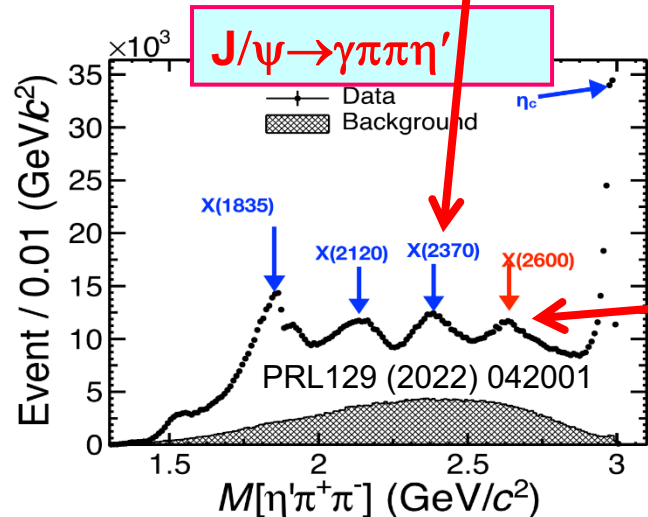
X(2370) and X(2600): new glueball candidate ?

An updated review of the new hadron states

6	Glueballs and light hybrid mesons	91
6.1	Glueballs	92
6.1.1	Lattice QCD and QCD sum rule calculations.	93
6.1.2	Scalar glueballs and the $f_0(1500)/f_0(1710)$	95
6.1.3	Tensor glueballs and the $f_2(2340)$	100
6.1.4	Pseudoscalar glueballs and the X(2370).	101

H.X.Chen, W.Chen, X.Liu, Y.R. Liu, S.L. Zhu *Rept.Prog.Phys.* 86 (2023) 2, 026201

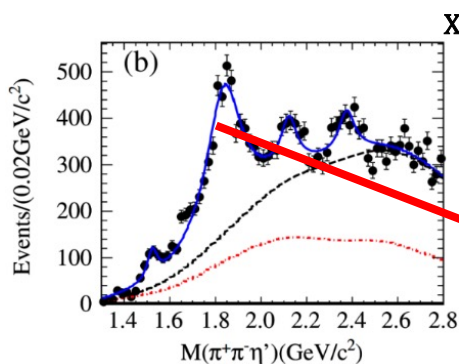
Motivated by the newly observed resonance X(2600) by BESIII Collaboration, we examine the triguon glueball interpretation for it in the framework of QCD sum rules. We evaluate the mass spectra of the triguon glueballs with quantum numbers 0^{-+} and 2^{-+} up to dimension 8 condensate in the operator product expansion. Our numerical results indicate that the mass of the 2^{-+} triguon glueball is about 2.66 ± 0.06 GeV, which is consistent with the mass of the X(2600) within the uncertainties, while 0^{-+} has a mass of 2.01 ± 0.14 GeV. The possible decay channels of the 2^{-+} state are analyzed, which are crucial in decoding X(2600)'s internal structure and are hopefully measurable in BESIII, BELLEII, PANDA, and LHCb experiments.



QCD sum rules

S.Q. Zhang et al, *PRD* 106 (2022) 7, 074010

$X(p\bar{p})$: Baryonium state?



$X(1835)$ observed in $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$

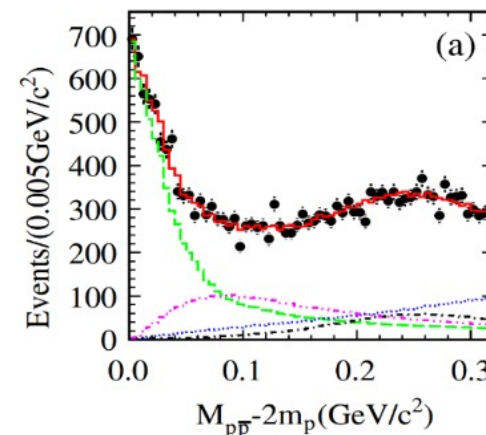
$X(1835) J^{PC}=0^{--+}$
$M = 1844 \pm 9^{+16}_{-25} \text{ MeV}/c^2$
$\Gamma = 192^{+20+62}_{-17-43} \text{ MeV}/c^2$

PRL 106, 072002 (2011)

$X(p\bar{p})$ observed in $J/\psi \rightarrow \gamma p\bar{p}$

$X(p\bar{p}) J^{PC}=0^{--+}$
$M = 1832^{+19+18}_{-5-17} \pm 19 \text{ MeV}/c^2$
$\Gamma = 13 \pm 19 \text{ MeV}/c^2$ ($< 76 \text{ MeV}/c^2$ @ 90% C.L.)

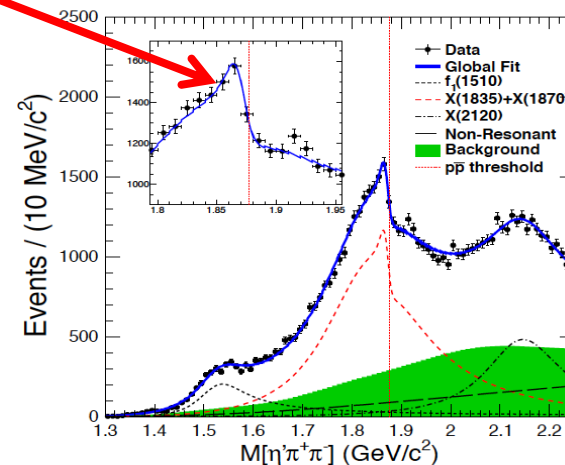
PRL 108, 112003 (2012)



connection between $X(1835)$ and $X(p\bar{p})$

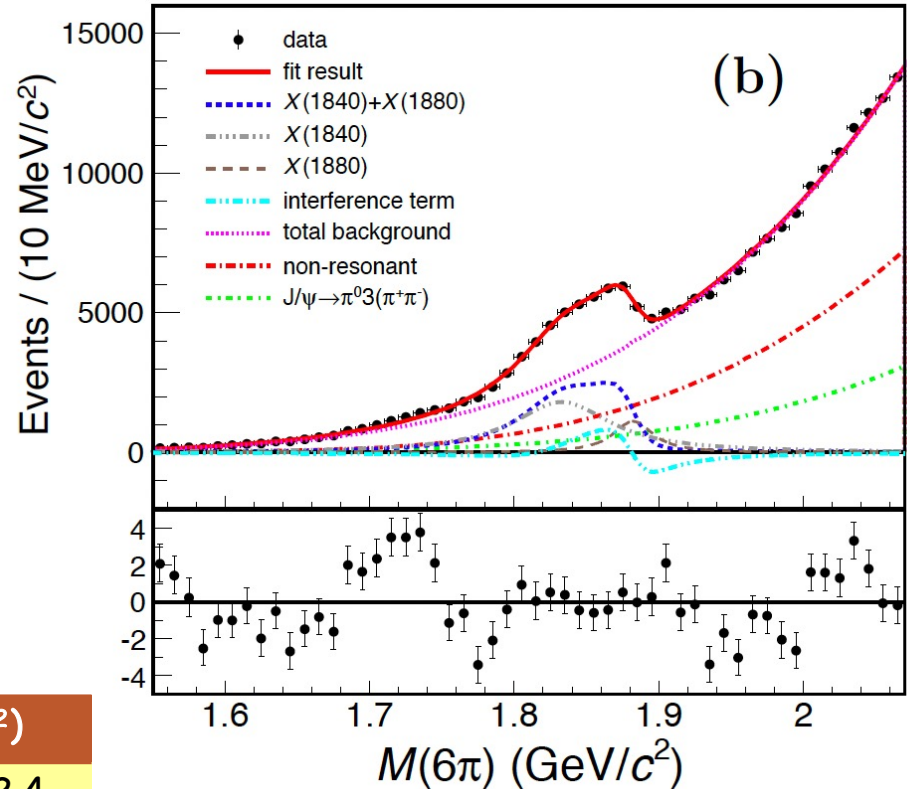
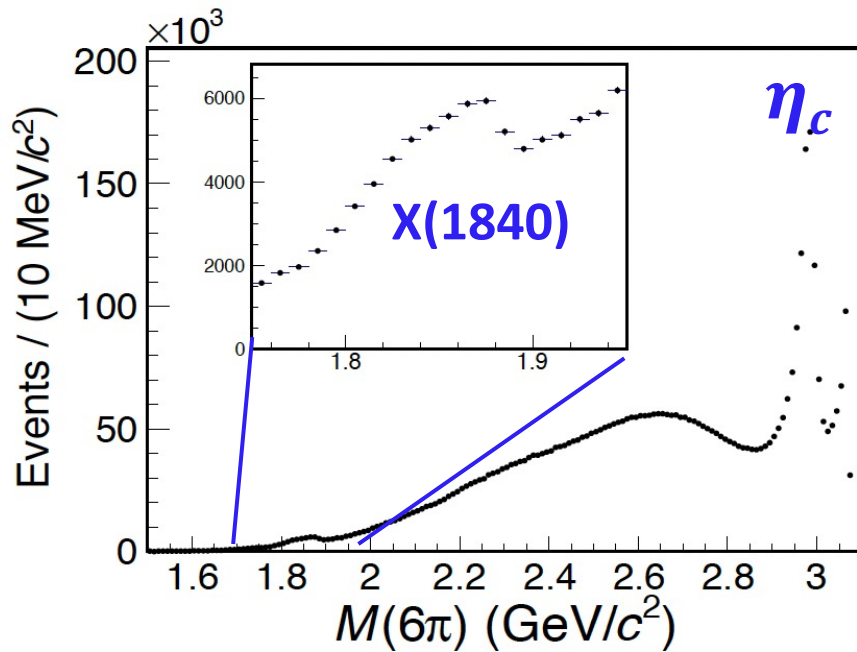
The anomalous line shape :

- Suggest the existence of a state, either a broad state with strong couplings to $p\bar{p}$, or a narrow state just below the $p\bar{p}$ mass threshold
- the existence of a $p\bar{p}$ molecule-like state or bound state?



PRL 117, 042002 (2016)

A narrow state around $p\bar{p}$ threshold

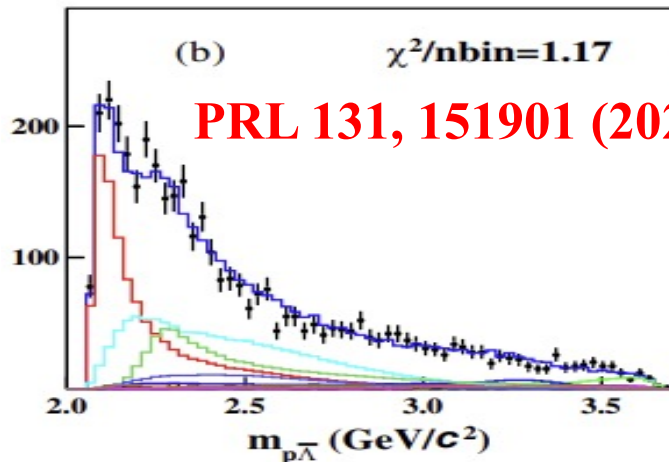
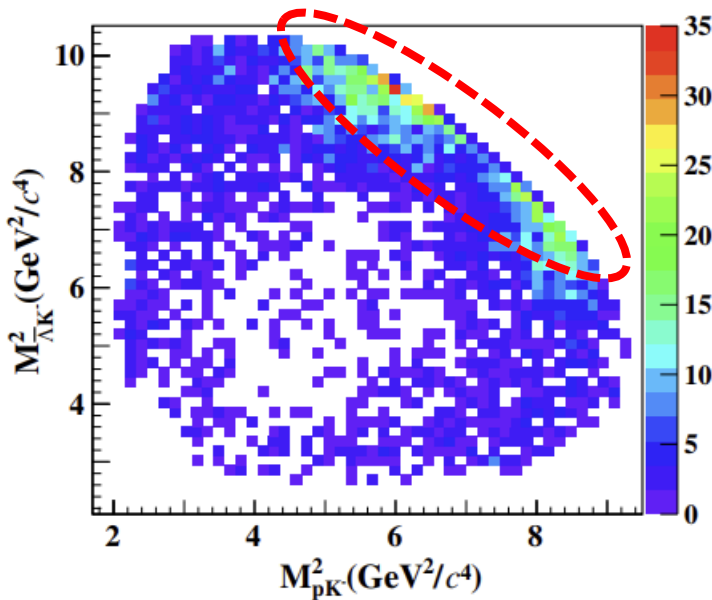


Resonance	M (MeV/c ²)	Γ (MeV/c ²)
X(1880)	1882.1±1.7±0.7	30.7±5.5±2.4
X(1840)	1832.5±3.1±2.5	80.7±5.2±7.7

PRL 132, 151904 (2024)

Support the existence of $p\bar{p}$ bound state !

