

如何系统计算分子态贡献和传统夸克模型贡献

吴佳俊(中国科学院大学)

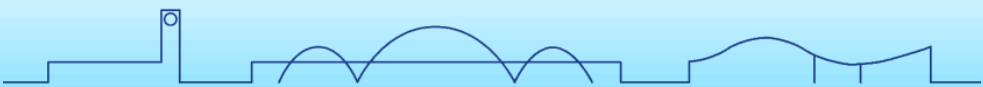
合作者: 郝伟(NKU), 王广娟(KEK), 杨智(UESTC), Makoto Oka(RIKEN),
朱世琳(PKU), 余康(UCAS)

Scib.2024.07.012, Phys.Rev.D 110 (2024) 11, 114029, New paper....



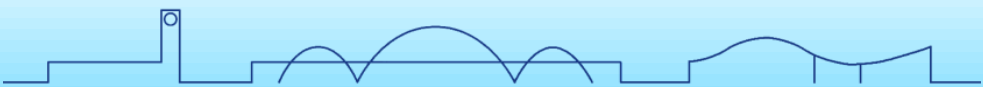
目录

- 动机
- HEFT方案
- 从Tcc 到 X(3872)
- 总结和展望



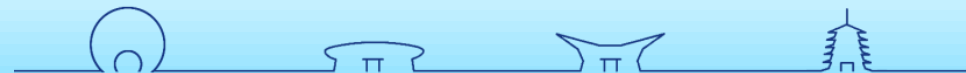
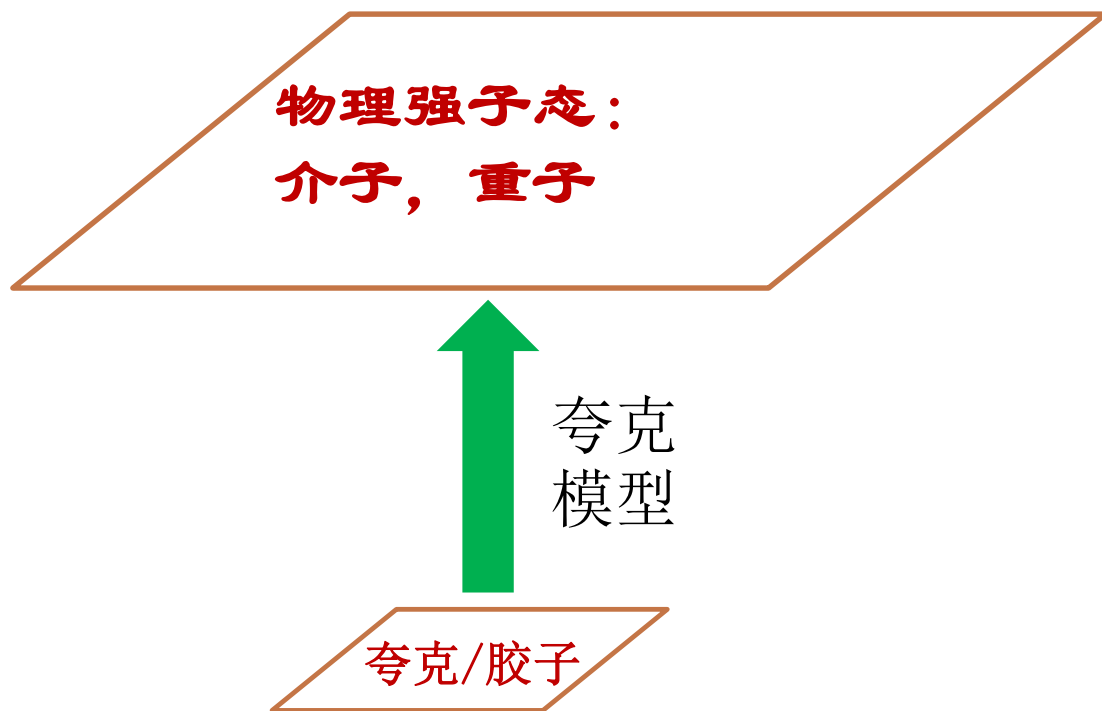
动机

强子谱？ 强子结构——
—强子内部的成分？



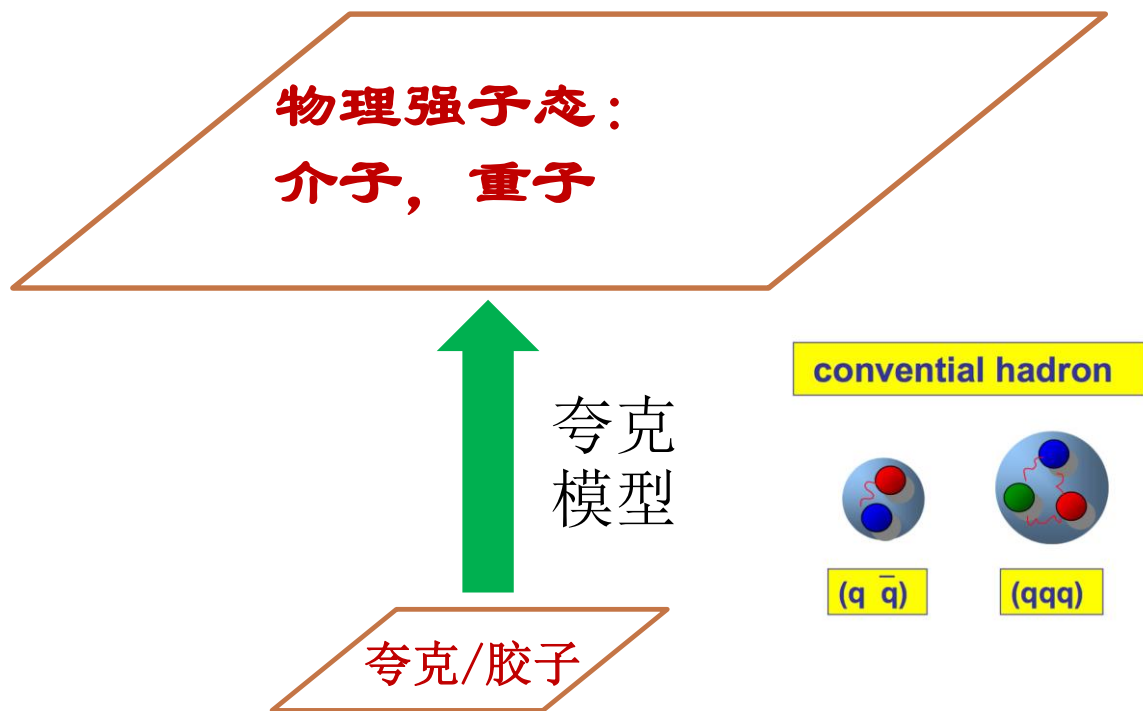
动机

强子谱？ 强子结构——
—强子内部的成分？



动机

强子谱？ 强子结构——
—强子内部的成分？



UNQUENCHED quark model
非淬火夸克模型



动机

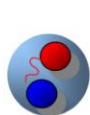
强子谱？ 强子结构——
—强子内部的成分？

物理强子态：
介子，重子

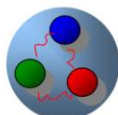
夸克
模型

夸克/胶子

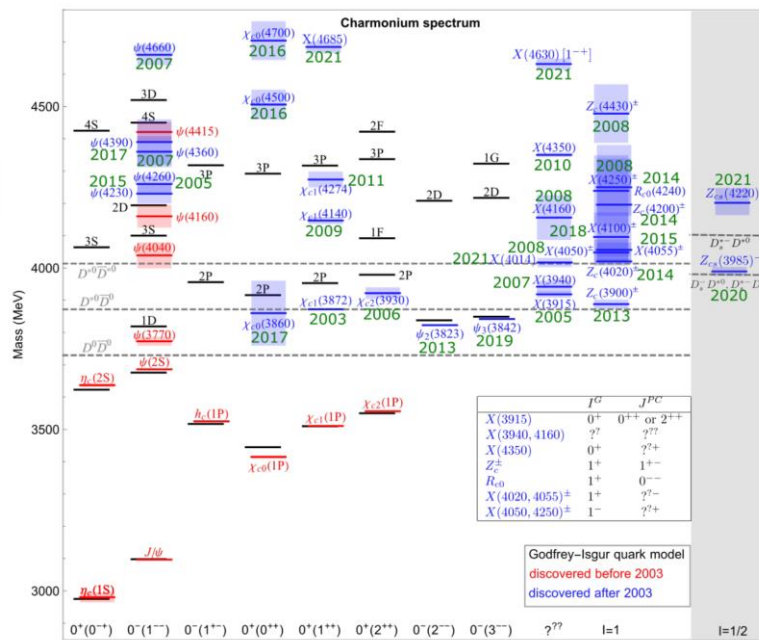
conventional hadron



(q q̄)



(qqq)



UNQUENCHED quark model
非淬火夸克模型



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动机

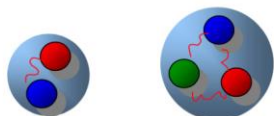
强子谱？ 强子结构——
—强子内部的成分？

物理强子态：
介子，重子，奇特态

夸克模型

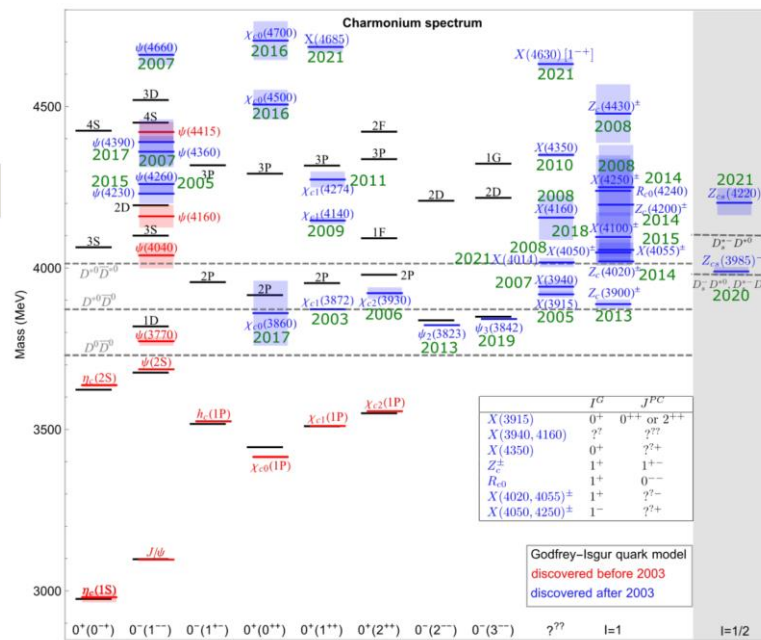
夸克/胶子

conventional hadron

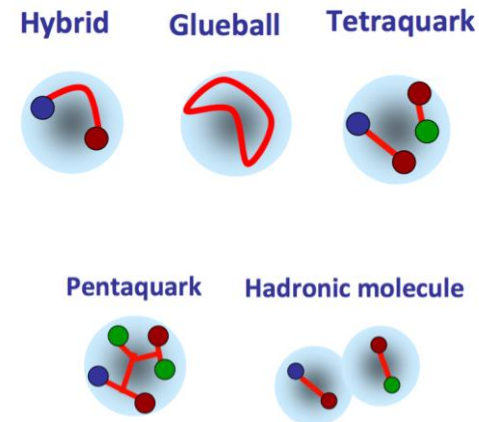


(q q̄)

(qqq)



