

Phenomenology of exotic hadron and heavy quarkonium in heavy-ion collisions

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Outline

1. Production of charmed hadrons: D , $X(3872)$, B_c , J/ψ

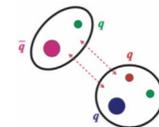
D meson spectrum ($c - \bar{q}$)

J/ψ spectrum ($c - \bar{c}$)

B_c production ($c - \bar{b}$)

$X(3872)$ as a tetraquark: $c + \bar{c} + q + \bar{q} \rightarrow X(3872)$ **in QGP**

as a meson molecule: $c + \bar{q} \rightarrow D$, $D^0 + \bar{D}^{*0} \rightarrow X(3872)$ **in hadronic gas**



2. Heavy flavor spin dynamics

3. Summary

Heavy quark dynamical evolution

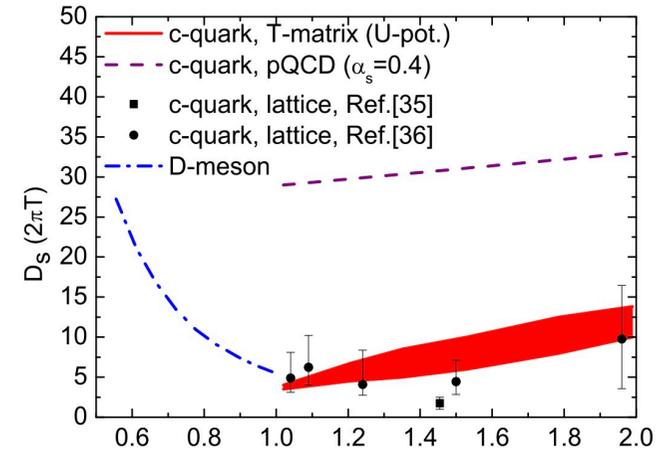
$$\frac{d\vec{p}}{dt} = -\eta\vec{p} + \vec{\xi} + f_g$$

$$\eta = \kappa/(2TE) \quad \kappa D_s = 2T^2$$

$$D_s(2\pi T) = 5$$

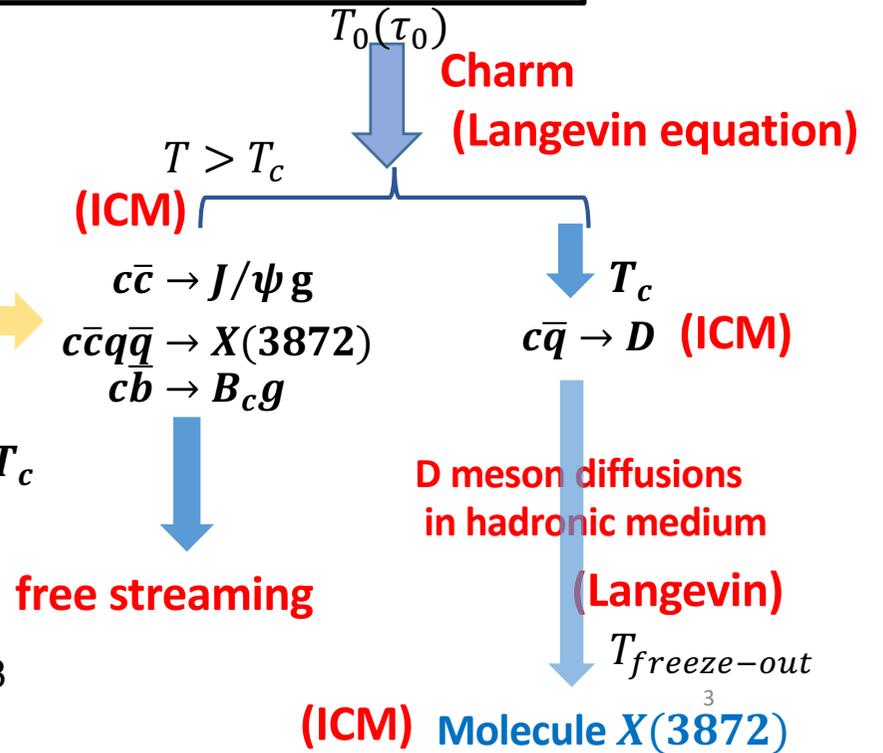
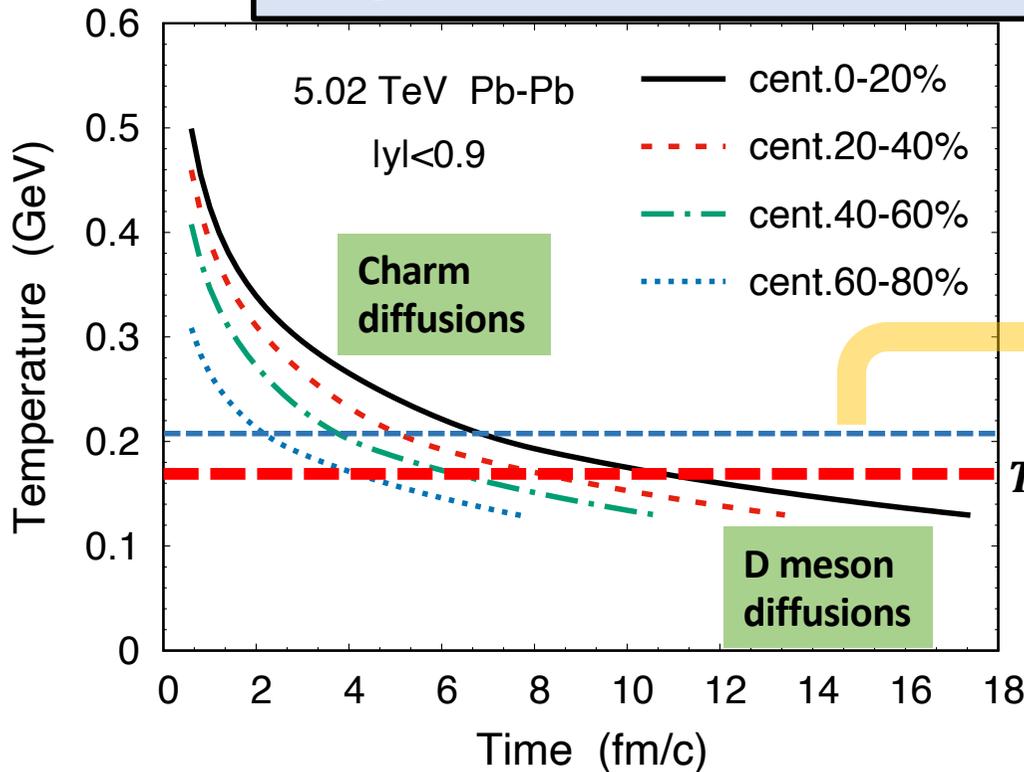
D_s, κ :

Spatial and Momentum Diffusion coefficients



Langevin + Instantaneous coalescence model (LICM)

[et al PRL 2012](#)



Heavy quark dynamical evolution

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D_s, κ :
Spatial and Momentum Diffusion Coefficient

