



中国科学院大学
University of Chinese Academy of Sciences



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

宇宙相变引力波和新物理

郭怀珂

中国科学院大学
国际理论物理中心-亚太地区

2024-8-28

2024年BESIII新物理研讨会

Radius of the Visible Universe

Quantum
Fluctuations

Inflation
Inflation Ends

Protons Formed

Nuclear Fusion Begins

Nuclear Fusion Ends

Cosmic Microwave Background

Dark Ages

First Stars & Galaxies Form

Modern Universe

Today

0

10^{-32}

$1 \mu\text{s}$

0.01 s

3 min

380,000 yrs

200 Million yrs

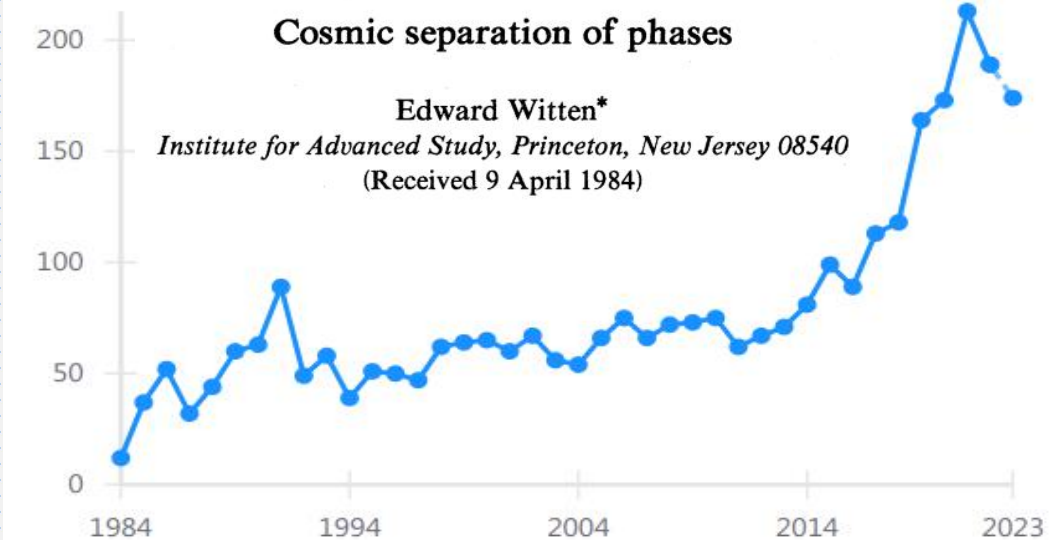
13.8 Billion yrs

Age of the Universe

GW, and baryon asymmetry, Higgs physics, ...

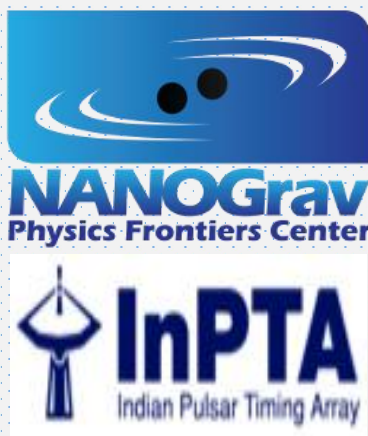
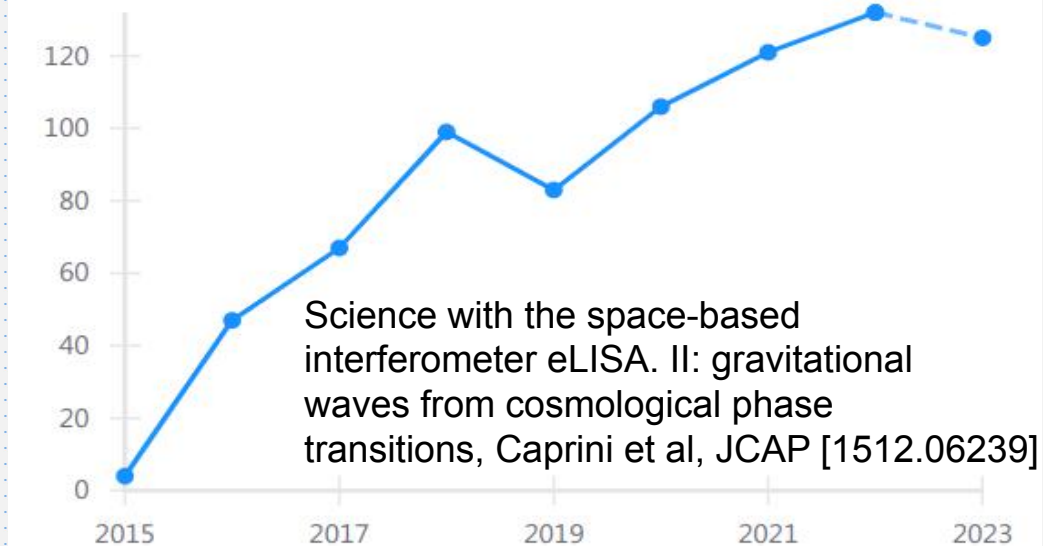
Citations per year

inspirehep.net

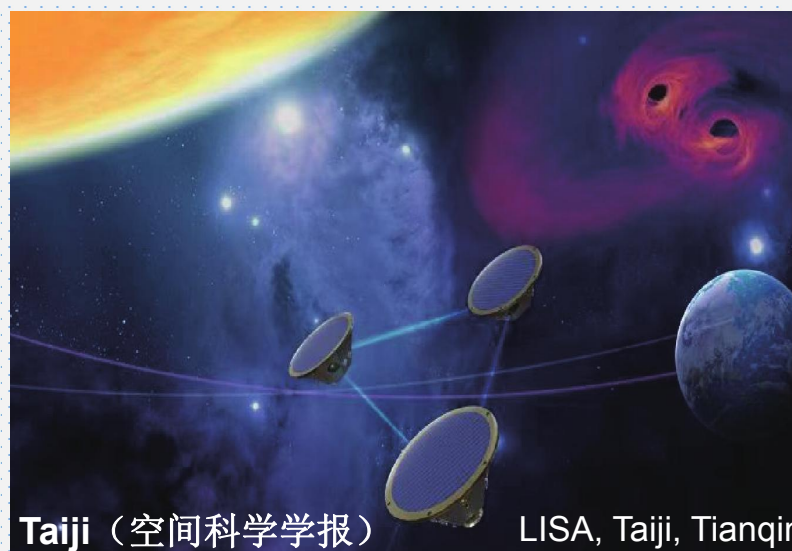


Citations per year

inspirehep.net



中国脉冲星测时阵列 (CPTA)



Taiji (空间科学学报)

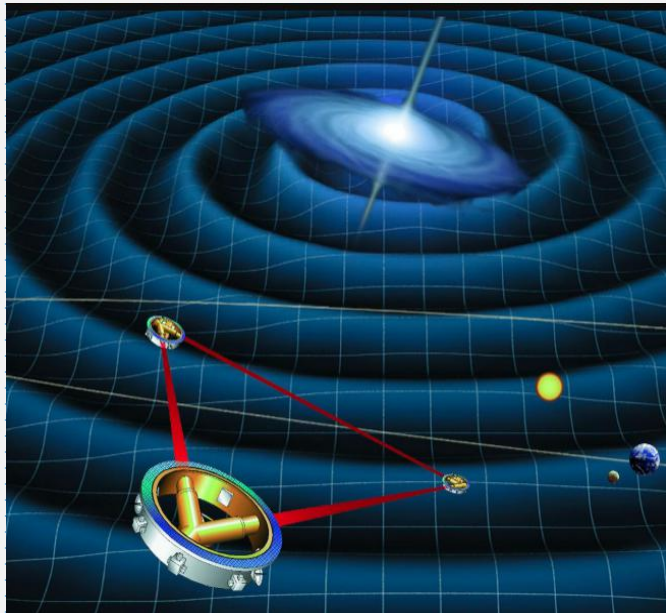
LISA, Taiji, Tianqin



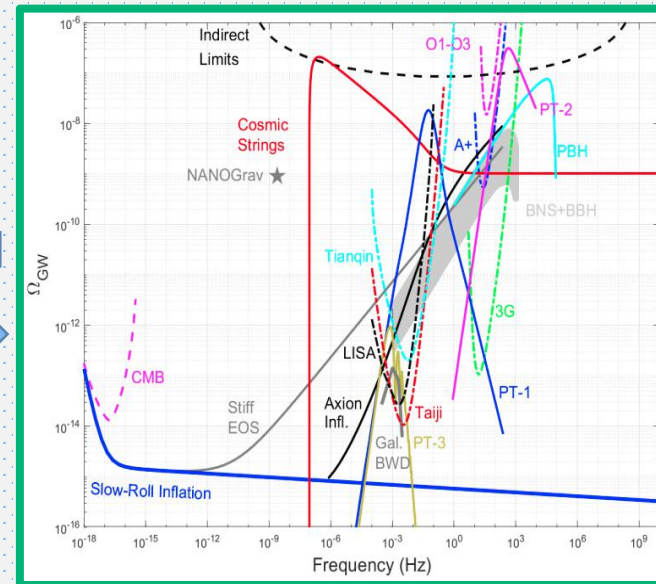
ligo.caltech.edu

From Theory to Experiment

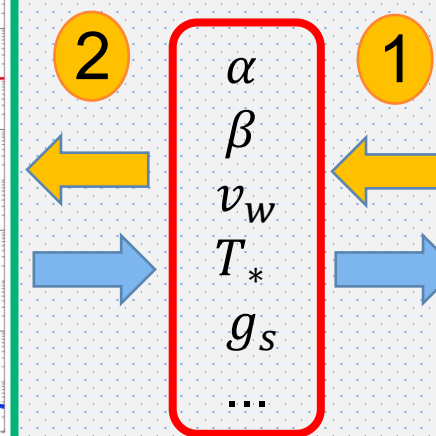
theorist



LIGO, LISA/Taiji/Tianqin, PTA, ...



Gravitational Wave Spectrum



α
 β
 v_w
 T_*
 g_s
...

Phase Transition Parameters



Standard Model of Elementary Particles

three generations of matter (fermions)						interactions / force carriers (bosons)	
I		II		III			
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$		
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0		
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0		
	u	c	t	g	H		
	up	charm	top	gluon	higgs		
	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$				
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$				
	d	s	b	γ	BSM		
	down	strange	bottom	photon			
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0			
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0			
	e	μ	τ	Z			
	electron	muon	tau	Z boson			
	-1	-1	-1	0			
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1			
	ν_e	ν_μ	ν_τ	W			
	electron neutrino	muon neutrino	tau neutrino	W boson			
	$< 1.0 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 18.2 \text{ MeV}/c^2$	± 1			
	0	0	0	1			
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$				
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$				

QUARKS (I, II, III)

LEPTONS (e, μ , τ)

GAUGE BOSONS (g, γ , Z, W)

SCALAR BOSONS (H)

BSM

Particle Physics Model



experimentalist

Phenomenological Studies

Detection of early-universe gravitational-wave signatures and fundamental physics

[Robert Caldwell](#), [Yanou Cui](#), [Huai-Ke Guo](#) , [Vuk Mandic](#), [Alberto Mariotti](#), [Jose Miguel No](#), [Michael J. Ramsey-Musolf](#), [Mairi Sakellariadou](#) , [Kuver Sinha](#), [Lian-Tao Wang](#), [Graham White](#), [Yue Zhao](#), [Haipeng An](#), [Ligong Bian](#), [Chiara Caprini](#), [Sebastien Clesse](#), [James M. Cline](#), [Giulia Cusin](#), [Bartosz Fornal](#), [Ryusuke Jinno](#), [Benoit Laurent](#), [Noam Levi](#), [Kun-Feng Lyu](#), [Mario Martinez](#), [Andrew L. Miller](#), [Diego Redigolo](#), [Claudia Scarlata](#), [Alexander Sevrin](#), [Barmak Shams Es Haghi](#), [Jing Shu](#), [Xavier Siemens](#), [Danièle A. Steer](#), [Raman Sundrum](#), [Carlos Tamarit](#), [David J. Weir](#), [Ke-Pan Xie](#), [Feng-Wei Yang](#) & [Siyi Zhou](#) — Show fewer authors

[General Relativity and Gravitation](#) **54**, Article number: 156 (2022) | [Cite this article](#)

arXiv > hep-ph > arXiv:2203.08206

High Energy Physics - Phenomenology

[Submitted on 15 Mar 2022]

Probing the Electroweak Phase Transition with Exotic Higgs Decays

Marcela Carena, Jonathan Kozaczuk, Zhen Liu, Tong Ou, Michael J. Ramsey-Musolf, Jessie Shelton, Yikun Wang, Ke-Pan Xie

arXiv > hep-ph > arXiv:2203.10046

High Energy Physics - Phenomenology

[Submitted on 18 Mar 2022]

