Theoretical study on the recently observed $T_{c\bar{s}}$ state

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Hadron spectra and hadron structures：Exotic states

Volume 8, number 3 PHYSICS LETTERS 1 February 1964

A SCHEMATIC MODEL OF BARYONS AND MESONS *

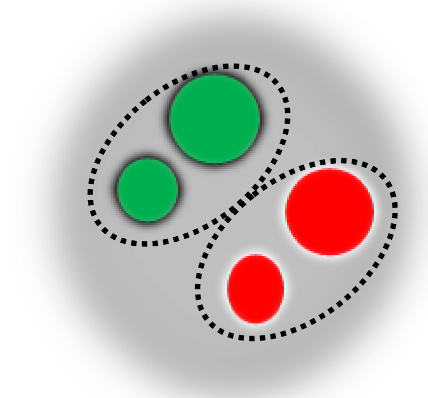
M. GELL-MANN
California Institute of Technology, Pasadena, California

Received 4 January 1964

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" [1-3], we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone [4]. Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

ber $n_t - n_{\bar{t}}$ would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin $\frac{1}{2}$ and $z = -1$, so that the four particles d^-, s^-, u^0 and b^0 exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon b if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" [6] q and the members of the anti-triplet as anti-quarks $\bar{q}$. Baryons can now be constructed from quarks by using the combinations $(q\,q\,q)$, $(q\,q\,q\,q\,\bar{q})$, etc., while mesons are made out of $(q\,\bar{q})$, $(q\,q\,\bar{q}\,\bar{q})$, etc. It is assuming that the lowest



Compact multiquark

8419/TH.412
21 February 1964

AN SU_3 MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

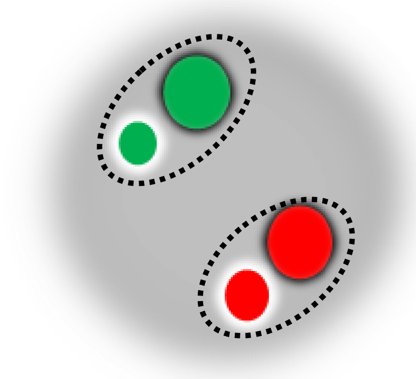
II *)

G. Zweig
CERN---Geneva

*) Version I is CERN preprint 8182/TH.401, Jan. 17, 1964.

...

6) In general, we would expect that baryons are built not only from the product of three aces, AAA, but also from $\bar{A}$AAAA, $\bar{A}\bar{A}$AAAAA, etc., where $\bar{A}$ denotes an anti-ace. Similarly, mesons could be formed from $\bar{A}$A, $\bar{A}\bar{A}$AA etc. For the low mass mesons and baryons we will assume the simplest possibilities, $\bar{A}$A and AAA, that is, "deuces and treys".



