

第八届强子谱与强子结构研讨会

Phys. Rev. D 111 (2025) 016004

The $\Lambda_c^+ \rightarrow \eta \pi^+ \Lambda$ reaction and the Λa_0^+ (980) and $\pi^+ \Lambda$ (1670) contributions

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2025年7月13日@桂林

Background





Nature Rev. Phys. 1, 480 (2019)

Low-lying baryons with J^P=1/2⁻



		W	orkma	n R	L, et	<i>al.</i> , R	eviev	v of	Partic	le P	hysi	cs (202	4).	
p	$1/2^{+}$	****	∆ (1232)	3/2+	****	Σ^+	$1/2^{+}$	****	Λ_c^+	$1/2^{+}$	****	Λ_{b}^{0}	$1/2^{+}$	***
n	$1/2^{+}$	****	$\Delta(1600)$	$3/2^{+}$	****	Σ^0	$1/2^{+}$	****	$\Lambda_{c}(2595)^{+}$	$1/2^{-}$	***	$\Lambda_{b}(5912)^{0}$	$1/2^{-}$	***
N(1440)	$1/2^{+}$	****	$\Delta(1620)$	$1/2^{-}$	****	Σ^{-}	$1/2^{+}$	****	$\Lambda_{c}(2625)^{+}$	$3/2^{-}$	***	$\Lambda_{b}(5920)^{0}$	3/2-	***
N(1520)	$3/2^{-}$	****	$\Delta(1700)$	$3/2^{-}$	****	$\Sigma(1385)$	$3/2^{+}$	****	$\Lambda_{c}(2765)^{+}$		*	$\Lambda_{b}(6070)^{0}$	$1/2^{+}$	***
N(1535)	$1/2^{-}$	****	$\Delta(1750)$	$1/2^{+}$	*	$\Sigma(1580)$	$3/2^{-}$	*	$\Lambda_{c}(2860)^{+}$	$3/2^{+}$	***	$\Lambda_{b}(6146)^{0}$	$3/2^{+}$	***
N(1650)	$1/2^{-}$	****	$\Delta(1900)$	$1/2^{-}$	***	Σ(1620)	$1/2^{-}$	*	$\Lambda_{c}(2880)^{+}$	$5/2^{+}$	***	$\Lambda_b(6152)^0$	$5/2^{+}$	***
N(1675)	$5/2^{-}$	****	$\Delta(1905)$	$5/2^{+}$	****	$\Sigma(1660)$	$1/2^{+}$	***	$\Lambda_{c}(2910)^{+}$		*	Σ_b	$1/2^{+}$	***
N(1680)	$5/2^{+}$	****	$\Delta(1910)$	$1/2^{+}$	****	$\Sigma(1670)$	$3/2^{-}$	****	$\Lambda_{c}(2940)^{+}$	$3/2^{-}$	***	Σ_{b}^{*}	3/2+	***
N(1700)	$3/2^{-}$	***	$\Delta(1920)$	3/2+	***	$\Sigma(1750)$	$1/2^{-}$	***	$\Sigma_c(2455)$	$1/2^{+}$	****	$\Sigma_{b}(6097)^{+}$		***
N(1710)	$1/2^{+}$	****	Δ (1930)	$5/2^{-}$	***	$\Sigma(1775)$	$5/2^{-}$	****	$\Sigma_{c}(2520)$	$3/2^{+}$	***	$\Sigma_{b}(6097)^{-}$		***
N(1720)	$3/2^{+}$	****	$\Delta(1940)$	$3/2^{-}$	**	$\Sigma(1780)$	$3/2^{+}$	*	$\Sigma_{c}(2800)$		***	Ξ_{b}^{-}	$1/2^{+}$	***
N(1860)	$5/2^{+}$	**	$\Delta(1950)$	$7/2^{+}$	****	$\Sigma(1880)$	$1/2^{+}$	**	Ξ_c^+	$1/2^{+}$	***	$= \tilde{b}$	$1/2^{+}$	***
N(1875)	$3/2^{-}$	***	$\Delta(2000)$	$5/2^{+}$	**	$\Sigma(1900)$	$1/2^{-}$	**	=0	$1/2^{+}$	****	$\Xi'_{k}(5935)^{-}$	$1/2^{+}$	***