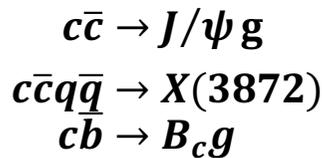
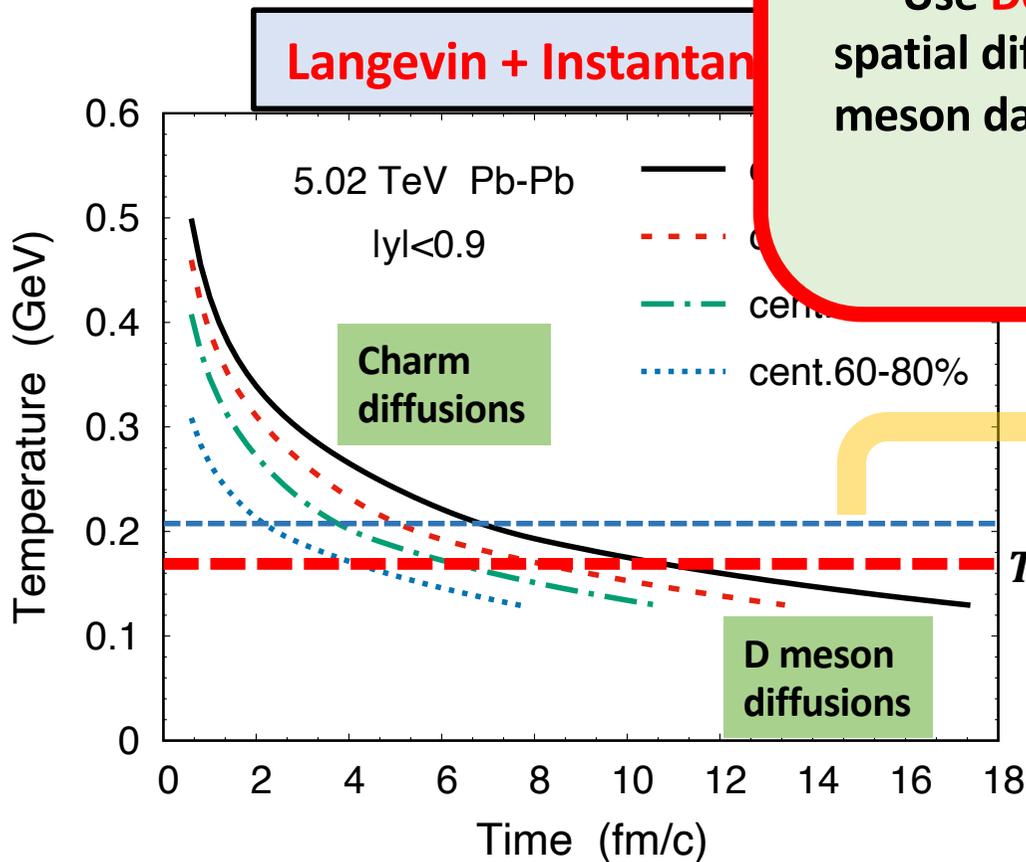
$$D_s(2\pi T) = 5$$

Spatial diffusion coefficient (T, p_T) -dependence

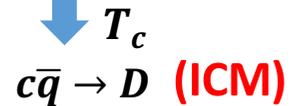
→ 刘佳敏的海报

Use **Deep neural network** to quantify the spatial diffusion coefficient with (RAA, v_2) of D meson data at (5.02, 2.76, 0.2) TeV

collaborate with Kai Zhou



free streaming

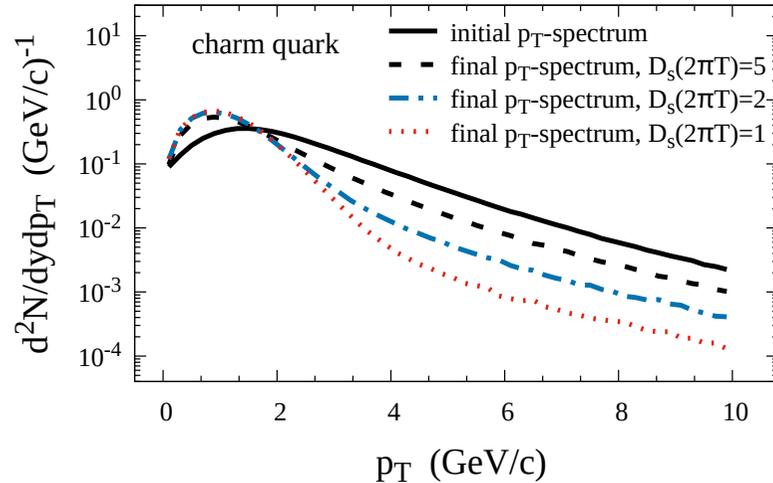


D meson diffusions
in hadronic medium
(Langevin)

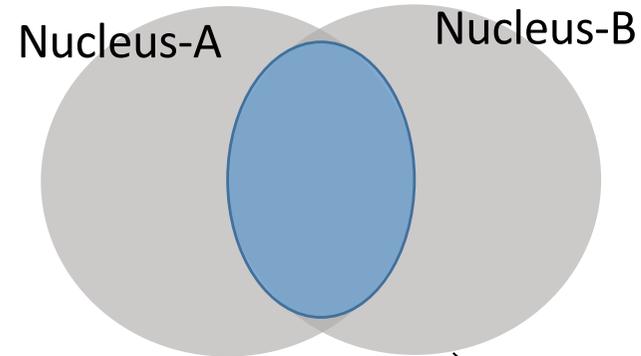
(ICM) Molecule X(3872)

Heavy quark dynamical evolution

(1) initial distribution



charm initial spectrum: FONLL model



$$\frac{dN^{test}}{d\vec{x}_T} \propto T_A(\vec{x}_T - \frac{\vec{b}}{2}) T_B(\vec{x}_T + \frac{\vec{b}}{2})$$

Charm initial positions:

Proportional to the $N_{coll}(\vec{x}_T)$,
Corrected by shadowing effect (EPS09)

(2) Charmonium coalescence at the hadronization temperature

$$P_{c+\bar{c} \rightarrow \psi}(\vec{x}_M, \vec{p}_M) = g_M \int d\vec{x}_1 d\vec{x}_2 \frac{d\vec{p}_1}{(2\pi)^3} \frac{d\vec{p}_2}{(2\pi)^3} \frac{d^2 N_1}{d\vec{x}_1 d\vec{p}_1} \frac{d^2 N_2}{d\vec{x}_2 d\vec{p}_2} f_M^W(\vec{x}_r, \vec{q}_r) \\ \times \delta^{(3)}(\vec{p}_M - \vec{p}_1 - \vec{p}_2) \delta^{(3)}(\vec{x}_M - \frac{\vec{x}_1 + \vec{x}_2}{2})$$

- $g_M = 1/12$ Vector meson degeneracy factor from color and spin
- $f_M^W(\vec{x}_r, \vec{q}_r)$: Wigner function. (\vec{x}_r, \vec{q}_r) in the center of mass frame of $c - \bar{c}$

charmed hadron production

Wigner function: encodes the information of formed states

$$f_{J/\psi}^W(\vec{x}_r, \vec{q}_r) = 8 \exp\left[-\frac{x_r^2}{\sigma^2} - \sigma^2 q_r^2\right]$$

$$W(\mathbf{r}, \mathbf{p}) = \int d^3\mathbf{y} e^{-i\mathbf{p}\cdot\mathbf{y}} \psi\left(\mathbf{r} + \frac{\mathbf{y}}{2}\right) \psi^*\left(\mathbf{r} - \frac{\mathbf{y}}{2}\right)$$

$$\sigma^2 = \frac{4}{3} \frac{(m_1 + m_2)^2}{m_1^2 + m_2^2} \langle r^2 \rangle_M$$

$$\sqrt{\langle r^2 \rangle_{J/\psi}} = 0.54 \text{ fm}$$

Give **consistent formation conditions** on the relative distance and relative momentum of two particles.

