
GNN for tracking at BESIII and STCF

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Outline

- ◆ BESIII and STCF
- ◆ Methodology
- ◆ Preliminary Results
- ◆ Summary

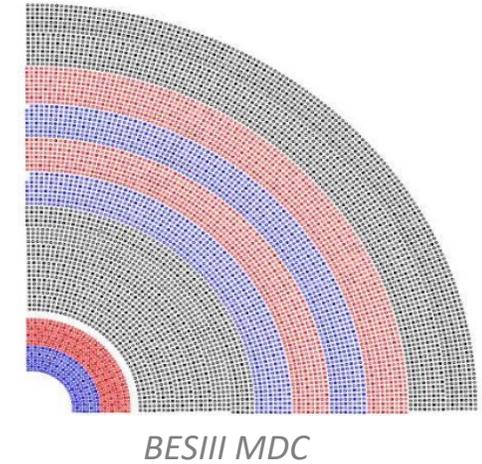
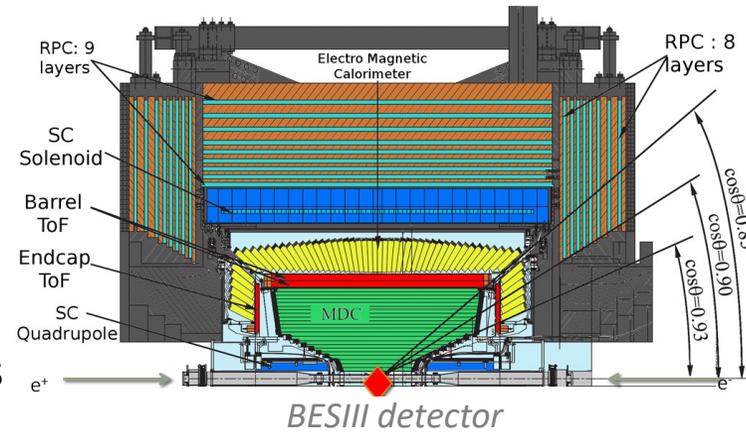
MDC at BESIII and STCF

Beijing electron-positron collider (BEPCII)

- Peak luminosity : $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
- CMS: 2.0 - 4.95 GeV, τ -charm region
- World's largest J/ψ dataset : 10 billion

◆ Main Drift Chamber (MDC) at BESIII

- 43 sense wire layers
- 5 axial wire super-layers, 6 stereo wire super-layers
- dE/dx resolution : 6%
- Momentum resolution : $0.5\% @ 1\text{GeV}/c$

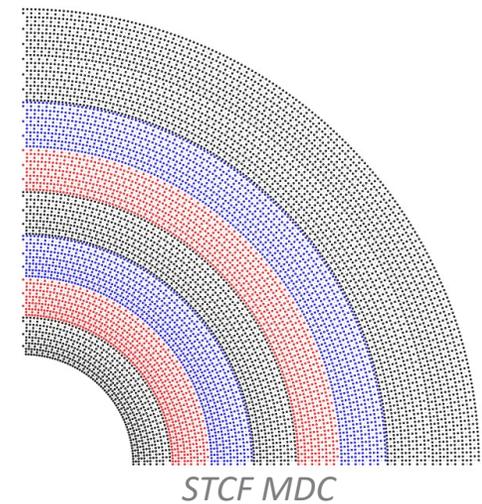
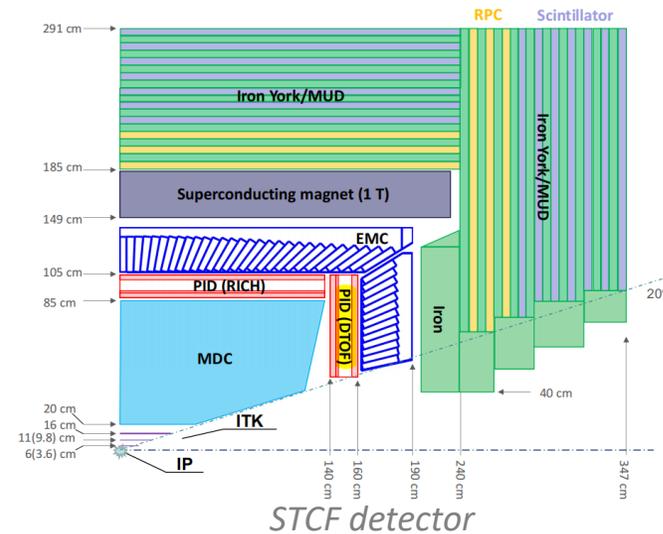


Super Tau-Charm Facility (STCF)

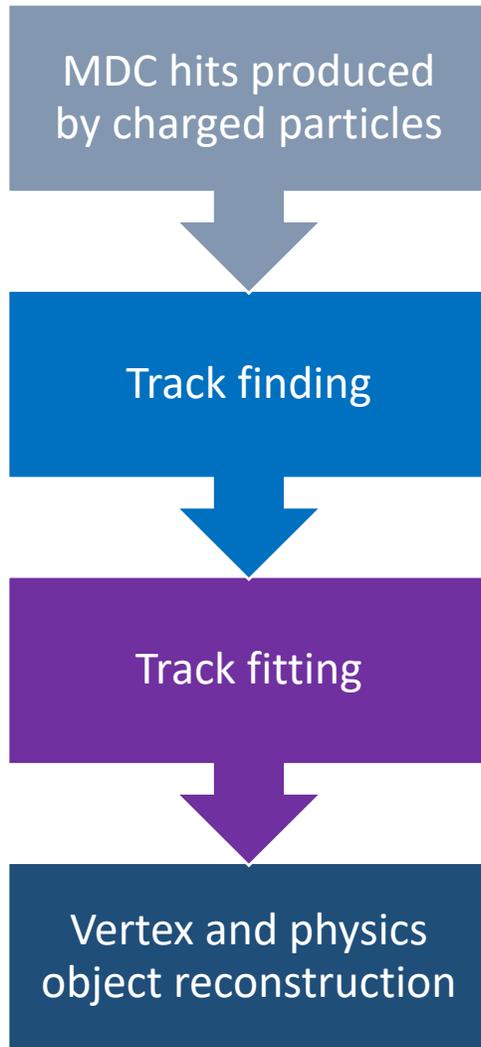
- High Luminosity: $> 0.5 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1} @ 4\text{GeV}$
- CMS: 2.0 - 7 GeV

◆ Main Drift Chamber (MDC) at STCF

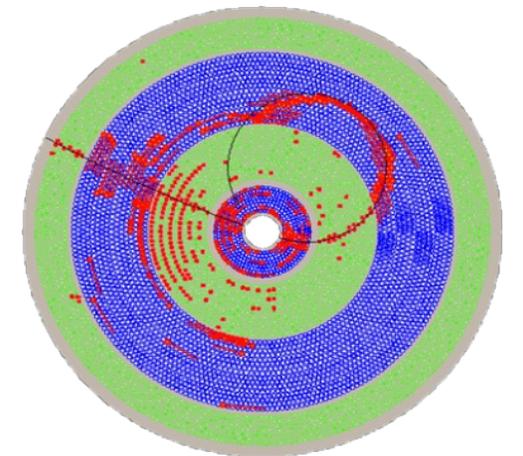
- 48 sense wire layers
- 4 axial wire super-layers, 4 stereo wire super-layers
- dE/dx resolution : $\sim 6\%$
- Momentum resolution : $0.5\% @ 1\text{GeV}/c$



