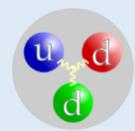


实用中子衍射晶体学
Practical Neutron Diffraction Crystallography
(I)

粉末衍射和材料科学
Powder Diffraction and Materials Science

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中国散裂中子源
China Spallation Neutron Source



China Spallation Neutron Source (CSNS)

In different periods, the design and construction of different instruments and equipment must be based on needs of national and/or regional science and technology and economic development.

第一期

[BL18: General-Purpose Powder Diffractometer](#)

[BL02: Multi-Purpose Reflectometer](#)

[BL01: Small-Angle Neutron Scattering](#)

[BL16: Multi-Physics Instrument](#)

[BL11: Atmospheric Neutron Irradiation Spectrometer](#)

[BL05: High-Energy Direct-Geometry Inelastic Spectrometer](#)

[BL13: Energy-Resolved Neutron Imaging Instrument](#)

[BL14: Very Small-Angle Neutron Scattering](#)

[BL15: High-Pressure Neutron Diffractometer](#)

[BL09: High-Resolution Neutron Diffractometer](#)

[BL08A: Engineering Material Neutron Diffractometer](#)

第二期

[BL20: Direct-Geometry Polarized Inelastic Spectrometer](#)

[BL12: Neutron Physics and Application Spectrometer](#)

[BL19: Macromolecular Single-Crystal Neutron Diffractometer](#)

[BL17: Elastic Diffuse Scattering Neutron Diffractometer](#)

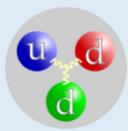
[BL10: Neutron Backscattering Spectrometer](#)

[BL04: Cold Neutron Inelastic Spectrometer](#)

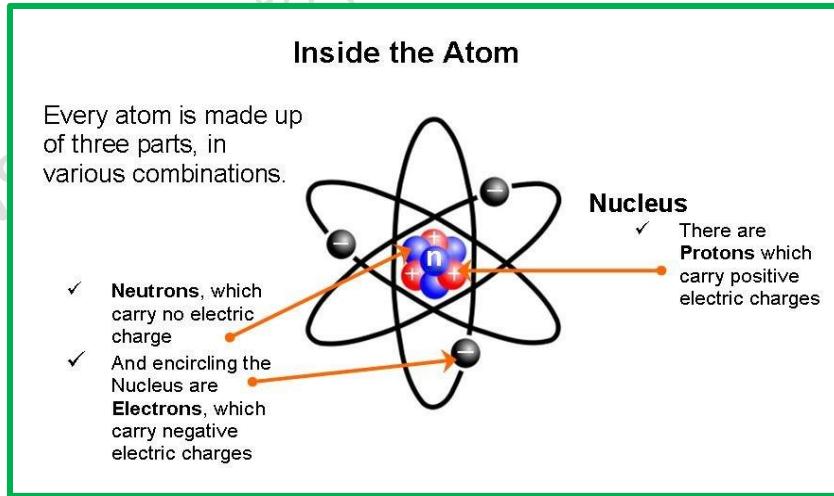
[BL08B: Neutron Technology Development](#)

[BL03: Liquid Reflectometer](#)

[BL06: Indirect-Geometry Molecular Vibrational Spectrometer](#)



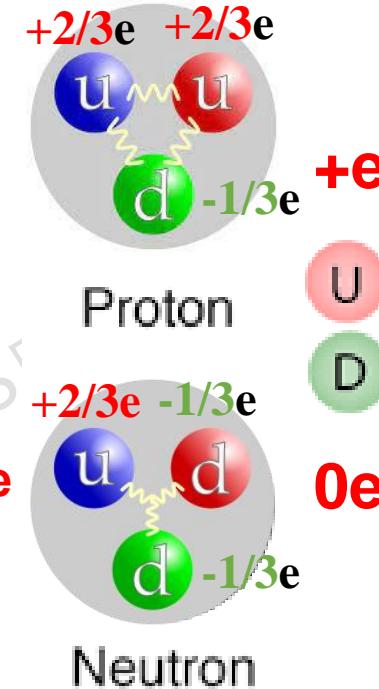
Neutron, A Subatomic Particle



All matters are composed of tiny particles call atom. Every atom is made up of three types of smaller subatomic particles, electron, neutron, and proton. Proton and neutron make up nucleus, surrounded by electrons.

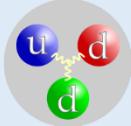
Proton
two “up” quarks (charge $+4/3$ e)
one “down” quark (charge $-1/3$ e)

Neutron
one “up” quark (charge $+2/3$ e)
two “down” quarks (charge $-2/3$ e)



$$\begin{aligned} U &= \text{"up" quark} & +\frac{2}{3} e \\ D &= \text{"down" quark} & -\frac{1}{3} e \\ 0e & & \end{aligned}$$

The proton carries two “up” quarks and one “down” quark, while the neutron carries one “up” quark and two “down” quarks. The “up” quark have $+2/3$ e, and the “down quark has $-1/3$ e. So that the proton carries $+e$, and the neutron is a neutral particle.

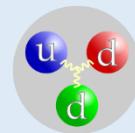


Intrinsic Properties of Neutron, Wave-particle Duality

中子的本征性质，波粒二象性

<u>Theorized</u>	<u>Ernest Rutherford (1920)</u>
<u>Discovered</u>	<u>James Chadwick (1932)</u>
<u>Mass</u>	$1.67492749804(95) \times 10^{-27}$ kg, $939.56542052(54)$ MeV/c ² , $1.00866491588(49)$ Da
<u>Mean lifetime</u>	879.4(6) s (free)
<u>Electric charge</u>	0 e ($-2 \pm 8 \times 10^{-22}$ e (experimental limits))
<u>Electric dipole moment</u>	$< 2.9 \times 10^{-26}$ e·cm (experimental upper limit)
<u>Electric polarizability</u>	$1.16(15) \times 10^{-3}$ fm ³
<u>Magnetic moment</u>	$-1.04187563(25) \times 10^{-3}$ μ_B , $-1.91304273(45)$ μ_N
<u>Magnetic polarizability</u>	$3.7(20) \times 10^{-4}$ fm ³
<u>Spin</u>	1/2
<u>Wavevector</u>	Magnitude $2\pi / \lambda$
<u>Wavelength</u>	h/mv
<u>Energy (E)</u>	$(1/2)mv^2 = h^2/2m\lambda^2$

1. The most mass of an atom comes from proton and neutron. The mass of a neutron ($1.67492749804(95) \times 10^{-27}$ kg) is slightly greater than a proton.
2. Neutrons accompany protons in nucleus. When neutrons leave nucleus become free, the average lifetime of a free neutron is about 14.66 minutes.
3. Although neutron is a neutral particle, it carries zero electric charge. The magnetic moment of neutron is not zero.
4. It has spin $1/2$ with moment of $-0.001042 \mu_B$.
5. This is an indication of its quark substructure and internal charge distribution.
6. Energy $E = \frac{1}{2} mv^2 = h^2/2m\lambda^2$, that is the lower v the lower E or the shorter λ the higher E .
7. Neutrons move in a wave mode; the wavelength $\lambda = h/mv$, i.e. the higher v the shorter λ .
8. The magnitude of wavevector ($2\pi / \lambda$) is a function of wavelength.
9. Neutrons possess wave-particle duality.



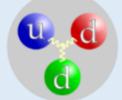
Neutron, Wave-Particle Duality

Wave Neutron diffraction is a form of elastic scattering where the neutrons exiting the experiment have the same energy as the incident neutrons. This technique can be used to study the atomic and magnetic structures of a material, such as crystalline solids, amorphous, liquids, and gasses.

Particle Inelastic scattering occurs because the atoms in a solid are of finite mass and they can gain or loss energy when neutrons, or any kind of radiation, collide with them. It can be used to study the atomic dynamics of the sample, such as quantum materials, energy-related materials, soft matter, complex fluids, biology, magnetic excitations, vibrational and rotational, diffusional processes and quantum tunnelling.

中子衍射类似X-射线衍射，是一种弹性散射，即实验中的入射与散射的中子具有相同的能力。但不同的辐射所得到的信息具有互补性。中子衍射用于分析晶体结构/磁结构，适用研究结晶固体，气体，液体以及非晶材料。

非弹性散射发生在当中子或任何类型的辐射与固体中的原子碰撞时获得或损失能量。用来研究量子材料，能量相关材料，软物质，复合流体，生物学，磁激发，振动和旋转光谱，扩散过程和量子隧道等。



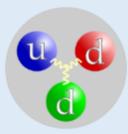
Elastic and Inelastic Scattering

Table 1.1.1

Types of scattering from a sample

Type of scattering	Coherent	Incoherent
Elastic Wave Neutrons scattering from a sample have the same energy as the incident neutrons.	Bragg scattering Magnetic Bragg scattering Bragg scattering from ferroelectric/magnetic order Diffuse scattering from static defects Diffuse signal from small nanoparticles (<10 nm) Scattering from amorphous material (except excitations) Multiple scattering (coherent)	Laue monotonic diffuse scattering Neutron incoherent scattering Multiple scattering (incoherent)
Inelastic Particle The neutrons gain or lose some energy as scattering from a sample.	Thermal diffuse scattering Spin-wave scattering Paraelectric/paramagnetic scattering Scattering from liquids	Compton scattering Fluorescence Incoherent scattering from hydrogen

When atoms in a solid are of finite mass and they do or don't gain or loss energy when neutrons, or any kind of radiation, collide with them.



中子的优势特点

为什么用中子? 中子有揭示了其他探针无法获得的特性的能力。它可以像波一样衍射或反射，或者像粒子在运动过程中与物质碰撞时获得或失去能量。

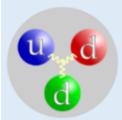
波长 从 0.1\AA 到 100\AA 不等，允许它们测量从像原子一样小到蛋白质一样大的结构。

能量 在毫电子伏特量级，与固体或液体中原子运动，磁性材料中的波或分子振动的能量相同。可以检测的小的纳米电子伏特和十分之一电子伏特的中子与物质之间的能量交换。

散射本领 几乎随机地因原子核而异。有利于对探测轻的原子，同位分离等。

磁性 使得中子对原子中的电子自旋和电子的轨道自旋的有序度都很敏感。

穿透能力强 中性的中子使得其能够深入样品，更容易穿过极端条件环境设备壁达到样品，深入测量工程部件中的应力应变。

**Table 2.3.5**

Advantages of CW and TOF instruments (modified from Kisi & Howard, 2008)

CW	TOF
(1) Incident beam may be essentially monochromatic, in which case the spectrum is well characterized 入射中子基本单一波长，谱图特性好	(1) The whole incident spectrum is utilized, but it needs to be carefully characterized if intensity data are to be used 运用全入射谱，强度数据需仔细进行刻度校正。
(2) Large d -spacings are easily accessible for study of complex magnetic and large-unit-cell structures 能测量大d值晶面间距，有利于分析复杂磁结构和大晶胞晶体结构	(2) Data are collected to very large Q values (small d -spacings) 能测量非常大Q值数据 (小晶面间距d)
(3) Can fine tune the resolution during an experiment 在实验过程中能调整分辨率	(3) Few cold neutron instruments are available for study of complex magnetic and large-unit-cell structures 冷中子谱议可用于研究磁结构和大晶胞结构。
(4) More common 更通用	(4) Resolution is constant across the whole pattern 整个谱图的分辨率不变
(5) Peak shapes are simpler to model 峰型简单更容易拟合	(5) Very high resolution is readily attained by using long flight paths 用长的飞行管道可达到非常好的分辨率
(6) Absorption and extinction corrections are relatively straightforward 吸收和消光校正相对简单	(6) Complex sample environments are very readily used if 90° detector banks are available 复杂的样品环境可用于90度的探测器组。
(7) Data storage and reduction is simpler 数据存储和简化简单	(7) Simpler to intersect a large proportion of the Debye–Scherrer cones with large detector banks 用大的探测器组对横切大比例Debye-Scherrer锥更为简单。
(8) Extremely rapid data collection and stroboscopic measurements are feasible 可进行极快的数据收集和频闪测量	(8) Very fast data collection is feasible 数据采集非常快捷。
(9) Engineering diffractometers are very well suited for strain scanning in complex objects 工程衍射仪非常适合复杂构件的应变扫描	(9) Engineering diffractometers use an extended diffraction pattern, ideal for <i>in situ</i> loading and/or heating 工程谱议适合原位加载和/或加热，连续采集衍射谱。
(10) Texture is straightforward to measure on engineering diffractometers 工程衍射仪对织构测量简单容易	(10) Texture can be measured on universal instruments 通用谱议可测织构。

Table 2.3.6

Suitability of problems to high-resolution or high-intensity diffractometers

Reproduced from Kisi & Howard (2008) by permission of Oxford University Press.

Problem	High resolution	High intensity (medium resolution)
Solve a complex crystal or magnetic structure 分析复杂晶体结构或磁结构	Essential, especially in the presence of pseudo-symmetry	Not usually suitable†‡
Refine a complex crystal or magnetic structure 精化复杂晶体结构或磁结构	Essential. Will benefit from a high Q -range if available	Not usually suitable†‡
Solve or refine small inorganic structures 解析或精化小分子无机晶体结构	Beneficial, but not usually essential unless pseudosymmetry is present	Usually adequate
Quantitative phase analysis 定量相分析	Only required when peaks from the different phases are heavily overlapped	Usually adequate. Allows phase quantities to be tracked in fine environmental variable steps (T, P, E, H etc.) during <i>in situ</i> experiments
Phase transitions 相转变	Depends on the nature of the transition and complexity of the structures. Essential for transitions involving subtle unit-cell distortions and pseudosymmetry	Often adequate for small inorganic structure transitions and order-disorder transitions. Allows fine steps in an environmental variable (T, P, E, H etc.)
Line-broadening analysis 线-宽分析	Essential for complex line broadening such as from a combination of strain and particle size, dislocations, stacking faults etc.	Adequate for tracking changes in severe line broadening as a function of an environmental variable (T, P etc.) especially if the pure instrumental peak shape is well characterized
Rapid kinetic studies 快速动力学研究	Not appropriate	Essential

† In some cases the symmetry and lattice parameters are such that the diffraction peaks are well spaced and not severely overlapped even at modest resolution. ‡ May be necessary to supplement high-resolution data to observe weak superlattice reflections in the presence of very subtle or incomplete order-disorder transitions.

Table 2.3.7

Guidance on choice of wavelength/detector bank

Reproduced from Kisi & Howard (2008) by permission of Oxford University Press.

Problem	Choice	Reasons
Solve complex or low-symmetry structures 分析复杂或低对称性的结构	Longer wavelength	Increase d -spacing resolution to allow correct symmetry and space group to be assigned
Refine a large or complex crystal structure 精修大的或复杂的晶体结构	Shorter wavelength	Ensure that the number of peaks greatly exceeds the number of parameters. Improve determination of site occupancies and displacement parameters
Solve or refine magnetic structures 解磁结构或精修磁结构	Longer wavelength	Ensure that large d -spacing peaks are observed. Spread the magnetic form factor over the entire diffraction pattern
Quantitative phase analysis 定量相分析	Usually shorter wavelength	Improve the accuracy of the determination. Longer wavelengths only required if peak overlap is severe
Phase transitions 相转变分析	Shorter wavelength Longer wavelength	Ensures adequate data for order-disorder or other unit-cell-enlarging transitions Subtle unit-cell distortion or pseudosymmetric structures

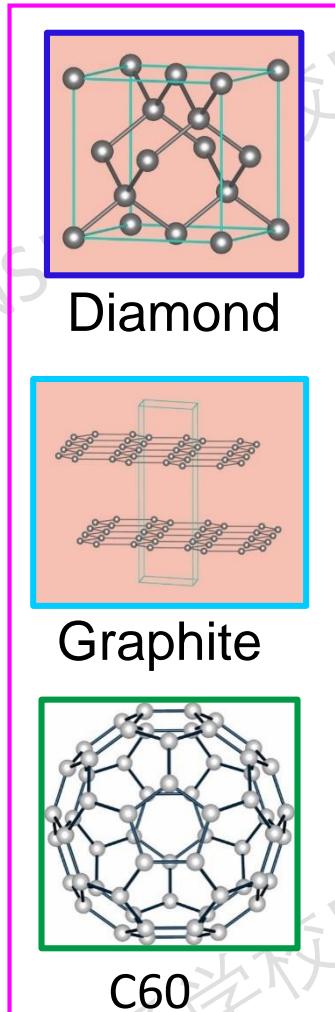
结构与性能

Structure and Property

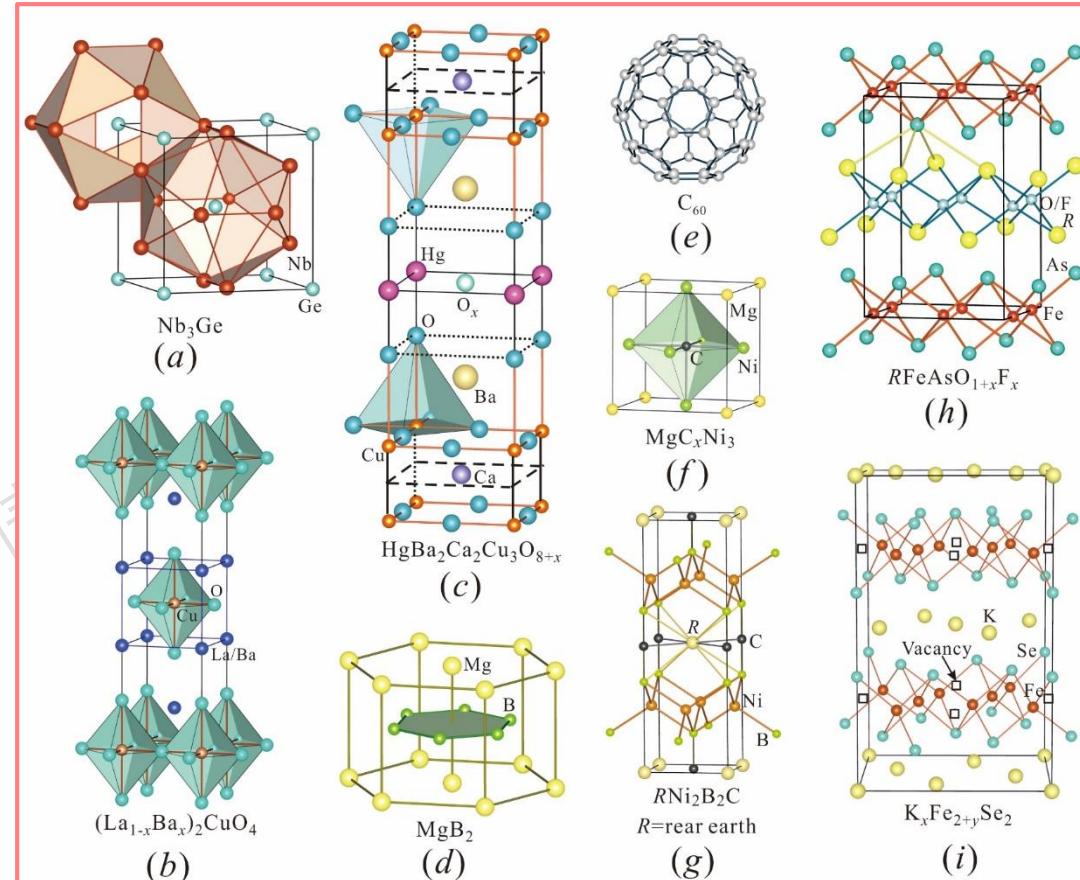
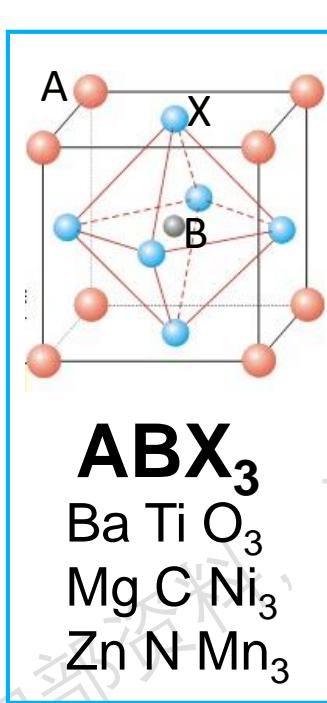
材料科学: 一级学科，包括金属材料，无机非金属材料，有机材料，有机高分子材料等。

主要研究: 材料成分，组织结构，制备工艺与材料性能及应用之间相互关系。

核心问题: 结构与性能。



(A) 同质异构
性能不同



(C) 异质异构 同种性能

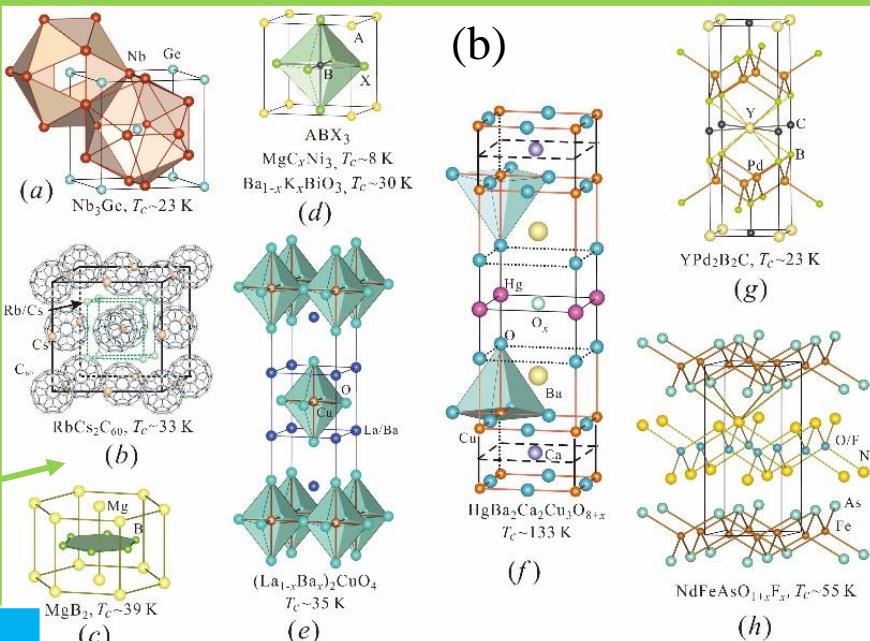
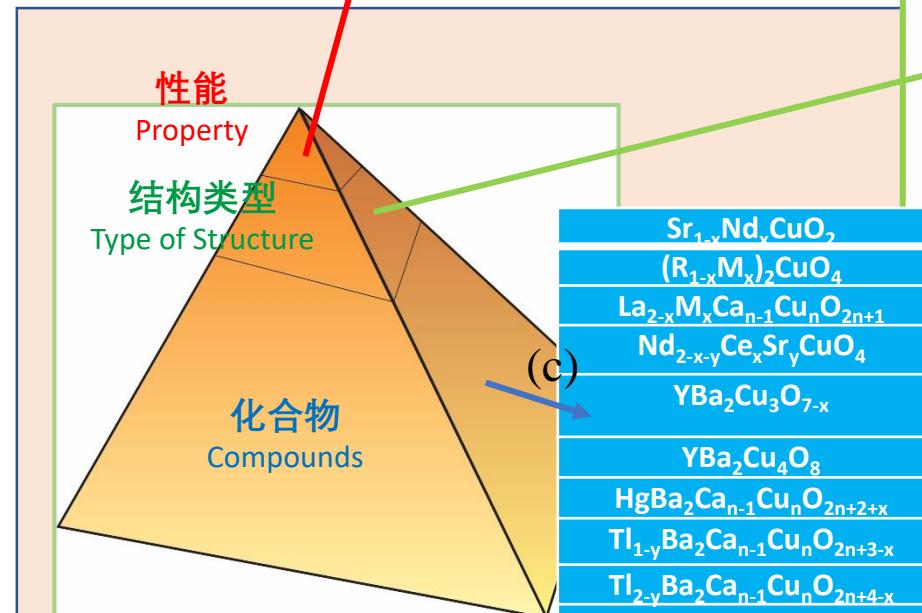
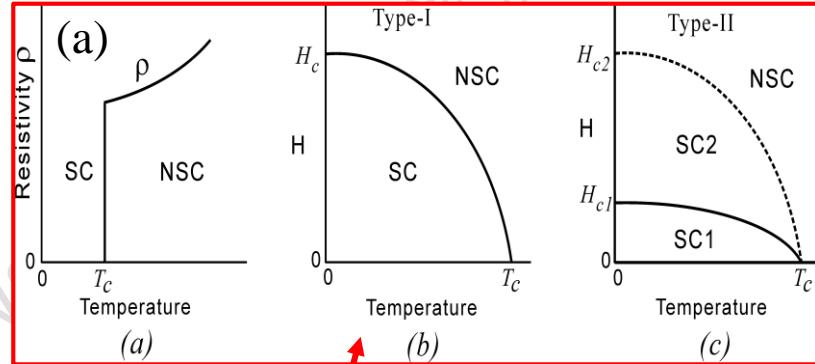
在材料科学中，性能是由结构和结构中的成分及其分布决定，例如：

1. 图(A)中的三种不同的结构都由碳元素组成，但它们具有不同的特性。
2. 图(B)列出的三种化合物都具有相同的结构，但它们的性能完全不同。
3. 图(C)所示的所有结构和成分都不相同，但它们都可能具有超导性能。其超导性能也随着部分改变其中的组分而变化。

结构材料也与功能材料类似，性能与结构紧密关联。因此在材料科学中，结构的研究是建立材料基因库的重中之重。

功能材料探索中的重要步骤

Search for new Functional Materials



1. 确定研究的性能；
2. 选择结构类型；
3. 选择结构，化合物制备；
4. 分析结构和性能及其关系；
5. 理论探讨其机理。

在新材料的探索研究过程中一般有以下几个过程：

1. 首先选择要研究材料的性能，例如选择研究图(a)超导性能。
2. 选择可能具有超导性能的已知的结构类型（如图(b)）或根据经验和理论推测一种新的结构模型。
3. 设计切合该结构的化合物。
4. 化合物制备并进行性能测试和结构分析。
5. 结果分析。

Powder diffraction: a useful toll for revealing
the most important structural information in materials science



X-ray
Neutron }
Electron } Diffraction

Rietveld 方法和相应的峰型分析软件的发展

Development of Rietveld method and related software for profile analysis

粉末样品制备简易

Easy to prepare powder sample

困难或不可能生长足够大的单晶体

Difficulty or impossible to grow single crystal

使用特殊的环境条件方便

Convenient for using special environmental condition

容易中子衍射研究磁结构和性能

Easy for studying magnetic structure and properties by NPD

...

定量物相分析 Quantitative phase analysis

结构精化 Structure refinement

化学成分确定 Chemical composition

对称性分析 Symmetry analysis

分析元素分布 Element distribution

织构, 应变等研究 Texture, stress ...

二维结构测定 2-D structure

局部结构等 Local structure...

有序度研究 Order degree

磁结构和性能 Magnetic structure & properties (NPD only)

多晶衍射方法的广泛应用

Macromolecules 大分子

Zeolites 沸石

Minerals and Mining 矿物和采矿

Inorganic Structures 无机结构

Glass Ceramics 玻璃陶瓷

Ceramic Materials (incl medicals) 陶瓷材料

Metals and Alloys 金属和合金

Cement 水泥

Polymers and Fibers 聚合物和纤维

Pharmaceuticals 制药

Forensic Science 法医科学

Materials for Energy Storage and Conversion 能源储存和转换材料

Magnetic Materials 磁性材料

Catalysis 催化

Peroleum and Petrochemicals 石油和石化产品

Superconductivity 超导

Composites 复合材料

Paint and Pigments 油漆和颜料

Piezo Ceramics 压电陶瓷

Aeronautics and Space Materials 航空航天材料

Metal-Organic Framework 金属有机框架

• • • • •

X射线和中子粉末衍射峰的位置，强度和结构因子

Powder diffraction positions, intensity, and structural factors for XRPD & NPD

Peaks Position: $2dsin\theta = n\lambda$

where λ is the incident beam wavelength, d and θ are the distance between successive hkl planes and Bragg angles of reflections, respectively.

Diffraction Intensity: $I_{hkl} = C|F_{hkl}|^2$

where $|F_{hkl}|^2$ is the hkl reflection amplitude of the diffracted X-ray, or neutron, or magnetic, and C is all others.

X-ray: $|F_{hkl}|^2 = |\sum f_j \exp(2\pi i (hx + ky + lz))|^2 e^{-2W}$

where f_j is the X-ray atomic scattering factor of atom j for X-ray.

Neutron: $|F_{hkl}|^2 = \sum b_j \exp(2\pi i (hx + ky + lz))|^2 e^{-2W}$

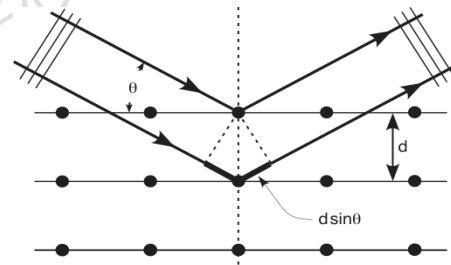
where b_j is the neutron scattering length for atom j .

Magnetic: $|F_{hkl}|^2 = \sum q_j f_{Mj} \exp(2\pi i (hx + ky + lz))|^2 e^{-2W}$

where q_j and f_{Mj} are the magnetic interaction vector and the magnetic form factor for atom j , respectively.

X-射线衍射与中子衍射具有许多共同点。峰的位置都遵循Bragg方程：

$$2dsin\theta = n\lambda$$



衍射峰的强度：

$$I_{hkl} = C|F_{hkl}|^2$$

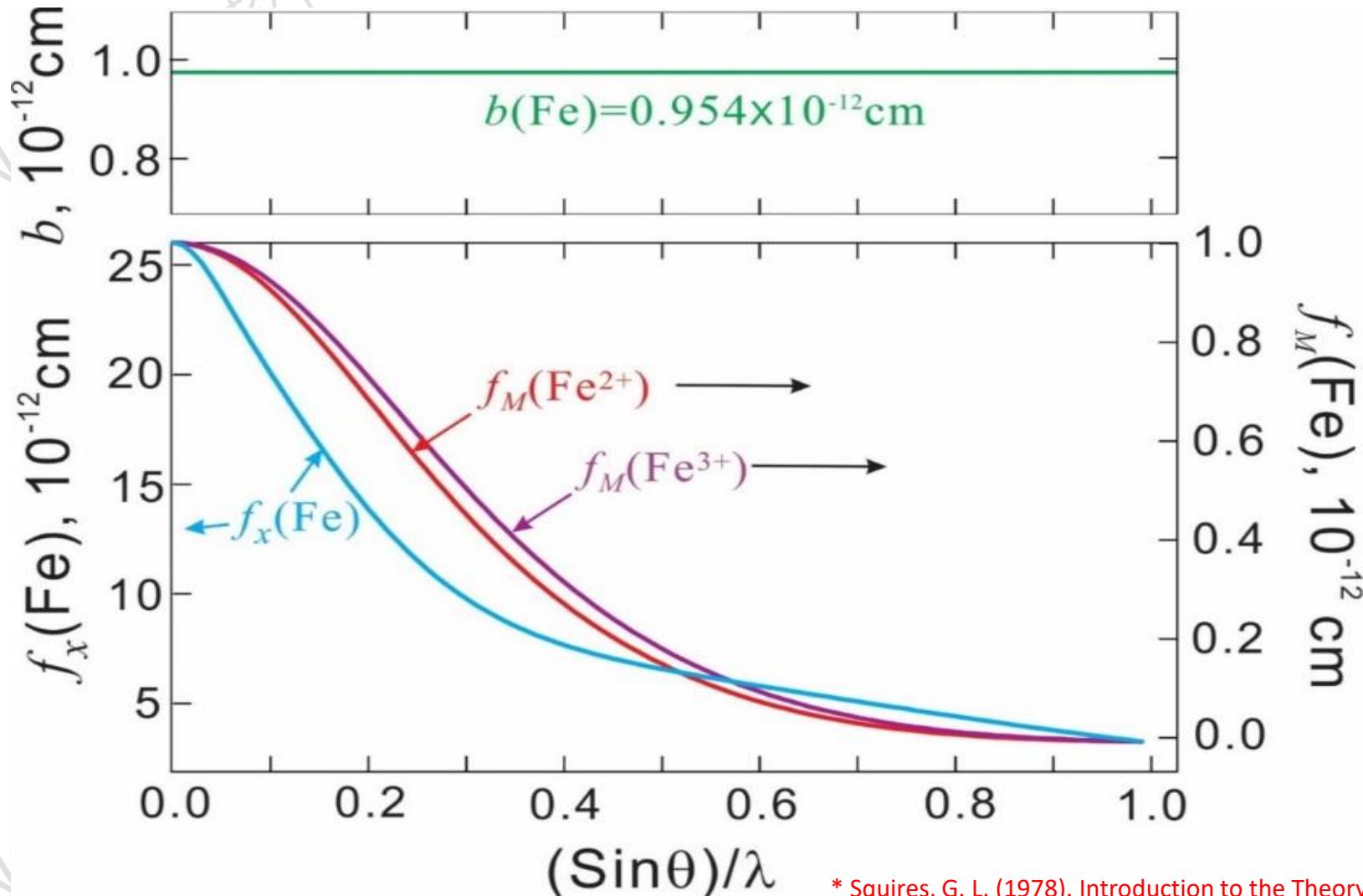
式中 C 是与晶体结构无关的参数, F_{hkl} 是结构因子。

(1) 在结构因子中, 除了由于元素的散射因子差异使得衍射峰强度不同外, 其它与结构有关的参数都一样。

(2) 在中子衍射中, 磁有序的衍射谱图是一套独立于晶体结构的衍射图, 因此磁相可作为一个独立的相精化得到磁结构信息。

中子, X射线和粉末衍射峰的位置, 强度和结构因子
Powder diffraction positions, intensity, and structural factors for XRPD & NPD

$f_X(\text{Fe})$, $b_N(\text{Fe})$, and $f_M(\text{Fe})$

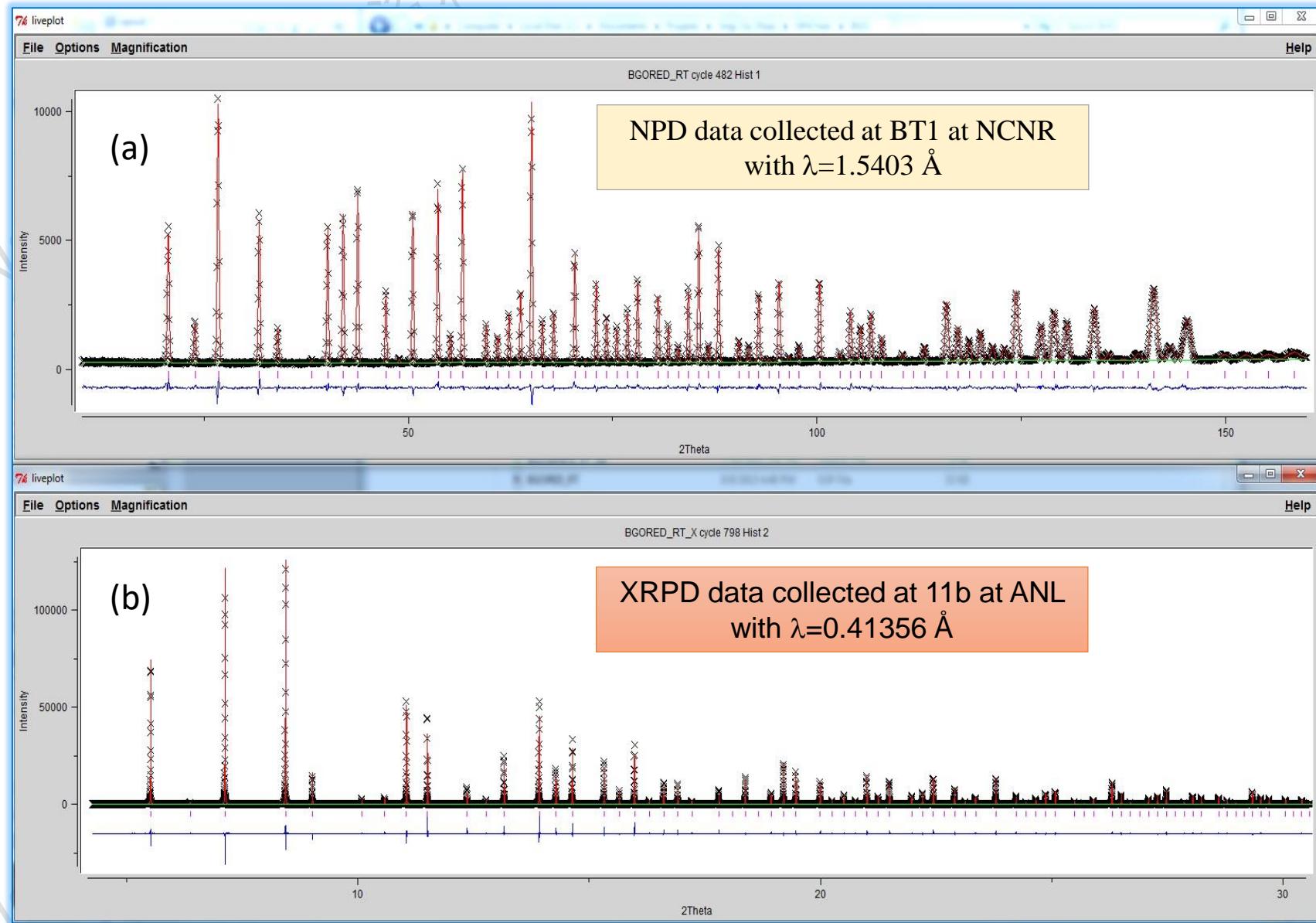


x-射线的电子散射因子

(f_x) 和磁形状因子 (f_M)

