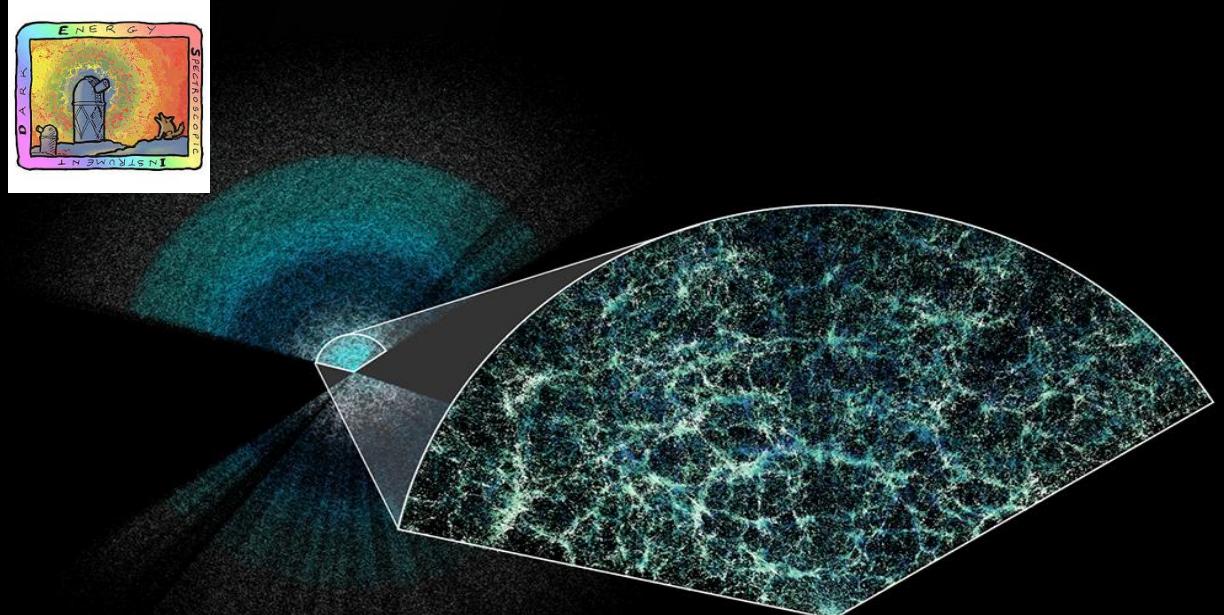
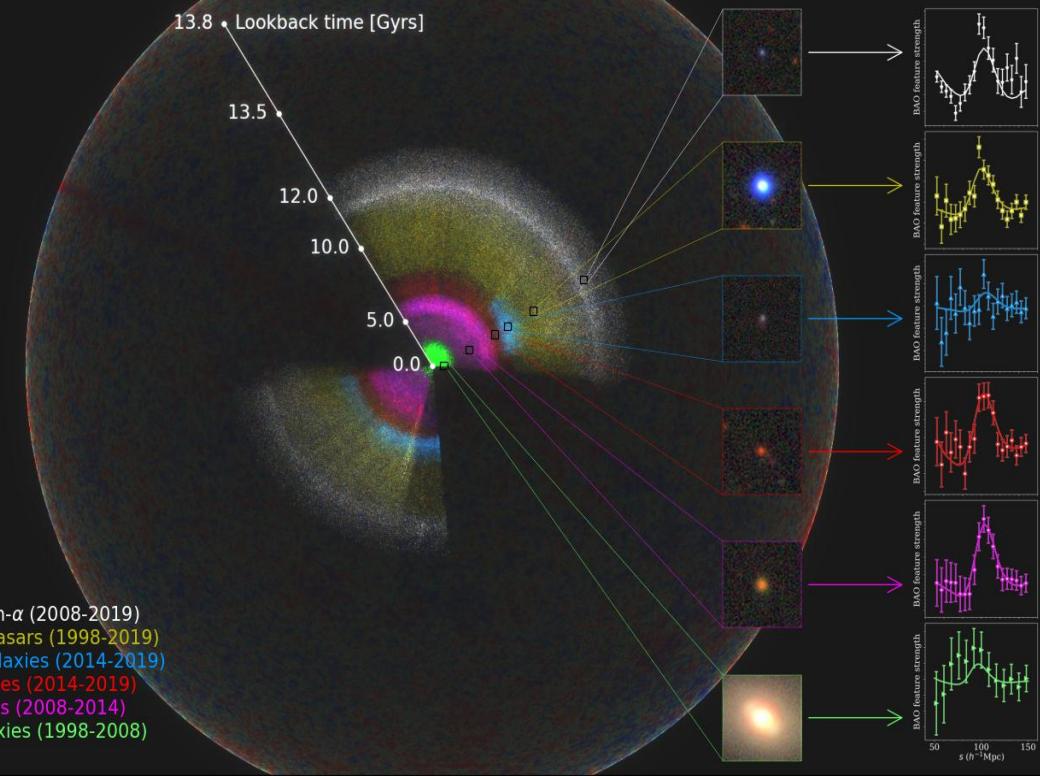


Cosmological implications of massive galaxy surveys



eBOSS + BOSS Lyman- α (2008-2019)
eBOSS + SDSS I-II Quasars (1998-2019)
eBOSS Young Blue Galaxies (2014-2019)
eBOSS Old Red Galaxies (2014-2019)
BOSS Old Red Galaxies (2008-2014)
SDSS I-II Nearby Galaxies (1998-2008)



Gong-Bo Zhao

National Astronomical Observatories, CAS
July 18, 2025

Multiple cosmological probes

CMB



Multiple cosmological probes

CMB



1978, 2006

Multiple cosmological probes

CMB



1978, 2006

SNe



Multiple cosmological probes

CMB



1978, 2006

SNe



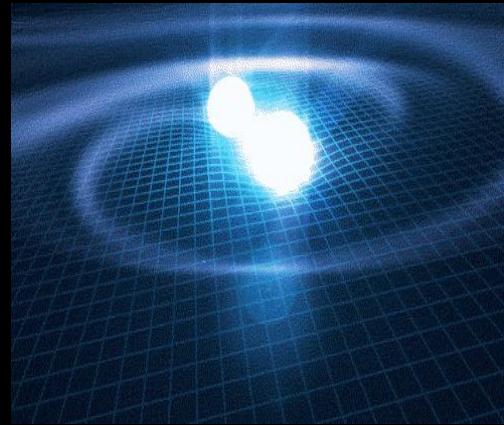
2011

Multiple cosmological probes

CMB



1978, 2006



Gravitational
waves

SNe



2011

Multiple cosmological probes

CMB



1978, 2006



Gravitational
waves

SNe



2011



Multiple cosmological probes

CMB



1978, 2006

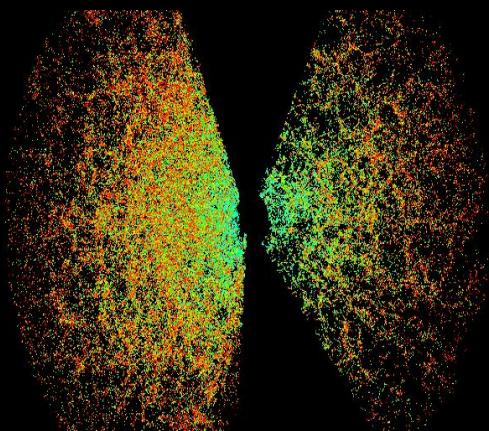


Gravitational
waves

SNe



2011



LSS

Multiple cosmological probes

CMB



1978, 2006



2017

Gravitational
waves

SNe

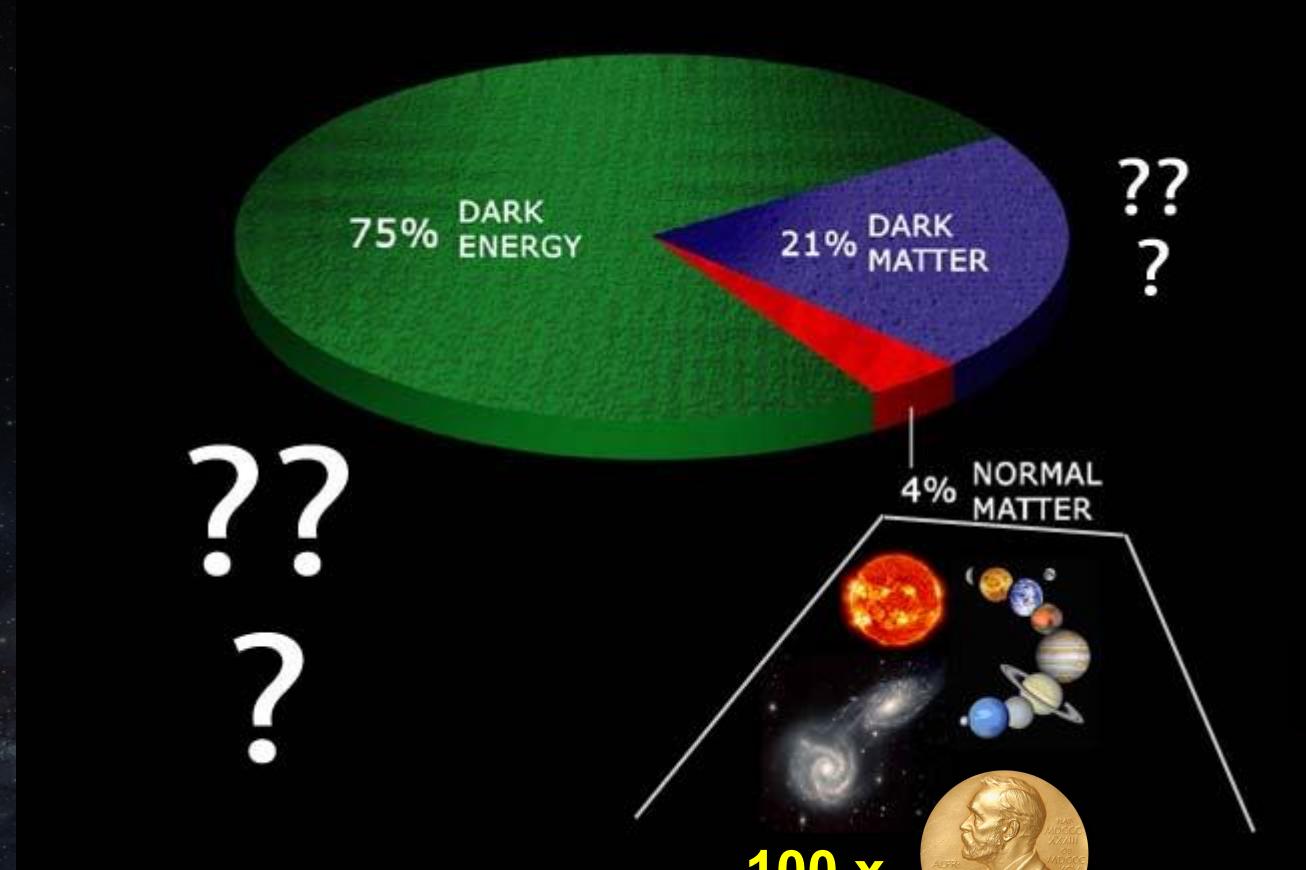


2011



2014

LSS





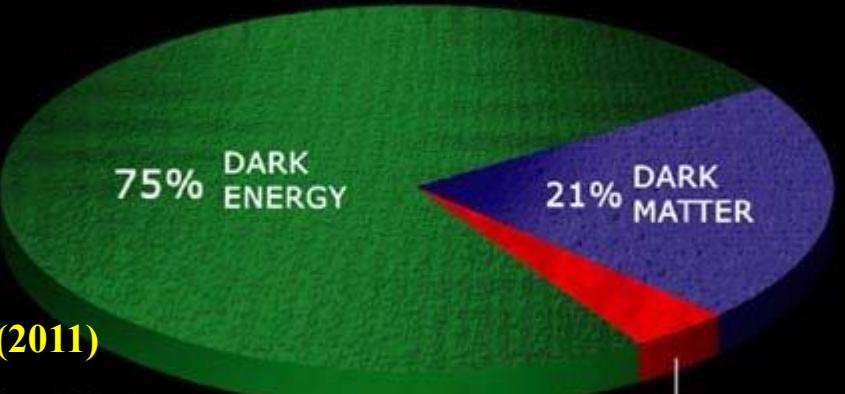
CMB (1978)



CMB (2006)



Cosmic Acceleration (2011)



??
?
??



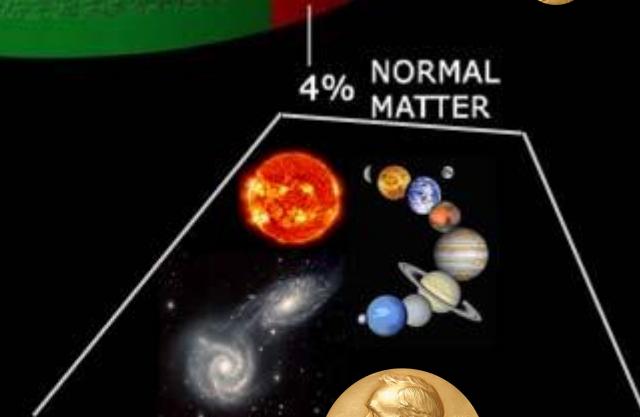
Gravitational waves (2017)



Theoretical cosmology (2019)



Black holes (2020)





The accelerating Universe!



2011



Photo: Ariel Zambelich, Copyright © Nobel Media AB

Saul Perlmutter



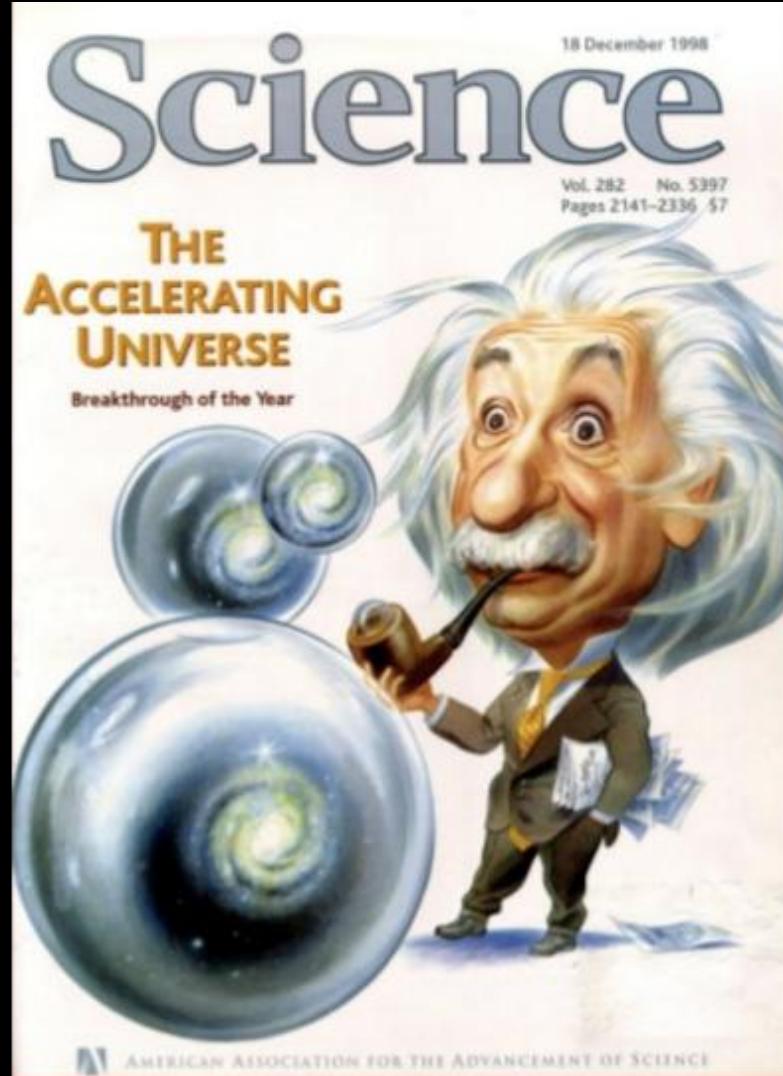
Photo: Belinda Pratten, Australian National University

Brian P. Schmidt



Photo: Homewood Photography

Adam G. Riess

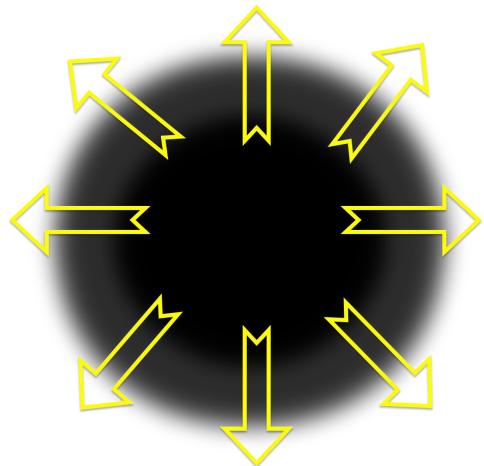


The expansion of the Universe can **accelerate** if



In GR, to add new ‘repulsive matter’,
which contributes 70% total energy

To modify General
Relativity



Dark Energy

$$G_{\mu\nu} = 8\pi G \tilde{T}_{\mu\nu}$$



Modified Gravity

$$\tilde{G}_{\mu\nu} = 8\pi G T_{\mu\nu}$$

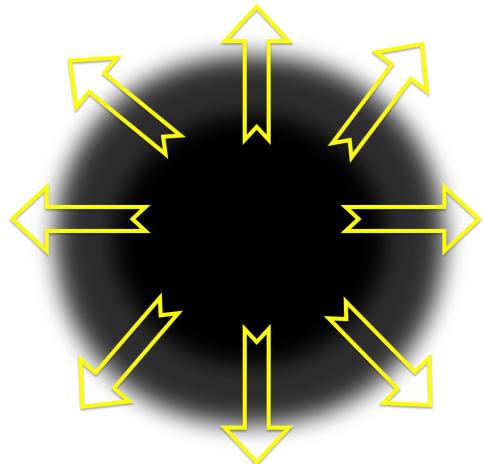
The expansion of the Universe can **accelerate** if



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To modify General
Relativity



Dark Energy

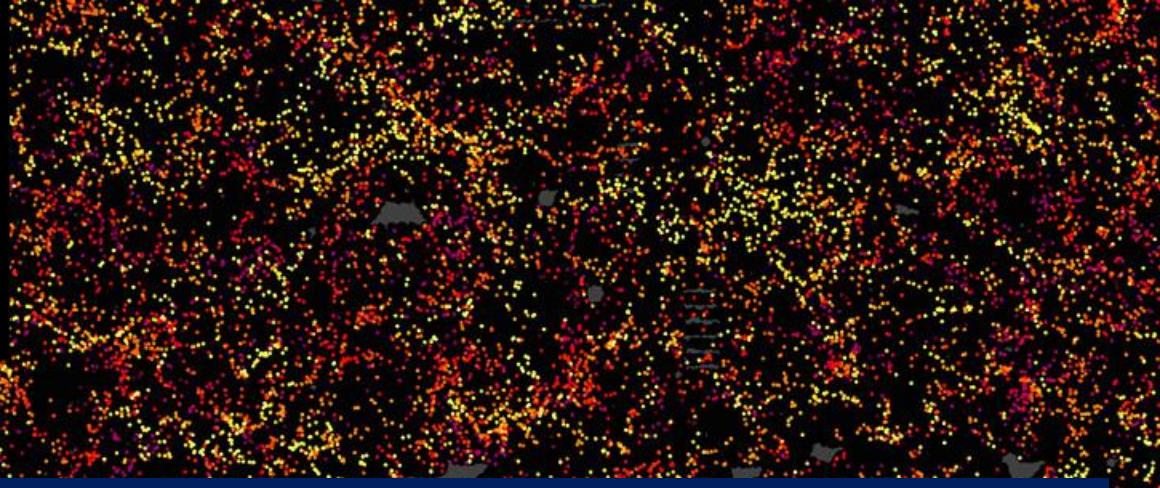
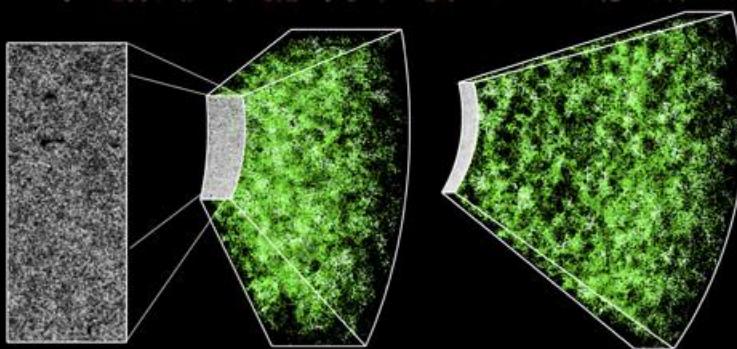
$$G_{\mu\nu} = 8\pi G \tilde{T}_{\mu\nu}$$



