

# Dark Matter and New Physics at Neutrino Experiments

**Ningqiang Song**

**宋宁强**

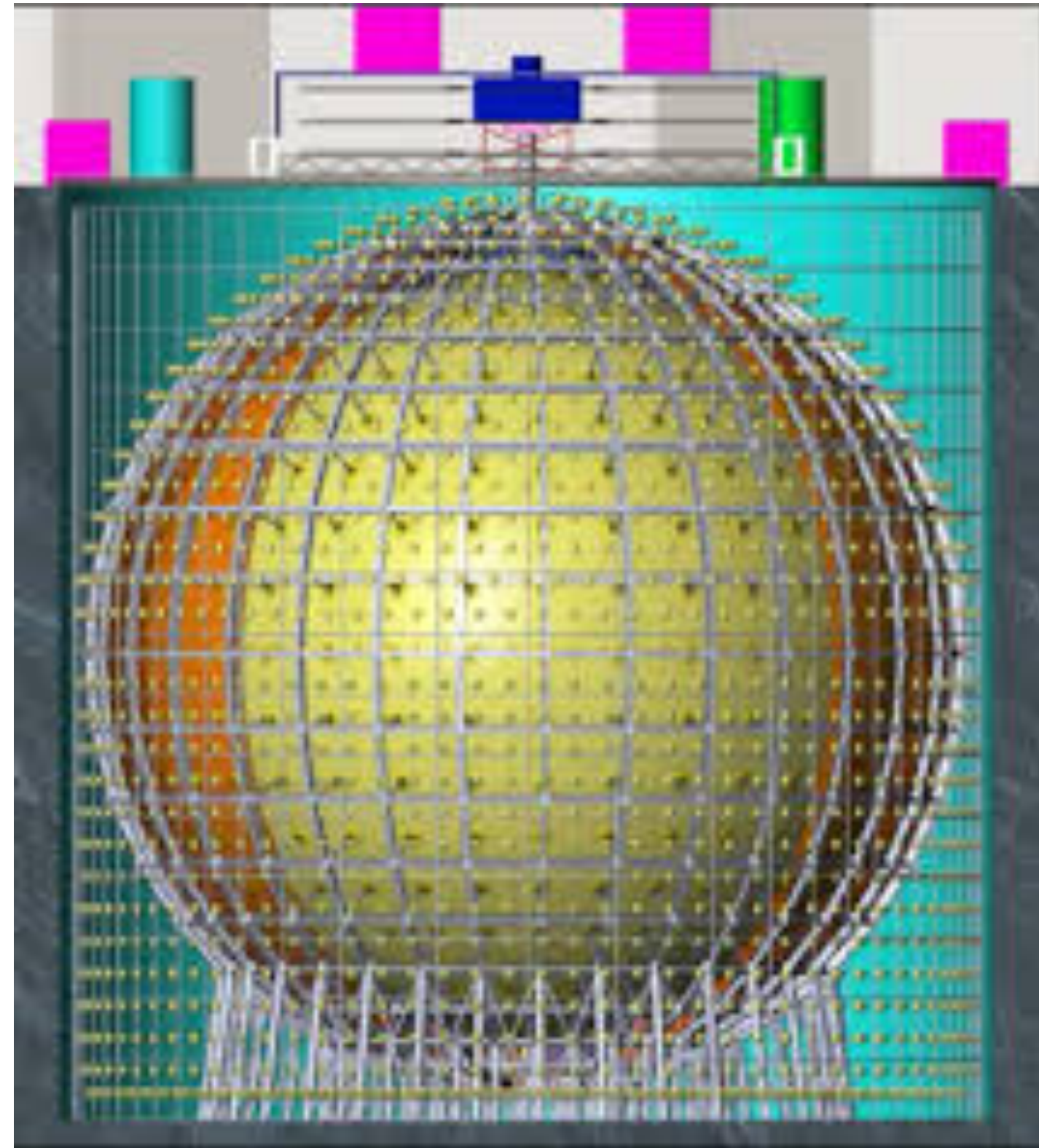
**Institute of Theoretical Physics, Chinese Academy of Sciences**

**November 3, 2024**



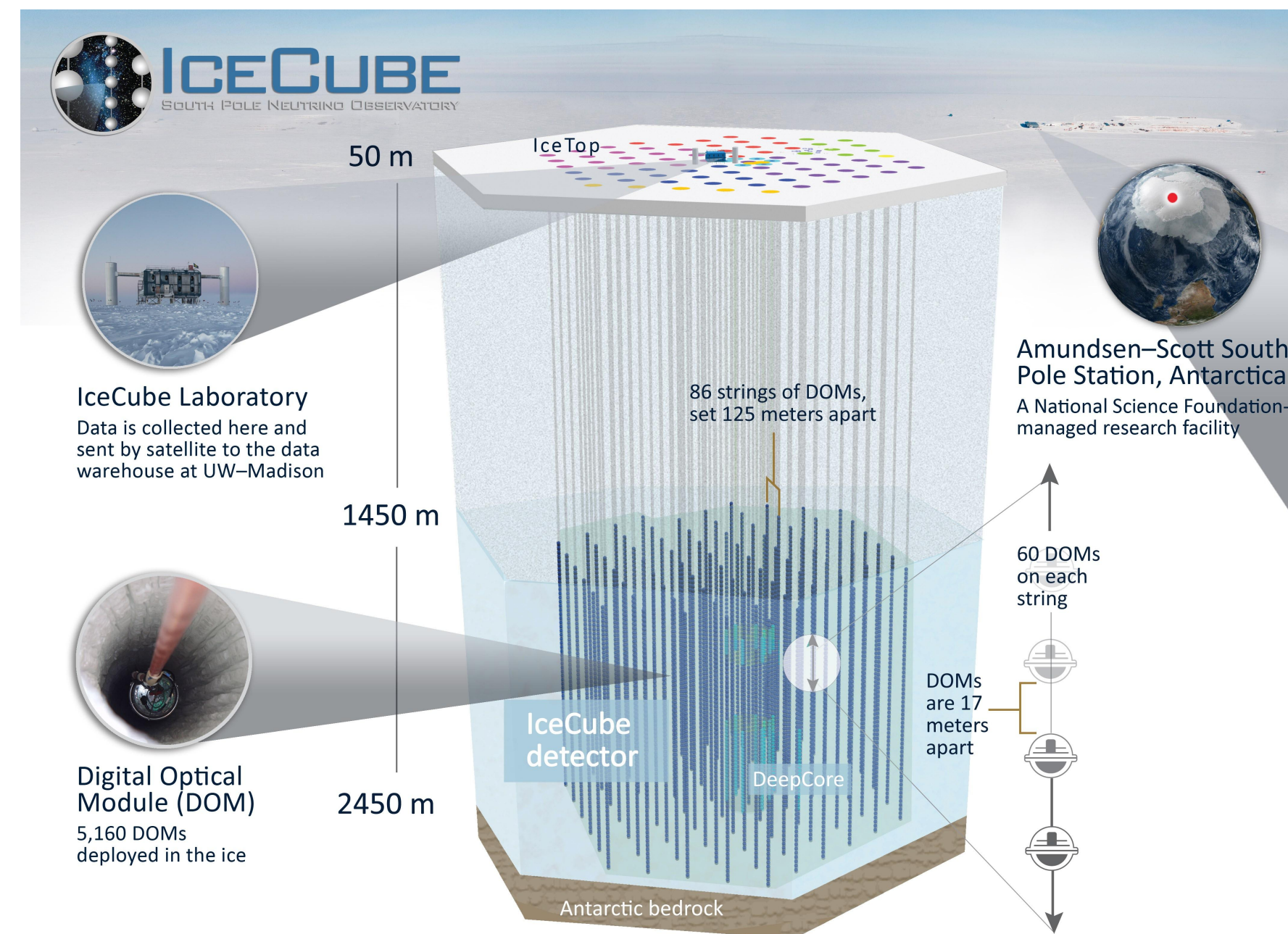
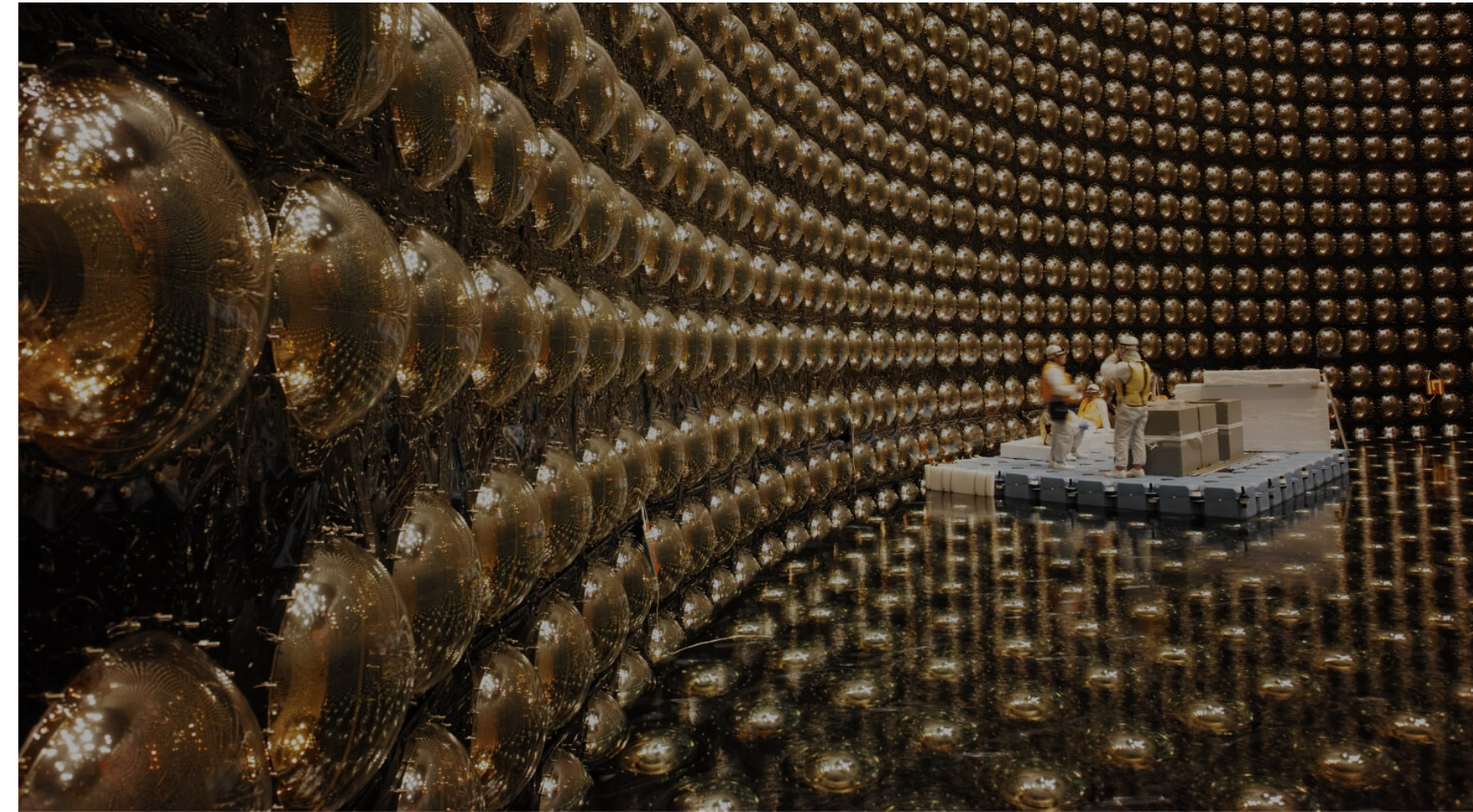


# Neutrino Experiments



JUNO

- Large exposure
- Different thresholds

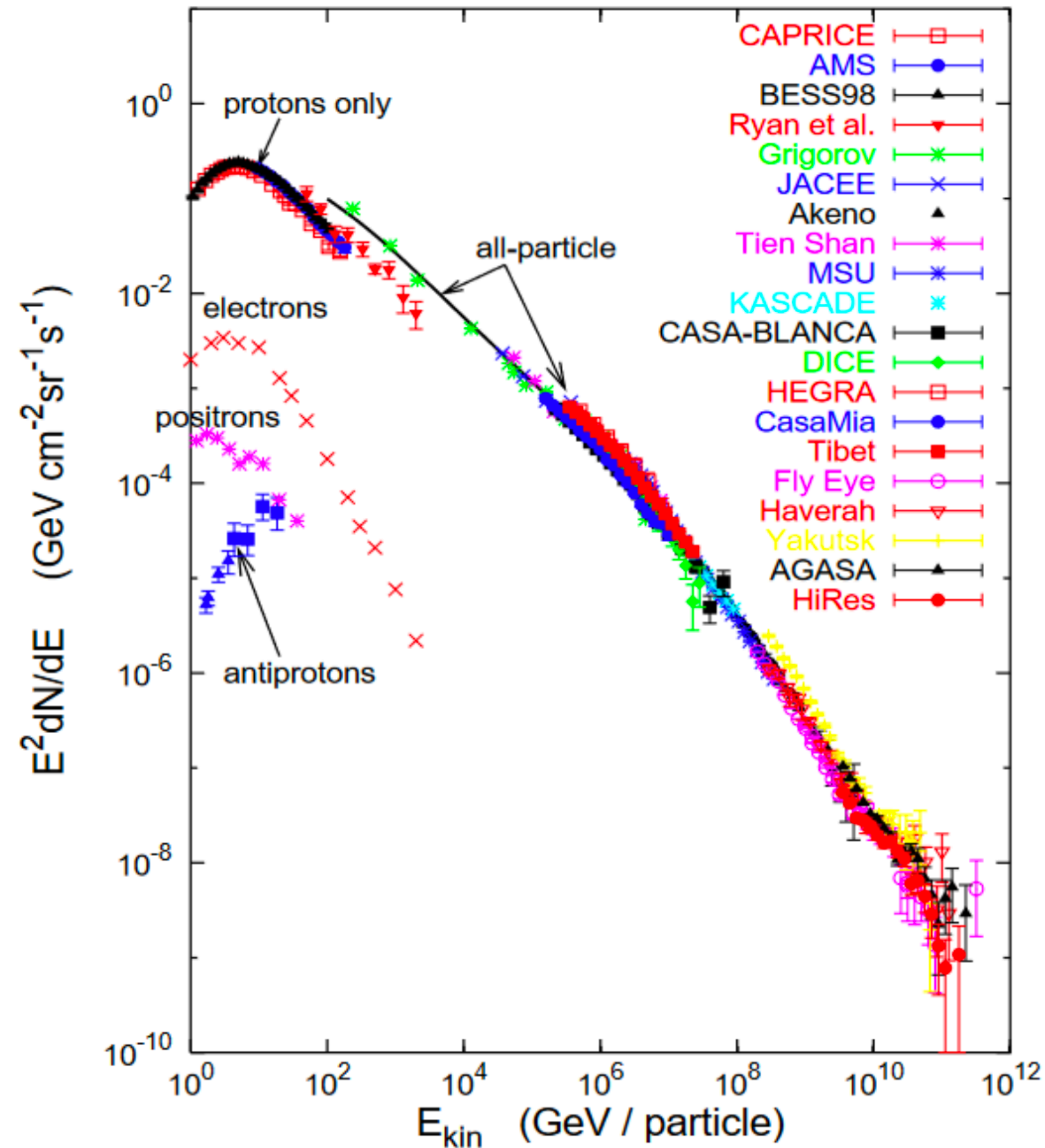


IceCube

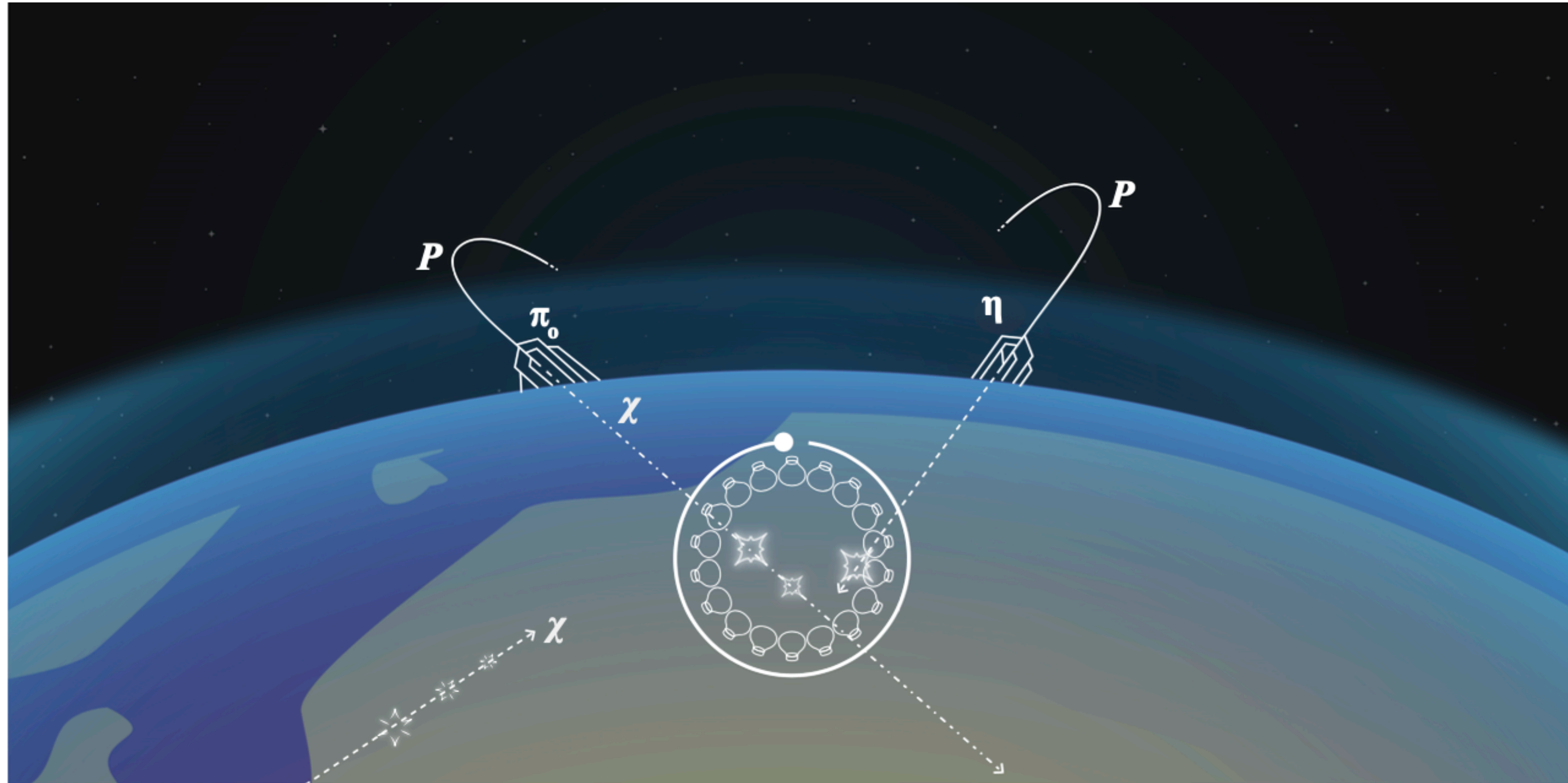


# Atmospheric beam dump and new physics

- Heavy neutral leptons
- Hadrophilic dark matter
- Axion-like particles
- Long-lived neutralinos
- Monopoles
- Dark photon
- Millicharged particles
- ...



# Atmospheric Beam Dump



# Dark Photon Kinetic Mixing

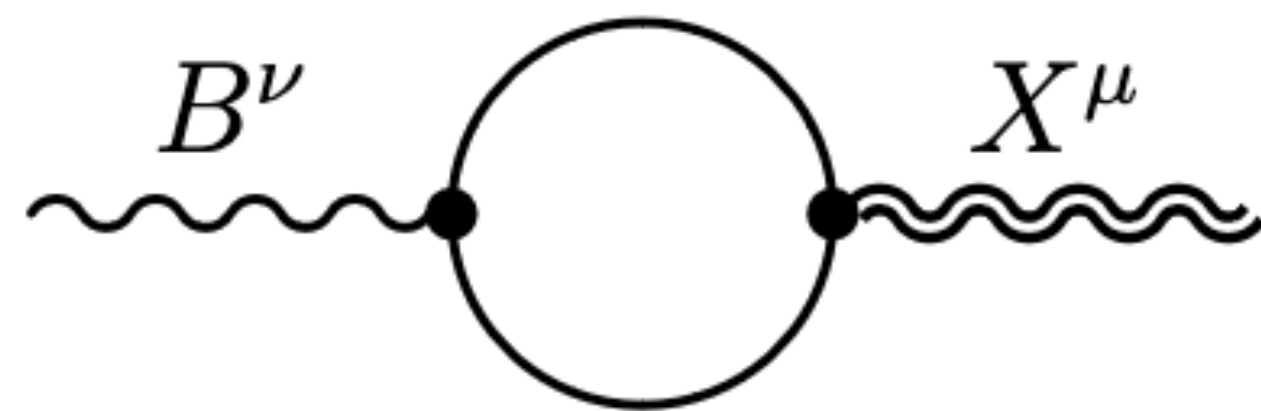
Extra  $U(1)$ ?  $SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)'$

Pospelov' 2008

Ackerman, Buckley, Carrol, Kamionkowski' 2008

Arkani-Hame, Finkbeine, Slatyer, Weiner' 2008

$$\mathcal{L} = -\frac{1}{4}(F_{\mu\nu}F^{\mu\nu} - 2\kappa F_{\mu\nu}F'^{\mu\nu} + F'_{\mu\nu}F'^{\mu\nu}) + \frac{m_{A'}^2}{2}A'_\mu A'^\mu - J^\mu A_\mu$$



$$\epsilon = -\frac{g'g_X}{16\pi^2} \sum_i Y_i q_i \ln \frac{M_i^2}{\mu^2} \sim 10^{-1} - 10^{-3}$$



# Millicharge Particles

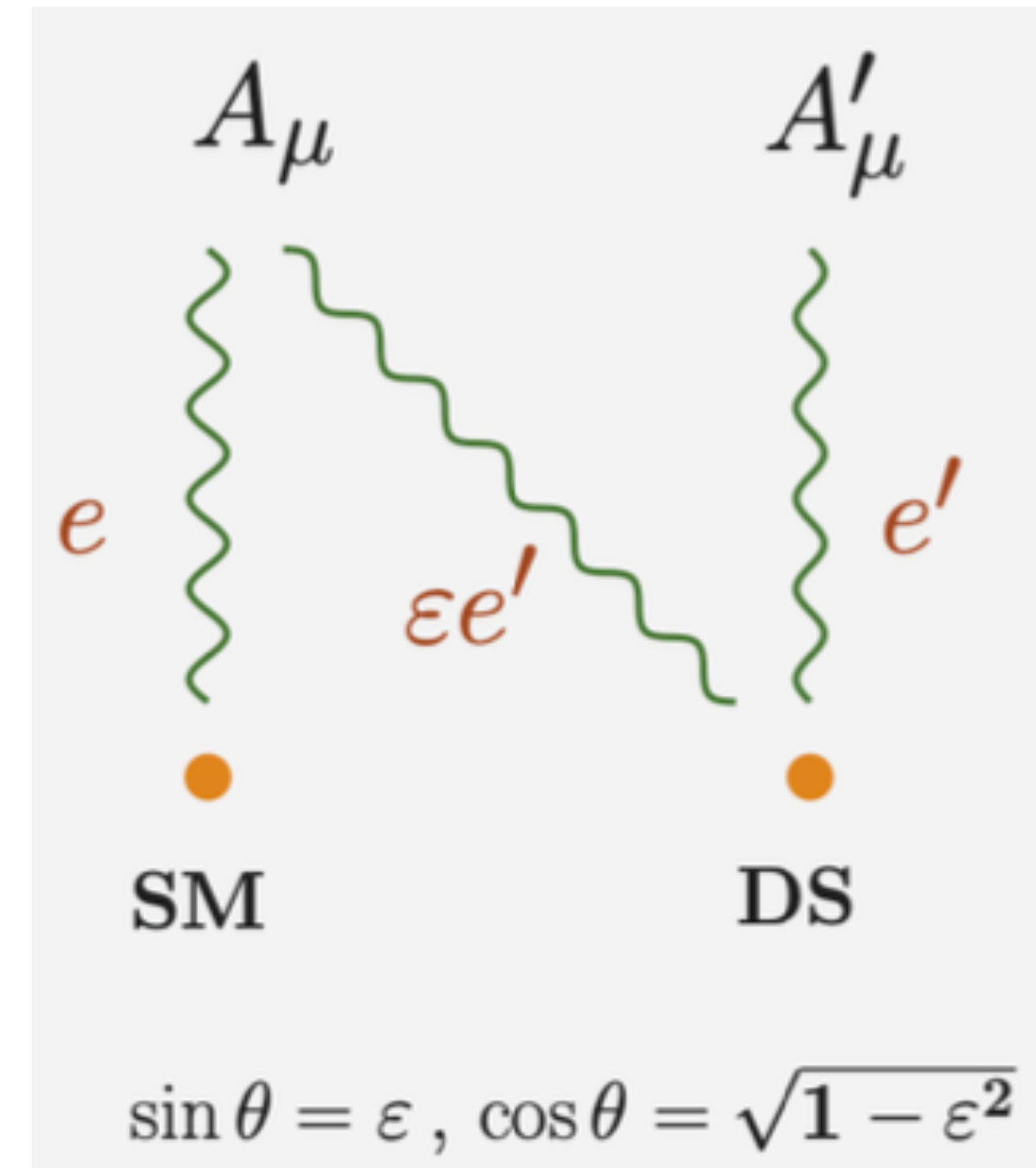
Massless dark photon  $\mathcal{L}_0 = -\frac{1}{4}F_{a\mu\nu}F_a^{\mu\nu} - \frac{1}{4}F_{b\mu\nu}F_b^{\mu\nu} - \frac{\varepsilon}{2}F_{a\mu\nu}F_b^{\mu\nu}$

$$\mathcal{L} = e J_\mu A_b^\mu + e' J'_\mu A_a^\mu$$

$$\begin{pmatrix} A_a^\mu \\ A_b^\mu \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{1-\varepsilon^2}} & 0 \\ -\frac{\varepsilon}{\sqrt{1-\varepsilon^2}} & 1 \end{pmatrix} \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} A'^\mu \\ A^\mu \end{pmatrix}$$

$$\begin{aligned} \mathcal{L}' &= \left[ \frac{e' \cos\theta}{\sqrt{1-\varepsilon^2}} J'_\mu + e \left( \sin\theta - \frac{\varepsilon \cos\theta}{\sqrt{1-\varepsilon^2}} \right) J_\mu \right] A'^\mu \\ &+ \left[ -\frac{e' \sin\theta}{\sqrt{1-\varepsilon^2}} J'_\mu + e \left( \cos\theta + \frac{\varepsilon \sin\theta}{\sqrt{1-\varepsilon^2}} \right) J_\mu \right] A^\mu \end{aligned}$$

$$\mathcal{L}' = e' J'_\mu A'^\mu + \left[ -\frac{e'\varepsilon}{\sqrt{1-\varepsilon^2}} J'_\mu + \frac{e}{\sqrt{1-\varepsilon^2}} J_\mu \right] A^\mu$$

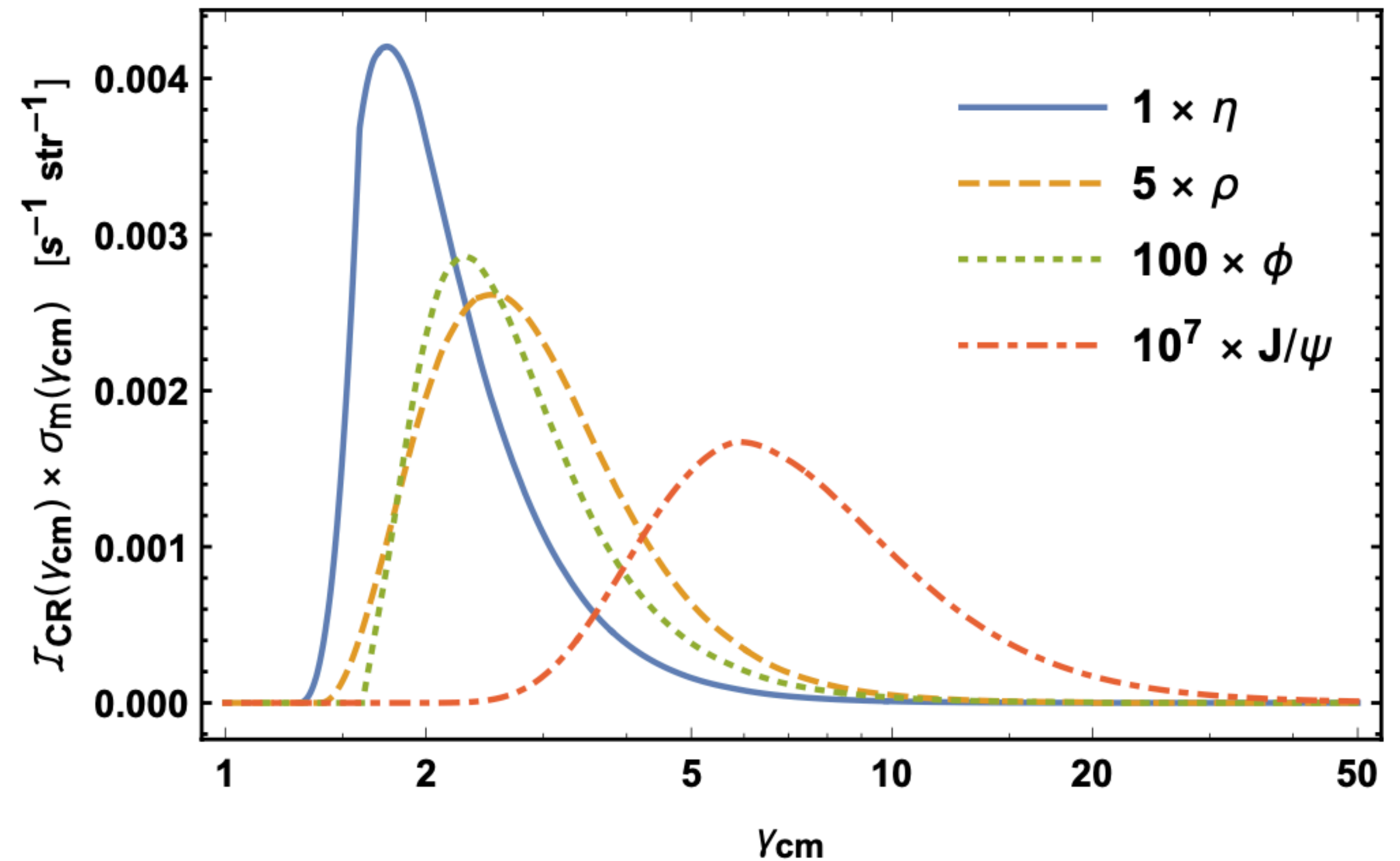
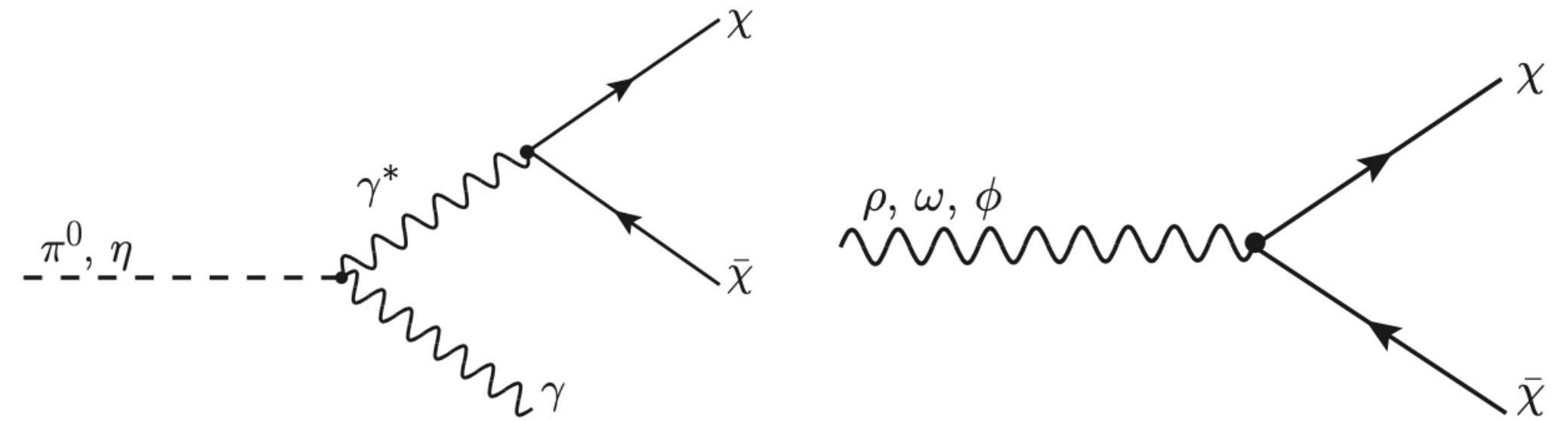


