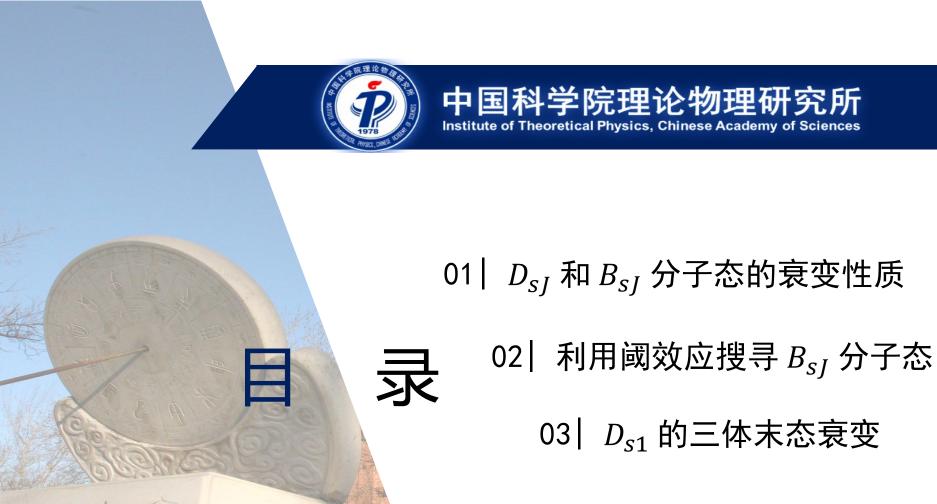


# 築-奇异奇特强子及其伙伴态的衰变 性质

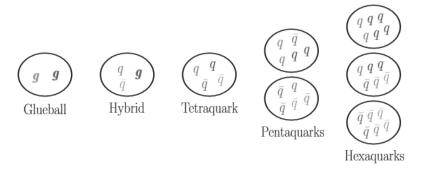
付海龙

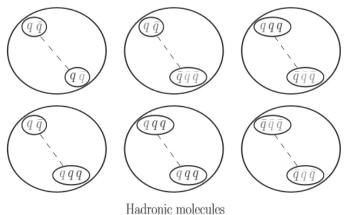
2025.07.14

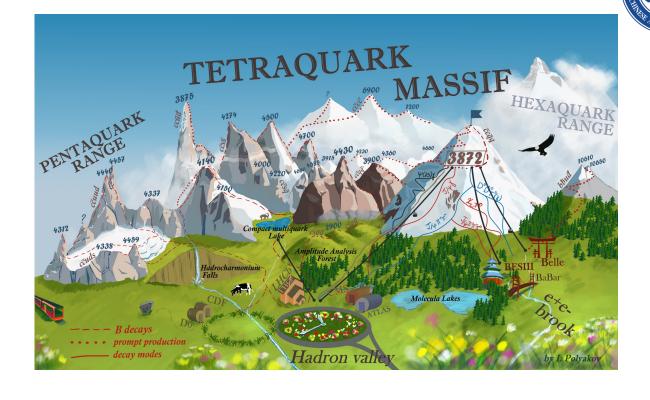
中国科学院理论物理研究所第八届强子谱和强子结构研讨会



## 背景介绍:奇特强子态







- 奇特强子态:超出传统的夸克模型
- 近二十年来大量新强子态的实验发现
- 随着实验技术的提高,对于强子性质的描述越来越精确

## 强子分子态的概念

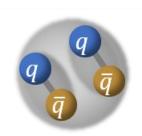




● 强子分子态:

类似于原子核, 由无色的强子之间的相互作用束缚起来

- 区别于紧致多夸克态,空间尺度较大,位于强子对的阈值附近
- 低能系统:具备良好的有效场论描述



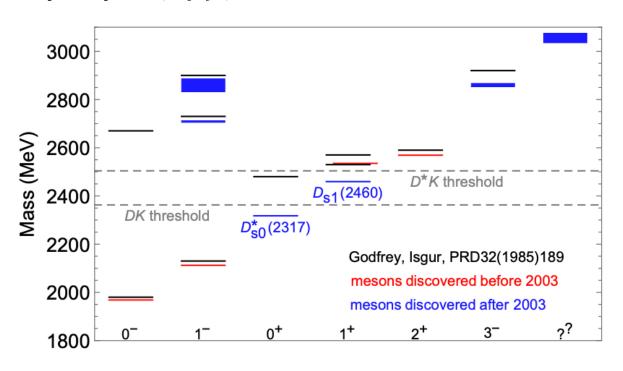


温伯格复合度关系:

$$a \approx -\frac{2(1-Z)}{(2-Z)\sqrt{2\mu E_B}}, \quad r_e \approx \frac{Z}{(1-Z)\sqrt{2\mu E_B}}$$

## 粲-轻奇特强子





$$D_{s0}^*(2317)$$
: BaBar (2003)

$$J^P = 0^+, \ \Gamma < 3.8 \ {\rm MeV}$$

$$D_{s1}(2460)$$
: CLEO (2003)

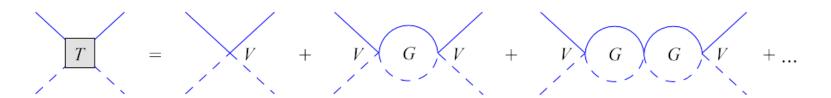
$$J^P=1^+,~\Gamma<3.5~{\rm MeV}$$

- 质量低于夸克模型的预言
- 精细调节的质量:  $M_{D_{s1}(2460)} M_{D_{s0}^*(2317)} \simeq M_{D^{*\pm}} M_{D^{\pm}}$ ? (141.8±0.8) MeV

