

Proton Decay

质子衰变

Wanlei Guo (郭万磊)

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(1) 大统一理论与质子衰变

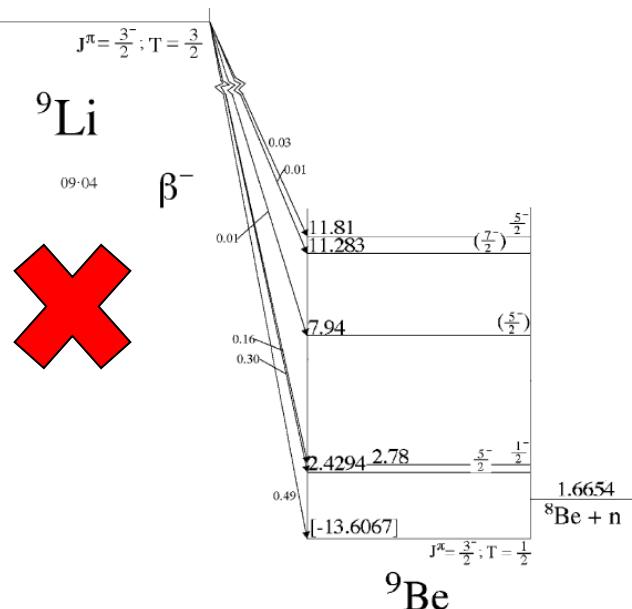


什么是质子衰变?

原子核中的质子或中子发生重子数(B)破坏的衰变，也称核子衰变!

原子核的beta衰变不是核子衰变：

核子衰变：



相当于： $n \rightarrow p + e^- + \bar{\nu}_e$
B: 1 1 0 0

为什么寻找核子衰变?

- ✓ 宇宙物质-反物质不对称
- ✓ 检验大统一理论
- ✓ 探究大统一能标的物理
- ✓ ...

Sakharov 3 conditions:

B violation; C&CP violation;
departure from thermal equilibrium



核子衰变的末态性质



核子的基本性质：

- 质子(uud)和中子(udd)都是由3夸克构成的重子
- 质量: $m_p = 938.27 \text{ MeV}$, $m_n = 939.56 \text{ MeV}$

末态质量和一定小于核子质量

$$E_N = E_1 + E_2 + E_3 + \dots$$

$$\rightarrow m_N = \sqrt{m_1^2 + p_1^2} + \dots > m_1 + m_2 + \dots$$

可能的末态粒子：

QUARKS		GAUGE BOSONS			
mass →	$\approx 2.3 \text{ MeV}/c^2$	u	c	t	g
charge →	2/3	1.275 GeV/c^2	1/2	2/3	173.07 GeV/c^2
spin →	1/2	2/3	1/2	1/2	0
	up	charm	top	gluon	Higgs boson
mass →	$\approx 4.8 \text{ MeV}/c^2$	d	s	b	γ
-1/3	1/2	95 MeV/c^2	-1/3	94.18 GeV/c^2	0
1/2	down	strange	bottom	-1/3	1
mass →	0.511 MeV/c^2	e	μ	τ	Z
-1	1/2	105.7 MeV/c^2	-1	1.777 GeV/c^2	0
1/2	electron	muon	tau	1/2	1
mass →	<2.2 eV/c^2	ν_e	ν_μ	ν_τ	W
0	1/2	<0.17 MeV/c^2	0	<15.5 MeV/c^2	± 1
1/2	electron neutrino	muon neutrino	tau neutrino	80.4 GeV/c^2	1
					W boson

末态是以下3类的组合：

➤ 正反夸克对构成的介子:

$\pi^\pm(139.6), \pi^0(135.0), K^\pm(493.7),$
 $K^0(497.6), \eta(548), \rho(775), \omega(782), K^*(892)$

➤ 轻子: 电子、缪子、中微子

➤ 光子

新物理粒子

满足电荷守恒；末态通常有轻子



标准模型中有核子衰变吗？



不衰变<--重子数守恒（偶然对称性，经典层面）：

- 重子数B：正夸克 $1/3$, 反夸克 $-1/3$
- 质子和中子的重子数为 1 , 反质子为 -1
- 介子、轻子和光子的重子数都为 0
- 质子是最轻的重子 → 不衰变

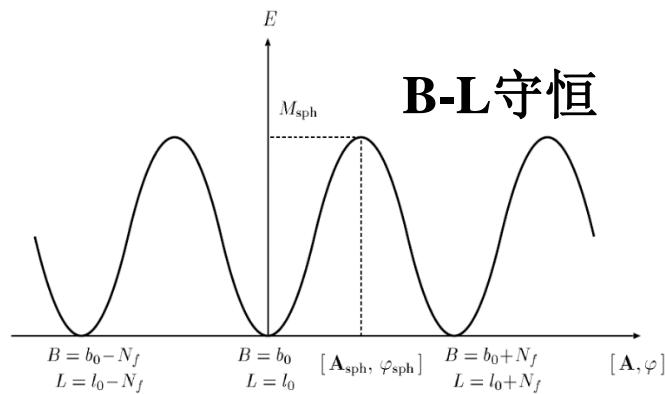
核子衰变要求重子数破坏！
→超出标准模型！

标准模型中的重子数破坏过程(Sphaleron, 量子效应)：

随温度下降指数压低，零温不可观测： $\tau(d \rightarrow e^+ \nu_\mu) \sim 10^{120} \text{ years}$ ；高温 \Rightarrow Leptogenesis

Sphaleron表明标准模型破坏重子数

轻子数守恒（偶然对称性）：



	e^-	μ^-	τ^-	$\bar{\nu}_e$	$\bar{\nu}_\mu$	$\bar{\nu}_\tau$
L_e	1	0	0	1	0	0
L_μ	0	1	0	0	1	0
L_τ	0	0	1	0	0	1

$\bar{\nu}_e + p \rightarrow e^+ + n$ 反轻子的
 $L_e = -1 \quad B = 1 \quad L_e = -1 \quad B = 1$ 轻子数为 -1
 中微子振荡破坏 L_i , 但 L 守恒!



标准模型的不足



- 标准模型基于 $SU(3)_C \times SU(2)_L \times U(1)_Y$
 - 3个独立的耦合常数，没有将强、弱和电磁统一
- 标准模型拥有太多的自由参数：19+9
- 为什么夸克、轻子只有3代，且重复填写同样的表示？

	$SU(2)_L$ doublets	$SU(2)_L$ singlets
Quarks	$\begin{pmatrix} u_L \\ d_L \end{pmatrix}, \begin{pmatrix} c_L \\ s_L \end{pmatrix}, \begin{pmatrix} t_L \\ b_L \end{pmatrix}$	$u_R, d_R, c_R, s_R, t_R, b_R$
Leptons	$\begin{pmatrix} \nu_{eL} \\ e_L \end{pmatrix}, \begin{pmatrix} \nu_{\mu L} \\ \mu_L \end{pmatrix}, \begin{pmatrix} \nu_{\tau L} \\ \tau_L \end{pmatrix}$	e_R, μ_R, τ_R

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

- 中微子的质量为零
 - 无法解释宇宙中的物质-反物质不对称，夸克CP破坏仅产生当前观测值的 10^{-18}
 - 无法解释暗物质的存在
- 标准模型没有错误，只是复杂、任意和有一些无法解释的问题！

扩充标准模型 → 大统一理论

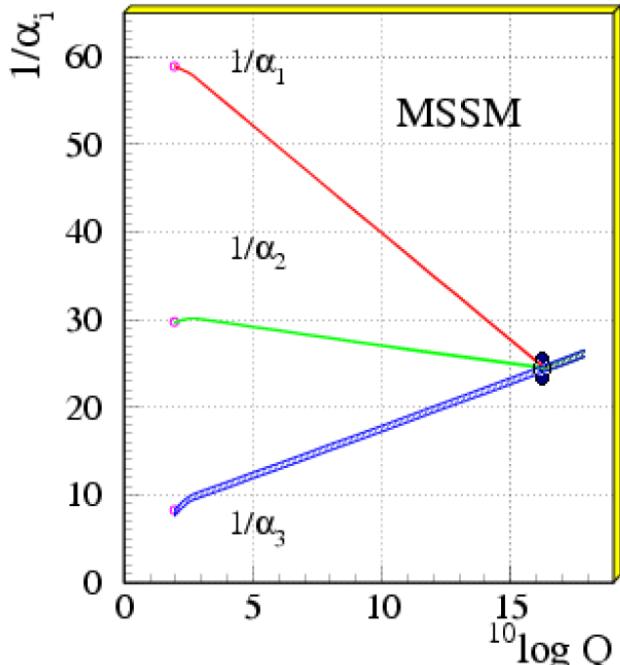


3个基本的要求:

- ① 基于更大的规范对称群[SU(5), SO(10), E6和超对称等]
- ② 可以自发破缺到 $SU(3)_C \times SU(2)_L \times U(1)_Y$
- ③ 将强、弱和电磁相互作用统一

3个要求的结果:

- 一个表示中的所有粒子的电荷之和为0,
即轻子和夸克必须放在一个表示中
- 新的规范玻色子会连接轻子和夸克, 导致重子数破坏
- 重子数破坏 -> 核子衰变
$$\tau_p \sim \frac{M^4}{m_p^5} \rightarrow M > 10^{15} \text{ GeV}$$
- 重子数破坏 -> 宇宙中物质-反物质不对称
- 预测存在磁单极子 (Magnetic Monopole)



寻找质子衰变是检验大统一理论最有效的方法!



最小SU(5)大统一模型



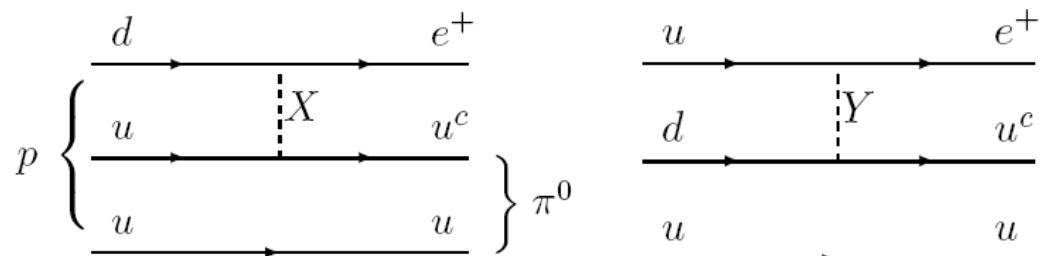
表示:

$$\bar{5} = \begin{pmatrix} d^c_1 \\ d^c_2 \\ d^c_3 \\ e^- \\ -\nu_e \end{pmatrix}_L = \psi_{L_a} \quad 10 = \begin{pmatrix} 0 & u^c_3 & -u^c_2 & -u_1 & -d_1 \\ & 0 & u^c_1 & -u_2 & -d_2 \\ & & 0 & -u_3 & -d_3 \\ & & & 0 & -e^c \\ & & & & 0 \end{pmatrix}_L = \psi^{ab} L$$

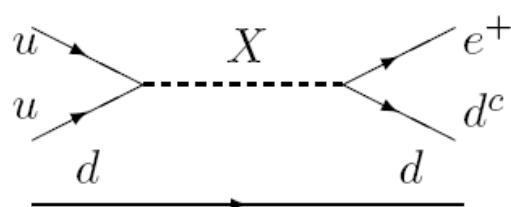
H. Georgi, S.L. Glashow, PRL 32,8 (1974)

$$\begin{pmatrix} G_1^1 - 2B' & G_2^1 & G_3^1 \\ G_1^2 & G_2^2 - 2B' & G_3^2 \\ G_1^3 & G_2^3 & G_3^3 - 2B' \\ X^1 & X^2 & X^3 \\ Y^1 & Y^2 & Y^3 \end{pmatrix} \quad \begin{pmatrix} \bar{X}^1 & \bar{Y}^1 \\ \bar{X}^2 & \bar{Y}^2 \\ \bar{X}^3 & \bar{Y}^3 \\ W^3 + 3B' & W^+ \\ W^- & -W^3 + 3B' \end{pmatrix}$$

质子衰变 $p \rightarrow e^+ + \pi^0$ 过程, 分支比最大~30% - 40%:



X和Y为新引入的超重规范玻色子, 电荷分别是4/3 和1/3



理论预测和实验结果:

理论: $\tau_{p \rightarrow e^+ + \pi^0} = 4.5 \times 10^{29 \pm 1.7} \text{ 年}$
 实验: $\tau_{p \rightarrow e^+ + \pi^0} > 2.4 \times 10^{34} \text{ 年}$

质子衰变排除最小SU(5) 大统一模型!

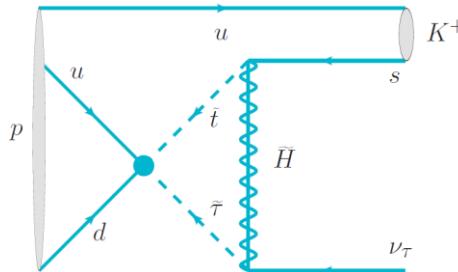
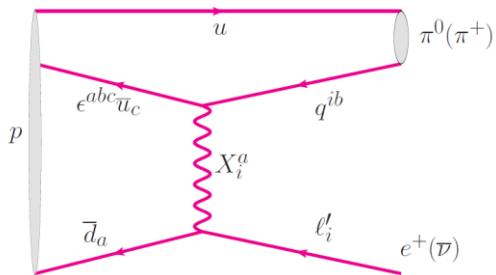


当前大统一理论的预测

2个显著的核子衰变道:

$$p \rightarrow e^+ \pi^0$$

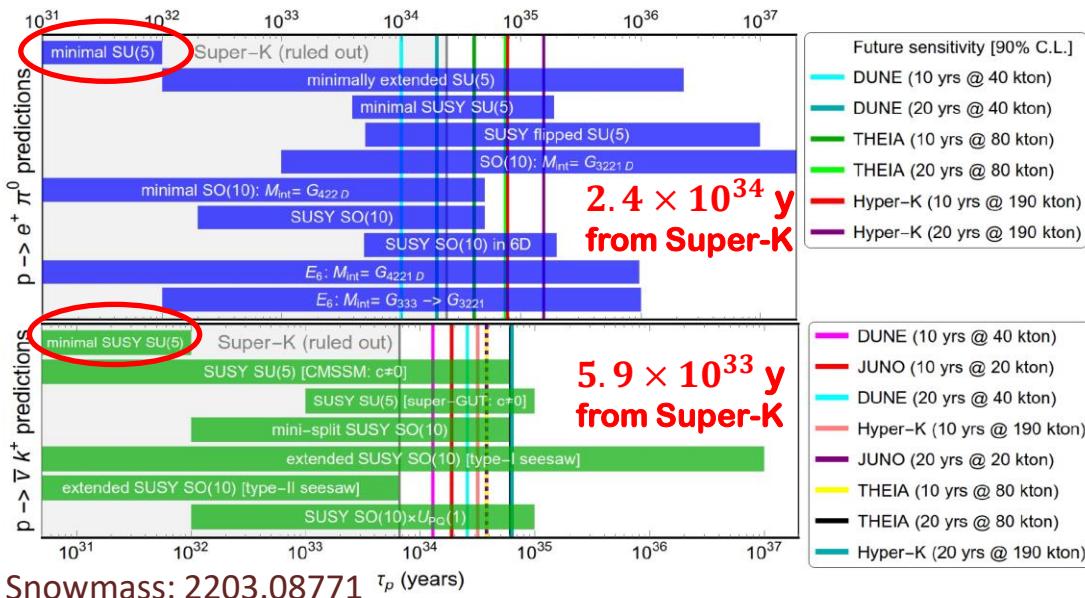
Non-SUSY GUTs



$$p \rightarrow \bar{\nu} K^+$$

SUSY GUTs

主要GUT模型的预测:



不同核子衰变道之间的联系:

	Br. (%)				
	SU(5)		SO(10)		
References	[72]	[73]	[74]	[75]	[75]
$p \rightarrow e^+ \pi^0$	33	37	9	35	30
$p \rightarrow e^+ \eta^0$	12	7	3	15	13
$p \rightarrow e^+ \rho^0$	17	2	21	2	2
$p \rightarrow e^+ \omega^0$	22	18	56	17	14
Others	17	35	11	31	31
τ_p/τ_n	0.8	1.0	1.3		

Hyper-K:1109.3262



试试寻找其他的核子衰变道?