都是衍射角和波长 $(\sin \theta / \lambda)$ 的函数, 数值随着 $\sin \theta / \lambda$ 增大而减小, 因而其衍射峰强度随着 $\sin \theta / \lambda$ 增大而衰减。而中子散射因子(b^*)和磁矩(μ_B)是常数, 不随 $\sin \theta / \lambda$ 变化而变化, 因此中子衍射在高角度仍然有强峰。

X射线与中子衍射谱图 XRPD& NPD diffraction patterns

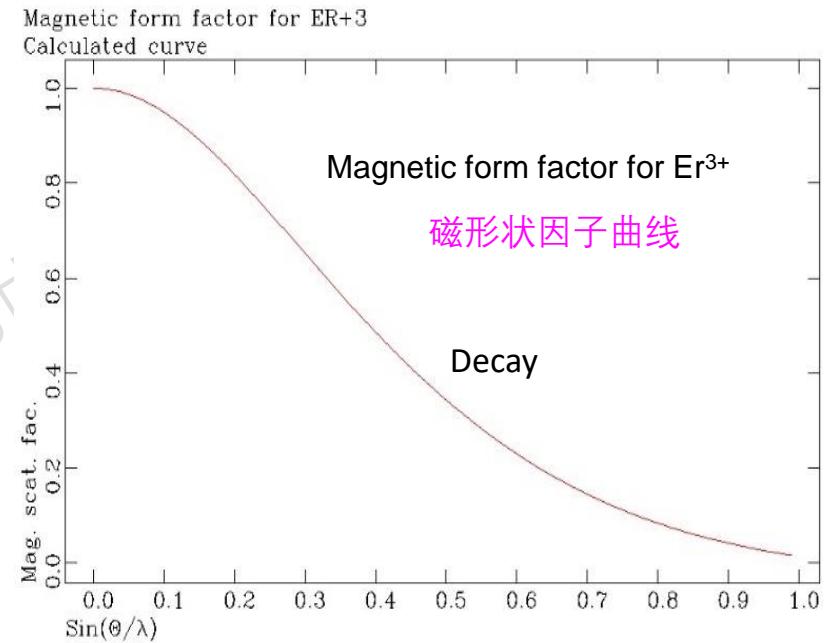
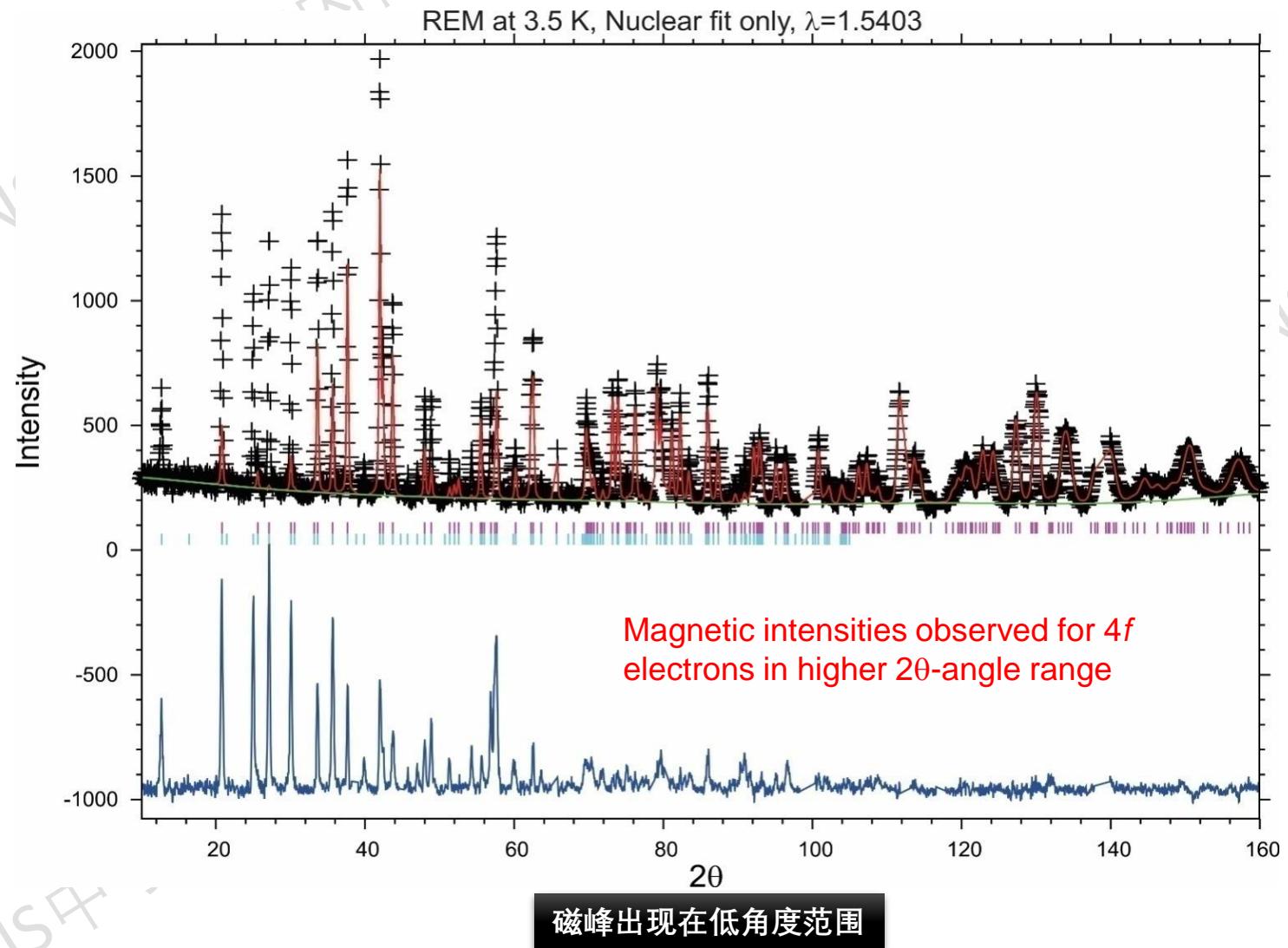


左图所示的是 $\text{Bi}_4\text{Ge}_3\text{O}_{12}$ 的中子(a) 和 X 射线(b) 在相同 Q 范围的粉末衍射精修谱。该化合物为立方晶系，样品由单晶体研磨并过 300 目筛，衍射数据在室温收集。可以看到：

1. 衍射峰没有重叠现象；
2. 图(a)的中子衍射在整给角度范围内强度都比较均匀，高 Q 的峰强没有明显的减小，这是因为中子的散射振幅是常数；
3. 图(b)的 XRPD 的衍射谱图随着角度的增大强度迅速减弱，这是由于 X 射线衍射中的电子散射振幅随着角度增大而减小，最终趋近零。

磁有序, 磁晶胞, 磁对称性, 磁结构及性能

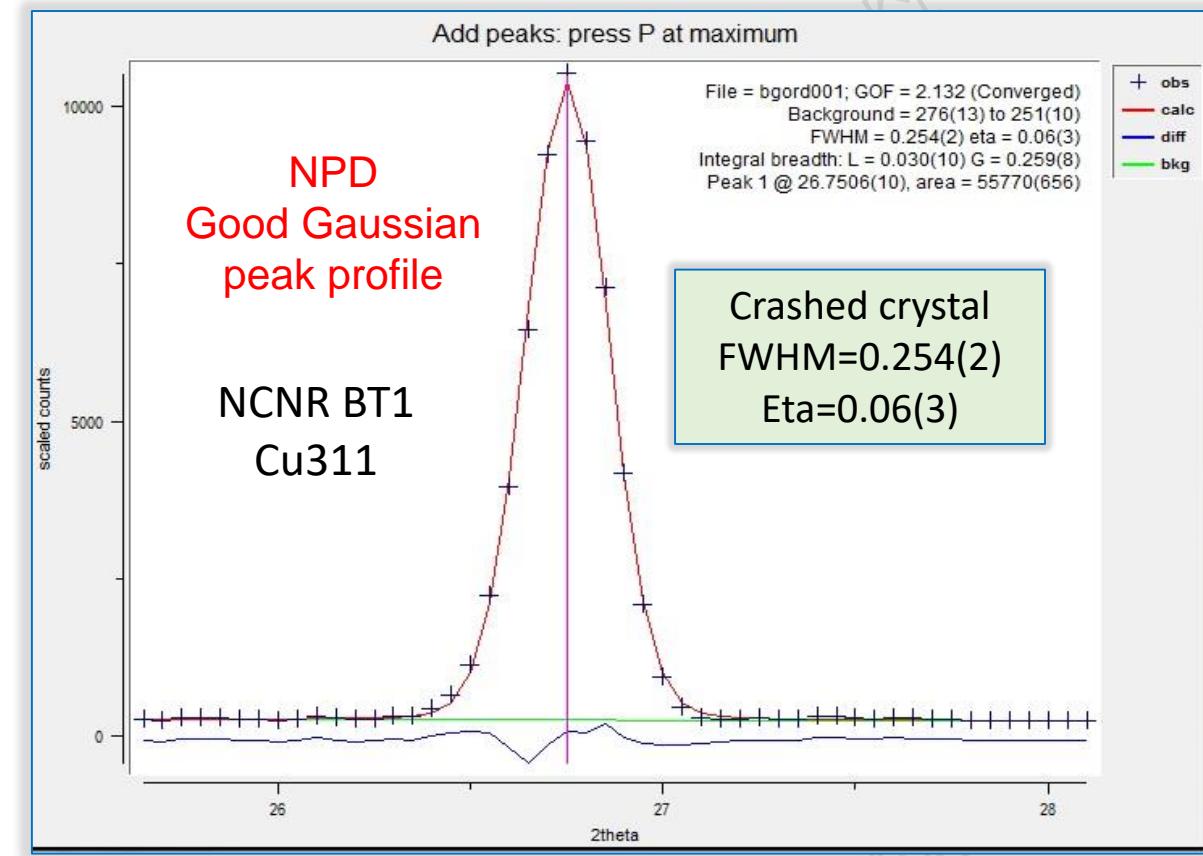
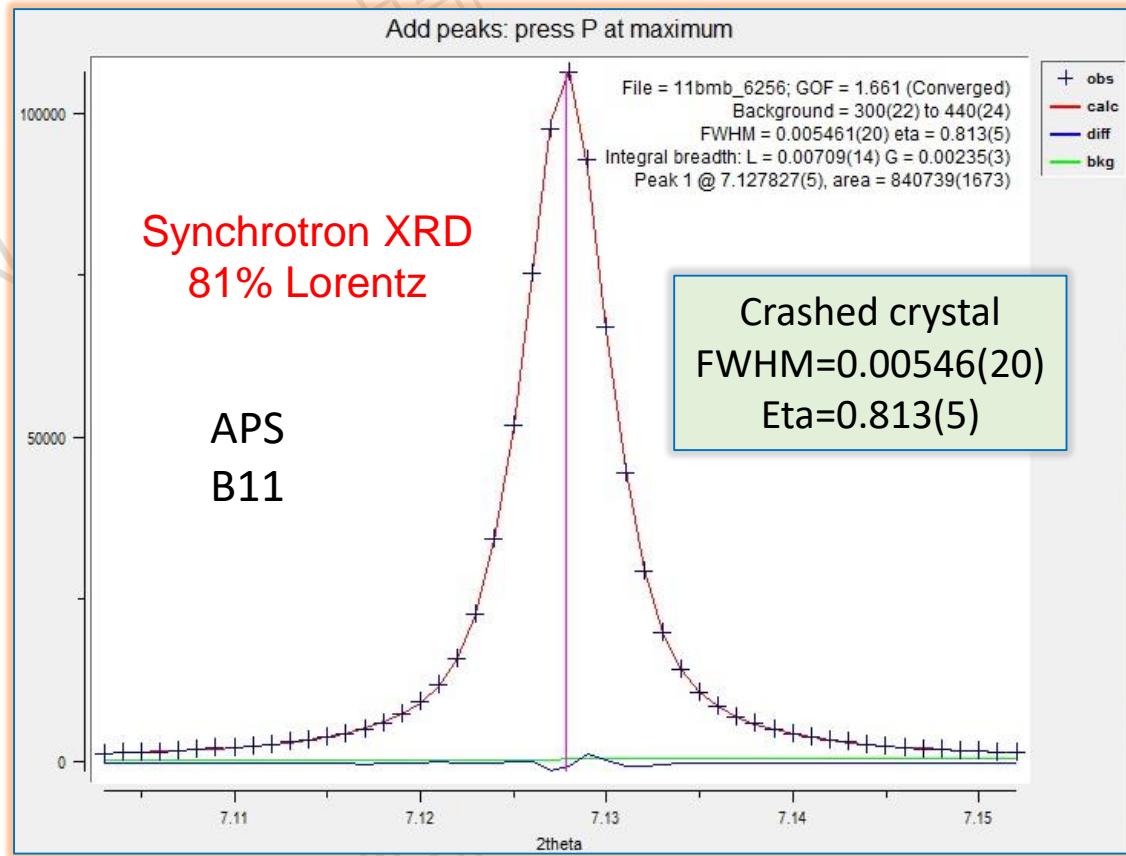
Spins order, magnetic cell, magnetic symmetry, and structure & properties



含重稀土 Er^{3+} 合金的中子衍射谱图。图中红线是以晶体结构拟合曲线，图的下部观察数据与计算数据的差值是 Er^{3+} 的有序的磁衍射峰。

X射线和中子衍射峰的峰型剖面

Diffraction Peak Profile of XRPD and NPD



$$L(2\theta - 2\theta_{hkl}) = \frac{1}{2\pi} \left(\frac{\text{FWHM}}{(2\theta - 2\theta_{hkl}) + \text{FWHM}^2/4} \right)$$

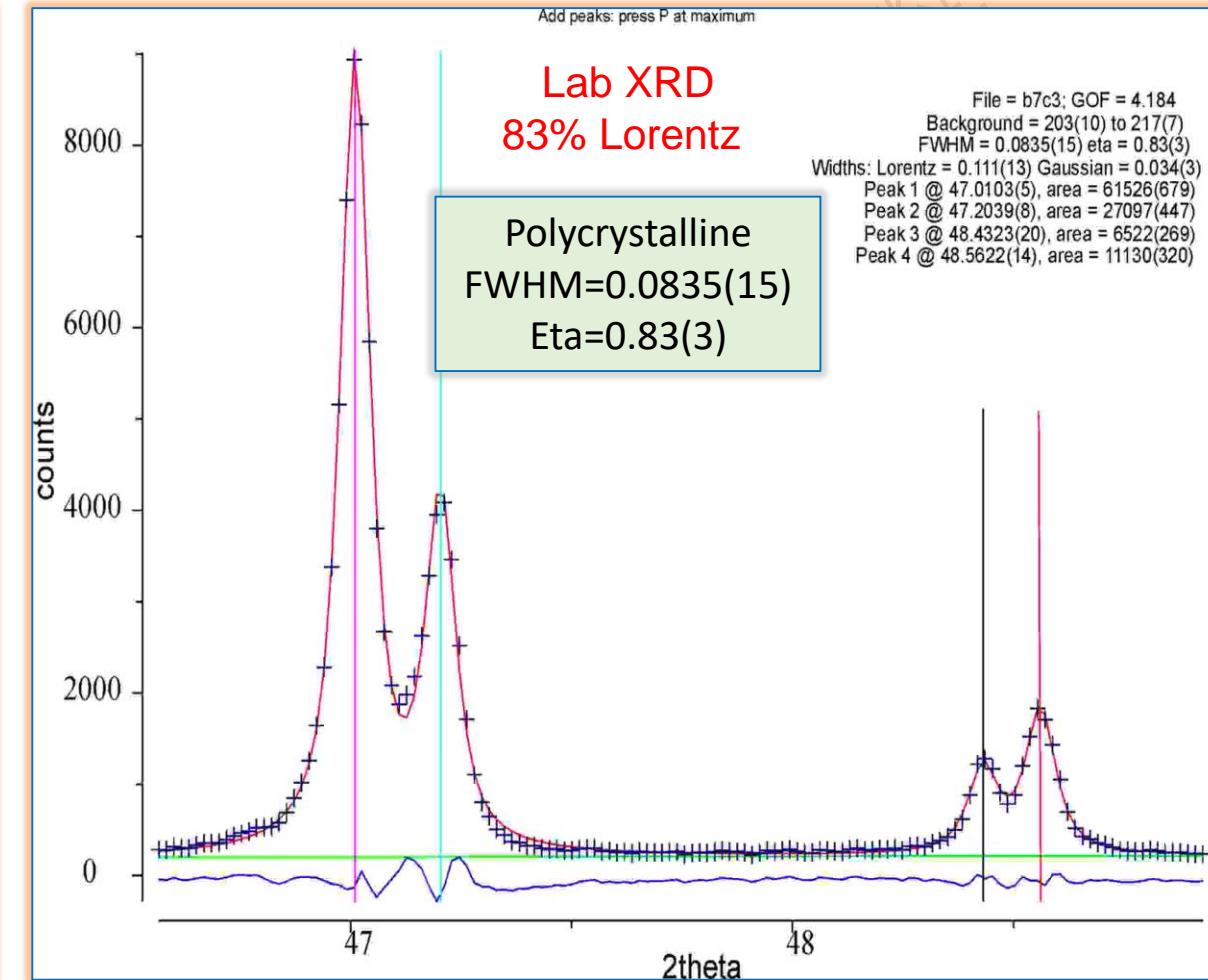
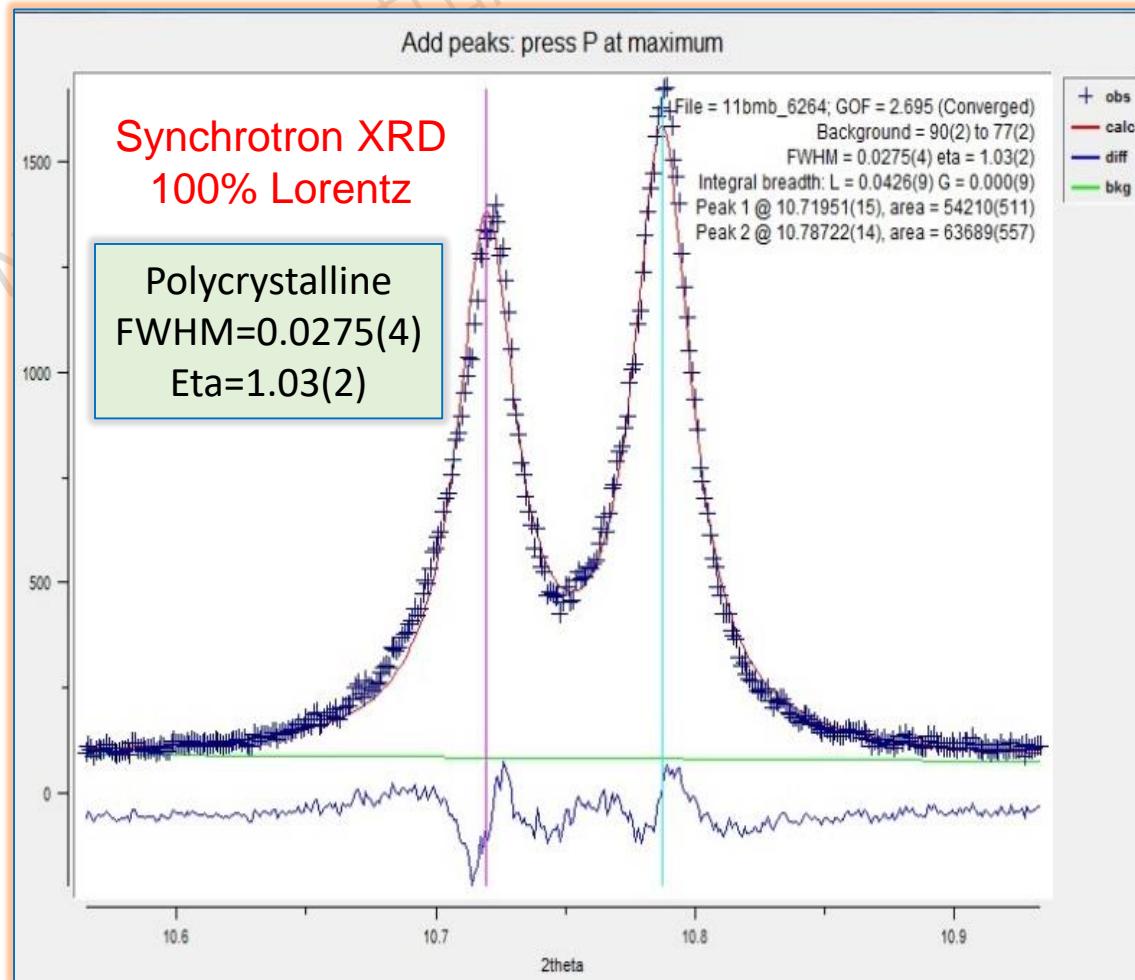
理想的X射线衍射的峰型可用洛伦兹函数描述

$$G(2\theta - 2\theta_{hkl}) = \left(\frac{2\sqrt{\ln(2)/\pi}}{\text{FWHM}} \right) \exp \left(\frac{-4 \ln(2)(2\theta - 2\theta_{hkl})^2}{\text{FWHM}^2} \right)$$

反应堆单色波中子衍射的峰型函数则是高斯函数

X射线和中子衍射峰的峰型剖面

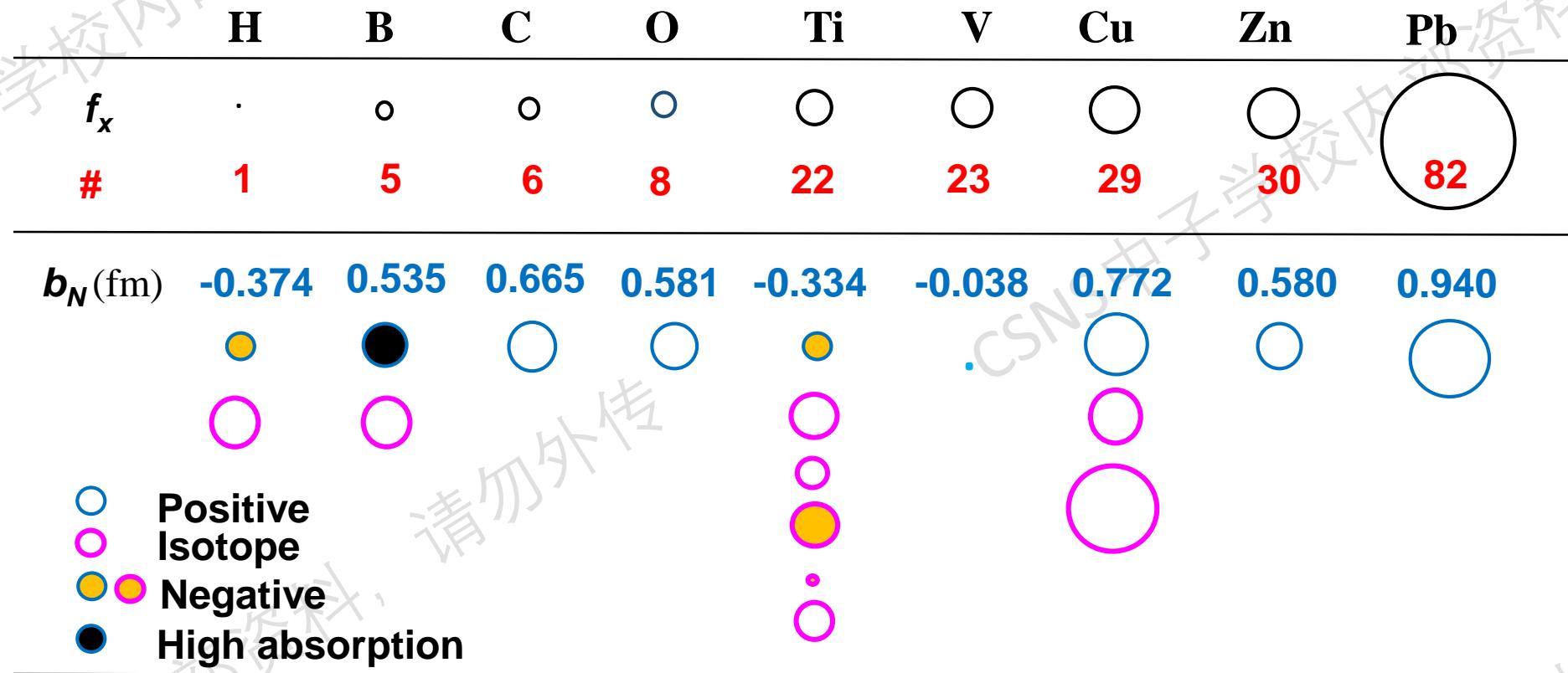
Diffraction Peak Profile of XRPD and NPD



对于一般合成的粉末样品，由于晶粒大小不均匀因而引起衍射峰的展宽，特别是高分辨衍射仪尤其明显。

部分X射线散射和中子散线截面

Some scattering cross section of x-ray and neutron



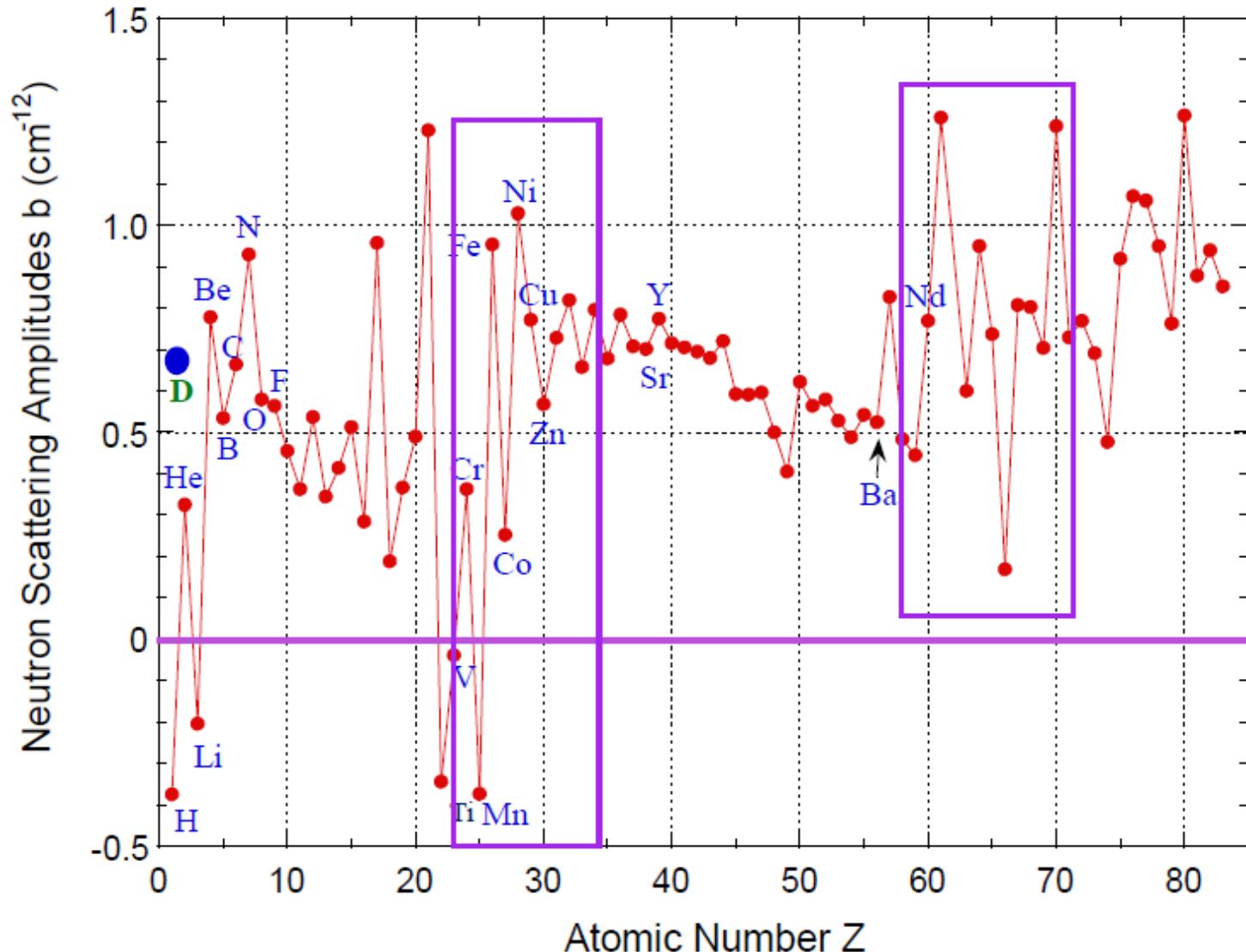
部分X射线散射和中子散线截面（以图中的圆圈的面积表示）

1. X射线衍射的强度随着元素内部的电子数目的增加而增强，即X射线散射的截面随着原子序数增大而增加，因此对原子序数低的元素不敏感。
2. 中子散射截面不随原子序数的规律变化，对原子序数小的元素也可能有较大的散射截面。而且对非相干散射大和吸收大的元素可以用相应的同位素替代。

Representations of the scattering of X-rays and neutrons by selected elements. The scattering cross sections are proportional to the areas of the circles shown. For the neutron case, separate entries appear for the different isotopes and negative scattering lengths are indicated by shading.

部分元素的中子散射因子

Representations of the neutron scattering amplitudes of selected elements



Atom	Atomic #	$b(\text{cm}^{-12})$
Ti	22	-0.3438
V	23	-0.0382
Cr	24	0.3635
Mn	25	-0.373
Fe	26	0.954
Co	27	0.253
Ni	28	1.03
Cu	29	0.7718

与X射线散射因子不同，中子散射因子与原子序数无关，是常数，即不随衍射角变化，有正值也有负值等特点。因此在运用粉末衍射方法测定晶体结构上弥补了X射线衍射方法上一些不足。对序数是小的元素较敏感，如 H, D, Li, Be, ¹¹B, C, N, O 等，通常用来测定这类元素的位置和占有率。对过渡金属，稀土等相邻元素具有较强的分辨能力，常用来探测其在共占位中的比例。

应该指出不宜用中子测量含有大量高吸收元素，如 B, Cd, Pm, Sm, Eu, 和 Gd，有些可用同位素替代，如在中子测量 MgB_2 就是用 ¹¹B 来替代 B。而对于 H 元素，由于非相干散射很强，用中子测量产生很高的背底，因此测量对大量含 H 的化合物，可以用同位素氘 (D) 替代。

由于元素的中子散射因子有负值，在与正值元素共占位，结果会相互抵消。

Higher background and absorption due to samples contain higher incoherent scattering elements

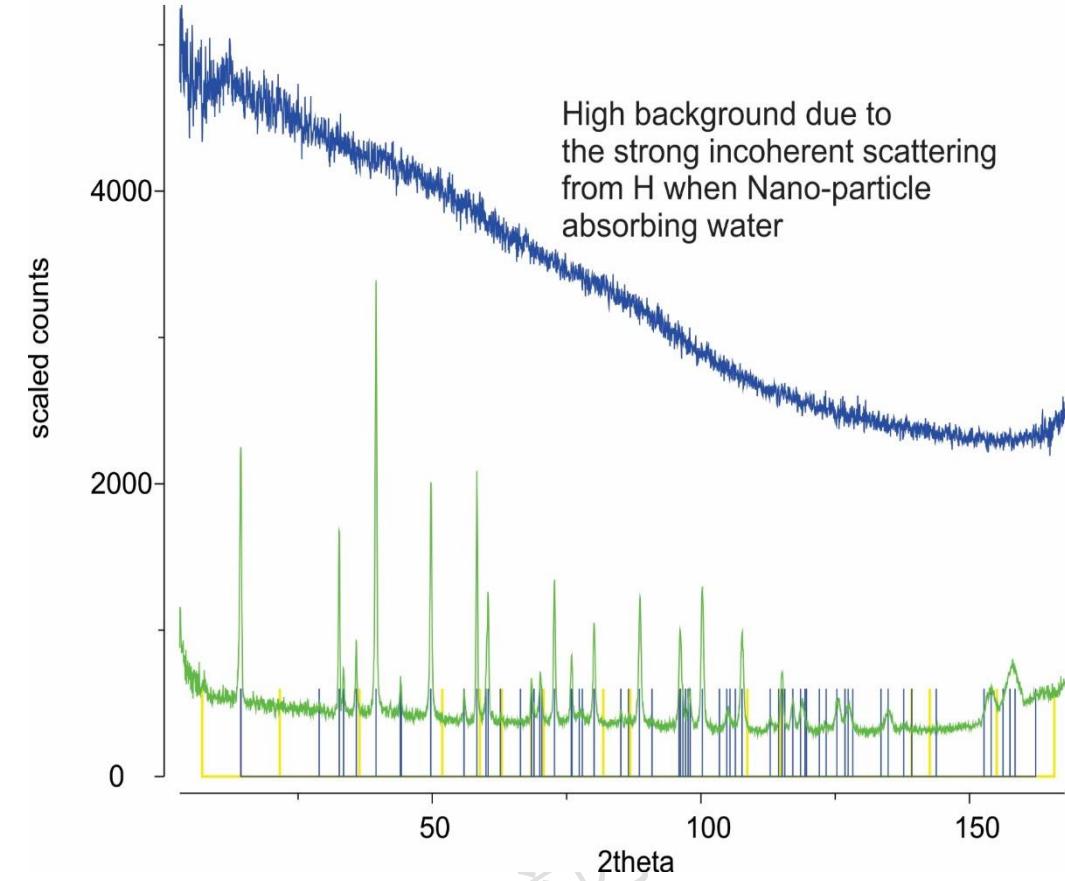
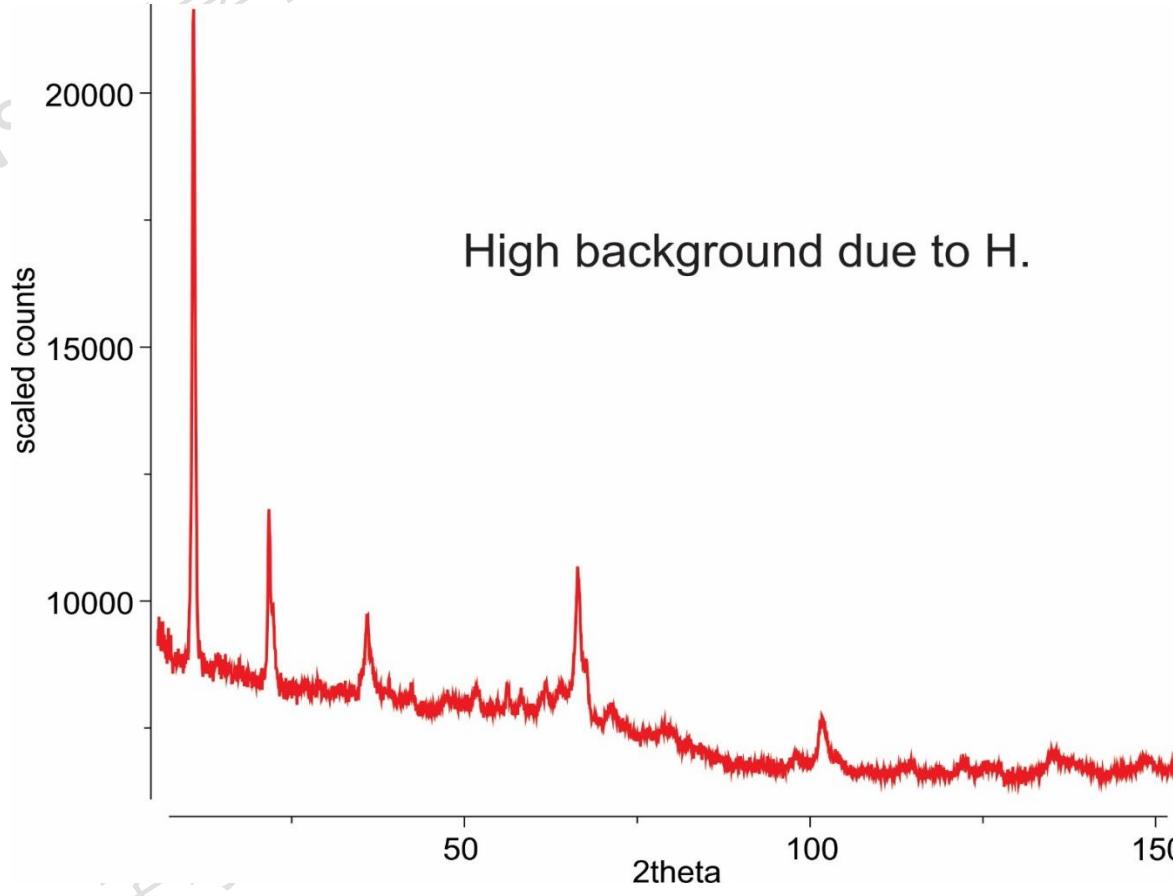


Table 4.4.4.1. Bound scattering lengths, b , in fm and cross sections, σ , in barns (1 barn = 100 fm 2) of the elements and their isotopes

Z: atomic number; A: mass number; $I(\pi)$: spin (parity) of the nuclear ground state; c: % natural abundance (for radioisotopes, the half-life is given instead in annums); b_c : bound coherent scattering length; b_i : bound incoherent scattering length; σ_c : bound coherent scattering cross section; σ_i : bound incoherent scattering cross section; σ_t : total bound scattering cross section; σ_a : absorption cross section for 2200 m s $^{-1}$ neutrons ($E = 25.30$ meV, $k = 3.494 \text{ \AA}^{-1}$, $\lambda = 1.798 \text{ \AA}$); $i = \sqrt{-1}$.