## 粲-轻系统的手征幺正方法



● 手征幺正方法



● 手征拉氏量

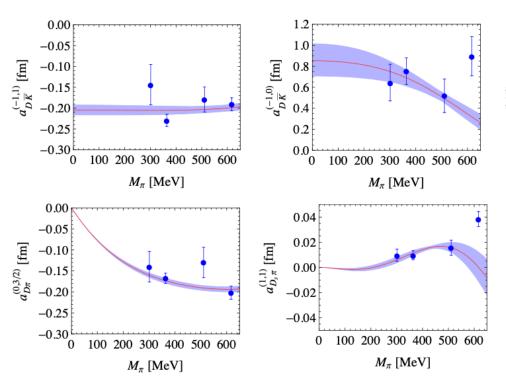
$$\mathcal{L}_{\phi P}^{(1)} = D_{\mu}PD^{\mu}P^{\dagger} - m^{2}PP^{\dagger} \propto E_{\phi} + \mathcal{O}(1/M_{D})$$
 ( $S$ -wave) Weinberg-Tomozawa
  $P = (D^{0}, D^{+}, D_{s}^{+})$   $\mathcal{L}_{\phi P}^{(2)} = P\left[-h_{0}\langle\chi_{+}\rangle - h_{1}\chi_{+} + h_{2}\langle u_{\mu}u^{\mu}\rangle - h_{3}u_{\mu}u^{\mu}\right]P^{\dagger}$   $+D_{\mu}P\left[h_{4}\langle u_{\mu}u^{\nu}\rangle - h_{5}\{u^{\mu}, u^{\nu}\}\right]D_{\nu}P^{\dagger}$ 

Feng-Kun Guo et al., Phys.Lett.B 666 (2008)

#### ● 通过格点QCD的结果拟合低能常数







Liuming Liu et al., Phys.Rev.D 87 (2013)

$a_D$	h <sub>24</sub>	$h_4'$	h <sub>35</sub>	$h_5'$
-1.88	-0.10	-0.32	0.25	-1.88

#### ● 势能项:

$$V(s,t,u) = \frac{1}{F_{\pi}^{2}} \left[ \frac{C_{LO}}{4} (s-u) - 4C_{0}h_{0} + 2C_{1}h_{1} - 2C_{24}H_{24} + 2C_{35}H_{35} \right]$$

$$H_{35} = h_{35}p_2 \cdot p_4 + h_5(p_1 \cdot p_2p_3 \cdot p_4 + p_1 \cdot p_4p_2 \cdot p_3 - 2\bar{M}_D^2p_2 \cdot p_4)$$

$$H_{24} = 2h_{24}p_2 \cdot p_4 + h_4(p_1 \cdot p_2p_3 \cdot p_4 + p_1 \cdot p_4p_2 \cdot p_3 - 2\bar{M}_D^2p_2 \cdot p_4)$$

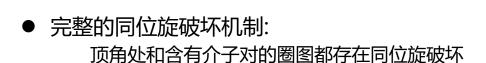
#### ● 低能常数的关系

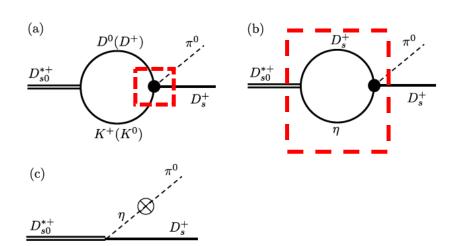
$$\{h_i^{\prime B}\} \sim \{h_i^{\prime D}\} \frac{m_B}{m_D}$$

## 粲-轻奇特强子: 衰变宽度



强子分子态图像下可以给出较大的同位旋破 坏衰变宽度,与紧致态有显著差别

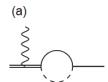




衰变道	卷图	$\pi^0$ -η 混合	完整结果 keV
$D_{s0}^* \to D_s \pi^0$	$50 \pm 3$	$20 \pm 2$	$132 \pm 7$
$D_{s1}\to D_s^*\pi^0$	$37 \pm 7$	$20 \pm 3$	$111 \pm 15$
$B_{s0}^* \to B_s \pi^0$	$15 \pm 2$	$22 \pm 3$	$75 \pm 6$
$B_{s1} \rightarrow B_s^* \pi^0$	$16 \pm 2$	$23 \pm 3$	$76 \pm 7$



Electric Charge (EC):







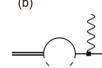




$$\begin{split} \mathcal{L}_{MM} = & \frac{i}{2} e F^{\mu\nu} \sqrt{m_D m_{D^*}} [\varepsilon^{\mu\nu\alpha\beta} v_\alpha (\beta Q + \frac{Q'}{m_Q})_{ab} (P_a V_b^{\dagger\beta} - V_a^\beta P_b^\dagger) \\ & + V_a^\mu V_b^{\dagger\nu} (\beta Q - \frac{Q'}{m_Q})_{ab}] \end{split} \qquad \text{ Jie Hu \& T. Mehen, Phys.Rev.D 73 (2006)} \end{split}$$