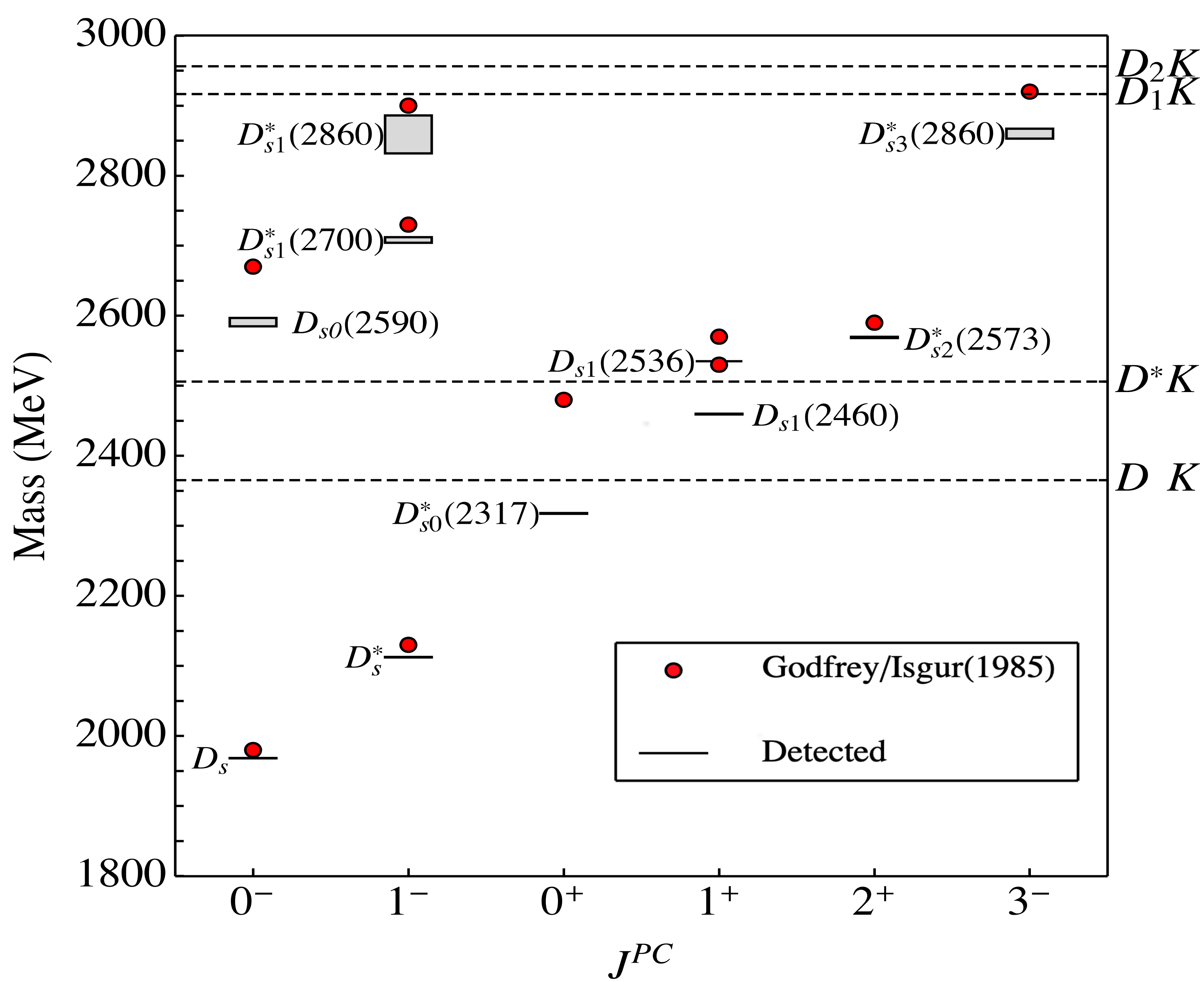
Hadronic molecule

GI quark model for D_s meson

Mesons in a Relativized Quark Model with Chromodynamics #1

S. Godfrey (Toronto U.), Nathan Isgur (Toronto U.) (1985)

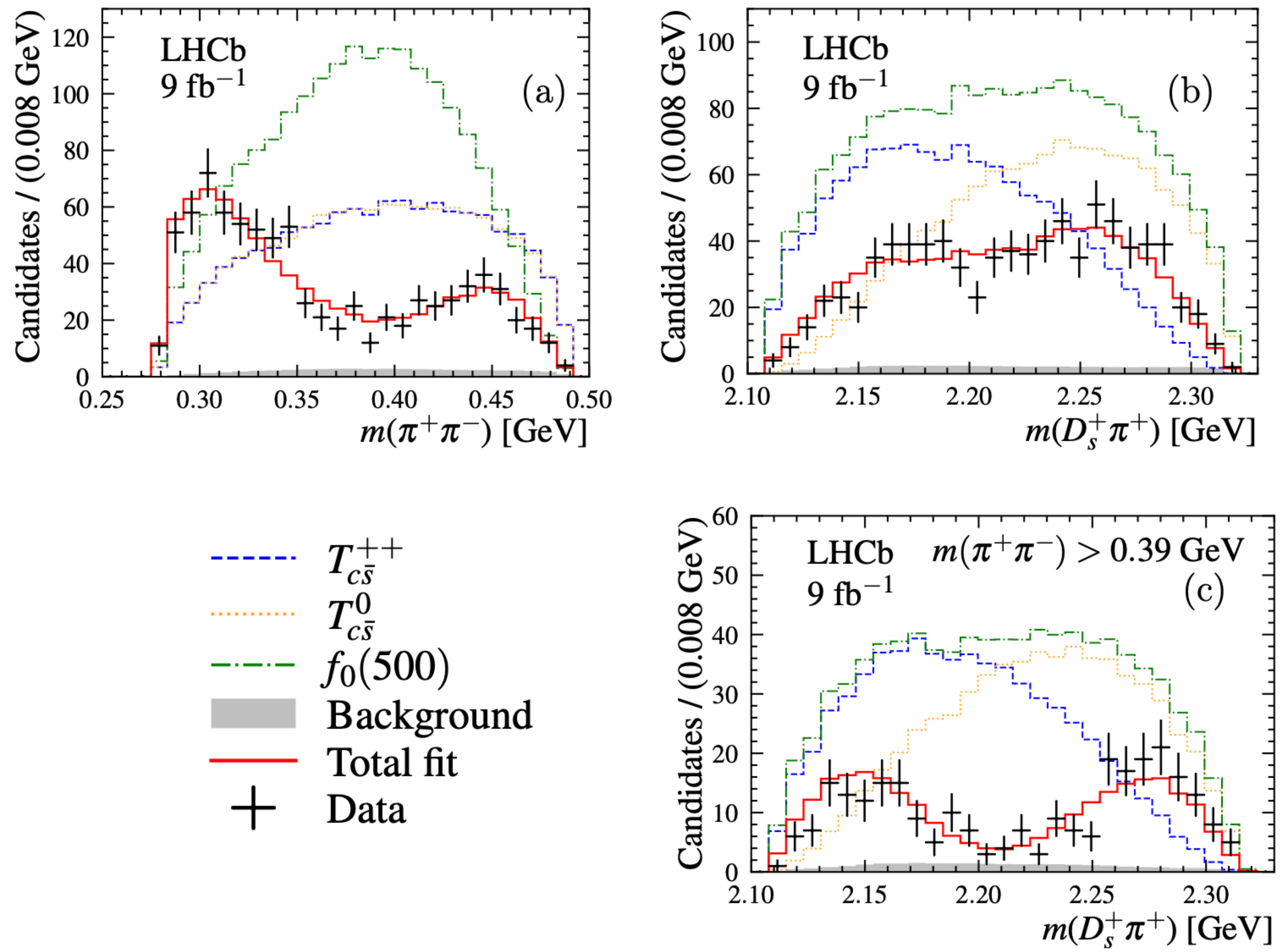
Published in: *Phys.Rev.D* 32 (1985) 189-231