Mode	Partial mean life (10^{30} years)	Scale Factor/ Conf. Level	$P(\text{MeV/c})$	$\tau_{22} \ N \rightarrow \nu K^*(892)$	> 78 [n], > 51 [p]			Cl=90%	45	▼	Antilepton + single massless	$\Delta B = 2$ dinucleon modes				
Antilepton + meson																
$\tau_1 \ N \rightarrow e^+ \pi^-$	B	$> 5300 \{n\},$ $> 16000 \{p\}$	Cl=90%	459	▼	$\tau_{23} \ p \rightarrow e^+ \pi^+ \pi^-$		> 82	Cl=90%	448	▼	Three (or more) leptons	$\tau_{67} \ p \ p \rightarrow \pi^+ \pi^-$	> 72.2	Cl=90%	▼
$\tau_2 \ N \rightarrow \mu^+ \pi^-$	B	$> 3500 \{n\},$ $> 7700 \{p\}$	Cl=90%	453	▼	$\tau_{24} \ p \rightarrow e^+ \pi^0 \pi^0$		> 147	Cl=90%	449	▼		$\tau_{68} \ p \ n \rightarrow \pi^0 \pi^0$	> 170	Cl=90%	▼
$\tau_3 \ N \rightarrow \nu \pi$		$> 1100 \{n\},$ $> 390 \{p\}$	Cl=90%	459	▼	$\tau_{25} \ n \rightarrow e^+ \pi^- \pi^0$		> 52	Cl=90%	449	▼		$\tau_{69} \ n \ n \rightarrow \pi^+ \pi^-$	> 0.7	Cl=90%	▼
$\tau_4 \ p \rightarrow e^+ \eta$		> 10000	Cl=90%	309	▼	$\tau_{26} \ p \rightarrow \mu^+ \pi^+ \pi^-$		> 133	Cl=90%	425	▼		$\tau_{70} \ n \ n \rightarrow \pi^0 \pi^0$	> 404	Cl=90%	▼
$\tau_5 \ p \rightarrow \mu^+ \eta$		> 4700	Cl=90%	297	▼	$\tau_{27} \ p \rightarrow \mu^+ \pi^0 \pi^0$		> 101	Cl=90%	427	▼		$\tau_{71} \ p \ p \rightarrow K^+ K^-$	> 170	Cl=90%	▼
$\tau_6 \ n \rightarrow \nu \eta$		> 158	Cl=90%	310	▼	$\tau_{28} \ n \rightarrow \mu^+ \pi^- \pi^0$		> 74	Cl=90%	427	▼		$\tau_{72} \ p \ p \rightarrow e^+ e^-$	> 5.8	Cl=90%	▼
$\tau_7 \ N \rightarrow e^+ \rho^-$		$> 217 \{n\},$ $> 720 \{p\}$	Cl=90%	149	▼	$\tau_{29} \ n \rightarrow e^+ K^-$		> 18	Cl=90%	319	▼		$\tau_{73} \ p \ p \rightarrow e^+ \mu^+$	> 3.6	Cl=90%	▼
$\tau_8 \ N \rightarrow \mu^+ \rho^-$		$> 228 \{n\},$ $> 570 \{p\}$	Cl=90%	113	▼	$\tau_{30} \ n \rightarrow e^- \rho^+$		> 65	Cl=90%	459	▼		$\tau_{74} \ p \ p \rightarrow \mu^+ \mu^+$	> 1.7	Cl=90%	▼
$\tau_9 \ N \rightarrow \nu \rho$		$> 19 \{n\},$ $> 162 \{p\}$	Cl=90%	149	▼	$\tau_{31} \ n \rightarrow \mu^- \pi^+$		> 49	Cl=90%	453	▼		$\tau_{75} \ p \ n \rightarrow e^+ \bar{\nu}_e$	> 260	Cl=90%	▼
$\tau_{10} \ p \rightarrow e^+ \omega$		> 1600	Cl=90%	143	▼	$\tau_{32} \ n \rightarrow e^- \rho^+$		> 62	Cl=90%	150	▼		$\tau_{76} \ p \ n \rightarrow \mu^+ \bar{\nu}_e$	> 200	Cl=90%	▼
$\tau_{11} \ p \rightarrow \mu^+ \omega$		> 2800	Cl=90%	105	▼	$\tau_{33} \ n \rightarrow \mu^- \rho^+$		> 7	Cl=90%	115	▼		$\tau_{77} \ p \ n \rightarrow \tau^+ \bar{\nu}_\tau$	> 29	Cl=90%	▼
$\tau_{12} \ n \rightarrow \nu \omega$		> 108	Cl=90%	144	▼	$\tau_{34} \ n \rightarrow e^- K^+$		> 32	Cl=90%	340	▼		$\tau_{78} \ n \ n \rightarrow \text{invisible}$	> 1.4	Cl=90%	▼
$\tau_{13} \ N \rightarrow e^+ K^-$	B	$> 17 \{n\},$ $> 1000 \{p\}$	Cl=90%	339	▼	$\tau_{35} \ n \rightarrow \mu^- K^+$		> 57	Cl=90%	330	▼	Inclusive modes	$\tau_{79} \ n \ n \rightarrow \nu_e \bar{\nu}_e$	> 1.4	Cl=90%	▼
$\tau_{14} \ p \rightarrow e^+ K_S^0$				337	▼	$\tau_{36} \ p \rightarrow e^- \pi^+ \pi^+$		> 30	Cl=90%	448	▼		$\tau_{80} \ n \ n \rightarrow \nu_\mu \bar{\nu}_\mu$	> 1.4	Cl=90%	▼
$\tau_{15} \ p \rightarrow e^+ K_L^0$				337	▼	$\tau_{37} \ n \rightarrow e^- \pi^+ \pi^0$		> 29	Cl=90%	449	▼		$\tau_{81} \ p \ n \rightarrow \text{invisible}$	> 0.06	Cl=90%	▼
$\tau_{16} \ N \rightarrow \mu^+ K^-$	B	$> 26 \{n\},$ $> 1600 \{p\}$	Cl=90%	329	▼	$\tau_{38} \ p \rightarrow \mu^- \pi^+ \pi^+$		> 17	Cl=90%	425	▼		$\tau_{82} \ p \ p \rightarrow \text{invisible}$	> 0.11	Cl=90%	▼
$\tau_{17} \ p \rightarrow \mu^+ K_S^0$				326	▼	$\tau_{39} \ n \rightarrow \mu^- \pi^+ \pi^0$		> 34	Cl=90%	427	▼					
$\tau_{18} \ p \rightarrow \mu^+ K_L^0$				326	▼	$\tau_{40} \ p \rightarrow e^- \pi^+ K^+$		> 75	Cl=90%	320	▼					
$\tau_{19} \ N \rightarrow \nu K$		$> 86 \{n\},$ $> 5900 \{p\}$	Cl=90%	339	▼	$\tau_{41} \ p \rightarrow \mu^- \pi^+ K^+$		> 245	Cl=90%	279	▼					
$\tau_{20} \ n \rightarrow \nu K_S^0$		> 260	Cl=90%	338	▼	$\tau_{42} \ p \rightarrow e^+ \gamma$		> 670	Cl=90%	469	▼					
$\tau_{21} \ p \rightarrow e^+ K^*(892)^0$		> 84	Cl=90%	45	▼	$\tau_{43} \ p \rightarrow \mu^+ \gamma$		> 478	Cl=90%	463	▼					
						$\tau_{44} \ n \rightarrow \nu \gamma$		> 550	Cl=90%	470	▼					
						$\tau_{45} \ p \rightarrow e^+ \gamma \gamma$		> 100	Cl=90%	469	▼					
						$\tau_{46} \ n \rightarrow \nu \gamma \gamma$		> 219	Cl=90%	470	▼					

From PDG 2023

Total Channels: 82

Mesons: $\pi^\pm, \pi^0, K^\pm, K^0, \eta, \rho, \omega, K^*(892)$;

Leptons: e^\pm, μ^\pm, ν ; Photon: γ

实验上至今没有发现核子衰变!



GUTs还预言了哪些未被寻找的核子衰变道？



Proton 3-body:

Channel	$ \Delta(B - L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$p \rightarrow e^- + e^+ + e^+$	0	793 [46]
$p \rightarrow e^- + e^+ + \mu^+$	0	529 [46]
$p \rightarrow e^+ + e^+ + \mu^-$	0	529* [46]
$p \rightarrow e^- + \mu^+ + \mu^+$	0	6 [73] (359* [46])
$p \rightarrow e^+ + \mu^- + \mu^+$	0	359 [46]
$p \rightarrow \mu^- + \mu^+ + \mu^+$	0	675 [46]
$p \rightarrow e^+ + 2\nu$	0,2	170 [81]
$p \rightarrow \mu^+ + 2\nu$	0,2	220 [81]
$p \rightarrow e^- + 2\pi^+$	2	30 [52] (82* [46])
$p \rightarrow e^- + \pi^+ + \rho^+$	2	
$p \rightarrow e^- + K^+ + \pi^+$	2	75 [46]
$p \rightarrow e^+ + 2\gamma$	0	100 [82] (793* [46])
$p \rightarrow e^+ + \pi^- + \pi^+$	0	82 [46]
$p \rightarrow e^+ + \rho^- + \pi^+$	0	
$p \rightarrow e^+ + K^- + \pi^+$	0	75* [46]
$p \rightarrow e^+ + \pi^+ + \rho^+$	0	
$p \rightarrow e^+ + \pi^- + K^+$	0	
$p \rightarrow e^+ + 2\pi^0$	0	75* [46]
$p \rightarrow e^+ + \pi^0 + \eta$	0	147 [46]
$p \rightarrow e^+ + \pi^0 + \rho^0$	0	
$p \rightarrow e^+ + \pi^0 + \omega$	0	
$p \rightarrow e^+ + \pi^0 + K^0$	0	
$p \rightarrow \mu^- + 2\pi^+$	2	17 [52] (133* [46])
$p \rightarrow \mu^- + K^+ + \pi^+$	2	245 [46]
$p \rightarrow \mu^+ + 2\gamma$	0	529* [46]
$p \rightarrow \mu^- + \pi^+ + \pi^+$	0	133 [46]
$p \rightarrow \mu^- + K^- + \pi^+$	0	245* [46]
$p \rightarrow \mu^- + \pi^- + K^+$	0	245* [46]
$p \rightarrow \mu^+ + 2\pi^0$	0	101 [46]
$p \rightarrow \mu^+ + \pi^0 + \eta$	0	
$p \rightarrow \mu^+ + \pi^0 + K^0$	0	
$p \rightarrow \nu + \pi^+ + \pi^0$	0,2	
$p \rightarrow \nu + \pi^+ + \eta$	0,2	
$p \rightarrow \nu + \pi^+ + \rho^0$	0,2	
$p \rightarrow \nu + \pi^+ + \omega$	0,2	
$p \rightarrow \nu + \pi^+ + K^0$	0,2	
$p \rightarrow \nu + \rho^+ + \pi^0$	0,2	
$p \rightarrow \nu + K^+ + \pi^0$	0,2	

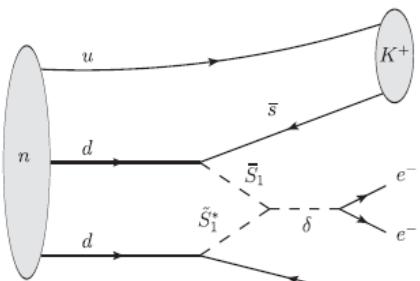
Neutron 3-body:

Channel	$ \Delta(B - L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$n \rightarrow \nu + e^- + e^+$	0,2	257 [46]
$n \rightarrow \nu + e^- + \mu^+$	0,2	83 [46]
$n \rightarrow \nu + e^+ + \mu^-$	0,2	83* [46]
$n \rightarrow \nu + \mu^- + \mu^+$	0,2	79 [46]
$n \rightarrow 3\nu$	0,2,4	0.58 [83]
$n \rightarrow e^- + \pi^+ + \pi^0$	2	29 [52] (52* [46])
$n \rightarrow e^- + \pi^+ + \eta$	2	
$n \rightarrow e^- + \pi^+ + \rho^0$	2	
$n \rightarrow e^- + \pi^+ + \omega$	2	
$n \rightarrow e^- + \pi^+ + K^0$	2	
$n \rightarrow e^- + \rho^+ + \pi^0$	2	
$n \rightarrow e^- + K^+ + \pi^0$	2	
$n \rightarrow e^+ + \pi^- + \pi^0$	0	
$n \rightarrow e^+ + \pi^- + \eta$	0	
$n \rightarrow e^+ + \pi^- + \rho^0$	0	
$n \rightarrow e^+ + \pi^- + \omega$	0	
$n \rightarrow e^+ + K^- + \pi^0$	0	
$n \rightarrow e^+ + \pi^- + \pi^0$	0	
$n \rightarrow e^+ + \pi^- + K^0$	0	
$n \rightarrow e^+ + \rho^- + \pi^0$	0	
$n \rightarrow e^+ + \pi^- + \omega$	0	
$n \rightarrow e^+ + K^- + \pi^0$	0	
$n \rightarrow e^+ + \pi^- + \eta$	0	
$n \rightarrow e^+ + \pi^- + \rho^0$	0	
$n \rightarrow e^+ + \pi^- + \omega$	0	
$n \rightarrow e^+ + K^- + \pi^0$	0	
$n \rightarrow e^+ + \pi^- + K^0$	0	
$n \rightarrow \mu^- + \pi^+ + \pi^0$	2	
$n \rightarrow \mu^- + \pi^+ + \eta$	2	
$n \rightarrow \mu^- + \pi^+ + \rho^0$	2	
$n \rightarrow \mu^- + \pi^+ + \omega$	2	
$n \rightarrow \mu^- + K^+ + \pi^0$	2	
$n \rightarrow \mu^- + K^+ + \eta$	2	
$n \rightarrow \mu^- + K^+ + \rho^0$	2	
$n \rightarrow \mu^- + K^+ + \omega$	2	
$n \rightarrow \nu + 2\gamma$	0,2	
$n \rightarrow \nu + \pi^- + \pi^+$	0,2	
$n \rightarrow \nu + \rho^- + \pi^+$	0,2	
$n \rightarrow \nu + K^- + \pi^+$	0,2	
$n \rightarrow \nu + \pi^- + \rho^+$	0,2	
$n \rightarrow \nu + \pi^- + K^+$	0,2	
$n \rightarrow \nu + 2\pi^0$	0,2	
$n \rightarrow \nu + \pi^0 + \eta$	0,2	
$n \rightarrow \nu + \pi^0 + \rho^0$	0,2	
$n \rightarrow \nu + \pi^0 + \omega$	0,2	
$n \rightarrow \nu + \pi^0 + K^0$	0,2	

Dinucleon decay:

Channel	$ \Delta(B - L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$nn \rightarrow \pi^0 + \phi$	2	
$nn \rightarrow 2\eta$	2	
$nn \rightarrow \eta + \rho^0$	2	
$nn \rightarrow \eta + \omega$	2	
$nn \rightarrow \eta + \eta'$	2	
$nn \rightarrow \eta + K^0$	2	
$nn \rightarrow \eta + K^{*,0}$	2	
$nn \rightarrow \eta + \phi$	2	
$nn \rightarrow 2\rho^0$	2	
$nn \rightarrow \rho^0 + \omega$	2	
$nn \rightarrow \eta' + \rho^0$	2	
$nn \rightarrow K^0 + \rho^0$	2	
$nn \rightarrow K^{*,0} + \rho^0$	2	
$nn \rightarrow \rho^0 + \phi$	2	
$nn \rightarrow \rho^- + \rho^+$	2	
$nn \rightarrow K^+ + \rho^-$	2	
$nn \rightarrow K^{*,+} + \rho^-$	2	
$nn \rightarrow K^- + \rho^+$	2	
$nn \rightarrow K^{*-} + \rho^+$	2	
$nn \rightarrow 2\omega$	2	
$nn \rightarrow \eta' + \omega$	2	
$nn \rightarrow K^0 + \omega$	2	
$nn \rightarrow K^{*,0} + \omega$	2	
$nn \rightarrow \omega + \phi$	2	
$nn \rightarrow \eta' + K^0$	2	
$nn \rightarrow \eta' + K^{*,0}$	2	
$nn \rightarrow K^- + K^+$	2	170* [116]
$nn \rightarrow K^+ + K^{*-}$	2	
$nn \rightarrow K^- + K^{*,+}$	2	
$nn \rightarrow 2K^0$	2	
$nn \rightarrow K^{*,0} + K^0$	2	
$nn \rightarrow K^0 + \phi$	2	
$nn \rightarrow 2K^{*,0}$	2	
$nn \rightarrow K^{*,+} + K^{*-}$	2	

4-body decay:



From PRD 101, 015005 (2020)

Others?



