



Funded by the
European Union



Tensions in Cosmology: Are we Approaching New Physics?

Emmanuel N. Saridakis

National Observatory of Athens

IHEP, Beijing July 2025

CANTATA

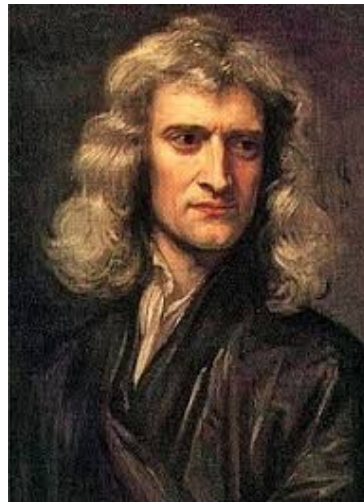
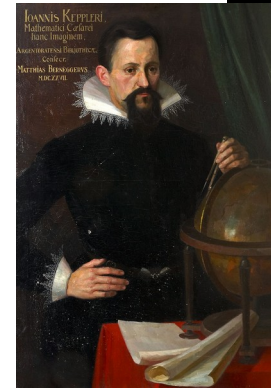
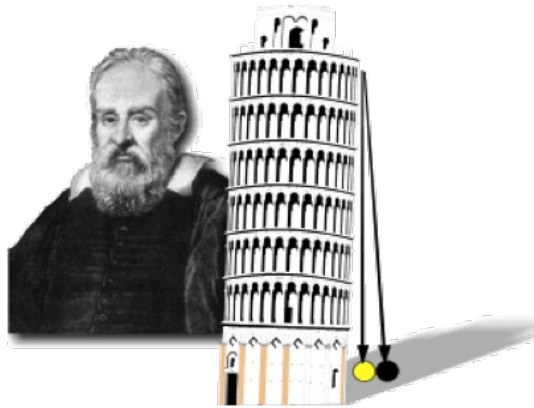
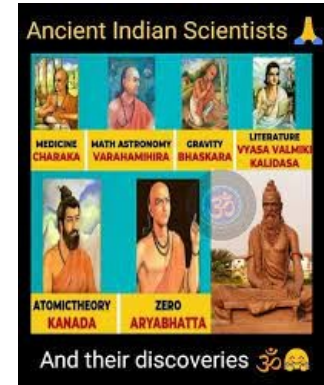
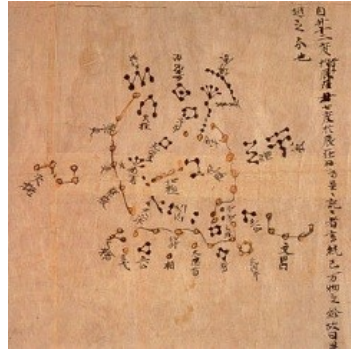
Cosmology and Astrophysics Network for
Theoretical Advances and Training Actions



- The **history** of **Science** is a **history of tensions** between **theoretical predictions** and **observations**
- **Astrophysics and Cosmology** have become **precision sciences** with an incredibly **huge amount of data**
 - **New Tensions appear.**

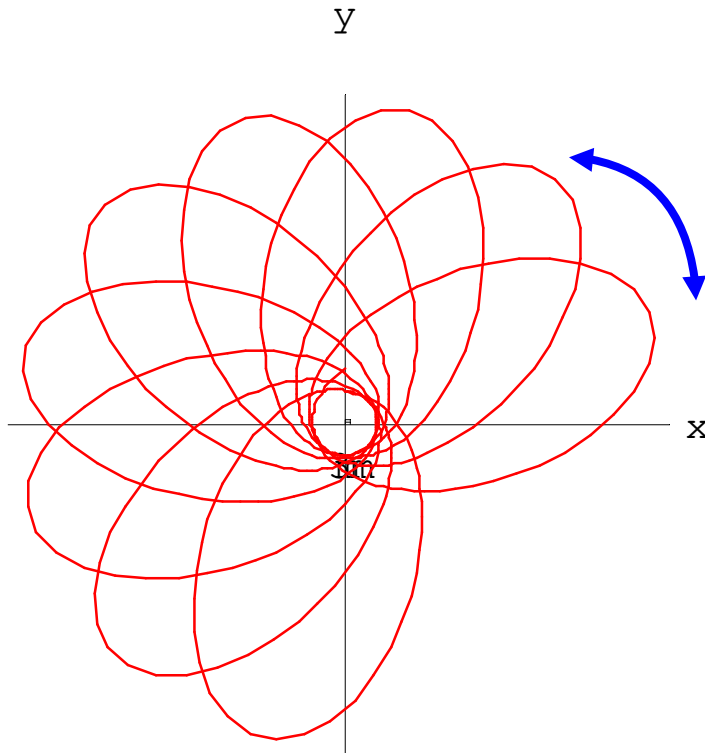
Are we approaching New Physics?

History of Science - History of Tensions



Mercury perihelium - 1859

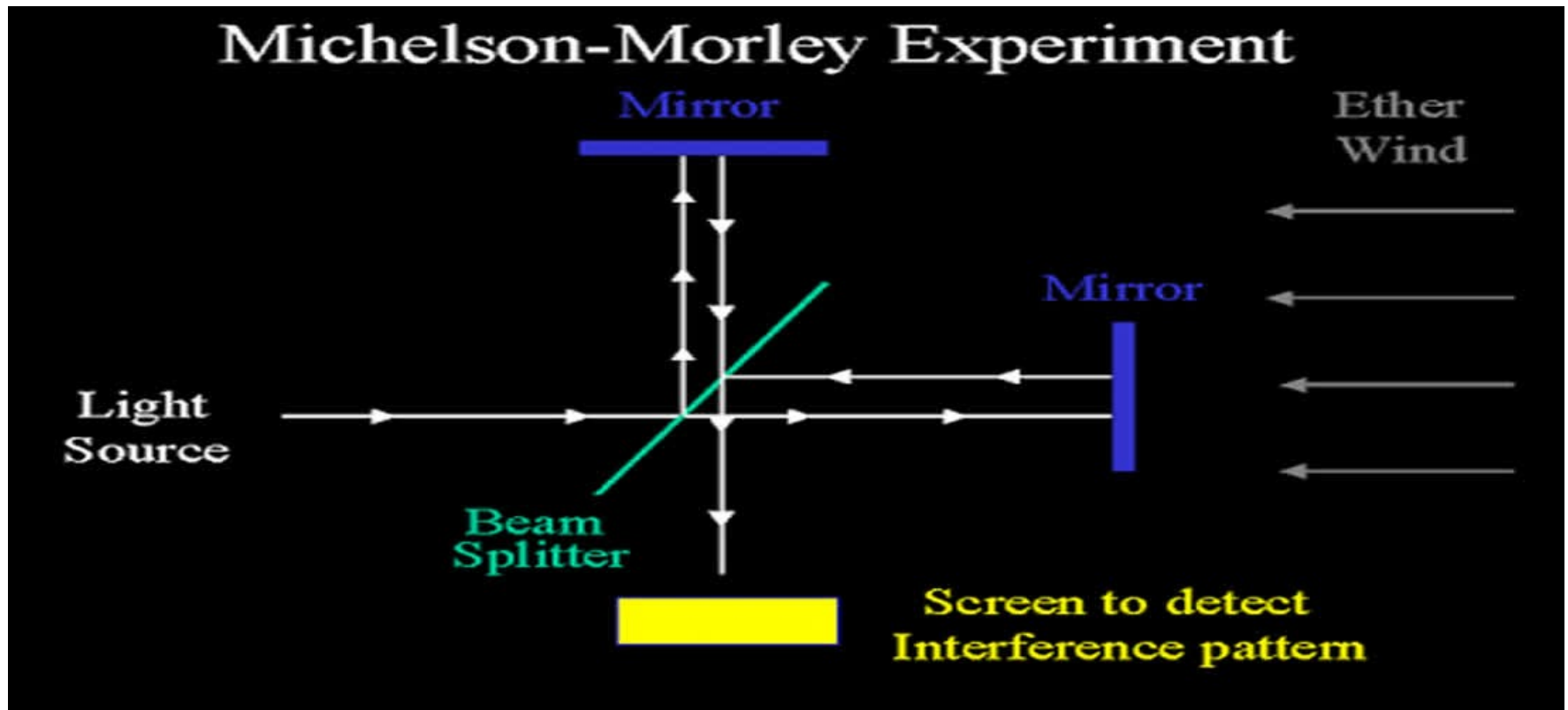
- The true orbits of planets, even if seen from the SUN are not ellipses. They are rather curves of this type:



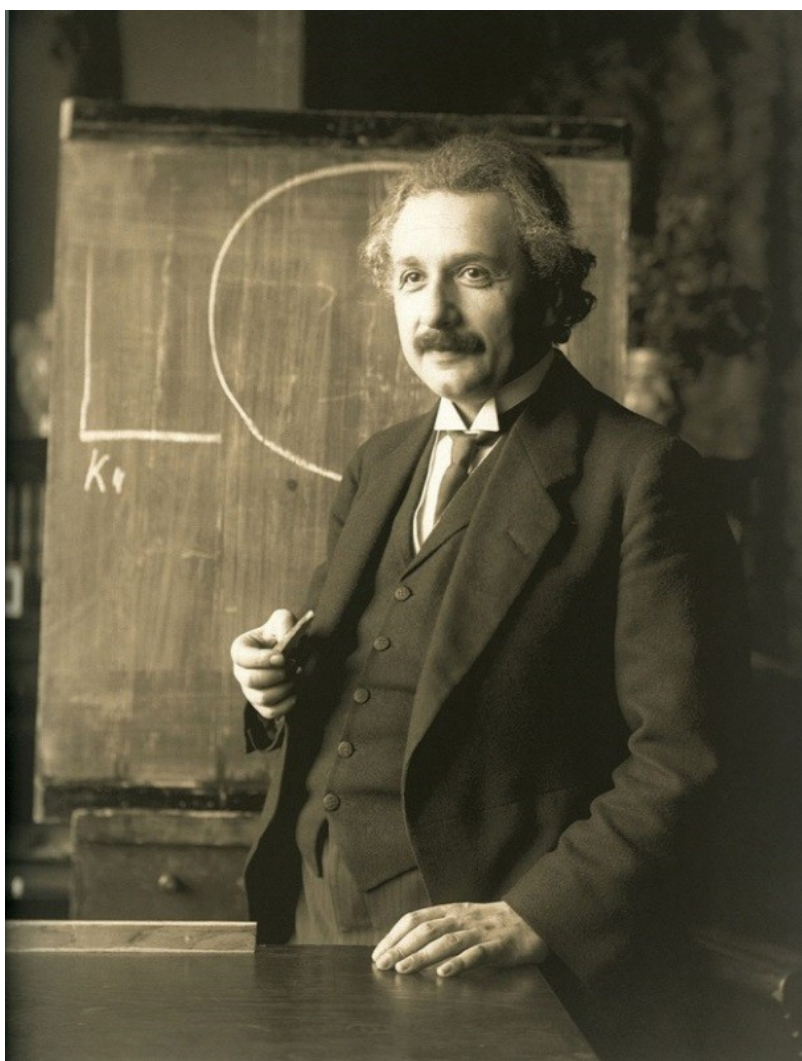
For the planet Mercury it is

$\Delta\varphi = 43''$ of arc per century

Michelson-Morley experiment - 1887



The Theory of Relativity

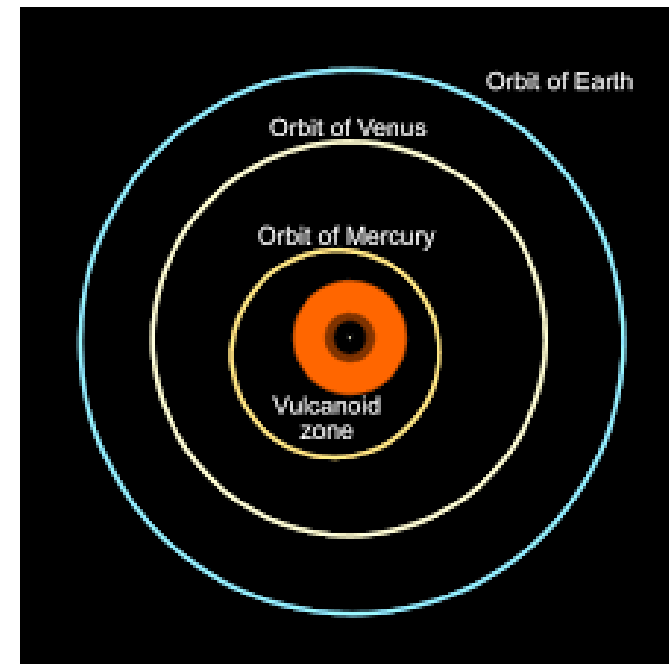


$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} [R - 2\Lambda] + \int d^4x L_m(g_{\mu\nu}, \psi)$$

$$\Rightarrow R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R + g_{\mu\nu} \Lambda = 8\pi G T_{\mu\nu}$$

$$T^{\mu\nu} \equiv \frac{2}{\sqrt{-g}} \frac{\delta L_m}{\delta g_{\mu\nu}}$$

60 years of tension



Modified Gravity before General Relativity

- Modifications to **Newton's Law**
- **Inverse Cube Law**.
- **Extended Inverse-Square Law** (Simon Newcomb - 1880's)
- **Lord Kelvin** - theory of everything (end of 19th century)
- **Hendrik Lorentz**: gravity on the basis of his ether theory and Maxwell's equations. (1900)
- **Nordström's theory of gravitation** (1912 and 1913)
- **Einstein's scalar theory of gravity** (1913)

History of Major Shifts of Cosmological Models

Aristarchus of Samos (c. 310-230 BCE)

- ▶ **Geocentric (Ptolemy) to Heliocentric (Copernicus, 16th-17th c.):**
 - ▶ Retrograde motion (Copernicus)
 - ▶ Phases of Venus, Moons of Jupiter (Galileo, 1610)
- ▶ **Heliocentric to Infinite Universe (18th-19th c.):**
 - ▶ Improved telescopes, Uranus discovery (Herschel, 1781)
 - ▶ Stellar parallax (Bessel, 1838)
- ▶ **Infinite to Static Universe (Einstein, early 20th c.):**
 - ▶ Nebulae spectroscopy (Slipher)
 - ▶ Stellar distances (Leavitt, Hertzsprung)
- ▶ **Static to Expanding Universe (Lemaître, Hubble, 1920s-30s):**
 - ▶ Galactic redshift (Slipher, 1912-14)
 - ▶ Hubble's law (Hubble, 1929)
- ▶ **Expanding Universe to Inflationary Big Bang (1960s-80s):**
 - ▶ CMB (Penzias & Wilson, 1964)
 - ▶ Light element abundance (Alpher, Herman)
 - ▶ Inflation theory (Guth, Linde, 1980s)
- ▶ **Introduction of Dark Matter (1970s-80s):**
 - ▶ Galaxy rotation curves (Rubin, 1970s)
 - ▶ Gravitational lensing (Walsh et al., 1979)
 - ▶ Galaxy clusters (Zwicky, 1930s)
- ▶ **Lambda-CDM (late 1990s-present):**
 - ▶ Supernova observations (Perlmutter, Schmidt, Riess, 1998-99)
 - ▶ CMB (WMAP, Planck), BAO (SDSS, 2005)
- ▶ **Potential Future Shift (2020s-?):**
 - ▶ Hubble tension (Riess et al. vs Planck Collaboration)
 - ▶ S8 (growth rate) tension (KiDS, DES, Planck collaborations)
 - ▶ Cosmic dipoles tension (Various teams)
 - ▶ CMB anomalies (Planck Collaboration)
 - ▶ ISW (Integrated Sachs-Wolfe) tension
 - ▶ Lithium problem (Primordial Nucleosynthesis)