Exotic



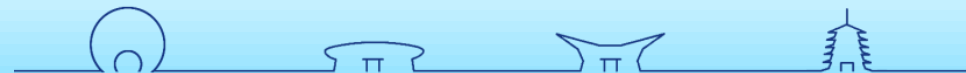
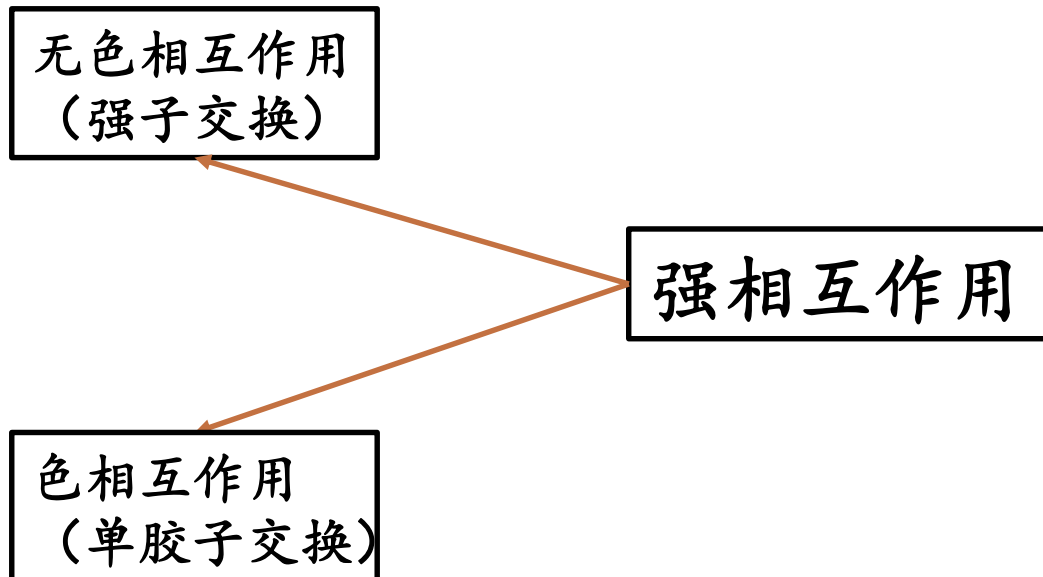
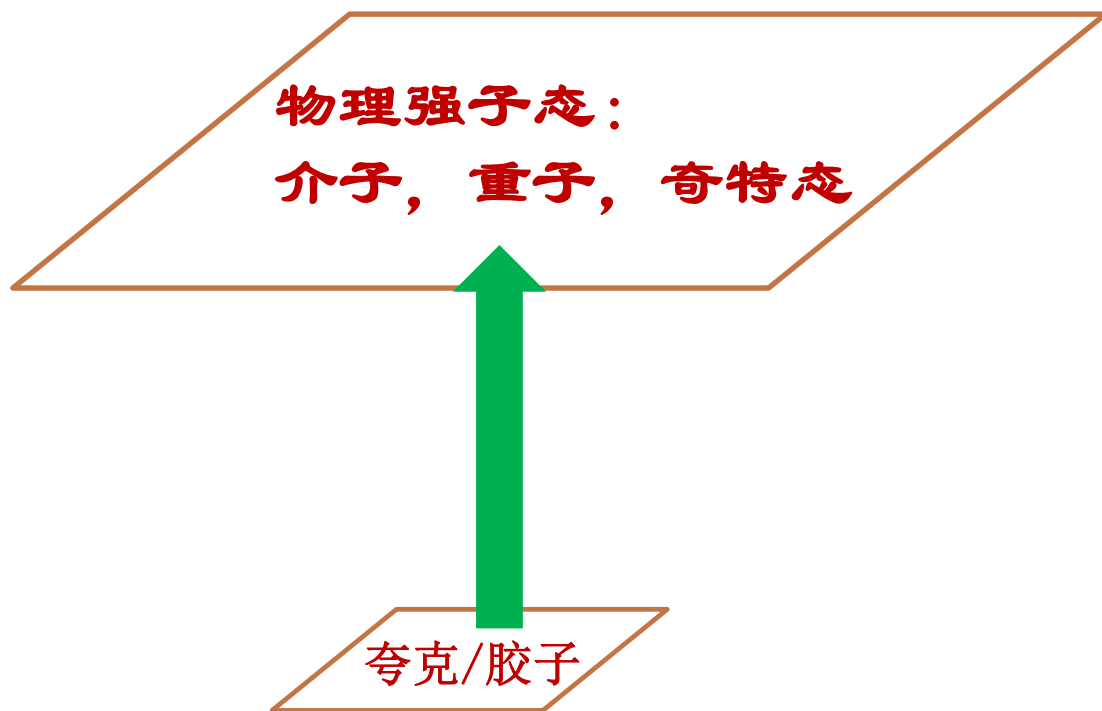
UNQUENCHED quark model
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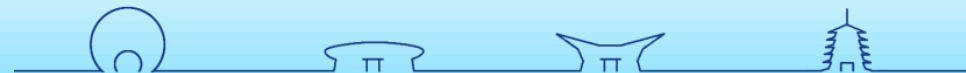
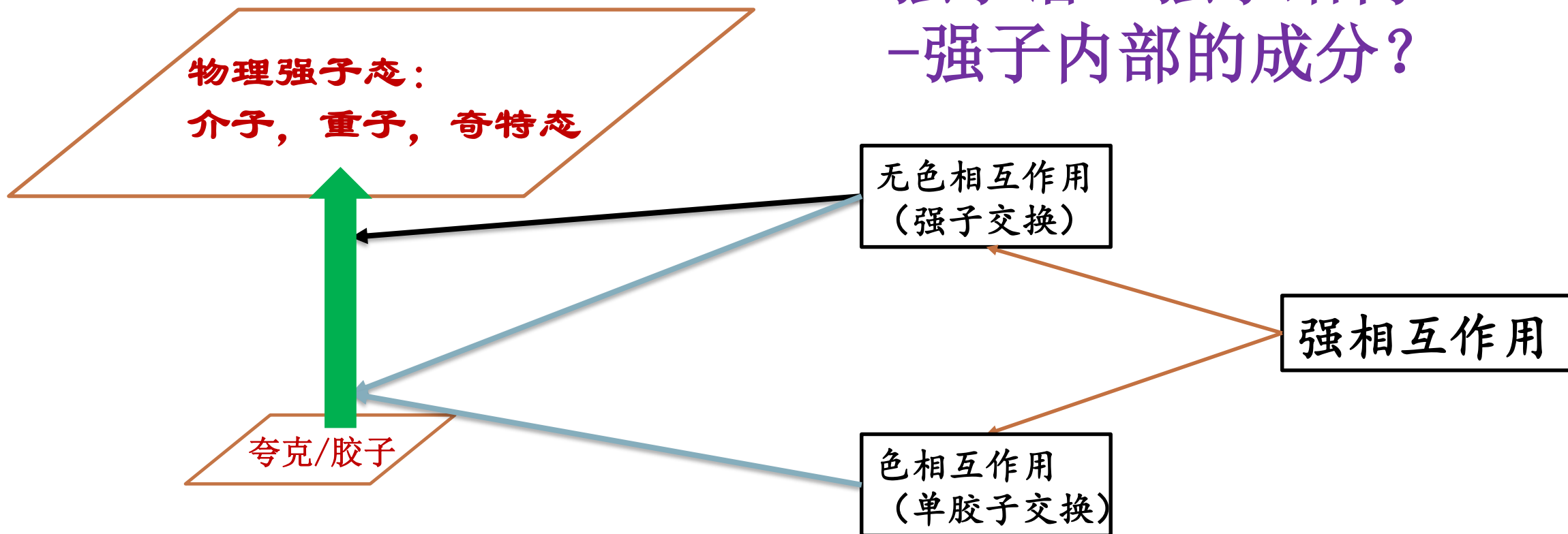
动机

强子谱？ 强子结构——
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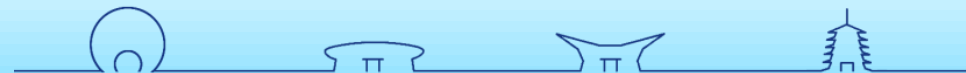
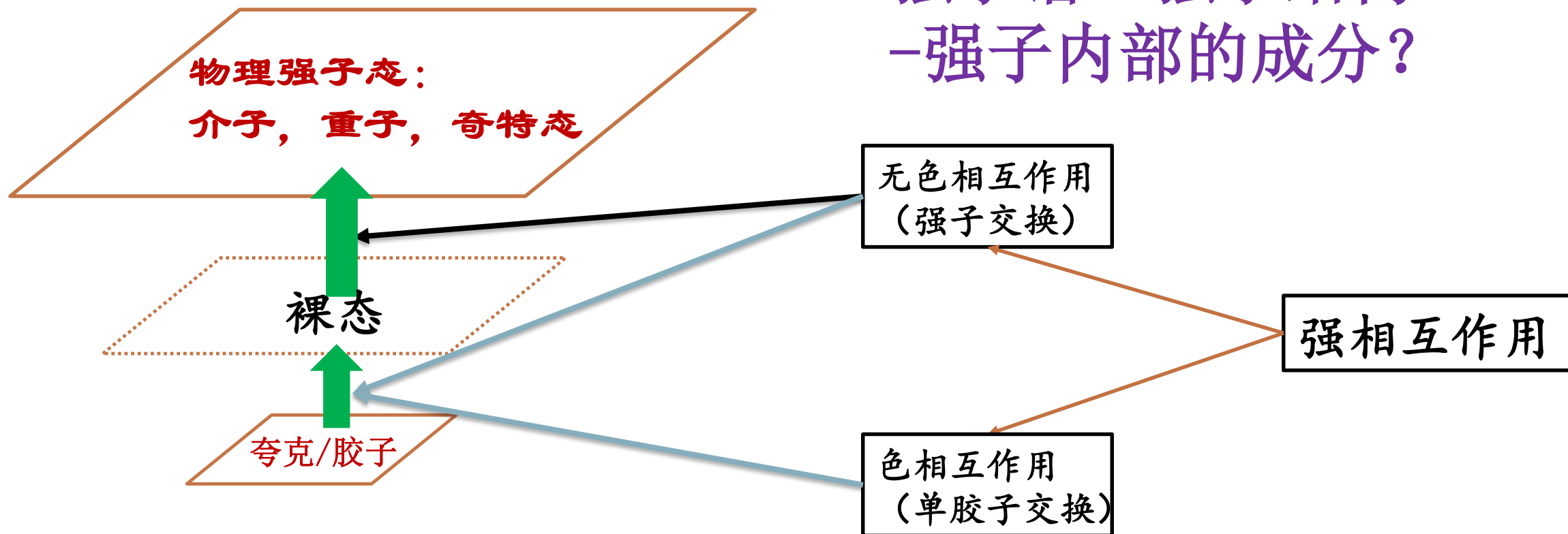
动机

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动机

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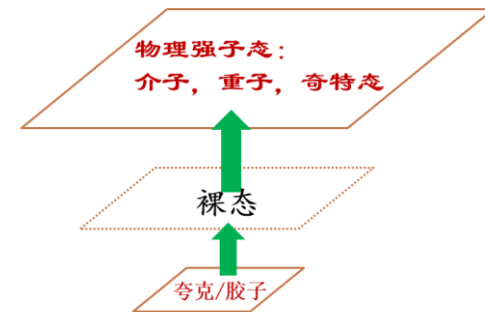


动机

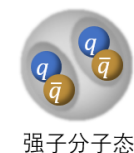
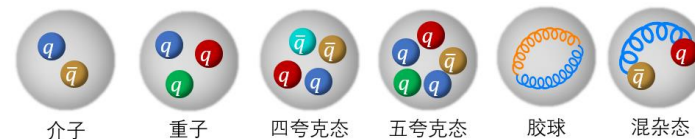
相互作用的完整性

夸克胶子层次

强子层次



传统夸克模型贡献



分子态贡献

耦合道模型



强子

夸克胶子层次: 单强子态

强子层次: 多强子态

能够系统描述强子的较为完整的框架

能够描述一系列强子, 不是一个两个

HEFT介绍

$$H = H_0 + H_I$$

$$H_0 = \sum_{i=1,n} |B_i\rangle m_i \langle B_i| + \sum_{\alpha} |\alpha(k_{\alpha})\rangle \left[\sqrt{m_{\alpha 1}^2 + k_{\alpha}^2} + \sqrt{m_{\alpha 2}^2 + k_{\alpha}^2} \right] \langle \alpha(k_{\alpha})|$$

$|B_i\rangle$ bare state, bare mass m_i

$|\alpha(k_{\alpha})\rangle$ non-interaction channels

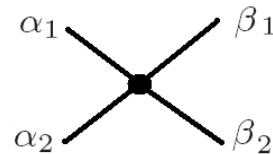
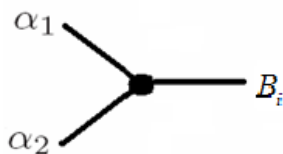
$$H_I = \hat{g} + \hat{v}$$

$$\hat{g} = \sum_{\alpha} \sum_{i=1,n} \left[|\alpha(k_{\alpha})\rangle g_{i,\alpha}^+ \langle B_i| + |B_i\rangle g_{i,\alpha} \langle \alpha(k_{\alpha})| \right]$$

$$\hat{v} = \sum_{\alpha,\beta} |\alpha(k_{\alpha})\rangle v_{\alpha,\beta} \langle \beta(k_{\beta})|$$

夸克胶子层次的相互作用

强子层次相互作用



共振态
(质量, 宽度, 极点位置, 耦合强度)

HEFT

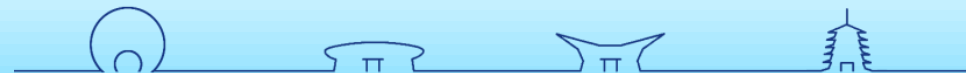
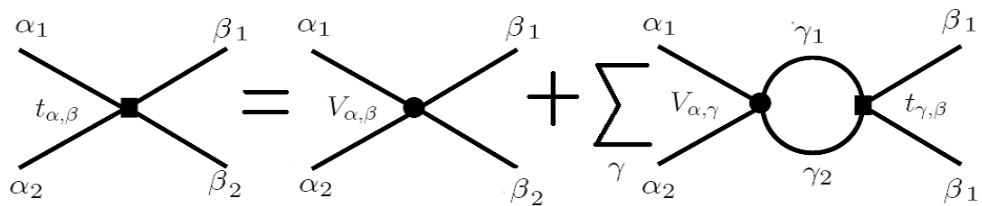
T 矩阵
(相移, 非弹系数)

格点能谱



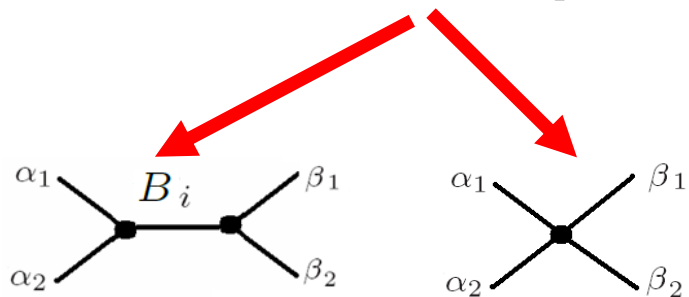
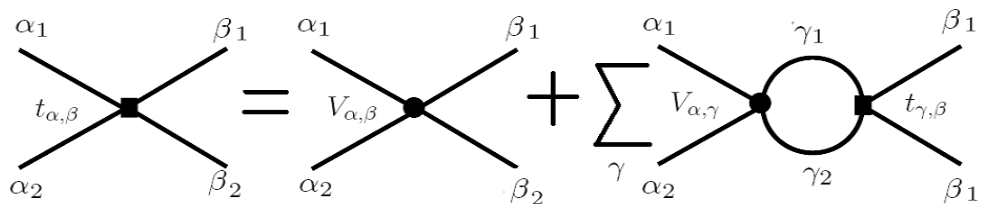
HEFT介绍

$$T_{\alpha\beta}(k_\alpha, k_\beta, E) = V_{\alpha\beta}(k_\alpha, k_\beta) + \sum_\gamma \int k_\gamma^2 dk_\gamma \frac{V_{\alpha\gamma}(k_\alpha, k_\gamma) T_{\gamma\beta}(k_\gamma, k_\beta, E)}{E - \sqrt{m_{\gamma 1}^2 + k_\gamma^2} - \sqrt{m_{\gamma 2}^2 + k_\gamma^2} + i\varepsilon}$$



HEFT介绍

$$T_{\alpha\beta}(k_\alpha, k_\beta, E) = V_{\alpha\beta}(k_\alpha, k_\beta) + \sum_\gamma \int k_\gamma^2 dk_\gamma \frac{V_{\alpha\gamma}(k_\alpha, k_\gamma) T_{\gamma\beta}(k_\gamma, k_\beta, E)}{E - \sqrt{m_{\gamma 1}^2 + k_\gamma^2} - \sqrt{m_{\gamma 2}^2 + k_\gamma^2} + i\epsilon}$$



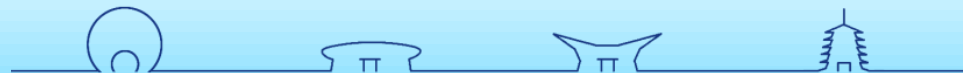
$$G_\alpha^{B^*} \frac{1}{E - m_B} G_\beta^B$$

$$V_{\alpha,\beta}$$

$$G_{MN}^B(k) = \frac{g_{MN}^B}{m_M} \frac{k}{\sqrt{\omega_M(k)}} u(k).$$

$$v_{\alpha\beta}(k, k') = v_{\alpha\beta} f_\alpha(k) f_\beta(k')$$

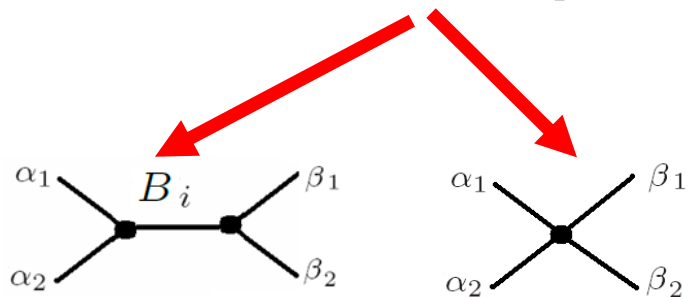
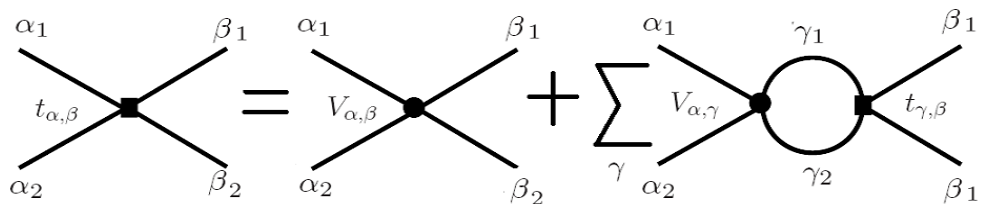
$$f(k) = \frac{1}{m_M^2} \frac{k}{\omega_M(k)} u(k)$$