N(1880)	$1/2^{+}$	***	$\Delta(2150)$	$1/2^{-}$	*	$\Sigma(1910)$	$3/2^{-}$	***	Ξ'^+	$1/2^{+}$	***	$\Xi_{h}(5945)^{0}$	$3/2^{+}$	***
N(1895)	$1/2^{-}$	****	$\Delta(2200)$	7/2	***	$\Sigma(1915)$	$5/2^{+}$	****	="0"	$1/2^{+}$	***	$\Xi_{h}(5955)^{-}$	3/2+	***
N(1900)	$3/2^{+}$	****	$\Delta(2300)$	9/2+	**	$\Sigma(1940)$	$3/2^{+}$	*	$\Xi_{c}(2645)$	$3/2^{+}$	***	$\Xi_{b}(6087)^{0}$	3/2-	***
N(1990)	$7/2^{+}$	**	Δ (2350)	5/2	*	$\Sigma(2010)$	3/2	*	$\Xi_{c}(2790)$	$1/2^{-}$	***	$\Xi_{b}(6095)^{0}$	3/2-	***
N(2000)	$5/2^{+}$	**	$\Delta(2390)$	$7/2^{+}$	*	Σ(2030)	7/2+	****	$\Xi_{c}(2815)$	$3/2^{-}$	***	$\Xi_{b}(6100)^{-}$	3/2-	***
N(2040)	$3/2^{+}$	*	Δ (2400)	9/2	**	$\Sigma(2070)$	5/2+	*	$\Xi_{c}(2882)$,	*	$\Xi_{b}(6227)^{-}$,	***
N(2060)	5/2	***	Δ (2420)	$11/2^+$	****	$\Sigma(2080)$	$3/2^{+}$	*	$\Xi_{c}(2923)$		**	$\Xi_{b}(6227)^{0}$		***
N(2100)	$1/2^{+}$	***	$\Delta(2750)$	13/2	**	$\Sigma(2100)$	$7/2^{-}$	*	$\Xi_{c}(2930)$		**	$\Xi_{b}(6327)^{0}$		***
N(2120)	$3/2^{-}$	***	Δ (2950)	$15/2^+$	**	$\Sigma(2110)$	$1/2^{-}$	*	$\Xi_{c}(2970)$	$1/2^{+}$	***	$\Xi_{b}(6333)^{0}$		***
N(2190)	7/2	****				Σ(2230)	3/2+	*	$\Xi_{c}(3055)$,	***	Ω_{h}^{-}	$1/2^{+}$	***
N(2220)	9/2+	****	Λ	$1/2^{+}$	****	$\Sigma(2250)$		**	$\Xi_{c}(3080)$		***	$\Omega_{b}^{-}(6316)^{-}$,	***
N(2250)	9/2-	****	<i>Л</i> (1380)	$1/2^{-}$	**	Σ(2455)		*	$\Xi_{c}(3123)$		*	$\Omega_{h}(6330)^{-}$		***
N(2300)	$1/2^{+}$	**	Λ(1405)	$1/2^{-}$	****	$\Sigma(2620)$		*	Ω_{c}^{0}	$1/2^{+}$	***	$\Omega_{b}(6340)^{-}$		***
N(2570)	$5/2^{-}$	**	A(1520)	3/2-	****	Σ(3000)		*	$\Omega_{c}^{(2770)^{0}}$	$3/2^{+}$	***	$\Omega_b(6350)^-$		***
N(2600)	$11/2^{-}$	***	A(1600)	1/2+	****	Σ(3170)		*	$\Omega_{c}(3000)^{0}$	/	***	5(1111)		
N(2700)	$13/2^{+}$	**	$\Lambda(1670)$	$1/2^{-}$	****	- 0			$\Omega_{c}(3050)^{0}$		***	$P_{c\overline{c}}(4312)^{+}$		*
			A(1690)	3/2	****	=0	$1/2^{+}$	****	$\Omega_{c}(3065)^{0}$		***	$P_{c\overline{c}s}(4338)^{(1)}$	$^{0}1/2^{-}$	*
			<i>Л</i> (1710)	$1/2^{+}$	*	Ξ^{-}	1/2+	****	$\Omega_{c}(3090)^{0}$		***	$P_{c\bar{c}}(4380)^+$,	*

These exotic properties of the low-lying excited baryons with the quantum numbers of spinparity $J^P = 1/2^-$ are difficult to explain in the simple quenched quark model. EW-Geng-Wu-Xie-Zou, CPL. 41 (2024) 101401