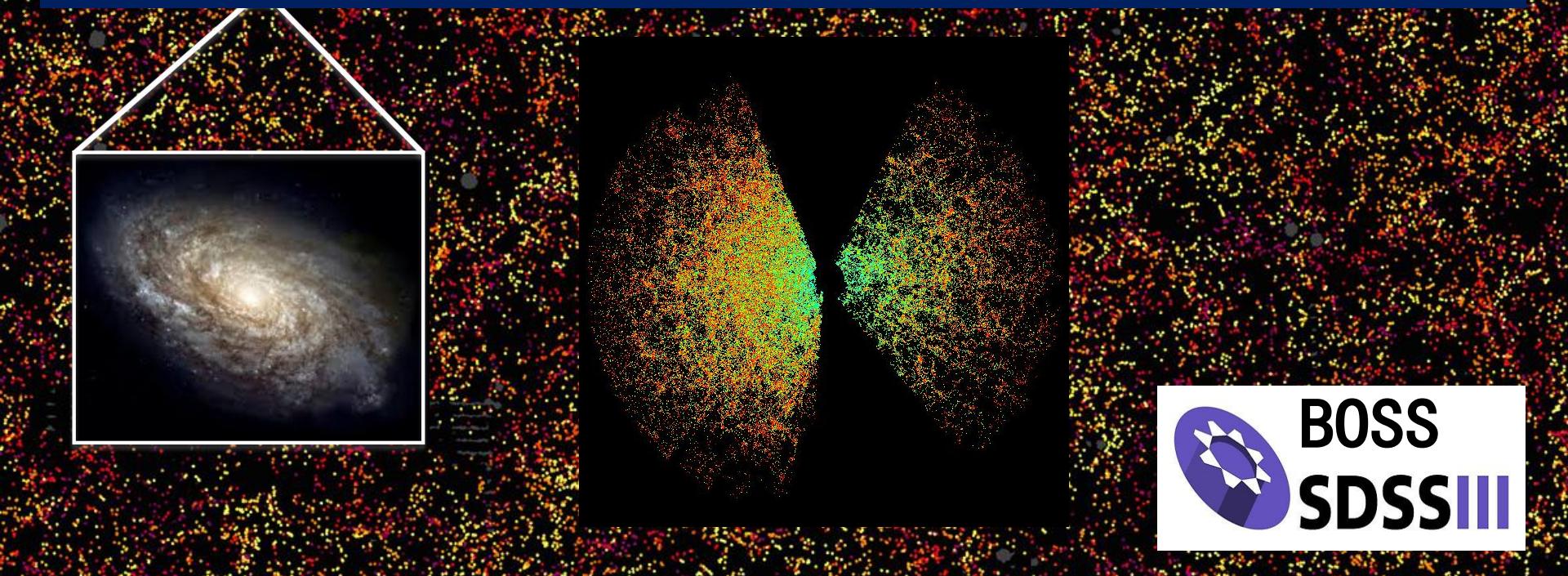
Modified Gravity

$$\tilde{G}_{\mu\nu} = 8\pi G T_{\mu\nu}$$

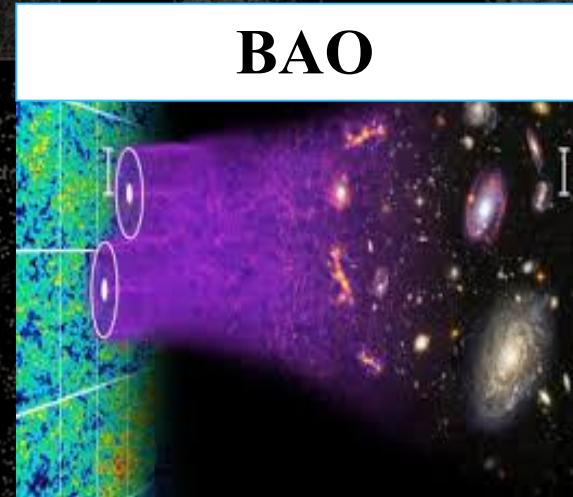
Galaxy surveys can break the dark degeneracy!



Massive redshift surveys as a key cosmological probe



Large z-surveys: a key probe of the Universe



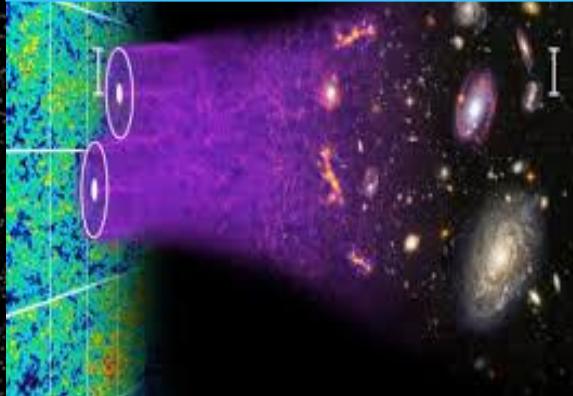
DARK ENERGY
Simplified

Exploring the Invisible Force

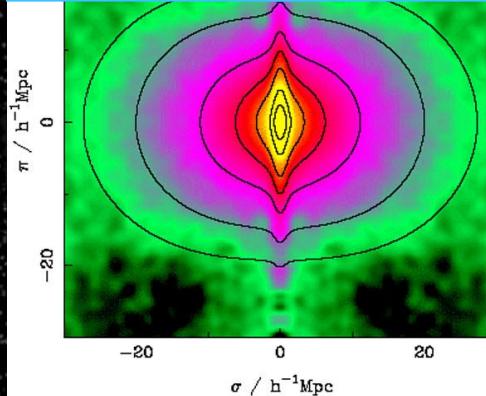
Dark Energy

Large z-surveys: a key probe of the Universe

BAO



RSD



DARK ENERGY
Simplified

Exploring the Invisible Force

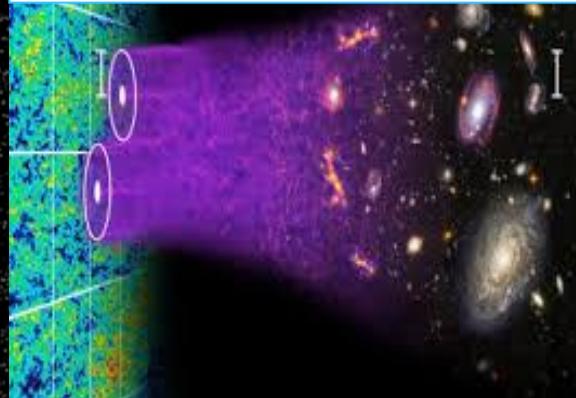
Dark Energy

GRAVITY

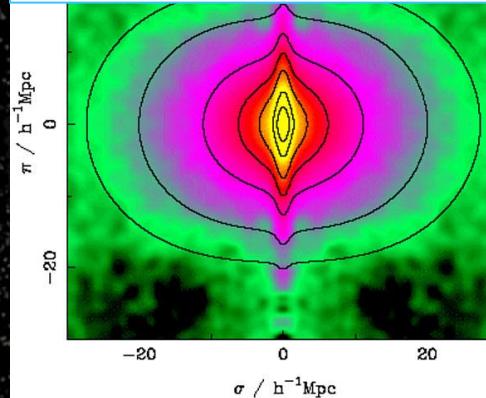
Modified Gravity

Large z-surveys: a key probe of the Universe

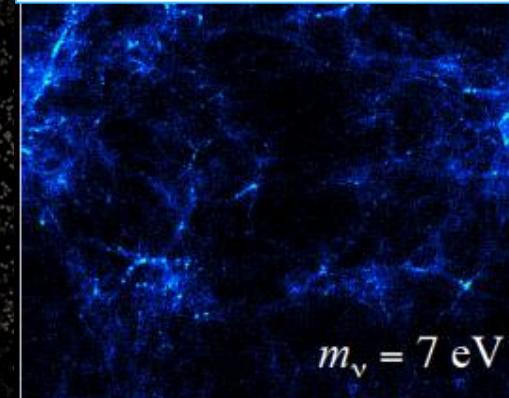
BAO



RSD



Free-streaming



DARK ENERGY
Simplified

Exploring the Invisible Force

Dark Energy

GRAVITY

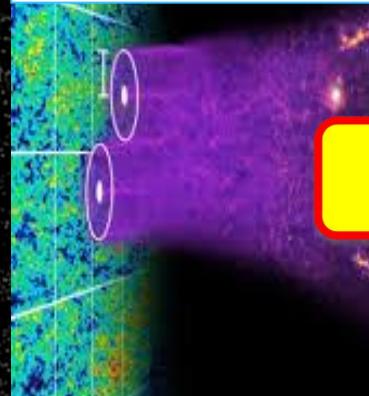
Modified Gravity



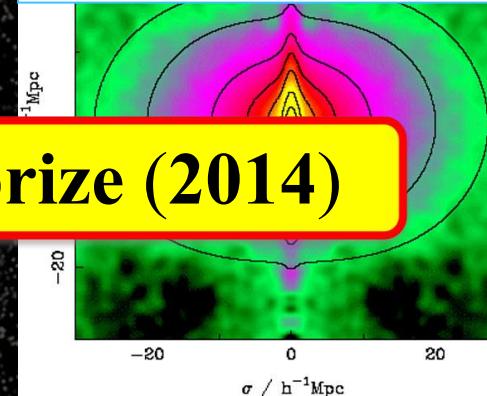
Neutrino masses

Large z-surveys: a key probe of the Universe

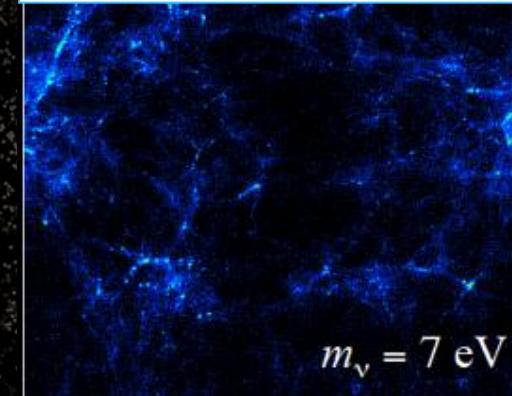
BAO



RSD



Free-streaming



Shaw's prize (2014)

Nobel Prize
(2011)

Nobel Prize
(2015)

