

# **Two-pole structures in QCD**

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– Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

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Details in: UGM, *Symmetry* **12** (2020) 981 [2005.06909 [hep-ph]] Mai, UGM, Urbach, *Phys. Rept.* **1001** (2023)1 [2206.01477 [hep-ph]]

# *Short introduction: Bound states in QCD*

– Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

#### **Bound states in QCD**

- Long time a playground of the Quark Model (QM):
	- $\hookrightarrow$  mesons  $(\bar{q}q)$  and baryons  $(qqq)$
- Exotics w.r.t. the QM (already mentioned by Gell-Mann in 1964): Phys.Lett. 8 (1964) 214
	- $\hookrightarrow$  tetraquarks, pentaquarks, hybrids,..., glueballs (truely exotic)
- Even more structures:
	- $\hookrightarrow$  dynamically generated states, hadronic molecules, ..., nuclei  $\rightarrow$  next slide
- Revival of hadron spectroscopy started around 2003:
	- $\hookrightarrow D_{s0}^\star(2317), D_{s1}(2460), \chi_{c1}(3872)$  aka  $X(3872), ...$
- ⇒ The hadron spectrum is arguably the least understood part of the Standard Model
- $\Rightarrow$  Discuss one new feature here, the two-pole structures

#### **Dynamically generated states / hadronic molecules**

• Hadron-hadron (or three-hadron) interactions can dynamically generate resonances

5

- Hadronic molecules: a subclass of these (shallow binding, close to the real axis)
- Prime example: The light scalar mesons  $f_0(500)$ ,  $f_0(700)$ ,  $f_0(980)$



#### **Two-pole structures**

• What is a two-pole structure?

The term two-pole structure refers to the fact that particular single states in the hadron spectrum as listed in the PDG tables are indeed two states.

- Basic ingredients:
	- − coupled channels
	- − molecular states / dynamically generated states

# *A tale of the two* Λ*(1405) states*

– Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

## **The first exotic – the story of the two**  $\Lambda(1405)$

- Quark model:  $uds$  excitation with  $J^P = \frac{1}{2}$ 2 − CLAS (2014) a few hundred MeV above the  $\Lambda(1116)$  $m=1405.1^{+1.3}_{-1.0}\,$  $_{-1.0}^{+1.5}$  MeV ,  $\Gamma = 50.5 \pm 2.0 \,\mathrm{MeV}~[{\rm PDG} \, 2015]$
- Prediction as early as 1959 by Dalitz and Tuan: Resonance between the coupled  $\pi\Sigma$  and  $\bar{K}N$  channels Dalitz, Tuan, Phys. Rev. Lett. **2** (1959) 425; J.K. Kim, PRL **14** (1965) 29
- Clearly seen in  $K^-p\rightarrow \Sigma 3\pi$  reactions at 4.2 GeV at CERN Hemingway, Nucl.Phys. B **253** (1985) 742
- An enigma: Too low in mass for the quark model, but well described in unitarized chiral perturbation theory:  $\phi B \to \phi B$



Kaiser, Siegel, Weise, Ramos, Oset, Oller, UGM, Lutz, ...





#### **Enter chiral dynamics** <sup>9</sup>

#### • Great idea:

Combine (leading-order) chiral SU(3) Lagrangian with coupled-channel dynamics Kaiser, Siegel, Weise, Nucl. Phys. A **594** (1995) 325

$$
\mathcal{D} = \mathcal{V} - \mathcal{
$$

 $\rightarrow$  Dominance of the Weinberg-Tomozawa term, excellent description of  $K^-p$  data and  $\pi\Sigma$  mass distribution, also inclusion of NLO terms with constrained fits

 $\hookrightarrow$  The  $\Lambda(1405)$  appears as a dynamically generated state (MB molecule)

 $\hookrightarrow$  Highly cited follow-ups from TUM group plus other groups, esp. "Spanish Mafia" Oset, Ramos, Nucl. Phys. A **635** (1998) 99, . . .

• But: unpleasant regulator dependence (Yukawa-type, momentum cut-off) gauge invariance in photo-reactions?