Magnetic Moment (MM):





$$\mathcal{L}_{contact} = \kappa F_{\mu\nu} (v^{\mu} D_{s0}^{*} D_{s}^{*\dagger\nu} + D_{s1}^{\mu} v^{\nu} D_{s}^{\dagger} + \varepsilon^{\mu\nu\alpha\beta} D_{s1\alpha} D_{s\beta}^{*\dagger})$$
$$+ \tilde{\kappa} \varepsilon^{\mu\nu\alpha\beta} F_{\mu\nu} v_{\beta} D_{s1\alpha} D_{s0}^{*\dagger} + h.c.$$

• 实验输入: 
$$R_2 = \frac{\Gamma(D_{s1} \to D_s \gamma)}{\Gamma(D_{s1} \to D_s^* \pi^0)}$$
  $\Gamma(D^{*0} \to D^0 \gamma)$   $\Gamma(D^{*+} \to D^+ \gamma)$ 

衰变道	EC	MM	CT	完整结果 keV
$D_{s0}^* \to D_s^* \gamma$	$3.5 \pm 0.3$	$0.06 \pm 0.02$	0.04	$3.7 \pm 0.3$
$D_{s1} \rightarrow D_s \gamma$	$13 \pm 1$	$6.5 \pm 0.6$	0.1	$42 \pm 4$
$D_{s1} \to D_s^* \gamma$	$12 \pm 2$	$0.8 \pm 0.1$	0.1	$13 \pm 2$
$D_{s1} \to D_{s0}^* \gamma$	_	$3.0 \pm 0.6$	?	?
$B_{s0}^* \to B_s^* \gamma$	$58 \pm 8$	$2.1 \pm 0.3$	0.02	$59 \pm 8$
$B_{s1} \rightarrow B_s \gamma$	$70 \pm 10$	$41 \pm 6$	0.02	$220 \pm 31$
$B_{s1} \to B_s^* \gamma$	$110 \pm 15$	$0.19 \pm 0.02$	0.03	$100 \pm 15$
$B_{s1} \rightarrow B_{s0}^* \gamma$	_	$0.03 \pm 0.01$	?	?

## 衰变分支比



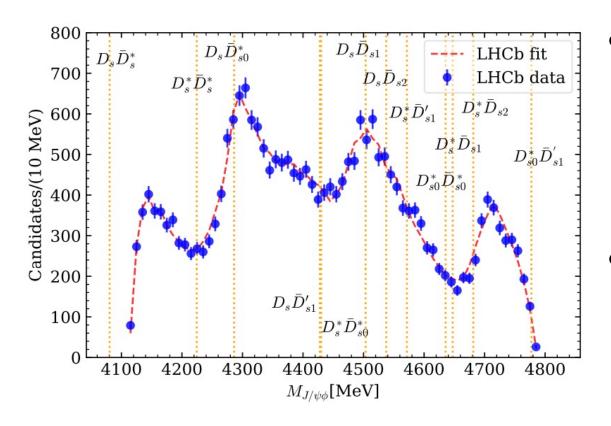
$R_{1} = \frac{\Gamma(D_{s0}^{*} \to D_{s}^{*}\gamma)}{\Gamma(D_{s0}^{*} \to D_{s}\pi^{0})},  R_{2} = \frac{\Gamma(D_{s1} \to D_{s}\gamma)}{\Gamma(D_{s1} \to D_{s}^{*}\pi^{0})},$
$R_{3} = \frac{\Gamma(D_{s1} \to D_{s}^{*}\gamma)}{\Gamma(D_{s1} \to D_{s}^{*}\pi^{0})},  R_{4} = \frac{\Gamma(D_{s1} \to D_{s0}^{*}\gamma)}{\Gamma(D_{s1} \to D_{s}^{*}\pi^{0})},$
$R_5 = \frac{\Gamma(D_{s1} \to D_s^* \pi^0)}{\Gamma(D_{s1} \to D_s^* \pi^0) + \Gamma(D_{s1} \to D_{s0}^* \gamma)},$
$R_{6} = \frac{\Gamma(D_{s1} \to D_{s} \gamma) + \Gamma(D_{s1} \to D_{s0} \gamma)}{\Gamma(D_{s1} \to D_{s}^{*} \pi^{0}) + \Gamma(D_{s1} \to D_{s0}^{*} \gamma)},$
$R_7 = \frac{\Gamma(D_{s1} \to D_s \pi^0) + \Gamma(D_{s1} \to D_{s0} \gamma)}{\Gamma(D_{s1} \to D_s^* \pi^0) + \Gamma(D_{s1} \to D_{s0}^* \gamma)},$
$\Gamma(D_{s1} \to D_{s0}^* \gamma)$
$R_8 = \frac{1}{\Gamma(D_{s1} \to D_s^* \pi^0) + \Gamma(D_{s1} \to D_{s0}^* \gamma)}.$

分支比	理论结果	测量值	理论结果
	粲介子	粲介子	底介子
$R_1$	$0.028 \pm 0.009$	< 0.059	$0.79 \pm 0.13$
$R_2$	0.38(固定) ± 0.08	$0.38 \pm 0.05$	$2.9 \pm 0.5$
$R_3$	$0.12 \pm 0.02$	< 0.16	$1.4 \pm 0.2$
$R_4$	$0.028 \pm 0.006$	< 0.22	$(4\pm1)\times10^{-4}$
$R_5$	$0.97 \pm 0.01$	$0.93 \pm 0.09$	$1.0 \pm 0.1$
$R_6$	$0.37 \pm 0.08$	$0.35 \pm 0.04$	$2.9 \pm 0.5$
$R_7$	$0.12 \pm 0.02$	< 0.24	$1.4 \pm 0.2$
$R_8$	$0.027 \pm 0.004$	< 0.25	$(4\pm1)\times10^{-4}$