Element	Z	A	$I(\pi)$	c	b_c	b_i	σ_c	σ_i	σ_t	σ_a
H	1	1/2(+)		-3.7390(11)	1.7568(10)	80.26(6)	82.02(6)	0.3326(7)		
				99.985	-3.7406(11)	25.274(9)	1.7583(10)	80.27(6)	82.03(6)	0.3326(7)
				0.015	6.671(4)	4.04(3)	5.592(7)	2.05(3)	7.64(3)	0.000519(7)
He	2	1/2(+)		-1.04(17)	2.89(3)	0.14(4)	3.03(5)	0		
				(12.32a)	4.792(27)					
He	2	3	1/2(+)	0.00014	3.26(3)	1.34(2)	0.00	1.34(2)	0.00747(1)	
				5.74(7)	-2.5(6)	4.42(10)	1.6(4)	6.04(4)	5333.(7.)	
				-1.483(2)i	+2.568(3)i					
Li	3	0(+)		99.99986	3.26(3)	0	1.34(2)	0	1.34(2)	0
Li	3	6	1(+)	7.5	-1.90(2)	0.454(14)	0.92(3)	1.37(3)	70.5(3)	
				2.00(11)	-1.89(5)	0.51(5)	0.46(2)	0.97(7)	940.(4.)	
				-0.261(1)i	0.257(11)i					
Be	4	7	3/2(-)	92.5	-2.22(2)	-2.49(5)	0.619(11)	0.78(3)	1.40(3)	0.0454(3)
Be	4	9	3/2(-)	100	7.79(1)	0.12(3)	7.63(2)	0.0018(9)	7.63(2)	0.0076(8)
B	5	10		5.30(4)	0.213(2)i	3.54(5)	1.70(12)	5.24(11)	767.(8.)	
				20.0	-0.1(3)	-4.7(3)	0.144(8)	3.0(4)	3.1(4)	3835.(9.)
				1.066(3)i	1.231(3)i					
C	6	11	3/2(-)	80.0	6.65(4)	-1.3(2)	5.56(7)	0.22(6)	5.78(9)	0.0055(33)
C	6	12	0(+)	98.90	6.6460(12)	5.550(2)	0.001(4)	5.551(3)	0.00350(7)	
				6.6511(16)	0	5.559(3)	0	5.559(3)	0.00353(7)	
				1.10	6.19(9)	-0.52(9)	4.81(14)	0.034(12)	4.84(14)	0.00137(4)
N	7	14	1(+)	99.63	9.36(2)	11.01(5)	0.50(12)	11.51(11)	1.90(3)	
				9.37(2)	2.0(2)	11.03(5)	0.5(1)	11.53(11)	1.91(3)	
				0.37	6.44(3)	-0.02(2)	5.21(5)	0.00005(10)	5.21(5)	0.000024(8)
O	8	16	0(+)	99.762	5.803(4)	4.232(6)	0.000(8)	4.232(6)	0.00019(2)	
				0.038	5.803(4)	0	4.232(6)	0	4.232(6)	0.00010(2)
				5.78(12)	0.18(6)	4.20(22)	0.004(3)	4.20(22)	0.236(10)	
F	9	17	0(+)	0.200	5.84(7)	0	4.29(10)	0	4.29(10)	0.00016(1)
Ne	10	20	1/2(-)	90.51	4.566(6)	2.620(7)	0.008(9)	2.628(6)	0.039(4)	
				0.27	4.631(6)	0	2.695(7)	0	2.695(7)	0.036(4)
				6.66(19)	$\pm 0.6(1)$	5.6(3)	0.05(2)	5.7(3)	0.67(11)	
Na	11	21	0(+)	9.22	3.87(1)	0	1.88(1)	0	1.88(1)	0.046(6)
Na	11	23	3/2(+)	100	3.63(2)	3.59(3)	1.66(2)	1.62(3)	3.28(4)	0.530(5)
Mg	12	24	0(+)	78.99	5.375(4)	3.631(5)	0.08(6)	3.71(4)	0.063(3)	
				10.00	5.66(3)	0	4.03(4)	0	4.03(4)	0.050(5)
				11.01	3.62(14)	1.48(10)	1.65(13)	0.28(4)	1.93(14)	0.19(3)
Al	13	27	5/2(+)	100	3.449(5)	0.256(10)	1.495(4)	0.0082(7)	1.503(4)	0.231(3)
Si	14	28	0(+)	92.23	4.1491(10)	2.1633(10)	0.004(8)	2.167(8)	0.171(3)	
				4.107(6)	0	2.120(6)	0	2.120(6)	0.177(3)	
				4.70(10)	0.09(9)	2.78(12)	0.001(2)	2.78(12)	0.101(14)	
P	15	30	0(+)	3.10	4.58(8)	0	2.64(9)	0	2.64(9)	0.107(2)
S	16	32	0(+)	95.02	2.847(1)	3.307(13)	0.005(10)	3.312(16)	0.172(6)	
				2.804(2)	0	0.1086(7)	0.007(5)	1.026(5)	0.53(1)	
				0.75	4.74(19)	1.5(1.5)	2.8(2)	0.3(6)	3.1(6)	0.54(4)
S	33	34	0(+)	4.21	3.48(3)	0	1.52(3)	0	1.52(3)	0.227(5)
				0.02	3.(1.) E	0	1.1(8)	0	1.1(8)	0.15(3)

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_c	b_i	σ_c	σ_i	σ_t	σ_a
Cl	17	35	3/2(+)	75.77	9.5770(8)	6.1(4)	11.526(2)	5.3(5)	16.8(5)	33.5(3)
			3/2(+)	24.23	11.65(2)	0.1(1)	17.06(6)	4.7(6)	21.8(6)	44.1(4)
					3.08(6)	0	1.19(5)	0.001(3)	1.19(5)	0.433(6)
Ar	18	36	0(+)	0.337	1.909(6)	0	0.458(3)	0.22(2)	0.683(4)	0.675(9)
			0(+)	0.063	24.90(7)	3.5(3.5)	77.9(4)	0	77.9(4)	5.2(5)
			0(+)	99.600	3.1(1.) E	0	1.5(3.1)	0	1.5(3.1)	0.8(2)
K	19	39	3/2(+)	93.258	3.67(2)	1.4(3)	1.69(2)	0.27(11)	1.96(11)	2.1(1)
			4(-)	0.012	3.74(2)	1.1(8)	1.76(2)	0.25(11)	2.01(11)	2.1(1)
			3/2(+)	6.730	2.69(8)	1.5(1.5)	0.91(5)	0.3(6)	1.2(6)	1.46(3)
Ca	20	40	0(+)	96.941	4.70(2)	0	2.78(2)	0.05(3)	2.83(2)	0.43(2)
			0(+)	0.647	4.80(2)	0	2.90(2)	0	2.90(2)	0.41(2)
			7/2(-)	0.135	3.36(10)	0	1.42(8)	0	1.42(8)	0.68(7)
Sc	21	45	7/2(-)	100	12.29(11)	-6.0(3)	19.0(3)	4.5(5)	23.5(6)	27.5(2)
			5/2(-)	8.2	4.725(5)	0	1.427(11)	2.63(3)	4.06(3)	6.43(6)
			5/2(-)	7.4	3.53(7)	-3.5(2)	1.57(6)	1.5(2)	3.1(2)	1.7(2)
Ti	22	46	0(+)	4.725(5)	0	2.80(6)	0	2.80(6)	0	0.59(18)
			0(+)	73.8	-5.86(2)	0	4.32(3)	0	4.32(3)	8.30(9)
			7/2(-)	5.4	0.98(5)	5.1(2)	0.12(1)	3.3(3)	3.4(3)	2.2(3)
V	23	50	6(+)	0.250	-0.3824(12)	0	0.01838(12)	5.08(6)	5.10(6)	5.08(2)
			7/2(-)	99.750	-0.402(2)	6.435(4)	0.0203(2)	5.07(6)	7.8(1.0)	60.40(4)
Cr	24	50	0(+)	4.35	3.635(7)	0	1.660(6)	1.83(2)	3.49(2)	3.05(8)
			0(+)	83.79	4.920(10)	0	2.54(6)	0	2.54(6)	15.8(2)
			3/2(-)	9.50	-4.20(3)	6.87(10)	0	3.042(12)	0	0.76(6)
Mn	25	55	1/2(-)	2.36	4.55(10)	0	2.60(11)	0	2.60(11)	0.36(4)
			5/2(-)	100	-3.750(18)	1.79(4)	1.77(2)	0.40(2)	2.17(3)	13.3(2)
Fe	26	54	0(+)	5.8	9.45(2)	0	11.22(5)	0.40(11)	11.62(10)	2.56(3)
			0(+)	91.7	4.2(1)	0	2.2(1)	0	2.2(1)	2.25(18)
			1/2(-)	2.2	9.94(3)	0	12.42(7)	0</		

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_c	b_l	σ_c	σ_l	σ_s	σ_a
Ga	31	69	3/2(–)	60.1	7.288(2)	–0.85(5)	6.675(4)	0.16(3)	6.83(3)	2.75(3)
		71	3/2(–)	39.9	7.88(2)	–0.82(4)	7.80(4)	0.091(11)	7.89(4)	2.18(5)
					6.40(3)		5.15(5)	0.084(8)	5.23(5)	3.61(10)
Ge	32				8.185(20)		8.42(4)	0.18(7)	8.60(6)	2.20(4)
		70	0(+)	20.5	10.0(1)	0	12.6(3)	0	12.6(3)	3.0(2)
		72	0(+)	27.4	8.51(10)	0	9.1(2)	0	9.1(2)	0.8(2)
		73	9/2(+)	7.8	5.02(4)	3.4(3)	3.17(5)	1.5(3)	4.7(3)	15.1(4)
		74	0(+)	36.5	7.58(10)	0	7.2(2)	0	7.2(2)	0.4(2)
		76	0(+)	7.8	8.21(1.5)	0	8.(3.)	0	8.(3.)	0.16(2)
As	33	75	3/2(–)	100	6.58(1)	–0.69(5)	5.44(2)	0.060(10)	5.50(2)	4.5(1)
Se	34				7.970(9)		7.98(2)	0.33(6)	8.30(6)	11.7(2)
		74	0(+)	0.9	0.8(3.0)	0	0.16(1)	0	0.16(1)	51.8(1.2)
		76	0(+)	9.0	12.2(1)	0	18.7(3)	0	18.7(3)	85.(7.)
		77	1/2(–)	7.6	8.25(8)	±0.6(1.6)	8.6(2)	0.05(26)	8.65(16)	42.(4.)
		78	0(+)	23.5	8.24(9)	0	8.5(2)	0	8.5(2)	0.43(2)
		80	0(+)	49.6	7.48(3)	0	7.03(6)	0	7.03(6)	0.61(5)
Br	35	82	0(+)	9.4	6.34(8)	0	5.05(13)	0	5.05(13)	0.044(3)
					6.795(15)		5.80(3)	0.10(9)	5.90(9)	6.9(2)
		79	3/2(–)	50.69	6.80(7)	–1.1(2)	5.81(12)	0.15(6)	5.96(13)	11.0(7)
Kr	36	81	3/2(–)	49.31	6.79(7)	0.6(1)	5.79(12)	0.05(2)	5.84(12)	2.7(2)
					7.81(2)		7.67(4)	0.01(14)	7.68(13)	25.(1.)
		78	0(+)	0.35		0	0	6.4(9)		
		80	0(+)	2.25		0	0	11.8(5)		
		82	0(+)	11.6		0	0	29.(20.)		
		83	9/2(+)	11.5		185.(30.)				
Rb	37	84	0(+)	57.0		0	0	0.113(15)		
		86	0(+)	17.3	8.1(2)	0	8.2(4)	0	8.2(4)	0.003(2)
					7.09(2)		6.32(4)	0.5(4)	6.8(4)	0.38(4)
Sr	38	85	5/2(–)	72.17	7.03(10)	6.2(2)	0.5(5)	E	6.7(5)	0.48(1)
		87	3/2(–)	27.83	7.23(12)	6.6(2)	0.5(5)	E	7.1(5)	0.12(3)
					7.02(2)		6.19(4)	0.06(11)	6.25(10)	1.28(6)
Y	39	84	0(+)	0.56	7.(1.) E	0	6.(2.)	0	6.(2.)	0.87(7)
		86	0(+)	9.86	5.67(5)	0	4.04(7)	0	4.04(7)	1.04(7)
		87	9/2(+)	7.00	7.40(7)	6.88(13)	0.5(5)	E	7.4(5)	16.3(3.)
Zr	40	88	0(+)	82.58	7.15(6)	0	6.42(11)	0	6.42(11)	0.058(4)
					7.16(3)		6.44(5)	0.02(15)	6.46(14)	0.185(3)
		90	0(+)	51.45	6.4(1)	0	5.1(2)	0	5.1(2)	0.011(5)
		91	5/2(+)	11.32	8.7(1)	–1.08(15)	9.5(2)	0.15(4)	9.7(2)	1.17(10)
		92	0(+)	17.19	7.4(2)	0	6.9(4)	0	6.9(4)	0.22(6)
		94	0(+)	17.28	8.2(2)	0	8.4(4)	0	8.4(4)	0.0499(24)
Nb	41	96	0(+)	2.76	5.5(1)	0	3.8(1)	0	3.8(1)	0.0229(10)
					7.054(3)	–0.139(10)	6.253(5)	0.0024(3)	6.255(5)	1.15(5)
					6.715(2)		5.67(3)	0.04(5)	5.71(4)	2.48(4)
Mo	42	92	0(+)	14.84	6.91(8)	0	6.00(14)	0	6.00(14)	0.019(2)
		94	0(+)	9.25	6.80(7)	0	5.81(12)	0	5.81(12)	0.015(2)
		95	5/2(+)	15.92	6.91(6)	6.00(10)	0.5(5)	E	6.5(5)	13.1(3.)
		96	0(+)	16.68	6.20(6)	0	4.83(9)	0	4.83(9)	0.5(2)
		97	5/2(+)	9.55	7.24(8)	6.59(15)	0.5(5)	E	7.1(5)	2.5(2)
		98	0(+)	24.13	6.58(7)	0	5.44(12)	0	5.44(12)	0.127(6)
Tc	43	100	0(+)	9.63	6.73(7)	0	5.69(12)	0	5.69(12)	0.4(2)
					(2.13 × 10 ⁵ a)	6.8(3)	5.8(5)	0.5(5)	E	6.3(7)
										20.(1.)

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_c	b_l	σ_c	σ_l	σ_s	σ_a
Ru	44	96	0(+)	5.5	7.03(3)	0	6.21(5)	0.4(1)	6.6(1)	2.56(13)
		98	0(+)	1.9	0	0	0.28(2)	<8.0		
		99	5/2(+)	12.7	6.9(1.0)					
		100	0(+)	12.6	0	0	4.8(6)			
		101	5/2(+)	17.0	3.3(9)					
		102	0(+)	31.6	0	0	1.17(7)			
Rh	45	104	0(+)	18.7	0	0	0.31(2)			
		103	1/2(–)	100	5.88(4)	4.34(6)	0.3(3)	E	4.6(3)	144.8(7)
Pd	46	102	0(+)	1.02	5.91(6)		4.39(9)	0.093(9)	4.48(9)	6.9(4)
		104	0(+)	11.14	7.7(7) E	0	7.5(1.4)	0	7.5(1.4)	3.4(3)
		105	5/2(+)	22.33	5.5(3)	–2.6(1.6)	3.8(4)	0.8(1.0)	4.6(1.1)	20.(3.)
		106	0(+)	27.33	6.4(4)	0	5.1(6)	0	5.1(6)	0.304(29)
		108	0(+)	26.46	4.1(3)	0	2.1(3)	0	2.1(3)	8.5(5)
		110	0(+)	11.72	7.7(7)E	0	7.5(1.4)	0	7.5(1.4)	0.226(31)
Ag	47	107	1/2(–)	51.839	5.922(7)		4.407(10)	0.58(3)	4.99(3)	63.3(4)
		109	1/2(–)	48.161	7.555(11)	1.00(13)	7.17(2)	0.13(3)	7.30(4)	37.6(1.2)
					4.165(11)	–1.60(13)	2.18(1)	0.32(5)	2.50(5)	91.0(1.0)
Cd	48				4.87(5)		3.04(6)	3.46(13)	6.50(12)	2520.(50.)
		106	0(+)	1.25	5.(2.) E	0	3.1(2.5)	0	3.1(2.5)	1.
		108	0(+)	0.89	5.4(1)	0	3.7(1)	0	3.7(1)	1.1(3)
		110	0(+)	12.51	5.9(1)	0	4.4(1)	0	4.4(1)	11.(1.)
		111	1/2(+)	12.81	6.5(1)	5.3(2)	0.3(3)	E	5.6(4)	24.(3.)
		*113	1/2(+)	12.22	–8.0(2)	12.1(4)	0.3(3) E	12.4(5)		20600(400.)
In	49				4.065(20)	2.08(2)	0.54(11)	2.62(11)	193.8(1.5)	
		113	9/2(+)	43	5.39(6)	±0.017(1)	3.65(8)	0.000037(5)	3.65(8)	12.0(1.1)
		115	9/2(+)	957	4.01(2)	–2.1(2)	2.02(2)	0.55(11)	2.57(11)	202(2.)
Sn	50	112	0(+)	1.0	6.225(2)		4.870(3)	0.022(5)	4.892(6)	0.626(9)
		114	0(+)	0.7	6.2(3)	0	4.8(5)	0	4.8(5)	0.114(30)
		115	1/2(+)	0.4	6.1(1.) E	4.5(1.5)	0.3(3) E	4.8(1.5)	30(7.)	
		116	0(+)	14.7	5.93(5)	0	4.42(7)	0	4.42(7)	0.14(3)
		117	1/2(+)	7.7	6.48(5)	5.28(8)	0.3(3) E	5.6(3)	2.3(5)	
		118	0(+)	24.3	6.07(5)	0	4.63(8)	0	4.63(8)	0.22(5)
Sb	51	119	1/2(+)	8.6	6.12(5)	4.71(8)	0.3(3) E	5.0(3)	2.2(5)	
		120	0(+)	32.4	6.49(5)	0	5.29(8)	0	5.29(8)	0.14(3)
		122	0(+)	4.6	5.74(5)	0	4.14(7)	0	4.14(7)	0.18(2)
Te	52	124	0(+)	5.6	5.97(5)	0	4.48(8)	0	4.48(8)	0.133(5)
		121	7/2(+)	57.3	5.71(6)	–0.05(15)	4.10(9)	0.0003(19)	4.10(9)	5.75(12)
		123	5/2(+)	42.7	5.38(7)	–0.10(15)	3.64(9)	0.0014(4)	3.64(9)	3.8(2)
Te	52				5.80(3)		4.23(4)	0.09(1)	4.32(4)	4.05(5)
		120	0(+)	0.096	5.3(5)	0	3.5(7)	0	3.4(7)	2.3(3)
		122	0(+)	2.60	3.8(2)	0	1.8(2)	0	1.8(2)	3.4(5)
		123	1/2(+)	0.908	–0.05(25)	–2.04(9)	0.002(3)	0.52(5)	0.52(5)	418(30.)
		124	0(+)	4.816	7.96(10)	0	8.0(2)	0	8.0(2)	6.8(1.3)
		125	1/2(+)	7.14	5.02(8)	–0.26(13)	3.17(10)	0.008(8)	3.18(10)	1.55(16)
Tc	43	126	0(+)	18.95	5.56(7)	0	3.88(10)	0	3.88(10)	1.04(15)
		128	0(+)	31.69	5.89(7)	0				

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_c	b_i	σ_c	σ_i	σ_s	σ_a
I	53	127	5/2(+)	100	5.28(2)	1.58(15)	3.50(3)	0.31(6)	3.81(7)	6.15(6)
Xe	54				4.92(3)		3.04(4)		23.9(1.2)	
		124	0(+)	0.10		0		0	165.(20.)	
		126	0(+)	0.09		0		0	3.5(8)	
		128	0(+)	1.91		0		0	< 8.	
		129	1/2(+)	26.4					21.(5.)	
		130	0(+)	4.1		0		0	< 26.	
		131	3/2(+)	21.2					85.(10.)	
		132	0(+)	26.9		0		0	0.45(6)	
		134	0(+)	10.4		0		0	0.265(20)	
		136	0(+)	8.9		0		0	0.26(2)	
Cs	55	133	7/2(+)	100	5.42(2)	1.29(15)	3.69(3)	0.21(5)	3.90(6)	29.0(1.5)
Ba	56				5.07(3)		3.23(4)	0.15(11)	3.38(10)	1.1(1)
		130	0(+)	0.11	-3.6(6)	0	1.6(5)	0	1.6(5)	30.(5.)
		132	0(+)	0.10	7.8(3)	0	7.6(6)	0	7.6(6)	7.0(8)
		134	0(+)	2.42	5.7(1)	0	4.08(14)	0	4.08(14)	2.0(1.6)
		135	3/2(+)	6.59	4.67(10)		2.74(12)	0.5(5) E	3.2(5)	5.8(9)
		136	0(+)	7.85	4.91(8)	0	3.03(10)	0	3.03(10)	0.68(17)
		137	3/2(+)	11.23	6.83(10)		5.86(17)	0.5(5) E	6.4(5)	3.6(2)
		138	0(+)	71.70	4.84(8)	0	2.94(10)	0	2.94(10)	0.27(14)
La	57				8.24(4)		8.53(8)	1.13(19)	9.66(17)	8.97(5)
		138	5(+)	0.09	8.(2.) E	8.(4.)	0.5(5) E	8.5(4.0)	57.(6.)	
		139	7/2(+)	99.91	8.24(4)	3.0(2)	8.53(8)	1.13(15)	9.66(17)	8.93(4)
Ce	58				4.84(2)		2.94(2)	0.00(10)	2.94(10)	0.63(4)
		136	0(+)	0.19	5.80(9)	0	4.23(13)	0	4.23(13)	7.3(1.5)
		138	0(+)	0.25	6.70(9)	0	5.64(15)	0	5.64(15)	1.1(3)
		140	0(+)	88.48	4.84(9)	0	2.94(11)	0	2.94(11)	0.57(4)
		142	0(+)	11.08	4.75(9)	0	2.84(11)	0	2.84(11)	0.95(5)
Pr	59	141	5/2(+)	100	4.58(5)	-0.35(3)	2.64(6)	0.015(3)	2.66(6)	11.5(3)
Nd	60				7.69(5)		7.43(10)	9.2(8)	16.6(8)	50.5(1.2)
		142	0(+)	27.16	7.7(3)	0	7.5(6)	0	7.5(6)	18.7(7)
		143	7/2(-)	12.18	14.2(5) E	$\pm 21.1(6)$	25.(7.)	55.(7.)	80.(2.)	334.(10.)
		144	0(+)	23.80	2.8(3)	0	1.0(2)	0	1.0(2)	3.6(3)
		145	7/2(-)	8.29	14.2(5)	E	25.(7.)	5.(5.) E	30.(9.)	42.(2.)
		146	0(+)	17.19	8.7(2)	0	9.5(4)	0	9.5(4)	1.4(1)
		148	0(+)	5.75	5.7(3)	0	4.1(4)	0	4.1(4)	2.5(2)
		150	0(+)	5.63	5.3(2)	0	3.5(3)	0	3.5(3)	1.2(2)
Pm	61				(2.62a)	12.6(4)	$\pm 3.2(2.5)$	20.0(1.3)	1.3(2.0)	21.3(1.5)
Sm	62					0.80(2)		0.422(9)	39.(3.)	39.(3.)
						-1.65(2)i			5922.(56.)	
		144	0(+)	3.1	-3.(4.) E	0	1.(3.)	0	1.(3.)	0.7(3)
		147	7/2(-)	15.1	14(3.)	$\pm 11.(7.)$	25.(11.)	14.(19.)	39(16.)	57(3.)
		148	0(+)	11.3	-3.(4.) E	0	1.(3.)	0	1.(3.)	2.4(6)
		*149	7/2(-)	13.9	-19.2(1)	$\pm 31.4(6)$	63.5(6)	137.(5.)	200.(5.)	42080.(400.)
					-11.7(1)i	-10.3(1)i				
		150	0(+)	7.4	14(3.)	0	25(11.)	0	25(11.)	104(4.)
		152	0(+)	26.6	-5.0(6)	0	3.1(8)	0	3.1(8)	206(6.)
		154	0(+)	22.6	9.3(1.0)	0	11.(2.)	0	11.(2.)	8.4(5)
Eu	63					7.22(2)		6.75(4)	2.5(4)	9.2(4)
		*151	5/2(+)	47.8	-1.26(1)i					4530.(40.)
					6.13(14)	$\pm 4.5(4)$	5.5(2)	3.1(4)	8.4(4)	9100.(100.)
		153	5/2(+)	52.2	-2.53(3)i	$\pm 2.14(2)i$	8.5(2)	1.3(7)	9.8(7)	312.(7.)

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_c	b_i	σ_c	σ_i	σ_s	σ_a
Gd	64				6.5(5)		29.3(8)	151.(2.)	180.(2.)	49700.(125.)
		152	0(+)	0.2	-13.82(3)i		13.(8.)	0	13.(8.)	735.(20.)
		154	0(+)	2.1	10.(3.) E	0	13.(8.)	0	13.(8.)	85.(12.)
		*155	3/2(-)	14.8	6.0(1)	$\pm 5.(5.) E$	40.8(4.)	25.(6.)	66.(6.)	61100.(400.)
		156	0(+)	20.6	6.3(4)	0	5.0(6)	0	5.0(6)	1.5(1.2)
		*157	3/2(-)	15.7	-17.0(1)i	-13.16(9)i	650(4.)	394.(7.)	1044.(8.)	259000.(700.)
		158	0(+)	24.8	9.(2.)	0	10.(5.)	0	10.(5.)	2.2(2)
		160	0(+)	21.8	9.15(5)	0	10.52(11)	0	10.52(11)	0.77(2)
Tb	65	159	3/2(+)	100	7.38(3)	-0.17(7)	6.84(6)	0.004(3)	6.84(6)	23.4(4)
Dy	66				16.9(2)		35.9(8)	54.4(1.2)	90.3(9)	994.(13.)
					-0.276(4)i					
		156	0(+)	0.06	6.1(5)	0	4.7(8)	0	4.7(8)	33.(3.)
		158	0(+)	0.10	6.(4.) E	0	5.(6.)	0	5.(6.)	43.(6.)
		160	0(+)	2.34	6.7(4)	0	5.6(7)	0	5.6(7)	56.(5.)
		161	5/2(+)	19.0	10.3(4)	$\pm 4.9(8)$	13.3(1.0)	3.(1.)	16.(1.)	600.(25.)
		162	0(+)	25.5	-1.4(5)	0	0.25(18)	0	0.25(18)	194.(10.)
		163	5/2(-)	24.9	5.0(4)	1.3(3)	3.1(5)	0.21(10)	3.3(5)	124.(7.)
		164	0(+)	28.1	49.4(5)	0	307.(3.)	0	307.(3.)	2840.(40.)
					-0.79(1)i					
Ho	67	165	7/2(-)	100	8.01(8)	-1.70(8)	8.06(16)	0.36(3)	8.42(16)	64.7(1.2)
Er	68					7.79(2)		7.63(4)	1.1(3)	8.7(3)
		162	0(+)	0.14	8.8(2)	0	9.7(4)	0	9.7(4)	159.(4.)
		164	0(+)	1.56	8.2(2)	0	8.4(4)	0	8.4(4)	13.(2.)
		166	0(+)	33.4	10.6(2)	0	14.1(5)	0	14.1(5)	19.6(1.5)
		167	7/2(+)	22.9	3.0(3)	1.0(3)	1.1(2)	0.13(8)	1.2(2)	659.(16.)
		168	0(+)	27.1	7.4(4)	0	6.8(7)	0	6.8(7)	2.74(8)
		170	0(+)	14.9	9.6(5)	0	11.6(1.2)	0	11.6(1.2)	5.8(3)
Tm	69	169	1/2(+)	100	7.07(3)	0.9(3)	6.28(5)	0.10(7)	6.38(9)	100.(2.)
Yb	70				12.43(3)		19.42(9)	4.0(2)	23.05(18)	34.8(8)
		168	0(+)	0.14	-4.07(2)	0	2.13(2)	0	2.13(2)	2230.(40.)
		170	0(+)	3.06	6.77(10)	0	5.8(2)	0	5.8(2)	11.4(1.0)
		171	1/2(-)	143	9.66(10)	-5.59(17)	11.7(2)	3.9(2)	15.6(3)	48.6(2.5)
		172	0(+)	21.9	9.43(10)	0	11.2(2)	0	11.2(2)	0.8(4)
		173	5/2(-)	16.1	9.56(7)	-5.3(2)	11.5(2)	3.5(3)	15.0(4)	17.1(1.3)
		174	0(+)	31.8	19.3(1)	0	46.8(5)	0	46.8(5)	69.4(5.0)
		176	0(+)	12.7	8.72(10)	0	9.6(2)	0	9.6(2)	2.85(5)
Lu	71				7.21(3)		6.53(5)	0.7(4)	7.2(4)	74.(2.)
		*175	7/2(+)	97.39	7.24(3)	$\pm 2.2(7)$	6.59(5)	0.6(4)	7.2(4)	21.(3.)
		*176	7(-)	2.61	6.1(1)	$\pm 3.0(4)$	4.7(2)	1.2(3)	5.9(4)	2065.(35.)
					-0.57(1)i	+0.61(1)i				
Hf	72				7.77(14)		7.6(3)	2.6(5)	10.2(4)	104.1(0.5)
		174	0(+)	0.2	10.9(1.1)	0	15.(3.)	0	15.(3.)	561.(35.)
		176	0(+)	5.2	6.61(18)	0	5.5(3)	0	5.5(3)	23.5(3.1)
		177	7/2(-)	18.6	0.8(1.0) E	$\pm 0.9(1.3)$	0.1(2)	0.1(3)	0.2(2)	373.(10.)
		178	0(+)	27.1	5.9(2)	0	4.4(3)	0	4.4(3)	84.(4.)
		179	9/2(+)	13.7	7.46(16)	$\pm 1.06(8)$	7.0(3)	0.14(2)	7.1(3)	41.(3.)
		180	0(+)	35.2	13.2(3)	0	21.9(1.0)	0	21.9(1.0)	13.04(7)
Ta	73				6.91(7)		6.00(12)	0.01(17)	6.01(12)	20.6(5)
		*180	9(-)	0.012	7.(2.) E	6.2(3.5)	0.5(5)	7.(4.)	563.(60.)	
		181	7/2(+)	99.988	6.91(7)	-0.29(3)	6.00(12)	0.011(2)	6.01(12)	20.5(5)

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_e	b_i	σ_e	σ_i	σ_s	σ_a
W	74	180	0(+)	0.1	4.86(2) 5.(3.) E	0	2.97(2) 3.(4.)	1.63(6) 0	4.60(6) 3.(4.)	18.3(2) 30.(20.)
		182	0(+)	26.3	6.97(14)	0	6.10(7)	0	6.10(7)	20.7(5)
		183	1/2(-)	14.3	6.53(4)		5.36(7)	0.3(3) E	5.7(3)	10.1(3)
		184	0(+)	30.7	7.48(6)	0	7.03(11)	0	7.03(11)	1.7(1)
		186	0(+)	28.6	-0.72(4)	0	0.065(7)	0	0.065(7)	37.9(0.6)
		185	5/2(+)	37.40	9.2(2) 9.0(3)	$\pm 2.0(1.8)$	10.6(5) 10.2(7)	0.9(6) 0.5(9)	11.5(3) 10.7(6)	89.7(1.0) 112.(2.)
Re	75	187	5/2(+)	62.60	9.3(3)	$\pm 2.8(1.1)$	10.9(7)	1.0(8)	11.9(4)	76.4(1.0)
		184	0(+)	0.02	10.7(2) 10.(2.) E	0	14.4(5) 13.(5.)	0.3(8)	14.7(6)	16.0(4)
		186	0(+)	1.58	11.6(1.7)	0	17.(5.)	0	17.(5.)	80.(13.)
		187	1/2(-)	1.6	10.(2.) E	13.(5.)	0.3(3)	E	13.(5.)	320(10.)
		188	0(+)	13.3	7.6(3)	0	7.3(6)	0	7.3(6)	4.7(5)
		189	3/2(-)	16.1	10.7(3)		14.4(8)	0.5(5) E	14.9(9)	25(4.)
Os	76	190	0(+)	26.4	11.0(3)	0	15.2(9)	0	15.2(8)	13.1(3)
		192	0(+)	41.0	11.5(4)	0	16.6(1.2)	0	16.6(1.2)	2.0(1)
		191	3/2(+)	37.3	10.6(3)		14.1(8)	0.(3.)	14.(3.)	425.3(2.4)
		193	3/2(+)	62.7						954.(10.)
		190	0(+)	0.01	9.60(1) 9.0(1.0)	0	11.58(2) 10.(2.)	0.13(11) 0	11.7(11) 10.(2.)	10.3(3) 152.(4.)
		192	0(+)	0.79	9.9(5)	0	12.3(1.2)	0	12.3(1.2)	10.0(2.5)
Pt	78	194	0(+)	32.9	10.55(8)	0	14.0(2)	0	14.0(2)	1.44(19)
		195	1/2(-)	33.8	8.83(9)	-1.00(17)	9.8(2)	0.13(4)	9.9(2)	27.5(1.2)
		196	0(+)	25.3	9.89(8)	0	12.3(2)	0	12.3(2)	0.72(4)
		198	0(+)	7.2	7.8(1)	0	7.7(2)	0	7.6(2)	3.66(19)
		197	3/2(+)	100	7.63(6)	-1.84(10)	7.32(12)	0.43(5)	7.75(13)	98.65(9)
		196	0(+)	0.2	12.692(15) 30.3(1.0)	0	20.24(5) 115(8.)	6.6(1) 0	26.8(1) 115(8.)	372.3(4.0) 3080(180.)
Au	79	198	0(+)	10.1	0	0	0	0	2.0(3)	
		199	1/2(-)	17.0	16.9(4)	$\pm 15.5(8)$	36.(2.)	30.(3.)	66.(2.)	2150.(48.)
		200	0(+)	23.1	0		0	0	< 60.	
		201	3/2(-)	13.2	0	7.8(2.0)	0	0	4.89(5)	
		202	0(+)	29.6	0		0	0	0.43(10)	
		204	0(+)	6.8	0		0	0		
Hg	80	203	1/2(+)	29.524	8.776(5) 6.99(16)	1.06(14)	9.678(11) 6.14(28)	0.21(15) 0.14(4)	9.89(15) 6.28(28)	3.43(6) 11.4(2)
		205	1/2(+)	70.476	9.52(7)	-0.242(17)	11.39(17)	0.007(1)	11.40(17)	0.104(17)
		204	0(+)	1.4	9.405(3) 9.90(10)	0	11.115(7)	0.0030(7)	11.118(7)	0.171(2)
		206	0(+)	24.1	9.22(5)	0	12.3(2)	0	12.3(2)	0.65(7)
		207	1/2(-)	22.1	9.28(4)	0.14(6)	10.82(9)	0.002(2)	10.82(9)	0.699(10)
		208	0(+)	52.4	9.50(2)	0	11.34(5)	0	11.34(5)	0.00048(3)
Bi	83	209	9/2(-)	100	8.532(2)	0.259(15)	9.148(4)	0.0084(10)	9.156(4)	0.0338(7)
Po	84									
At	85									
Rn	86									
Fr	87									
Ra	88	226	0(+)	(1.60×10^3 a)	10.0(1.0)	0	13.(3.)	0	13.(3.)	12.8(1.5)

Table 4.4.4.1. Bound scattering lengths (cont.)