The width σ in the Wigner function

is connected with the internal structure of the formed state

Hadron Spectrum in heavy-ion collisions

$$\frac{d^2 N_\psi}{dy_M d\vec{p}_T} = \int d\vec{x}_M \frac{dp_z}{2\pi} \langle P_{c+\bar{c} \rightarrow \psi}(\vec{x}_M, \vec{p}_M) \rangle_{events} \times \frac{(\Delta N_{c\bar{c}}^{AA})^2}{\Delta y_M}$$

$$\Delta N_{c\bar{c}}^{AA} = \int d\vec{x}_T T_A(\vec{x}_T - \frac{\vec{b}}{2}) T_B(\vec{x}_T + \frac{\vec{b}}{2}) \frac{d\sigma_{pp}^{c\bar{c}}}{dy} R_S(\vec{b}, \vec{x}_T) \Delta y_{c\bar{c}}$$

Shadowing factor

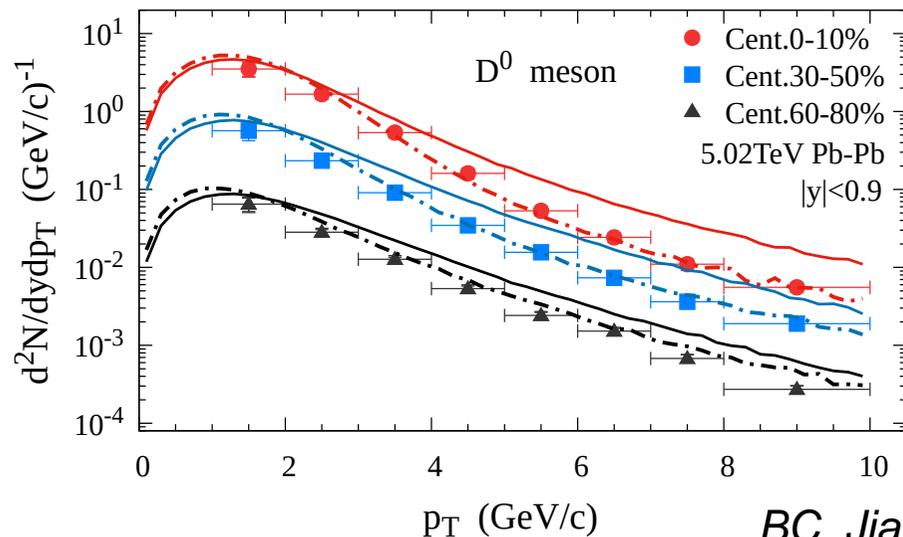
charmed hadron production: D meson

● D meson coalescence

$$P_{c\bar{q}\rightarrow D^0}(\vec{p}_M) = H_{c\rightarrow D^0} \int \frac{d\vec{p}_1}{(2\pi)^3} \frac{d\vec{p}_2}{(2\pi)^3} \frac{dN_1}{d\vec{p}_1} \frac{dN_2}{d\vec{p}_2} f_D^W(\vec{q}_r) \times \delta^{(3)}(\vec{p}_M - \vec{p}_1 - \vec{p}_2)$$

$$\frac{d^2 N_D}{dy_M d\vec{p}_T} = \int \frac{dp_z}{2\pi} \langle P_{c\bar{q}\rightarrow D^0}(\vec{p}_M) \rangle_{events} \times \frac{\Delta N_{c\bar{c}}^{AA}}{\Delta y_M}$$

- $H_{c\rightarrow D^0} = 9.5\%$ (20%): Charm turning into **direct** D^0 (D^{*0}) at Tc
- $\frac{dN_1}{d\vec{p}_1}$: **charm** momentum distribution
- $\frac{dN_2}{d\vec{p}_2}$: **light quark** momentum distribution: Fermi.



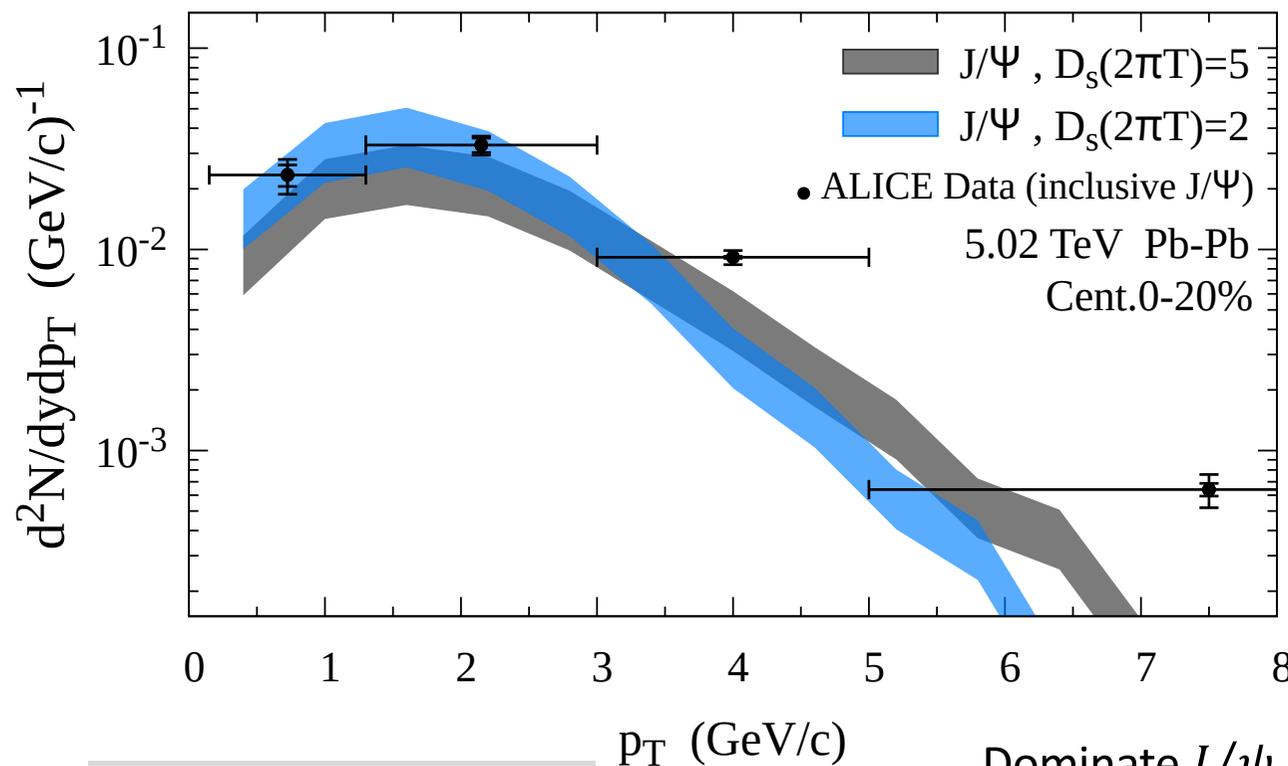
- We take the ratio of prompt D^0 over charm:

$$N(D^0)/N_{c\bar{c}} = 39\%$$

ALICE pp, arXiv:2105.06335

- Different thermalization: $D_s(2\pi T) = 5$ (solid line) and $D_s(2\pi T) = 2$ (dotted-dashed line)

charmed hadron production: J/ψ



Theoretical bands:
 With/without
 the shadowing effect.

Experimental data:

inclusive production = primordial + B-decay + $c - \bar{c}$ coalescence

Dominant J/ψ production at high p_T

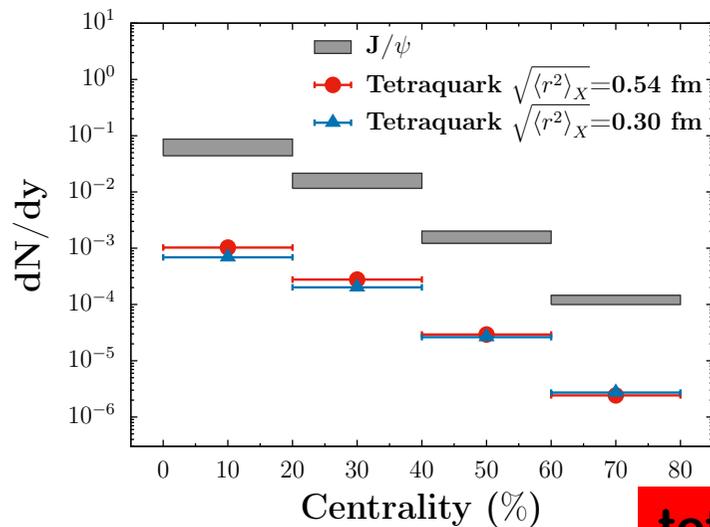
Dominant at low p_T and **total yield**

Theoretical calculation:

$c - \bar{c}$ coalescence

charmed hadron production: X(3872)

- $g_{X(3872)} = 1/432$ with X(3872) spin $J=1$
- Root-mean-square radius of tetraquark: $\langle r^2 \rangle_X = 0.30 - 0.54 \text{ fm}^2$
- diquark (cq) is formed firstly, then two diquarks form a tetraquark state.