## 利用阈效应测量强子分子态质量







 $B_{s0}^*$ 和 $B_{s1}$ 的主要衰变道:

$$B_{s0}^* \to B_s^0 \pi^0, B_s^{*0} \gamma$$
  
 $B_{s1} \to B_s^{*0} \pi^0, B_s \gamma, B_s^* \gamma, B_{s0}^* \gamma$ 

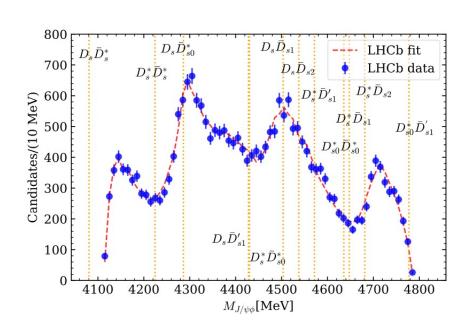
末态光子难以精确测量对发现这些奇特态提出挑战

利用阈效应间接测量辐射衰变为主的强子态质量

## 近阈结构

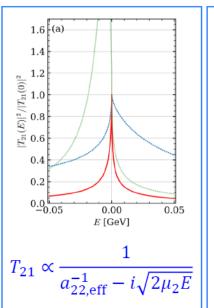
$$T(E) = 8\pi \Sigma_2 \begin{pmatrix} -\frac{1}{a_{11}} + ik_1 & \frac{1}{a_{12}} \\ \frac{1}{a_{12}} & -\frac{1}{a_{22}} - \sqrt{-2\mu_2 E - i\epsilon} \end{pmatrix}^{-1}$$

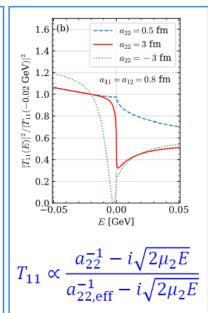
$$\frac{1}{a_{22,\text{eff}}} = \frac{1}{a_{22}} - \frac{a_{11}}{a_{12}^2(1 + a_{11}^2 k_1^2)} - i \frac{a_{11}^2 k_1}{a_{12}^2(1 + a_{11}^2 k_1^2)}$$



Xiang-Kun Dong et al., Prog.Phys. 41 (2021)

#### Xiang-Kun Dong et al., Phys.Rev.Lett. 126 (2021)







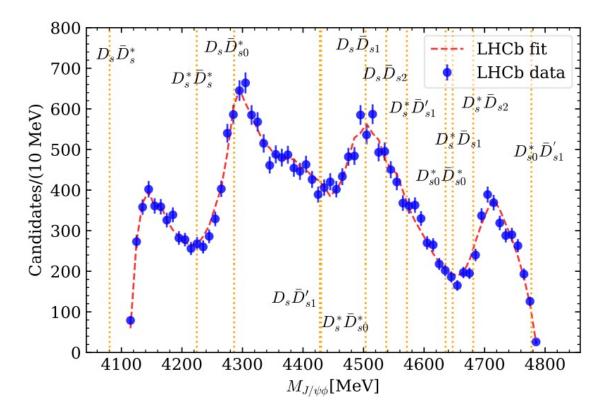


- 对于吸引的相互作用,在一对强子的阈值附近必定出现峰-谷的结构
- 对于虚态,阈值处出现尖峰(cusp),对于束缚态,极点处出现共振峰

## 利用阈效应测量强子分子态质量







- 利用阈效应精确测量辐射衰变为主的强子态质量
- 对于重味系统 $Y\phi$ : 耦合到 $B_{s0}^*\bar{B}_s$

虚态:  $M_{virtual} = M_1 + M_2$ 

束缚态:  $M_{res} = M_1 + M_2 - \Delta M$ 

例子:

$$J/\psi \phi$$
末态:  $X(4274)$  PDG., Phys.Rev.D 110 (2024)

$$4286 \text{ MeV} - m_{D_s} = 2318 \text{ MeV}$$

## 三体系统的低能有效场论

# A STATE OF S



有效场论描述 辅助场方法

$$\mathcal{L}_d = \psi^{\dagger} \left( i \partial_t + rac{
abla^2}{2m} 
ight) \psi + g_2 \ d^{\dagger} d - g_2 \left( d^{\dagger} \psi^2 + \left( \psi^{\dagger} 
ight)^2 d 
ight) - g_3 \ d^{\dagger} d \psi^{\dagger} \psi$$

dimer传播子:

$$\begin{split} iD(p_0,\mathbf{p}) &= iD^0 + iD^0 i\Sigma D^0 + \dots \\ &= iD^0 \sum_{n=0}^{\infty} (-\Sigma D^0)^n = \frac{i}{(D^0)^{-1} + \Sigma}. \\ &iD(p_0,\mathbf{p}) = -\frac{2\pi}{mg_2^2} \frac{i}{-\gamma + \sqrt{-mp_0 + \frac{\mathbf{p}^2}{4} - i\varepsilon}}. \end{split}$$