Element	Z	A	$I(\pi)$	c	b_e	b_i	σ_e	σ_i	σ_s	σ_a
Ac	89									
Th	90	232	0(+)	100	10.31(3)	0	13.36(8)	0	13.36(8)	7.37(6)
Pa	91	231	3/2(-)	(3.28×10^4 a)	9.1(3)	1	0.4(7)	0.1(3.3)	10.5(3.2)	200.6(2.3)
U	92	233	5/2(+)	(1.59×10^5 a)	10.1(2)	$\pm 1.(3.)$	8.417(5)	8.903(11)	0.005(16)	8.908(11)
	234	0(+)		0.005	12.4(3)	0	12.8(5)	0.1(6)	12.9(3)	574.7(1.0)
	235	7/2(-)		0.720	10.47(3)	$\pm 1.3(6)$	13.78(11)	0.2(2)	14.0(2)	680.9(1.1)
	238	0(+)		99.275	8.402(5)	0	8.871(11)	0	8.871(11)	2.68(2)
Np	93	237	5/2(+)	(2.14×10^6 a)	10.55(10)		14.0(3)	0.5(5) E	14.5(6)	175.9(2.9)
Pu	94	238	0(+)	(87.74 a)	14.1(5)	0	25.0(1.8)	0	25.0(1.8)	558.7(7.)
	239	1/2(+)		(2.41×10^4 a)	7.7(1)	$\pm 1.3(1.9)$	7.5(2)	0.2(6)	7.7(6)	1017.3(2.1)
	240	0(+)		(6.56×10^3 a)	3.5(1)	0	1.54(9)	0	1.54(9)	289.6(1.4)
	242	0(+)		(3.76×10^3 a)	8.1(1)	0	8.2(2)	0	8.2(2)	18.5(5)
Am	95	243	5/2(-)	(7.37×10^3 a)	8.3(2)	$\pm 2.(7.)$	8.7(4)	0.3(2.6)	9.0(2.6)	75.3(1.8)
Cm	96	244	0(+)	(18.10 a)	9.5(3)	0	11.3(7)	0	11.3(7)	16.2(1.2)
	246	0(+)		(4.7×10^3 a)	9.3(2)	0	10.9(5)	0	10.9(5)	1.36(17)
	248	0(+)		(3.5×10^3 a)	7.7(2)	0	7.5(4)	0	7.5(4)	3.00(26)

比较X射线衍射与中子衍射的应用

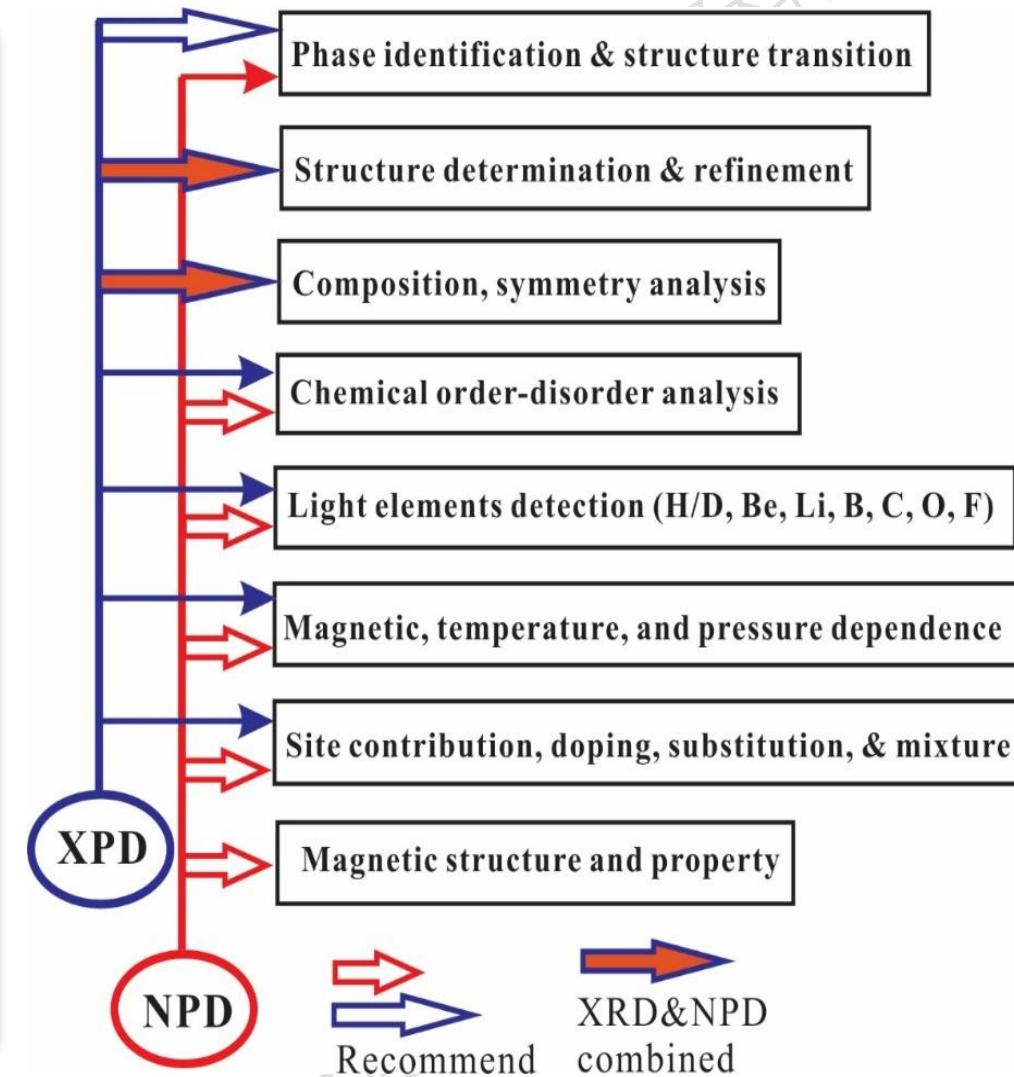
Comparison the Application of XRPD and NPD

中子相对优势 (Neutron Advantage)

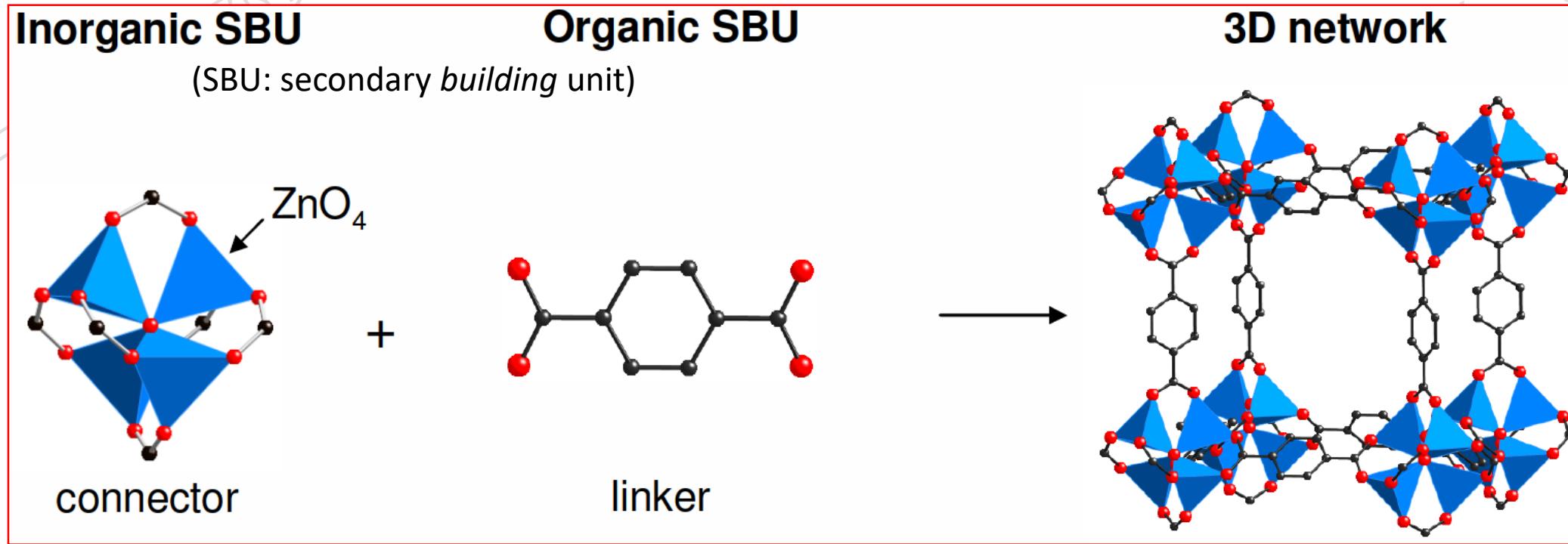
- 保持高角度峰强 (Comparable intensity at High-Q)
- 轻元素位置和占有率 (Position & occupancy for Light elements)
- 近邻过渡族金属元素分布与共占位 (Distinguishing neighbor transition & rear-earth elements)
- 占有率与温度因子的相关性小 (Smaller correlation between occupancy and temperature factor)
- 有序磁对称性, 磁结构及性能 (Ordered magnetic symmetry & structure and properties)
- 穿透力强 (Strong penetration)

中子相对劣势 (Neutron Disadvantage)

- 衍射强度低 (Lower intensity)
- 角分辨率低 (Lower Resolution)
- 要求样品量多 (Larger sample required)
- 中子源少 (High cost)



Metal-organic frameworks (MOFs)



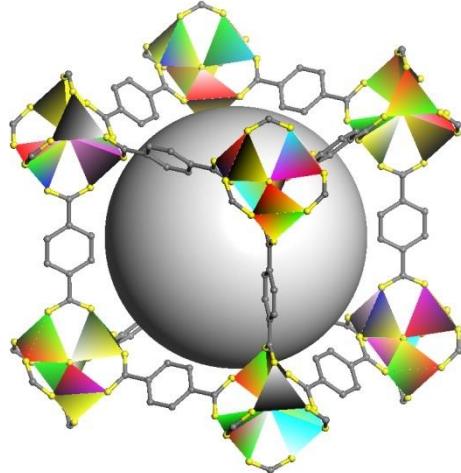
- ◆ Modular synthesis: hydrothermal or solvothermal methods
 - ◆ Well-defined structure: crystal with uniform pore geometry
 - ◆ Versatile chemistry: various metal clusters and organic linkers possible
 - Tunable pore size
 - Tunable functionality
 - ◆ Gas-adsorption related applications: gas storage, gas separation etc.

*Omar M. Yaghi et al., *Nature* 402, 276 (1999).

Some prototypical MOFs

MOF-5

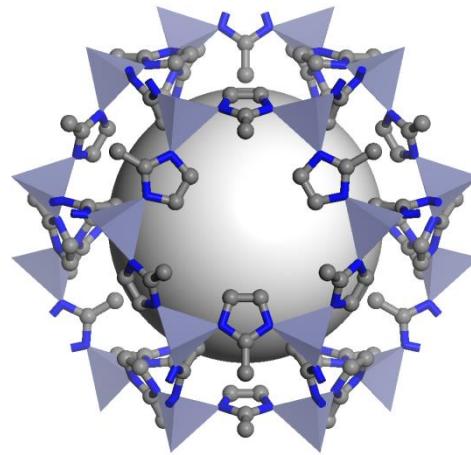
(Metal Organic Framework-5)



$\text{ZnO}_4+(\text{C}_6\text{H}_4)-(\text{CO}_2)_2$
(Yaghi's group)

ZIF-8

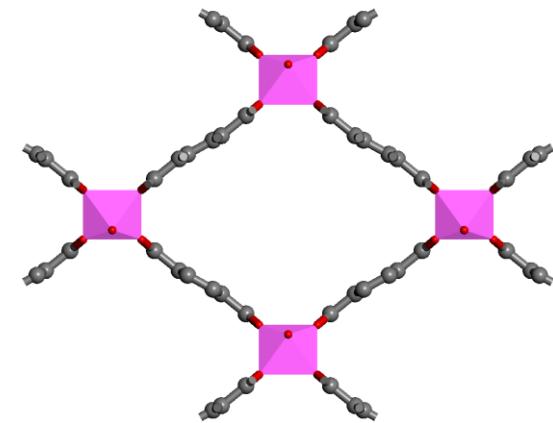
(Zeolitic Imidazolate Framework-8)



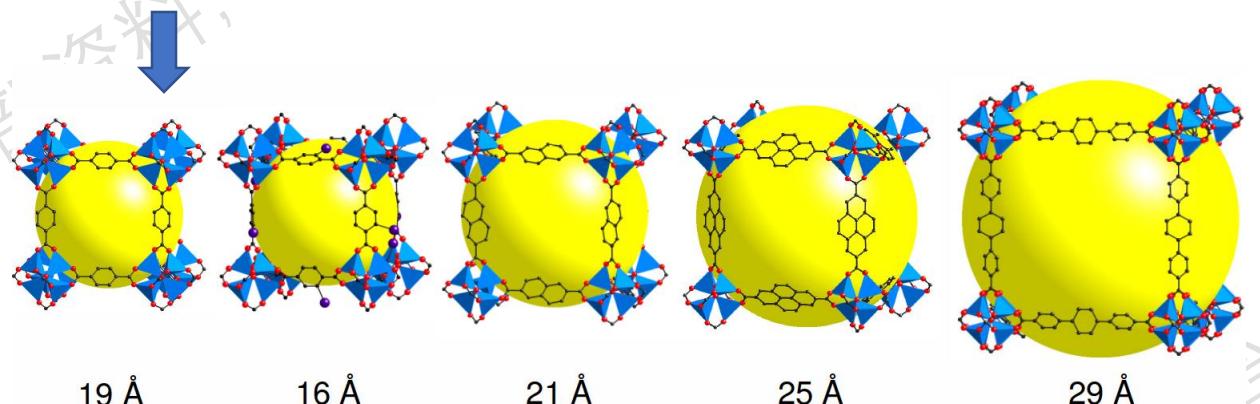
$\text{ZnN}_4+(\text{C}_3\text{N}_2\text{H}_2)-\text{CH}_3$
(Yaghi's group)

MIL-53

(Materials of Institut Lavoisier-53)



$\text{AlO}_6+(\text{C}_6\text{H}_4)-(\text{CO}_2)_2$
(Férey's group)

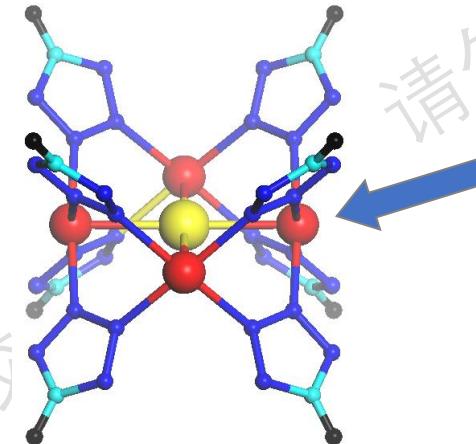
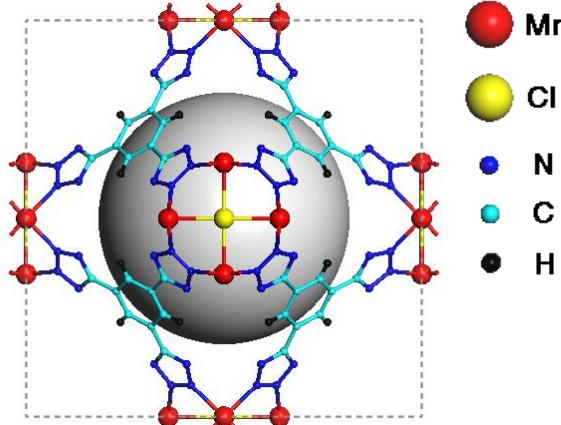


Large sphere:
the void/pore
in the structure

MOFs with open M coordination sites

Mn₄Cl-MOF

(Mn₄Cl)₃(btt)₈ / Mn₄ClC₂₄H₈N₃₂

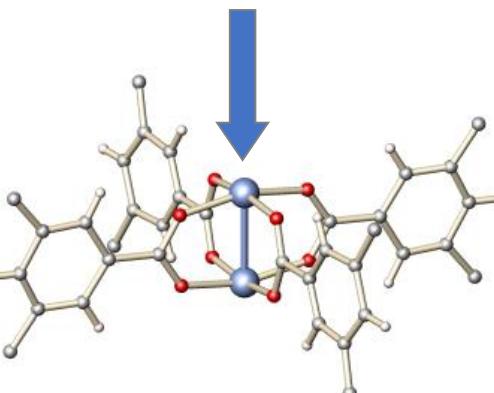
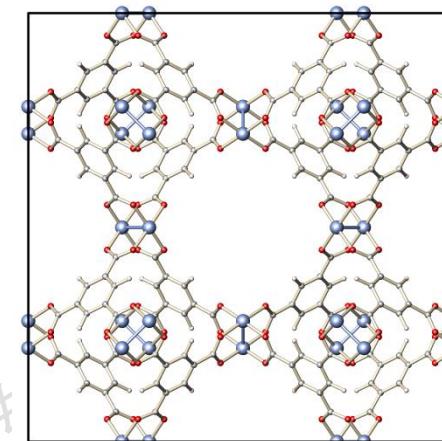


Mn: unsaturated

(Long's group)

HKUST-1

Cu₃(btc)₂ / Cu₃C₁₂H₄O₈

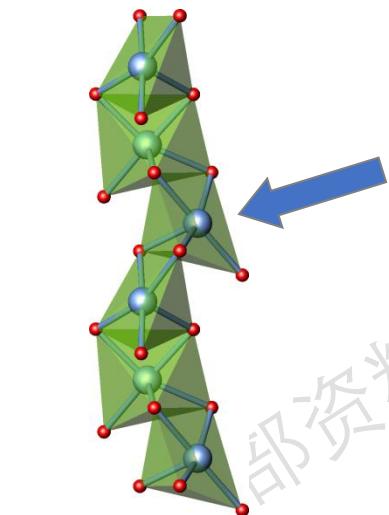
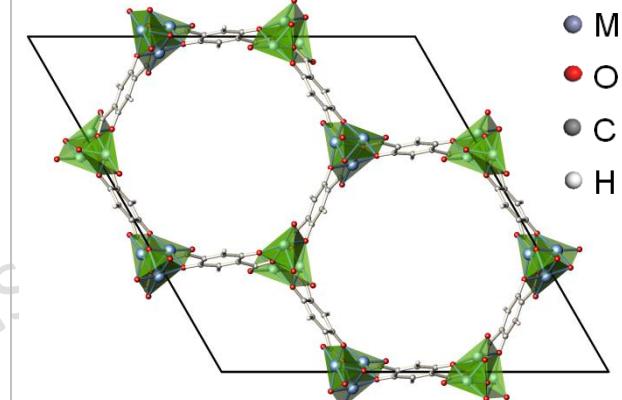


Cu: unsaturated

(Williams's group)

MOF-74

Zn₂(dhtp) / Zn₂C₈H₂O₆



Zn: unsaturated

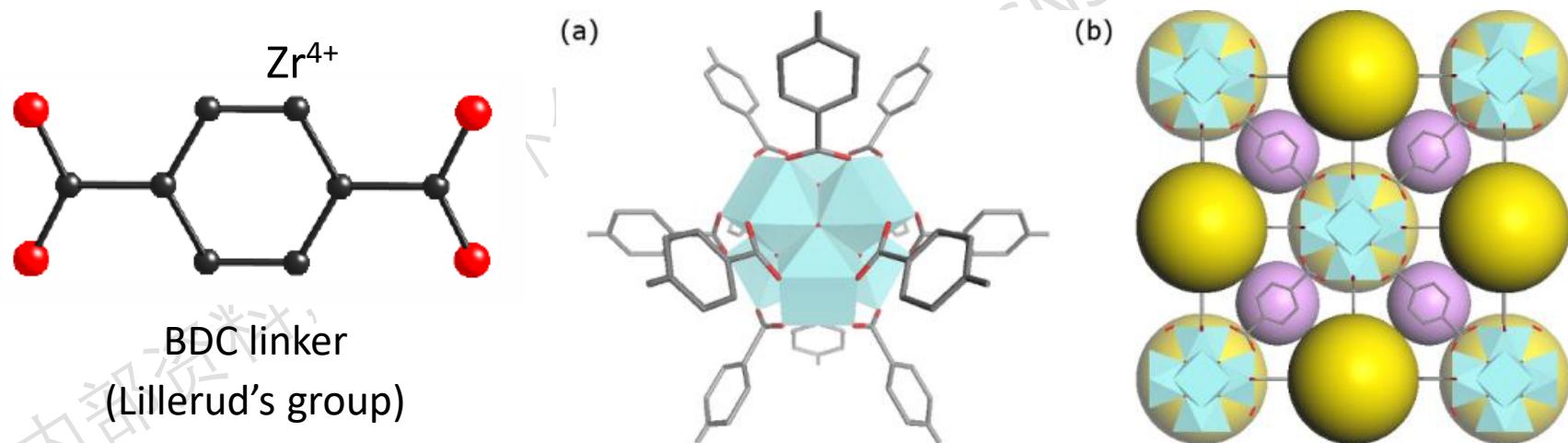
(Yaghi's group)

MOF结构中缺陷的研究

Study of Vacancy in MOF

一个典型的Zr基MOF，能连接多个有机单元，具有其它一般的MOF所不具备的不寻常的化学、热学性质以及框架结构的稳定性。实验得到的空隙容积比理论值大20%，暗示这种MOF结构中可能有大量的空位。但同步辐射X射线衍射并没有发现空位的存在。

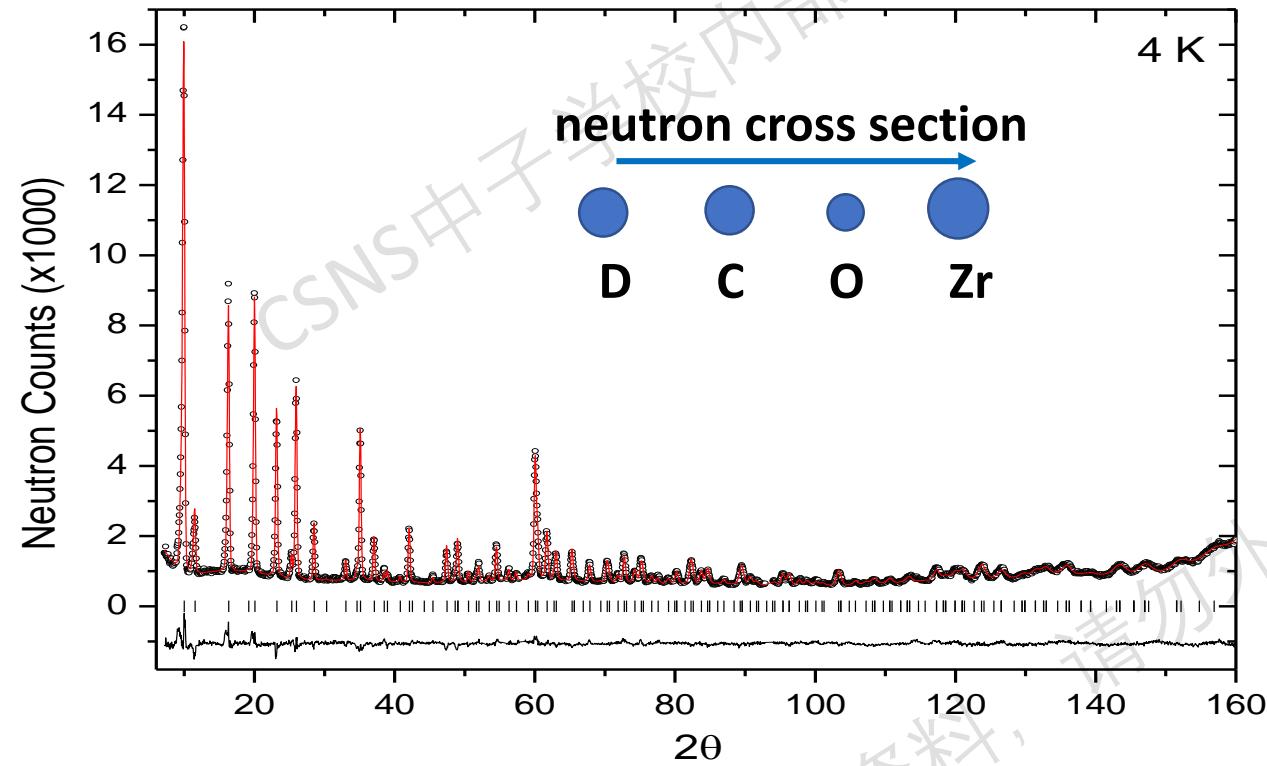
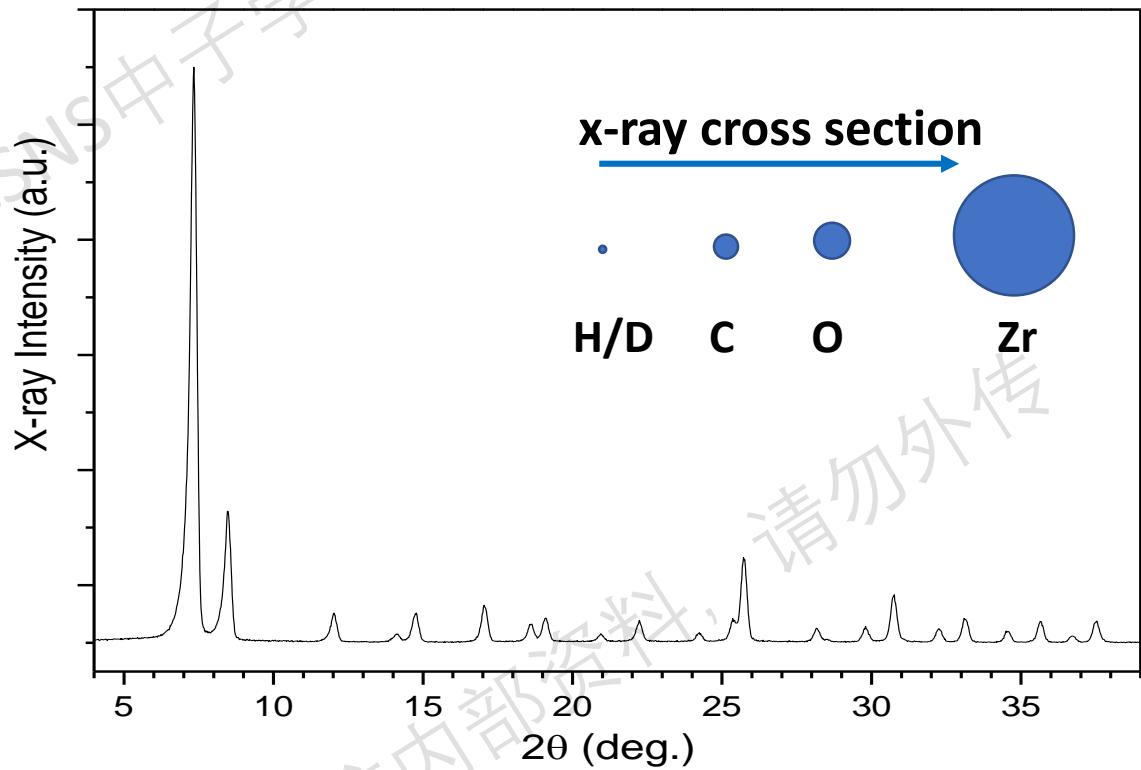
- ◆ Zr-UIO-66: an important prototypical Zr-based MOF; each metal center connected to 12 linkers. Because of its high framework connectivity, it exhibits exceptional chemical, thermal, and mechanical stabilities not commonly found in other MOFs.



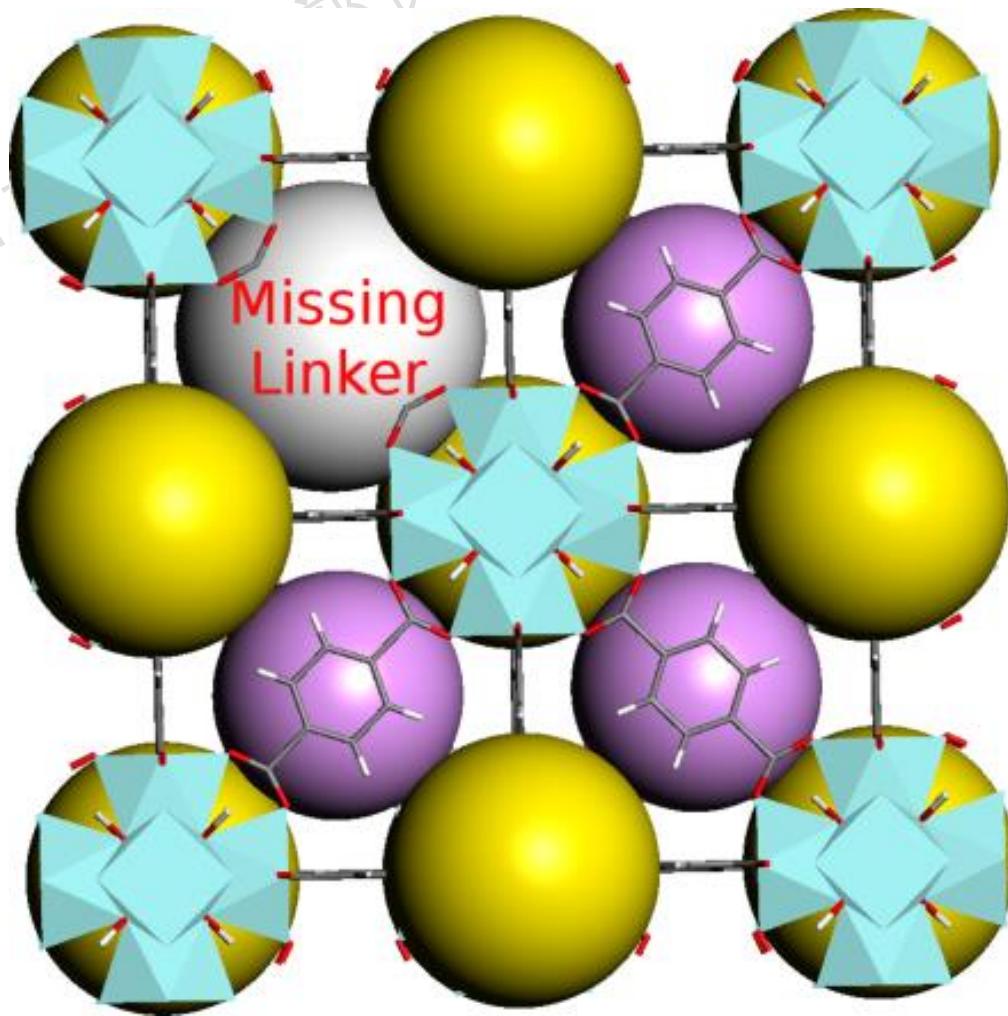
- ◆ A long-standing myth about this MOF: The experimental pore volume is ~20% higher than the theoretical value, suggesting that this MOF might contain significant amount of vacancy defects. However, synchrotron XRD data fit nicely with the ideal crystal structure.

X-射线比较中子粉末衍射

Neutron solved the myth in Zr-Uio-66



Neutron solved the myth in Zr-Uio-66

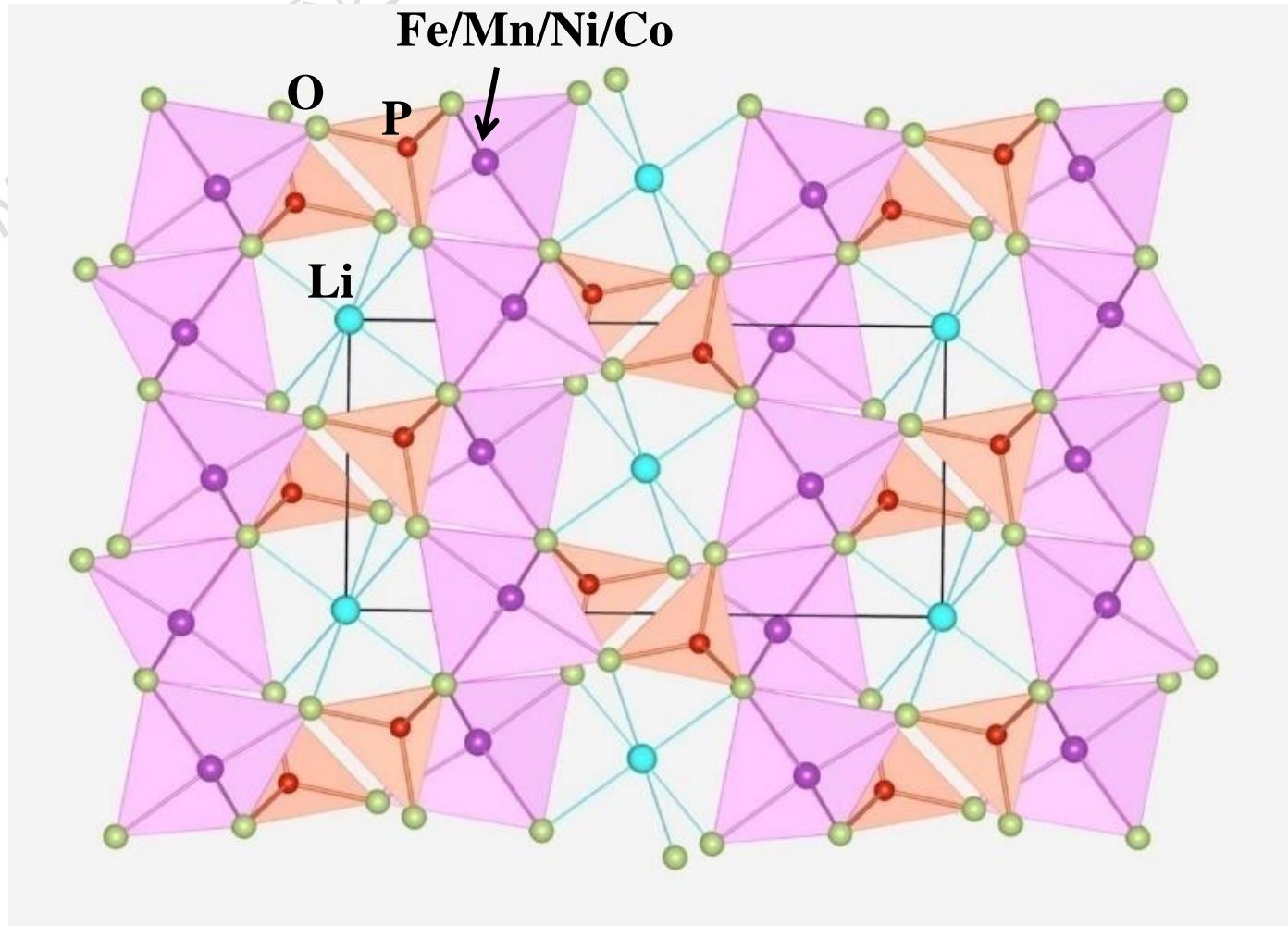


中子粉末衍射方法分析发现框架网络中只有连接有11个有机单元而不是理论的12个。而由于X射线衍射强度中重元素Zr占主导地位，因此没能发现丢了一个不敏感的较轻元素组成的有机单元。

Neutron diffraction shows that Zr-Uio-66 contains significant amount of **missing-linker defects**, which effectively reduce the framework connection from 12 to 11. (In contrast, x-ray diffraction is dominated by scattering from heavy element Zr, and thus is much less sensitive to linker vacancies.)