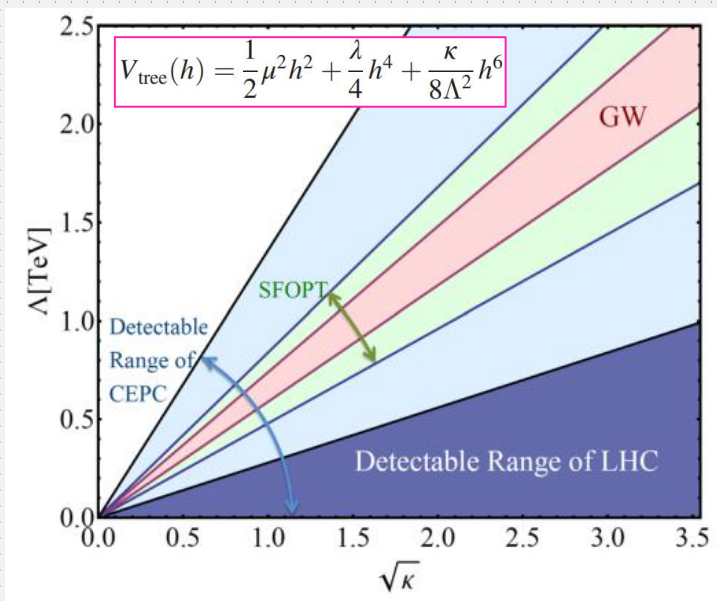
Scalar-mediated dark matter model at colliders and gravitational wave detectors -- A White paper for Snowmass 2021

Jia Liu, Xiao-Ping Wang, Ke-Pan Xie

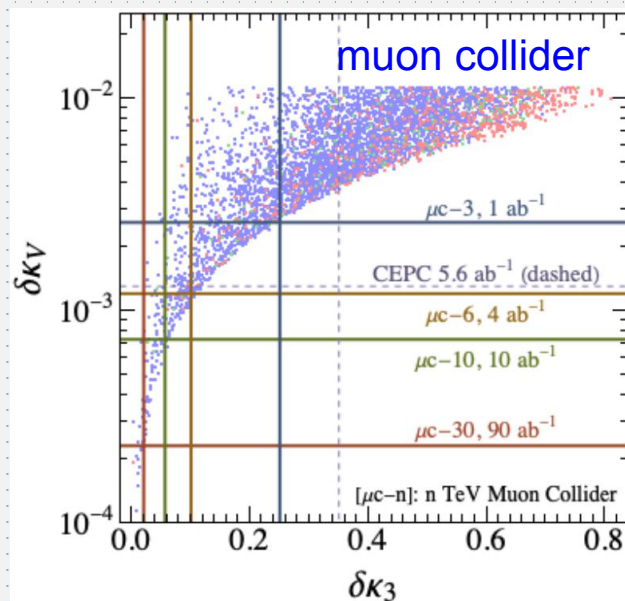
Snowmass 2021 White papers

Models	Strong 1 st order phase transition	GW signal	Cold DM	Dark Radiation and small scale structure
SM charged				
Triplet [20–22]	✓	✓	✓	✗
complex and real Triplet [23] (Georgi-Machacek model)	✓	✓	✓	✗
Multiplet [24]	✓	✓	✓	
2HDM [25–30]	✓	✓		✗
MLRSM [31]	✓	✓	✗	✗
NMSSM [32–36]	✓	✓	✓	✗
SM uncharged				
S_ν (xSM) [37–49]	✓	✓	✗	✗
2 S_ν 's [50]	✓	✓	✓	✗
S_c (cxSM) [49, 51–54]	✓	✓	✓	✗
$U(1)_D$ (no interaction with SM) [55]	✓	✓	✓	✗
$U(1)_D$ (Higgs Portal) [56]	✓	✓	✓	
$U(1)_D$ (Kinetic Mixing) [57]	✓	✓	✓	
Composite $SU(7)/SU(6)$ [58]	✓	✓	✓	
$U(1)_L$ [59]	✓	✓	✓	✗
$SU(2)_D \rightarrow$ global $SO(3)$ by a doublet [60–62]			✓	✗
$SU(2)_D \rightarrow U(1)_D$ by a triplet [63–65]			✓	✓
$SU(2)_D \rightarrow Z_2$ by two triplets [66]			✓	✗
$SU(2)_D \rightarrow Z_3$ by a quadruplet [67, 68]			✓	✗
$SU(2)_D \times U(1)_{B-L} \rightarrow Z_2 \times Z_2$ by a quintuplet and a S_c [69]			✓	✗
$SU(2)_D$ with two dark Higgs doublets [70]	✓	✓	✗	✗
$SU(3)_D \rightarrow Z_2 \times Z_2$ by two triplets [62, 71]			✓	✗
$SU(3)_D$ (dark QCD) (Higgs Portal) [72, 73]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times Z_2$ [74]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times G_{D,SM} \cdots$ [75]	✓	✓	✓	
Current work				
$SU(2)_D \rightarrow U(1)_D$ (see the text)	✓	✓	✓	✓

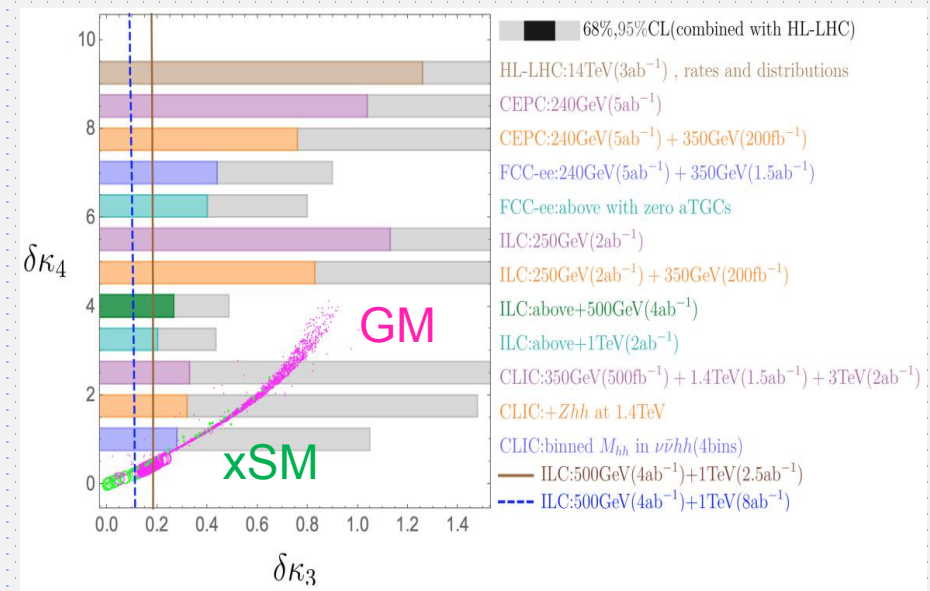
Ghosh,[HG](#),Han,Liu, JHEP [2012.09758]



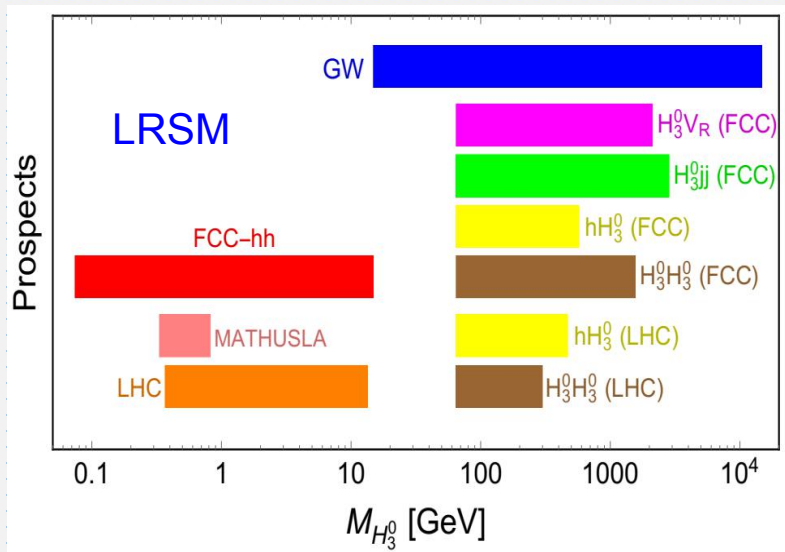
Fapeng Huang, Yi-Fu Cai, Xinmin Zhang, et al, PRD [1601.01640]



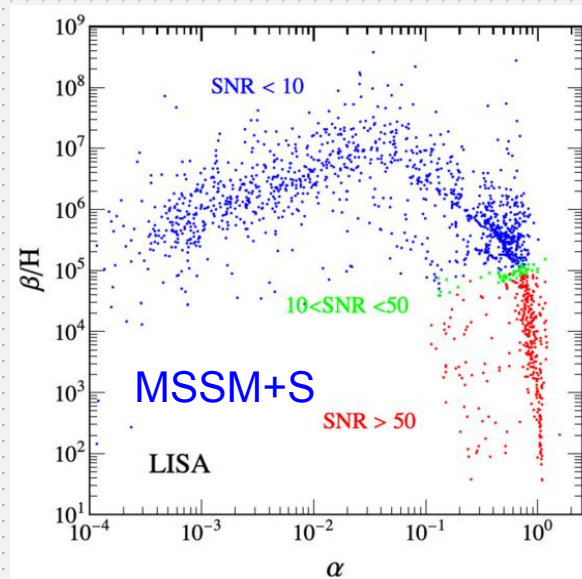
Wei Liu, Ke-Pan Xie, JHEP [2101.10469]



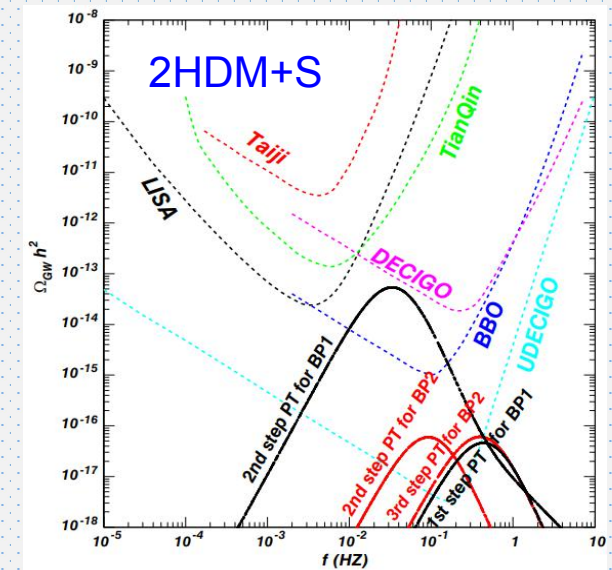
Ligong Bian, HG, Yongcheng Wu, Ruiyu Zhou, PRD [1906.11664]



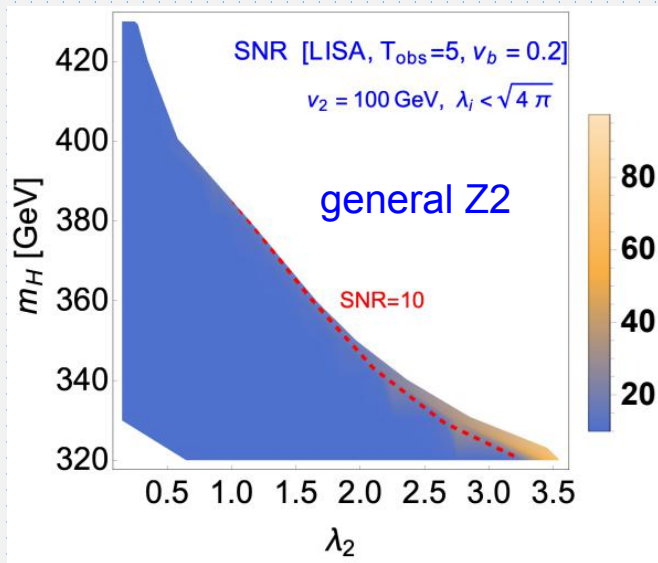
Mingqiu Li, Qi-Shu Yan, Yongchao Zhang, Zhijie Zhao, JHEP [2012.13686]



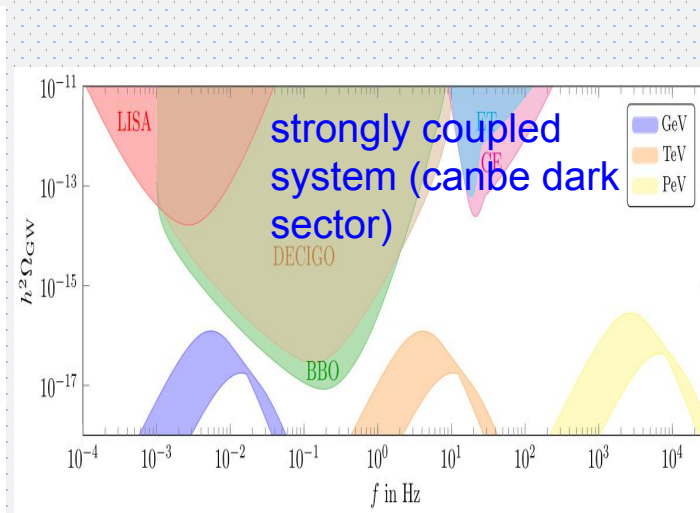
Wenyu Wang, Ke-Pan Xie, Wu-Long Xu, Jin Min Yang, EPJC [2204.01928]