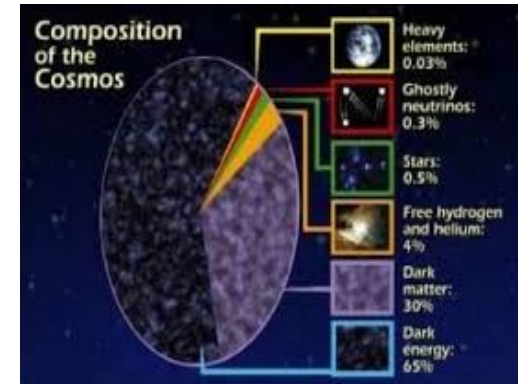
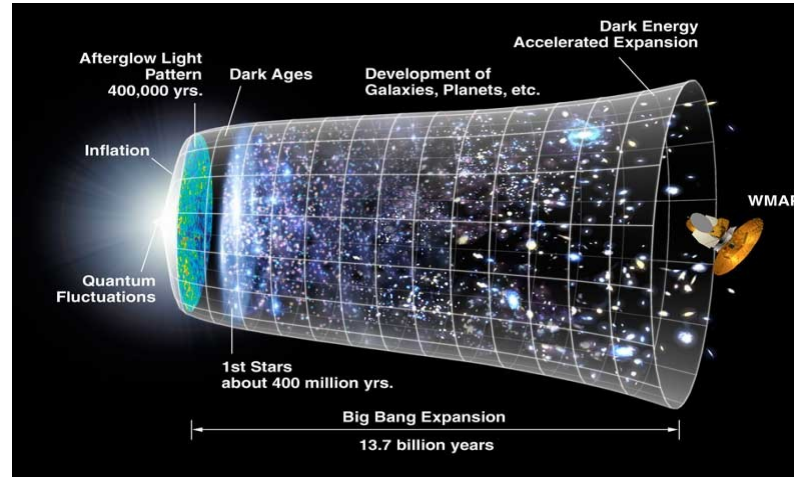
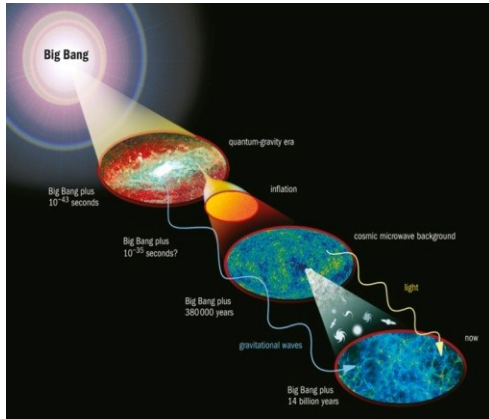
New Astronomy Reviews
Volume 95, December 2022, 101659



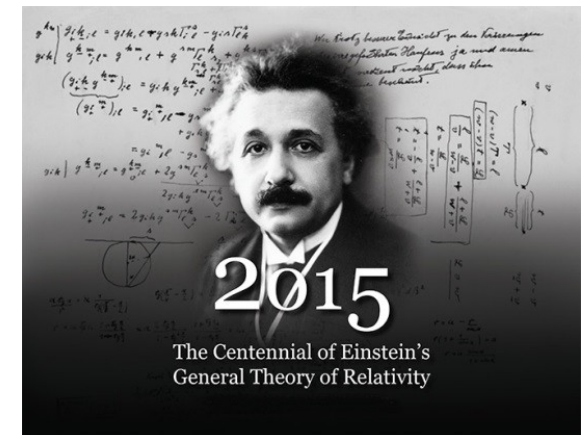
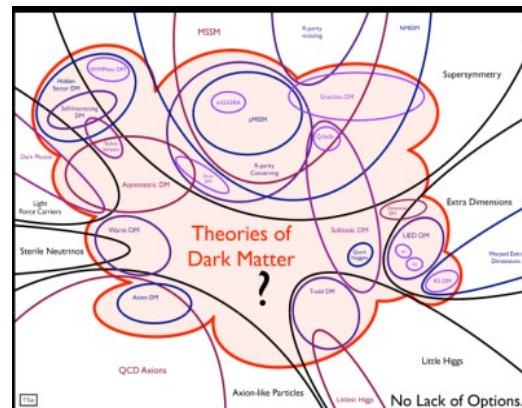
Challenges for Λ CDM: An update

L. Perivolaropoulos , F. Skara

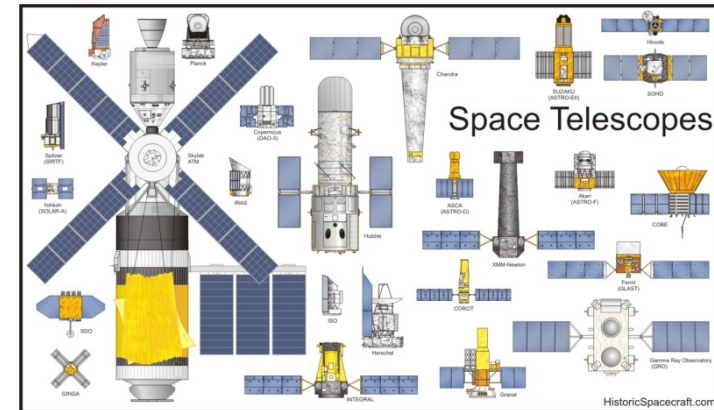
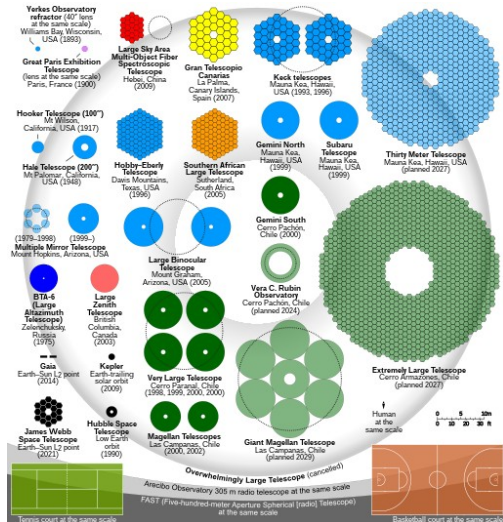
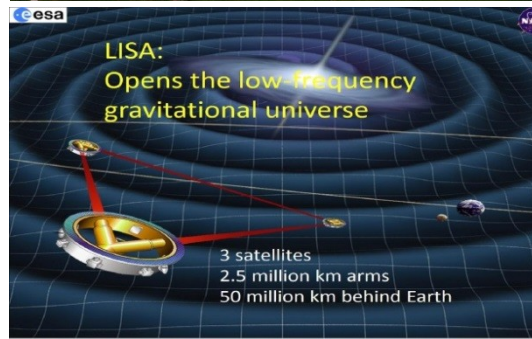
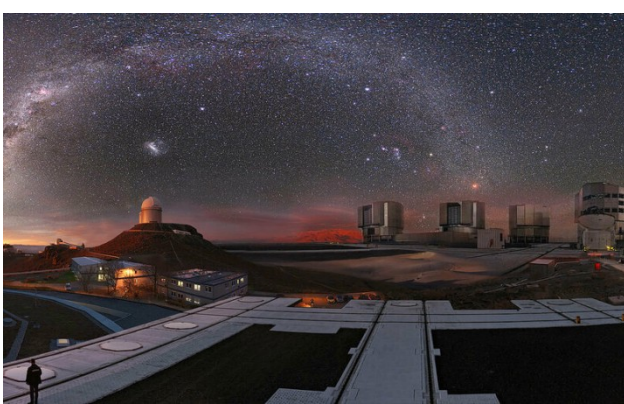
Summary of 20th century Observations



mass →	≈2.3 MeV/c ²	≈1.275 GeV/c ²	≈173.07 GeV/c ²	0	≈126 GeV/c ²
charge →	2/3	2/3	2/3	0	0
spin →	1/2	1/2	1/2	1	0
	u up	c charm	t top	g gluon	H Higgs boson
	≈4.8 MeV/c ²	≈95 MeV/c ²	≈4.18 GeV/c ²	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	d down	s strange	b bottom	γ photon	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	0	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
	≈2.2 eV/c ²	≈0.17 MeV/c ²	≈15.5 MeV/c ²	80.4 GeV/c ²	
	0	1/2	1/2	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	



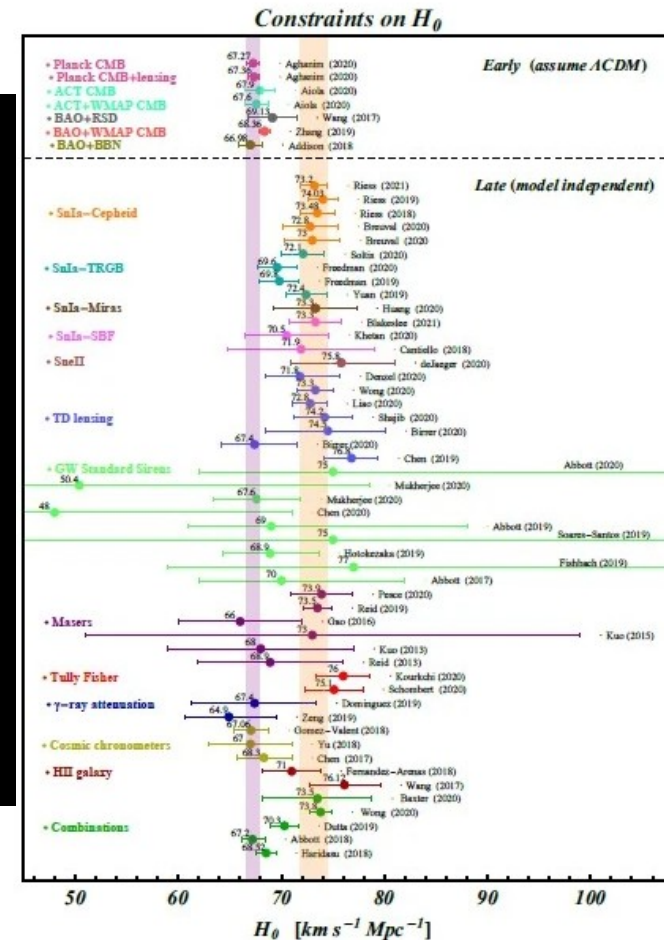
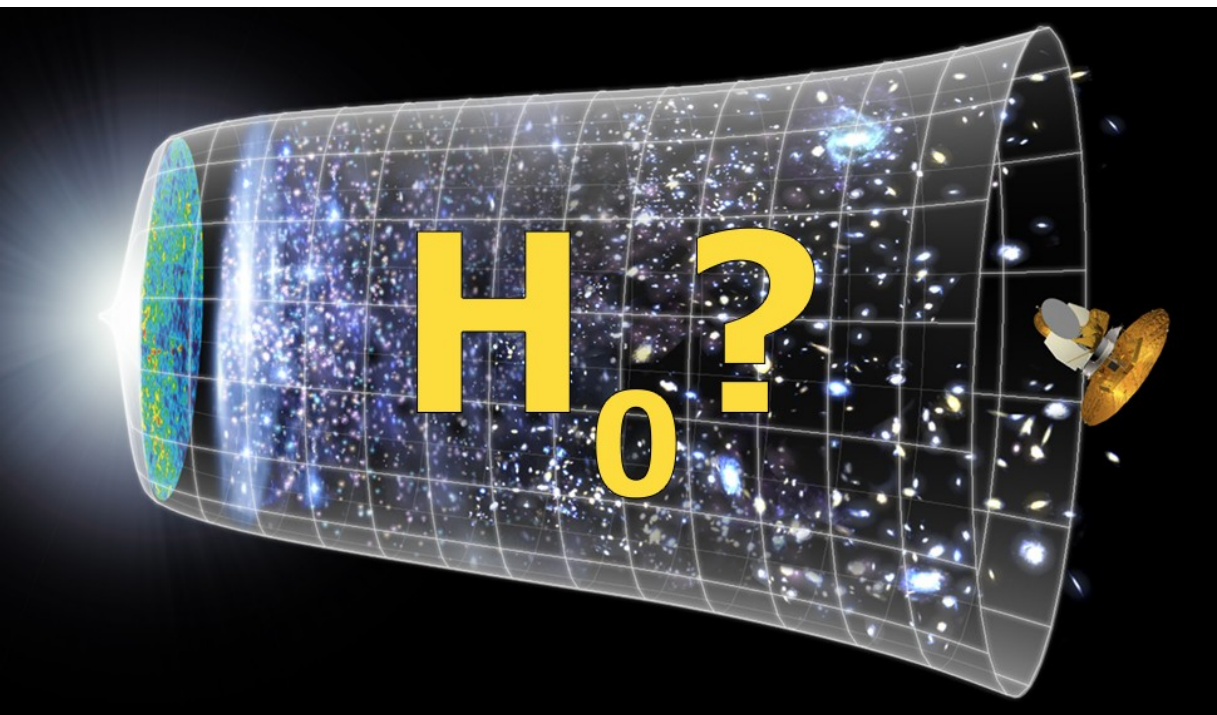
Astrophysics and Cosmology in the 21st century



So what do
these new
observations
tell us?

