

高激发态轻强子性质的研究

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第十届XYZ研讨会

C.X.Liu, L.M.Wang, T.Y.Li and X.Liu, Phys. Rev. D 110, no.11, 114049 (2024)

L.M.Wang, W.X.Tian, T.Y.Li, C.X.Liu and X.Liu, Phys. Rev. D 110, no.7, 074021 (2024)

Outline

- 1. Background**
- 2. Mass spectrum**
- 3. Decay behaviors**
- 4. Summary**



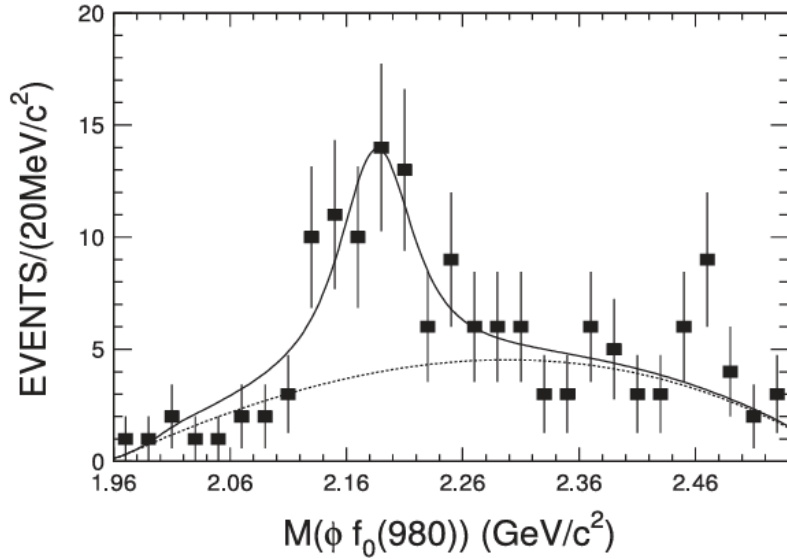
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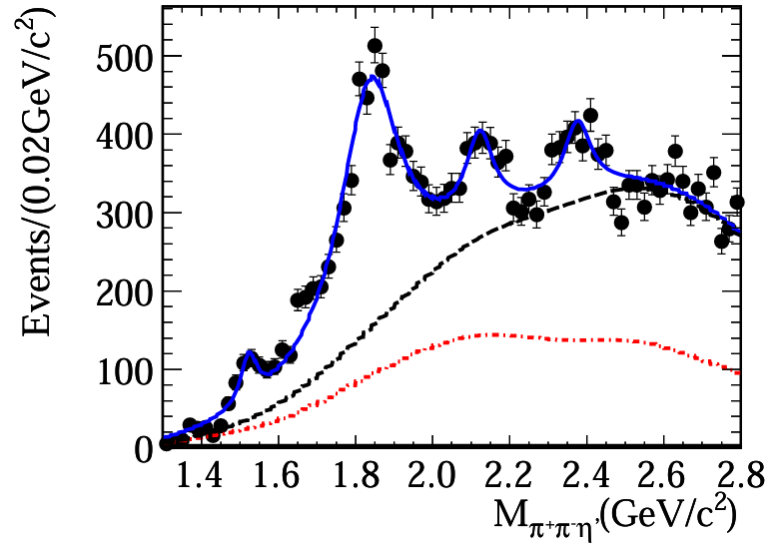
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Background

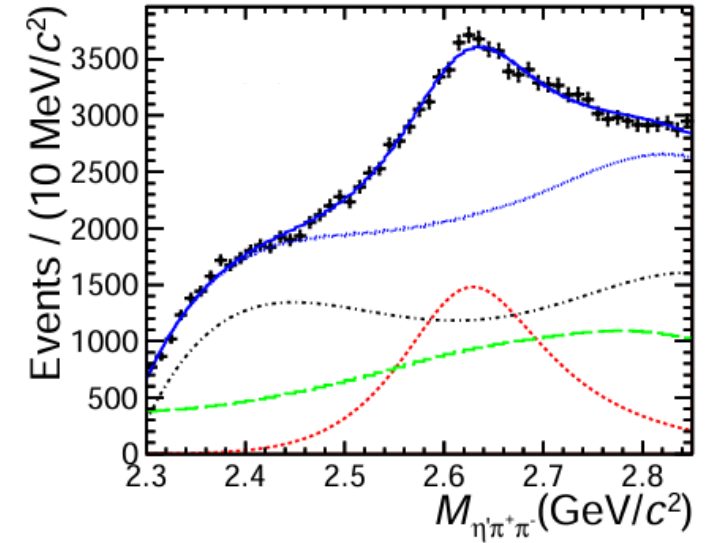
New observed high-lying states



Observation of Y(2175)
Phys. Rev. Lett. 106, 072002 (2011)



Observation of X(2370)
Phys. Rev. Lett. 100, 102003 (2008)

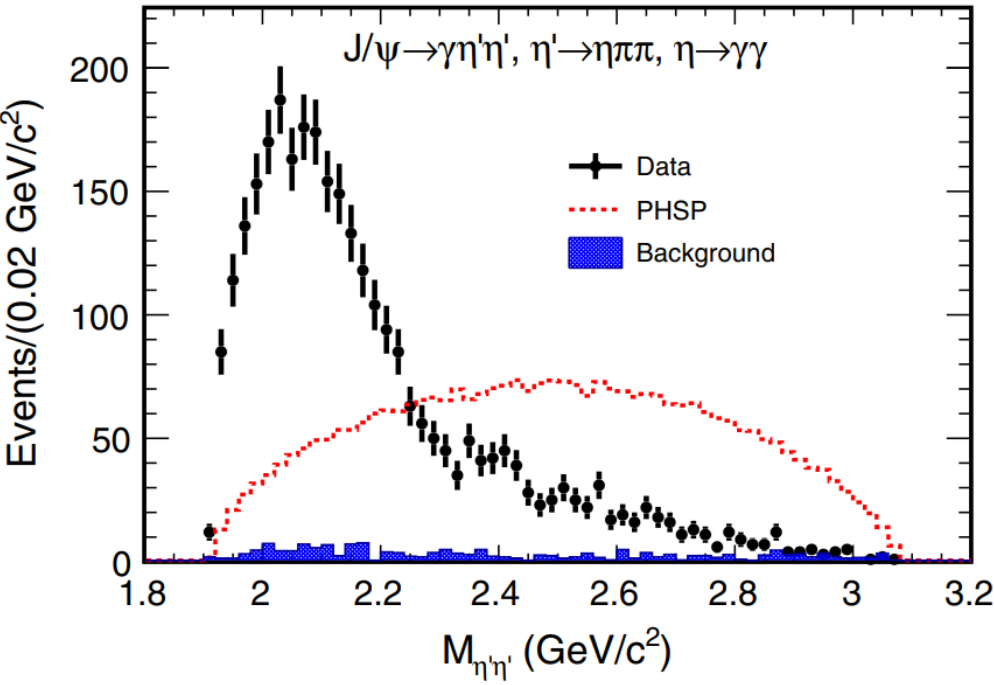


Observation of X(2600)
Phys. Rev. Lett. 129, 042001 (2022)

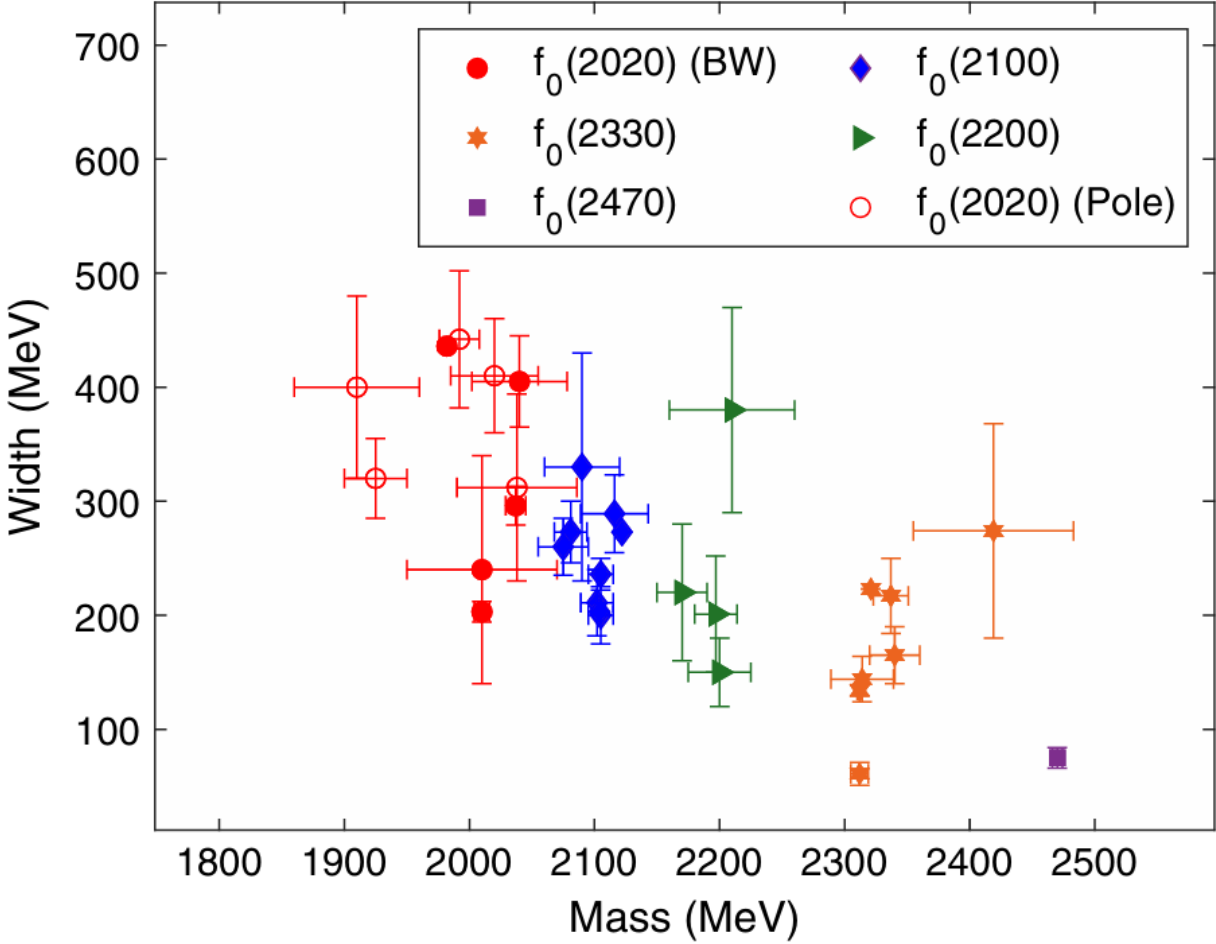
We propose that it is an appropriate time to establish high-lying mesons