# Millicharge Particles from Light Meson Decay

$$\Phi_m(\gamma_m) = \Omega_{\text{eff}} \int \mathcal{I}_{\text{CR}}(\gamma_{\text{cm}}) \frac{\sigma_m(\gamma_{\text{cm}})}{\sigma_{\text{in}}(\gamma_{\text{cm}})} P(\gamma_m | \gamma_{\text{cm}}) d\gamma_{\text{cm}}$$

$$\gamma_{\text{cm}} = \frac{1}{2} \sqrt{s/m_p}$$

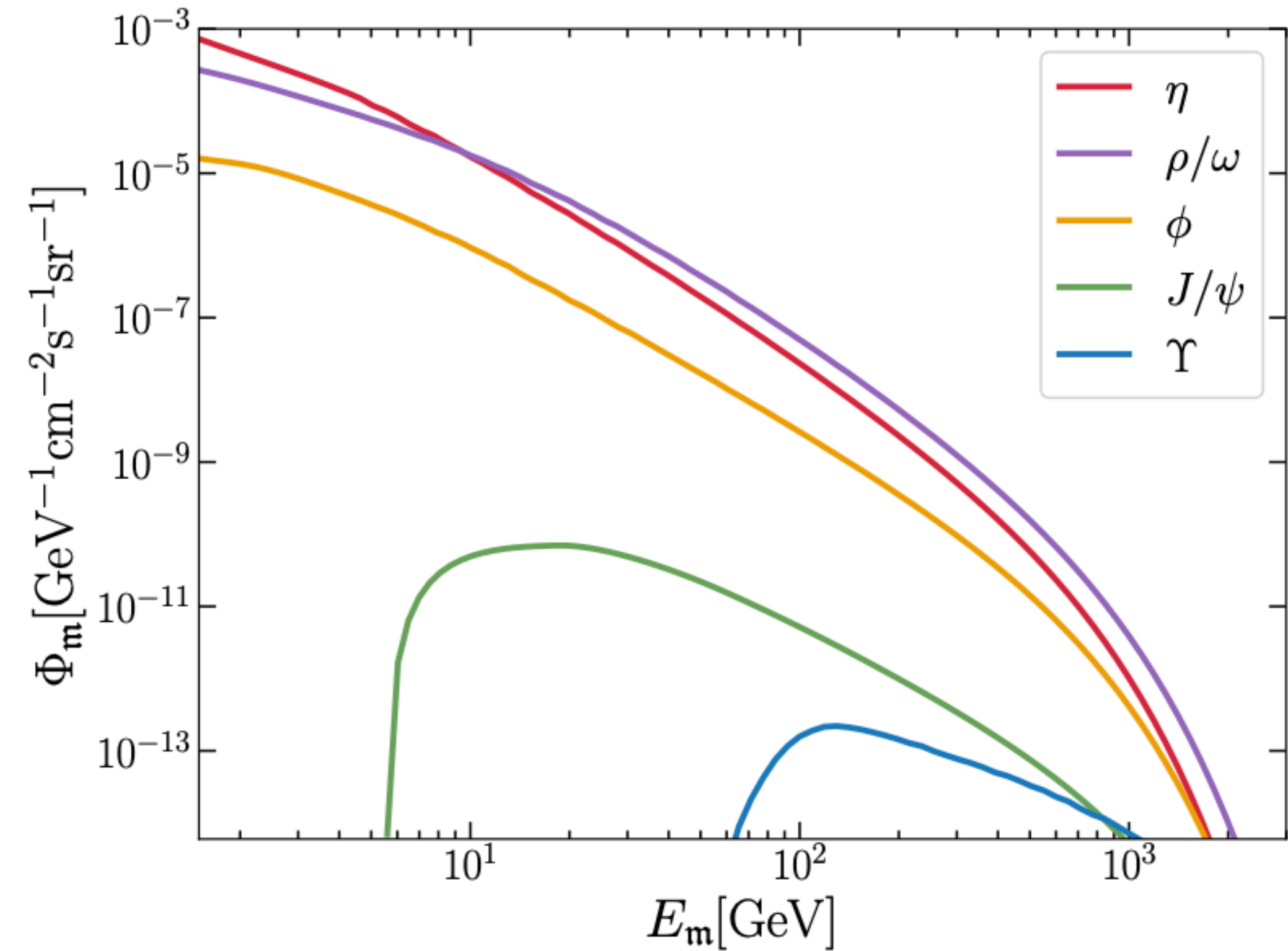
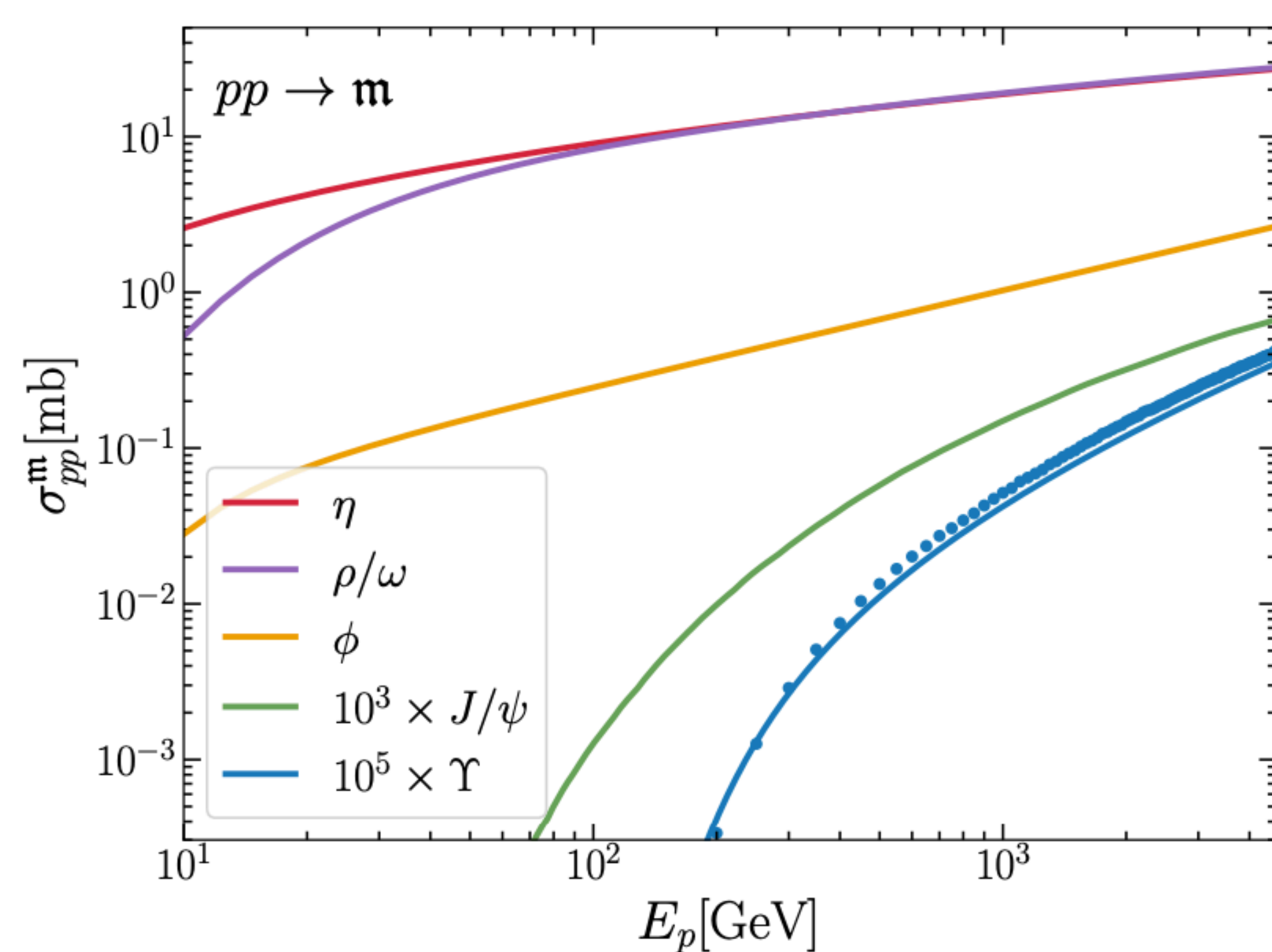
$$P(\gamma_m | \gamma_{\text{cm}}) \approx \sum_{\alpha} \frac{1}{\sigma_m} \times \frac{d\sigma_m}{dx_F} \times \frac{dx_F^{(\alpha)}}{d\gamma_m}$$



Plestid et al PRD/2002.11732

# Millicharge Particles from Upsilon Meson Decay

Pythia8 simulations



Wu, Hardy, **NS**, arXiv: 2406.01668



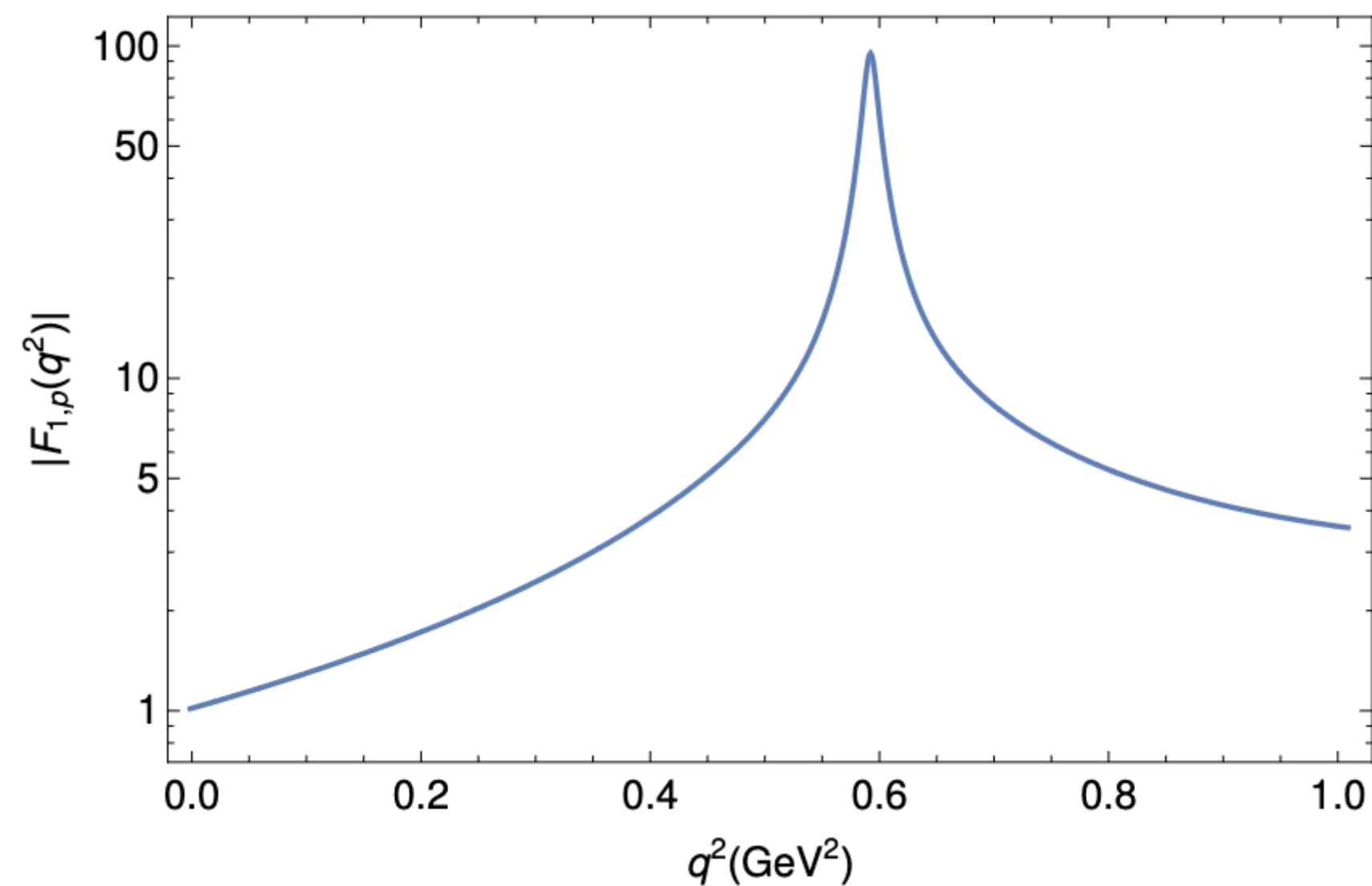
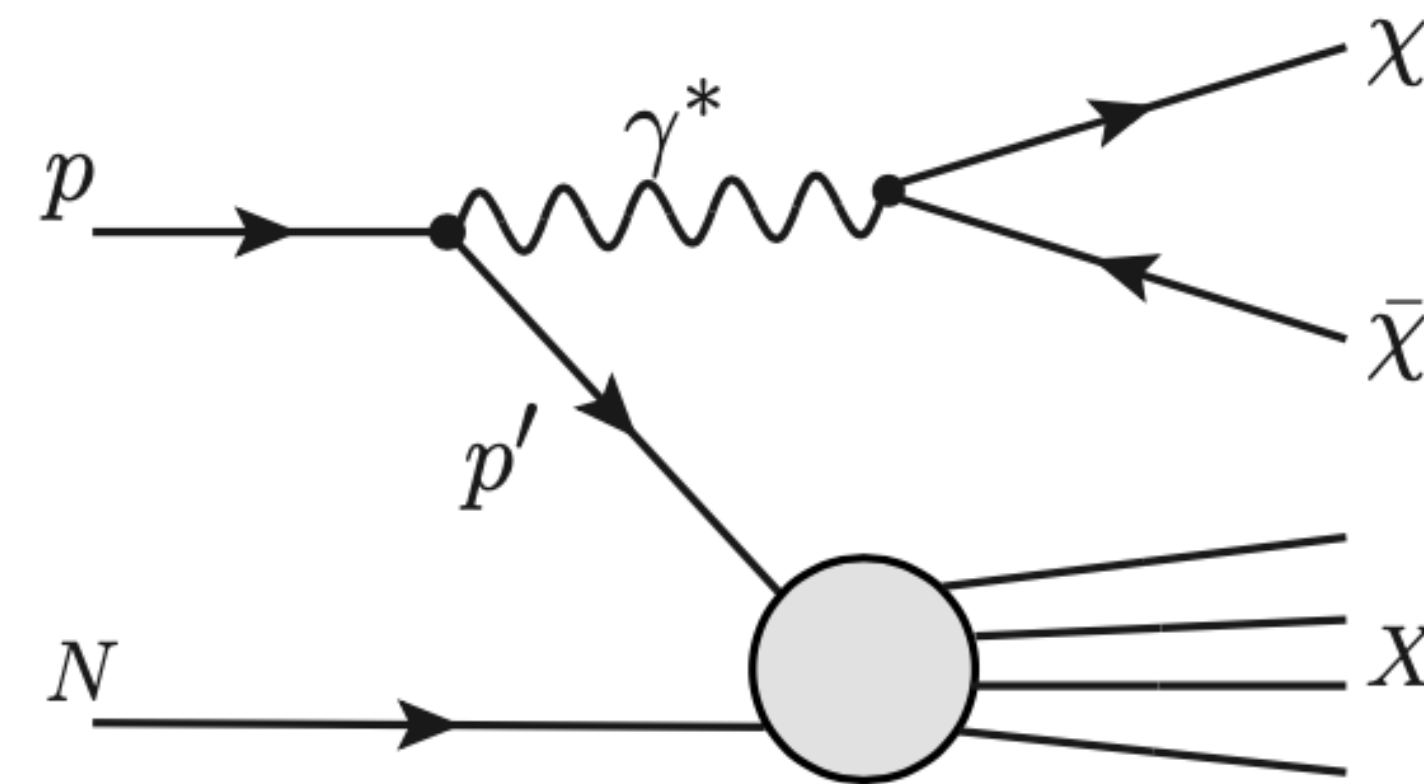
# Millicharge Particles from Proton Bremsstrahlung

Fermi-Weizsacker-Williams (FWW) approximation with the splitting-kernel approach

$$d\sigma^{\text{PB}}(s) \simeq d\mathcal{P}_{p \rightarrow \gamma^* p'} \times \sigma_{pN}(s')$$

$$\frac{d^2 \mathcal{P}_{p \rightarrow \gamma^* p}^{\text{FWW}}}{dE_k d \cos \theta_k} = |\mathbf{J}(z, p_T^2)| \frac{d^2 \mathcal{P}_{p \rightarrow \gamma^* p}^{\text{FWW}}}{dz dp_T^2} = |\mathbf{J}(z, p_T^2)| |F_V(k)|^2 \omega(z, p_T^2)$$

EM form factor Kernel



deNiverville et al PRD/1609.01770

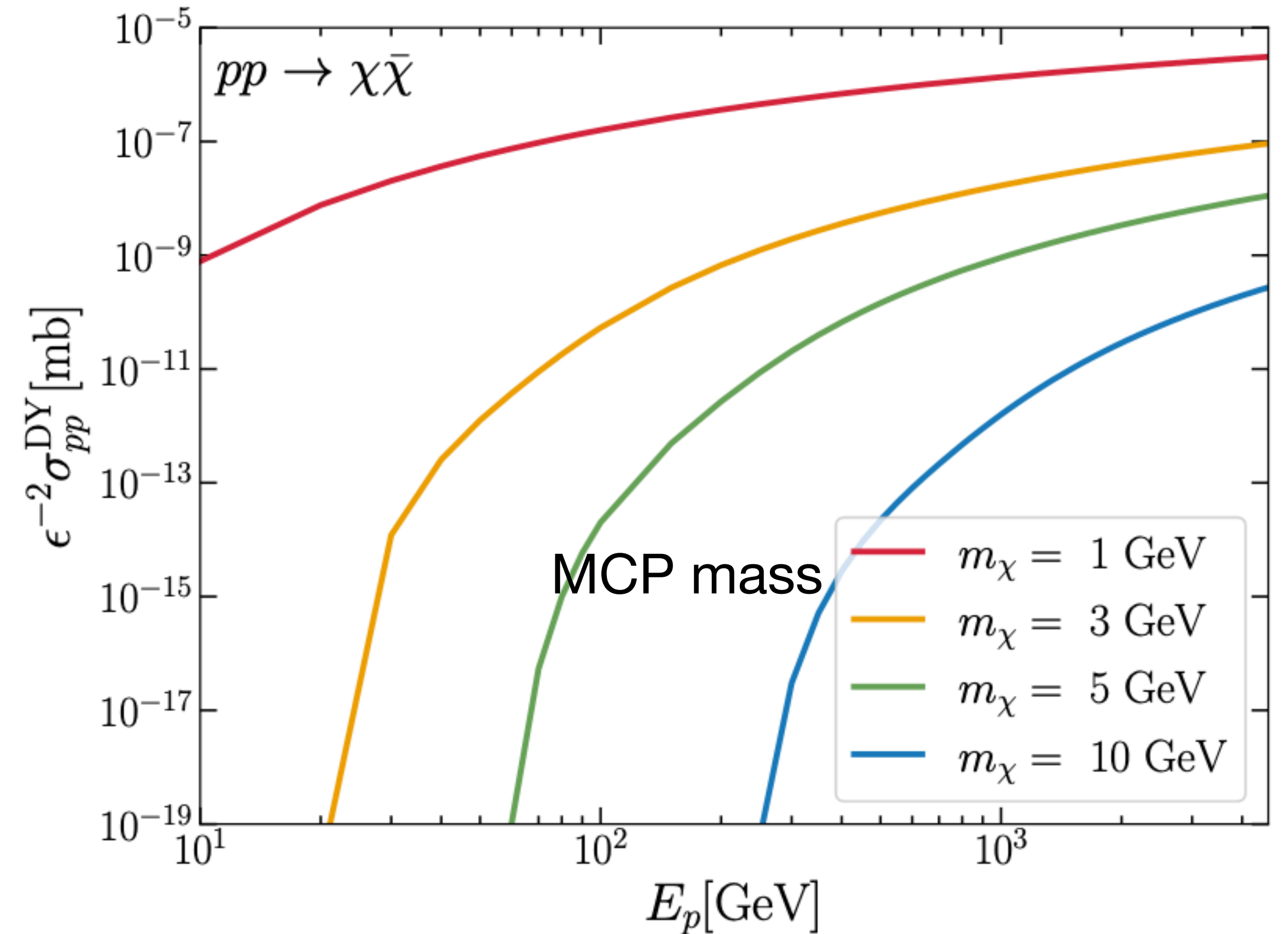
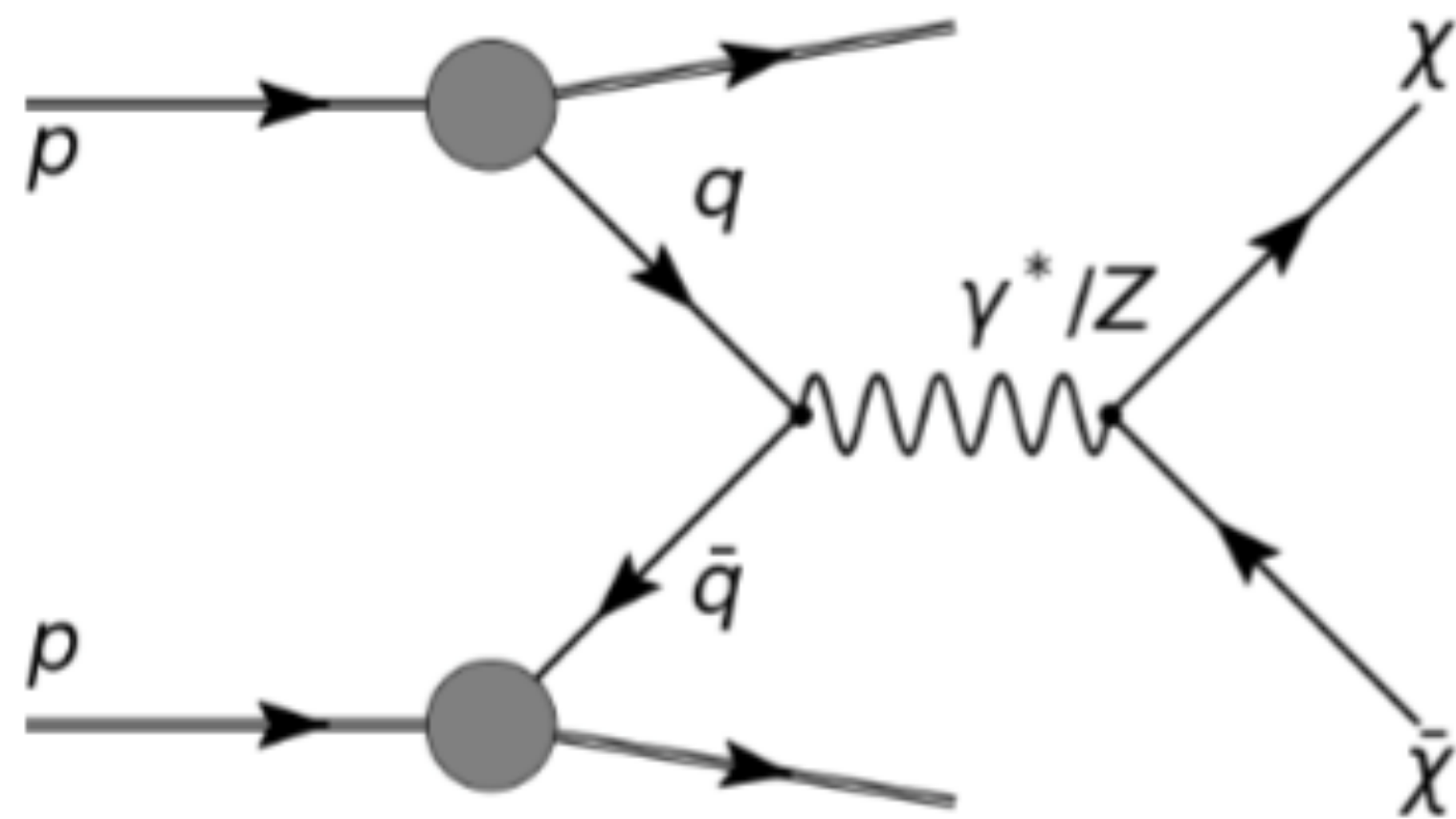
$$\Phi_{\chi}^{\text{PB}} = \int dE_p \Phi_p \frac{\epsilon^2 e^2}{6\pi^2} \int \frac{dk^2}{k^2} \sqrt{1 - \frac{4m_{\chi}^2}{k^2}} \left( 1 + \frac{2m_{\chi}^2}{k^2} \right) \times \int dE_k \frac{1}{\sigma_{pN}} \frac{d\sigma^{\text{PB}}}{dE_k} \frac{\Theta(E_{\chi} - E_{\min}) \Theta(E_{\max} - E_{\chi})}{E_{\max} - E_{\min}}$$

Du et al arXiv: 2211.11469

Du et al arXiv: 2308.05607

# Millicharge Particles from Drell-Yan Process

Madgraph simulations



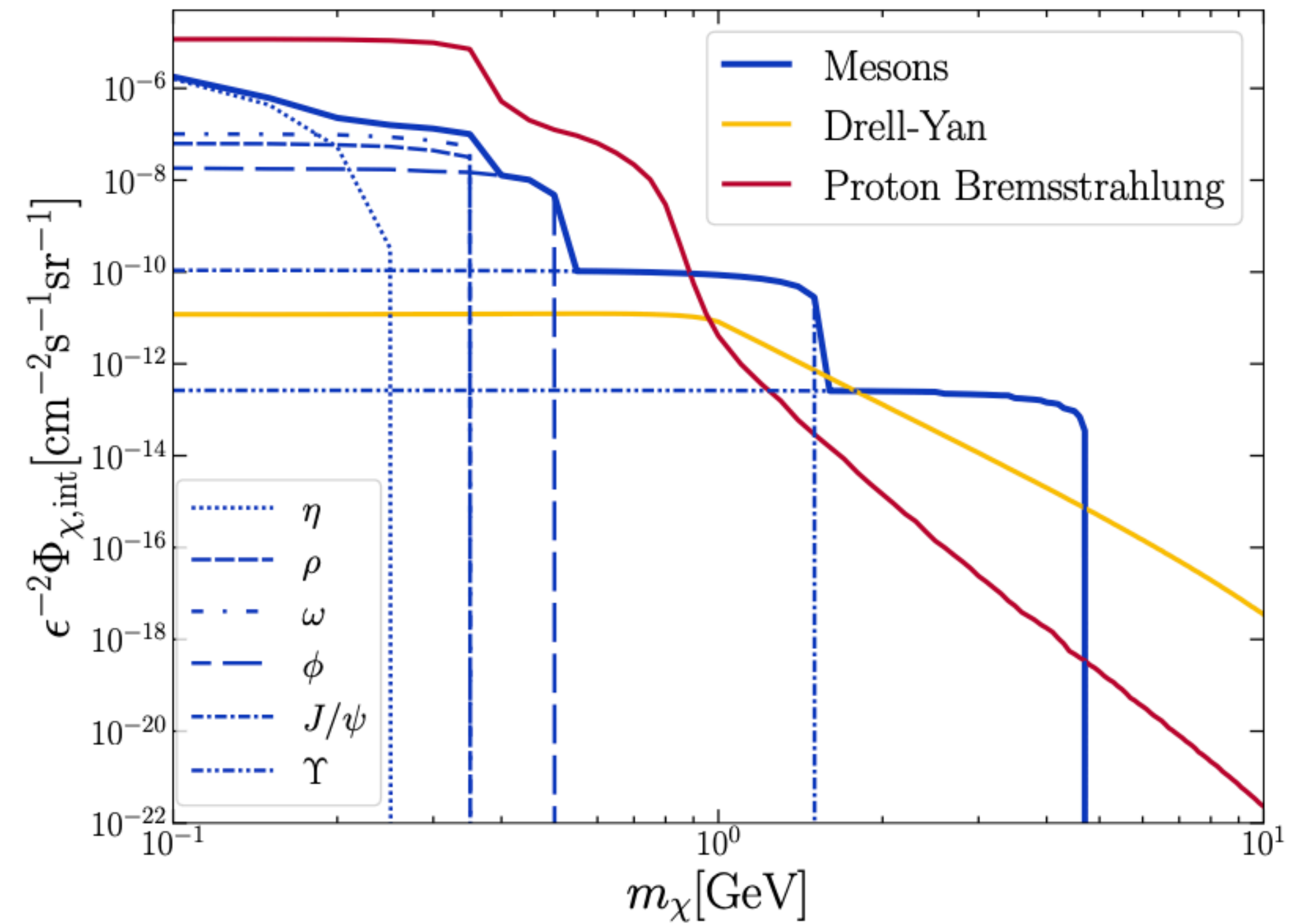
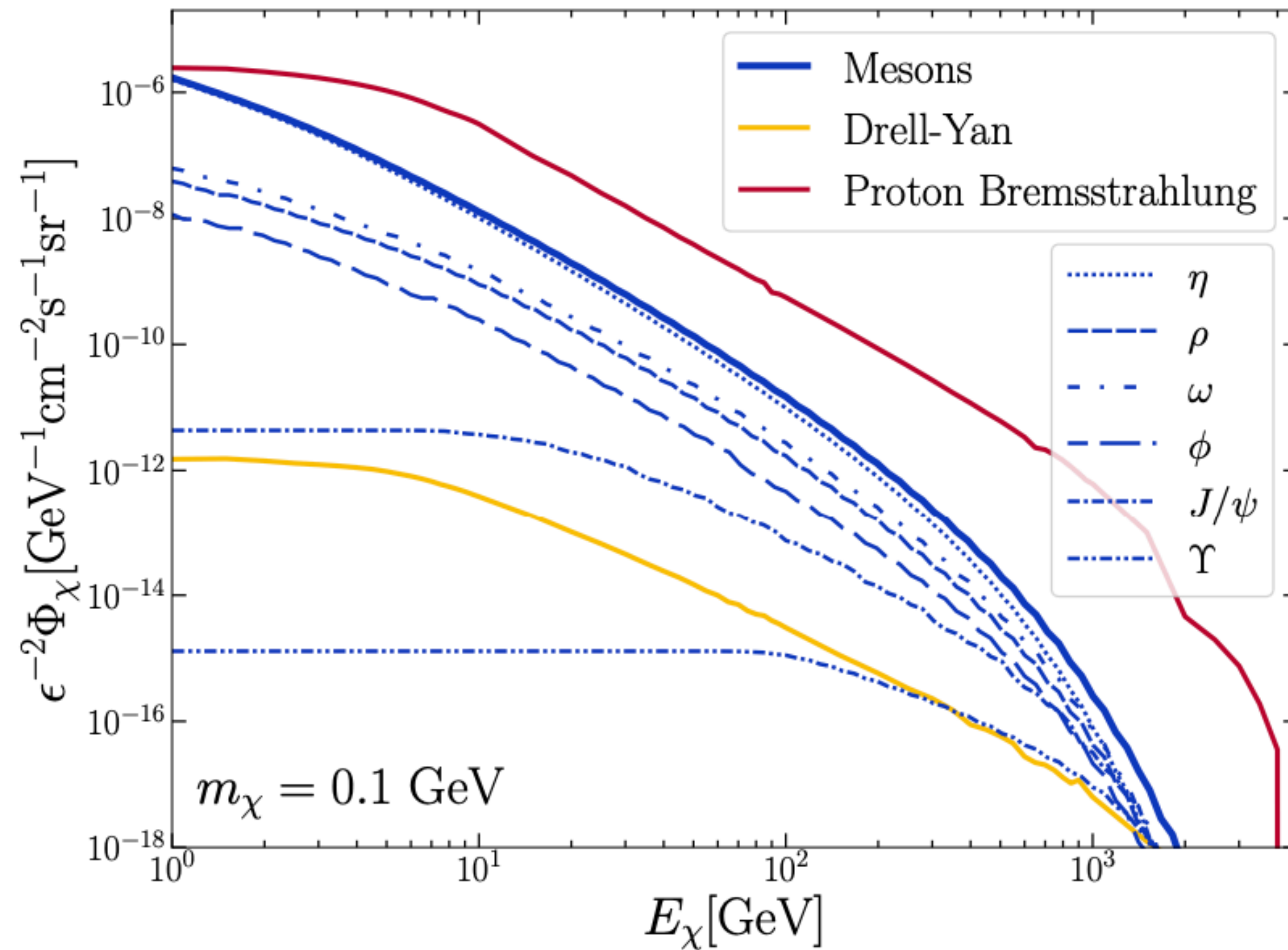
$$\hat{\sigma} (q(p_1) \bar{q}(p_2) \rightarrow l^+ l^-) = \frac{4\pi\alpha^2}{3\hat{s}} \frac{1}{N_c} Q_q^2$$