### **A new twist**

• Re-analysis of coupled-channel  $K^-p$  scattering and the  $\Lambda(1405)$ 

```
Oller, UGM Phys. Lett. B 500 (2001) 263
```
- Technical improvements:
	- − Subtracted meson-baryon loop with dim reg ,→ **standard method**
	- $-$  Coupled-channel approach to the  $\pi\Sigma$  mass distribution
	- − Matching formulas to any order in chiral perturbation theory established

• Most significant finding:

"Note that the  $\Lambda(1405)$  resonance is described by **two poles** on sheets II and III with rather different imaginary parts indicating a clear departure from the Breit-Wigner situation..."

[pole 1: (1379.2 -i 27.6) MeV, pole 2: (1433.7 -i 11.0) MeV on RS II]

,→ Chiral dynamics generates **two** poles, but: how?

Jido, Oller, Oset, Ramos, UGM, Nucl. Phys. A **725** (2003) 181

#### **Some formalism** 11

• Coupled channels with  $S = -1$ :

 $K^-p\to K^-p,\,\bar{K}^0 n,\,\pi^0\Sigma^0,\,\pi^+\Sigma^-,\,\pi^-\Sigma^+,\,\pi^0\Lambda,\,\eta\Lambda,\,\eta\Sigma^0,\,K^+\Xi^-, \,K^0\Xi^0$ 

• Lippmann-Schwinger eq. in matrix space:

$$
T(W) = [\mathcal{I} + \mathcal{V}(W) \cdot g(s)]^{-1} \cdot \mathcal{V}(W)
$$
  

$$
g(s)_i = \frac{1}{16\pi^2} \left\{ a_i(\mu) + \log \frac{m_i^2}{\mu^2} \frac{M_i^2 - m_i^2 + s}{2s} \log \frac{M_i^2}{m_i^2} + \frac{q_i}{\sqrt{s}} \log \frac{m_i^2 + M_i^2 - s - 2\sqrt{s}q_i}{m_i^2 + M_i^2 - s + 2\sqrt{s}q_i} \right\}
$$

• Matching to chiral perturbation theory, say to orders  $\mathcal{O}(p)$ ,  $\mathcal{O}(p^2)$ ,  $\mathcal{O}(p^3)$ :

$$
T_1 = \mathcal{V}_1, \qquad T_1 + T_2 = \mathcal{V}_1 + \mathcal{V}_2
$$
  

$$
T_1 + T_2 + T_3 = \mathcal{V}_1 + \mathcal{V}_2 + \mathcal{V}_3 - \mathcal{V}_1 \cdot g \cdot \mathcal{V}_1
$$

#### <sup>12</sup> **The two-pole scenario explained**

- Detailed analysis found **two** poles in the complex energy plane
- $\rightarrow$  generated by chiral dynamics, but can we understand this in more detail?
- Group theory:
- $\ket{8 \otimes 8}=1\oplus 8_s\oplus 8_a\oplus 10\oplus \overline{10}\oplus 27$ binding at LO
- Follow the pole movement from the SU(3) limit to the physical masses: Jido, Oller, Oset, Ramos, UGM, Nucl. Phys. A **725** (2003) 181
- Verified by various groups world-wide
- However: scattering and kaonic atom data alone do not lead to a unique solution (two poles, but spread in the complex plane)
- Photoproduction to the rescue:  $\gamma p \to K^+ \Sigma \pi$  CLAS, Phys. Rev. C 87, 035206 (2013)



#### <sup>13</sup> **SU(3) symmetry considerations - details**

Jido, Oller, Oset, Ramos, UGM, Nucl. Phys. A **725** (2003) 181

 $\bullet$  SU(3) limit:  $m_u=m_d=m_s\neq 0$ 

 $\hookrightarrow$  all GB mesons have equal mass  $M_0$  , all octet baryons have equal mass  $m_0$ 