HEFT介绍

$$T_{\alpha\beta}(k_\alpha, k_\beta, E) = V_{\alpha\beta}(k_\alpha, k_\beta) + \sum_\gamma \int k_\gamma^2 dk_\gamma \frac{V_{\alpha\gamma}(k_\alpha, k_\gamma) T_{\gamma\beta}(k_\gamma, k_\beta, E)}{E - \sqrt{m_{\gamma 1}^2 + k_\gamma^2} - \sqrt{m_{\gamma 2}^2 + k_\gamma^2} + i\epsilon}$$

$$T_{\alpha\beta}(k, k'; E) = t_{\alpha\beta}(k, k'; E) + T_{\alpha\beta}^{bare}(k, k'; E)$$



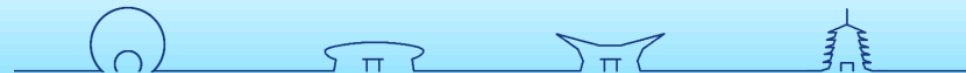
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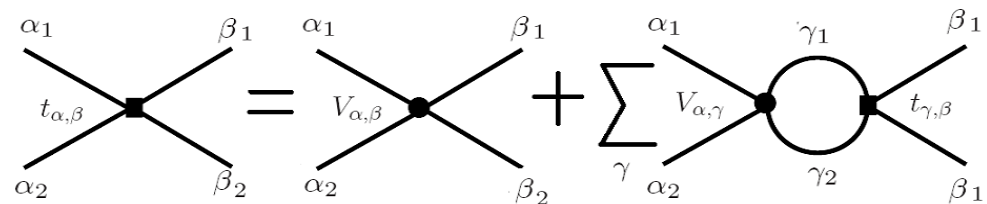
$$v_{\alpha\beta}(k, k') = v_{\alpha\beta} f_\alpha(k) f_\beta(k')$$

$$f(k) = \frac{1}{m_M^2} \frac{k}{\omega_M(k)} u(k)$$



HEFT介绍

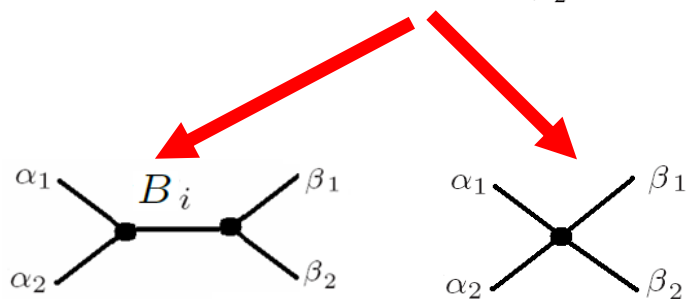
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$$T_{\alpha\beta}(k, k'; E) = t_{\alpha\beta}(k, k'; E) + T_{\alpha\beta}^{bare}(k, k'; E)$$

$$t_{\alpha\beta}(k, k'; E) = V_{\alpha\beta}(k, k') + \sum_\gamma \int dq q^2 \frac{V_{\alpha\gamma}(k, q) T_{\gamma\beta}(q, k'; E)}{E - \omega_\gamma(q) + i\epsilon}$$

$$t_{\alpha\beta}(k, k'; E) = f_\alpha(k) \tilde{t}_{\alpha\beta}(E) f_\beta(k') \quad \tilde{t}_{\alpha\beta}(E) = v_{\alpha\beta} + \sum_\gamma \int dq q^2 \frac{v_{\alpha\gamma} f_\gamma(q)^2}{E - \omega_\gamma(q) + i\epsilon} \tilde{t}_{\gamma\beta}(E)$$



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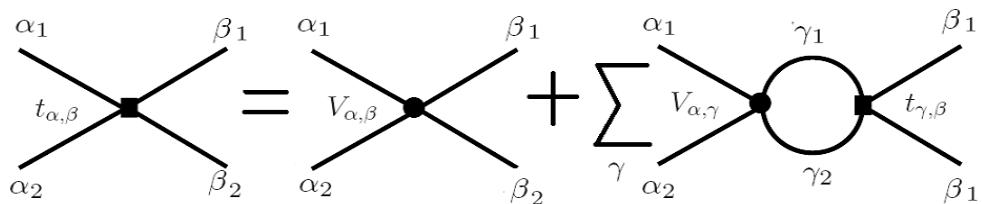
$$v_{\alpha\beta}(k, k') = v_{\alpha\beta} f_\alpha(k) f_\beta(k')$$

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HEFT介绍

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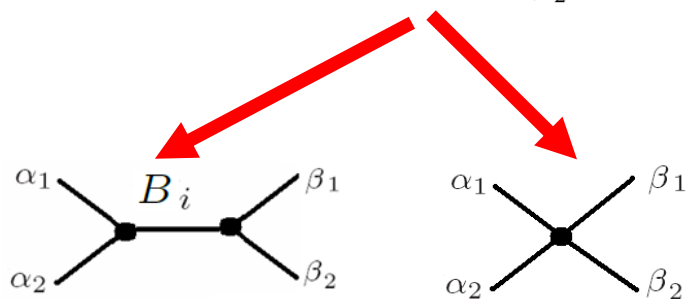


$$T_{\alpha\beta}(k, k'; E) = t_{\alpha\beta}(k, k'; E) + T_{\alpha\beta}^{\text{bare}}(k, k'; E)$$

$$t_{\alpha\beta}(k, k'; E) = V_{\alpha\beta}(k, k') + \sum_\gamma \int dq q^2 \frac{V_{\alpha\gamma}(k, q) T_{\gamma\beta}(q, k'; E)}{E - \omega_\gamma(q) + i\epsilon}$$

$$t_{\alpha\beta}(k, k'; E) = f_\alpha(k) \tilde{t}_{\alpha\beta}(E) f_\beta(k') \quad \tilde{t}_{\alpha\beta}(E) = v_{\alpha\beta} + \sum_\gamma \int dq q^2 \frac{v_{\alpha\gamma} f_\gamma(q)^2}{E - \omega_\gamma(q) + i\epsilon} \tilde{t}_{\gamma\beta}(E)$$

$$T_{\alpha\beta}^{\text{bare}}(k, k'; E) = \bar{\mathcal{G}}_\alpha^{B\dagger}(k; E) A_{BB'}(E) \mathcal{G}_\beta^{B'}(k'; E)$$



$$G_\alpha^{B*} \frac{1}{E - m_B} G_\beta^B$$

$$V_{\alpha, \beta}$$

$$G_{MN}^B(k) = \frac{g_{MN}^B}{m_M} \frac{k}{\sqrt{\omega_M(k)}} u(k).$$

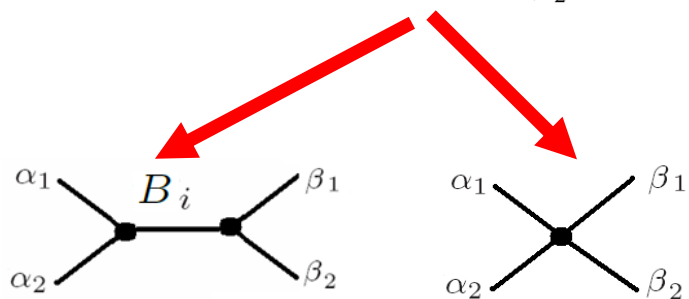
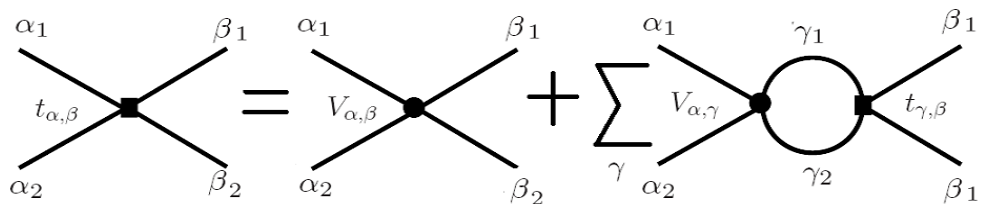
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$$t_{\alpha\beta}(k, k'; E) = f_\alpha(k) \tilde{t}_{\alpha\beta}(E) f_\beta(k') \quad \tilde{t}_{\alpha\beta}(E) = v_{\alpha\beta} + \sum_\gamma \int dq q^2 \frac{v_{\alpha\gamma} f_\gamma(q)^2}{E - \omega_\gamma(q) + i\epsilon} \tilde{t}_{\gamma\beta}(E)$$

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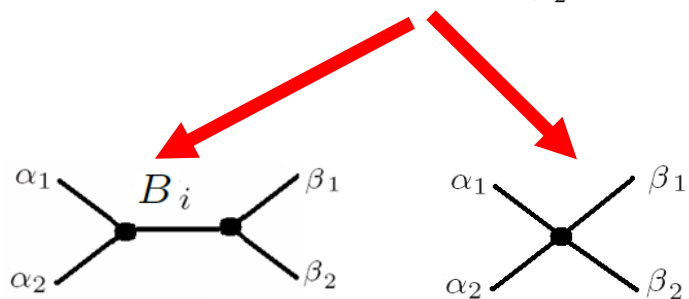
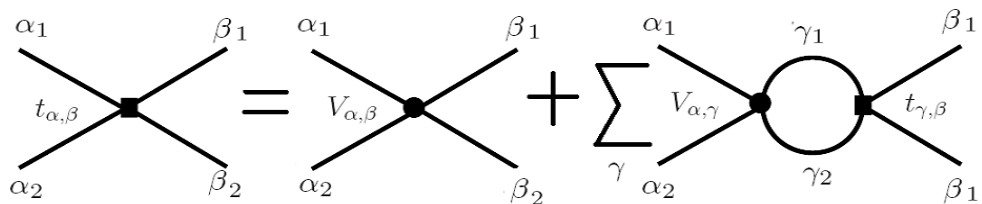
$$\mathcal{G}_\alpha^B(k; E) = G_\alpha^B + \sum_\gamma f_\alpha(k) \tilde{t}_{\alpha\gamma}(E) g_{f,\gamma}^B(E) \quad g_{f,\gamma}^B(E) = \int dq q^2 \frac{f_\gamma(q) G_\gamma^B(q)}{E - \omega_\gamma(q) + i\epsilon}$$

$$\bar{\mathcal{G}}_\alpha^B(k; E) = G_\alpha^{B*} + \sum_\gamma \bar{g}_{f,\gamma}^B(E) \tilde{t}_{\gamma\alpha}(E) f_\alpha(k) \quad \bar{g}_{f,\gamma}^B(E) = \int dq q^2 \frac{f_\gamma(q) G_\gamma^{B*}(q)}{E - \omega_\gamma(q) + i\epsilon}$$



HEFT介绍

$$T_{\alpha\beta}(k_\alpha, k_\beta, E) = V_{\alpha\beta}(k_\alpha, k_\beta) + \sum_\gamma \int k_\gamma^2 dk_\gamma \frac{V_{\alpha\gamma}(k_\alpha, k_\gamma) T_{\gamma\beta}(k_\gamma, k_\beta, E)}{E - \sqrt{m_{\gamma 1}^2 + k_\gamma^2} - \sqrt{m_{\gamma 2}^2 + k_\gamma^2} + i\epsilon}$$



$$G_\alpha^{B*} \frac{1}{E - m_B} G_\beta^B \quad V_{\alpha, \beta}$$

$$G_{MN}^B(k) = \frac{g_{MN}^B}{m_M} \frac{k}{\sqrt{\omega_M(k)}} u(k), \quad v_{\alpha\beta}(k, k') = v_{\alpha\beta} f_\alpha(k) f_\beta(k')$$

$$f(k) = \frac{1}{m_M} \frac{k}{\omega_M(k)} u(k)$$

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$$T_{\alpha\beta}^{\text{bare}}(k, k'; E) = \bar{G}_\alpha^{B\dagger}(k; E) A_{BB'}(E) G_\beta^{B'}(k'; E)$$

$$G_\alpha^B(k; E) = G_\alpha^B + \sum_\gamma f_\alpha(k) \tilde{t}_{\alpha\gamma}(E) g_{f,\gamma}^B(E) \quad g_{f,\gamma}^B(E) = \int dq q^2 \frac{f_\gamma(q) G_\gamma^B(q)}{E - \omega_\gamma(q) + i\epsilon}$$

$$\bar{G}_\alpha^B(k; E) = G_\alpha^{B*} + \sum_\gamma \bar{g}_{f,\gamma}^B(E) \tilde{t}_{\gamma\alpha}(E) f_\alpha(k) \quad \bar{g}_{f,\gamma}^B(E) = \int dq q^2 \frac{f_\gamma(q) G_\gamma^{B*}(q)}{E - \omega_\gamma(q) + i\epsilon}$$

$$A_{BB'}^{-1}(E) = \delta_{BB'}(E - m_B) - \bar{\Sigma}_{BB'}(E)$$

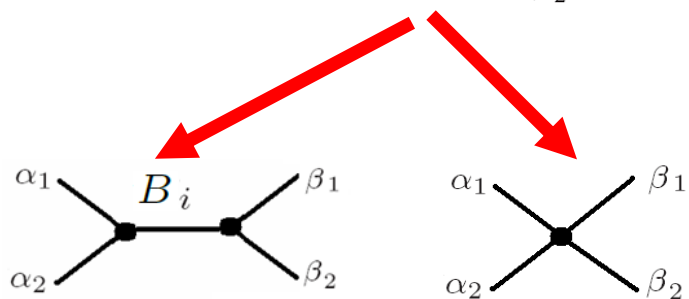
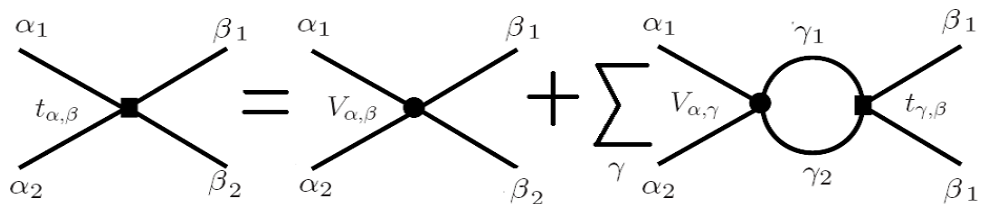
$$\bar{\Sigma}_{BB'}(E) = \Sigma_{BB'}(E) + \Sigma_{BB'}^I(E) \quad \Sigma_{BB'}(E) = \sum_\gamma \int dq q^2 \frac{G_\gamma^B(q) G_\gamma^{B'*}(q)}{E - \omega_\gamma(k) + i\epsilon}$$

$$\Sigma_{BB'}^I(E) = \sum_{\alpha, \beta} \bar{g}_{f,\alpha}^B(E) \tilde{t}_{\alpha\beta}(E) g_{f,\beta}^{B'}(E)$$