Wu, Hardy, **NS**, arXiv: 2406.01668



# Millicharge Particles Flux

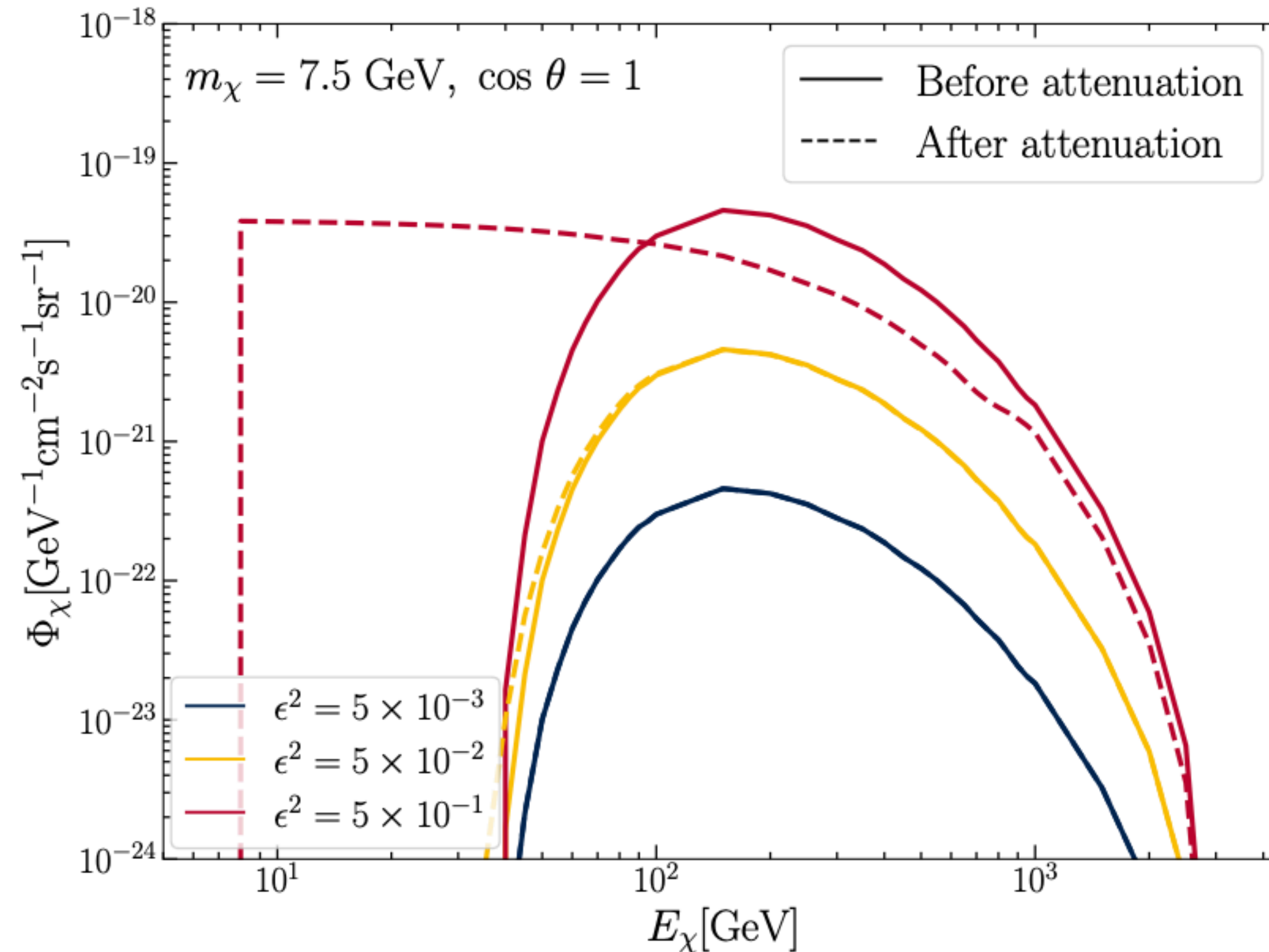
Meson decay+Proton Bremsstrahlung+Drell-Yan



Wu, Hardy, **NS**, arXiv: 2406.01668

# Earth Attenuation

$$-\frac{dE}{dX} = \varepsilon^2 \left( a_{\text{ion.}} + b_{\text{el.-brem.}} \varepsilon^2 E + b_{\text{inel.-brem.}} E + b_{\text{pair}} E + b_{\text{photo-had.}} E \right) \approx \varepsilon^2 (a + bE)$$

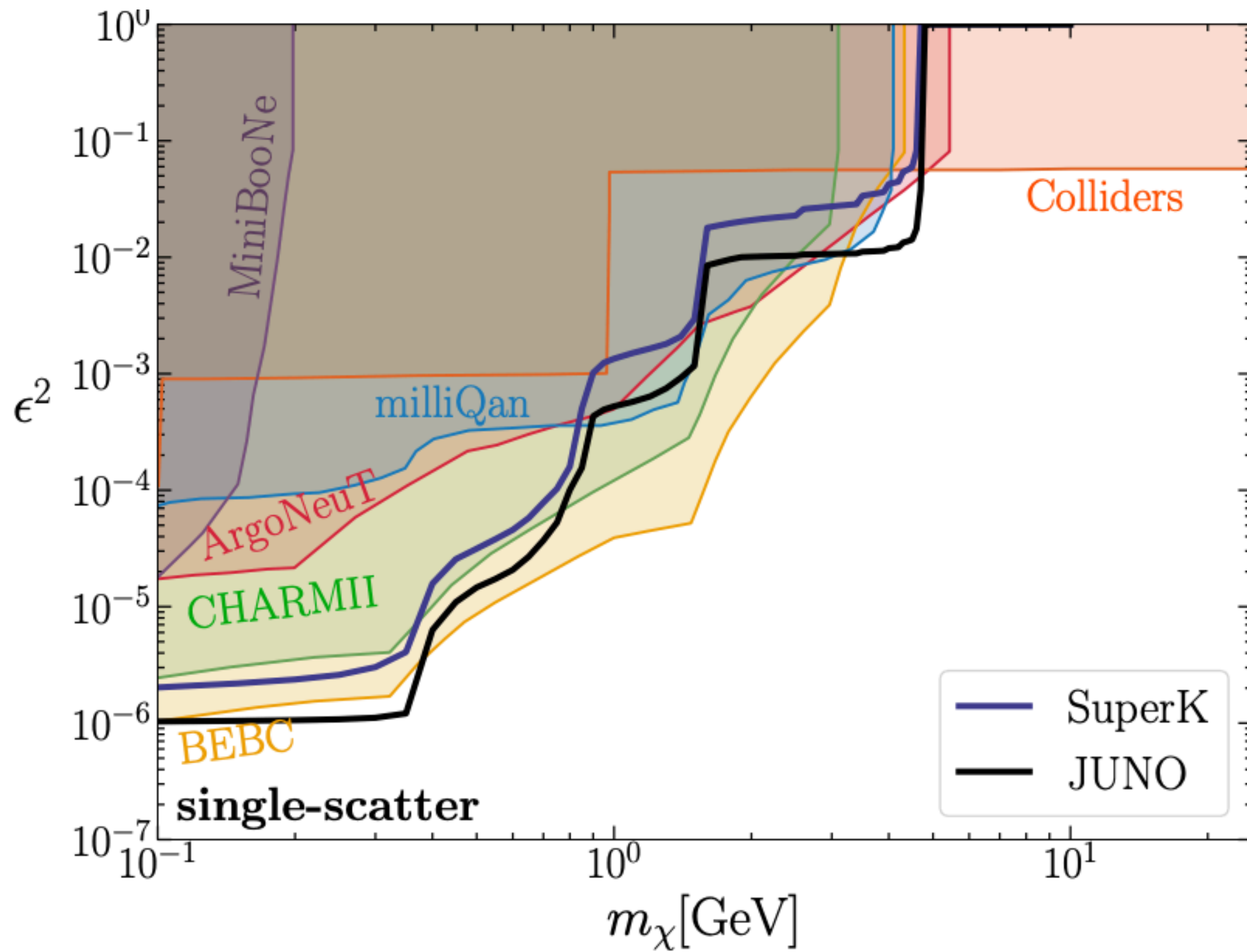


Wu, Hardy, **NS**, arXiv: 2406.01668

For  $\varepsilon^2 \gtrsim 10^{-2}$ , the down-going flux becomes significantly attenuated



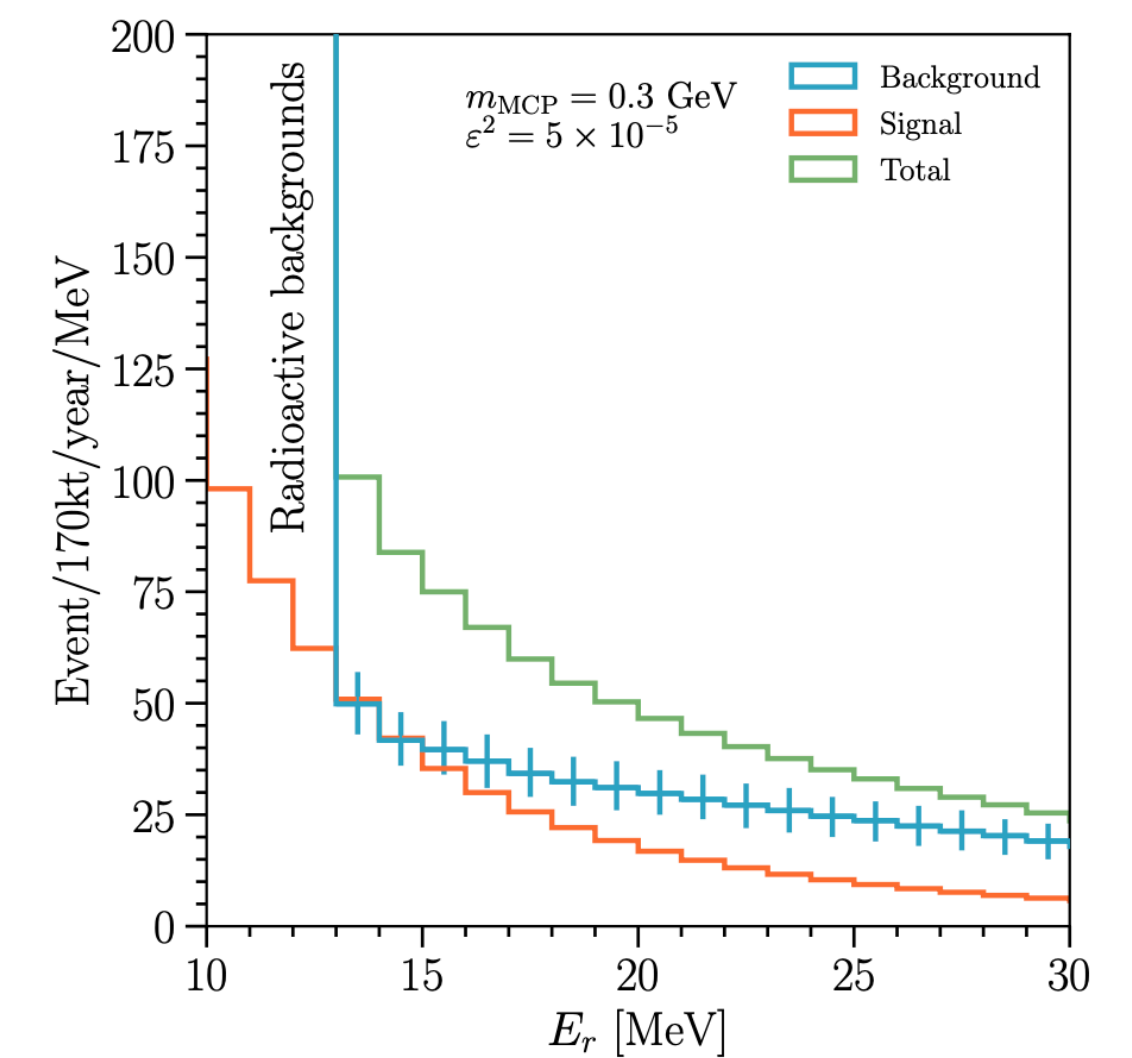
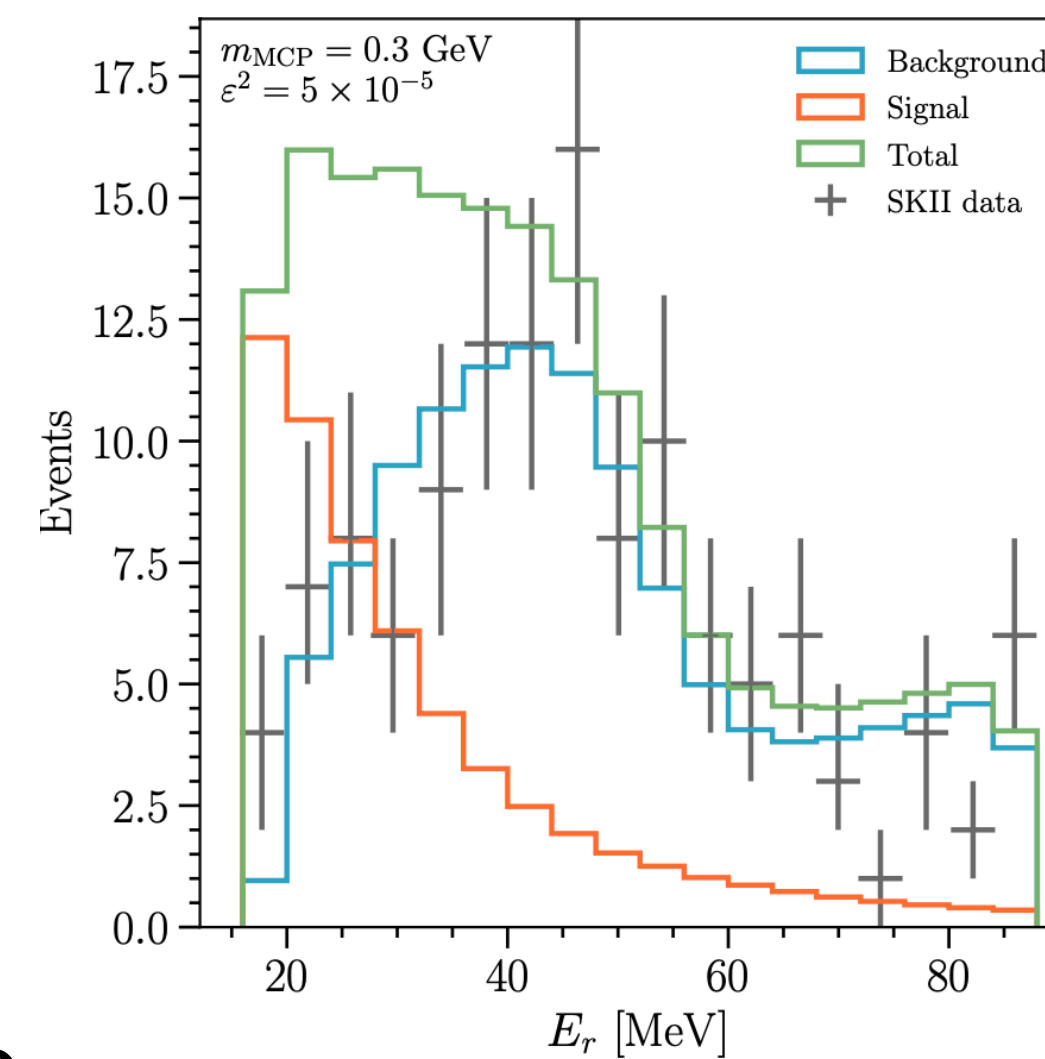
# Single Scatter Constraint



$$\frac{d\sigma_{\chi e}}{dE_r} = \pi\epsilon^2\alpha^2 \frac{(E_r^2 + 2E_\chi^2)m_e - ((2E_\chi + m_e)m_e + m_\chi^2) E_\chi}{E_r^2 m_e^2 (E_\chi^2 - m_\chi^2)}$$

$$d\sigma_{\chi e}/dE_r \propto 1/E_r^2$$

$$\sigma_{\chi e} \simeq \frac{\pi\alpha_{EM}\epsilon^2}{m_e T_{\min}} = 2.6 \times 10^{-25} \epsilon^2 \text{ cm}^2 \frac{\text{MeV}}{T_{\min}}$$



Assuming JUNO 10 MeV threshold+170 kton·yr exposure

Wu, Hardy, NS, arXiv: 2406.01668

Arguelles et al JHEP/2104.13924

# Multiple Scatter Constraint

Single scatter probability  $P_1 = 1 - \exp\left(-\frac{L_D}{\lambda(T_{\min})}\right)$

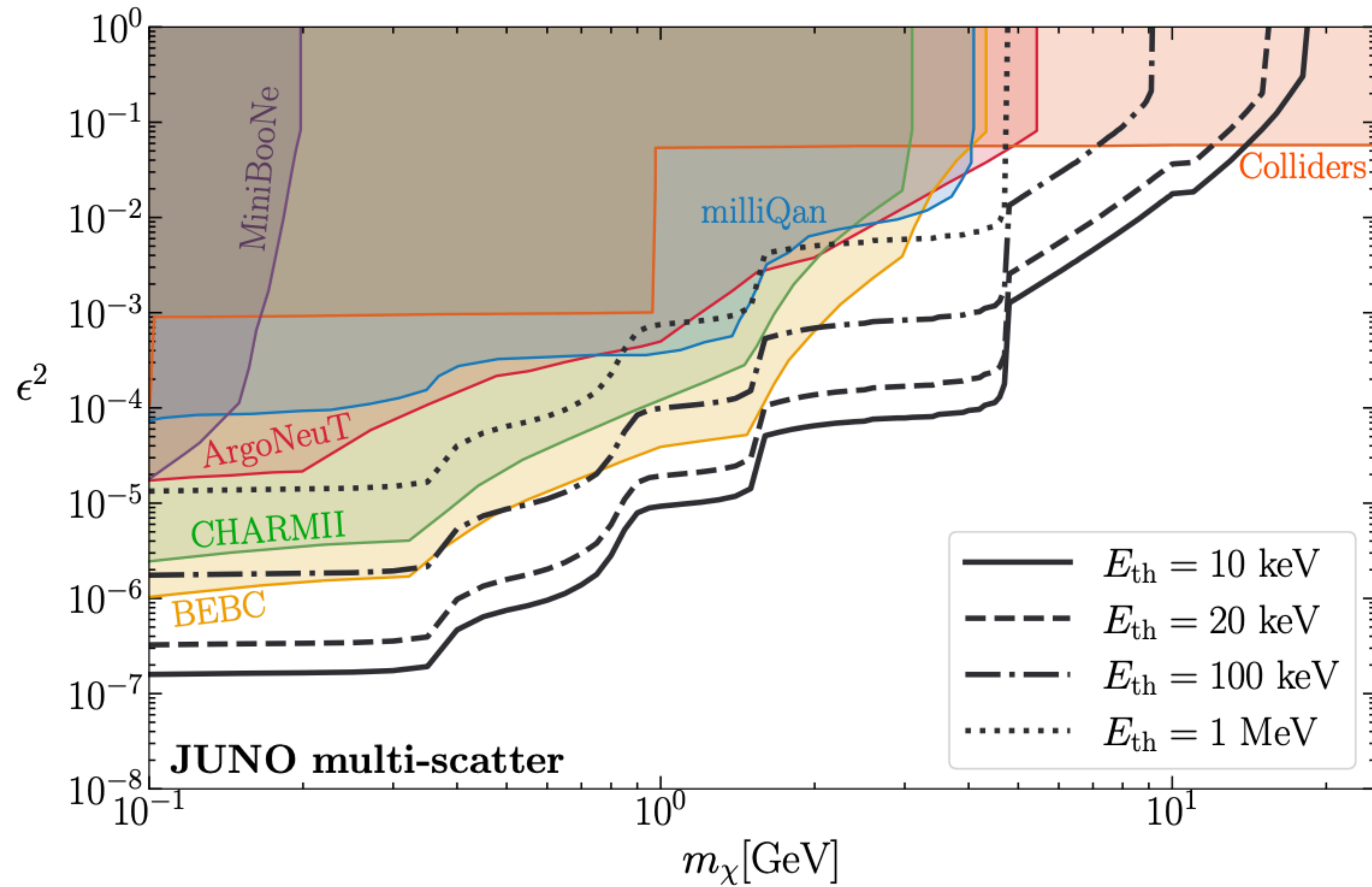
Multiple scatter probability  $P_{n \geq 2}(T_{\min}) = 1 - \exp\left(-\frac{L_D}{\lambda}\right) \left(1 + \frac{L_D}{\lambda}\right)$

Number of observed events  $N_{\text{multi}} = N_{\text{single}} P_{n \geq 2}(T_{\min, \text{multi}}) / P_1(T_{\min, \text{single}})$

$$N_{\text{single}}(m_\chi, \epsilon) = N_e T \int_{E_{i, \min}}^{E_{i, \max}} dE_r \epsilon_D(E_r) \times \int dE_\chi d\Omega \Phi_\chi^D(E_\chi, \Omega) \frac{d\sigma_{\chi e}}{dE_r}$$



# Multiple Scatter Constraint



Assuming JUNO 170 kton·yr exposure

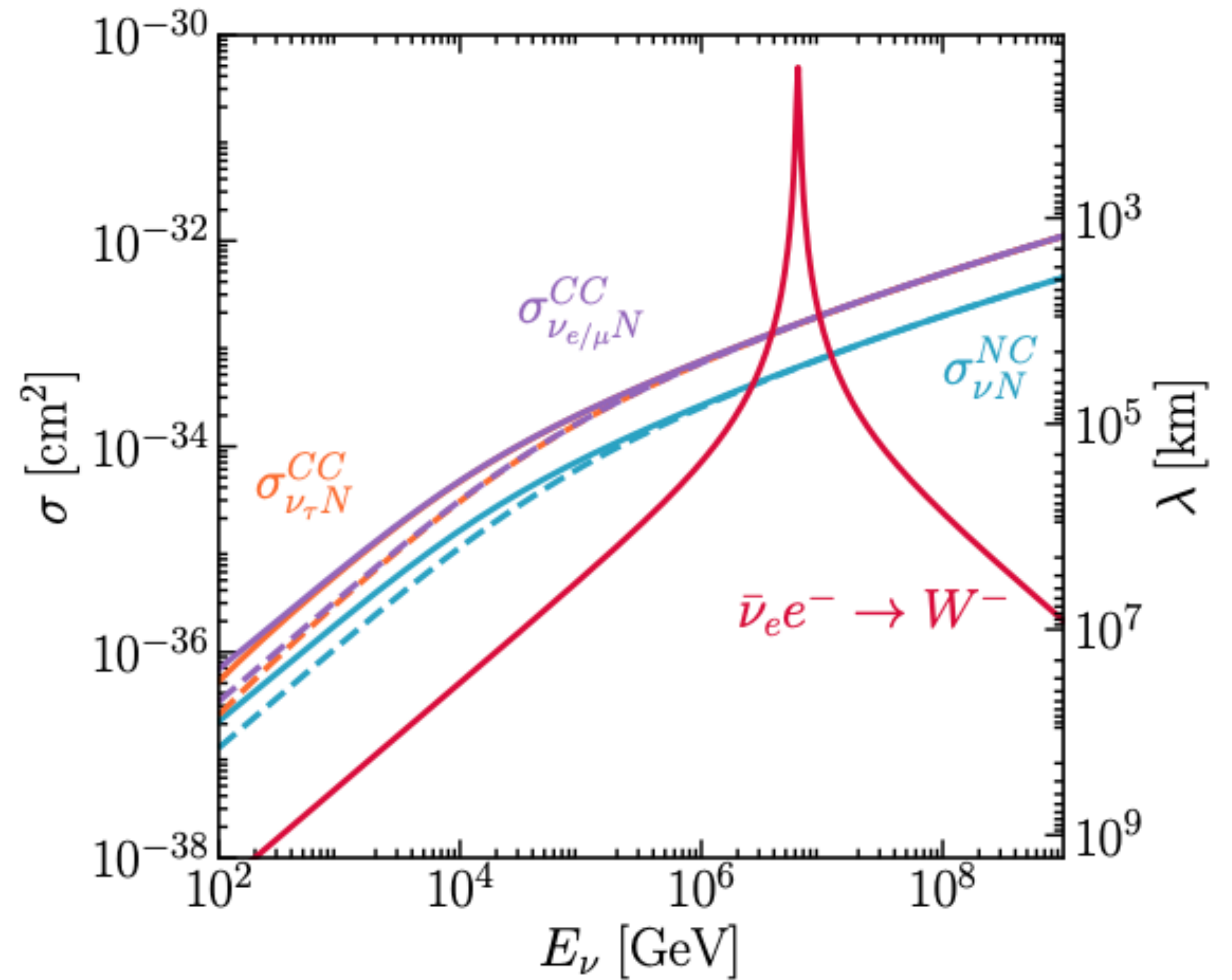
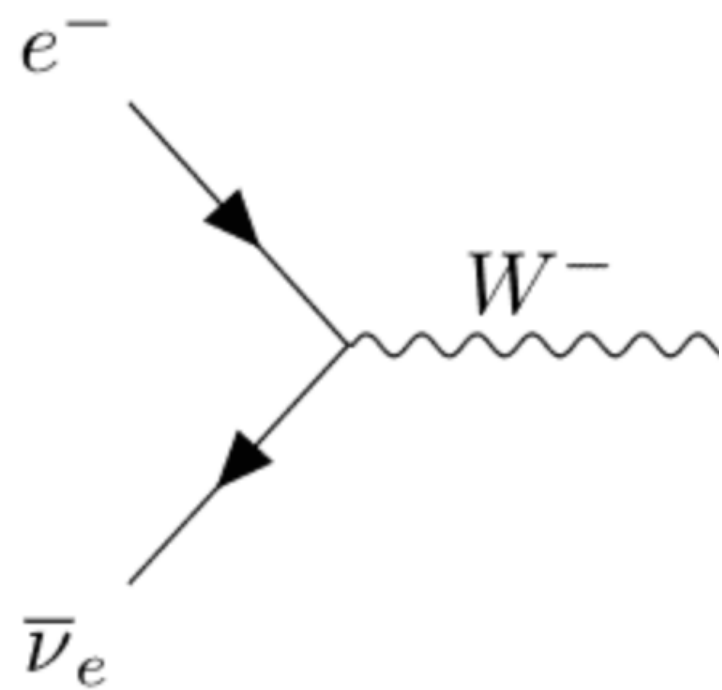
Wu, Hardy, **NS**, arXiv: 2406.01668

# Glashow Resonance (GR)

Huang, Liu , 1912.02976

When the centre of mass energy is close to  $W$  boson mass,  $\bar{\nu}_e$ -electron interaction is enhanced by the resonant production of  $W$

$$\sigma_{\bar{\nu}_e e}(s) = 24\pi \Gamma_W^2 \text{Br}(W^- \rightarrow \bar{\nu}_e + e^-) \times \frac{s/M_W^2}{(s - M_W^2)^2 + (M_W \Gamma_W)^2},$$





# Glashow Resonance at IceCube

Article | [Published: 10 March 2021](#)