✬  $\Rightarrow$  from the SU(3) limit at  $x = 0$ *x*=1.0  $250$ to the physical world w/  $x = 1$ 200 [ $MeV$ ]  $z_{\mathsf{R}}$  [MeV]  $m_i(x)=m_0+x(m_i-m_0)$ 150 disappear  $(I=1)$  $M_i^2(x)=M_0^2+x(M_i^2-M_0^2)$  $Im z_R$ 100 *x*=0.6 — 1390I *x*=1.0 *x*=0.5  $a_i(x)=a_0+x(a_i-a_0)$  $(I=0)$ 50  $(I=0)$ *x*=1.0  $m_0 = 1151$  MeV 0 *x*=0.5 *x*=0.5  $M_0 = 368$  MeV  $1300$   $1400$   $1500$   $1600$   $1700$ Singlet **Constant**  $a_0 = -2.148$ ✫

 $\operatorname{\sf Re}\, {\sf z}_{_{\sf R}} \;$  [MeV]

 $x=0.5$   $x=1.0$ 

 $+ 1680$  $(I=0)$ 

Đ

 $-$  1580  $(I=1)$ 

*x*=0.5

#### **Present status of the two-pole scenario** 14

• Two poles from scattering + SIDDHARTA data (one well, the other not-so-well fixed): for details, see Mai, Eur. Phys. J. ST **230** (2021) 1593 [arXiv:2010.00056 [nucl-th]]



 $\mathbf{a}$ <br>Figures courtesy Maxim the complex plane!<br>Resoances are $\frac{1}{\mathbf{a}}$ 

Im Maritolevy

 $1.45^{0.00}$ 

Resoances are poles in the complex plane!

#### → PDG 2016: **http://pdg.lbl.gov/2015/reviews/rpp2015-rev-lam-1405-pole-struct.pdf**

POLE STRUCTURE OF THE  $\Lambda(1405)$  REGION Written first November 2015 by Ulf-G. Meißner and Tetsuo Hyodo

– Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

### <sup>15</sup> **SU(3) symmetry considerations - a new twist**

Guo, Kamiya, Mai, UGM, PLB **846** (2023) 138264

• Interesting interchange of trajectories from LO to NLO



 $\hookrightarrow$  can be tested on the lattice

 $\rightarrow$  different findings in Zhuang, Molina, Lu, Geng, [2405.07686 [hep-ph]] ?

## **Status in the Review of Particle Physics**

Status: \*\*

#### • Two excited A states listed in the 2020 RPP edition:

P. A. Zyla *et al.* [Particle Data Group], PTEP **2020** (2020) 083C01

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. 2020, 083C01 (2020)



- a new two-star resonance at 1380 MeV
- still not in the summary table
- there are more such two-pole states!
- this is a fascinating phenomenon Fole Structure of the  $A(1405)$  Region Hyodo, UGM intimately tied to molecular structures

Citation: P.A. Zyla et al. (Particle Data Group). Prog. Theor. Exp. Phys. 2020, 083C01 (2020).

#### $\Lambda(1405)$  1/2

 $I(J^P) = 0(\frac{1}{2}^{-})$  Status: \*\*\*\*

In the 1998 Note on the  $\Lambda$ (1405) in PDG 98, R.H. Dalitz discussed the S-shaped cusp behavior of the intensity at the  $N\overline{K}$  threshold observed in THOMAS 73 and HEMINGWAY 85. He commented that this behavior "is characteristic of S-wave coupling; the other below threshold hyperon, the  $\Sigma(1385)$ , has no such threshold distortion because its  $N-\overline{K}$  coupling is P-wave. For  $\Lambda(1405)$  this asymmetry is the sole direct evidence that  $J^P = 1/2^{-}$ ."

A recent measurement by the CLAS collaboration, MORIYA 14, definitively established the long-assumed  $J^P = 1/2^-$  spin-parity assignment of the  $\Lambda(1405)$ . The experiment produced the  $\Lambda(1405)$  spin-polarized in the photoproduction process  $\gamma p \rightarrow$  $K^+$   $\Lambda$ (1405) and measured the decay of the  $\Lambda$ (1405)(polarized)  $\rightarrow$  $\Sigma^+$ (polarized) $\pi^-$ . The observed isotropic decay of  $\Lambda(1405)$  is consistent with spin  $J = 1/2$ . The polarization transfer to the  $\Sigma^+$ (polarized) direction revealed negative parity, and thus established  $J^P = 1/2^-$ .