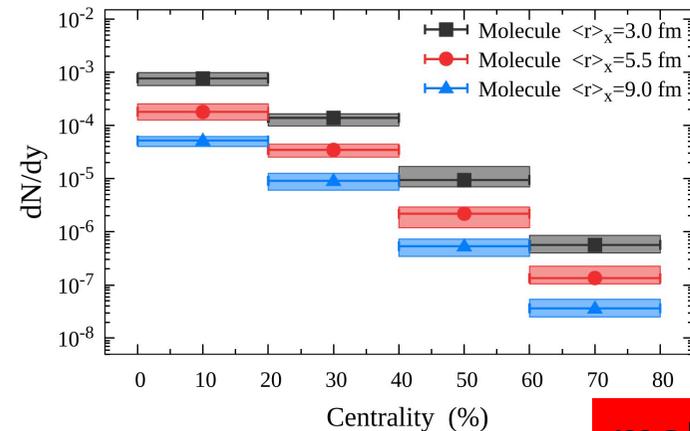
tetraquark

- Tetraquark yield is around **40 times** smaller than J/ψ
- Tetraquark yield is controlled by both **spatial** and **momentum** part of the Wigner function

Molecule state with potential model

$$V_{mole} = V_{\pi} + V_{\omega} + V_{\eta} + V_{\rho}$$

| Λ | 0.55 | 0.555 | 0.56 | 0.565 | 0.57 | 0.575 | 0.579 |
|-----------------------------------|--------|--------|-------|-------|-------|-------|-------|
| BE.(keV) | 1600.3 | 1098.5 | 698.4 | 394.4 | 180.6 | 51.2 | 3.3 |
| $\langle r \rangle$ (fm) | 2.47 | 2.85 | 3.41 | 4.31 | 6.01 | 10.52 | 22.60 |
| $\sqrt{\langle r^2 \rangle}$ (fm) | 3.08 | 3.59 | 4.36 | 5.61 | 8.00 | 14.33 | 28.94 |



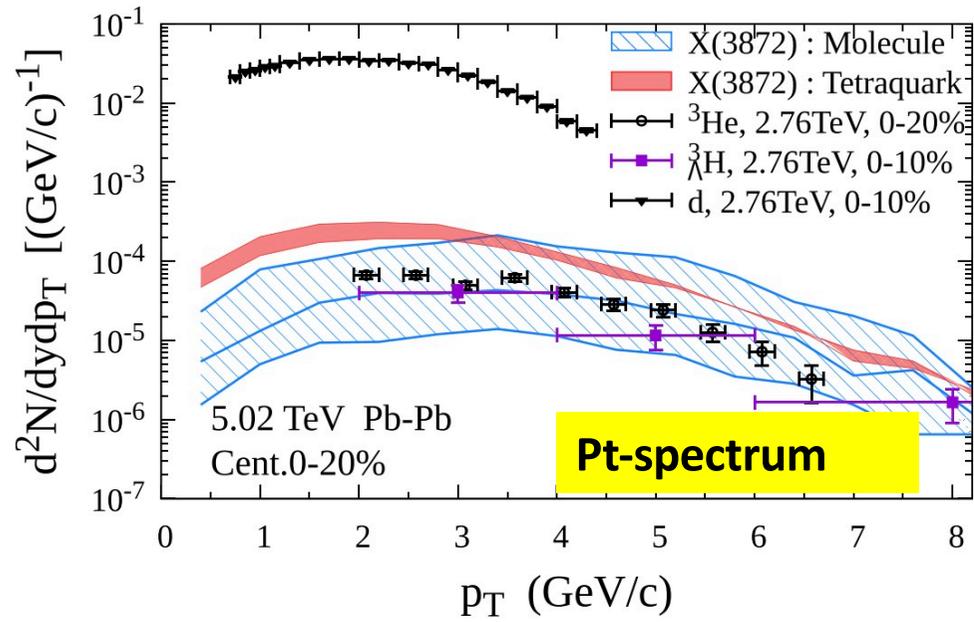
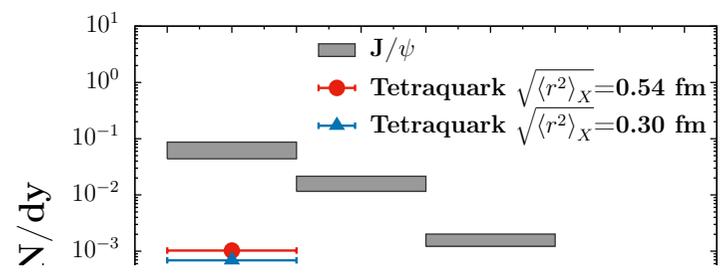
molecule

Bands:

Volume dependence in freeze-out

charmed hadron production: X(3872)

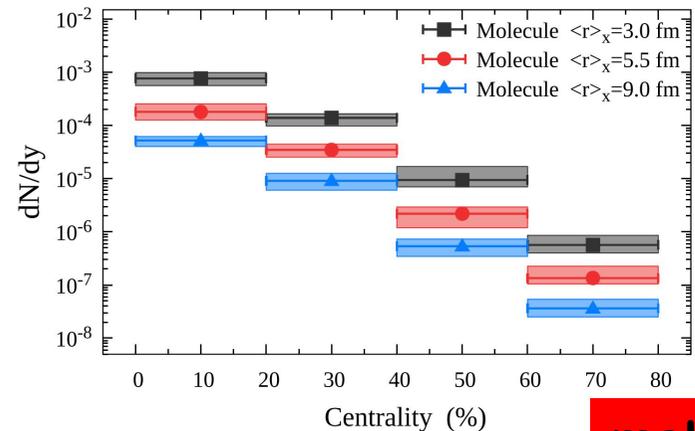
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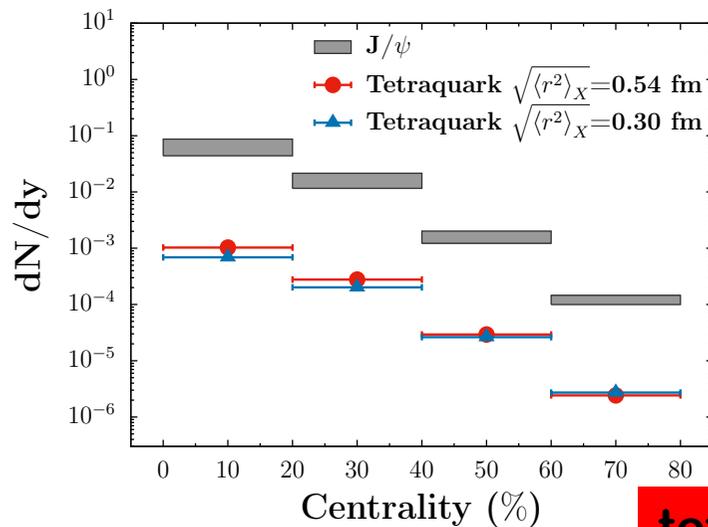