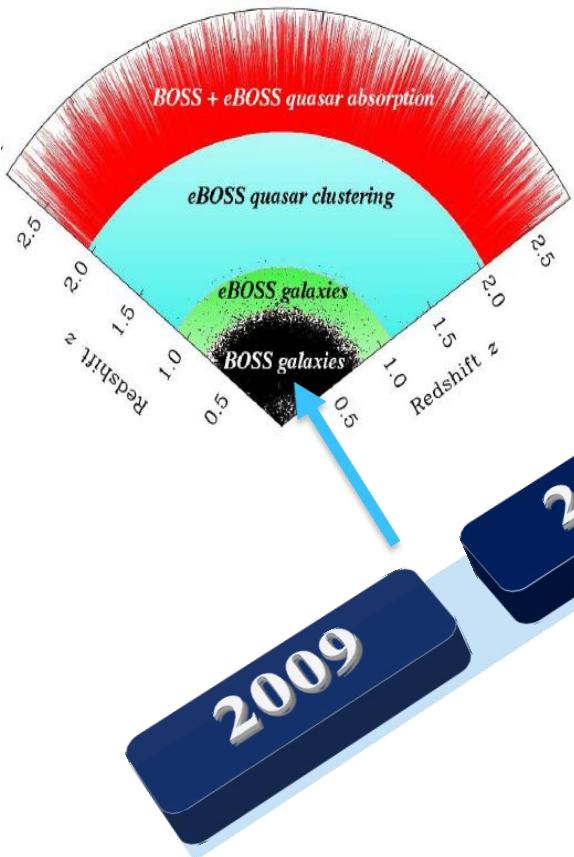
Dark Energy

Modified Gravity

Neutrino masses

DARK ENERGY
SIMPLIFIED

Exploring the Invisible Force



New Mexico

2.5m

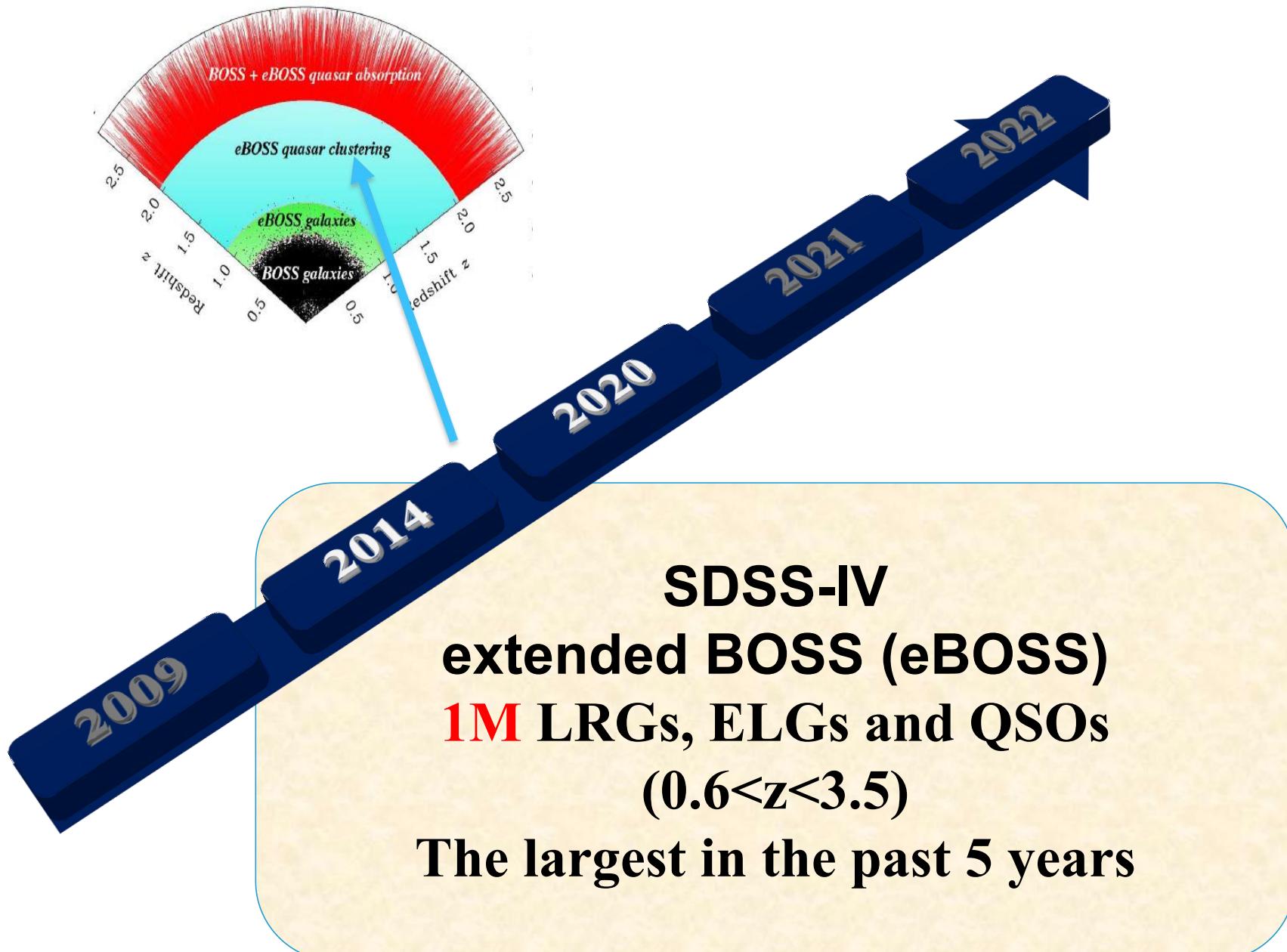
2014

2020

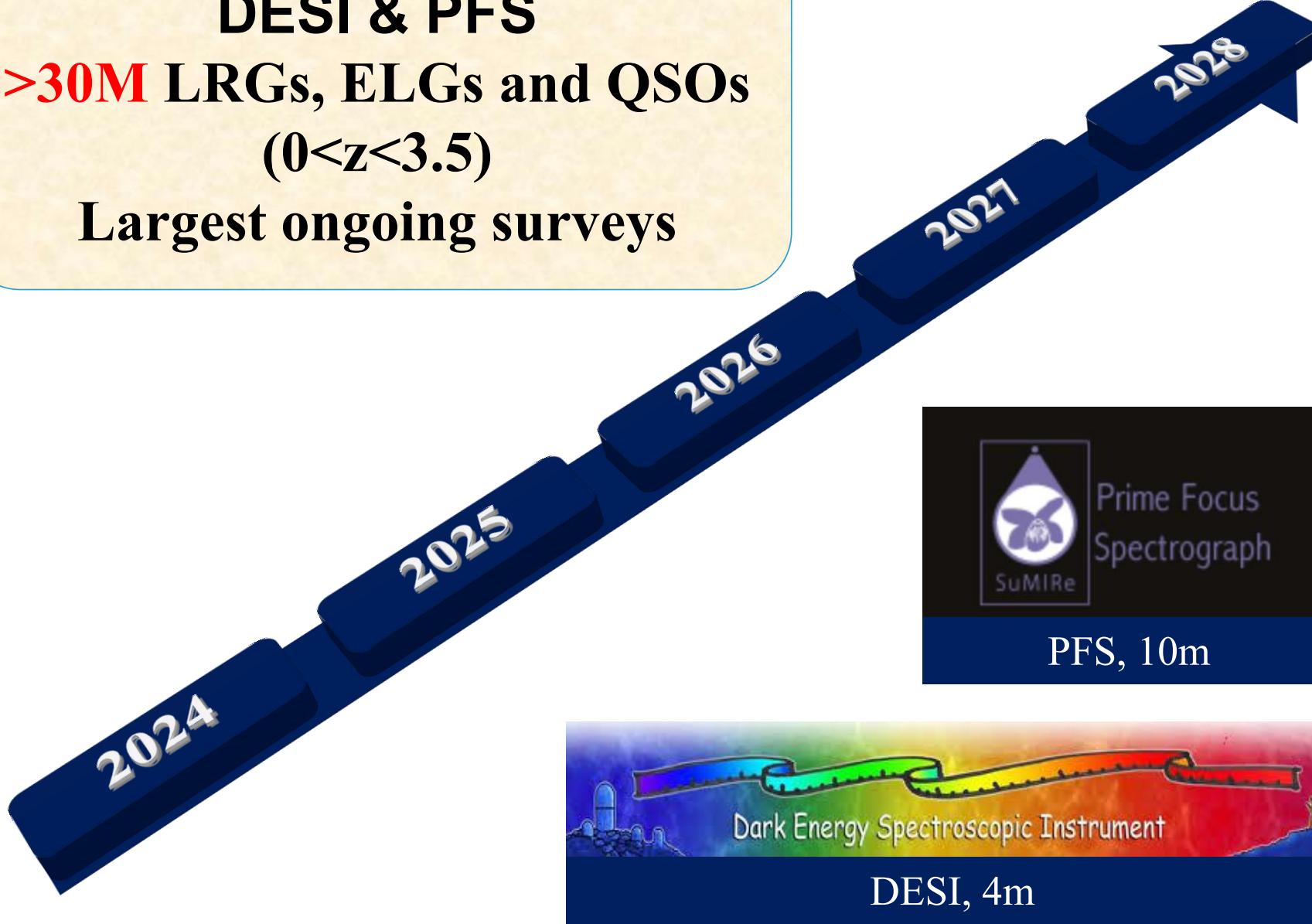
2021

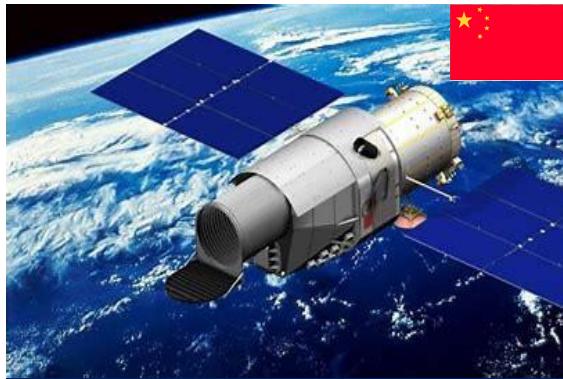
2022

**SDSS-III
Baryon Oscillation
Spectroscopic Survey
(BOSS) ($z < 0.6$)
1.6M LRGs
The largest in last decade**



DESI & PFS
>30M LRGs, ELGs and QSOs
($0 < z < 3.5$)
Largest ongoing surveys

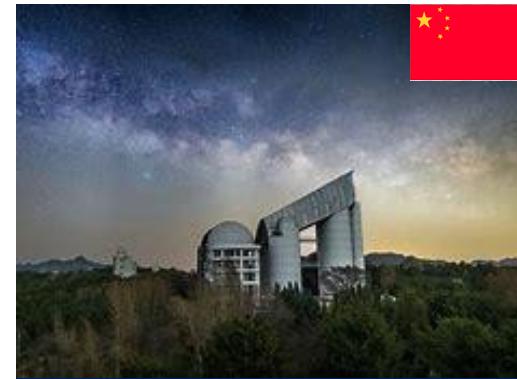




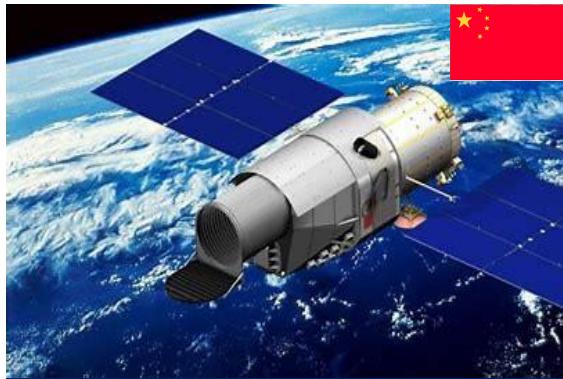
CSST, 2m in space



MUST, 6.5m



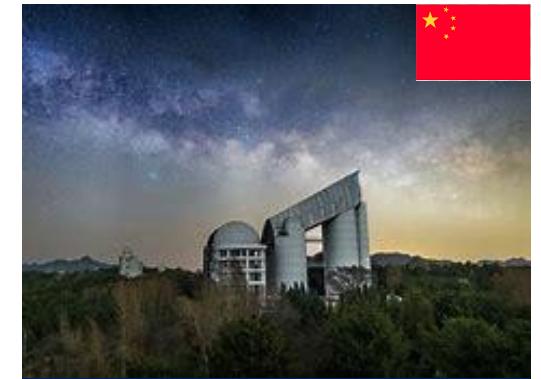
ESST, 10+m



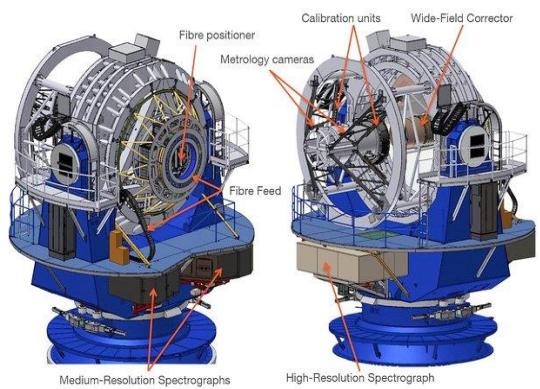
CSST, 2m in space



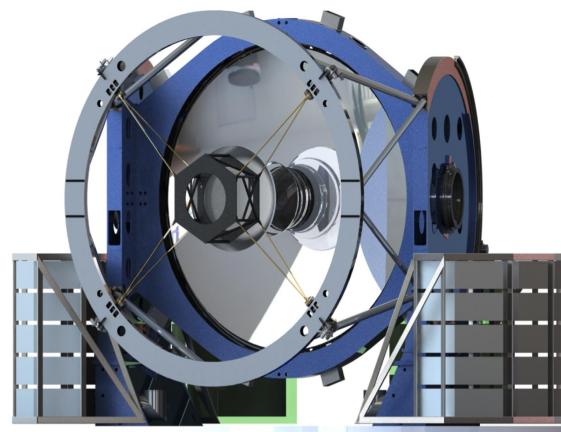
MUST, 6.5m



ESST, 10+m



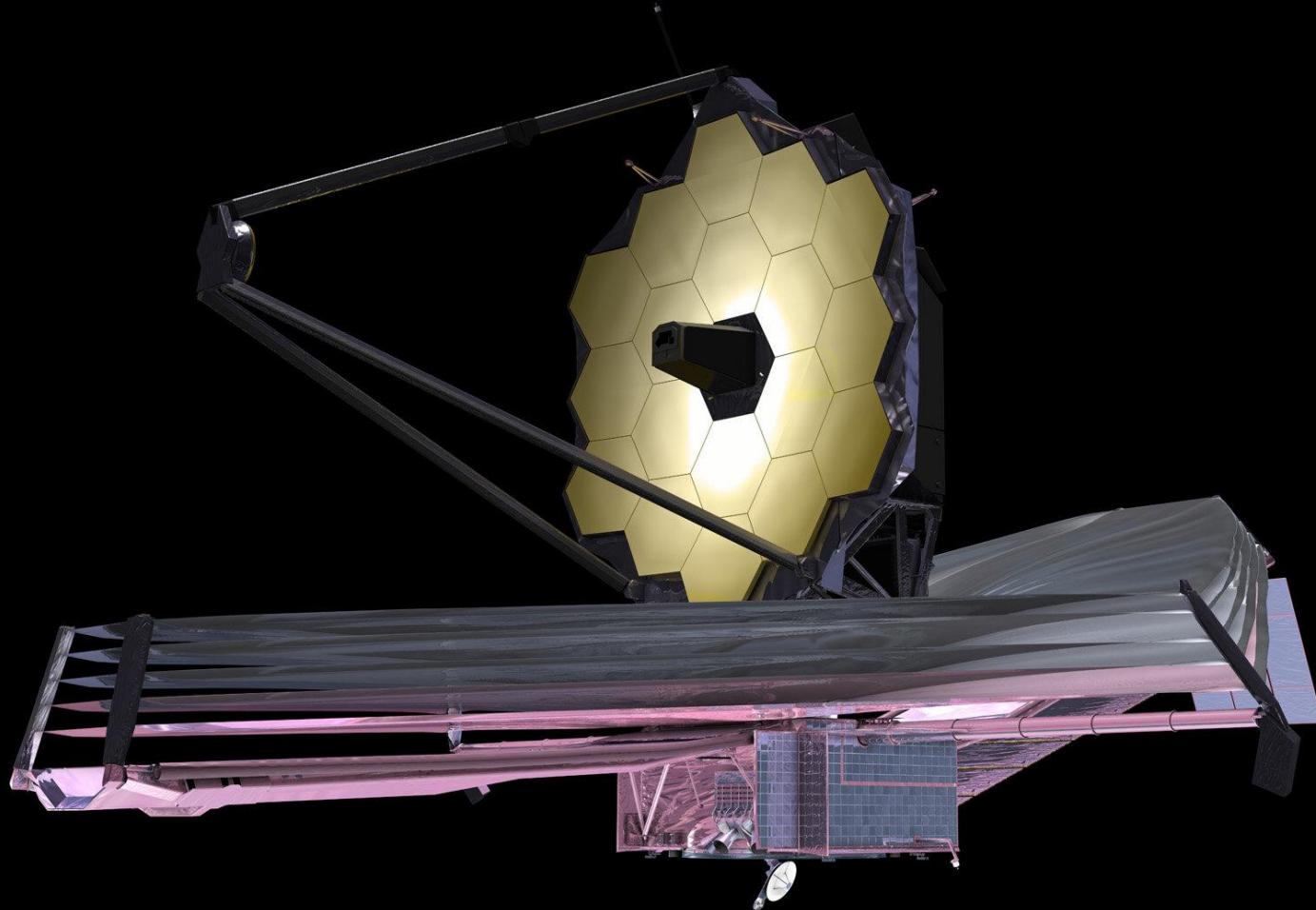
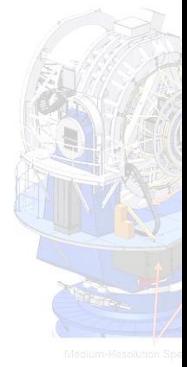
4MOST, 4m



MegaMapper, 6.5m

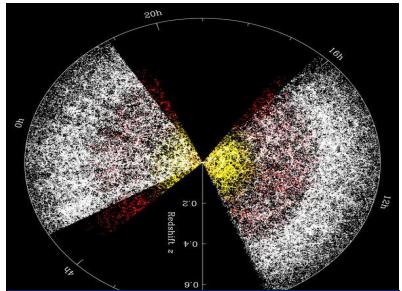


WST, 10+m

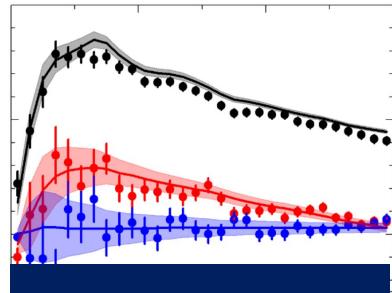


280 m at L2!!
arXiv: 2010.06064

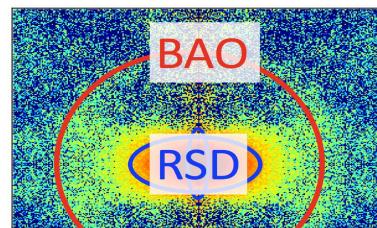




LSS survey



$\xi(s), P(k)$



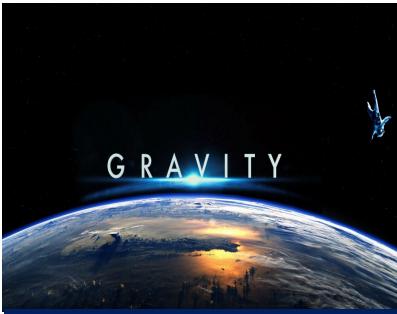
BAO, RSD

Model
Sim.
Stat.

Cosmic acceleration

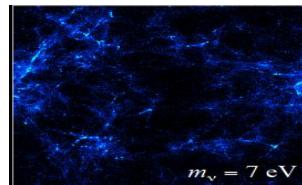


Dark Energy

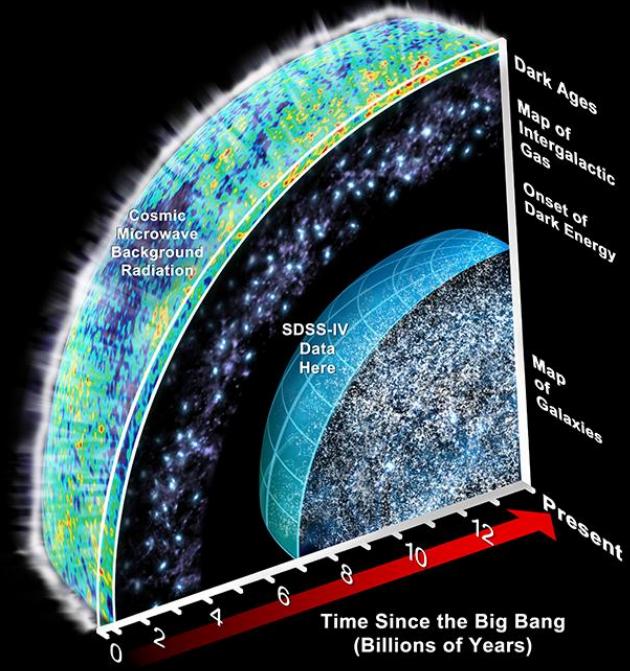


Modified Gravity

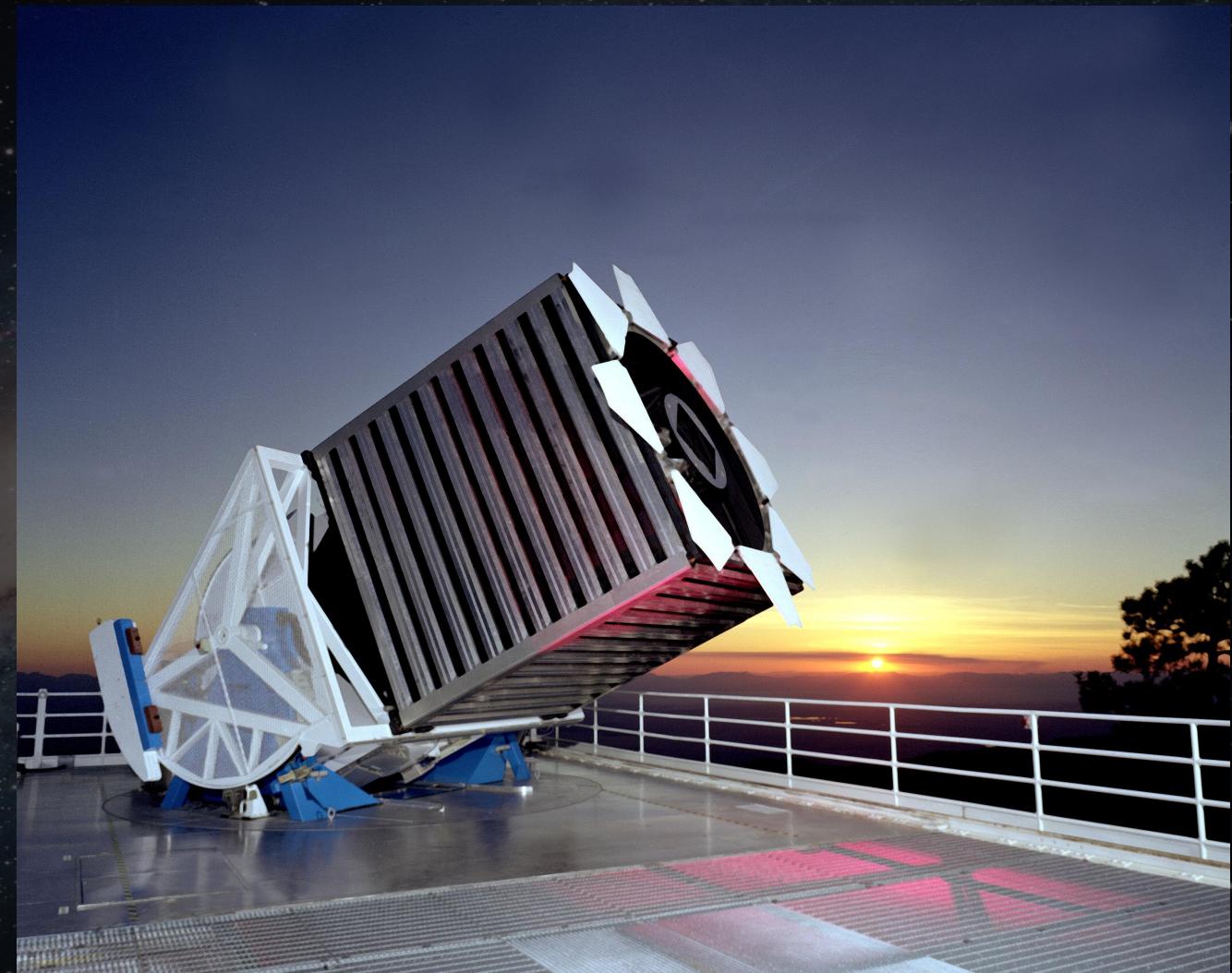
Neutrino masses



SDSS-IV Catches the Rise of Dark Energy



eBOSS (2014-2020)



2.5 m SDSS telescope @ New Mexico

eBOSS result released on July 20, 2020 in 20+ papers



SDSS

Data Surveys Instruments Collaboration Science

Search www.sdss.org

No need to Mind the Gap: Astrophysicists fill in 11 billion years of our universe's expansion history

⌚ July 19, 2020

The Sloan Digital Sky Survey (SDSS) released today a comprehensive analysis of the largest three-dimensional map of the Universe ever created, filling in the most significant gaps in our possible exploration of its history.

