

The status of fine-tuning arguments in the CEPC era



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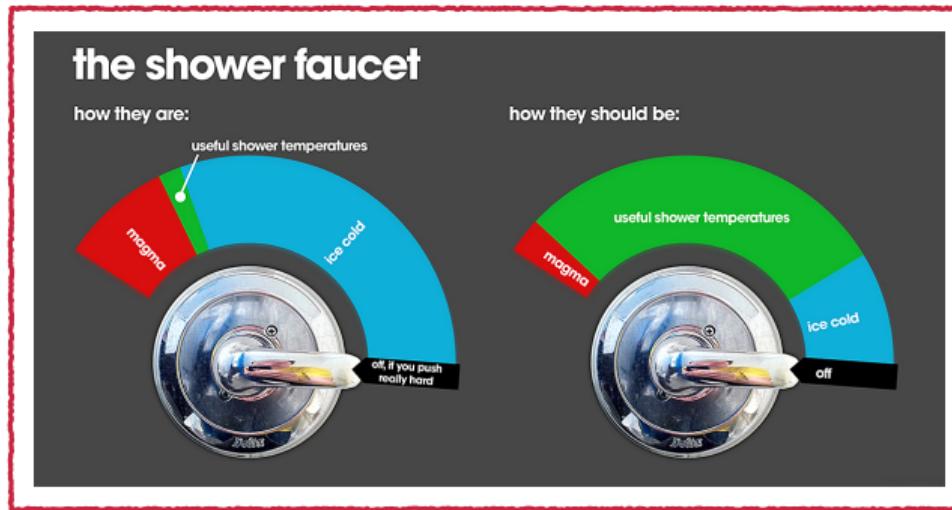
CEPC New Physics Workshop

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Partially based on work with Gonzalo Herrera [2406.03533]

Background

Fine-tuning in everyday life



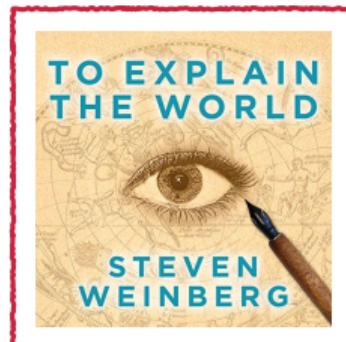
We know that showers that require **fine-tuning** are bad showers!

Background

Fine-tuning in physics

In high-energy physics, a theory is considered **fine-tuned or unnatural** if small variations in its parameters result in dramatic changes in its predictions. For reviews, see ref. [1–3]

Fine-tuning in a scientific theory is like a cry of distress from nature, complaining that something needs to be better explained

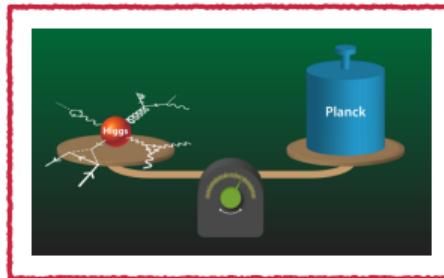


Background

Hierarchy problem

Higgs mass parameter must be **fine-tuned**. This is the hierarchy problem [4–8]

$$m^2 \simeq m_0^2 + M_{\text{UV}}^2$$



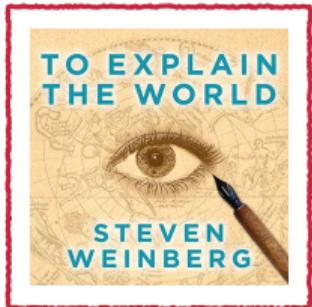
Require **fine-tuning** of bare mass and loop correction $\sim M_{\text{UV}}^2$ such that $m^2 \lll M_{\text{UV}}^2$

Decades searching for solutions — e.g. supersymmetry [9–11], large extra dimensions [12] and technicolor [4] — that canceled UV corrections or eliminated any UV scales

Background

Cosmological constant

Cosmological constant requires **fine-tuning** — $\rho \lesssim 10^{-121}$ but corrections from known physics are at least 60 orders of magnitude greater [13]