Exotic structure in $B \to D^{(*)} D_s^+ \pi^+ \pi^-$ decays

LHCb, arXiv:2411.03399

$$B \to D^{(*)} D_{s1}(2460)$$
$$\downarrow$$
$$D_s^+ \pi^+ \pi^-$$

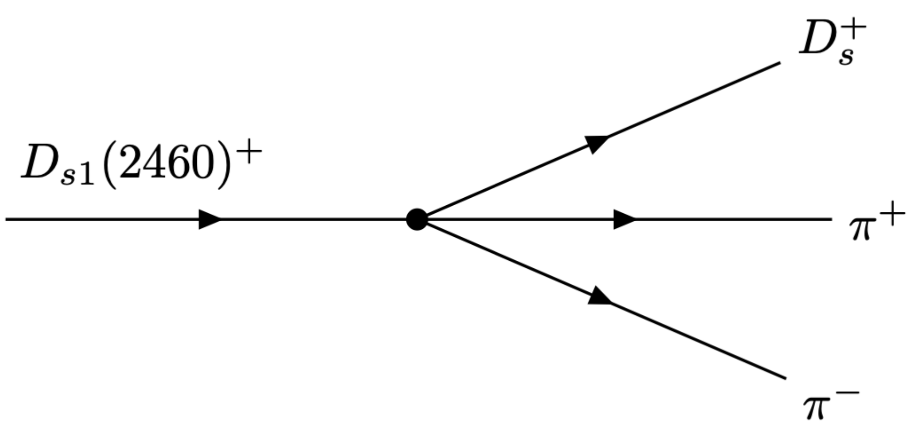


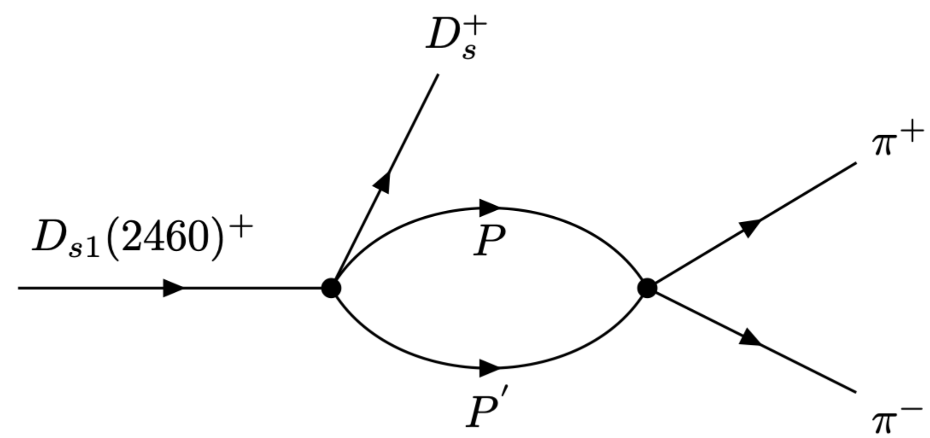
Model	Resonance	Mass (MeV)	Width (MeV)
$f_0(500)$ + RBW $T_{c\bar{s}}(0^+)$	$f_0(500)$	$464 \pm 23 \pm 14$	$214 \pm 28 \pm 8$
	$T_{c\bar{s}}^{++}/T_{c\bar{s}}^{0}$	$2312 \pm 27 \pm 11$	$264 \pm 46 \pm 21$
$f_0(500)$ + K-matrix $T_{c\bar{s}}(0^+)$	$f_0(500)$	$472 \pm 32 \pm 19$	$226 \pm 24 \pm 18$
	$T_{c\bar{s}}^{++}/T_{c\bar{s}}^{0}$	$2328 \pm 12 \pm 12$	$96 \pm 16 \pm 23$

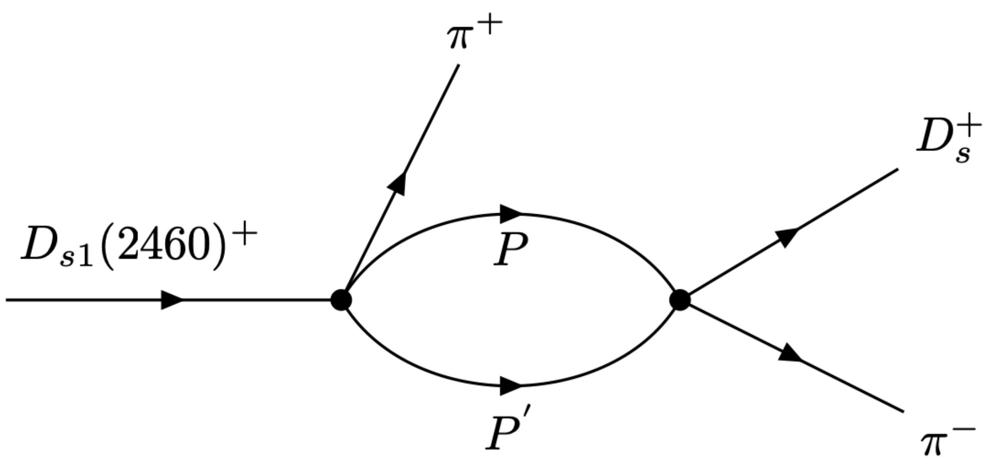
Theoretical interpretation

- $D_s\pi - DK$ coupled channel scattering: $T_{c\bar{s}}$ resonances is dynamically generated from the pseudoscalar-pseudoscalar meson interaction within the chiral unitary approach.

ZY Wang, YS Li and SQ Luo, Phys.Rev.D 111 (2025) 7, 076009





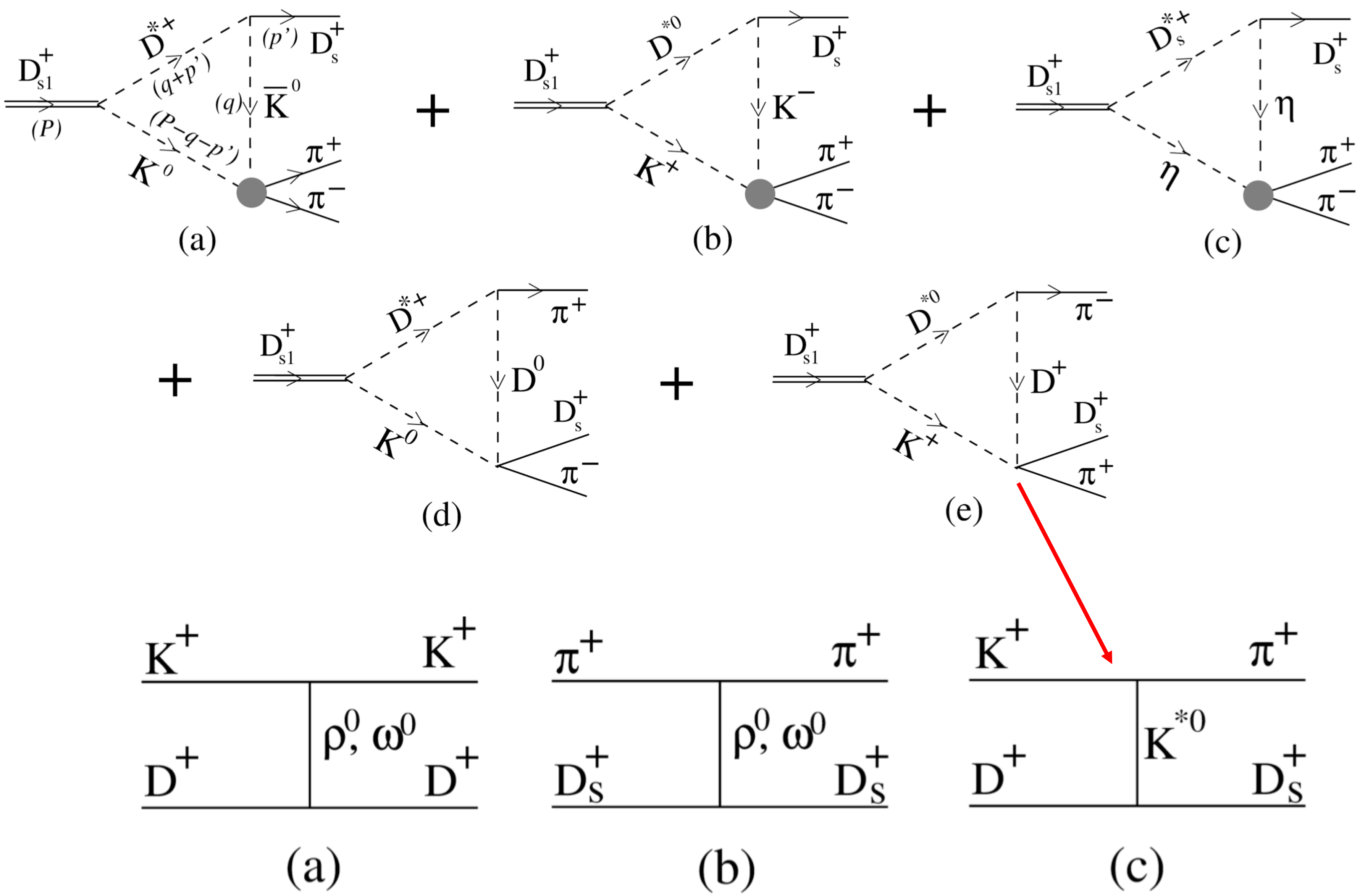


$$V^{I=1}_{D_s\pi\to D_s\pi} = 0,$$
$$V^{I=1}_{D_s\pi\to DK} = -\frac{1}{8f^2}\left(3s - \left(M_1^2 + M_2^2 + m_1^2 + m_2^2\right) - \frac{\Delta_1\Delta_2}{s}\right),$$
$$V^{I=1}_{DK\to DK} = 0,$$