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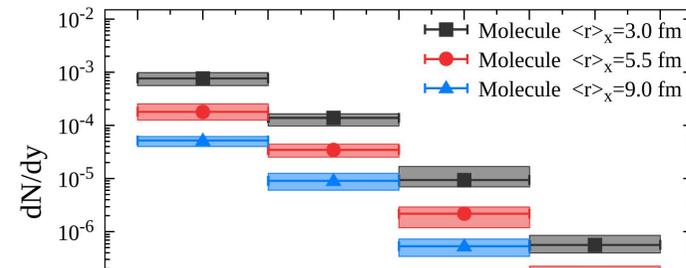


tetraquark

- Tetraquark yield is around

Molecule state with potential model

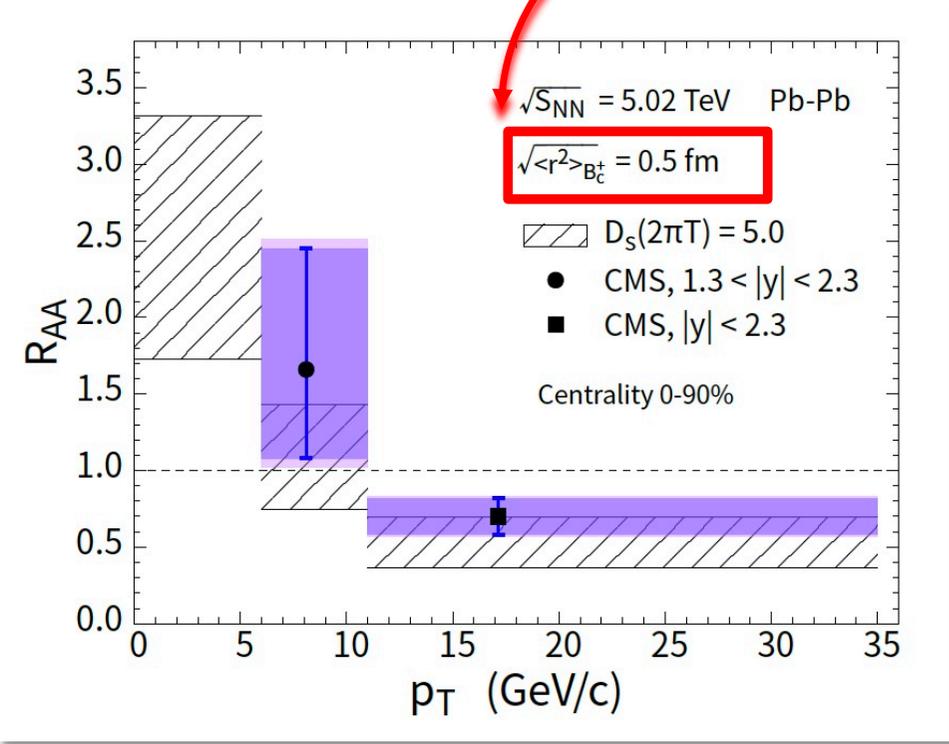
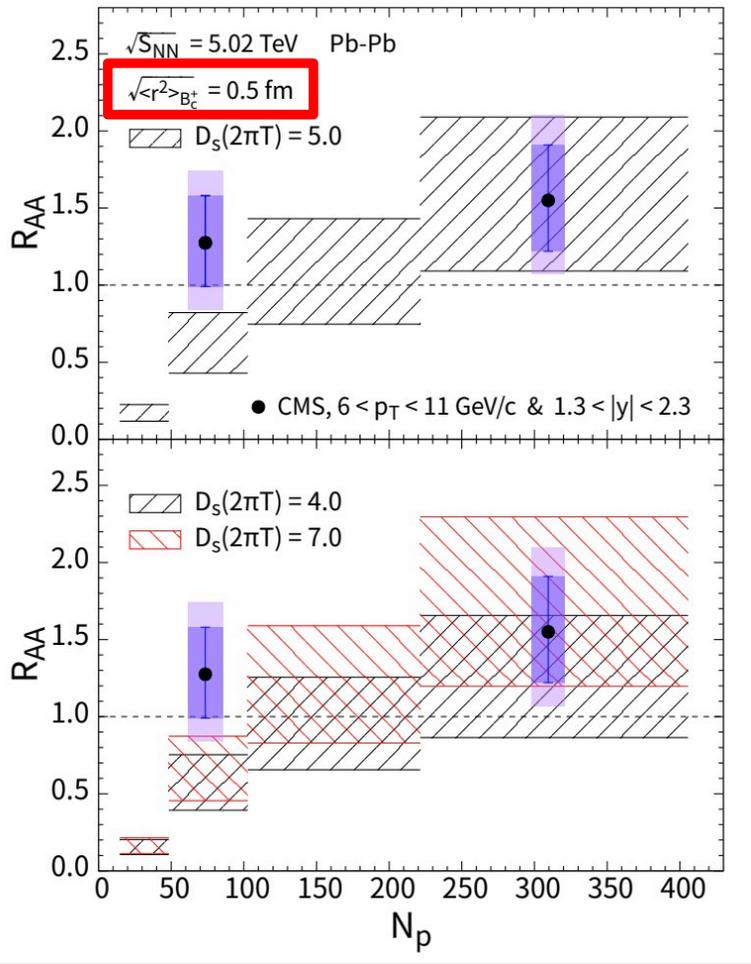
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- Our tetraquark yield $\sim 10^{-3}$ is consistent with Cho. Prog.Part.Nucl.Phys. 95,279-322 (2017); when taking same coalescence temperature
- **Relations** between **tetraquark** and **molecule** production: ours is consistent with rate equation model Rapp EPJA 57, 122 (2021);

charmed hadron production: B_c

Geometry size



[BC, Wen, Liu, Phys.Lett.B 834 \(2022\) 137448](#)

$$\frac{d\sigma_{pp}^{cc}}{dy} = 1.165 \text{ mb}$$

B_c : spin 0
fig: $B_c(1s) + B_c(2s \rightarrow 1s)$

$$\frac{d\sigma_{pp}^{bb}}{dy} = 47.5 \mu\text{b}$$

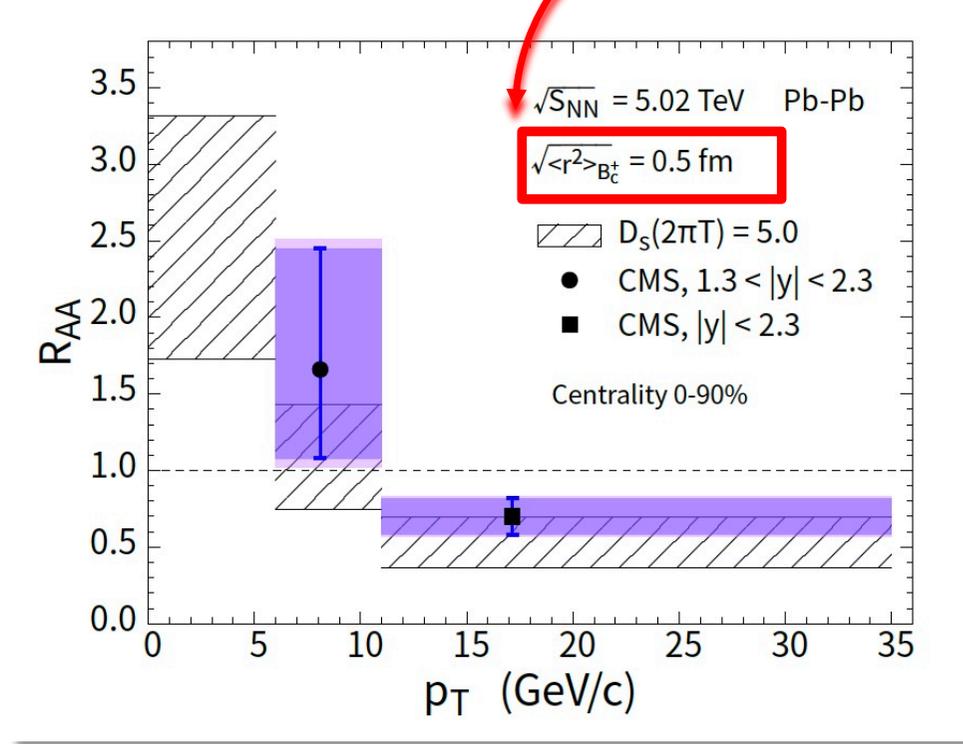
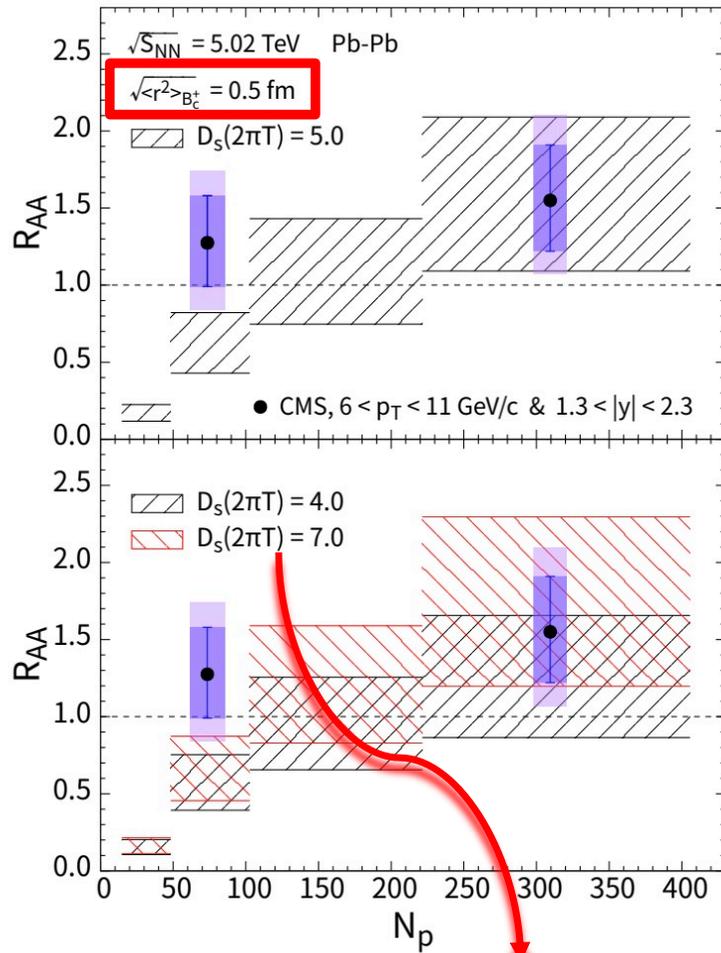
$$\frac{d\sigma_{pp}^{Bc}}{dy} = (151.9 - 79.3) \text{ nb}$$