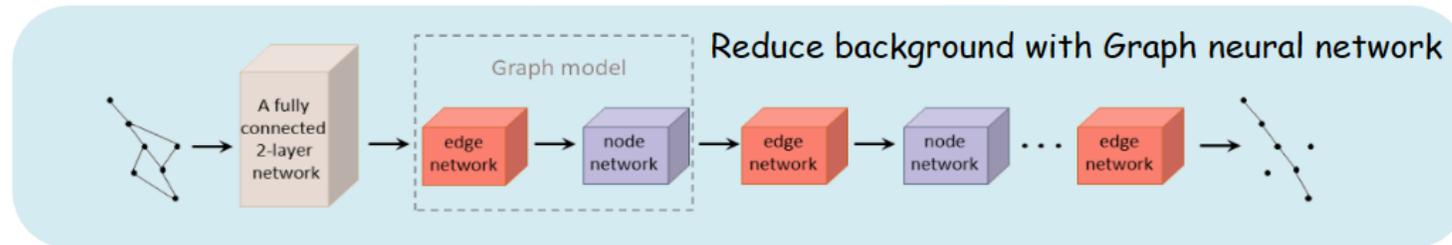
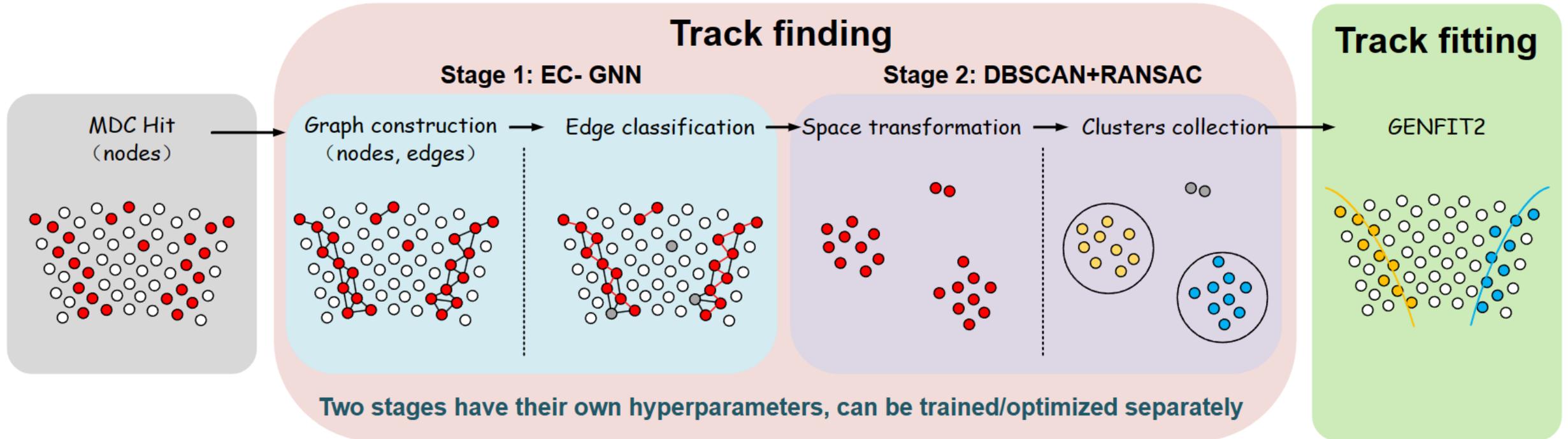
Traditional tracking of drift chamber



- ◆ Build candidate tracks and perform hits assignment
 - Global approach : Hough Transform (HOUGH)
 - Local approach : Template Matching (PAT) Track Segment Finding (TSF)
Combinatorial Kalman Filter (CKF)
- ◆ Estimate the track parameters
 - Global fit : Least Square Method, Runge-Kutta Method
 - Recursive fit : Kalman filter



Methodology: GNN based tracking pipeline



Graph and Graph Neural Network

◆ A type of neural network that are specifically designed to operate on graph-structured data

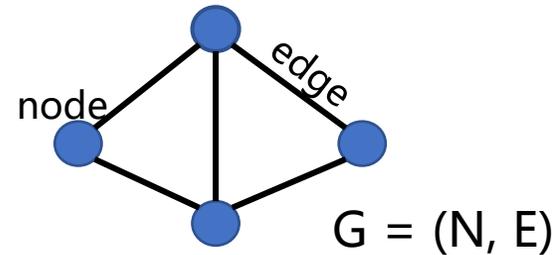
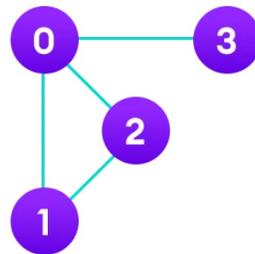
◆ Graph: nodes, edges

◆ Graph \rightarrow Track

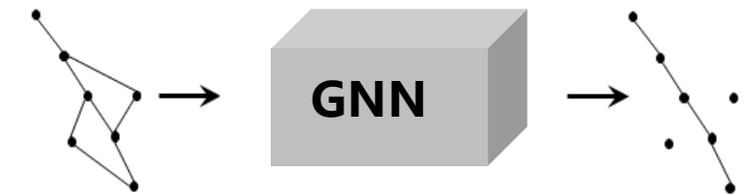
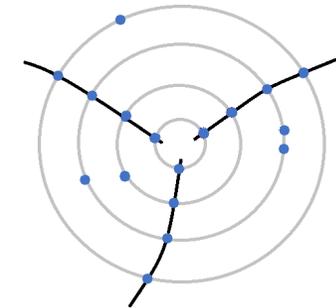
- Nodes \rightarrow Hits
- edges \rightarrow track segments

◆ The storage structure of graphs

- Adjacency matrix ✓
- Adjacency table
- Orthogonal list
- Adjacency multiple table
- Edge set array
-



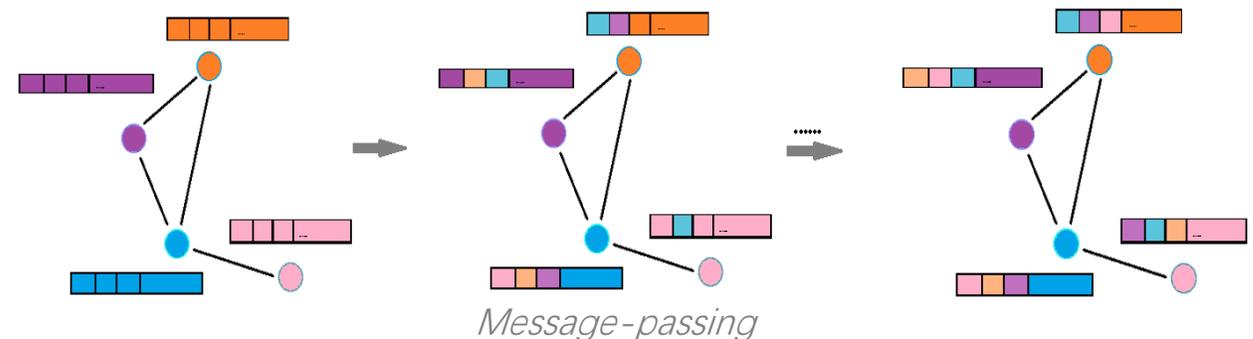
	0	1	2	3
0	0	1	1	1
1	1	0	1	0
2	1	1	0	0
3	1	0	0	0