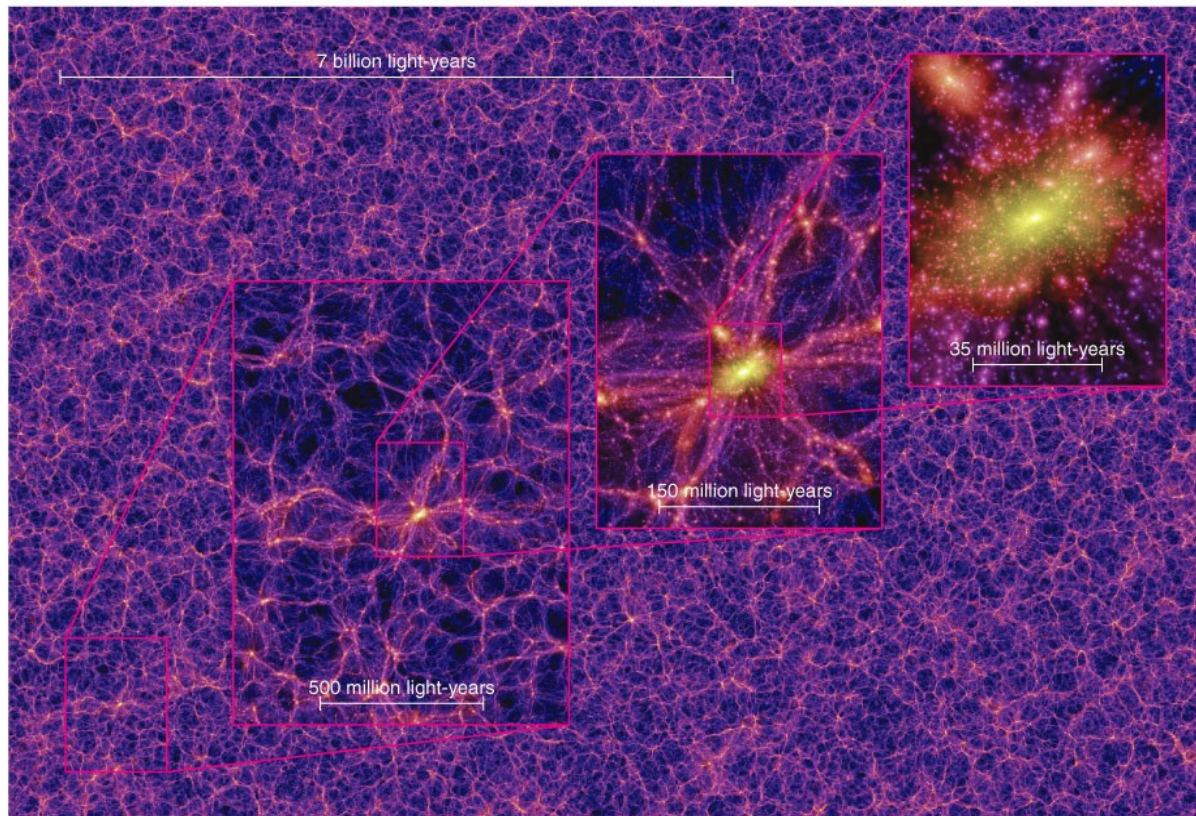
H₀ tension

- The Universe **expands faster** than **expected!**

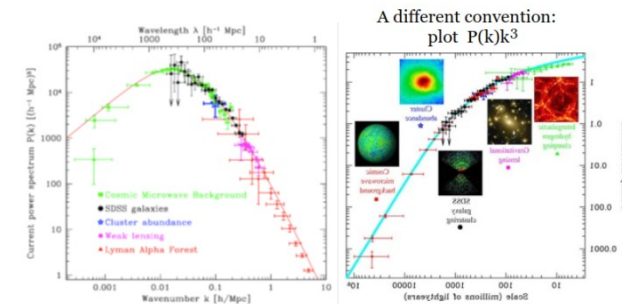


S8 Tension

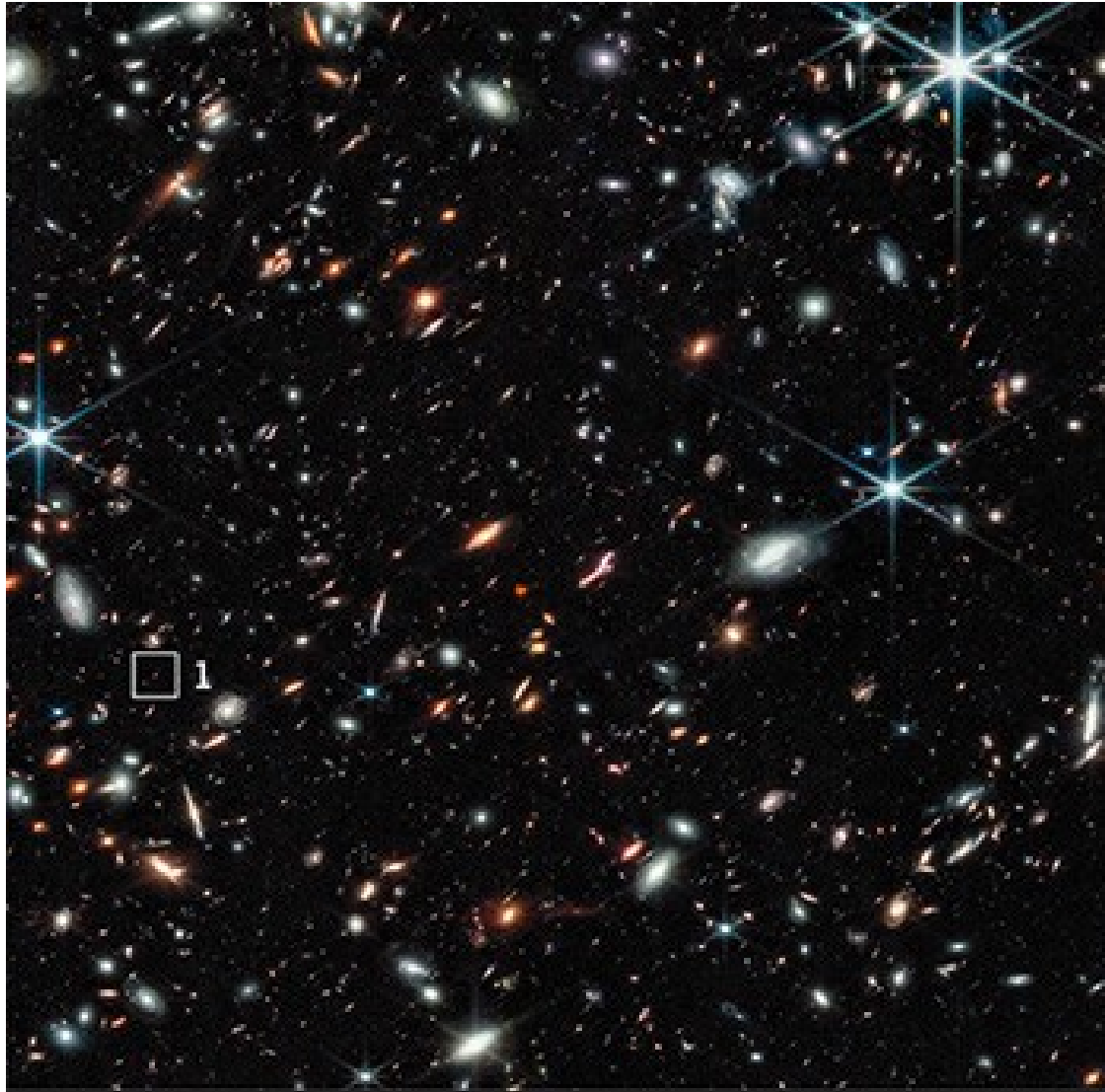
- “Less” Matter clustering than expected!



Matter Density Fluctuation
Power Spectrum

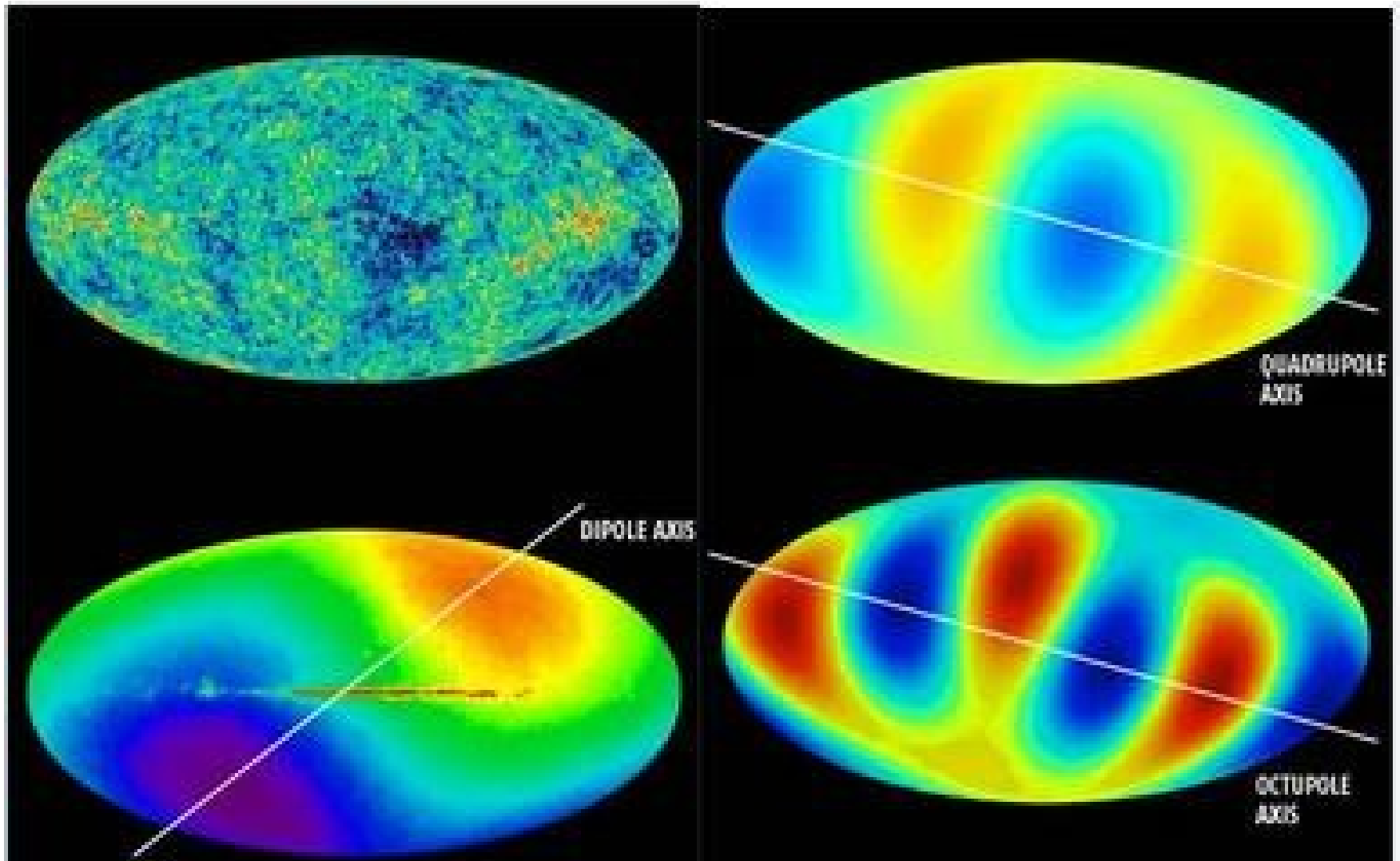


Too many galaxies too early!