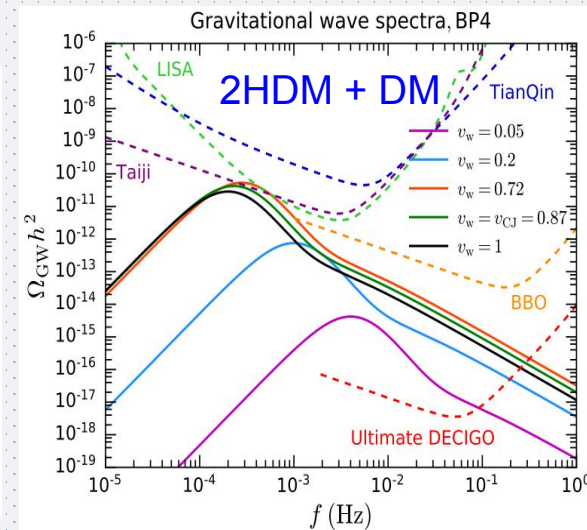
Songtao Liu, Lei Wang, PRD [2302.04639]



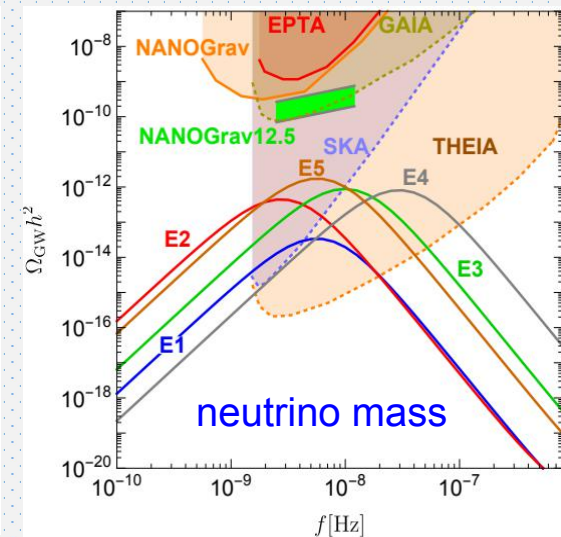
Qing-Hong Cao, Katsuya Hashino, Xu-Xiang Li, Jiang-Hao Yu [2212.07756]



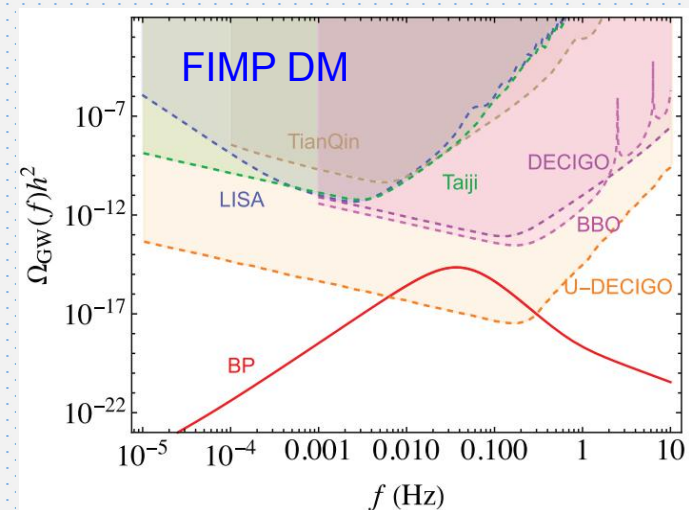
Zhi-Wei Wang, et al, PRD [2012.11614]



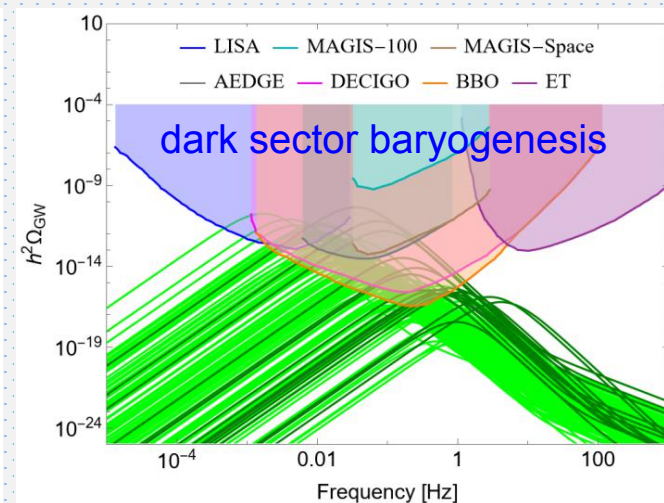
Zhao Zhang, Chengfeng Cai, Xue-Min Jiang, Yi-Lei Tang, Zhao-Huan Yu, and Hong-Hao Zhang, JHEP [2102.01588]



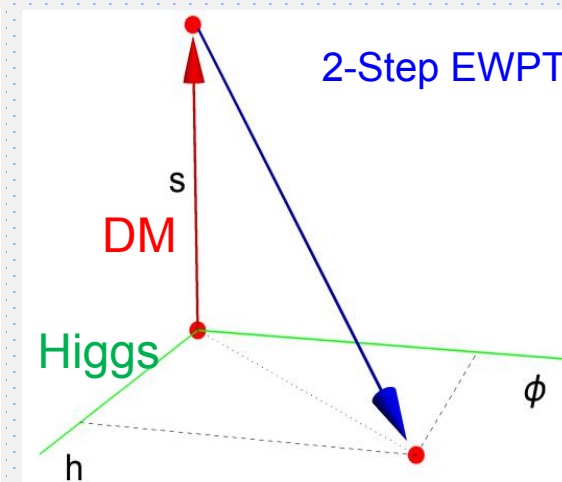
Pasquale Di Bari, Danny Marfatia, Ye-Ling Zhou, JHEP [2106.00025]



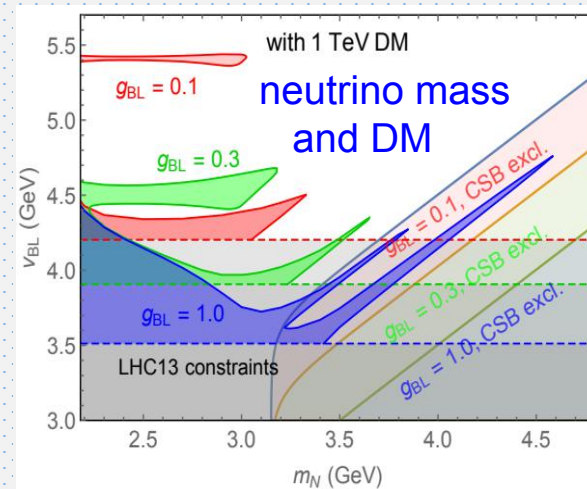
Xuwen Liu, Shu-Yuan Guo, Bin Zhu, Ying Li, Sci.Bull. [2022.06.011]



Marcela Carena, Ying-Ying Li, Tong Ou, Yikun Wang, JHEP [2210.14352]



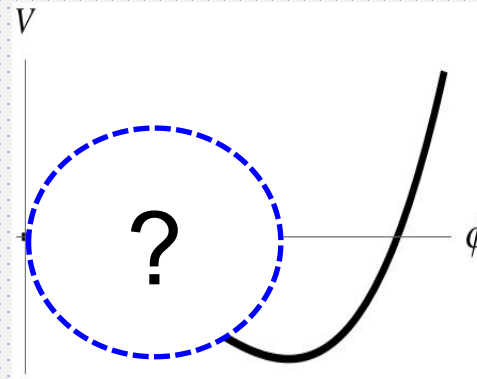
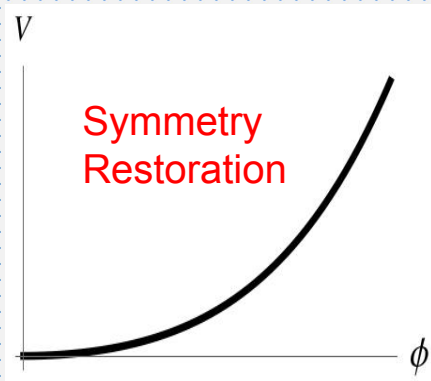
Wei Chao, [HG](#), Jing Shu, JCAP [1702.02698]



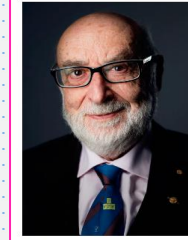
Ligong Bian, Wei Cheng, [HG](#), Yongchao Zhang, CPC [1907.13589]

Electroweak Phase Transition

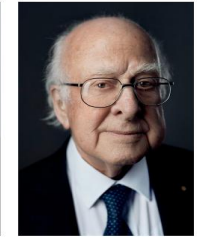
$$SU(3)_C \times SU(2)_L \times U(1)_Y \rightarrow SU(3)_C \times U(1)_{EM}$$



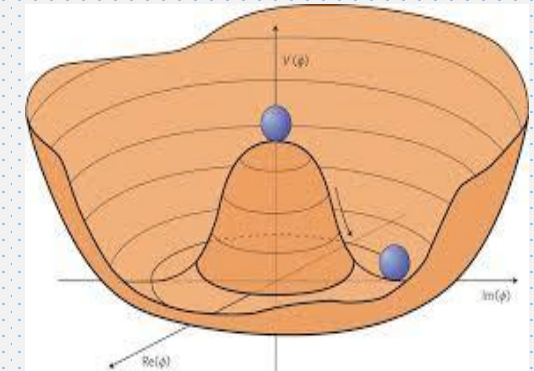
The Nobel Prize in Physics 2013



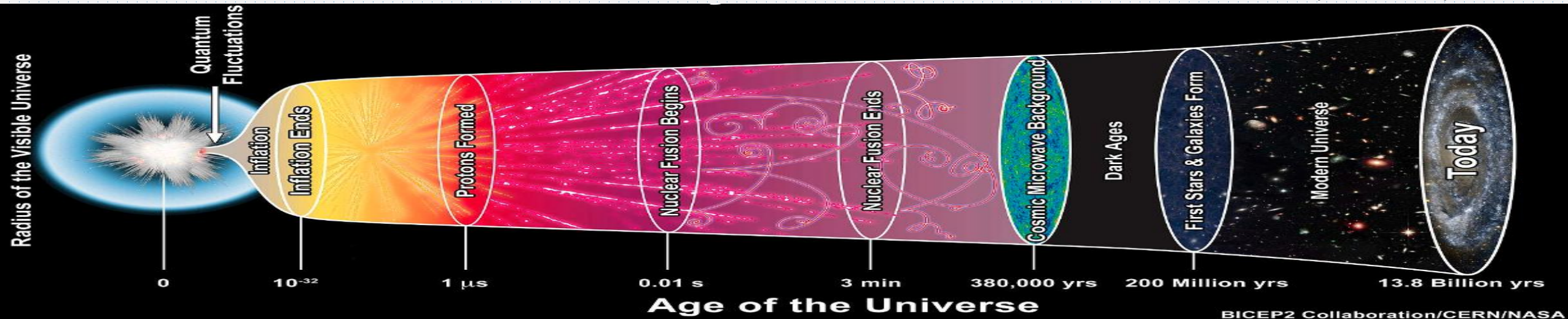
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François Englert
Prize share: 1/2



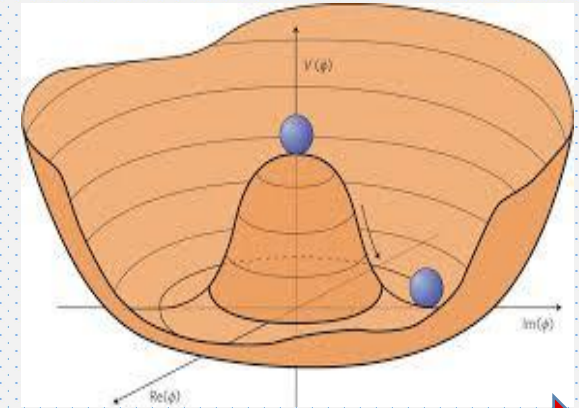
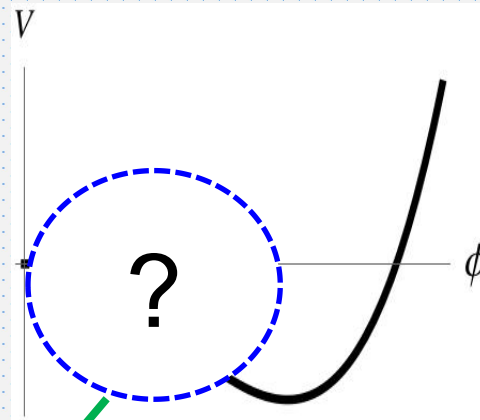
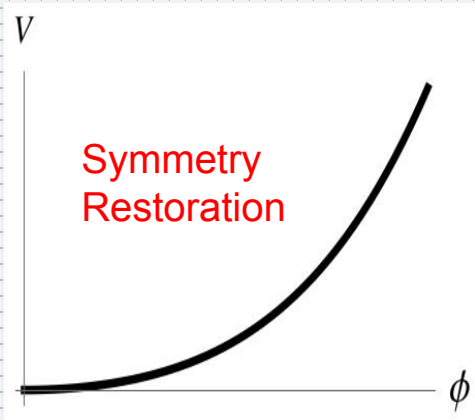
© Nobel Media AB. Photo: A. Mahmoud
Peter W. Higgs
Prize share: 1/2
nobelprize.org