$$B(B_c^+ \rightarrow J/\psi \mu^+ \nu) = (2.37 - 4.54)\%$$

- B_c final production is evidently enhanced, due to a large number of c and b quarks in QGP. $c + \bar{b} \rightarrow B_c + g$
- $R_{AA} > 1$ at central collisions:
QGP signal
 $R_{AA} < 1$ at peripheral collisions:
absence of initial production

charmed hadron production: B_c

Geometry size



[BC, Wen, Liu, Phys.Lett.B 834 \(2022\) 137448](#)

1) B_c final production is evidently enhanced, due to a large number of c and b quarks in QGP.

$$\frac{d\sigma_{p1}^c}{dy} \frac{d\sigma_l}{dy}$$

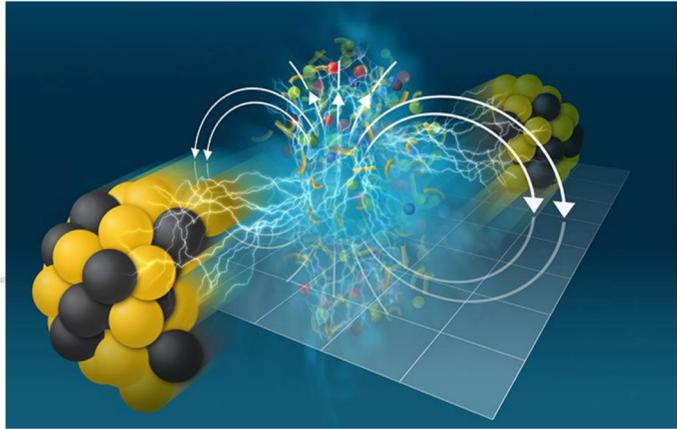
Different thermalization

of charm and bottom quarks on B_c production,

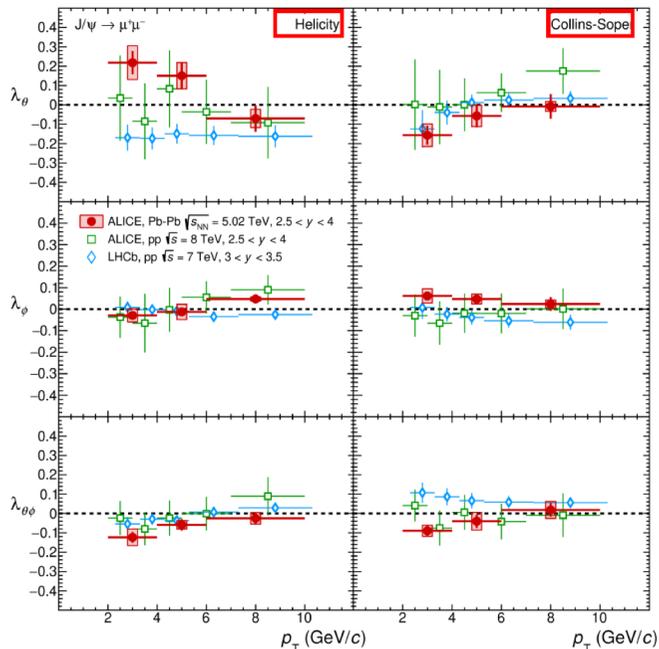
By taking spatial diffusion coefficient $D_s(2\pi T) = 4$ and 7

+ g

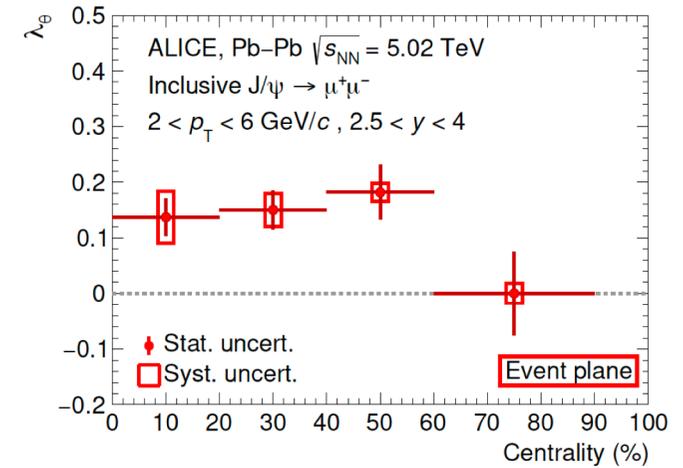
Can heavy quark be polarized in the rotating QGP and strong B-field ?



[T. Bowman and J. Abramowitz/Brookhaven National Laboratory] PLB 815 (2021) 136146

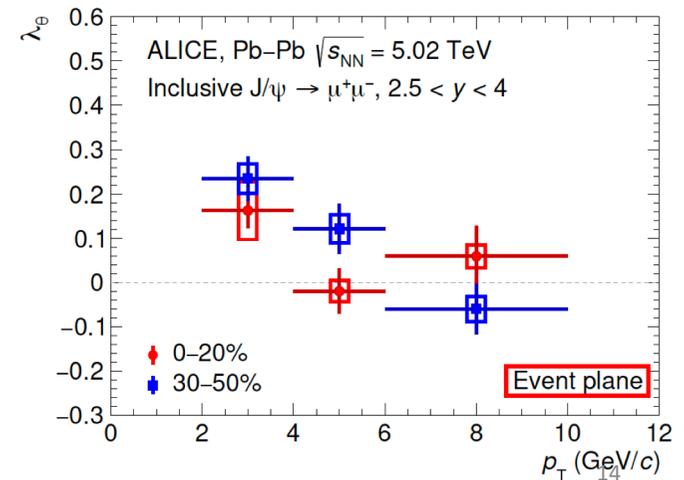


Recent polarization data-points:



ALI-PUB-521052

ALICE: PRL 131 (2023) 042303



Can heavy quarks be polarized ?

By magnetic field or vorticity ?