Theoretical interpretation

- Molecular $D_{s1}(2460)[D^*K, D_s^*\eta]$ state decay

Roca, Dias and Oset, arXiv:2502.18401

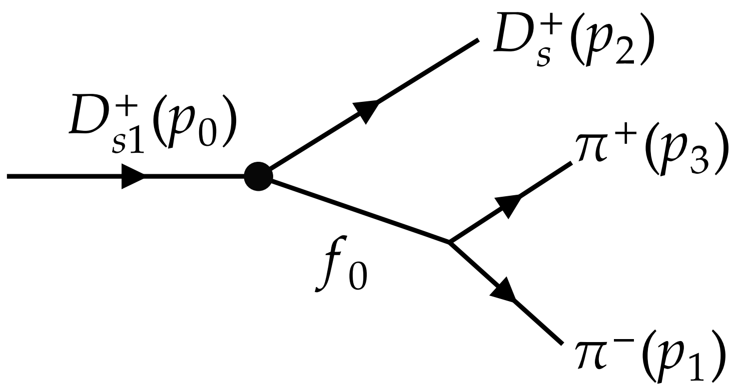


$$V_{K^+D^+,K^+D^+} = 0; \quad V_{\pi^+D_s^+,\pi^+D_s^+} = 0;$$

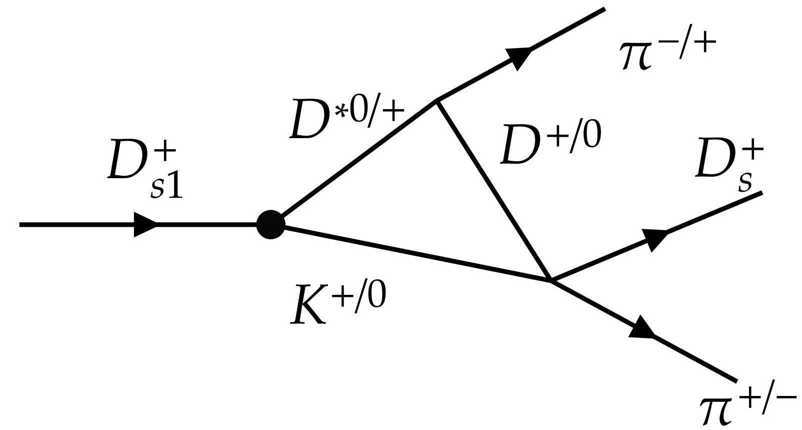
$$V_{K^+D^+,\pi^+D_s^+} = \frac{g^2}{m_{K^*}^2}(p_1+p_3)_\mu(p_2+p_4)^\mu.$$

Our model

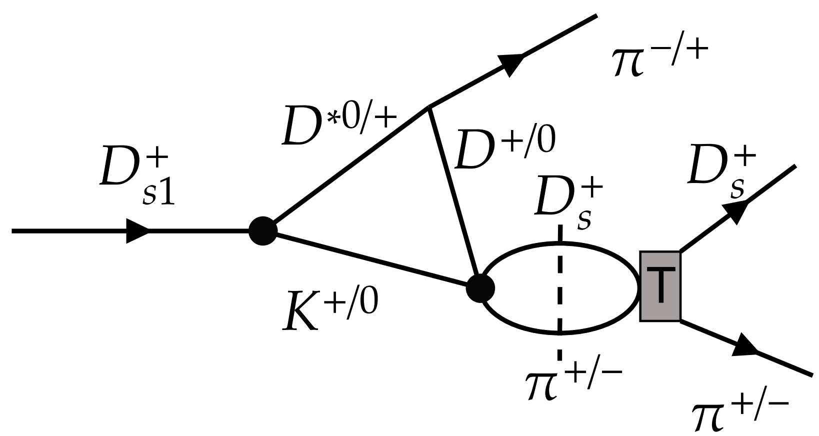
- The feynman diagrams



(a)



(b)



(c)

- The amplitude

$$i\mathcal{M} = \frac{ir_1\epsilon\cdot p_2}{m_{13}^2 - m_{f_0} + im_{f_0}\Gamma_{f_0}} + \left\{\int \frac{ir_{2S}d^4q}{(2\pi)^4}\frac{\epsilon^{\mu}N_{\mu}(q,p_0,p_1,p_2)(1+G_{D_s\pi}(p_{\rm on})T_{D_s\pi\to D_s\pi})(g_{K^*},g_{D^*})}{[q^2-m_D^2][(q+p_1)^2-m_{D^*}^2][(p_0-p_1-q)^2-m_K^2]} + (p_1\to p_3)\right\},$$

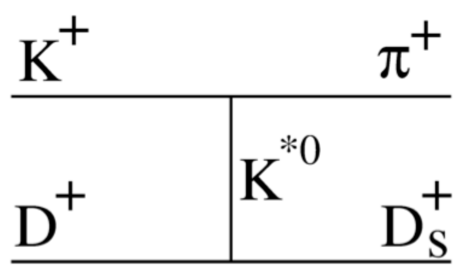
$$N_{\mu}(q,p_0,p_1,p_2) = (-g_{\mu\nu} + \frac{(p_1+q)_{\mu}(p_1+q)_{\nu}}{m_{D^*}^2})(p_1-q)_{\nu}(p_2-q+2p_3)_{\alpha}(-g_{\alpha\beta} + \frac{(p_2-q)_{\alpha}(p_2-q)_{\beta}}{m_{K^*}^2})(p_2+q)_{\beta}$$

Our model

- For the T-matrix,

$$T(\vec{k}_{D^*},\vec{k}'_{D^*};E)=\mathcal{V}(\vec{k}_{D^*},\vec{k}'_{D^*};E)+\int d\,\vec{q}\,\frac{\mathcal{V}(\vec{k}_{D^*},\vec{q};E)T(\vec{q},\vec{k}'_{D^*};E)}{E-\sqrt{m_D^2+q^2}-\sqrt{m_{D^*}^2+q^2}+i\epsilon}$$

$$V_{DK\to D_s\pi}^{K^*}=\frac{g_{K^*}}{m_{K^*}^2}(p_1+p_3)_\mu(p_2+p_4)^\mu$$



Similar for $V_{DK\to D_s\pi}^{D^*}$. The resulting effective potential reads

$$\mathcal{V}_{\alpha\beta}=\left(V_{\alpha\beta}^{K^*}+V_{\alpha\beta}^{D^*}\right)\left(\frac{\Lambda_\alpha^2}{\Lambda_\alpha^2+p_\alpha^2}\right)^2\left(\frac{\Lambda_\beta^2}{\Lambda_\beta^2+p_\beta'^2}\right)^2$$

$\alpha,\beta=1,2$ for $D_s\pi$ and DK channel, respectively. The cutoff for these two channels can be different.