High-lying scalar states

High-lying scalar states
 $f_0(2020)$, $f_0(2330)$ and
 $f_0(2470)$



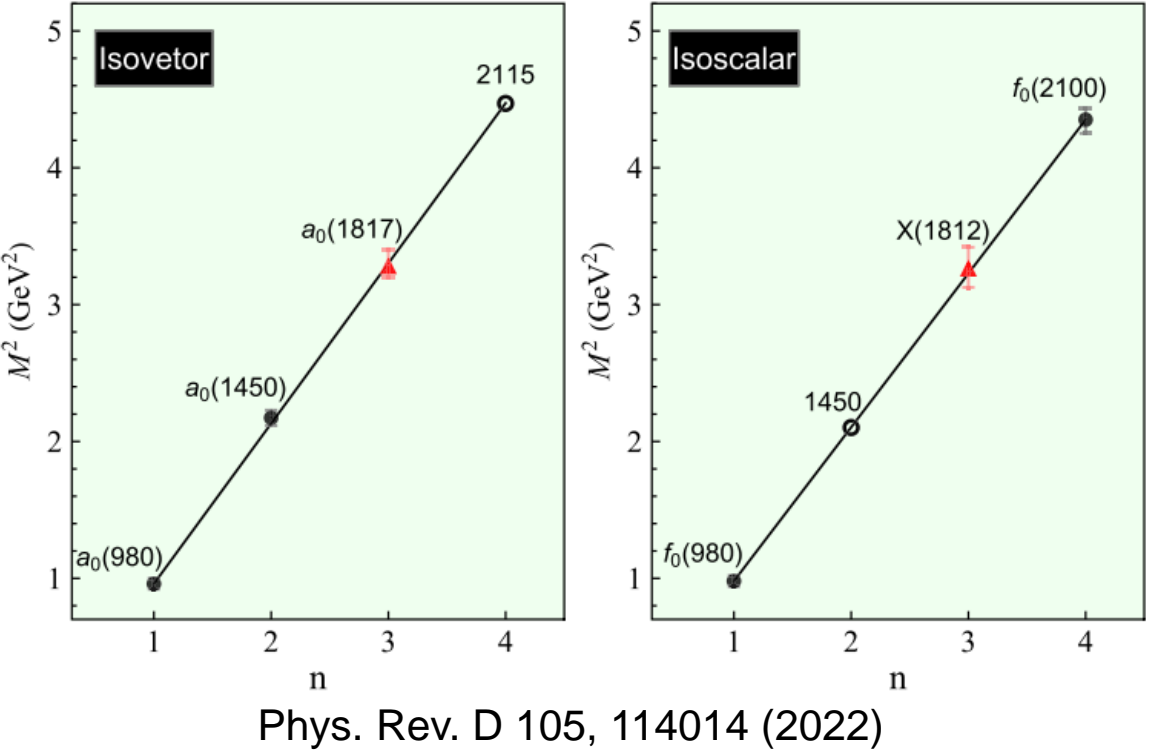
Phys. Rev. D 105, 072002 (2022)



This mess situation should be clarified by further studies

Our previous work of scalar mesons

Low-lying scalar mesons family including new observed $a_0(1817)$



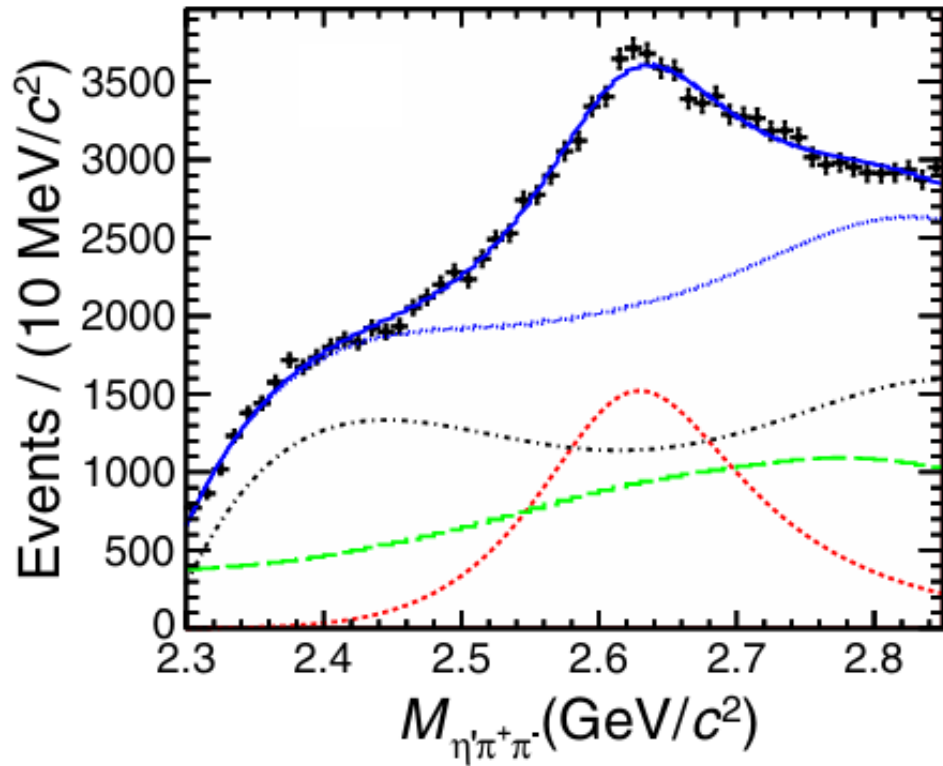
← Our prior research focused on selected low-mass scalar meson states

These high-lying states also have not been established in our work →

• $f_0(2020)$	$0^+(0^{++})$
• $f_4(2050)$	$0^+(4^{++})$
$\pi_2(2100)$	$1^-(2^{+-})$
$f_0(2100)$	$0^+(0^{++})$
$f_2(2150)$	$0^+(2^{++})$
$\rho(2150)$	$1^+(1^{--})$
• $\phi(2170)$	$0^-(1^{--})$
$f_0(2200)$	$0^+(0^{++})$
$f_7(2220)$	$0^+(2^{++})$ or 4^{++}
$\omega(2220)$	$0^-(1^{--})$
$\eta(2225)$	$0^+(0^{++})$
$\rho_3(2250)$	$1^+(3^{--})$
• $f_2(2300)$	$0^+(2^{++})$
$f_4(2300)$	$0^+(4^{++})$
$f_0(2330)$	$0^+(0^{++})$
• $f_2(2340)$	$0^+(2^{++})$
$\rho_5(2350)$	$1^+(5^{--})$
$X(2370)$	$?^?(?^{??})$
$f_0(2470)$	$0^+(0^{++})$

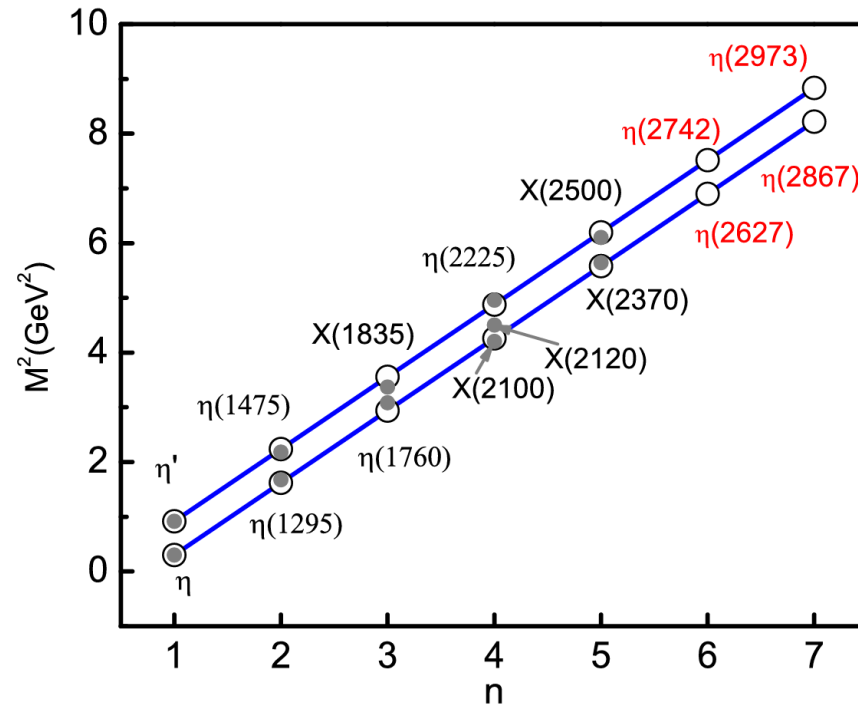
New observed $X(2600)$

The $X(2600)$ state



Phys. Rev. Lett. 129, 042001 (2022)