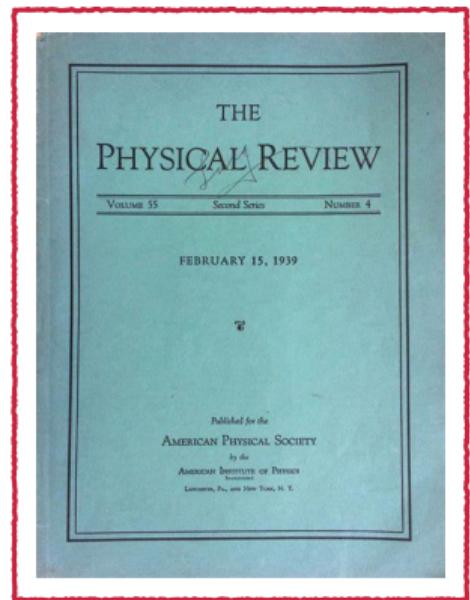


This level of fine-tuning is intolerable, and theorists have been working hard to find a better way to explain why the amount of dark energy is so much smaller than that suggested by our calculations

Background

History of fine-tuning

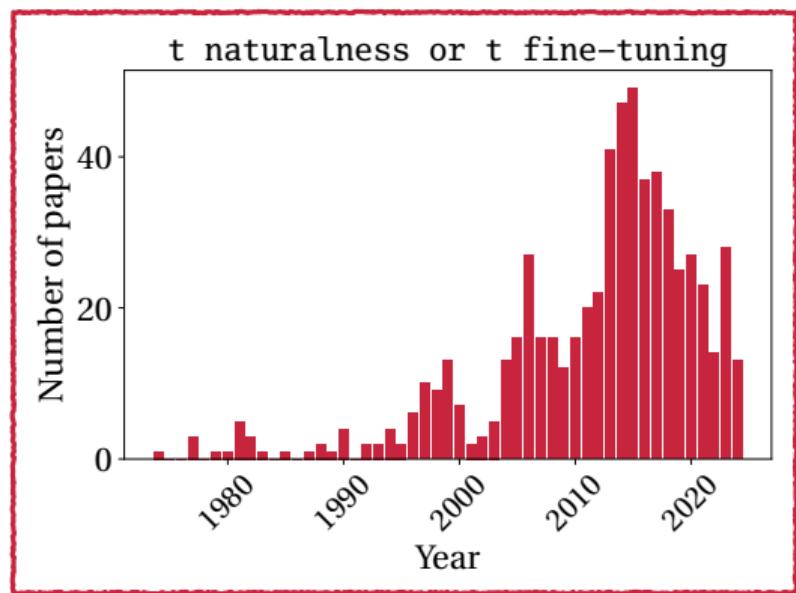
- ▶ **1934** — Weisskopf's calculation of electron self-energy [14]
- ▶ **1938** — Dirac's large numbers hypothesis [15]
- ▶ **1973** — Wilson understanding of effective field theory [16]
- ▶ **1974** — Gaillard and Lee predict charm quark mass [17]
- ▶ **1988** — Weinberg makes anthropic argument [18]



Background

Popularity of fine-tuning — data from INSPIRE

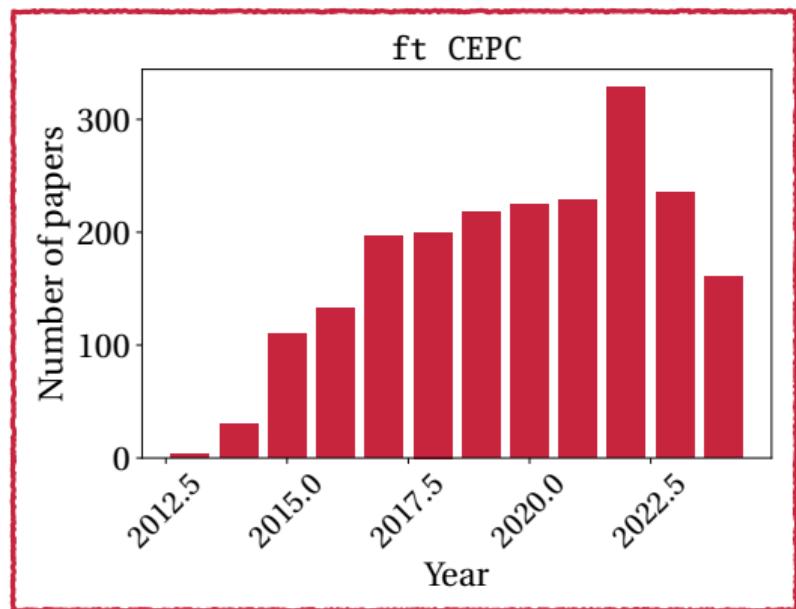
- ▶ **1974** — first hit by Georgi [19]
- ▶ **1979** — 't Hooft [20]
- ▶ **1987** — Barbieri-Giudice measure [21]
- ▶ **2000** — fine-tuning at LEP [22]
- ▶ **2006** — pre-LHC forecasts
- ▶ **2010 onward** — LHC-era