Fit to the experimental lineshapes

χ^2/dof =1.5

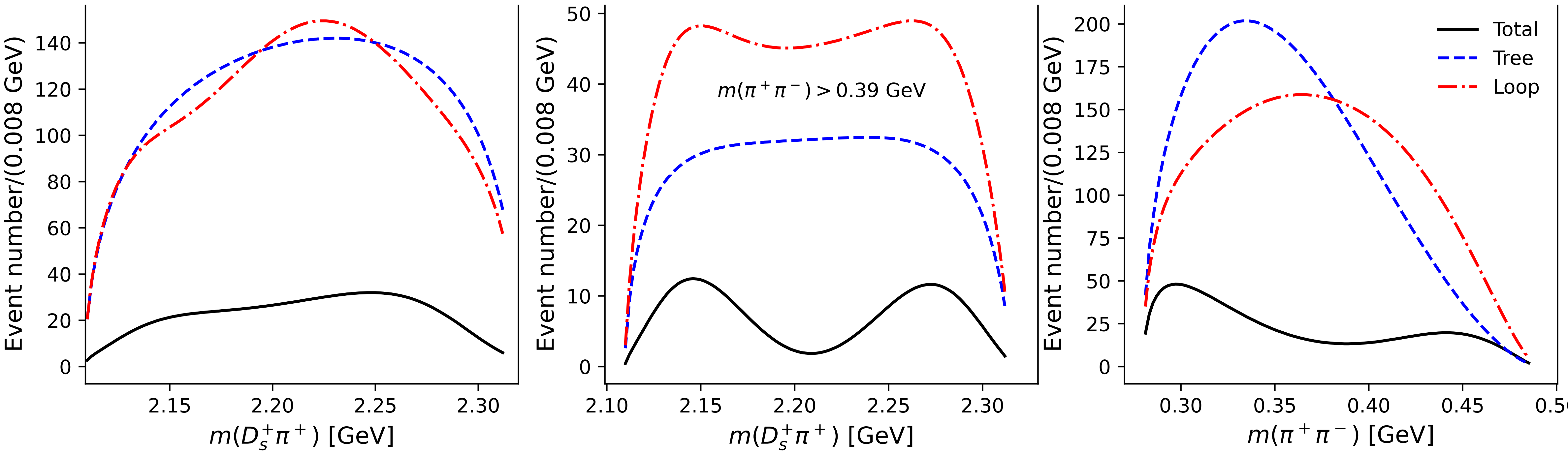


TABLE I. The parameters of the model determined from the fit and the pole position ($E_p = M - \Gamma/2i$). The coupling constant g_{K^*} and g_{D^*} are in unit of GeV^2, while the others are in units of GeV.

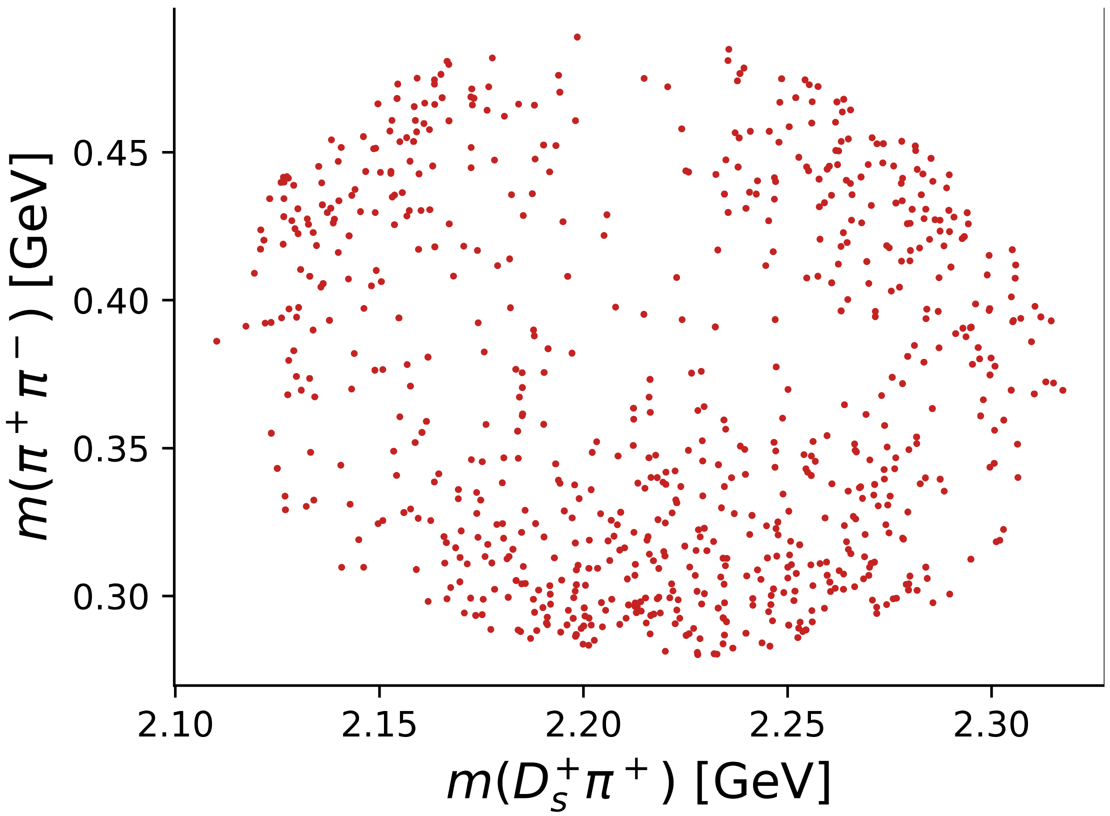
Λ_1	Λ_1	g_{K^*}	g_{D^*}	m_{f_0}	Γ_{f_0}	E_p
1.8	0.4	69.6	-	0.3	0.5	2.31-0.09i
1.3	0.4	120	-60	0.31	0.47	2.29-0.1i