The quantum numbers J^{PC} of the $X(2600)$ could be either 0^{-+} or 2^{-+} . In our previous work, it is proposed as an $\eta(6S)$ state



Phys. Rev. D 102, 114034 (2020)

The possibility of the $X(2600)$ being a pseudotensor meson with $J^{PC} = 2^{-+}$ still needs to be examined

The η_2 family

The summary table in the PDG includes the $\eta_2(1645)$ and $\eta_2(1870)$ states

The $\eta_2(2030)$ and $\eta_2(2250)$ are listed as further states

Including the previously discussed $X(2600)$, there are **five isoscalar pseudotensor states awaiting classification**

$$\eta_2(1645) \quad I^G(J^{PC}) = 0^+(2^{-+})$$

$$\eta_2(1645) \text{ MASS} \quad 1617 \pm 5 \text{ MeV}$$

$$\eta_2(1645) \text{ WIDTH} \quad 181 \pm 11 \text{ MeV}$$

$$\eta_2(1870) \quad I^G(J^{PC}) = 0^+(2^{-+})$$

$$\eta_2(1870) \text{ MASS} \quad 1842 \pm 8 \text{ MeV}$$

$$\eta_2(1870) \text{ WIDTH} \quad 225 \pm 14 \text{ MeV}$$

J^{PC}	Mass M (MeV)	Width Γ (MeV)
2^{-+}	2267 ± 14	290 ± 50
2^{-+}	(2030)	(205)
2^{-+}	(1860)	(250)

Phys. Lett. B 491, 47 (2000)

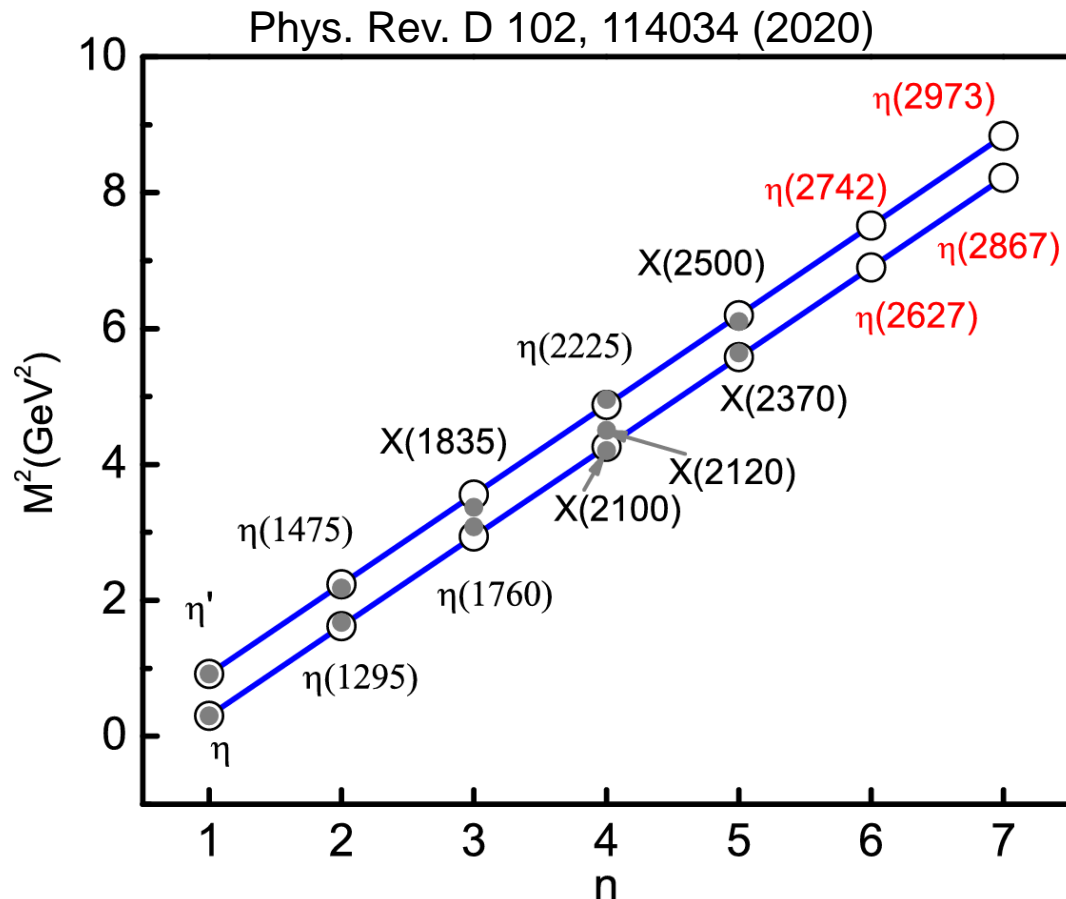


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Mass spectrum

The Regge trajectories

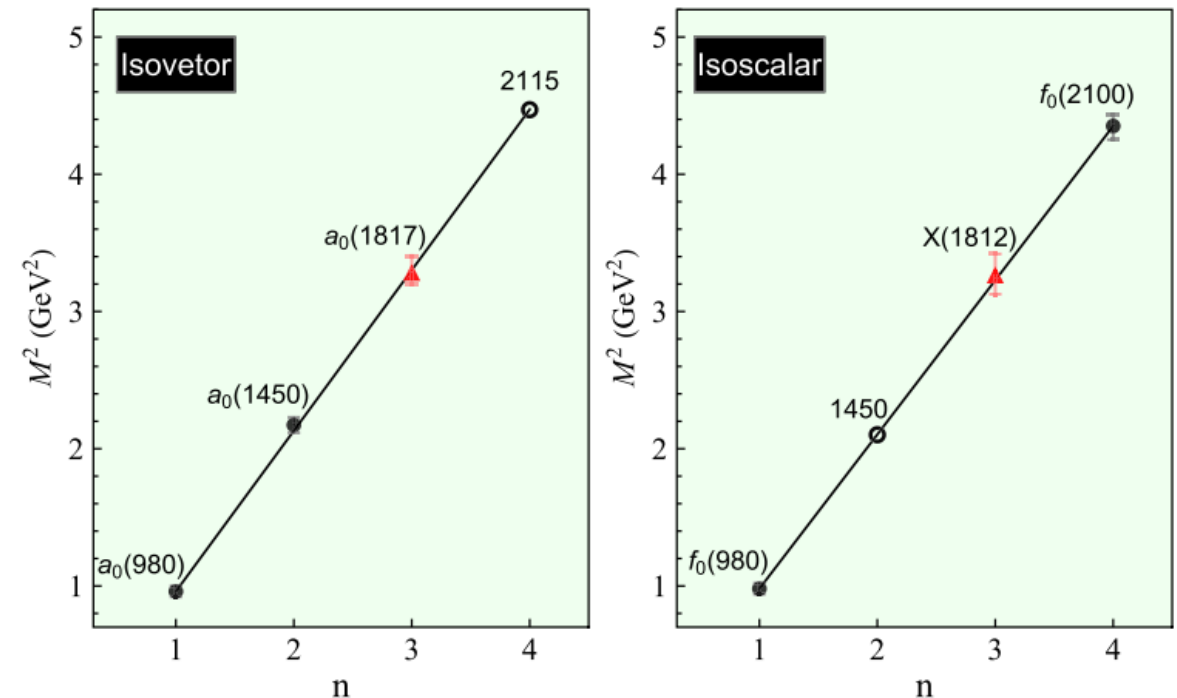
In our previous work, we studied low-lying scalar mesons and pseudoscalar mesons using the Regge trajectory



The Regge trajectory shows that the masses of hadrons follow a pattern that can be written as