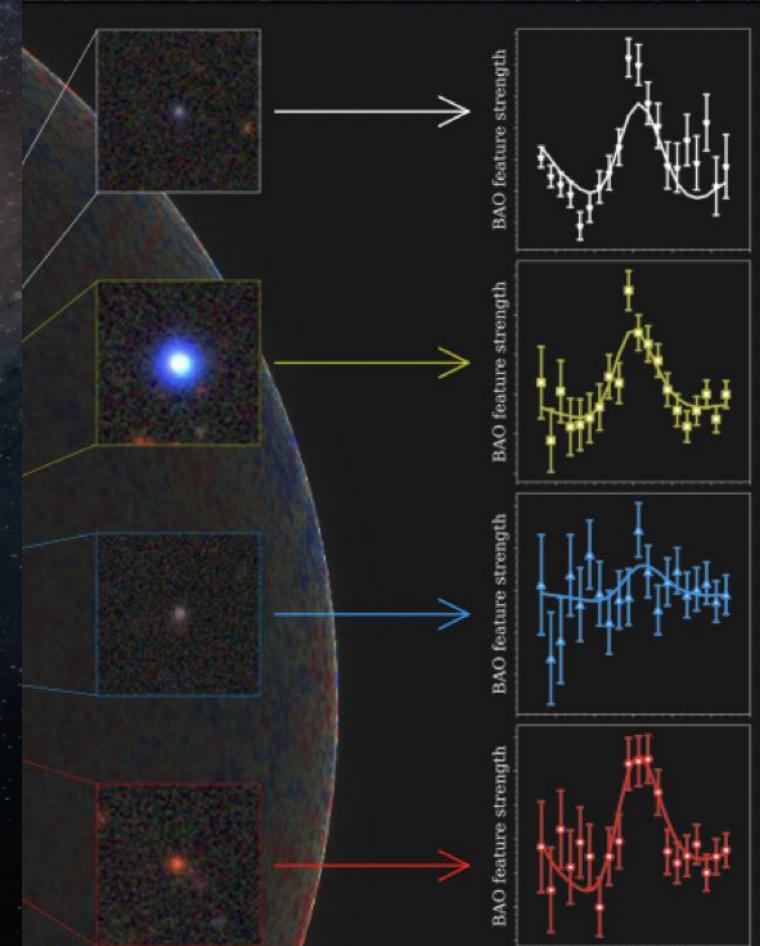
eBOSS tracers

Lyman-a forest

Clustering quasars

Emission Line Galaxies (ELGs)

Luminous Red Galaxies (LRGs)



- ELG (k-space): De Mattia et al, 2007.09008
- ELG (s-space): Tamone et al, 2007.09009
- LRG (k-space): Gil-Marin et al, 2007.08994
- LRG (s-space): Bautista et al, 2007.08993
- ELG × LRG (k-space): G-B. Zhao et al, 2007.09011
- ELG × LRG (s-space): Y. Wang et al, 2007.09010
- QSO (k-space): Neveux et al, 2007.08999
- QSO (s-space): Hou et al, 2007.08998
- LyA BAO (s-space): du Mas des Bourboux et al, 2007.08995
- Cosmological implications: Alam et al, 2007.08991
- Mocks, Catalog papers



SDSS

Lookback time [Gyrs]

13.5

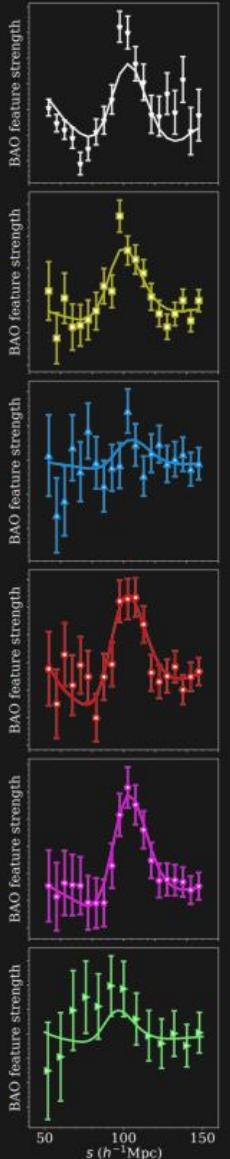
12.0

10.0

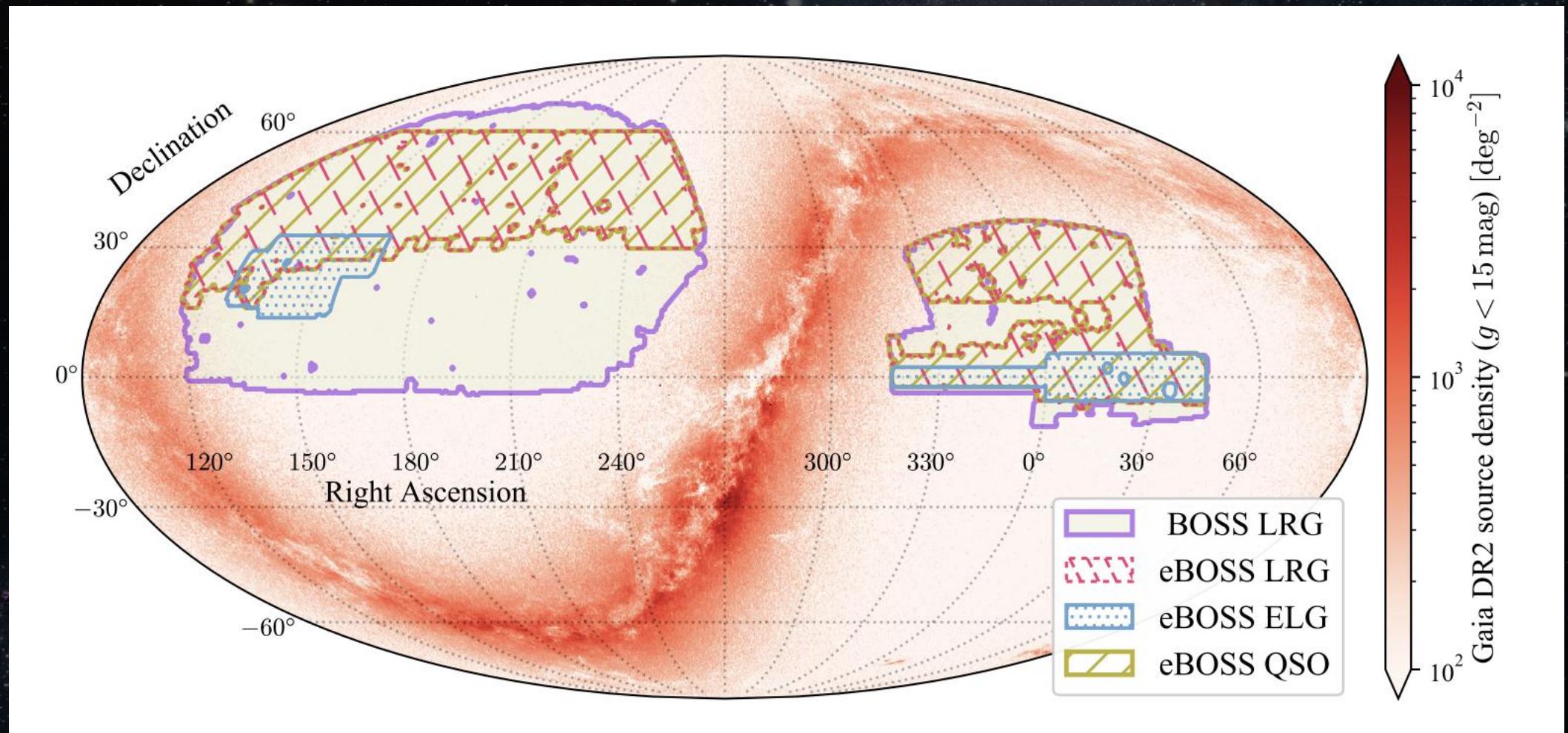
5.0

0.0

- eBOSS + BOSS Lyman- α (2008-2019)
- eBOSS + SDSS I-II Quasars (1998-2019)
- eBOSS Young Blue Galaxies (2014-2019)
- eBOSS Old Red Galaxies (2014-2019)
- BOSS Old Red Galaxies (2008-2014)
- SDSS I-II Nearby Galaxies (1998-2008)



eBOSS footprint



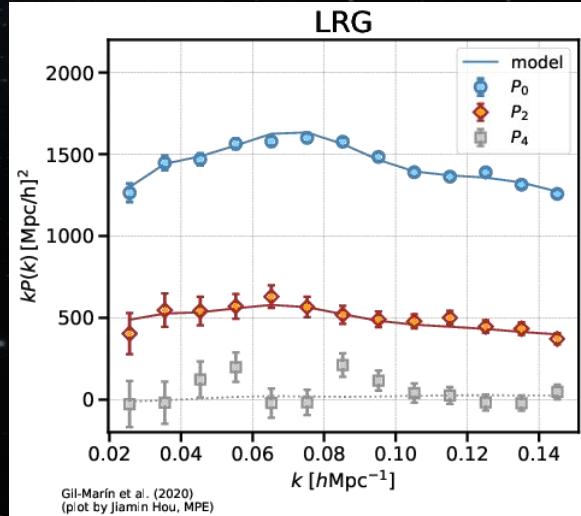
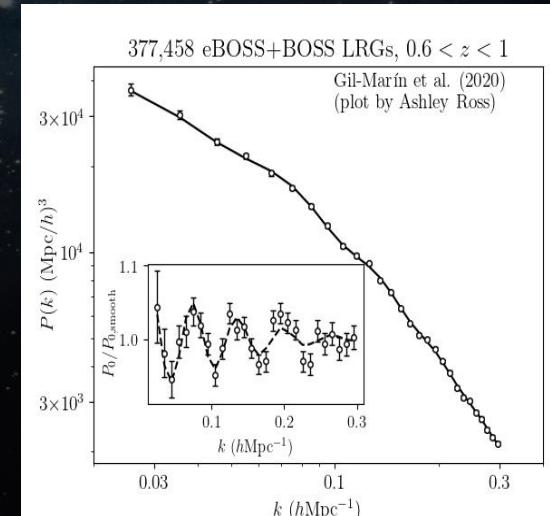
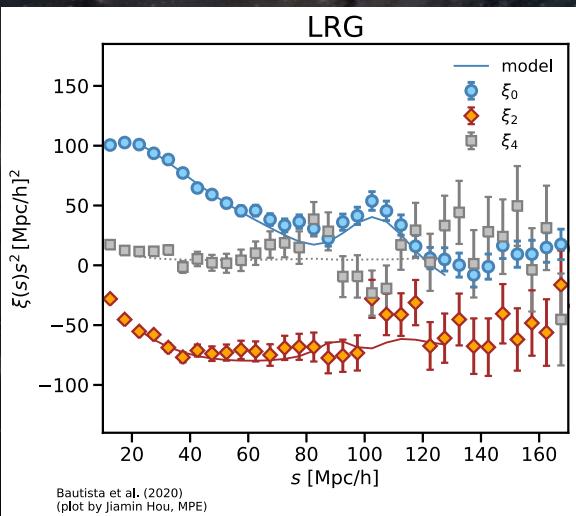
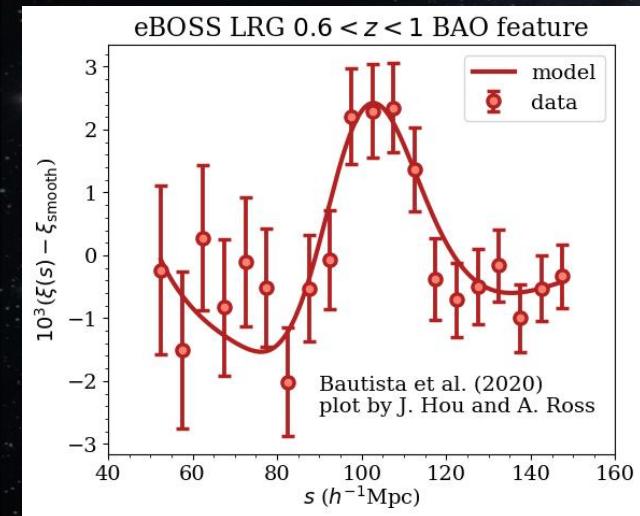
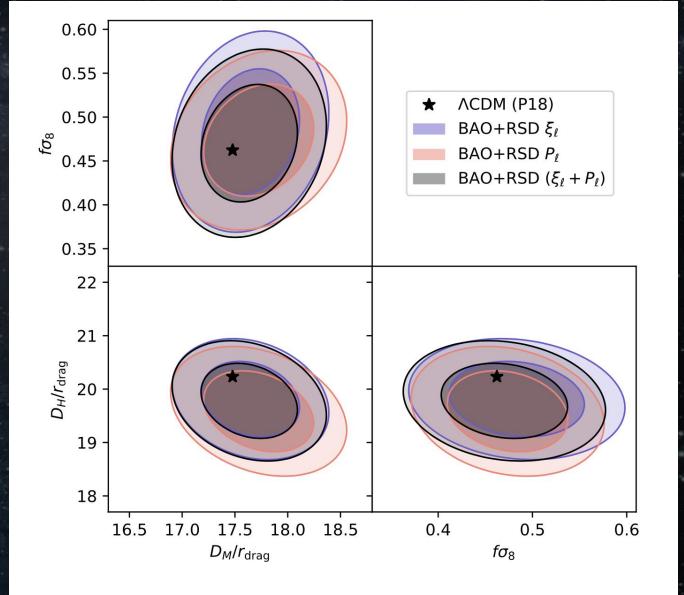
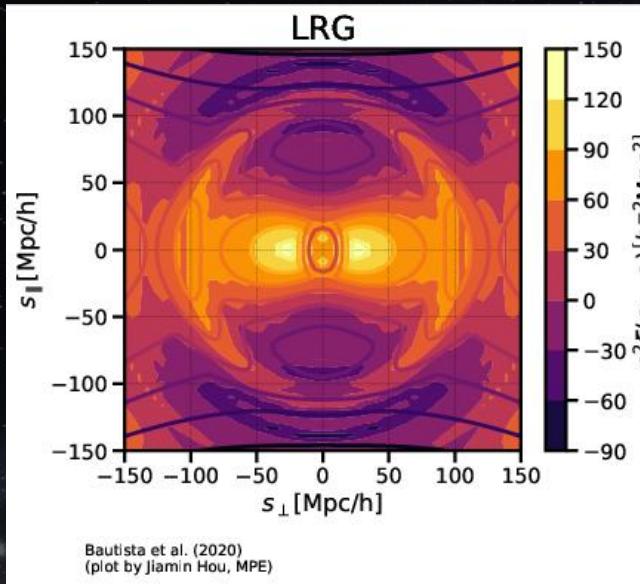
Luminous Red Galaxies (LRGs)

$0.6 < z < 1.0, z_{\text{eff}} = 0.77$

$\sim 9500 \text{ deg}^2$

$\sim 400 \text{ K spectra}$

Bautista+, 2020; Gil-Marín+, 2020



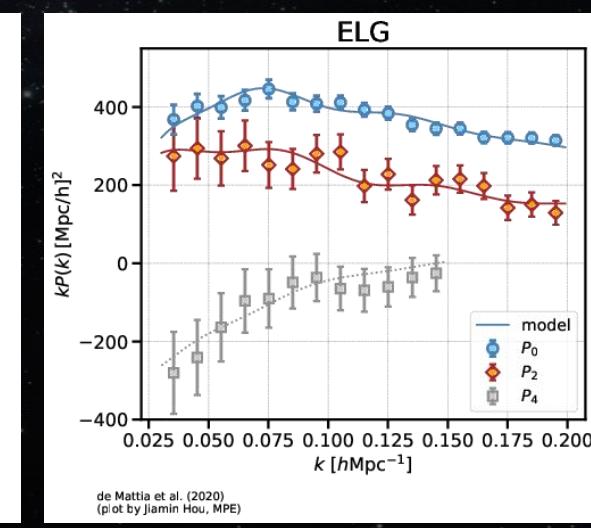
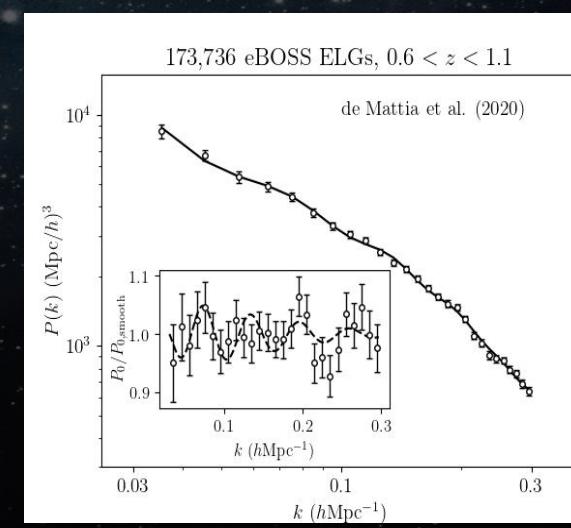
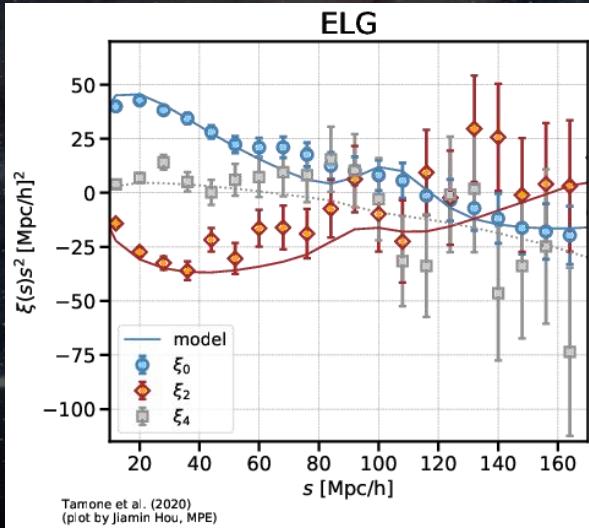
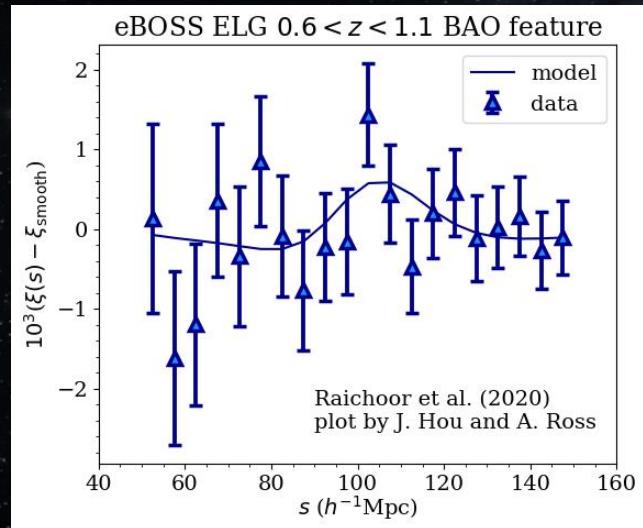
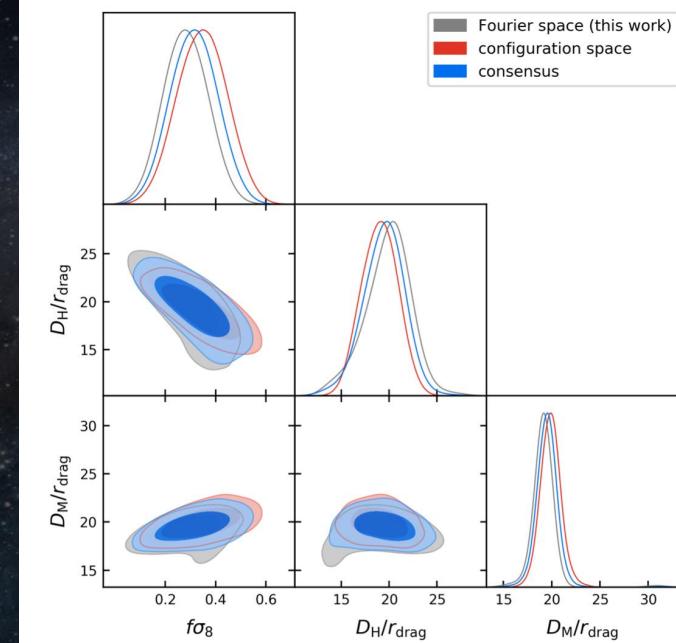
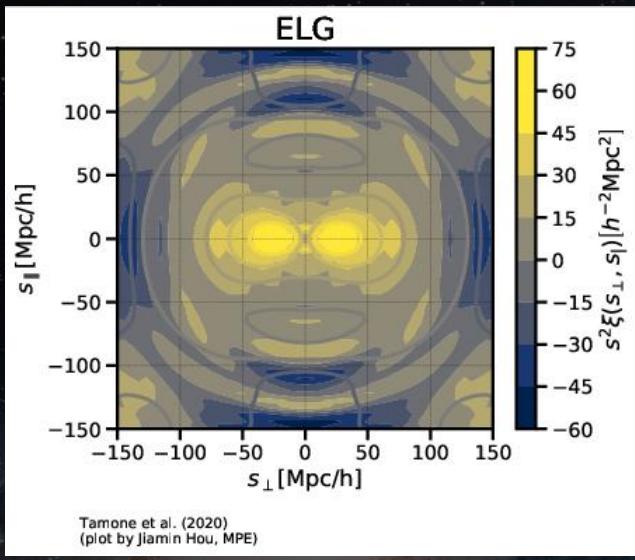
Emission line Galaxies (ELGs)