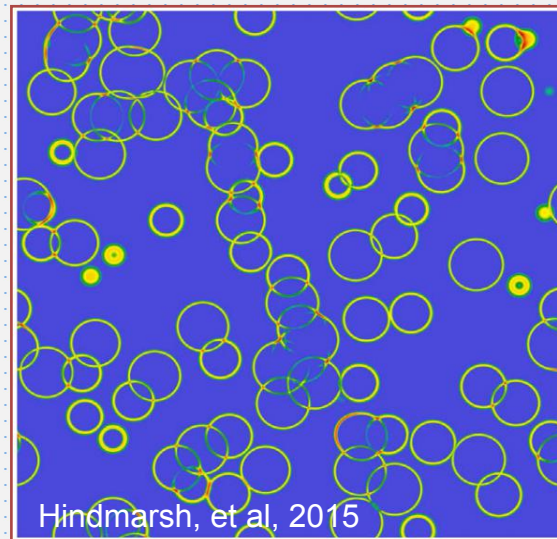
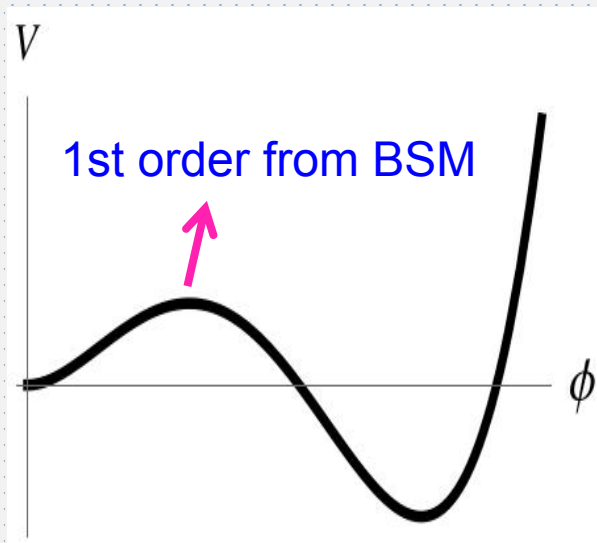
Temperature drops



Electroweak Phase Transition



Temperature drops



Electroweak Baryogenesis

- Modified Higgs potential (Higgs physics, GW)
- Extra CP-violation (EDM, LHC, BESIII)
- New particles, symmetries (LHC, GW)

Trodden, Rev.Mod.Phys [9803479]

Collider and GW Complementarity

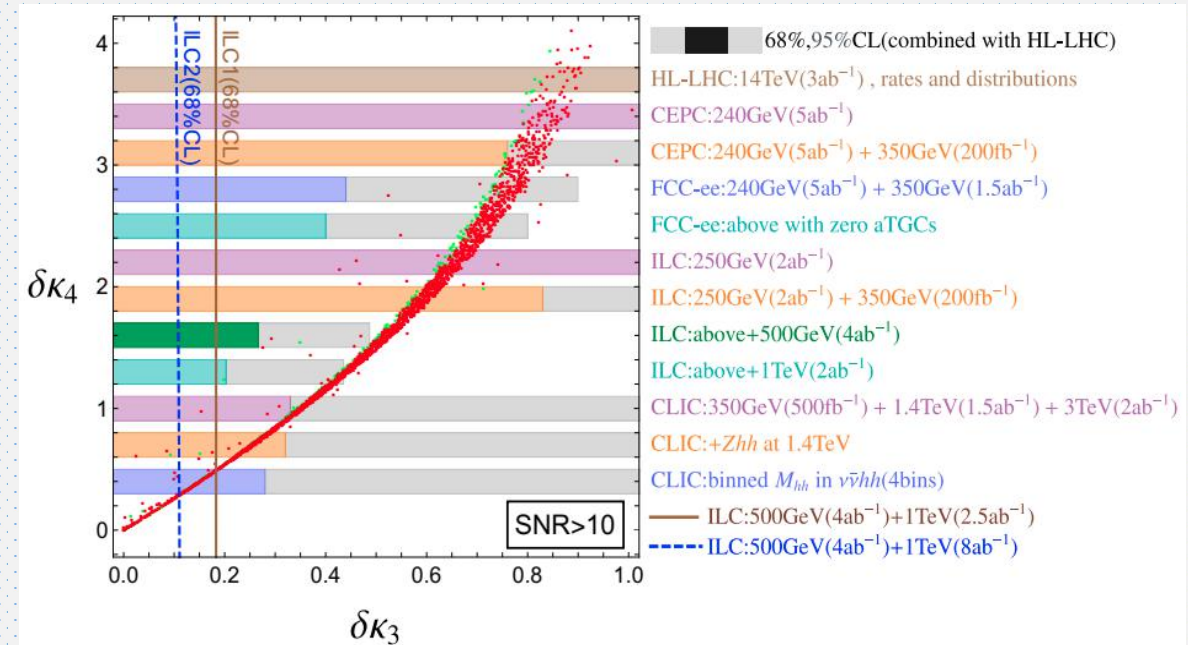
Contents

Snowmass 2021 Whitepaper, GRG [2203.07972]

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	Session leads: Michael Ramsey-Musolf and Lian-Tao Wang	
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Simplest model: xSM (SM + S)

$$\Delta\mathcal{L} = -\frac{1}{2} \frac{m_{h_1}^2}{v} (1 + \delta\kappa_3) h_1^3 - \frac{1}{8} \frac{m_{h_1}^2}{v^2} (1 + \delta\kappa_4) h_1^4$$



Alves, Ghosh, HG, Sinha, Vagie, JHEP [1812.09333]

Collider and Gravitational Wave Complementarity in Exploring the Singlet Extension of the Standard Model

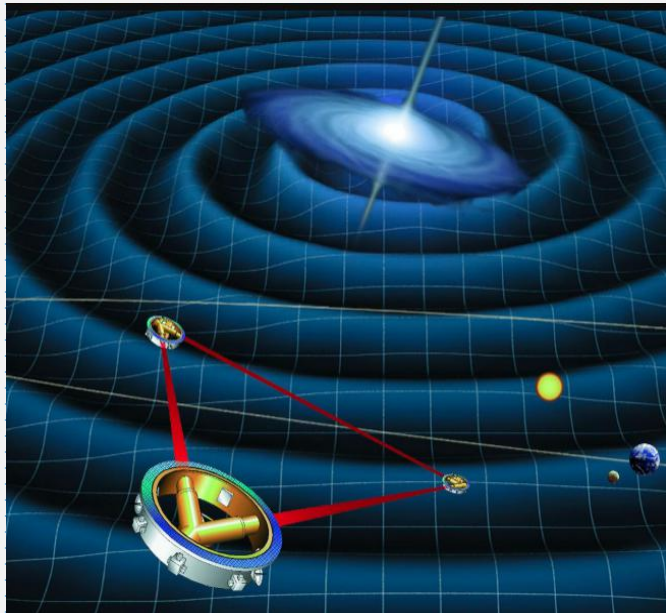
Alexandre Alves (Diadema, Sao Paulo Fed. U.), Tathagata Ghosh (Hawaii U.), Huai-Ke Guo (Oklahoma U.), Kuver Sinha (Oklahoma U.), Daniel Vagie (Oklahoma U.) (Dec 21, 2018)

Published in: JHEP 04 (2019) 052 • e-Print: 1812.09333 [hep-ph]

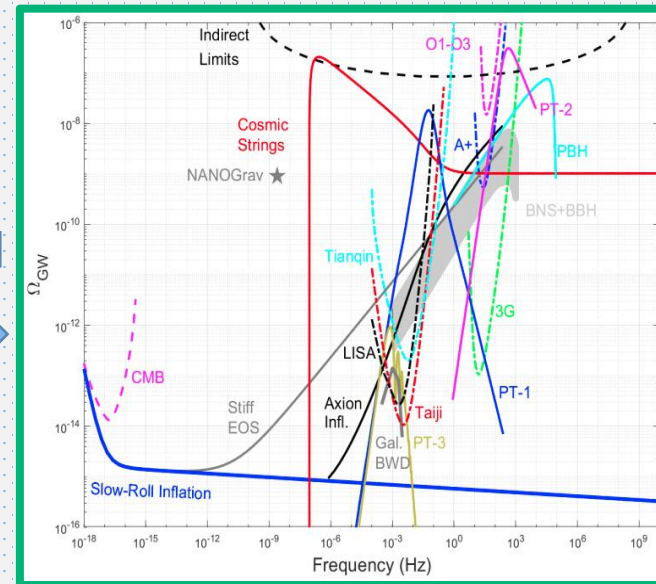
pdf DOI cite claim reference search 120 citations

Recent Developments

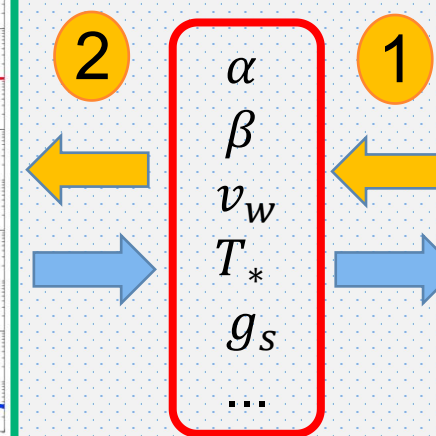
theorist



LIGO, LISA/Taiji/Tianqin, PTA, ...



Gravitational Wave Spectrum



Phase Transition Parameters

Standard Model of Elementary Particles

three generations of matter (fermions)			interactions / force carriers (bosons)	
I	II	III		
mass $\approx 2.2 \text{ MeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ u up	mass $\approx 1.28 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ c charm	mass $\approx 173.1 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ t top	mass $\approx 124.97 \text{ GeV}/c^2$ charge 0 spin 0 H higgs	BSM SCALAR BOSONS
mass $\approx 4.7 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ d down	mass $\approx 96 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ s strange	mass $\approx 4.18 \text{ GeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ b bottom	mass 0 charge 0 spin 1 g gluon	
mass $\approx 0.511 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ e electron	mass $\approx 105.66 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ μ muon	mass $\approx 1.7768 \text{ GeV}/c^2$ charge -1 spin $\frac{1}{2}$ τ tau	mass $\approx 91.19 \text{ GeV}/c^2$ charge 0 spin 1 Z Z boson	
mass $< 1.0 \text{ eV}/c^2$ charge 0 spin $\frac{1}{2}$ ν_e electron neutrino	mass $< 0.17 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ ν_μ muon neutrino	mass $< 18.2 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ ν_τ tau neutrino	mass $\approx 80.39 \text{ GeV}/c^2$ charge ± 1 spin 1 W W boson	GAUGE BOSONS VECTOR BOSONS

Particle Physics Model



experimentalist

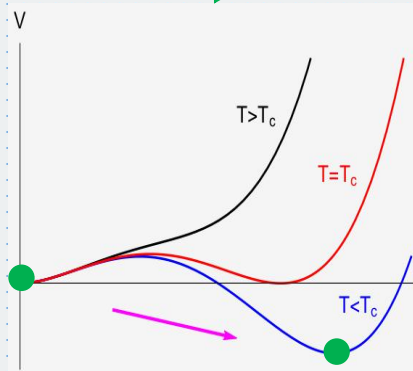
Bubble Nucleation Rate

How fast the bubbles are generated?

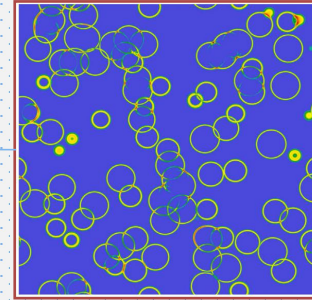
Perturbative Method

$$V_T = V_{\text{tree}} + V_{\text{CW}} + \frac{T^2}{24} \sum_i c_i M_i^2(\phi) - \frac{T}{12\pi} \sum_j d_j [M_j^2(\phi)]^{3/2}$$

$$V(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda}{4}\phi^4$$

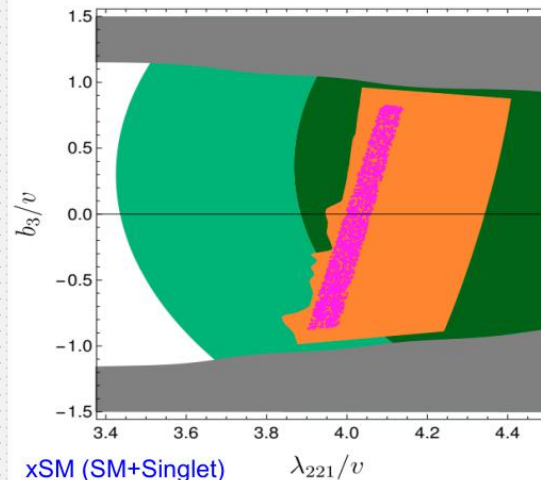


- Infrared problem (Linde, 1980)
- Gauge invariance (ok for high-T expansion)
possible solution: Löfgren, Ramsey-Musolf, et al,
PRL [2112.05472], JHEP [2112.08912]