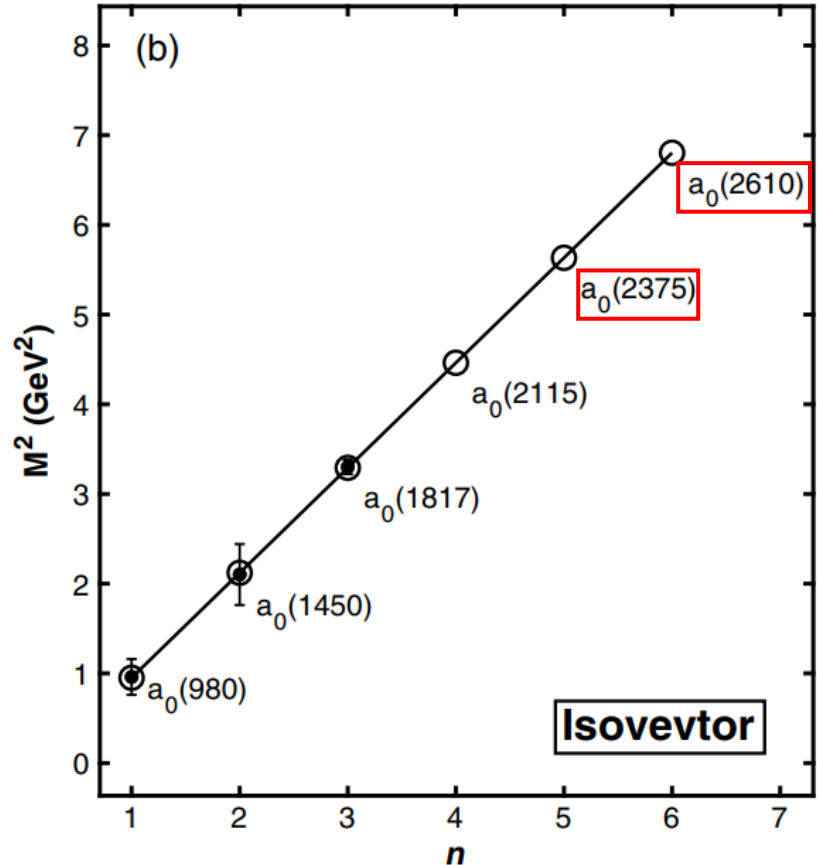
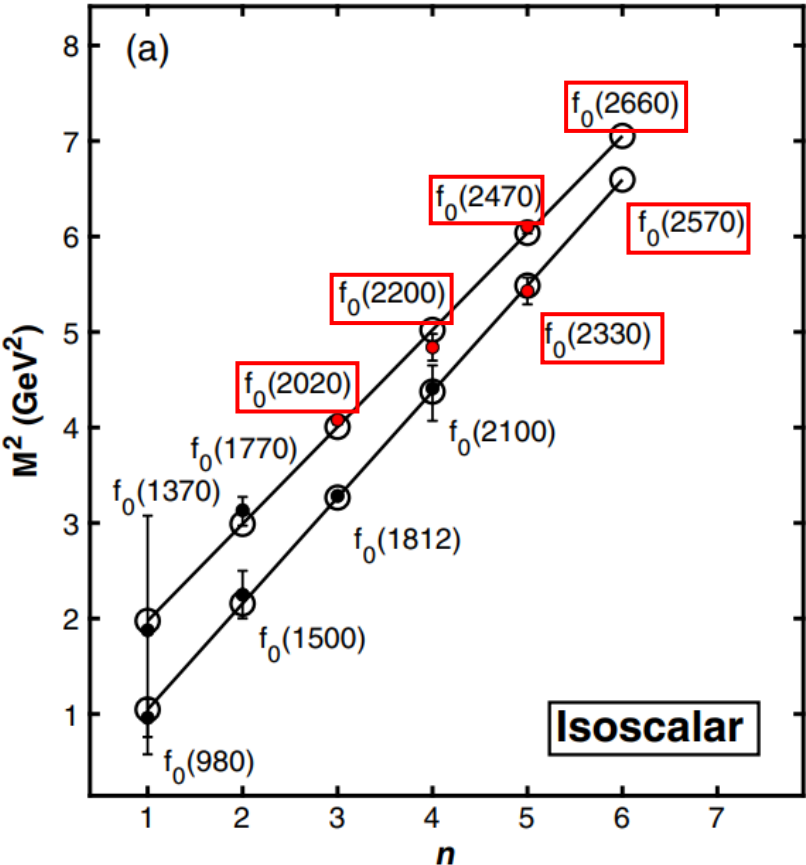
$$M^2 = M_0^2 + (n - 1)\mu^2$$

Phys. Rev. D 105, 114014 (2022)



The Regge trajectories of scalar mesons

Three Regge trajectories of the scalar mesons family: f_0 states (a) and a_0 states (b), while f_0 states can be categorized into $n\bar{n}$ states ($f_0(980)$) and $s\bar{s}$ states ($f_0(1370)$)



← The states are studied in our work
 Not included $f_0(500)$ and $f_0(1710)$
 $n\bar{n}$: u and d quarks
 $s\bar{s}$: s quarks

The Godfrey-Isgur (GI) model

In the nonrelativistic limit, the effective potential:

$$\tilde{H} = \sqrt{m_1^2 + \mathbf{p}^2} + \sqrt{m_2^2 + \mathbf{p}^2} + \tilde{V}_{\text{eff}}(\mathbf{p}, \mathbf{r}),$$

$$V_{\text{eff}}(r) = H^{\text{conf}} + H^{\text{hyp}} + H^{\text{so}},$$

$$H^{\text{conf}} = \left[-\frac{3}{4}(c + br) + \frac{\alpha_s(r)}{r} \right] (\mathbf{F}_1 \cdot \mathbf{F}_2)$$

$$= S(r) + G(r), \quad \uparrow \text{Cornell potential}$$

$$H^{\text{hyp}} = -\frac{\alpha_s(r)}{m_1 m_2} \left[\frac{8\pi}{3} \mathbf{S}_1 \cdot \mathbf{S}_2 \delta^3(\mathbf{r}) + \frac{1}{r^3} \left(\frac{3\mathbf{S}_1 \cdot \mathbf{r} \mathbf{S}_2 \cdot \mathbf{r}}{r^2} - \mathbf{S}_1 \cdot \mathbf{S}_2 \right) \right]$$

$$\times (\mathbf{F}_1 \cdot \mathbf{F}_2),$$

$$H^{\text{so}} = H^{\text{so(cm)}} + H^{\text{so(tp)}},$$

$$H^{\text{so(cm)}} = \frac{-\alpha_s(r)}{r^3} \left(\frac{1}{m_1} + \frac{1}{m_2} \right) \left(\frac{\mathbf{S}_1}{m_1} + \frac{\mathbf{S}_2}{m_2} \right) \cdot \mathbf{L} (\mathbf{F}_1 \cdot \mathbf{F}_2),$$

$$H^{\text{so(tp)}} = -\frac{1}{2r} \frac{\partial H^{\text{conf}}}{\partial r} \left(\frac{\mathbf{S}_1}{m_1^2} + \frac{\mathbf{S}_2}{m_2^2} \right) \cdot \mathbf{L}$$

To account for relativistic effects, two modifications are introduced, a smearing function and momentum-dependent factors are

$$\tilde{f}(r) = \int d^3 r' \rho(\mathbf{r} - \mathbf{r}') f(r'), \quad \rho(\mathbf{r} - \mathbf{r}') = \frac{\sigma^3}{\pi^{3/2}} e^{-\sigma^2(\mathbf{r}-\mathbf{r}')^2},$$

$$\tilde{G}(r) \rightarrow \left(1 + \frac{p^2}{E_1 E_2} \right)^{1/2} \tilde{G}(r) \left(1 + \frac{p^2}{E_1 E_2} \right)^{1/2}$$

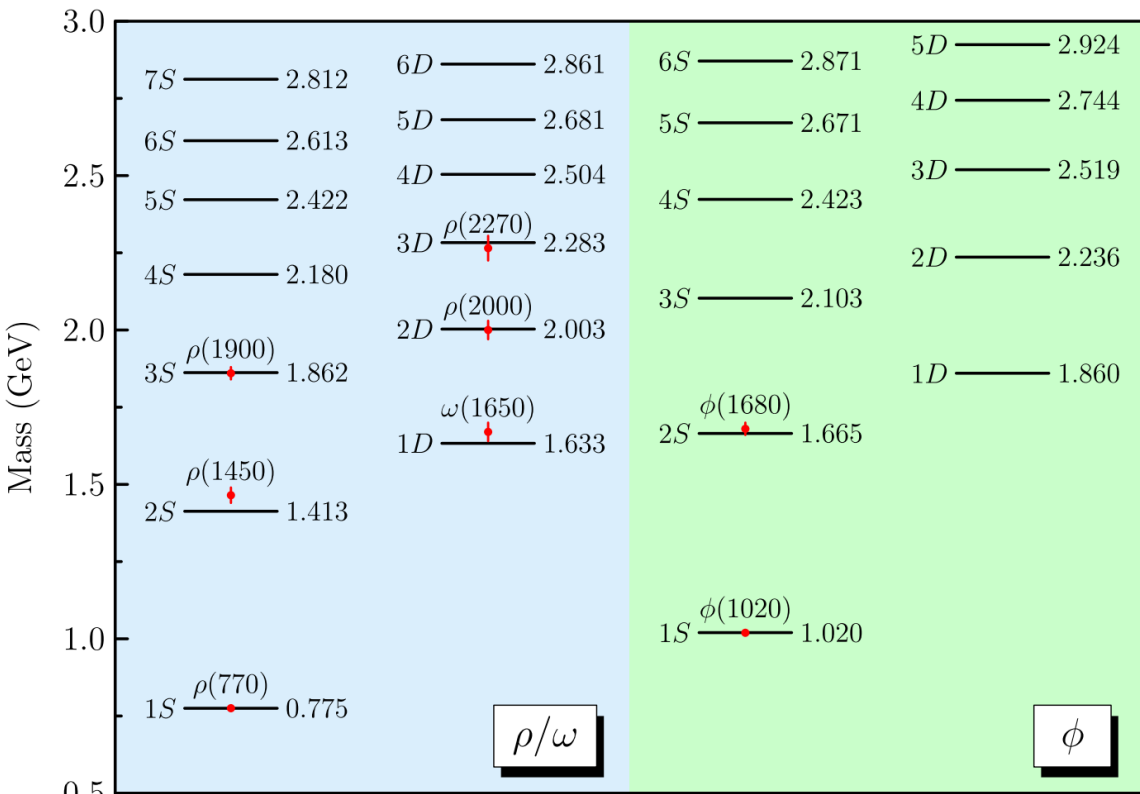
$$\frac{\tilde{V}_i(r)}{m_1 m_2} \rightarrow \left(\frac{m_1 m_2}{E_1 E_2} \right)^{1/2 + \epsilon_i} \frac{\tilde{V}_i(r)}{m_1 m_2} \left(\frac{m_1 m_2}{E_1 E_2} \right)^{1/2 + \epsilon_i},$$