### S-波散射方程

E. Braaten & H.W. Hammer, Phys.Rept. 428 (2006)

$$\begin{split} T(E,k,p) &= \frac{16\pi\,\gamma}{m} \left[ \frac{1}{2kp} \ln \left( \frac{p^2 + pk + k^2 - E - i\varepsilon}{p^2 - pk + k^2 - E - i\varepsilon} \right) - \frac{1}{4m} \frac{g_3}{g_2^2} \right] \\ &\quad + \frac{4}{\pi} \int_0^{\Lambda} dq \frac{q^2\,T(E,k,q)}{-\gamma + \sqrt{-mE + \frac{3}{4}q^2 - i\varepsilon}} \left[ \frac{1}{2qp} \ln \left( \frac{p^2 + pq + q^2 - E - i\varepsilon}{p^2 - pq + q^2 - E - i\varepsilon} \right) - \frac{1}{4m} \frac{g_3}{g_2^2} \right] \end{split}$$

不加入三体项,在Λ→∞时无法收敛到唯一解。

## 三体力的准周期性行为

#### 三体项作为重整化要求的截断依赖项

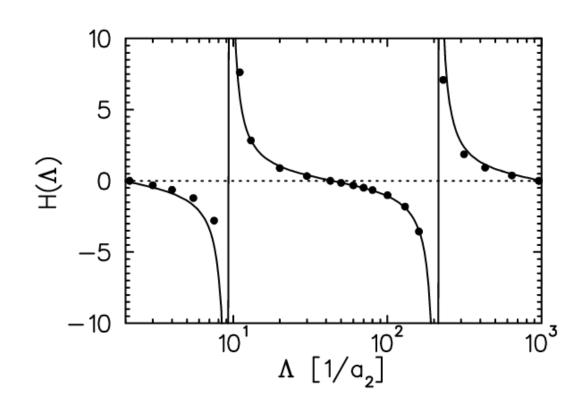
$$g_3 = -\frac{4mg_2^2}{\Lambda^2}H(\Lambda)$$

P. Bedaque et al., Phys.Rev.Lett. 82 (1999)

$$H(\Lambda) = \frac{\cos\left[s_0 \ln\left(\frac{\Lambda}{\Lambda_*}\right) + \arctan\left(s_0\right)\right]}{\cos\left[s_0 \ln\left(\frac{\Lambda}{\Lambda_*}\right) - \arctan\left(s_0\right)\right]}$$

- 新的参数 Λ<sub>\*</sub>,物理意义是三体力为0的点,需要额外的输入来固定
- 所有截断依赖性被三体项吸收
- 周期性行为是重整化群极限环的体现  $\frac{g}{r^2}$ 类型的势能

D.Kaplan et al., Phys.Rev.D 80 (2009)



## 三体 $\overline{D}_sDK$ 系统的散射方程





$$\mathcal{L}_1 = \psi_a^{\dagger} \left( i \partial_0 + \frac{\nabla^2}{2m_i} \right) \psi_a$$

$$\psi_a = (\psi_K, \psi_{\bar{D}_s}, \psi_D)$$

$$\mathcal{L}_2 = \sigma_i^{\dagger} \left( -i\partial_0 + \Delta_i \right) \sigma_i - g_i \left( \sigma_i^{\dagger} \psi_a \psi_b + \text{h.c.} \right)$$

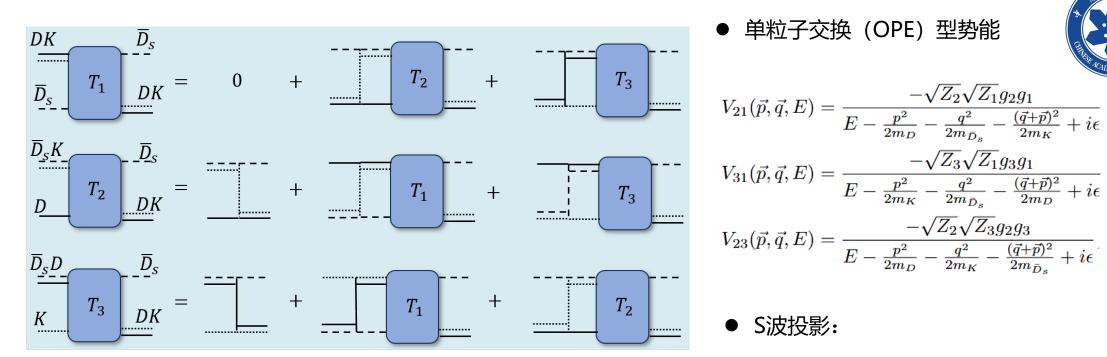
能量: 
$$E(p) = \frac{p^2}{2\mu} - B_{DK}$$

$$iG_i(E, \vec{p}) = \frac{-i 2\pi / (\mu_i g_i^2)}{-1/a_i + \left[2\mu_i \left(\frac{\vec{p}^2}{2M_i} - E - i\epsilon\right)\right]^{1/2}} \qquad Z_i^{-1} = \frac{\mu_i^2 g_i^2 |a_i|}{2\pi}$$

$$|D_{s0}^*\bar{D}_s\rangle = \frac{1}{\sqrt{2}}(|D^0K^+\rangle|\bar{D}_s\rangle + |D^+K^0\rangle|\bar{D}_s\rangle)$$
 1道:  $J = 0, I = 0$ 

$$|\sigma_{\bar{D}_sK}D\rangle = \frac{1}{\sqrt{2}}(|\bar{D}_sK^+\rangle|D^0\rangle + |\bar{D}_sK^0\rangle|D^+\rangle)$$
 2道:  $J = 0, I = 0$ 

$$|\sigma_{\bar{D}_sD}K\rangle = \frac{1}{\sqrt{2}}(|\bar{D}_sD^0\rangle|K^+\rangle + |\bar{D}_sD^+\rangle|K^0\rangle)$$
 3道:  $J = 0, I = 0$ 