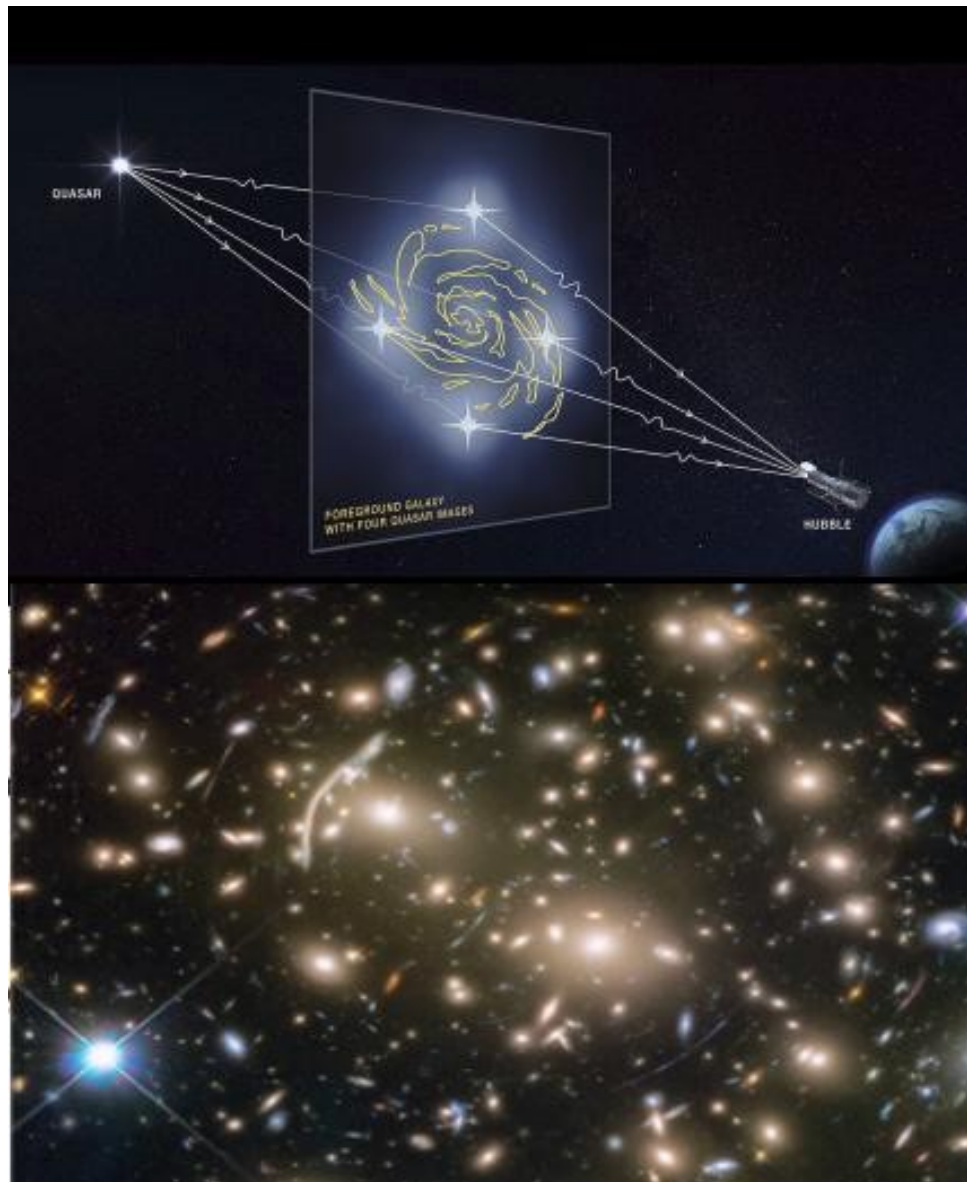


James Webb space telescope

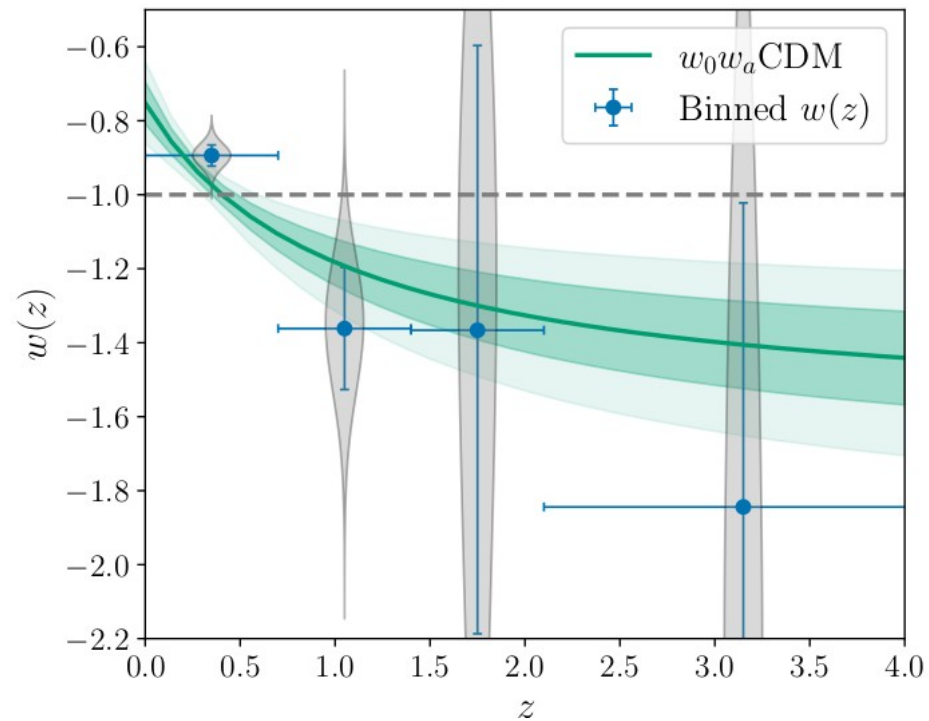
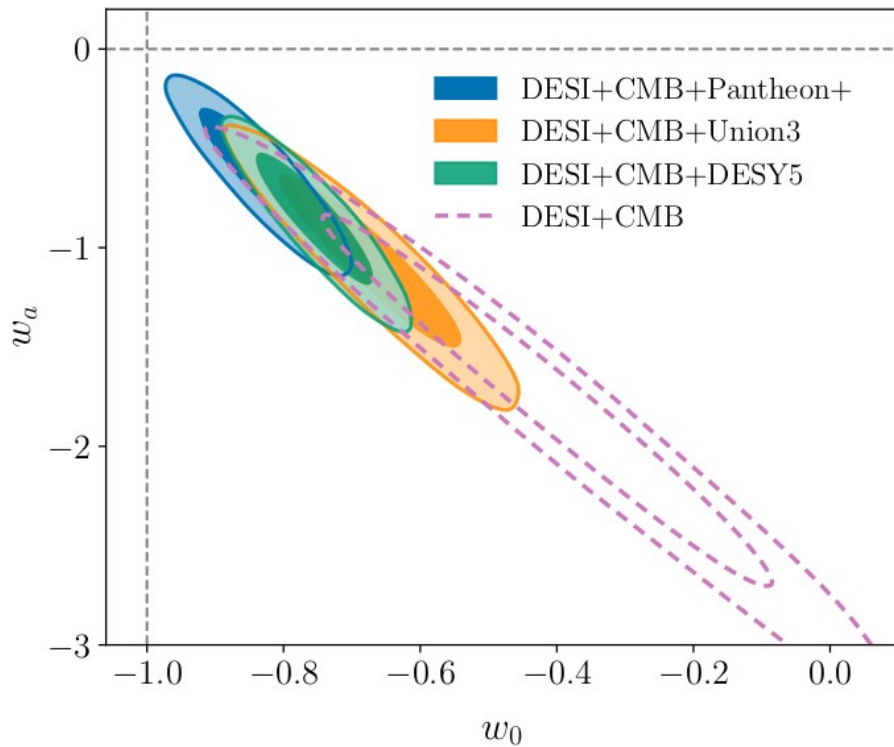
Cosmic dipole tension!



The lensing anomaly



DESI2 DATA and QUINTOM BEHAVIOR



Cosmology Intertwined:

A Review of the Particle Physics, Astrophysics, and Cosmology Associated with the Cosmological Tensions and Anomalies

Elcio Abdalla,¹ Guillermo Franco Abellán,² Amin Aboubrahim,³ Adriano Agnello,⁴ Özgür Akarsu,⁵ Yashar Akrami,^{6,7,8,9} George Alestas,¹⁰ Daniel Aloni,¹¹ Luca Amendola,¹² Luis A. Anchordoqui,^{13,14,15} Richard I. Anderson,¹⁶ Nikki Arendse,¹⁷ Marika Asgari,^{18,19} Mario Ballardini,^{20,21,22,23} Vernon Barger,²⁴ Spyros Basilakos,^{25,26} Ronaldo C. Batista,²⁷ Elia S. Battistelli,^{28,29} Richard Battye,³⁰ Micol Benetti,^{31,32} David Benisty,^{33,34,35} Asher Berlin,³⁶ Paolo de Bernardis,^{28,29} Emanuele Berti,³⁷ Bohdan Bilenko,^{38,39} Simon Birrer,⁴⁰ John P. Blakeslee,⁴¹ Kimberly K. Boddy,⁴² Clecio R. Bom,^{43,44} Alexander Bonilla,⁴⁵ Nicola Borghi,^{46,47} François R. Bouchet,⁴⁸ Matteo Braglia,^{49,51} Thomas Buchert,⁵⁰ Elizabeth Buckley-Geer,^{51,52} Erminia Calabrese,⁵³ Robert R. Caldwell,⁵⁴ David Camarena,⁵⁵ Salvatore Capozziello,^{56,57} Stefano Casertano,⁵⁷ Angela Chen,^{58,59} Geoff C.-F. Chen,⁶⁰ Hsin-Yu Chen,⁶¹ Jens Chluba,³⁰ Anton Chudaykin,⁶² Michele Cicoli,^{20,22} Craig J. Copi,⁶ Fred Courbin,¹⁶ Francis-Yan Cyr-Racine,⁶³ Bożena Czerny,⁶⁴ Maria Dainotti,^{65,66,67} Guido D'Amico,^{68,69} Anne-Christine Davis,^{34,34} Javier de Cruz Pérez,⁷⁰ Jaume de Haro,⁷¹ Jacques Delabrouille,^{72,73,74,75} Peter B. Denton,⁷⁶ Suhail Dhawan,⁷⁷ Keith R. Dienes,^{78,79} Eleonora Di Valentino,^{80,*} Pu Du,⁸¹ Dominique Eckert,⁸² Celia Escamilla-Rivera,⁸³ Agnès Ferté,⁸⁴ Fabio Finelli,^{85,86} Pablo Fosalba,^{86,87} Wendy L. Freedman,⁵² Noemi Frusciante,⁸⁸ Enrique Gaztañaga,^{86,87} William Giarè,^{89,29} Elena Giusarma,⁹⁰ Adrià Gómez-Valent,⁹¹ Will Handley,^{92,93} Ian Harrison,⁹⁴ Luke Hart,³⁰ Dhiraj Kumar Hazra,⁹⁵ Alan Heavens,⁷ Asta Heinenes,⁹⁶ Hendrik Hildebrandt,⁹⁶ J. Colin Hill,^{97,98} Natalie B. Hogg,⁹⁹ Daniel E. Holz,^{52,100,101} Deanna C. Hooper,¹⁰² Niko Hosseininejad,¹⁰³ Dragan Huterer,^{104,105} Mustapha Ishak,¹⁰⁶ Mikhail M. Ivanov,¹⁰⁷ Andrew H. Jaffe,⁷ In Sung Jang,⁵² Karsten Jedamzik,¹⁰⁸ Raul Jimenez,^{109,110} Melissa Joseph,¹¹ Shahab Joudaki,^{111,112} Marc Kamionkowski,³⁷ Tanvi Karwal,¹¹³ Lavrentios Kazantzidis,¹⁰ Ryan E. Keckley,¹¹⁴ Michael Klasek,³ Eiichiro Komatsu,^{115,116} Léon V.E. Koopmans,¹¹⁷ Suresh Kumar,¹¹⁸ Luca Lamagna,^{28,29} Ruth Lazkoz,¹¹⁹ Chung-Chi Lee,¹²⁰ Julien Lesgourgues,¹²¹ Jackson Levi Said,^{122,123} Tiffany R. Lewis,¹²⁴ Benjamin L'Huillier,¹²⁵ Matteo Lucca,¹²⁶ Roy Maartens,^{23,127,128} Lucas M. Macri,¹²⁹ Danny Marfatia,¹³⁰ Valerio Marra,^{131,132,133} Carlos J. A. P. Martins,^{134,135} Silvia Masi,^{28,29} Sabino Matarrese,^{136,137,138,139} Arindam Mazumdar,¹⁴⁰ Alessandro Melchiorri,^{28,29} Olga Mena,¹⁴¹ Laura Mersini-Houghton,¹⁴² James Mertens,¹⁴³ Dinko Milaković,^{133,132,144} Yuto Minami,¹⁴⁵ Vivian Miranda,¹⁴⁶ Cristian Moreno-Pulido,¹⁴⁷ Michele Moresco,^{46,47} David F. Mota,¹⁴⁸ Emil Mottola,⁶³ Simone Mozzon,¹⁴⁹ Jessica Muir,¹⁵⁰ Anjan Mukherjee,¹⁵¹ Suvodip Mukherjee,¹⁵⁰ Pavel Naselsky,¹⁵² Pran Nath,¹⁵³ Savvas Nesseris,⁹⁹ Florian Niedermann,¹⁵⁴ Alessio Notari,¹⁵⁵ Rafael C. Nunes,¹⁵⁶ Eoin Ó Colgáin,^{157,158} Kayla A. Owens,⁵² Emre Özülker,⁵ Francesco Pace,^{159,160} Andronikos Paliathanasis,^{161,162} Antonella Palmese,¹⁶³ Supriya Pan,¹⁶⁴ Daniela Paoletti,^{85,22} Santiago E. Perez Bergliffa,¹⁶⁵ Leandros Perivolaropoulos,¹⁰ Dominic W. Pesce,^{166,167} Valeria Pettorino,¹⁶⁸ Oliver H. E. Philcox,^{169,107} Levon Pogosian,¹⁷⁰ Vivian Poulin,² Gaspard Poulot,⁸⁰ Marco Raveri,¹⁷¹ Mark J. Reid,¹⁷² Fabrizio Renzi,¹⁷³ Adam G. Riess,³⁷ Vivian I. Sabla,⁵⁴ Paolo Salucci,^{174,175} Vincenzo Salzano,¹⁷⁶ Emmanuel N. Saridakis,^{26,75,177} Bangalore S. Sathyaprakash,^{178,179,94} Martin Schmaltz,¹¹ Nils Schöneberg,¹⁸⁰ Dan Scolnic,¹⁸¹ Anjan A. Sen,^{182,183} Neelima Sehgal,¹⁸⁴ Arman Shafieloo,¹⁸⁵ M.M. Sheikh-Jabbari,¹⁸⁶ Joseph Silk,¹⁸⁷ Alessandra Silvestri,¹⁷³ Foteini Slara,¹⁰ Martin S. Sloth,¹⁸⁸ Marcelle Soares-Santos,⁵⁸ Joan Solà Peracaula,¹⁴⁷ Yu-Yang Songsheng,⁸¹ Jorge F. Soriano,^{13,14} Denitsa Staicova,¹⁸⁹ Glenn D. Starkman,^{6,7} István Szapudi,¹⁹⁰ Elsa M. Teixeira,⁸⁰ Brooks Thomas,¹⁹¹ Tommaso Treu,⁶⁰ Emery Trott,⁵⁸ Carsten van de Bruck,⁸⁰ J. Alberto Vazquez,¹⁹² Licia Verde,^{193,194} Luca Visinelli,¹⁹⁵ Deng Wang,¹⁹⁶ Jian-Min Wang,⁸¹ Shao-Jiang Wang,¹⁹⁷ Richard Watkins,¹⁹⁸ Scott Watson,¹⁹⁹ John K. Webb,¹²⁰ Neal Weiner,²⁰⁰ Amanda Weltman,²⁰¹ Samuel J. Witte,²⁰² Radosław Wojtak,⁴ Anil Kumar Yadav,²⁰³ Weiqiang Yang,²⁰⁴ Gong-Bo Zhao,^{205,206} and Miguel Zumalacárregui²⁰⁷

¹Instituto de Física, Universidade de São Paulo - C.P. 66318, CEP: 05315-970, São Paulo, Brazil

²Laboratoire Univers Et Particules de Montpellier (LUPM), Université de Montpellier (UMR-5299)

Challenges for Λ CDM Beyond H_0 and S_8

- A. The A_{lens} Anomaly in the CMB Angular Power Spectrum
- B. Hints for a Closed Universe from *Planck* Data
- C. Large-Angular-Scale Anomalies in the CMB Temperature and Polarization
 1. The Lack of Large-Angle CMB Temperature Correlations
 2. Hemispherical Power Asymmetry
 3. Quadrupole and Octopole Anomalies
 4. Point-Parity Anomaly
 5. Variation in Cosmological Parameters Over the Sky
 6. The Cold Spot
 7. Explaining the Large-Angle Anomalies
 8. Predictions and Future Testability
 9. Summary
- D. Abnormal Oscillations of Best Fit Parameter Values
- E. Anomalously Strong ISW Effect
- F. Cosmic Dipoles
 1. The α Dipole
 2. Galaxy Cluster Anisotropies and Anomalous Bulk Flows
 3. Radio Galaxy Cosmic Dipole
 4. QSO Cosmic Dipole and Polarisation Alignments
 5. Dipole in SNIa
 6. Emergent Dipole in H_0
 7. CMB Dipole: Intrinsic Versus Kinematic?
- G. The Ly- α Forest BAO and CMB Anomalies
 1. The Ly- α Forest BAO Anomaly
 2. Ly- α -*Planck* 2018 Tension in n_s - Ω_m
- H. Parity Violating Rotation of CMB Linear Polarization
 1. The Lithium Problem
- J. Quasars Hubble Diagram Tension with Planck- Λ CDM
- K. Oscillating Force Signals in Short Range Gravity Experiments
- L. Λ CDM and the Dark Matter Phenomenon at Galactic Scales



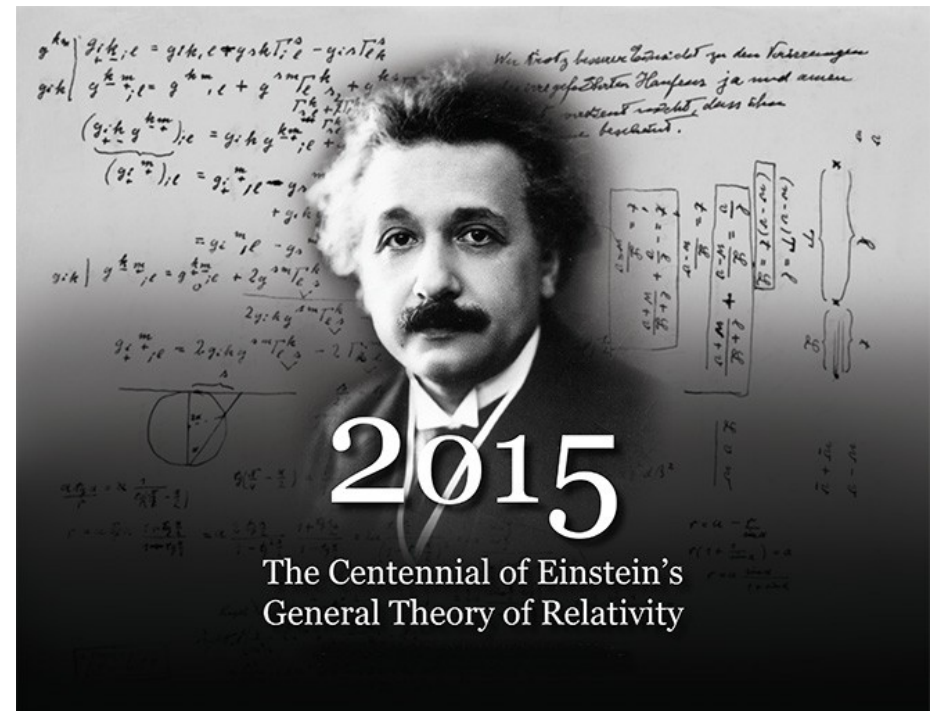
THE NEW CRISIS IN COSMOLOGY



Are we approaching a Revolution in Physics?