The screening effect replaces the line potential to account for **the unquenched effect**

$$br \rightarrow \frac{b(1 - e^{-\mu r})}{\mu}, \quad H^{\text{scr}} = \frac{b(1 - e^{-\mu r})}{\mu} - \frac{4\alpha_s(r)}{3r} + c.$$

The mass spectrum of η_2 family

The mass spectrum of ρ , ω , ϕ



Phys. Rev. D 105, 034011 (2022)

The parameters involved in the GI model from our previous work

Parameter	Value	Parameter	Value
m_u (GeV)	0.22	m_d (GeV)	0.22
m_s (GeV)	0.424	b (GeV ²)	0.229
ϵ_c	-0.164	ϵ_{sos}	0.9728
σ_0 (GeV)	1.8	s (GeV)	3.88
μ (GeV)	0.081	c (GeV)	-0.30
ϵ_{sov}	0.262	ϵ_t	1.993

Comparison of the calculated results and the experimental data

States	This work	Experimental values
$\eta_2(1D)$	1650	$1645 \pm 14 \pm 15$ [22]
$\eta_2(2D)$	2003	$2030 \pm 10 \pm 15$ [23]
$\eta_2(3D)$	2279	2267 ± 14 [24]
$\eta_2(4D)$	2498	...
$\eta_2'(1D)$	1882	$1881 \pm 32 \pm 40$ [25]
$\eta_2'(2D)$	2238	...
$\eta_2'(3D)$	2520	...
$\eta_2'(4D)$	2764	...



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Decay behaviors

The Quark-Pair-Creation model

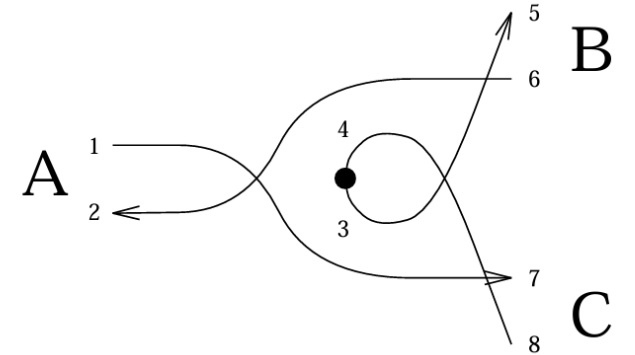
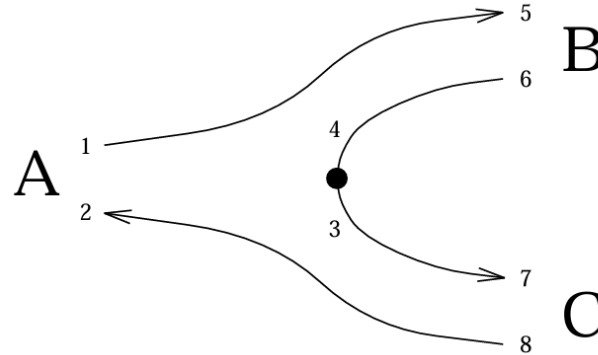
$$\langle BC|T|A\rangle = \delta^3(\mathbf{P}_B + \mathbf{P}_C)\mathcal{M}^{M_{J_A}M_{J_B}M_{J_C}}$$

$$\begin{aligned} T = & -3\gamma \sum_m \langle 1m; 1-m|00\rangle \int d\mathbf{p}_3 d\mathbf{p}_4 \delta^3(\mathbf{p}_3 + \mathbf{p}_4) \\ & \times \mathcal{Y}_{1m}\left(\frac{\mathbf{p}_3 - \mathbf{p}_4}{2}\right) \chi_{1,-m}^{34} \phi_0^{34}(\omega_0^{34})_{ij} b_{3i}^\dagger(\mathbf{p}_3) d_{4j}^\dagger(\mathbf{p}_4). \end{aligned}$$

$$\begin{aligned} |A(n_A^{2S_A+1} L_A J_A M_{J_A})(\vec{P}_A)\rangle & \equiv \sqrt{2E_A} \sum_{M_{L_A}, M_{S_A}} \langle L_A M_{L_A} S_A M_{S_A} | J_A M_{J_A} \rangle \\ & \times \int d^3\vec{p}_A \psi_{n_A L_A M_{L_A}}(\vec{p}_A) \chi_{S_A M_{S_A}}^{12} \phi_A^{12} \omega_A^{12} \\ & \times |q_1(\frac{m_1}{m_1+m_2} \vec{P}_A + \vec{p}_A) \bar{q}_2(\frac{m_2}{m_1+m_2} \vec{P}_A - \vec{p}_A)\rangle. \end{aligned}$$

$$\begin{aligned} \mathcal{M}^{JL}(\mathbf{P}) = & \frac{\sqrt{4\pi(2L+1)}}{2J_A+1} \sum_{M_{J_B} M_{J_C}} \langle L0; J M_{J_A} | J_A M_{J_A} \rangle \\ & \times \langle J_B M_{J_B}; J_C M_{J_C} | J_A M_{J_A} \rangle \mathcal{M}^{M_{J_A} M_{J_B} M_{J_C}}. \end{aligned}$$

$$\Gamma = \frac{\pi |P_E|}{4 m_A^2} \sum_{J,L} |\mathcal{M}^{JL}(\mathbf{P})|^2$$



$\gamma = 7.1$ for the scalar mesons, $\gamma = 6.57$ for the η_2 family

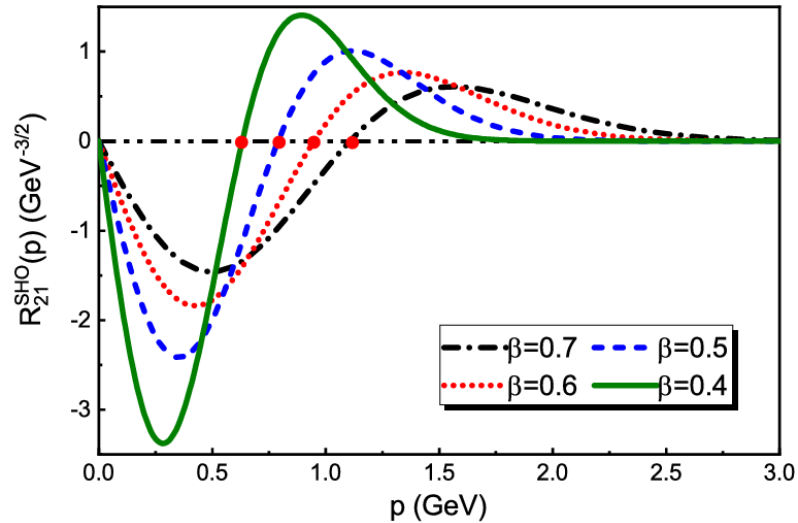
The simple harmonic oscillator (SHO) wave function

$$\phi_{nlm}^p(R, p) = R_{nl}^p(R, p) Y_{lm}(\hat{P}),$$

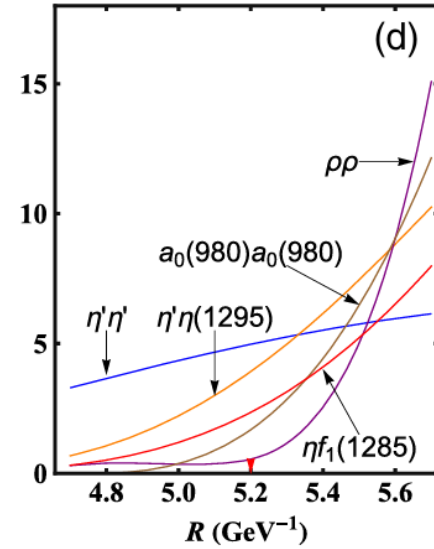
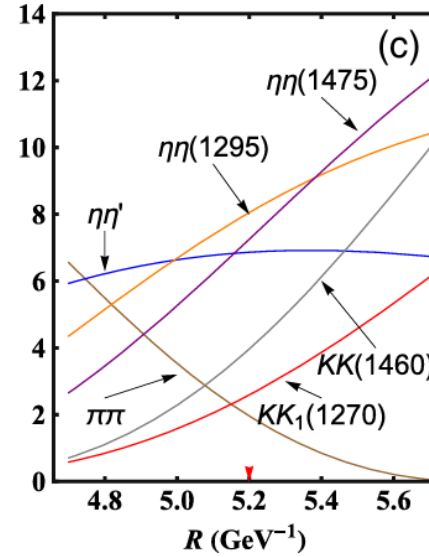
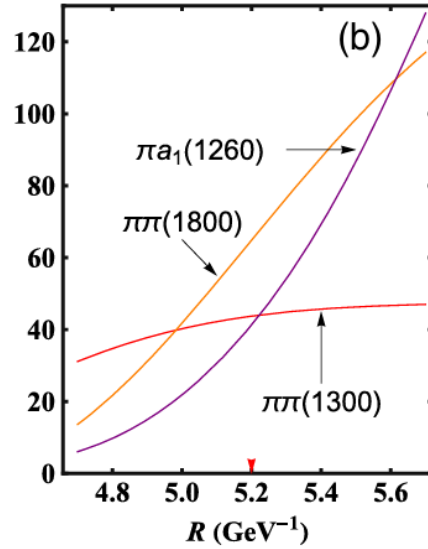
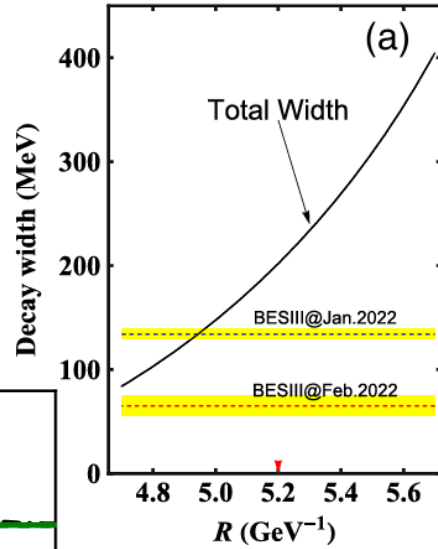
$$R_{nl}^p(R, p) = (-1)^n (-i)^l R^{\frac{3}{2}+l} \sqrt{\frac{2n!}{\Gamma(n+l+\frac{3}{2})}} L_n^{l+\frac{1}{2}}(R^2 p^2) e^{-\frac{R^2 p^2}{2}} p^l$$