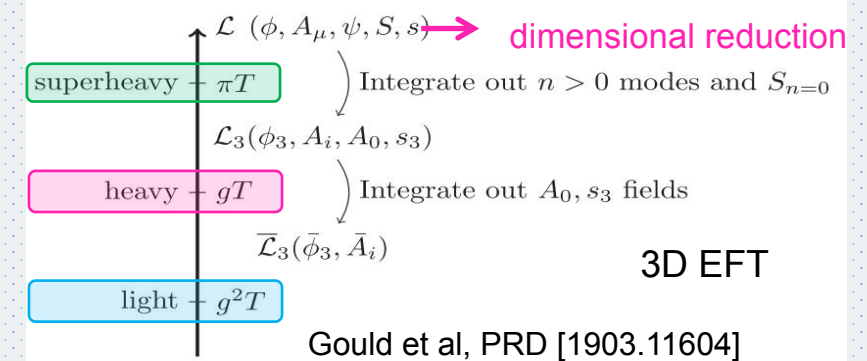
perturbative vs non-perturbative

$m_{h_2} = 400 \text{ GeV}, b_4 = 0.25, \sin \theta = -0.05$



xSM (SM+Singlet) Alves, Gonçalves, Ghosh, HG, Sinha, JHEP [1909.05268]

Nonperturbative Method

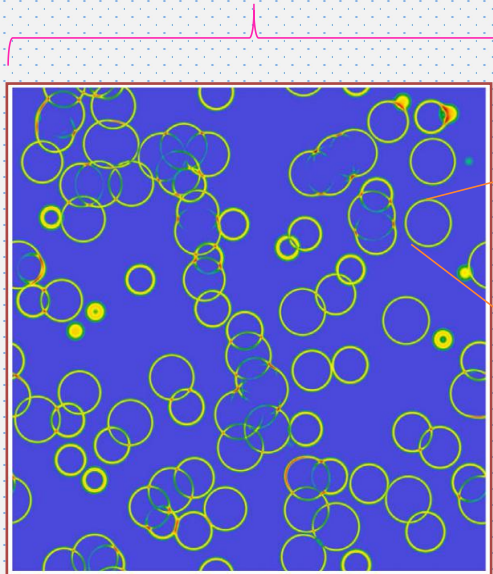
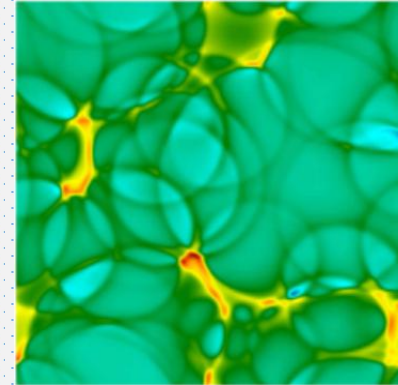


Dimensional Reduction (Status)

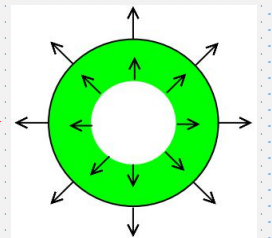
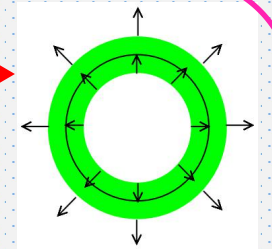
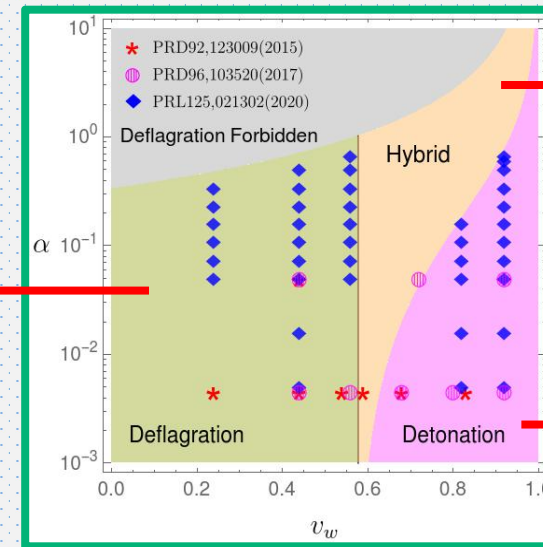
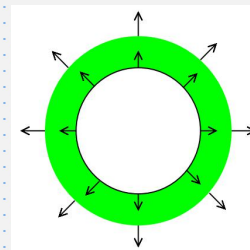
SM	✓	Farakos, Kajantie, Rummukainen, Shaposhnikov (1994)
MSSM	✓	Cline, Kainulainen (1996), Losada (1996), Laine (1996)
xSM (SM + Singlet)	✓	Brauner, Tenkanen, Tranberg, Vuorinen, Weir, JHEP [1609.06230]
ΣSM (SM + Triplet)	✓	Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir, PRD [1802.10500]
2HDM	✓	Gorda, Helset, Niemi, Tenkanen, Weir, JHEP [1802.05056]

Better Understand the Picture

- How fast the wall expands?
- How the energy is distributed?
- Are there new phenomena?
- ...



Hindmarsh et al, 2015



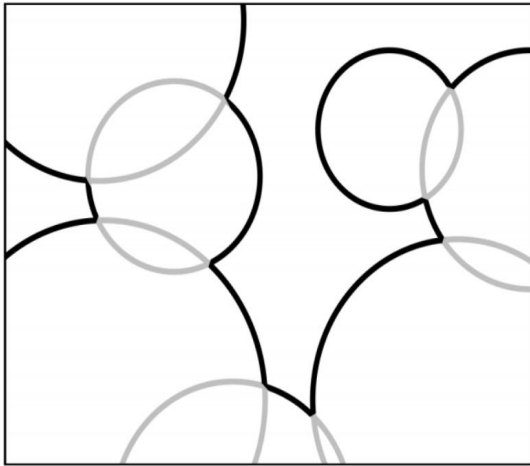
Espinosa, Konstandin, No, Servant JCAP [1004.4187]

Gravitational Wave Production

The current understanding:

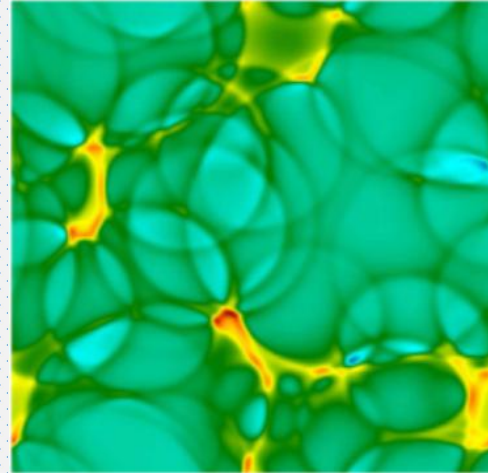
$$\square \bar{h}_{\mu\nu} = -\frac{16\pi G}{c^4} T_{\mu\nu}$$

energy near the wall



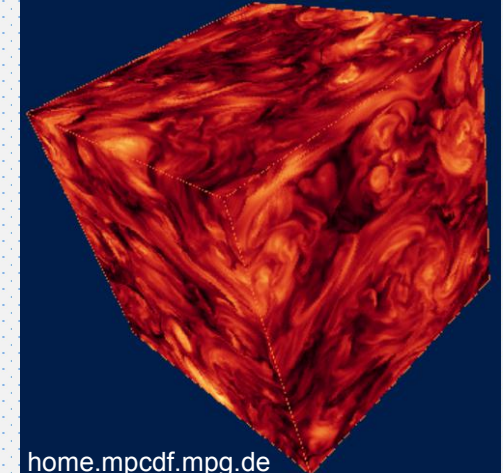
Bubble Collisions

fluid kinetic energy



Sound Waves

turbulent fluid + magnetic field



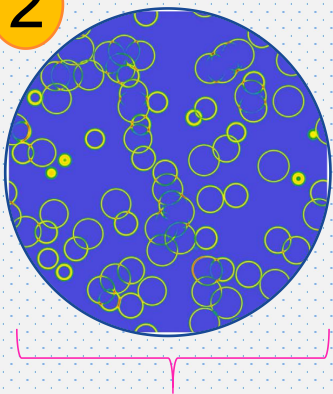
home.mpcdf.mpg.de

Magnetohydrodynamic Turbulence

Observable:

$$\Omega_{\text{GW}}(f) = \frac{d\rho_{\text{GW}}}{\rho_c d \log f}$$

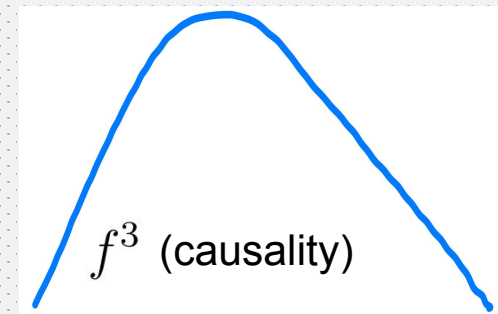
2

Hubble size: $1/H^*$

Basic Properties

$$f_{\text{now}} = 1.65 \times 10^{-5} \left(\frac{f_{\text{PT}}}{\beta} \right) \left(\frac{\beta}{H_*} \right) \left(\frac{T_*}{100 \text{ GeV}} \right) \left(\frac{g_*}{100} \right)^{1/6} \text{ Hz}$$

~100-1000



Cai, Pi, Sasak, PRD [1909.13728]

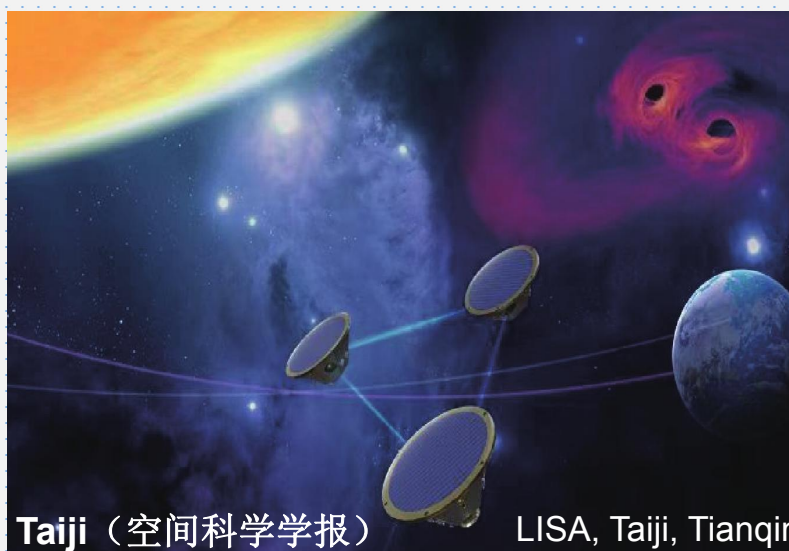
nHz (~100MeV) QCD scale

~mHz : (~100GeV) weak scale

~100Hz (~PeV - EeV) high scale



中国脉冲星测时阵列 (CPTA)



Taiji (空间科学学报)

LISA, Taiji, Tianqin



LIGO

ligo.caltech.edu

Bubble Collisions

Envelope approximation:

Kosowsky, Turner, Watkins, Kamionkowski,
PRL69,2026(1992), PRD45,4514(1992), PRD47,4372(1993), PRD [9310044]

$$h^2 \Omega_{\text{BC}}(f) = 1.67 \times 10^{-5} \left(\frac{100}{g_*} \right)^{1/3} \Delta(v_w) \left(\frac{H_n}{\beta} \right)^2 \left(\frac{\kappa \phi \alpha}{1 + \alpha} \right)^2 S_{\text{env}}(f)$$

simulation

analytical

$$\Delta = \frac{0.11 v_w^3}{0.42 + v_w^2},$$

$$\frac{f_*}{\beta} = \frac{0.62}{1.8 - 0.1 v_w + v_w^2},$$

$$S_{\text{env}} = \left[\frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}} \right]$$

Huber, Konstandin, JCAP [0806.1828]

Chiara Caprini et al JCAP [1512.06239]

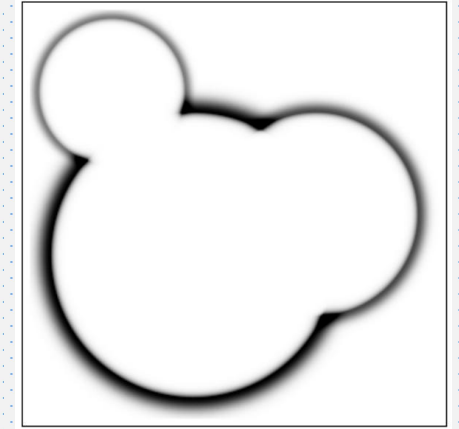
$$\Delta = \frac{0.48 v_w^3}{1 + 5.3 v_w^2 + 5 v_w^4},$$

$$\frac{f_*}{\beta} = \frac{0.35}{1 + 0.069 v_w + 0.69 v_w^4},$$

$$S_{\text{env}} = \left[c_l \left(\frac{f}{f_{\text{env}}} \right)^{-3} + (1 - c_l - c_h) \left(\frac{f}{f_{\text{env}}} \right)^{-1} + c_h \left(\frac{f}{f_{\text{env}}} \right) \right]^{-1}$$

$$(c_l = 0.064, \quad c_h = 0.48)$$

Jinno, Takimoto, PRD [1605.01403]



thin shell of uncollided walls

Bubble Collisions: Recent Development

- Wall thickness (probe effective potential)

Cutting et al, PRD [2005.13537], Gould et al, PRD [2107.05657], Mégevand, Membiela, JCAP [2302.13349]