(2) 质子衰变实验



质子衰变实验的探测能力



事例数变化：

$$\frac{dN}{dt} = -\lambda N \rightarrow N_t = N_0 e^{-\lambda t} = N_0 e^{-\frac{t}{\tau}} \quad [t \ll \tau]$$

$$N_t = N_0 \left(1 - \frac{t}{\tau}\right) \rightarrow N_0 - N_t = N_{decay} = N_0 \frac{t}{\tau}$$

N_0 : 靶核子数
 ϵ_i : 探测效率
 t : 实验时间
 N_{S_i} : 实验限制

考虑某个衰变道的分支比 B_i 和实验探测效率 ϵ_i ：

$$N_{S_i} = N_{decay} \cdot B_i \cdot \epsilon_i = B_i \cdot \epsilon_i \cdot N_0 \frac{t}{\tau} \rightarrow \frac{\tau}{B_i} = \frac{N_0 \cdot \epsilon_i}{N_{S_i}} t$$

核子衰变实验关键量：(1) 曝光量 $N_0 \cdot t$ (2) 效率 ϵ_i (3) 背景

简单的估算公式： $\tau/B_i > 1.5 \times M(\text{kton}) \times \epsilon_i \times t \times 10^{32} \text{ yr}$

实验对事例数 N_{S_i} 的限制：

$$L(N_{obs}, N_S) = \frac{(N_S + N_B)^{N_{obs}}}{N_{obs}!} e^{-(N_S + N_B)} \rightarrow 90\% = \frac{\int_0^{N_{90}} L(N_{obs}, N_S) dN_S}{\int_0^{\infty} L(N_{obs}, N_S) dN_S}$$

$N_{obs} = N_B$	0.0	1.0	2.0	5.0	10	20	50	100	200	1000
N_{90}	2.3	3.3	3.9	5.2	6.6	8.8	13.0	17.8	24.6	53.3

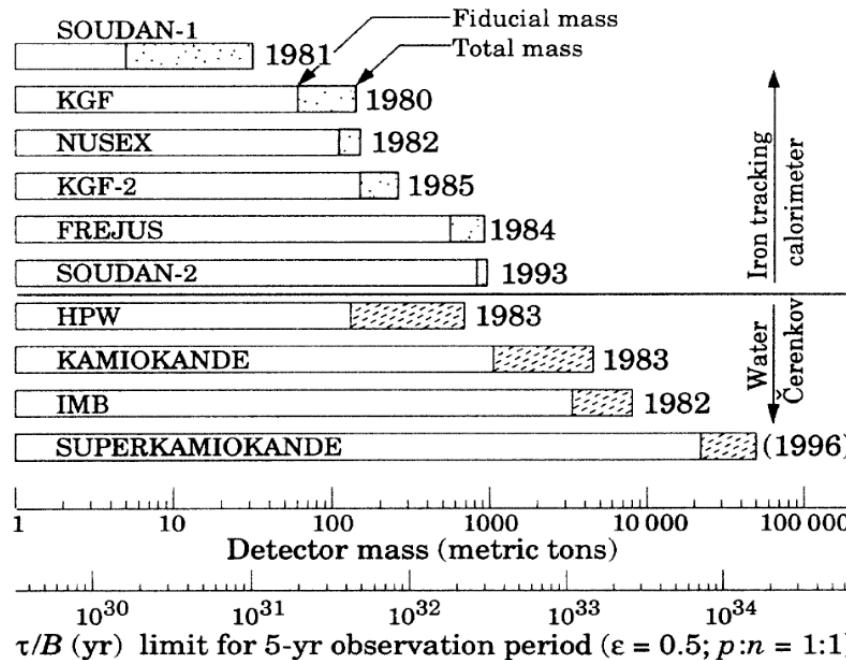


质子衰变实验的发展历史

早期实验对质子衰变的限制:

大统一理论提出之前（1950s-60s）→ 检验质子是否稳定

第一代(80s)和第二代(90s)质子衰变实验:



2000年之后，KamLAND、SNO、BOREXINO、DAMA等实验也对不可见质子衰变道给出限制。

第三代(2020s)质子衰变实验:

- Hyper-K (Water Cerenkov)
- DUNE (LAr TPC)
- JUNO (Liquid Scintillator)



早期质子衰变实验



Experimental tests of proton decays before GUTs

- In 1954, Reines, Cowan and Goldhaber give the first limit: $\tau(p) > 10^{22}$ yrs
- Before the discovery of $\bar{\nu}_e$ in 1956. Phys. Rev. 96, 1157 (1954)

Authors	Experiment	Decay mode	Depth (mwe)	τ_{\min} (yrs)
Reines, Cowan, and Goldhaber 1954 [4]	300 & liquid scint.	All ($E_{ch} > 100$ MeV)	200	10^{22}
Reines, Cowan and Kruse 1958 [49]	As above, with delayed neutron pulse	All	200	$4 \cdot 10^{23}$
Backenstoss et al. 1960 [8]	50 & liquid Cerenkov, upward rel. sec.	At least one secondary of > 250 MeV	2400	$3 \cdot 10^{26}$
Giamati and Reines 1962 [50] Kropp and Reines 1965 [51]	200 & liquid scint.	All	1760	$6 \cdot 10^{27}$ $\sim 10^{28}$
Gurr et al. 1967 [52]	Scint. hodoscope	All	8000	$2 \cdot 10^{28}$



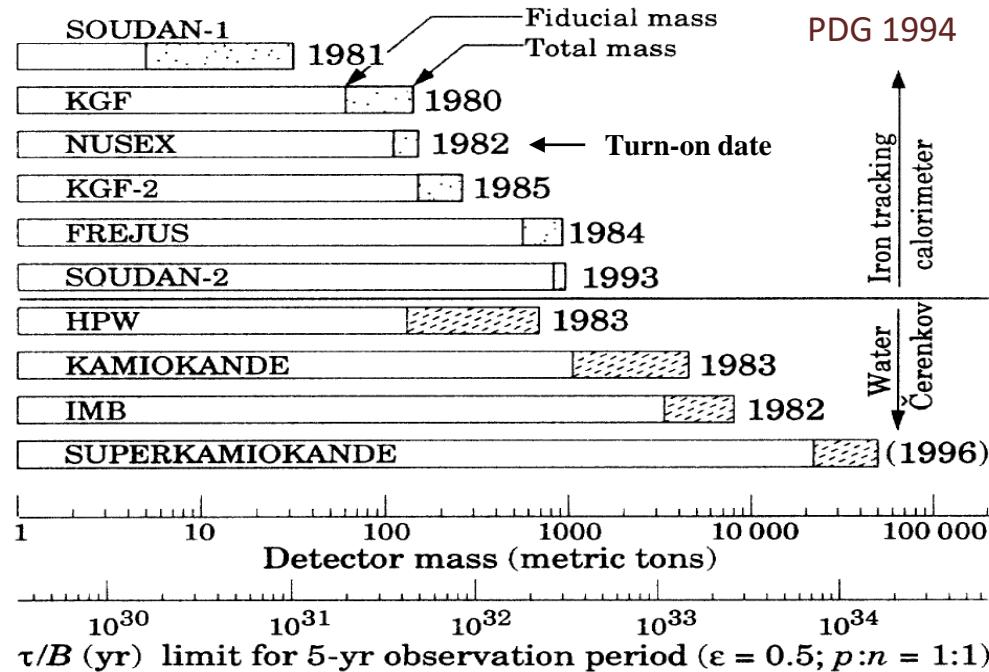
第一代质子衰变实验 (80年代)



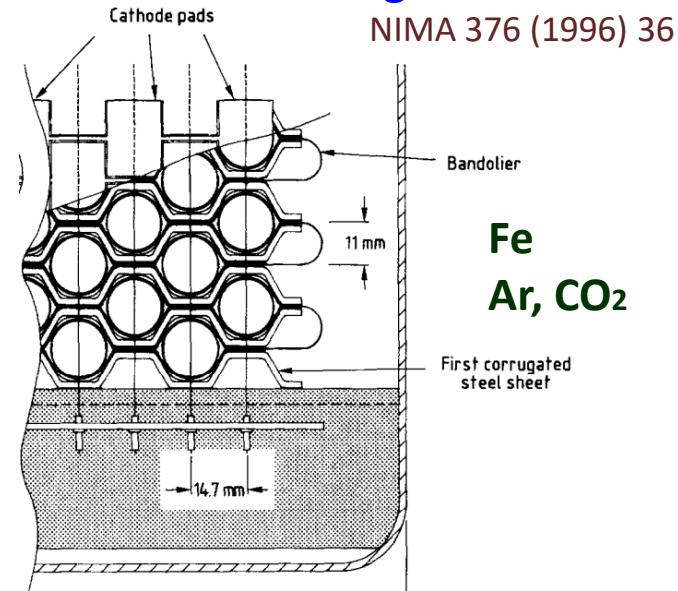
In 1974, Georgi and Glashow give SU(5) GUT, $\rightarrow p$ lifetime $\sim 4.5 \times 10^{29} \pm 1.7$ yrs

→ Detector with about 1000 ton mass can test the SU(5) GUT

→ The first generation of experiments are proposed and constructed



SOUDAN-2 Iron tracking calorimeter



Fe
Ar, CO₂

First corrugated
steel sheet

Fe

Ar, CO₂

NIMA 376 (1996) 36

They do not find the evidence for proton decay, excluding minimal SU(5)! 16



第二代质子衰变实验 (仅有 Super-K)



Super-Kamiokande:

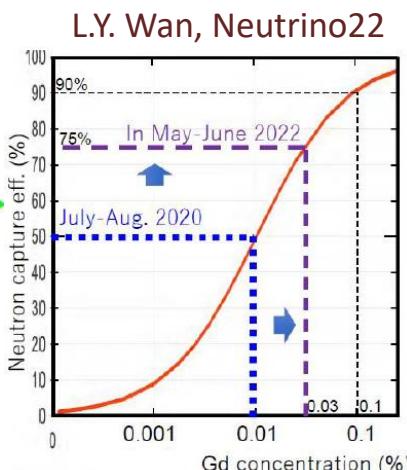
Super-Kamiokande => Super-Kamioka Neutrino Detection Experiment
 KamiokaNDE => Kamioka Nucleon Decay Experiment

Water Cerenkov, 50 kton → 22.5 kton

通过探测切伦科夫光来鉴别**有能量粒子的类型**,
 并重建其**能量和方向等信息**

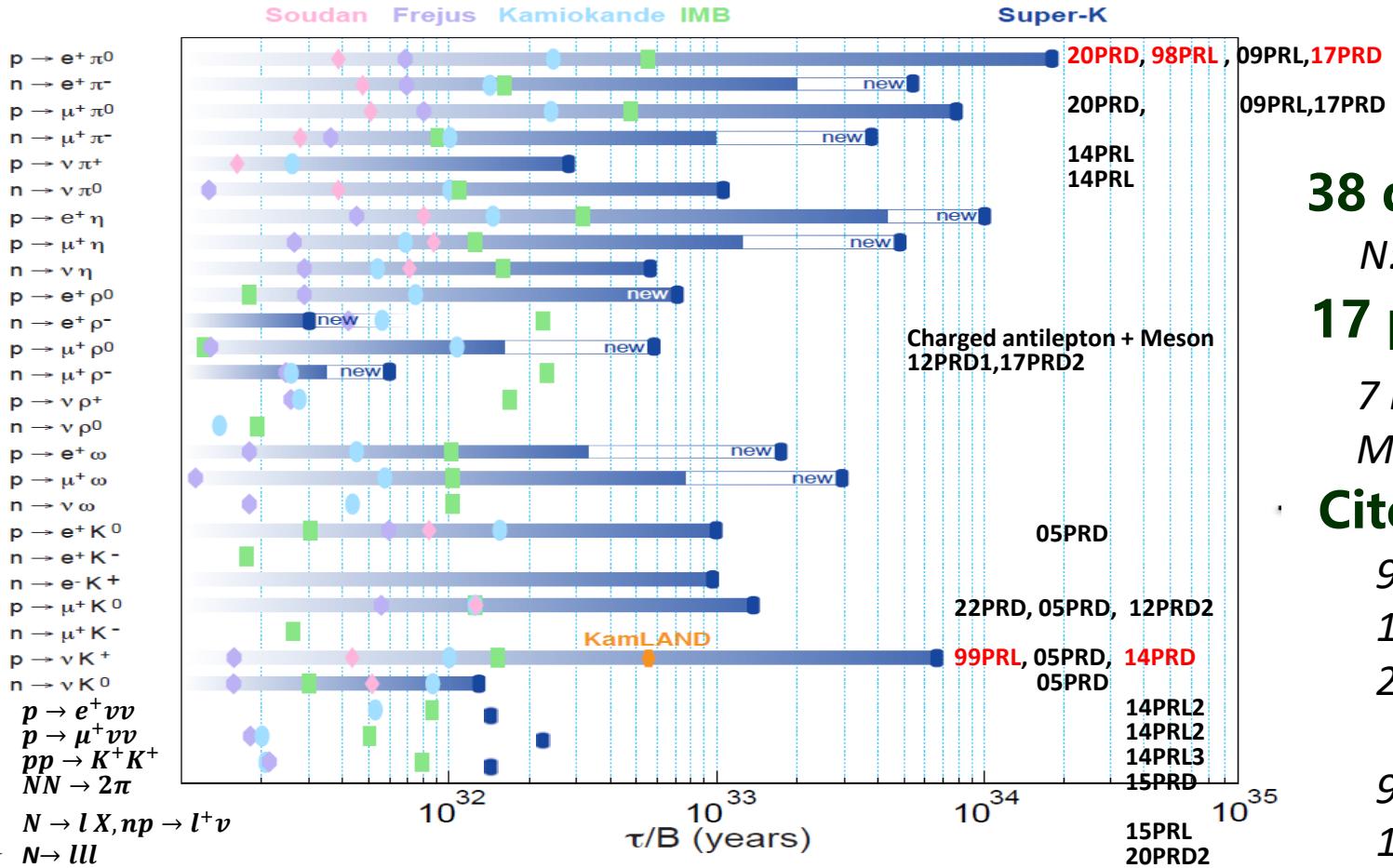


Gd concentration at SK-VI:
 0.011% in weight.





Super-K的质子衰变结果



38 decay modes:

$N: 31; NN: 7$

17 paper:

7 PRL, 10 PRD

Most after 2012

Cites:

98PRL: 208

17PRD: 304

20PRD: 80

99PRL: 201

14PRD: 212

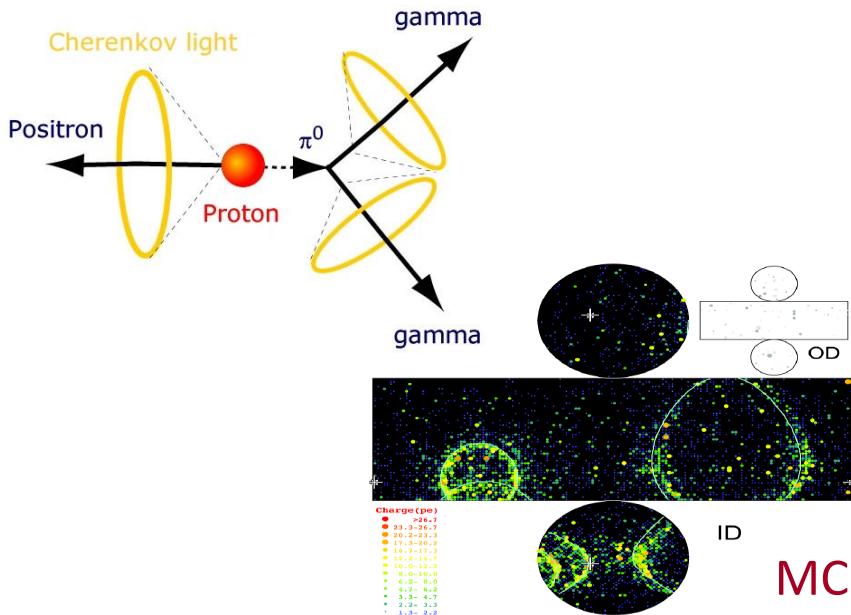


Super-K searching for $p \rightarrow e^+ \pi^0$



Signal features:

- Momentum of e^+ and π^0 is 460 MeV
- Kinetic energy : 459 MeV and 344 MeV



Event selection:

- A. Two or three rings
- B. e-like rings
- C. Invariant mass of π^0 (135MeV) : 85-185MeV
- D. No Michel electron
- E. \vec{P}_{tot} (<250MeV) and M_{invar} (800-1050 MeV)

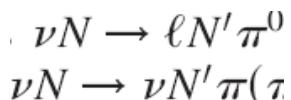
Results:

450 kton years

Efficiency: ~20%

$$\tau/B(p \rightarrow e^+ \pi^0) > 2.4 \times 10^{34} \text{ yrs}$$

Background: ~0.6





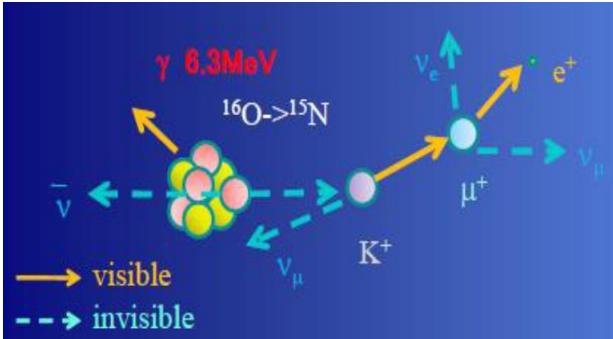
Super-K searching for $p \rightarrow \bar{v} K^+$



Signal features:

- Momentum of \bar{v} and K^+ is 339 MeV (105 MeV)
- 89% K^+ decay at rest (12.38ns):

$$K^+ \rightarrow \mu^+ \nu_\mu \text{ (63.43\%)}, K^+ \rightarrow \pi^+ \pi^0 \text{ (21.13\%)},$$



Event selection:

- 1: $K^+ \rightarrow \mu^+ \nu_\mu \rightarrow \gamma$ (6.3 MeV, 41%) from $^{16}\text{O} + \mu^+ + \text{Michel } e^+$
- 2: $K^+ \rightarrow \mu^+ \nu_\mu \rightarrow \text{Monoenergetic } \mu^+ (p = 236\text{MeV})$
- 3: $K^+ \rightarrow \pi^+ \pi^0 \rightarrow \text{two rings from } \pi^0 (M_{inv}, p) + \pi^+ (\text{direction, } e^+)$

$\nu p \rightarrow \nu K^+ \Lambda$ (48%),
 $\nu_\mu \text{ CCQE}$ (25%),

CC $1\pi^0$ with μ (38%),
 kaon production (37%),
 NC multi- π (11%)

Results:

260 kton years

Efficiency: ~8.4%, 9%



$$\tau/B(p \rightarrow \bar{v} K^+) > 5.9 \times 10^{33} \text{ yrs}$$

Background: ~0.24, 0.45

PRD 90, 072005 (2014)



未来质子衰变实验的方向

质子衰变实验的探测潜力：

$$\frac{\tau}{B_i} = \frac{N_0 \cdot \epsilon_i}{N_{S_i}} t$$

N_0 ：靶核子数

ϵ_i ：探测效率

t ：实验时间

N_{S_i} ：实验限制

$N_{obs} = N_B$	0.0	1.0	2.0	5.0	10	20	50	100	200	1000
N_{90}	2.3	3.3	3.9	5.2	6.6	8.8	13.0	17.8	24.6	53.3

未来质子衰变实验的方向？



未来质子衰变实验的方向



质子衰变实验的探测潜力：

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N_{90}	2.3	3.3	3.9	5.2	6.6	8.8	13.0	17.8	24.6	53.3

未来质子衰变实验的方向？

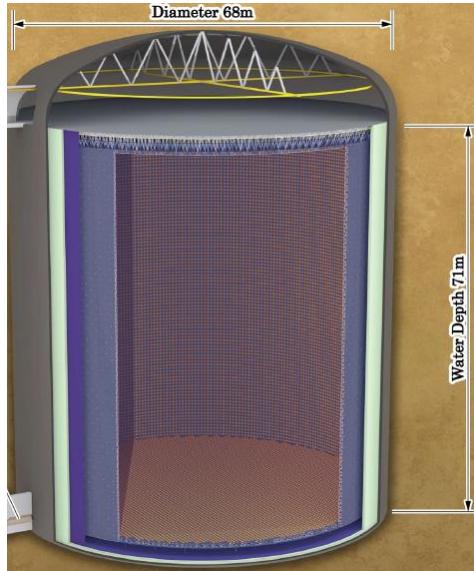
1. 增加探测器靶质量 N_0 → 相对容易
2. 增加取数时间 t → 提升有限
3. 保持高 ϵ_i 同时压低背景 → 分析方法
4. 寻找新的方法，如古矿物中的径迹： $1\text{kton} \cdot 10\text{y} = 10\text{g} \cdot 10^9\text{y}$
5. ...