Decay behaviors of $f_0(2330)$

Node effect \rightarrow



Phys. Rev. D 101, 054029 (2020)



Center R value ± 0.5

R value:

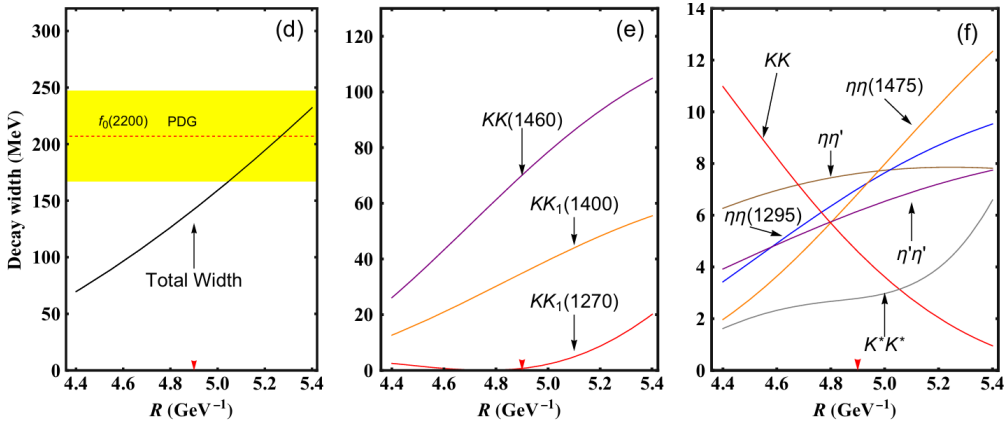
Phys. Rev. D 72, 094004 (2005)

Phys. Rev. D 55, 4157 (1997)

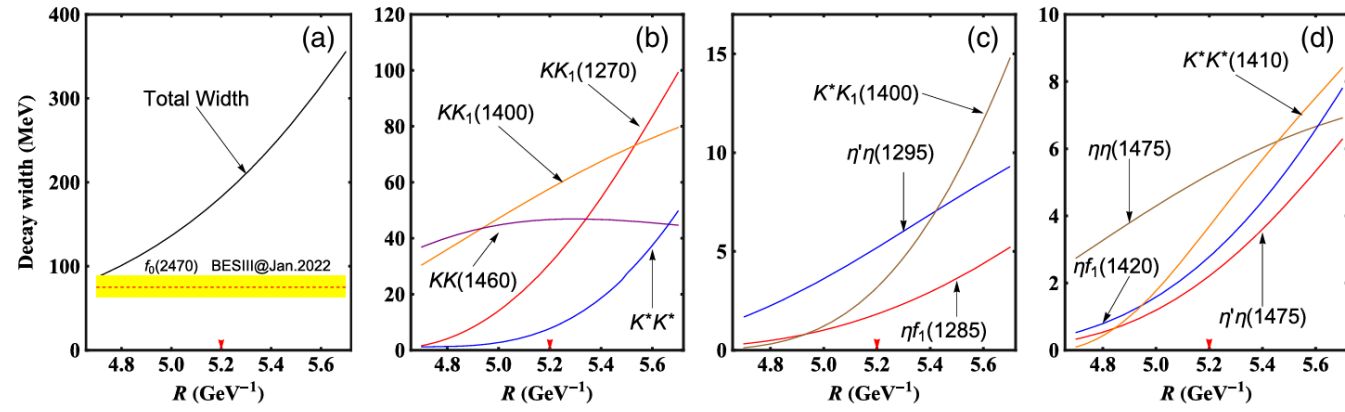
Consist with the result of BESIII Collaboration

Major decay channels:
 $\pi a_1(1260)$ $\pi\pi(1800)$
 and $\pi\pi(1300)$

Decay behaviors of other scalar states



Consist with PDG data at $R = 5.0$ to 5.4

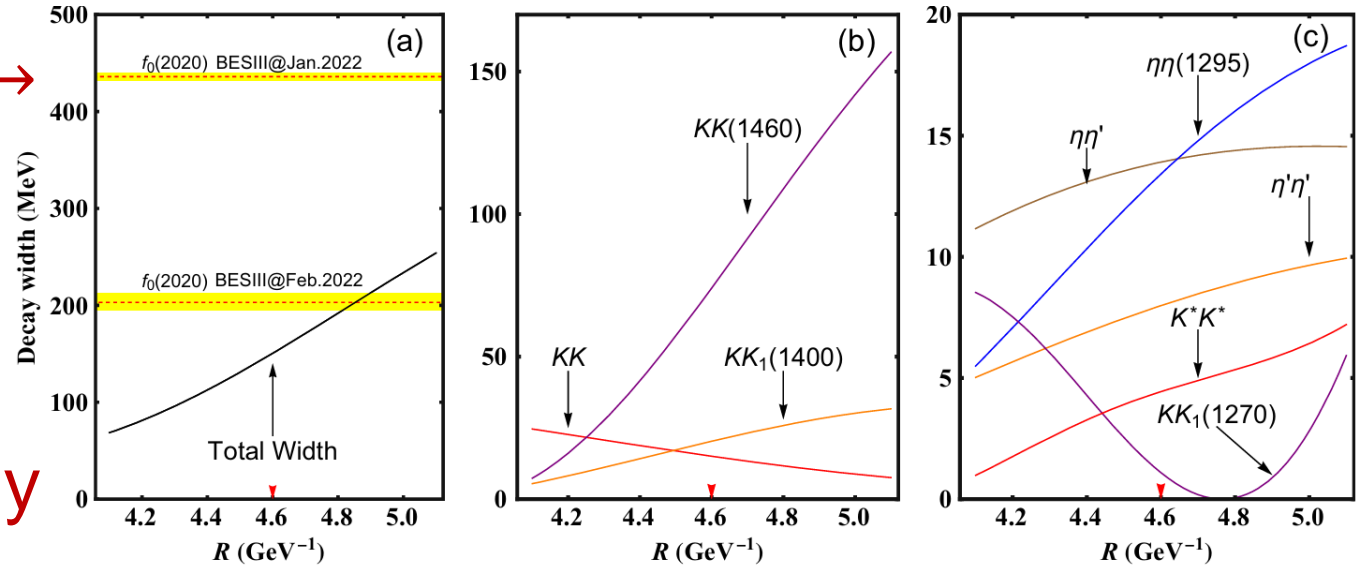


Consist with PDG data at $R = 4.7$

$J/\psi \rightarrow \gamma \eta' \eta'$ result \rightarrow
Phys. Rev. D 105, 072002 (2022)

$J/\psi \rightarrow \gamma \eta \eta'$ result \rightarrow
Phys. Rev. D 106, 072012 (2022)

$f_0(2020)$ requires further study

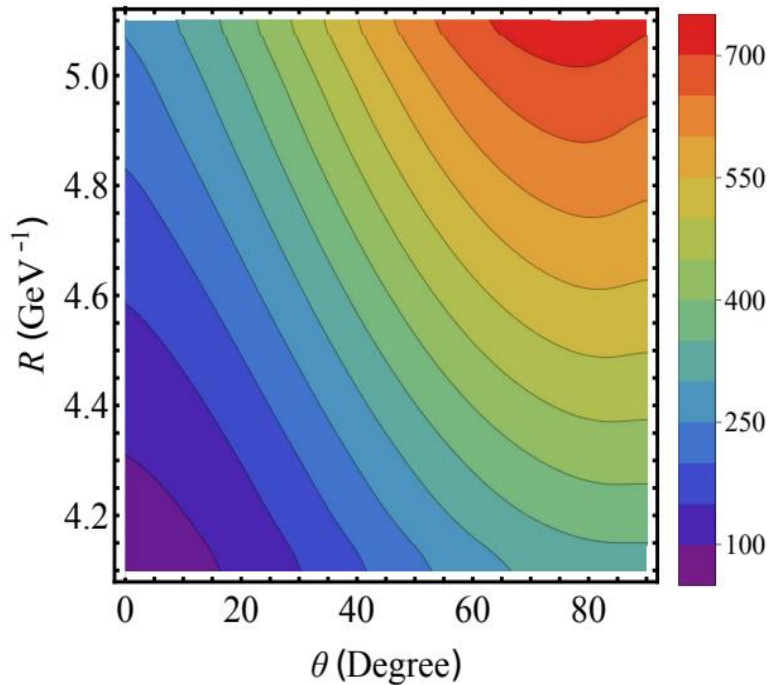


The mixing of f_0 (2020)