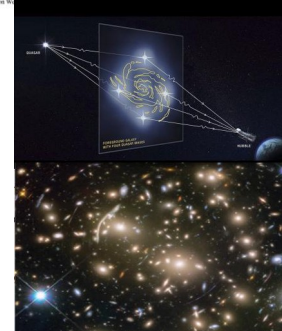
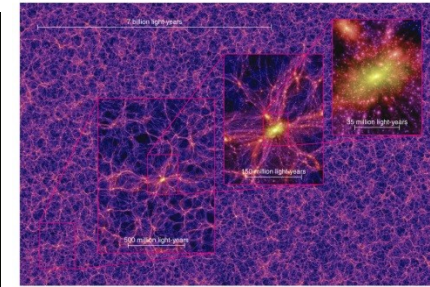
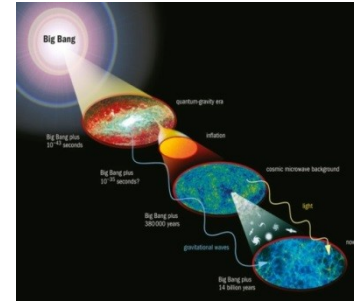
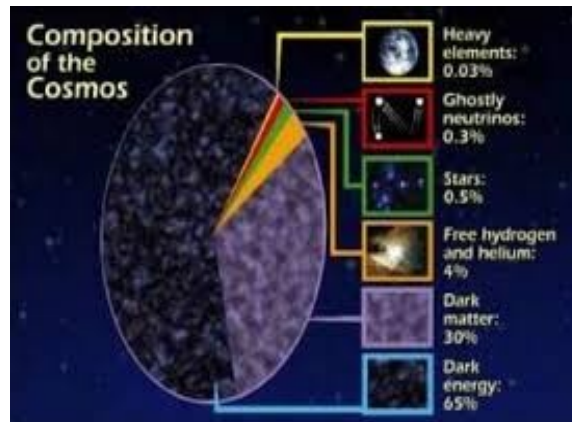
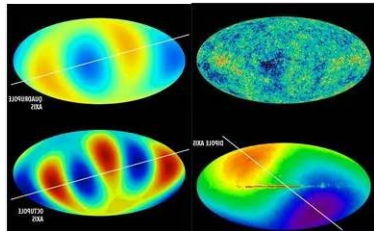
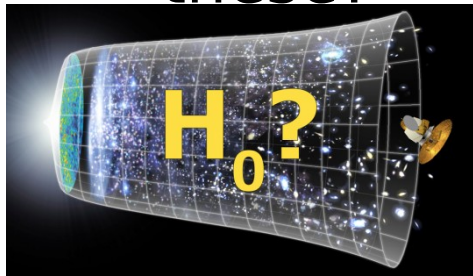
Knowledge of Physics: **Standard Model** + **General Relativity**

mass →	≈2.3 MeV/c ²	≈1.275 GeV/c ²	≈173.07 GeV/c ²	0	≈126 GeV/c ²
charge →	2/3	2/3	2/3	0	0
spin →	1/2	1/2	1/2	1	0
	u up	c charm	t top	g gluon	H Higgs boson
	≈4.8 MeV/c ²	≈95 MeV/c ²	≈4.18 GeV/c ²	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	d down	s strange	b bottom	γ photon	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	91.2 GeV/c ²	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²	80.4 GeV/c ²	
	0	0	0	±1	
	1/2	1/2	1/2	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	



Are we approaching a Revolution in Physics?

So can our **knowledge of Physics** describes all these?



NO! We need **new physics!**

We need to **modify** something:

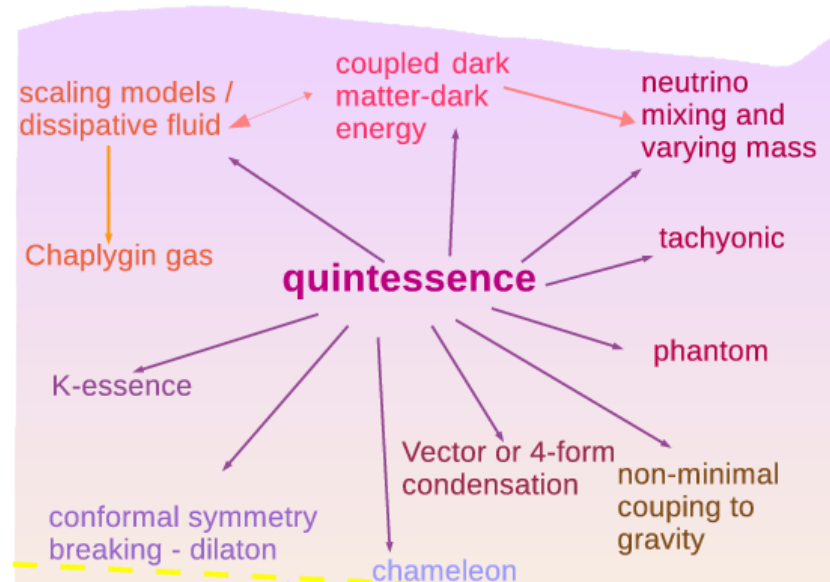
The universe content

or

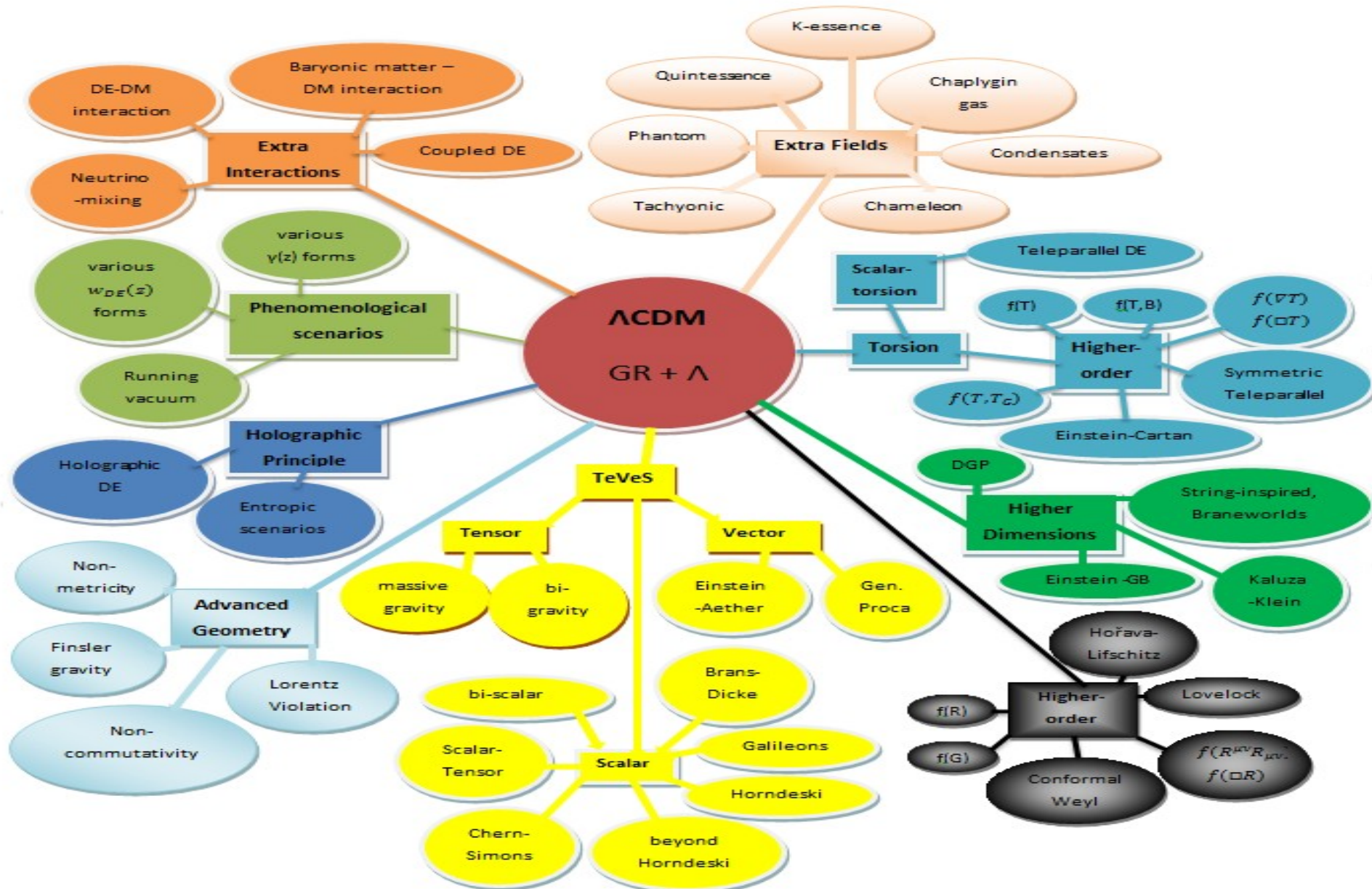
The theory of Gravity

New particles/interactions

mass → charge → spin →	$\sim 2.3 \text{ MeV}/c^2$ 2/3 1/2	$\sim 1.275 \text{ GeV}/c^2$ 2/3 1/2	$\sim 173.07 \text{ GeV}/c^2$ 2/3 1/2	0 0 1	$\sim 126 \text{ GeV}/c^2$ 0 0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS					
	$\sim 4.8 \text{ MeV}/c^2$ -1/3 1/2	$\sim 95 \text{ MeV}/c^2$ -1/3 1/2	$\sim 4.18 \text{ GeV}/c^2$ -1/3 1/2	0 0 1	
	d down	s strange	b bottom	γ photon	
	$0.511 \text{ MeV}/c^2$ -1 1/2	$105.7 \text{ MeV}/c^2$ -1 1/2	$1.777 \text{ GeV}/c^2$ -1 1/2	$91.2 \text{ GeV}/c^2$ 0 1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS					
	$< 2.2 \text{ eV}/c^2$ 0 1/2	$< 0.17 \text{ MeV}/c^2$ 0 1/2	$< 15.5 \text{ MeV}/c^2$ 0 1/2	$80.4 \text{ GeV}/c^2$ +1 1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
					GAUGE BOSONS

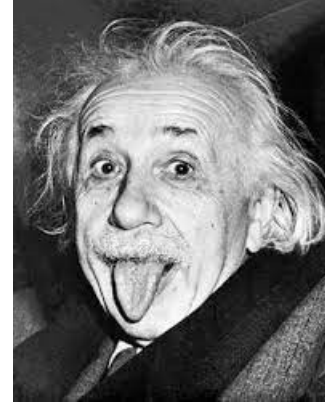


Modified Gravity



Standard Model vs General Relativity

$$S = -\frac{1}{16\pi G} \int \sqrt{-g}(R(g)+2\Lambda) d^4x$$



$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \\
 & \frac{1}{2}ig_s^2(\bar{q}_i^\sigma \gamma^\mu q_j^\sigma)g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2}M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2}M\phi^0 \phi^0 - \beta_h[\frac{2M^2}{g^2} + \\
 & \frac{2M}{g}H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - Z_\nu^0(W_\mu^+ \partial_\nu W_\mu^- - W_\mu^+ \partial_\nu W_\mu^-) + Z_\mu^0(W_\nu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^+ \partial_\nu W_\mu^-)] - igc_w[\partial_\nu A_\mu(W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu(W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^+ \partial_\nu W_\mu^-) + A_\mu(W_\nu^+ \partial_\nu W_\mu^- - W_\nu^+ \partial_\nu W_\mu^-)] - \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \\
 & \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^- + g^2 c_w^2(Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) + \\
 & g^2 s_w^2(A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w[A_\mu Z_\nu^0(W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g\alpha[H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-] - \\
 & \frac{1}{8}g^2 \alpha_h[H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - \\
 & gMW_\mu^+ W_\mu^- H - \frac{1}{2}g\frac{M}{c_w^2}Z_\mu^0 Z_\mu^0 H - \frac{1}{2}ig[W_\mu^+(\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - \\
 & W_\mu^-(\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2}g[W_\mu^+(H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^-(H \partial_\mu \phi^+ - \\
 & \phi^+ \partial_\mu H)] + \frac{1}{2}g\frac{1}{c_w}(Z_\mu^0(H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig\frac{s_w^2}{c_w}M Z_\mu^0(W_\mu^+ \phi^- - W_\mu^- \phi^+) + \\
 & igc_w M A_\mu(W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig\frac{1-2c_w^2}{2c_w}Z_\mu^0(\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\
 & igc_w A_\mu(\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4}g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \\
 & \frac{1}{4}g^2 \frac{1}{c_w^2}Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w}Z_\mu^0 \phi^0(W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w}Z_\mu^0 H(W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H(W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w}(2c_w^2 - 1)Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^-] - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma \partial \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - \\
 & \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + igc_w A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \\
 & \frac{ig}{4c_w}Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - \\
 & 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{ig}{2\sqrt{2}}W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + \\
 & (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{ig}{2\sqrt{2}}W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \\
 & \gamma^5) u_j^\lambda)] + \frac{ig}{2\sqrt{2}}\frac{m_e^\lambda}{M}[-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \\
 & \frac{g}{2}\frac{m_e^\lambda}{M}[H(\bar{e}^\lambda e^\lambda) + i\phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{ig}{2M\sqrt{2}}\phi^+ [-m_e^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + \\
 & m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa)] + \frac{ig}{2M\sqrt{2}}\phi^- [m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \\
 & \gamma^5) u_j^\kappa) - \frac{g}{2}\frac{m_u^\lambda}{M}H(\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2}\frac{m_d^\lambda}{M}H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2}\frac{m_u^\lambda}{M}\phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \\
 & \frac{ig}{2}\frac{m_d^\lambda}{M}\phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda)] + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \\
 & \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + igc_w W_\mu^- (\partial_\mu \bar{X}^- Y - \\
 & \partial_\mu \bar{X}^+ Y) + igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + igc_w W_\mu^- (\partial_\mu \bar{X}^- Y - \\
 & \partial_\mu \bar{Y} X^+) + igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) + igc_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \\
 & \partial_\mu \bar{X}^- X^-) - \frac{1}{2}gM[\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2}\bar{X}^0 X^0 H] + \\
 & \frac{1-2c_w^2}{2c_w}igM[\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w}igM[\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \\
 & igM s_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2}igM[\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
 \end{aligned}$$

General Relativity

Assumptions and Considerations

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} [R - 2\Lambda] + \int d^4x L_m(g_{\mu\nu}, \psi)$$

- Diffeomorphism invariance
- Spacetime dimensionality=4
- **Geometry=Curvature** (connection=Levi Civita)
- Linear in Ricci scalar
- **Metric compatibility** (zero non-metricity)
- Minimal matter coupling
- Equivalence principle
- Lorentz invariance
- Locality

“Those that do not know geometry are not allowed to enter”.