Dynamical process: simulating Heavy quark polarization in B-field

- Landau-Lifshitz-Gilbert (LLG) equation

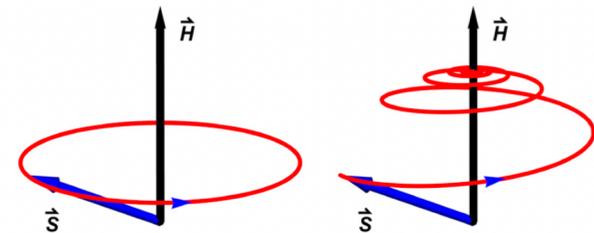
PRB 83, 134418 (2011)

$$\frac{d\vec{S}}{dt} = -\frac{\gamma}{1 + \alpha^2} [\vec{S} \times (\vec{H} + \vec{H}_{th})] - \frac{\alpha\gamma}{1 + \alpha^2} \vec{S} \times [\vec{S} \times (\vec{H} + \vec{H}_{th})]$$

$$\vec{S} = \vec{s}/|\vec{s}|$$

Unit vector

stochastic dynamics of a spin in the medium with magnetic field



Polarization of heavy quark is induced by:
spin-magnetic field interaction
+ particle-particle interaction

$$\gamma = g \frac{q}{2m}$$

Electric charge

$\alpha = 0.1$ Gilbert damping factor
(to be determined later)

noise term

$$\langle H_{th,i}(t) \rangle = 0,$$

$$\langle H_{th,i}(t) H_{th,j}(t') \rangle = \frac{2\alpha T}{|\mu|\gamma} \delta_{ij} \delta(t - t').$$

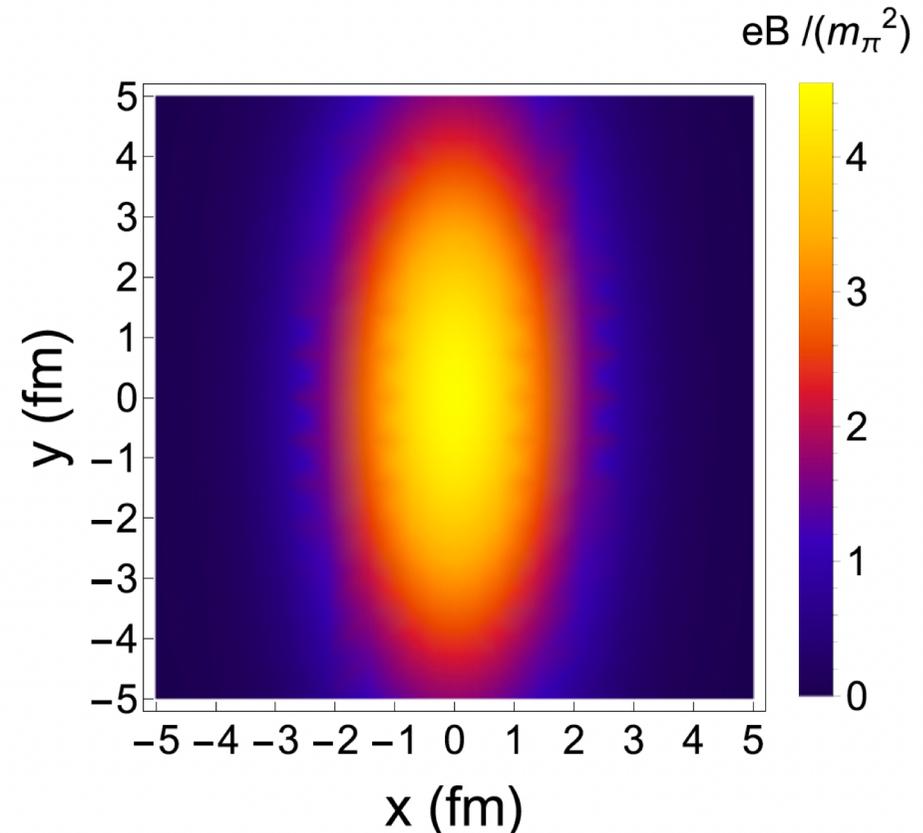
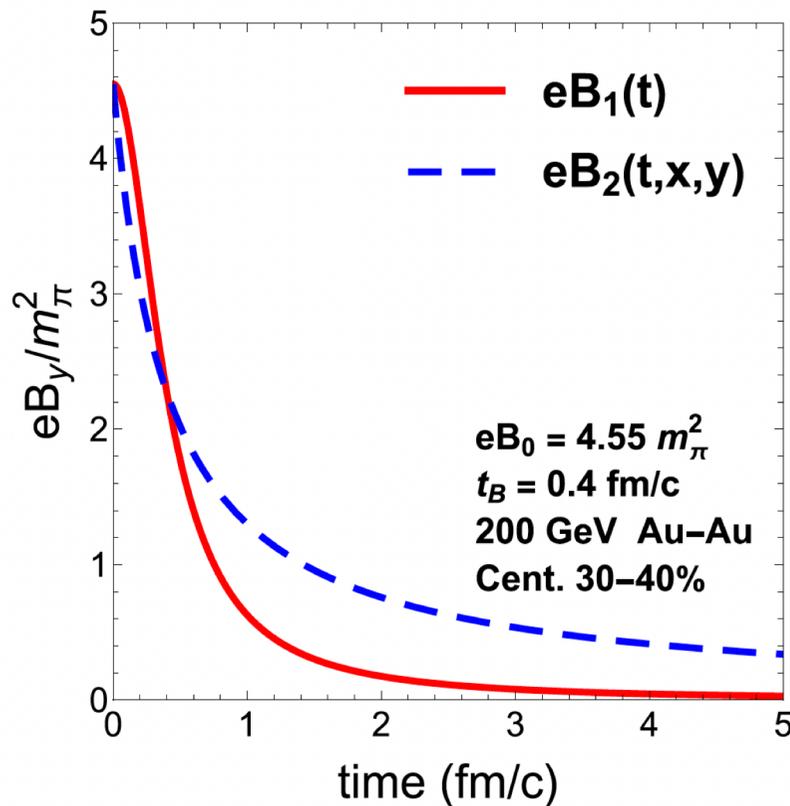
Heavy quark polarization in magnetic field

In-medium magnetic field
(two cases are considered)

Liu, Bai, Zheng, Huang, **BC**,
PRC110, 034910 (2024)

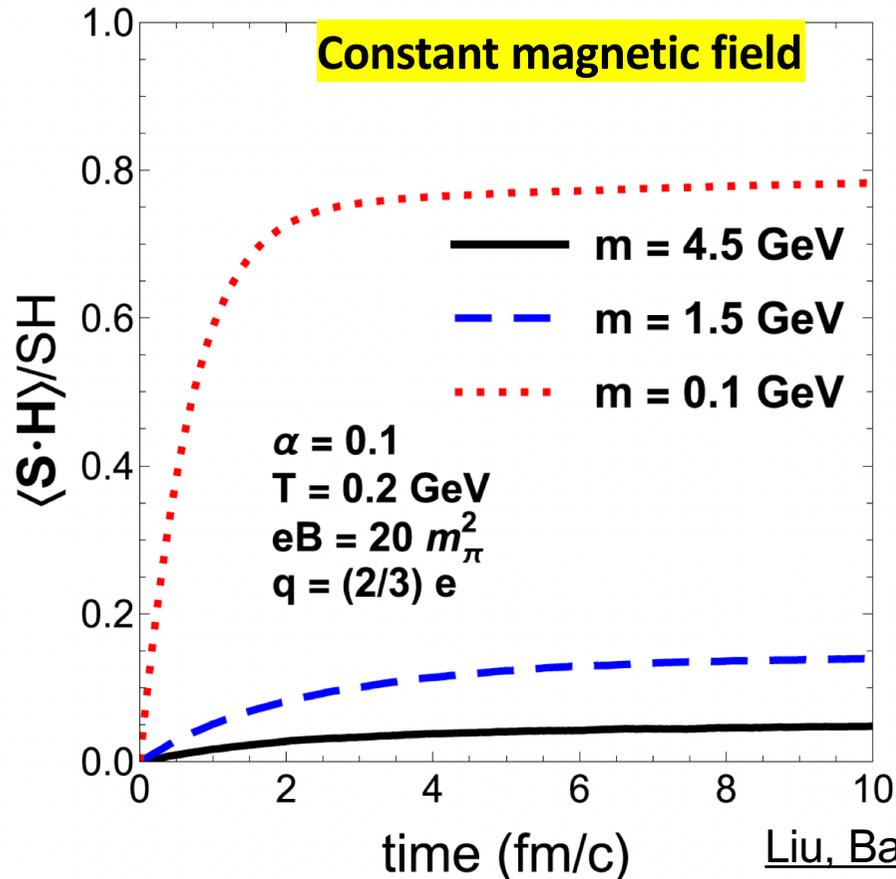
$$eB_1(t) = \frac{eB_0}{1 + \left(\frac{t}{t_B}\right)^2}$$

$$eB_2(t, x, y) = \frac{eB_0}{1 + \left(\frac{t}{t_B}\right)^2} \exp\left(-\frac{x^2}{2\sigma_x^2} - \frac{y^2}{2\sigma_y^2}\right)$$