Experimental position

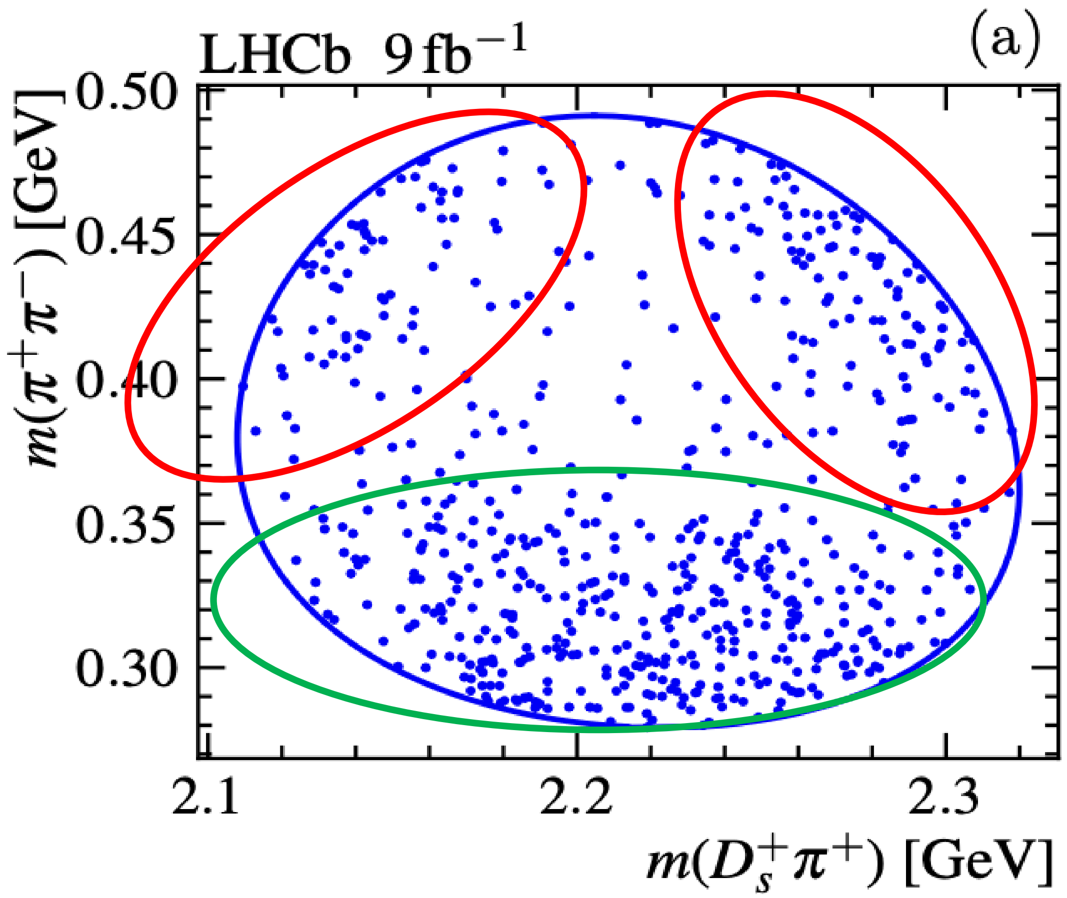
Mass (MeV)	Width (MeV)
$2328 \pm 12 \pm 12$	$96 \pm 16 \pm 23$