A narrow state around $p\bar{\Lambda}$ threshold



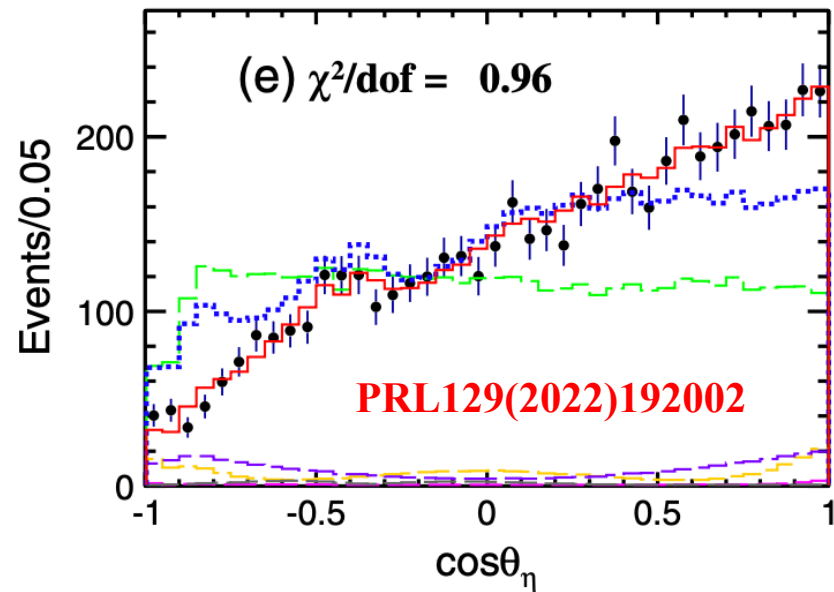
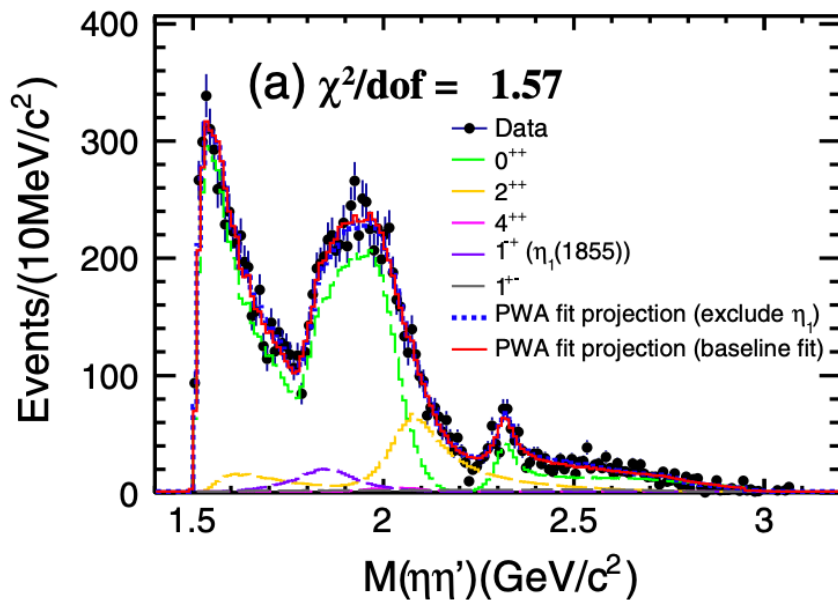
\sqrt{s}	\mathcal{L}_{int}	M_{pole}	Γ_{pole}
4.008	482.0 ± 4.7	2082_{-9}^{+13}	56_{-14}^{+15}
4.178	3189.0 ± 31.9	2083_{-4}^{+6}	63_{-7}^{+8}
4.226	1100.9 ± 7.0	2086_{-8}^{+11}	71_{-13}^{+15}
4.258	828.4 ± 5.5	2081_{-6}^{+9}	52_{-9}^{+10}
4.416	1090.7 ± 7.2	2085_{-7}^{+10}	59_{-9}^{+11}
4.682	1669.3 ± 9.0	2090_{-7}^{+9}	55_{-5}^{+8}
Average	—	2084_{-2}^{+4}	58_{-3}^{+4}

A narrow structure in the $p\bar{\Lambda}$ system, named as $X(2085)$, is observed with greater than 20σ , J^P is determined to be 1^+ , pole position is:

$$M_{\text{pole}} = (2084_{-2}^{+4} \pm 9) \text{ MeV}/c^2$$

$$\Gamma_{\text{pole}} = (58_{-3}^{+4} \pm 25) \text{ MeV}$$

Observation of 1^{-+} $\eta_1(1885)$ in $J/\psi \rightarrow \gamma \eta \eta'$



Isoscalar state with exotic quantum numbers $J^{PC}=1^{-+}$

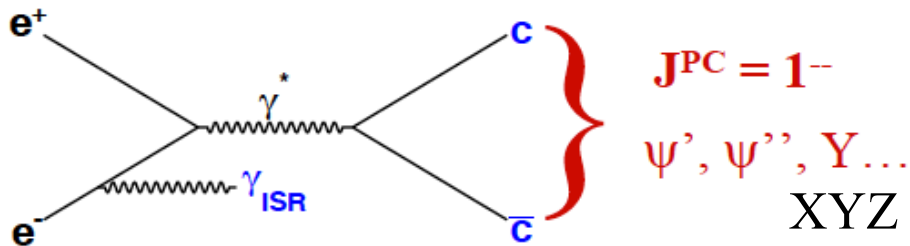
Critical to establish the 1^{-+} spectroscopy !

More works in progress for establishing the state with $I=1$

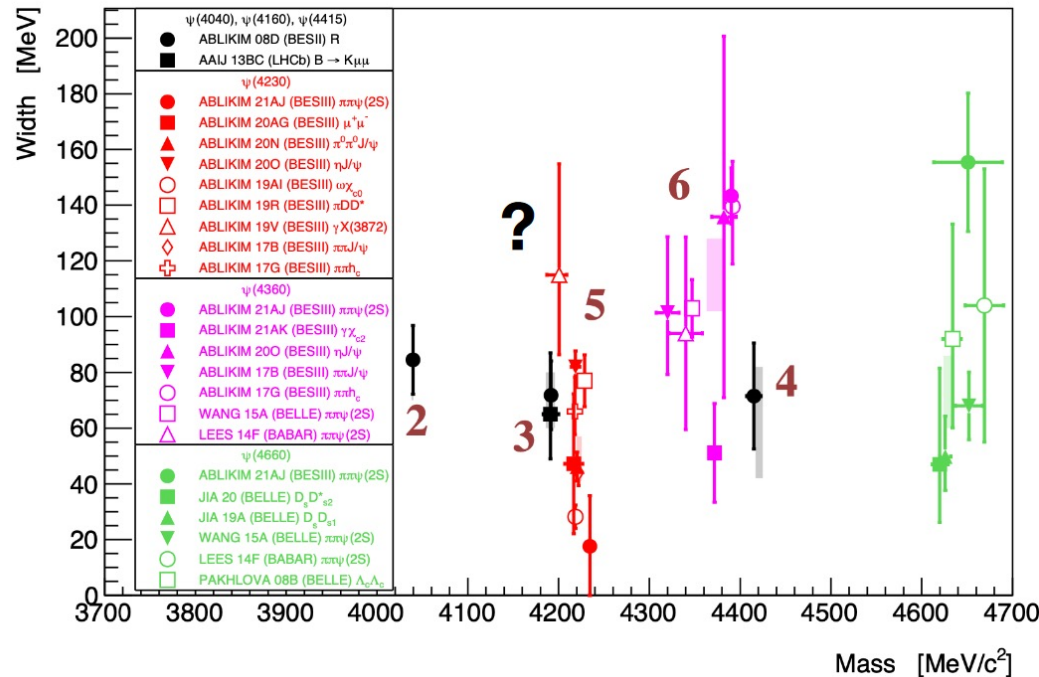
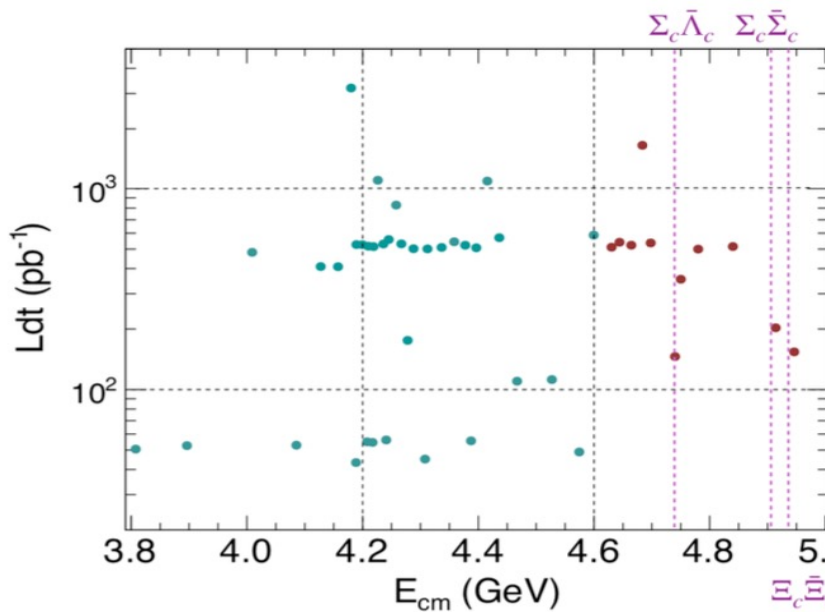
$$M = 1855 \pm 9_{-1}^{+6} \text{ MeV}/c^2$$

$$\Gamma = 188 \pm 18_{-8}^{+3} \text{ MeV}$$

Charmonium(-like) states



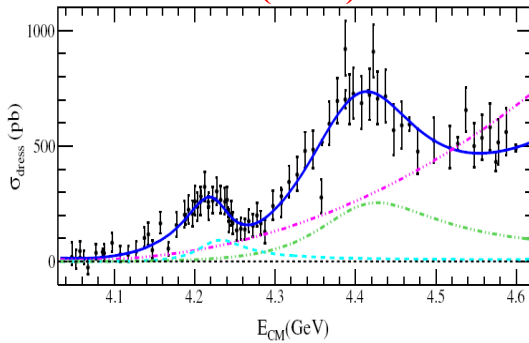
XYZ studies with $\sim 25 \text{ fb}^{-1}$ data above 3.8 GeV



Fine structure of $Y(4260) \rightarrow Y(4220) + Y(4320)$?

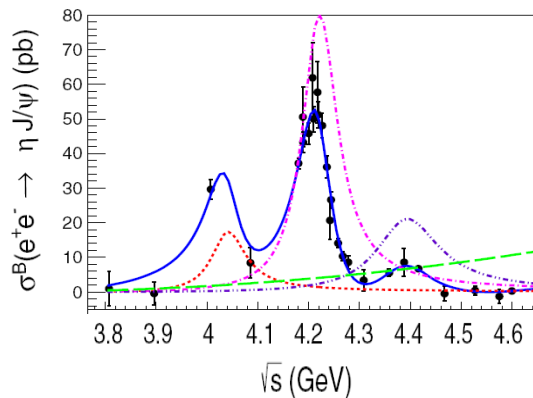
$$e^+e^- \rightarrow \pi^+ D^0 D^{*-} + \text{c.c.}$$

PRL122(2019)102002



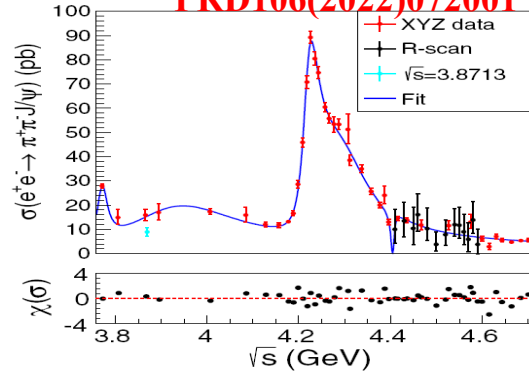
$$e^+e^- \rightarrow \eta J/\psi$$

PRD102(2020)031101(RC)



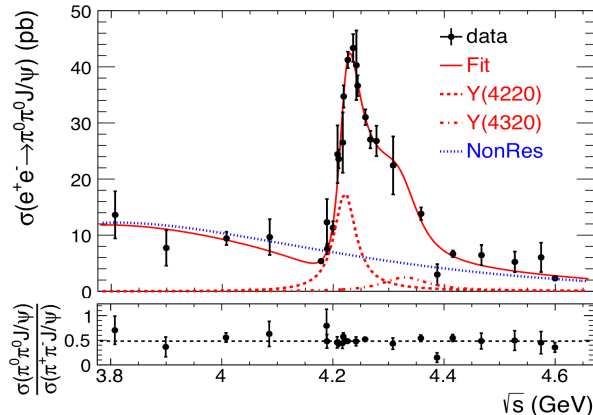
$$e^+e^- \rightarrow \pi^+ \pi^- J/\psi$$