锂离子电极材料 $\text{Li}^+ \text{x} (\text{Fe/Ni})^{2+ \sim 3+} \text{P}^{5+} \text{O}_4^{2-}$ 结构分析及讨论

Discussion of Structure of electrode material $\text{Li}^+ \text{x} \text{Fe}^{2+ \sim 3+} \text{P}^{5+} \text{O}_4^{2-}$



价态变化

$$\text{Li}_{\frac{x}{4}}^{1+} \text{M}_{\frac{2}{4}}^{2+} \text{P}_{\frac{5}{4}}^{5+} \text{O}_{\frac{2}{4}}^{2-}$$

x=0-1: Li¹⁺_xM²⁺_{1-x}M³⁺_xP⁵⁺O²⁻₄

x~0: Li¹⁺_xM³⁺P⁵⁺O²⁻₄

Neutron scattering amplitude

$$b_{\text{Fe}}=0.954$$

$$b_{\text{Ni}}=1.03$$

$$b_{Lj} = -0.203$$

$$b_0 = 0.5805$$

$$b_p = 0.513$$

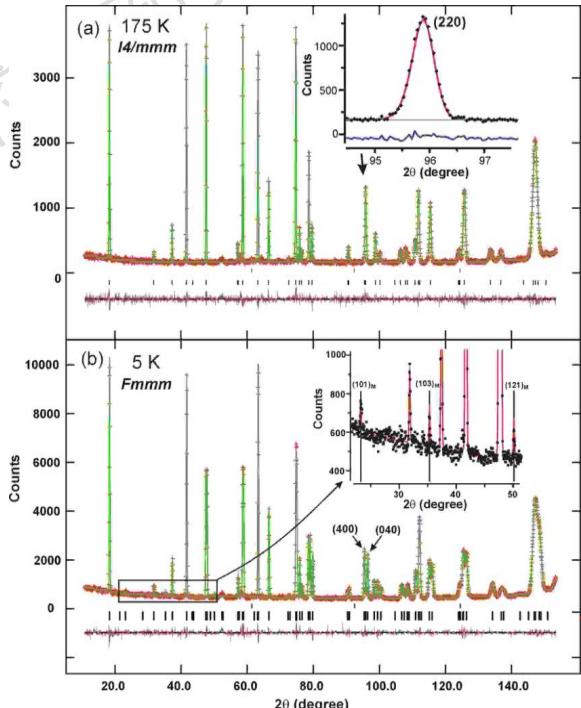
$$b_{\text{Mn}} = -0.373$$

$$b_{\text{C}_0} = 0.254$$

中子测定锂电池电极材料 $\text{Li}_x\text{Fe}^{2+/\sim 3+}\text{P}^{5+}\text{O}_4^{-4}$ 中离子通道中Li含量和混合占位引起的结构和性能变化，因为X射线对轻元素Li极不敏感，很难测出准确的Li的占位率以及不同Li离子占位率对结构的影响。在充放电过程中，由于Li离子占位率变化，Fe和Ni的价态发生变化而伴随的晶胞体积的变化可能对电池的运用受到影响。

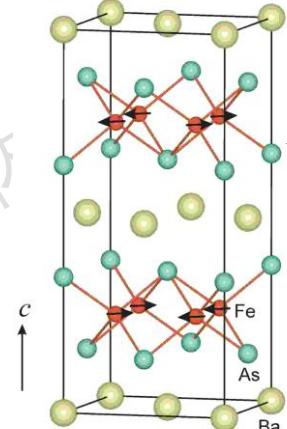
BaFe₂As₂晶体结构和磁结构,相转变与性能

Crystal & Magnetic Structure, Phase Transformation, and properties of BaFe₂As₂

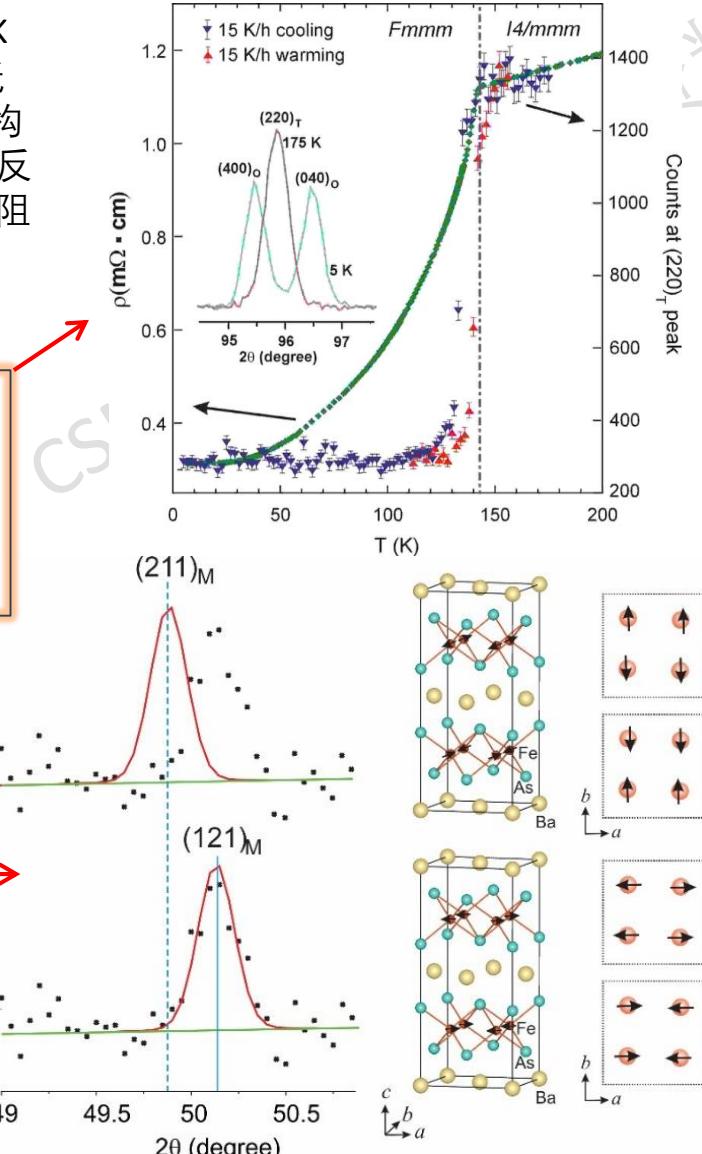


化合物BaFe₂As₂在~142 K经历由高温 $I4/mmm$ 到低温 $Fmmm$ 的一级晶体结构相变，伴随着从顺磁到反铁磁的磁有序转变和电阻急剧下降的突变。

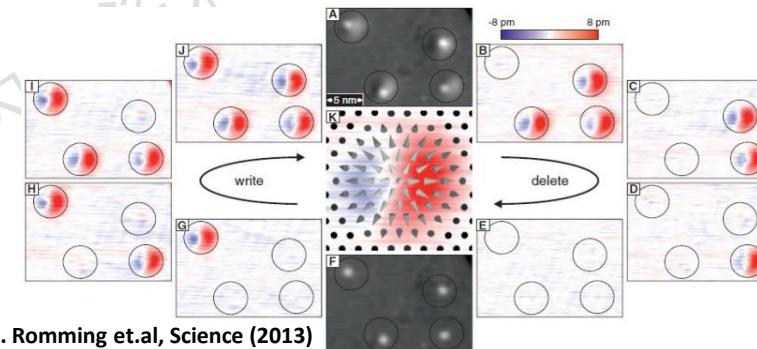
Relationships
between structure
and
properties
...



Determine and refine
crystal and magnetic
structures:
Chemical & symmetry
Atomic distribution
Magnetic order-disorder
Spin arrangement
...



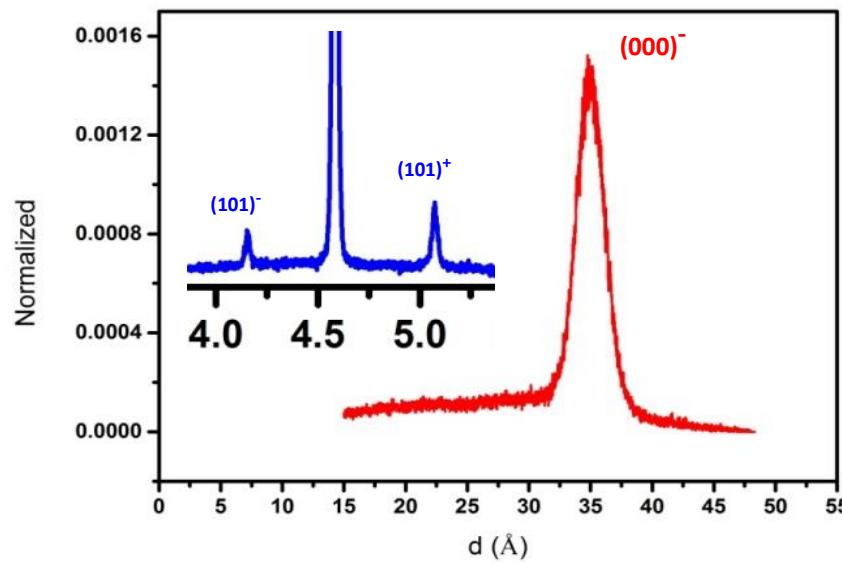
Magnetic Skyrmions



N. Romming et.al, Science (2013)

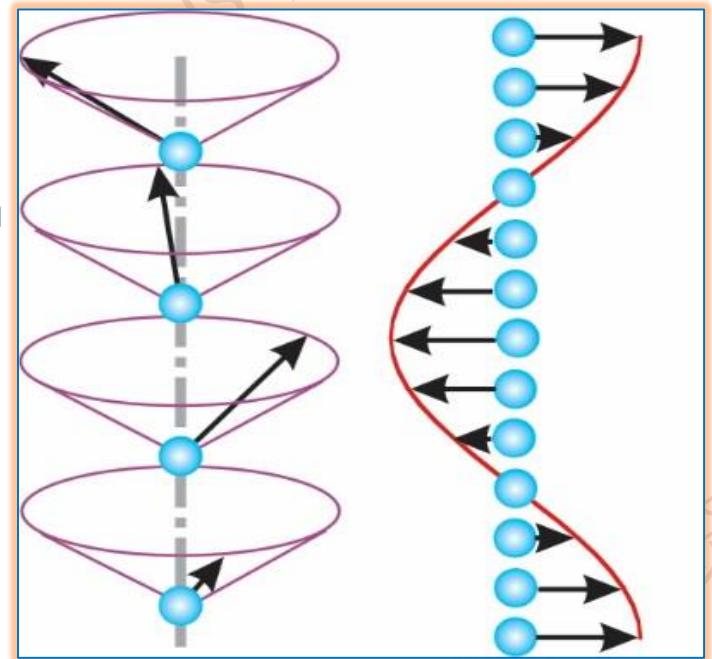
Skyrmions has a potential applications

C. Pfleiderer, Nature Physics (2011)



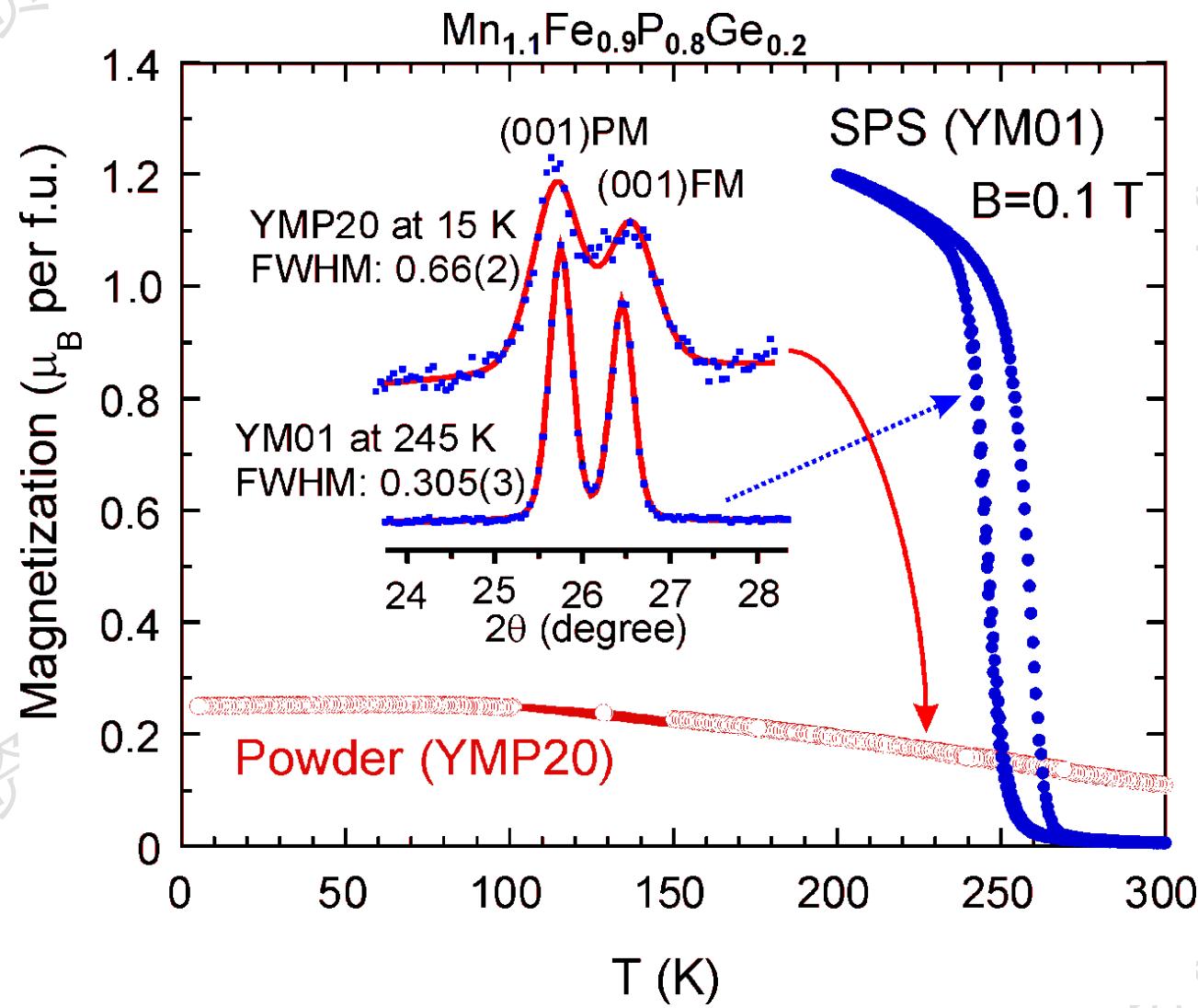
Satellite peaks of incommensurate magnetic ordering observed at GPPD

在中国散裂源GPPD探测到的无公度磁有序卫星峰



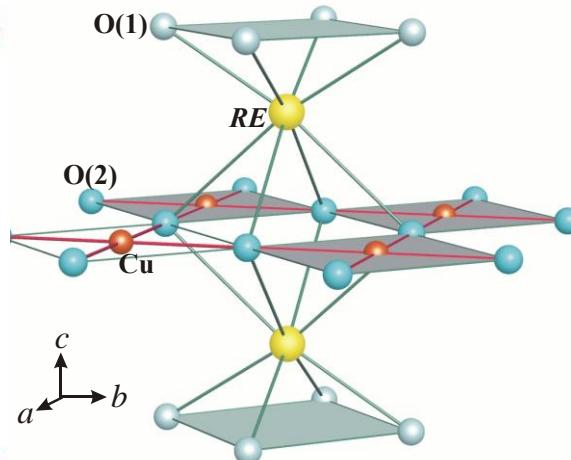
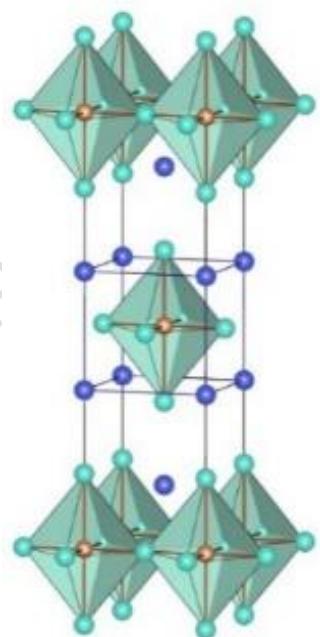
Incommensurate magnetic

晶粒尺度对铁磁有序度的影响



Small crystalline size inhibits the magnetic order

结构中得到 $\text{LaPr}_{0.88}\text{Ce}_{0.12}\text{CuO}_{4+\delta}$ 是 E-doping 超导体的证据



Hole doping



Electron doping



	<i>SC crystal</i>	<i>As-grown powder</i>	<i>SC powder</i>	<i>NSC powder</i>
<i>n</i> (La)	0.481(4)	0.489(4)	0.479(4)	0.480(4)
<i>n</i> (Cu)	1.001(6)	0.977(6)	1.001(6)	0.988(5)
<i>n</i> (O2)	0.974(5)	0.988(6)	0.972(5)	0.986(5)
Ratio(Cu:O)	1:3.94	1:4.07	1:3.94	1:4.02
<i>RE</i> -O(1)	2.3640(3)	2.3609(3)	2.3636(3)	2.3615(3)
RE-O(2)	2.6922(4)	2.6948(4)	2.6933(4)	2.6952(4)
O(1)-O(1)	2.81995(3)	2.81921(3)	2.82001(2)	2.81923(2)
O(2)-O(2)	3.07875(4)	3.07805(3)	3.07940(3)	3.07980(3)
<i>V</i> (<i>REO</i> ₈)	24.4826(6)	24.4642(5)	24.4888(5)	24.4781(5)
Cu-O(2)	1.99401(2)	1.99348(2)	1.99405(1)	1.99350(2)
<i>V</i>(Cu)* (e.u.)	1.661	1.729	1.658	1.706

根据实验测得的键长，用表中的数据计算离子的价态

$$V_i = \sum_j v_{ij}, v_{ij} = \exp[(R_{ij} - d_{ij})/b], e=2.71828, b=0.37, d_{ij} \text{ is bond distance}$$

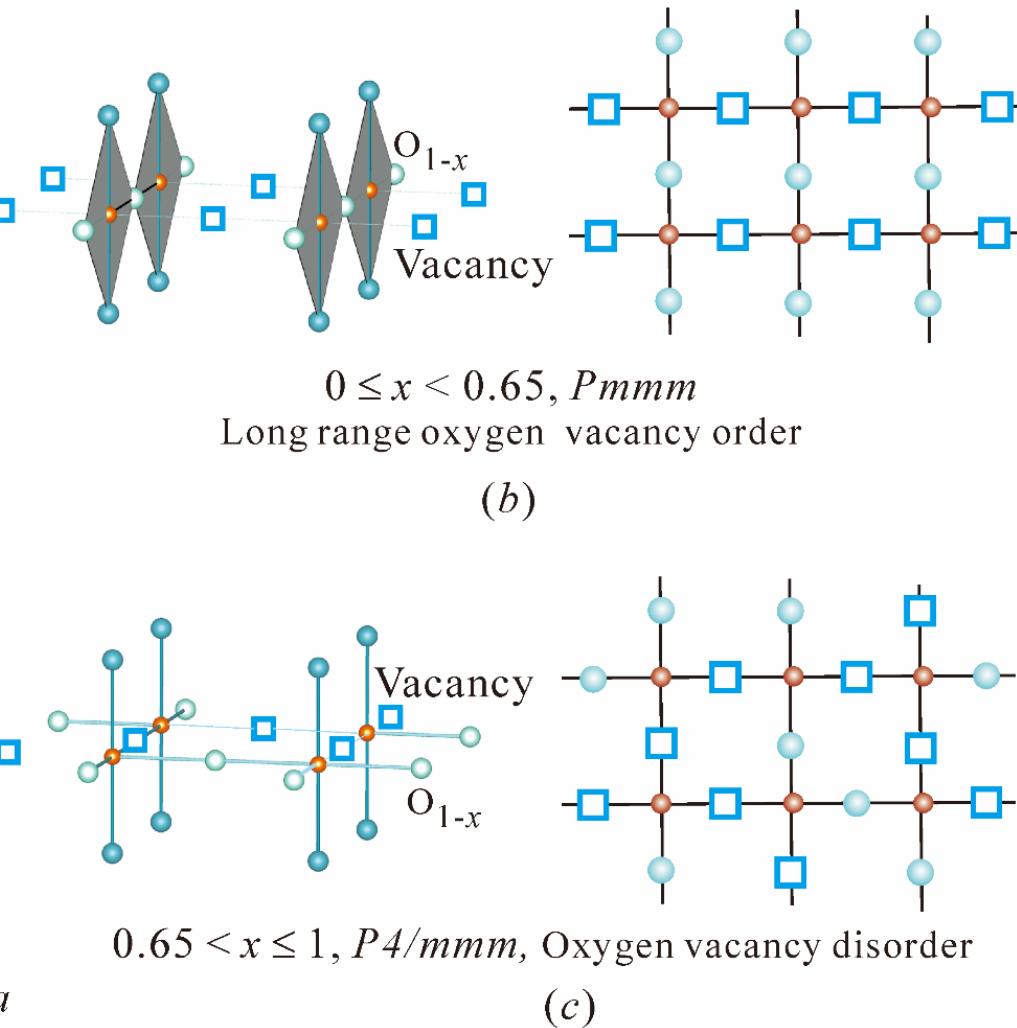
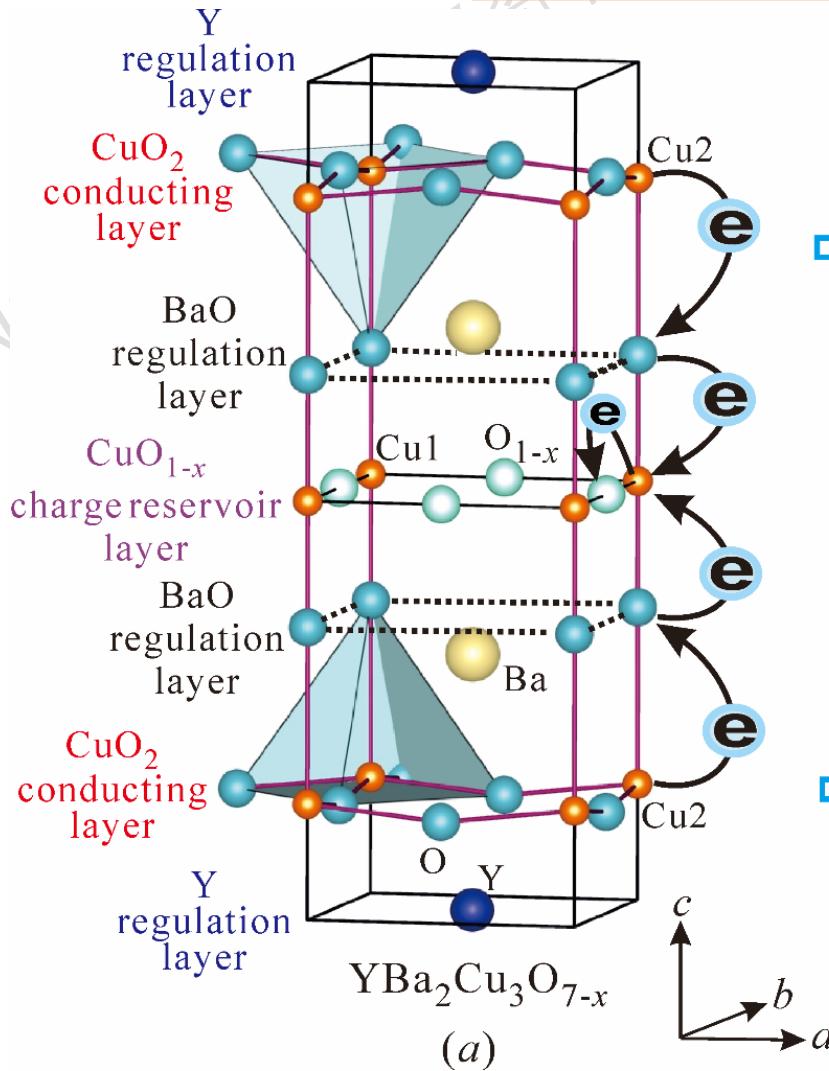
Recommended bond-valence parameters for oxides, fluorides and chlorides

Cation	O	F	Cl	Cation	O	F	Cl	Cation	O	F	Cl	Cation	O	F	Cl
Ac ^{III}	2.24	2.13	2.63	Mn ^{IV}	1.753	1.71	2.13	Dy ^{III}	2.036	1.922	2.41	Sm ^{III}	2.088	1.977	2.466
Ag ^I	1.805	1.80	2.09	Mn ^{VII}	1.79	1.72	2.17	Er ^{III}	2.010	1.906	2.39	Sn ^{II}	1.984	1.925	2.36
Al ^{III}	1.651	1.545	2.03	Mo ^{VI}	1.907	1.81	2.28	Eu ^{II}	2.147	2.04	2.53	Sn ^{IV}	1.905	1.84	2.28
Am ^{III}	2.11	2.00	2.48	N ^{III}	1.361	1.37	1.75	Eu ^{III}	2.076	1.961	2.455	Sr ^{II}	2.118	2.019	2.51
As ^{III}	1.789	1.70	2.16	N ^V	1.432	1.36	1.80	Fe ^{II}	1.734	1.65	2.06	Ta ^V	1.920	1.88	2.30
As ^V	1.767	1.62	2.14	Na ^I	1.80	1.677	2.15	Fe ^{III}	1.759	1.67	2.09	Tb ^{III}	2.049	1.936	2.427
Au ^{III}	1.833	1.81	2.17	Nb ^V	1.911	1.87	2.27	Ga ^{III}	1.730	1.62	2.07	Te ^{IV}	1.977	1.87	2.37
B ^{III}	1.371	1.31	1.74	Nd ^{III}	2.117	2.008	2.492	Gd ^{III}	2.065	1.95	2.445	Te ^{VI}	1.917	1.82	2.30
Ba ^{II}	2.29	2.19	2.69	Ni ^{II}	1.654	1.599	2.02	Ge ^{IV}	1.748	1.66	2.14	Th ^{IV}	2.167	2.07	2.55
Be ^{II}	1.381	1.28	1.76	Os ^{IV}	1.811	1.72	2.19	H ^I	0.95	0.92	1.28	Ti ^{III}	1.791	1.723	2.17
Bi ^{III}	2.09	1.99	2.48	P ^V	1.604	1.521	1.99	Hf ^{IV}	1.923	1.85	2.30	Ti ^{IV}	1.815	1.76	2.19
Bi ^V	2.06	1.97	2.44	Pb ^{II}	2.112	2.03	2.53	Hg ^I	1.90	1.81	2.28	Tl ^I	2.172	2.15	2.56
Bk ^{III}	2.08	1.96	2.46	Pb ^{IV}	2.042	1.94	2.43	Hg ^{II}	1.93	1.90	2.25	Tl ^{III}	2.003	1.88	2.32
Br ^{VII}	1.81	1.72	2.19	Pd ^{II}	1.792	1.74	2.05	Ho ^{III}	2.023	1.908	2.401	Tm ^{III}	2.000	1.842	2.38
C ^{IV}	1.39	1.32	1.76	Pr ^{III}	2.135	2.022	2.50	I ^V	2.00	1.90	2.38	U ^{IV}	2.112	2.034	2.48
Ca ^{II}	1.967	1.842	2.37	Pt ^{II}	1.768	1.68	2.05	I ^{VII}	1.93	1.83	2.31	U ^{VI}	2.075	1.966	2.46
Cd ^{II}	1.904	1.811	2.23	Pt ^{IV}	1.879	1.759	2.17	In ^{III}	1.902	1.79	2.28	V ^{III}	1.743	1.702	2.19
Ce ^{III}	2.151	2.036	2.52	Pu ^{III}	2.11	2.00	2.48	Ir ^V	1.916	1.82	2.30	V ^{IV}	1.784	1.70	2.16
Ce ^{IV}	2.028	1.995	2.41	Rb ^I	2.26	2.16	2.65	K ^I	2.13	1.99	2.52	V ^V	1.803	1.71	2.16
Cr ^{III}	2.07	1.95	2.45	Re ^{VII}	1.97	1.86	2.23	La ^{III}	2.172	2.057	2.545	W ^{VI}	1.921	1.83	2.27
Cl ^{VII}	1.632	1.55	2.00	Rh ^{III}	1.791	1.71	2.17	Li ^I	1.466	1.360	1.91	Y ^{III}	2.014	1.904	2.40
Cm ^{III}	2.23	2.12	2.62	Ru ^{IV}	1.834	1.74	2.21	Lu ^{III}	1.971	1.876	2.361	Yb ^{III}	1.985	1.875	2.371
Co ^{II}	1.692	1.64	2.01	S ^{IV}	1.644	1.60	2.02	Mg ^{II}	1.693	1.581	2.08	Zn ^{II}	1.704	1.62	2.01
Co ^{III}	1.70	1.62	2.05	S ^{VI}	1.624	1.56	2.03	Mn ^{II}	1.790	1.698	2.13	Zr ^{IV}	1.937	1.854	2.33
Cr ^{II}	1.73	1.67	2.09	Sb ^{III}	1.973	1.90	2.35	Mn ^{III}	1.760	1.66	2.14				
Cr ^{III}	1.724	1.64	2.08	Sb ^V	1.942	1.80	2.30								
Cr ^{VII}	1.794	1.74	2.12	Sc ^{III}	1.849	1.76	2.23								
Cs ^I	2.42	2.33	2.79	Se ^{IV}	1.811	1.73	2.22								
Cu ^I	1.593	1.6	1.85	Se ^{VI}	1.788	1.69	2.16								
Cu ^{II}	1.679	1.60	2.00	Si ^{IV}	1.624	1.58	2.03								

Cu^{III}-O, R=1.724; Co^{IV}-O, R=1.75; Fe^{IV}-O, R=1.78;
Ni^{III}-O, R=1.68; Ni^{IV}-O, R=1.72

N.E.Brese and M.O'Keefe. Bond-Valence Parameters for Solids. Acta Cryst., B47, 192-197(1991)

化学成分，结构对称性 & 元素分布与性能的关系

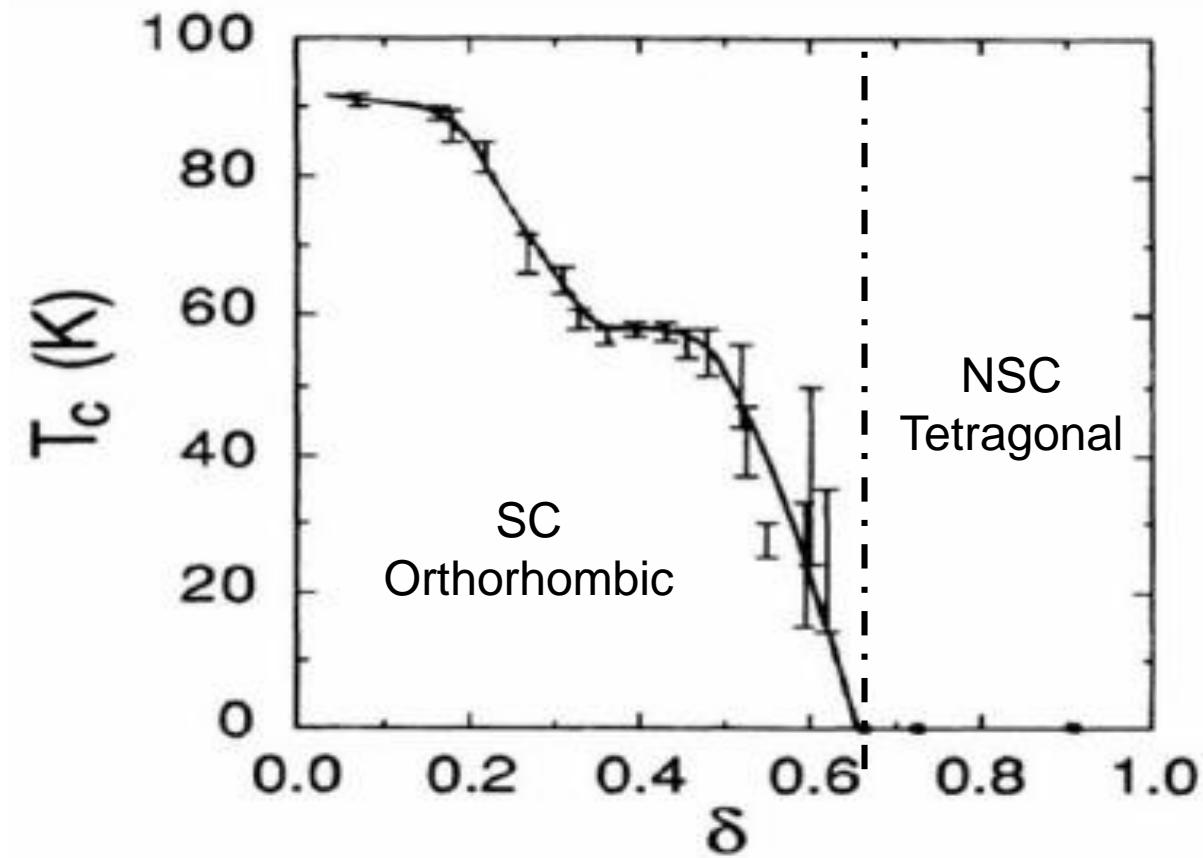
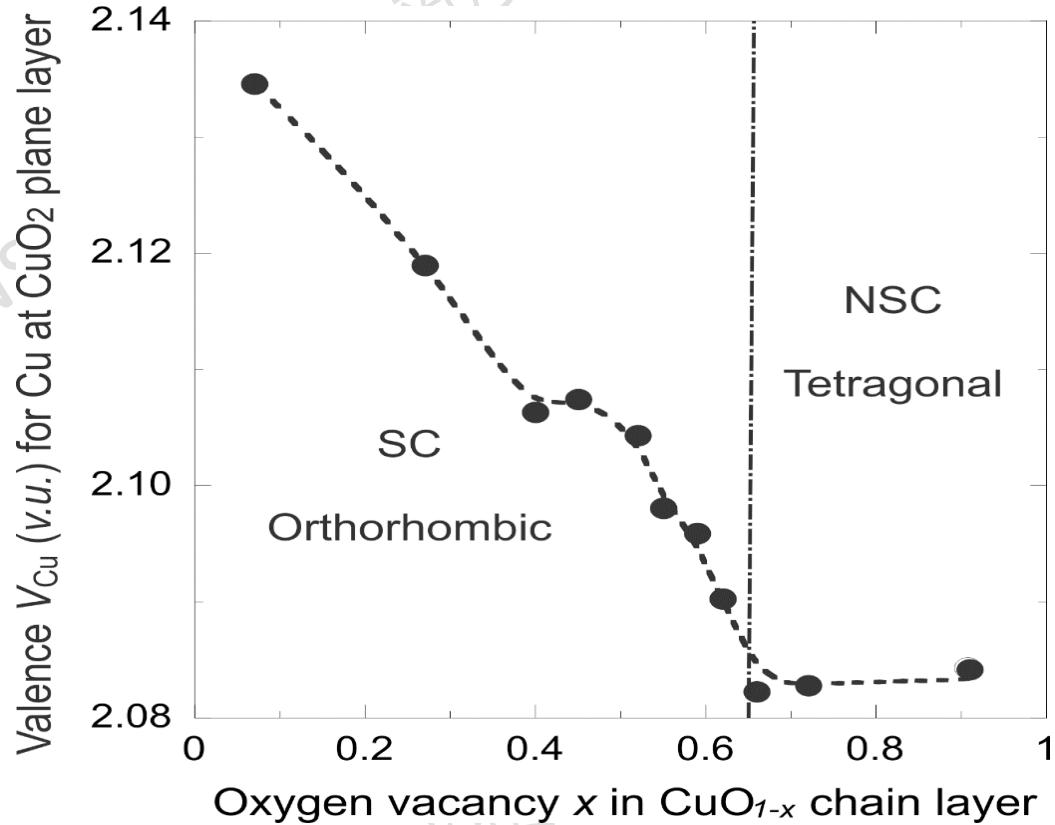


Schematic view of charge transfer between conduction layer and charge reservoir layer in superconducting and related compounds. Electron transfer from the conduction layer to the charge reservoir layer is known as “hole doping” and moving electrons from the charge reservoir layer to the conduction layer is known as “electron doping”.

