# **PULSAR WIND NEBULAE:** HALOES, JETS AND THE PROBLEM OF PARTICLE ESCAPE.

## NICCOLO' BUCCIANTINI INAF ARCETRI - UNIV. FIRENZE - INFN



AF - OSSERVATORIO ASTROFISICO DI ARCETRI

AVVISO / CODICE E TITOLO PROGETTO

**Missione / Componente / Investimento** 

# PWNE



PWNE ARE HOT BUBBLES OF RELATIVISTIC PARTICLES AND MAGNETIC FIELD EMITTING NON-THERMAL RADIATION.

ORIGINATED BY THE INTERACTION OF THE ULTRA-Relativistic magnetised pulsar wind with the Expanding SNR (or with the ISM)

GALACTIC ACCELERATORS. THE ONLY PLACE WHERE WE CAN STUDY THE PROPERTIES OF RELATIVISTIC SHOCKS (AS IN GRBS AND AGNS)

#### NATURAL LEPTONIC PEVATRONS, MOST EFFICIENT ANTIMATTER FACTORIES IN THE UNIVERSE

## **DEATH OF A MASSIVE STAR – THE BIRTH OF PULSAR**

**STARS MORE MASSIVE THAN 8 M<sub>SUN</sub> END THEIR** LIFE IN SUPERNOVA EXPLOSION

STARS LESS MASSIVE THAN 25-30 M<sub>SUN</sub> LEAVE **BEHIND A COMPACT STELLAR REMNANT IN THE** FORM OF A NEUTRON STAR



THE COMBINATION OF STRONG MAGNETIC FIELD (10<sup>12</sup>G) AND RAPID **ROTATION (P=0.001-1S) CREATES STRONG ELECTRIC FIELD AT THE** SURFACE EXTRACTING PAIRS AND PRODUCING PAIR CASCADES. **OBSERVED AS PULSARS** 



## **CRAB SYNCHROTRON SPECTRUM**



The most efficient non-thermal accelerator.

## **IC GAMMA SPECTRUM**



## IC GAMMA SPECTRUM



## FINE STRUCTURES – A LAB FOR RELTIVISTICN FLUID DYNAMICS



## **RELATIVISTIC MHD MODELS**

THE WIND ANISOTROPY SHAPES THE TS STRUCTURE. DOWNSTREAM FLOW – EQUATORIAL COLLIMATION DUE TO THE TS SHAPE: A: ULTRARELATIVISTIC PULSAR WIND B: SUBSONIC EQUATORIAL OUTFLOW C: SUPERSONIC EQUATORIAL FUNNEL D: SUPER-FASTMAGNETOSONIC FLOW A: TERMINATION SHOCK FRONT B: RIM SHOCK C: FASTMAGNETOSONIC SURFACE





# **REPRODUCING OBSERVATIONS**



MAIN TORUS INNER RING (WISPS STRUCTURE) KNOT BACK SIDE OF THE INNER RING

#### **EACH FEATURE TRACES AN EMITTING REGION**



# **REPRODUCING OBSERVATIONS**



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## THE COMPLEXITY OF GOING 3D – STATE OF THE ART COMPUTATIONS



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## **FERMI VS RECONNECTION**

# FERMI DSA HIGHLY INEFFICIENT IN PSR WIND SHOCK – VERY LOW MAGNETISATION



## **SPECTRAL EVOLUTION**



## **SPECTRAL EVOLUTION**





## **CUTOFF ENERGY IS HIGHER AT PEAK**

## **SPECTRAL EVOLUTION**



PSR WINDS ARE STRIPED AND THIS IMPLIES ALTERNATING FIELD POLARITIES IN THE PWN



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## IXPE - X-RAY POLARIMETRY - VELA

Fei et al 2023

	- $2^b$	<b>-1</b> <sup>b</sup>	$0^{b}$	$1^{b}$	$2^{b}$	
na	$37{\pm}18$	$27 \pm 13$	$61{\pm}12$	$37 \pm 13$	$47 \pm 15$	PD <sup>c</sup>
4	$-14{\pm}14$	$-21{\pm}14$	$-41.7 \pm 5.3$	$-52{\pm}10$	$-53.8{\pm}8.9$	$\mathbf{P}\mathbf{A}^d$
$1^{a}$	$33{\pm}10$	$48.5 {\pm} 5.0$	$53.5 \pm 4.1$	$56.8 \pm 7.1$	$47{\pm}13$	PD <sup>c</sup>
-	$6.3 {\pm} 9.0$	$-22.4{\pm}3.0$	$-42.2 \pm 2.2$	$-50.2 \pm 3.6$	$-58.2 \pm 7.7$	$PA^d$
na	$10.3 {\pm} 8.8$	$34.4{\pm}3.9$	$49.0{\pm}2.5$	$62.8{\pm}4.0$	$44{\pm}11$	$PD^{c}$
0	$-7.4{\pm}24$	$-34.3 \pm 3.3$	$-50.3{\pm}1.5$	$-53.9{\pm}1.9$	$-50.5 \pm 7.4$	$\mathbf{P}\mathbf{A}^d$
10	$21{\pm}12$	$27.5 \pm 7.2$	$38.5{\pm}4.0$	$57.1 \pm 5.4$	$44{\pm}12$	$PD^{c}$
$\cdot 1^a$	$-47{\pm}17$	$-68.3 \pm 7.5$	$-70.0{\pm}3.0$	$-69.8{\pm}2.7$	$-57.3 \pm 7.9$	$\mathbf{P}\mathbf{A}^d$
•	$34{\pm}15$	$4.5^{+13}_{-4.5}$	$34.9{\pm}9.5$	$43 \pm 12$	$17 \pm 14$	$PD^{c}$
2"	$-51{\pm}13$	$-6.0\pm 85$	$86.1{\pm}7.8$	$-84.2{\pm}7.6$	$-70{\pm}23$	$\mathbf{P}\mathbf{A}^d$