PRD106(2022)072001

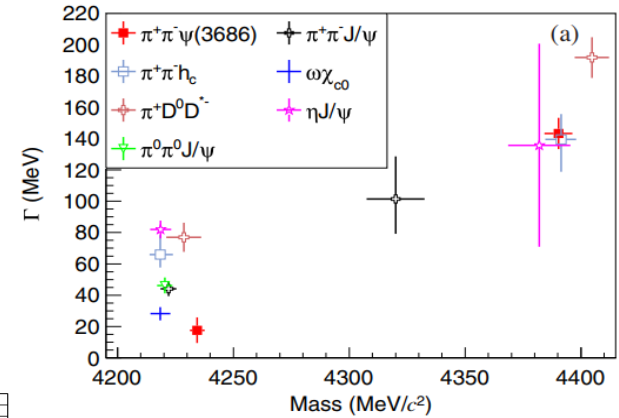


$$e^+e^- \rightarrow \pi^0 \pi^0 J/\psi$$

PRD102(2020)012009

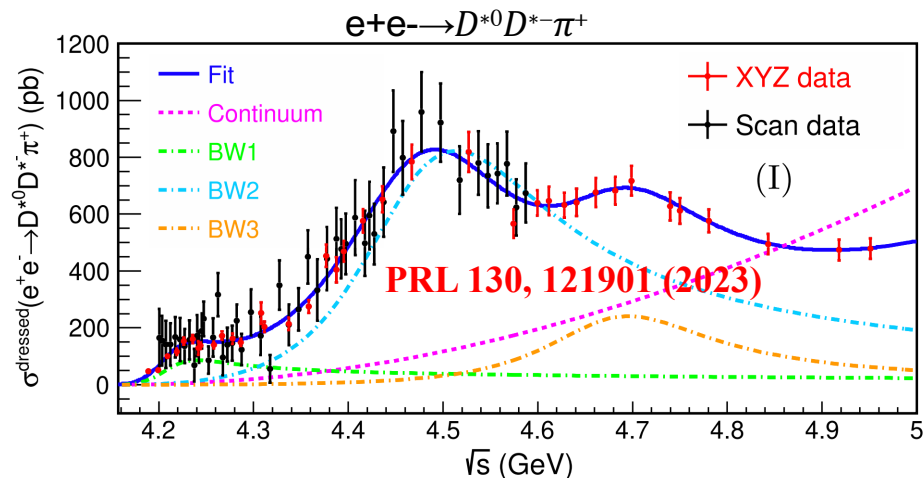
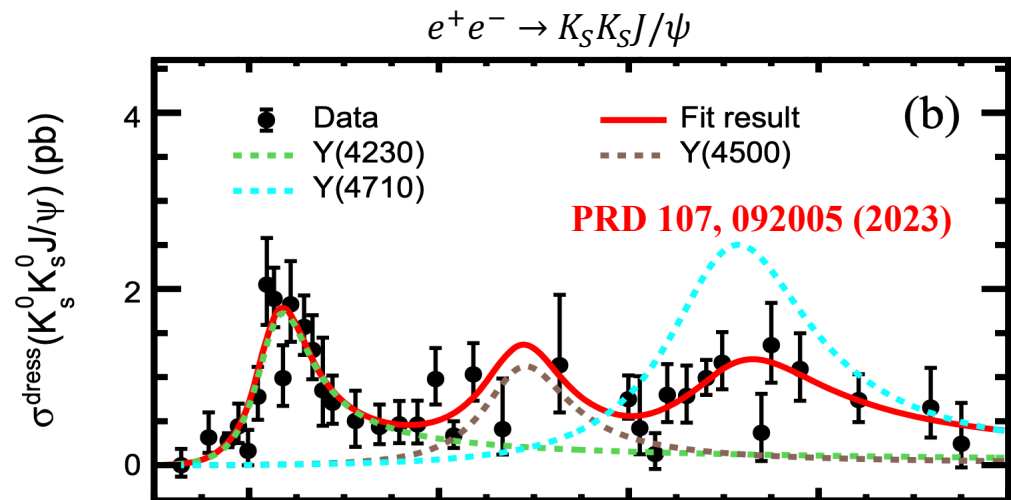
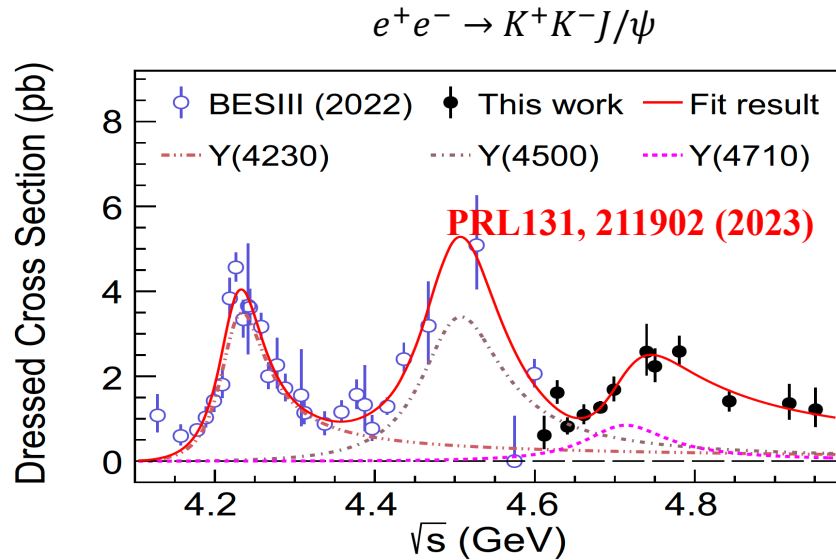


Different masses and widths in various processes



Mass $\sim 4220 \text{ MeV}/c^2$
width $\sim 50 \text{ MeV}$

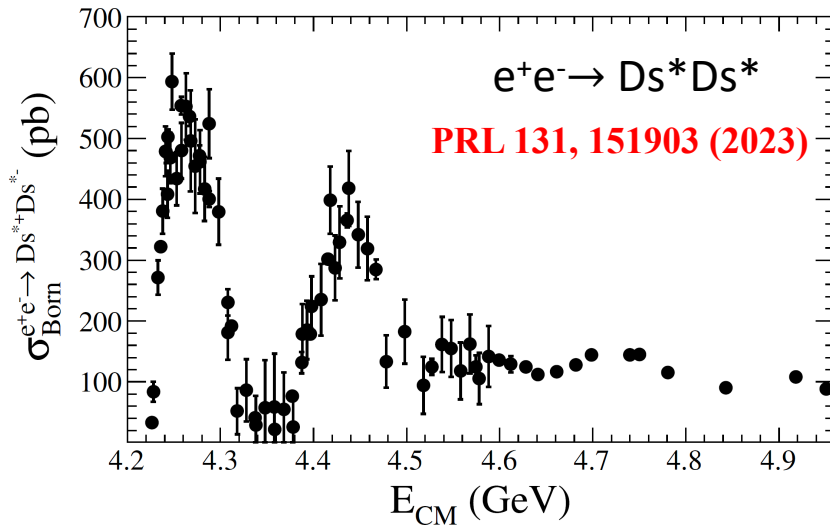
Observations of Y(4230), Y(4500) and Y(4710)



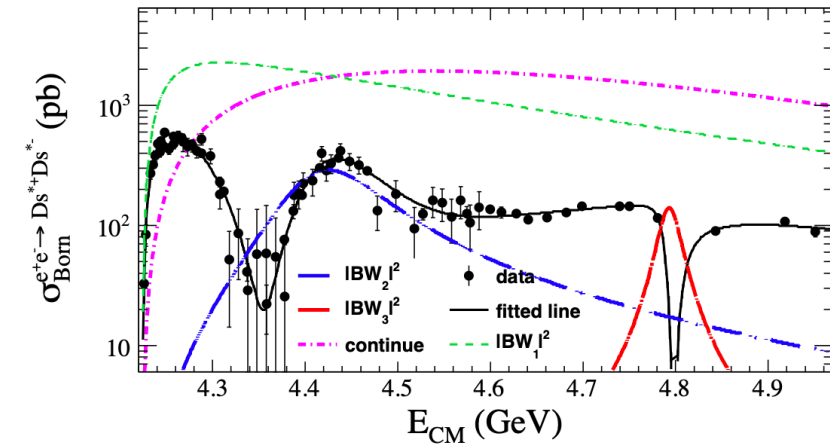
- New decay mode of Y(4230)
- Confirmation of Y(4500)
- Y(4710): one of the heaviest vector charmonium-like state, hybrid, 5S charmonium, 5S-4D/6S-5D mixing?

Mass ~ 4710 MeV/ c^2 , Width ~ 180 MeV

Observation of a new charmonium-like state Y(4790)

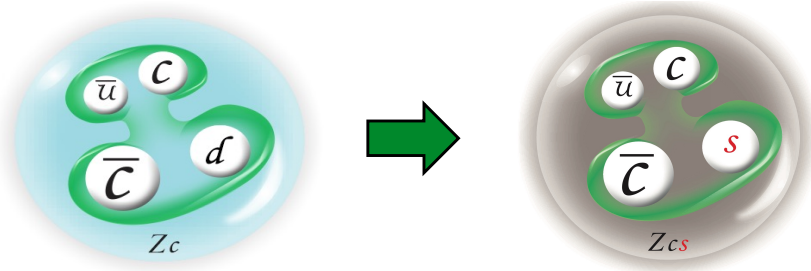


	Result 1	Result 2	Result 3
M_1 (MeV/ c^2)	4186.5 ± 9.0	4193.8 ± 7.5	4195.3 ± 7.5
Γ_1 (MeV)	55 ± 17	61.2 ± 9.0	61.8 ± 9.0
M_2 (MeV/ c^2)	4414.5 ± 3.2	4412.8 ± 3.2	4411.0 ± 3.2
Γ_2 (MeV)	122.6 ± 7.0	120.3 ± 7.0	120.0 ± 7.0
M_3 (MeV/ c^2)	4793.3 ± 7.5	4789.8 ± 9.0	4786 ± 10
Γ_3 (MeV)	27.1 ± 7.0	41 ± 39	60 ± 35



- Y(4160) or Y(4260) [strong coupling to $D_s^*D_s^*$?]
- Consistent with Y(4415)
- Y(4790): necessary to improve fit quality ($>6\sigma$)

Observation of $Z_{cs}(3985)$

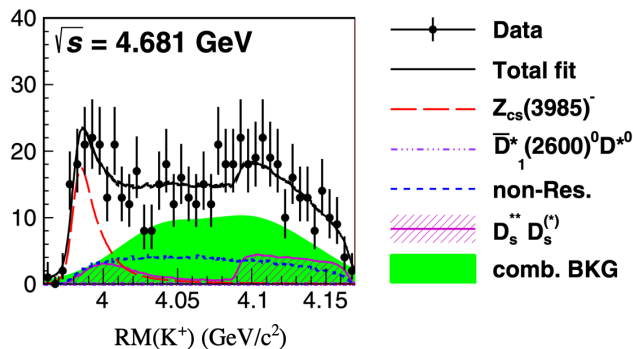


$$e^+e^- \rightarrow K^+K^-J/\psi$$

Given tetraquark state assumption, there should exist SU(3) partner Z_{cs} state with strangeness

$$e^+e^- \rightarrow K^+(D_s^-D^{*0} + D_s^{*-}D^0)$$

PRL126(2021)102001

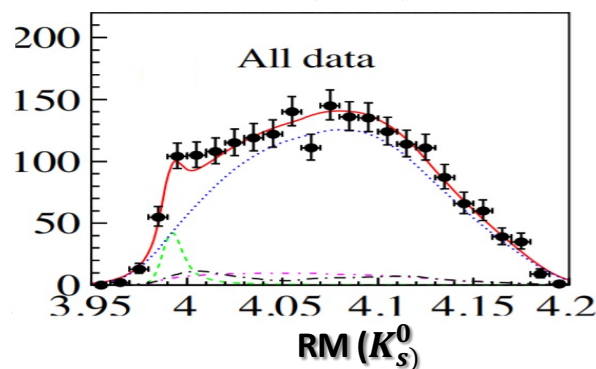


$$\text{M} = (3985.2^{+2.1}_{-2.0} \pm 1.7) \text{ MeV}/c^2$$

$$\text{M} = (13.8^{+8.1}_{-5.2} \pm 4.9) \text{ MeV}$$

$$e^+e^- \rightarrow K_s^0(D_s^+D^{*-} + D_s^{*+}D^-)$$

PRL129(2022)112003

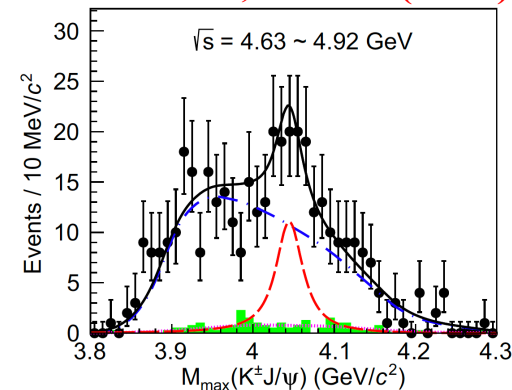


$$\text{M} = 3992.2 \pm 1.7 \pm 1.6 \text{ MeV}/c^2$$

$$\text{M} = (7.7^{+4.1}_{-3.8} \pm 4.3) \text{ MeV}$$

$$e^+e^- \rightarrow K^+K^-J/\psi$$

PRL131, 211902 (2023)



Not significant !