HEFT介绍

$$T_{\alpha\beta}(k_\alpha, k_\beta, E) = V_{\alpha\beta}(k_\alpha, k_\beta) + \sum_\gamma \int k_\gamma^2 dk_\gamma \frac{V_{\alpha\gamma}(k_\alpha, k_\gamma) T_{\gamma\beta}(k_\gamma, k_\beta, E)}{E - \sqrt{m_{\gamma 1}^2 + k_\gamma^2} - \sqrt{m_{\gamma 2}^2 + k_\gamma^2} + i\epsilon}$$



$$G_\alpha^{B*} \frac{1}{E - m_B} G_\beta^B \quad V_{\alpha,\beta}$$

$$G_{MN}^B(k) = \frac{g_{MN}^B}{m_M} \frac{k}{\sqrt{\omega_M(k)}} u(k), \quad v_{\alpha\beta}(k, k') = v_{\alpha\beta} f_\alpha(k) f_\beta(k')$$

$$f(k) = \frac{1}{m_M} \frac{k}{\omega_M(k)} u(k)$$

$$T_{\alpha\beta}(k, k'; E) = t_{\alpha\beta}(k, k'; E) + T_{\alpha\beta}^{\text{bare}}(k, k'; E)$$

$$t_{\alpha\beta}(k, k'; E) = V_{\alpha\beta}(k, k') + \sum_\gamma \int dq q^2 \frac{V_{\alpha\gamma}(k, q) T_{\gamma\beta}(q, k'; E)}{E - \omega_\gamma(q) + i\epsilon}$$

$$t_{\alpha\beta}(k, k'; E) = f_\alpha(k) \tilde{t}_{\alpha\beta}(E) f_\beta(k') \quad \tilde{t}_{\alpha\beta}(E) = v_{\alpha\beta} + \sum_\gamma \int dq q^2 \frac{v_{\alpha\gamma} f_\gamma(q)^2}{E - \omega_\gamma(q) + i\epsilon} \tilde{t}_{\gamma\beta}(E)$$

$$T_{\alpha\beta}^{\text{bare}}(k, k'; E) = \bar{G}_\alpha^{B\dagger}(k; E) A_{BB'}(E) G_\beta^{B'}(k'; E)$$

$$G_\alpha^B(k; E) = G_\alpha^B + \sum_\gamma f_\alpha(k) \tilde{t}_{\alpha\gamma}(E) g_{f,\gamma}^B(E) \quad g_{f,\gamma}^B(E) = \int dq q^2 \frac{f_\gamma(q) G_\gamma^B(q)}{E - \omega_\gamma(q) + i\epsilon}$$

$$\bar{G}_\alpha^B(k; E) = G_\alpha^{B*} + \sum_\gamma \bar{g}_{f,\gamma}^B(E) \tilde{t}_{\gamma\alpha}(E) f_\alpha(k) \quad \bar{g}_{f,\gamma}^B(E) = \int dq q^2 \frac{f_\gamma(q) G_\gamma^{B*}(q)}{E - \omega_\gamma(q) + i\epsilon}$$

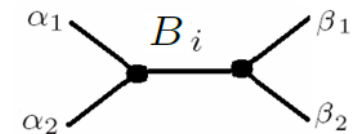
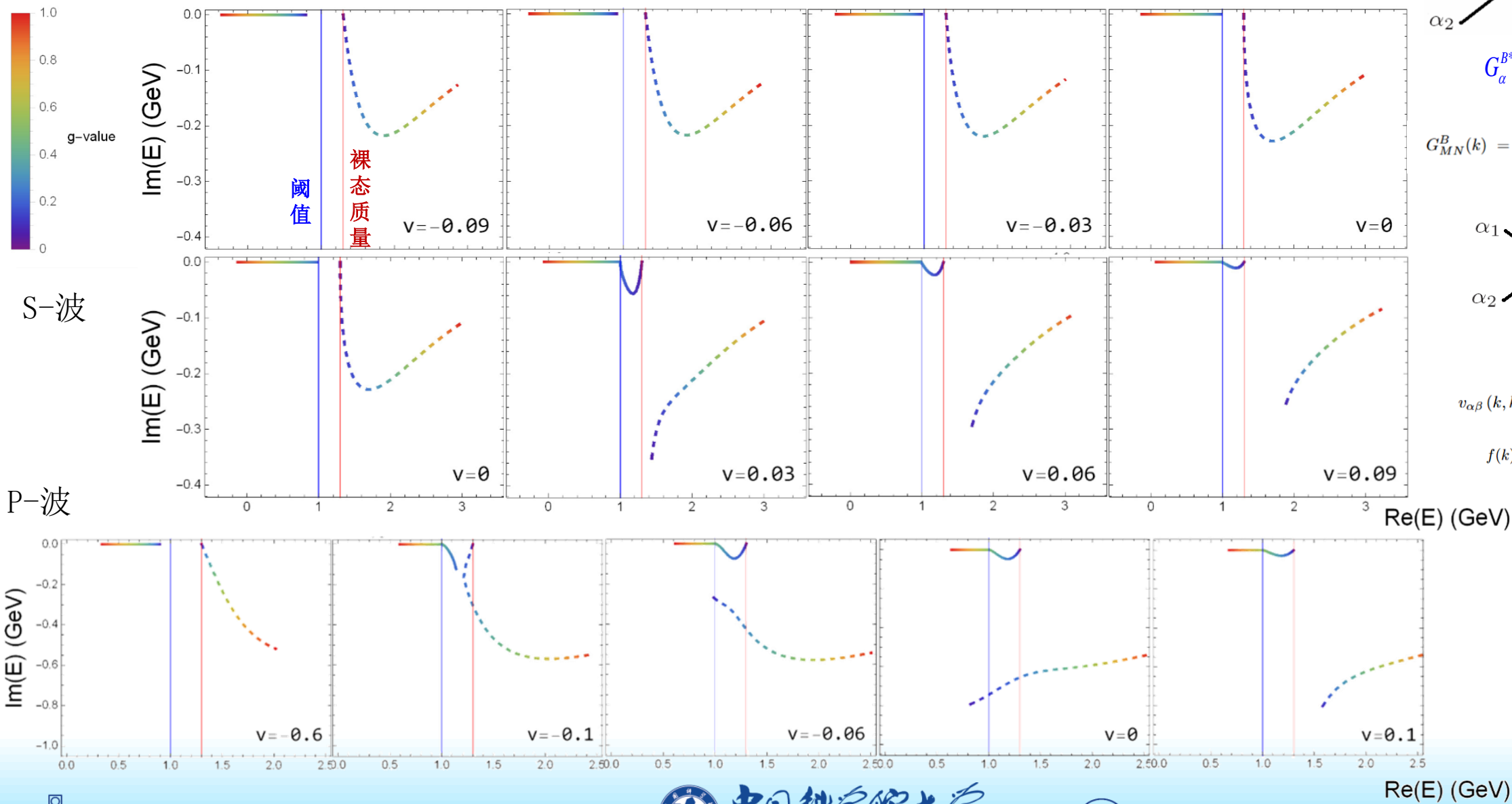
$$A_{BB'}^{-1}(E) = \delta_{BB'}(E - m_B) - \bar{\Sigma}_{BB'}(E) \quad \det[A^{-1}] = 0$$

$$\bar{\Sigma}_{BB'}(E) = \Sigma_{BB'}(E) + \Sigma_{BB'}^I(E) \quad \Sigma_{BB'}(E) = \sum_\gamma \int dq q^2 \frac{G_\gamma^B(q) G_\gamma^{B'*}(q)}{E - \omega_\gamma(k) + i\epsilon}$$

$$\Sigma_{BB'}^I(E) = \sum_{\alpha,\beta} \bar{g}_{f,\alpha}^B(E) \tilde{t}_{\alpha\beta}(E) g_{f,\beta}^{B'}(E)$$

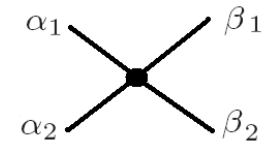


HEFT介绍----奇点的轨迹 (初步)



$$G_a^{B^*} \frac{1}{E - m_B} G_\beta^B$$

$$G_{MN}^B(k) = \frac{g_{MN}^B}{m_M} \frac{k}{\sqrt{\omega_M(k)}} u(k).$$



$$V_{\alpha,\beta}$$

$$v_{\alpha\beta}(k, k') = v_{\alpha\beta} f_\alpha(k) f_\beta(k')$$

$$f(k) = \frac{1}{m_M^2} \frac{k}{\omega_M(k)} u(k)$$



Tcc-X(3872)

$$H = H_0 + H_I$$

$$H_0 = \sum_{i=1,n} |B_i\rangle m_i \langle B_i| + \sum_{\alpha} |\alpha(k_{\alpha})\rangle \left[\sqrt{m_{\alpha 1}^2 + k_{\alpha}^2} + \sqrt{m_{\alpha 2}^2 + k_{\alpha}^2} \right] \langle \alpha(k_{\alpha})|$$

$|B_i\rangle$ bare state, bare mass m_i

$|\alpha(k_{\alpha})\rangle$ non-interaction channels

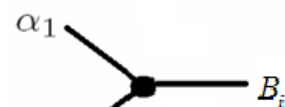
$$H_I = \hat{g} + \hat{v}$$

$$\hat{g} = \sum_{\alpha} \sum_{i=1,n} \left[|\alpha(k_{\alpha})\rangle g_{i,\alpha}^+ \langle B_i| + |B_i\rangle g_{i,\alpha} \langle \alpha(k_{\alpha})| \right]$$

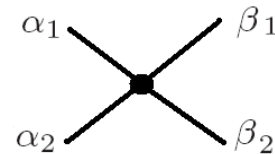
$$\hat{v} = \sum_{\alpha,\beta} |\alpha(k_{\alpha})\rangle v_{\alpha,\beta} \langle \beta(k_{\beta})|$$

夸克胶子层次
的相互作用

强子层次
相互作用



3P0模型，利用从夸克模型中得到的裸态波函数。



单玻色子交换 OBE

T 矩阵
(相移, 非弹性系数)

共振态
(质量, 宽度, 极点位置, 耦合强度)

HEFT

格点能谱

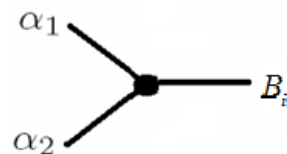


HEFT介绍

$$H = H_0 + H_I = H_0 + g + \hat{v}$$

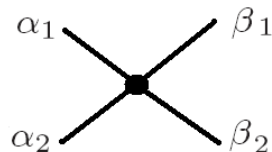
$$H_0 = \sum_{i=1,n} |B_i\rangle m_i \langle B_i| + \sum_{\alpha} |\alpha(k_{\alpha})\rangle \left[\sqrt{m_{\alpha 1}^2 + k_{\alpha}^2} + \sqrt{m_{\alpha 2}^2 + k_{\alpha}^2} \right] \langle \alpha(k_{\alpha})|$$

$$\hat{g} = \sum_{\alpha} \sum_{i=1,n} \left[|\alpha(k_{\alpha})\rangle g_{i,\alpha}^+ \langle B_i| + |B_i\rangle g_{i,\alpha} \langle \alpha(k_{\alpha})| \right]$$



3P0模型，利用从夸克模型中得到的裸态波函数。

$$\hat{v} = \sum_{\alpha,\beta} |\alpha(k_{\alpha})\rangle v_{\alpha,\beta} \langle \beta(k_{\beta})|$$



单玻色子交换 OBE

共振态
(质量, 宽度, 极点位置, 耦合强度)

HEFT

T 矩阵
(相移, 非弹
系数)

格点能谱

问题：两种相互作用怎么办？

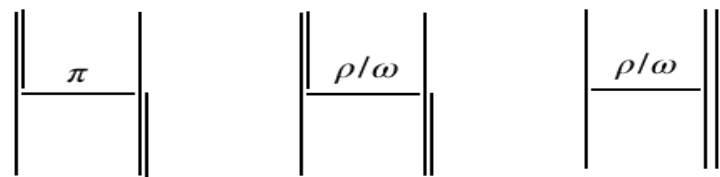
a+b=5的解有太多了

以T_{cc}和X(3872)给出方案



单玻色子交换势能 DD^* vs $D\bar{D}^*$

D 和 D^* 在单玻色子交换势下 (OBE)



$$V_\pi = \frac{g^2}{f_\pi^2} \frac{(q \cdot \epsilon_\lambda)(q \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_\pi^2},$$

$$V_{\rho/\omega}^u = -2\lambda^2 g_V^2 \frac{(\epsilon_{\lambda'}^\dagger \cdot q)(\epsilon_\lambda \cdot q) - q^2 (\epsilon_\lambda \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_{\rho/\omega}^2},$$

$$V_{\rho/\omega}^t = \frac{\beta^2 g_V^2}{2} \frac{(\epsilon_\lambda \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_{\rho/\omega}^2}. \quad \text{PWA 仅仅S波}$$

$$\mathcal{V}(l, l', S, j) = \frac{1}{(2\pi)^3} \sqrt{\frac{1}{2E_D^i 2E_D^f 2E_K^i 2E_K^f}} \\ 2\pi \int d\cos\theta V^v(\vec{p}_f, \vec{p}_i) \left(\frac{\Lambda^2}{\Lambda^2 + p_f^2}\right)^2 \left(\frac{\Lambda^2}{\Lambda^2 + p_i^2}\right)^2$$

- $g = 0.57$ 从 $D^* \rightarrow D\pi$ 的衰变宽度获得, λ & β 是自由参数

重夸克对称性

$$H_a^{(Q)} = \frac{1+\not{v}}{2} [P_a^{*\mu} \gamma_\mu - P_a \gamma_5] \quad \boxed{D^{(*)} D^{(*)}}$$

$$\bar{H}_a^{(Q)} \equiv \gamma_0 H^{(Q)\dagger} \gamma_0 = [P_a^{*\mu} \gamma_\mu + P_a^\dagger \gamma_5] \frac{1+\not{v}}{2}$$

$$P = (D^0, D^+, D_s^+) \& P^* = (D^{*0}, D^{*+}, D_s^{*+})$$

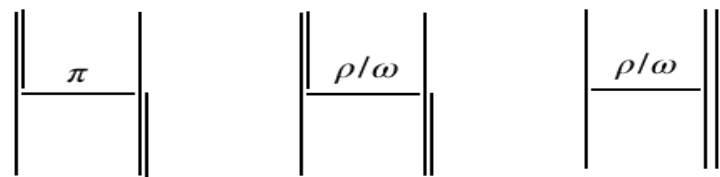
$$\mathcal{L}_{MH^{(Q)}H^{(Q)}} = ig \text{Tr} \left[H_b^{(Q)} \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a^{(Q)} \right]$$

$$\mathcal{L}_{VH^{(Q)}H^{(Q)}} = i\beta \text{Tr} \left[H_b^{(Q)} v_\mu (V_{ba}^\mu - \rho_{ba}^\mu) \bar{H}_a^{(Q)} \right] \\ + i\lambda \text{Tr} \left[H_b^{(Q)} \sigma_{\mu\nu} F^{\mu\nu} (\rho)_{ba} \bar{H}_a^{(Q)} \right]$$



单玻色子交换势能 DD^* vs $D\bar{D}^*$

D 和 D^* 在单玻色子交换势下 (OBE)



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$$V_{\rho/\omega}^t = \frac{\beta^2 g_V^2}{2} \frac{(\epsilon_\lambda \cdot \epsilon_\lambda^\dagger)}{q^2 - m_{\rho/\omega}^2}.$$