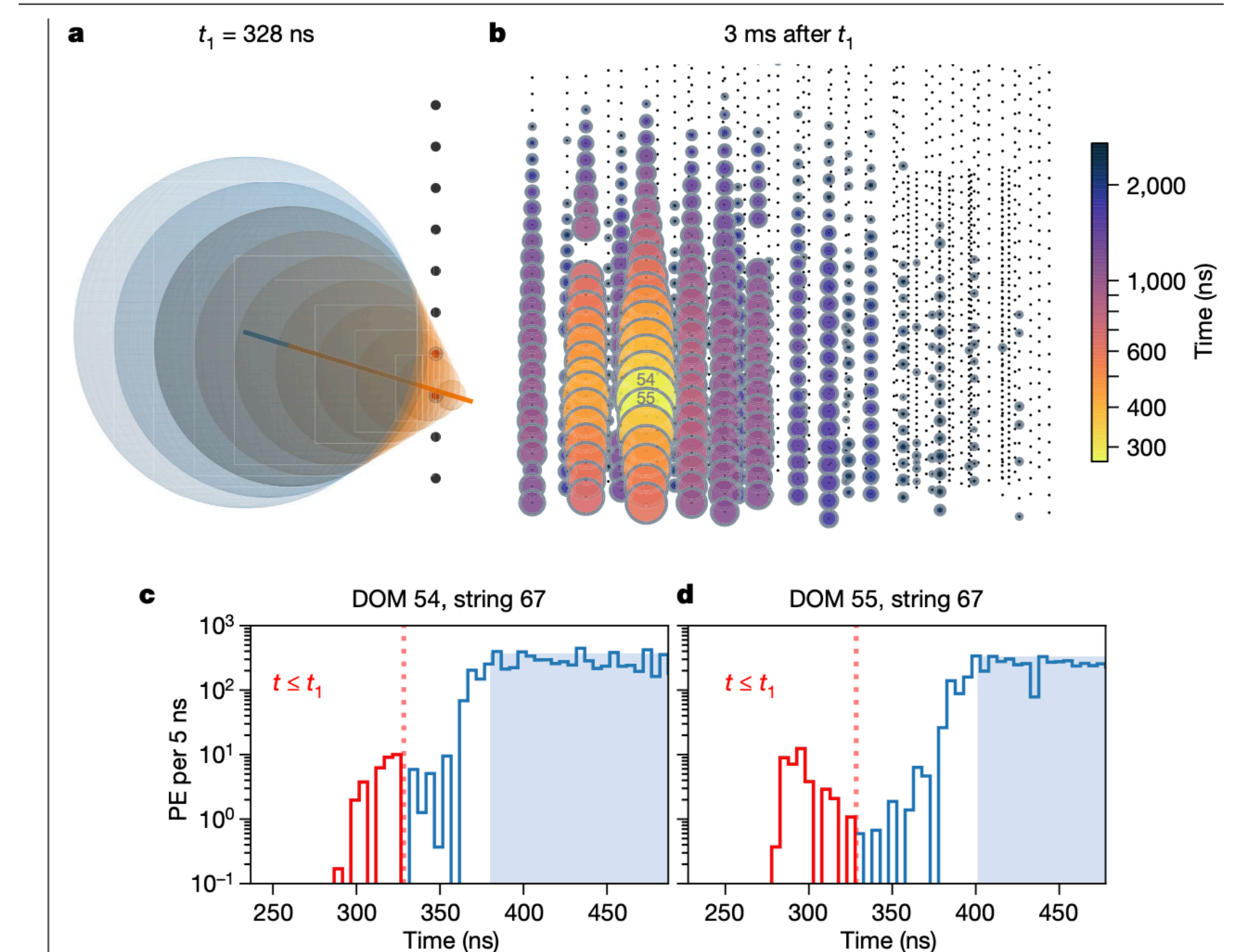
## Detection of a particle shower at the Glashow resonance with IceCube

[The IceCube Collaboration](#)

[Nature](#) **591**, 220–224 (2021) | [Cite this article](#)

16k Accesses | 63 Citations | 507 Altmetric | [Metrics](#)

- ▶ Glashow resonance candidate was identified with **2.3  $\sigma$  significance** assuming  $E^{-2.5}$  spectrum
- ▶ The cascade is **partially contained (PEPE)**, with muon early pulses consistent with W decay



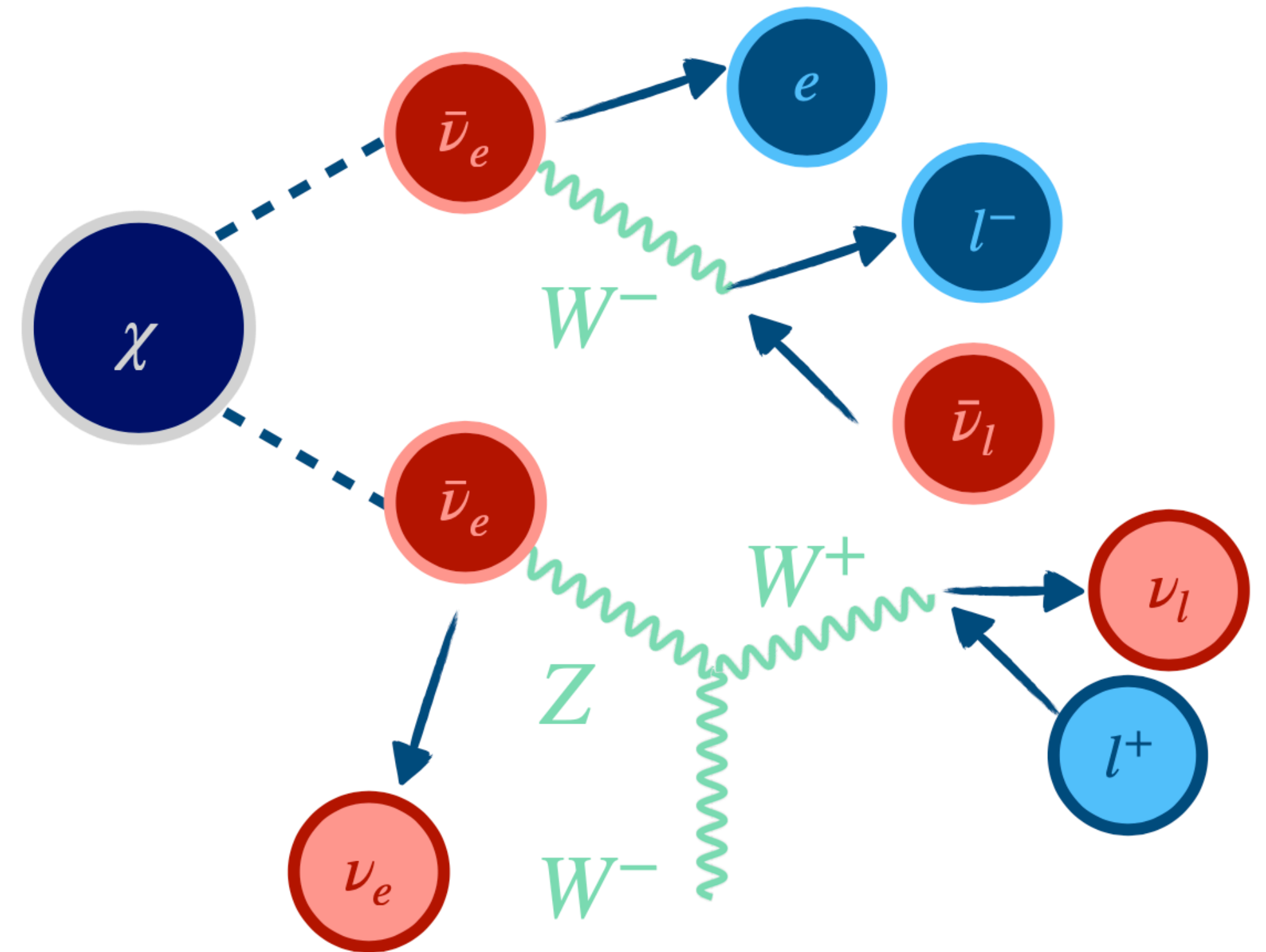
# Asymmetric Dark Matter Decay

Credit: Qinrui Liu

$$\mathcal{O}_{X \rightarrow \nu} = \frac{1}{\Lambda^2} X \psi L \Phi, \quad \frac{1}{\Lambda^2} X (L \Phi)^2, \quad \frac{1}{\Lambda^{3n-1}} \bar{X} l \psi^n$$



$$X \rightarrow \bar{\nu}, \quad X \rightarrow \bar{\nu}\bar{\nu}, \quad X \rightarrow \nu\bar{\nu}\bar{\nu}$$



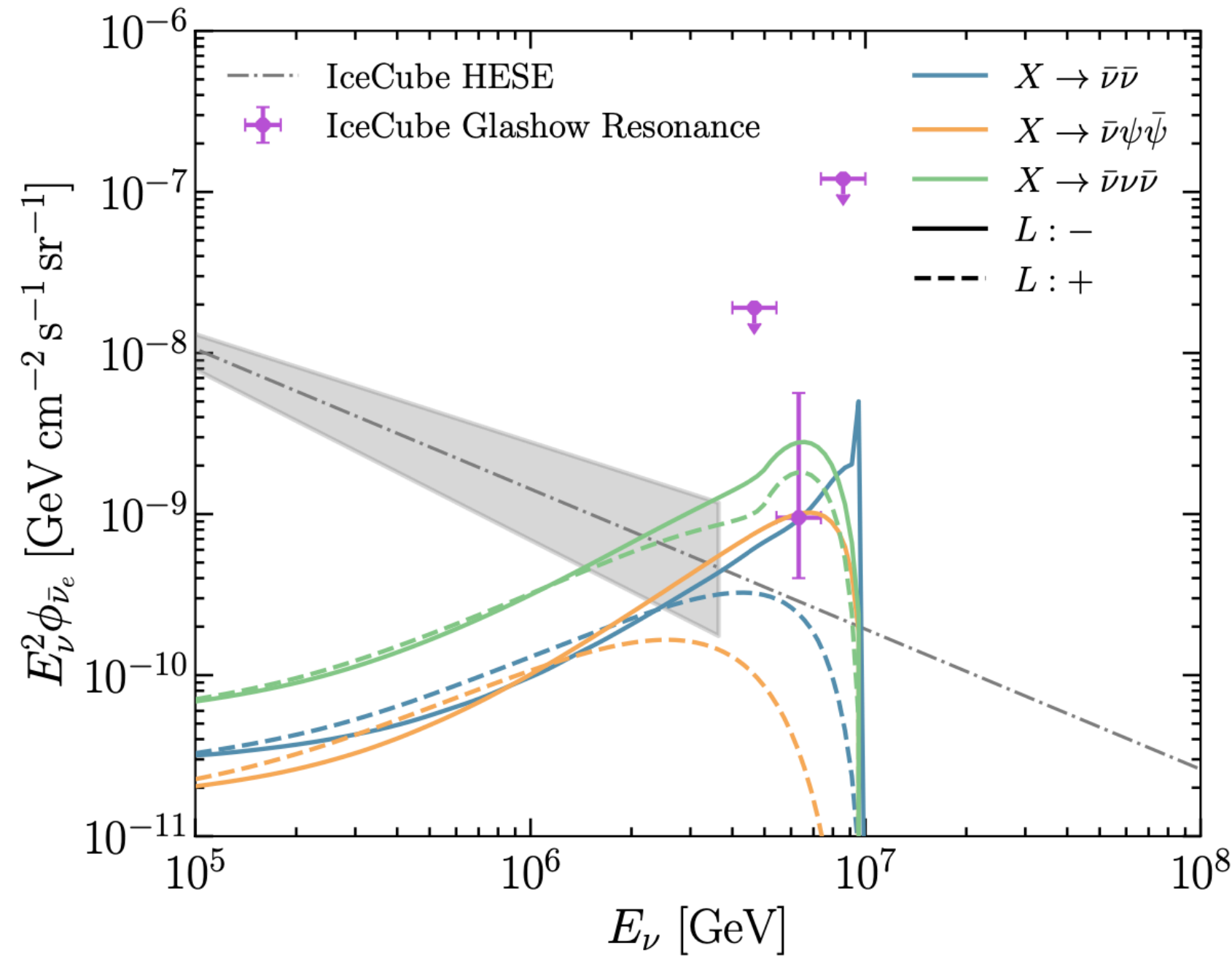
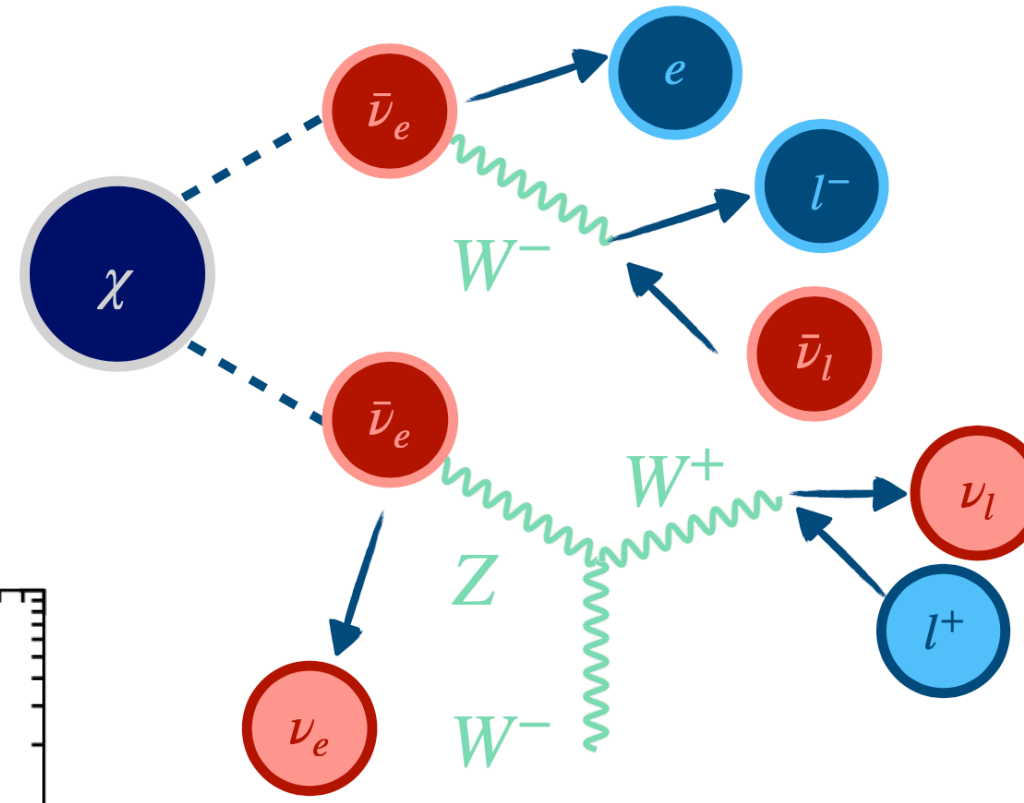


# Asymmetric Dark Matter Decay

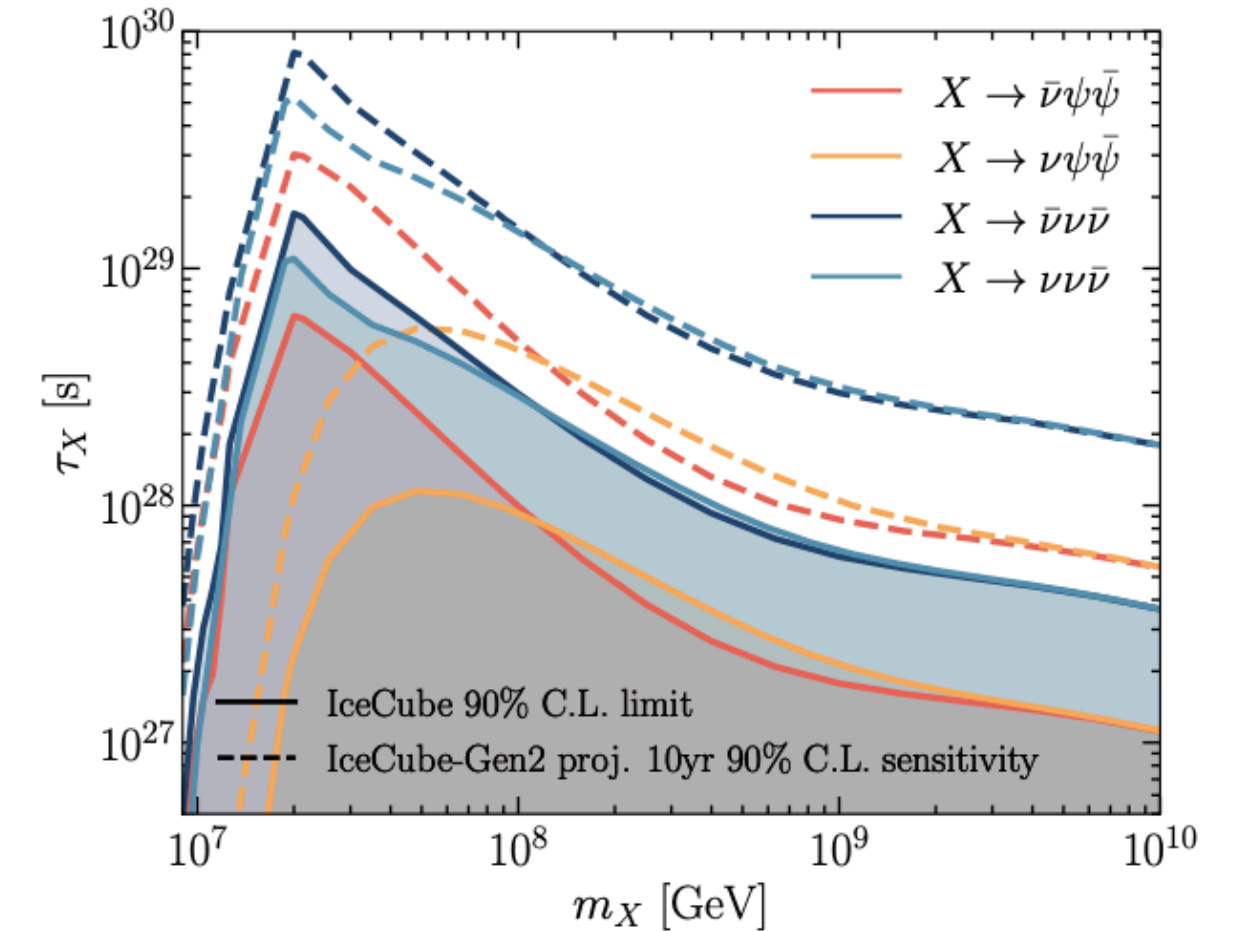
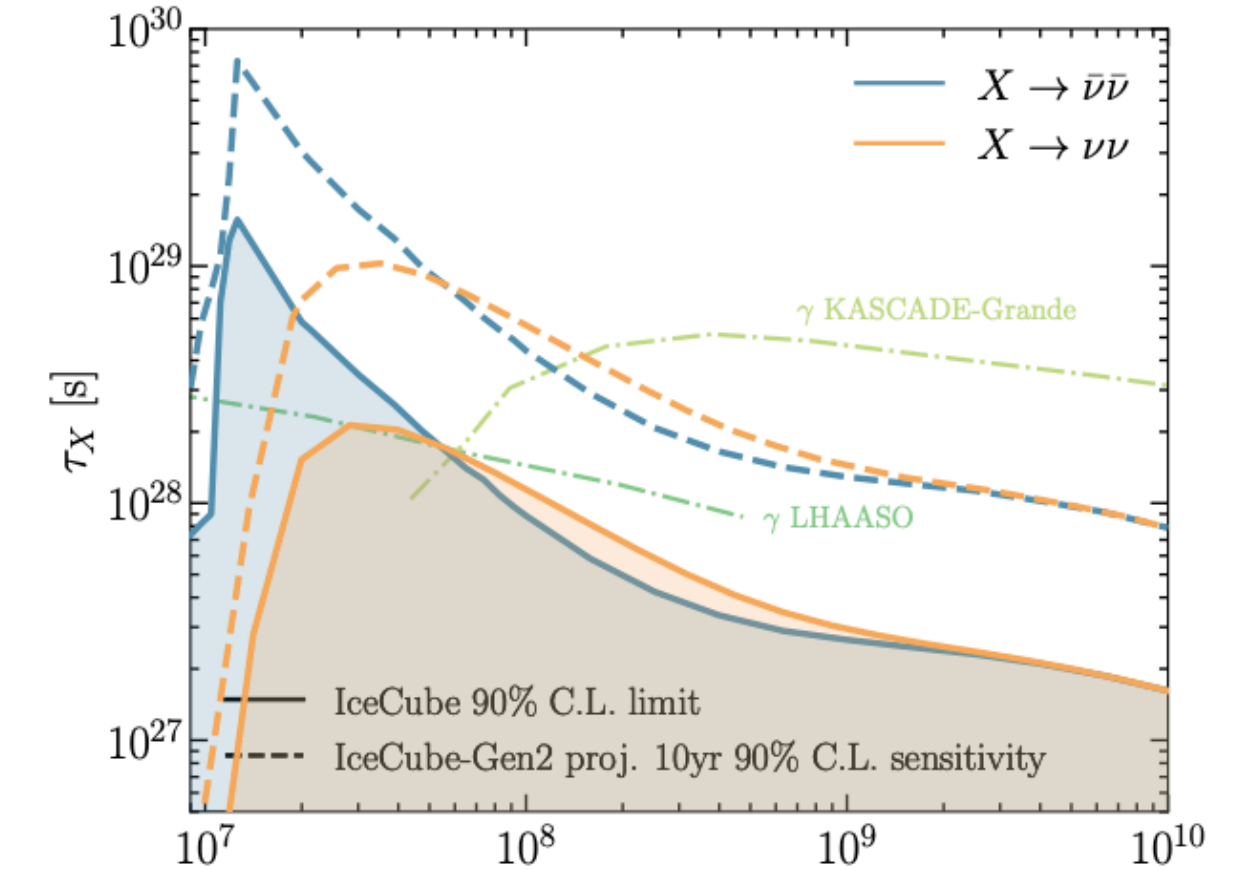
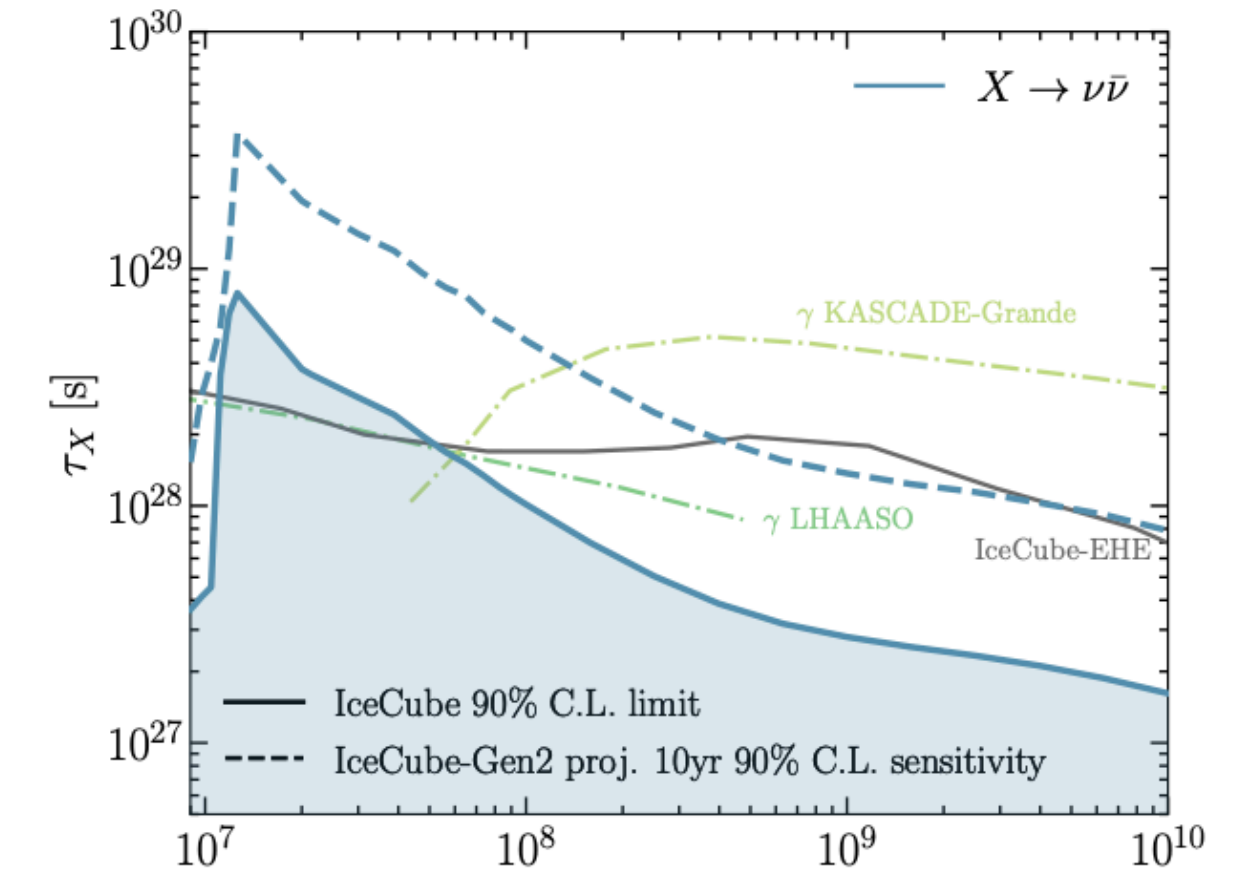
$$\mathcal{O}_{X \rightarrow \nu} = \frac{1}{\Lambda^2} X \psi L \Phi, \quad \frac{1}{\Lambda^2} X (L \Phi)^2, \quad \frac{1}{\Lambda^{3n-1}} \bar{X} l \psi^n$$



$$X \rightarrow \bar{\nu}, \quad X \rightarrow \bar{\nu}\bar{\nu}, \quad X \rightarrow \nu\bar{\nu}\bar{\nu}$$



Liu, NS, Vincent, arXiv: 2406.14602



# Summary

- Neutrino experiments could be powerful probes of dark matter thanks to their large exposure
- Search for millicharged particles from atmospheric beam dump at JUNO and SuperK
- Search for heavy dark matter decay at IceCube



谢谢

# Heavy neutral leptons

Type-I seesaw  $\mathcal{L}_N = \mathcal{L}_{SM} + \sum_j i\bar{N}_j \gamma^\mu \partial_\mu N_j - \left( Y_{\alpha j} \bar{L}_\alpha \tilde{\Phi} N_j + \frac{m_{N_j}}{2} \bar{N}_j N_j^c \right)$

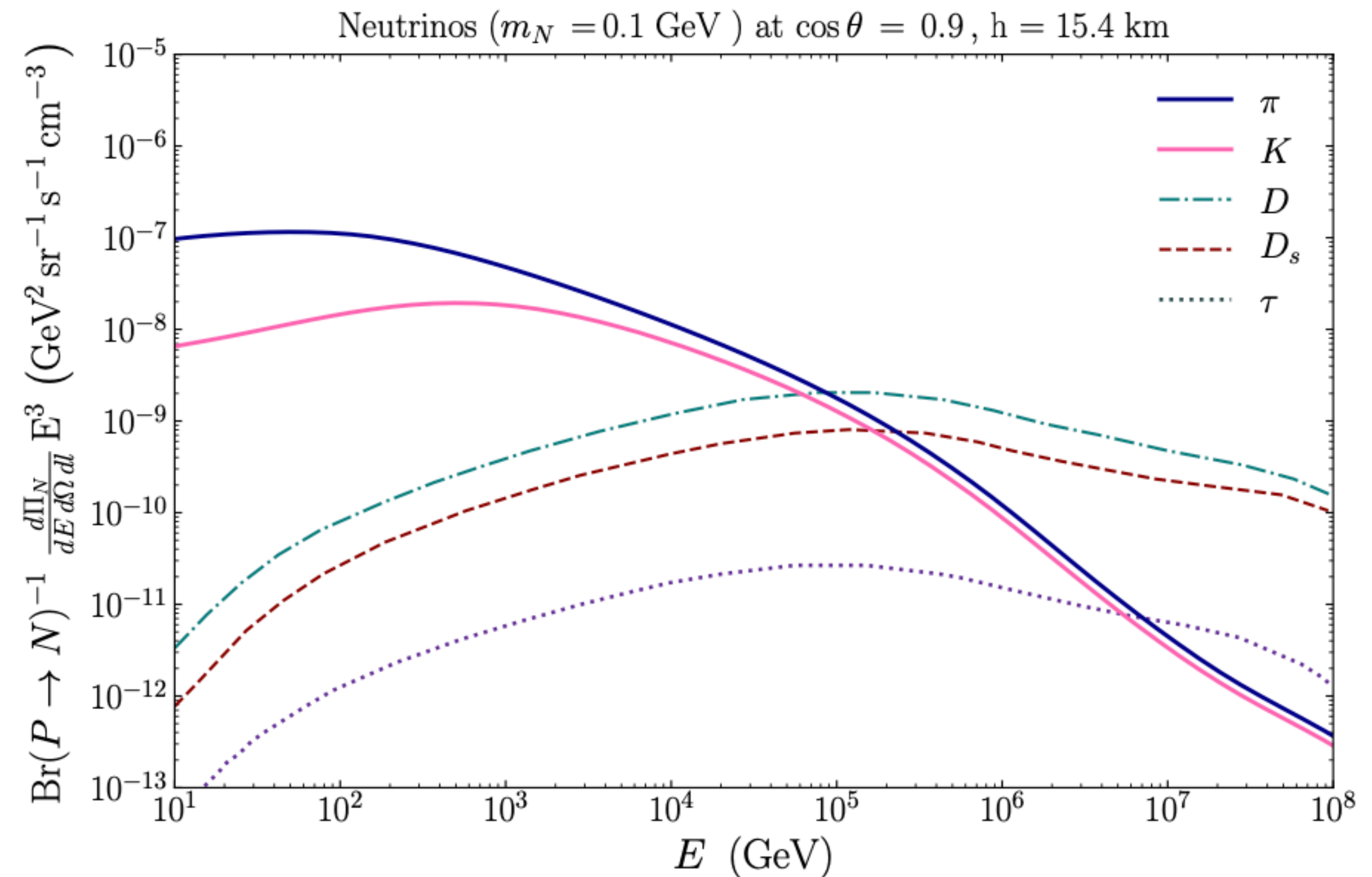
Neutrino mass  $m_\nu \propto \frac{(Y_\nu)^2}{m_N}$       mixing  $U_{\alpha j} \propto \frac{Y_{\nu}}{m_N}$