#### 单粒子交换 (OPE) 型势能



$$V_{21}(\vec{p}, \vec{q}, E) = \frac{-\sqrt{Z_2}\sqrt{Z_1}g_2g_1}{E - \frac{p^2}{2m_D} - \frac{q^2}{2m_{\bar{D}_s}} - \frac{(\vec{q} + \vec{p})^2}{2m_K} + i\epsilon}$$

$$V_{31}(\vec{p}, \vec{q}, E) = \frac{-\sqrt{Z_3}\sqrt{Z_1}g_3g_1}{E - \frac{p^2}{2m_K} - \frac{q^2}{2m_{\bar{D}_s}} - \frac{(\vec{q} + \vec{p})^2}{2m_D} + i\epsilon}$$

$$V_{23}(\vec{p}, \vec{q}, E) = \frac{-\sqrt{Z_2}\sqrt{Z_3}g_2g_3}{E - \frac{p^2}{2m_D} - \frac{q^2}{2m_K} - \frac{(\vec{q} + \vec{p})^2}{2m_{\bar{D}_s}} + i\epsilon}$$

#### S波投影:

$$V_{ij}(p,q,E) = \sqrt{Z_i}\sqrt{Z_j}g_ig_j\frac{m_3}{2pq}\log\frac{-E + \frac{p^2}{2m_1} + \frac{q^2}{2m_2} + \frac{(p+q)^2}{2m_3} - i\epsilon}{-E + \frac{p^2}{2m_1} + \frac{q^2}{2m_2} + \frac{(p-q)^2}{2m_2} - i\epsilon}$$

#### 散射方程 (不含三体项)

$$\begin{pmatrix} iT_1(p,q) \\ iT_2(p,q) \\ iT_3(p,q) \end{pmatrix} = \begin{pmatrix} 0 \\ iV_{21}(p,q) \\ iV_{31}(p,q) \end{pmatrix} + \int_0^{\Lambda} \frac{k^2 dk}{2\pi^2} \begin{pmatrix} 0 & iV_{12}(p,k) & iV_{13}(p,k) \\ iV_{21}(p,k) & 0 & iV_{23}(p,k) \\ iV_{31}(p,k) & iV_{32}(p,k) & 0 \end{pmatrix} \begin{pmatrix} Z_1^{-1}iG_1(E - \frac{k^2}{2m_D}, k)iT_1(k,q) \\ Z_2^{-1}iG_2(E - \frac{k^2}{2m_D}, k)iT_2(k,q) \\ Z_3^{-1}iG_3(E - \frac{k^2}{2m_K}, k)iT_3(k,q) \end{pmatrix}$$

## 数值结果





$$DK a_{DK} = 1.04 \text{ fm}$$

$$B_i = 1/(2\mu_i a_i^2)$$

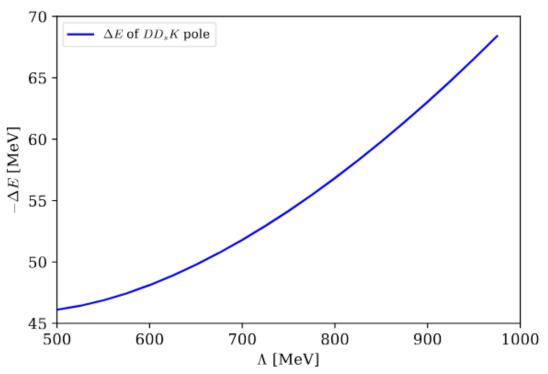
$$\overline{D}_s K \quad a_{\overline{D}_s K} = -2.57 \text{ fm}$$

由手征幺正方法计算:

$$\overline{D}_{S}K-\overline{D}\pi-\overline{D}\eta$$

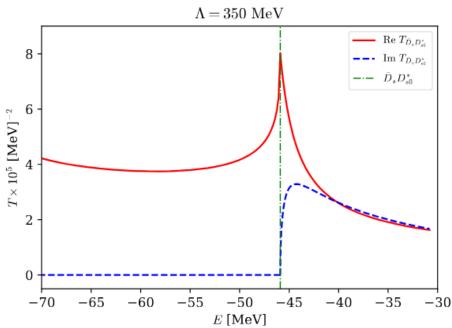
 $\overline{D}_S D$   $\overline{H}H$  系统的SU(3)多重态分析: Teng Ji et al., Phys.Rev.D 106 (2022)