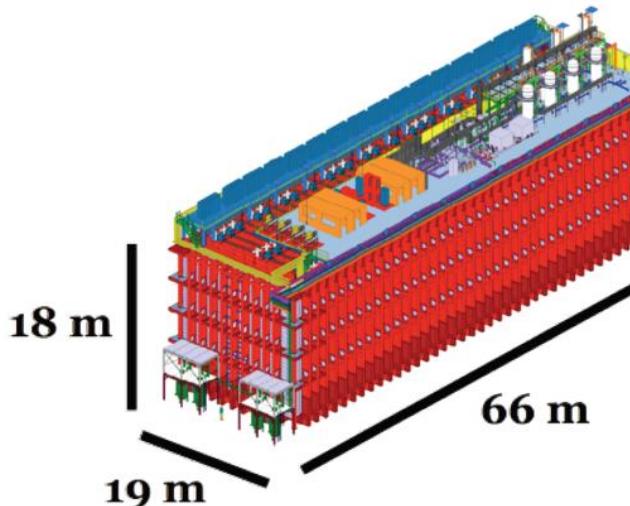
第三代核子衰变实验



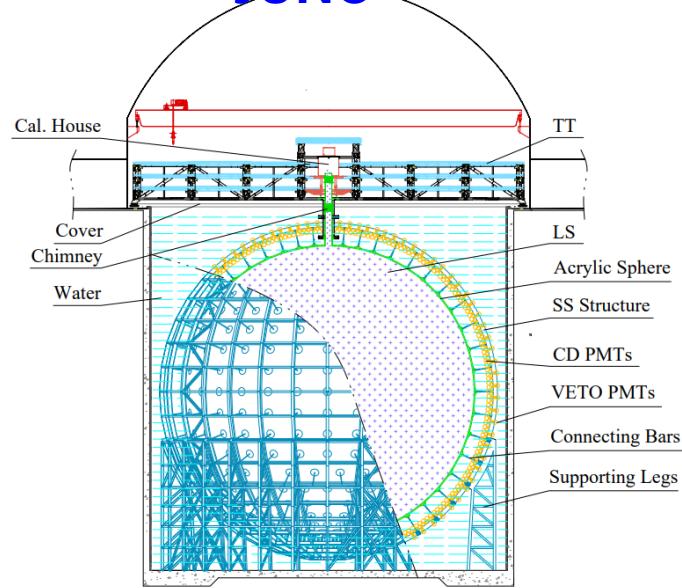
Hyper-K



DUNE



JUNO



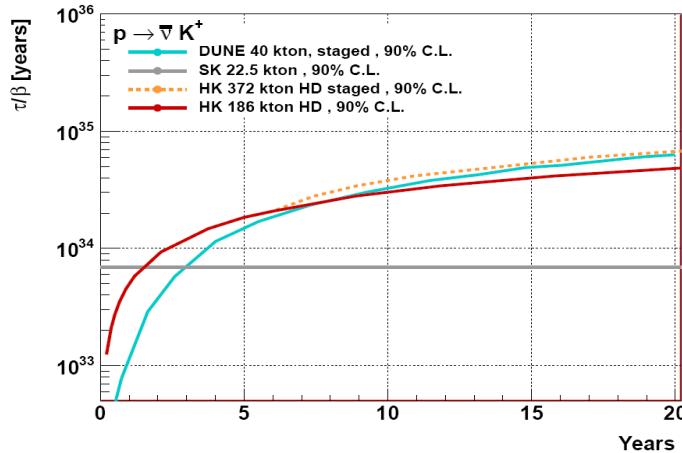
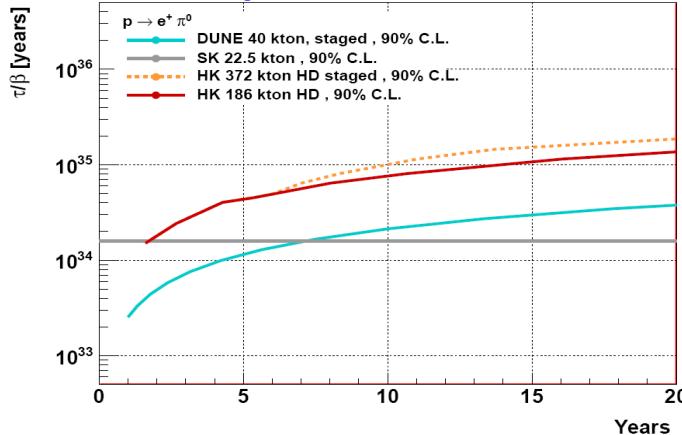
	Hyper-K	DUNE	JUNO
Mass (kton)	258 (186)	4*17 (4*10)	20
Target Nucleus	H ₂ O	Ar40	12% H, 88% C12
Technology	Water Cerenkov	LAr TPC	Liquid Scintillator
Start Time	2027	2028/29	2025



Proton decay searches in Hyper-K



Similar analysis methods with Super-K:



10 years sensitivity with 1 TANK:

Mode	Sensitivity (90% CL) [years]	Current limit [years]
$p \rightarrow e^+ \pi^0$	7.8×10^{34}	2.4×10^{34}
$p \rightarrow \bar{\nu} K^+$	3.2×10^{34}	0.59×10^{34}
$p \rightarrow \mu^+ \pi^0$	7.7×10^{34}	0.77×10^{34}
$p \rightarrow e^+ \eta^0$	4.3×10^{34}	1.0×10^{34}
$p \rightarrow \mu^+ \eta^0$	4.9×10^{34}	0.47×10^{34}
$p \rightarrow e^+ \rho^0$	0.63×10^{34}	0.07×10^{34}
$p \rightarrow \mu^+ \rho^0$	0.22×10^{34}	0.06×10^{34}
$p \rightarrow e^+ \omega^0$	0.86×10^{34}	0.16×10^{34}
$p \rightarrow \mu^+ \omega^0$	1.3×10^{34}	0.28×10^{34}
$n \rightarrow e^+ \pi^-$	2.0×10^{34}	0.53×10^{34}
$n \rightarrow \mu^+ \pi^-$	1.8×10^{34}	0.35×10^{34}

Hyper-Kamiokande Design Report: 1805.04163



Liquid Argon TPC: DUNE

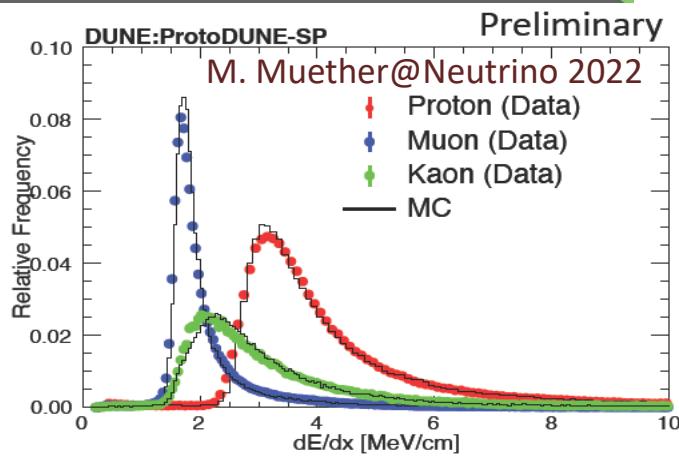
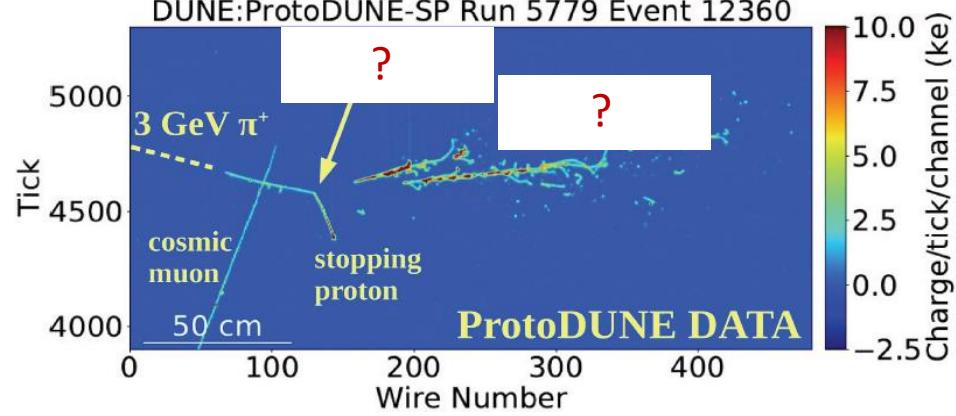


4x10 kton, LArTPC, 87 K, 1475m, 1300 km → δ_{CP} , MH, B-violation

1300 km



DUNE: ProtoDUNE-SP Run 5779 Event 12360



400 kton yrs



$$\tau/B(p \rightarrow e^+\pi^0) > 0.87 - 1.1 \times 10^{34} \text{ yrs } (E \text{ smearing})$$

$$\tau/B(\bar{p} \rightarrow \bar{e} K^+) > 1.3 \times 10^{34} \text{ yrs, } (30\%, 0.4 \text{ bkg})$$

DUNE Physics 2002.03005

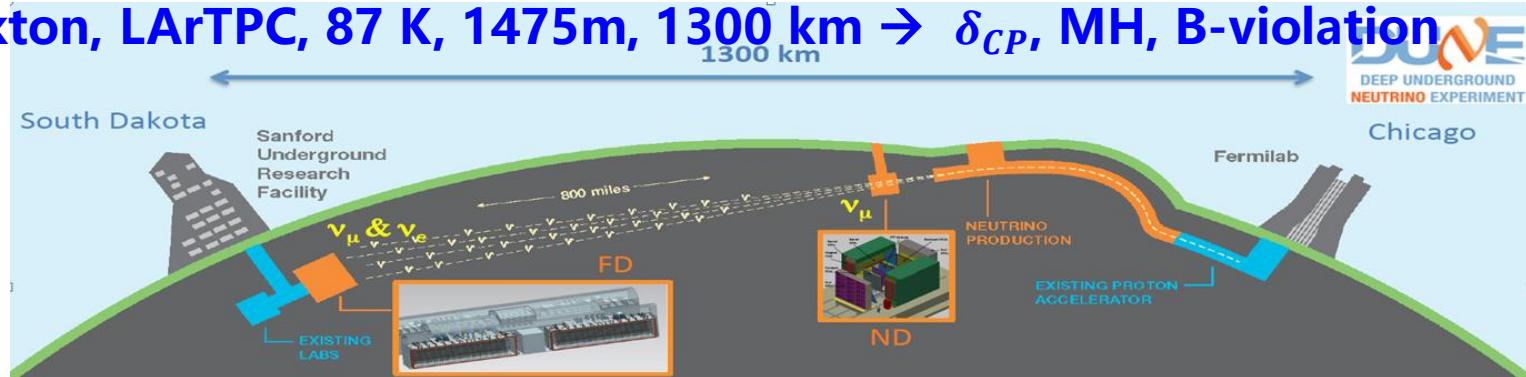


Liquid Argon TPC: DUNE

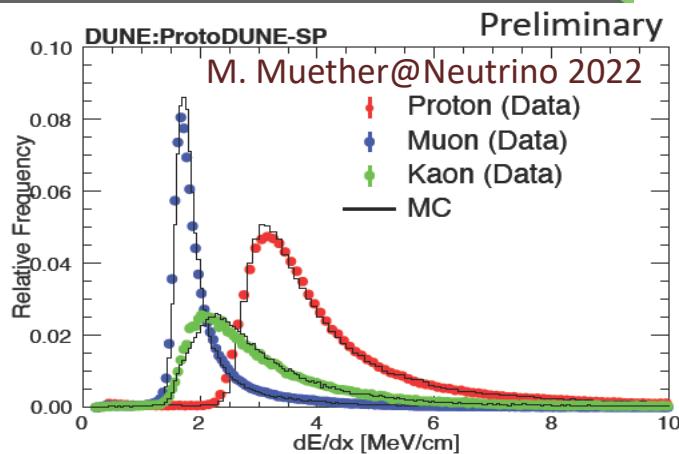
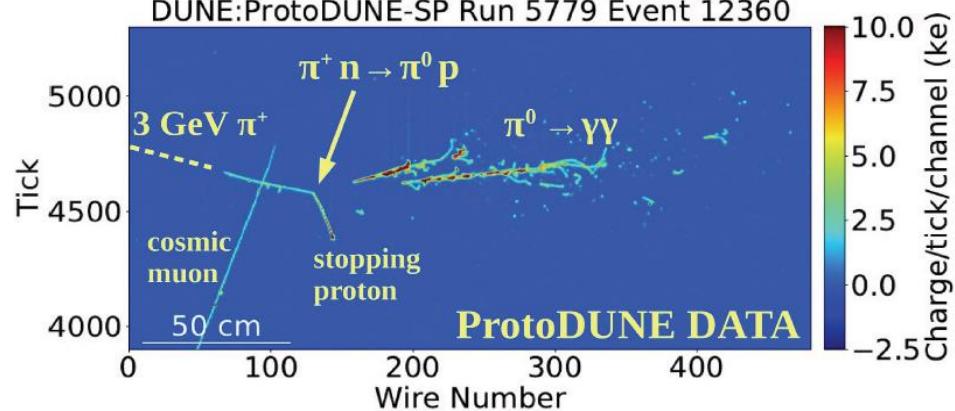


4x10 kton, LArTPC, 87 K, 1475m, 1300 km → δ_{CP} , MH, B-violation

1300 km



DUNE:ProtoDUNE-SP Run 5779 Event 12360



400 kton yrs

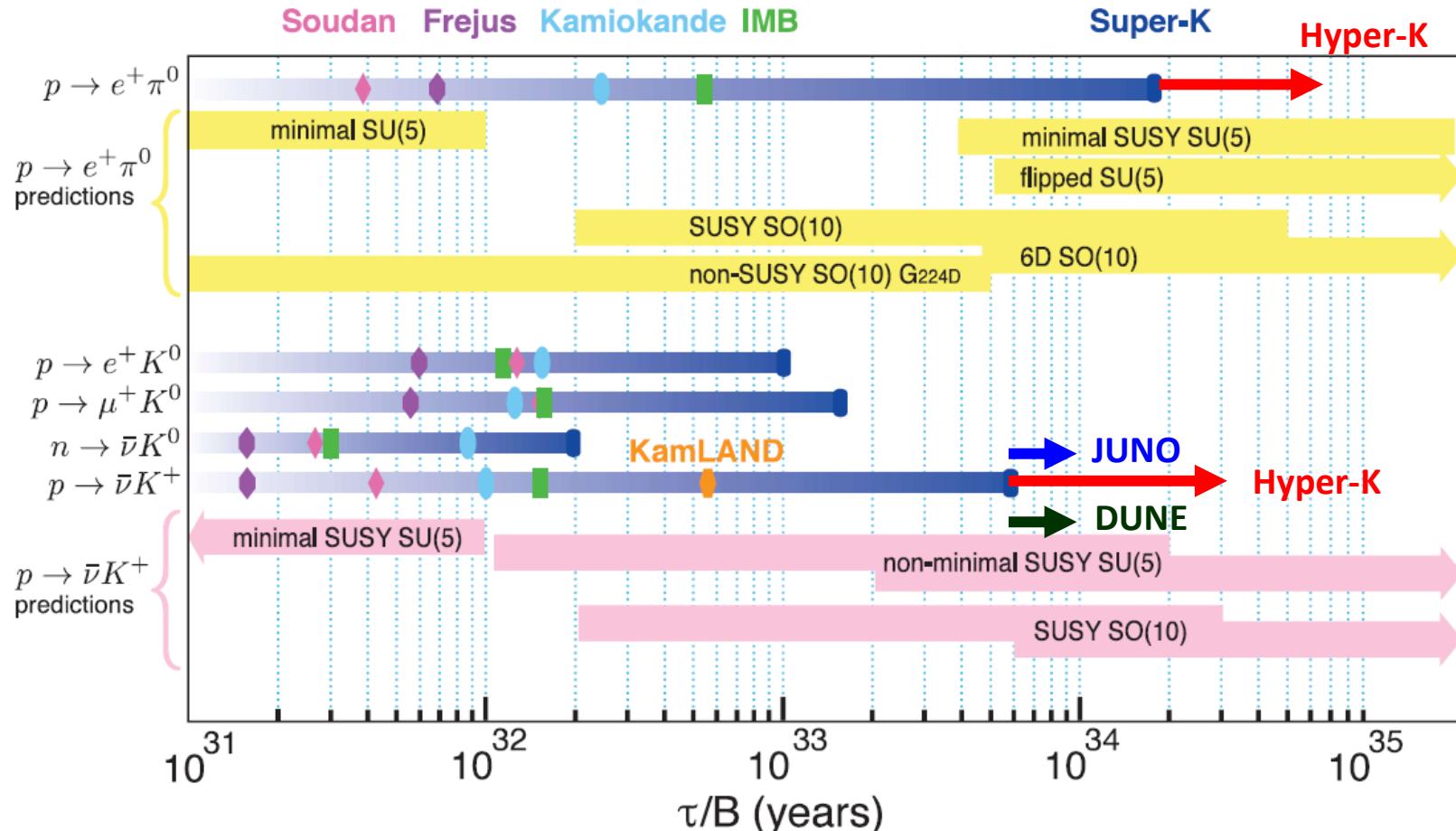


$$\tau/B(p \rightarrow e^+\pi^0) > 0.87 - 1.1 \times 10^{34} \text{ yrs } (E \text{ smearing})$$

$$\tau/B(p \rightarrow \bar{\nu} K^+) > 1.3 \times 10^{34} \text{ yrs, } (30\%, 0.4 \text{ bkg}) \quad \text{DUNE Physics 2022.03005}$$