◆ GNN key idea: propagate information across the graph using a set of learnable functions that operate on node and edge features

◆ Graph Neural Network edge classifier

- High classification score
 \rightarrow *the edge belongs to a true particle track*
- Low classification score
 \rightarrow *it is a spurious or noise edge*



Graph construction at BESIII

To reduce the number of fake edges during graph construction

Pattern Map based on MC simulation at BESIII

◆ Definition of valid neighbors

- Hits on the same layer
 - Two adjacent sense wires on the left and right
- Hits on the next layer

The collection of sense wires that could potentially represent **two successive hits on a track**

◆ MC sample used to build pattern map

- Two million single tracks produced with BESIII offline software (BOSS)
- 5 types of charged particles (e^\pm , K^\pm , μ^\pm , p^\pm , π^\pm)
- $0.05 \text{ GeV}/c < P < 3 \text{ GeV}/c$

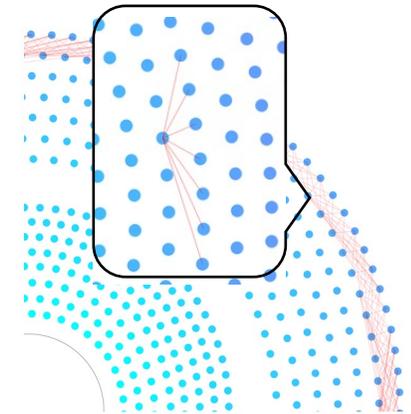
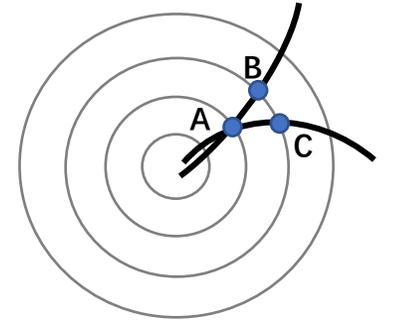
◆ Edge assignment based on Pattern Map

- Hit with its neighbors on the **same layer** and **next layer**
- Hit with its neighbors' neighbors on **one layer apart**

◆ To reduce the size of the graphs, the Pattern Map is further reduced based on **a probability cut**

◆ Graph representation

- Node features (raw time, position coordinates r , ϕ of the sense wires), adjacency matrices, edge labels

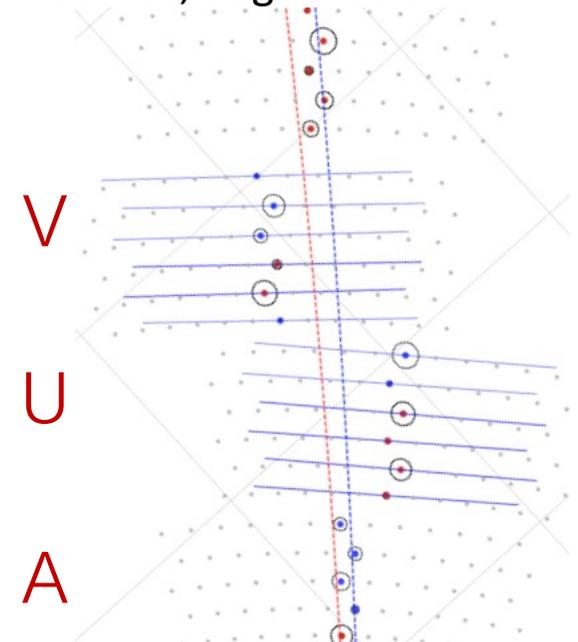
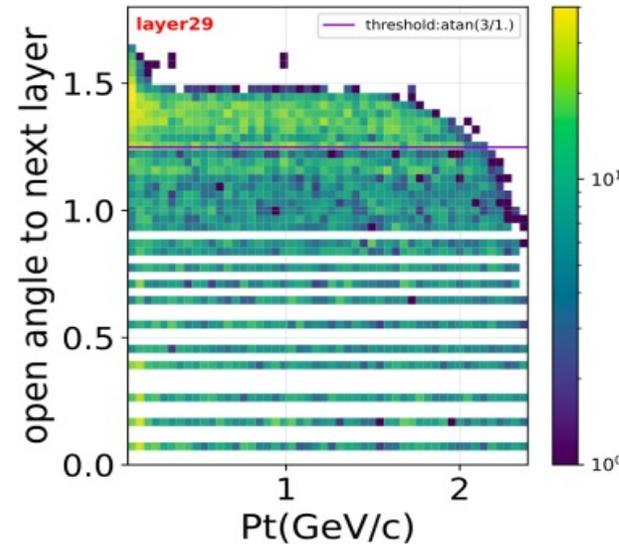
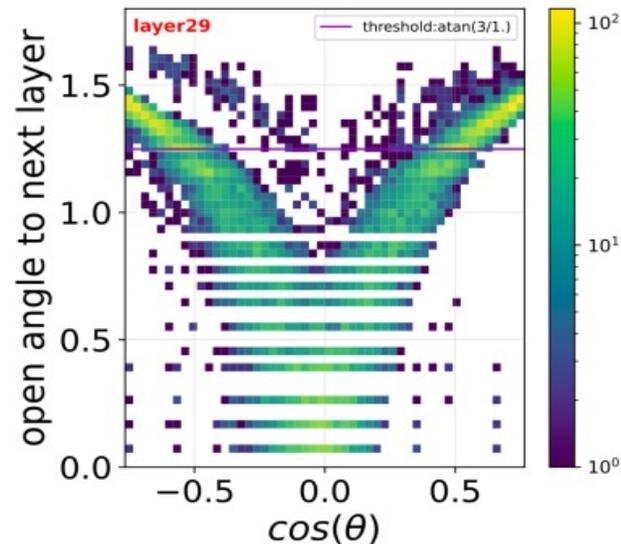
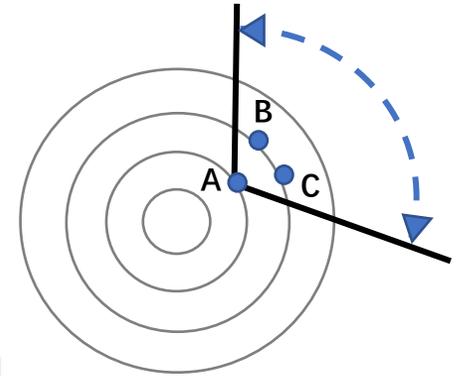


A wire on layer13 and its neighbors on layer14

Graph construction at STCF

Geometric cut at STCF

- ◆ Edge assignment
 - Hit and two adjacent hits on the left and right sides (same layer)
 - Within a certain opening angle (the next layer and one layer apart)
- ◆ Angle range
 - No sense wire efficiency
 - The junction of U-V superlayers (layers 11 and 29) appropriately amplify the threshold
- ◆ Graph representation
 - Node features (raw time, position coordinates r , ϕ of the sense wires), adjacency matrices, edge labels