See the related review(s):

- Two Λ's: recenty confirmed by lattice QCD Bulava et al., PRL **132** (2024) 051901  $\hookrightarrow$  nature of the lower pole not really pinned down
- for a review, see UGM, *Symmetry* **12** (2020) 981

#### *Two-pole structure* of the D<sup>\*</sup><sub>0</sub> 0 (2300)

#### **Coupled channel scattering on the lattice** <sup>18</sup>

Moir, Peardon, Ryan, Thomas, Wilson [HadSpec], JHEP **1610** (2016) 011

- $D\pi$ ,  $D\eta$ ,  $D_s\bar{K}$  scattering with  $I = 1/2$ :
- 3 volumes, one  $a_s$ , one  $a_t$ ,  $M_\pi \simeq 390$  MeV, various K-matrix type extrapolations





- S-wave pole at  $(2275.9 \pm 0.9)$  MeV
- close to the  $D_{\pi}$  threshold
- $\bullet$  consistent w/  $\overline{D_0^{\star}}(2300)$  of PDG
- BUT: symmetries ignored... :-(

## **Coupled channel dynamics 19 and 19 an**

Kaiser, Weise, Siegel (1995), Oset, Ramos (1998), Oller, UGM (2001), Kolomeitsev, Lutz (2002),Jido et al. (2003), Guo et al. (2006), . . .

•  $D\phi$  bound states: Poles of the T-matrix (potential from CHPT and unitarization)

$$
\mathcal{D}(\mathbf{C}) = \mathbf{V} \mathbf{A}(\mathbf{G}) + \mathbf{V} \mathbf{A}(\mathbf{G}) \mathbf{A}(\mathbf{V}) + \mathbf{V} \mathbf{A}(\mathbf{G}) \mathbf{A}(\mathbf{V}) + \cdots
$$

• Unitarized CHPT as a non-perturbative tool:

$$
T^{-1}(s)=\mathcal{V}^{-1}(s)-G(s)
$$

•  $V(s)$ : derived from the SU(3) heavy-light chiral Lagrangian, 6 LECs up to NLO

 $\rightarrow$  next slide

- $G(s)$ : 2-point scalar loop function, regularized w/ a subtraction constant  $a(\mu)$
- $\bullet$  T,  $\mathcal{V}, G$ : all these are matrices, channel indices suppressed

## **Coupled channel dynamics cont'd** <sup>20</sup>

Barnes et al. (2003), van Beveren, Rupp (2003), Kolomeitsev, Lutz (2004), Guo et al. (2006), . . .

• NLO effective chiral Lagrangian for coupled channel dynamics

Guo, Hanhart, Krewald, UGM, Phys. Lett. B **666** (2008) 251

$$
\mathcal{L}_{\text{eff}} = \mathcal{L}^{(1)} + \mathcal{L}^{(2)}
$$
\n
$$
\mathcal{L}^{(1)} = \mathcal{D}_{\mu} D \mathcal{D}^{\mu} D^{\dagger} - M_{D}^{2} D D^{\dagger}, \quad D = (D^{0}, D^{+}, D_{s}^{+})
$$
\n
$$
\mathcal{L}^{(2)} = D \left[ -h_{0} \langle \chi_{+} \rangle - h_{1} \chi_{+} + h_{2} \langle u_{\mu} u^{\mu} \rangle - h_{3} u_{\mu} u^{\mu} \right] D
$$
\n
$$
+ \mathcal{D}_{\mu} D \left[ h_{4} \langle u^{\mu} u^{\nu} \rangle - h_{5} \{ u^{\mu}, u^{\nu} \} \right] \mathcal{D}_{\nu} D
$$
\nwith  $u_{\mu} \sim \partial_{\mu} \phi$ ,  $\chi_{+} \sim \mathcal{M}_{\text{quark}}$ , ...