Future sensitivities of 10yrs on two flavor channels





Comparison of Hyper-K, DUNE and JUNO



	Hyper-K	DUNE	JUNO
Mass (kton)	258 (186)	4*17 (4*10)	20
Target Nucleus	H ₂ O	Ar40	12% H, 88% C12
Technology	Water Cerenkov	LAr TPC	Liquid Scintillator
Start Time	2027	2028/29	2025
Advantages	Large mass and cheap Good particle Identification Good direction resolution	Excellent track reconstruction Excellent particle Identification Good energy resolution	Excellent energy resolution 3% Excellent E threshold 0.7MeV
Shortcomings	Cerenkov threshold	Complex FSI for Ar40	Direction information lost

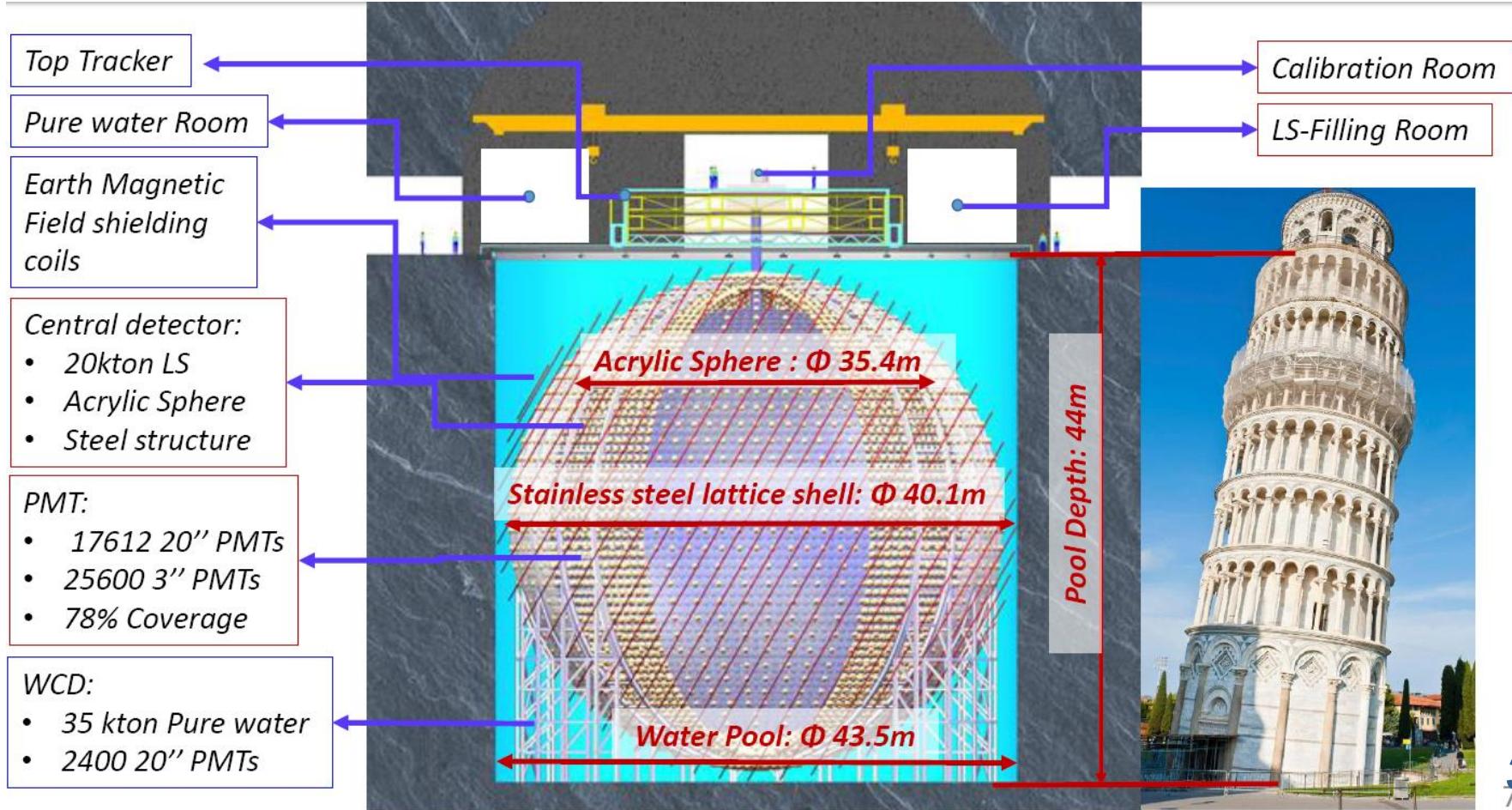
未来3大质子衰变实验!



(3) *JUNO* 寻找质子衰变的潜力



JUNO Detector





JUNO Detection Principle

Fermions		
Leptons	Baryons	Mesons
Electron (e^-)	Proton (p^+)	Photon (γ)
Electron Neutrino (ν_e)	Pion (π^+)	W (W^\pm)
Tau (τ^-)	Anti Proton (\bar{p})	W' (W'^\pm)
Tau Neutrino (ν_τ)	Kaon (K^\pm)	Z (Z^\pm)
Muon (μ^-)	Rho (ρ^\pm)	Z' (Z'^\pm)
Muon Neutrino (ν_μ)	Beta-zero (Λ^0)	Gluon?
Lambda		

Charged particles enter or are produced in LS

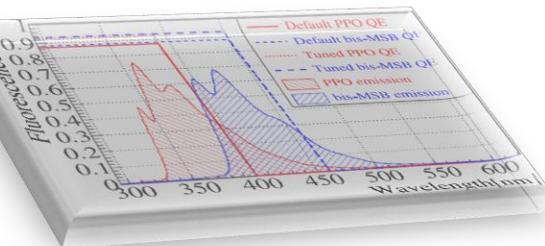
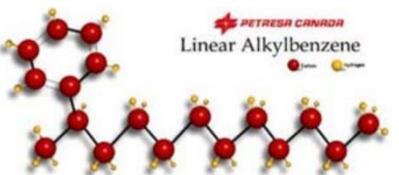
$$\sigma_E \approx \frac{\sqrt{1665}}{1665} \approx 2.5\%$$

$E_{\text{threshold}} = 0.7 \text{ MeV}$

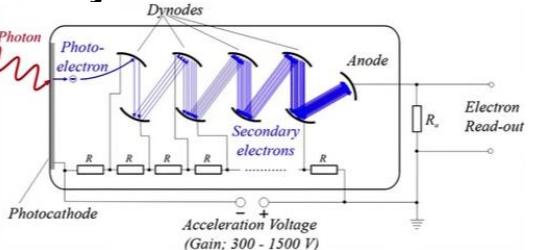
Waveform and Reconstruction
PEs $\sim 1665/\text{MeV}$

Very high PMT coverage (78%)

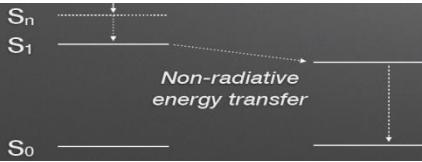
Ionize LAB molecule



PMT amplification:
Dynode & MCP

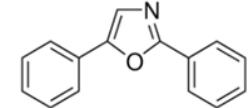


PPO as Fluor: De-excite

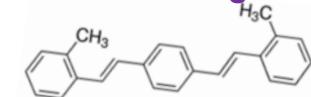


$\sim 10000 \text{ photons/MeV}$

PPO 2.5g/L



Bis-MSB 3 mg/L



Highly transparent LS

Propagate in the LS:
bis-MSB as λ shifter



Photon electron via photoelectric effect,
PMT collects PEs

Highly efficient PMTs
(PDE $\sim 30\%$)





JUNO探测质子衰变的优缺点



优点:

1. Large mass (20 kton) → Free p : 1.43×10^{33} ; Bounded p/n : 5.30×10^{33}
2. Excellent $\sigma_E = 3\%/\sqrt{E}$ → Mono-energy products from free p decay
3. Low threshold (0.2 MeV) → Residual nucleus
4. Neutron tag (2.2 MeV) → Separate signals from BG
5. 1GHz sampling rate → Waveform

缺点:

1. Difficult to reconstruct direction → can't use momentum conservation
2. Difficult to identify particles → can't effectively separate S/B

JUNO可用的物理量:

能量、位置、时间、波形、米歇尔电子数、中子数、残余核

粒子方向重建的突破将会极大改善JUNO对很多核子衰变道的敏感度!



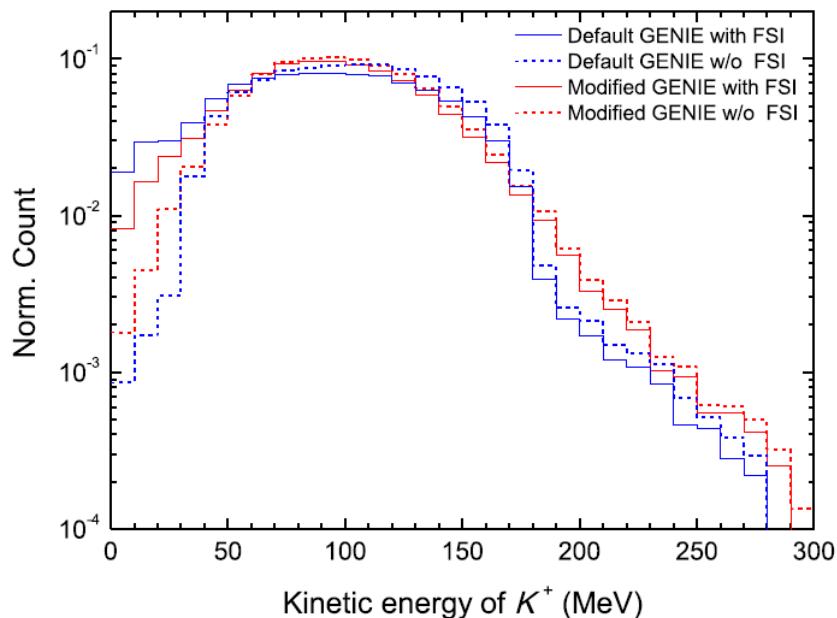
Search for $p \rightarrow \bar{\nu} K^+$ in JUNO



20 kton LS: Free proton: 1.45×10^{33}
Bound proton: 5.30×10^{33}

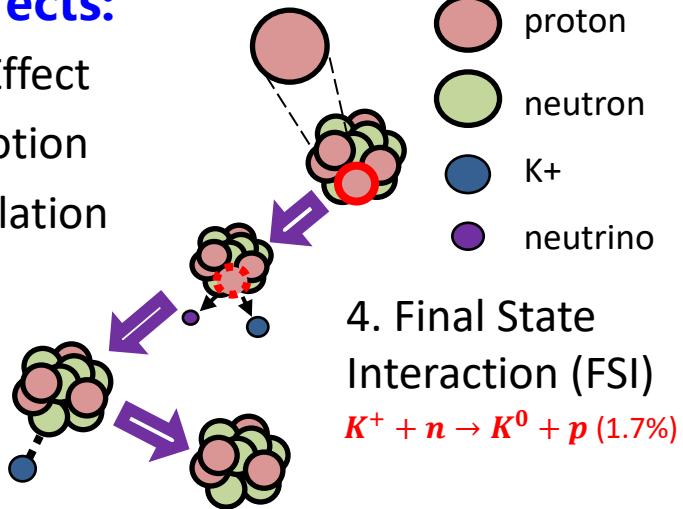
Kinetic energy of K^+

Free proton $\rightarrow 105$ MeV
Bound proton: \downarrow



Nuclear Effects:

1. Binding Effect
2. Fermi Motion
3. NN correlation



5. De-excitation of remaining nuclear:
could emit $\gamma/p/n$.

- **Modify GENIE generator**
- **Implement de-excitation with TALYS**

H. Hu, W.L. Guo et al, PLB 831, 137183(2022)

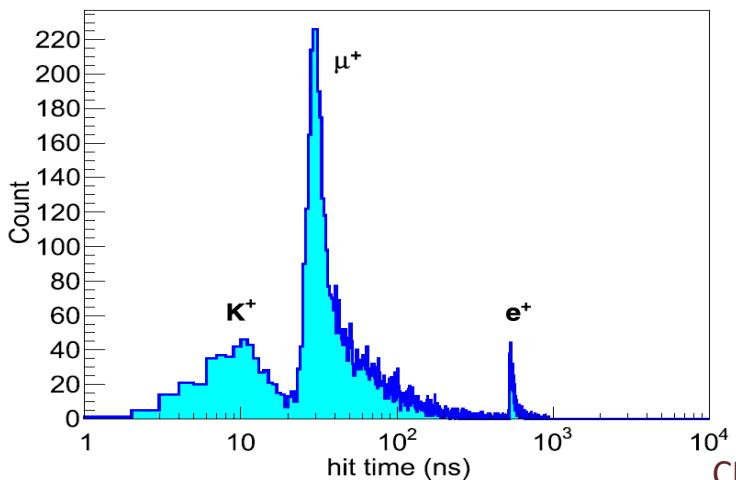


Signal characters of $p \rightarrow \bar{\nu} K^+$ in JUNO



Triple coincident signals :

Decay mode	Branching ratio (%)	Kinetic energy sum (MeV)
$K^+ \rightarrow \mu^+ \nu_\mu$	63.55 ± 0.11	152
$K^+ \rightarrow \pi^+ \pi^0$	20.66 ± 0.08	354
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	5.59 ± 0.04	75
$K^+ \rightarrow \pi^0 e^+ \nu_e$	5.07 ± 0.04	265–493
$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$	3.353 ± 0.034	200–388
$K^+ \rightarrow \pi^+ \pi^0 \pi^0$	1.761 ± 0.022	354



CPC 47, 113002 (2023)

First pulse: K^+ kinetic energy of ~105 MeV, decay at rest

$K^+ \rightarrow \nu_\mu + \mu^+$

Second pulse
 $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$

152 MeV (μ^+) or 354 MeV(π^+, π^0)

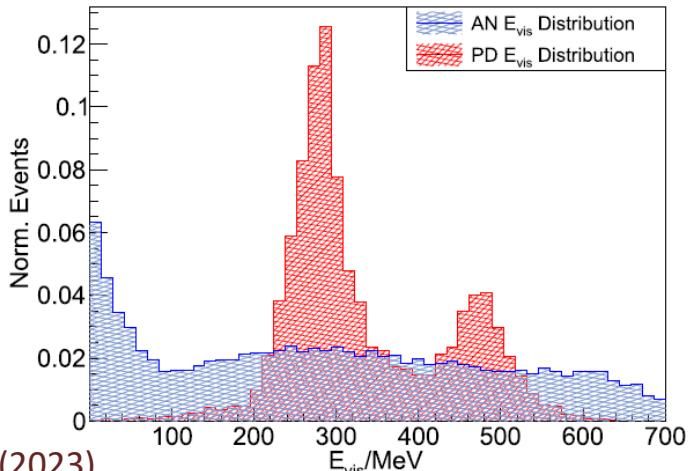
$K^+ \rightarrow \pi^+ + \pi^0$

Second pulse
 $\pi^0 \xrightarrow{8.4 \times 10^{-8} \text{ ns}} 2\gamma$

$\pi^+ \rightarrow \nu_\mu + \mu^+$

Third pulse: Michel e^+
 $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$

AN and PD candidates Evis Distribution





Backgrounds



Type	Ratio (%)	Ratio with E_{vis} in [100 MeV, 600 MeV](%)	Interaction	Signal characteristics
N CES	20.2	15.8	$\nu + n \rightarrow \nu + n$ $\nu + p \rightarrow \nu + p$	Single Pulse
CCQE	45.2	64.2	$\nu_l + p \rightarrow n + l^+$ $\nu_l + n \rightarrow p + l^-$	Single Pulse
Pion Production	33.5	19.8	$\nu_l + p \rightarrow l^- + p + \pi^+$ $\nu + p \rightarrow \nu + n + \pi^+$	Approximate Single Pulse (Second pulse too low)
Kaon Production	1.1	0.2	$\nu_l + n \rightarrow l^- + \Lambda + K^+$ $\nu_l + p \rightarrow l^- + p + K^+$	Double Pulse

- If energetic neutrons do not lost most of the energy within ~10ns
- Kaon Production has a negligible contribution!