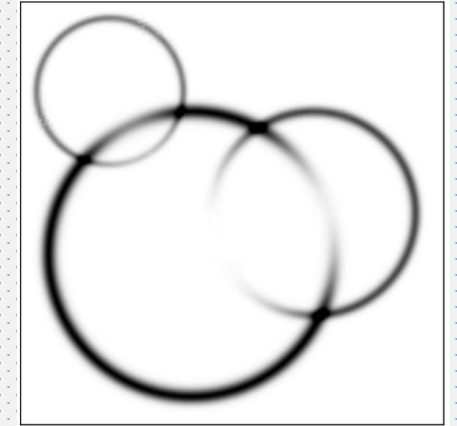
- Duration and Expanding Universe

Zhong, Gong, Qiu, JHEP [2107.01845]

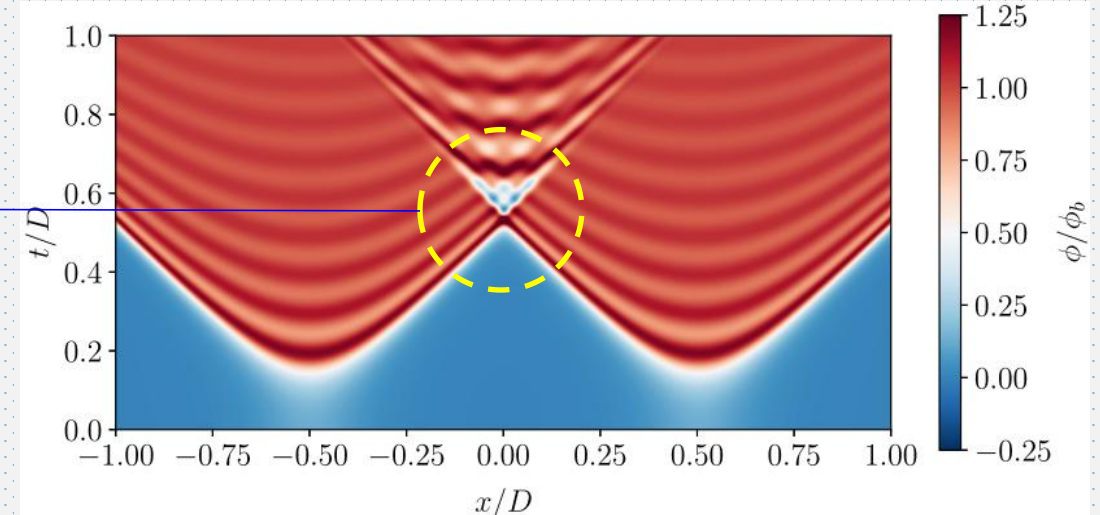
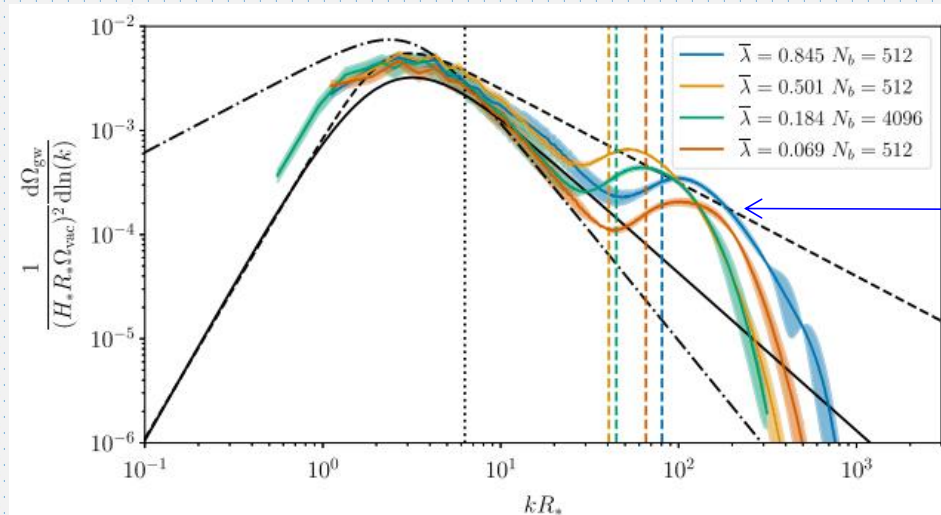
- Scalar + Gauge

Di, Wang, Zhou, Bian, Cai, Liu, PRL [2012.15625], Yang, Bian, PRD [2102.01398],
Lewicki, Vaskonen, EPJC [2007.04967]

Bulk flow model



Jinno, Takimoto, JCAP [1707.03111],
Konstandin, JCAP [1712.06869]

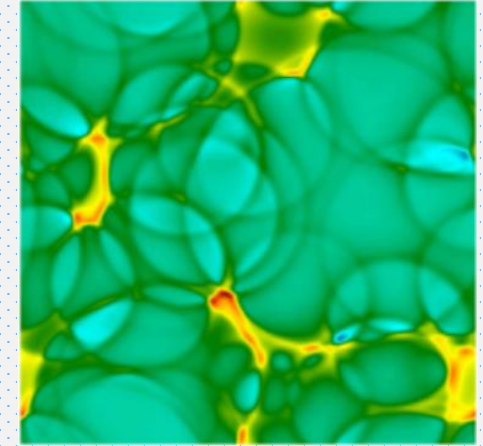


Sound Waves

Hindmarsh, Huber, Rummukainen, Weir, PRL [1304.2433]

$$T^{ij} \propto (p + e) v^i v^j$$

$$h^2 \Omega_{\text{sw}}(f) = 2.65 \times 10^{-6} \left(\frac{100}{g_*} \right)^{\frac{1}{3}} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 v_w S_{\text{sw}}(f) \Upsilon(\tau_{\text{sw}})$$



$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}} H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

HG, Sinha, Vagie, White, JCAP [2007.08537]

Widely adopted, including LIGO, NANOGrav, ...

Phase Transitions in an Expanding Universe: Stochastic Gravitational Waves in Standard and Non-Standard Histories

Huai-Ke Guo (Oklahoma U.), Kuver Sinha (Oklahoma U.), Daniel Vagie (Oklahoma U.), Graham White (TRIUMF) (Jul 16, 2020)

Published in: JCAP 01 (2021) 001 • e-Print: 2007.08537 [hep-ph]



pdf



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cite



claim



reference search



189 citations

Sound Waves: Recent Development

Analytical Modelling

- Refine the sound shell model
- Synergy with simulations

Sound Shell Model

Hindmarsh, PRL [1608.04735]

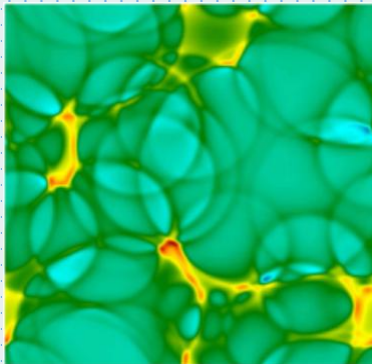
Hindmarsh, Hijazi, JCAP [1909.10040]

HG, Sinha, Vagie, White, JCAP [2007.08537]

Cai, Wang, Yuwen, PRD Letter [2305.00074]

Pol, Procacci, Caprini [2308.12943]

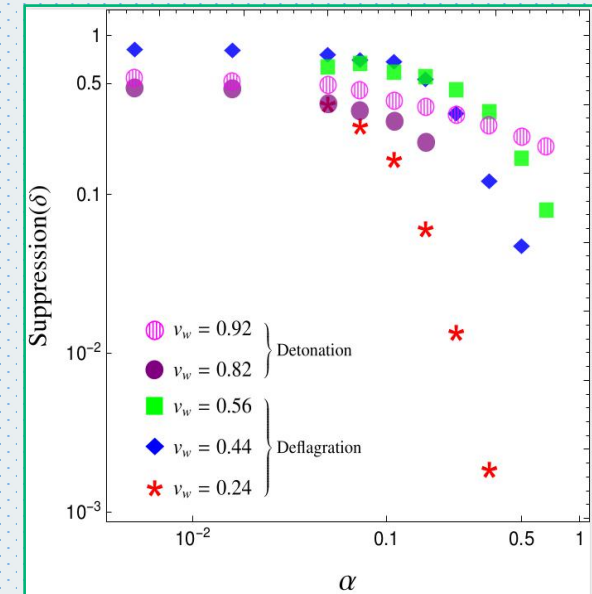
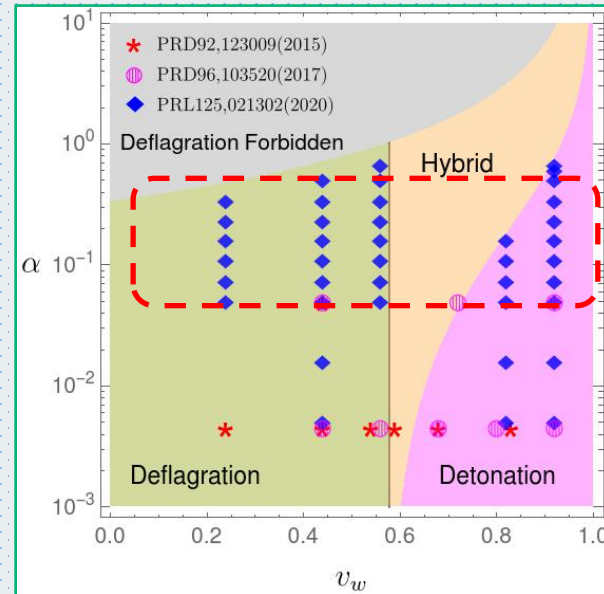
$$v_{\mathbf{q}}^i = \sum_{n=1}^{N_b} v_{\mathbf{q}}^{i(n)}$$



Numerical Simulation

- Suppression found for strong transitions with small v_w
- Need to cover more parameter space (very strong PT)

$$h^2 \Omega_{\text{sw}}(f) = 2.65 \times 10^{-6} \left(\frac{100}{g_*} \right)^{\frac{1}{3}} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 v_w S_{\text{sw}}(f) \Upsilon(\tau_{\text{sw}})$$



Cutting, Hindmarsh, Weir, PRL [1906.00480]

Magnetohydrodynamic Turbulence

Earlier studies based on Kolmogorov spectrum:

Kamionkowski, Kosowsky, Turner, PRD [9310044]

Kosowsky, Mack, Kahniashvili, PRD [0111483]

Gogoberidze, Kahniashvili, Kosowsky, PRD [0705.1733]

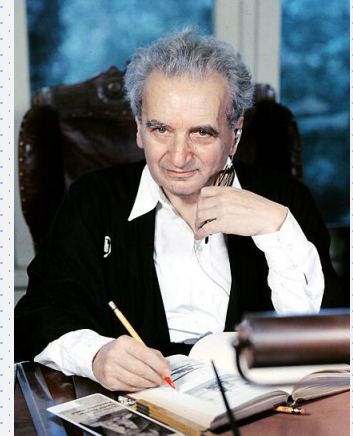
$$T^{ij} \sim (p + e)v^i v^j - B_i B_j$$

$$h^2 \Omega_{\text{turb}}(f) = 3.35 \times 10^{-4} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{\frac{3}{2}} \left(\frac{100}{g_*} \right)^{1/3} v_w S_{\text{turb}}(f)$$

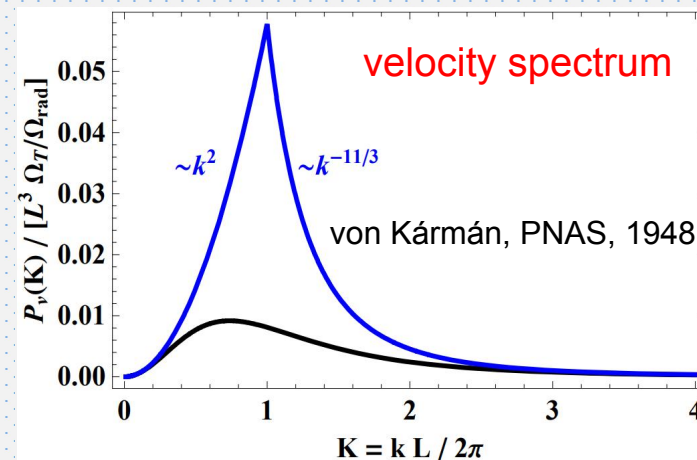
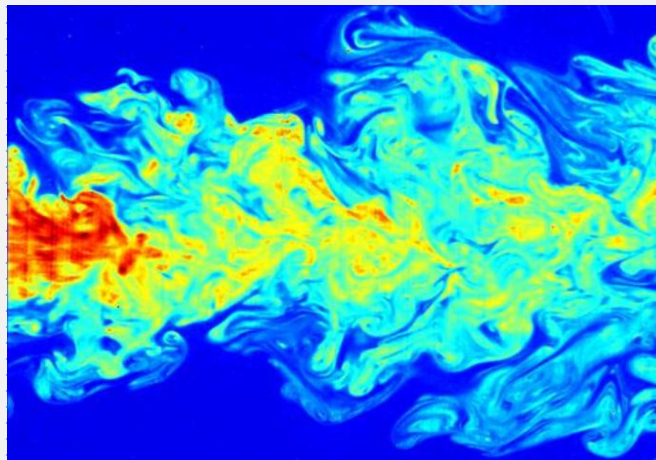
Caprini, Durrer, Servant, JCAP [0909.0622] (used von Kármán's spectrum)



Andrey Nikolaevich Kolmogorov



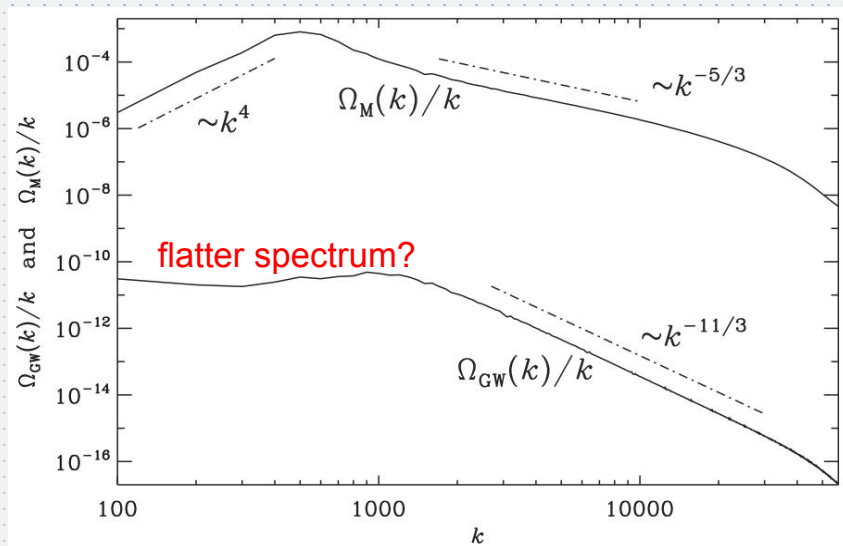
Theodore von Kármán



2 Magnetohydrodynamic Turbulence: Recent Development

Progress on **numerical** simulations, and **analytical** modellings

- Strong dependence on initial conditions
- Flatter spectrum at low frequency (violate causality?)