Front Door of Plato's Academy



Descriptions of Gravity

- Einstein 1916: **General Relativity:**
energy-momentum source of spacetime
Curvature
Levi-Civita connection: Zero Torsion
- Einstein 1928: **Teleparallel Equivalent of GR:**
Weitzenböck connection: Zero Curvature

[Cai, Capozziello, De Laurentis, Saridakis, Rept.Prog.Phys. 79]

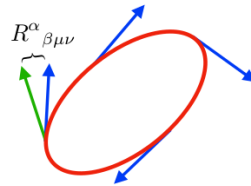
$$\left\{ \begin{smallmatrix} \alpha \\ \mu\nu \end{smallmatrix} \right\} = \frac{1}{2} g^{\alpha\lambda} (g_{\lambda\nu,\mu} + g_{\mu\lambda,\nu} - g_{\mu\nu,\lambda}). \quad (1.3)$$

The corresponding covariant derivative will be denoted by \mathcal{D} so that we will have $\mathcal{D}_\alpha g_{\mu\nu} = 0$. A general connection $\Gamma^\alpha_{\mu\nu}$ then admits the following convenient decomposition:

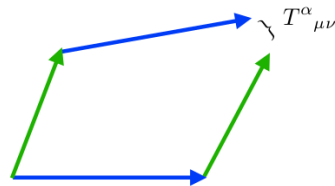
$$\Gamma^\alpha_{\mu\nu} = \left\{ \begin{smallmatrix} \alpha \\ \mu\nu \end{smallmatrix} \right\} + K^\alpha_{\mu\nu} + L^\alpha_{\mu\nu} \quad (1.4)$$

with

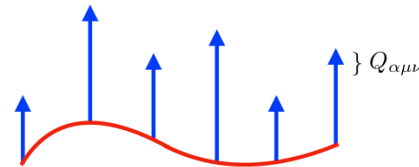
$$K^\alpha_{\mu\nu} = \frac{1}{2} T^\alpha_{\mu\nu} + T_{(\mu}{}^\alpha{}_{\nu)}, \quad L^\alpha_{\mu\nu} = \frac{1}{2} Q^\alpha_{\mu\nu} - Q_{(\mu}{}^\alpha{}_{\nu)} \quad (1.5)$$



The rotation of a vector transported along a closed curve is given by the curvature: General Relativity.



The non-closure of parallelograms formed when two vectors are transported along each other is given by the torsion: Teleparallel Equivalent of General Relativity.



The variation of the length of a vector as it is transported is given by the non-metricity: Symmetric Teleparallel Equivalent of General Relativity.

Metric-Affine Modified Gravity

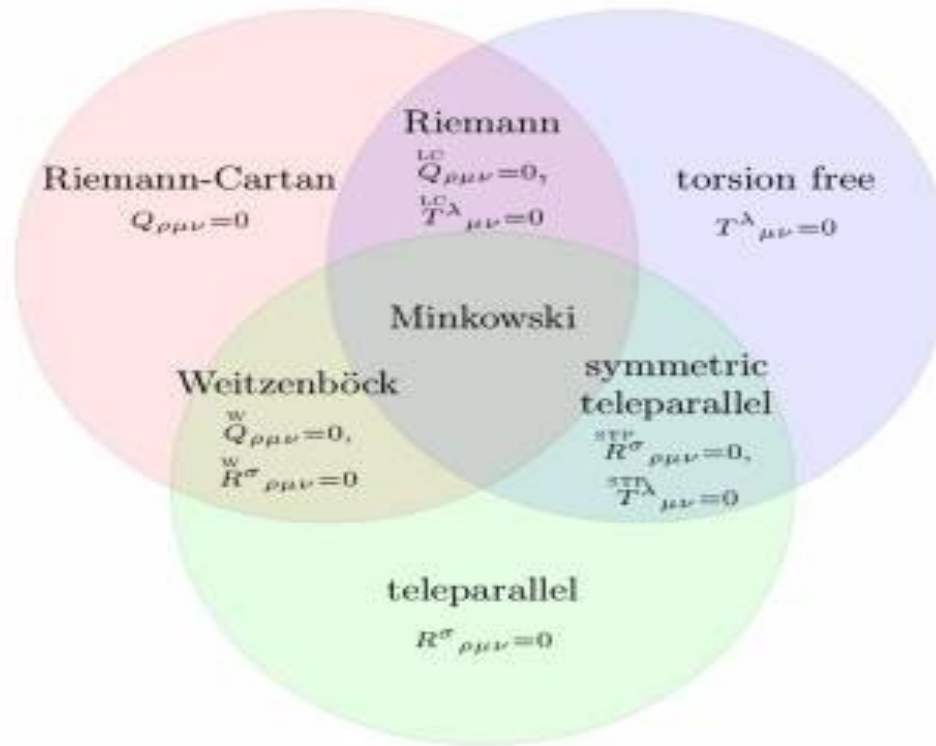


FIG. 1. Subclasses of metric-affine geometry, depending on the properties of connection.

$$S_{\text{GR}} = \frac{1}{2\kappa^2} \int \left\{ g^{\mu\nu} \hat{R}_{\mu\nu} + \lambda_{(1)}^{\mu\nu\lambda} T_{\mu\nu\lambda} + \lambda_{(2)}^{\mu\nu\lambda} Q_{\mu\nu\lambda} \right\} \sqrt{-g} d^4x ,$$

$$S_{\text{total}} = S_{\text{GR}} + S_{\text{matter}} ,$$

Curvature and Torsion

- **Vierbeins** e_A^μ : four linearly independent fields in the **tangent space**

$$g_{\mu\nu}(x) = \eta_{AB} e_\mu^A(x) e_\nu^B(x)$$

- **Connection**: ω_{ABC}

- **Curvature tensor**: $R_{B\mu\nu}^A = \omega_{B\nu,\mu}^A - \omega_{B\mu,\nu}^A + \omega_{C\mu}^A \omega_{B\nu}^C - \omega_{C\nu}^A \omega_{B\mu}^C$

- **Torsion tensor**: $T_{\mu\nu}^A = e_{\nu,\mu}^A - e_{\mu,\nu}^A + \omega_{B\mu}^A e_\nu^B - \omega_{B\nu}^A e_\mu^B$

- **Levi-Civita** connection and **Contortion** tensor: $\omega_{ABC} = \Gamma_{ABC} + K_{ABC}$

$$K_{ABC} = \frac{1}{2}(T_{CAB} - T_{BCA} - T_{ABC}) = -K_{BAC}$$

- **Curvature** and **Torsion** Scalars:

$$R = \bar{R} + T - 2(T_v^{\nu\mu})_{;\mu}$$

$$R = g^{\mu\nu} R_{\mu\nu} = g^{\mu\nu} R_{\mu\rho\nu}^\rho$$

$$T = \frac{1}{4} T^{\rho\mu\nu} T_{\rho\mu\nu} + \frac{1}{2} T^{\rho\mu\nu} T_{\nu\mu\rho} - T_{\rho\mu}^\rho T_\nu^{\nu\mu}$$

f(T) Gravity and f(T) Cosmology

- **f(T) Gravity:** Simplest torsion-based modified gravity
- Generalize T to **f(T)** (inspired by **f(R)**)

$$S = \frac{1}{16\pi G} \int d^4x \, e \, [T + f(T)] + S_m$$

- Equations of motion:

$$e^{-1} \partial_\mu (e e^\rho_\lambda S^{\mu\nu}_\rho) (1 + f_T) - e^\lambda_\mu T^{\rho\mu}_\lambda S^{\nu\mu}_\rho + e^\rho_\lambda S^{\mu\nu}_\rho \partial_\mu (T) f_{TT} - \frac{1}{4} e^\nu_\lambda [T + f(T)] = 4\pi G e^\rho_\lambda T^{\nu\lambda}_{\text{EM}}$$

- **f(T) Cosmology:** Apply in FRW geometry:

$$e^A_\mu = \text{diag}(1, a, a, a) \Rightarrow ds^2 = dt^2 - a^2(t) \delta_{ij} dx^i dx^j \quad (\text{not unique choice})$$

- Friedmann equations:

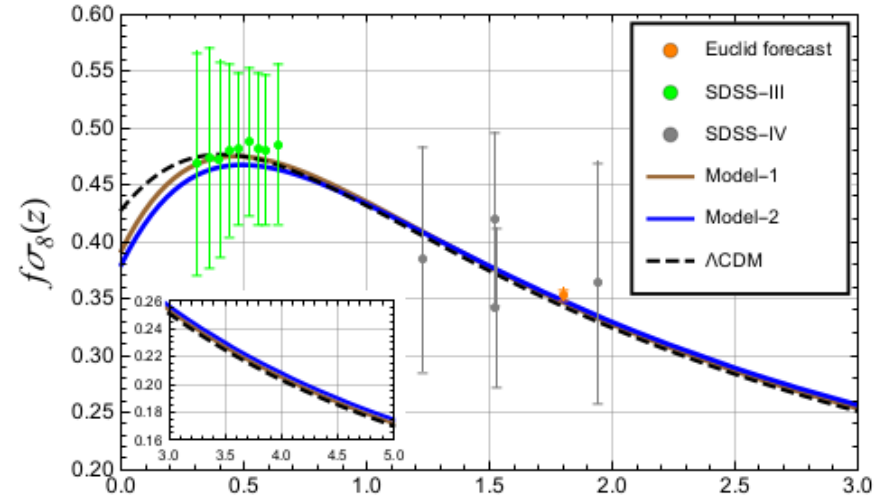
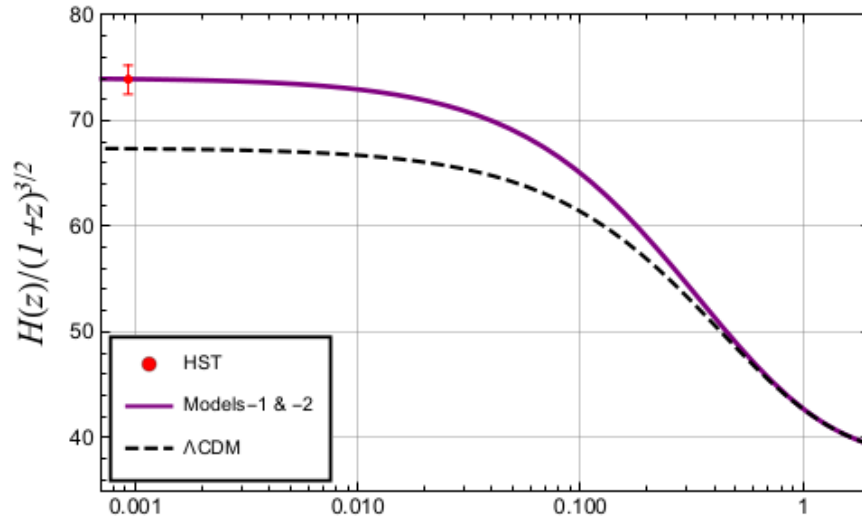
$$H^2 = \frac{8\pi G}{3} \rho_m - \frac{f(T)}{6} - 2f_T H^2$$

$$\dot{H} = -\frac{4\pi G(\rho_m + p_m)}{1 + f_T - 12H^2 f_{TT}}$$

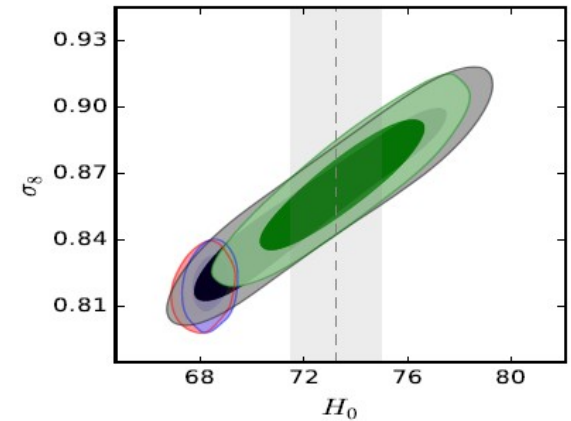
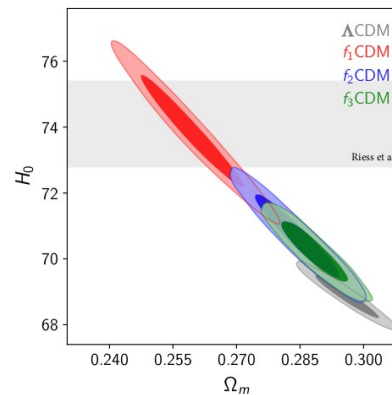
- Find easily

$$T = -6H^2$$

Solving H0 and S8 tensions in f(T) Gravity



Parameter	CMB + BAO	CMB + BAO + H_0
$10^2 \omega_b$	$2.235^{+0.013}_{-0.013}$	$2.235^{+0.013}_{-0.013}$
ω_{cdm}	$0.1181^{+0.001}_{-0.001}$	$0.118^{+0.001}_{-0.001}$
$100\theta_s$	$1.041^{+0.00027}_{-0.00027}$	$1.041^{+0.00030}_{-0.00027}$
$\ln 10^{10} A_s$	$3.078^{+0.023}_{-0.023}$	$3.08^{+0.022}_{-0.022}$
n_s	$0.9678^{+0.0039}_{-0.0039}$	$0.9684^{+0.0039}_{-0.0044}$
τ_{reio}	$0.073^{+0.012}_{-0.013}$	$0.075^{+0.012}_{-0.012}$
n	$0.0043^{+0.0033}_{-0.0039}$	$0.0054^{+0.0020}_{-0.0020}$
$\log \alpha$	$10.00^{+0.081}_{-0.12}$	$10.03^{+0.06}_{-0.06}$
Ω_{F0}	$0.73^{+0.021}_{-0.028}$	$0.738^{+0.015}_{-0.015}$
H_0	$72.4^{+3.3}_{-4.1}$	$73.5^{+2.1}_{-2.1}$
σ_8	$0.855^{+0.023}_{-0.033}$	$0.866^{+0.02}_{-0.02}$
$\chi^2_{min}/2$	6480.48	6482.27



[S-F Yan, P. Zhang, J-W Chen, X_Z Zhang, Y-F Cai, E.N. Saridakis, PRD 101]

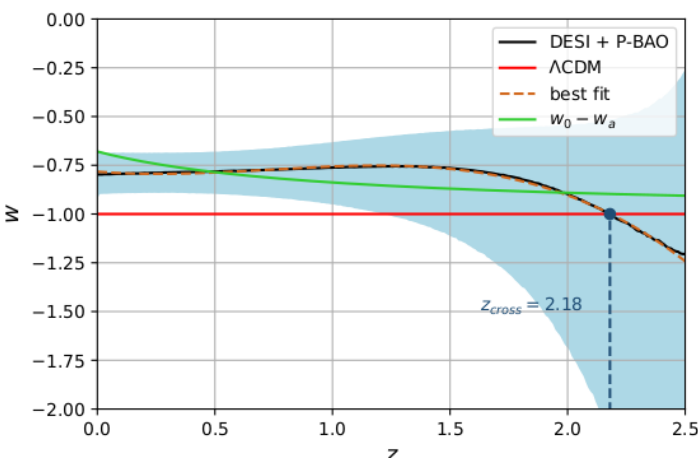
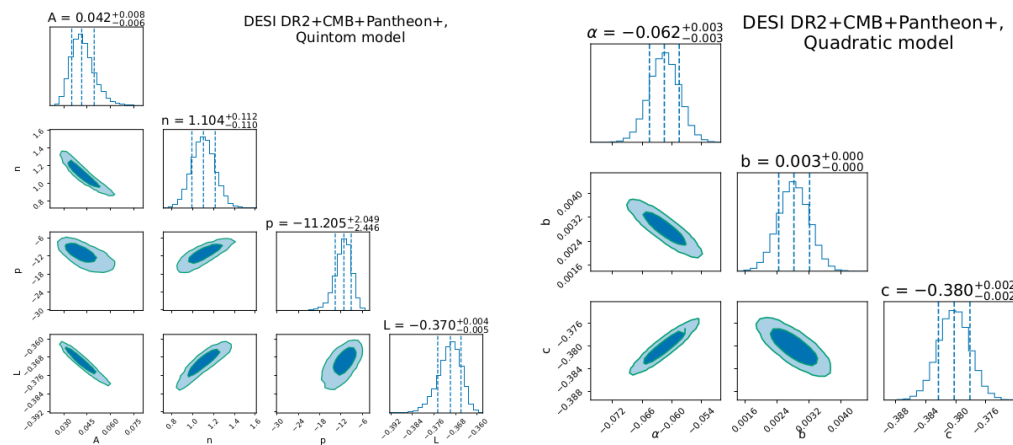
[J-W Chen, W. Luo, Y-F Cai, E.N. Saridakis, PRD 102]