## Very high PF suggest no turbulence in the PWNe

Unlikely reconnection to play a major role in accelerating particles

Old sytems should be more turbulent.

#### **POTENTIAL LIMITED ACCELERATION**



$$mc^2\gamma_{max} = e\sqrt{\frac{L}{c}} = e\Phi_{psr}$$

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#### **ACCELERATION LIMIT AT THE TS**

# MAGNETISATION IN THE CRAB IS JUST BELOW EQUIPARTITION B $\sim$ 150–120 UG

$$\frac{L}{4\pi c R_{ts}^2} = \frac{1}{2} \frac{3Lt}{4\pi R_n^3}$$
$$\frac{L}{4\pi c R_{ts}^2} = P_{neb} = \frac{1}{\sigma} \frac{B_{ts}^2}{8\pi}$$
$$R_{ts} = \frac{1}{B_{ts}} \sqrt{\frac{\sigma L}{c}}$$

 $\frac{eB_{ts}}{mc^2\gamma_{max}} = R_L = R_{ts}$ 

$$\frac{mc^2\gamma_{max}}{eB_{ts}} = R_L = R_{ts}$$

$$\frac{E_{max}}{eB_{ts}} = e\sqrt{\frac{\sigma L}{c}} = e\Phi_{psr}\sqrt{\sigma}$$

#### LOSS LIMITED ACCELERATION

## COMPARING GYRO-PERIOD WRT SYNCH COOLING TIME

$$\tau_{gyr} = \frac{mc\gamma}{eB} \qquad \tau_{syn} = \frac{3m^3c^5}{2e^4B^2\gamma} \qquad \gamma_{max} \simeq 10^8 \frac{1}{\sqrt{E}}$$

#### LOSS LIMITED ACCELERATION

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#### MAXIMUM FREQUENCY IS FIXED



 $\nu_{syn,max} \simeq 150 MeV$ 

 $\overline{B}$ 

#### LOSS LIMITED ACCELERATION

## **COMPARING GYRO-PERIOD WRT SYNCH COOLING TIME**

$$\tau_{gyr} = \frac{mc\gamma}{eB}$$
  $\tau_{syn} = \frac{3m^3c^5}{2e^4B^2\gamma}$   $\gamma_{max} \simeq 10^7$ 

#### **MAXIMUM FREQUENCY IS FIXED**

 $\nu_{syn,max} \simeq 150 MeV$ 

## IN CRAB THE LIMITS ALL Coincide

**OTHERS ALL POTENTIAL LIMITED** 



## **12 INITIAL SOURCES DETECTED BY LHAASO ABOVE 100 TEV**

#### Table 1 | UHE γ-ray sources

Source name	RA (°)	dec. (°)	Significance above 100 TeV (×o)	E <sub>max</sub> (PeV)	Flux at 100 TeV (CU)
LHAASO J0534+2202	83.55	22.05	17.8	0.88 ± 0.11	1.00(0.14)
LHAASO J1825-1326	276.45	-13.45	16.4	0.42 ± 0.16	3.57(0.52)
LHAASO J1839-0545	279.95	-5.75	7.7	0.21±0.05	0.70(0.18)
LHAASO J1843-0338	280.75	-3.65	8.5	0.26-0.10 <sup>+0.16</sup>	0.73(0.17)
LHAASO J1849-0003	282.35	-0.05	10.4	0.35 ± 0.07	0.74(0.15)
LHAASO J1908+0621	287.05	6.35	17.2	0.44 ± 0.05	1.36(0.18)
LHAASO J1929+1745	292.25	17.75	7.4	0.71-0.07 <sup>+0.16</sup>	0.38(0.09)
LHAASO J1956+2845	299.05	28.75	7.4	0.42 ± 0.03	0.41(0.09)
LHAASO J2018+3651	304.75	36.85	10.4	0.27±0.02	0.50(0.10)
LHAASO J2032+4102	308.05	41.05	10.5	1.42 ± 0.13	0.54(0.10)
LHAASO J2108+5157	317.15	51.95	8.3	$0.43 \pm 0.05$	0.38(0.09)
LHAASO J2226+6057	336.75	60.95	13.6	0.57 ± 0.19	1.05(0.16)