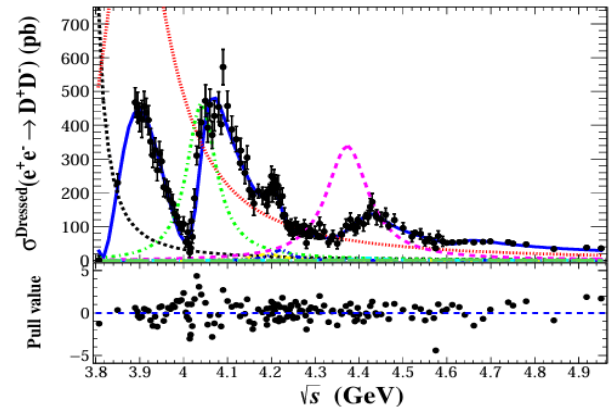
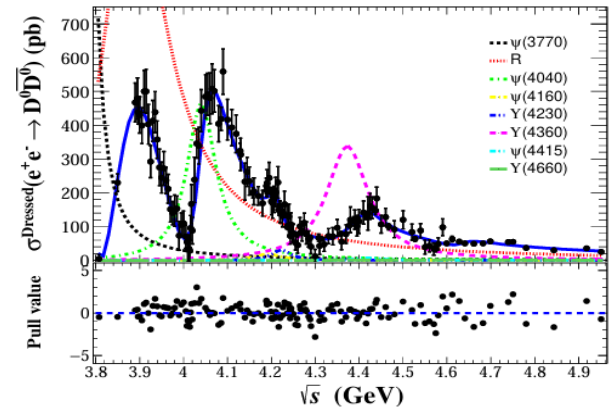
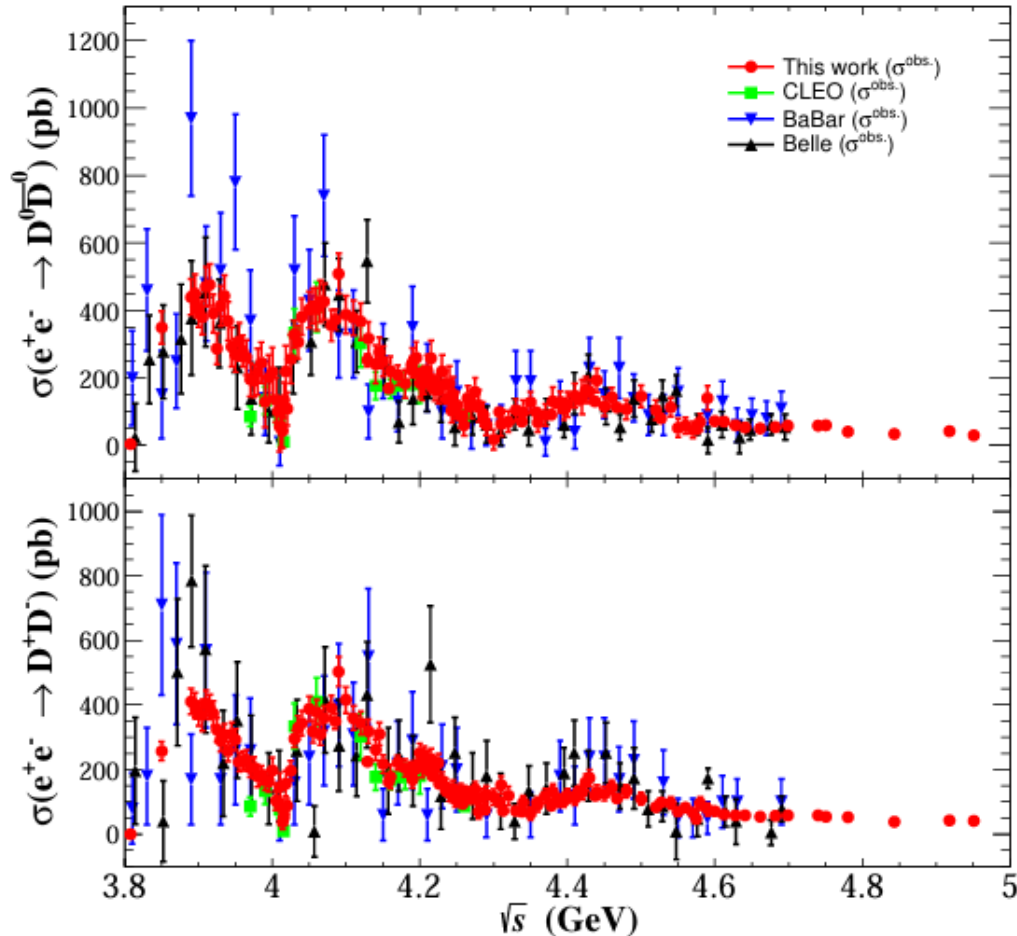
Close mass but very different widths for $Z_{cs}(4000)$ at LHCb !

LHCb: PRL127, 082001 (2021)

Observation of a new structure around 3.9 GeV/c²

Cross section of $e^+e^- \rightarrow D^+D^-/D^0\bar{D}^0$:

[arXiv:2402.03829](https://arxiv.org/abs/2402.03829)



Resonance	R
Mass (MeV/c ²)	$3872.5 \pm 14.2 \pm 3.0$
Width (MeV/c ²)	$179.7 \pm 14.1 \pm 7.0$
$\Gamma_{ee}\mathcal{B}$ (eV)	202-292
$S(\sigma)$	> 20

Recent studies on the Λ_c^+ measurements at BESIII

- Λ_c^+ leptonic decays
 - $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e, \Lambda \mu^+ \nu_\mu$: PRL 129.231803 (2022). PRD 108.L031105 (2023).
 - $\Lambda_c^+ \rightarrow p K^- e^+ \nu_e$: PRD 106.112010 (2022).
 - $\Lambda_c^+ \rightarrow X e^+ \nu_e$: PRD 107.052005 (2023).
 - $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^- e^+ \nu_e, p K_S^0 \pi^- e^+ \nu_e$: PLB 843.137993 (2023).
- Λ_c^+ hadronic decays (two body)
 - $\Lambda_c^+ \rightarrow n \pi^+$: PRL 128.142001 (2022).
 - $\Lambda_c^+ \rightarrow p \eta'$: PRD 106.072002 (2022).
 - $\Lambda_c^+ \rightarrow p \eta, p \omega$: JHEP 11.137 (2023).
 - $\Lambda_c^+ \rightarrow p \pi^0, p \eta$: arXiv2311.06883.
 - $\Lambda_c^+ \rightarrow \Lambda K^+$: PRD 106.L111101 (2022).
 - $\Lambda_c^+ \rightarrow \Sigma^0 K^+, \Sigma^+ K_S^0$: PRD 106.052003 (2022).
 - $\Lambda_c^+ \rightarrow \Xi^0 K^+$: PRL 132.031801(2024) ✓
- Λ_c^+ hadronic decays (multi-body)
 - $\Lambda_c^+ \rightarrow n \pi^+ \pi^0, n \pi^+ \pi^- \pi^+, n K^- \pi^+ \pi^+$: CPC 47.023001 (2023).
 - $\Lambda_c^+ \rightarrow n K_S^0 \pi^+, n K_S^0 K^+$: arXiv2311.17131.
 - $\bar{\Lambda}_c^- \rightarrow \bar{n} X$: PRD 108.L031101 (2023).
 - $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^0$: JHEP 12.033 (2022).
 - $\Lambda_c^+ \rightarrow \Lambda K^+ \pi^0, \Lambda K^+ \pi^+ \pi^-$: arXiv2311.12903.
 - $\Lambda_c^+ \rightarrow \Sigma^- K^+ \pi^+$: arXiv2309.05484.
 - $\Lambda_c^+ \rightarrow \Xi^0 K^+ \pi^0$: arXiv2311.02347.

Decay asymmetry for pure W-exchange process $\Lambda_c^+ \rightarrow \Xi^0 K^+$

PRL 132, 031801 (2024)

Theory or experiment	$\mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$ ($\times 10^{-3}$)	$\alpha_{\Xi^0 K^+}$	$ A $ ($\times 10^{-2} G_F \text{ GeV}^2$)	$ B $ ($\times 10^{-2} G_F \text{ GeV}^2$)	$\delta_p - \delta_s$ (rad)
Körner (1992), CCQM [7]	2.6	0	-	-	-
Xu (1992), Pole [8]	1.0	0	0	7.94	-
Żencaykowski (1994), Pole [9]	3.6	0	-	-	-
Ivanov (1998), CCQM [10]	3.1	0	-	-	-
Sharma (1999), CA [11]	1.3	0	-	-	-
Geng (2019), SU(3) [12]	5.7 ± 0.9	$0.94^{+0.06}_{-0.11}$	2.7 ± 0.6	16.1 ± 2.6	-
Zou (2020), CA [5]	7.1	0.90	4.48	12.10	-
Zhong (2022), SU(3) ^a [13]	$3.8^{+0.4}_{-0.5}$	$0.91^{+0.03}_{-0.04}$	3.2 ± 0.2	$8.7^{+0.6}_{-0.8}$	-
Zhong (2022), SU(3) ^b [13]	$5.0^{+0.6}_{-0.9}$	0.99 ± 0.01	$3.3^{+0.5}_{-0.7}$	$12.3^{+1.2}_{-1.8}$	-
BESIII (2018) [14]	$5.90 \pm 0.86 \pm 0.39$	-	-	-	-
PDG Fit (2022) [3]	5.5 ± 0.7	-	-	-	-

- $\Lambda_c^+ \rightarrow \Xi^0 K^+$ is pure W-exchange process which have significant contributions in charmed baryon decay.
- Nonfactorizable W-exchange diagram cannot be calculated using theoretical approaches.
- Long-standing puzzle on how large the S-wave amplitude.
- Experimental measurement of decay asymmetry is crucial and urgent.

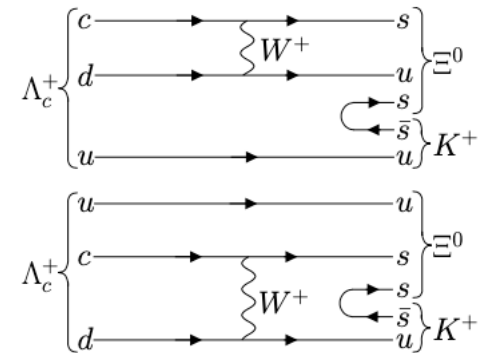


FIG. 1. Feynman diagrams for $\Lambda_c^+ \rightarrow \Xi^0 K^+$

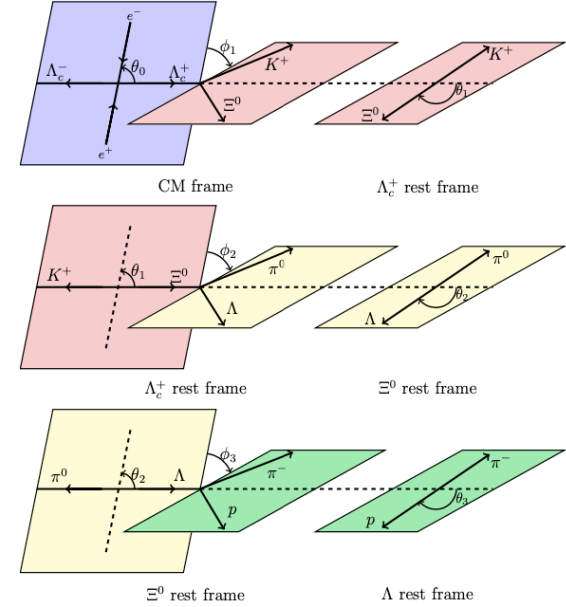
Decay asymmetry for pure W-exchange process $\Lambda_c^+ \rightarrow \Xi^0 K^+$

$$\alpha_{BP} = \frac{2\text{Re}(s^*p)}{|s|^2 + |p|^2}, \quad \beta_{BP} = \frac{2\text{Im}(s^*p)}{|s|^2 + |p|^2}, \quad \gamma_{BP} = \frac{|s|^2 - |p|^2}{|s|^2 + |p|^2},$$

PRL 132, 031801 (2024)