Modified gravity realizations of Quintom after DESI DR2

[Z-K Guo, Y-S Piao, X-M Zhang, Y-Z Zhang, Phys.Lett.B 608 (2005)]

$$f(T) = T + \alpha(-T)^n \left[1 - e^{pT_0/T} \right] - 2\Lambda$$

$$\frac{f(T)}{T_0} = \frac{T}{T_0} + \alpha \frac{T}{T_0} + b \frac{T^2}{T_0^2} - 2c$$



DESI DR2+CMB+Pantheon+ datasets		
Criteria	Quintom model	Quadratic model
AIC	97.81	95.146
BIC	117.824	117.1

[Y. Yang, X. Ren ,Q. Wang, Z.Lu, D. zhang, YF. Cai, E. N. Saridakis. Sci.Bull. 69 (2024)]

[Y. Yang, Q. Wang,X. Ren, E. N. Saridakis. YF. Cai, 2504.06784 [astro-ph.CO]]

f(Q) gravity

$$T^\lambda_{\mu\nu} \equiv \Gamma^\lambda_{\mu\nu} - \Gamma^\lambda_{\nu\mu}$$

$$R^\sigma_{\rho\mu\nu} \equiv \partial_\mu \Gamma^\sigma_{\nu\rho} - \partial_\nu \Gamma^\sigma_{\mu\rho} + \Gamma^\alpha_{\nu\rho} \Gamma^\sigma_{\mu\alpha} - \Gamma^\alpha_{\mu\rho} \Gamma^\sigma_{\nu\alpha} \quad (5)$$

while the nonmetricity can be expressed as

$$Q_{\rho\mu\nu} \equiv \nabla_\rho g_{\mu\nu} = \partial_\rho g_{\mu\nu} - \Gamma^\beta_{\rho\mu} g_{\beta\nu} - \Gamma^\beta_{\rho\nu} g_{\mu\beta} . \quad (6)$$

$$Q = -\frac{1}{4} Q_{\alpha\beta\gamma} Q^{\alpha\beta\gamma} + \frac{1}{2} Q_{\alpha\beta\gamma} Q^{\gamma\beta\alpha} + \frac{1}{4} Q_\alpha Q^\alpha - \frac{1}{2} Q_\alpha \tilde{Q}^\alpha , \quad (7)$$

where $Q_\alpha \equiv Q^\mu_{\alpha\mu}$, and $\tilde{Q}^\alpha \equiv Q_\mu^{\mu\alpha}$.

$$S = -\frac{1}{2} \int d^4x \sqrt{-g} f(Q). \quad (8)$$

$$\begin{aligned} & \frac{2}{\sqrt{-g}} \nabla_\alpha \left\{ \sqrt{-g} g_{\beta\nu} f_Q \left[-\frac{1}{2} L^{\alpha\mu\beta} + \frac{1}{4} g^{\mu\beta} (Q^\alpha - \tilde{Q}^\alpha) \right. \right. \\ & \quad \left. \left. - \frac{1}{8} (g^{\alpha\mu} Q^\beta + g^{\alpha\beta} Q^\mu) \right] \right\} \\ & + f_Q \left[-\frac{1}{2} L^{\mu\alpha\beta} - \frac{1}{8} (g^{\mu\alpha} Q^\beta + g^{\mu\beta} Q^\alpha) \right. \\ & \quad \left. + \frac{1}{4} g^{\alpha\beta} (Q^\mu - \tilde{Q}^\mu) \right] Q_{\nu\alpha\beta} + \frac{1}{2} \delta^\mu_\nu f = T^\mu_\nu , \quad (9) \end{aligned}$$

with $f_Q = \partial f / \partial Q$.

f(Q) cosmology

$$\begin{aligned} 6f_Q H^2 - \frac{1}{2}f &= \rho_m, \\ (12H^2 f_{QQ} + f_Q)\dot{H} &= -\frac{1}{2}(\rho_m + p_m). \end{aligned} \quad (11)$$

$$Q = 6H^2, \quad (12)$$

$$\begin{aligned} -a^2 \delta \rho &= 6(f_Q + 12a^{-2} \mathcal{H}^2 f_{QQ}) \mathcal{H}(\mathcal{H}\phi + \varphi') + 2f_Q k^2 \psi \\ &\quad - 2[f_Q + 3a^{-2} f_{QQ}(\mathcal{H}' + \mathcal{H}^2)] \mathcal{H} k^2 B. \end{aligned} \quad (19)$$

$$\begin{aligned} \frac{1}{2}a^2(\rho + p)v &= [f_Q + 3a^{-2} f_{QQ}(\mathcal{H}' + \mathcal{H}^2)] \mathcal{H}\phi \\ &\quad + 6a^{-2} f_{QQ} \mathcal{H}^2 \varphi' - 9a^{-2} f_{QQ}(\mathcal{H}' - \mathcal{H}^2) \mathcal{H}\varphi \\ &\quad + f_Q \psi' - a^{-2} f_{QQ} \mathcal{H}^2 k^2 B, \end{aligned} \quad (20)$$

$$\delta' = (1+w) \left(-k^2 v - k^2 B + 3\varphi' \right) + 3\mathcal{H} \left(w\rho - \frac{\delta p}{\rho} \right), \quad (22)$$

$$v' = -\mathcal{H}(1 - c_s^2)v + \frac{\delta p}{\rho + p} + \phi. \quad (23)$$

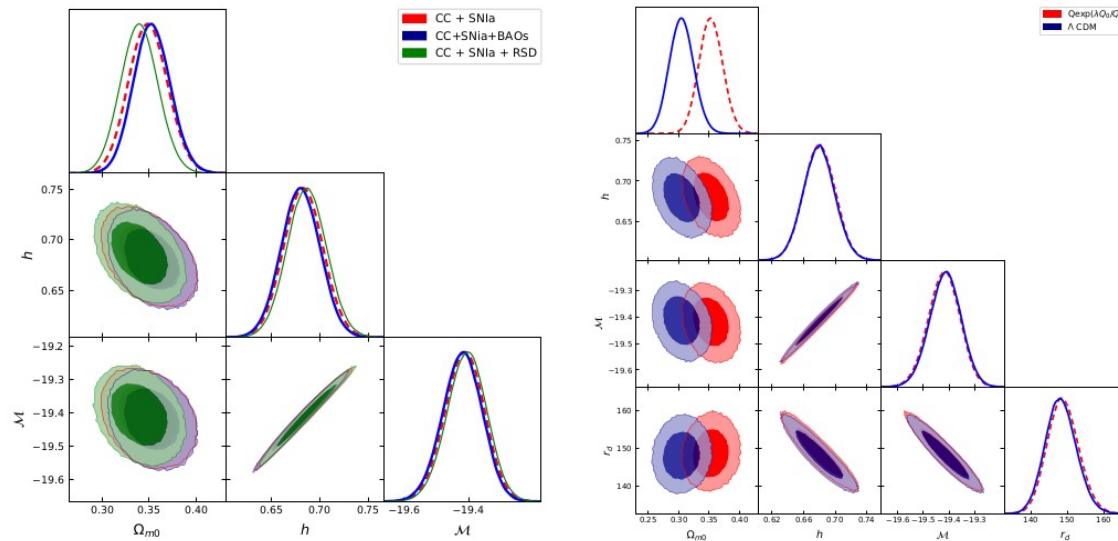
$$\begin{aligned} \frac{1}{2}a^2 \delta p &= (f_Q + 12a^{-2} f_{QQ} \mathcal{H}^2)(\mathcal{H}\phi' + \varphi'') + \left[f_Q \left(\mathcal{H}' + 2\mathcal{H}^2 - \frac{1}{3}k^2 \right) + 12a^{-2} f_{QQ} \mathcal{H}^2 (4\mathcal{H}' - \mathcal{H}^2) + 12a^{-2} \frac{df_{QQ}}{d\tau} \mathcal{H}^3 \right] \phi \\ &\quad + 2 \left[f_Q + 6a^{-2} f_{QQ} (3\mathcal{H}' - \mathcal{H}^2) + 6a^{-2} \frac{df_{QQ}}{d\tau} \mathcal{H} \right] \mathcal{H}\varphi' + \frac{1}{3} f_Q k^2 \psi \\ &\quad - \frac{1}{3} (f_Q + 6a^{-2} f_{QQ} \mathcal{H}^2) k^2 B' - \frac{1}{3} \left[2f_Q + 3a^{-2} f_{QQ} (5\mathcal{H} - \mathcal{H}^2) + 6a^{-2} \frac{df_{QQ}}{d\tau} \mathcal{H} \right] \mathcal{H} k^2 B, \end{aligned} \quad (21)$$

$$\begin{aligned} &- f_{QQ} \mathcal{H} [2\mathcal{H}\varphi' + (\mathcal{H}' + \mathcal{H}^2)\phi + (\mathcal{H}' - \mathcal{H}^2)(\psi - B')] \\ &- \left[f_{QQ} \left(\mathcal{H}'^2 + \mathcal{H}\mathcal{H}'' - 3\mathcal{H}^2 \mathcal{H}' - \frac{1}{3}\mathcal{H}^2 k^2 \right) \right. \\ &\quad \left. + \frac{df_{QQ}}{d\tau} (\mathcal{H}' - \mathcal{H}^2) \mathcal{H} \right] B = 0, \end{aligned} \quad (24)$$

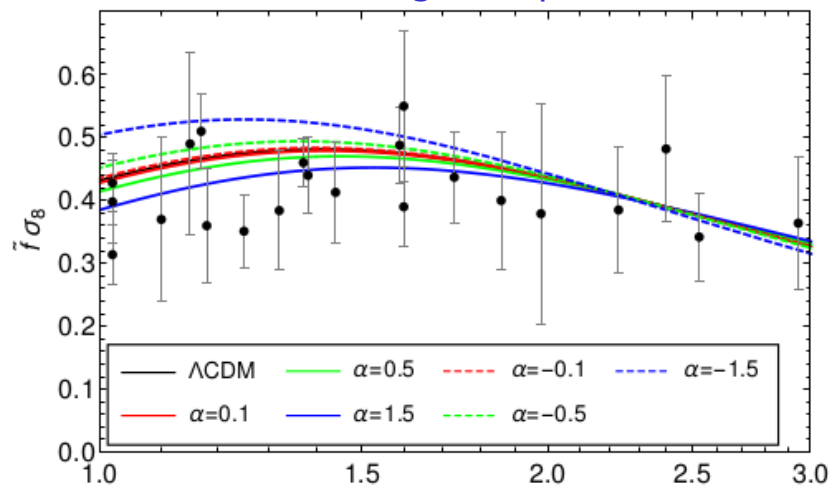
$$\delta'' + \mathcal{H}\delta' = \frac{4\pi G\rho}{f_Q} \delta, \quad (30)$$

$$G_{eff} \equiv \frac{G}{f_Q}, \quad (31)$$

Solving the tensions in $f(Q)$ gravity



[F. Anagnostopoulos, S. Basilakos, E.N.Saridakis, JCAP 2019]



$z+1$ [S. Peirone, G. Benevento, N. Frusciante, S. Tsujikawa, PRD 100]

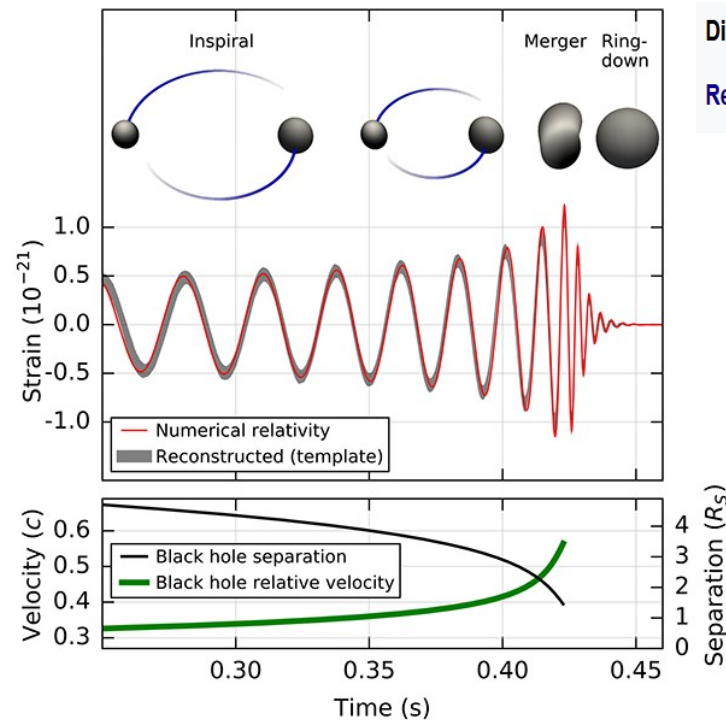
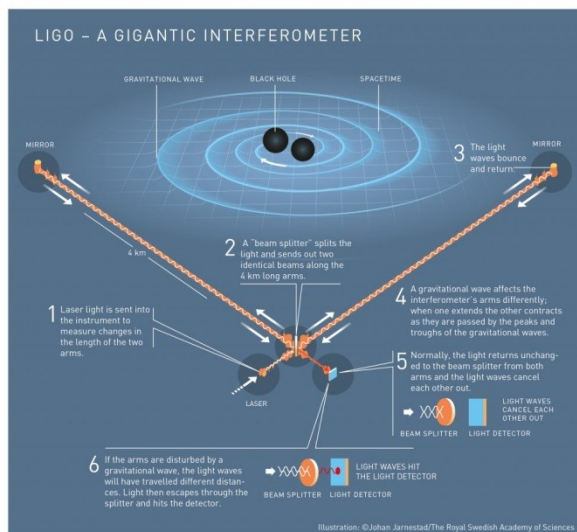
Testing GR and Modified Gravity

- Solar-System data
- Galaxy data
- Galaxy-cluster data
- Cosmological data (SNIa, BAO, CMB, CC, LSS)
- Early Universe (Inflation, Baryogenesis, BBN)
- Black-Hole-shadow data
- Gravitational-wave data
(multi-messenger astronomy)

Gravitational waves

- **GW150914**: Two **black holes** $36^{+5}_{-4} M_{\odot}$ and $29^{+4}_{-4} M_{\odot}$, resulting in a $62^{+4}_{-4} M_{\odot}$ black hole

Louisiana.
Washington
4km
 $10^{-18}m$



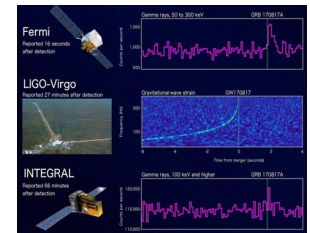
Distance	$410^{+160}_{-180} \text{ Mpc}$
Redshift	$0.093^{+0.030}_{-0.036}$

[Abbott et al, LIGO Virgo PRL 116]

2017 **Nobel Price** in Physics

Gravitational waves

- In case of GWs from **black hole mergers** we know their **properties** at the **moment of detection**, and their direction (in case of three detectors).
Assuming GR and Λ CDM we can extract their speed, distance, and properties at the **moment of emission**.
- In case of GWs from **neutron star mergers**, and their **E/M counterpart**, we know their **properties** at the **moment of detection** and their direction, but using the implied physics from the E/M information we can extract their speed, distance and **properties** at the **moment of emission**, **independently** of the **underlying gravitational theory and cosmological scenario**.
- **Great tool** for **testing General Relativity** and **cosmological scenarios**!