$$a_{\overline{D}_S D} = 0.22 \text{ fm } (\Lambda_2 = 0.5 \text{ GeV})$$
  
-0.45 fm  $(\Lambda_2 = 1.0 \text{ GeV})$ 

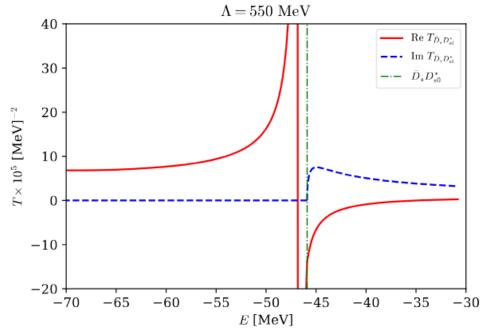


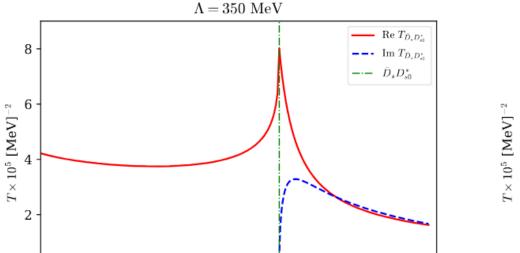
#### ● 极点位置表现出明显的截断依赖性

P. Bedaque et al., Phys.Rev.Lett. 82 (1999)



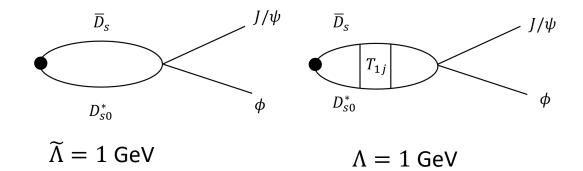
需引入三体项:  $iV_{ij}^S=i\mu_ig_icg_j\mu_j$ 





## 拟合LHCb实验数据

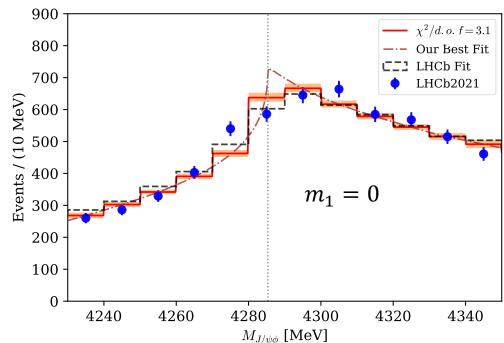




$$iF = iF_1 + iF_2$$

$$F_2 = U_1 i G_1 i V_{10} + U_1 i G_1 i T_{1j} i G_j i V_{j0}$$

- 拟合参数:  $c = c_1 + ic_2$   $\mathcal{N}, m_0 = m_1 + im_2$
- 与LHCb最佳拟合之间的  $\chi^2/d.o.f.=0.9$
- $D_{s0}^* \overline{D}_s$ 极点位置:  $4264.85_{-0.02}^{+0.02} + (-1.70_{-0.09}^{+0.08})i$  MeV



$$\frac{dN}{dM_{J/\psi\phi}} = \mathcal{N}^2 |f_1 + f_2 + m_0|^2 \text{ p.s.}$$

## 重夸克味道伙伴态系统

$$BK a_{BK} = 0.88 \text{ fm}$$

$$\bar{B}_s K$$
  $a_{\bar{B}_s K} = -5.73 \text{ fm}$ 

● 与BK和B̄<sub>s</sub>K计算方法相同

### $\bar{B}_{S}B$

● 只存在势能水平的重夸克味道对称性,近似估计:V.Baru et al., Eur.Phys.J.C 79 (2019)

$$a_{\overline{D}_SD} \rightarrow \Lambda_2 \rightarrow a_{\overline{B}_SB}$$

$$\downarrow$$

$$0.5 \sim 1.0 \text{ GeV}$$

$$a_{\bar{B}_SB} = 0.44 \text{ fm } (\Lambda_2 = 0.5 \text{ GeV})$$
  
2.43 fm  $(\Lambda_2 = 1.0 \text{ GeV})$ 



$c_* = 17.6 - 11.0i \text{ GeV}^{-3}$	pole position	$\Delta E_B({ m MeV})$
$\Lambda=0.50~{\rm GeV}$	-/-	_
$\Lambda = 0.75  \mathrm{GeV}$	v/v	-6.07/-6.68
$\Lambda=1.00~{\rm GeV}$	v/v	-1.18/-1.66
$\Lambda=1.25~{\rm GeV}$	b/v	-0.08/-0.0004
$\Lambda = 1.50  \mathrm{GeV}$	b/b	-2.22/-1.24

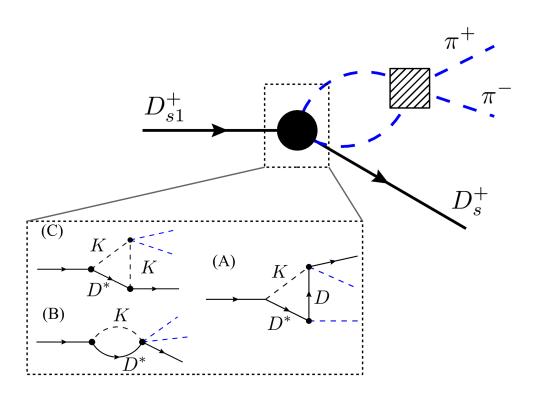
- 对底介子系统: 三体项仅使用粲介子系统中三体项的 实部
- 当减小截断值时,底介子三体系统的极点由束缚态向 虚态转变

## $D_{s1}(2460) \rightarrow D_s \pi \pi$



● 不变质量分布中的双峰结构

Meng-Na Tang et al., CTP 75 (2023)



● 被LHCb的观测所证实

LHCb Sci.Bull. 70 (2025)