Event Selection

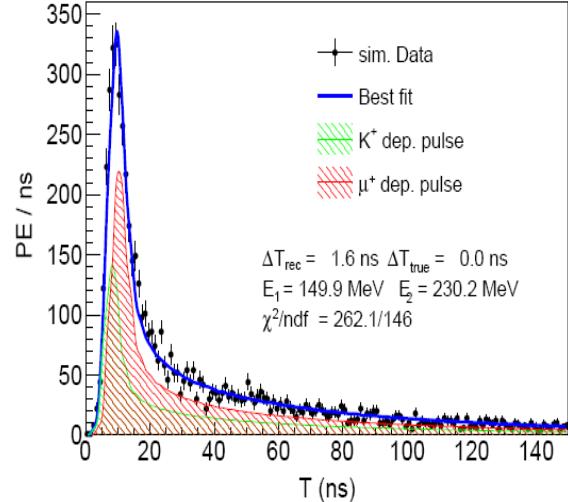
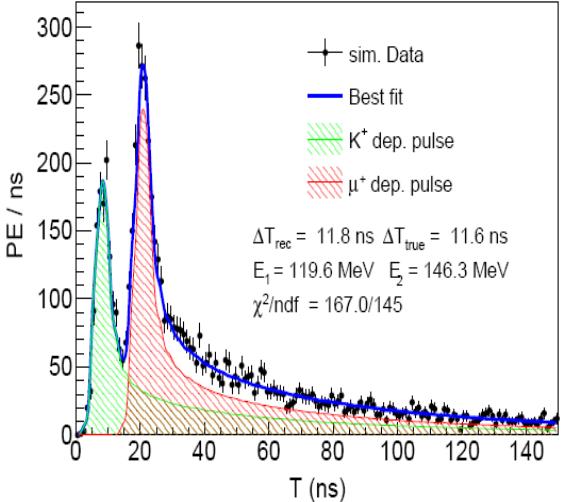
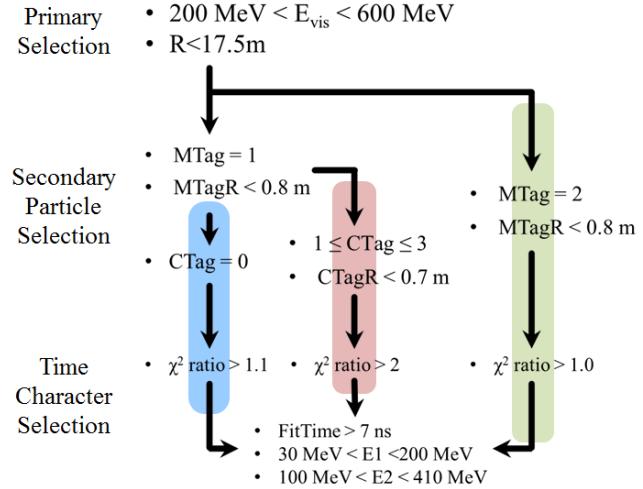


TABLE II. Detection efficiencies of $p \rightarrow \bar{\nu}K^+$ and the number of atmospheric $\bar{\nu}$ background after each selection criterion. The total amount of atmospheric $\bar{\nu}$ background simulated is 160 k, which corresponds to an exposure of 890 kton-years.

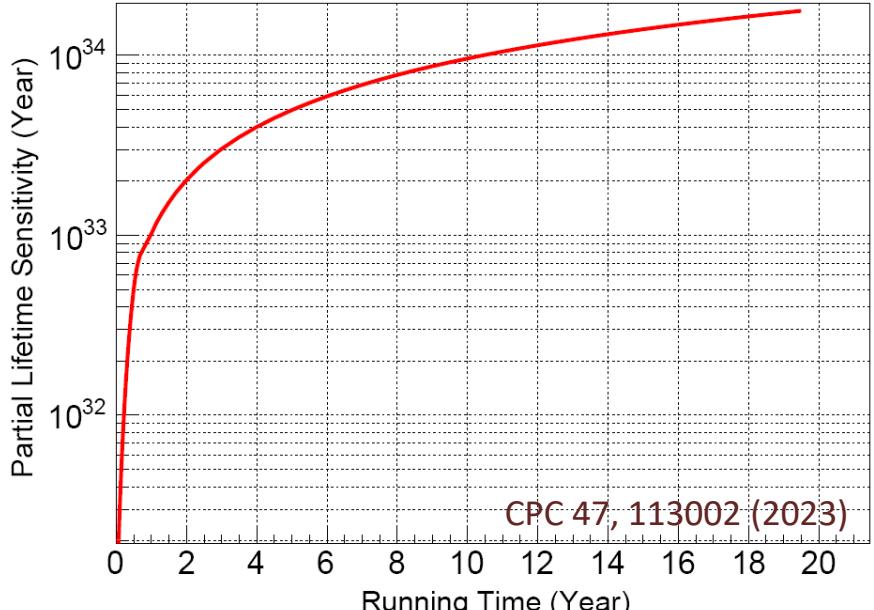
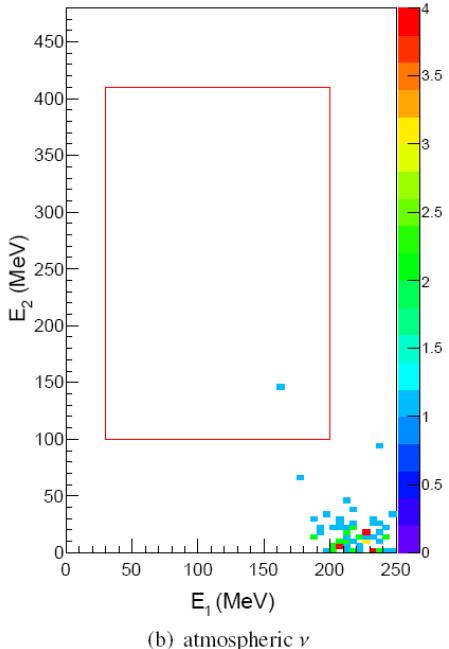
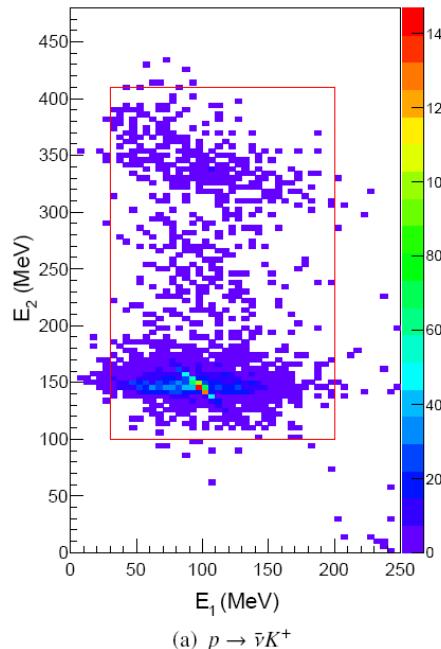
Criteria	Survival rate of $p \rightarrow \bar{\nu}K^+$ (%)			Survival count (fraction) of atmospheric $\bar{\nu}$		
	Sample 1	Sample 2	Sample 3	Sample 1	Sample 2	Sample 3
basic selection	E_{vis}	94.6		51299 (32.1%)		
	R_V	93.7		47849 (29.9%)		
Delayed signal selection	N_M	74.4		20739 (13.0%)	1143 (0.7%)	
	ΔL_M	67.0		13796 (8.6%)	994 (0.6%)	
	N_n	48.4	17.9	—	5403 (3.4%)	6857 (4.3%)
	ΔL_n	—	16.6	—	4472 (2.8%)	—
Time character selection	R_χ	45.9	9.0	3.8	4326 (2.7%)	581 (0.4%)
	ΔT	28.3	7.7	2.4	121 (0.07%)	18 (0.01%)
	E_1, E_2	27.4	7.3	2.2	1 (0.0006%)	0
Total		36.9		1	0	

Efficiency uncertainties:

Source	Uncertainty
Statistic	1.6%
Position reconstruction	1.7%
Nuclear model	6.8%
Energy deposition model	11.1%
Total	13.2%



Sensitivity to $p \rightarrow \bar{v} K^+$



Background: 0.2/10years

Efficiency : 36.9%



$\tau/B(p \rightarrow \bar{v} K^+) > 0.96 \times 10^{34}$ yrs

$n \rightarrow \mu^- K^+, \quad p \rightarrow e^+ K^*(892)^0, \quad n \rightarrow \nu K^*(892)^0, \quad \text{and} \quad p \rightarrow \nu K^*(892)^+$



Neutron invisible decays in JUNO



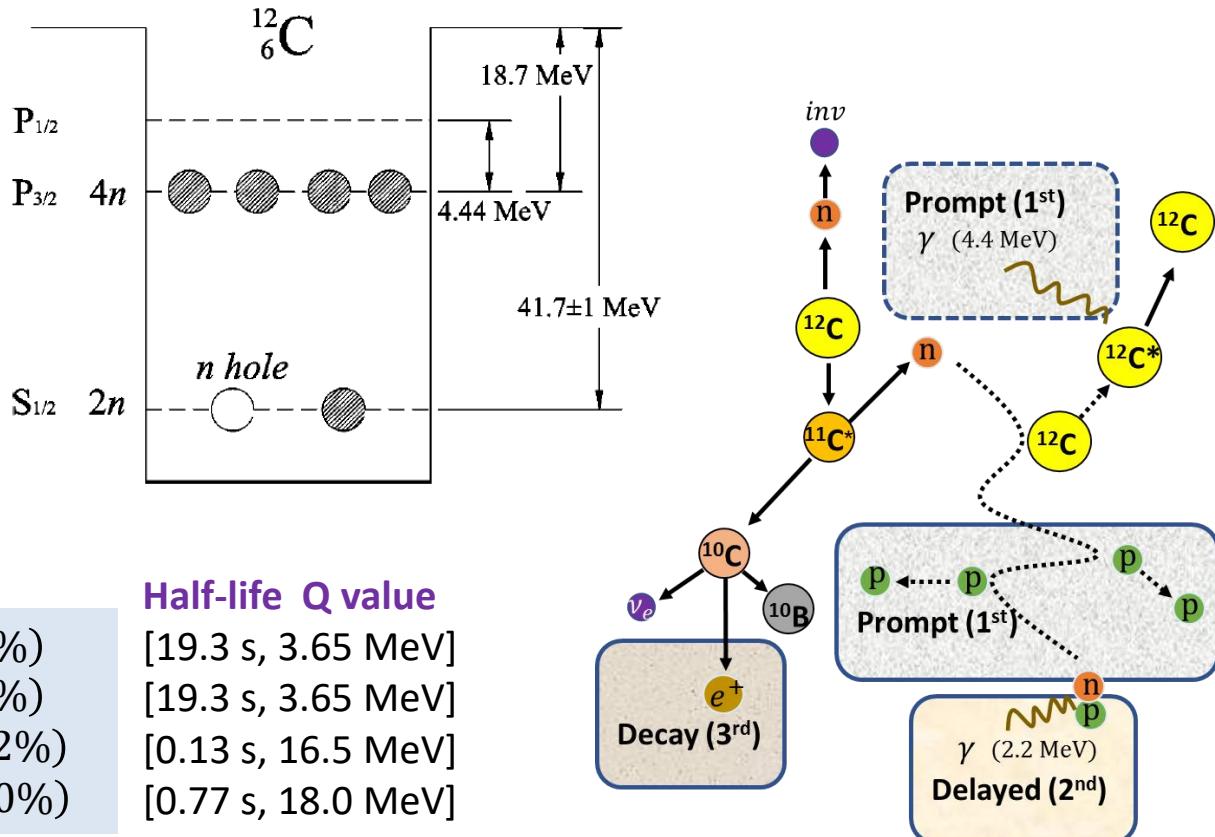
Bounded neutrons in ^{12}C :

- $n \rightarrow \text{inv}$ ($^{12}\text{C} \rightarrow ^{11}\text{C}^*$)
- $nn \rightarrow \text{inv}$ ($^{12}\text{C} \rightarrow ^{10}\text{C}^*$)

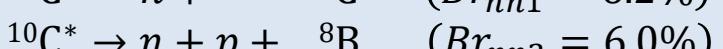
Invisible particle:

neutrinos, NP particles

**Detect de-excitation products
of $^{11}\text{C}^*$ and $^{10}\text{C}^*$**



Triple coincident signals :



Half-life Q value

[19.3 s, 3.65 MeV]

[19.3 s, 3.65 MeV]

[0.13 s, 16.5 MeV]

[0.77 s, 18.0 MeV]

Y. Kamshkov and E. Kolbe, PRD 67, 076007 (2003)



Background Sources



➤ Singles

- Radioactivity
- Long-lived isotope

➤ Correlated (prompt-delayed)

- IBD
- Long-lived isotope (Li9/He8)
- Fast neutron
- Alpha-n
- Atm- ν NC

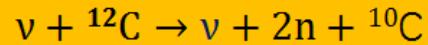
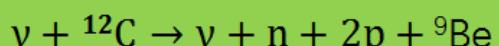
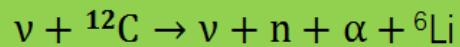
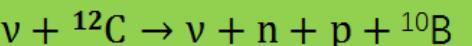
➤ Triple (prompt-delayed-decay)

- Atm- ν NC
- Li9/He8 + isotope (from same muon)



Combination

- Correlated + Singles
- Singles + Singles + Singles

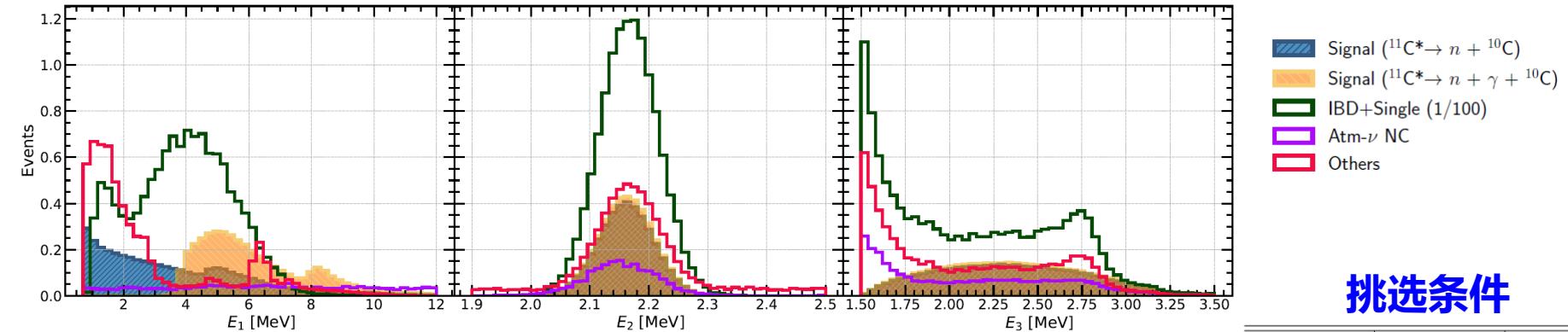




Signal vs backgrounds



Dominant BKGs of $n \rightarrow inv$: IBD + Singles (1235), Atm- ν NC (3.0) per 10 years



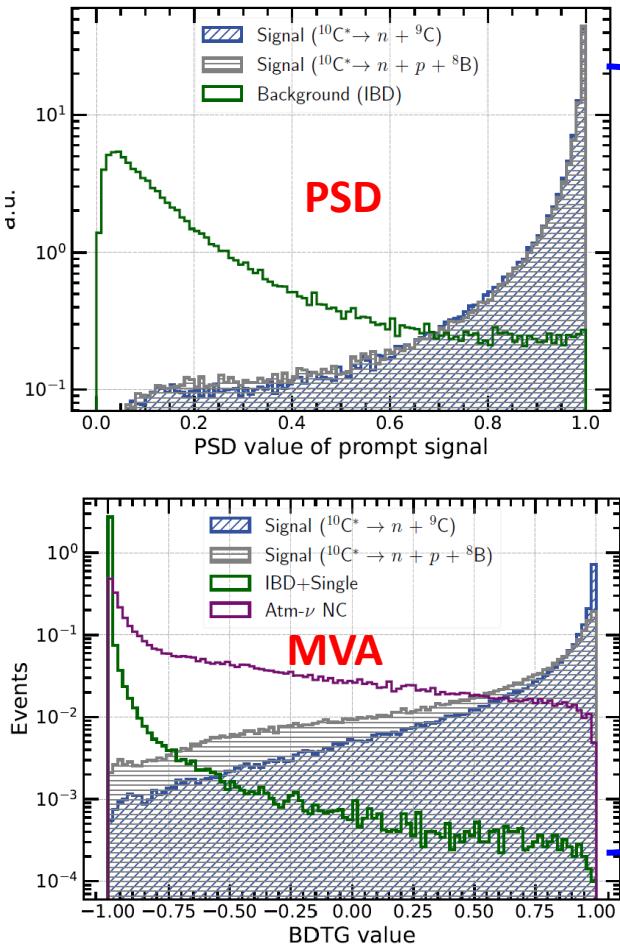
挑选条件

Quantity	$n \rightarrow inv$	$nn \rightarrow inv$
$R_{1,2,3}$ [m]	< 16.7	< 16.7
E_1 [MeV]	0.7-12	0.7-30
E_2 [MeV]	1.9-2.5	1.9-2.5
E_3 [MeV]	1.5-3.5	3.0-16.0
ΔT_{12} [ms]	< 1	< 1
ΔT_{23} [s]	0.002-100	0.002-3.0
ΔR_{12} [m]	< 1.5	< 1.5
ΔR_{23} [m]	< 1.5	< 1.5
ΔR_{13} [m]	< 1.0	< 1.0

Dominant BKGs of $nn \rightarrow inv$: IBD + Singles (3.0), Atm- ν NC (4.3) per 10 years