Meson and lepton decay

$$M \rightarrow l + N$$

$$\tau \rightarrow l + \nu + N$$

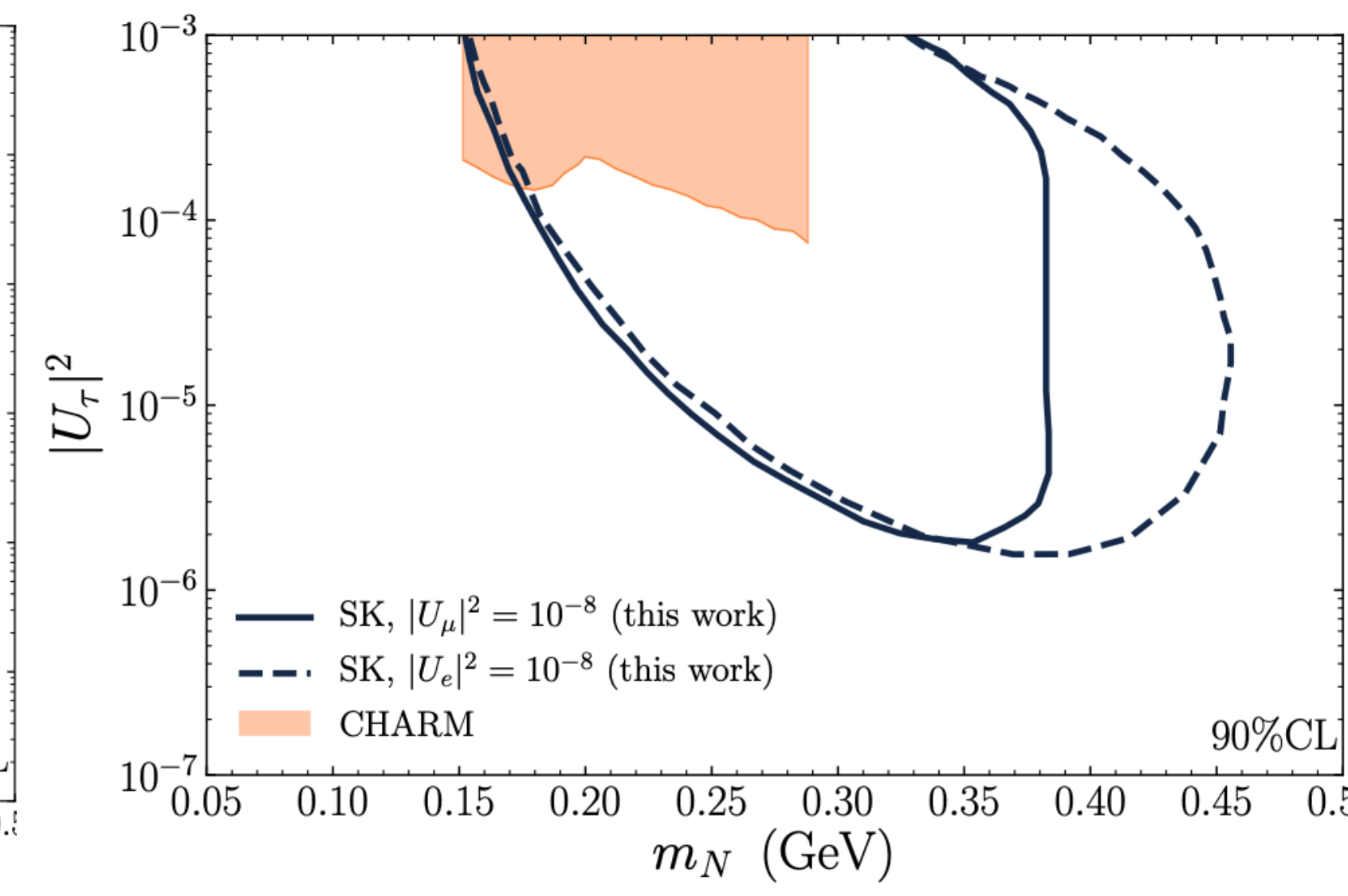
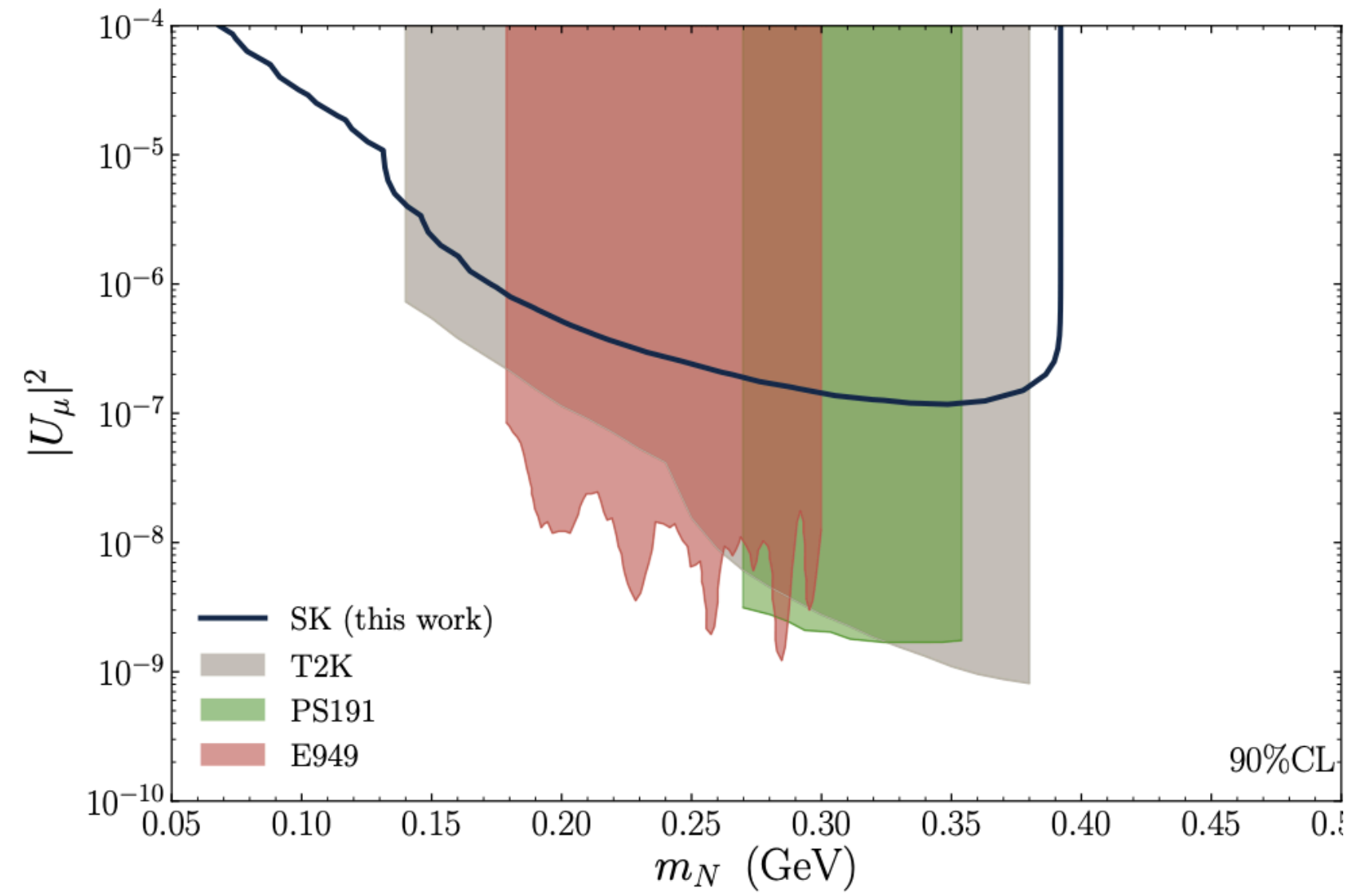
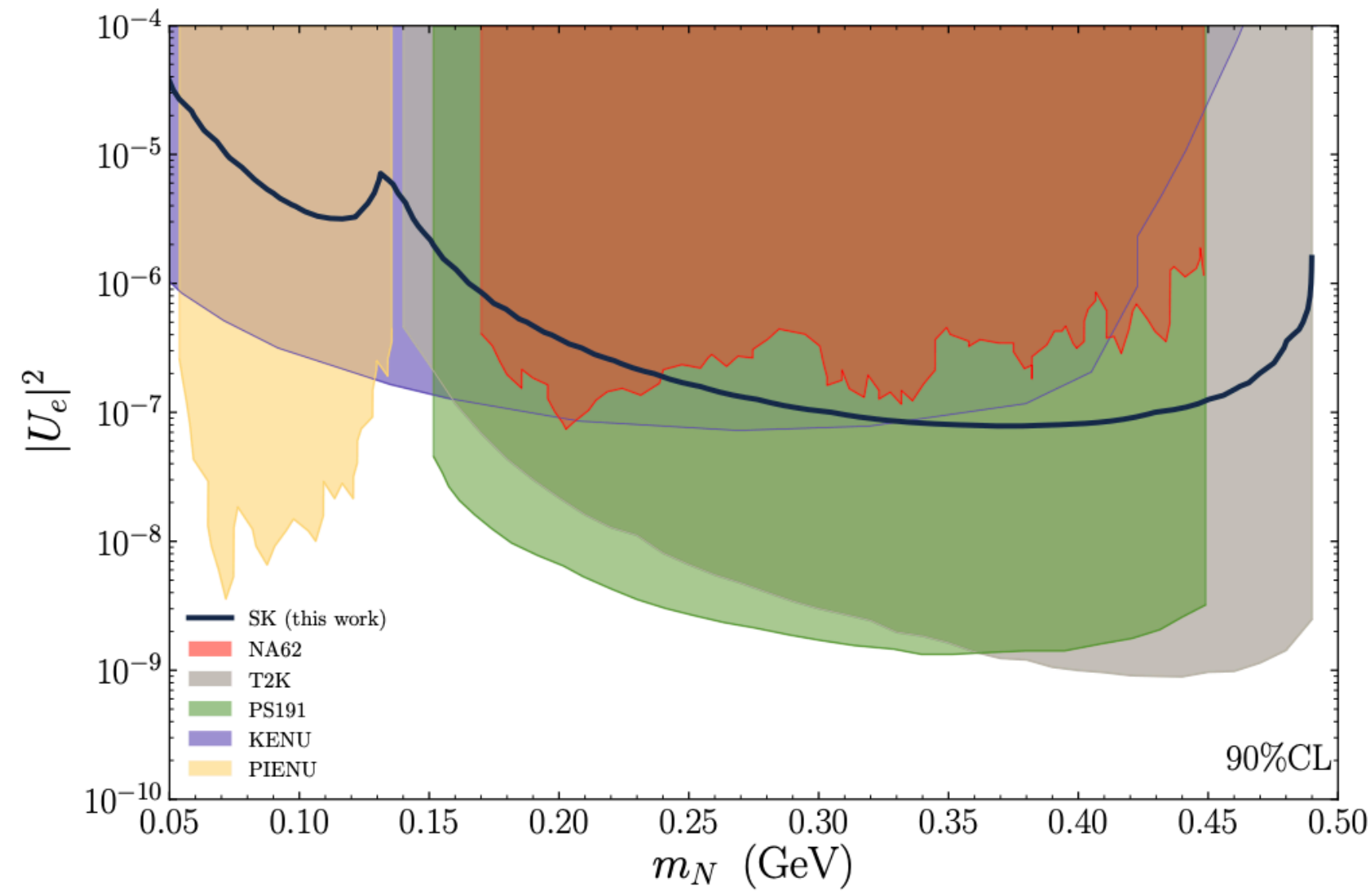
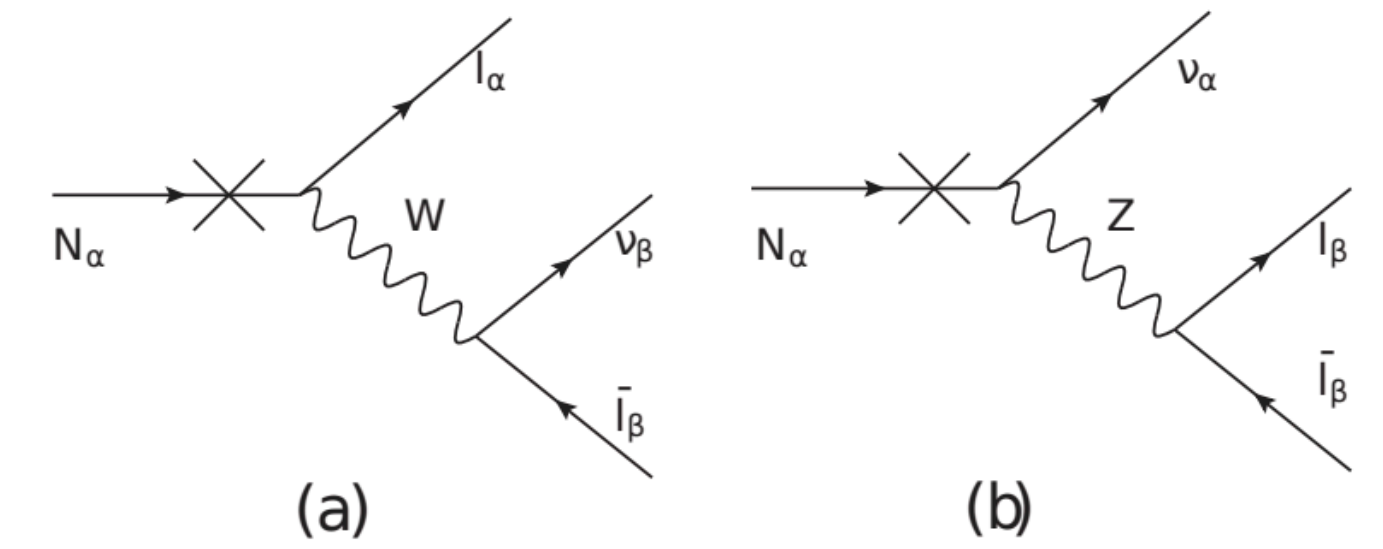
Coloma et al EPJC/1911.09129





# Heavy neutral leptons

Heavy neutral lepton decay to electron/muon at neutrino detectors



Coloma et al EPJC/1911.09129

# Hydrophilic dark matter

$$\mathcal{L} \supset i\bar{\chi}(\not{D} - m_\chi)\chi + \frac{1}{2}\partial_\mu S\partial^\mu S - \frac{1}{2}m_S^2 S^2 - \left(g_\chi S\bar{\chi}_L\chi_R + g_u S\bar{u}_L u_R + h.c.\right),$$

Meson decay

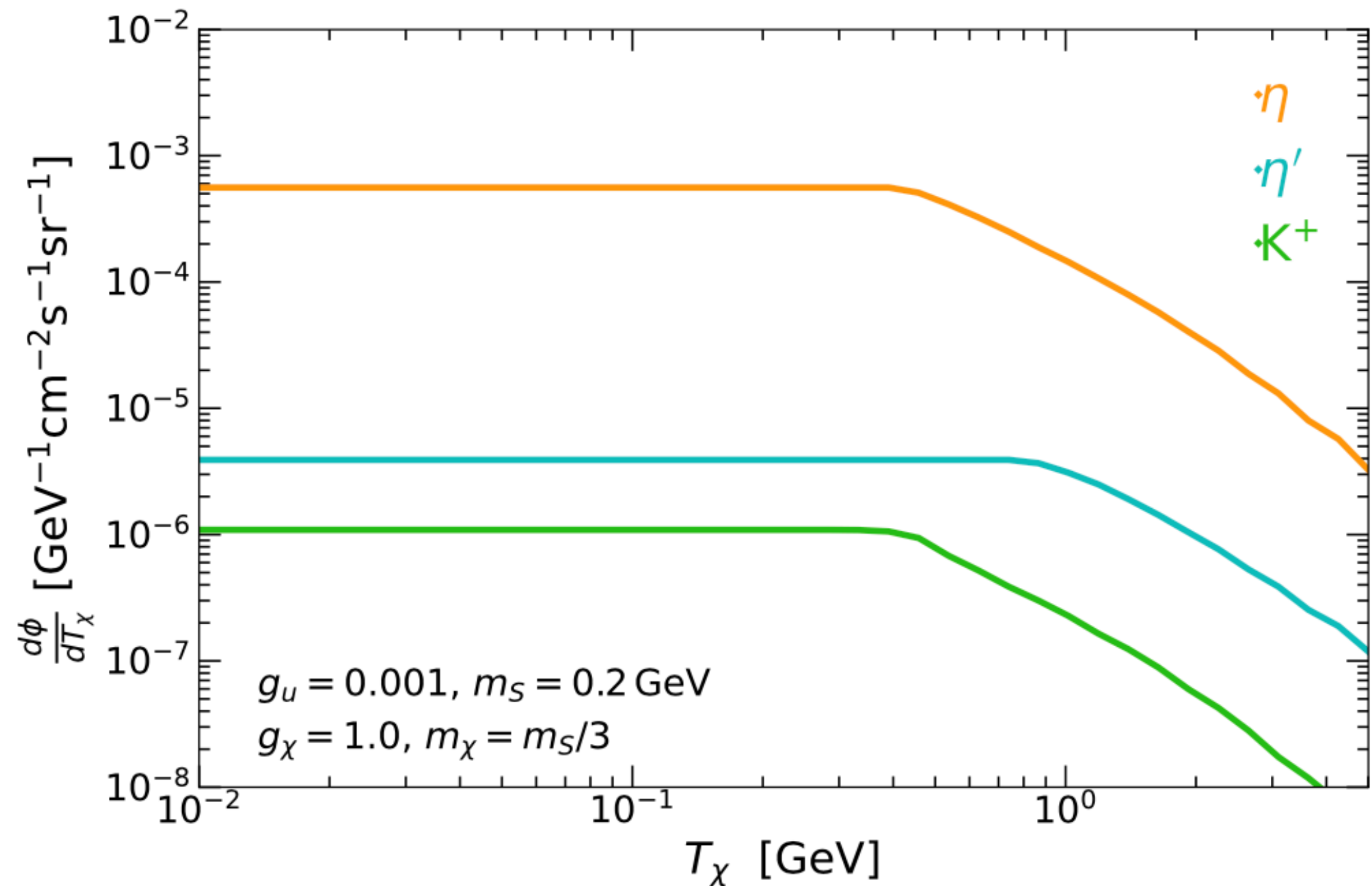
$$\eta \rightarrow \pi^0 + S$$

$$\eta' \rightarrow \pi^0 + S$$

$$K^+ \rightarrow \pi^+ + S$$

$$S \rightarrow 2\chi$$

Arguelles et al PLB/2203.12630

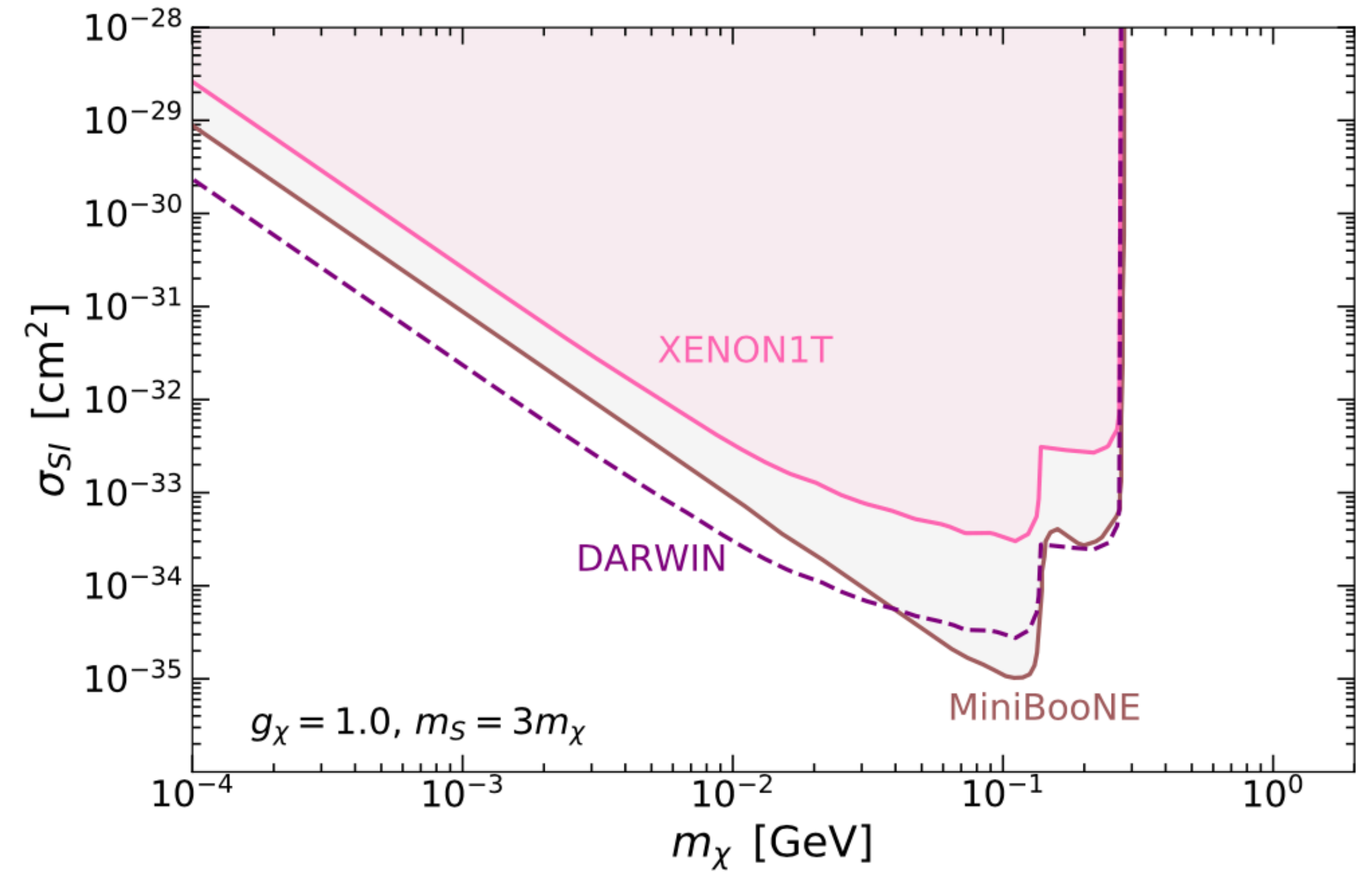
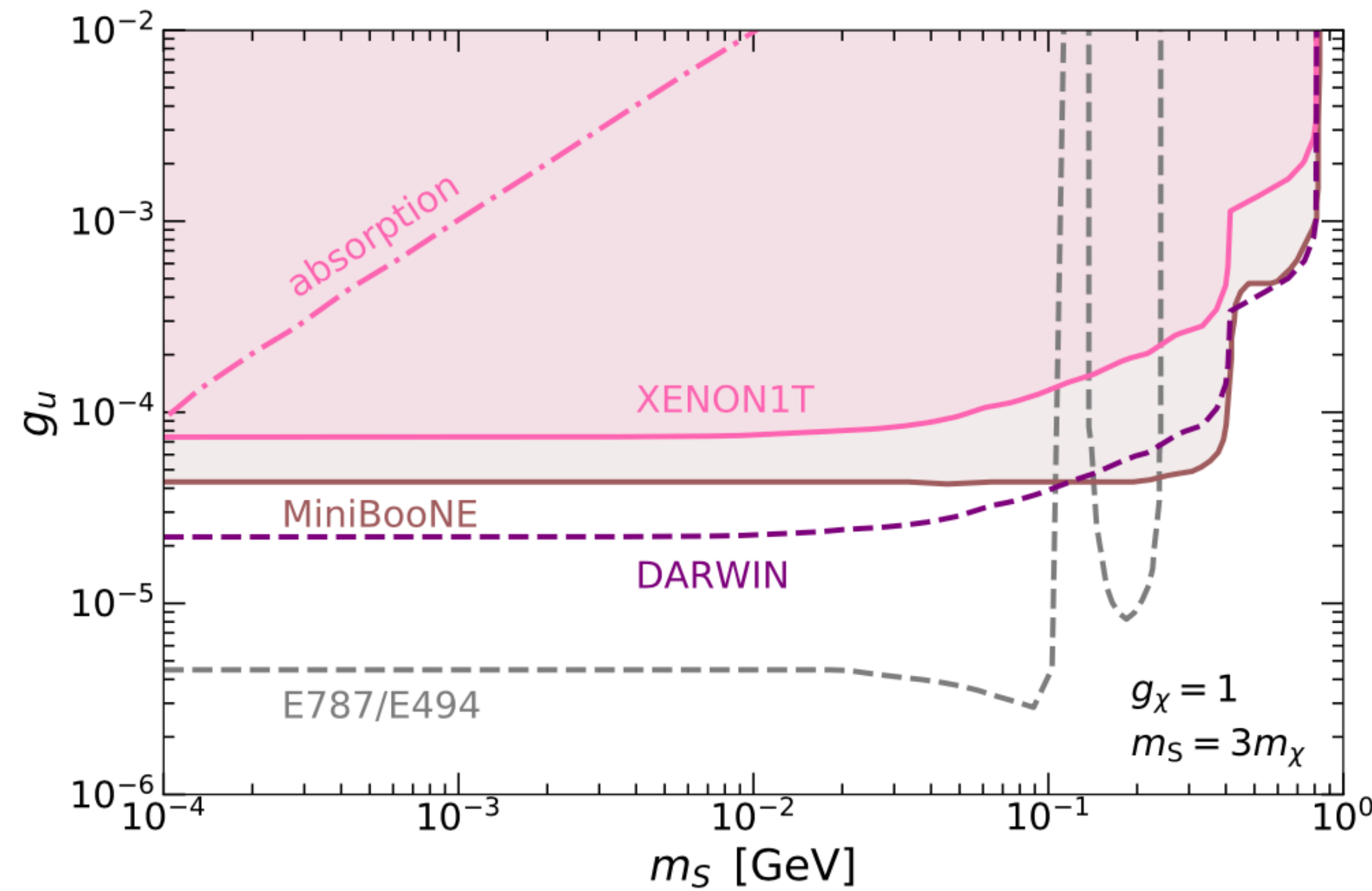




# Hydrophilic dark matter

$$S \rightarrow 2\chi$$

Dark matter scatters at neutrino and dark matter detectors

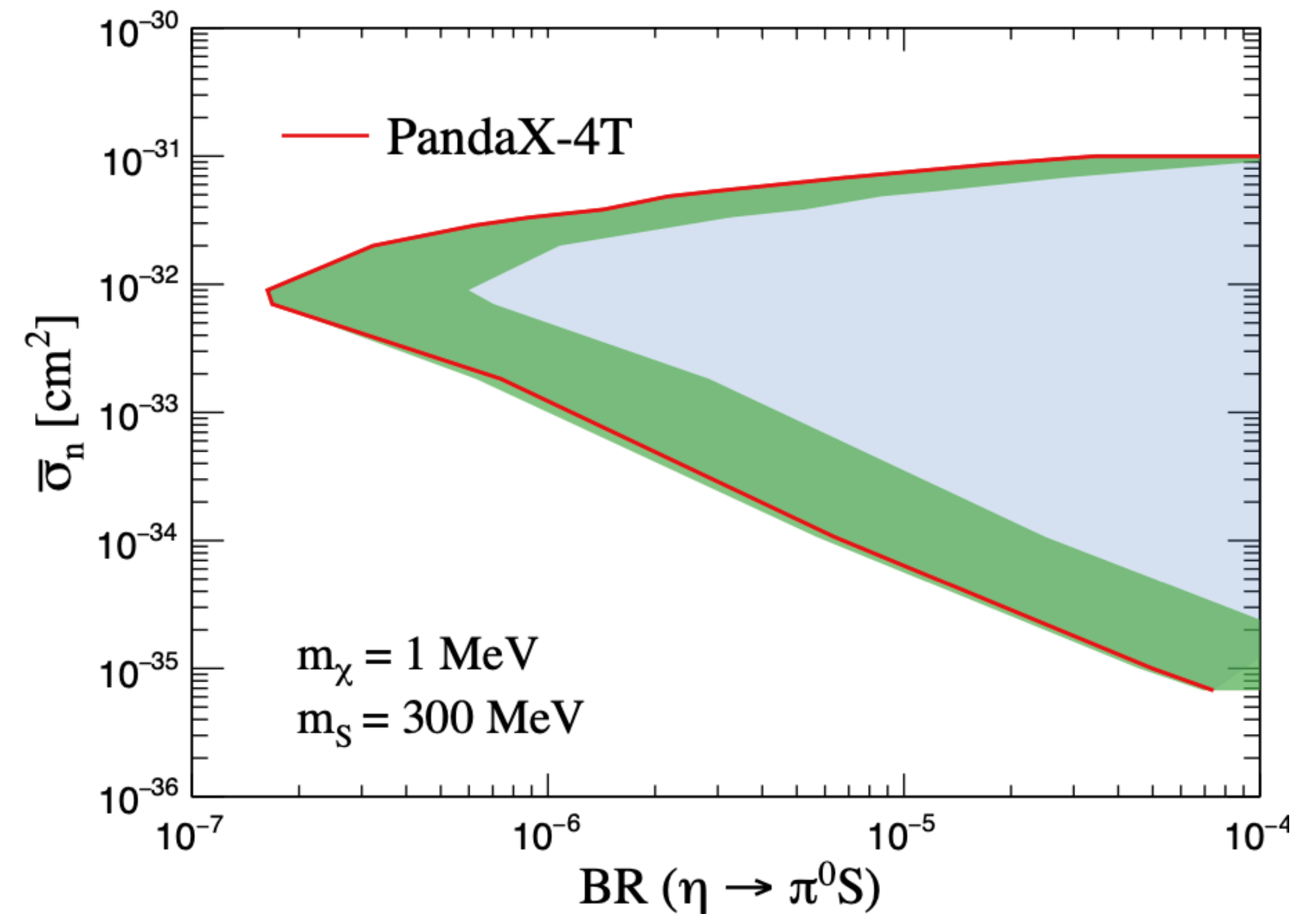
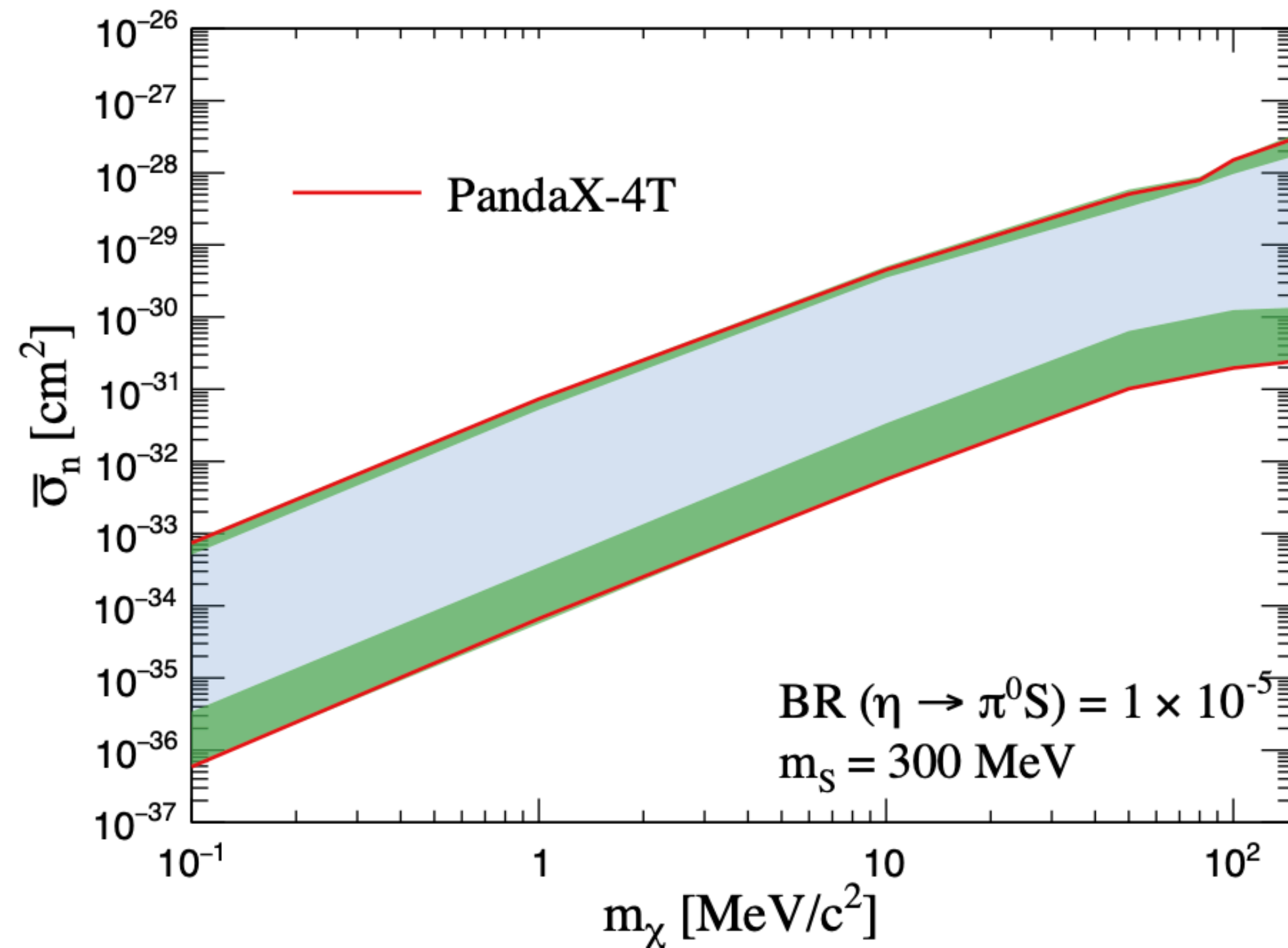