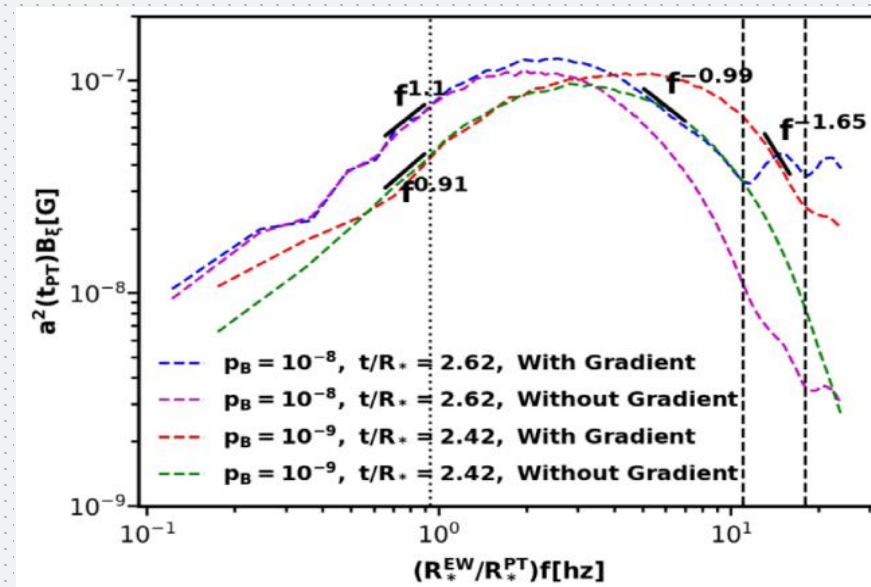


Pol et al, PRD [1903.08585]

Modelling: Sharma, Brandenburg, PRD [2206.00055]
 Time decorrelation: Auclair et al, JCAP [2205.02588]
 Decay, viscosity: Dahl et al, PRD [2112.12013]
 Polarization: Pol et al, JCAP [2107.05356]

as initial conditions?

Magnetic Field Generation (simulation)



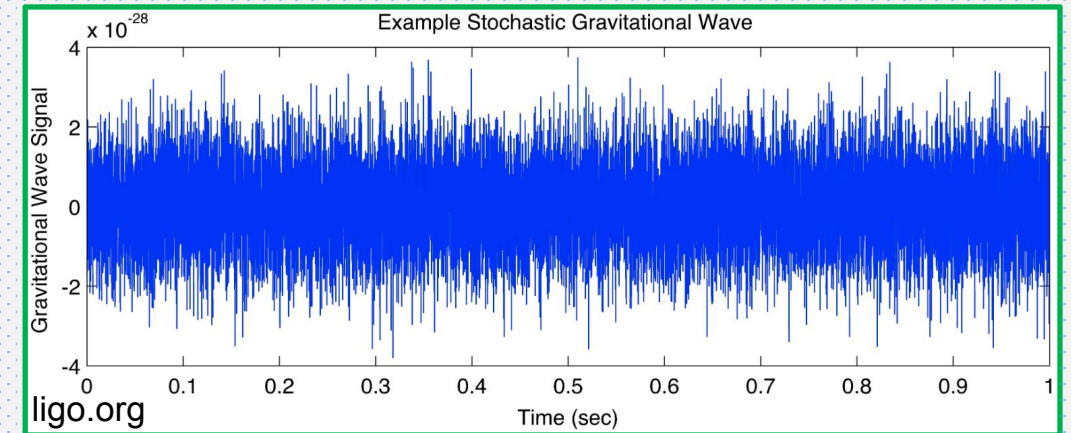
Di,Wang,Zhou,Bian,Cai, PRL [2012.15625]
 Yang,Bian,PRD [2102.01398]

Romero, Martinovic, Callister, [HG](#), Martínez, Sakellariadou, Yang, Zhao, PRL [2102.01714]

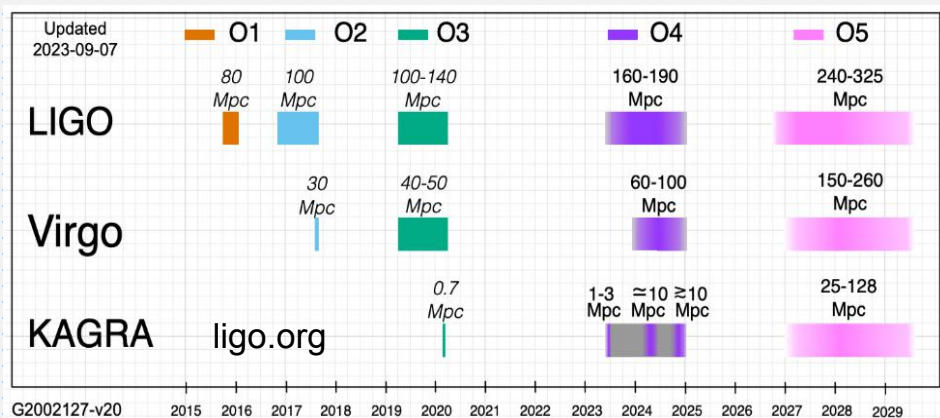
- No Evidence for Broken Power Law Signal
- No Evidence for Bubble Collision Domination Signal
- No Evidence for Sound Waves Domination Signal

See also: Jiang, Huang, JCAP [2203.11781], Yu, Wang, PRD [2211.13111]

stochastic GWs: noise-like



O1+O2+O3@LIGO (H1, L1), Virgo

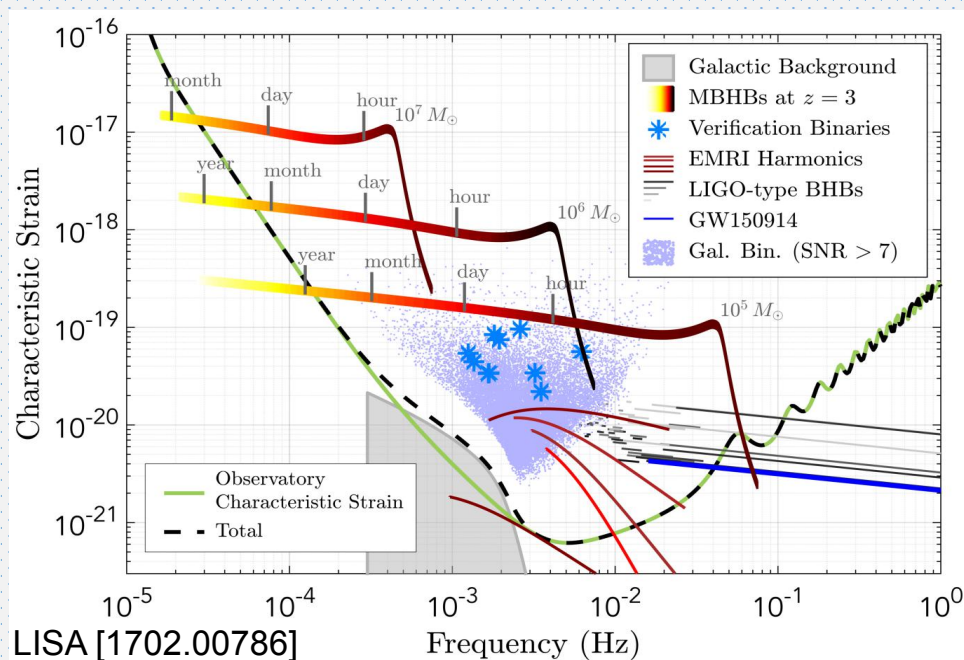


solution:
cross-correlation



Detection with a single detector

- Complicated, and correlated noise
- Complications from time-delay interferometry
- Solution: null channel method, or with a network

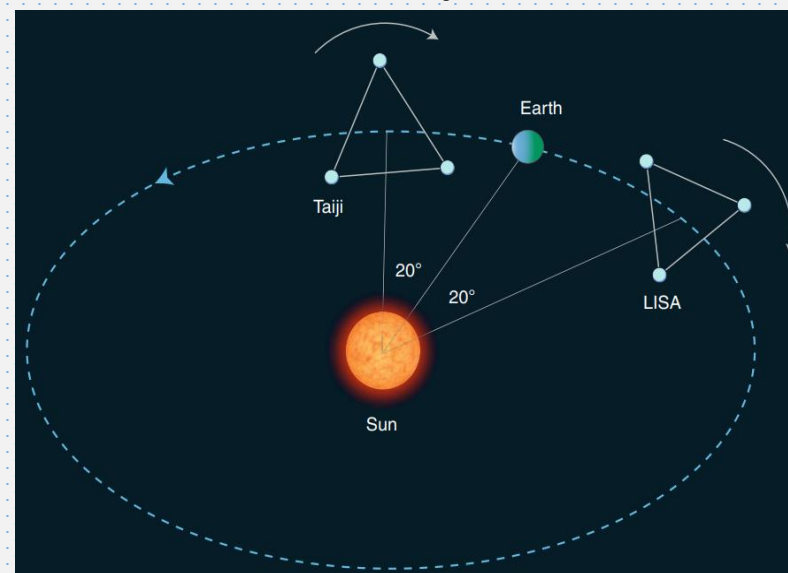


galactic foreground + astro background + cosmic background

SGWB detectable down to $\Omega_{GW} \sim \mathcal{O}(10^{-13})$

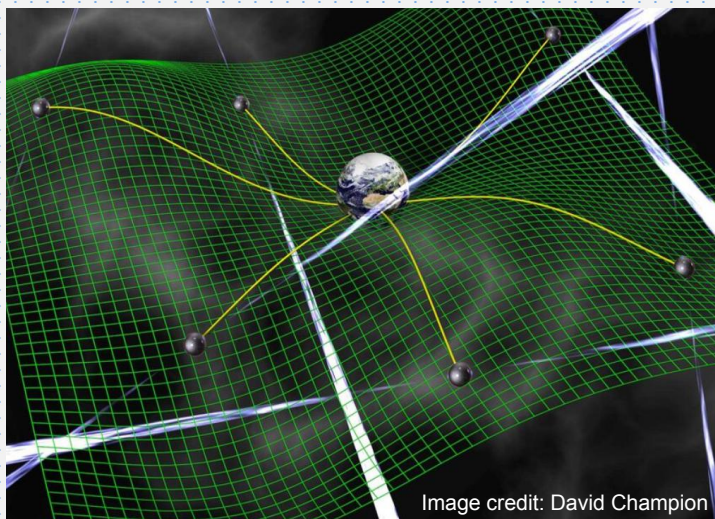
Boileau et al, MNRAS [2105.04283]