GNN edge classifier based on PyTorch

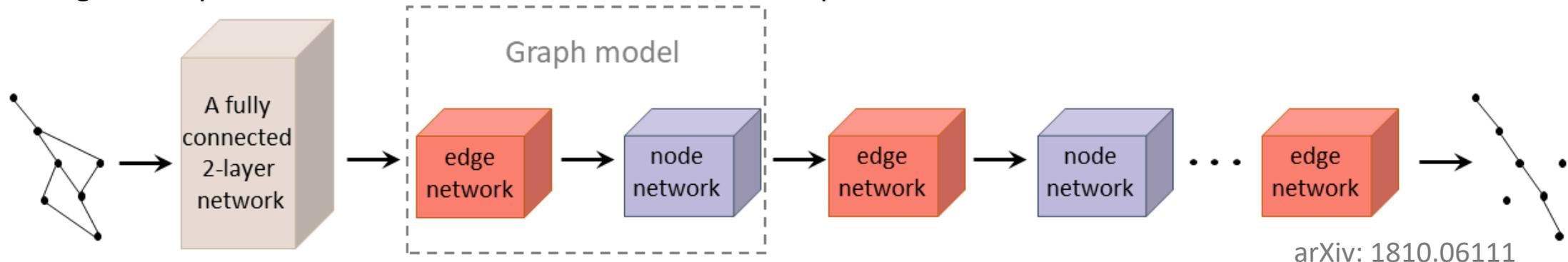
◆ Input network

- Node features embedded in latent space

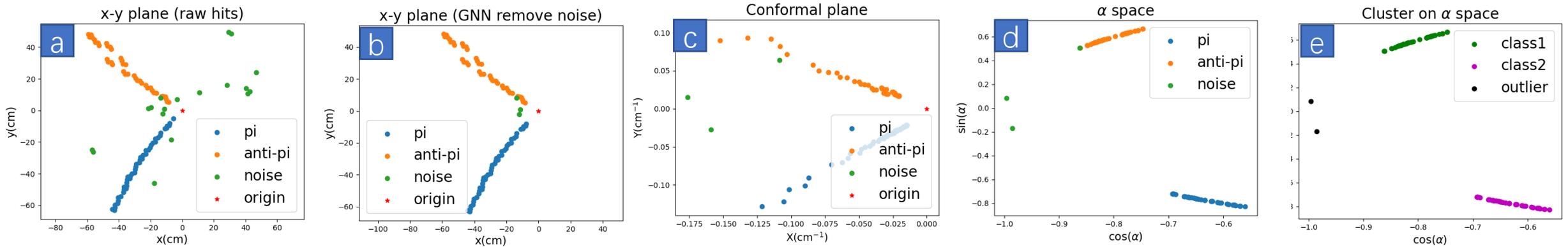
◆ Graph model

- Edge network computes **weights for edges** using the features of the start and end nodes
- Node network computes **new node features** using the edge weight aggregated features of the connected nodes and the nodes' current features
- MLPs
- 8 graph iterations

◆ Strengthen important connections and weaken useless or spurious ones



Clustering based on DBSCAN



a) Original MC data sample

- $J/\Psi \rightarrow \rho^0 \pi^0 \rightarrow \gamma \gamma \pi^+ \pi^-$
- $\pi^+, \pi^- : \text{Pt} (0.2\text{GeV} - 1.4\text{GeV})$

b) Remove noise via GNN

c) Transform to Conformal plane

$$\mathbf{X} = \frac{2x}{x^2+y^2} \quad \mathbf{Y} = \frac{2y}{x^2+y^2}$$

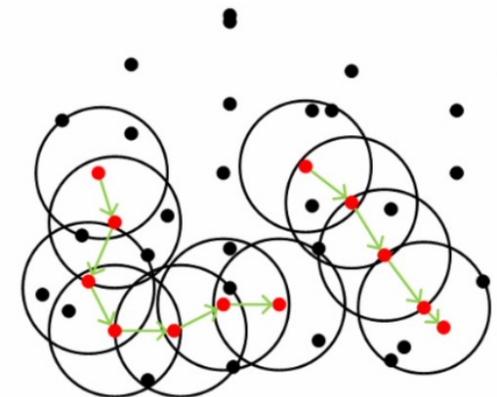
- Circle passing the origin
- transform into a straight line

d) Transform to ' α ' parameter plane

- Hits connected in the X-Y plane in a straight line
- α as the angle between the straight line and X axis
- The parameter space as $\cos\alpha$ and $\sin\alpha$

e) DBSCAN clustering in ' α ' parameter plane

- Density-Based Spatial Clustering of Application with Noise
- Hits in a cluster are considered to be in the same track



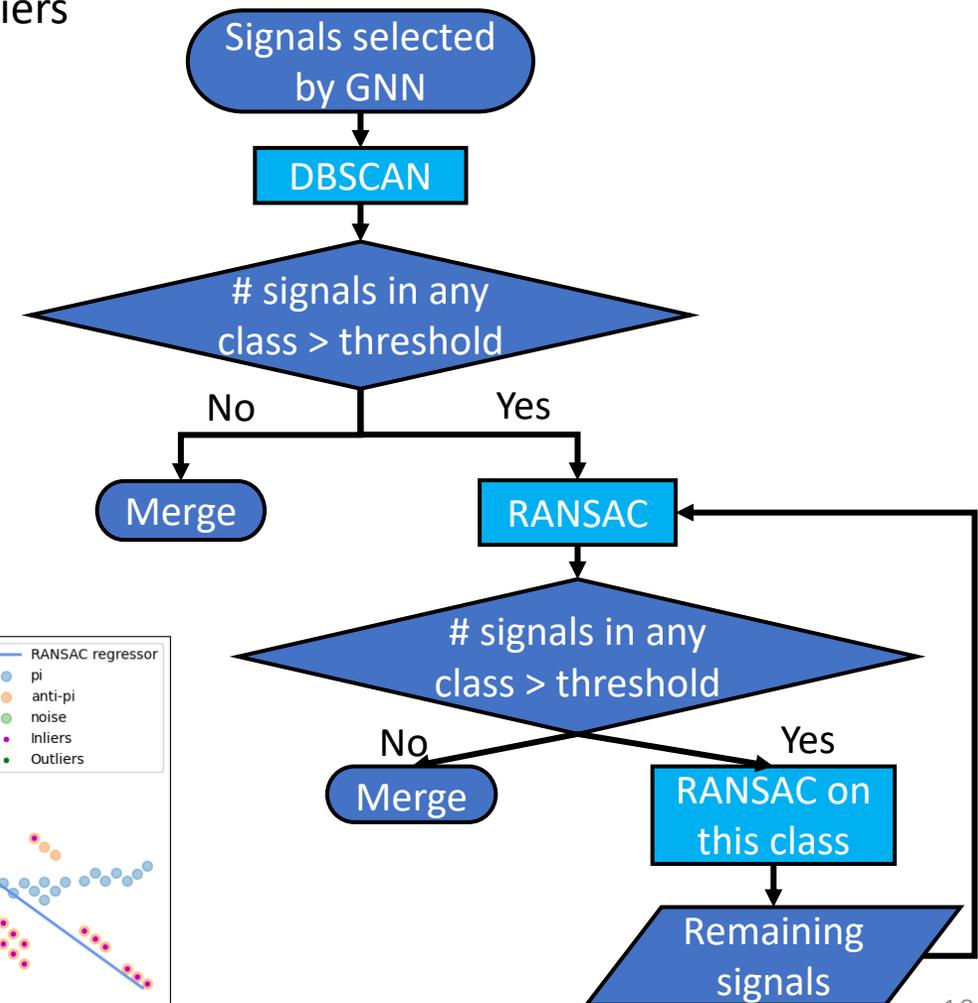
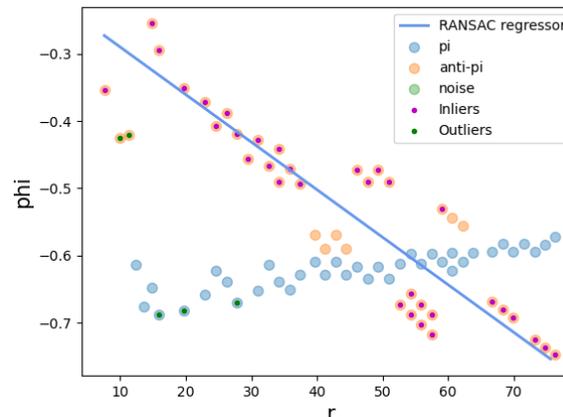
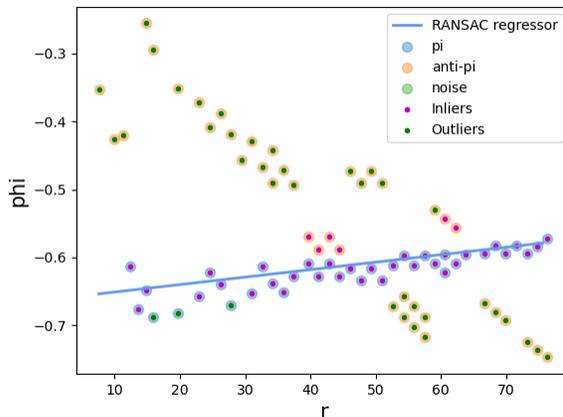
Clustering salvage algorithm RANSAC