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$$\mathcal{V}(l, l', S, j) = \frac{1}{(2\pi)^3} \sqrt{\frac{1}{2E_D^i 2E_D^f 2E_K^i 2E_K^f}}$$

$$2\pi \int d\cos\theta V^v(\vec{p}_f, \vec{p}_i) \left(\frac{\Lambda^2}{\Lambda^2 + p_f^2}\right)^2 \left(\frac{\Lambda^2}{\Lambda^2 + p_i^2}\right)^2$$

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$$D^{(*)} D^{(*)}$$

$$\bar{H}_a^{(Q)} \equiv \gamma_0 H_a^{(Q)\dagger} \gamma_0 = [P_a^{*\dagger} \gamma_\mu + P_a^\dagger \gamma_5] \frac{1+\not{p}}{2}$$

$$P = (D^0, D^+, D_s^+) \& P^* = (D^{*0}, D^{*+}, D_s^{*+})$$

$$\mathcal{L}_{MH^{(Q)}H^{(Q)}} = ig \text{Tr} [H_b^{(Q)} \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a^{(Q)}]$$

$$\mathcal{L}_{VH^{(Q)}H^{(Q)}} = i\beta \text{Tr} [H_b^{(Q)} v_\mu (V_{ba}^\mu - \rho_{ba}^\mu) \bar{H}_a^{(Q)}] + i\lambda \text{Tr} [H_b^{(Q)} \sigma_{\mu\nu} F^{\mu\nu}(\rho)_{ba} \bar{H}_a^{(Q)}]$$

$$H_a^{(\bar{Q})} \equiv C (\mathcal{C} H_a^{(Q)} \mathcal{C}^{-1})^T \mathcal{C}^{-1} = [P_{a\mu}^{(\bar{Q})} \gamma^\mu - P_a^{(\bar{Q})} \gamma_5] \frac{1-\not{p}}{2}$$

$$\bar{H}_a^{(\bar{Q})} \equiv \gamma_0 H_a^{(\bar{Q})\dagger} \gamma_0 = \frac{1-\not{p}}{2} [P_{a\mu}^{(\bar{Q})} \gamma^\mu + P_a^{(\bar{Q})} \gamma_5]$$

$$\tilde{P} = (\bar{D}^0, D^-, D_s^-) \& \tilde{P}^* = (\bar{D}^{*0}, D^{*-}, D_s^{*-})$$

$$\mathcal{L}_{MH^{(\bar{Q})}H^{(\bar{Q})}} = ig \text{Tr} [\bar{H}_a^{(\bar{Q})} \gamma_\mu \gamma_5 A_{ab}^\mu H_b^{(\bar{Q})}]$$

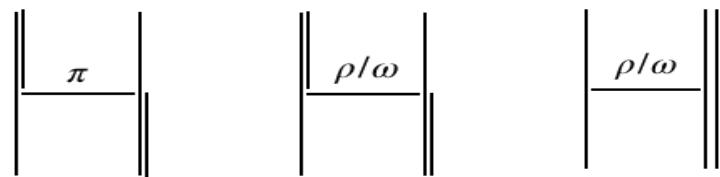
$$\mathcal{L}_{VH^{(\bar{Q})}H^{(\bar{Q})}} = -i\beta \text{Tr} [\bar{H}_a^{(\bar{Q})} v_\mu (V_{ab}^\mu - \rho_{ab}^\mu) H_b^{(\bar{Q})}]$$

$$D^{(*)} \bar{D}^{(*)} + i\lambda \text{Tr} [\bar{H}_a^{(\bar{Q})} \sigma_{\mu\nu} F_{ab}^{\prime\mu\nu}(\rho) H_b^{(\bar{Q})}]$$



单玻色子交换势能 DD^* vs $D\bar{D}^*$

D 和 D^* 在单玻色子交换势下 (OBE)



$$V_\pi = \frac{g^2}{f_\pi^2} \frac{(q \cdot \epsilon_\lambda)(q \cdot \epsilon_\lambda^\dagger)}{q^2 - m_\pi^2},$$

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$$2\pi \int d\cos\theta V^v(\vec{p}_f, \vec{p}_i) \left(\frac{\Lambda^2}{\Lambda^2 + p_f^2}\right)^2 \left(\frac{\Lambda^2}{\Lambda^2 + p_i^2}\right)^2$$

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$$P = (D^0, D^+, D_s^+) \& P^* = (D^{*0}, D^{*+}, D_s^{*+})$$

$$\mathcal{L}_{MH^{(Q)}H^{(Q)}} = ig \text{Tr} \left[H_b^{(Q)} \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a^{(Q)} \right]$$

$$\mathcal{L}_{VH^{(Q)}H^{(Q)}} = i\beta \text{Tr} \left[H_b^{(Q)} v_\mu (V_{ba}^\mu - \rho_{ba}^\mu) \bar{H}_a^{(Q)} \right]$$

$$+ i\lambda \text{Tr} \left[H_b^{(Q)} \sigma_{\mu\nu} F^{\mu\nu} (\rho)_{ba} \bar{H}_a^{(Q)} \right]$$

$$H_a^{(\bar{Q})} \equiv C (\mathcal{C} H_a^{(Q)} \mathcal{C}^{-1})^T C^{-1} = [P_{a\mu}^{(\bar{Q})} \gamma^\mu - P_a^{(\bar{Q})} \gamma_5] \frac{1-\not{p}}{2}$$

$$\bar{H}_a^{(\bar{Q})} \equiv \gamma_0 H_a^{(\bar{Q})\dagger} \gamma_0 = \frac{1-\not{p}}{2} [P_{a\mu}^{(\bar{Q})} \gamma^\mu + P_a^{(\bar{Q})} \gamma_5]$$

$$\tilde{P} = (\bar{D}^0, D^-, D_s^-) \& \tilde{P}^* = (\bar{D}^{*0}, D^{*-}, D_s^{*-})$$

$$\mathcal{L}_{MH^{(\bar{Q})}H^{(\bar{Q})}} = ig \text{Tr} \left[\bar{H}_a^{(\bar{Q})} \gamma_\mu \gamma_5 A_{ab}^\mu H_b^{(\bar{Q})} \right]$$


$$\mathcal{L}_{VH^{(\bar{Q})}H^{(\bar{Q})}} = -i\beta \text{Tr} \left[\bar{H}_a^{(\bar{Q})} v_\mu (V_{ab}^\mu - \rho_{ab}^\mu) H_b^{(\bar{Q})} \right]$$

$$\boxed{D^{(*)} \bar{D}^{(*)}} + i\lambda \text{Tr} \left[\bar{H}_a^{(\bar{Q})} \sigma_{\mu\nu} F_{ab}^{\prime\mu\nu} (\rho) H_b^{(\bar{Q})} \right]$$

	wave function	$I(J^{PC})$	u -channel : π	u -channel : ρ/ω	t -channel : ρ/ω
DD^*	$\frac{1}{\sqrt{2}}(D^+D^{*0} - D^0D^{*+})$	$0(1^+) [T_{cc}^+]$	$\frac{3}{2}V_\pi$	$\frac{3}{2}V_\rho^u - \frac{1}{2}V_\omega^u$	$-\frac{3}{2}V_\rho^t + \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}(D^+D^{*0} + D^0D^{*+})$	$1(1^+)$	$\frac{1}{2}V_\pi$	$\frac{1}{2}V_\rho^u + \frac{1}{2}V_\omega^u$	$\frac{1}{2}V_\rho^t + \frac{1}{2}V_\omega^t$
$D\bar{D}^*$	$\frac{1}{\sqrt{2}}([D^+D^{*-}] + [D^0\bar{D}^{*0}])$	$0(1^{++})[X(3872)]$	$\frac{3}{2}V_\pi$	$-\frac{3}{2}V_\rho^u - \frac{1}{2}V_\omega^u$	$-\frac{3}{2}V_\rho^t - \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}([D^+D^{*-}] - [D^0\bar{D}^{*0}])$	$1(1^{++})$	$-\frac{1}{2}V_\pi$	$\frac{1}{2}V_\rho^u - \frac{1}{2}V_\omega^u$	$\frac{1}{2}V_\rho^t - \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}(\{D^+D^{*-}\} + \{D^0\bar{D}^{*0}\})$	$0(1^{+-})[h_c]$	$-\frac{3}{2}V_\pi$	$\frac{3}{2}V_\rho^u + \frac{1}{2}V_\omega^u$	$-\frac{3}{2}V_\rho^t - \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}(\{D^+D^{*-}\} - \{D^0\bar{D}^{*0}\})$	$1(1^{+-}) [Z_c(3900)]$	$\frac{1}{2}V_\pi$	$-\frac{1}{2}V_\rho^u + \frac{1}{2}V_\omega^u$	$\frac{1}{2}V_\rho^t - \frac{1}{2}V_\omega^t$

带电和中性粒子的质量不同会导致同位旋破坏, 因此在实际计算中我们的态矢量直接使用粒子态而不是同位旋本征态。

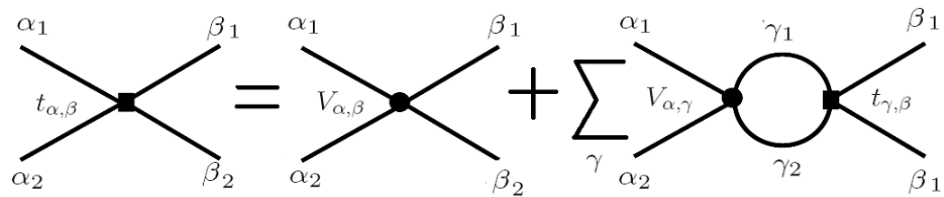
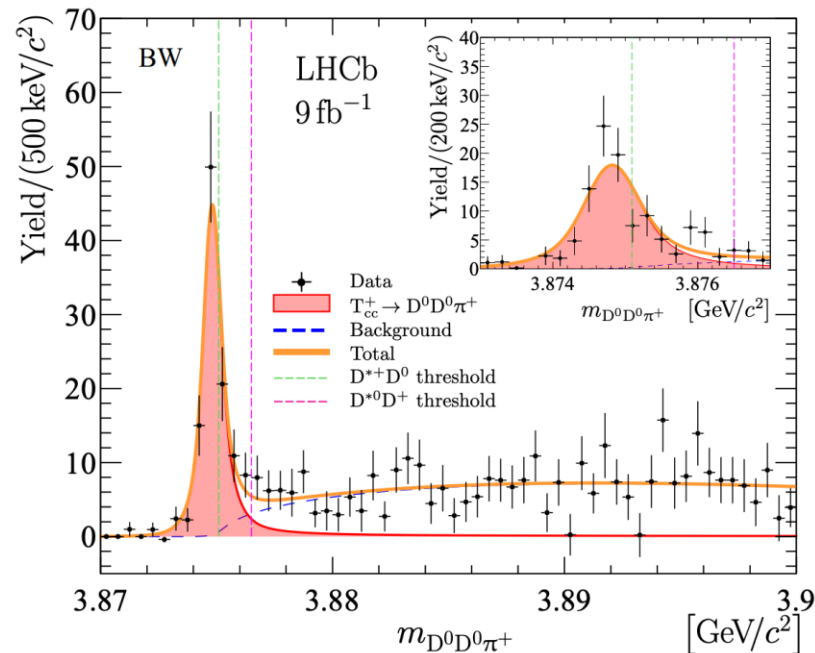
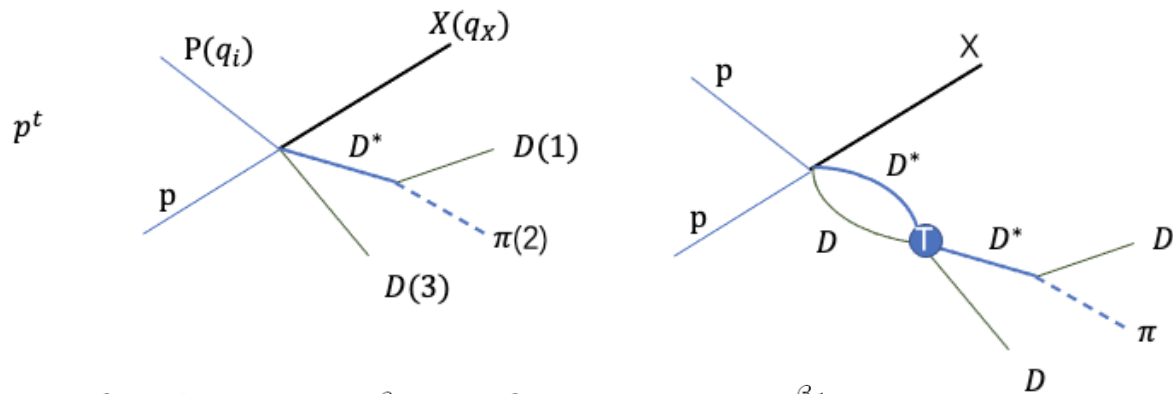


T_{cc}  $DD^*, D\bar{D}^*$
interaction



T_{cc} 的产生

$$pp \rightarrow X D^0 D^0 \pi^+$$



$$t_{\alpha,\beta}(k_\alpha, k_\beta, E) = V_{\alpha,\beta}(k_\alpha, k_\beta) + \sum_\gamma \int k_\gamma^2 dk_\gamma \frac{V_{\alpha,\gamma}(k_\alpha, k_\gamma) t_{\gamma,\beta}(k_\gamma, k_\beta, E)}{E - \sqrt{m_{\gamma_1}^2 + k_\gamma^2} - \sqrt{m_{\gamma_2}^2 + k_\gamma^2} + i\epsilon}$$

$$|\mathcal{M}|^2 = |a_{pp \rightarrow DD^* X}|^2 \sum_{\lambda_X} \epsilon_\mu(p_X, \lambda_X) \epsilon_{\mu'}^\dagger(p_X, \lambda_X) \sum_j \mathcal{B}_{j\mu} \mathcal{B}_j^{\dagger\mu'}$$

$$\mathcal{B}_j^\mu(p_{12}, p_{23}) = g \left\{ \frac{-i(p_\pi^\mu - \frac{p_{12}^\mu p_{12} \cdot p_\pi}{m_{D^*}^2})}{p_{12}^2 - m_{D^*}^2 + im_{D^*} \Gamma_{D^*}} \right\}_j + \sum_{i=1,2} ig \left\{ \int dq_{D^*} q_{D^*}^2 \frac{d\Omega_{q_{D^*}}}{4\pi} \frac{\sqrt{2w_{D_2}}}{\sqrt{2w_{D^*}}} \frac{\sqrt{2w_{D_{12}^*}}}{\sqrt{2w_D}} \frac{T_{ij}^{J00}(M, |q_{D^*}|, |p_{12}|)}{(M - w_{D^*}^i) - w_D^i + i\epsilon} \frac{\epsilon_a^{*\mu}(w_{D^*}, q_{D^*}) \epsilon_a(p_{12}) \cdot p_\pi}{p_{12}^2 - m_{D^*}^2 + im_{D^*} \Gamma_{D^*}} \right\}_j + (p_{D_1} \rightarrow p_{D_2})$$