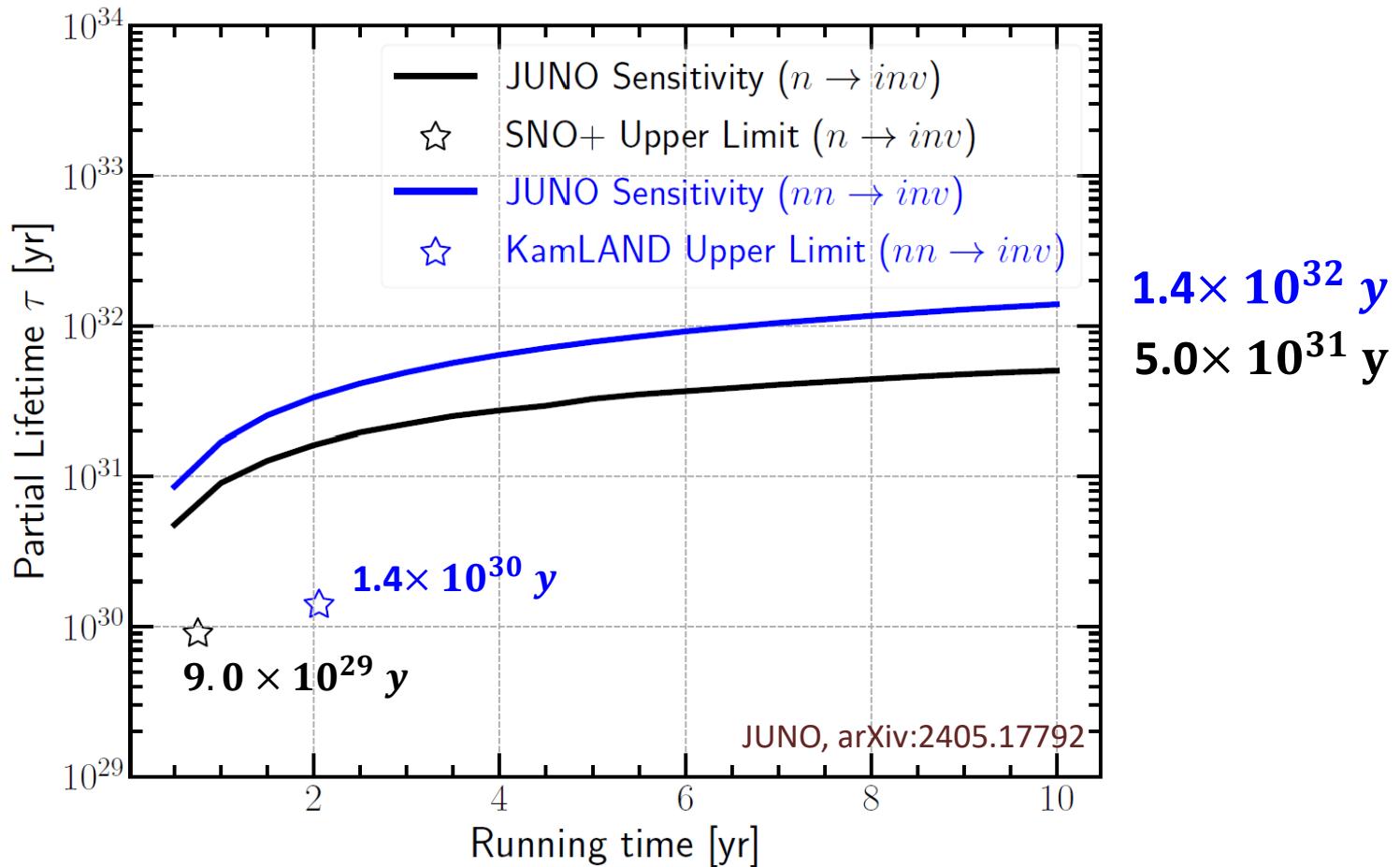
Summary of Backgrounds and Signal efficiency



Backgrounds (10 years)	$n \rightarrow \text{inv}$		$nn \rightarrow \text{inv}$	
	Basic selection	PSD + MVA	Basic selection	PSD + MVA
IBD + Single	1235 ± 50	2.72 ± 0.10	3.01 ± 0.09	0.0110 ± 0.0003
Atm- ν NC	3.0 ± 1.1	0.93 ± 0.67	4.3 ± 3.5	0.55 ± 0.63
$^{13}\text{C}(\alpha, n){}^{16}\text{O}$ + Single	3.4 ± 1.4	0.036 ± 0.013	-	-
${}^9\text{Li}/{}^8\text{He}$ + Single	1.55 ± 0.39	0.29 ± 0.17	0.13 ± 0.13	0.13 ± 0.13
Accidental	1.46 ± 0.05	0.095 ± 0.004	-	-
Total	1244 ± 50	4.07 ± 0.68	7.4 ± 3.5	0.69 ± 0.64
Signal efficiency (%)	$n \rightarrow \text{inv}$		$nn \rightarrow \text{inv}$	
	Basic selection	PSD + MVA	Basic selection	PSD + MVA
$\epsilon_{n(nn)1}$	35.6 ± 0.2	23.5 ± 0.2	54.0 ± 0.3	48.2 ± 0.3
$\epsilon_{n(nn)2}$	43.6 ± 0.3	30.3 ± 0.3	49.2 ± 0.3	36.3 ± 0.3

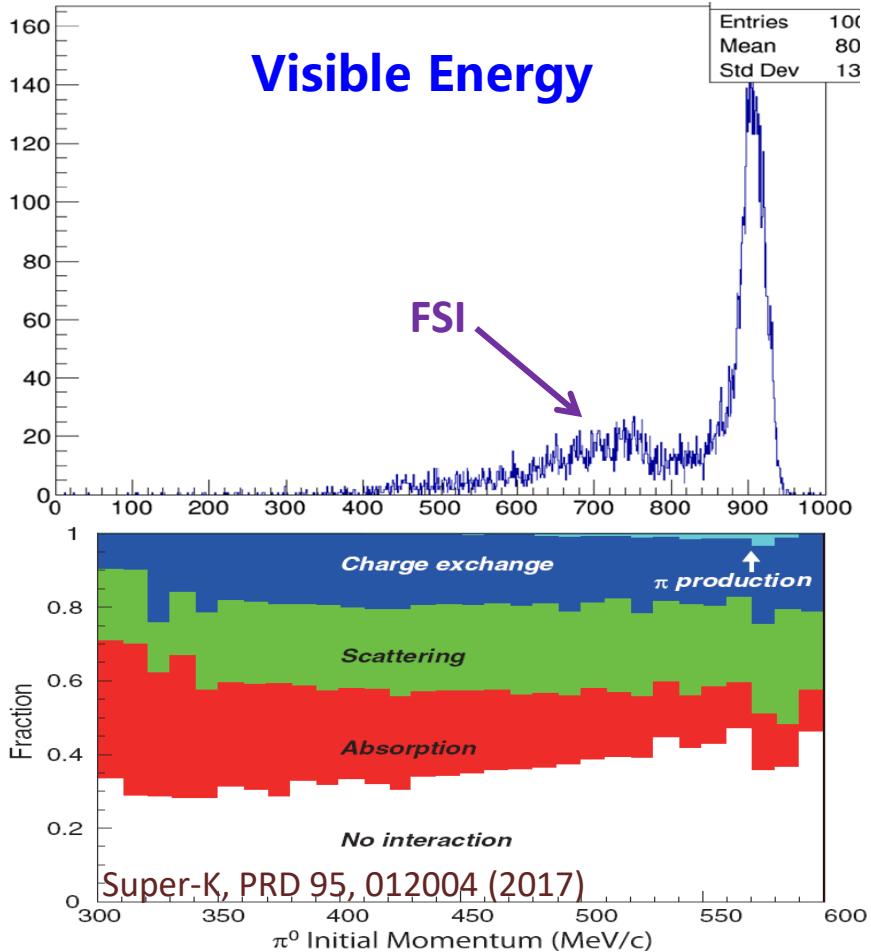


JUNO sensitivity

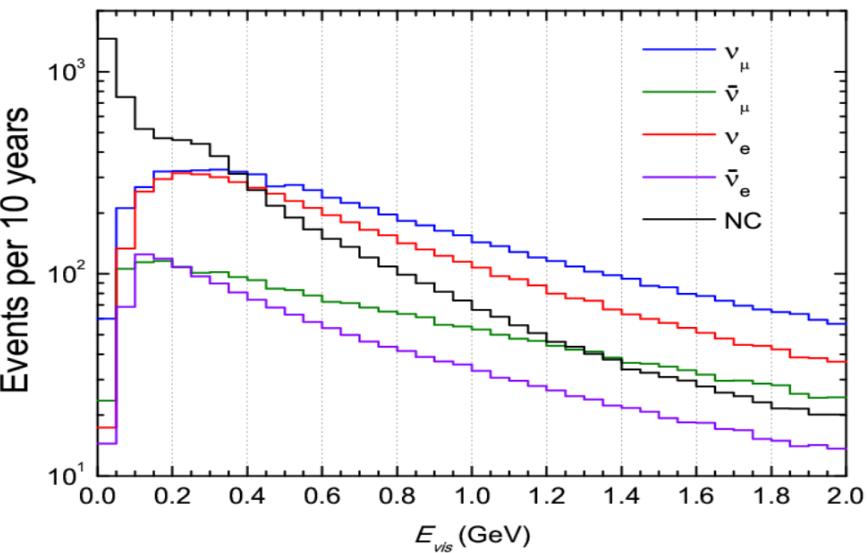




Search for $p \rightarrow e^+ + \pi^0$ in JUNO



Atmospheric v backgrounds:



10 years:
 $0.05\text{-}1\text{GeV} \rightarrow \mathbf{18114}$
(CC:11714; NC:6400)



Sensitivity estimation for $p \rightarrow e^+ + \pi^0$



Event Selection: $860 \text{ MeV} < \text{Evis} < 940 \text{ MeV}$; no Michel; no neutron capture

→ **Signal Efficiency** : 50.9%; **Background**: **97.8**/10years

$$\tau/B(p \rightarrow e^+ \pi^0) > 0.19 \times 10^{34} \text{ yrs} \quad (\ll 2.4 \times 10^{34} \text{ yrs from Super-K})$$

How to estimate sensitivity?

$$N_{S_i} = N_{decay} \cdot B_i \cdot \epsilon_i = B_i \cdot \epsilon_i \cdot N_0 \frac{t}{\tau} \rightarrow \frac{\tau}{B_i} = \frac{N_0 \cdot \epsilon_i}{N_{90}} t$$

N_{S_i} : Signal number

N_0 : Nucleon number = 6.75×10^{33}

ϵ_i : Signal Efficiency = 50.9%

t : Running Time = 10 years

N_{90} : 90% CL upper limit = 17.7

N_B : Expected BG number = 97.8

90% CL upper limit N_{90} :

$$L(N_{obs}, N_S) = \frac{(N_S + N_B)^{N_{obs}}}{N_{obs}!} e^{-(N_S + N_B)} \rightarrow 90\% = \frac{\int_0^{N_{90}} L(N_{obs}, N_S) dN_S}{\int_0^{\infty} L(N_{obs}, N_S) dN_S}$$

$N_{obs} = N_B$	0.0	1.0	2.0	5.0	10	20	50	100	200	1000
N_{90}	2.3	3.3	3.9	5.2	6.6	8.8	13.0	17.8	24.6	53.3

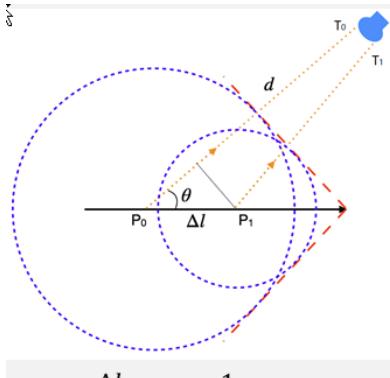
BKG number is the key quantity!!! → How to suppress BKG?



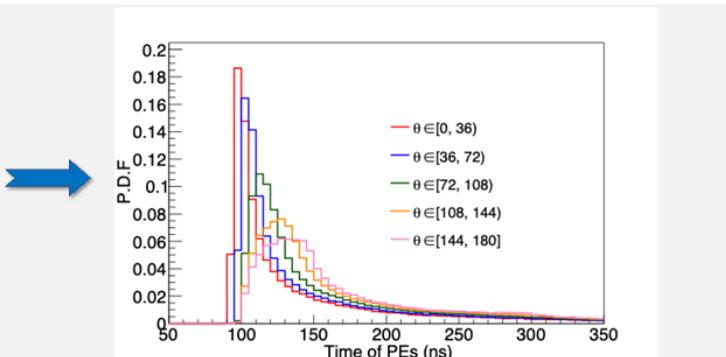
How to suppress BKG ? → Momentum information



ν directional information reflects in each PMT waveform

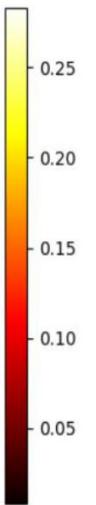
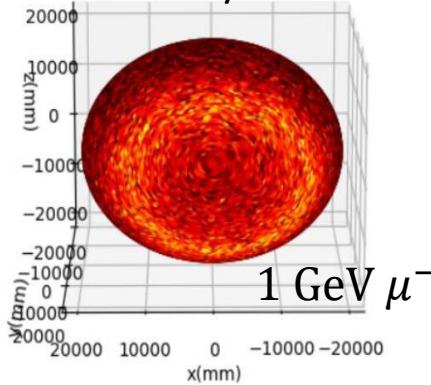


$$\frac{\Delta l}{\Delta t} \propto \frac{1}{|1 - n\beta \cos\theta|}$$

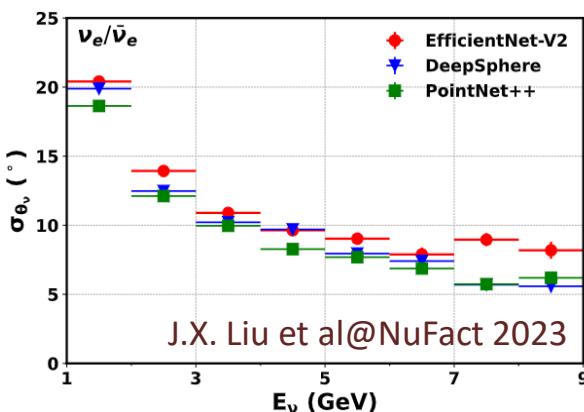
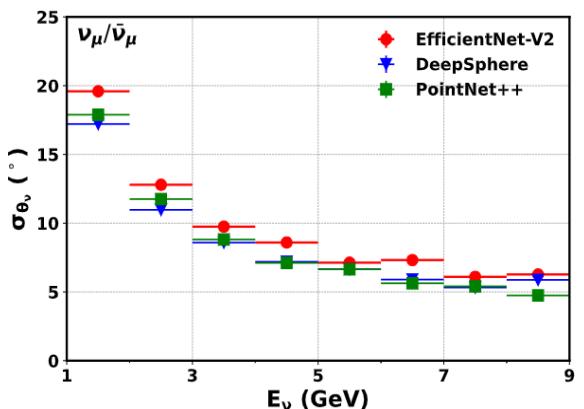
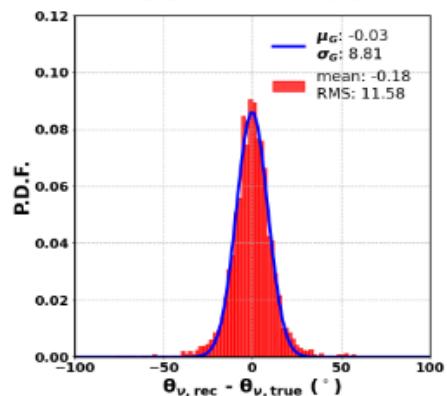


Distribution of the number of photoelectrons (PEs) over time for PMTs with different angles θ to the particle track

Cerenkov-like Ring:
First 4ns PEs/total PEs



3GeV < E < 4GeV



J.X. Liu et al@NuFact 2023



Simply estimate JUNO sensitivities to other channels (1)



Y.J. Niu et al

Only use:

1. Energy
2. Michel e^\pm
3. n capture
4. Assumption

Antilepton+ Meson									
ID	Channels	n_b	n_{90}	$\epsilon(\%)$	$\tau_{10}(10^{33} \text{ yrs})$	$\tau_3(10^{33} \text{ yrs})$	$\tau_{exp}(10^{33} \text{ yrs})$	TECN	Rank
1	$p \rightarrow e^+\pi^0$	97.8	17.7	50.9	1.9	1	24	SKAM(20)	E
*1	$n \rightarrow e^+\pi^-$	1943.0	73.9	83.44	0.578	0.312	5.3	SKAM(17D)	E
2	$p \rightarrow \mu^+\pi^0$	152.6	21.7	54.68	1.6	0.9	16	SKAM(20)	E
*2	$n \rightarrow \mu^+\pi^-$	2101.3	76.8	85.14	0.568	0.306	3.5	SKAM(17D)	E
3	$p \rightarrow \bar{\nu}\pi^+$	7172.09,3405.55	162.8	91.24	0.366	0.199	0.39	SKAM(14E)	D
*3	$n \rightarrow \bar{\nu}\pi^0$	2668.9	86.3	59.06	0.351	0.189	1.1	SKAM(14E)	E
4	$p \rightarrow e^+\eta$	97.8	17.7	30.62	1.1	0.56	10	SKAM(17D)	E
5	$p \rightarrow \mu^+\eta$	134.1	20.4	30.62	1	0.5	4.7	SKAM(17D)	E
6	$n \rightarrow \bar{\nu}\eta$	336.1	37.8	31.42	0.528	0.2657	0.158	IMB3(99)	B
7	$p \rightarrow e^+\rho^0$	4398.9	110.4	91.11	0.5384	0.2918	0.72	SKAM(17D)	D
*7	$n \rightarrow e^+\rho^-$	2067.5	76.1	83.75	0.564	0.304	0.217	IMB3(99)	B
8	$p \rightarrow \mu^+\rho^0$	3067.4	92.4	93.48	0.6600	0.3566	0.57	SKAM(17D)	C
*8	$n \rightarrow \mu^+\rho^-$	2323.6	80.6	87.71	0.557	0.301	0.228	IMB3(99)	B
9	$p \rightarrow \bar{\nu}\rho^+$	1657.6,1394.7,102.8	81.8	70.17	0.559	0.300	0.162	IMB3(99)	B
*9	$n \rightarrow \bar{\nu}\rho^0$	214.1	25.5	41	0.8237	0.432	0.019	IMB(88)	A
10	$p \rightarrow e^+\omega$	1:1024.2,97.8 2:4398.9	106.1	30.61	0.1947	0.1052	1.6	SKAM(17D)	E
11	$p \rightarrow \mu^+\omega$	1:116.2, 118.7 2:3067.4	45.5	30.44	0.4425	0.2303	2.8	SKAM(17D)	E
12	$n \rightarrow \bar{\nu}\omega$	1: 640 2:4398.9	92.2	28.23	0.1623	0.087	0.108	IMB3(99)	C

Three and more leptons									
ID	Channels	n_{bkg}	n_{90}	$\epsilon(\%)$	$\tau_{10}(10^{33} \text{ yrs})$	$\tau_3(10^{33} \text{ yrs})$	$\tau_{exp}(10^{33} \text{ yrs})$	TECN	Rank
49	$p \rightarrow e^+e^+e^-$	97.8	17.7	77.78	2.9	1.5	34	SKAM(20)	E
50	$p \rightarrow e^+\mu^+\mu^-$	24.5	9.6	79.24	5.38	2.58	9.2	SKAM(20)	D
51	$p \rightarrow e^+\bar{\nu}\nu$	2460.1	83	90.83	0.714	0.386	0.17	SKAM(14)	B
52	$n \rightarrow e^+e^-\bar{\nu}\nu$	1255.7	59.7	88.39	0.758	0.408	0.257	IMB3(99)	B
53	$n \rightarrow \mu^+e^-\bar{\nu}\nu$	1256.7	59.7	90.75	0.779	0.419	0.083	IMB3(99)	A
54	$n \rightarrow \mu^+\mu^-\bar{\nu}\nu$	115.4	19.1	89.37	2.397	1.237	0.079	IMB3(99)	A
55	$n \rightarrow \mu^+e^+e^-$	133.9	20.4	83.3	2.1	1.1	23	SKAM(20)	E
56	$n \rightarrow \mu^+\mu^+\mu^-$	0.0	2.4	83.15	17.7	5.3	10	SKAM(20)	A
57	$p \rightarrow \mu^+\bar{\nu}\nu$	983.1	52.9	82.33	1.015	0.544	0.22	SKAM(20)	B
58	$p \rightarrow e^-\mu^+\mu^+$	23.1	9.29	68.43	4.8	2.3	11	SKAM(20)	D

VS Super-K?