◆ Random sample consensus (RANCAS)

- Estimate a mathematical model from the data that contains outliers
- Its good robustness to noise and outliers
- Model can be specified

◆ RANCAS is triggered by the events that DBSCAN processing fails

- Polar coordinate space
- linear model
- Inliers \rightarrow a track , outliers \rightarrow other tracks
- Stop condition: outliers $<$ threshold

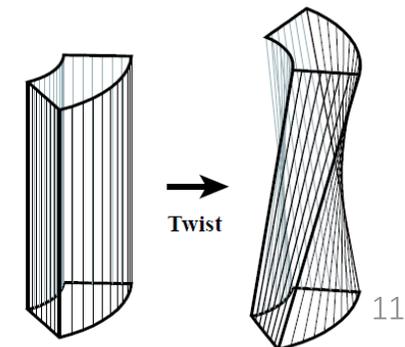
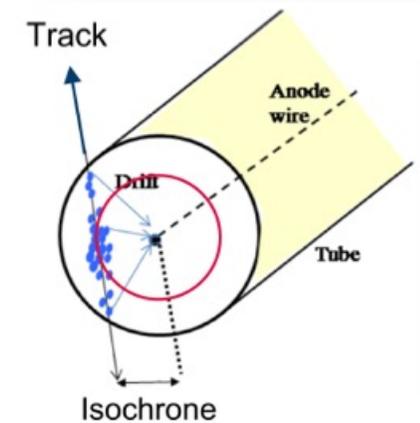
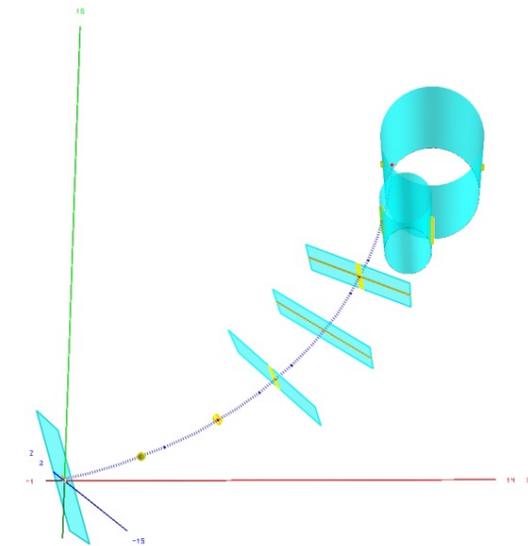


Track fitting

Genfit2

- A Generic Track-Fitting Toolkit
 - Experiment-independent framework
 - PANDA, Belle II, FOPI and other experiments
 - Deterministic annealing filter (DAF) to resolving the left-right ambiguities of wire measurements
- ◆ Configuration: Detector geometry and materials; TGeoManager
 - ◆ Input : Signal wire position, initial values of position and momentum, particle hypothesis for e, μ, π, k, p
 - ◆ Fitting procedure:
 - Start 1st try: drift distance roughly estimated from TDC、 ADC of sense wires
 - Iteration to update information of drift distance, left-right assignment, hit position on z direction and entrancing angle in the cell et al.

$$t_{\text{drift}} = t_{\text{TDC}} - t_{\text{EST}} - t_{\text{flight}} - t_{\text{wp}} - t_{\text{elec}}$$



Performance of filtering noise at BESIII

◆ Dataset

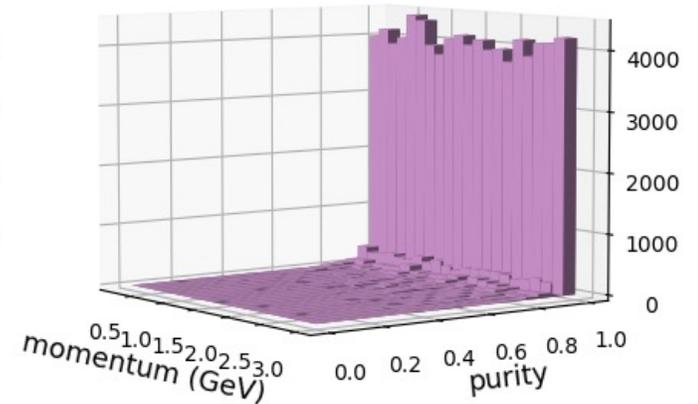
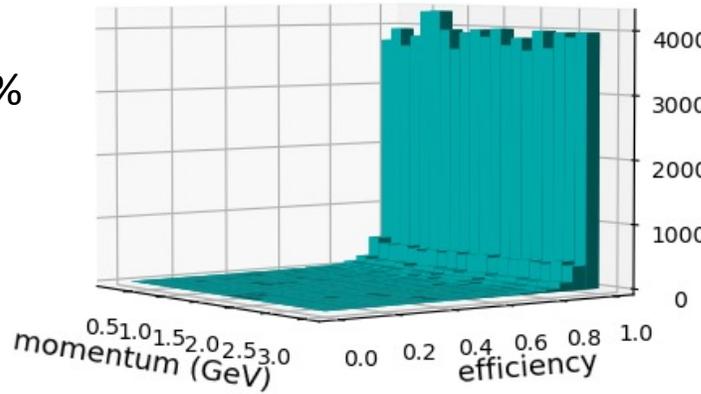
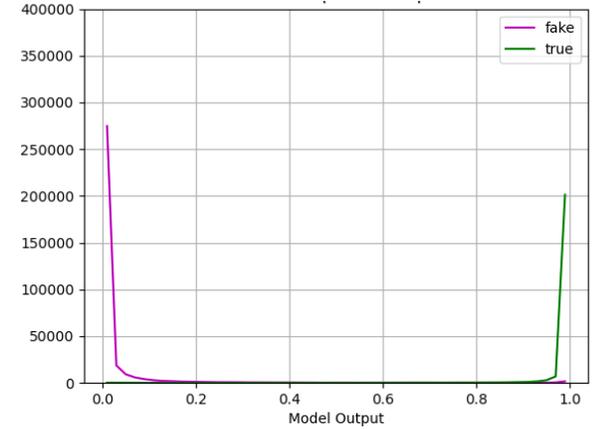
- Single-particle (e^\pm , K^\pm , μ^\pm , p^\pm , π^\pm) MC sample
- $0.2 \text{ GeV}/c < P < 3.0 \text{ GeV}/c$
- Mixed with BESIII random trigger data as background (~45% hits)
- Train: Validation: Test = 4: 1: 1