• LECs:

 $\hookrightarrow h_0$  absorbed in masses

 $\rightarrow h_1 = 0.42$  from the  $D_s$ -D splitting

 $\hookrightarrow h_{2,3,4,5}$  from a fit to lattice data  $(D\pi \to D\pi, D\bar K \to D\bar K,...)$ 

Liu, Orginos, Guo, Hanhart, UGM, Phys. Rev. D **87** (2013) 014508

#### <sup>21</sup> **Fit to lattice data**

Liu, Orginos, Guo, Hanhart, UGM, PRD **87** (2013) 014508

• Fit to lattice data in 5 "simple" channels: no disconnected diagrams



• Prediction: Pole in the  $(S, I) = (1, 0)$  channel:  $2315^{+18}_{-28}$  MeV

Experiment:

 $\zeta_{\rm s0}(2317) = (2317.8 \pm 0.5)$  MeV PDG2021

## **What about the**  $D_0^{\star}(2300)$ **?**

• Calculate the finite volume energy levels for  $I = 1/2$ , compare w/ the LQCD results Albaladejo, Fernandez-Soler, Guo, Nieves, Phys. Lett. B **767** (2017) 465



• this is NOT a fit!

• all LECs taken from the earlier study of Liu et al. (discussed before)

#### **What about the**  $D_0^{\star}(2300)$ **? – cont'd** 0 (2300)**? – cont'd**

#### Albaladejo, Fernandez-Soler, Guo, Nieves (2017)

- reveals a two-pole scenario! [cf.  $\Lambda(1405)$ ]
- understood from group theory

 $\bar{3} \otimes 8 =$ attractive  $\bar{3} \oplus 6 \oplus \bar{15}$ 

• this was seen earlier in various calc's

Kolomeitsev, Lutz (2004), F. Guo, Shen, Chiang, Ping, Zou (2006), F. Guo, Hanhart, UGM (2009), Z. Guo, UGM, Yao (2009)

- Again: important role of **chiral symmetry**
- Lattice QCD test: sextet pole becomes a b.s.

for  $M_{\phi} > 575$  MeV in the SU(3) limit

Du et al., Phys.Rev. D **98** (2018) 094018

- FZJ LQCD finds a b.s. for  $M_\pi = 600$  MeV Gregory et al., 2106.15391 [hep-ph]
- HadSpec finds a virtual state ( $M_\pi = 700$  MeV) Yeo et al., 2403.10498 [hep-lat]



#### **Two-pole structure consistent with the lattice data?**

Ashokan, Tang, Guo, Hanhart, Kamiya, UGM, EPJ **C 83** (2023) 850

- Can we understand why HadSpec only reported one pole?
- Impose  $SU(3)$  symmetry on the K-matrix to fit the FV energy levels  $\rightarrow$  less parameters!

$$
K=\left(\frac{g_{\bar{3}}^2}{m_{\bar{3}}^2-s}+c_{\bar{3}}\right)C_{\bar{3}}+\left(\frac{g_{6}^2}{m_{6}^2-s}+c_{6}\right)C_{6}+c_{\overline{15}}\,C_{\overline{15}}.
$$

- perform various fits (switch off various terms)
- $\hookrightarrow$  Poles are consistent w/ UChPT !
- → never ignore symmetries!



#### <sup>25</sup> **Two-pole scenario in the heavy-light sector**

- Invoke HQSS and HQFS:
- $\hookrightarrow$  Two states in various  $I = 1/2$  states in the heavy meson sector  $(M, \Gamma/2)$



 $\rightarrow$  but is there further experimental support for this?

# *Amplitude Analysis of*  $B\to D\pi\pi$

#### **Data for**  $B \to D \pi \pi$

• Recent high precision results for  $B \to D \pi \pi$  from LHCb

Aaji et al. [LHCb], Phys. Rev. D **94** (2016) 072001, . . .