$0.6 < z < 1.1$, $z_{\text{eff}} = 0.845$

$\sim 730 \text{ deg}^2$

$\sim 170 \text{ K spectra}$

de Mattia+, 2020; Tamone+, 2020



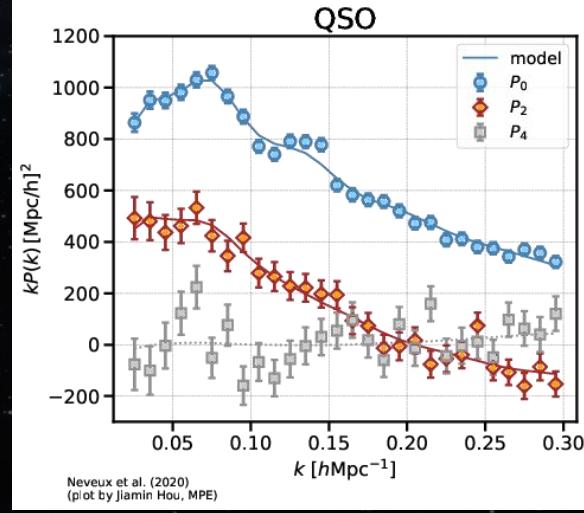
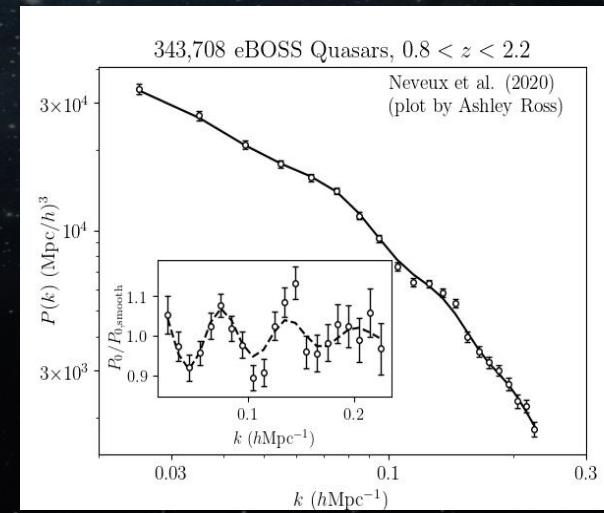
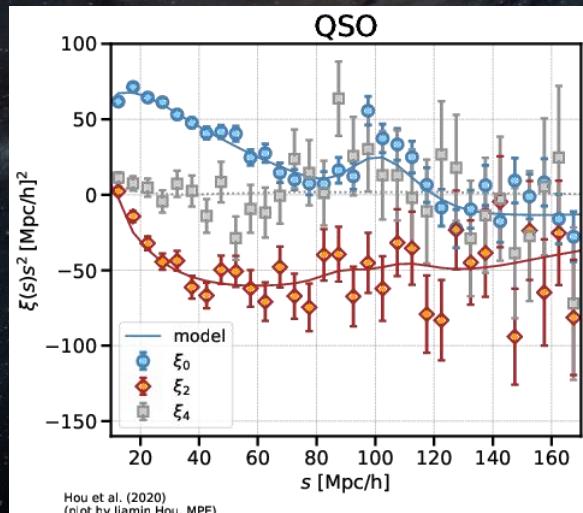
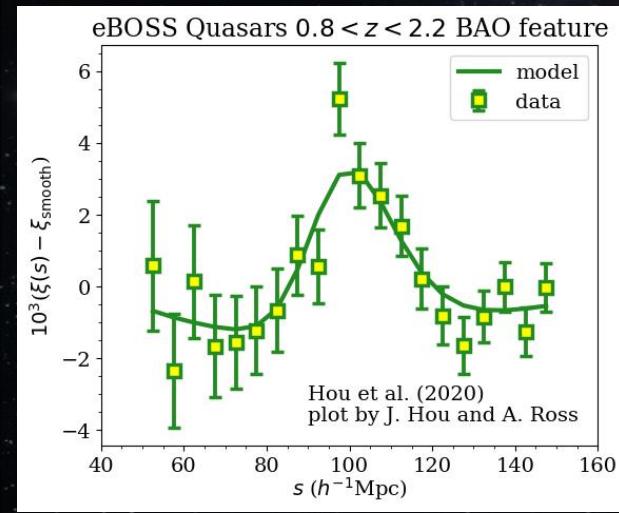
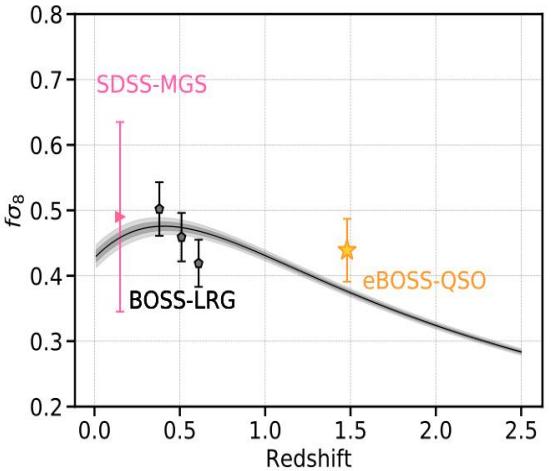
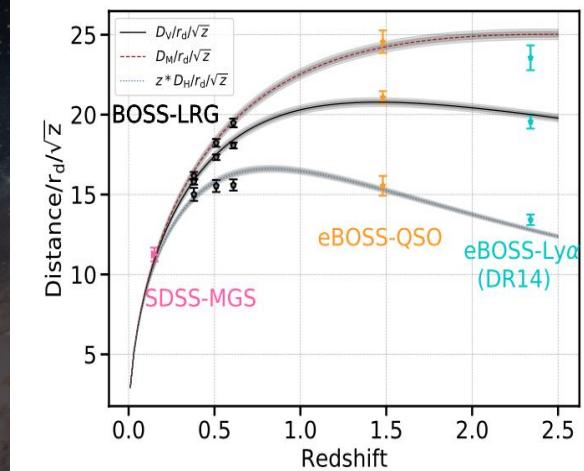
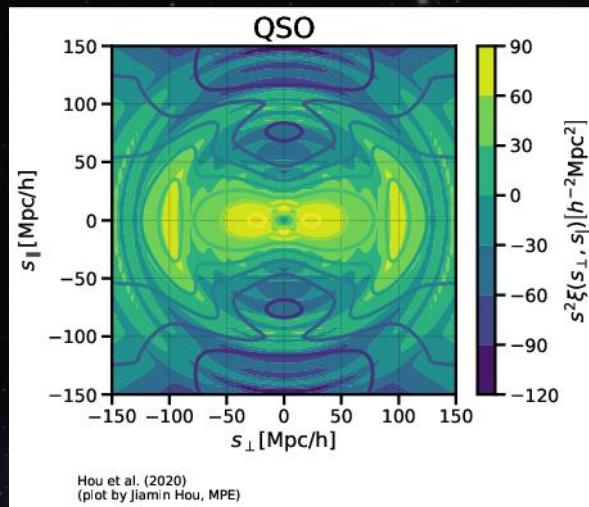
Clustering quasars (QSOs)

$0.8 < z < 2.2$, $z_{\text{eff}} = 1.48$

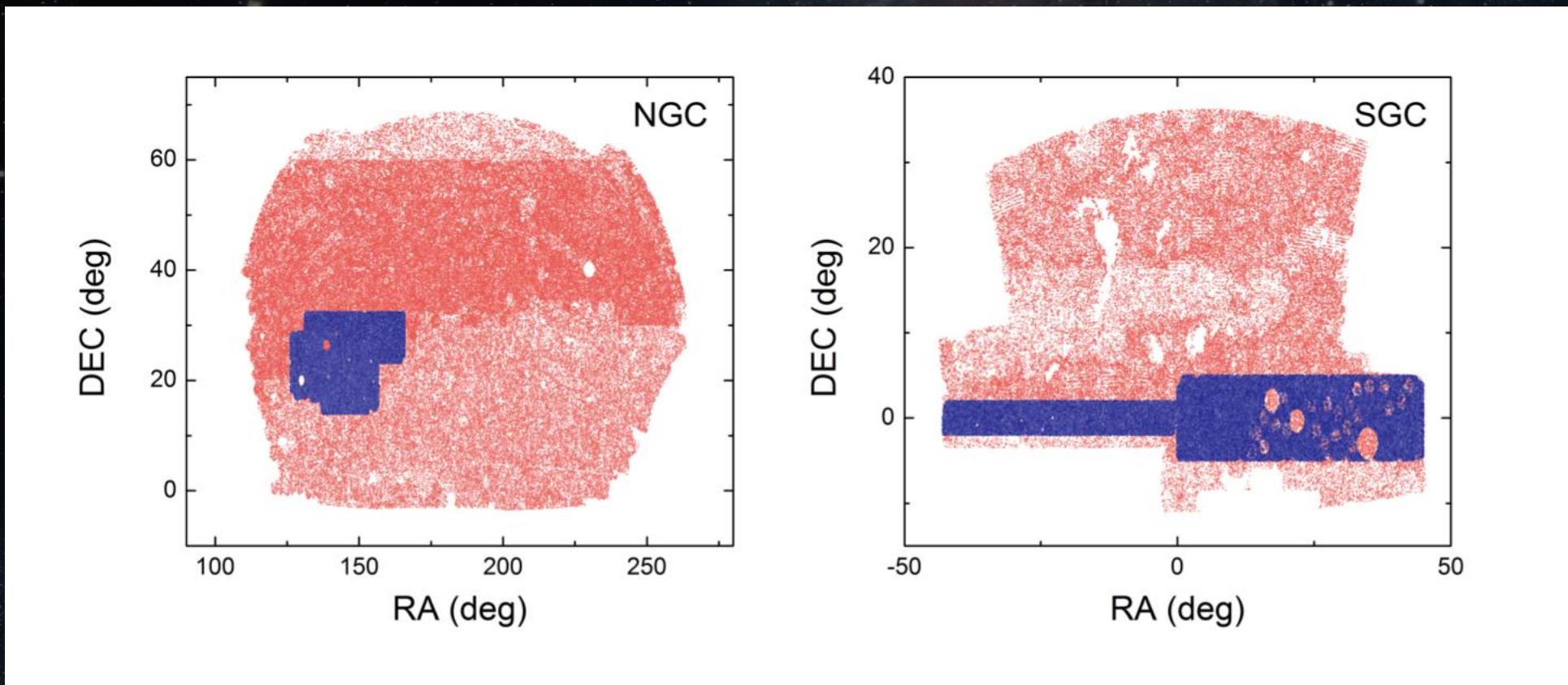
$\sim 4700 \text{ deg}^2$

$\sim 340 \text{ K spectra}$

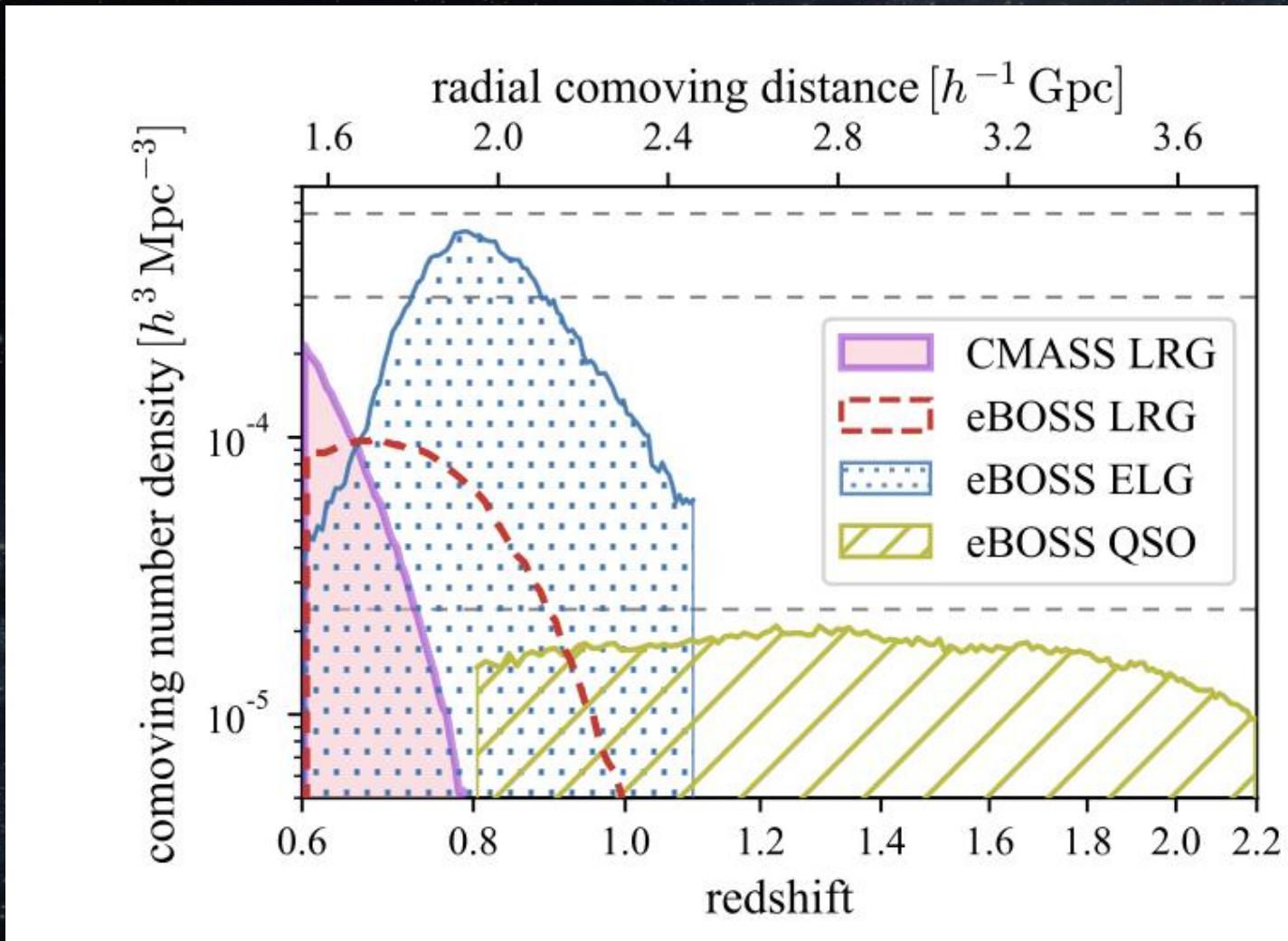
Hou+, 2020; Neveux+, 2020



Angular overlap



Radial overlap



Why cross-correlation is cool?

- It can remove the cosmic variance, thus reduce the statistical uncertainty!

1-tracer: $\delta_{g1} = (b_1 + f\mu^2)\delta + \epsilon_1 = f(\beta^{-1} + \mu^2)\delta + \epsilon_1$

$$C = 2\langle\delta_{g1}^2\rangle \quad \frac{\sigma_\beta^2}{\beta^2} = \frac{(1+\beta)^2}{\beta^2}$$

2-tracers: $\delta_{g1} = f(\beta^{-1} + \mu^2)\delta + \epsilon_1 \quad \delta_{g2} = f(\alpha\beta^{-1} + \mu^2)\delta + \epsilon_2$

$$C \equiv \begin{bmatrix} \langle\delta_{g1}^2\rangle & \langle\delta_{g1}\delta_{g2}\rangle \\ \langle\delta_{g2}\delta_{g1}\rangle & \langle\delta_{g2}^2\rangle \end{bmatrix} = \frac{P_{\theta\theta}}{2} \begin{bmatrix} (\beta^{-1} + \mu^2)^2 & (\beta^{-1} + \mu^2)(\alpha\beta^{-1} + \mu^2) \\ (\beta^{-1} + \mu^2)(\alpha\beta^{-1} + \mu^2) & (\alpha\beta^{-1} + \mu^2)^2 \end{bmatrix} + \frac{N}{2}$$

$$\frac{\delta_{g2}}{\delta_{g1}} = \frac{\alpha\beta^{-1} + \mu^2}{\beta^{-1} + \mu^2}.$$

McDonald & Seljak 2008; Seljak 2009

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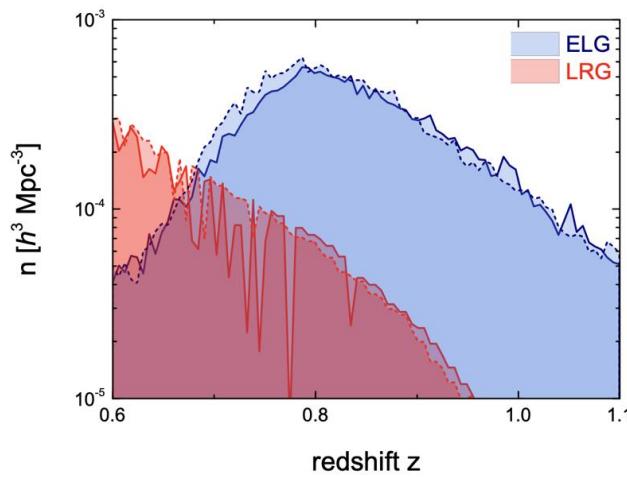
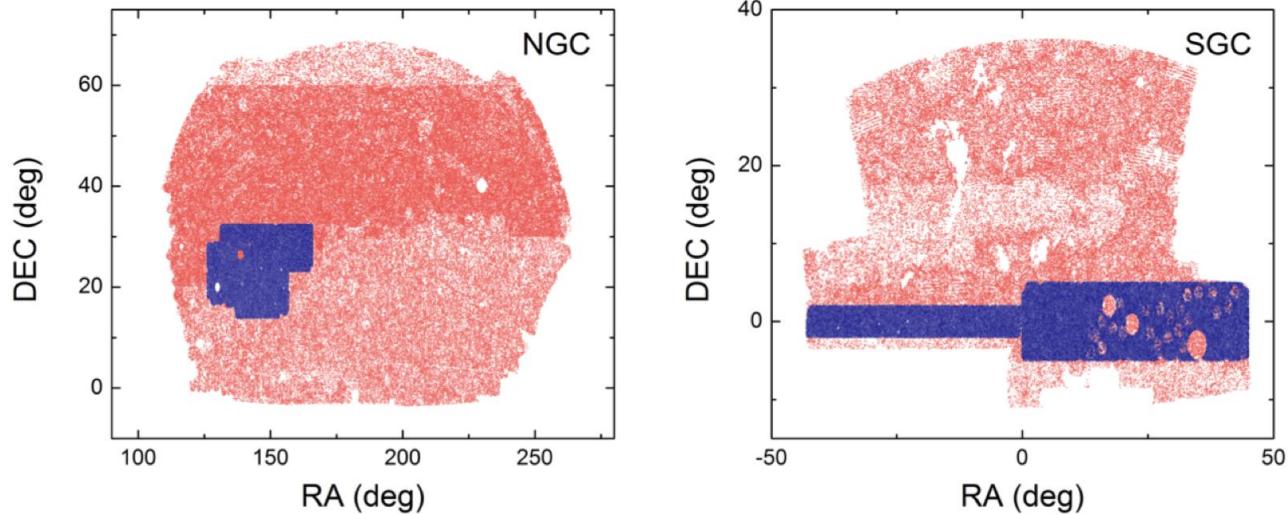
2-tracers: $\delta_{g1} = f(\beta^{-1} + \mu^2)\delta + \epsilon_1 \quad \delta_{g2} = f(\alpha\beta^{-1} + \mu^2)\delta + \epsilon_2$

$$C \equiv \begin{bmatrix} \langle\delta_{g1}^2\rangle & \langle\delta_{g1}\delta_{g2}\rangle \\ \langle\delta_{g2}\delta_{g1}\rangle & \langle\delta_{g2}^2\rangle \end{bmatrix} = \frac{P_{\theta\theta}}{2} \begin{bmatrix} (\beta^{-1} + \mu^2)^2 & (\beta^{-1} + \mu^2)(\alpha\beta^{-1} + \mu^2) \\ (\beta^{-1} + \mu^2)(\alpha\beta^{-1} + \mu^2) & (\alpha\beta^{-1} + \mu^2)^2 \end{bmatrix} + \frac{N}{2}$$

$$\frac{\delta_{g2}}{\delta_{g1}} = \frac{\alpha\beta^{-1} + \mu^2}{\beta^{-1} + \mu^2}.$$