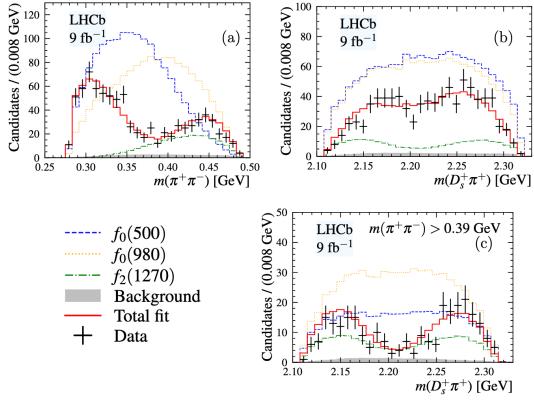
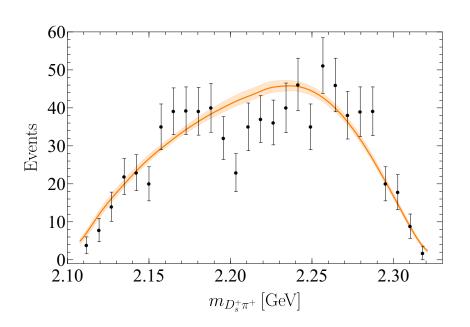
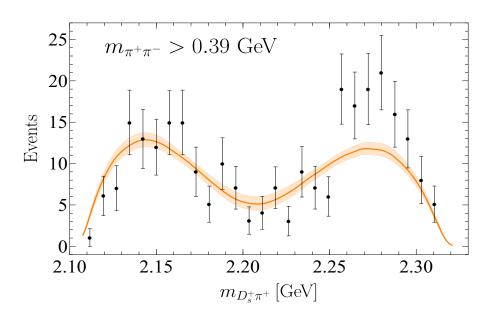
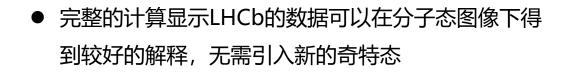


Figure 3: Comparison between data (black error bars) and results of the fit with the  $f_0(500)+f_0(980)+f_2(1270)$  model (red solid line). The distributions are for the three channels combined in (a)  $m(\pi^+\pi^-)$ , (b)  $m(D_s^+\pi^+)$ , and (c)  $m(D_s^+\pi^+)$  requiring  $m(\pi^+\pi^-)>0.39\,\mathrm{GeV}$ . Individual components, corresponding to the background contribution estimated from  $m(D_s^+\pi^+\pi^-)$  sideband regions (gray-filled) and the different resonant contributions (coloured dashed lines), are also shown as indicated in the legend.

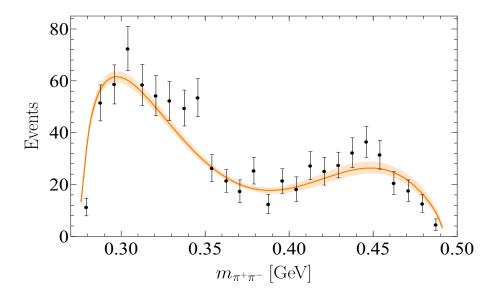




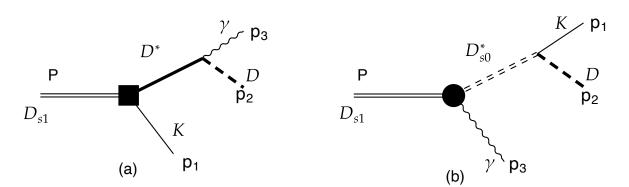


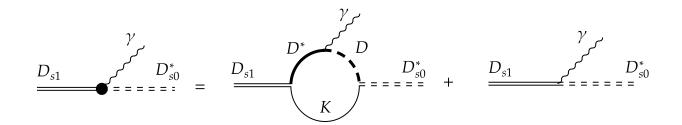


Hai-Long Fu et. al., in preparation



## $D_{s1}(2460) \rightarrow DK \gamma$

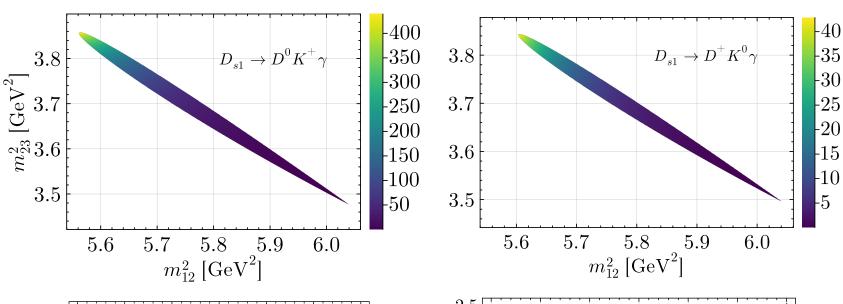


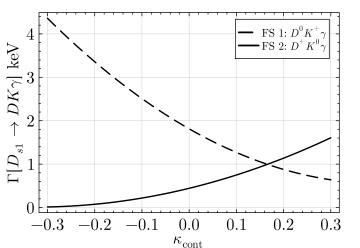


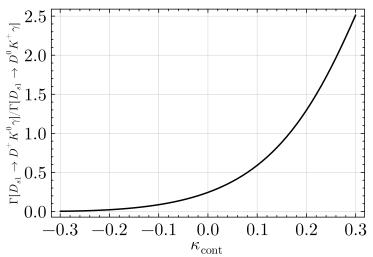
$$\kappa_{\rm loop} \sim 0.19$$



- $D_{s1} \rightarrow D_{s0} \gamma$ 的参数未能完全确定
- 接触项强度 $\Lambda_{\rm QCD}/m_c$ ~0.3







Mode	$D_s^*\pi^0$	$D_s \gamma$	$D_s^*\gamma$	$D_s\pi^+\pi^-$	$D_s\pi^0\pi^0$	$\gamma DK$
Width, keV	111	42	13	16	8	$\simeq 110$



- $D_{s1} \rightarrow D_{s0} \gamma$ 的短程相互作用对于三体末态的辐射衰变较为敏感。
- 相对于总宽度的分支比在百分之一的水平