Zou, EPJA 35 (2008) 325							
Mass pattern : quenched or unquenched ?							
uds (L=1) 1/2 ⁻ ~ A*(1670)~ [us][ds] s							
uud (L=1) 1/2 ⁻ ~ N*(1535) ~ [ud][us] s							
uds (L=1) $1/2^- \sim \Lambda^*(1405) \sim [ud][su] \overline{u}$							
uus (L=1) 1/2 ⁻ ~ $\Sigma^*(1390)$ ~ [us][ud] \overline{d}							
Zou et al, NPA835 (2010) 199 ; CLAS, PRC87(2013)035							

N*(1535) large couplings $g_{N^*N\eta}$, $g_{N^*K\Lambda}$, $g_{N^*N\eta}$, $g_{N^*N\eta}$, $g_{N^*N\phi}$ $\Lambda^*(1670)$ large coupling $g_{\Lambda^*\Lambda\eta}$

Report of Bing-Song Zou

**** Existence is certain, and properties are at least fairly explored.

*** Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, etc. are not well determined.

** Evidence of existence is only fair.

Evidence of existence is poor.

The spectrum shape of $\Lambda(1670)$





Background



- PART of theoretical explanations of spectrum shape of Λ(1670)
 Cusp:
 - Phys. Rev. D 100 (2019) 054006: Considering the Triangle mechanism (a_0 -loop and $\Sigma(1660)$ -loop) Eur. Phys. J. C (2024) 84:1253 : Considering the Triangle mechanism (a_0 -loop) Phys. Lett. B 857 (2024) 139003 : Considering the meson-baryon rescattering
- ➢ Dip:

Phys. Rev. C 92 (2015) 025205: Comprehensive partial-wave analysis of K^-p reactions Nucl. Phys. B 119 (1977) 362-400: Partial wave analyses of $\overline{K}N$ two-body reactions

> Peak :

Phys. Rev. D 106 (2022) 056001: Considering the meson-baryon rescatteringPhys. Rev. D 110 (2024) 054020: Considering the meson-baryon rescattering

Scalar meson



□ Masses puzzle

Traditional quark model

 $f_0(500) \approx a_0(980) < K_0^*(700) < f_0(980)$

> Experiment

$$f_0(500) < K_0^*(700) < a_0(980) < f_0(980)$$

The light scalar meson $a_0(980)$ has been explained to be either a molecular state, a tetraquark state, a conventional $q\overline{q}$ meson, or the mixing of different components.

D PART of theoretical interpretation of $a_0(980)$

> $K\overline{K}$ molecular state:

Phys. Rev. Lett. 48 (1982) 659 Phys. Rev. D 41 (1990) 2236

- Compact tetraquark state:
 Phys. Rev. Lett. 92 (2004) 102001
 Eur. Phys. J. A 30 (2006) 423-426
 Phys. Rev. Lett. 111 (2013) 062001
- Dynamically generated states:
 Phys. Rev. D 52 (1995) 2690
 Phys. Lett. B 803 (2020) 135279
 Phys. Lett. B 846 (2023) 138185

Analysis the Belle data







Belle Collaboration, PRD 103 (2021) 052005

PRD 106 (2022) 056001

Reanalysis the Belle data





The BESIII measurement



\Box In 2025, $\Lambda_c^+ \rightarrow \Lambda \eta \pi^+$ has been posteriorly measured by the BESIII **Collaboration** BESIII Collaboration, Phys. Rev. Lett. 134 (2025) 021901 200 + sWeighted data + sWeighted data Events / (0.025 GeV/c²) Events / (0.020 GeV/c²) Events / (0.021 GeV/c²) — Total fit Baseline model 40 200 $- \Lambda a_0(980)^+$ 100 Model A Events / 0.080 $\Lambda NR_{0^+}(\pi^+\eta)$ Model B 100 $-\Sigma(1385)^{+}\eta$ $-\Lambda(1670)\pi^+$ 50 100 Total interference 1.8 -0.5 0.5 0.8 0.9 1.3 1.5 1.6 1.7 0 0.7 1.4 1.1 M_{π^+n} (GeV/ c^2) $M_{\Lambda n} \,({\rm GeV}/c^2)$ $\cos(\theta_{\gamma^{*+}})$ $M_{\Lambda\pi^+}$ (GeV/c²)

TABLE II. Fit results of FFs and statistical significances for different components in alternative models including $\Sigma(1380)^+$. The total FFs are 115.8% and 119.8% for models A and B, respectively. The uncertainties are statistical only.