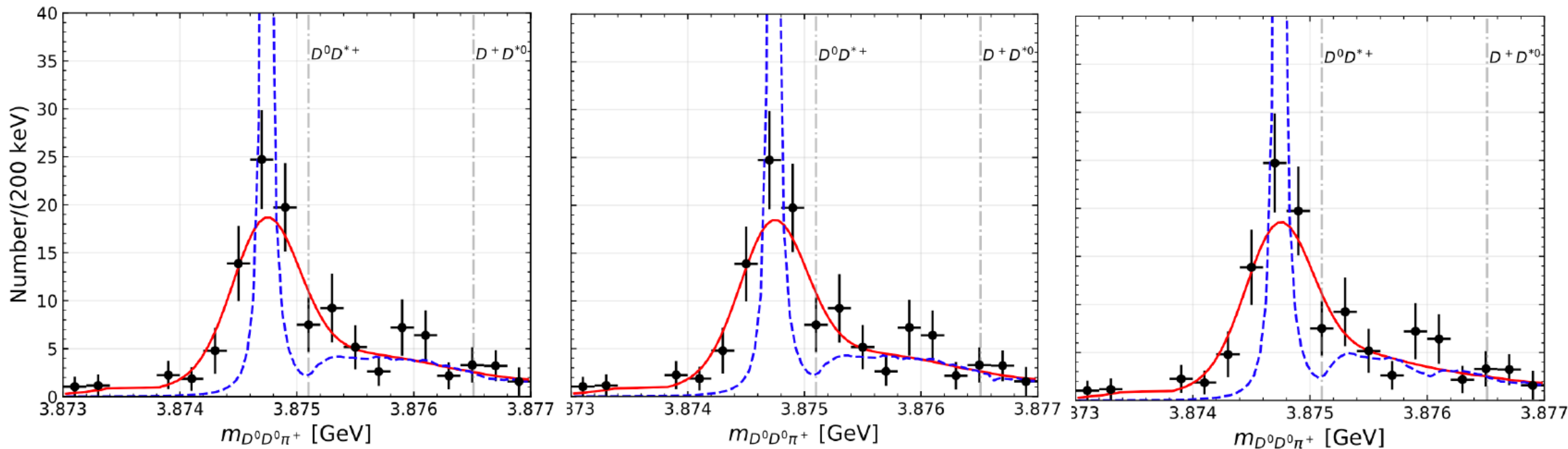
检查阶段参数的稳定性

T_{cc} 的产生

$$pp \rightarrow X D^0 D^0 \pi^+$$

Λ (fixed)	λ (/GeV)	β
0.8 GeV	0.890 ± 0.20	0.810 ± 0.11
1 GeV	0.683 ± 0.025	0.687 ± 0.017
1.2 GeV	0.587 ± 0.21	0.550 ± 0.12
1.17 GeV	0.56	0.9

Cheng, et al. PRD 106,016012



Λ (GeV)	BE (keV)	Γ (keV)	$\sqrt{\langle r^2 \rangle}$	$I = 0$	$I = 1$	$P(D^0 D^{*+})$	$P(D^+ D^{*0})$	$\frac{\text{Res}(D^0 D^{*+})}{\text{Res}(D^+ D^{*0})}$
0.8	-387.7	67.3	4.8 fm	95.8%	4.2%	70.0%	30.0%	$-1.063 + 0.001I$
1.0	-393.0	70.4	4.7 fm	95.8%	4.2%	70.0%	30.0%	$-1.055 + 0.001I$
1.2	-391.6	72.7	4.7 fm	95.7%	4.3%	70.3%	29.7%	$-1.052 + 0.001I$

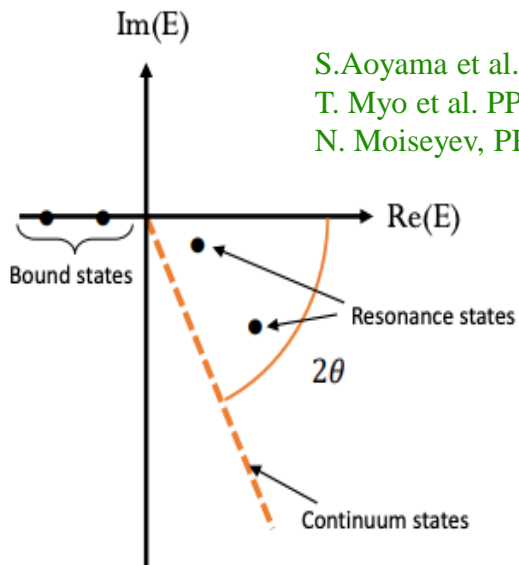


T_{cc} 的性质

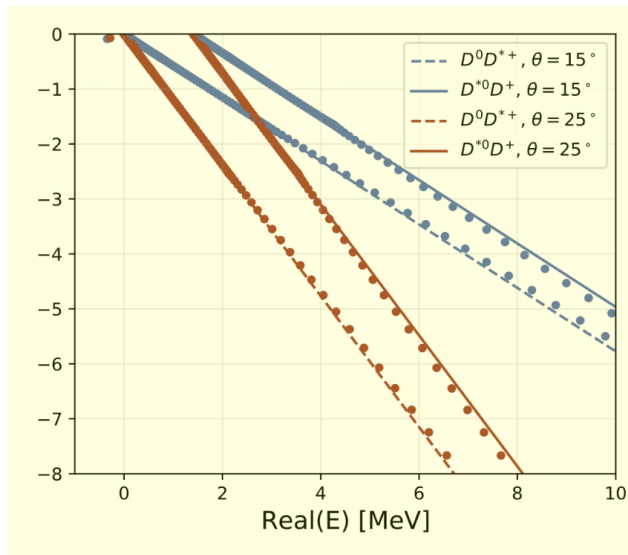
Complex scaling method

$$\mathbf{r} \rightarrow \mathbf{r}e^{i\theta}, \quad \mathbf{q} \rightarrow \mathbf{q}e^{-i\theta} \quad H_\theta \Phi_\theta = E_\theta \Phi_\theta,$$

$$\left[\begin{array}{l} \overline{D^{*0}D^0} / \overline{D^0D^{*0}} \\ \dots \\ D^{*-} D^+ / D^{*+} D^- \end{array} \right. \left. \begin{array}{l} \text{Coupled-channel} \\ \text{effect} \end{array} \right]$$



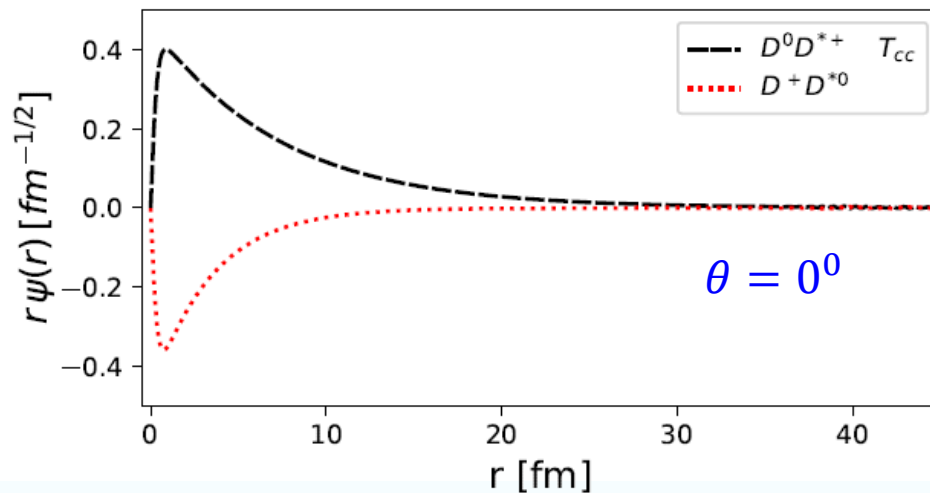
S.Aoyama et al. PTP. 116, 1 (2006).
T. Myo et al. PPNP. 79, 1 (2014)
N. Moiseyev, PR 302, 212 (1998)



- **Bound state: T_{cc}**
 $m_{T_{cc}} = 3874.7 \text{ MeV}$,
 $\Delta E = -393 \text{ keV}$
 $\Gamma_{T_{cc}} = 70.4 \text{ keV}$

- $\sqrt{\langle r^2 \rangle} = 4.7 \text{ fm}$

- 70.0% $D^{*+}D^0$, 30.0% D^+D^{*0}



- 95.8%, $DD^*(I=0)$
- 4.2% $DD^*(I=1)$

Because of mass difference

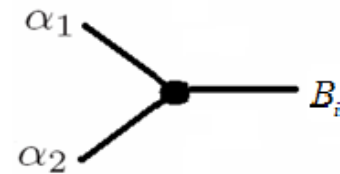
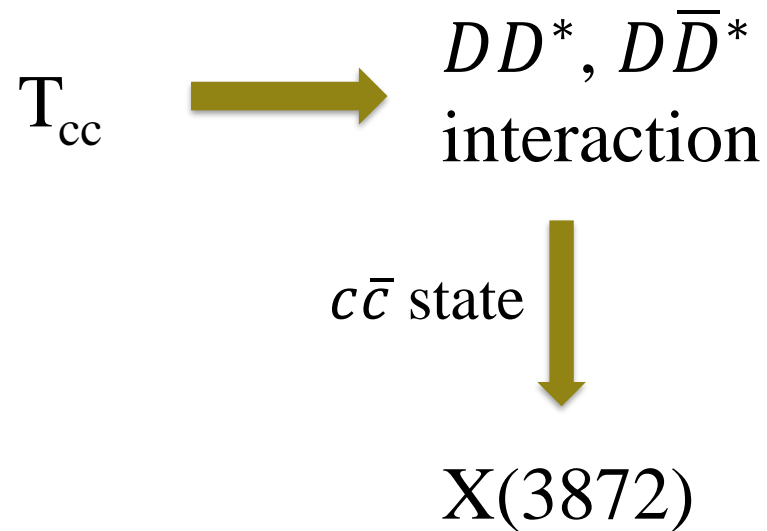
$$[I=0] = \frac{1}{\sqrt{2}}(D^{*+}D^0 - D^{*0}D^+)$$

$$[I=1] = \frac{1}{\sqrt{2}}(D^{*+}D^0 + D^{*0}D^+)$$

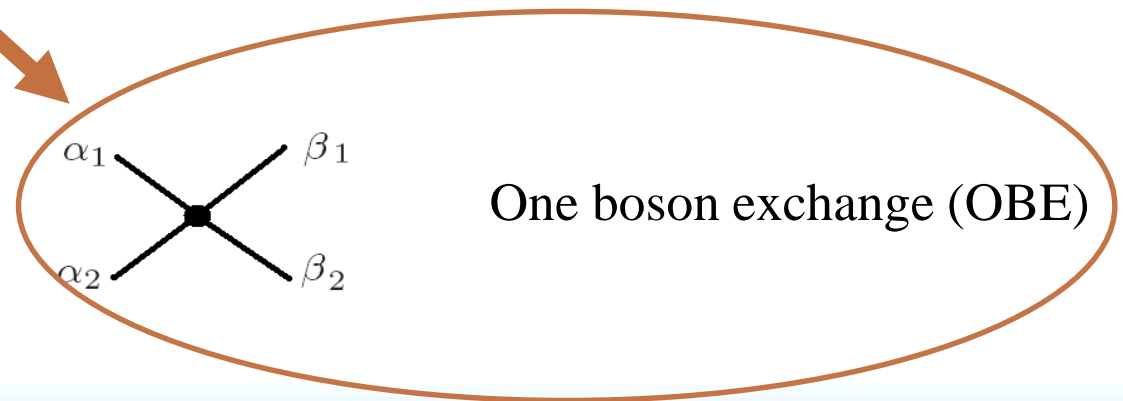


问题：两种相互作用怎么办？
a+b=5的解有太多了

利用 T_{cc} 限定强子耦合道相互作用再确定 X(3872) 的性质



From 3P0 model, and the wavefunction of quark model

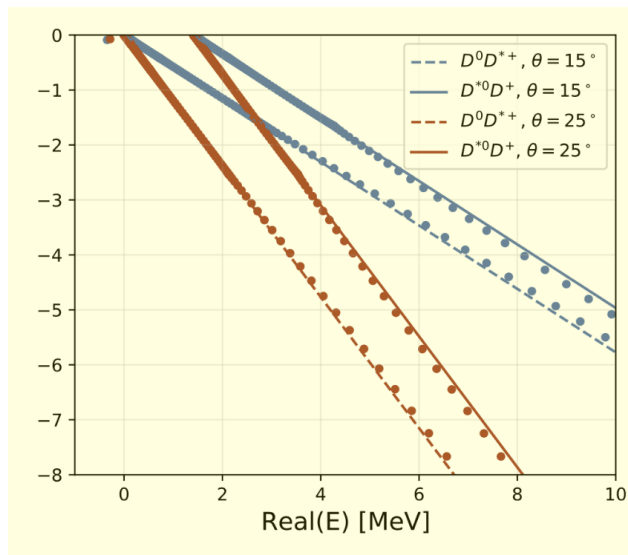
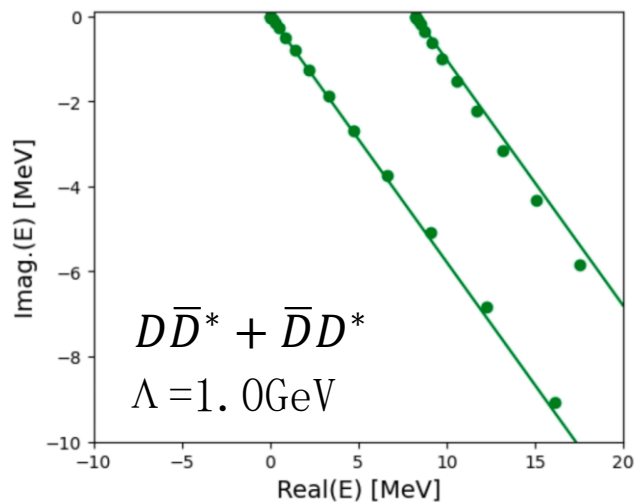


One boson exchange (OBE)



X(3872) 从纯 $D\bar{D}^* + \bar{D}D^*$ 产生

From the interaction of DD^* to obtain the interaction of $D\bar{D}^* + \bar{D}D^*$, check X(3872) exists or not by pure $D\bar{D}^* + \bar{D}D^*$ interaction, without $c\bar{c}$ state.