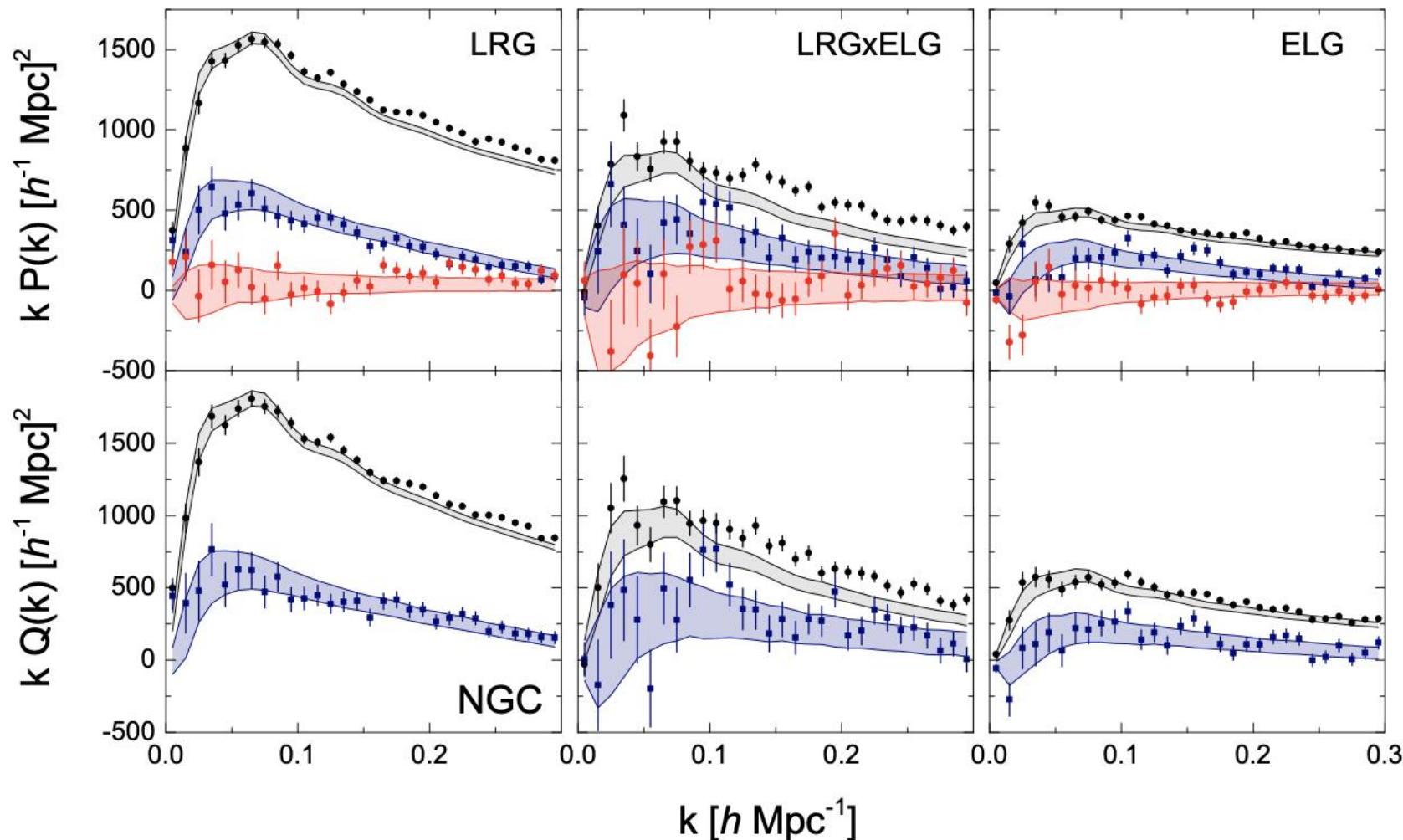
McDonald & Seljak 2008; Seljak 2009

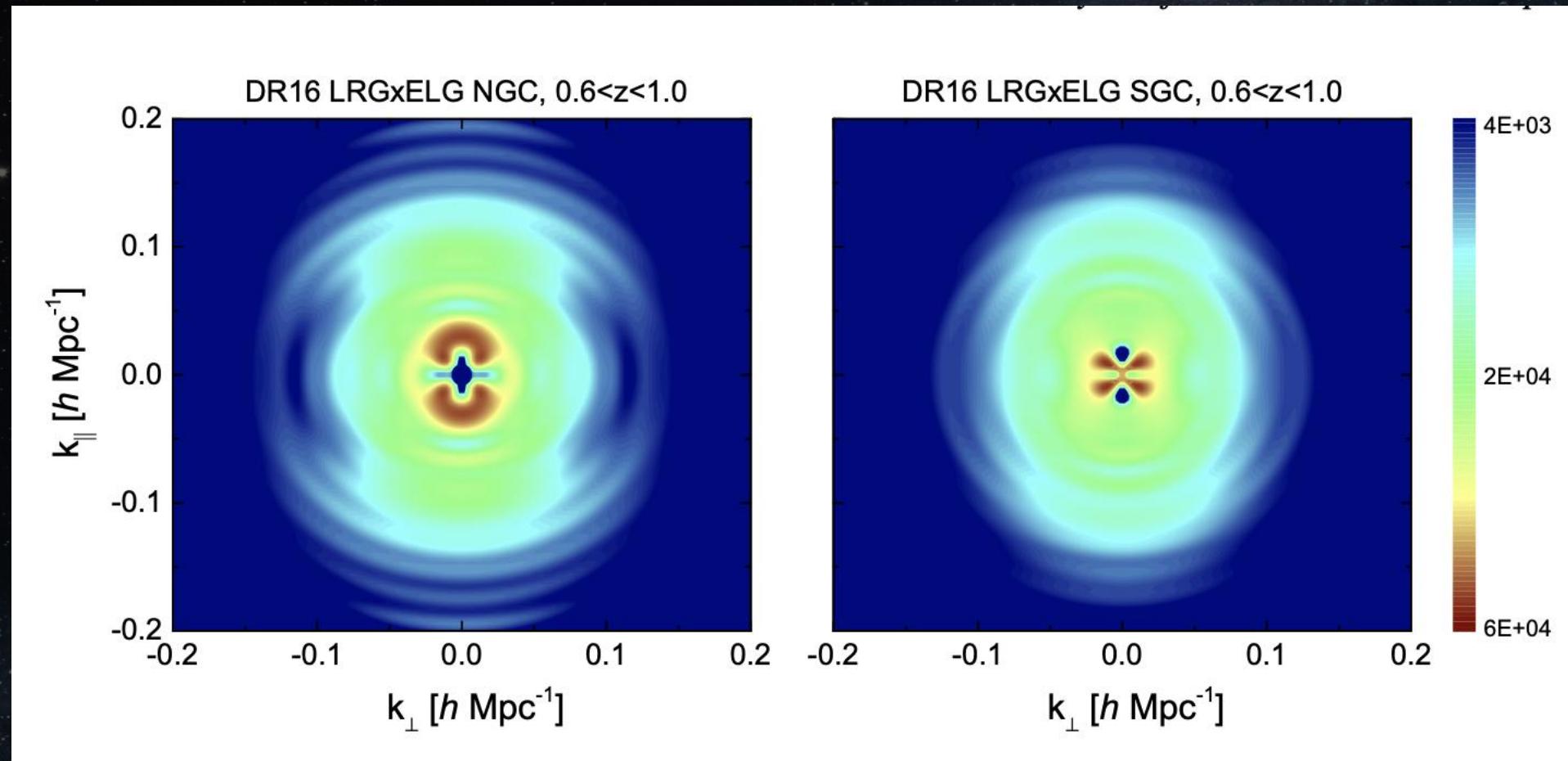
- It can reduce the systematics, as the photometry used for observing different tracers are usually uncorrelated!

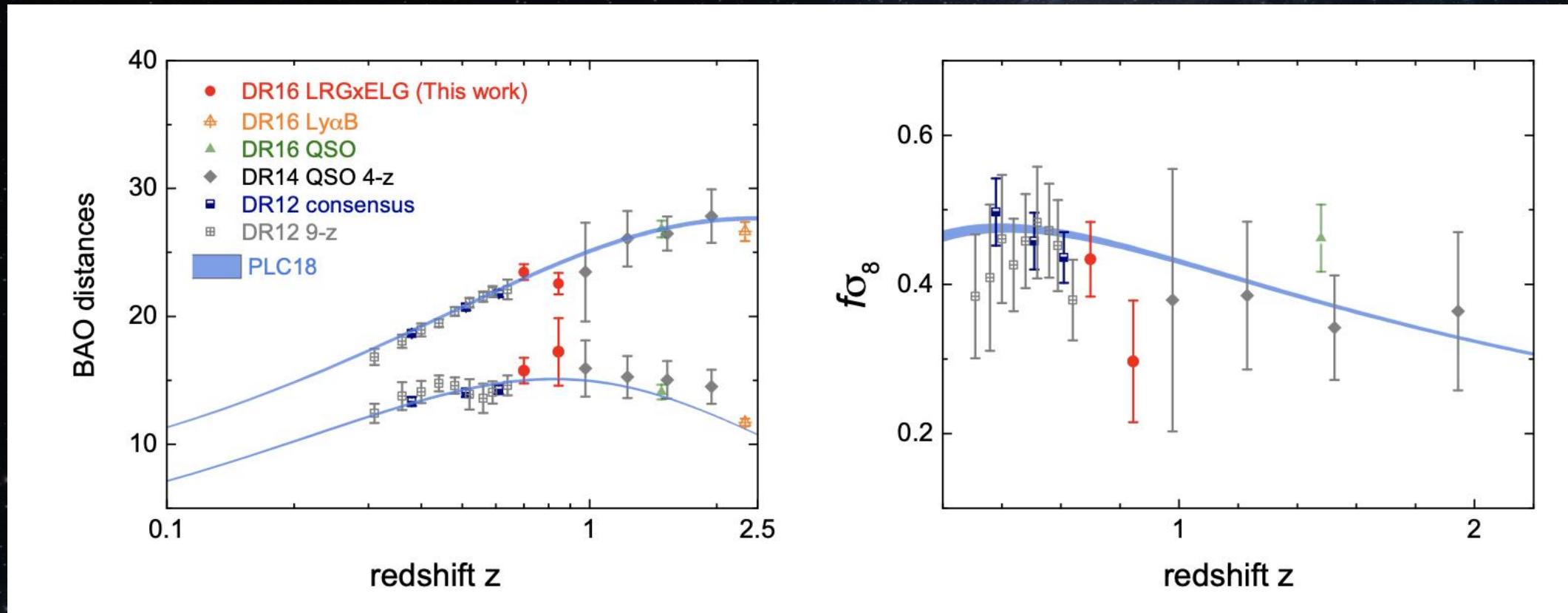


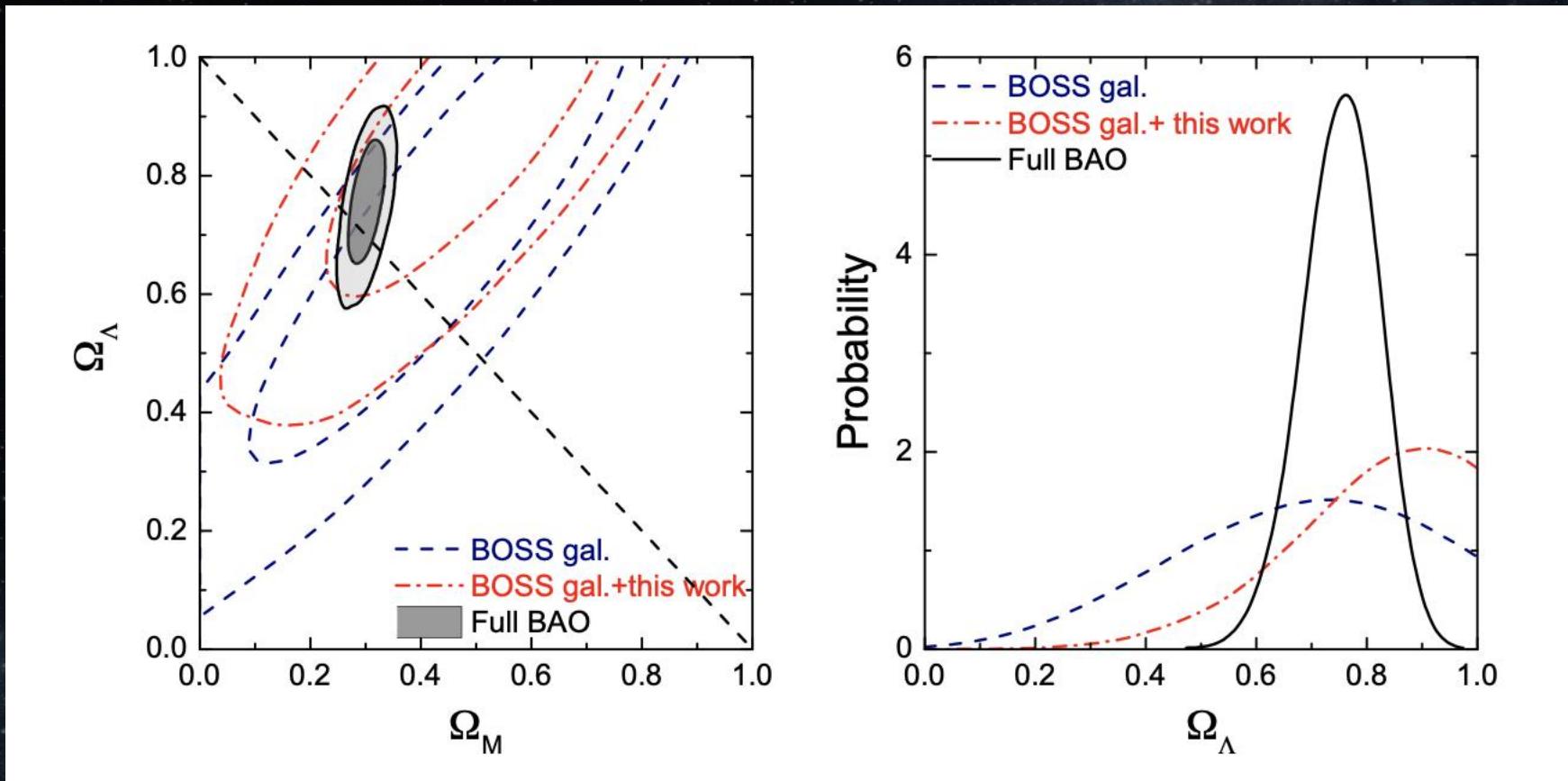
Decent overlap between
eBOSS DR16
LRGs and ELGs
in AREA $\sim 800 \text{ deg}^2$
and in REDSHIFT $[0.6, 1.0]$

Zhao, Wang et al, (eBOSS), 2007.09011 (k-space)
Wang, Zhao et al, (eBOSS), 2007.09010 (s-space)