$\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$ 是第一个被发现 T_c 在液氮以下的高温超导体。研究发现：

- $\text{O}1$ 位置的占有率为35%时为有序占有，结构变为正交 $Pmmm$ 对称性，化合物超导。
- $\text{O}1$ 位置的占有率为低于35%时为无序占有，结构为四方 $P4/mmm$ 对称性，不超导。
- 超导温度随着 $\text{O}1$ 的占有率增加上升到91 K。

YBa₂Cu₃O_{7-x}超导温度T_C和对应的价态ν_{Cu(plane)}随氧空位δ(O1) 的变化



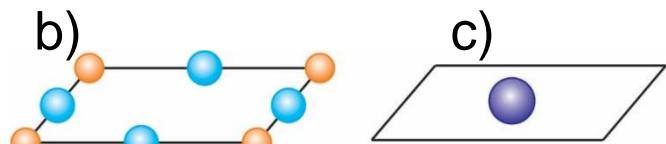
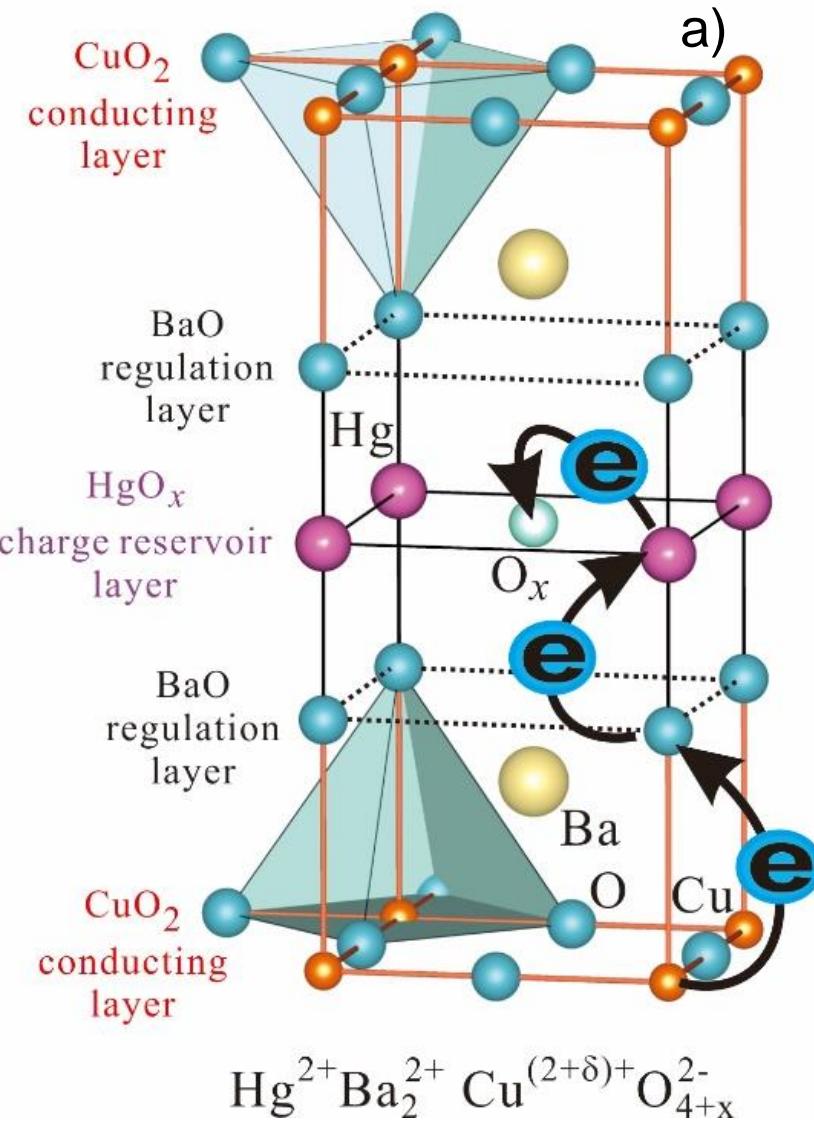
(a) Calculated bond-valence for Cu in the CuO₂ plane layer versus oxygen content in the chain layer of YBa₂Cu₃O_{7-x}. The data of bond distances used in the calculation are based on the structure information reported by Jorgensen *et al.* (1990). (b) T_C versus oxygen content in the chain layer of YBa₂Cu₃O_{7-x}.

$$\nu = \sum \nu_{ij}, \quad \nu_{ij} = \exp[(R_{ij} - d_{ij})/b], \quad e = 2.71828, \quad b = 0.37, \quad d_{ij} \text{ is observed interatomic distance.}$$

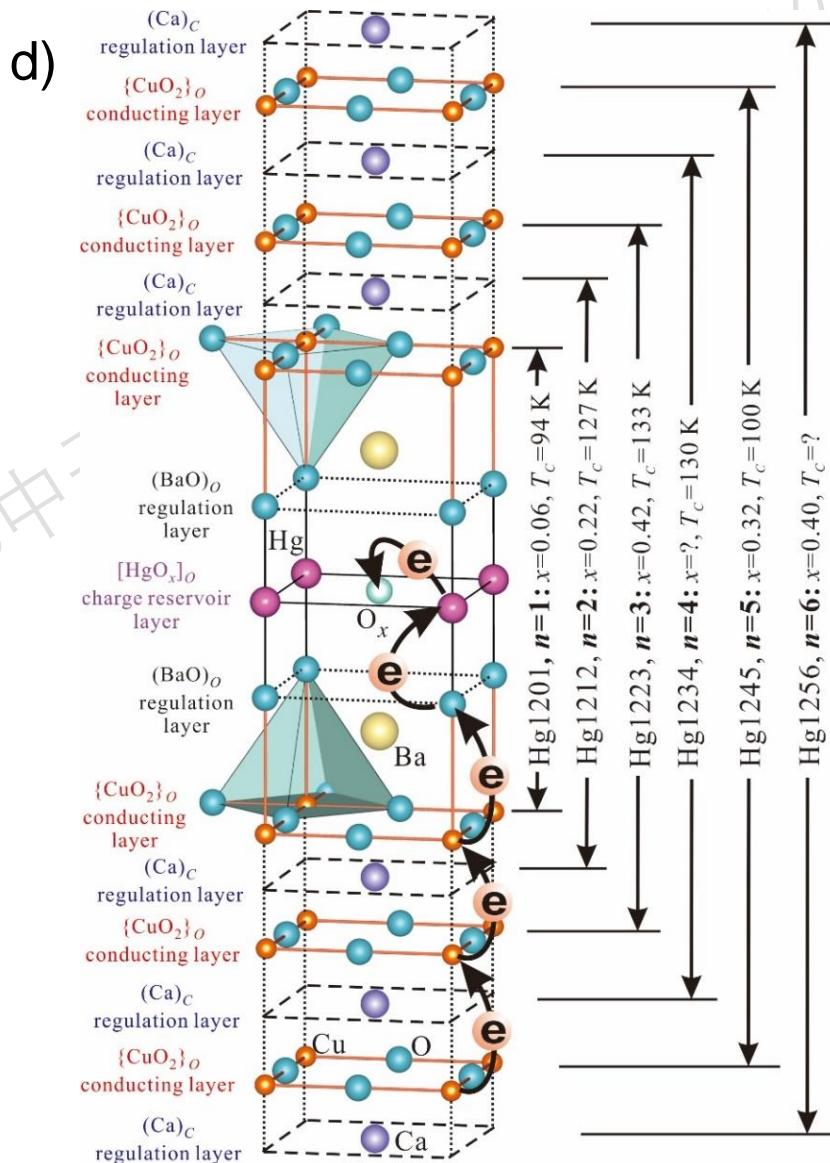
N. E. Brese and M. O'Keeffe. Bond-Valence Parameters for Solid. Acta Cryst. B47, 192-197(1991).

层状汞系铜基高温超导体 $\text{HgBa}_2\text{Ca}_{n-1}\text{Cu}_n\text{O}_{(2n+2)+x}$ 结构分析

Analysis of High- T_c superconductors $\text{HgBa}_2\text{Ca}_{n-1}\text{Cu}_n\text{O}_{(2n+2)+x}$



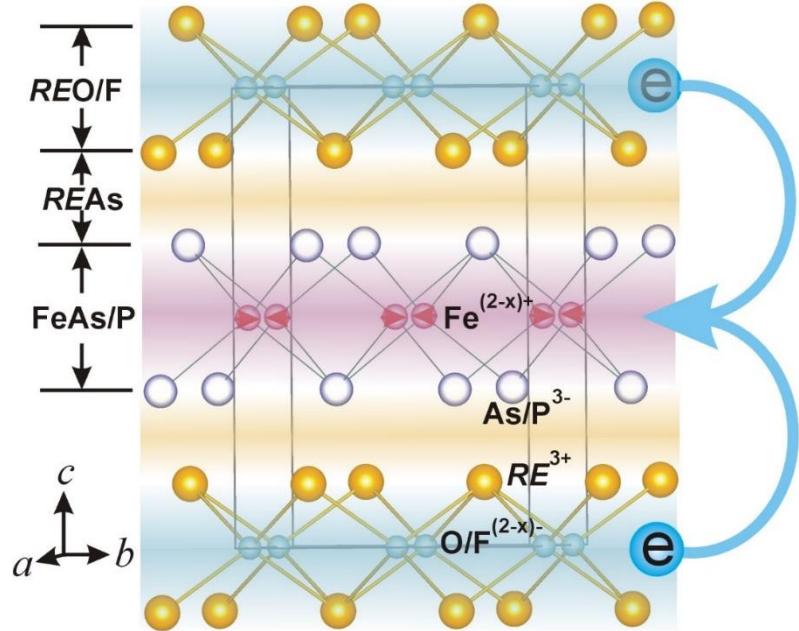
以图a的 $\text{HgBa}_2\text{CuO}_{4+x}$ 的结构为基础，在 c 轴方向叠加图b和c的平面构成图d的三维层状结构层状汞系铜基高温超导系列化合物 $\text{HgBa}_2\text{Ca}_{n-1}\text{Cu}_n\text{O}_{(2n+2)+x}$ 是。最高超导温度达到133 K。如图所示的电荷转移示意。当 HgO_x 层的 $X=0$ 时，化合物不超导。因此，准确测定 HgO_x 层中的O的占有率是研究化合物结构与性能的关系的关键。电荷转移可以用半经验方法计算Cu的价态得以估计。同时可以根据层间距估计化合物晶胞 c 轴的长度。



$P4/mmm$

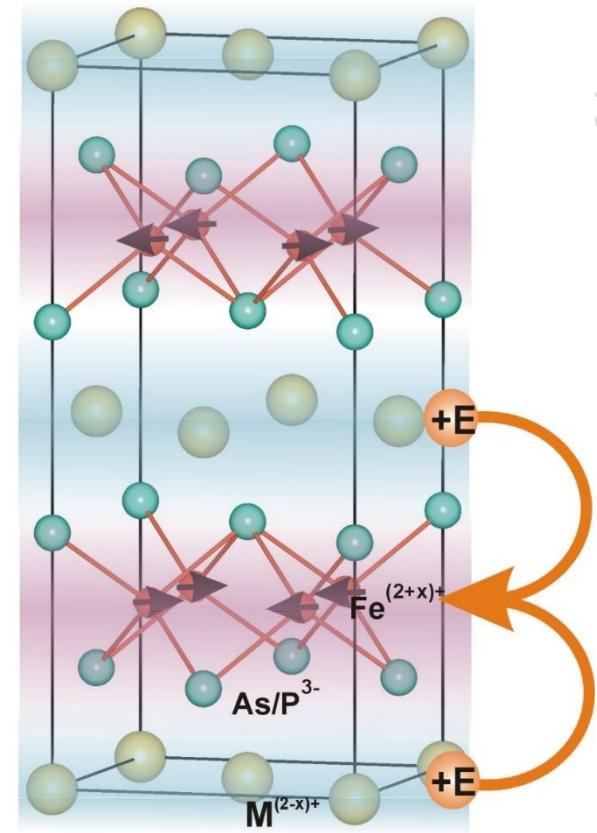
$\text{HgBa}_2\text{Ca}_{n-1}\text{Cu}_n\text{O}_{(2n+2)+x}$

铁基超导机理研究

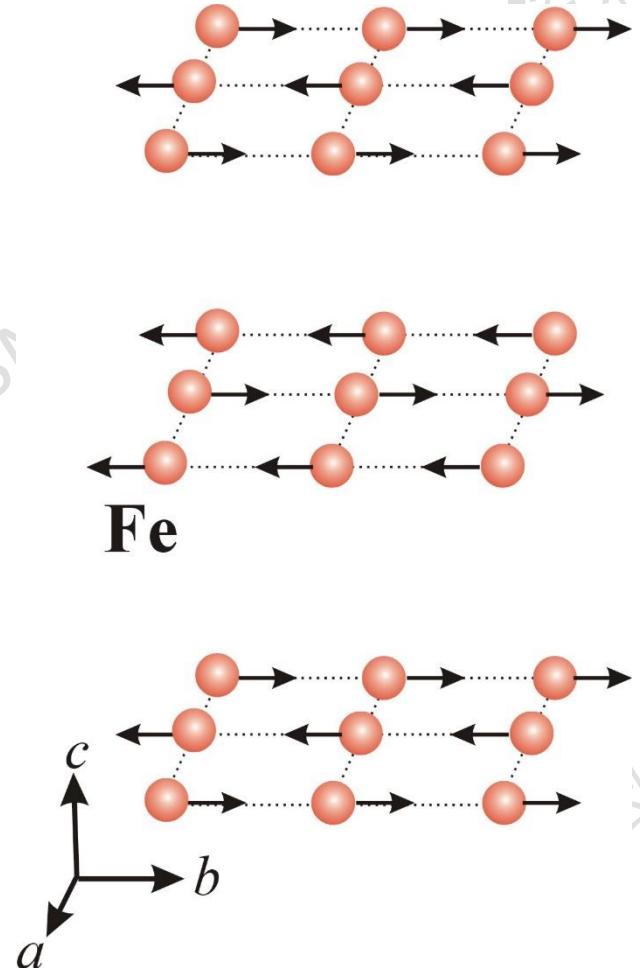
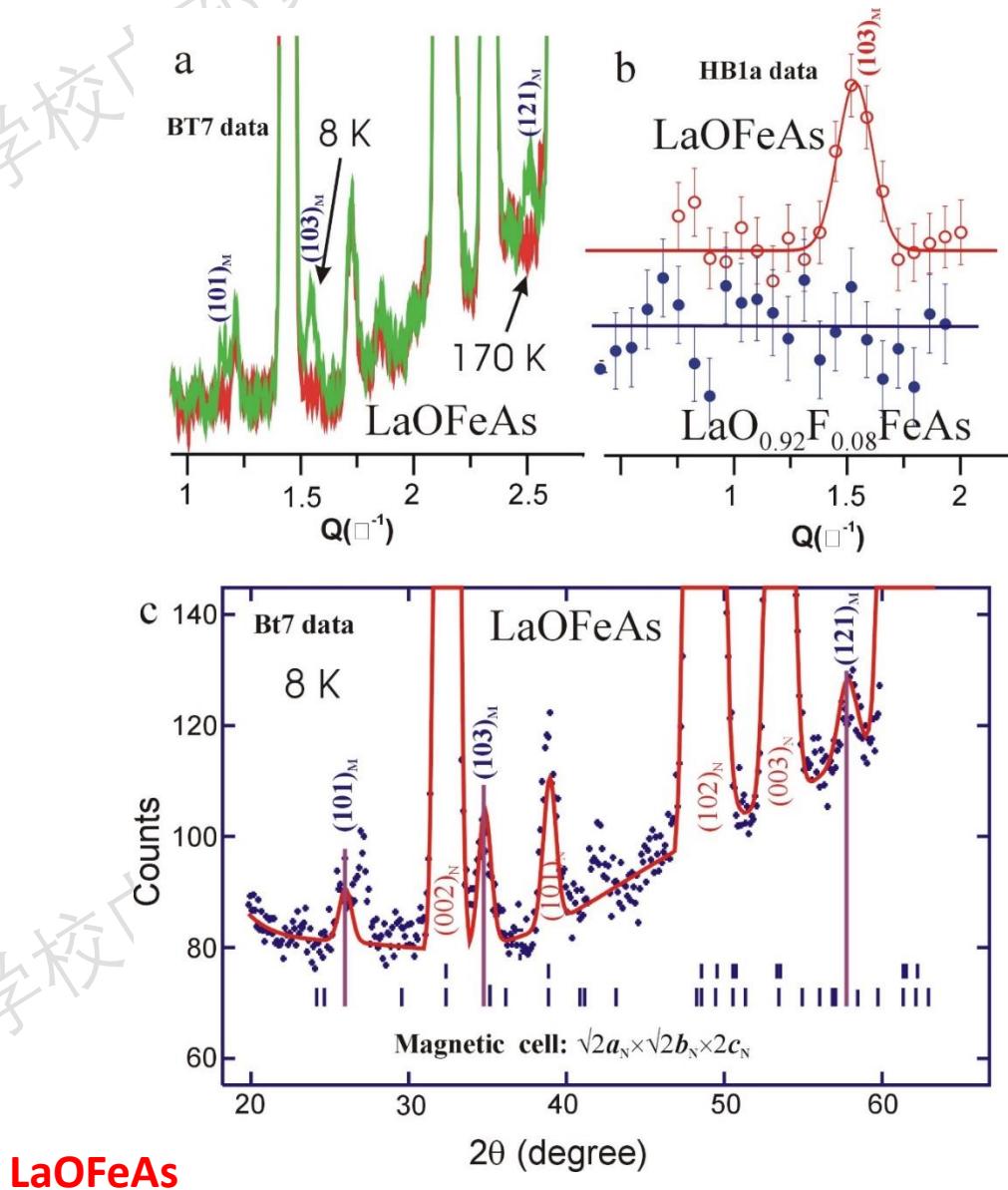


Fe-As~2.4 Å; RE-As~3.4 Å; RE-O/F~2.4 Å; M-As~3.3 Å.

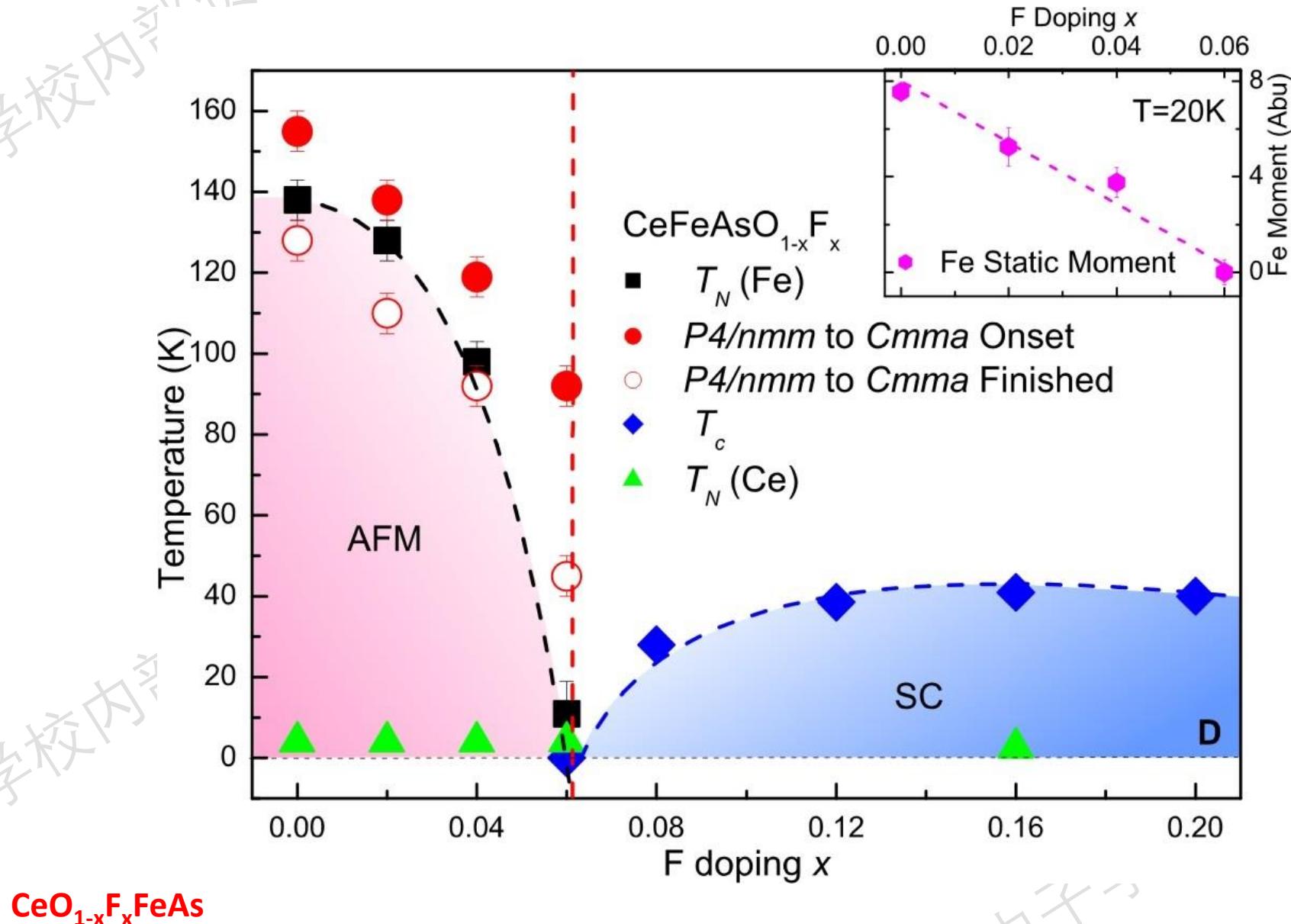
Charge Transforms



铁基超导机理研究

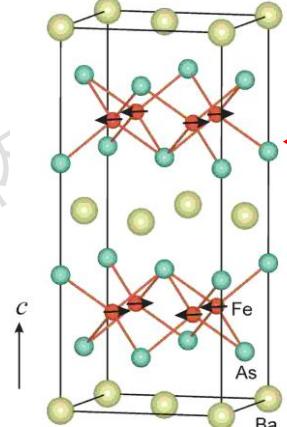
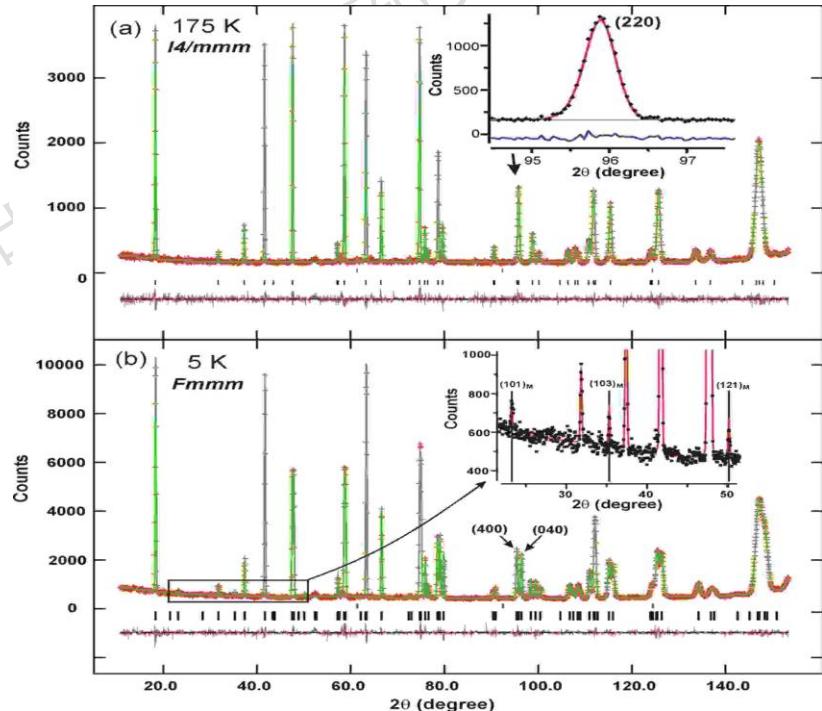


铁基超导机理研究



BaFe₂As₂晶体结构和磁结构,相转变与性能

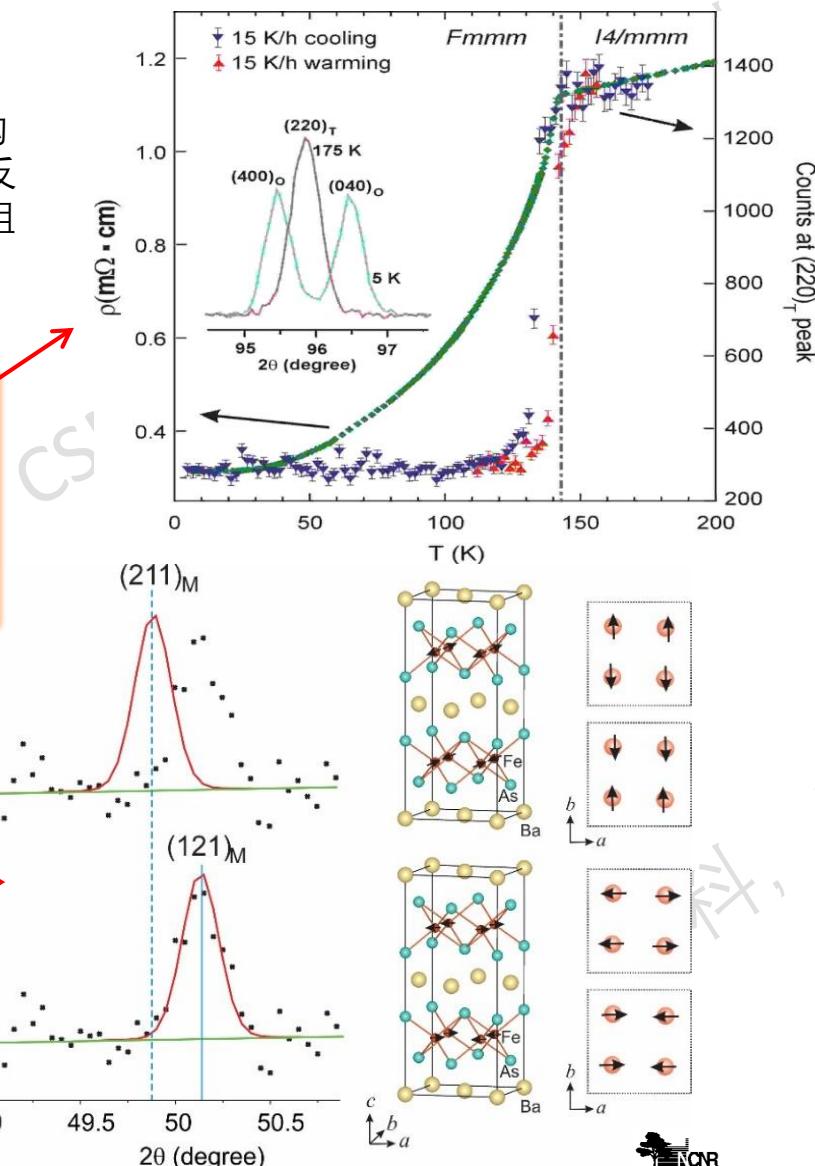
Crystal & Magnetic Structure, Phase Transformation, and properties of BaFe₂As₂



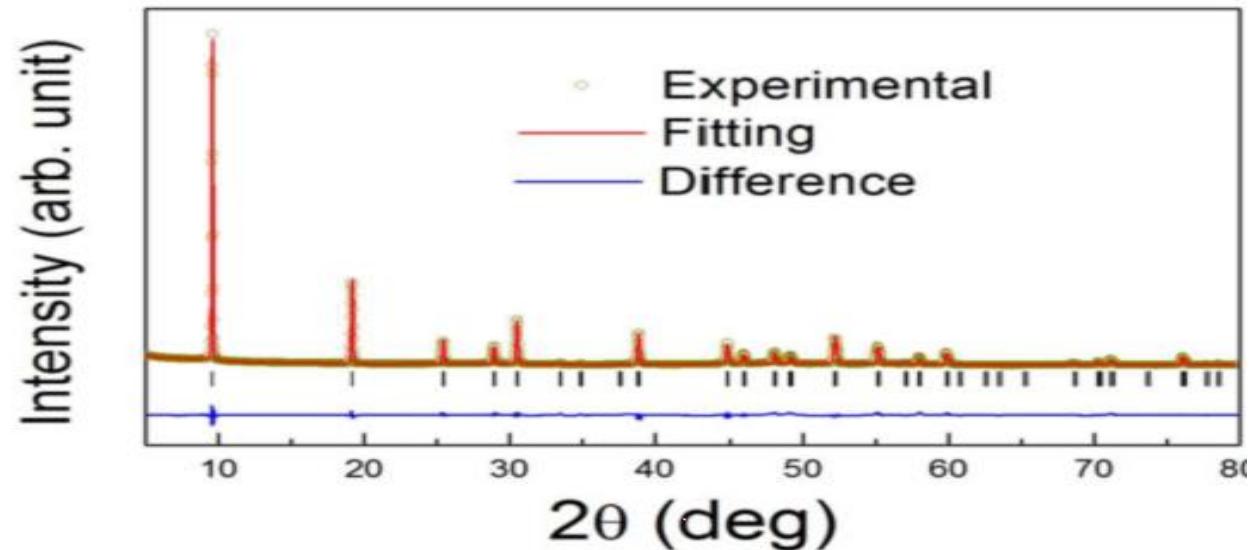
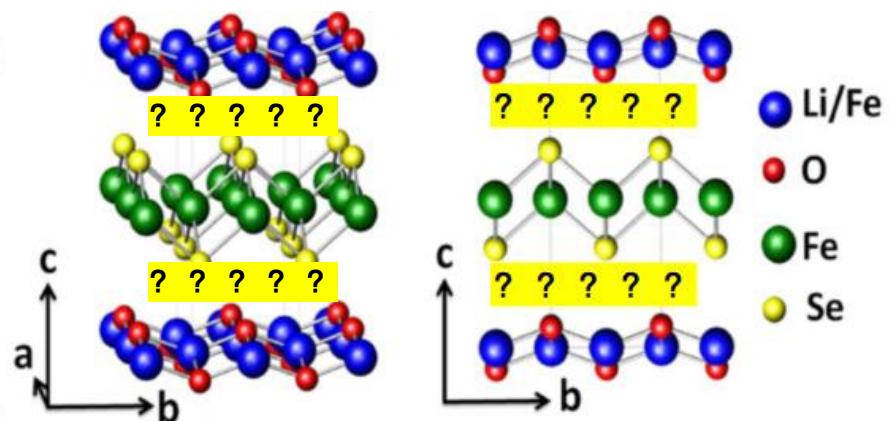
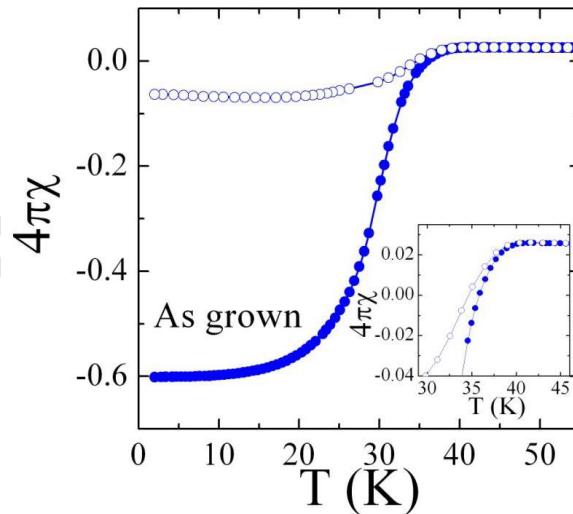
化合物BaFe₂As₂在~142 K经历由高温I4/mmm到低温Fmmm的一级晶体结构相变，伴随着从顺磁到反铁磁的磁有序转变和电阻急剧下降的突变。

Relationships
between structure
and
properties
...

Determine and refine
crystal and magnetic
structures:
Chemical & symmetry
Atomic distribution
Magnetic order-disorder
Spin arrangement
...



超导化合物(Li/Fe)OH-FeSe 的晶体结构测定
Structure Determination of (Li/Fe)OH-FeSe Superconductor, $T_c=43$ K



X.F.Lu et al. PHYSICAL REVIEW B. 89, 020507(R) (2014)

利用中子对元素H和Li敏感优势，准确地测定了(Li/Fe)OH-FeSe的晶体结构。化合物具有43K的超导温度使得铁基超导体进入高温超导行列。由于X射线对H和Li的不敏感，先前的X射线粉末衍射工作未能发现H的位置和确定Fe/Li混合占位的比例。可以假定结构中，FeSe层与(Li/Fe)O层之间是通过Se与O存在有Van der Waals键连接，结构也合理。

铁基超导化合物 (Li/Fe)OH-FeSe 的X射线与中子衍射谱图

XRPD & NPD pattern of superconductor (Li/Fe)OH-FeSe

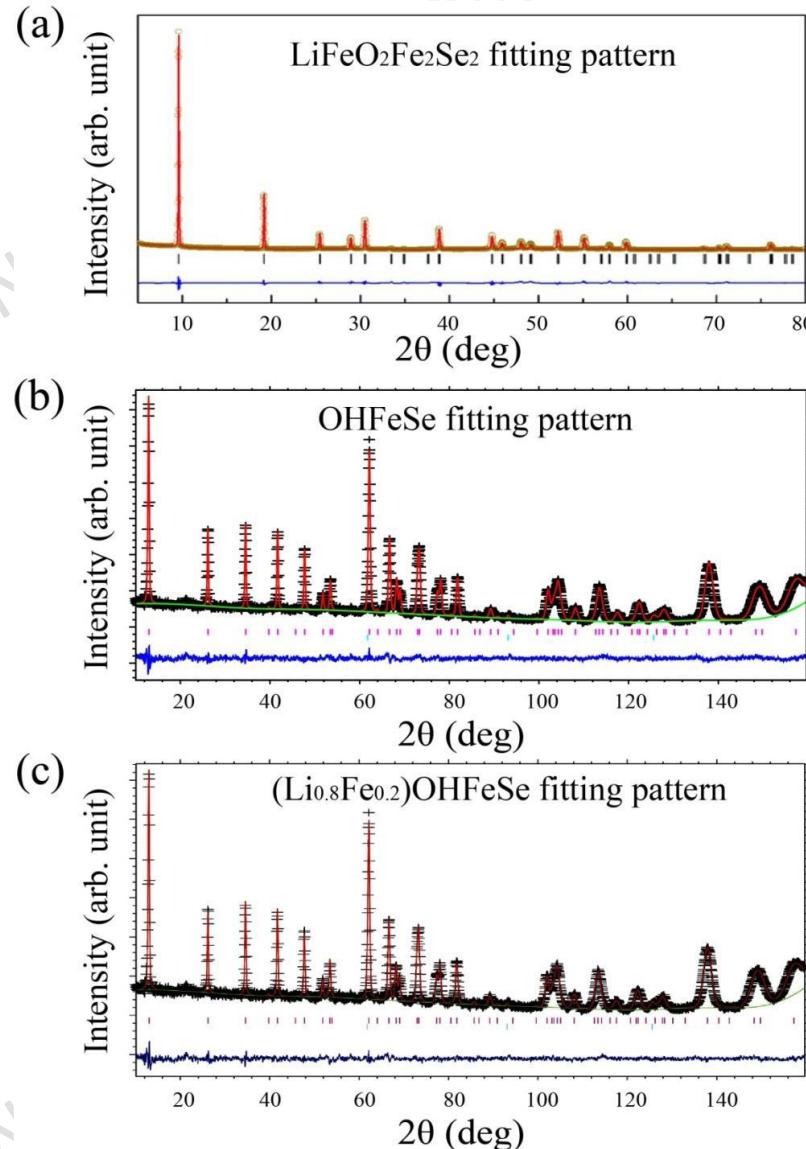


Figure S2:

(a): Rietveld refinement on XRD data collected at 298 K for the structural model of $\text{LiFeO}_2\text{Fe}_2\text{Se}_2$, which was shown in Fig. S1(a).

(b): Rietveld refinement on NPD data with the structural model of OHFeSe shown in Fig. S1(b). The NPD data was collected over the 2-Theta range of $1.3\text{--}166.3^\circ$ using Ge311 ($\lambda=2.0775\text{\AA}$) monochromator at 4 K.

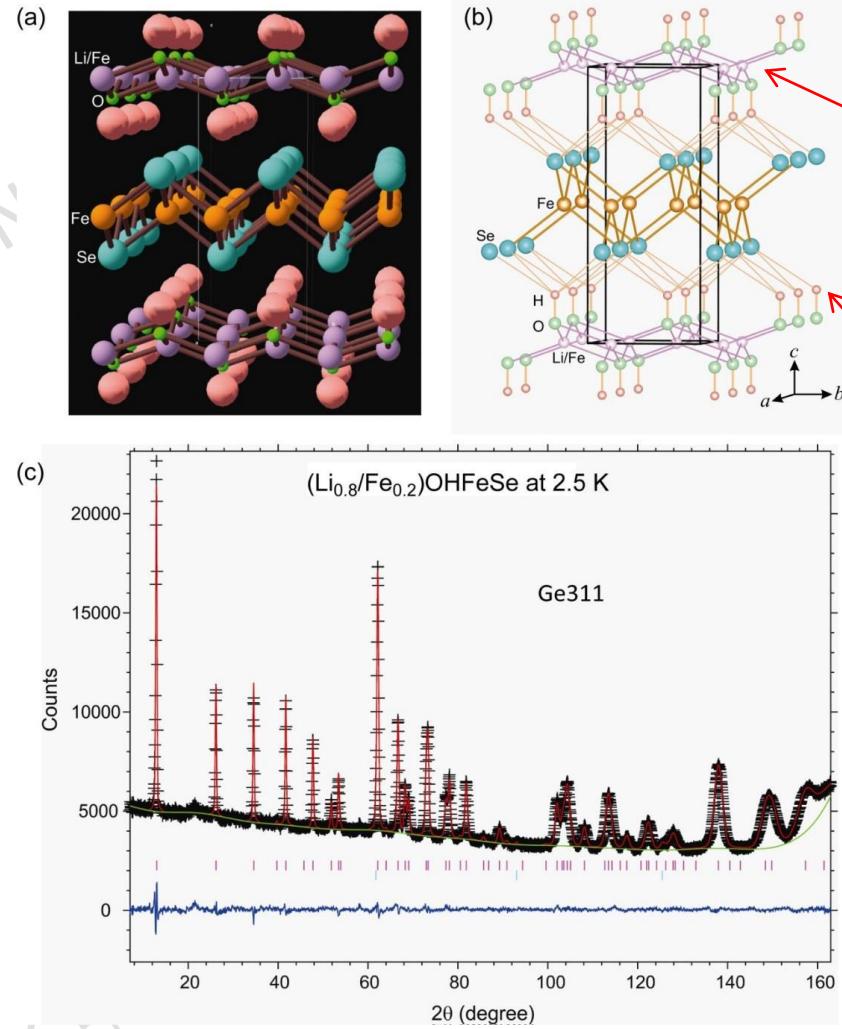
(c): Rietveld refinement on NPD pattern which was collected at 4 K using Ge311 ($\lambda=2.0775\text{\AA}$) monochromator with the structural model of $(\text{Li}_{0.8}\text{Fe}_{0.2})\text{OHFeSe}$ shown in Fig. S1(c).