◆ Hit selection performance

- The preliminary results show that GNN provides high efficiency and purity of hits selection

- *Hit selection Efficiency* : $\frac{N_{signal}^{predicted}}{N_{signal}^{real}}$ 98.7%

- *Hit selection Purity* : $\frac{N_{signal}^{predicted}}{N_{all}^{predicted}}$ 96.5%

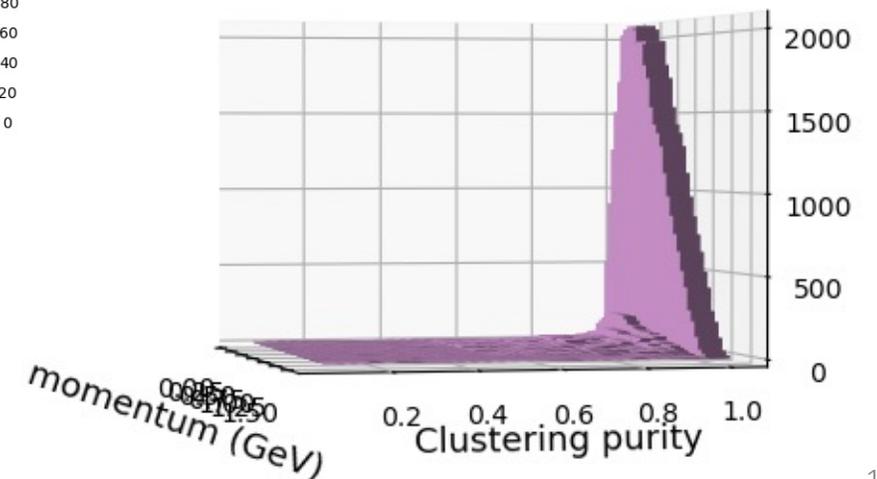
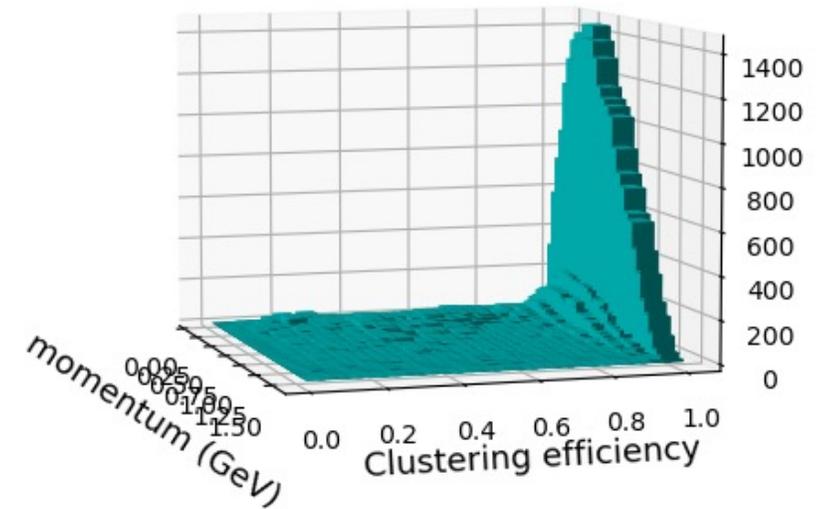
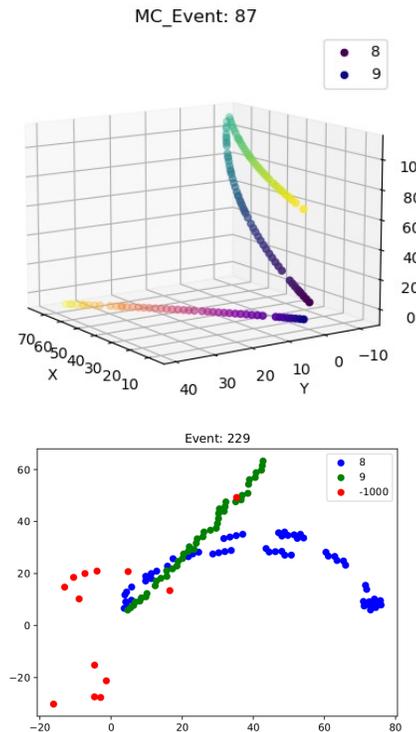
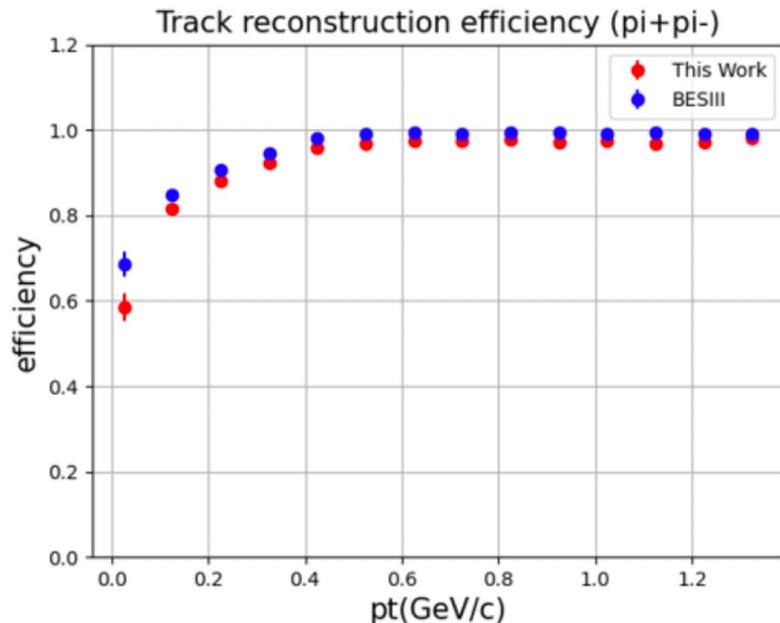