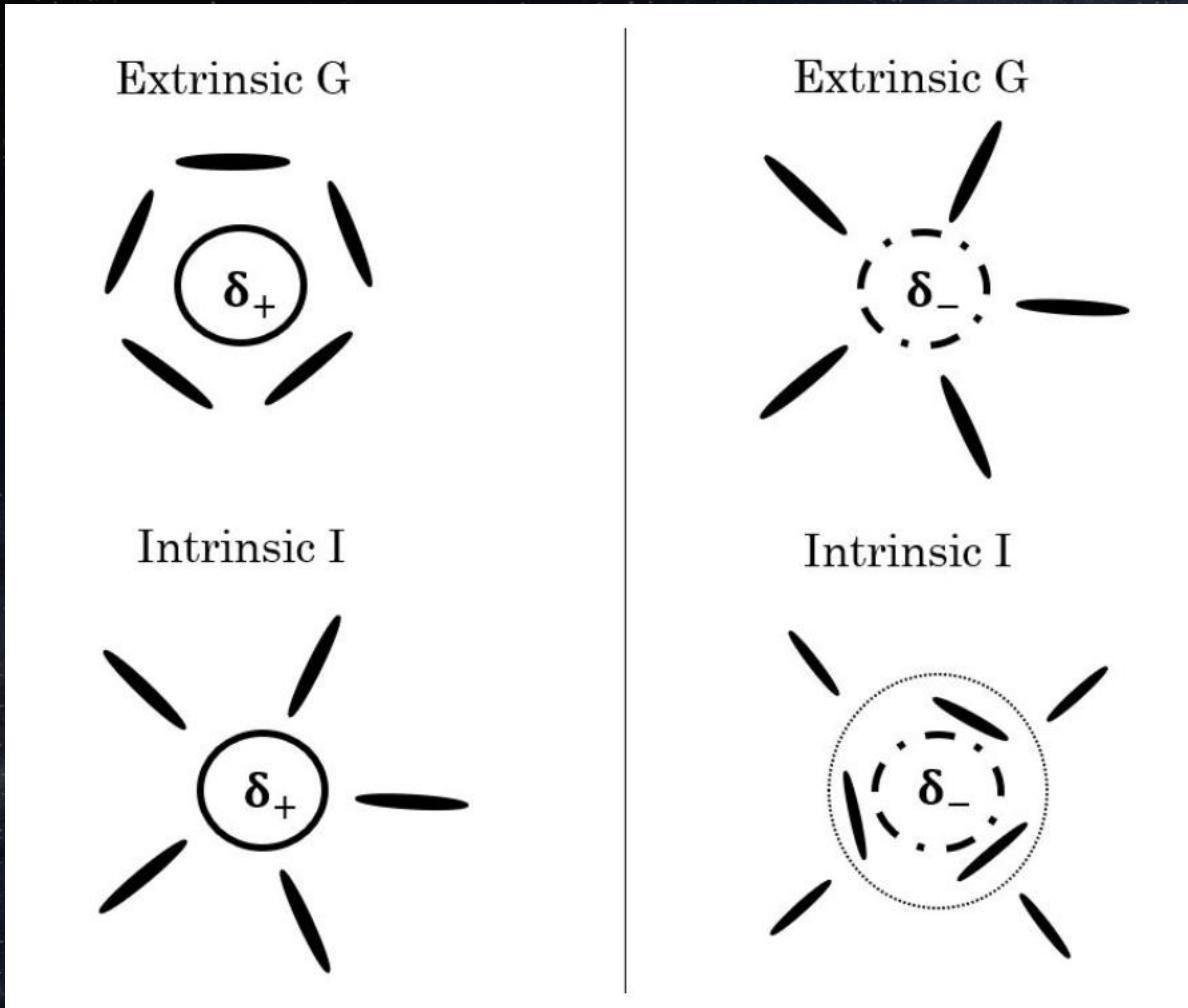




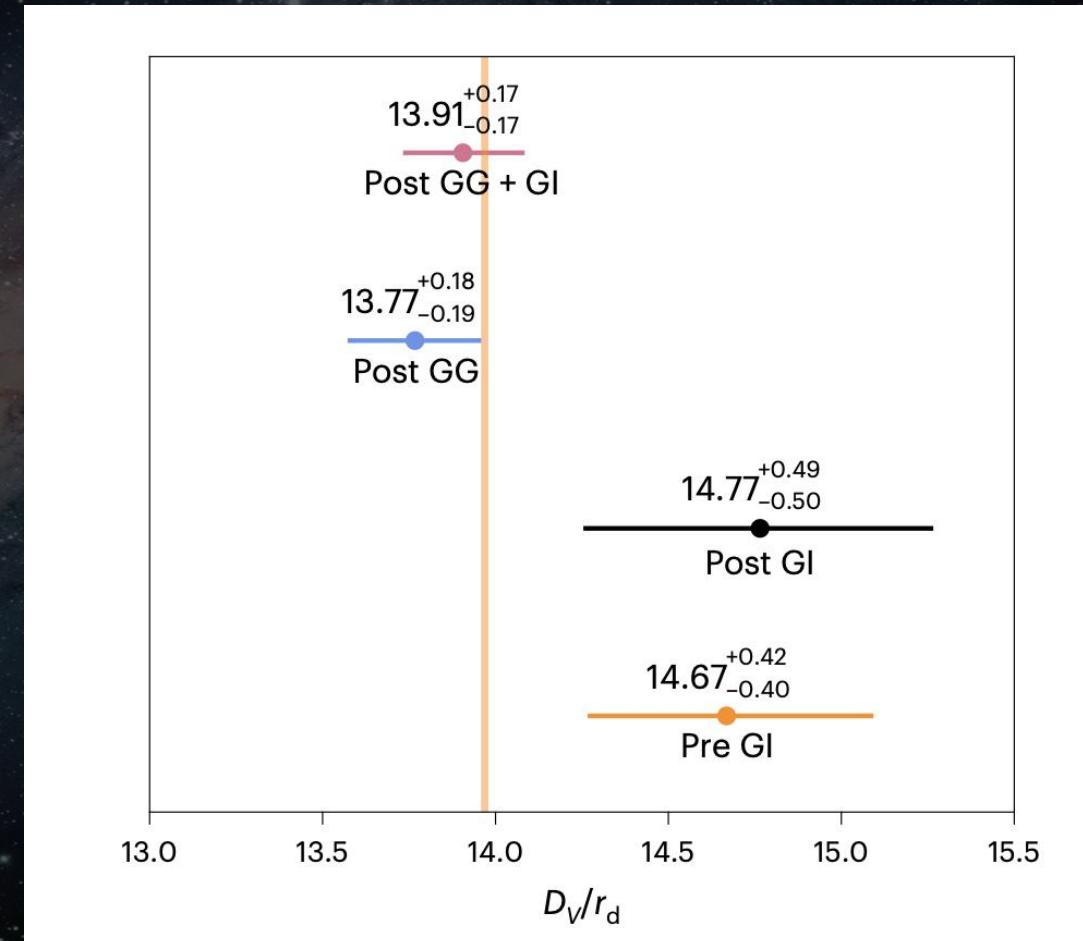
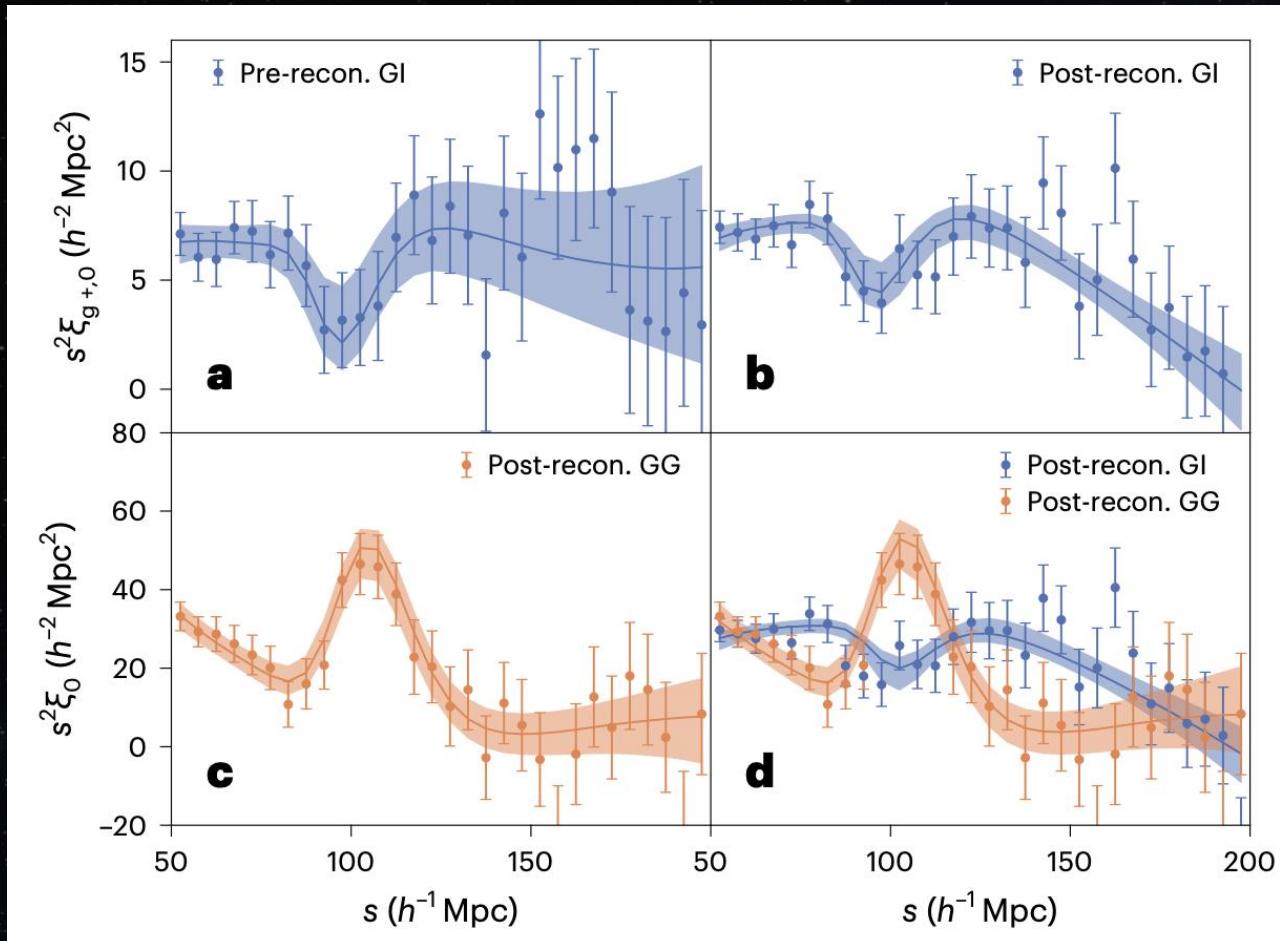
A 11σ detection of $\Omega_\Lambda > 0$

Zhao, Wang et al, (eBOSS), 2007.09011

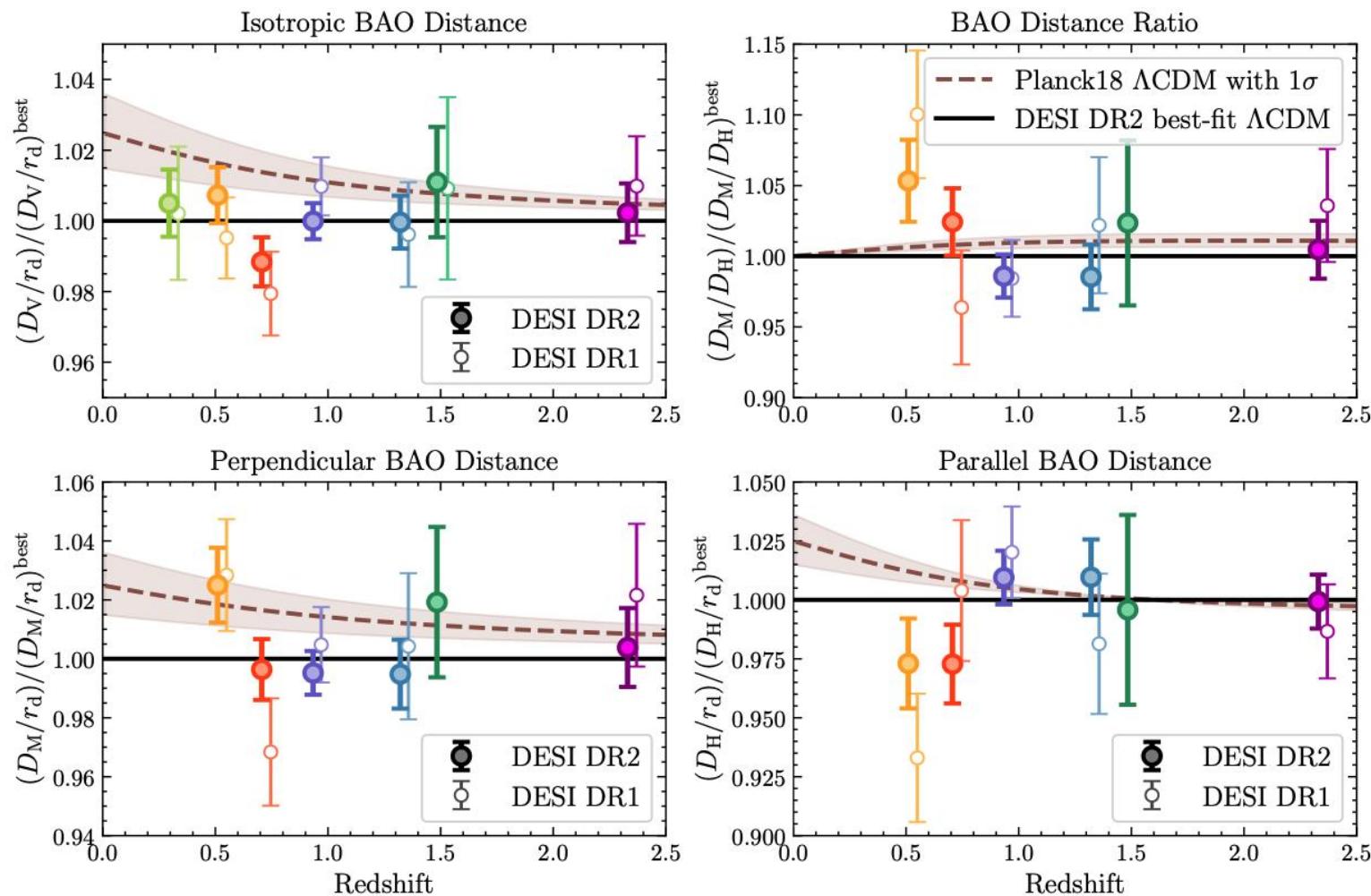
A first detection of BAO from galaxy-ellipticity correlations



d'Assagies D. et al. 2021

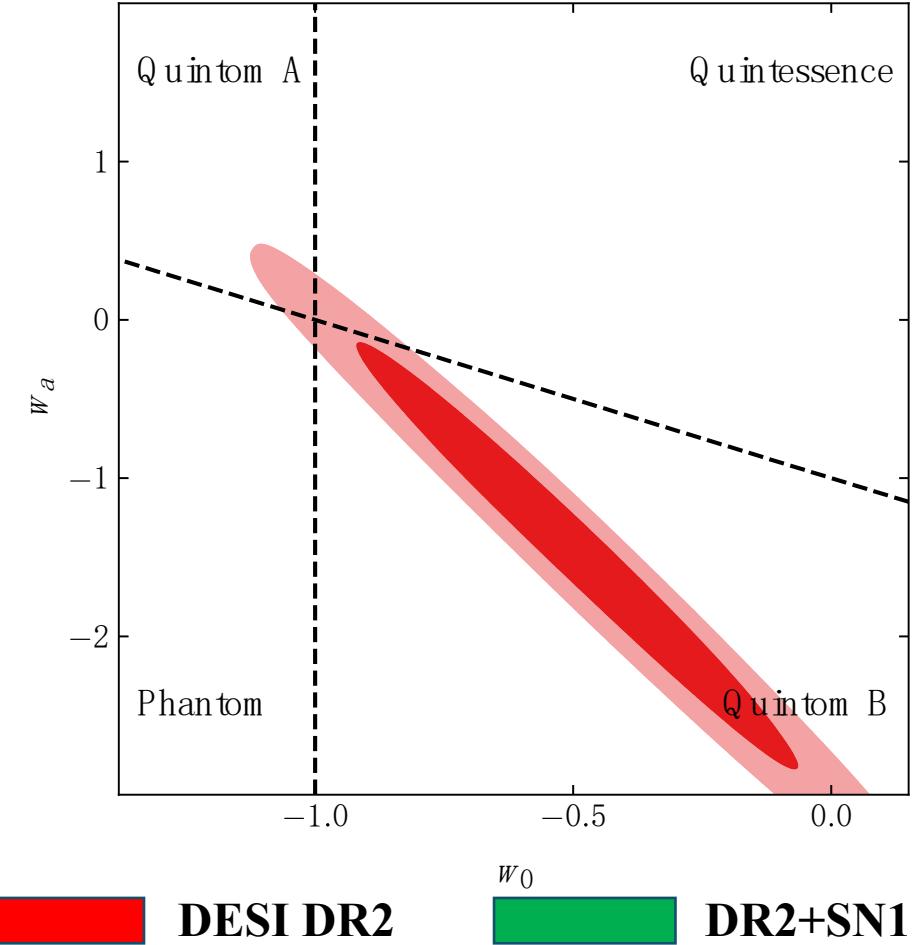
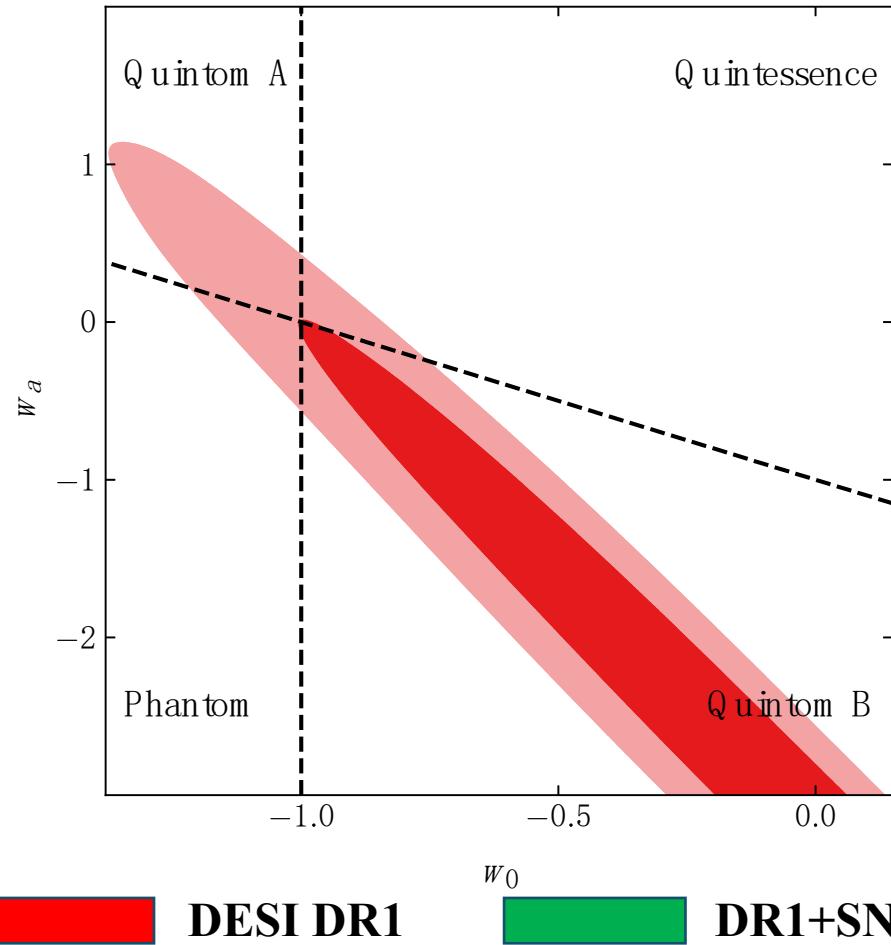


A study of dynamical dark gravity using DESI



A study of dynamical dark gravity using DESI

$$w(a) = w_0 + w_a(1-a)$$



Two ways to study dynamics of dark energy

- Indirect: get features of $w(z)$ directly from distance measurements

✓ : cheap; no data combination needed

✗ : no $w(z)$ derived

Two ways to study dynamics of dark energy

- Indirect: get features of $w(z)$ directly from distance measurements

✓ : cheap; no data combination needed

✗ : no $w(z)$ derived

- Direct: reconstruct $w(z)$ from observations

✓ : show $w(z)$ with details

✗ : expensive; usually requires datasets to be combined

Probing dynamical DE from distance measurements

(Gu et al, 2404.06303; Wang et al, 2404.06310)

$$\frac{D_A(z)}{D_{A,\text{fid}}(z)} = \alpha_0 \left(1 + \alpha_1 x + \frac{1}{2} \alpha_2 x^2 + \frac{1}{6} \alpha_3 x^3 + \frac{1}{24} \alpha_4 x^4 \right) \quad (\text{Zhu et al, 2015})$$

$$\frac{H_{\text{fid}}(z)}{H(z)} = \alpha_0 \left[1 + \alpha_1 + (2\alpha_1 + \alpha_2)x + \left(\frac{3}{2}\alpha_2 + \frac{1}{2}\alpha_3 \right) x^2 + \left(\frac{2}{3}\alpha_3 + \frac{1}{6}\alpha_4 \right) x^3 + \frac{5}{24}\alpha_4 x^4 \right]$$

$$1 + x \equiv D_{A,\text{fid}}(z)/D_{A,\text{fid}}(z_\star)$$

$$S(a) \equiv A\;H^2(a)a^3 = B\;X(a)a^3 + C$$

$$A=r_{\rm d}^2,\;B=AH_0^2(1-\Omega_{\rm M}),\;C=AH_0^2\Omega_{\rm M}\quad X(a)\;\;\equiv\;\;\rho_{\rm DE}(a)/\rho_{\rm DE}(1)$$

$$S(a) \equiv A \; H^2(a) a^3 = B \; X(a) a^3 + C$$

$$A = r_{\rm d}^2, \; B = A H_0^2 (1 - \Omega_{\rm M}), \; C = A H_0^2 \Omega_{\rm M} \quad X(a) \;\; \equiv \;\; \rho_{\rm DE}(a)/\rho_{\rm DE}(1)$$

$$S_0(a) \equiv a^3 - \frac{3[S(a) - S(1)]}{S'(1)} = a^3 + \frac{X(a)a^3 - 1}{w(1)} \stackrel{\Lambda}{\rightarrow} 1.$$