Process	Model A	Model B
$\overline{\Lambda a_0(980)^+}$	$52.9 \pm 4.5(13.4\sigma)$	$50.6 \pm 8.0(11.1\sigma)$
$\Sigma(1385)^+\eta$	$36.6 \pm 2.6(15.8\sigma)$	$31.3 \pm 3.0(14.6\sigma)$
$\Lambda(1670)\pi^+$	$10.7 \pm 1.4(15.0\sigma)$	$9.0 \pm 1.6(11.9\sigma)$
$\Sigma(1380)^{+}\eta$	$15.5 \pm 4.4(6.1\sigma)$	$17.7 \pm 5.7(3.3\sigma)$
ΛNR_{0^+}	••••	$11.3 \pm 4.4(4.2\sigma)$



In spite of the small signal seen in the Dalitz plot, the analysis reports a branching fraction of approximately 50% for the Λa_0^+ (980) decay mode.

Belle Collaboration, PRD 103 (2021) 052005



Quark level diagram



Hadronization

$$\begin{split} \Lambda_{c}^{+} &= \frac{1}{\sqrt{2}} c(ud - du) \chi_{MA} \to \pi^{+} \frac{1}{\sqrt{2}} s(ud - du) \chi_{MA} \\ &= \pi^{+} \sum_{i} \frac{1}{\sqrt{2}} s \bar{q}_{i} q_{i} (ud - du) \chi_{MA} \\ &= \frac{1}{\sqrt{2}} \pi^{+} \sum_{i} P_{3i} q_{i} (ud - du) \chi_{MA} \\ &= \frac{1}{\sqrt{2}} \pi^{+} \left\{ K^{-} (uud - udu) + \bar{K}^{0} (dud - ddu) \\ &- \frac{\eta}{\sqrt{3}} (sud - sdu) \right\}, \end{split}$$

$$H = \pi^{+} \left\{ \frac{1}{\sqrt{2}} K^{-} p + \frac{1}{\sqrt{2}} \bar{K}^{0} n + \frac{1}{3} \eta \Lambda \right\}$$



Mechanisms for tree level and rescattering



The mechanisms from the intermediate $\Sigma(1385)$



Spin flip part

ţ.



□ The total decay amplitude

 $t = t_1 + t_2,$

$$t_{1} = A \left\{ h_{\pi^{+}\eta\Lambda} + h_{\pi^{+}\eta\Lambda}G_{\eta\Lambda}(M_{\mathrm{inv}}(\eta\Lambda))t_{\eta\Lambda,\eta\Lambda}(M_{\mathrm{inv}}(\eta\Lambda)) + h_{\pi^{+}\eta\Lambda}G_{\pi^{+}\eta}(M_{\mathrm{inv}}(\pi^{+}\eta))t_{\pi^{+}\eta,\pi^{+}\eta}(M_{\mathrm{inv}}(\pi^{+}\eta)) + h_{\pi^{+}\bar{K}N}G_{K^{-}p}(M_{\mathrm{inv}}(\eta\Lambda))t_{K^{-}p,\eta\Lambda}(M_{\mathrm{inv}}(\eta\Lambda)) + h_{\pi^{+}\bar{K}N}G_{\bar{K}^{0}n}(M_{\mathrm{inv}}(\eta\Lambda))t_{\bar{K}^{0}n,\eta\Lambda}(M_{\mathrm{inv}}(\eta\Lambda)) + \frac{\beta}{M_{\Lambda}}\frac{2}{3}\vec{P}_{\pi}^{*}\cdot\vec{P}_{\eta}^{*}D \right\},$$

$$h_{\pi^+\eta\Lambda} = \frac{1}{3}; \quad h_{\pi^+\bar{K}N} = \frac{1}{\sqrt{2}},$$
$$t_2 = -\frac{i}{3} \frac{A\beta}{M_\Lambda} \epsilon_{ijs} \sigma_s \vec{P}^*_{\pi i} \vec{P}^*_{\eta j} D,$$

 $K^- p \quad \bar{K}^0 n \quad \pi^0 \Lambda \quad \pi^0 \Sigma^0 \quad \eta \Lambda \quad \eta \Sigma^0 \quad \pi^+ \Sigma^- \quad \pi^- \Sigma^+ \quad K^+ \Xi^- \quad K^0 \Xi^0$