Name	X,#	N, b	
H	1	-0.3741	●
Li	3	-0.203	●
O	8	0.5805	○
Fe	26	0.954	○
Se	34	0.797	○

图 a 和 b 分别是 XRPD 和 NPD 的谱图。对于 XRPD，衍射峰的强度随着衍射角的增大而迅速衰减。而在 NPD 图中，由于中子散射因子是常数，高角度衍射峰并没有明显减弱。再比较 X 射线和中子散射因子，H 和 Li 的原子序数为 1 和 3，X 射线的散射本领极低。而 H 和 Li 的中子分别为 -0.3741 和 -0.203，对 NPD 的贡献要比 XRPD 大的多。

超导化合物(Li/Fe)OH-FeSe晶体结构测定

Structure determination of (Li/Fe)OH-FeSe superconductor



? at $(0\ 0\ 0)$

$b(\text{H}) = -0.374$

$b(\text{Fe}) = 0.954$

$b(\text{Li}) = -0.203$

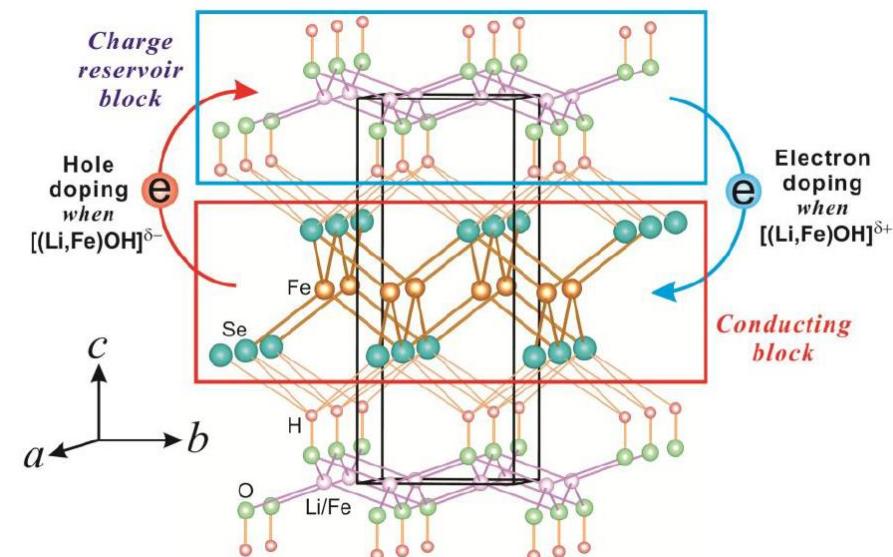
$b(0.814\text{Li} + 0.186\text{Fe}) = 0.012$

Neutron cross section

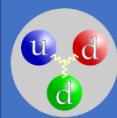
DELF: H at $(3/4, 3/4, 0.175)$

- a, Neutron scattering Fourier difference analysis using NPD data. Fourier difference contours are highlighted in pink. Oxygen atoms (green), Li/Fe atoms (purple).
- b, A schematic view of the structure of $(\text{Li}_{0.8}\text{Fe}_{0.2})\text{OHFeSe}$.
- c, Observed (crosses) and calculated (red solid line) NPD pattern for $(\text{Li}_{0.8}\text{Fe}_{0.2})\text{OHFeSe}$ ($\lambda = 2.0775 \text{ \AA}$) at 2.5 K.

用中子粉末衍射数据进行差傅里叶分析发现了夹层中存在H，同时中子数据分析最后确认，在 (000) 的位置上 $\text{Fe}_{0.186}$ 和 $\text{Li}_{0.814}$ 共同占位。最后确定以H-O和H-Se连接FeSe和(Fe/Li)O形成三维结构。

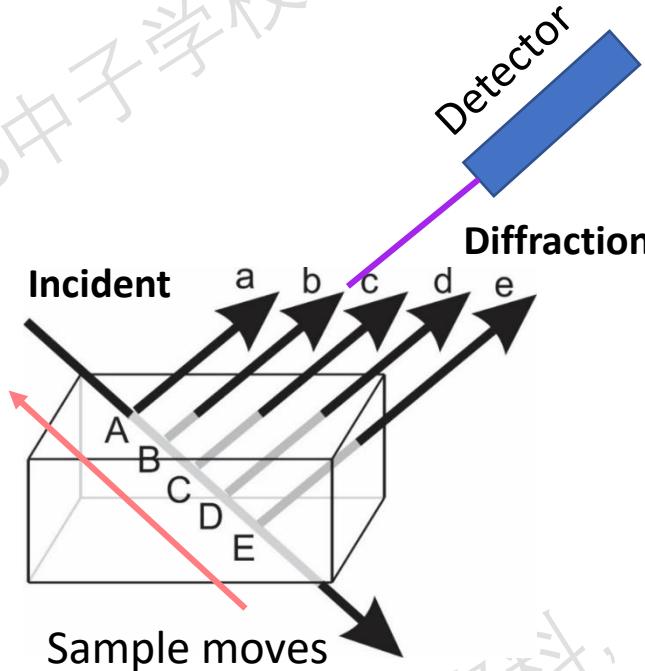


A schematic view of the structure of $(\text{Li}_{0.8}\text{Fe}_{0.2})\text{OHFeSe}$. The FeSe layer, which acts as the conducting block, alternately stacks with the charge reservoir block $(\text{Li}_{0.8}\text{Fe}_{0.2})\text{OH}$ layer in this model.



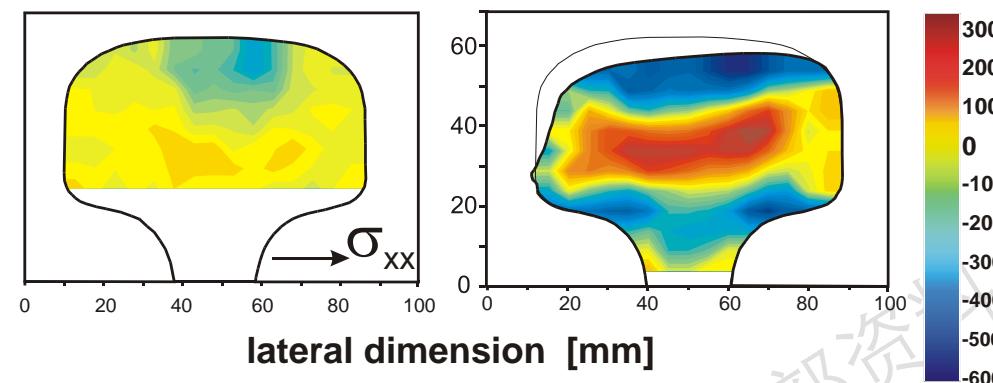
Strong penetration

When there is stress in solid materials, lattice deformation causes diffraction peak displacement.



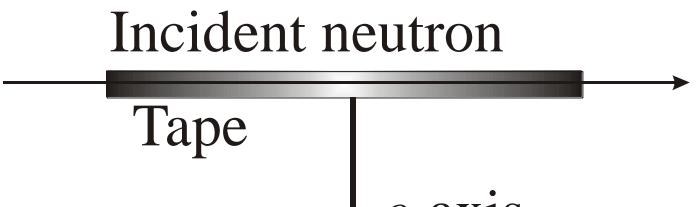
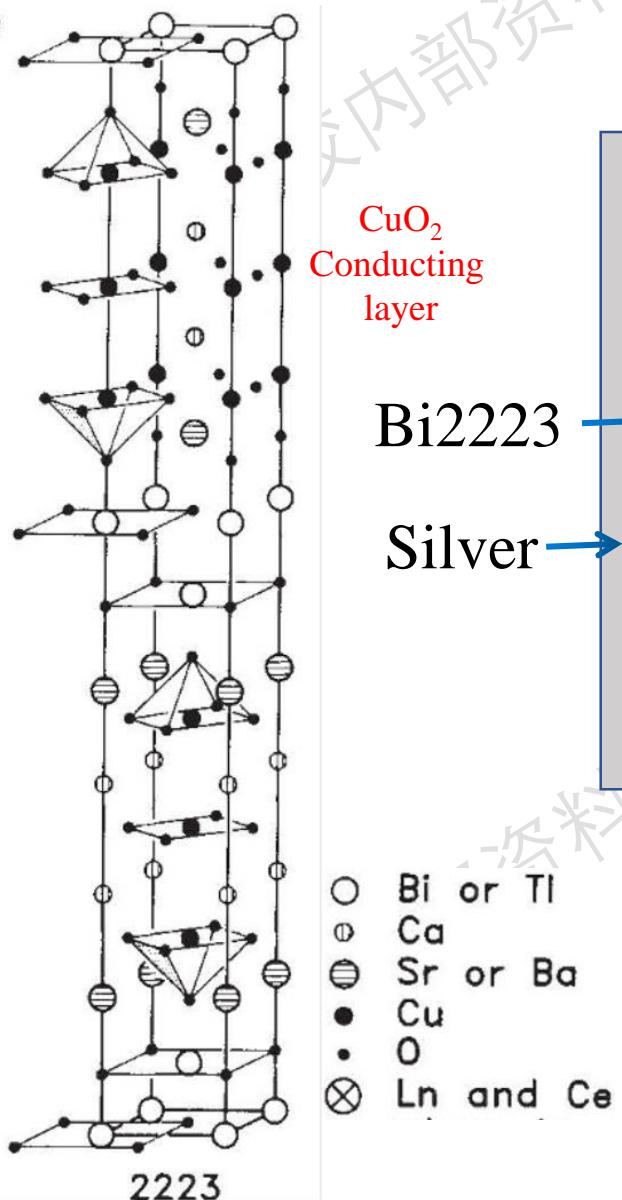
Neutrons can penetrate deeply without destroying samples, and pass through walls controlling a sample's environment allowing measurements under extreme conditions. Non-destructive residual stress, texture, and microstructure investigation in engineering components.

To study residual stresses in steel, aluminum, superalloys, and other such structural materials. Elastic strain in these materials can be determined by measuring their interplanar atomic spacing, and the instrument should be designed to use the high-penetration power of neutrons to generate "maps" of the strain resulting from residual or applied stresses in bulk materials.

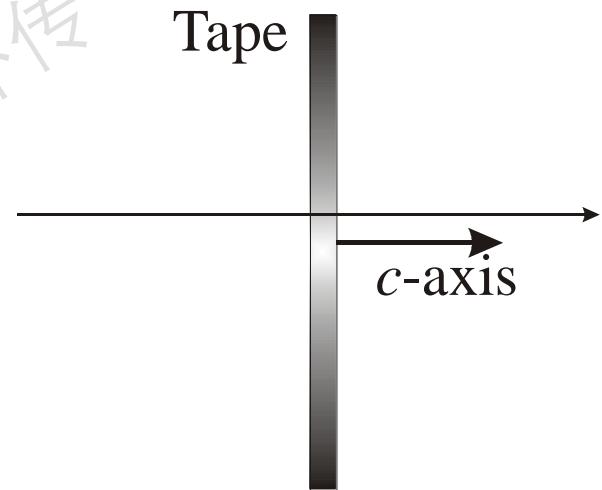


Neutron Diffraction Residual Stress Measurement: Stresses in Railroad Rails before and after Service

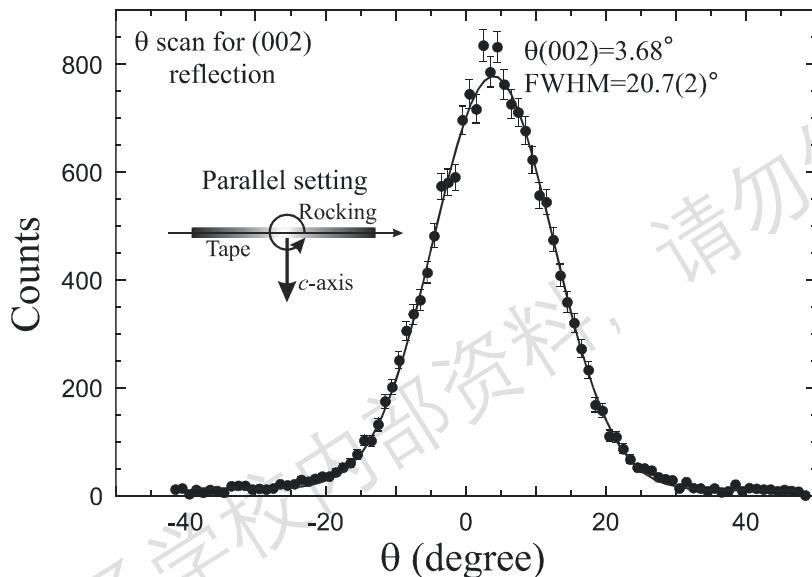
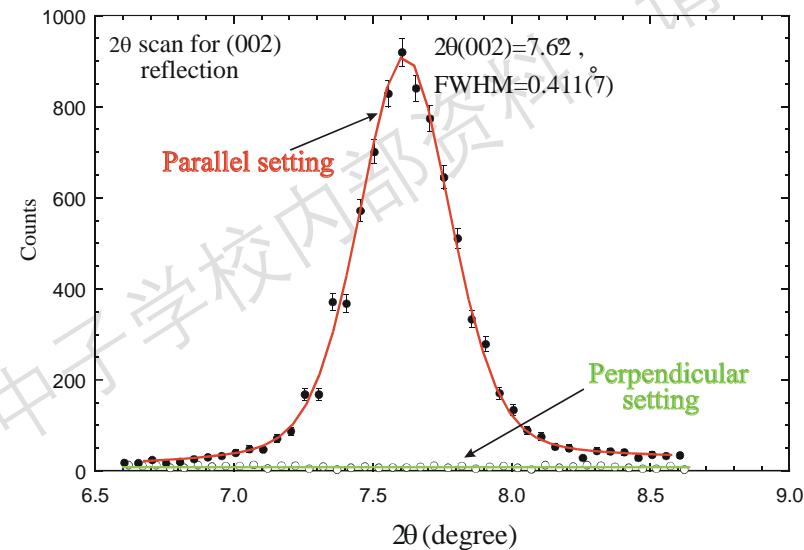
Bi2223 超导带中晶粒取向



(a) Parallel setting



(b) Perpendicular setting



中子的性质, 波粒二象性 Wave-particle Duality

Table 2.3.1

Properties of the neutron (adapted from Kisi & Howard, 2008)

Mass (m)	1.675×10^{-27} kg
Charge	0
Spin	$\frac{1}{2}$
Magnetic moment (μ_n)	$-1.913 \mu_N$
Wavelength (λ)	h/mv
Wavevector (\mathbf{k})	Magnitude $2\pi/\lambda$
Momentum (\mathbf{p})	$\hbar\mathbf{k}$
Energy (E)	$(1/2)mv^2 = h^2/2m\lambda^2$

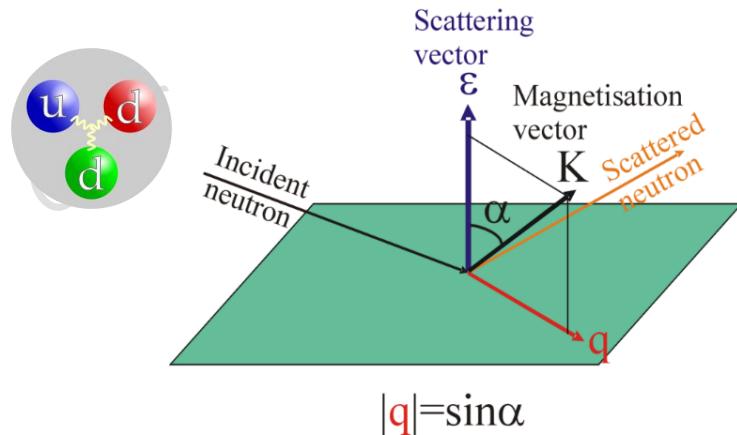
Although the neutron is a neutral particle, the magnetic moment of a neutron is not zero. It has spin $\frac{1}{2}$ and a moment of $-0.001042 \mu_B$, an indication of its quark substructure and internal charge distribution. It can be modeled as a sum of the magnetic moments of the constituent quarks. The calculation assumes that the quarks behave like pointlike Dirac (迪拉克 An English physicist) particles, each having their own magnetic moment. Simplistically, the magnetic moment of the neutron can be viewed as resulting from the vector sum of the three quark magnetic moments, plus the orbital magnetic moments caused by the movement of the three charged quarks within the neutron.

根据微观粒子的波粒二象性, 中子具有波动性, 慢中子的波长约 10^{-10} 米, 与晶体内原子间距相当。中子衍射是研究晶体结构的重要技术。中子是不带电的基本粒子, 静止质量为 1.6748×10^{-27} kg, 它的半径约为 0.8×10^{-15} m, 与质子大小类似。

The neutron contains one “up” quark (charge $+2/3 e$) and two “down” quarks (charge $-1/3 e$). Neutron is a neutral particle.

Magnetic interaction vector

$$\mathbf{q} = \epsilon(\epsilon \cdot \mathbf{K}) - \mathbf{K}$$



Definition of the vectors relevant in the evaluation of factor (Bacon, G. E. (1962)). ϵ and \mathbf{K} are unit vectors in the directions of the scattering and magnetic moment, respectively. The magnetic interaction vector \mathbf{q} is always perpendicular to the scattering vector.

Magnetic Intensity

Peaks Position: $2dsin\theta = n\lambda$

where λ is the incident beam wavelength, d and θ are the distance between successive hkl planes and Bragg angles of reflections, respectively.

Diffraction Intensity: $I_{hkl} = C |F_{hkl}|^2$

where F_{hkl} is the amplitude of the diffracted X-ray or neutron hkl reflection, and **C** is all others.

X-ray: $F_{hkl} = \sum f_j \exp(2\pi i (hx + ky + lz)) e^{-2w}$

where f_j is the X-ray atomic scattering factor of atom j for X-ray.

Neutron: $F_{hkl} = \sum b_j \exp(2\pi i (hx + ky + lz)) e^{-2w}$

where b_j is the neutron scattering length for atom j .

Magnetic: $F_{hkl} = \sum q_j f_{Mj} \exp(2\pi i (hx + ky + lz)) e^{-2w}$

where q_j and f_{Mj} are the magnetic interaction vector and the magnetic form factor for atom j , respectively.

$$I_M = C \mathcal{M}_T A(\theta_B) [(\gamma e^2)/(2mc^2)]^2 \langle 1 - (\tau \cdot M)^2 \rangle / F_M^2$$

C- Instrumental constant

\mathcal{M}_T Multiplicity (for powder)

$A(\theta_B)$ - angular factor, $1/(\sin \theta \sin 2\theta)$

$[(\gamma e^2)/(2mc^2)] = -0.27$ - neutron-electron coupling

$\langle 1 - (\tau \cdot M)^2 \rangle$ -orientation factor

F_M - Magnetic structure factor

$$F_M = \sum \mu f \exp(2\pi i (hx + ky + lz)) e^{-W}$$

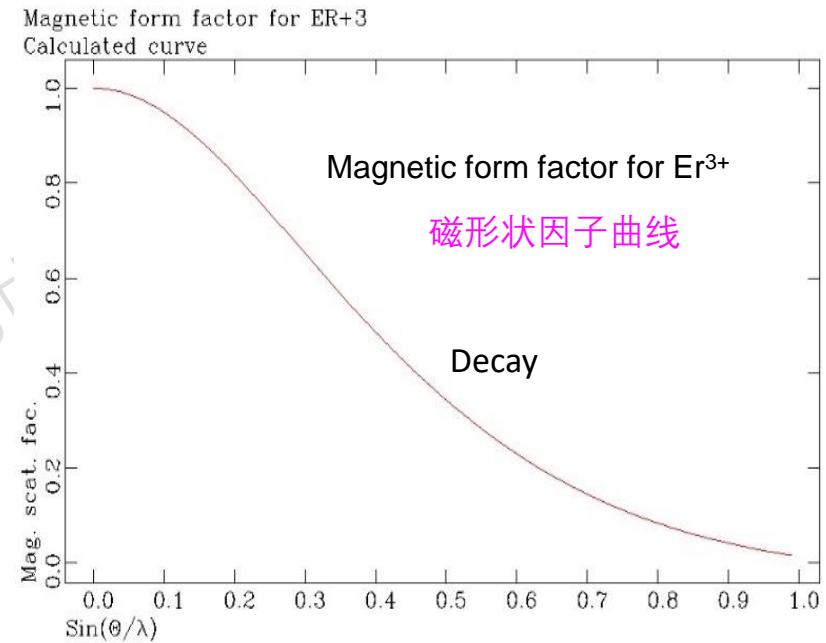
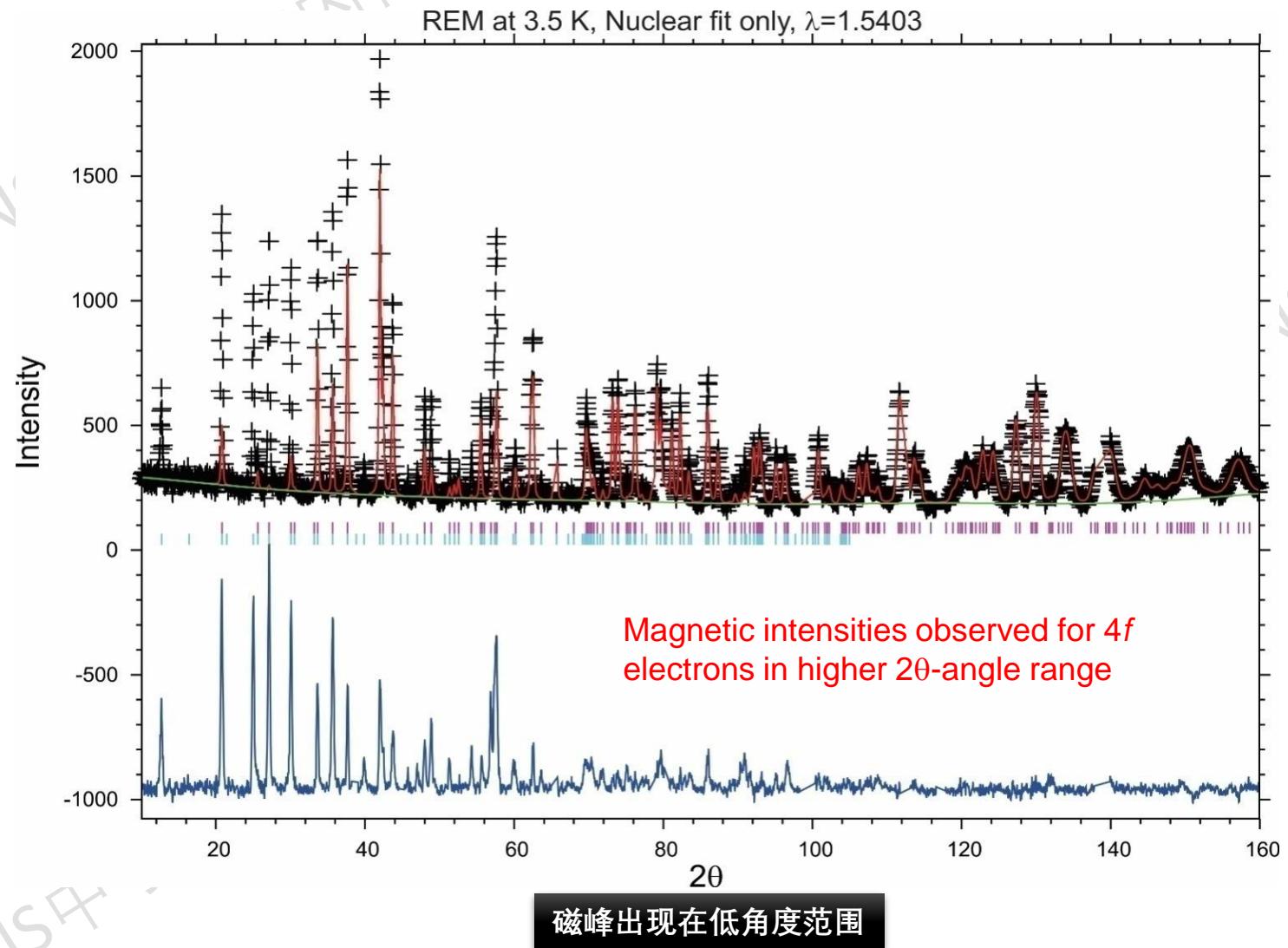
μ - magnetic moment

f - magnetic form factor

W -Debye Waller factor

磁有序, 磁晶胞, 磁对称性, 磁结构及性能

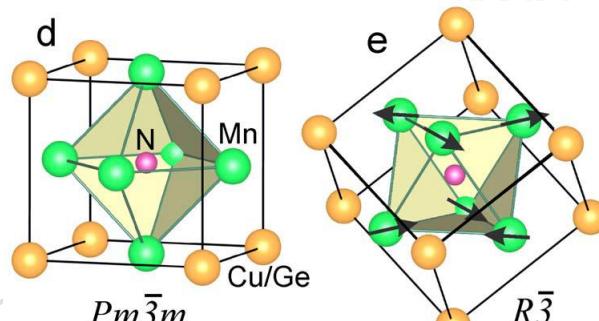
Spins order, magnetic cell, magnetic symmetry, and structure & properties



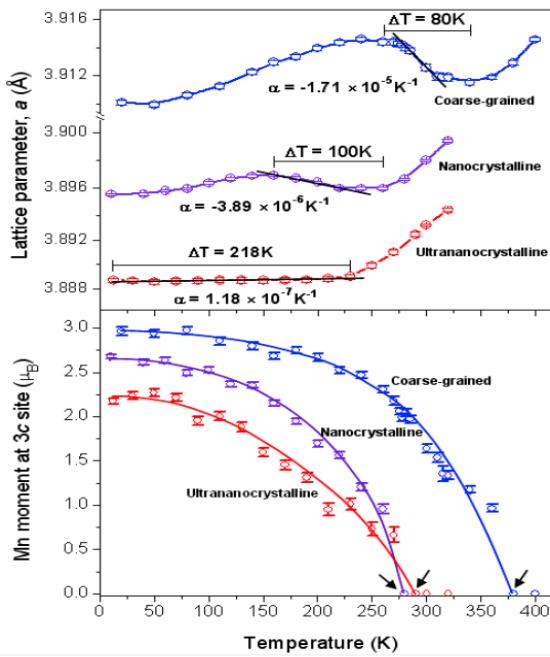
含重稀土 Er^{3+} 合金的中子衍射谱图。图中红线是以晶体结构拟合曲线，图的下部观察数据与计算数据的差值是 Er^{3+} 的有序的磁衍射峰。

具有反钙钛矿结构 $Mn_3Cu_{0.5}Ga_{0.5}N$ 的零热膨胀研究

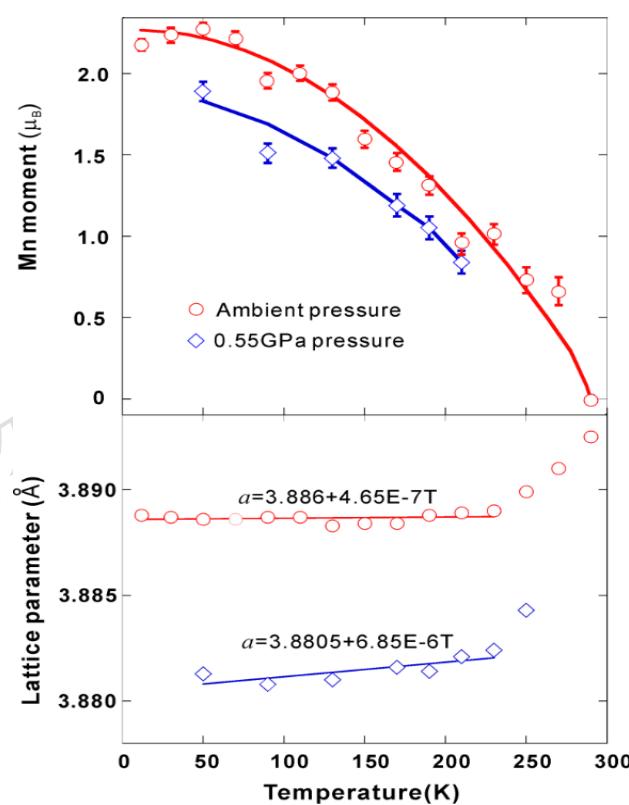
Zero Thermal Expansion in Antiperovskite $Mn_3Cu_{0.5}Ga_{0.5}N$



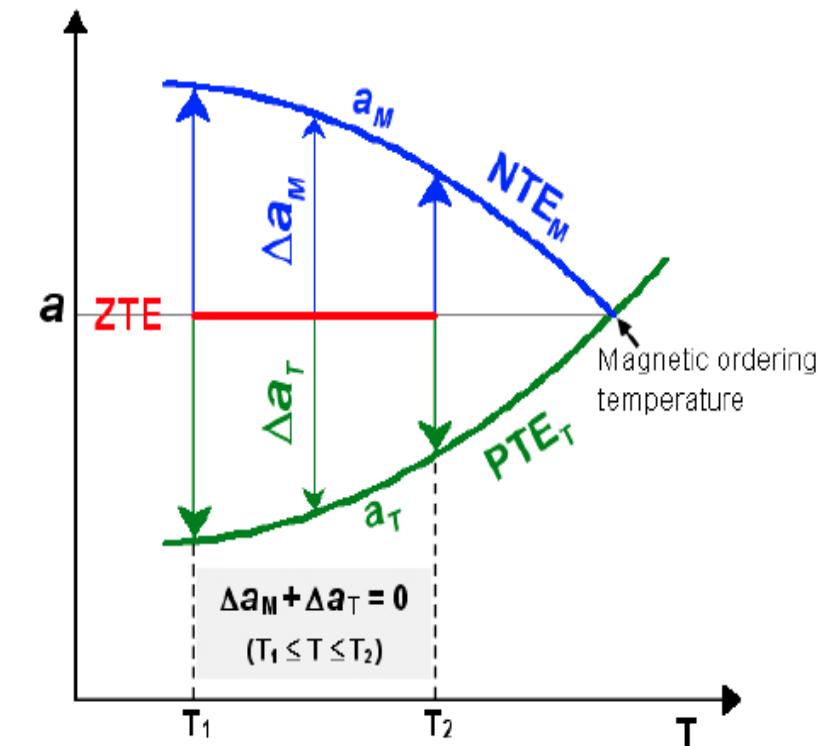
晶体结构和磁结构



磁有序度引起的负膨胀与温度引起的正膨胀完全抵消时，材料呈现零膨胀。



负膨胀与磁有序度有密切关联，样品的结晶晶粒大小也直接影响磁有序行为。



磁有序度引起的负膨胀与温度引起的正膨胀完全抵消时，材料呈现零膨胀。

元素周期表(二)

IA	
H	六方H
0.32	2.1
—	0.106
2.08(-1)	0.014
—	—
14.1	0.004
313	3.45

IIA

Li	立方I	Be	六方H
1.23	1.0	0.90	1.5
1.55	32.48	1.12	73.9
0.69(+1)	0.72	0.31(+2)	2.8
—	0.108	—	0.25
13.1	0.17	5.0	0.38
124	0.79	215	0.45

Mg

Na	立方I	Mg	六方H
1.54	0.9	1.36	1.2
1.90	24.12	1.60	32.517
0.95(+1)	0.62	0.65(+2)	2.14
—	0.218	—	0.224
23.7	0.32	14.0	0.38
110	0.295	176	0.25

VIIA

K	立方I	Ca	立方F
2.05	0.8	1.74	1.0
2.35	18.9	1.97	36.74
1.33(+1)	0.55	0.99(+2)	2.1
—	0.143	—	0.216
45.3	0.23	29.9	0.3
100	0.177	141	0.149

VIIIB

Rb	立方I	Sr	立方F
2.16	0.8	1.91	1.0
2.48	18.1	2.15	35.8
1.48(+1)	0.55	1.13(+2)	2.1
—	0.080	—	0.042
55.9	—	33.7	—
96	0.080	131	0.176

IIIIB

Cs	立方I	Ba	立方I
2.35	0.7	1.98	0.9
2.67	16.3	2.22	35.7
1.69(+1)	0.50	1.35(+2)	1.63
—	0.053	—	0.015
70	—	39	—
90	0.052	120	0.068

IVB

Fr	立方I	Ra	Ac**
—	0.7	—	0.6
—	—	27.4	1.88
1.76(+1)	—	1.40(+2)	2.4
—	—	—	1.18(+3)
—	—	45	—
—	—	—	—

V

元素名称	Zn	六方H	晶体结构(1)
半径 \AA (6)	1.25	1.6	电负性
半径 \AA (5)	1.38*	27.4	高发热(千卡/克·原子)(3)
原子体积	0.74(+2)	1.76	熔化热(千卡/克·原子)
密度/(克/原子)	0.2	0.27	导电(微欧) ⁽⁴⁾
第一电离能/(千卡/克·原子)	216	0.0915	导热率(卡/厘米 ² /℃/秒)(2)
			比热(卡/克·℃)
			比热(卡/克·℃)

元素周期表(二)												VIIIA														
IA		IIA		VA		VIA		VIIA		VIIIA		He		六方H		VA		VIA		VIIA		VIIIA				
0.32	2.1	—	0.106	2.08(-1)	0.014	—	—	0.73	3.5	0.72	4.0	0.71	—	—	0.93	—	0.020	—	0.005	—	0.0003	—	0.242	—		
—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	0.080		
14.1	0.004	313	3.45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
1.23	1.0	0.90	1.5	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
1.55	32.48	1.12	73.9	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
0.69(+1)	0.72	0.31(+2)	2.8	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
—	0.108	—	0.25	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
13.1	0.17	5.0	0.38	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
124	0.79	215	0.45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
Na	立方I	Mg	六方H	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
1.54	0.9	1.36	1.2	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
1.90	24.12	1.60	32.517	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
0.95(+1)	0.62	0.65(+2)	2.14	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
—	0.218	—	0.224	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
23.7	0.32	14.0	0.38	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
110	0.295	176	0.25	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
K	立方I	Ca	立方F	Sc	六方H	Ti	六方H	V	立方I	Cr	立方I	Mn	立方P	Fe	立方I	Co	六方H	Ni	立方F	Cu	六方H	Zn	六方H	Ga	正交P	
2.05	0.8	1.74	1.0	1.44	1.3	1.32	1.5	1.6	1.18	1.6	1.17	1.3	1.16	1.8	1.15	1.8	1.25	1.6	1.26	1.5	1.20	2.0	0.75	1.14	2.8	
2.35	18.9	1.97	36.74	1.62	81	1.47	106.5	1.34	106	1.30	1.27	1.26	1.25	93	1.25	91.0	1.28	72.8	1.38	2.4	1.41	1.37	68	1.40	3.34	
1.33(+1)	0.55	0.99(+2)	2.1	0.81(+5)	3.8	0.80(+2)	3.7	0.79(+3)	3.3	0.80(+2)	2.50	0.76(+2)	3.67	0.74(+2)	3.64	0.72(+2)	3.61	0.71(+1)	3.54	0.70(+1)	3.48	0.70(+1)	3.42	0.71(+1)	3.36	
—	0.143	—	0.216	—	—	0.015	0.68(+4)	0.024	0.58(+5)	0.034	0.56(+2)	0.054	0.53(+3)	0.064	0.52(+3)	0.073	0.51(+2)	0.082	0.50(+1)	0.091	0.49(+1)	0.080	0.48(+1)	0.089		
—	0.080	—	0.042	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—		
45.3	0.23	29.9	0.3	15.0	—	10.6	—	7.25	—	7.59	—	7.1	—	6.7	—	6.2	—	5.9	—	5.6	—	5.3	—	5.0	—	
100	0.177	141	0.149	151	0.13	158	0.126	156	0.11	171	0.15	142	0.11	181	0.099	176	0.105	178	0.092	173	0.0915	138	0.079	187	0.0002	
Rb	立方I	Sr	立方F	Y	六方H	Nb	立方I	Mo	立方I	Tc	六方H	Ru	六方H	Rh	立方F	Pd	立方F	Ag	立方F	Cd	六方H	In	立方P	Sn	四方R	
2.16	0.8	1.91	1.0	1.62	1.3	1.34	1.5	1.30	1.26	1.27	1.25	2.2	1.25	1.24	1.23	1.28	2.2	1.34	1.24	1.26	1.22	1.20	1.19	1.36	2.1	
2.48	18.1	2.15	35.8	1.76	83	1.60	120	1.45	128	1.36	120	1.34	127	1.34	127	1.37	120	1.37	120	1.37	120	1.37	120	1.37	120	1.37
1.48(+1)	0.55	1.13(+2)	2.1	0.83(+3)	2.7	0.80(+4)	4.6	0.70(+5)	6.4	—	5.5	0.69(+3)	6.1	0.66(+2)	5.2	0.86(+2)	4.0	—	5.4	0.67(+2)	5.0	0.67(+2)	5.2	0.67(+2)	5.0	
—	0.080	—	0.042	—	—	0.016	—	0.024	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	
55.9	—	33.7	—	15.8	—	10.8	—	8.22	—	8.3	—	8.3	—	8.21	—	8.17	—	8.17	—	8.17	—	8.17	—	8.17	—	
70	—	39	—	22.5	0.033	13.6	0.022</																			