Efficiency and purity can be balanced by adjusting the model parameter

Preliminary tracking performance at BESIII

◆ Particle reconstructed performance

- $J/\psi \rightarrow \rho^0 \pi^0 \rightarrow \gamma \gamma \pi^+ \pi^-$ from MC simulation
- $track\ eff = \frac{N_{rec\ tracks}}{N_{total\ tracks}}$
- Efficiency loss mainly due to track finding (clustering):
 - multi-circular, decays, interaction with detector boundary/material,
 - 2D crossing tracks



Performance of filtering noise at STCF

◆ Dataset

- $J/\Psi \rightarrow \rho^0\pi^0 \rightarrow \gamma\gamma\pi^+\pi^-$ from MC simulation
- Mixing background (Luminosity-related, Beam-gas effect, Touschek effect) within the framework

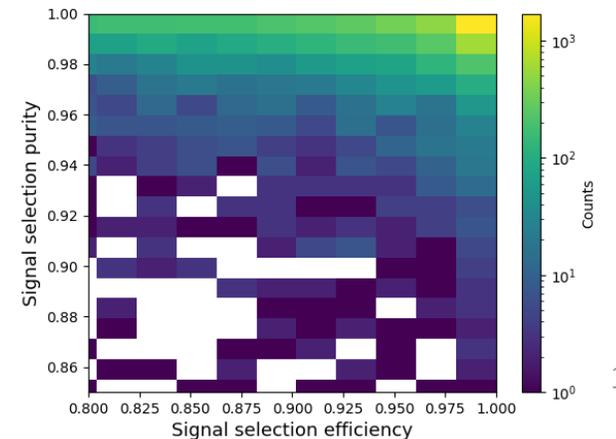
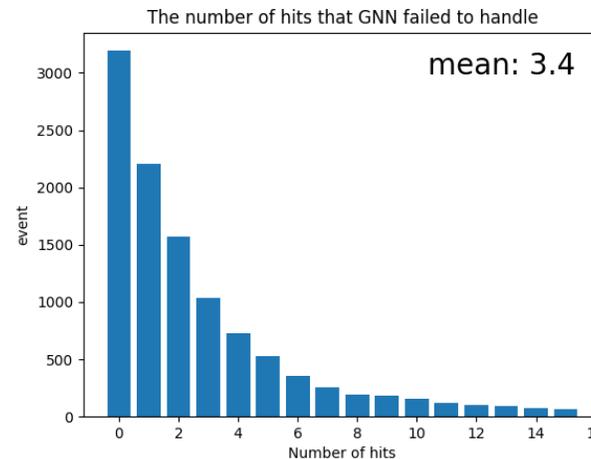
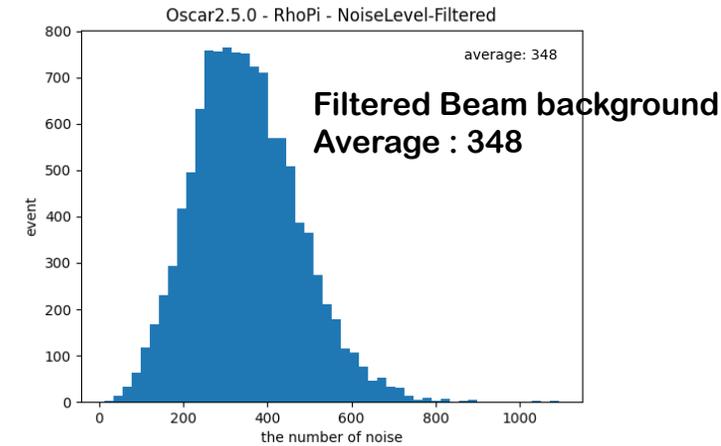
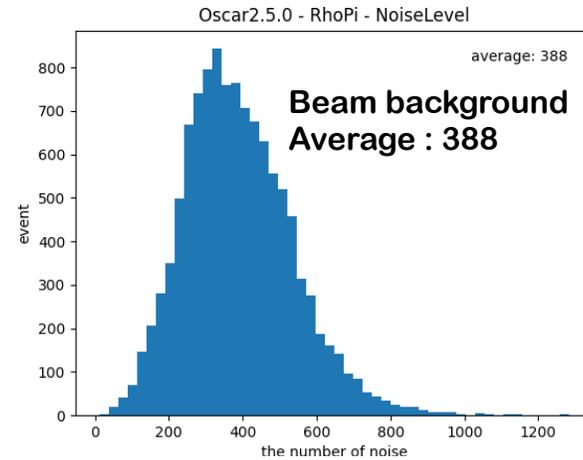
◆ Hit selection performance

- The background includes ‘track’ background, after removal, the noise level is 348

- *Hit selection Efficiency* : $\frac{N_{signal}^{predicted}}{N_{signal}^{real}}$ 91.7%

- *Hit selection Purity* : $\frac{N_{signal}^{predicted}}{N_{all}^{predicted}}$ 97.0%