\Box The $\Lambda(1670)$ amplitudes

Nucl. Phys. A 635 (1998) 99-120

$$V_{ij} = -C_{ij}\frac{1}{4f^2}(k^0 + k'^0)$$

$$T = [1 - VG]^{-1}V,$$



\Box The $a_0(980)$ amplitudes

$$K^+\overline{K}^0$$
 (1) and $\pi^+\eta$ (2)

$$V_{11} = -\frac{s}{4f^2}, \quad (f = 93 \text{ MeV}),$$

$$V_{12} = -\frac{1}{3\sqrt{3}f^2}(3s - 2m_K^2 - m_\eta^2),$$

$$V_{22} = -\frac{2m_\pi^2}{3f^2},$$

D The cutoff method

$$\begin{split} G(s) = & \frac{1}{16\pi^2 s} \left\{ \sigma \left(\arctan \frac{s + \Delta}{\sigma \lambda_1} + \arctan \frac{s - \Delta}{\sigma \lambda_2} \right) \\ & - \left[(s + \Delta) \ln \frac{q_{\max} \left(1 + \lambda_1 \right)}{m_1} \right. \\ & \left. + (s - \Delta) \ln \frac{q_{\max} \left(1 + \lambda_2 \right)}{m_2} \right] \right\}, \end{split}$$

$$\sigma = \left[-\left(s - (m_1 + m_2)^2\right) \left(s - (m_1 - m_2)^2\right) \right]^{1/2},$$

$$\Delta = m_1^2 - m_2^2,$$

$$\Box$$ The $a_0(980)$ amplitudes

 $M_{cut} = 1050 \text{ MeV}$

$$Gt(M_{\rm inv}) = Gt(M_{\rm cut})e^{-\alpha(M_{\rm inv}-M_{\rm cut})}, \text{ for } M_{\rm inv} > M_{\rm cut}$$

$$\lambda_1 = \sqrt{1 + \frac{m_1^2}{q_{\max}^2}}, \quad \lambda_2 = \sqrt{1 + \frac{m_2^2}{q_{\max}^2}},$$

Results



\Box The invariant mass distributions of the $\Lambda_c^+ \to \Lambda \eta \pi^+$ decay



Formalism-internal emission



Quark level diagram



Hadronization

$$\frac{1}{\sqrt{2}}c(ud - du)\chi_{MA} \to \frac{1}{\sqrt{2}}\bar{K}^{0}(u\bar{q}_{i}q_{i}(ud - du))\chi_{MA} \\
= \frac{1}{\sqrt{2}}\bar{K}^{0}\left\{\left(\frac{\pi^{0}}{\sqrt{2}} + \frac{\eta}{\sqrt{3}}\right)u(ud - du) + \pi^{+}d(ud - du) \\
+K^{+}s(ud - du)\right\}\chi_{MA} \\
= \frac{\bar{K}^{0}}{\sqrt{2}}\left\{\left(\frac{\pi^{0}}{\sqrt{2}} + \frac{\eta}{\sqrt{3}}\right)p + \pi^{+}n - \sqrt{\frac{2}{3}}K^{+}\Lambda\right\}\chi_{MA},$$

D The internal emission amplitudes

$$\begin{split} t^{\rm ie} &= \gamma h_{\bar{K}^0 K^+ \Lambda} G_{\bar{K}^0 K^+} (M_{\rm inv} (\pi^+ \eta)) t_{\bar{K}^0 K^+, \pi^+ \eta} (M_{\rm inv} (\pi^+ \eta)), \\ & \gamma = -\frac{1}{3} \\ & h_{\bar{K}^0 K^+ \Lambda} = -\frac{1}{\sqrt{3}}, \end{split}$$

Results



\Box The invariant mass distributions of the $\Lambda_c^+ \rightarrow \Lambda \eta \pi^+$ decay







- ➤ The consideration of the $a_0(980)$ and $\Lambda(1670)$ as dynamically generated has allowed us to find a reasonable description of the invariant mass distributions for the $\Lambda_c^+ \rightarrow \eta \pi^+ \Lambda$.
- > While the spin flip part of the $\Sigma(1385)$ contribution appears with a strength of 1/4 with respect to the non spin flip part in the mass distributions, the different dependence on the invariant masses of these two terms, makes them to show up with different shapes in the mass distributions.

Thank you very much!