The LISA–Taiji network

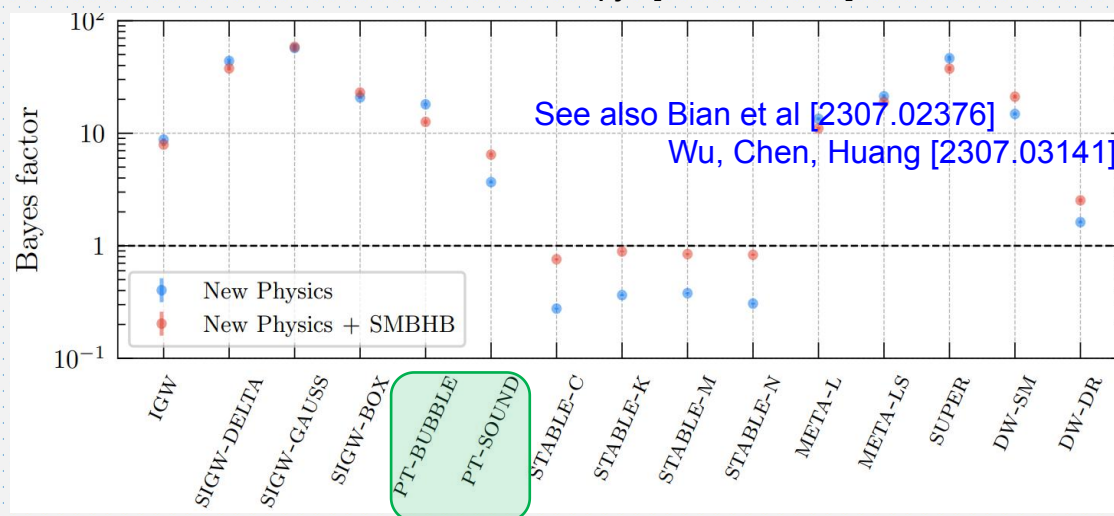


Ruan, Liu, Guo, Wu, Cai, Nature Astron [2002.03603]

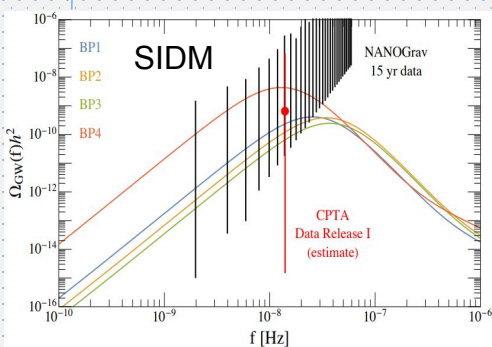
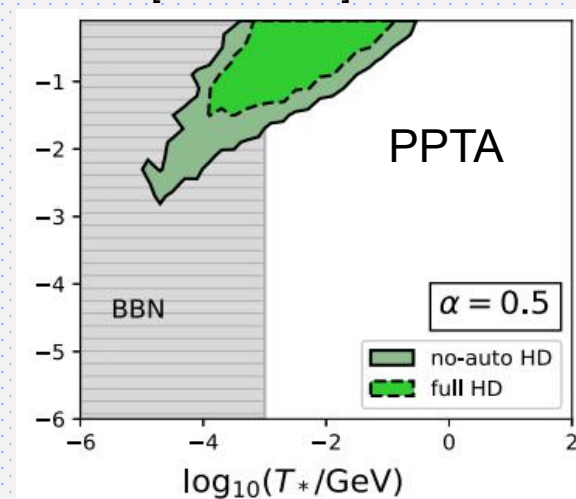
Cai et al [2305.04551]



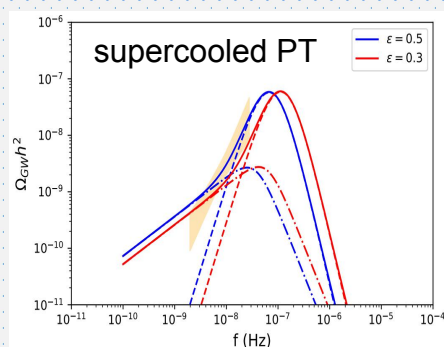
NANOGrav, ApJL [2306.16219]



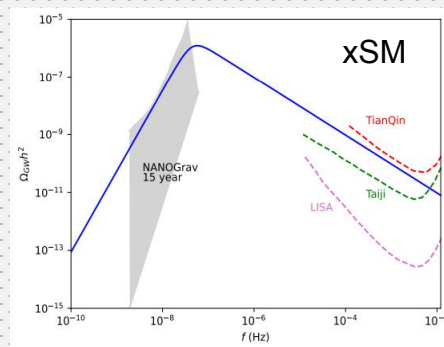
Xue, Bian, Shu, Yuan, Zhu, et al, PRL [2110.03096]



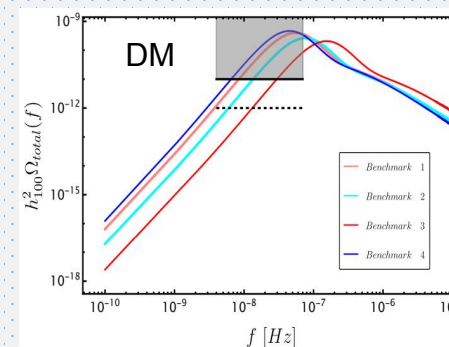
Han, Xie, Yang, Zhang [2306.16966]



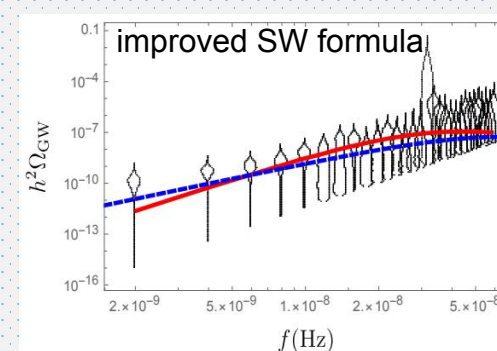
Zu, Zhang, Li, Gu, Tsai, Fan [2306.17239]



Xiao, Yang, Zhang [2307.01072]



Yang, Ma, Jiang, Huang [2306.17827]

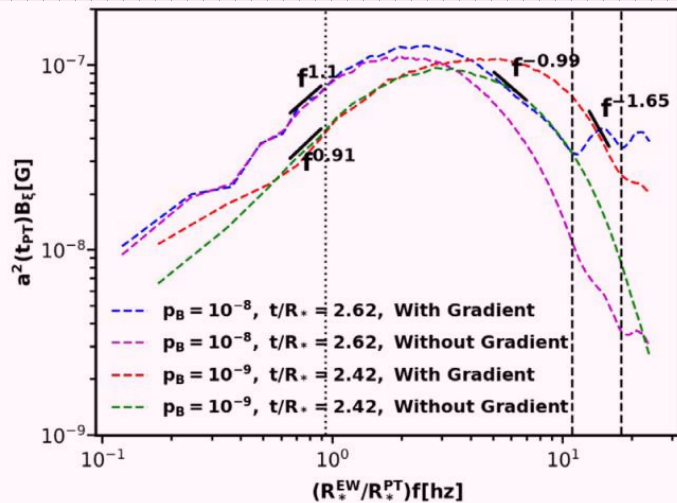


Ghosh, Ghoshal, HG, ... [2307.02259]

and many more...

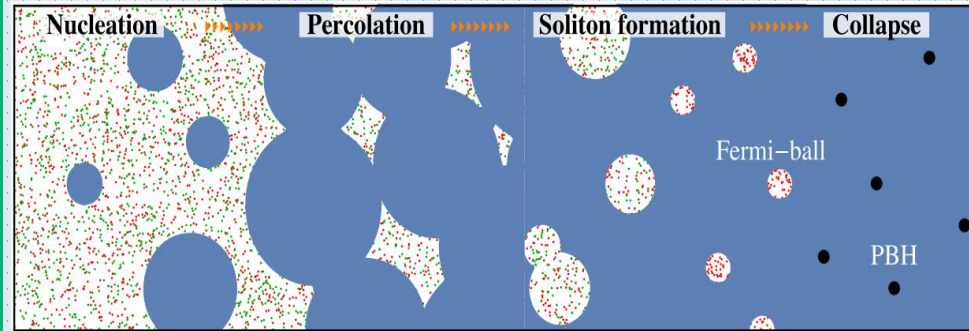
New Observables

Primordial magnetic field



Di, Wang, Zhou, Bian, Cai, PRL [2012.15625]
 Yang, Bian, PRD [2102.01398], ...

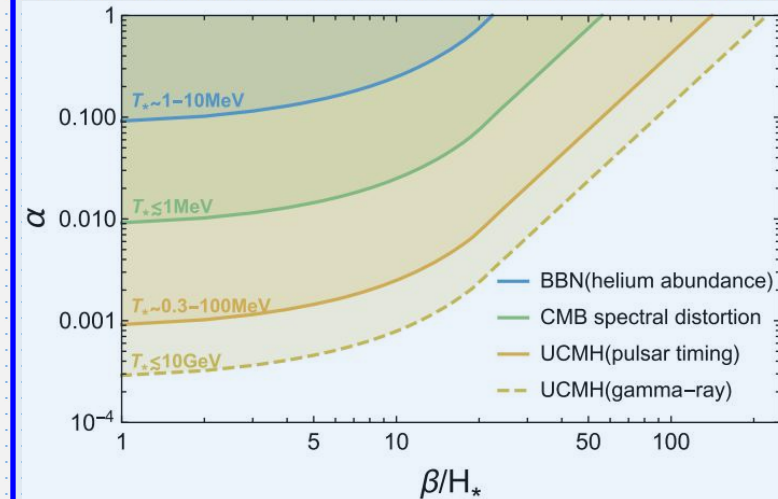
Primordial black holes and Solitons



Hong, Jung, Xie, PRD [2008.04430]
 Kawana, Xie, PLB [2106.00111]
 Lu, Kawana, Xie, PRD [2202.03439]
 Liu, Bian, Cai, Guo, Wang, PRD [2106.05637]

and more...

Curvature perturbations



Liu, Bian, Cai, Guo, Wang, PRL [2208.14086]
 Jiang, Liu, Sun, Wang, PLB [1512.07538]

GW Anisotropy: Geller, Hook, Sundrum, Yuhsin Tsai, PRL [1803.10780]
 Li, Huang, Wang, Zhang, PRD [2112.01409]
 Li, Yan, Huang, PRD [2211.03368]

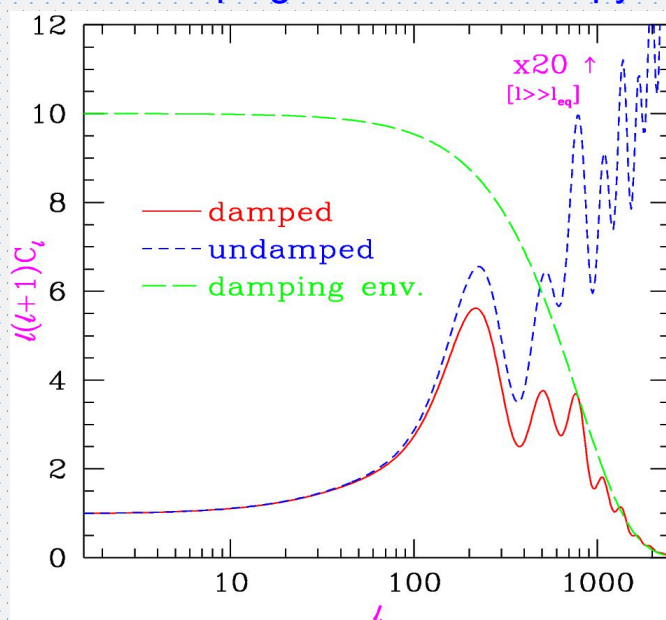
Dissipative Effects as New Observables

- Going beyond the perfect fluid approximation (viscosity, heat conduction)
- Particle physics origin of dissipations (very weak interactions)
- Can be searched for at LIGO, PTA, LISA/Taiji/Tianqin ...

Weinberg, ApJ, 1971

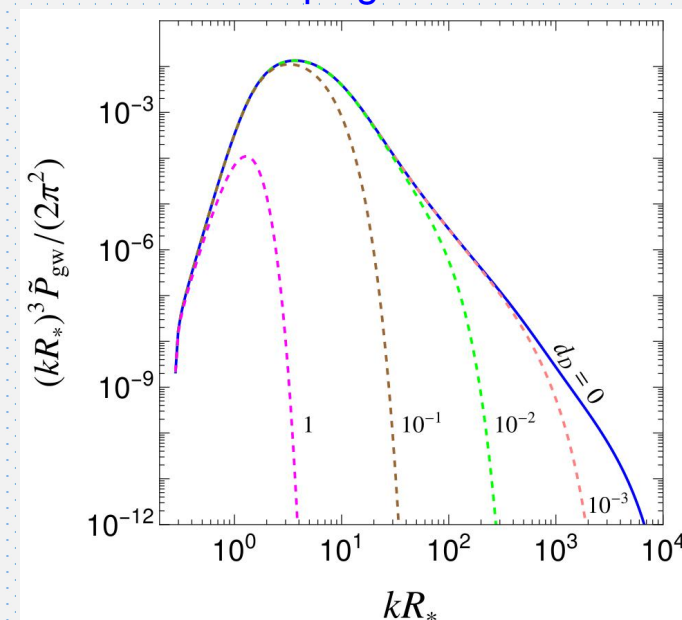
$$\begin{aligned}\Delta T^{ij} &= -\eta \left(\frac{\partial U_i}{\partial x^j} + \frac{\partial U_j}{\partial x^i} - \frac{2}{3} \delta_{ij} \nabla \cdot \mathbf{U} \right) - \zeta \delta_{ij} \nabla \cdot \mathbf{U}, \\ \Delta T^{i0} &= -\chi \left(\frac{\partial T}{\partial x^i} + T \dot{U}_i \right).\end{aligned}\quad (1)$$

Silk damping of CMB Anisotropy



Hu, White, ApJ [9609079]

damping of GW



HG [2310.10927]

Summary

- Comprehensive phenomenological studies
- Significant advances in PT and GW calculations
- Significant advances in experimental detections (LIGO, PTA, etc)
- Future: more precise predictions, and measurements

Thanks!