Arguelles et al PLB/2203.12630

# Hydrophilic dark matter

Including both elastic and quasi-elastic scattering in the overburden

$$\chi(k) + A(p_A) \rightarrow \chi(k') + X(\rightarrow n + Y)$$



PandaX PRL/2301.03010

Su et al PRD/2006.11837

# Axion-like particles

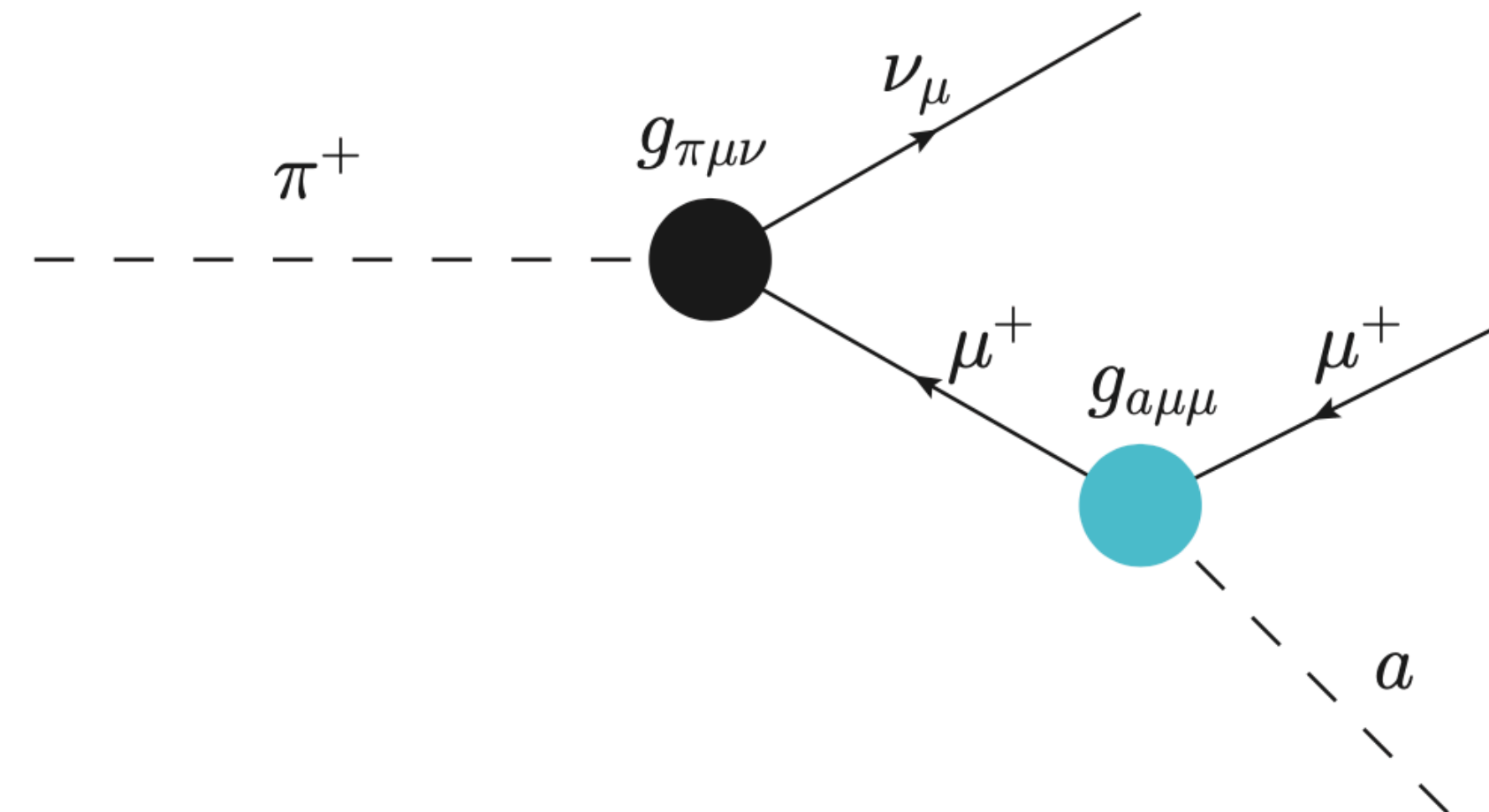
$$\mathcal{L} \supset -ig_{a\mu\mu} a \bar{\mu} \gamma_5 \mu$$

$$\mathcal{L}_{\text{loop}} \supset -\frac{1}{4} g_{a\gamma\gamma}^{\text{eff}} a F^{\mu\nu} \tilde{F}_{\mu\nu}$$

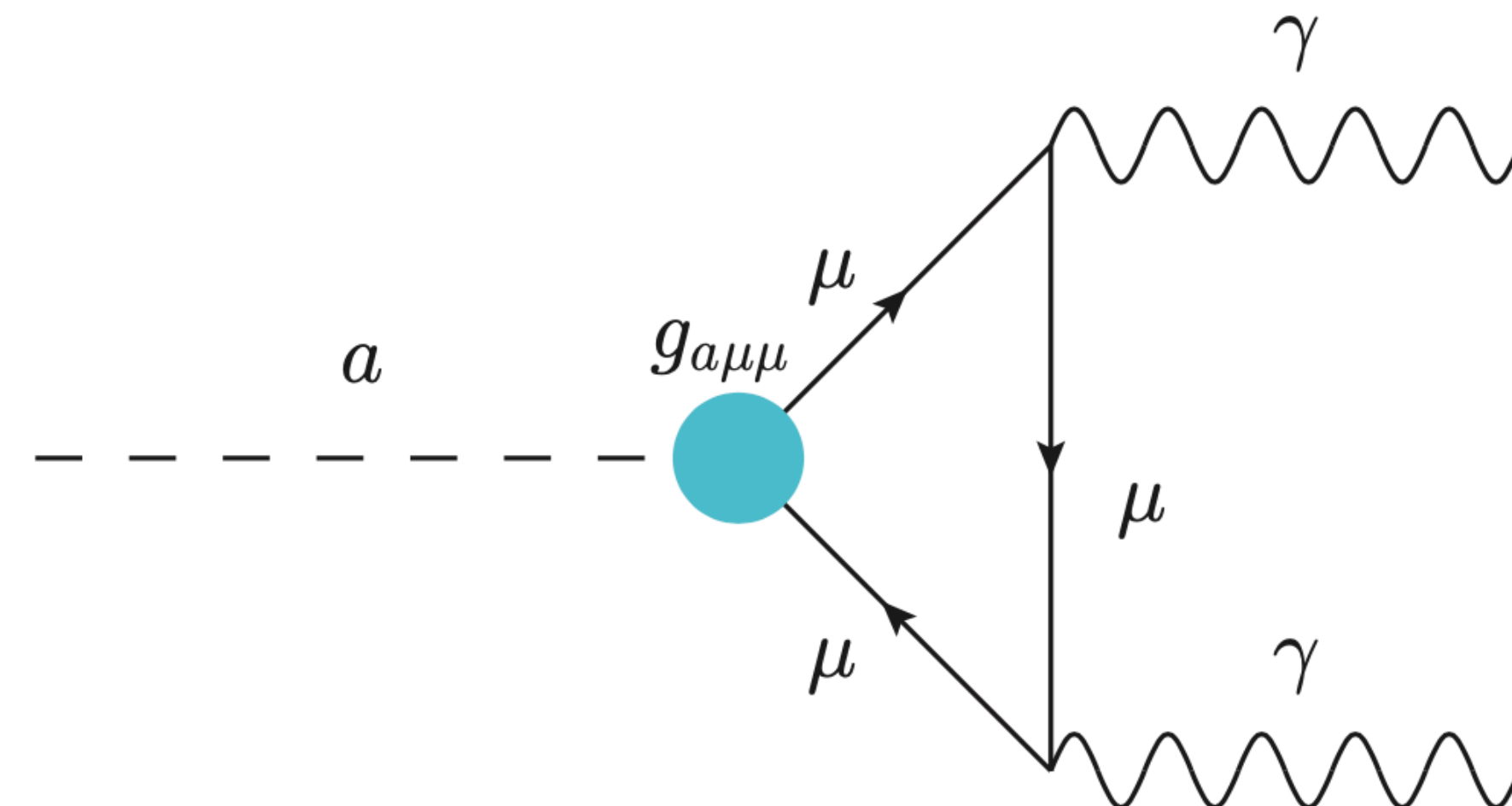
$$g_{a\gamma\gamma}^{\text{eff}} = \frac{g_{a\mu\mu} \alpha}{m_\mu \pi} \left[ 1 - \frac{4m_\mu^2}{m_a^2} \arcsin^2 \left( \frac{m_a}{2m_\mu} \right) \right]$$

$$\tau_a = \Gamma_{a \rightarrow \gamma\gamma}^{-1} = \frac{64\pi}{(g_{a\gamma\gamma}^{\text{eff}})^2 m_a^3}$$

$$\pi^+ \rightarrow \mu^+ + \nu_\mu + a$$



$$m_a < 2m_\mu \quad a \rightarrow \gamma + \gamma$$

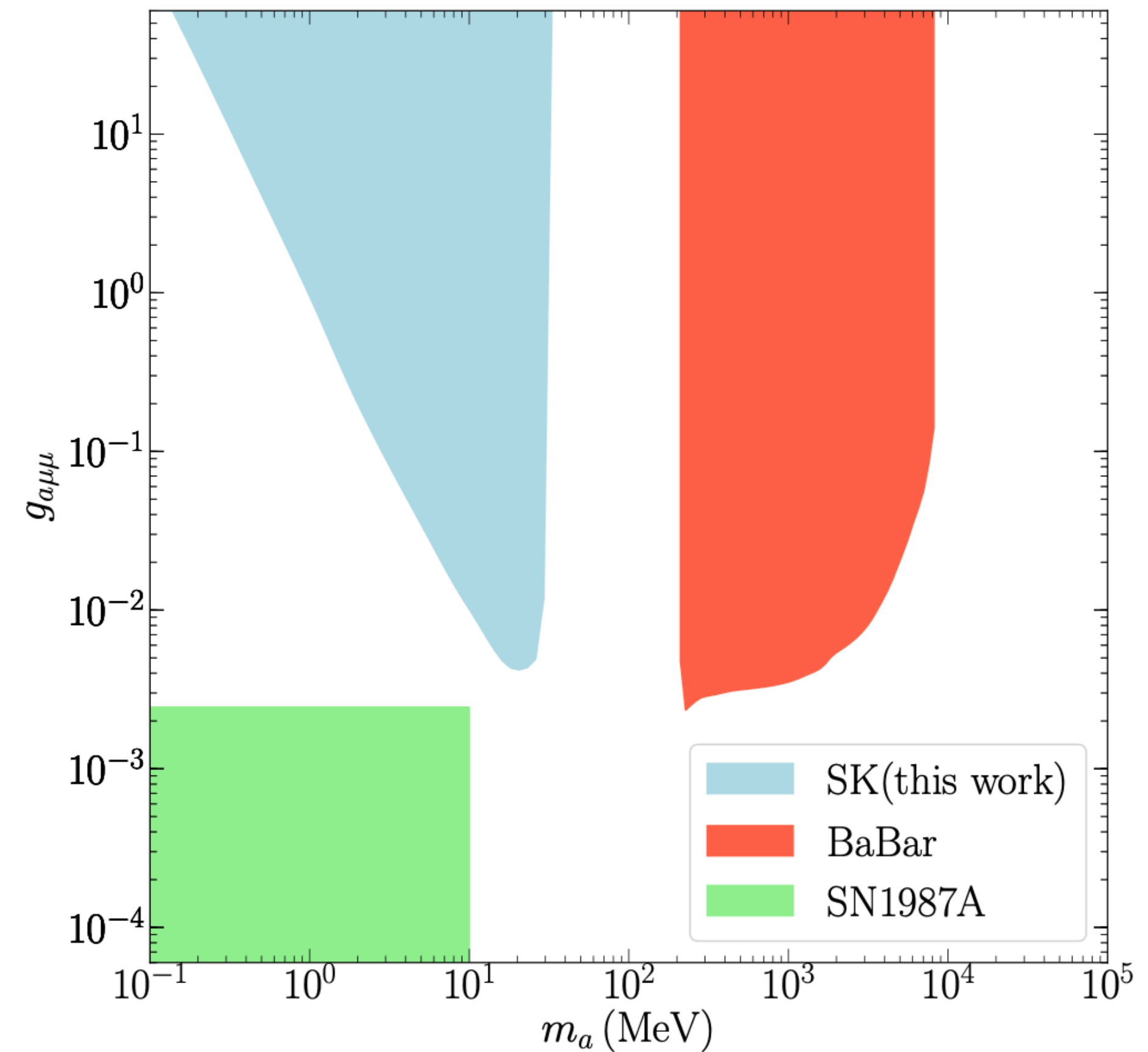
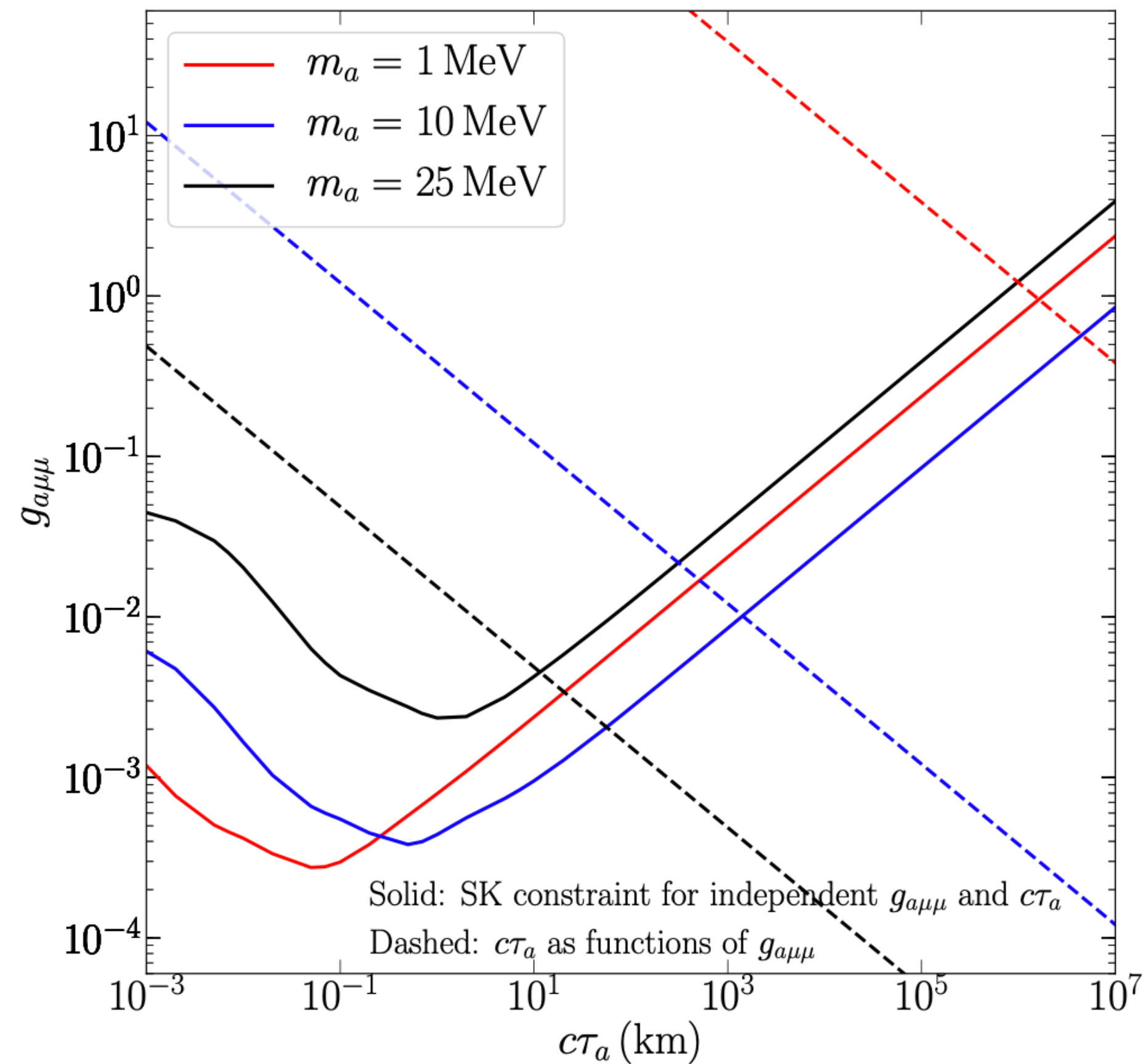




# Axion-like particles

Two electron-like Cherenkov rings at neutrino detectors

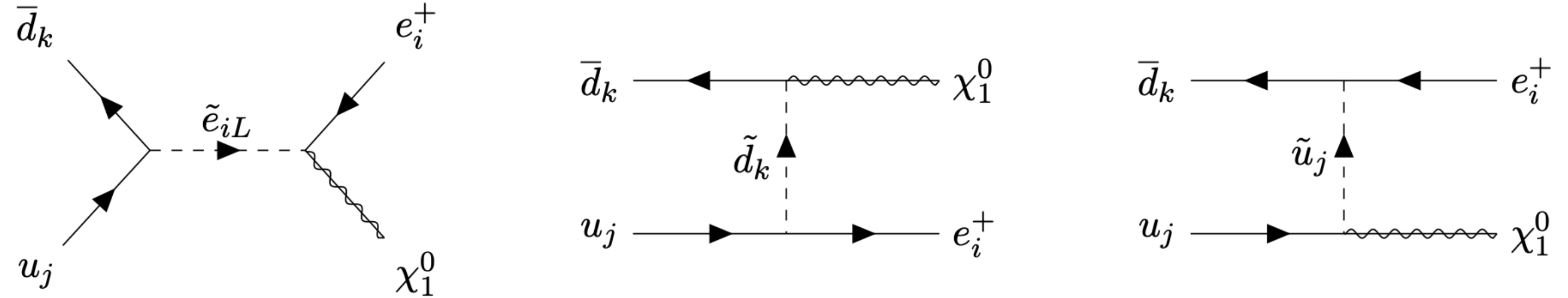
$$a \rightarrow \gamma + \gamma$$



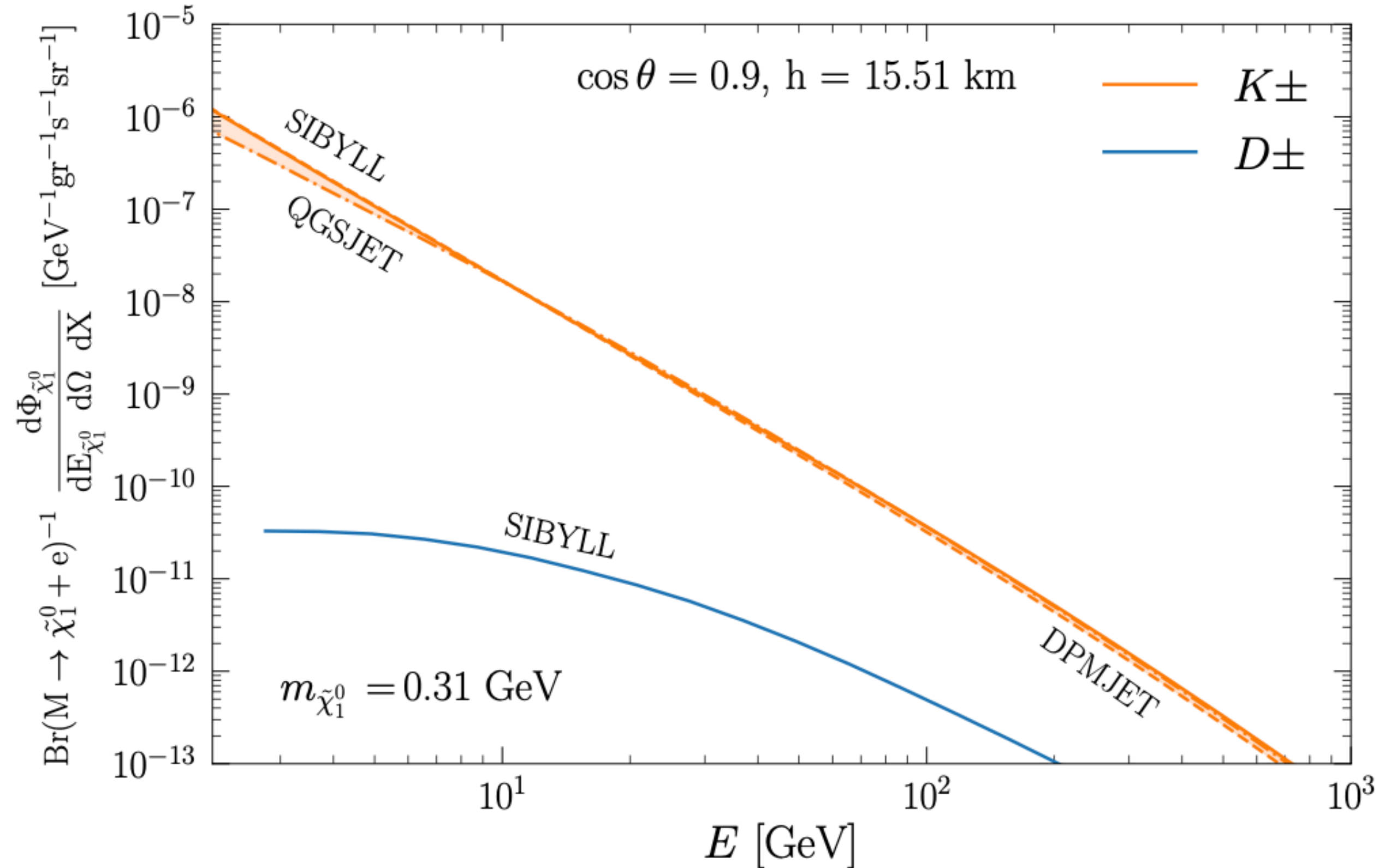
Cheung et al PRD/2208.05111

# Long-lived neutralinos

$$\mathcal{L} \supset \lambda'_{ijk} \hat{L}_i \hat{Q}_j \hat{D}_k^c$$



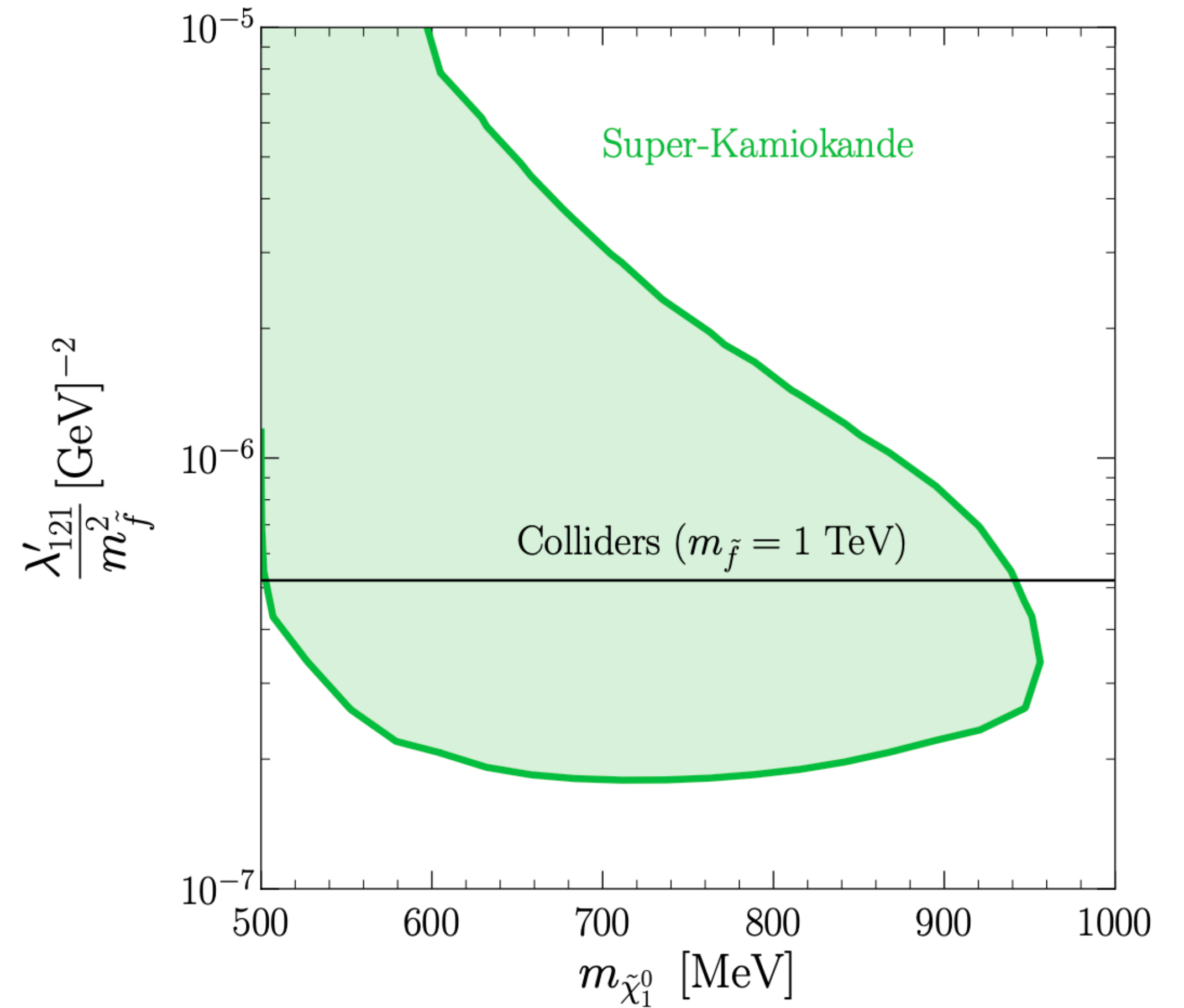
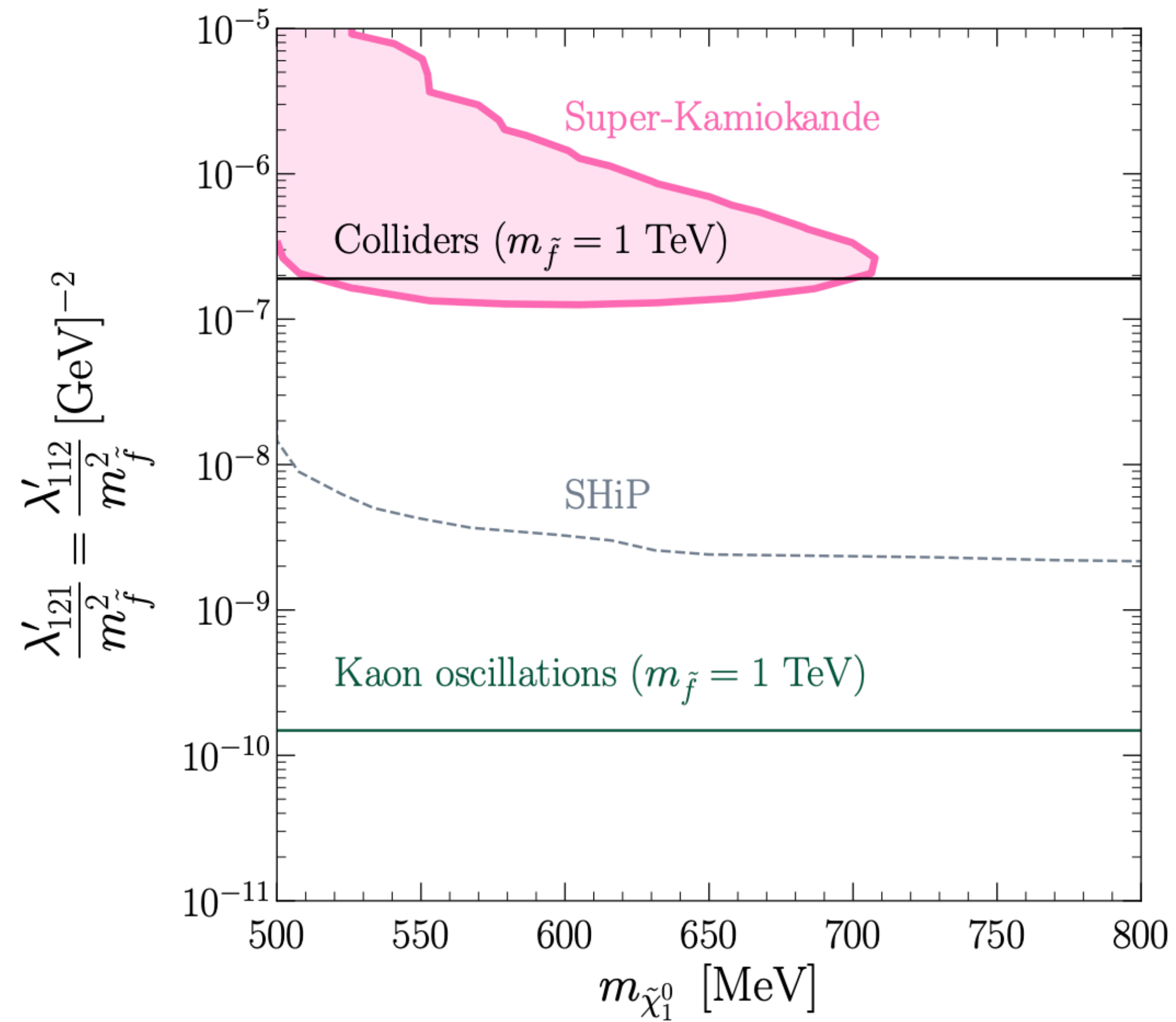
	RPV coupling	Production	Decay mode
<b>B1</b>	$\lambda'_{121}, \lambda'_{112}$	$D^\pm \xrightarrow{\lambda'_{121}} e^\pm + \tilde{\chi}_1^0$	$\tilde{\chi}_1^0 \xrightarrow{\lambda'_{121}} K_S^0 + \nu_e$ $\tilde{\chi}_1^0 \xrightarrow{\lambda'_{121}} K^{*0} + \nu_e$ $\tilde{\chi}_1^0 \xrightarrow{\lambda'_{112}} K^{(*)+} + e^-$ $\tilde{\chi}_1^0 \xrightarrow{\lambda'_{112}} K_S^0 + \nu_e$ $\tilde{\chi}_1^0 \xrightarrow{\lambda'_{112}} K^{*0} + \nu_e$
<b>B2</b>	$\lambda'_{112}, \lambda'_{111}$	$K^\pm \xrightarrow{\lambda'_{112}} e^\pm + \tilde{\chi}_1^0$	$\tilde{\chi}_1^0 \xrightarrow{\lambda'_{111}} \pi^+ + e^-$ $\tilde{\chi}_1^0 \xrightarrow{\lambda'_{111}} \pi^0 + \nu_e$