Background

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Background

Measures of fine-tuning

Fine-tuning of electroweak scale usually quantified by sensitivity measure [21, 23],
e.g. Barbieri-Giudice (BG)

$$\Delta_{\text{BG}} = \left| \frac{d \ln M_Z}{d \ln a_i} \right| = \left| \frac{a_i}{M_Z} \frac{d M_Z}{d a_i} \right|$$

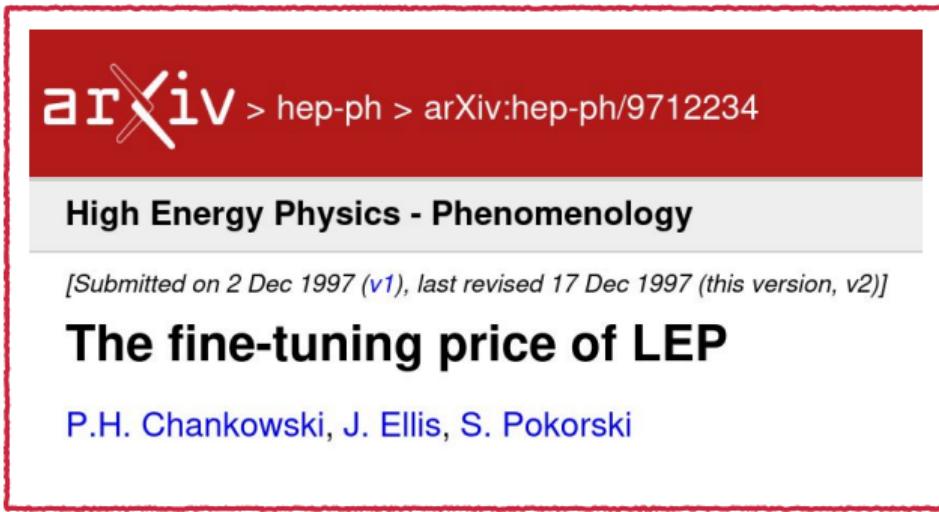
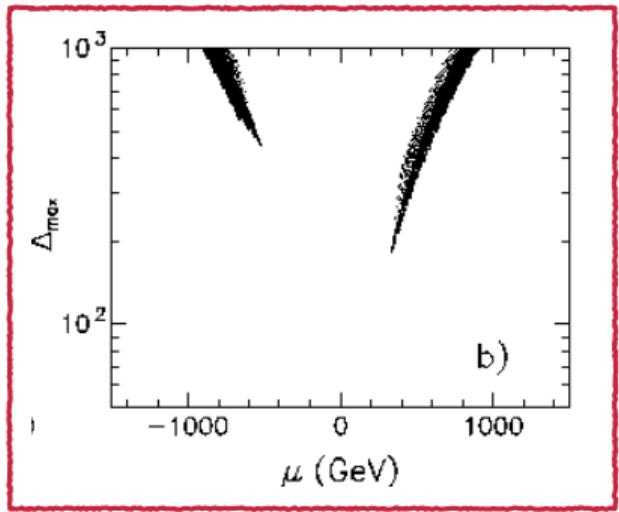
We could combine them by maximizing across parameters or summing in quadrature.

Why though? What's the connection between these measures and plausible models?

Background

Fine-tuning at LEP

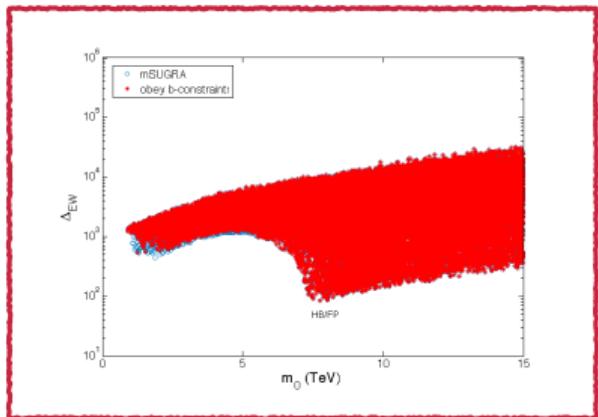
Fine-tuning price of LEP [22, 24–26] — allowed points show $\Delta_{\text{BG}} \gtrsim 100$