#### 35 OUT 43 >100 TEV SOURCES HAVE A PSR/PWN ASSOCIATED

**PEV PROTONS OR ELECTRONS?** 

## THERE ARE NO-COUNTERPART SOURCES

#### **PSR VOLTAGE**



IN YOUNG ENERGETIC SYSTEMS ACCELERATION IS LIKELY LOSS LIMITED

$$t_{acc} = \frac{E}{e\xi_e Bc} < t_{loss} = \frac{6\pi (mc^2)^2}{\sigma_T c B^2 E}$$

$$E_{max} \approx 6 \ PeV \ \xi_e^{1/2} \ B_{-4}^{-1/2}$$

#### **TIME EVOLUTION I**

#### Kolb et al 2017



Blondin et al 2001

Ma et al 2016

#### **TIME EVOLUTION I**



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#### OLDER SYSTEMS SHOW A DISPLACEMENT OF THE TEV GAMMA EMISSION FROM THE PULSAR: REVERBERATION, BOW-SHOCK



#### **PWNE WILL BE THE MOST NUMEROUS GALACTIC GAMMA-RAY SOURCES**

#### **DISTRIBUTION IN THE GALAXY**



#### **PWN IN THE GALAXY MODELLED WITH NUMERICAL SIMULATIONS + RADIATIVE CODE**

PWN ARE PRIMARY TARGETS FOR CTA AND ASTRI MA

#### **CONTRIBUTION AT GAMMA-RAYS**





## **BOW SHOCK PWNE**

# MOST PULSARS KICK VELOCITY IS SUPERSONIC IN ISM

#### FORWARD SHOCK VISIBLE IN HA PWN VISIBLE AS A RADIO AND X-RAYS TAIL



# PAIR ESCAPE

The are BS PWNe where the X-ray "tail" is where it should not be!

The particles in these features are ~ PSR voltage







Guitar (Wong et al 2003) Cuitar Nebula

# TeV halo suggest strong diffusion

## **BOW-TAILS IN X-RAY**

#### Kargaltsev & Pavlov 2008



#### De Vries et al 2022



Region	Counts	Γ	$f_{-15}{}^{\rm b}$	$\chi^2/{ m DoF}$	$B_{eq}$
					$[\mu G]$
Inner	$214\pm17$	$1.31\pm0.16$	9.9	29.3/27	13
Middle	$209\pm17$	$1.37\pm0.17$	10.2	24.3/24	14
Outer	$489\pm32$	$1.58\pm0.15$	24.1	53.2/48	8
$\operatorname{CF}$	$86\pm11$	$1.71\pm0.30$	3.5	23.8/24	17
Leading	$273\pm19$	$1.39\pm0.14$	13.6	22.7/33	19
Trailing	$154\pm16$	$1.60\pm0.20$	7.1	30.5/30	17
Remnant	$174\pm19$	$1.40\pm0.27$	7.2	38.0/33	9

<sup>a</sup>  $\overline{N_H}$  fixed at  $2.7 \times 10^{21} \text{cm}^{-2}$ . <sup>b</sup> 0.5 - 7 keV unabsorbed fluxes in units of  $10^{-15} \text{erg cm}^{-2} \text{s}^{-1}$ .

#### De Vries et al 2022



# 2021 2012

#### **NO EVIDENCE OF COOLING IN THE INNER REGION**

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#### **22 YEARS OF GUITAR**



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MUCH STEEPER SPECTRUM IN THE COUNTER JET

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## **BOW SHOCK PWNE: THEORY VS REALITY**





## **BOW SHOCK PWNE: INTERNAL TURBULENCE**

## **Isotropic Wind**

## Anisotropic Wind



## **BOW SHOCK PWNE: INTERNAL TURBULENCE**

## Isotropic Wind

## Anisotropic Wind







Olmi & Bucciantini 2019

ESCAPE ASSOCIATED TO RECONNECTION SITES AT THE MAGNETOPAUSE

> STRONG ENERGY DEPENDENCE

#### TURBULENCE IN THE TAIL DEPENDENT ON INTERACTION GEOMETRY



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#### **BOW-SHOCK E**<sub>MAX</sub> $\sim$ 0.1 PSR VOLTAGE



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#### ESCAPE FROM THE HEAD 0.1 – 1.0 E<sub>max</sub>

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#### **CURRENT CANONICAL PICTURE WELL ESTABLISHED**

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**PWNE WILL BE MAIN SOURCE OF GAMMA RAY SKY** 

LIKELY TO DOMINATE THE PEVATRONS

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**NO CLEAR IDENTIFICATION FOR THE ACCELERATION MECHANISM** 

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JET FEATURES DEPEND ON BOW SHOCK HEAD CONDITIONS

NON UNIFORM BOW SHOCK TAIL DYNAMICS