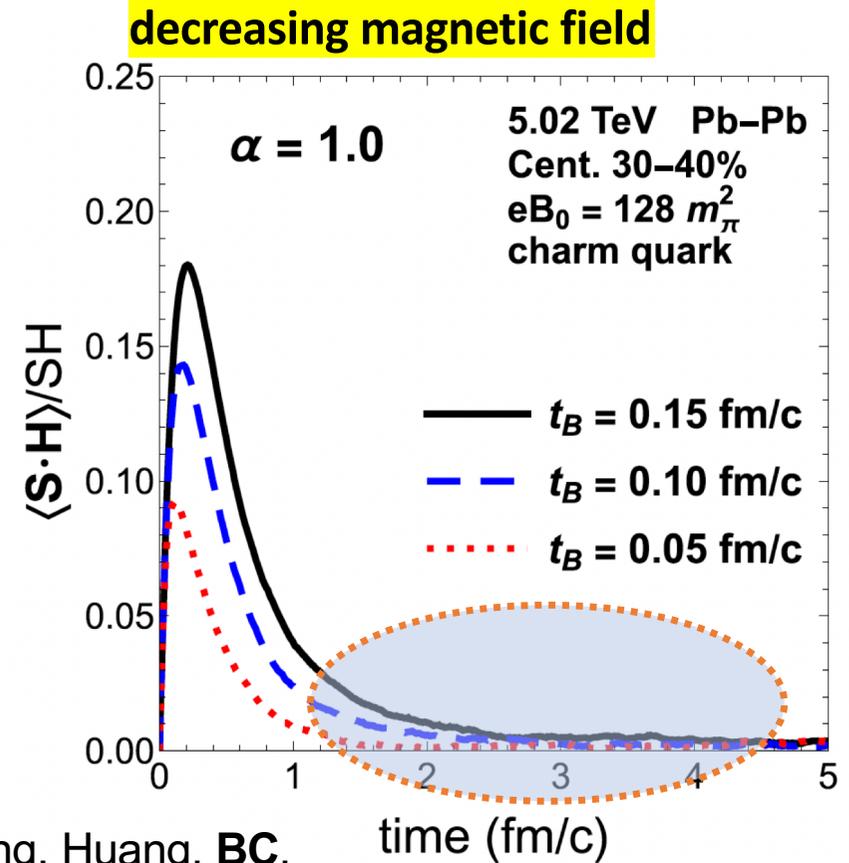


Heavy quark polarization in magnetic field

Mass dependence :



B dependence:



Liu, Bai, Zheng, Huang, **BC**,
PRC110, 034910 (2024)

- Larger Quark mass → smaller polarization
- smaller B field → smaller polarization

Heavy quark polarization in magnetic field

Liu, Bai, Zheng, Huang, **BC**, PRC110, 034910 (2024)

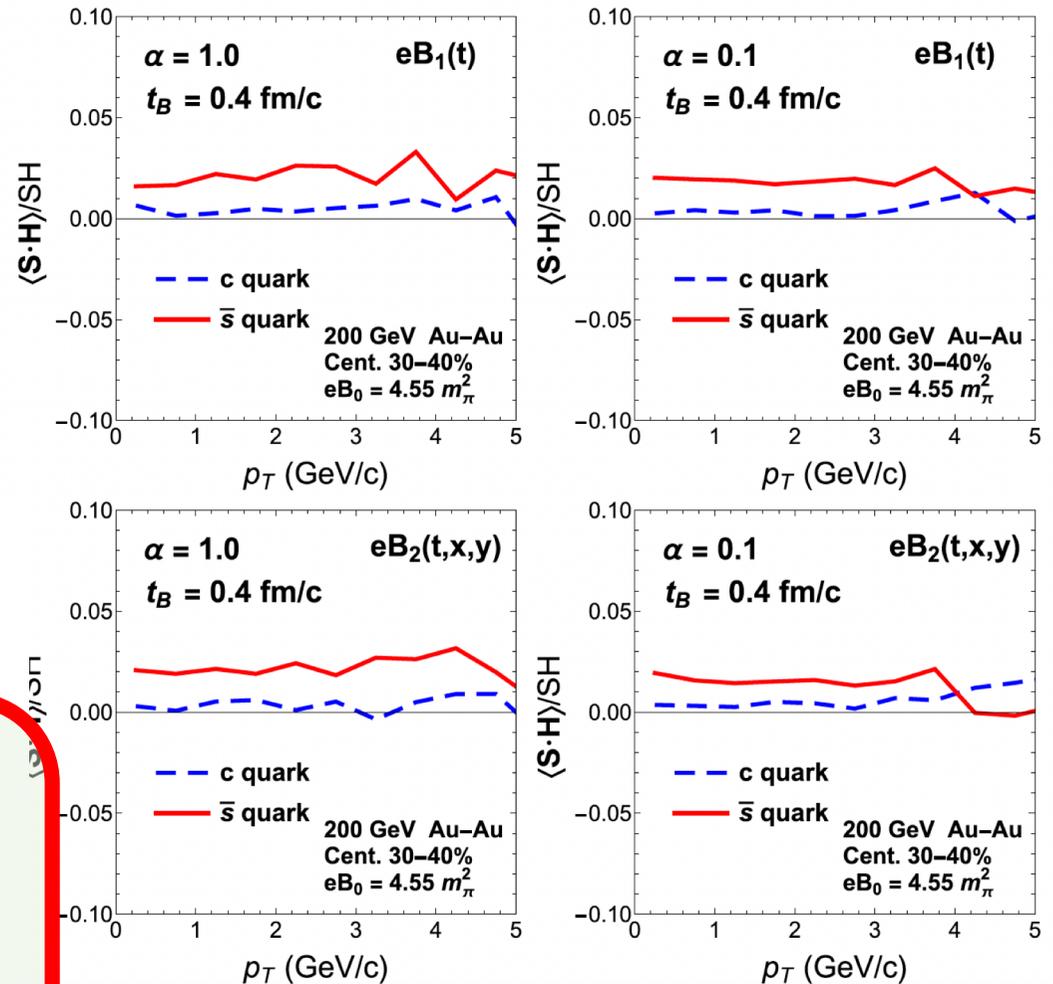
In realistic heavy-ion collisions

Key parameter: α
 Gilbert damping factor of
 HQ spin

It can be calculated with
Linear Response Theory.

→ 李天阳的海报
 (Gilbert damping factor of
 heavy quark spin)

Collaborate with Anping,
 paper in preparation



Magnetic field induced polarization &
 thermal particle **random collisions**

Summary

- X(3872) as a **tightly bound tetraquark** and a **hadronic molecule**, is formed via different processes.

Their production depends on the wave function of X(3872).

Therefore, heavy-ion collisions provide a new opportunity to study the nature of X(3872).

- **B_c meson is firstly observed in AA collisions,**
evident enhancement of R_{AA} : a very clear signal of QGP
- **heavy quark spin dynamics**

Thank you very much for your attention!