LHCb, arXiv:2411.03399

Dalitz plot

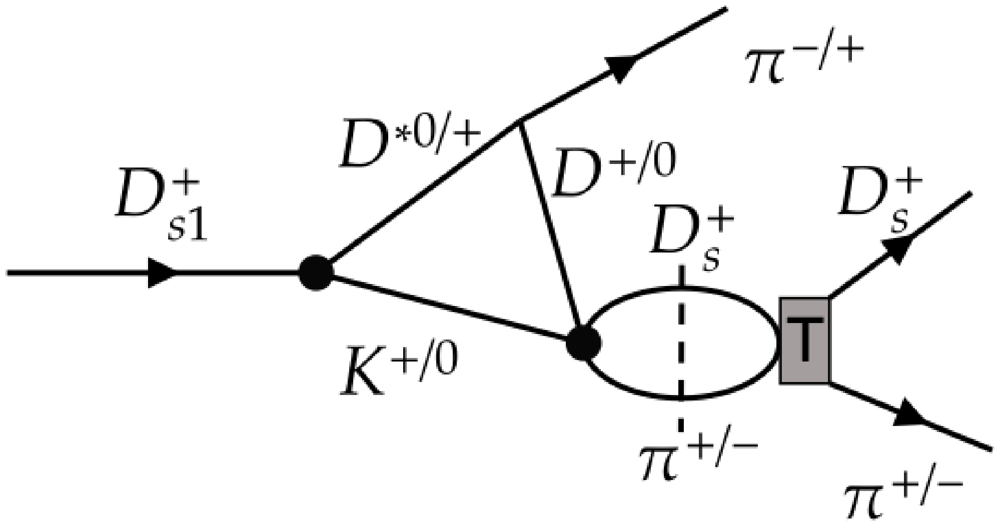


LHCb, arXiv:2411.03399

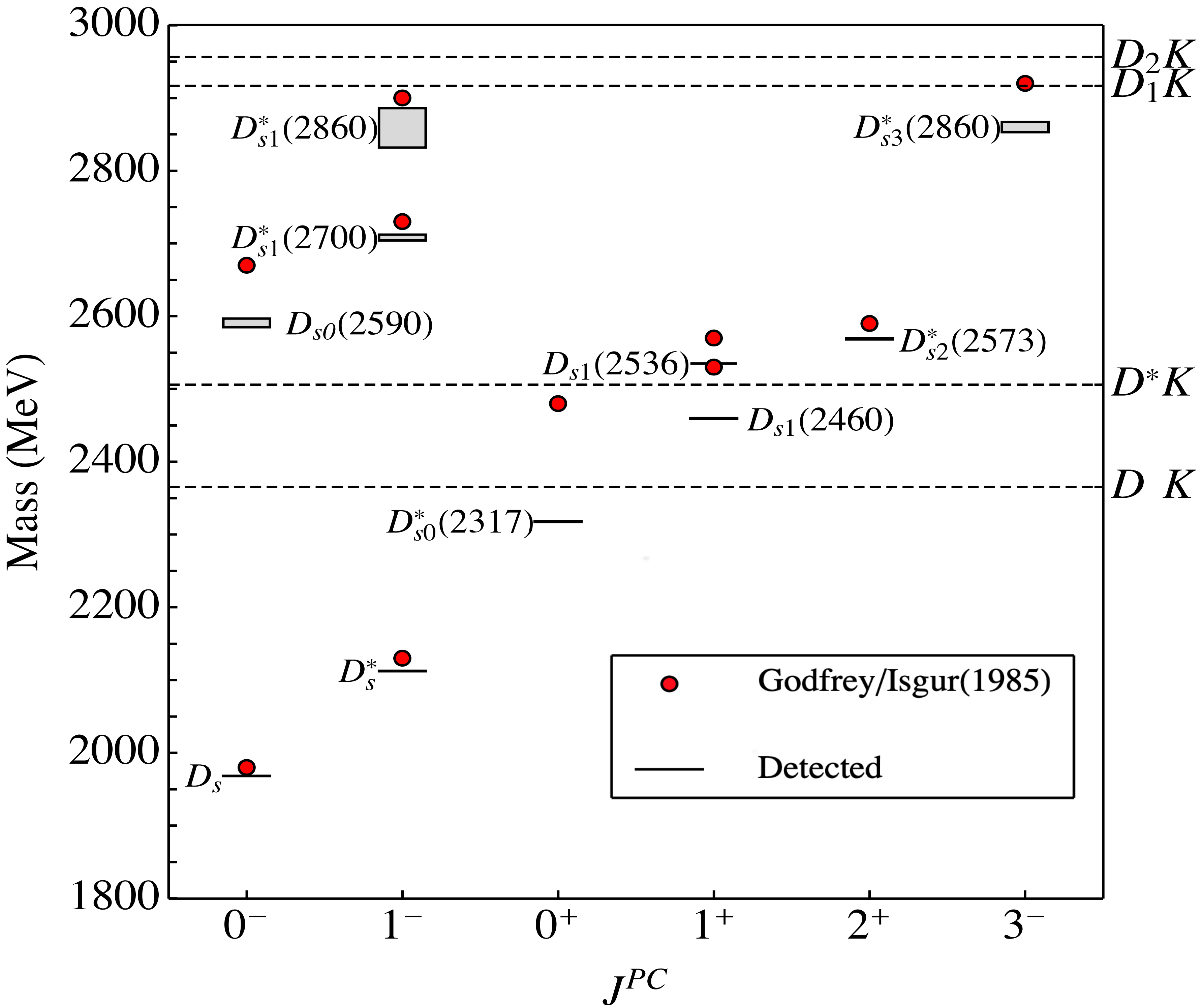


Is possible to investigate the structure of D_{s1} states?

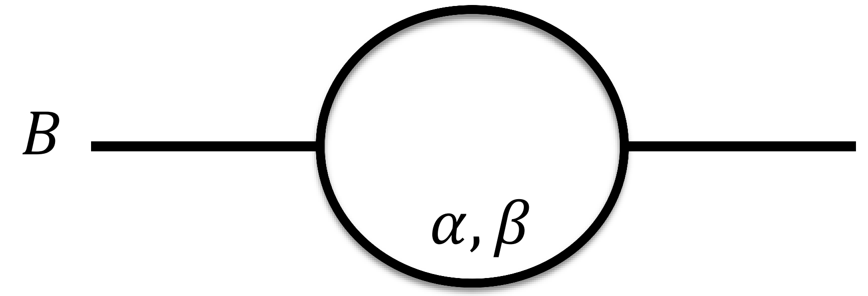
- $D_{s1}(2460) \to D_s^+ \pi^+ \pi^-$
- $D_{s1}(2536) \to D_s^+ \pi^+ \pi^-$



GI quark model for D_s meson

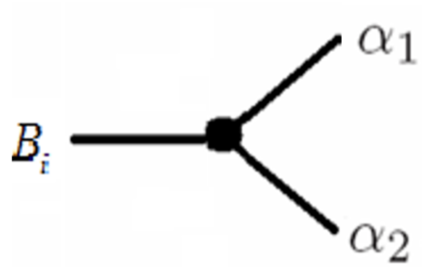


Coupled-channel framework

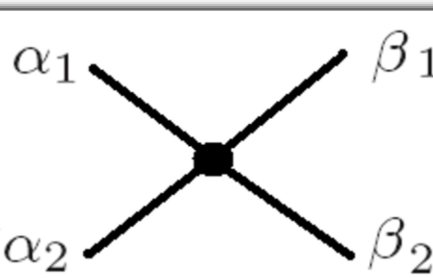


- Coupled-channel effect due to hadron loop could cause sizable mass shift on the state in quark model. Yu. S. Kalashnikova, Phys.Rev.D 72, 034010 (2005); Z.-Y. Zhou and Z. Xiao, Phys. Rev. D 84, 034023 (2011)

bare state core -> channel：



channel -> channel：



Phys.Rev.Lett. 128,112001(2022)

$$g = \sum_{\alpha, B} \int d^3\vec{k} \left\{ |\alpha(\vec{k})\rangle g_{\alpha\, B}(|\vec{k}|) \langle B| + h.c. \right\}$$

$$v = \sum_{\alpha,\beta} \int d^3\vec{k} d^3\vec{k}' |\alpha(\vec{k})\rangle V^L_{\alpha\,,\beta}(|\vec{k}|, |\vec{k}'|) \langle \beta(\vec{k}')|$$

Quark pair creation model (QPC):

$$g_{\alpha\, B}(|\vec{k}|) = \gamma I_{\alpha\, B}(|\vec{k}|) e^{-\frac{\vec{k}^2}{2\Lambda'^2}}$$

truncate the hard vertices given by usual QPC

P. G. Ortega, et al, Phys. Rev. D 94, 074037 (2016)

Effective Lagrangian: (exchanging mesons, e.g. ρ/ω)

Form factor: $\left(\frac{\Lambda^2}{\Lambda^2 + p_f^2}\right)^2 \left(\frac{\Lambda^2}{\Lambda^2 + p_i^2}\right)^2$

Component and pole mass of D_s states

Phys.Rev.Lett. 128,112001(2022)

	$P(c\bar{s})[\%]$	ours	exp
$D_{s0}^*(2317)$	$32.0^{+5.2}_{-3.9}$	$2338.9^{+2.1}_{-2.7}$	2317.8 ± 0.5
$D_{s1}^*(2460)$	$52.4^{+5.1}_{-3.8}$	$2459.4^{+2.9}_{-3.0}$	2459.5 ± 0.6
$D_{s1}^*(2536)$	$98.2^{+0.1}_{-0.2}$	$2536.6^{+0.3}_{-0.5}$	2535.11 ± 0.06
$D_{s2}^*(2573)$	$95.9^{+1.0}_{-1.5}$	$2570.2^{+0.4}_{-0.8}$	2569.1 ± 0.8

$D_{s1}(2460)$

- Both the bare $c\bar{s}$ core and molecular components are significant and essential.