Level	Decay	Helicity angle	Helicity amplitude
0	$e^+e^- \rightarrow \Lambda_c^+(\lambda_1)\bar{\Lambda}_c^-(\lambda_2)$	(θ_0)	A_{λ_1,λ_2}
1	$\Lambda_c^+ \rightarrow \Xi^0(\lambda_3)K^+$	(θ_1,ϕ_1)	B_{λ_3}
2	$\Xi^0 \rightarrow \Lambda(\lambda_4)\pi^0$	(θ_2,ϕ_2)	C_{λ_4}
3	$\Lambda \rightarrow p(\lambda_5)\pi^-$	(θ_3,ϕ_3)	D_{λ_5}

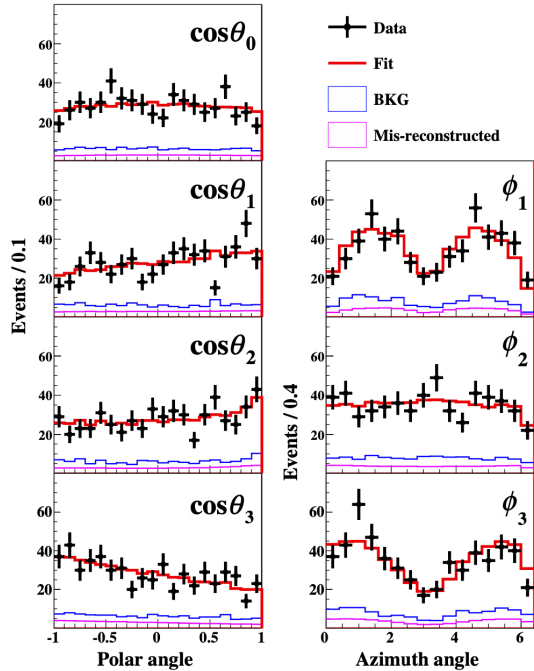
$$\begin{aligned} & \frac{d\Gamma}{d\cos\theta_0 d\cos\theta_1 d\cos\theta_2 d\cos\theta_3 d\phi_1 d\phi_2 d\phi_3} \\ & \propto 1 + \alpha_0 \cos^2 \theta_0 \\ & + (1 + \alpha_0 \cos^2 \theta_0) \alpha_{\Xi^0 K^+} + \alpha_{\Lambda\pi^0} \cos \theta_2 \\ & + (1 + \alpha_0 \cos^2 \theta_0) \alpha_{\Xi^0 K^+} + \alpha_{p\pi^-} \cos \theta_2 \cos \theta_3 \\ & + (1 + \alpha_0 \cos^2 \theta_0) \alpha_{\Lambda\pi^0} \alpha_{p\pi^-} \cos \theta_3 \\ & - (1 + \alpha_0 \cos^2 \theta_0) \alpha_{\Xi^0 K^+} + \sqrt{1 - \alpha_{\Lambda\pi^0}^2} \alpha_{p\pi^-} \sin \theta_2 \sin \theta_3 \cos(\Delta_{\Lambda\pi^0} + \phi_3) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \alpha_{\Xi^0 K^+} + \sin \theta_1 \sin \phi_1 \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \alpha_{\Lambda\pi^0} \sin \theta_1 \sin \phi_1 \cos \theta_2 \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \alpha_{\Xi^0 K^+} + \alpha_{\Lambda\pi^0} \alpha_{p\pi^-} \sin \theta_1 \sin \phi_1 \cos \theta_3 \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \alpha_{p\pi^-} - \sin \theta_1 \sin \phi_1 \cos \theta_2 \cos \theta_3 \\ & - \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Lambda\pi^0}^2} \alpha_{p\pi^-} \sin \theta_1 \sin \phi_1 \sin \theta_2 \sin \theta_3 \cos(\Delta_{\Lambda\pi^0} + \phi_3) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \alpha_{\Lambda\pi^0} \cos \phi_1 \sin \theta_2 \sin(\Delta_{\Xi^0 K^+} + \phi_2) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \alpha_{\Lambda\pi^0} \cos \theta_1 \sin \phi_1 \sin \theta_2 \cos(\Delta_{\Xi^0 K^+} + \phi_2) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \alpha_{p\pi^-} \cos \theta_1 \sin \phi_1 \sin \theta_2 \cos(\Delta_{\Xi^0 K^+} + \phi_2) \cos \theta_3 \\ & - \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \sqrt{1 - \alpha_{\Lambda\pi^0}^2} \alpha_{p\pi^-} \cos \theta_1 \sin \phi_1 \sin(\Delta_{\Xi^0 K^+} + \phi_2) \sin \theta_3 \sin(\Delta_{\Lambda\pi^0} + \phi_3) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \sqrt{1 - \alpha_{\Lambda\pi^0}^2} \alpha_{p\pi^-} \cos \theta_1 \sin \phi_1 \cos \theta_2 \cos(\Delta_{\Xi^0 K^+} + \phi_2) \sin \theta_3 \cos(\Delta_{\Lambda\pi^0} + \phi_3) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \sqrt{1 - \alpha_{\Lambda\pi^0}^2} \alpha_{p\pi^-} \cos \phi_1 \cos(\Delta_{\Xi^0 K^+} + \phi_2) \sin \theta_3 \sin(\Delta_{\Lambda\pi^0} + \phi_3) \\ & + \sqrt{1 - \alpha_0^2} \sin \Delta_0 \sin \theta_0 \cos \theta_0 \sqrt{1 - \alpha_{\Xi^0 K^+}^2} \sqrt{1 - \alpha_{\Lambda\pi^0}^2} \alpha_{p\pi^-} \cos \phi_1 \cos \theta_2 \sin(\Delta_{\Xi^0 K^+} + \phi_2) \sin \theta_3 \cos(\Delta_{\Lambda\pi^0} + \phi_3) \end{aligned}$$



- The joint angular distribution for $\Lambda_c^+ \rightarrow \Xi^0 K^+$ is derived based on helicity amplitude.

Decay asymmetry for pure W-exchange process $\Lambda_c^+ \rightarrow \Xi^0 K^+$

PRL 132, 031801 (2024)



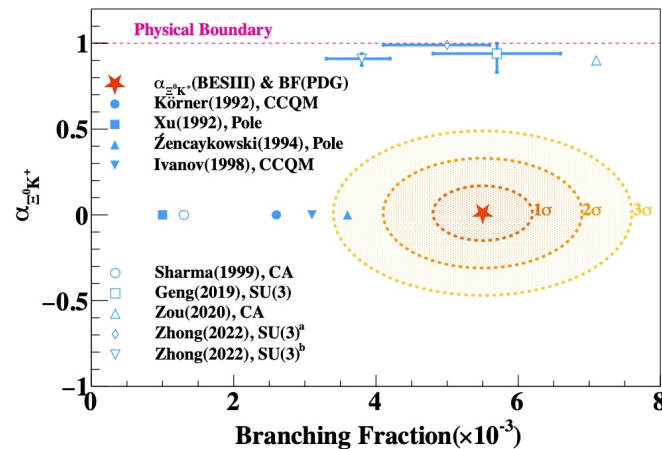
- From the fit, we obtain $\alpha_{\Xi^0 K^+} = 0.01 \pm 0.16_{stat} \pm 0.03_{syst}$ and $\beta_{\Xi^0 K^+} = -0.64 \pm 0.69_{stat} \pm 0.13_{syst}$ and $\gamma_{\Xi^0 K^+} = -0.77 \pm 0.58_{stat} \pm 0.11_{syst}$
- $\alpha_{\Xi^0 K^+}$ is in good agreement with zero \Rightarrow strong identification for theoretical predictions.

$$\Gamma = \frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)}{\tau_{\Lambda_c^+}} = \frac{|\vec{p}_c|}{8\pi} \left[\frac{(m_{\Lambda_c^+} + m_{\Xi^0})^2 - m_{K^+}^2}{m_{\Lambda_c^+}^2} |A|^2 + \frac{(m_{\Lambda_c^+} - m_{\Xi^0})^2 - m_{K^+}^2}{m_{\Lambda_c^+}^2} |B|^2 \right]$$

$$\alpha_{\Xi^0 K^+} = \frac{2\kappa|A||B|\cos(\delta_p - \delta_s)}{|A|^2 + \kappa^2|B|^2},$$

$$\Delta_{\Xi^0 K^+} = \arctan \frac{2\kappa|A||B|\sin(\delta_p - \delta_s)}{|A|^2 - \kappa^2|B|^2},$$

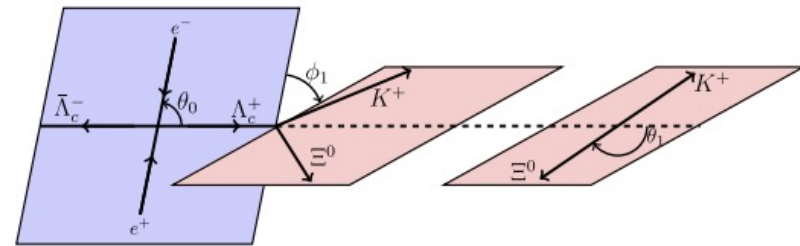
- Especially, $\cos(\delta_p - \delta_s)$ is measured to close to zero. \Rightarrow not considered in previous literature.
- Fills the long-standing puzzle on how to model $\alpha_{\Xi^0 K^+}$ and $\mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$ simultaneously.



Decay asymmetry parameter in $\Lambda_c^+ \rightarrow \Xi^0 K^+$

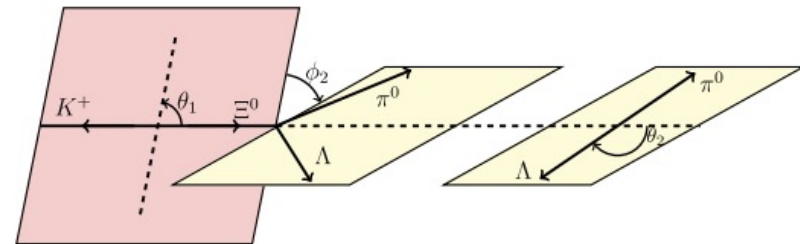
PRL 132, 031801 (2024)

- Helicity frame: W-boson-exchange decay:



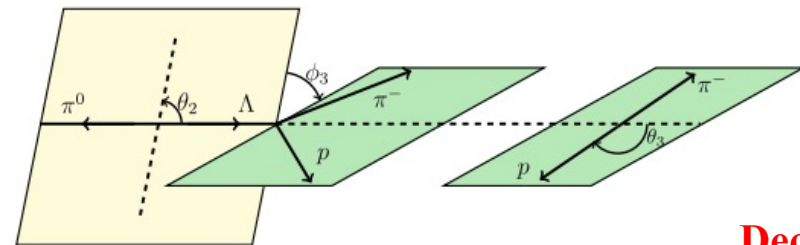
CM frame

Λ_c^+ rest frame



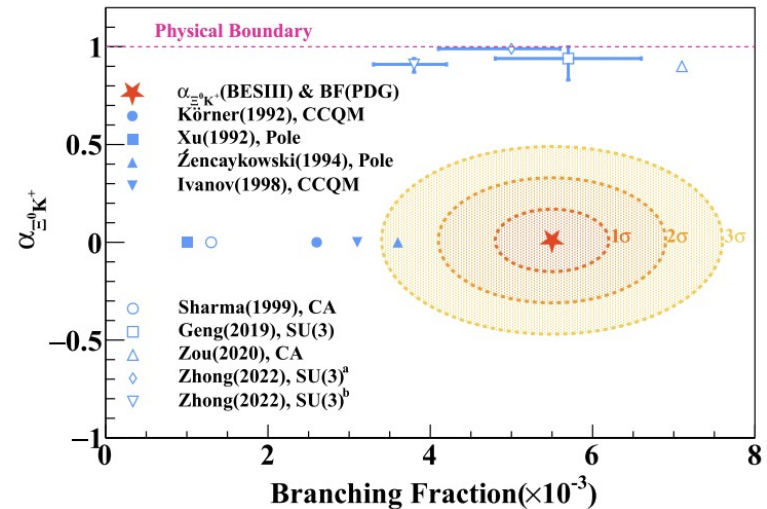
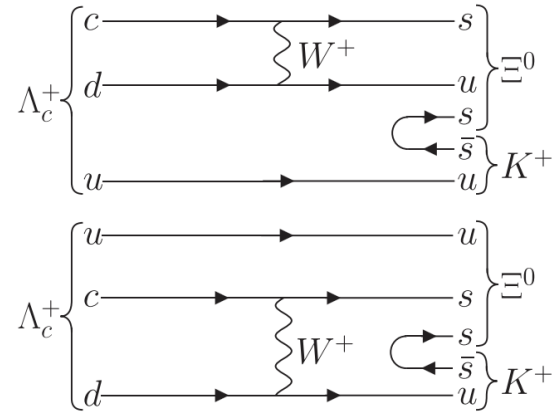
Λ_c^+ rest frame