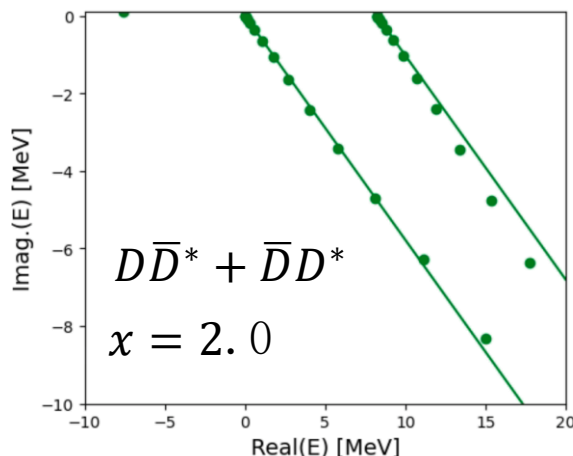
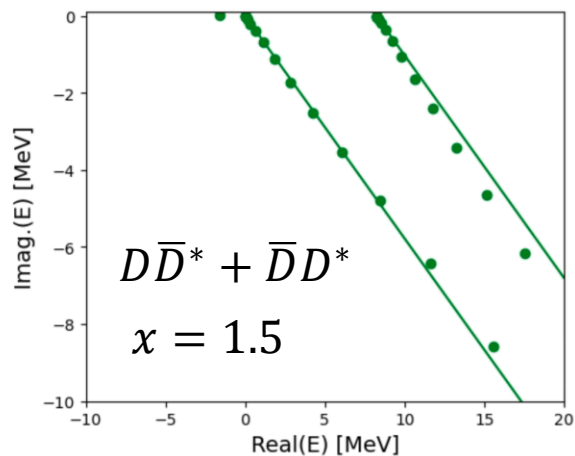


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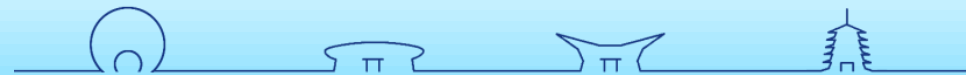
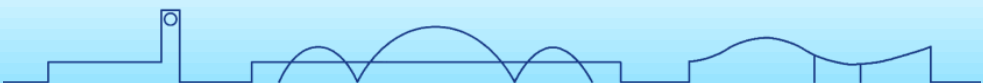
- 70.0% $D^{*+} D^0$, 30.0% $D^+ D^{*0}$

$$V'_{\bar{D}^* D} = \chi * V_{\bar{D}^* D}$$



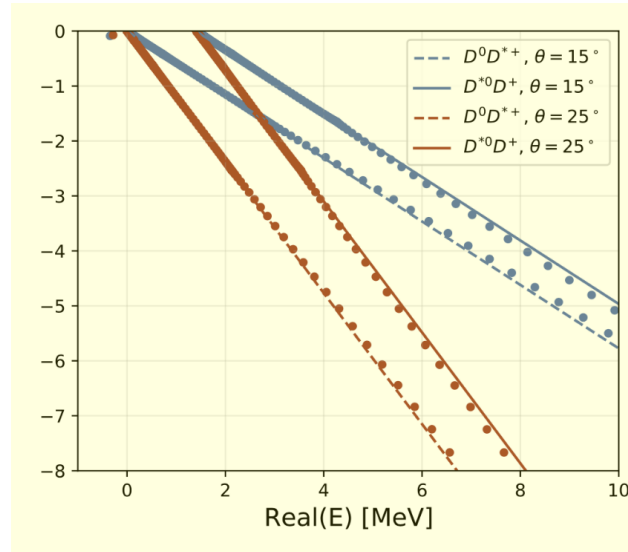
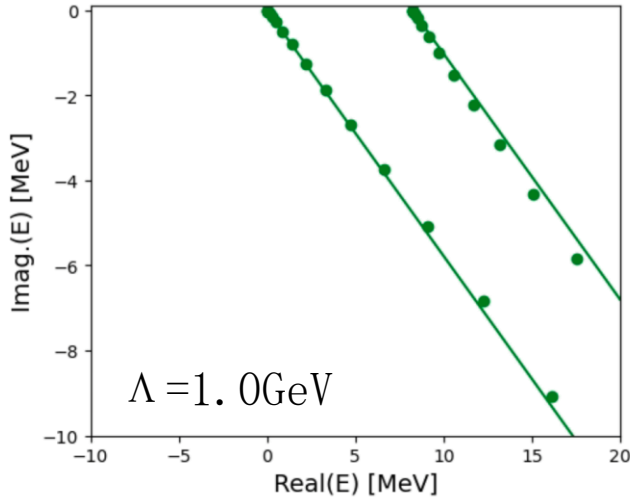
这是一个吸引势，但不足够产生一个束缚态，而只是一个虚态。

$$3870.0 + 0.26 i \text{ MeV}$$



X(3872) 从 $D\bar{D}^* + \bar{D}D^*$ 和 $c\bar{c}$ 产生

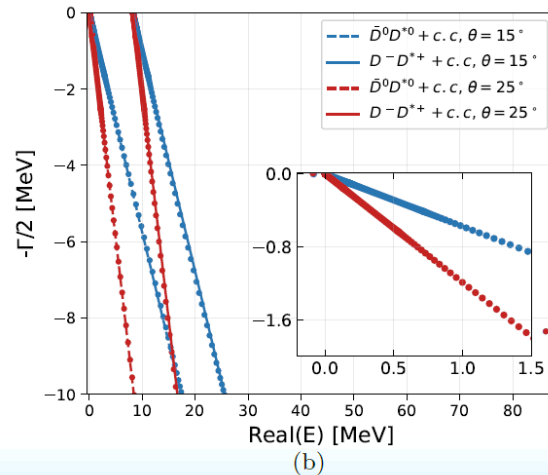
From the interaction of DD^* to obtain the intraction of $D\bar{D}^* + \bar{D}D^*$, check X(3872) exists or not by pure $D\bar{D}^* + \bar{D}D^*$ interaction, without $c\bar{c}$ state.



- **Bound state: T_{cc}**
 $m_{T_{cc}} = 3874.7 \text{ MeV}$,
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- 70.0% $D^{*+} D^0$, 30.0% $D^+ D^{*0}$

吸引势，但不足够产生一个束缚态

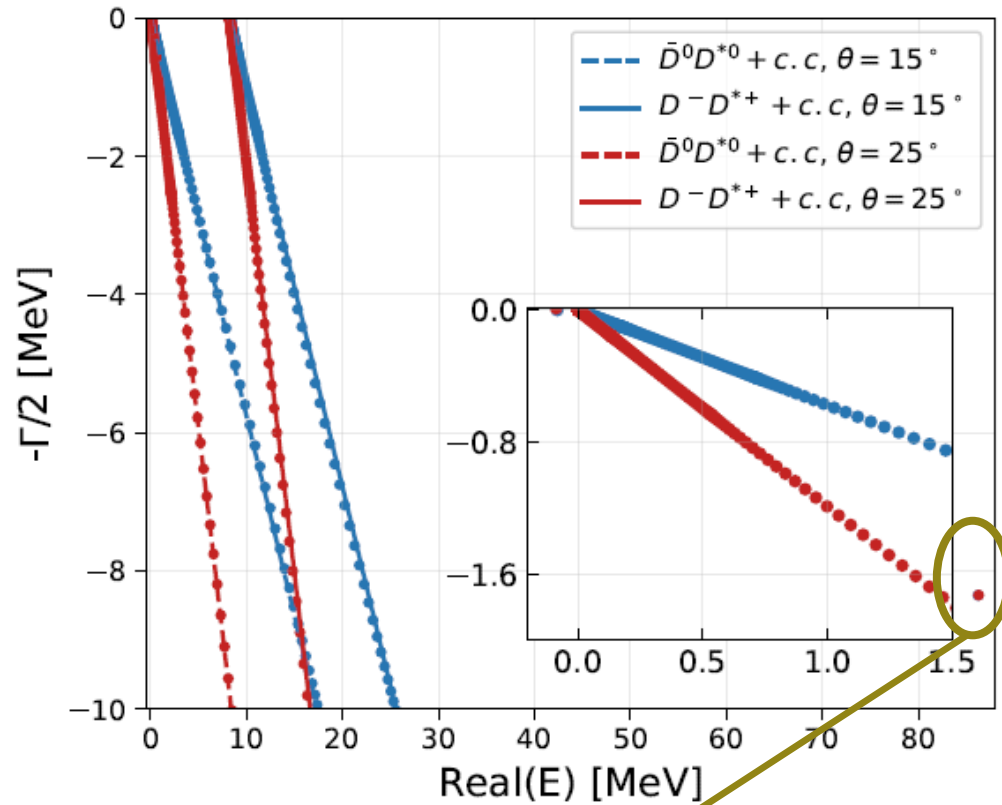
- 传统夸克模型 $c\bar{c}$ 裸态， $\chi_{c1}(2P, 3940)$ 和其波函数都可以从夸克模型中得到
- 3P0的耦合参数 $\gamma = 4.69$ 可以从 $\psi(3770) \rightarrow D\bar{D}$ 获得。
- X(3872) 的研究 **没有额外的自由参数**。



- **Bound state for X(3872)**
 $\Delta E = -80.4 \text{ keV}$
 $\Gamma_{T_{cc}} = 32.5 \text{ keV}$
- $\sqrt{\langle r^2 \rangle} = 11.2 \text{ fm}$
- 94.0% $\bar{D}^{*0} D^0$, 4.8% $D^{*-} D^+$, 1.2% $c\bar{c}$



预言



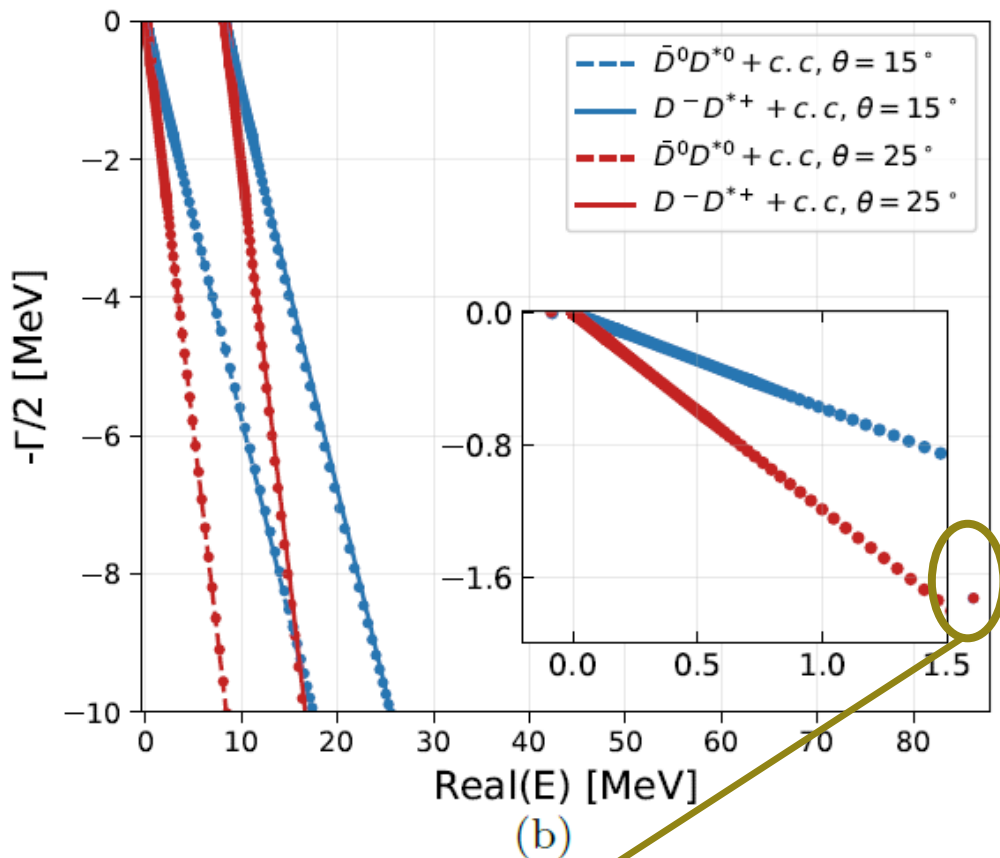
• $\chi_{c1}(2p)$

$M = 3957.9 \text{ MeV}$ $\Gamma_{\chi_{c1}(2P)} = 16.7 \text{ MeV}$

• Main decay channel: $\bar{D}^* D$



预言



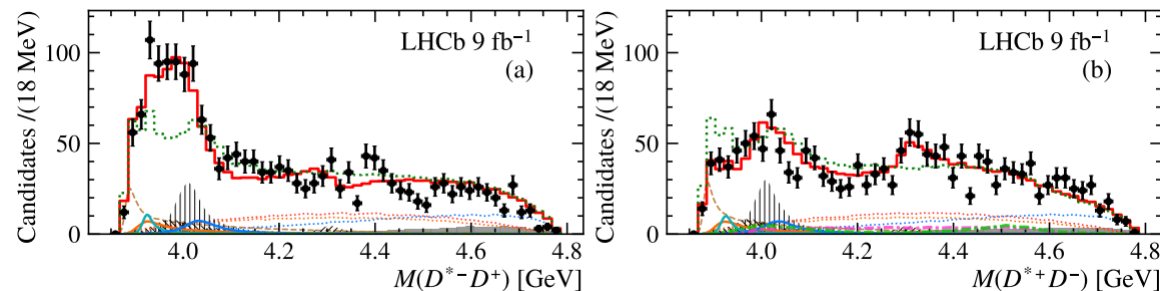
- $\chi_{c1}(2p)$
 $M = 3957.9 \text{ MeV}$ $\Gamma_{\chi_{c1}(2p)} = 16.7 \text{ MeV}$
- Main decay channel: $\bar{D}^* D$

Observation of new charmonium(-like) states
 in $B^+ \rightarrow D^{*\pm} D^{\mp} K^+$ decays

LHCb Collaboration 2406.03156

$$\chi_{c1}(4010) \quad J^{PC} = 1^{++}$$

$$m_0 = 4012.5^{+3.6+4.1}_{-3.9-3.7} \text{ MeV} \quad \Gamma_0 = 62.7^{+7.0+6.4}_{-6.4-6.6} \text{ MeV}$$



X(3872) Relevant $D\bar{D}^*$ Scattering in $N_f = 2$ Lattice QCD

H. Li, C. Shi, Y. Chen, M. Gong, J. Liang et al

CLQCD 2402.14541

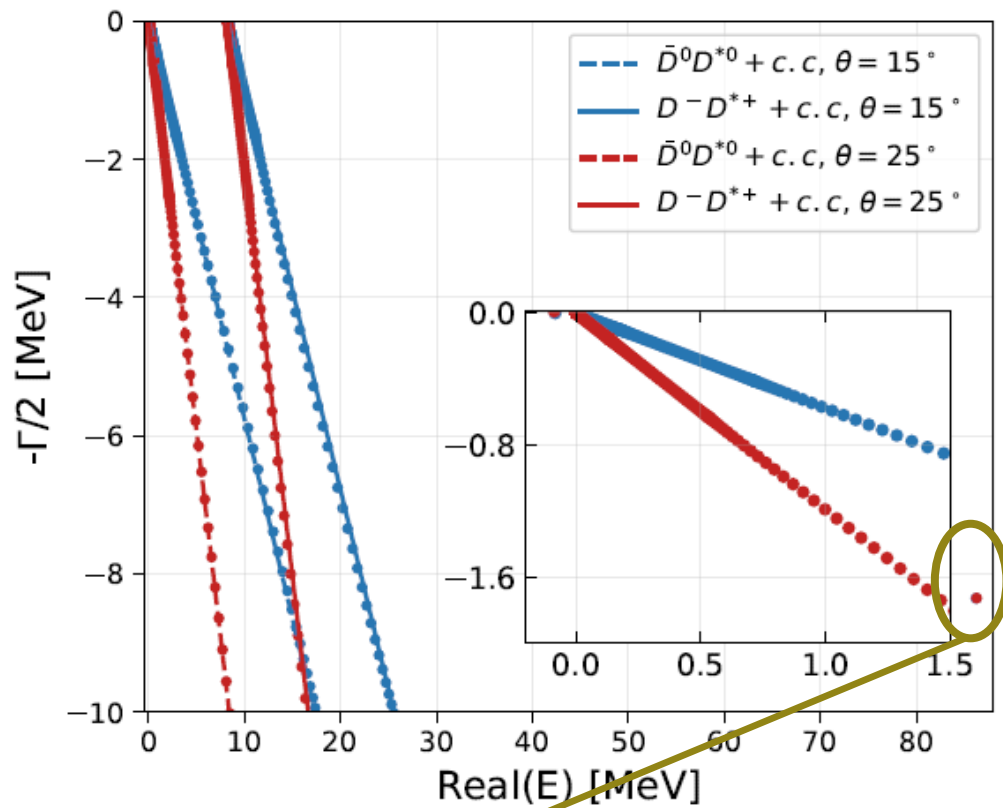
$$t(s) = \frac{K(s)}{1 - K(s)i\rho(s)}$$

$$K(s) = \frac{g}{M^2 - s} + \gamma$$

m_π (MeV)	250(3)	307(2)	362(1)	417(1)
Bound state from $E_{2,3}$				
E_B (MeV)	$-9.7^{+2.1}_{-2.2}$	$-9.7^{+1.9}_{-2.0}$	$-1.3^{+0.6}_{-0.8}$	$-1.3^{+0.8}_{-1.0}$
BW fit from $E_{3,4}$				
m_R (MeV)	3924(5)	3926(6)	3969(4)	3995(4)
Γ_R (MeV)	63(23)	57(18)	37(13)	57(10)
Bound state pole and residual from $E_{2,3,4}$				
E_B (MeV)	-11(1)	-10(2)	-1.6(7)	-1.7(7)
Resonance pole and residue				
m_R (MeV)	4008(4)	4029(4)	4050(3)	4071(3)
Γ_R (MeV)	60(6)	38(9)	43(8)	50(7)
$\text{Br}_{D\bar{D}^*}$ (%)	~ 100	~ 100	~ 100	~ 100