Simply estimate JUNO sensitivities to other channels (2)



Antilepton+Mesons									
ID	Channels	n_{bkg}	n_{90}	$\epsilon(\%)$	$\tau_{10}(10^{33} \text{ yrs})$	$\tau_3(10^{33} \text{ yrs})$	$\tau_{exp}(10^{33} \text{ yrs})$	TECN	Rank
23	$p \rightarrow e^+ \pi^+ \pi^-$	4398.9	110.4	91.11	0.5384	0.2918	0.082	IMB3(99)	A
24	$p \rightarrow e^+ \pi^0 \pi^0$	214.1	25.5	41	1.049	0.550	0.147	IMB3(99)	A
25	$n \rightarrow e^+ \pi^- \pi^0$	2067.5	76.1	83.75	0.564	0.304	0.052	IMB3(99)	A
26	$p \rightarrow \mu^+ \pi^+ \pi^-$	3067.4	92.4	93.48	0.6600	0.3566	0.133	IMB3(99)	B
27	$p \rightarrow \mu^+ \pi^0 \pi^0$	3591.5	99.9	93.84	0.613	0.332	0.101	IMB3(99)	A
28	$n \rightarrow \mu^+ \pi^- \pi^0$	2323.6	80.6	87.71	0.557	0.301	0.074	IMB3(99)	A
29	$n \rightarrow e^+ \pi^- K^0$	2932.3,460.2	96	96.71	0.516	0.279	0.018	IMB3(91)	A
Lepton+Meson									
ID	Channels	n_{bkg}	n_{90}	$\epsilon(\%)$	$\tau_{10}(10^{33} \text{ yrs})$	$\tau_3(10^{33} \text{ yrs})$	$\tau_{exp}(10^{33} \text{ yrs})$	TECN	Rank
30	$n \rightarrow e^- \pi^+$	1070.4,818.8,163.2	66	80.13	0.622	0.333	0.065	FREJ(88)	A
31	$n \rightarrow \mu^- \pi^+$	1308.9,118,219	40	79.98	1.024	0.534	0.049	IMB(88)	A
32	$n \rightarrow e^- \rho^+$	1657.6,1394.7,102.8	81.8	70.17	0.439	0.236	0.062	IMB(88)	A
33	$n \rightarrow \mu^- \rho^+$	1899.5,192,398,197.6	42.6	74.56	0.897	0.472	0.007	IMB(88)	A
34	$n \rightarrow \mu^- K^+$	257.7,132.0	33	59.54	0.924	0.583	0.032	FREJ(91B)	A
35	$n \rightarrow \mu^- K^+$	42.6,27.7	14.5	58.95	2.083	1.053	0.057	FREJ(91B)	A
Lepton+Mesons									
ID	Channels	n_{bkg}	n_{90}	$\epsilon(\%)$	$\tau_{10}(10^{33} \text{ yrs})$	$\tau_3(10^{33} \text{ yrs})$	$\tau_{exp}(10^{33} \text{ yrs})$	TECN	Rank
36	$p \rightarrow e^- \pi^+ \pi^+$	534.7,46.6,76.6	27.2	41.06	0.985	0.502	0.03	FREJ(91B)	A
37	$n \rightarrow e^- \pi^+ \pi^0$	1657.6,1394.7,102.8	81.8	70.17	0.439	0.236	0.029	FREJ(91B)	A
38	$p \rightarrow \mu^- \pi^+ \pi^+$	79.4,0.6,53.6	7.5	54.06	4.702	1.763	0.017	FREJ(91B)	A
39	$n \rightarrow \mu^- \pi^+ \pi^0$	1899.5,192,398,197.6	42.6	74.56	0.897	0.472	0.034	FREJ(91B)	A
40	$p \rightarrow e^- \pi^+ K^+$	32.9,314.8,581.3	19.2	57.54	1.955	0.963	0.075	IMB3(99)	A
41	$p \rightarrow \mu^- \pi^+ K^+$	0.1,89.3,0.5	3.2	63.48	12.942	4.284	0.245	IMB3(99)	A
Antilepton+Photon(s)									
ID	Channels	n_{bkg}	n_{90}	$\epsilon(\%)$	$\tau_{10}(10^{33} \text{ yrs})$	$\tau_3(10^{33} \text{ yrs})$	$\tau_{exp}(10^{33} \text{ yrs})$	TECN	Rank
42	$p \rightarrow e^+ \gamma$	97.8	17.7	75.88	2.8	1.442	0.67	IMB3(99)	A
43	$p \rightarrow \mu^+ \gamma$	100.1	17.9	77.83	2.8366	1.4647	0.478	IMB3(99)	A
44	$n \rightarrow \bar{\nu} \gamma$	1011.0	53.7	86.69	0.827	0.444	0.55	SKAM(15)	C
45	$p \rightarrow e^+ \gamma \gamma$	97.8	17.7	76.04	2.8	1.44	0.1	FREJ(91)	A
46	$n \rightarrow \bar{\nu} \gamma \gamma$	1552.3	66.2	88.83	0.987	0.370	0.219	IMB3(99)	B

A: Its result is much better than the best limit so far, if we get 3 years' events, we can come out on top. In this rank, τ_3 is at least 3 times bigger than τ_{exp} .

B: In this rank, τ_3 is bigger than τ_{exp} . And this channel is worthwhile studying more.

C: We have a better result than before for 10 years' data, but $\tau_3 < \tau_{exp}$.

D: $\tau_{10} < \tau_{exp}$, The disparity between our outcome and theirs is a little big. We can do more but may do in vain.

E: There is a big gap comparing to current limit τ_{exp} , we would better give up it.

OPEN: There is a better method to take event selection or the result is not very reliable.



(4) 寻找其他相关的新物理



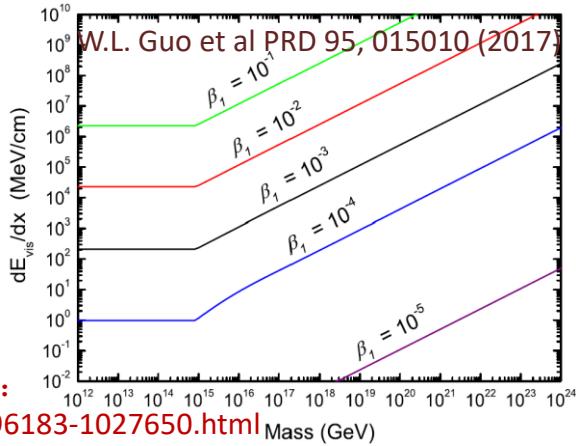
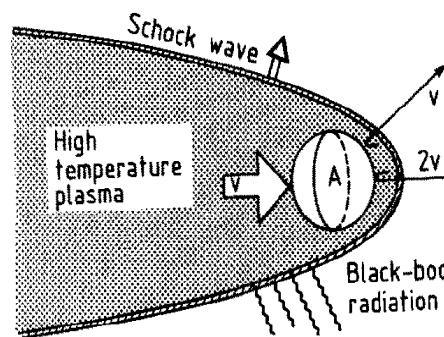
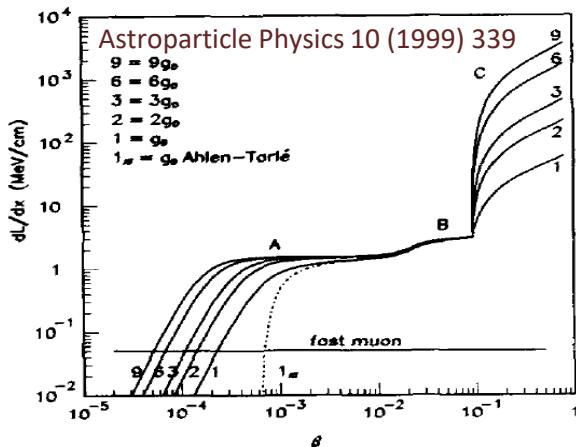
4.1 GUT magnetic monopole



大统一理论预言磁单极子的存在:

- GUT monopoles can be produced in the very early Universe
- Mass: $M_M \sim 10^{16} - 10^{18}$ GeV; Velocity: $\beta \sim 10^{-3}$; Charge: $g = n g_D$

磁单极子穿过JUNO会产生闪烁光: **奇异夸克物质 (SQM) 能产生类似的信号:**



寻找《三体》中的“水滴”杀手:
<https://blog.scientific.net/blog-296183-1027650.html>

Continuous trigger events in a line with the same energy for long time in JUNO LS!!!

- SQM is a hypothetical strongly interacting matter composed of roughly equal numbers of u, d, s quarks and a small amount of electrons; **Absolutely stable**; $\rho_N = 3.6 \times 10^{14} \text{ g/cm}^3$
- $A > 10^7$ **Nuclearites (奇异核素)**, typical $\beta \sim 10^{-3}$ (galaxy velocity)

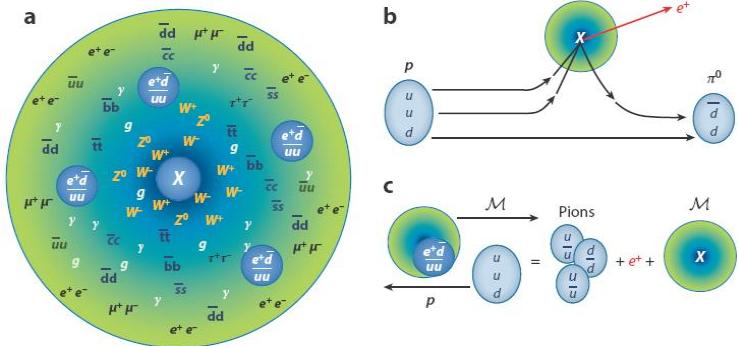


4.2 Proton decays catalyzed by GUT monopoles



大统一理论中预言磁单极子的存在:

- Rubakov-Callen effect, GUT model dependent
- Catalysis σ_R is the order of strong interaction



直接探测磁单极子:

速度~ 10^{-3}

想象一下磁单极子穿过JUNO会产生什么样的信号?

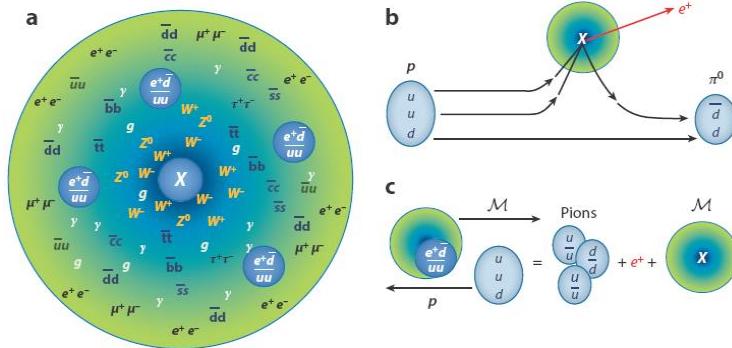


4.2 Proton decays catalyzed by GUT monopoles



大统一理论中预言磁单极子的存在:

- Rubakov-Callen effect, GUT model dependent
- Catalysis σ_R is the order of strong interaction



直接探测磁单极子:



间接探测磁单极子:

宇宙中的磁单极在穿越太阳时会损失能量，进而被捕获并集中在其中心，催化质子衰变
 → 可以有多种末态，只有 ν 可以到达地球!

$$M + p \rightarrow M + \mu^+ + K^0, \quad K^0 + p \rightarrow K^+ + n,$$

$$K^+ \rightarrow \mu^+ + \nu_\mu \text{ (236 MeV)}$$

H.Hu, W.L. Guo et al, JCAP 06 (2022) 003

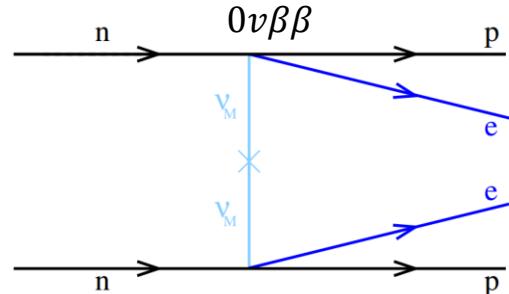
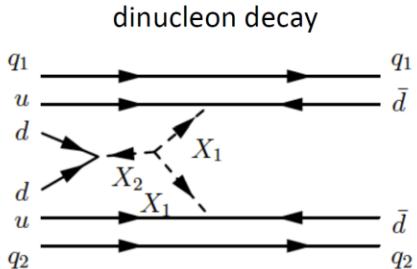
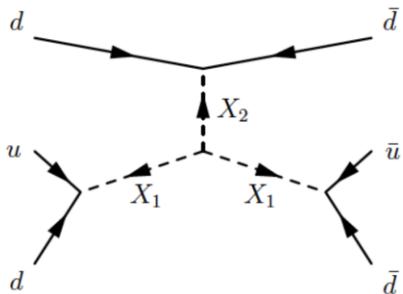
Discrete trigger events in a line with the same energy for long time in JUNO LS!!!



4.3 $n - \bar{n}$ oscillation ($\Delta B = 2, \Delta L = 0$)



nnbar oscillation
(free neutron or inside nucleus)



$$\Delta B = 0, \Delta L = 2$$

$n - \bar{n}$ oscillation searches:

- free neutrons
neutron sources
- bound neutrons
 ν experiments

$\bar{n} + N$ annihilation $\rightarrow \sim 2$ GeV

ID	Channel	ID	Channel
1	$p + \bar{n} \rightarrow \pi^+ + \pi^0$	9	$n + \bar{n} \rightarrow 2\pi^0$
2	$p + \bar{n} \rightarrow \pi^+ + 2\pi^0$	10	$n + \bar{n} \rightarrow \pi^+ + \pi^- + \pi^0$
3	$p + \bar{n} \rightarrow \pi^+ + 3\pi^0$	11	$n + \bar{n} \rightarrow \pi^+ + \pi^- + 2\pi^0$
4	$p + \bar{n} \rightarrow 2\pi^+ + \pi^- + \pi^0$	12	$n + \bar{n} \rightarrow \pi^+ + \pi^- + 3\pi^0$
5	$p + \bar{n} \rightarrow 2\pi^+ + \pi^- + 2\pi^0$	13	$n + \bar{n} \rightarrow 2\pi^+ + 2\pi^-$
6	$p + \bar{n} \rightarrow 2\pi^+ + \pi^- + 2\omega$	14	$n + \bar{n} \rightarrow 2\pi^+ + 2\pi^- + \pi^0$
7	$p + \bar{n} \rightarrow 3\pi^+ + 2\pi^- + \pi^0$	15	$n + \bar{n} \rightarrow \pi^+ + \pi^- + \omega$
8	$n + \bar{n} \rightarrow \pi^+ + \pi^-$	16	$n + \bar{n} \rightarrow 2\pi^+ + 2\pi^- + 2\pi^0$

Signal is similar with two nucleon decay case



总结



- ✓ 寻找核子衰变意义重大：宇宙物质-反物质不对称、检验GUTs
- ✓ 第三代核子衰变实验(JUNO, Hyper-K, DUNE)在几年内将相继运行
- ✓ 未来15年核子衰变的实验限制将得到极大的提升
- ✓ JUNO在一些衰变道是有优势的，值得全面深入研究
- ✓ 3个实验既竞争又互补：不同探测技术、不同靶核(C12,O16,Ar40)



Keep digging new physics !

Thanks for your attention!