元素周期表(一)

5Y

IA	
1	1.00797
-252.7	1
-259.2	H
0.071	
1s ¹	0.3741
Hydrogen 氢	
IIA	
3	6.941
1330	1
180.5	2
0.53	Li
1.74	Be
1s ² 2s ¹	0.203
Lithium 锂	Beryllium 镁
11	22.9898
892	1
97.8	2
0.97	Na
1.74	Mg
[Ne]3s ¹	3s ² 3p ¹ 5375
Sodium 钠	Magnesium 镁
IIIB	
21	44.956
760	2
63.7	Sc
0.86	Ca
1.55	4.51
[Ar]3d ¹ 4s ¹	1.23
Potassium 钾	Calcium 钙
IVB	
22	47.90
2730	3
1539	3260
838	4.3
1.55	Ti
5.0	1875
[Ar]3d ¹ 4s ¹	1.23
Rubidium 钠	Scandium 钛
VB	
23	50.942
3450	5, 4, 3, 2
2665	6, 3, 2
1900	2150
1875	7, 6, 4, 2, 3
Cr	1245
7.19	1536
[Ar]3d ¹ 4s ¹	1.23
Cobalt 钴	Vanadium 钛
VIB	
24	51.996
3000	5, 4, 3, 2
2900	2, 3
1453	1495
Fe	8.9
7.86	7.43
[Ar]3d ¹ 4s ¹	1.23
Iron 铁	Chromium 钛
VIIIB	
25	54.938
26	55.847
3000	2, 3
2730	2, 3
1453	1495
Co	8.9
8.9	7.43
[Ar]3d ¹ 4s ¹	1.23
Nickel 镍	Iron 铁
IB	
26	58.71
29	63.54
3000	2, 3
2730	2, 3
1453	1495
Fe	8.9
8.9	7.43
[Ar]3d ¹ 4s ¹	1.23
Copper 铜	Nickel 镍
IIB	
27	58.9
29	65.37
30	65.37
2900	2, 3
2730	2, 3
1453	1495
Co	8.9
8.9	7.43
[Ar]3d ¹ 4s ¹	1.23
Zinc 锌	Copper 铜
Aluminum 铝	
28	58.71
29	63.54
30	65.37
2730	2, 3
1453	1495
Co	8.9
8.9	7.43
[Ar]3d ¹ 4s ¹	1.23
Gallium 镓	Aluminum 铝
Silicon 硅	
29	63.54
30	65.37
2730	2, 3
1453	1495
Co	8.9
8.9	7.43
[Ar]3d ¹ 4s ¹	1.23
Phosphorus 磷	Silicon 硅
Sulphur 硫	
30	65.37
31	69.72
32	72.59
33	74.922
34	78.96
35	79.904
36	83.80
2237	3
230.8	4
937.4	8.96
5.91	7.14
[Ar]3d ¹ 4s ¹	1.23
As	Zn
Germanium 镉	
31	69.72
32	72.59
33	74.922
34	78.96
35	79.904
36	83.80
2237	3
230.8	4
937.4	8.96
5.91	7.14
[Ar]3d ¹ 4s ¹	1.23
Ge	Zn
Arsenic 砷	
32	72.59
33	74.922
34	78.96
35	79.904
36	83.80
2237	3
230.8	4
937.4	8.96
5.91	7.14
[Ar]3d ¹ 4s ¹	1.23
Se	As
Selenium 溴	
33	74.922
34	78.96
35	79.904
36	83.80
2237	3
230.8	4
937.4	8.96
5.91	7.14
[Ar]3d ¹ 4s ¹	1.23
Kr	As
Bromine 溴	
34	78.96
35	79.904
36	83.80
2237	3
230.8	4
937.4	8.96
5.91	7.14
[Ar]3d ¹ 4s ¹	1.23
Kr	Br
Iodine 碘	
35	79.904
36	83.80
2237	3
230.8	4
937.4	8.96
5.91	7.14
[Ar]3d ¹ 4s ¹	1.23
Iodine 碘	Iodine 碘
Xenon 氩	
36	83.80
37	100.904
38	120.904
39	131.30
40	142.904
41	153.30
42	163.904
43	173.904
44	183.904
45	193.904
46	203.904
47	213.904
48	223.904
49	233.904
50	243.904
51	253.904
52	263.904
53	273.904
54	283.904
55	293.904
56	303.904
57	313.904
58	323.904
59	333.904
60	343.904
61	353.904
62	363.904
63	373.904
64	383.904
65	393.904
66	403.904
67	413.904
68	423.904
69	433.904
70	443.904
71	453.904
72	463.904
73	473.904
74	483.904
75	493.904
76	503.904
77	513.904
78	523.904
79	533.904
80	543.904
81	553.904
82	563.904
83	573.904
84	583.904
85	593.904
86	603.904
87	613.904
88	623.904
89	633.904
90	643.904
91	653.904
92	663.904
93	673.904
94	683.904
95	693.904
96	703.904
97	713.904
98	723.904
99	733.904
100	743.904
101	753.904
102	763.904
103	773.904
104	783.904
Fr	—
Re	—
Ac*	—
Radium 钔	Actinium 钔
Thorium 钔	Protactinium 钔
Uranium 钔	Neptunium 钔
Plutonium 钔	Americium 钔
Curium 钔	Berkelium 钔
Bekelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium 钔
Neptunium 钔	Plutonium 钔
Plutonium 钔	Americium 钔
Americium 钔	Curium 钔
Curium 钔	Berkelium 钔
Berkelium 钔	Californium 钔
Californium 钔	Einsteinium 钔
Einsteinium 钔	Fermium 钔
Fermium 钔	Mendeleyev 钔
Mendeleyev 钔	Nobelium 钔
Nobelium 钔	Lanthanum 钔
Lanthanum 钔	Actinium 钔
Actinium 钔	Thorium 钔
Thorium 钔	Protactinium 钔
Protactinium 钔	Uranium 钔
Uranium 钔	Neptunium

Si 的晶胞常数及其热膨胀数据

晶胞参数: $a = 5.43054 \pm 0.00017 \text{ \AA}$ ($\pm 25^\circ \text{C}$ 时)

* 原数据修正值: $a = 5.430646 \text{ \AA}$

热膨胀数据:

温度 (°C)	30	166	285	387	618	740	860
$a (\text{\AA})$	5.42197	5.42262	5.42482	5.42701	5.43283	5.43696	5.44122

根据上表的实验结果, 利用下面的公式求之:

$$a_t = a_0 (1 + \alpha t + \beta t^2 + \gamma t^3 + \delta t^4)$$

这里 a_0 和 a_t 分别为在 0°C 和 $t^\circ \text{C}$ 的晶胞常数。求得:

$\alpha \approx 0 \sim 900^\circ \text{C}$ 之间。

$\alpha = 3.893 \times 10^{-6}$; $\beta = -2.101 \times 10^{-9}$; $\gamma = 5.125 \times 10^{-12}$; $\delta = -1.833 \times 10^{-15}$

参考: #633 杂志 Vol. 20, No. 8, (1964) 701. (青浦、刘益民)

X-ray Measurement of the Thermal expansion of Germanium, Silicon, Indium, Antimony and Gallium
A. R. SENDE Vol. 31V, No. 11, 1965, 1582

5-565 ASTM 253.5. Si

θ	d_{hkl}	l_{hkl}	h_{hkl}	θ	d_{hkl}	l_{hkl}	h_{hkl}	θ	d_{hkl}	l_{hkl}	h_{hkl}
38.4, 10.22	3.138	100	111	38.22, 12.69	1.246	13		57.14	2.9178	11	
120.23, 6.67	1.920	60	220	41.08, 13.033	17			63.88	0.8766	9	
37.428, 7	1.638	35	311	47.53, 1.0460	9			68.58	0.8281	5	
77.346, 1.357	8			53.03, 0.9999	5						

006

NaCl.

Table of ϵ , $\alpha (10^{-5} \text{ K}^{-1})$, and coefficients of linear expansion

温度 (°C)	$\epsilon (10^{-5})$	$\alpha (10^{-5} \text{ K}^{-1})$	温度 (°C)	$\epsilon (10^{-5})$	$\alpha (10^{-5} \text{ K}^{-1})$
-250	-766	0.3	100	329	42.3
-225	-758	7.3	200	766	44.2
-200	-726	18.2	300	1233	48.3
-150	-604	28.2	400	1733	51.9
-100	-445	33.8	500	2272	56.1
-50	-268	36.8	600	2852	60.9
0	-79	38.9	700	3492	67.3
20	0	39.7	800	4207	74.1

甲苯: 密度: Toluene

20°C . $\rho = 0.866 \text{ g/cm}^3$.

$V = V_0 (1 + \beta \Delta t)$, $\beta = 11 \times 10^{-4}$.

or. $\frac{V}{V_0} = \frac{1}{\rho_0} (1 + \beta \Delta t)$

$V_0 = 1.1299$

$\rho_0 = 0.865 \pm 2 \text{ g/cm}^3$

计算: $\rho = \frac{M_r Z}{V N}$. $N = 6.024 \times 10^{23}$

有机标准物质相变温度(°C) ^[13]			
化合物	相变性质	单斜相变温度	熔沸点温度
对氯苯酚	固-液	51.5	51.5
乙酰乙酸	固-固	71.4	
荼	固-液	80.3	80.4
二甲基苯	固-固	110.4	
苯甲酸	固-液	122.4	122.1
己二酸	固-液	141.4	141.0
茴香醇	固-液	183.0	183.1
2-氯蒽醌	固-液	209.1	209.4
2-溴丁酸	固-液	245.3	245.2
溴醚	固-液	280.6	283.9

不同温度校正热量的物质和焓变值^[14]

物质	相变 温度 (°C)	相变 性质	热焓变化 (J/g)	物质	相变 温度 (°C)	相变 性质	热焓变化(J/g)
H ₂ O	0	S-L	333.89	联苯	69.8	S-L	628.11
NH ₄ NO ₃	32	S-S	19.87	荼	80.3	S-L	149
CBr ₄	47	S-S	20.13	茚	99.3	S-L	104.63
二苯酮	98.2	S-L	98.35	邻二硝基苯	114	S-L	135.18
硬脂酸	69	S-L	198.79	安息香酸	121.8	S-L	141.87

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物质	相变 温度 (°C)	相变 性质	热焓变化(J/g)	物质	相变 温度 (°C)	相变 性质	热焓变化(J/g)
苯甲酸	122.4	S-L	108	KClO ₃	299.8	S-S	99.18
NH ₄ NO ₃	125	S-S	52.74	NaNO ₃	306.2	S-L	194.7; 184.98
KNO ₃	129	S-S	49.97; 53.03	Cd	320.9	S-L	53.99; 54.49;
AgI	154	S-S	26.21				55.96; 54.90;
In	157	S-L	28.5	Pb	327.5	S-L	22.6; 23.02; 24.69
AgNO ₃	160	S-S	14.65; 15.02	KNO ₃	335	S-L	98.35; 117.60
RbNO ₃	166	S-S	26.96	Na ₂ Cr ₂ O ₇	345	S-L	134.97
NH ₄ NO ₃	169.6	S-L	79.78	K ₂ Cr ₂ O ₇	395	S-L	137.28
季戊四醇	187.8	S-L	322.66	Zn	419.4	S-L	102.13; 108.90;
							113
NH ₄ Cl	196	S-S	83.71	Ag ₂ SO ₄	427	S-S	52.94; 54.82;
AgNO ₃	211	S-L	678; 71.56				56.65
RbNO ₃	228	S-S	18.45	CsCl	~440	S-S	148.2; 17.16
Sn	231.9	S-L	59.00; 59.70 59.99; 60.21; 60.69	PbCl ₂	498	S-L	87.47
				LiBr	553	S-L	150.66
				SiO ₂	573	S-S	5.99; 6.58
LiNO ₃	252	S-L	370.37	Li ₂ SO ₄	575	S-S	249.47; 307.41
Bi	271	S-L	50.22; 52.00 50.20; 53.79	Na ₂ WO ₄	528.8	S-S	119.5
RbNO ₃	278	S-S	9.93	Al	660	S-L	396; 400.9
				K ₂ Cr ₂ O ₇	667.3	S-S	35.66
				Ag	960.8	S-L	105
				Au	1063.0	S-L	62.8

标准物质相变温度 (°C)^[12]

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标准物质	相变性质	平衡相变 温度	ICTA 标准试验	
			升维始偏点	峰值
KNO ₃	固-固	127.7	128±5	135
In	固-液	157	154±6	159
Sn	固-液	231.9	230±5	237
KClO ₄	固-固	299.5	299±6	309
Pb	固-液	327.5		
Zn	固-液	419.6		
Ag ₂ SO ₄	固-固	424	424±7	433
SiO ₂	固-固	573	571±5	574
K ₂ SO ₄	固-固	583	582±7	588
Al	固-液	660.4		
K ₂ CrO ₄	固-固	665	665±7	673
BaCO ₃	固-固	810	808±8	819
SrCO ₃	固-固	925	928±7	938
Ge	固-液	937.4		
Ag	固-液	961.9		
Au	固-液	1060.4		
Cu	固-液	1083.4		
Si	固-液	1410		
Ni	固-液	1453		
Fe	固-液	1535		

Magnetic moment calculation.

$$I_N = C \frac{m_{BKR} A_{BKR}}{\sin \theta \cos \theta} |F_N(\tau)|^2$$

$$F_N = \sum_{j=1}^N b_j e^{i\tau r_j} e^{-W_j} = \sum_{j=1}^N b_j \exp(2\pi i (\hat{A}x_j + \hat{B}y_j + \hat{C}z_j))$$

$$I_M = C \left(\frac{re^2}{2mc^2} \right)^2 \frac{m_{BKR}}{\sin \theta \cos \theta} |F_M(\tau)|^2 <1 - (\hat{C} \cdot \hat{M})^2>$$

$$F_M = \sum_{j=1}^N \langle M_j \rangle_j f_j(\tau) \exp(2\pi i (\hat{A}x_j + \hat{B}y_j + \hat{C}z_j))$$

$$\text{Method 1: } \langle M_f \rangle^2 = \frac{I_M \cdot m_{BKR} \cdot F^2 N}{(2.27 \times 10^{-12})^2 m_{BKR} \cdot (\sum F_m) \cdot (1 - (\hat{C} \cdot \hat{M})^2) \cdot I_N}$$

$$\text{Method 2. ① } C = I_N \sin \theta \cos \theta / m_{BKR} A_{BKR} F_N^2$$

$$\text{② } \langle M_f \rangle^2 = \frac{1}{I_N \sin \theta \cos \theta} \left[\frac{I_M \sin \theta \cos \theta / (2.27 \times 10^{-12})^2 F_m \cdot m \cdot A_{BKR}}{m_{BKR} A_{BKR} F_N^2} \right] \left(\frac{re^2}{2mc^2} \right)^2$$

$$= \frac{m_{BKR} A_{BKR} F_N^2 \cdot I_N \sin \theta \cos \theta}{(2.27 \times 10^{-12})^2 \cdot (1 - (\hat{C} \cdot \hat{M})^2) \cdot \sum F_m \cdot m \cdot A_{BKR} \cdot \sin \theta \cos \theta \cdot I_N}$$

$$= \frac{I_M F_N^2 m_{BKR}}{\left(\frac{re^2}{2mc^2} \right)^2 \cdot \underbrace{(1 - (\hat{C} \cdot \hat{M})^2)}_{\approx 20} \cdot 2 F_m \cdot I_N}$$

$$(2.27 \times 10^{-12})^2 \approx 0.0729$$

$$+ I_N G_SAS. F_{CSq}^2 = \left(\frac{re^2}{2mc^2} \right)^2 |F_M(\tau)|^2 <1 - (\hat{C} \cdot \hat{M})^2>$$

纪念物的折射率计算经验公式.

$$n = 1 + d \sum j k_j. \quad j \text{为分子数, } k \text{为折射系数, } d \text{常数.}$$

氧化物	分子数	k_i	氧化物	分子数	k_i
H ₂ O	18	0.34	Y ₂ O ₃	226	0.14
Li ₂ O	30	0.31	La ₂ O ₃	326	0.15
Na ₂ O	62	0.18	Bi ₂ O ₃	464	0.16
K ₂ O	94	0.19	Cl ₂	44	0.22
BeO	25	0.24	SiO ₂	60	0.21
MgO	40	0.20	TiO ₂	80	0.40
CaO	56	0.23	ZrO ₂	123	0.20
SrO	104	0.14	SnO ₂	151	0.15
BaO	153	0.13	N ₂ O ₅	108	0.24
PbO	223	0.15	P ₂ O ₅	142	0.19
B ₂ O ₃	70	0.22	Nb ₂ O ₅	268	0.30
Al ₂ O ₃	102	0.20	SO ₃	80	0.18

The probable error for the value of weight w_j is

$$p_{w_j} = \pm 0.6745 \sqrt{\frac{\sum w_i d_i^2}{(n-1)w_j}}$$

and for the weighted average

$$P_w = \pm 0.6745 \sqrt{\frac{\sum w_i d_i^2}{(n-1)\sum w_i}}$$

It is possible to determine the relative weights to be attached to the individual measurements since the weight w_i is inversely proportional to $p_{w_i}^2$. The usual custom is to assign weights arbitrarily.

13.35. Probable Error of a Function.—In general the results of several independently measured quantities are combined to give the final value of the physical constant desired. Suppose X, Y, \dots have been obtained as the average value of certain quantities with probable errors P_X, P_Y, \dots . If they are combined to give Z , where

$$Z = f(X, Y, \dots)$$

then its probable error is

$$P = \sqrt{(P_X \partial Z / \partial X)^2 + (P_Y \partial Z / \partial Y)^2 + \dots}$$

We record a few special cases for convenience of reference.

1. $Z = X \pm Y; \quad P = \pm \sqrt{P_X^2 + P_Y^2}$
2. $Z = XY; \quad P = \pm \sqrt{(XP_Y)^2 + (YP_X)^2}$
3. $Z = X/Y; \quad P = \pm \frac{1}{Y^2} \sqrt{Y^2 P_X^2 + X^2 P_Y^2}$

4. $Z = a + bX$. Suppose we know the value Z_1 with its probable error p_1 at the point $X = X_1$ and Z_2 with error p_2 at $X = X_2$. We wish to fit the two points to a linear equation. Then

$$P_a = \sqrt{\left(\frac{X_2 p_1}{X_2 - X_1}\right)^2 + \left(\frac{X_1 p_2}{X_1 - X_2}\right)^2}$$

$$P_b = \sqrt{\left(\frac{p_1}{X_1 - X_2}\right)^2 + \left(\frac{p_2}{X_2 - X_1}\right)^2}$$

$$P_Z = \sqrt{\left(\frac{p_1(X_2 - X)}{(X_2 - X_1)}\right)^2 + \left(\frac{p_2(X_1 - X)}{(X_1 - X_2)}\right)^2}$$

where P_a, P_b and P_Z are the probable errors in a, b and Z , respectively.

Table I (cont.)

ION	EC	CN	SP	CR	*18*	ION	EC	CN	SP	CR	*18*	ION	EC	CN	SP	CR	*18*	
N+1 ZP + IV	1.13	.99				PR+3 AF 2 VI	1.13	.99				TC+4 -D 2 VI			.785	.645		
V	1.14	1.00					VII	1.266	1.125				TC+5 -D 2 VI			.74	.60	EX
V	1.16	1.02					VII	1.319	1.174				TC+7 -P 2 VI			.51	.37	
VII	1.26	1.12				PR+4 AF 1 VI	1.13	.95	.85	E		TE+2 SP 2 VI			.70	.56	E	
VII	1.32	1.18				VII	1.10	.96	E			TE+4 SS 2 VII			2.07	2.21	P	
IX	1.38	1.24	C			PR+2 SD 8 IVSQ	.74	.80				VII			.48	.52		
XII	1.53	1.39				VII	.94	.60	X			VII			.48	.52		
NB+2 -D 2 VI	.86					PR+4 SD 6 VI	.785	.625	X			VII			.48	.52		
NB+4 -D 1 VI	.82	1.08	E			VII	.71	.57	X			VII			.57	.43	C	
VII	.93	.79				PR+3 SD 5 VI	1.14	1.00	X			VII			.70	.56		
NB+5 -P 4 VI	.82	1.08	C			PR+4 SF 4 VI	1.00	.86	X			VII			.58	.44		
VII	.78	.65				VII	1.10	.96	X			VII			.48	.52		
VII	.83	.69	C			PR+5 SF 3 VI	.88	.74	E			VII			.48	.52		
VII	.88	.76				VII	.85	.71	E			VII			.48	.52		
ND+2 AF 4 VII	1.43	1.29				VII	1.62	1.48	E			VII			.48	.52		
IX	1.49	1.35				VII	1.66	1.52	X			TII+2 3D 2 VI			.135	.135	C	
ND+3 AF 3 VII	1.23	.983	E			VII	1.70	1.56				TII+3 3D 2 VI			1.00	.88	E	
VII	1.249	1.109	**			VII	1.75	1.61				TII+4 3P 2 VI			.56	.42	G	
IX	1.303	1.183	E			VII	1.77	1.63	E			VII			.45	.51	C	
XII	1.41	1.27	E			VII	1.80	1.68				VII			.45	.51	C	
NII+2 3D 8 IV	.89	.55				VII	1.83	1.69				VII			.745	.605	**	
VII	.83	.48				VII	1.86	1.72				VII			.76	.60		
VII	.77	.63	E			VII	1.97	1.83	E			VII			1.50	1.50	E	
VII	.830	1.090	**			VII	1.98	1.83	E			VII			1.59	1.59	E	
NII+1 3D 7 VI	L5	.70	.58	**		VII	2.00	1.88	E			VII			1.64	1.70	RE	
NII+2 3D 6 VI	L5	.62	.48			VII	2.04	1.91				VII			.89	.75		
NII+2 5T1N VI	1.24	1.11				VII	2.07	1.93				VII			1.225	.889	A	
NII+2 5T 5 VI	1.24	1.10				VII	2.07	1.93				VII			1.12	.98	C	
NII+2 5T 6 VI	1.15	1.01				VII	2.07	1.93				VII			1.07	.94	C	
NII+2 5T 2 VII	1.01	.87				VII	2.07	1.93				VII			1.07	.94	C	
NII+2 5T 1 VII	1.12	.89				VII	2.07	1.93				VII			1.07	.94	C	
NII+5 ST 2 VI	.89	.75				VII	2.07	1.93				VII			1.07	.94	C	
NII+5 ST 1 VI	.88	.72				VII	2.07	1.93				VII			1.07	.94	C	
NII+7 ST 2 VI	.85	.71				VII	2.07	1.93				VII			1.07	.94	C	
D-2 2P 4 VII	1.21	1.35	?			VII	2.07	1.93				VII			1.07	.94	C	
III	1.22	1.36				VII	2.07	1.93				VII			1.07	.94	C	
IV	1.25	1.38				VII	2.07	1.93				VII			1.07	.94	C	
VII	1.26	1.40				VII	2.07	1.93				VII			1.07	.94	C	
VII	1.28	1.42				VII	2.07	1.93				VII			1.07	.94	C	
D-1	1.18	1.32				VII	2.07	1.93				VII			1.07	.94	C	
III	1.20	1.34				VII	2.07	1.93				VII			1.07	.94	C	
IV	1.21	1.35	E			VII	2.07	1.93				VII			1.07	.94	C	
VII	1.23	1.37	E			VII	2.07	1.93				VII			1.07	.94	C	
DS+4 SD 6 VI	.770	.570	**			VII	2.07	1.93				VII			1.07	.94	C	
DS+4 SD 3 VI	.715	.575	E			VII	2.07	1.93				VII			1.07	.94	C	
DS+4 SD 2 VI	.671	.545	E			VII	2.07	1.93				VII			1.07	.94	C	
DS+7 SD 1 VI	.663	.545	E			VII	2.07	1.93				VII			1.07	.94	C	
DS+7 SD 6 IV	.53	.39				VII	2.07	1.93				VII			1.07	.94	C	
F-1 3S 2 VI	.58	.44				VII	2.07	1.93				VII			1.07	.94	C	
F-5 2P 4 VI	.31	.17	*			VII	2.07	1.93				VII			1.07	.94	C	
PR+2 2P 6 IV	.43	.29				VII	2.07	1.93				VII			1.07	.94	C	
VII	.52	.38	C			VII	2.07	1.93				VII			1.07	.94	C	
PR+2 SF 2 VI	1.18	1.04	E			VII	2.07	1.93				VII			1.07	.94	C	
PR+2 SD 1 VI	1.04	.90	E			VII	2.07	1.93				VII			1.07	.94	C	
VII	1.15	1.01				VII	2.07	1.93				VII			1.07	.94	C	
PR+3 AF 6 VI	.92	.78				VII	2.07	1.93				VII			1.07	.94	C	
VII	1.05	.91				VII	2.07	1.93				VII			1.07	.94	C	
IX	1.09	.95				VII	2.07	1.93				VII			1.07	.94	C	
PR+2 AS 2 IVPT	1.12	.98	C			VII	2.07	1.93				VII			1.07	.94	C	
VII	1.33	1.19				VII	2.07	1.93				VII			1.07	.94	C	
VII	1.37	1.23	C			VII	2.07	1.93				VII			1.07	.94	C	
VII	1.43	1.29	C			VII	2.07	1.93				VII			1.07	.94	C	
VII	1.49	1.35	C			VII	2.07	1.93				VII			1.07	.94	C	
VII	1.54	1.30	C			VII	2.07	1.93				VII			1.07	.94	C	
XI	1.59	1.42	C			SA+2 AF 6 VI	1.32	1.18				VII			1.22	1.18	C	
XII	1.61	1.49				VII	1.35	1.21				VII			1.28	1.14		
VII	.79	.65	E			VII	1.40	1.26				VII			1.058	.868	**	
VII	.87	.73	E			VII	1.45	1.31				VII			1.065	.925	E	
VII	.915	.775	E			A	1.50	1.30	C			VII			1.125	.985	E	
VII	1.06	.86	R			VII	1.58	1.44	C			VII			1.182	1.042	R	
VII	.73	.59				VII	.86	.72	E			VII			.74	.60	*	
PD+2 -D 4 II	.78	.66				VII	.82	.68				VII			.62	.48	*	
PD+2 -D 8 IVSQ	1.00	.86				VII	.78	.64				VII			.840	.740	**	
PD+2 -A 2 VI	.90	.76				VII	.83	.69				VII			1.04	.90	C	
PD+2 -A 0 VI	.755	.615	R			VII	.88	.74				VII			.73	.59	R	
PD+3 -B 4 VI	1.11	.97	R			VII	1.063	.923	R			VII			.80	.66	C	
VII	1.233	1.093	R			VII	1.12	.98	E			VII			.86	.72	*	
VII	1.284	1.144	R			VII	1.180	1.040	R			VII			.92	.78	*	
VII	1.22	1.08	R			VII	1.235	1.095	R			VII			.98	.84	*	
PD+4 SD 10 VI	.81	.67	A			VII	1.02	.88				VII			1.03	.89		

标准物质相变温度(°C)^[12]

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标准物质	相变性质	平衡相变 温度	ICTA 标准试验 升始偏点	峰值
KNO ₃	固-固	127.7	128±5	135
In	固-液	157	154±6	159
Sn	固-液	231.9	230±5	237
KClO ₄	固-固	299.5	299±6	309
Pb	固-液	327.5		
Zn	固-液	419.6		
Ag ₂ SO ₄	固-固	424	424±7	433
SiO ₂	固-固	573	571±5	574
K ₂ SO ₄	固-固	583	582±7	588
Al	固-液	660.4		
K ₂ CrO ₄	固-固	665	665±7	673
BaCO ₃	固-固	810	808±8	819
SrCO ₃	固-固	925	928±7	938
Ge	固-液	937.4		
Ag	固-液	961.9		
Au	固-液	1060.4		
Cu	固-液	1083.4		
Si	固-液	1410		
Ni	固-液	1453		
Fe	固-液	1535		

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指 标 特 性 物 质 相 变 温 度 (°C) [6]

物 质	相 变 性 质	相 变 温 度	相 变 温 度 (度)
水合物	相 变 性 质	相 变 温 度	相 变 温 度 (度)
对氨基苯酚	固 - 液	51.5	51.5
丙酮乙酸	固 - 固	71.4	
苯	固 - 液	80.3	80.4
2-甲基苯	固 - 固	110.2	
苯甲酸	固 - 液	122.4	122.4
乙二酸	固 - 液	123.4	123.4
丙二酸	固 - 液	151.4	151.0
葡萄糖	固 - 液	183.0	183.1
2-氯苯酚	固 - 液	209.1	209.4
D-甘油	固 - 液	245.3	245.2
蔗糖	固 - 液	250.6	253.9

不同温度下物质的物理和化学性质 [6]

物 质	相 变 性 质 (ΔT_f)	物 质	相 变 性 质 (ΔT_f)
H ₂ O	0	S-L	333.89
UH ₄ NO ₃	32	S-S	19.87
CBr ₄	47	S-S	20.13
二苯酮	68.2	S-L	98.35
碘仿	69	S-L	109.79

物 质	相 变 性 质 (ΔT_f)	物 质	相 变 性 质 (ΔT_f)
S _n	231.9	S-L	510.0; 71.56
RbNO ₃	228	S-S	18.05
AgNO ₃	211	S-L	6787; 71.56
LiCl ₂	228	PbCl ₂	498
Li ₂ SO ₄	231.9	LiBr	553
LiNO ₃	252	S-L	370.37
B ₂	271	S-L	502.5; 32.00
RbNO ₃	278	S-S	9.93
Au	103.0	S-L	141.27

L_1^{+}	6	> 6.5	5	80	6	23	N_{d}^{+}	6	126	P_b^{+}	$4Py$	112	
2_{1}^{+}	6	7	6	86	7	87	N_{e}^{-}	4	132	O_{H}^{-}	2	187	
K_{1}^{+}	4	> 1	2	> 1	N_{e}^{-}	4	N_{d}^{+}	9	$H_{O,3}$	3	120	8	
M_{1}^{+}	1	> 2	M_{d}^{2+}	445	> 2	N_{e}^{+}	6	30	$H_{O,3}$	3	143		
M_{1}^{+}	7	> 6	M_{d}^{2+}	445	> 2	N_{e}^{+}	3	44	A_{L}^{+}	4	121		
M_{1}^{+}	8	> 1	613	87	6	27	N_{d}^{+}	6	123	Q_{S}	10	174	
M_{1}^{+}	9	> 9	M_{d}^{2+}	97	N_{d}^{+}	4	113	N_{d}^{+}	5	D_{S}^{a+}	6	179	
M_{1}^{+}	10	> 2	745	104	5	114	N_{d}^{+}	6	83	D_{S}^{a+}	6	179	
M_{1}^{+}	12	> 5	8	110	6	116	N_{d}^{+}	6	> 1.5	C_{S}^{a+}	5	182	
L_{∞}^{3+}	6	> 7.2	M_{d}^{2+}	5	> 2	7	> 26	N_{d}^{+}	> 2	P_{d}^{+}	4	179	
L_{∞}^{3+}	7	> 4	613	> 2	8	132	N_{d}^{+}	6	> 2	P_{d}^{+}	5	187	
L_{∞}^{3+}	8	> 3	M_{d}^{2+}	> 5	9	> 38	N_{d}^{+}	6	> 2	P_{d}^{+}	6	195	
L_{∞}^{3+}	9	> 2.6	M_{d}^{2+}	4	> 3	12	> 53	N_{d}^{+}	6	> 2	P_{d}^{+}	8	198
L_{∞}^{3+}	10	> 1.4	M_{d}^{2+}	6	67	M_{d}^{3+}	6	86	P_{d}^{+}	4	P_{d}^{+}	124	
L_{∞}^{3+}	12	> 1.5	M_{d}^{2+}	4	47	M_{d}^{3+}	6	82	P_{d}^{+}	101	P_{d}^{+}	124	
L_{∞}^{3+}	14	> 1.3	M_{d}^{2+}	4	> 95	8	> 93	N_{d}^{+}	8	> 1.2	P_{d}^{+}	6	190
L_{∞}^{3+}	6	> 90	M_{d}^{2+}	4	39	N_{d}^{+}	4	62	P_{d}^{+}	6	P_{d}^{+}	62	
L_{∞}^{3+}	8	> 6	M_{d}^{2+}	6	60	6	> 78	M_{d}^{3+}	6	P_{d}^{+}	6	188	
L_{∞}^{3+}	6	> 10.1	M_{d}^{2+}	6	83	7	> 83	M_{d}^{3+}	6	P_{d}^{+}	6	188	
M_{1}^{2+}	8	> 11.7	M_{d}^{2+}	6	79	8	> 88	M_{d}^{3+}	8	P_{d}^{+}	6	183.3	
M_{1}^{2+}	9	> 17.2	M_{d}^{2+}	4	60	N_{d}^{2+}	8	> 103	P_{d}^{+}	3	P_{d}^{+}	104.7	
M_{1}^{2+}	4	> 1	6	24	9	> 149	N_{d}^{2+}	4	> 124	P_{d}^{+}	9	> 109	

V^{4+}	5	67		8	112.5		
	6	72		9	118.2		
	8	85	Zn^{2+}	4	74		
V^{5+}	4	49.5		5	82		
	5	60		6	88		
	6	68		8	100		
W^{6+}	6	80	Zr^{4+}	4	73		
W^{5+}	6	76		5	80		
W^{6+}	4	56		6	86		
	5	65		7	92		
	6	72		8	98		
Xe^{8+}	4	58		9	103		
	6	62					
Y^{3+}	6	102					
	7	110					
	8	117.9					
	9	121.5					
Yb^{2+}	6	116					
	7	122					
	8	128					
Yb^{3+}	6	100.8					
	7	106.5					

註 R. D. Shannon, Acta Crystallogr., A32, 751 (1976). (b). SQ 在 Li_2O
 Al_2O_3 , (c) PYT, (d) ZnCl₂, (e) H₂O, (f) LiOH 水溶液中, (g) LS 在水的低自旋状态。

离子	G	P	L	离子	G	P	L
H^-	1.54	2.08	1.39	O^{2-}	1.32	1.40	1.25
F^-	1.33	1.36	1.19	S^{2-}	1.74	1.84	1.70
Cl^-	1.81	1.81	1.70	Se^{2-}	1.91	1.98	1.81
Br^-	1.96	1.95	1.87	Te^{2-}	2.11	2.21	1.97
I^-	2.20	2.16	2.12				
Li^+	0.78	0.60	0.86	Co^{2+}	0.82	0.74	0.88
Na^+	0.98	0.95	1.12	Ni^{2+}	0.68	0.69	-
K^+	1.33	1.33	1.04	Cu^{2+}	0.72	-	-
Rb^+	1.49	1.48	1.58	Bi^{3+}	0.2	0.2	-
Cs^+	1.65	1.69	1.84	Al^{3+}	0.45	0.50	-
Cu^+	0.95	0.96	-	Sc^{3+}	0.68	0.83	-
Ag^+	1.13	1.26	1.27	Y^{3+}	0.90	0.93	-
Au^+		1.37	-	La^{3+}	1.04	1.14	-
Tl^+	1.49	1.40	1.51	Ga^{3+}	0.60	0.62	-
NH^+		1.48	1.66	Zn^{3+}	0.81	0.81	-
Be^{2+}	0.34	0.31	-	Tl^{3+}	0.91	0.95	-
Mg^{2+}	0.78	0.65	0.87				
Ca^{2+}	1.06	0.99	1.18	Fe^{3+}	0.83	-	-
Sr^{2+}	1.27	1.13	1.32	Cr^{3+}	0.53	-	-
Ba^{2+}	1.43	1.35	1.49				
Ra^{2+}		1.40	1.57	C^{4+}	0.15	0.15	-
Zn^{2+}	0.69	0.70	-	Si^{4+}	0.38	0.41	-
Cd^{2+}	1.03	0.97	1.14	Ti^{4+}	0.60	0.68	-
Hg^{2+}	0.93	1.10	-	Zr^{4+}	0.77	0.86	-
				Ge^{4+}	0.87	1.01	-
Pb^{2+}	1.17	1.21	-	Ge^{6+}	0.14	0.13	-
Mn^{2+}	0.91	0.80	0.93	Sn^{4+}	0.71	0.71	-
Fe^{2+}	0.83	0.76	0.90	Pb^{4+}	0.81	0.84	-