Ξ^0 rest frame



Ξ^0 rest frame

Λ rest frame



Decay asymmetry parameter: $\alpha = 0.01 \pm 0.16 \pm 0.03$

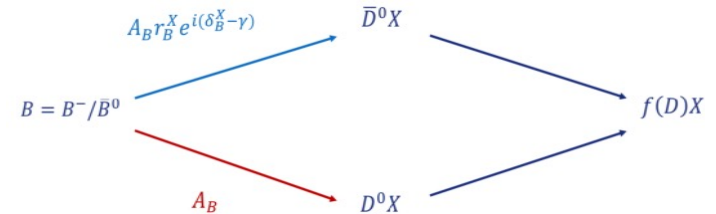
Phase between S and P wave: $\delta_P - \delta_S = -1.55 \pm 0.25 \pm 0.05, \text{ or } 1.59 \pm 0.25 \pm 0.05$

Recent studies on the charmed mesons at BESIII

- D^\pm, D^0, D_s^\pm purely leptonic decays
 - ▣ $D_s^{*+} \rightarrow e^+ \nu_e$: PRL 131, 141802 (2023).
 - ▣ $D_s^+ \rightarrow \mu^+ \nu_\mu$: PRD 108, 112001 (2023).
 - ▣ $D_s^+ \rightarrow \tau^+ \nu_\tau, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau$: JHEP 09, 124 (2023).
 - ▣ $D_s^+ \rightarrow \tau^+ \nu_\tau, \tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$: PRD 108, 092014 (2023).
- D^\pm, D^0, D_s^\pm semi-leptonic decays
 - ▣ $D_s^+ \rightarrow K_1(1270)/b_1(1235) e^+ \nu_e$: PRD 108, 112002 (2023).
 - ▣ $D_s^+ \rightarrow \eta(\eta') e^+ \nu_e$: PRD 108, 092003 (2023).
- D^\pm, D^0, D_s^\pm hadronic decays
 - ▣ $D^+ \rightarrow K_S^0 \pi^+ \pi^0 \pi^0$: JHEP 09, 077 (2023).
 - ▣ $D_s^+ \rightarrow \omega \pi^+ \eta$: PRD 107, 052010 (2023).
- D^\pm, D^0, D_s^\pm inclusive decays
 - ▣ $D^{+ / 0} \rightarrow K_S^0 X$: PRD 107, 112005 (2023).
 - ▣ $D^{+ / 0} \rightarrow \pi^+ \pi^+ \pi^- X$: PRD 107, 032002 (2023).
 - ▣ $D_s^+ \rightarrow \pi^+ \pi^+ \pi^- X$: PRD 108, 032001 (2023).
- Strong phase in D^\pm, D^0, D_s^\pm decays
 - ▣ $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$: PRD 108, 032003 (2023). ✓
 - ▣ $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$: PRD 107, 032009 (2023).
- Others
 - ▣ Determination of spin and parity of D_s^* : PLB 846, 138245 (2023). ✓
 - ▣ $D_s^* \rightarrow \gamma D_s$: PRD 107, 032011 (2023).

Strong phase in D^0 decays

- Determination of the CP-even fraction of $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$ [PRD 108, 032003 (2023)]



- The CKM unitarity angle $\gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$.
- The important source of CP violation for the quark sector.
- Search for indirect new physics.
- Test of CKM unitarity.

$$Y^\mp = h^\mp \int_{\mathbf{x} \in \mathcal{D}} \mathcal{P}(B^\mp(\mathbf{x})) d\mathbf{x}$$

$$= h^\mp \left[1 + r_B^2 + (2F_+^f - 1) 2r_B \cos(\delta_B \mp \gamma) \right]$$

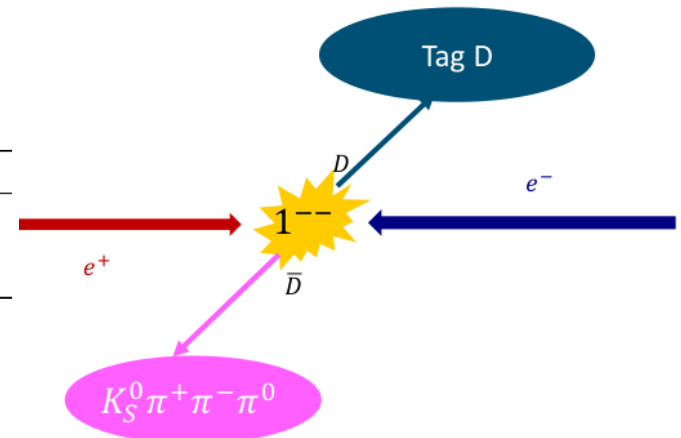
- With F_+^f , the γ angle can be extracted.
- ⇒ Important to determine F_+ for $D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$.

➤ Double tag method:

- With CP tags
- With $\pi^+ \pi^- \pi^0$ tag
- With $K_S^0 \pi^+ \pi^- \pi^0$ tag
- With $K_S^0 \pi^+ \pi^-$ tag

Type	Modes
CP-even	$K^+ K^-, \pi^+ \pi^-, K_S^0 \pi^0 \pi^0, K_L^0 \omega, K_L^0 \pi^0$
CP-odd	$K_S^0 \pi^0, K_S^0 \eta(\gamma\gamma), K_S^0 \eta'(\eta\pi^+ \pi^-), K_S^0 \eta'(\gamma\pi^+ \pi^-)$
Mixed CP	$\pi^+ \pi^- \pi^0, \pi^+ \pi^- \pi^+ \pi^-, K_{S,L}^0 \pi^+ \pi^-, K_S^0 \pi^+ \pi^- \pi^0$

Mixed CP tag modes



Strong phase in D^0 decays

➤ Determination of the CP-even fraction of $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$ [PRD 108, 032003 (2023)]

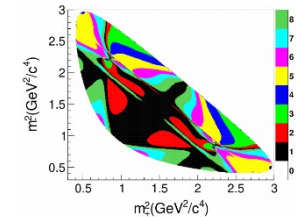
➤ Determination of F_+ :

• With CP tags: $N^\pm = \mathcal{B}(S)\varepsilon(S) \left[1 - \eta_{\text{CP}}^\mp (2F_+^S - 1) \right]$ $F_+ = \frac{N^+}{N^+ + N^-}$

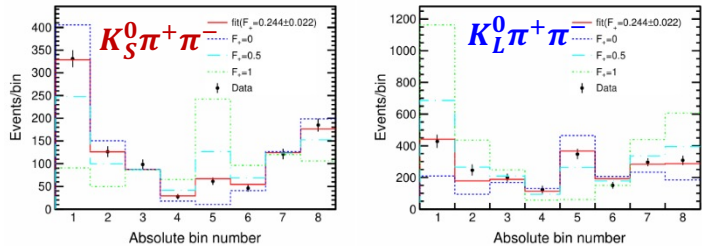
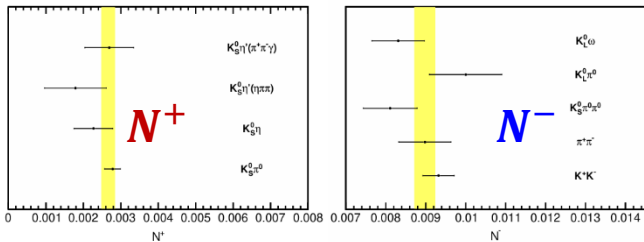
• With $\pi^+ \pi^- \pi^0$ tag: $\frac{N^{\pi^+ \pi^- \pi^0}}{\langle N^+ \rangle} = \frac{[1 - (2F_+^S - 1)(2F_+^{\pi^+ \pi^- \pi^0} - 1)]}{2F_+^S}$ $F_+^S = \frac{\langle N^+ \rangle F_+^{\pi^+ \pi^- \pi^0}}{N^{\pi^+ \pi^- \pi^0} - \langle N^+ \rangle + 2 \langle N^+ \rangle F_+^{\pi^+ \pi^- \pi^0}}$

• With $K_S^0 \pi^+ \pi^- \pi^0$ tag: $N^S = 2B_S \varepsilon(S) F_+^S (1 - F_+^S)$ $F_+^S = \frac{N^S}{\langle N^- \rangle}$

• With $K_S^0 \pi^+ \pi^-$ and $K_L^0 \pi^+ \pi^-$ tags: Divided into 8 bins of δ_D .



➤ F_+ Results:



Method	F_+
CP tags	$0.229 \pm 0.013 \pm 0.0018$
$\pi^+ \pi^- \pi^0$ tag	$0.227 \pm 0.014 \pm 0.0027$
$\pi^+ \pi^- \pi^+ \pi^-$ tag	$0.227 \pm 0.016 \pm 0.0034$
$K_S^0 \pi^+ \pi^- \pi^0$ self-tag	$0.244 \pm 0.019 \pm 0.0022$
$K_{S,L}^0 \pi^+ \pi^-$	$0.244 \pm 0.021 \pm 0.0062$
combined	$0.234 \pm 0.0096 \pm 0.0018$

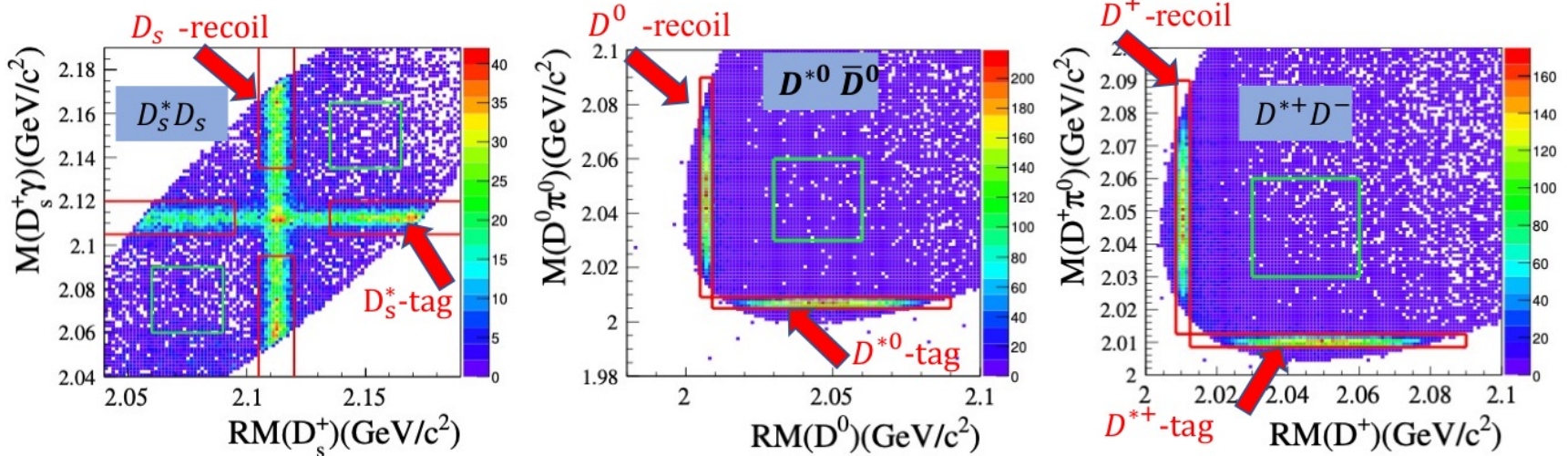
Spin and parity of D_s^* meson

➤ Determination of spin and parity for D_s^* meson. [PLB 846, 138245 (2023)]

- There is no decisive experimental results of spin and parity have been reported for the ground 1S states $D_{(s)}^*$. In PDG, the status of J^P for D^{*0} and D^{*+} are assigned to be 1^- while they need to be confirmed experimentally.

Decay chains:

- $e^+e^- \rightarrow D_s^{*+}D_s^-, D_s^{*+} \rightarrow \gamma D_s^+, D_s^+ \rightarrow K_S^0 K^+$
- $e^+e^- \rightarrow D^{*0}\bar{D}^0, D^{*0} \rightarrow \pi^0 D^0, D^0 \rightarrow K^-\pi^+, \pi^0 \rightarrow \gamma\gamma$
- $e^+e^- \rightarrow D^{*+}D^-, D^{*+} \rightarrow \pi^0 D^+, D^+ \rightarrow K^-\pi^+\pi^+, \pi^0 \rightarrow \gamma\gamma$



CHARMED, STRANGE MESONS

($C = S = \pm 1$)

$D_s^+ = c \bar{s}, D_s^- = \bar{c} s$, similarly for D_s^* 's

$$D_s^{*\pm} \quad I(J^P) = 0(??)$$

J^P is natural, width and decay modes consistent with 1^-

CHARMED MESONS

($C = \pm 1$)

$D^+ = c \bar{d}, D^0 = c \bar{u}, \bar{D}^0 = \bar{c} u, D^- = \bar{c} d$, similarly for D^{*} 's

$$D^*(2007)^0 \quad I(J^P) = 1/2(1^-) \quad |, J, P \text{ need confirmation}$$

J consistent with 1, value 0 ruled out (NGUYEN 1977).