• Spectroscopic information in the angular moments  $(D\pi$  FSI):



#### **Theory of**  $B \to D \pi \pi$

Du, Albadajedo, Fernandez-Soler, Guo, Hanhart, UGM, Nieves, Phys. Rev. D **98** (2018) 094018

- Effective Lagrangian for  $B \to D$  transitions w/ one fast & one slow pseudoscalar Savage, Wise, Phys. Rev. D **39** (1989) 3346
- $\bullet$   $B^ \rightarrow$   $D^+\pi^-\pi^-$  contains coupled-channel  $D\pi$  FSI
- Consider  $S, P, D$  waves:  $\mathcal{A}(B^-\to D^+\pi^-\pi^-)=\mathcal{A}_0(s)+\mathcal{A}_1(s)+\mathcal{A}_2(s)$ 
	- $\rightarrow$  P-wave:  $D^{\star}, D^{\star}(2680)$ ; D-wave:  $D_2(2460)$  as by LHCb
	- $\rightarrow$  S-wave: use coupled channel  $(D\pi, D\eta, D_s\bar{K})$  amplitudes with all parameters fixed before
	- $\rightarrow$  only two parameters in the S-wave (one combination of the LECs  $c_i$  and one subtraction constant in the  $G_{ij}$ )



$$
\mathcal{A}_0(s) \propto E_{\pi} \left[ 2 + G_{D\pi}(s) \left( \frac{5}{3} T_{11}^{1/2}(s) + \frac{1}{3} T_{11}^{3/2}(s) \right) \right]
$$
  
+  $\frac{1}{3} E_{\eta} G_{D\eta}(s) T_{21}^{1/2}(s) + \sqrt{\frac{2}{3}} E_{\bar{K}} G_{D_s \bar{K}}(s) T_{31}^{1/2}(s) + ...$ 



#### **Analysis of**  $B \to D \pi \pi$

Du, Albadajedo, Fernandez-Soler, Guo, Hanhart, UGM, Nieves, Yao, Phys. Rev. D **98** (2018) 094018

• More appropriate combinations of the angular moments:



• The S-wave  $D\pi$  can be very well described using pre-fixed amplitudes

• Fast variation in [2.4,2.5] GeV in  $\langle P_{13}\rangle$ : cusps at the  $D\eta$  and  $D_s\bar{K}$  thresholds  $\hookrightarrow$  should be tested experimentally

#### A closer look at the S–wave **30 and 20 and 30 and 30 and 30 and 30 and 30 and 40 and 40 and 30 a**

• LHCb provides anchor points, where the strength and the phase of the S-wave were extracted from the data and connected by cubic spline



 $t$ od in our amplitude predoctorales para la formación de la formació  $\bullet$  Higher mass pole at 2.46 GeV clearly amplifies the cusps predicted in our amplitude<br>- Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

## Theory of  $B_s^0 \to \bar{D}^0 K^- \pi^+$

Du, Albadajedo, Fernandez-Soler, Guo, Hanhart, UGM, Nieves, Yao, Phys. Rev. **D98** (2018) 094018

- $\bullet$  LHCb has also data on  $B^0_s \rightarrow \bar{D}^0 K^-\pi^+$ , but less precise
- Same formalism as before, one different combination of the LECs  $c_i$
- same resonances in the P- and D-wave as LHCb  $\rightarrow$  one parameter fit!



 $\Rightarrow$  these data are also well described

 $\Rightarrow$  better data for  $\langle P_{13} \rangle$  would be welcome

⇒ even more channels, see Du, Guo, UGM, Phys. Rev. D **99** (2019) 114002

#### Where is the lowest charm-strange meson?

Du, Guo, Hanhart, Kubis, UGM, Phys. Rev. Lett. 126 (2021) 192001 [2012.04599]

- Precise analysis of the LHCb data on  $B^- \to D^+\pi^-\pi^-$  using UChPT and Khuri-Treiman eq's (3-body unit.) Aaji et al. [LHCb], Phys. Rev. D 94 (2016) 072001
- Breit-Wigner description not appropriate for the S-wave but UChPT and the dispersive analysis are!
- First determination of the  $D\pi$  phase shift
- The lowest charm-strange meson is located at:

 $\left( 2105^{+6}_{-8} - i \, 102^{+10}_{-11} \right)$  MeV

• Recently confirmed by Lattice QCD! Cheung et al. [HadSpec], JHEP 02 (2021) 100 [2008.06432]



2200

 $M_{D^+\pi^-}$  [MeV]

2300

2400

2100

- Ulf-G. Meißner, Two-pole structures in QCD - seminer, IHEP, Beijing, September 11, 2024 -

#### **PDG update** 33

• The PDG group is like a heavy tanker, still there is motion:



RPP 2024: 79. Heavy Non- $q\bar{q}$  Mesons, Hanhart, Gutsche, Mitchell

⇒ stay tuned!

# *Summary*

– Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

- Chiral coupled-channel dynamics of QCD generates two-pole structures Oller, UGM (2001), Jido et al. (2005)
- Further two-pole structures beyond the  $\Lambda(1405)$  and  $D_0^{\star}(2300)$ 
	- $\rightarrow$  K<sub>1</sub>(1270) meson Roca et al., PRD 72 (2005) 014002, Geng et al., PRD 75 (2007) 014017
	- $\hookrightarrow \Xi(1820)$  baryon Sarkar et al., Nucl. Phys. A 750 (2005) 294, ...
	- $\rightarrow$  Y (4260) meson? Ablikim et al. [BESIII], Phys. Rev. D 102 (2020) 031101
	- $\rightarrow b_1, h_1$  mesons Clympton, Kim, Phys. Rev. D 108 (2023) 074021; 2409.02420 [hep-ph]
	- $\rightarrow$  more to be found ... (interplay of lattice QCD / EFT/ disp. rel./ data)
- All this is not properly reflected in the PDG tables
	- $\hookrightarrow$  summary tables e.g. only lists one pole for the  $\Lambda(1405)$
	- $\hookrightarrow$  many states analyzed using BW parametrization :-(
	- $\leftrightarrow$  exp. collaborations must stop committing sins like
		- using BW parametrization close to threshold (BESIII, LHCb, ...)
	- $\hookrightarrow$  PDG needs a more serious approach to the hadron spectrum!

# *SPARES*

– Ulf-G. Meißner, Two-pole structures in QCD – seminer, IHEP, Beijing, September 11, 2024 –

#### **Finite volume formalism** 37

• Goal: postdict the finite volume (FV) energy levels for  $I = 1/2$  and compare with the recent LQCD results from Moir et al. using the already fixed LECs  $\rightarrow$  parameter-free insights into the  $D_0^{\star}(2300)$ 

• In a FV, momenta are quantized:  $\vec{q} =$  $2\pi$ L  $\vec{n} ~,~~ \vec{n} \in \mathbb{Z}^3$ 

 $\Rightarrow$  Loop function  $G(s)$  gets modified:  $\int d^3\vec{q}\rightarrow$ 1  $\boldsymbol{L^3}$  $\sum$  $\vec{q}$ 



$$
\tilde{G}(s,L) = G(s) = \lim_{\Lambda \to \infty} \left[ \frac{1}{L^3} \sum_{\vec{n}}^{\vert \vec{q} \vert < \Lambda} I(\vec{q}\, ) - \int_0^\Lambda \frac{q^2 dq}{2\pi^2} I(\vec{q}\,) \right]
$$

Döring, UGM, Rusetsky, Oset, Eur. Phys. J. A47 (2011) 139

• FV energy levels from the poles of  $\tilde{T}(s, L)$ :

$$
\tilde T^{-1}(s,L) = \mathcal{V}^{-1}(s) - \tilde G(s,L)
$$

#### **Chiral Lagrangian for** B → D **transitions** <sup>38</sup>

Savage, Wise, Phys. Rev. D39 (1989) 3346

 $\bm{H} =$ 

 $\sqrt{ }$ 

0 0 0

 $\sum_{i=1}^{n}$ 

 $\mathbb{R}$ 

1 0 0

0 0 0

 $\overline{ }$ 

• Consider  $\bar{B}\to D$  transition with the emission of two light pseudoscalars (pions)