The mixing scheme of $f_0(2020)$

$$\begin{pmatrix} |f_0(2020)\rangle \\ |f_0(1812)\rangle \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} |s\bar{s}\rangle \\ |n\bar{n}\rangle \end{pmatrix}$$

The total decay widths of the $f_0(2020)$



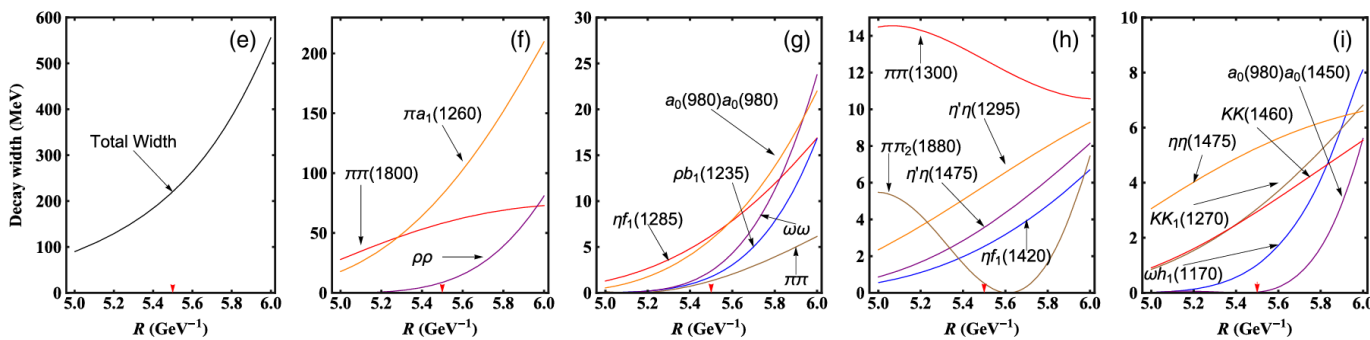
VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
$436 \pm 4^{+46}_{-49}$		¹ ABLIKIM	2022C BES3	$J/\psi \rightarrow \gamma \eta' \eta' \rightarrow 4 \gamma 2(\pi^+ \pi^-)$
$203 \pm 9^{+13}_{-11}$		² ABLIKIM	2022AS BES3	$J/\psi(1S) \rightarrow \gamma \eta'$

The partial decay widths of $f_0(2020)$ when taking center R value at 4.6 GeV

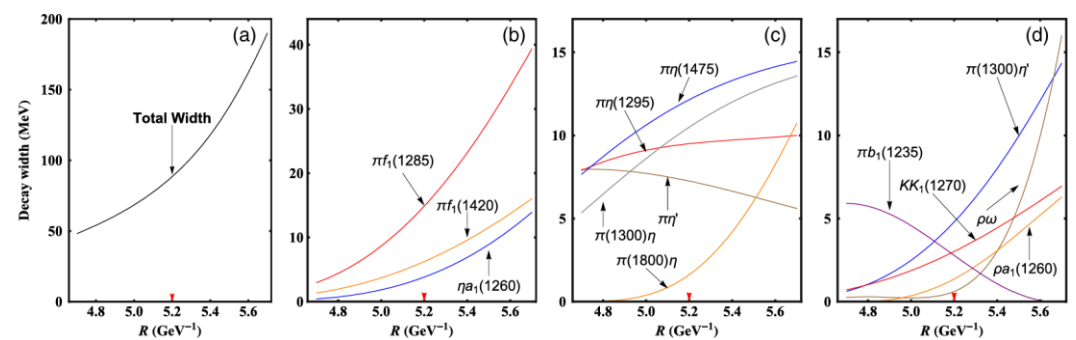
Channels	$\theta = 15^\circ$	$\theta = 50^\circ$
$\pi\pi$	1.44	12.58
$\pi\pi(1300)$	10.51	92.09
$\pi\pi(1800)$	14.41	126.25
$\pi a_1(1260)$	3.01	26.40
$\eta\eta$	5.79	9.56
$\eta\eta'$	5.86	1.21
$\eta\eta(1295)$	23.50	38.79
$\eta'\eta'$	12.43	17.41
KK	20.38	22.34
$KK_1(1400)$	17.50	6.74
$KK_1(1460)$	82.75	62.64
Total width	203.92	429.40

Assuming $R = 4.6 \text{ GeV}^{-1}$ and considering $\theta = 15^\circ$ or 50° , we derive different decay widths as reported by BESIII collaboration

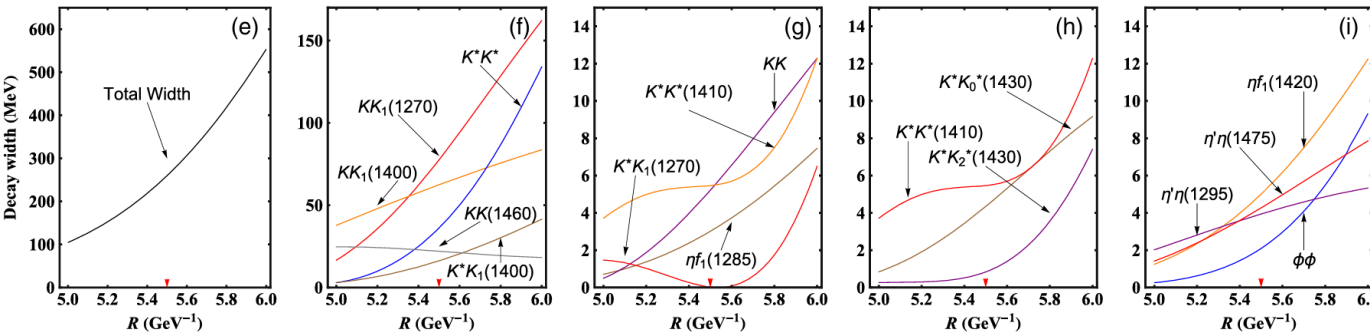
The predicted scalar mesons



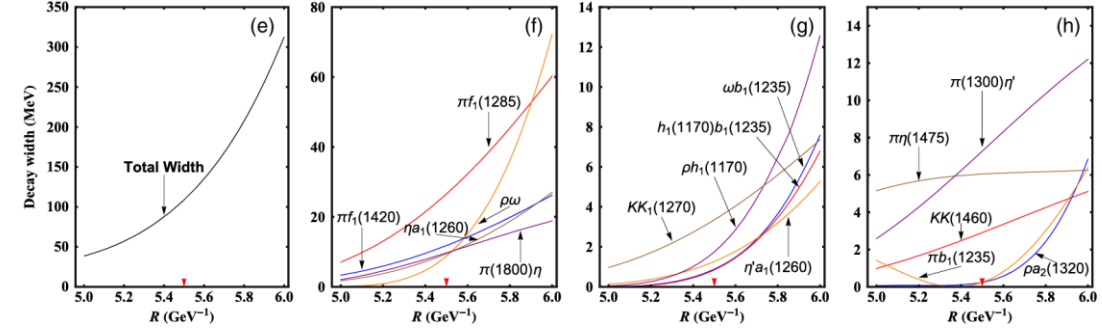
$f_0(2570)$, decay width is about **200 MeV** at center R value



$a_0(2375)$, decay width is about **80 MeV** at center R value



$f_0(2660)$, decay width is about **300 MeV** at center R value



$a_0(2610)$, decay width is about **100 MeV** at center R value

The decay behaviors of η_2 family

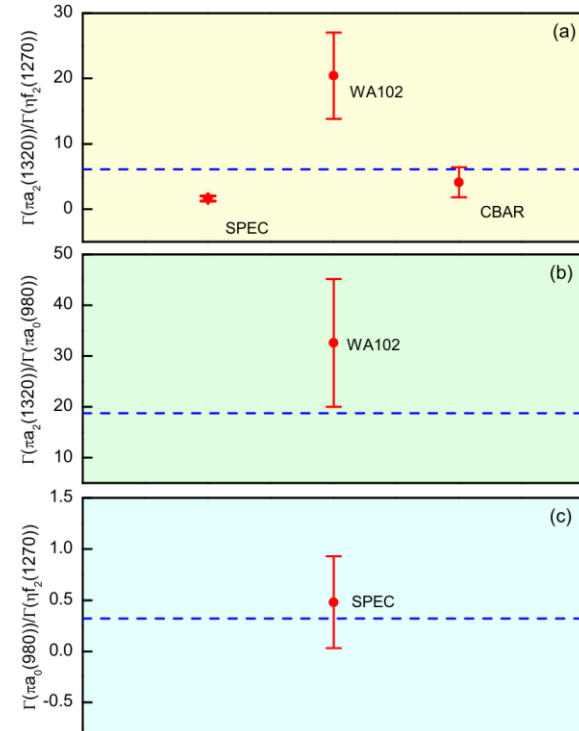
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$\eta_2(2D)$	2003	$2030 \pm 10 \pm 15$
$\eta_2(3D)$	2279	2267 ± 14
$\eta_2(4D)$	2498	...
$\eta'_2(1D)$	1882	$1881 \pm 32 \pm 40$
$\eta'_2(2D)$	2238	...
$\eta'_2(3D)$	2520	...
$\eta'_2(4D)$	2764	...