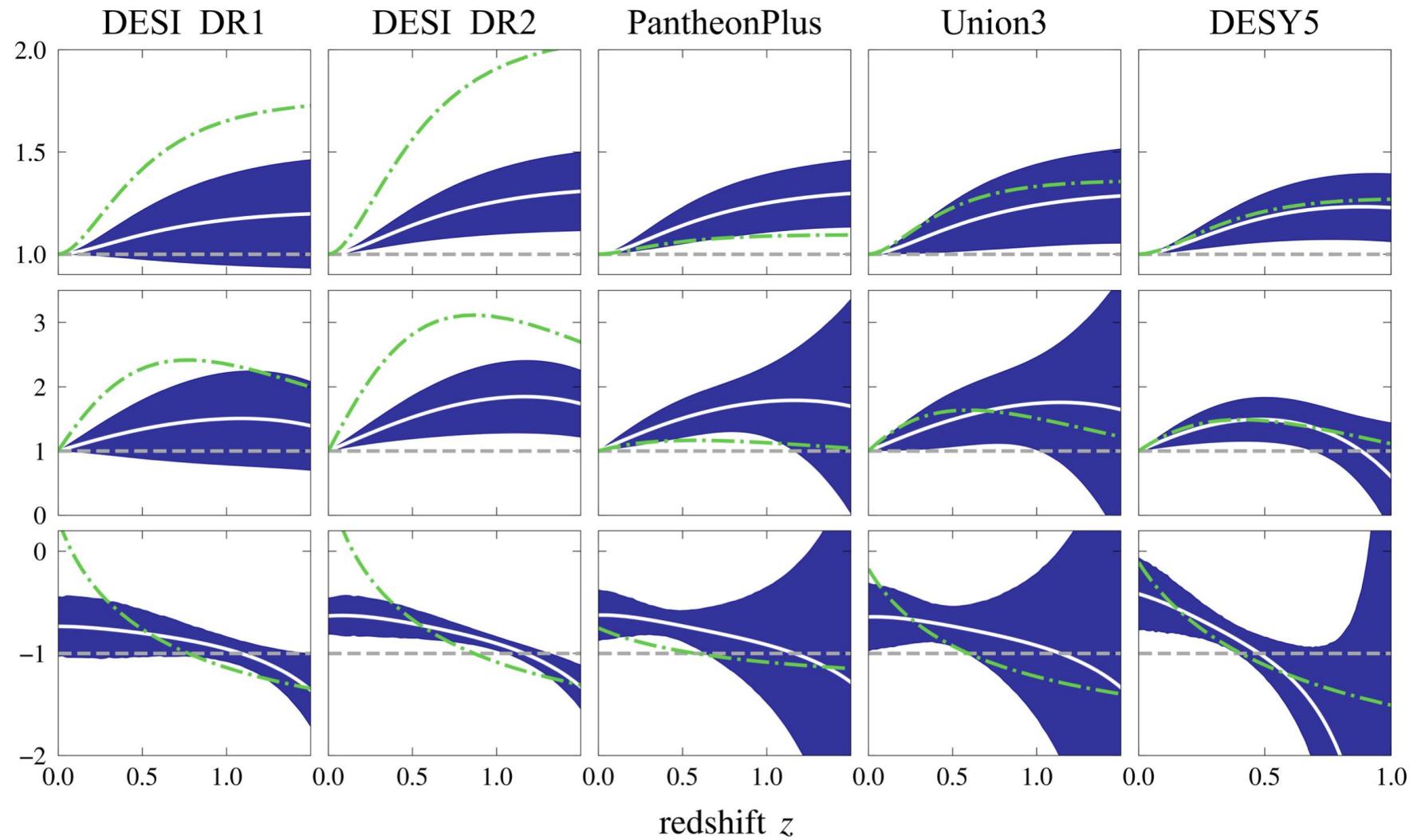
$$S_1(a) \equiv \frac{1}{a^3} \frac{S'(a)}{S'(1)} = \frac{P_{\rm DE}(a)}{P_{\rm DE}(1)} \stackrel{\Lambda}{\rightarrow} 1,$$

$$S_2(a) \equiv -\frac{S''(a)}{3S'(a)} = w(a) - \frac{w'(a)}{3w(a)} \stackrel{\Lambda}{\rightarrow} -1,$$

$$a^3 + \frac{X(a)a^3 - 1}{w(1)}$$

$$\frac{P_{\text{DE}}(a)}{P_{\text{DE}}(1)}$$

$$w(a) - \frac{w'(a)}{3w(a)}$$



Reconstructing the evolution history of dark energy

Crittenden, Pogosian, GBZ (**CPZ**, JCAP 2009)

Crittenden, GBZ, Pogosian, Samushia, Zhang (JCAP 2012)

$$\xi_w(|a - a'|) \equiv \langle [w(a) - w^{\text{fid}}(a)][w(a') - w^{\text{fid}}(a')] \rangle$$

$$w_i = \frac{1}{\Delta} \int_{a_i}^{a_i + \Delta} da w(a)$$

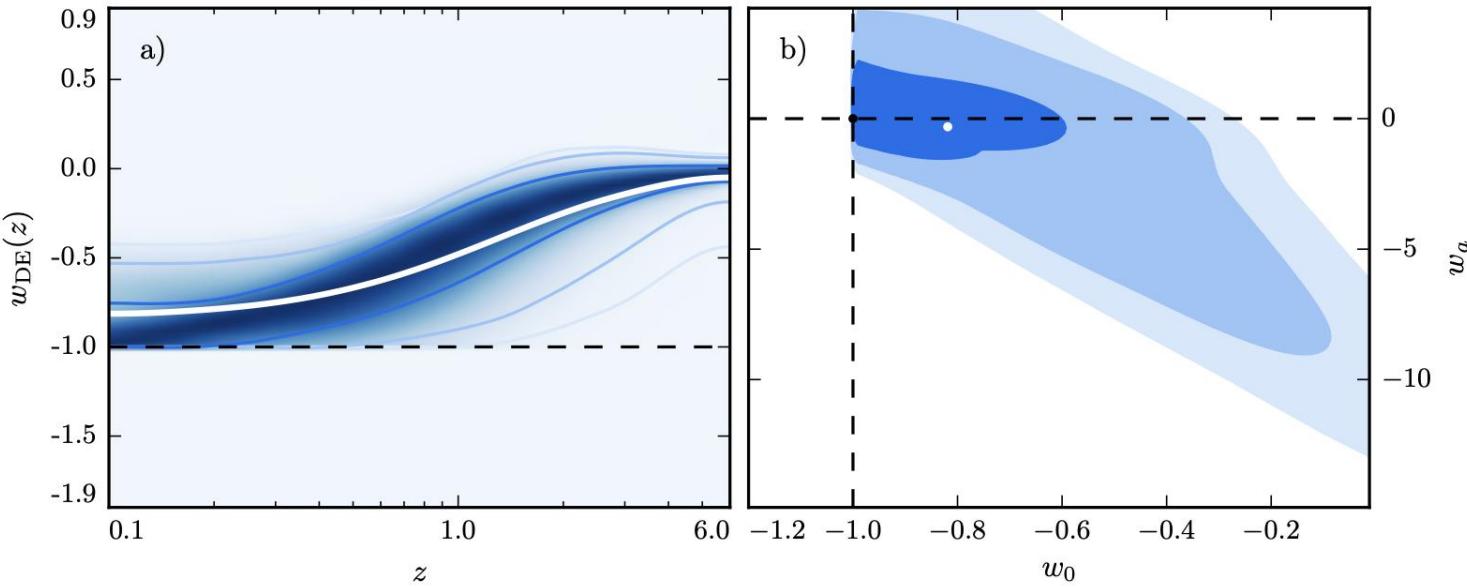
$$C_{ij} \equiv \langle \delta w_i \delta w_j \rangle = \frac{1}{\Delta^2} \int_{a_i}^{a_i + \Delta} da \int_{a_j}^{a_j + \Delta} da' \xi_w(|a - a'|)$$

$$\chi_{\text{prior}}^2 = -2 \ln \mathcal{P}_{\text{prior}} = (\mathbf{w} - \mathbf{w}^{\text{fid}})^T \mathbf{C}^{-1} (\mathbf{w} - \mathbf{w}^{\text{fid}})$$

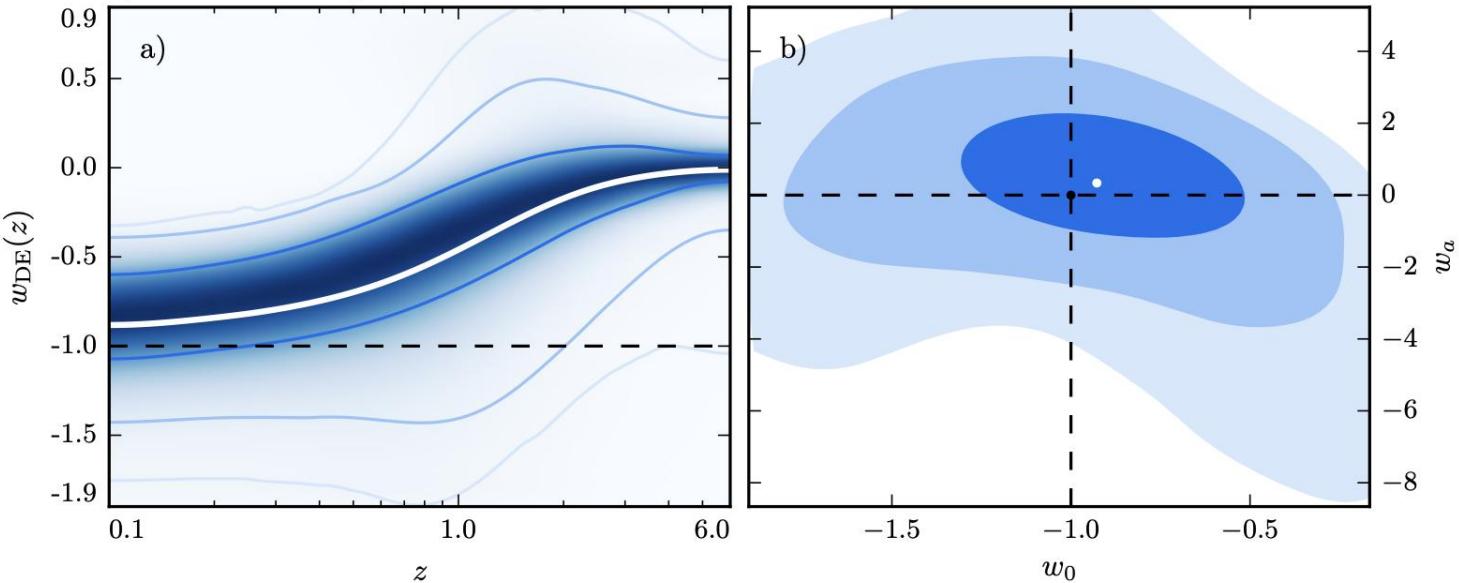
Theory-motivated correlated prior on $w(z)$ (Raveri et al, 1703.05297)

$$\begin{aligned}
 S = & \int d^4x \sqrt{-g} \left\{ \frac{m_0^2}{2} [1 + \Omega(\tau)] R + \Lambda(\tau) - c(\tau) a^2 \delta g^{00} \right. \\
 & + \frac{M_2^4(\tau)}{2} (a^2 \delta g^{00})^2 - \frac{\bar{M}_1^3(\tau)}{2} a^2 \delta g^{00} \delta K_\mu^\mu \\
 & + \frac{\bar{M}_3^2(\tau)}{2} \left[(\delta K_\mu^\mu)^2 - \delta K_\nu^\mu \delta K_\mu^\nu - \frac{a^2}{2} \delta g^{00} \delta \mathcal{R} \right] + \dots \left. \right\} \\
 & + S_m[g_{\mu\nu}, \chi_m], \tag{1}
 \end{aligned}$$

1) Results for the quintessence class of models

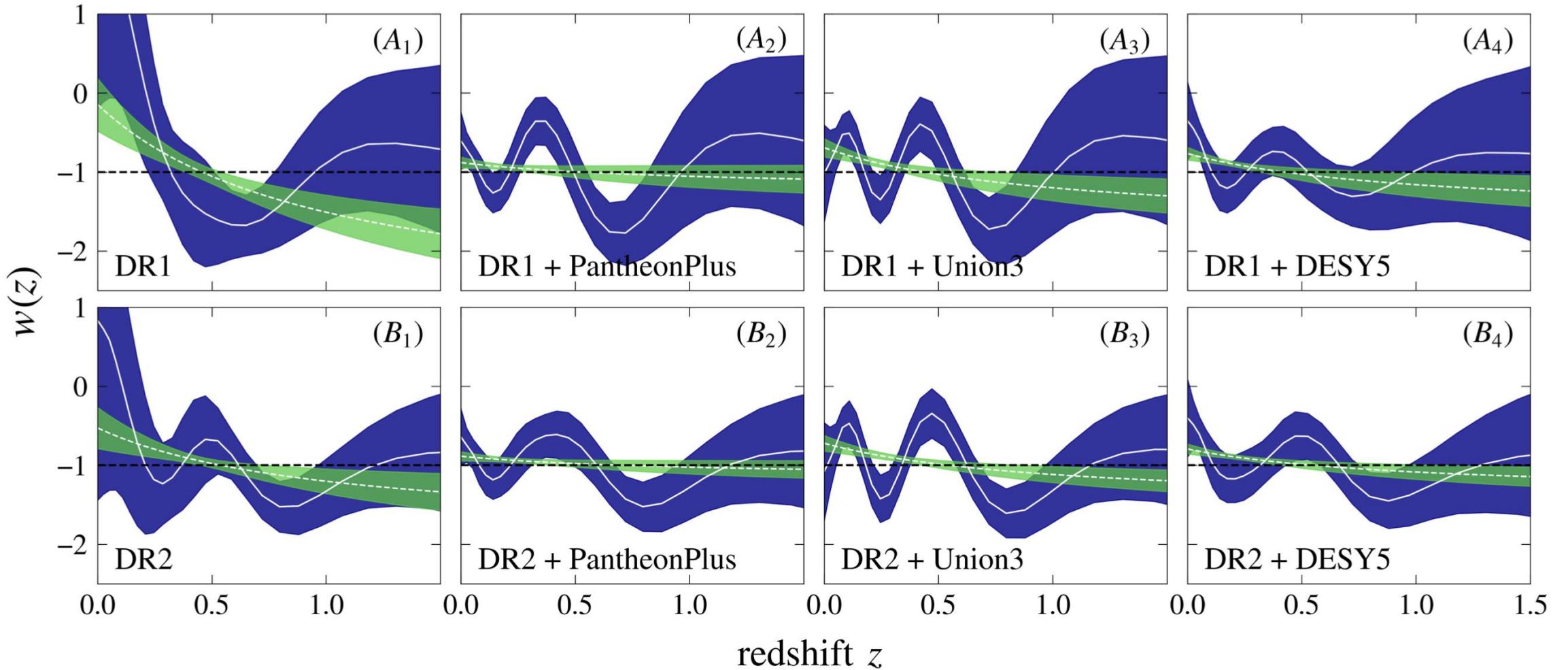


2) Results for the general Horndeski class of models

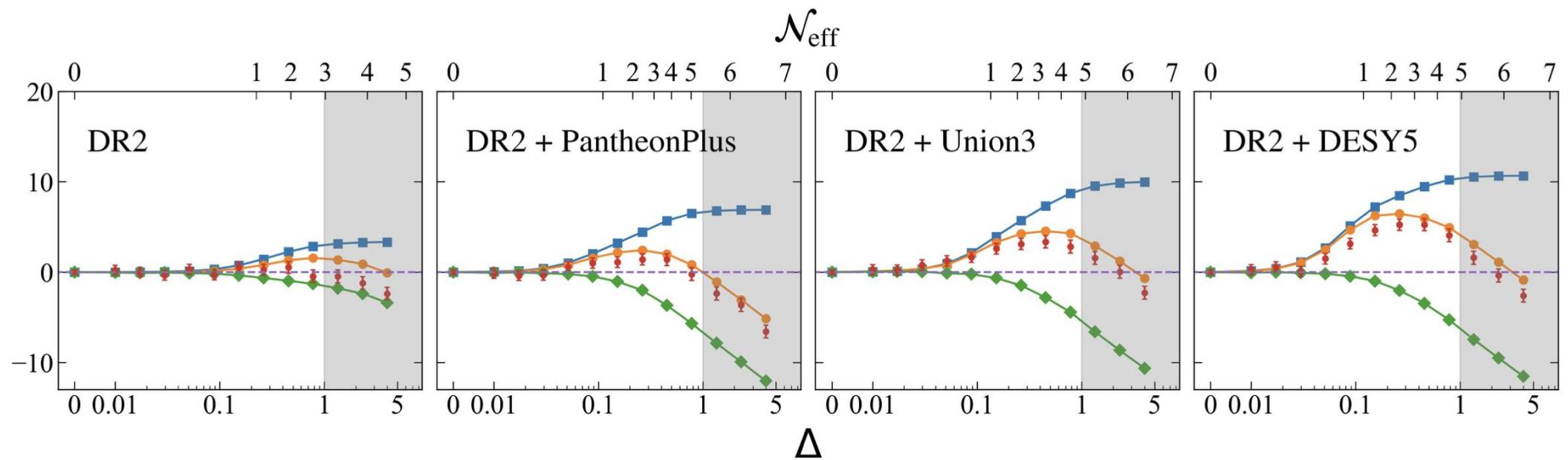
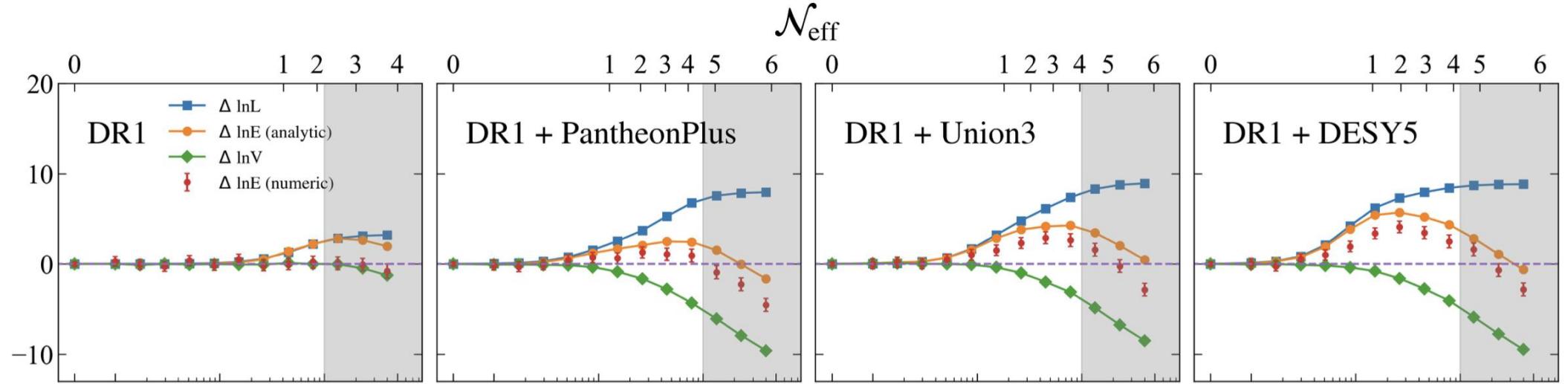


$$\begin{aligned} C(a, a') &\equiv \langle [w(a) - w_{\text{fid}}(a)][w(a) - w_{\text{fid}}(a')] \rangle \\ &= \sqrt{C(a)C(a')} R(a, a'), \end{aligned}$$

$$\begin{aligned} C(a) &= 0.05 + 0.8a^2, \\ R(a, a') &= \exp \left[- \left(|\ln a - \ln a'| / 0.3 \right)^{1.2} \right] \end{aligned}$$



Bayesian Evidence



Summary and next steps

- DESI BAO data show interesting signs of new physics, awaiting confirmation of Y5 and later observations;
- As statistical errors get reduced, more work is needed to mitigate the systematics;
- New statistics (MFs, wavelets, etc) and new ideas (tests of parity, etc) are needed to probe new physics from future galaxy surveys.