Cheung et al PRD/2208.05111

# Long-lived neutralinos

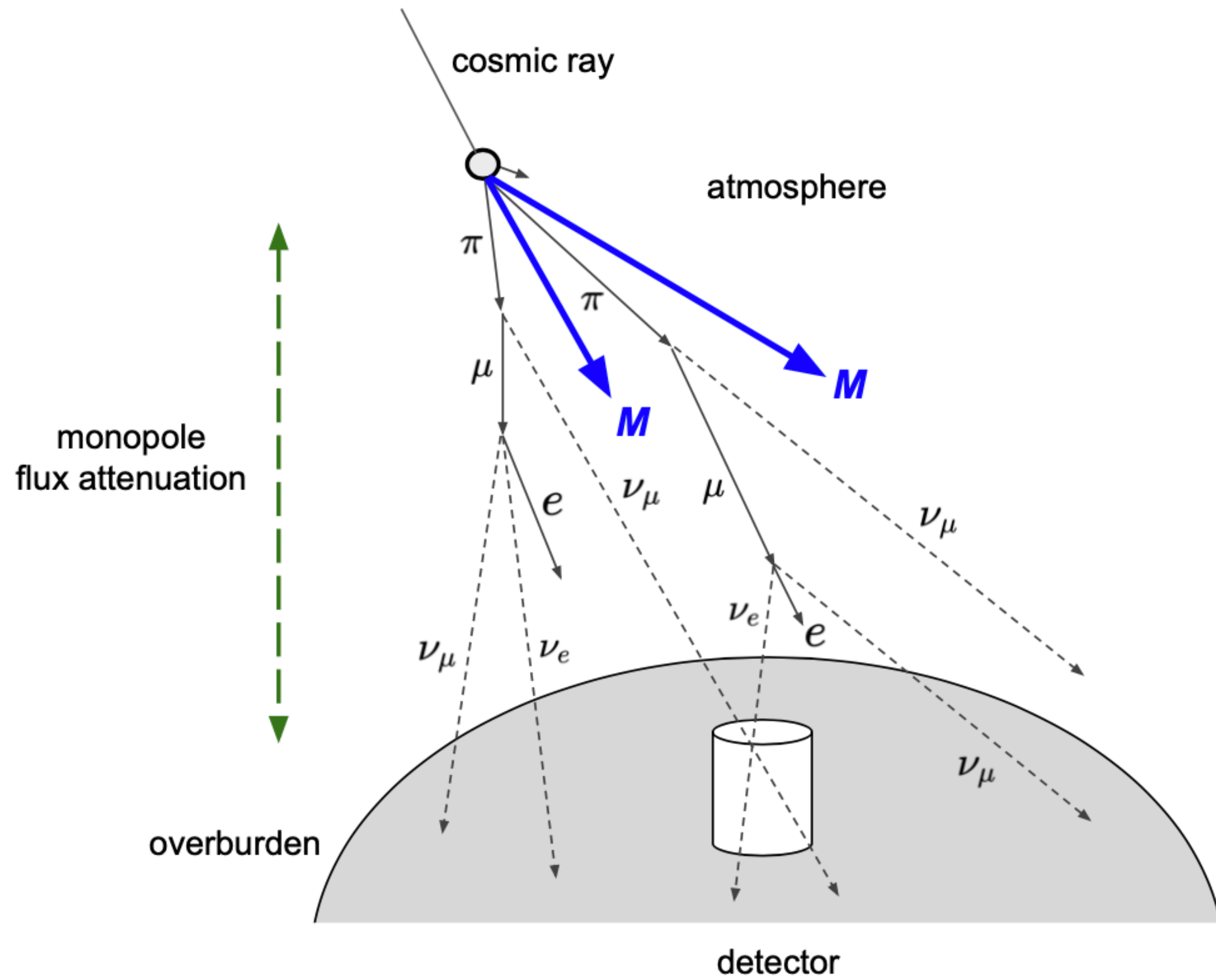
## Benchmark 1



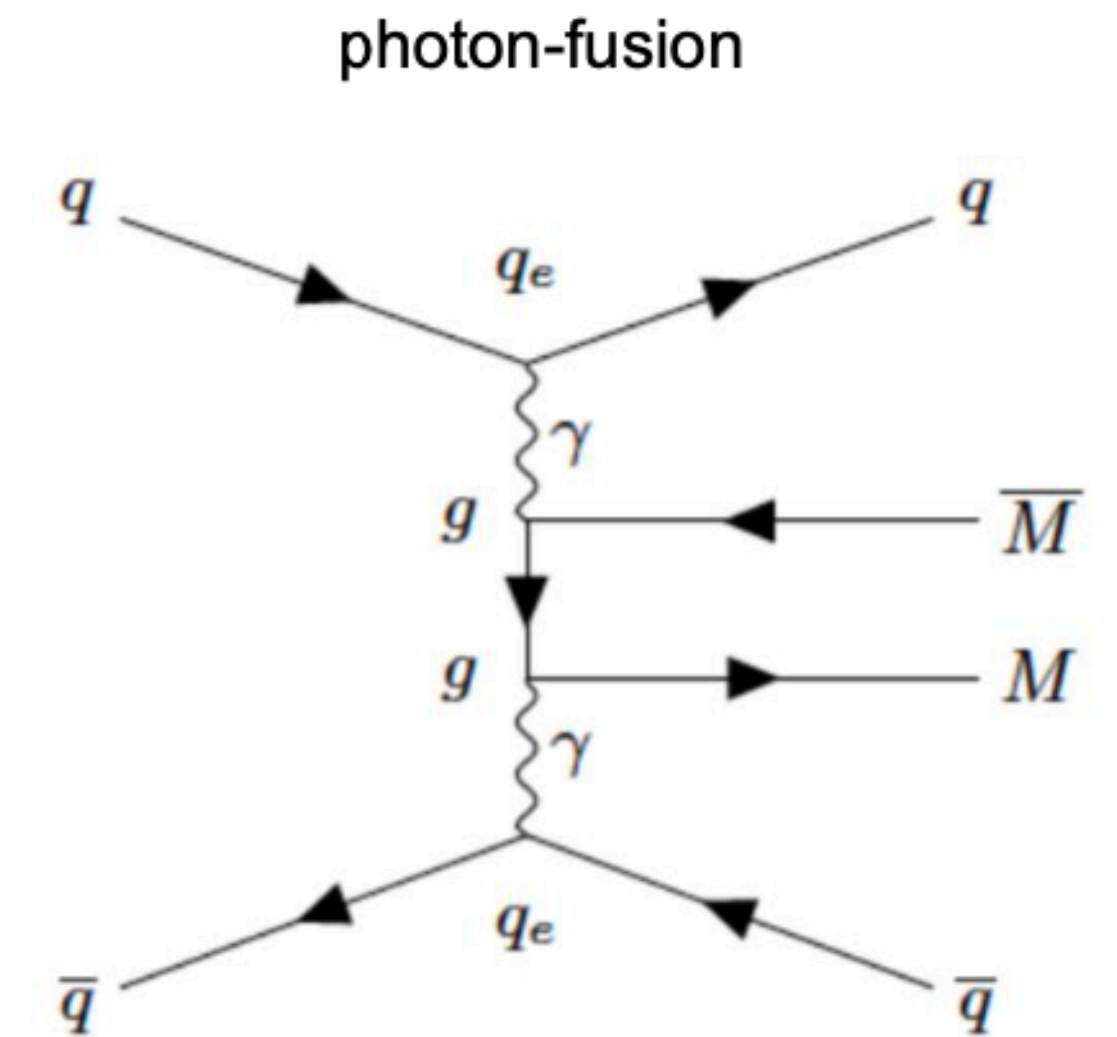
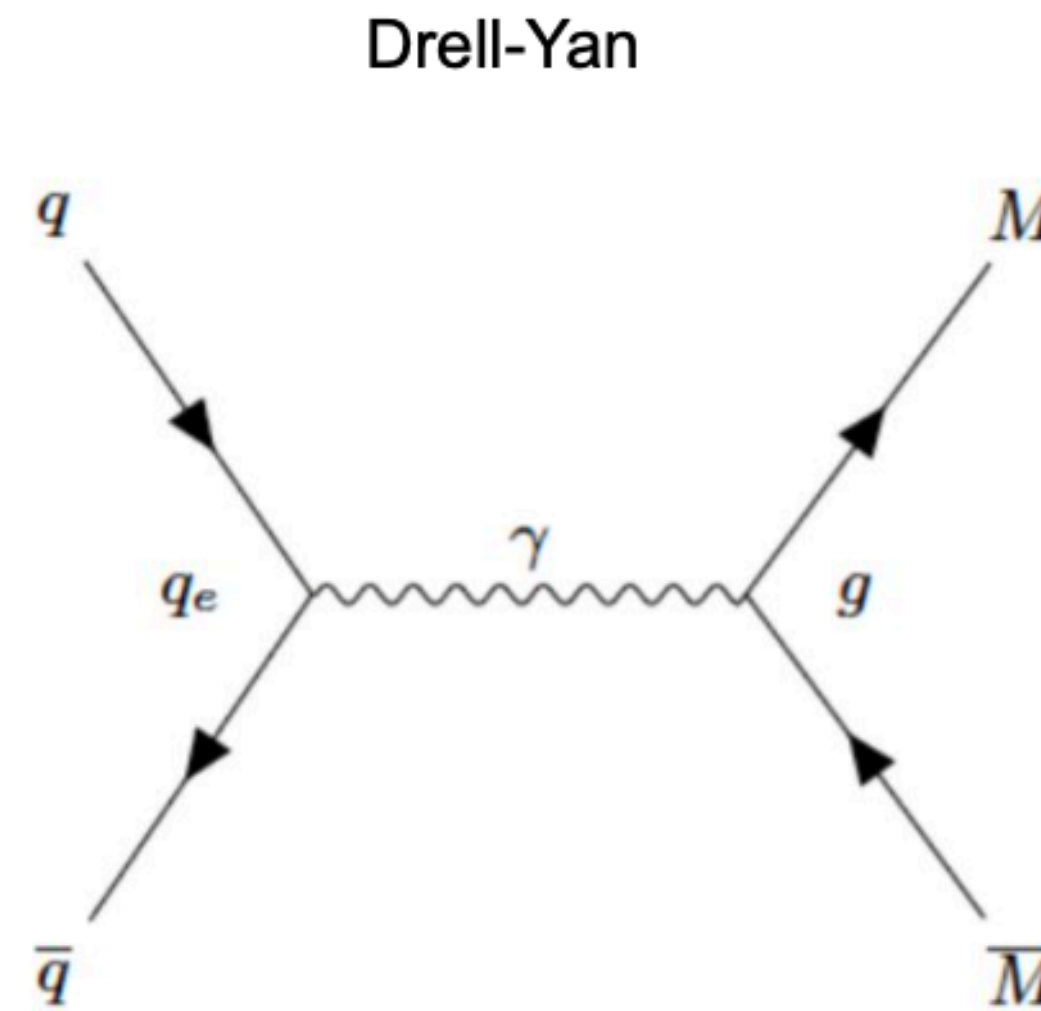
Candia et al PRD/2107.02804



# Magnetic monopoles



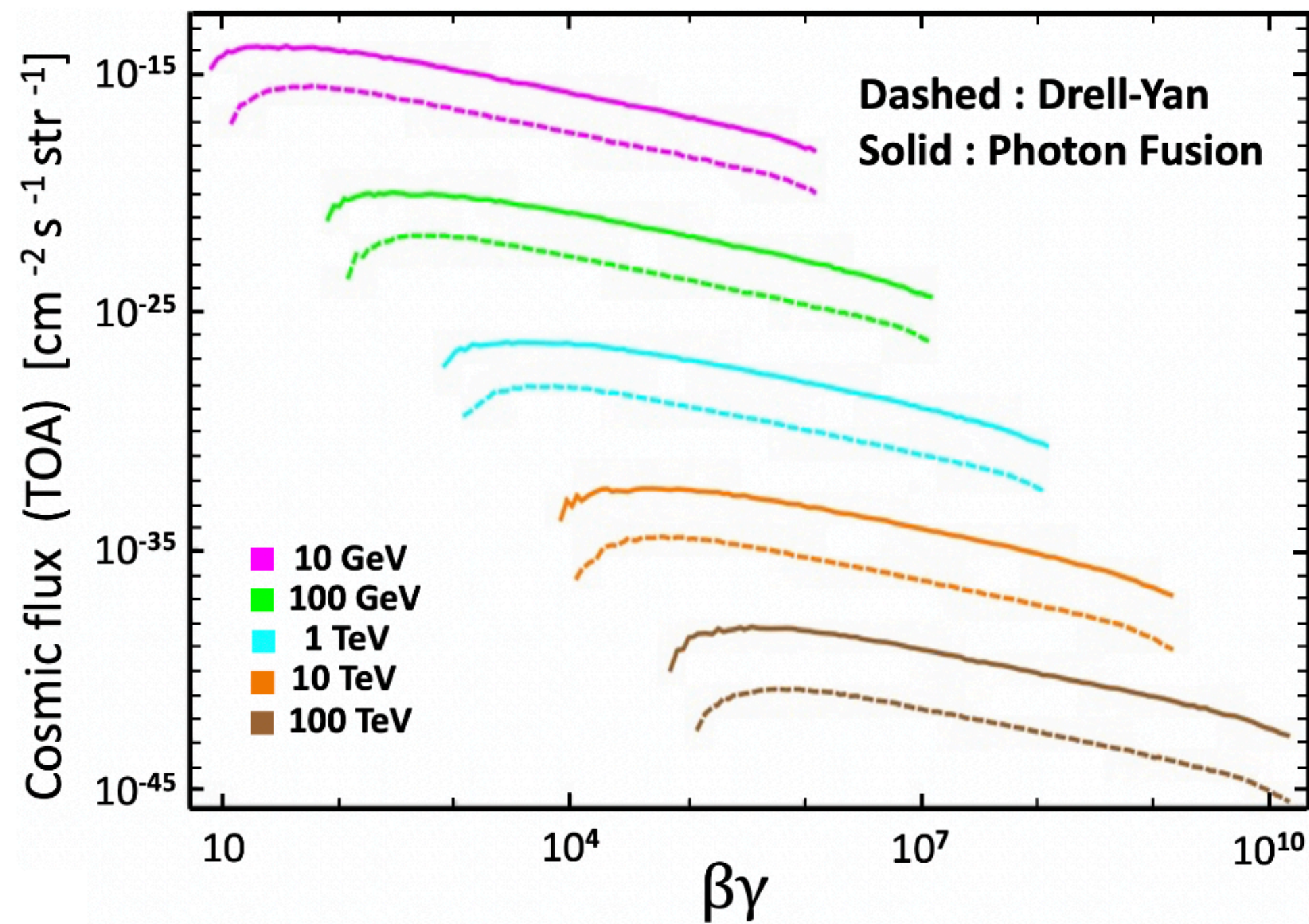
$$\sigma(pp \rightarrow M\bar{M}) = \kappa \times \sigma_{\text{sim}}$$



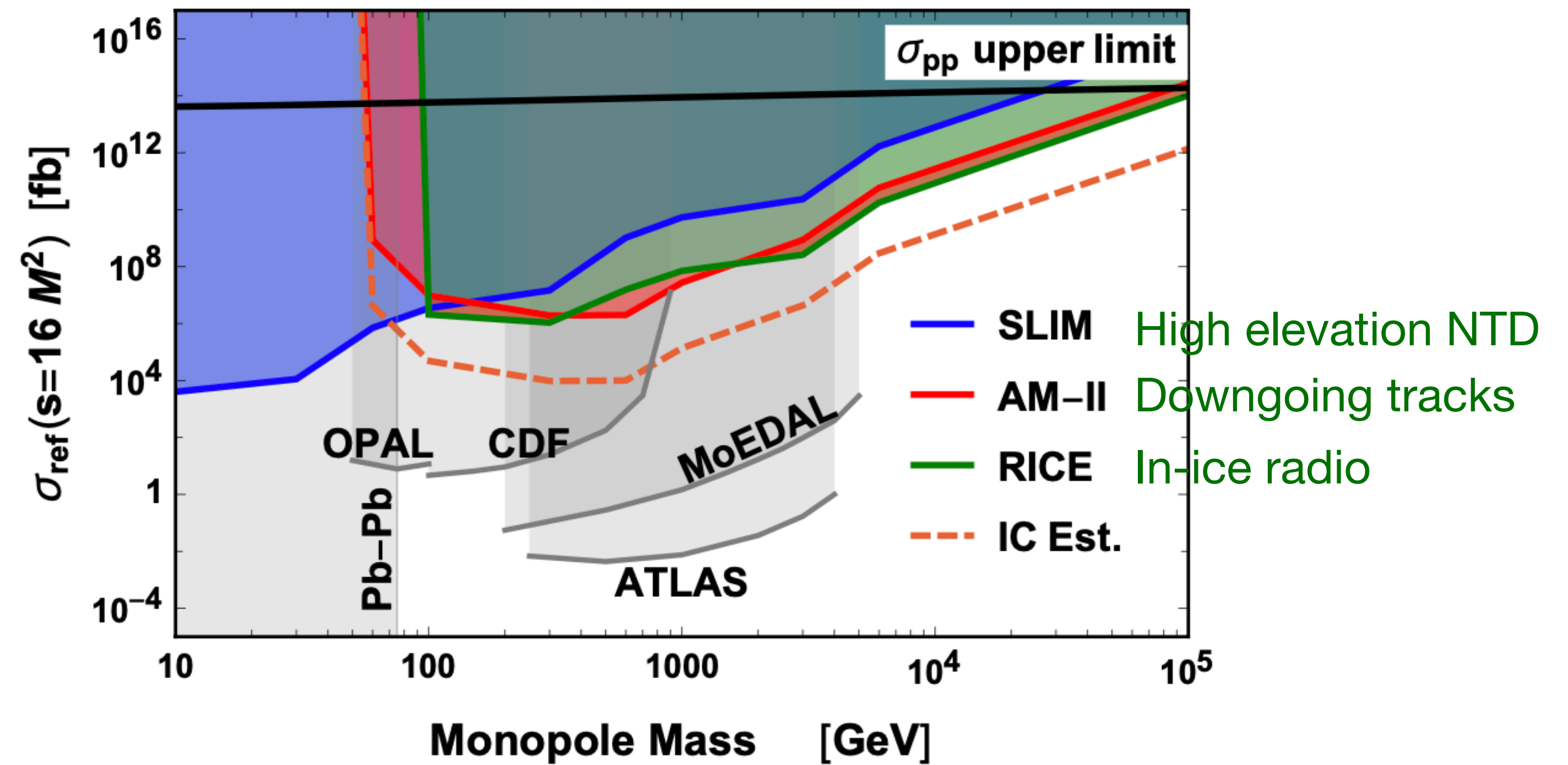
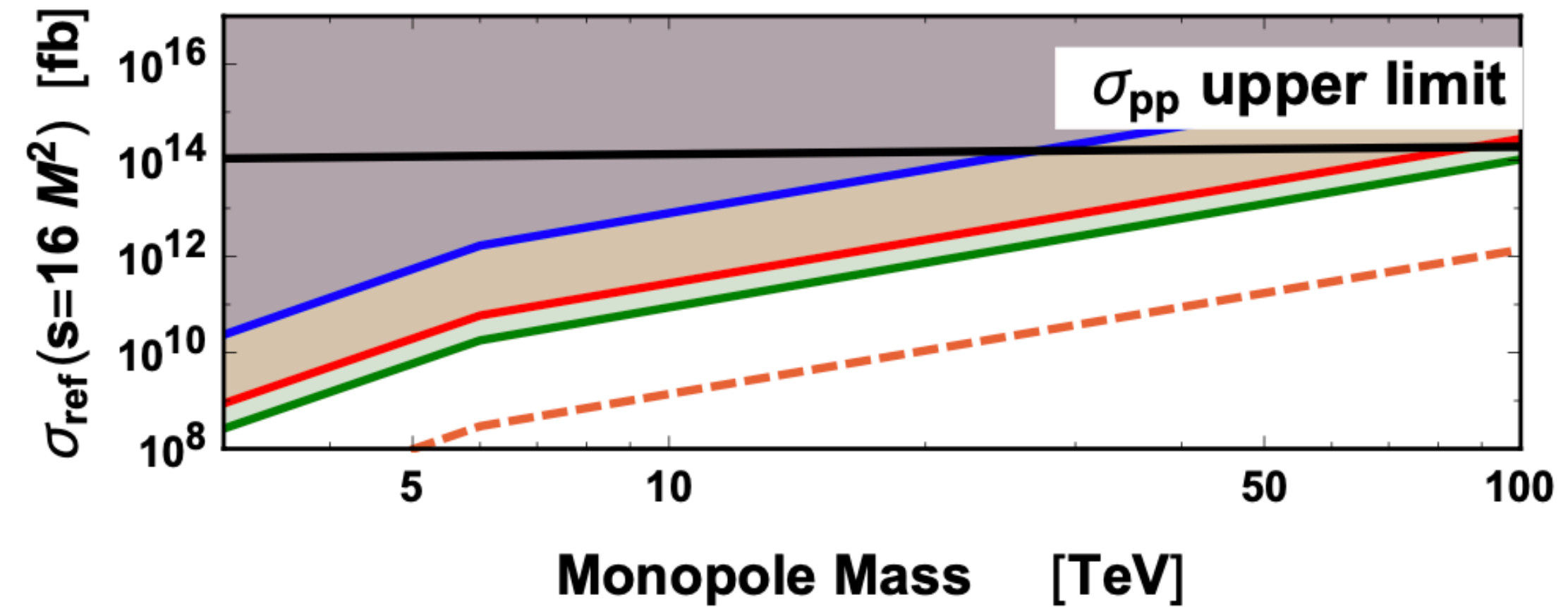
Iguro et al PRL/2111.12091

# Magnetic monopoles

$$\sigma(pp \rightarrow M\bar{M}) = \kappa \times \sigma_{\text{sim}}$$



Iguro et al PRL/2111.12091



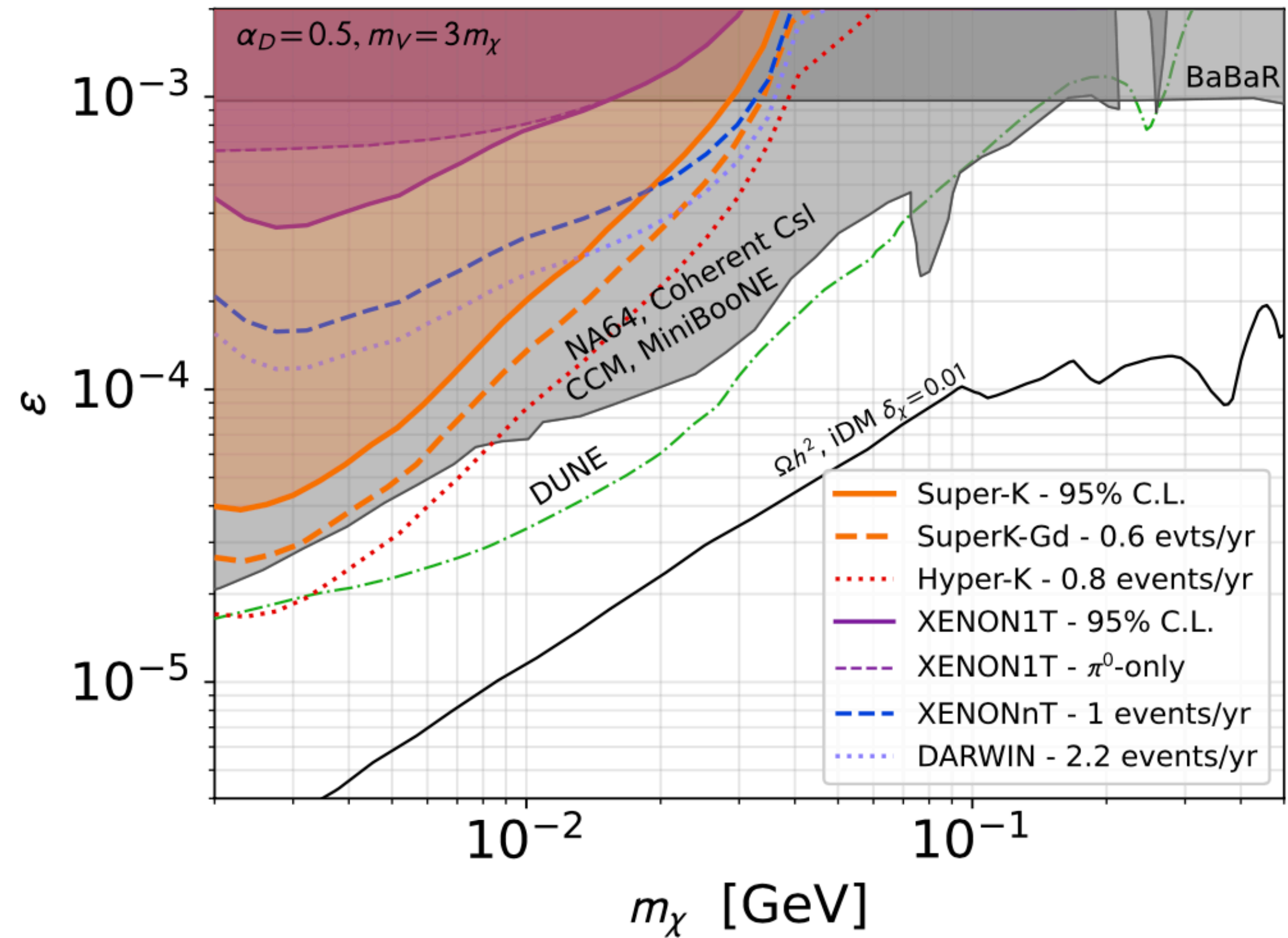
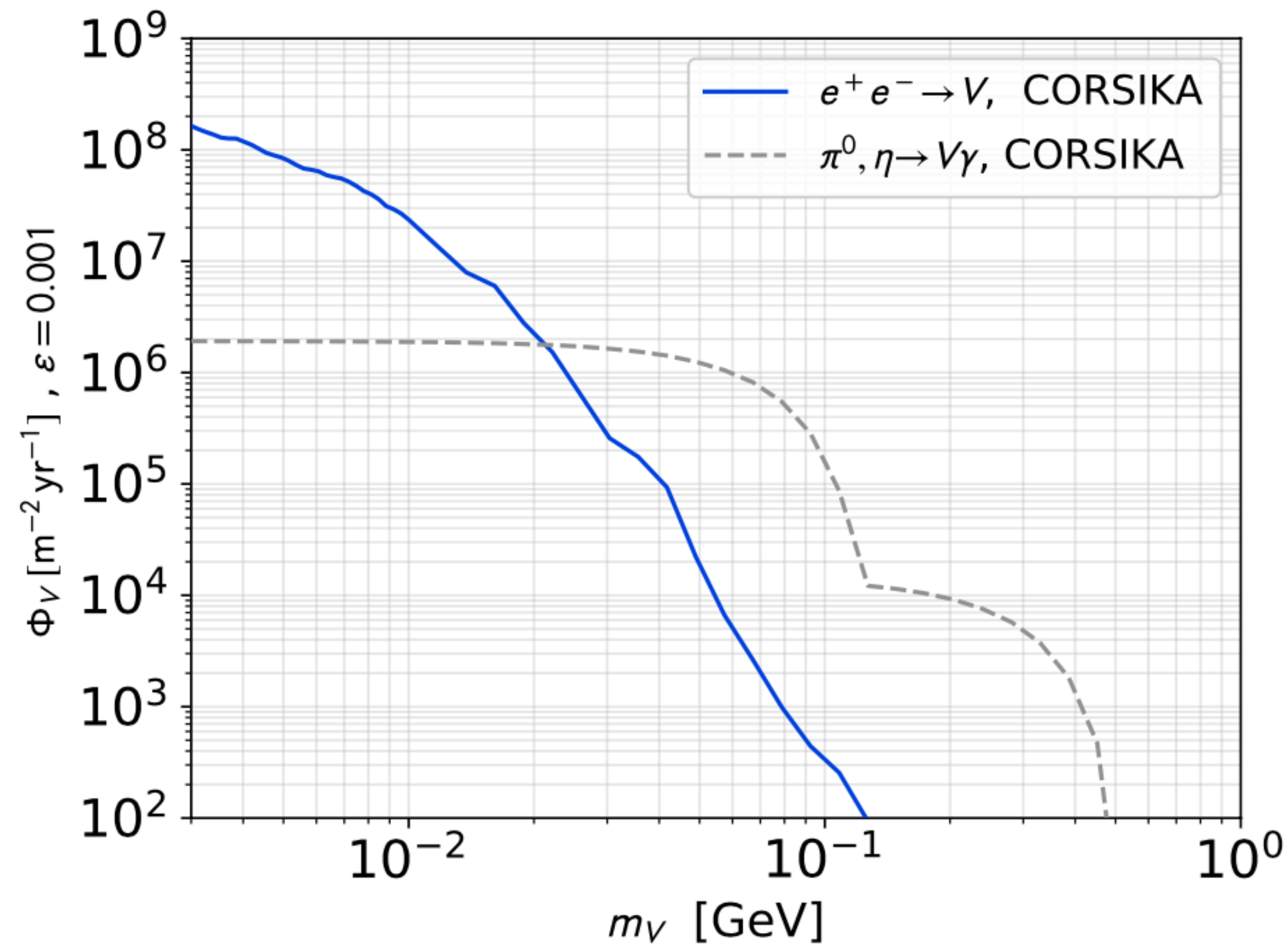


# Dark photon

$$\mathcal{L} \supset -V_\mu (e\varepsilon \mathcal{J}_{\text{em}}^\mu + g_D \mathcal{J}_D^\mu)$$

$$\mathcal{J}_D^\mu = -i \bar{\chi}_2 \gamma^\mu \chi_1$$

$$\sigma_{\text{res}} = \frac{2\pi^2 \varepsilon^2 \alpha_{\text{em}}}{m_e} \delta(E_+ - \frac{m_V^2}{2m_e}) \equiv \tilde{\sigma}_{\text{res}} \delta(E_+ - E_{\text{res}})$$





# Millicharge particles from light meson decay

$$\Phi_{\chi}(\gamma_{\chi}) = 2 \sum_{\mathbf{m}} \text{BR}(\mathbf{m} \rightarrow \chi\bar{\chi}) \int d\gamma_{\mathbf{m}} \Phi_{\mathbf{m}}(\gamma_{\mathbf{m}}) P(\gamma_{\chi}|\gamma_{\mathbf{m}})$$