$D_{s1}(2536)$

- Mainly pure $c\bar{s}$.

Coupling of D_{s1} to D^*K

The coupling of D_{s1} to D^*K can be obtained from the residue of the T-matrix:

$$g_i^2 = \frac{r}{2\pi}\int_0^{2\pi} T_{ii}(z(\theta))e^{i\theta}d\theta \longrightarrow \left|\frac{g_S^{D_{s1}(2536)}}{g_D^{D_{s1}(2536)}}\right|_{theory} = 0.7$$

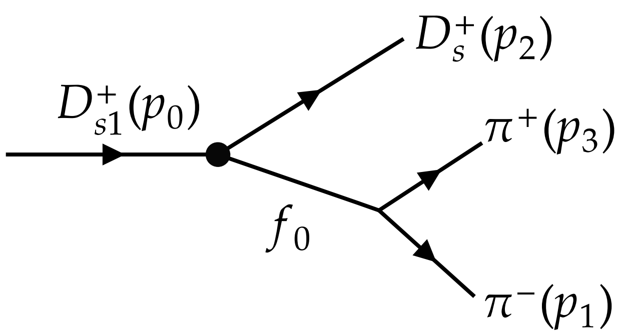
The coupling can also obtained using the experimental branching fractions:

Particle Data Group

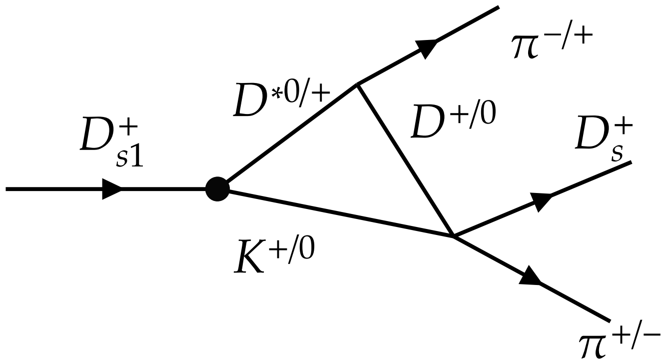
$$B(D^{*+}K^0)_{S-wave} = 0.61 \qquad B(D^{*+}K^0)_{D-wave} = 0.24$$

$$\mathcal{M}_S^i = g_S^i \epsilon_i^\mu \epsilon_{j,\mu}^\dagger, \quad \mathcal{M}_D^i = \frac{g_D^i}{M^2}\epsilon_i^\mu \epsilon_j^{\dagger\nu}\left(q_\mu q_\nu - \frac{g_{\mu\nu}q^2}{4}\right) \longrightarrow \left|\frac{g_S^{D_{s1}(2536)}}{g_D^{D_{s1}(2536)}}\right|_{\mathrm{exp}} = 0.6$$

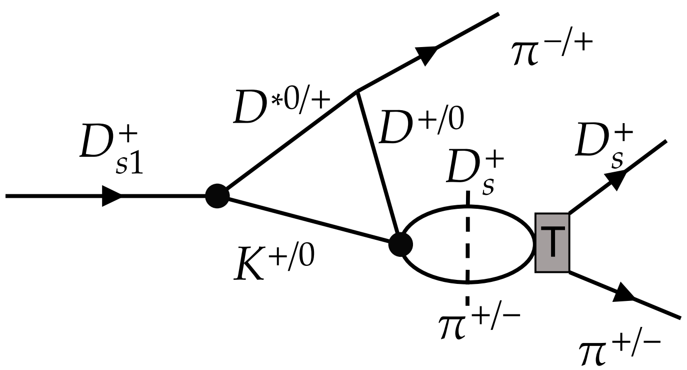
Estimate the lineshape for $D_{s1}(2536)$ decay



(a)

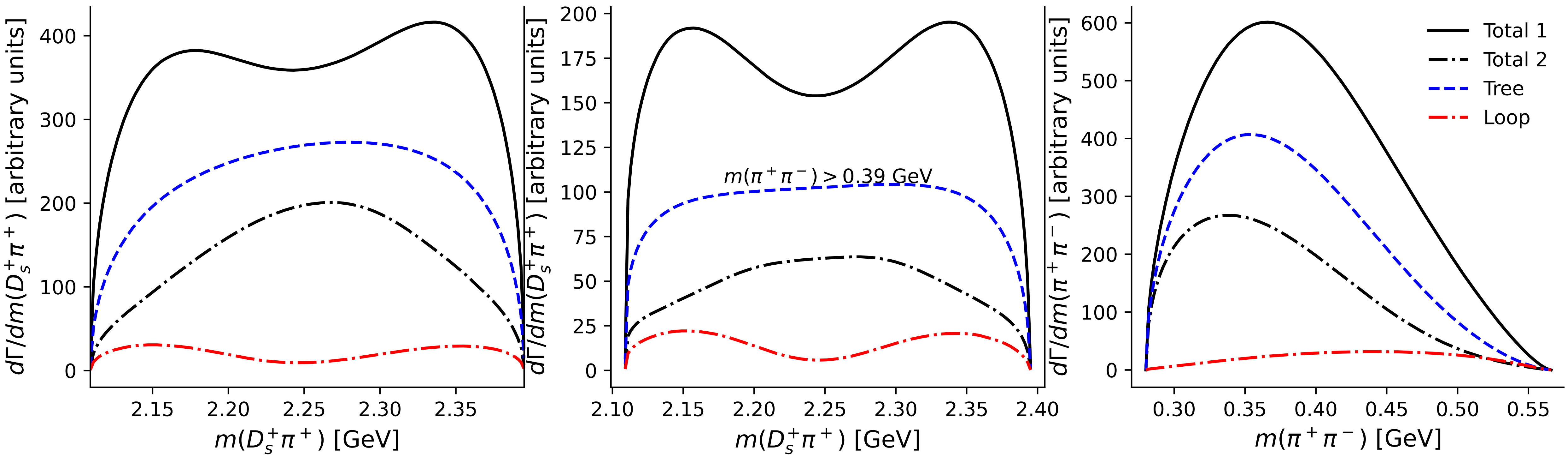


(b)



(c)

- Total 1 and Total 2 are for two choice of the phase for the tree diagram.
- No peak structure in the case of Total 2.



Summary

- The $T_{c\bar{s}}$ lineshape can be discribed through $D_s\pi - DK$ coupled-channel interactions, revealing how off-diagonal potential terms generate the observed resonance pole;
- Predictive calculations for $D_{s1}(2536)$ decays using structural parameters derived from our prior analysis.