预言



• $\chi_{c1}(2p)$

$M = 3957.9 \text{ MeV}$ $\Gamma_{\chi_{c1}(2p)} = 16.7 \text{ MeV}$

• Main decay channel: $\bar{D}^* D$

	wave function	$I(J^{PC})$	u -channel: π	u -channel: ρ/ω	t -channel: ρ/ω
DD^*	$\frac{1}{\sqrt{2}}(D^+ D^{*0} - D^0 D^{*+})$	$0(1^+) [T_{cc}^+]$	$\frac{3}{2} V_\pi$	$\frac{3}{2} V_\rho^u - \frac{1}{2} V_\omega^u$	$-\frac{3}{2} V_\rho^t + \frac{1}{2} V_\omega^t$
	$\frac{1}{\sqrt{2}}(D^+ D^{*0} + D^0 D^{*+})$	$1(1^+)$	$\frac{1}{2} V_\pi$	$\frac{1}{2} V_\rho^u + \frac{1}{2} V_\omega^u$	$\frac{1}{2} V_\rho^t + \frac{1}{2} V_\omega^t$
$D\bar{D}^*$	$\frac{1}{\sqrt{2}}([D^+ D^{*-}] + [D^0 \bar{D}^{*0}])$	$0(1^{++}) [X(3872)]$	$\frac{3}{2} V_\pi$	$-\frac{3}{2} V_\rho^u - \frac{1}{2} V_\omega^u$	$-\frac{3}{2} V_\rho^t - \frac{1}{2} V_\omega^t$
	$\frac{1}{\sqrt{2}}([D^+ D^{*-}] - [D^0 \bar{D}^{*0}])$	$1(1^{++})$	$-\frac{1}{2} V_\pi$	$\frac{1}{2} V_\rho^u - \frac{1}{2} V_\omega^u$	$\frac{1}{2} V_\rho^t - \frac{1}{2} V_\omega^t$
	$\frac{1}{\sqrt{2}}(\{D^+ D^{*-}\} + \{D^0 \bar{D}^{*0}\})$	$0(1^{+-}) [h_c]$	$-\frac{3}{2} V_\pi$	$\frac{3}{2} V_\rho^u + \frac{1}{2} V_\omega^u$	$-\frac{3}{2} V_\rho^t - \frac{1}{2} V_\omega^t$
	$\frac{1}{\sqrt{2}}(\{D^+ D^{*-}\} - \{D^0 \bar{D}^{*0}\})$	$1(1^{+-}) [Z_c(3900)]$	$\frac{1}{2} V_\pi$	$-\frac{1}{2} V_\rho^u + \frac{1}{2} V_\omega^u$	$\frac{1}{2} V_\rho^t - \frac{1}{2} V_\omega^t$

	$I(J^{PC})$	Our
DD^*	$0(1^+) [T_{cc}^+]$	$T_{cc}^+(3874)$
	$1(1^+)$	Unstable
$D\bar{D}^*$	$0(1^{++}) [\chi_{c1}]$	$X(3872), \chi_{c1}(3958)$
	$1(1^{++}) [W_{c1}]$	Missing...
	$0(1^{+-}) [h_c]$	$\tilde{X}(3870), h_c(3961)$
	$1(1^{+-}) [Z_c]$	Nopole around 3900

Black, $DD^*/D\bar{D}^*$
Red, $c\bar{c} + D\bar{D}^*$

LHCb 2406.03156

Teng Ji, Dong, Guo, Hanhart,
Meißner, 2502.04458

COMPASS, PLB 783,334 (2018)



Preliminary results of $X(3872)$ decay

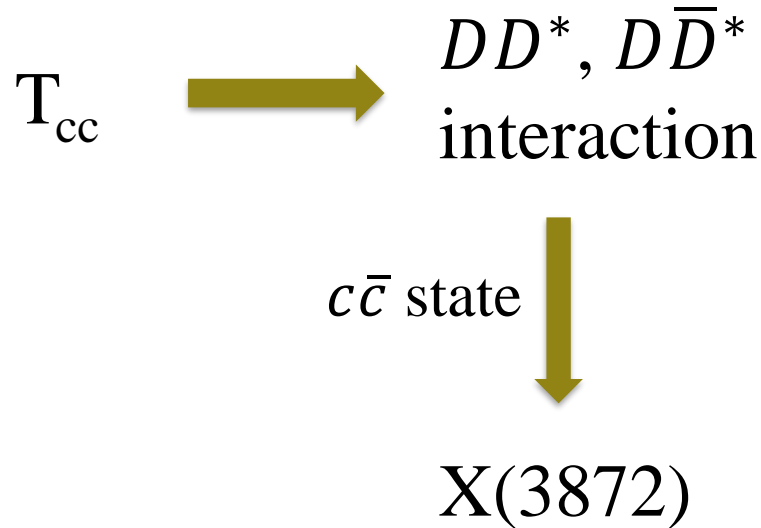


TABLE III. Branching ratio of different channels $\Gamma_i/\Gamma_{\text{total}}$

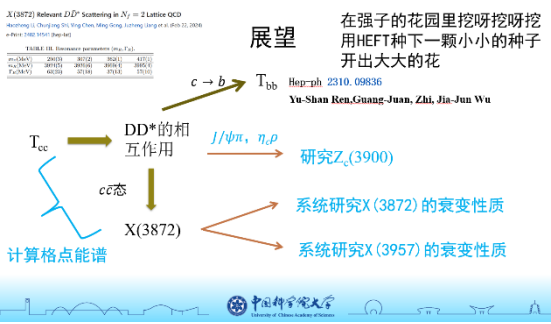
Decay channels	PDG [60]	Ref. [68]	Ours
$\chi_{c1}(3872) \rightarrow \pi^+\pi^-J/\psi$	0.035 ± 0.009	$4.1^{+1.9}_{-1.1}\%$	0.035
$\chi_{c1}(3872) \rightarrow \rho^0 J/\psi$	$2.8 \pm 0.7\%$	–	4.1%
$\chi_{c1}(3872) \rightarrow \omega J/\psi$	$4.1 \pm 1.4\%$	$4.4^{+2.3}_{-1.3}\%$	13.7%
$\chi_{c1}(3872) \rightarrow \pi\pi\pi J/\psi$	not seen	–	6.2%
$\chi_{c1}(3872) \rightarrow D^0\bar{D}^0\pi^0$	$45 \pm 21\%$	–	11.4%
$\chi_{c1}(3872) \rightarrow \bar{D}^{*0}D^0$	$34 \pm 12\%$	$52.4^{+25.3}_{-14.3}\%$	58.5%
$\chi_{c1}(3872) \rightarrow \pi^0\chi_{c2}$	$< 4\%$	–	1.8%
$\chi_{c1}(3872) \rightarrow \pi^0\chi_{c1}$	$3.1^{+1.5}_{-1.3}\%$	$3.6^{+2.2}_{-1.6}\%$	2.3%
$\chi_{c1}(3872) \rightarrow \pi^0\chi_{c0}$	$< 13\%$	–	1.5%
$\chi_{c1}(3872) \rightarrow \gamma D^+D^-$	$< 3.5\%$	–	0.1%
$\chi_{c1}(3872) \rightarrow \gamma\bar{D}^0D^0$	$< 6\%$	–	6.4%
$\chi_{c1}(3872) \rightarrow \gamma J/\psi$	$(7.8 \pm 2.9) \times 10^{-3}$	$1.1^{+0.6}_{-0.3}\%$	$< 5 \times 10^{-3}$
$\chi_{c1}(3872) \rightarrow \gamma\psi(2S)$	possibly seen	$2.4^{+1.3}_{-0.8}\%$	7×10^{-3}

$\Gamma_{\text{total}} \sim 280$ keV (LHCb)
 $\Gamma_{\text{total}} \sim 380$ keV (BESIII)
 $\Gamma_{\text{total}} \sim 284$ keV

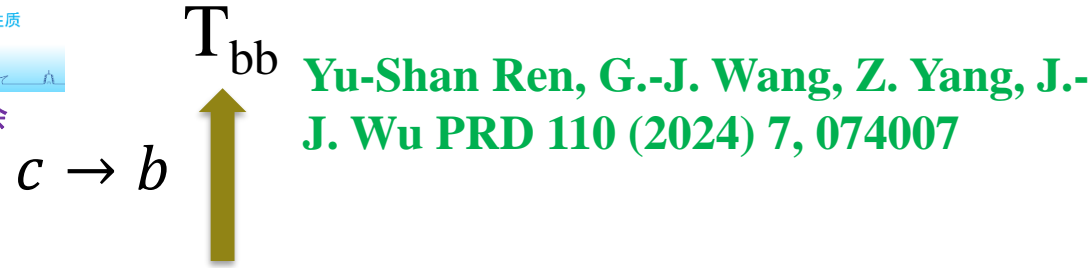
[68] C. H. Li, C. Z. Yuan, Phys. Rev. D 100, 094003

LHCb, Phys. Rev. D 102 (2020) 9, 092005.
 BESIII, Phys. Rev. Lett. 132, 151903.





能够系统描述强子的较为完整的框架



	I (J ^{PC})	Our
DD^*	$0(1^+) [T_{cc}^+]$	$T_{cc}^+(3874)$
	$1(1^+)$	Unstable
$D\bar{D}^*$	$0(1^{++}) [\chi_{c1}]$	$X(3872), \chi_{c1}(3958)$
	$1(1^{++}) [W_{c1}]$	Missing...
	$0(1^+) [h_c]$	$\tilde{X}(3870), h_c(3961)$
	$1(1^{++}) [Z_c]$	Nopole around 3900

Kang-Yu, G.-J. Wang, Z. Yang, J.-J. Wu
PRD 110 (2024) 11, 114029

Study $Z_c(3900)$

Study the decay of $X(3872)$, soon...

Study the decay of $\tilde{X}(3870)$,
 $\chi_{c1}(4010)$, $h_c(3961)$...

G.-J. Wang, Z. Yang, J.-J. Wu, M. Oka, S.-L. Zhu
Scib.2024.07.012 $c\bar{c}$ state

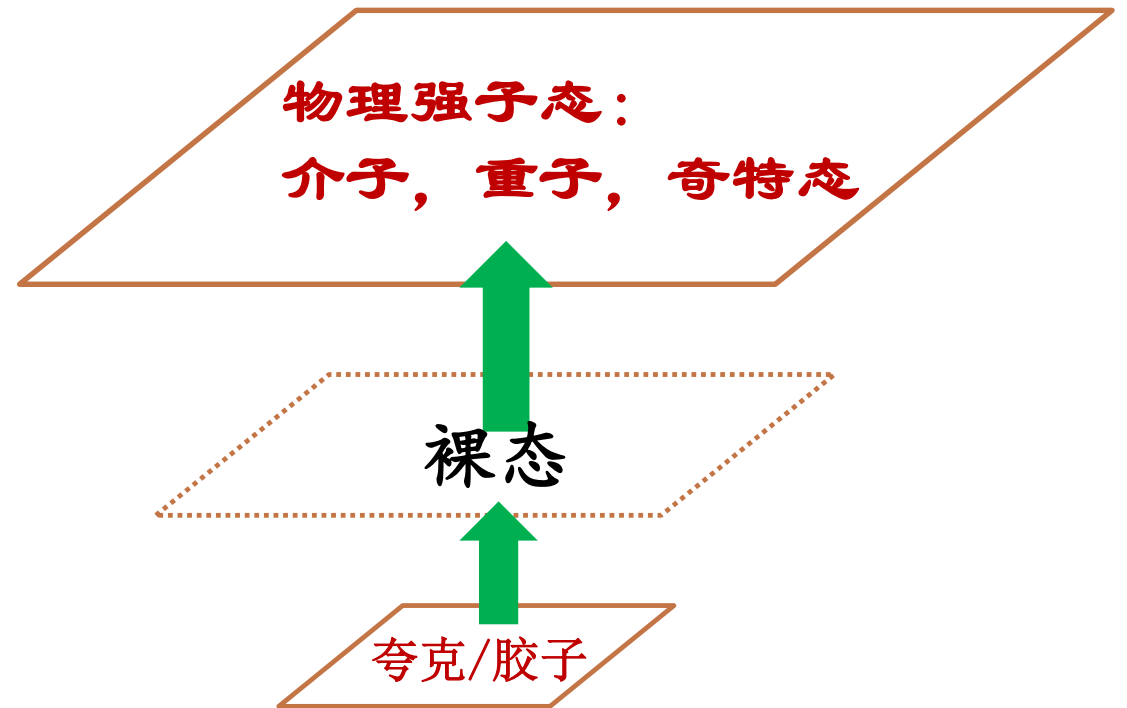
Lattice spectrum,
 T_{cc} soon...(Adelaide LQCD)

K. Yu, G.-J. Wang, J.-J. Wu, Z. Yang,
2502.05789 (Accept by JHEP)

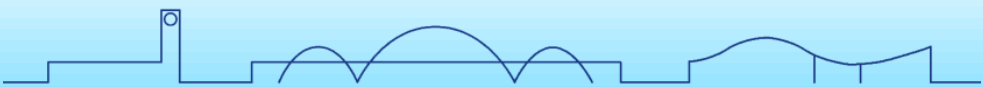


小结

- 探讨了裸态和分子态共同作用下产生的极点的轨迹
- 通过 T_{cc} 的研究确定 DD^* 的相互作用
- 由确定的 DD^* 的相互作用和裸态可以研究 $X(3872)$ 的性质



谢谢



中国科学院大学
University of Chinese Academy of Sciences