Background

Fine-tuning at the LHC

Fine-tuning price of the LHC [27, 28] — allowed points show $\Delta_{\text{BG}} \gtrsim 1000$, except in focus-point region



There are, thus, now criticisms and doubts about fine-tuning [29]

Recent developments

Statistical interpretation

Fine-tuning connected to probability of cancellations [30–35] and statistical inference [36–47]

Plausibility is updated by data via Bayes' theorem

$$p(A | B) = \frac{p(B | A)}{p(B)} \cdot p(A)$$



Contrasts with frequentist probability — frequency with which repeatable event occur in repeat trials [48]

Recent developments

Bayes factor

We want to find which model is most plausible in light of data. The relative plausibility is called the posterior odds [49, 50]

$$\frac{p(M_b | D)}{p(M_a | D)} = \frac{p(D | M_b)}{p(D | M_a)} \times \frac{p(M_b)}{p(M_a)}$$

Posterior odds = Bayes factor \times Prior odds

The Bayes factor updates the prior odds to the posterior odds. This requires more than one model

Recent developments

Bayes factor surface [56]

The Bayes factor surface shows the change in plausibility of a model as a function of that model's parameters relative to a reference model

$$B(\theta) = \frac{p(D | M, \theta)}{p(D | M_0)}$$

This is a new way to understand the impact of experimental measurements; see ref. [51–55] for recent related works in other contexts

Recent developments

Information theory

The Kullback-Leibler (KL) divergence between the prior and the posterior [57]

$$D_{\text{KL}} \equiv \int p(\phi | M_Z) \ln \left[\frac{p(\phi | M_Z)}{\pi(\phi)} \right] d\phi$$

This is a measure of the **extra information required about a parameter to fit the Z mass** [58]

Recent developments

Equivalence [59]

- ▶ Model of new physics with parameters θ , e.g. SUSY
- ▶ **Exchange one model parameter for the Z mass**, e.g. μ -parameter
- ▶ Reference model with M_Z as an input parameter

We found a link between the BG measure, statistics, and information theory

$$B(\theta) = e^{\Delta D_{\text{KL}}} = \Delta_{\text{BG}}$$

Bayes factor surface = Relative information = BG measure

... for the parameter that was exchanged for the Z mass

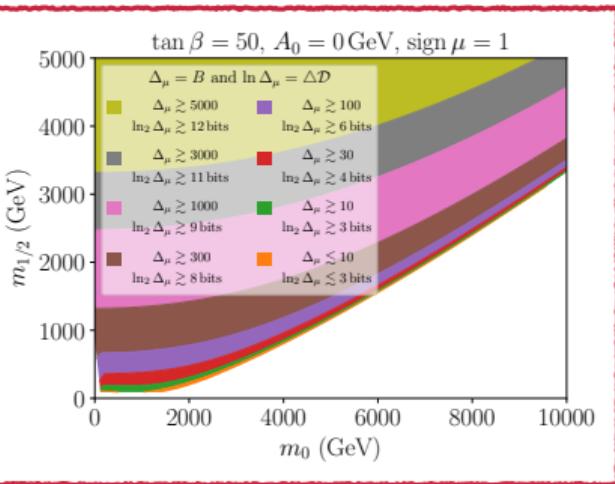
Recent developments

Interpretations of BG measure

- ▶ **Statistical** — the BG measure shows the Bayes factor surface versus an untuned model — *measures the change in plausibility of a model relative to an untuned model in light of the Z mass measurement*
- ▶ **Information-theoretic** — the BG measure shows the compression versus an untuned model — *measures the exponential of the extra information, measured in nats, relative to an untuned model that you must supply about a parameter in order to fit the Z mass*