CHARMED MESONS

($C = \pm 1$)

$D^+ = c \bar{d}, D^0 = c \bar{u}, \bar{D}^0 = \bar{c} u, D^- = \bar{c} d$, similarly for D^{*} 's

$$D^*(2010)^\pm \quad I(J^P) = 1/2(1^-) \quad |, J, P \text{ need confirmation.}$$

Spin and parity of D_S^* meson

➤ Determination of spin and parity for D_S^* meson. [PLB 846, 138245 (2023)]

• $J^P = 1^-$ for $D_S^{*\pm}$:

$$\mathcal{W}^{(1-)} \sim (3 + \cos 2\theta_1) - 4\cos 2\phi_1 \sin \theta_0 \sin \theta_1$$

• $J^P = 2^+$ for $D_S^{*\pm}$:

$$\mathcal{W}^{(2+)} \sim (3 + \cos 2\theta_0)(2 + \cos 2\theta_1 + \cos 4\theta_1) - 4(1 + 2\cos 2\theta_1)\cos 2\phi_1 \sin^2 \theta_0 \sin^2 \theta_1$$

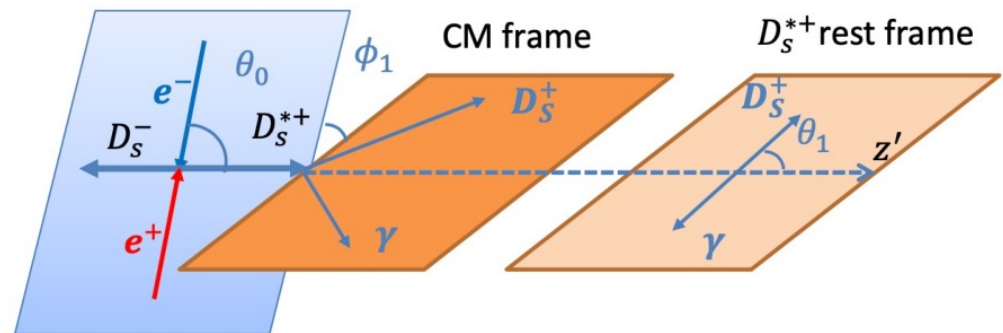
• $J^P = 3^-$ for $D_S^{*\pm}$:

$$\begin{aligned} \mathcal{W}^{(3-)} \sim & (398 + 271\cos 2\theta_1 + 130\cos 4\theta_1 + 255\cos 6\theta_1) \\ & - 16(163 + 380\cos 2\theta_0 + 255\cos 4\theta_0)(163 + 380\cos 2\theta_1 + 225\cos 4\theta_1)\cos 2\phi_1 \sin^2 \theta_0 \sin^2 \theta_1 \end{aligned}$$

➤ Test three possible J^P numbers for $D_S^{*\pm}$

J^P	$e^+e^- \rightarrow D_S^{*\pm} D_S^{\mp}$	$D_S^{*\pm} \rightarrow \gamma D_S^{\pm}$	$D_S^{*\pm} \rightarrow \pi^0 D_S^{\pm}$
0^-	O (Yes)	O (Yes)	× (No)
0^+	×	×	O
1^+	O	O	×
1^-	O[P]	O[P]	O[P]
1^+	O	O	×
2^-	O	O	×
2^+	O[D]	O[D]	O[D]
3^-	O[E]	O[E]	O[E]
3^+	O	O	×

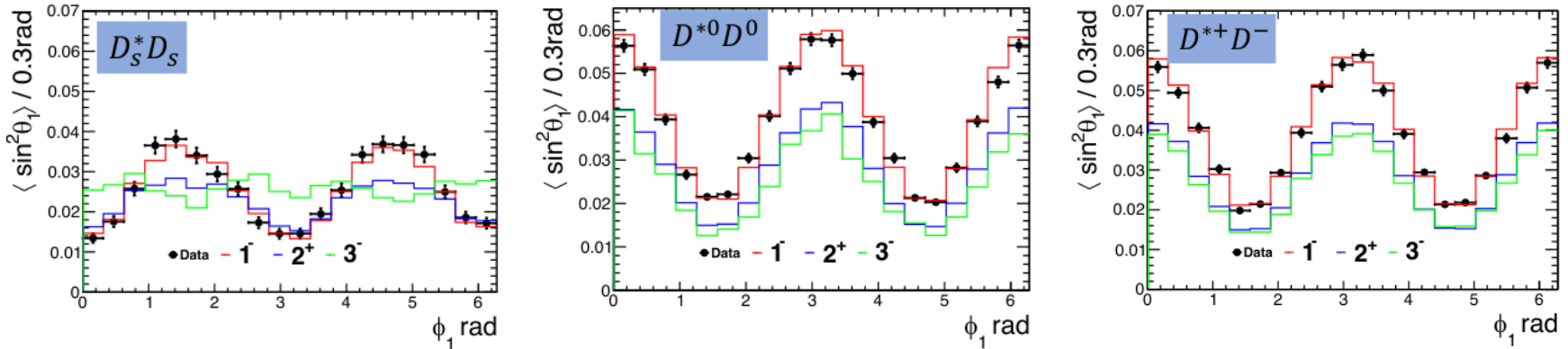
$$\langle \sin^2 \theta_1 \rangle \sim \phi_1$$



➤ Exactly same for D^{*0} and D^{*+}

Spin and parity of D_s^* meson

- Determination of spin and parity for D_s^* meson. [PLB 846, 138245 (2023)]
- Fit result $\langle \sin^2 \theta_1 \rangle$ v.s. ϕ_1 :



- $\langle \sin^2 \theta_1 \rangle$ v.s. ϕ_1 illustrate the different behavior.
- Data obviously favor the 1^- assignment over the 2^+ and 3^- .
- Estimation of statistical significance:

$$S = \sqrt{2(\ln \mathcal{L}_{\max}(H_1) - \ln \mathcal{L}_{\max}(H_0))}$$

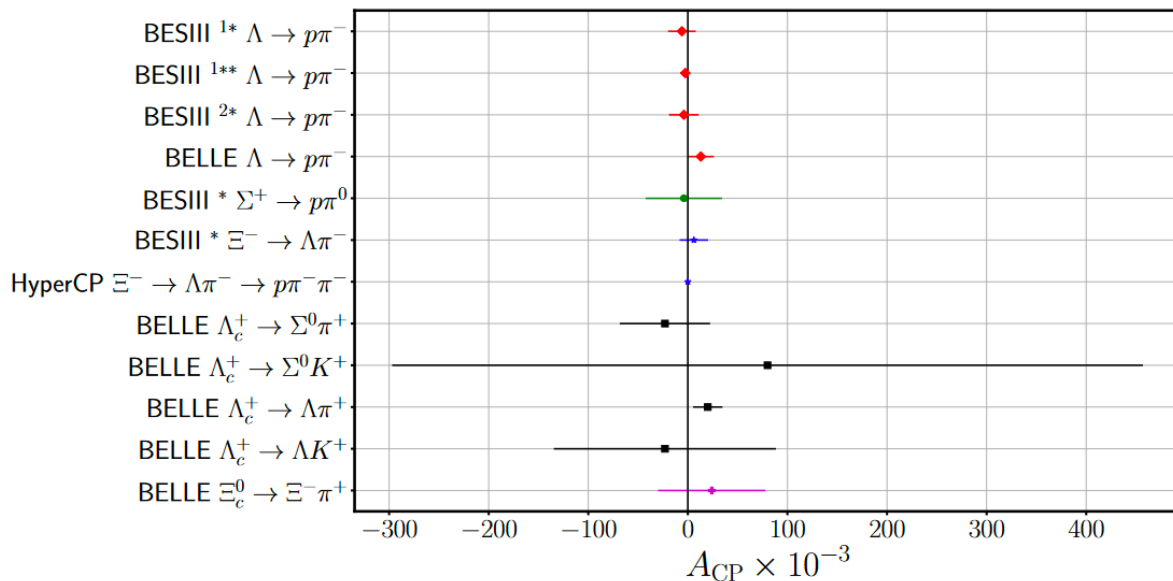
process	$2 \ln(\mathcal{L}^{J^P=2^+} / \mathcal{L}^{J^P=1^-,2^+}) $	significance	$2 \ln(\mathcal{L}^{J^P=3^-} / \mathcal{L}^{J^P=1^-,3^-}) $	significance
D_s^{*+}	1101.67	$>32\sigma$	2104.36	$>32\sigma$
D^{*0}	29251.08	$>32\sigma$	30989.46	$>32\sigma$
D^{*+}	25672.06	$>32\sigma$	31718.66	$>32\sigma$

The J^P is determined 1^- with large than 32σ significance against 2^+ and 3^- hypotheses.

Symmetry study

CP tests at BESIII & Belle

- SM predicts very small violations of charge conjugation and parity (CP) symmetry.
- Sizeable CP violations prerequisite for Baryogenesis
- Spin-carrying hyperons precision probe of CP symmetry.



BESIII:

Nature Phys. 15, p 631-634 (2019)
 Phys. Rev. Lett. 125, 052004 (2020)
 Nature 606, 64-69 (2022)
 Phys. Rev. Lett. 129, 131801 (2022)
 Phys. Rev. D 108, L031106 (2023)

Belle:

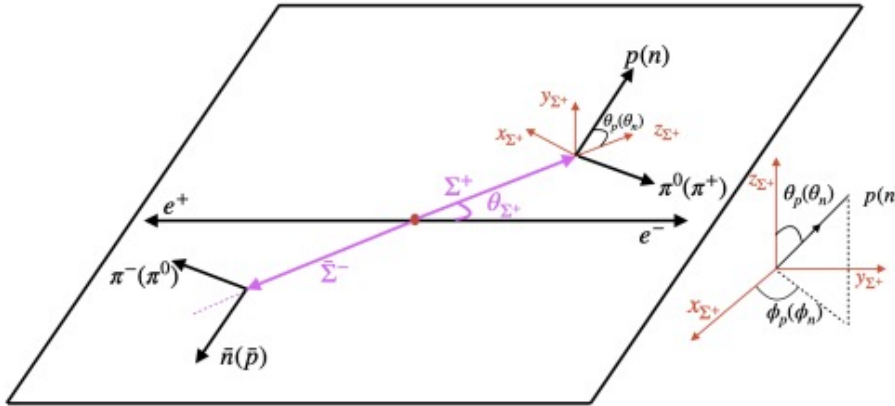
Sci. Bull. 68, 583-592 (2023)

HyperCP:

Phys. Rev. Lett. 93, 262001, 2004.

CP test in $\Sigma^+ \rightarrow n\pi^+$

- Helicity frame definition:



The weak decay parameters are determined to be:

$$\alpha_+ = 0.0481 \pm 0.0031 \pm 0.0019$$

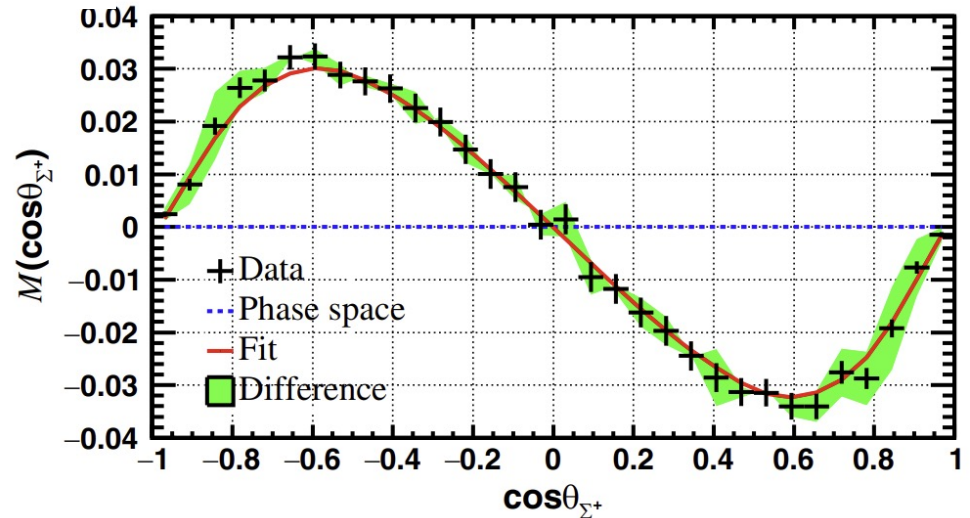
$$\alpha_- = -0.0565 \pm 0.0047 \pm 0.0022$$

$$A_{CP} = -0.080 \pm 0.052 \pm 0.028$$

Differential cross-section:

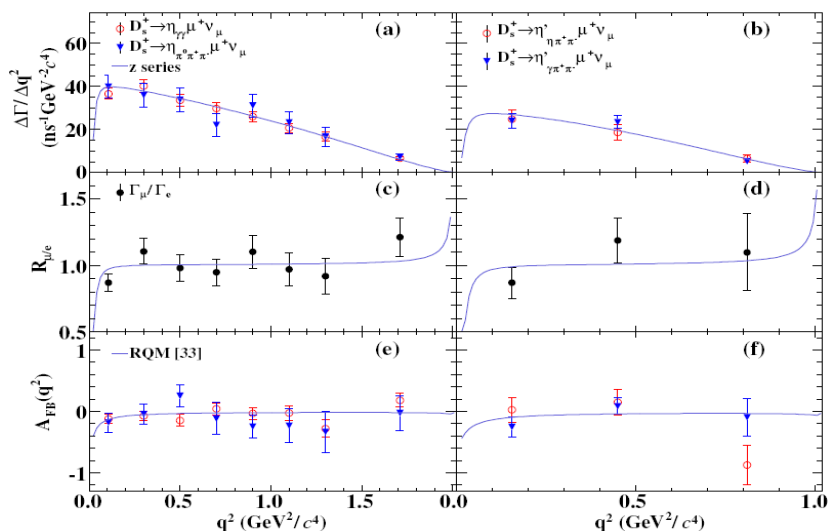
$$\begin{aligned} \mathcal{W}(\xi) = & T_0(\xi) + \alpha_{J/\psi} T_5(\xi) \\ & + \alpha \bar{\alpha} \left(T_1(\xi) + \sqrt{1 - \alpha_{J/\psi}^2} \cos(\Delta\Phi) T_2(\xi) \right. \\ & \left. + \alpha_{J/\psi} T_6(\xi) \right) + \sqrt{1 - \alpha_{J/\psi}^2} \sin(\Delta\Phi) (\alpha T_3(\xi) \\ & + \bar{\alpha} T_4(\xi)), \end{aligned}$$

PRL 131, 191802 (2023)



LFU tests in Charm decays at BESIII

$$D_s^+ \rightarrow \eta^{(\prime)} \mu^+ \nu_\mu \quad \text{PRL 132,091802(2024)}$$



$$R_{D_s^+ \eta} = \frac{\Gamma[D_s^+ \rightarrow \eta \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \eta e^+ \nu]} = 0.984 \pm 0.032$$

$$R_{D_s^+ \eta'} = \frac{\Gamma[D_s^+ \rightarrow \eta' \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \eta' e^+ \nu]} = 0.989 \pm 0.089$$

$$D_s^+ \rightarrow \phi \mu^+ \nu_\mu \quad \text{JHEP12(2023)072}$$

$$R_{D_s^+ \phi} = \frac{\Gamma[D_s^+ \rightarrow \phi \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \phi e^+ \nu]} = 0.94 \pm 0.08$$

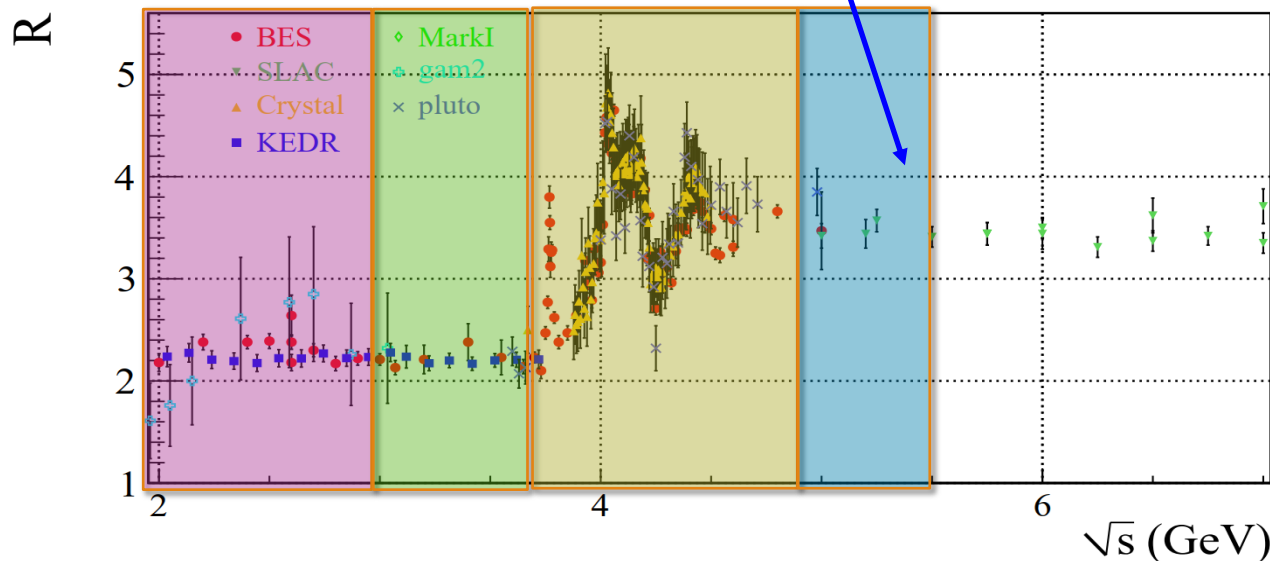
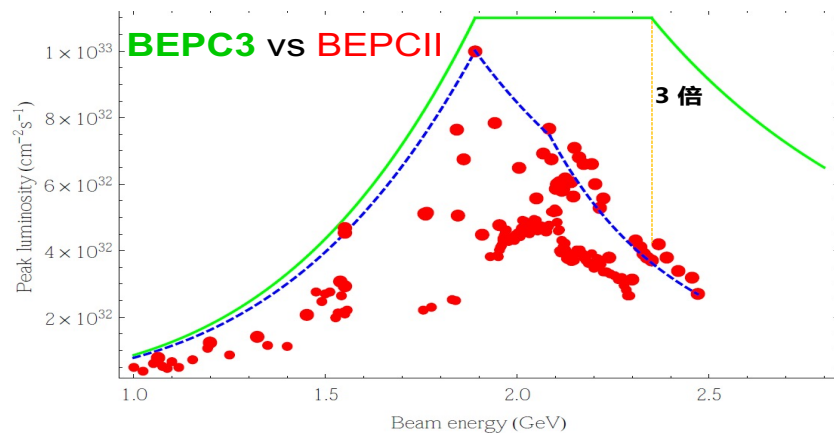
The $D^+ \rightarrow \tau^+ \nu$ and seven semimuonic D decays are observed for the first time. Five semimuonic charm decays are measured with better precision

	BF ratios		References
μ/e	$D^0 \rightarrow K^-$	$0.978 \pm 0.007 \pm 0.012$	PRL122(2019)011804
	$D^0 \rightarrow \pi^-$	$0.922 \pm 0.030 \pm 0.022$	PRL121(2018)171803
	$D^0 \rightarrow \rho^-$	0.90 ± 0.11	PRD104(2021)L091003
	$D^+ \rightarrow \bar{K}^0$	1.00 ± 0.03	EPJC76(2016)369
	$D^+ \rightarrow \pi^0$	$0.964 \pm 0.037 \pm 0.026$	PRL121(2018)171803
	$D^+ \rightarrow \omega$	1.05 ± 0.14	PRD101(2020)072005
	$D^+ \rightarrow \eta$	0.91 ± 0.13	PRL124(2020)231801
	$D_s^+ \rightarrow \eta$	$0.984 \pm 0.028 \pm 0.016$	arXiv:2307.12852 accepted by PRL
	$D_s^+ \rightarrow \eta'$	$0.989 \pm 0.082 \pm 0.034$	
	$D_s^+ \rightarrow \phi$	0.94 ± 0.08	JHEP12(2023)072
τ/μ	$\Lambda_c^+ \rightarrow \Lambda$	$0.98 \pm 0.05 \pm 0.03$	PRD108(2023)L031105
	$D^+ \rightarrow \tau^+ \nu$	$3.21 \pm 0.64 \pm 0.43$	PRL123(2019)211802
	$D_s^+ \rightarrow \tau^+ \nu$	10.05 ± 0.35	PRL127(2021)171801

Plan of BEPCII/BESIII upgrade

- Optimize E_{cm} at 4.7 GeV with luminosity 3 times higher than the current BEPCII
→ more effective data taking
- CGEM inner tracker
- Extend the maximum E_{cm} up to 5.6 GeV
→ more physics opportunity

Chin. Phys. C 44 (2020) 4, 040001



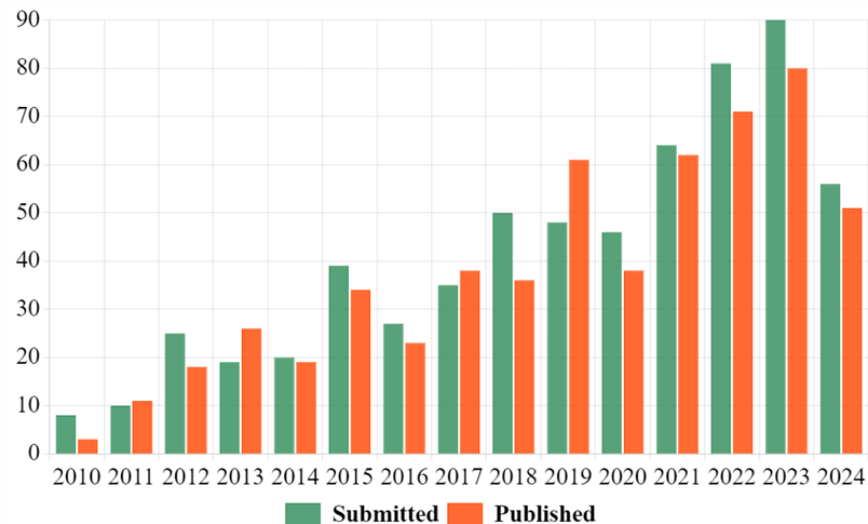
Summary & Prospect

- World largest data samples at **BESIII**
 - An excellent laboratory to study a wide physics program
- Recent highlights of BESIII results on flavor physics are briefly overviewed
 - A personal selection of latest BESIII results
- Latest large data-sets under study
- BEPCII-U: 3x lum above 4 GeV & max energy to 5.6 GeV) !

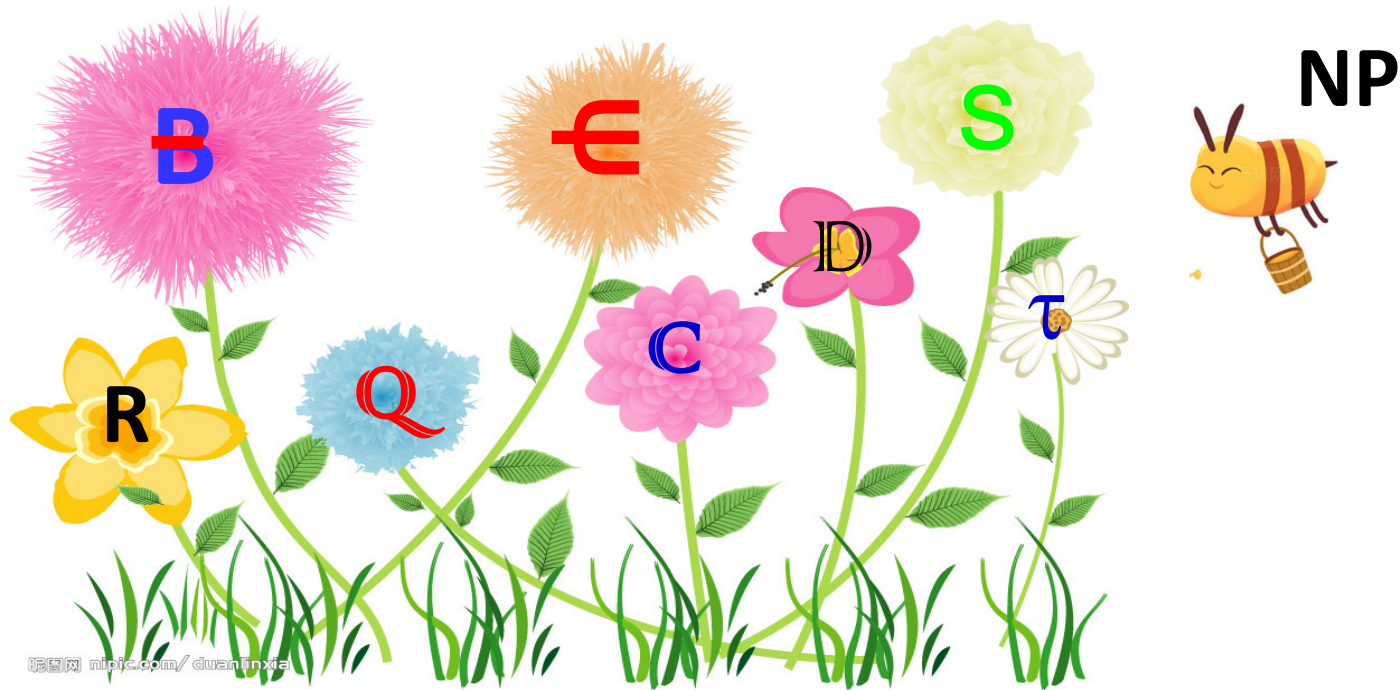
July 2024

Submitted: 621, Published: 571

PRL&Nature(physics): 115 published



More important results are expected from BESIII !



Many thanks for your attention !