- $\hookrightarrow$  chiral symmetry puts constraints on one of the two pions
- $\hookrightarrow$  the other pion moves fast and does not participate in the final-state interactions
- Chiral effective Lagrangian:

$$
\mathcal{L}_{\text{eff}} = \bar{B} \big[ c_1 \left( u_\mu t M + M t u_\mu \right) + c_2 \left( u_\mu M + M u_\mu \right) t \n+ c_3 t \left( u_\mu M + M u_\mu \right) + c_4 \left( u_\mu \langle M t \rangle + M \langle u_\mu t \rangle \right) \n+ c_5 t \langle M u_\mu \rangle + c_6 \langle (M u_\mu + u_\mu M) t \rangle \big] \partial^\mu D^\dagger
$$

with

$$
\bar{B}=(B^-,\bar{B}^0,\bar{B}^0_s)~,~~D=(D^0,D^+,D_s^+)
$$

 $M$  is the matter field for the fast-moving pion

 $t = uHu$  is a spurion field for Cabbibo-allowed decays

 $\rightarrow$  only some combinations of the LECs  $c_i$  appear

#### **Some formalism** 39

• Exact three-body unitarity via Khuri-Treiman equations: Khuri, Treiman (1960)

 $\hookrightarrow$  write  ${\cal A}_{+--}(B^-\to D^+\pi^-\pi^-)$  and  ${\cal A}_{00-}(B^-\to D^0\pi^0\pi^-)$  as [reconstruction theorem]

$$
\mathcal{A}_{+--}(s,t,u) = \mathcal{F}_0^{1/2}(s) + \frac{\kappa(s)}{4} z_s \mathcal{F}_1^{1/2}(s) + \frac{\kappa(s)^2}{16} (3z_s^2 - 1) \mathcal{F}_2^{1/2}(s) + (t \leftrightarrow s)
$$
  
\n
$$
\mathcal{A}_{00-}(s,t,u) = -\frac{1}{\sqrt{2}} \mathcal{F}_0^{1/2}(s) - \frac{\kappa(s)}{4\sqrt{2}} z_s \mathcal{F}_1^{1/2}(s) - \frac{\kappa(s)^2}{16\sqrt{2}} (3z_s^2 - 1) \mathcal{F}_2^{1/2}(s) + \frac{\kappa_u(u)}{4} z_u \mathcal{F}_1^{1}(u)
$$
  
\n
$$
z_s = \cos \theta_s = \frac{s(t-u) - \Delta}{\kappa(s)}, z_u = \cos \theta_u = \frac{t-s}{\kappa_u(u)}, \quad \Delta = (M_B^2 - M_\pi^2)(M_D^2 - M_\pi^2)
$$
  
\n
$$
\kappa(s) = \lambda^{1/2}(s, M_D^2, M_\pi^2) \lambda^{1/2}(s, M_B^2, M_\pi^2), \kappa_u(u) = \lambda^{1/2}(u, M_B^2, M_D^2) \sqrt{1 - 4M_\pi^2/u}
$$
  
\n
$$
\mathcal{F}_\ell^I
$$
: angular momentum  $\ell \le 2$ , isospin  $I < 3/2$ 

• Solve via the Omnès ansatz:

$$
\mathcal{F}_{\ell}^I(s) = \Omega_{\ell}^I(s) \bigg\{Q_{\ell}^I(s) + \frac{s^n}{\pi} \int_{s_{\rm th}}^{\infty} \frac{ds'}{s'^n} \frac{\sin \delta_{\ell}^I(s') \hat{\mathcal{F}}_{\ell}^I(s')}{|\Omega_{\ell}^I(s')|(s'-s)} \bigg\}\,,
$$

 $\boldsymbol{Q}_{\boldsymbol{\ell}}^{I}(s)$  = polynom of degree zero (one subtraction suffices)

$$
\Omega_{\ell}^{I}(s) = \exp \left\{ \frac{s}{\pi} \int_{s_{\text{th}}}^{\infty} ds' \frac{\delta_{\ell}^{I}(s')}{s'(s'-s)} \right\}
$$