Vector mesons  $\rho, \omega, \phi, J/\psi$  decay to MCP pairs

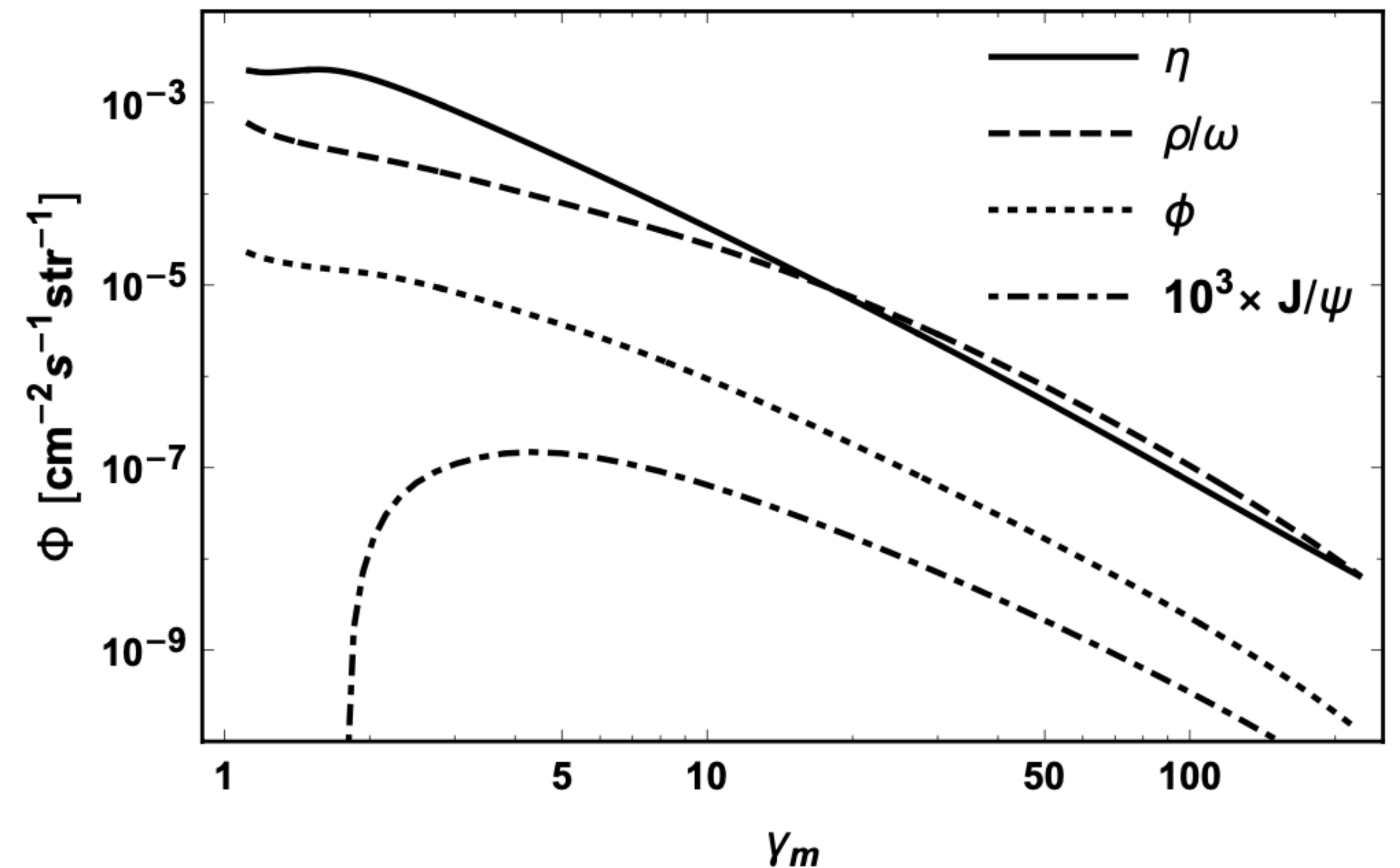
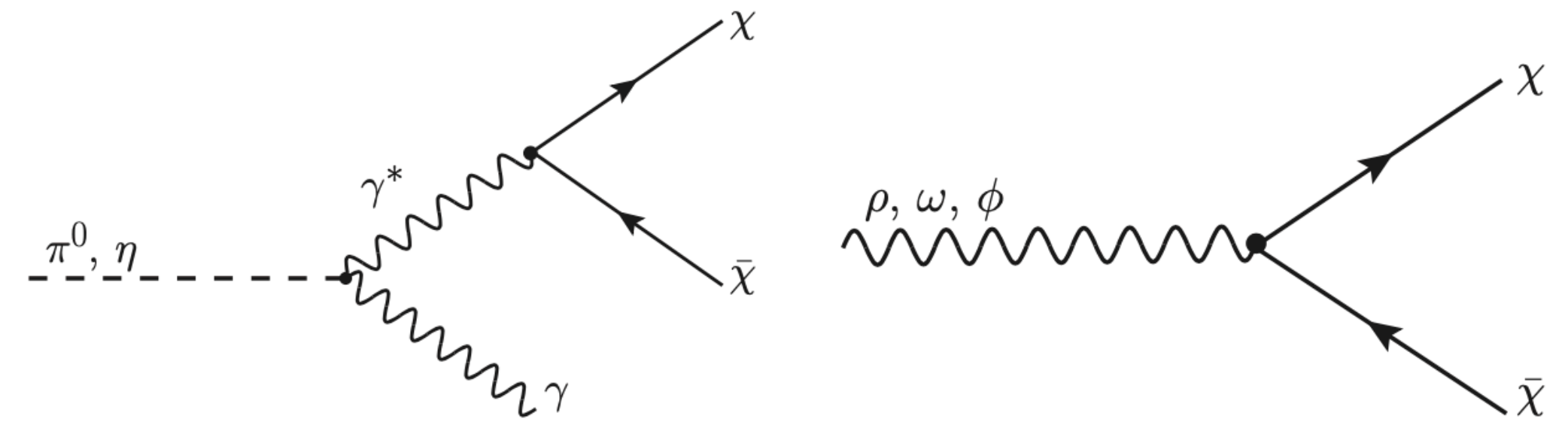
$$\frac{\text{BR}(\mathbf{m} \rightarrow \chi\bar{\chi})}{\text{BR}(\mathbf{m} \rightarrow \mu^+\mu^-)} = \epsilon^2 \sqrt{\frac{m_{\mathbf{m}}^2 - 4m_{\chi}^2}{m_{\mathbf{m}}^2 - 4m_{\mu}^2}}$$

$$P(E_{\chi}|E_{\mathbf{m}}) = \frac{1}{\Gamma_{\mathbf{m}}} \frac{d\Gamma_{\mathbf{m}}}{dE_{\chi}} = \frac{1}{E_{\chi}^+ - E_{\chi}^-}$$

$\eta$  decay to MCP pairs+photon

$$\text{BR}(\eta \rightarrow \gamma\chi\chi) = 2\epsilon^2\alpha\text{BR}(\eta \rightarrow \gamma\gamma)I^{(3)}\left(\frac{m_{\chi}^2}{m_{\eta}^2}\right)$$

$$\frac{1}{\Gamma_{\eta}} \frac{d\Gamma_{\eta}}{dz} = \frac{m_{\eta} - z}{72z^3 F_1(m_{\chi})} F_2(z, m_{\chi})$$

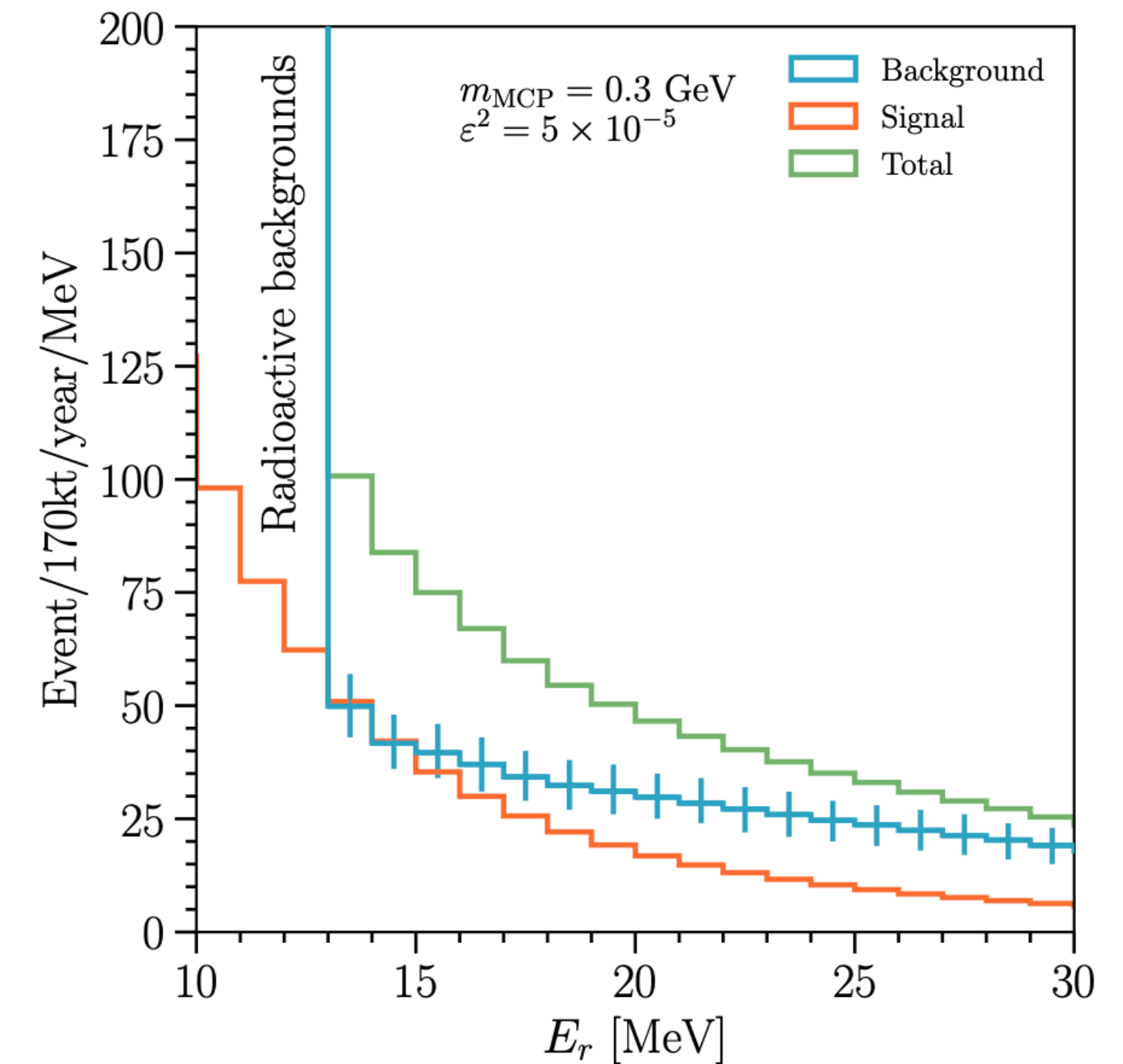
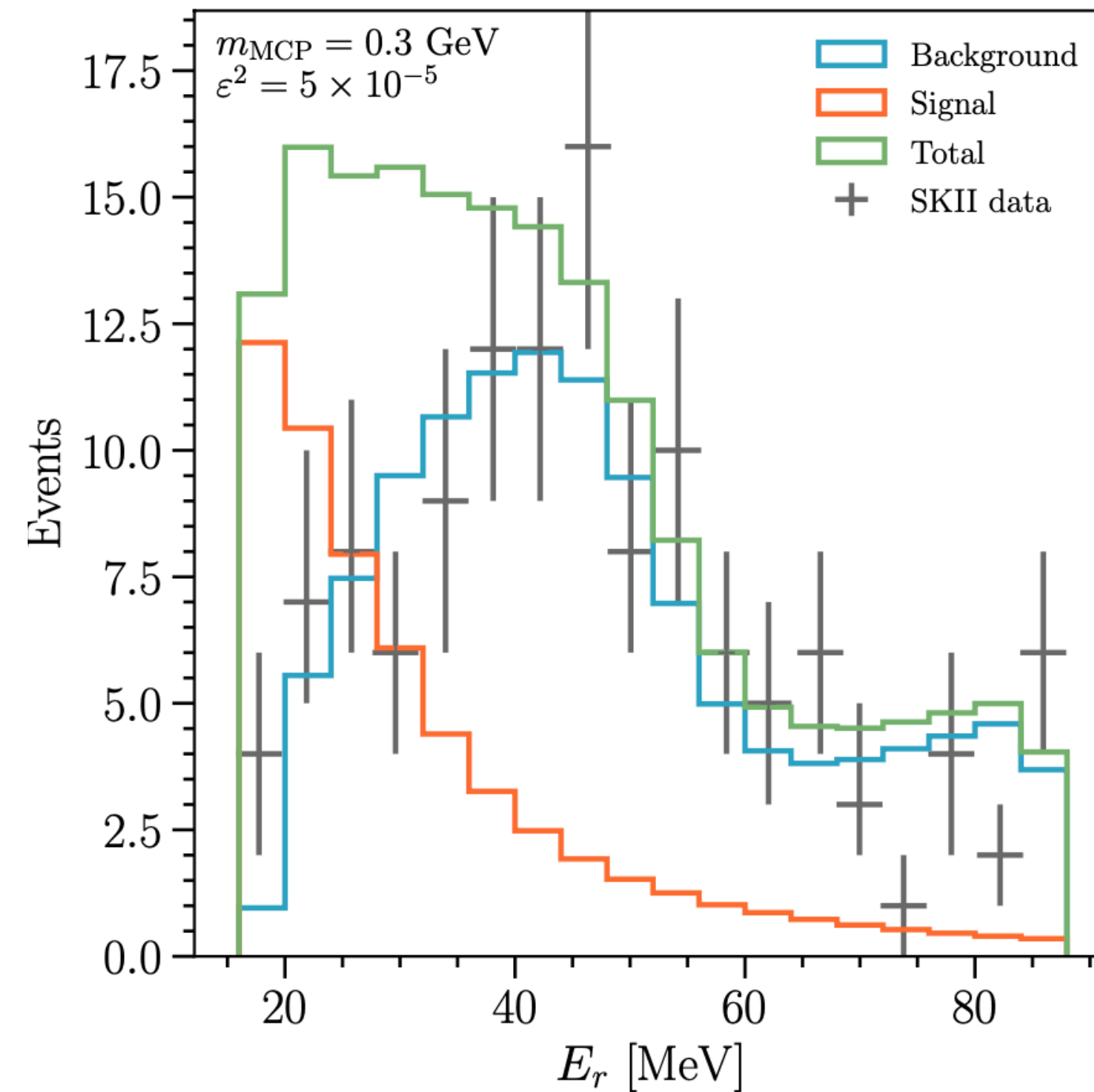


# Single scatter

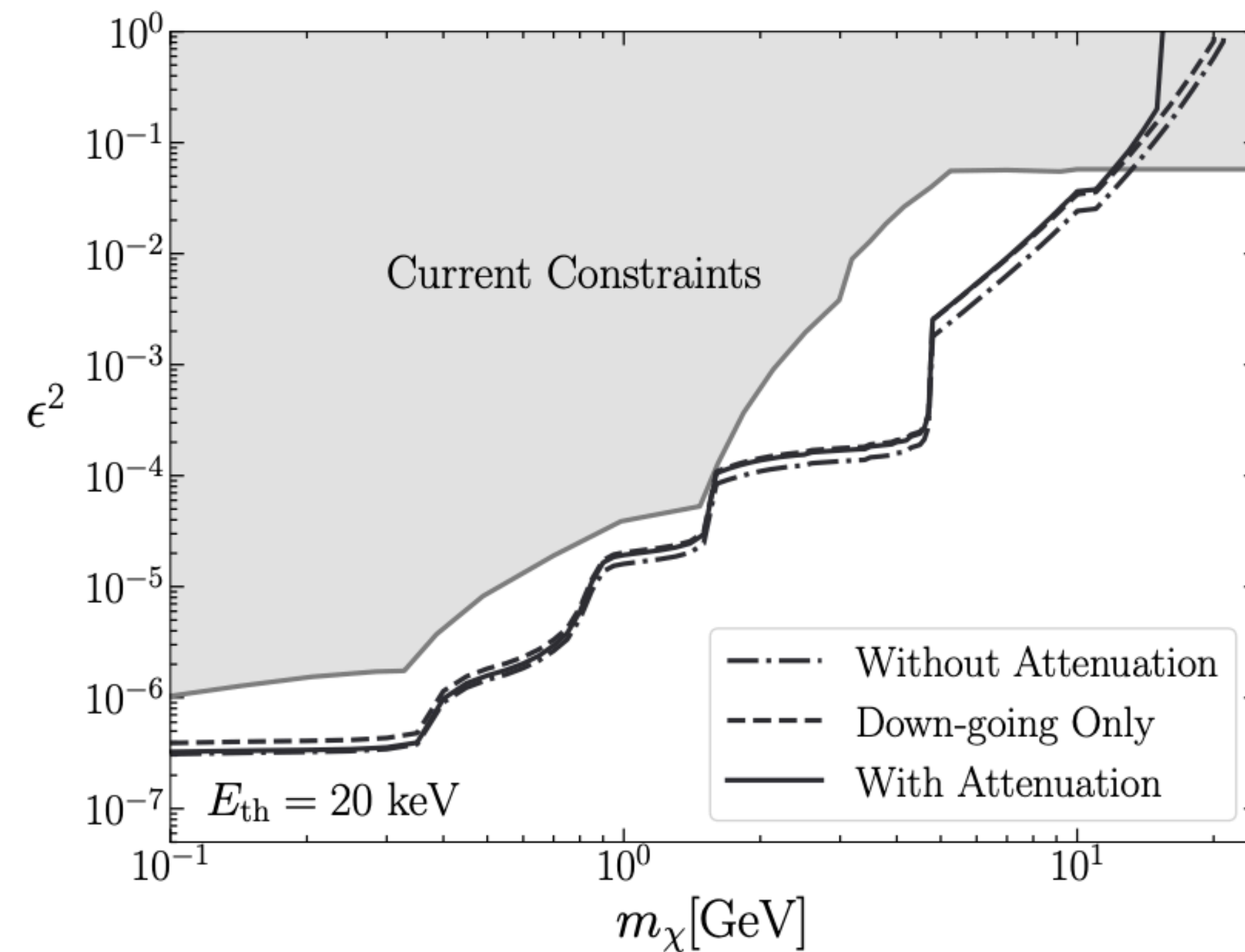
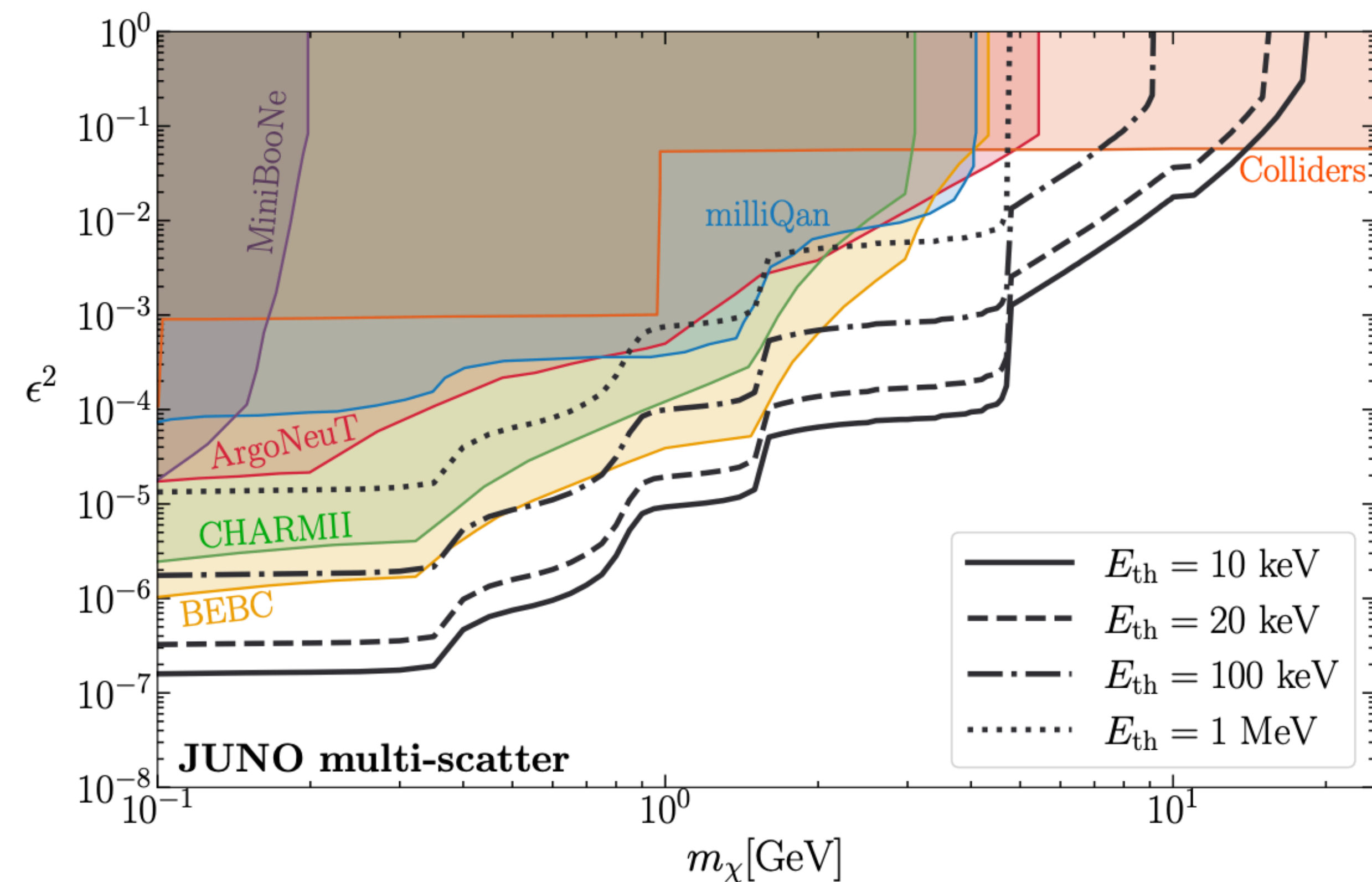
Elastic scattering 
$$\frac{d\sigma_{\chi e}}{dE_r} = \pi\epsilon^2\alpha^2 \frac{(E_r^2 + 2E_\chi^2)m_e - ((2E_\chi + m_e)m_e + m_\chi^2) E_r}{E_r^2 m_e^2 (E_\chi^2 - m_\chi^2)}$$

$$d\sigma_{\chi e}/dE_r \propto 1/E_r^2 \quad \sigma_{\chi e} \simeq \frac{\pi\alpha_{EM}\epsilon^2}{m_e T_{\min}} = 2.6 \times 10^{-25} \epsilon^2 \text{ cm}^2 \frac{\text{MeV}}{T_{\min}}$$

$$N_i(m_\chi, \epsilon) = N_e T \int_{E_{i,\min}}^{E_{i,\max}} dE_r \epsilon_D(E_r) \times \int dE_\chi d\Omega \Phi_\chi^D(E_\chi, \Omega) \frac{d\sigma_{\chi e}}{dE_r}$$



# Multiple scatter constraint



Assuming JUNO 170 kton·yr exposure

Wu, Hardy, **NS**, arXiv: 2406.01668



# Degeneracies at the high energy neutrino sources

Production	Source flavor ratio	Earth flavor ratio $\nu + \bar{\nu}$	Earth flavor ratio	$f_{\bar{\nu}_e}$
$pp$	$\{1, 1\} : \{2, 2\} : \{0, 0\}$	$0.33 : 0.34 : 0.33$	$\{0.17, 0.17\} : \{0.17, 0.17\} : \{0.16, 0.16\}$	0.17
$pp \mu$ damped	$\{0, 0\} : \{1, 1\} : \{0, 0\}$	$0.23 : 0.39 : 0.38$	$\{0.11, 0.11\} : \{0.20, 0.20\} : \{0.19, 0.19\}$	0.11
$p\gamma$	$\{1, 0\} : \{1, 1\} : \{0, 0\}$	$0.33 : 0.34 : 0.33$	$\{0.26, 0.08\} : \{0.21, 0.13\} : \{0.20, 0.13\}$	0.08
$p\gamma \mu$ damped	$\{0, 0\} : \{1, 0\} : \{0, 0\}$	$0.23 : 0.39 : 0.38$	$\{0.23, 0.00\} : \{0.39, 0.00\} : \{0.38, 0.00\}$	0

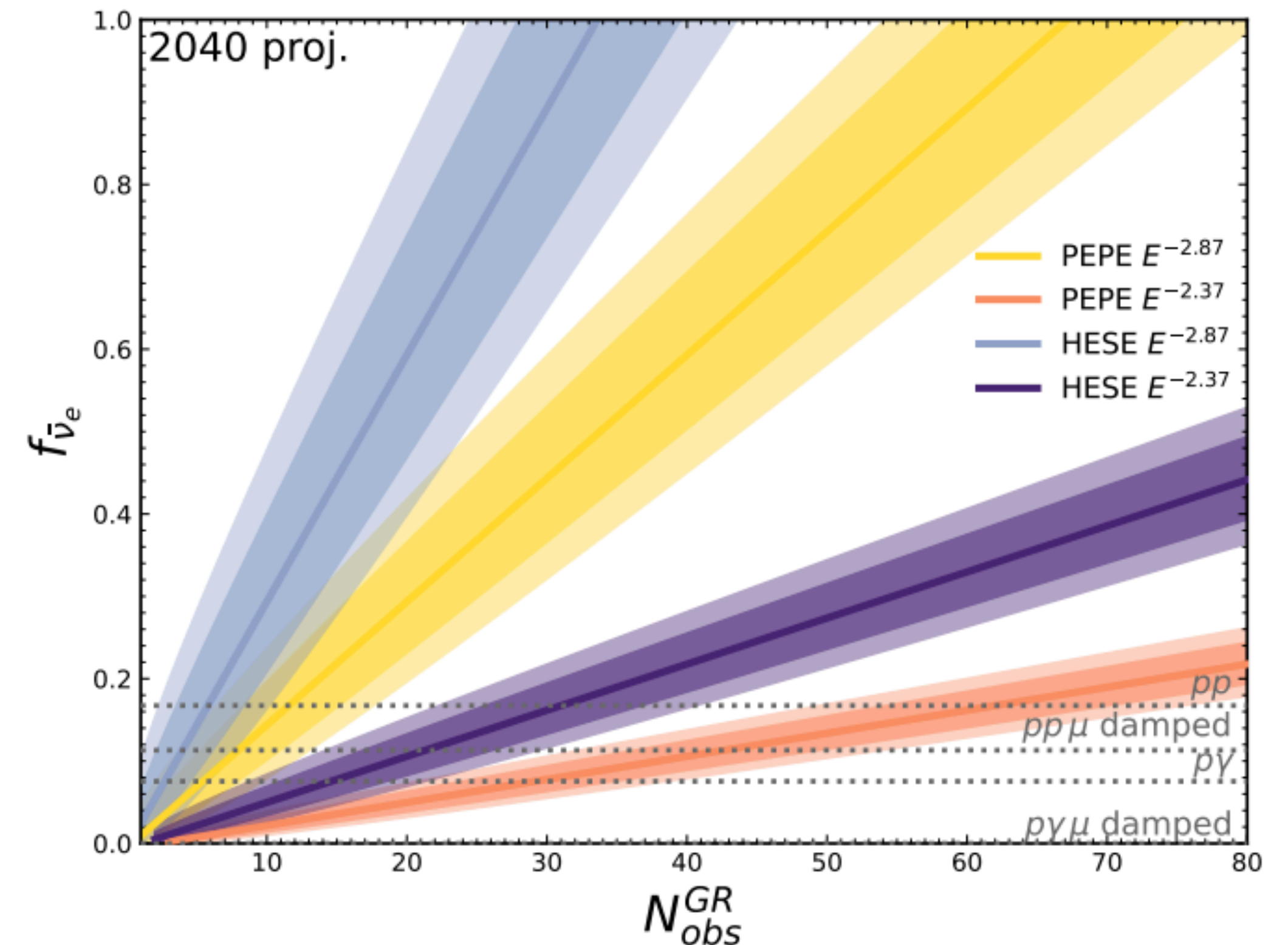
- ▶  $p\gamma$  produces **more neutrinos than antineutrinos**  $p + \gamma \rightarrow \Delta^+ \rightarrow \pi^+ + n$ , if  $\mu$  damped, no antineutrinos are produced
- ▶  $pp$  produces **equal amount of neutrinos and antineutrinos**  $p + p \rightarrow n_\pi [\pi^0 + \pi^+ + \pi^-]$ , which holds even if  $\mu$  damped
- ▶  $pp$  is **indistinguishable** from  $p\gamma$  if only  $\nu + \bar{\nu}$  is analyzed

# Event-wise Glashow Resonance Identification

- ▶ **GR cascade** (W hadronic decay,  $e$ ,  $\tau$  leptonic decay) indistinguishable from NC DIS. However, NC cascades are **less energetic**
- ▶ **GR track** without cascade at interaction vertex distinguishable from  $\nu_\mu$  CC
- ▶  $2\% \leq f_{\bar{\nu}_e} \leq 72\%$  with 4.6 years of PEPE,  $f_{\bar{\nu}_e} \leq 51\%$  with 7.5 years of HESE, assuming hard spectrum
- ▶  $pp$  separated from  $p\gamma$  at more than  $2\sigma$  significance regardless of flux assumption

See also 2303.13706

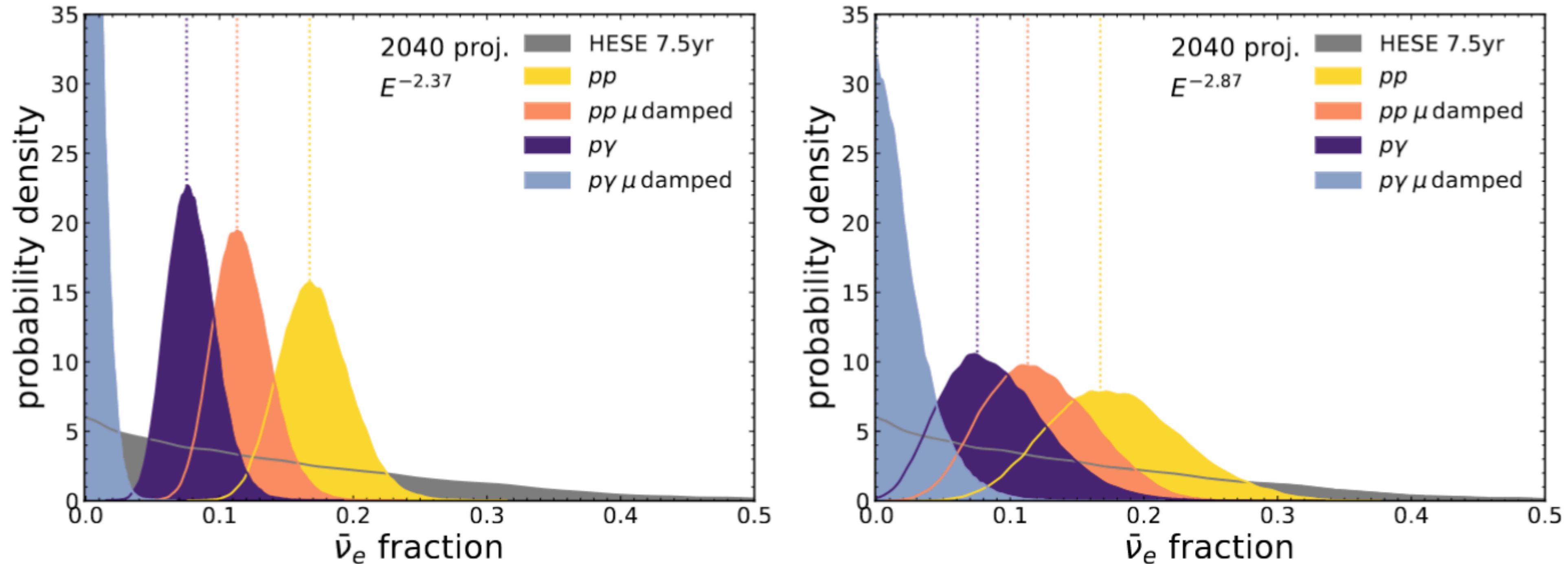
## All future $\nu$ telescopes



Liu, NS, Vincent, PRD/2304.06068

# Statistical Analysis of GR

Assuming event-wise identification not possible, consider only contained events



Analysis	Spectrum	$pp$ from $p\gamma$ $\pi$ decay	$p\gamma$ from $pp$ $\pi$ decay	$pp$ from $p\gamma$ $\mu$ damped	$p\gamma$ from $pp$ $\mu$ damped
HESE event-wise	soft	$1.6\sigma$	$1.4\sigma$	$> 5\sigma$	$0.7\sigma$
	hard	$3.8\sigma$	$3.3\sigma$	$> 5\sigma$	$6.0\sigma$
PEPE event-wise	soft	$2.3\sigma$	$2.0\sigma$	$> 5\sigma$	$1.4\sigma$
	hard	$5.3\sigma$	$4.7\sigma$	$> 5\sigma$	$6.9\sigma$
HESE Bayesian	soft	$2.6\sigma$	$2.1\sigma$	$3.5\sigma$	$3.1\sigma$
	hard	$4.4\sigma$	$3.9\sigma$	$6.3\sigma$	$6.5\sigma$

Liu, NS, Vincent, PRD/2304.06068