Example

CMSSM/mSUGRA



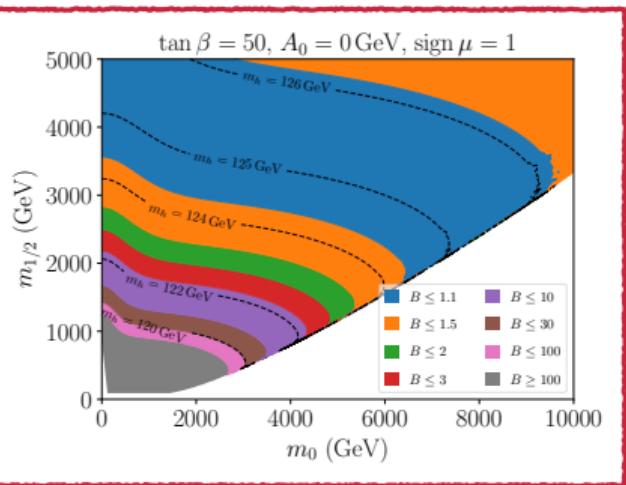
The traditional BG measure is equivalent to

- ▶ Bayes factor surface relative to untuned model
 - *CMSSM points disfavored by more than factor 300*
- ▶ Extra information that must be specified about a parameter — *at least 6 extra bits of information required about the μ -parameter*

... everywhere except in the narrow focus point strip where $\Delta_{BG} \leq 10$

Example

CMSSM/mSUGRA



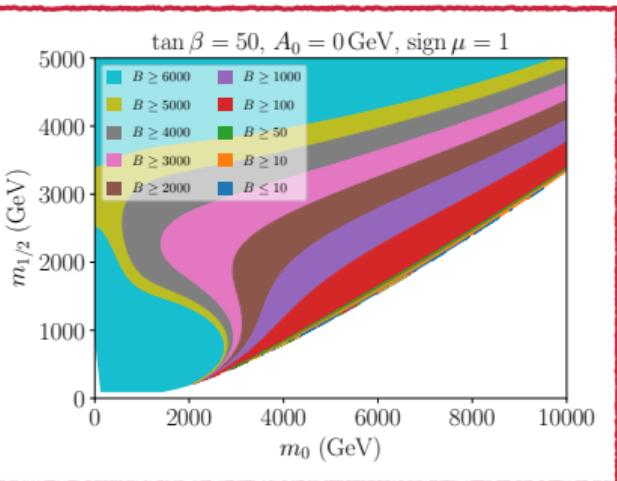
The Bayes factor surface for the $m_h \simeq 125 \text{ GeV}$ Higgs mass measurement

- ▶ Computed relative to a reference model — *model that predicts $m_h = 125 \text{ GeV}$ with no tuning*
- ▶ Requires $m_0 \gg \text{TeV}$ and $m_{1/2} \gg \text{TeV}$ — *except in narrow focus-point*

How can we combine the Higgs mass measurement with the BG measure?

Example

CMSSM/mSUGRA



Bayes factor surfaces from Z and Higgs mass measurements can be multiplied

- ▶ The Z and Higgs mass measurements select narrow focus-point strip — *disfavoured, but only by $B \leq 10$*
- ▶ ... and rule out other choices — *disfavored by at least $B > 100$*

The BG measure should not be thought of as a χ^2 , but as a Bayes factor

Relevance

Today & at the LHC

Predictions from naturalness continue to guide searches for new physics

- ▶ Searches for light stops e.g. [60, 61]
- ▶ Searches for light higgsino-like neutralinos and charginos & compressed spectra e.g. [62–64]

Novel strategies for hidden naturalness

- ▶ Compressed spectra
- ▶ R -parity violation
- ▶ Blind spots & secluded sectors

Relevance

CEPC era



- ▶ Fine-tuning a major motivation for CEPC and SppS in CDR [65]
- ▶ Neutral naturalness probed through ZZh precision — *reach 3 TeV in twin Higgs and 1 TeV in folded SUSY models* [65]
- ▶ Exploration of **higgsino world** at CEPC [66] — *possible through ee → WW to exclude $\mu \lesssim 210$ GeV at $\sqrt{s} = 240$ GeV*
- ▶ Higgsino or bino-like direct production [67] — *reach limit $\sqrt{s}/2$*
- ▶ Indirect constraints from precision Higgs in combination with other limits [68, 69]

Conclusions

- ▶ Doubts raised about fine-tuning — arbitrariness, lack of logical foundation & negative results from LEP and LHC
- ▶ There are, however, precise interpretations of the fine-tuning measure

- **Statistical** — *measures the change in plausibility of a model relative to an untuned model in light of the Z mass measurement*
- **Information-theoretic** — *measures the extra information that you must supply about a parameter in order to fit the Z mass*

- ▶ Fine-tuning thus a legitimate guide for new physics
- ▶ Motivating search strategies at the LHC and **should play role at CEPC**

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