- *Remove noises rate*: $\frac{N_{noise}^{predicted}}{N_{noise}^{real}}$ 99.0%



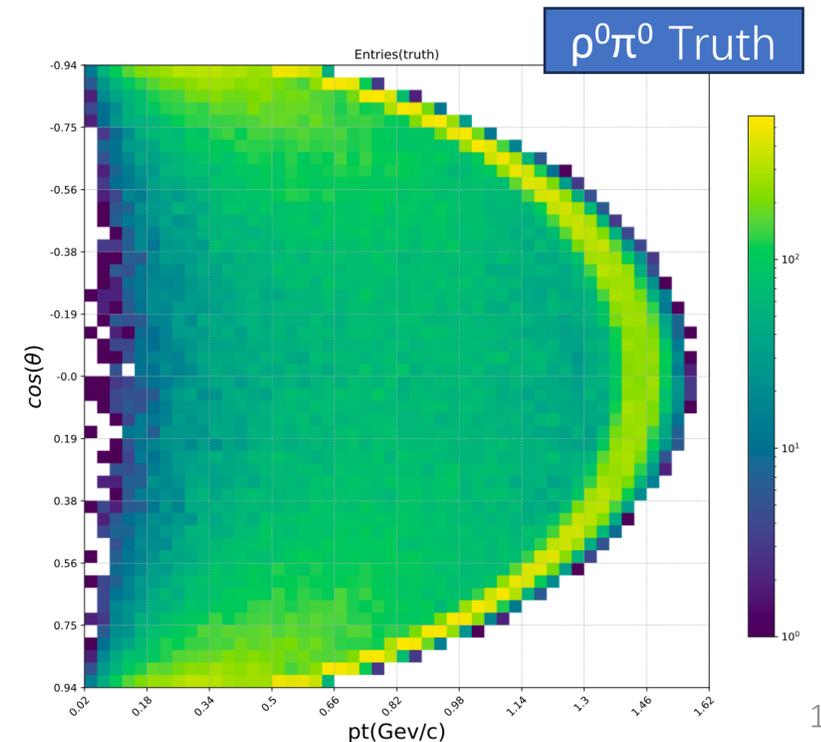
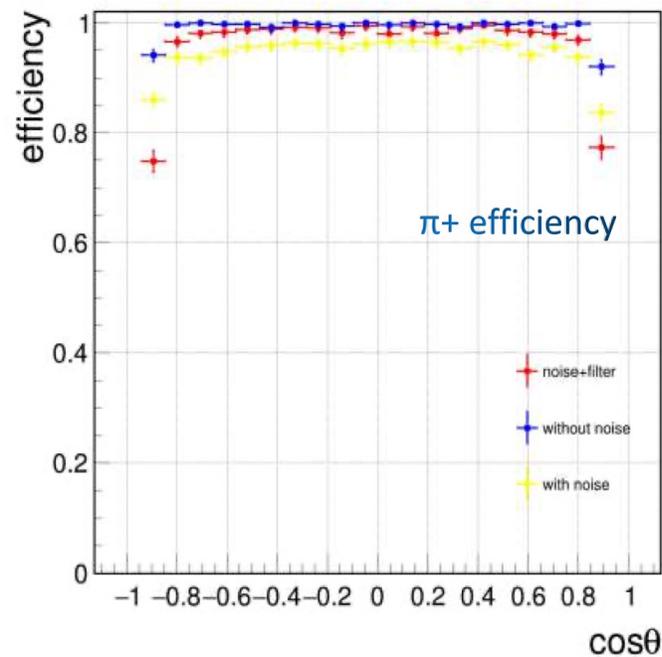
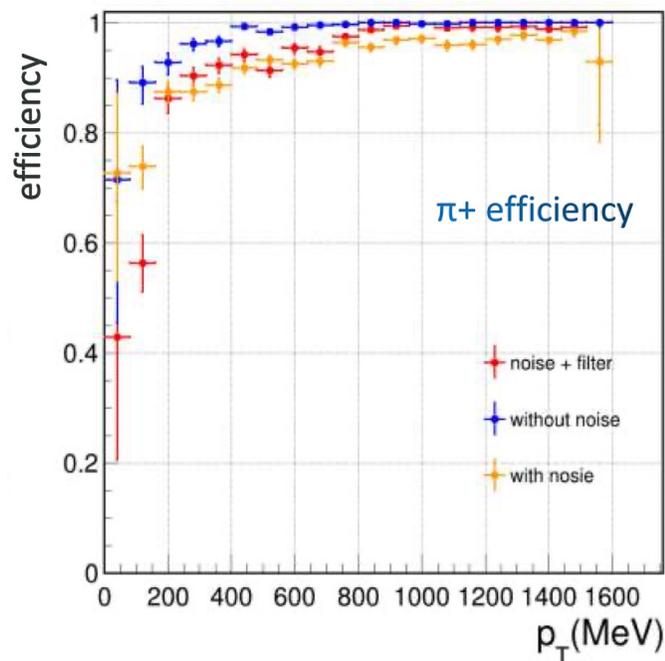
Performance of filtering noise at STCF

◆ Dataset

- $J/\psi \rightarrow \rho^0 \pi^0 \rightarrow \gamma \gamma \pi^+ \pi^-$ from MC simulation
- Mixing background (Luminosity-related, Beam-gas effect, Touschek effect) within the framework

◆ The reconstruction efficiency after GNN filtering noise is significantly improved

◆ At large $|\cos \theta|$, the tracking efficiency decreases due to **fewer signal and more noise**



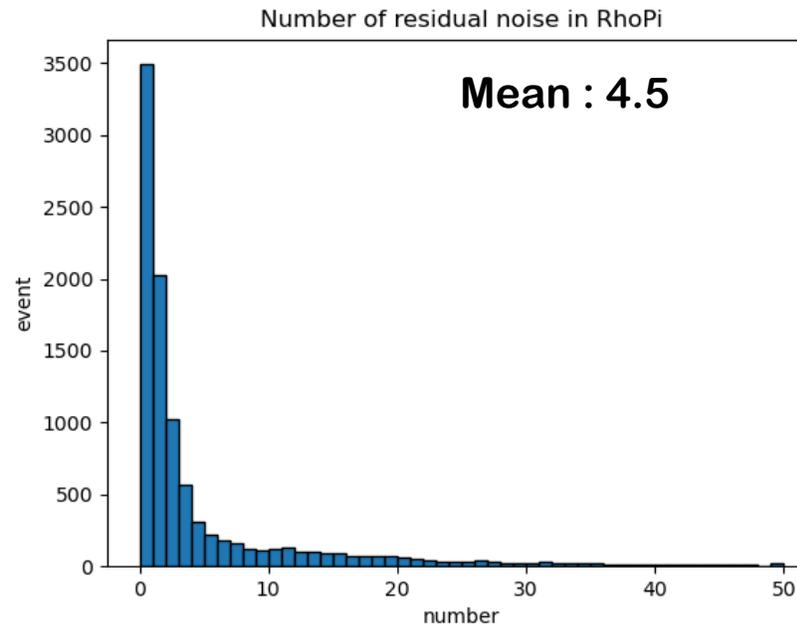
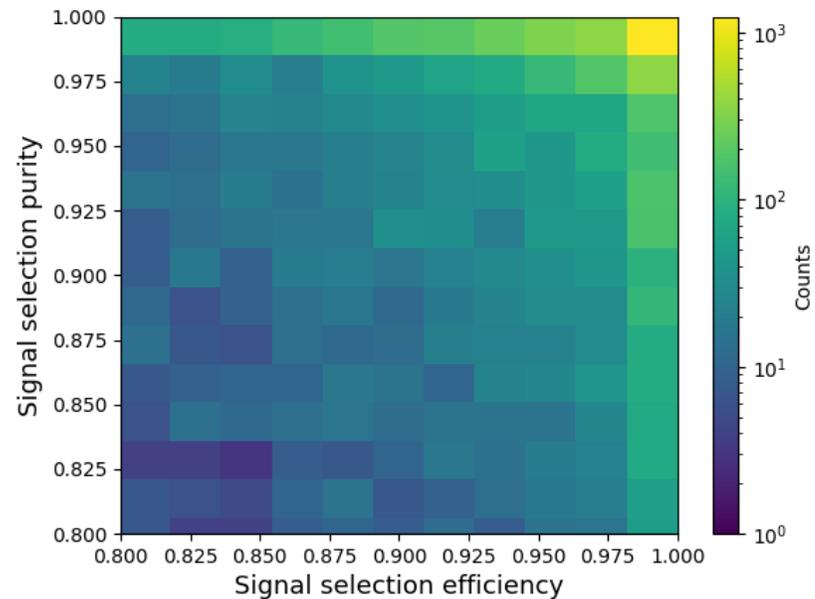
Performance of filtering noise at STCF

◆ Dataset

- $J/\psi \rightarrow \rho^0 \pi^0 \rightarrow \gamma \gamma \pi^+ \pi^-$ from MC simulation
- Mixed with 600 random trigger noises

◆ Hit selection performance

- Preliminary results shows promising performance



Summary

- ◆ A novel tracking algorithm prototype based on machine learning method at BESIII and STCF is under development
 - GNN to distinguish the hit-on-track from noise hits.
 - Clustering method based on DBSCAN and RANSAC to cluster hits from multiple tracks
- ◆ Preliminary results on MC data shows promising performance

Outlook

- ◆ Further optimization of the cluster model is needed
- ◆ Performance verification concerning events with more tracks and long lived particle
- ◆ Check the reconstruction time

Training process