State	$\eta_2(1D)$			$\eta'_2(1D)$		
	$\theta = 0^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 0^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$
Decay channel						
$a_2(1320)\pi$	173.3	161.8	130.0	...	15.3	57.2
$\rho\rho$	28.5	26.6	21.4	...	8.3	31.0
$\omega\omega$	7.7	7.2	5.8	...	2.7	10.0
$a_0(980)\pi$	7.0	6.5	5.2	...	0.8	3.1
$a_1(1260)\pi$	4.2	3.9	3.2	...	2.4	8.9
KK^*	2.6	10.1	20.7	79.8	60.4	39.7
K^*K^*	29.5	32.8	30.0
$\eta f_2(1270)$	0.2	1.8	9.4
Total width	223.3	216.1	186.3	109.5	123.5	189.3
Exp	$180_{-21}^{+40} \pm 25$			$221 \pm 82 \pm 44$		

The mixing within the η_2 family

$$\begin{pmatrix} |\eta_2(nD)\rangle \\ |\eta'_2(nD)\rangle \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} |n\bar{n}\rangle \\ |s\bar{s}\rangle \end{pmatrix}$$

The mixing angles θ for all η_2 meson states are constrained to $\theta < 30^\circ$



The branching ratio of $\eta_2(1870)$

The η_2 mesons

The $\eta_2(2030)$ and $\eta_2(2250)$ are currently listed as tentative state in the PDG

State	$\eta_2(2D)$			$\eta'_2(2D)$			State	$\eta_2(3D)$			$\eta'_2(3D)$		
	Decay channel	$\theta = 0^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 0^\circ$	$\theta = 15^\circ$		$\theta = 30^\circ$	Decay channel	$\theta = 0^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 0^\circ$
$\pi a_2(1700)$	91.7	85.5	68.7	\	7.1	26.4	$\pi a_2(1700)$	29.5	27.6	22.2	...	3.7	13.9
$\pi a_2(1320)$	51.7	48.3	38.8	\	6.3	23.6	$\pi a_2(1320)$	18.4	17.1	13.8	...	3.7	13.8
$\rho b_1(1235)$	20.6	19.2	15.4	\	4.9	18.4	$\rho\rho$	10.7	10.0	8.0	...	2.9	10.9
$\rho\rho$	19.2	17.9	14.4	\	3.0	10.1	$\pi a_0(980)$	6.1	5.7	4.6	...	0.1	0.5
$\omega h_1(1170)$	6.3	5.9	4.8	\	2.3	8.5	$\rho b_1(1235)$	6.1	5.7	4.6	...	3.1	11.7
$\omega\omega$	6.0	5.6	4.5	\	1.0	3.6	$\pi a_1(1260)$	3.8	3.5	2.8	...	0.4	1.6
$\pi a_0(1450)$	4.9	4.6	3.7	\	0.5	1.9	$\omega\omega$	3.3	3.1	2.5	...	1.0	3.5
$a_0(980)\pi$	3.3	3.1	2.5	\	9×10^{-4}	3×10^{-3}	$\rho\rho(1450)$	2.5	2.3	1.9	...	1.9	7.2
$\eta f_2(1270)$	3.1	3.0	2.5	2×10^{-2}	0.1	2.9	$\omega h_1(1170)$	2.4	2.2	1.8	...	1.4	5.1
$a_1(1260)\pi$	2.2	2.1	1.6	\	3×10^{-2}	0.1	$\omega\omega(1420)$	1.6	1.5	1.2	...	0.7	2.7
$KK^*(1410)$	1.3	4.8	9.6	44.0	27.3	17.2	$\eta f_0(1500)$	1.6	1.5	1.2	...	1×10^{-2}	4×10^{-2}
KK^*	0.4	2.7	6.7	23.4	24.1	17.7	$\eta f_2(1270)$	1.3	1.2	1.1	3×10^{-2}	0.3	1.6
K^*K^*	0.2	0.3	0.8	17.9	18.0	15.3	$\pi a_0(1450)$	1.3	1.2	0.9	...	0.4	1.4
$KK_2^*(1430)$	0.1	0.3	0.8	35.7	39.8	35.9	K^*K_1	0.7	0.4	0.2	5.6	12.2	10.2
$KK_0^*(1430)$	4×10^{-2}	6×10^{-3}	0.1	7.0	6.0	5.7	$KK^*(1410)$	0.2	1.6	3.9	13.5	19.7	15.0
K_1K^*	\	\	\	8.9	7.2	6.4	KK^*	0.1	1.1	3.1	16.0	14.1	10.6
$\omega\omega(1420)$	\	\	\	\	0.6	2.2	$KK_2^*(1430)$	0.1	0.4	1.2	20.3	26.5	22.7
Total width	211.0	203.3	174.9	136.9	148.2	195.9	$KK_0^*(1430)$	1×10^{-2}	3×10^{-2}	0.2	3.5	4.6	4.2
Exp	205 ± 10 ± 15 [23]			\			$KK_1(1650)$	1×10^{-2}	7×10^{-3}	4×10^{-3}	0.2	1.1	0.8
							$K^*K^*(1410)$	18.9	16.8	13.9
							$K^*K'_1$	5.5	5.0	4.0
							$K^*K(1460)$	4.0	5.6	4.3
							$\pi(1300)a_0(980)$	0.5	1.9
							$a_1(1260)a_1(1260)$	0.5	2.0
							Total width	89.9	84.9	76.0	101.8	142.9	177.6
							Exp	290 ± 50 [24]			...		

The $\eta_2(4D)$ and $X(2600)$

Case	$f_0(1500)$	$X(2600)$
Mass (MeV/ c^2)	$1498.0 \pm 4.5_{-15.2}^{+4.0}$	$2617.8 \pm 2.1_{-1.9}^{+18.2}$
Width (MeV)	$166 \pm 10_{-26}^{+13}$	$200 \pm 8_{-17}^{+20}$

Calculated decay width is significantly lower than $X(2600)$

This discrepancy rules out the possibility of identifying the $X(2600)$, as a $\eta'_2(4D)$ state

Proved our earlier result
Still need further exploration

State	$\eta_2(4D)$			$\eta'_2(4D)$		
	Decay channel	$\theta = 0^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 0^\circ$	$\theta = 15^\circ$
$\pi a_2(1700)$	18.0	16.8	13.5	...	2.8	10.3
$\pi a_2(1320)$	9.9	9.2	7.4	...	2.6	9.5
$\rho\rho(1450)$	5.2	4.8	3.9	...	2.8	10.4
$\pi a_0(980)$	4.7	4.4	3.5	...	0.3	1.1
$\rho\rho$	4.1	3.9	3.1	...	1.8	6.6
$\rho b_1(1235)$	3.9	3.7	2.9	...	2.3	8.5
$\pi a_1(1260)$	2.4	2.2	1.8	...	0.4	1.6
$\omega\omega(1420)$	2.1	2.0	1.6	...	1.0	3.8
$\omega h_1(1170)$	1.7	1.6	1.3	...	1.0	3.7
$\pi(1300)a_0(980)$	1.3	1.2	1.0	...	0.2	0.8
$\omega\omega$	1.3	1.2	1.0	...	0.6	2.1
$\eta f_0(1500)$	1.1	1.1	0.8	...	1×10^{-2}	5×10^{-2}
$\eta f_2(1270)$	0.8	0.8	0.6	1×10^{-2}	0.2	1.1
$K_1 K^*$	0.3	0.3	0.3	4.8	9.8	7.9
$a_1(1260)a_0(980)$	0.3	0.2	0.2	...	0.3	1.3
$KK^*(1410)$	0.2	0.8	2.1	6.2	11.7	9.9
$K^*K^*(1410)$	0.2	0.1	0.3	20.7	13.7	11.6
$KK_2^*(1430)$	0.1	0.4	1.4	15.4	19.4	16.0
$K^*K_2^*(1430)$	0.1	0.6	1.3	6.1	11.5	9.5
K^*K^*	7×10^{-2}	0.3	1.0	11.0	15.6	12.8
KK^*	3×10^{-2}	0.7	2.1	12.9	11.6	9.0
$K'_1 K^*$	2×10^{-2}	0.2	0.6	5.1	10.6	8.6
$K^*K(1460)$	2×10^{-2}	6×10^{-2}	0.1	6.1	5.7	4.4
$KK_0^*(1430)$	3×10^{-4}	4×10^{-2}	0.2	1.9	2.8	2.4
$K^*K_1(1650)$	7.1	15.8	12.7
$K_1 K^*(1410)$	2.4	0.9	1.2
$K_1 K_2^*(1430)$	1.2	1.3	0.9
$a_1(1260)a_2(1320)$	0.5	1.7
$\rho(1450)b_1(1235)$	0.4	1.6
Total width	57.9	55.9	52.0	98.5	147.6	171.0

Summary

- 1. We conduct a systematic investigation of high-lying scalar and η_2 mesons.**
- 2. The mass spectrums are constructed for scalar mesons and η_2 states through Regge trajectory and GI model.**
- 3. Strong decay behaviors are analyzed via the QPC model, calculating partial widths and branching ratios.**
- 4. The study of high-lying states may be a new task for experimental study.**

THANKS!