Gravitational waves

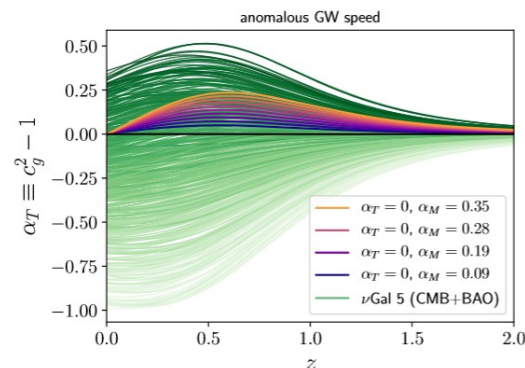
- An immediate result: **The speed of GWs is equal to the speed of light!**

GW170817 time delay $1.74 \pm 0.05\text{s}$ constrains:

$$-3 \cdot 10^{-15} \leq c_g/c - 1 \leq 7 \cdot 10^{-16}$$

- Excludes** a large number of theories that were consistent with other data!

	$c_g = c$	$c_g \neq c$
Horndeski	General Relativity quintessence/k-essence [46] Brans-Dicke/ $f(R)$ [47, 48] Kinetic Gravity Braiding [50]	quartic/quintic Galileons [13, 14] Fab Four [15] de Sitter Horndeski [49] $G_{\mu\nu}\phi^\mu\phi^\nu$ [51], $f(\phi)\cdot\text{Gauss-Bonnet}$ [52]
beyond H.	Derivative Conformal (19) [17] Disformal Tuning (21) quadratic DHOST with $A_1 = 0$	quartic/quintic GLPV [18] quadratic DHOST [20] with $A_1 \neq 0$ cubic DHOST [23]
	Viable after GW170817	Non-viable after GW170817



Gravitational waves

- For **tensor perturbation**

$$g_{00} = -1, \quad g_{0i} = 0,$$

$$g_{ij} = a^2 \left(\delta_{ij} + h_{ij} + \frac{1}{2} h_{ik} h_{kj} \right)$$

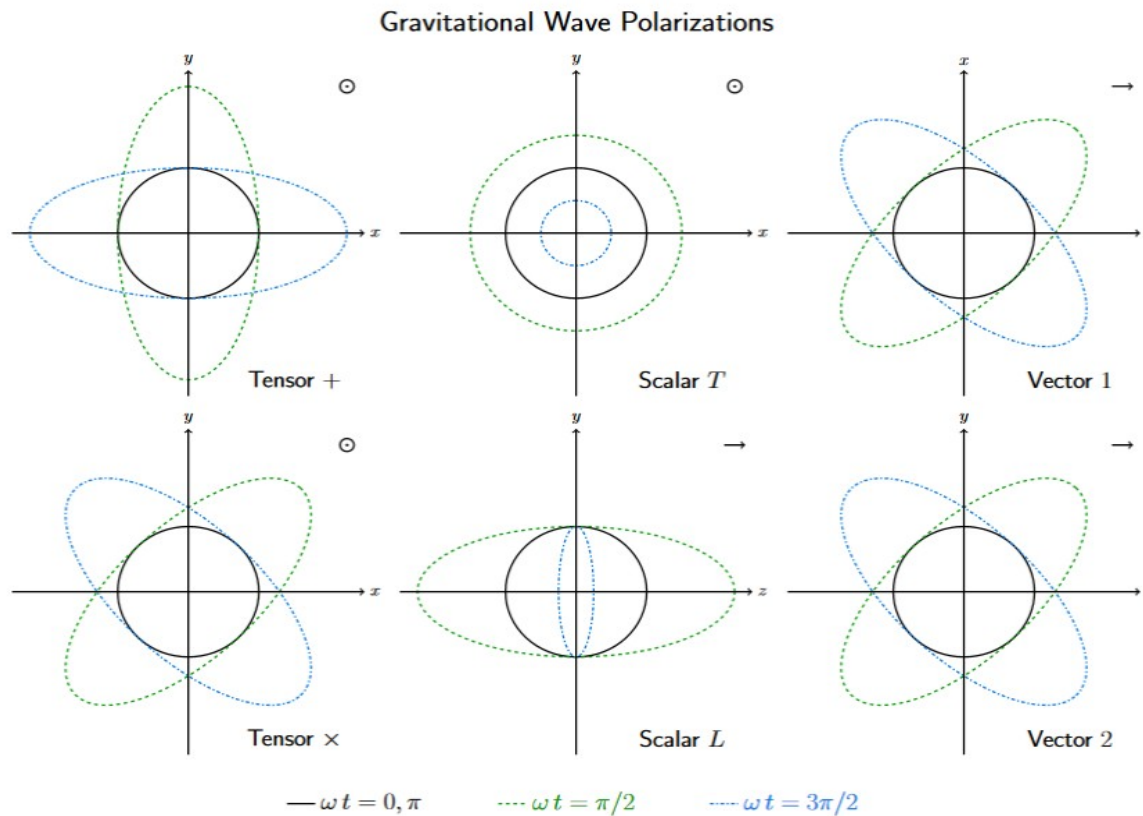
$$\ddot{h}_{ij} + (3 + \alpha_M) \dot{h}_{ij} + (1 + \alpha_T) \frac{k^2}{a^2} h_{ij} = 0$$

$$\alpha_M = \frac{d \log(M_*^2)}{d \log a} \quad c_g^2 = (1 + \alpha_T)$$

- $$h_{\text{GW}} \sim h_{\text{GR}} \underbrace{e^{-\frac{1}{2} \int \nu \mathcal{H} d\eta}}_{\text{Affects amplitude}} \underbrace{e^{ik \int (\alpha_T + a^2 m^2 / k^2)^{1/2} d\eta}}_{\text{Affects phase}}$$

Gravitational waves

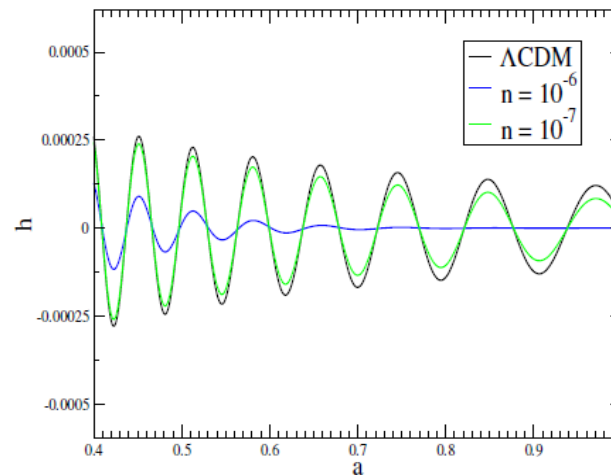
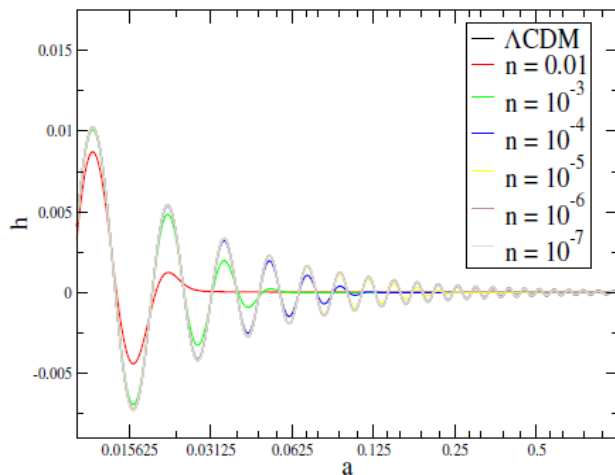
- Polarizations:



Gravitational waves in modified gravity

- Testing General Relativity, modified gravities, and various cosmological scenarios.
- The GWs properties at emission and detection are determined by them.

— — — — —



$$h_{\mu\nu}^{(1)} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 2\gamma_1^{(1)1} & B_1^2 \exp(ip_\mu x^\mu) & 0 \\ 0 & B_1^2 \exp(ip_\mu x^\mu) & -2\gamma_1^{(1)1} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

[Cai, Li, Saridakis, Xue PRD97]

[Li, Cai, Cai, Saridakis, JCAP 1810]

[Farrugia, Said, Gakis, Saridakis, PRD97]

Gravitational Waves in Modified Teleparallel Theories

- $$S = \frac{1}{16\pi G} \int d^4x e f(T, B) + \int d^4x e \mathcal{L}_m \quad R = -T - 2\nabla^\mu T^\nu_{\mu\nu}$$

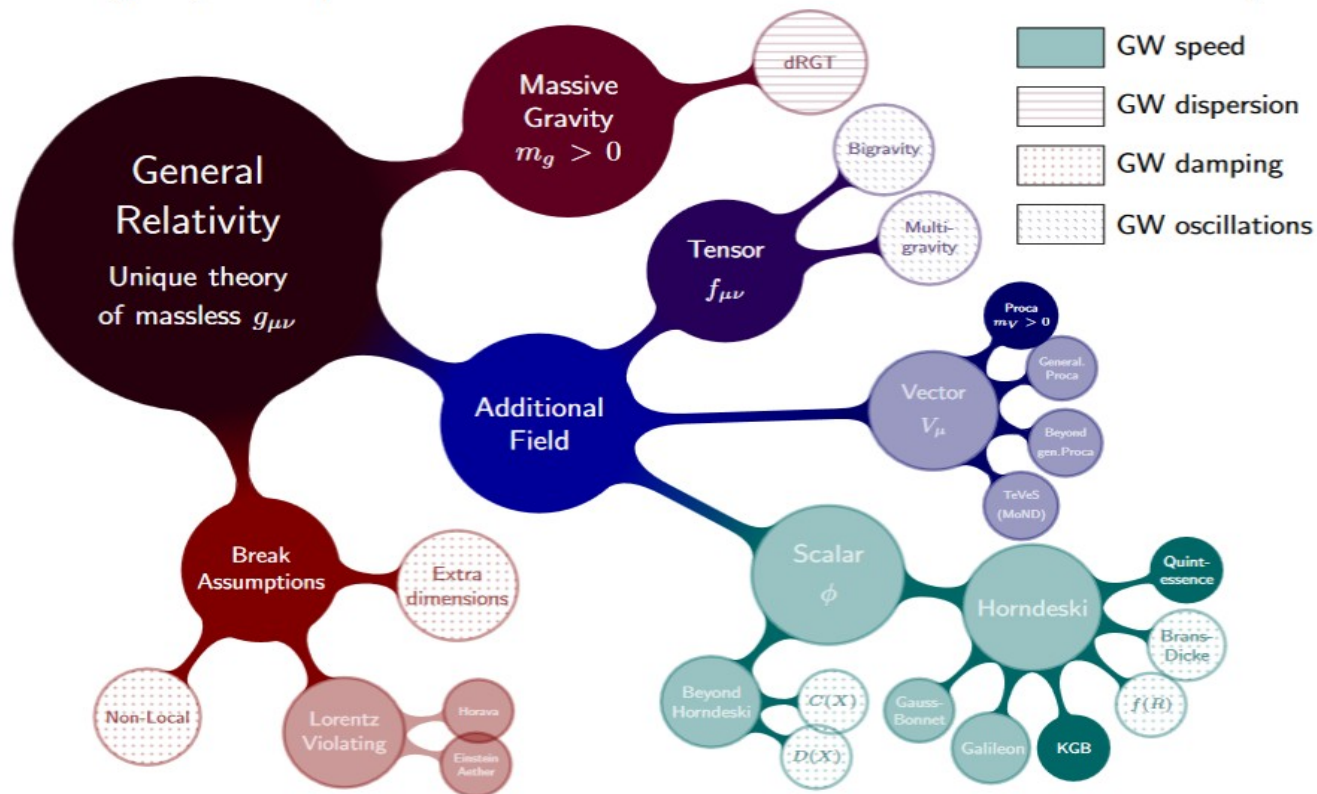
$$\begin{aligned} & -f_T G_{\mu\nu} + (g_{\mu\nu} \square - \nabla_\mu \nabla_\nu) f_B \\ & + \frac{1}{2} g_{\mu\nu} (f_B B + f_T T - f) \\ & + 2S_\nu{}^\alpha{}_\mu \partial_\alpha (f_T + f_B) = 8\pi G \Theta_{\mu\nu} \end{aligned}$$

- $$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}^{(1)} + \mathcal{O}(h_{\mu\nu}^{(2)})$$

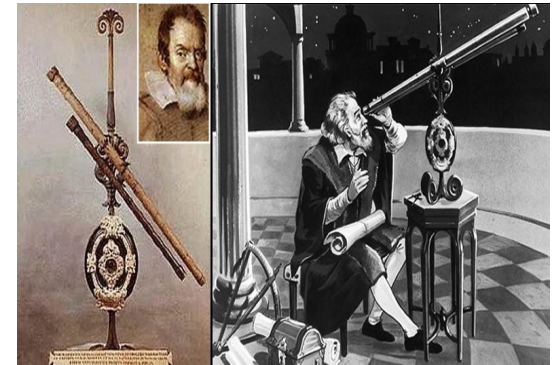
$$h_{\mu\nu}^{(1)} = \begin{pmatrix} -2A \exp(ik_\mu x^\mu) - \frac{f_{BB}^{(0)} B^{(1)}}{f_T^{(0)}} & B_1 \exp(ik_\mu x^\mu) & B_2 \exp(ik_\mu x^\mu) & -2A \exp(ik_\mu x^\mu) \\ B_1 \exp(ik_\mu x^\mu) & h_+ + \frac{f_{BB}^{(0)} B^{(1)}}{f_T^{(0)}} & h_\times & B_1 \exp(ik_\mu x^\mu) \\ B_2 \exp(ik_\mu x^\mu) & h_\times & -h_+ + \frac{f_{BB}^{(0)} B^{(1)}}{f_T^{(0)}} & B_2 \exp(ik_\mu x^\mu) \\ -2A \exp(ik_\mu x^\mu) & B_1 \exp(ik_\mu x^\mu) & B_2 \exp(ik_\mu x^\mu) & -2A \exp(ik_\mu x^\mu) + \frac{f_{BB}^{(0)} B^{(1)}}{f_T^{(0)}} \end{pmatrix}$$

Gravitational waves and Modified Gravity

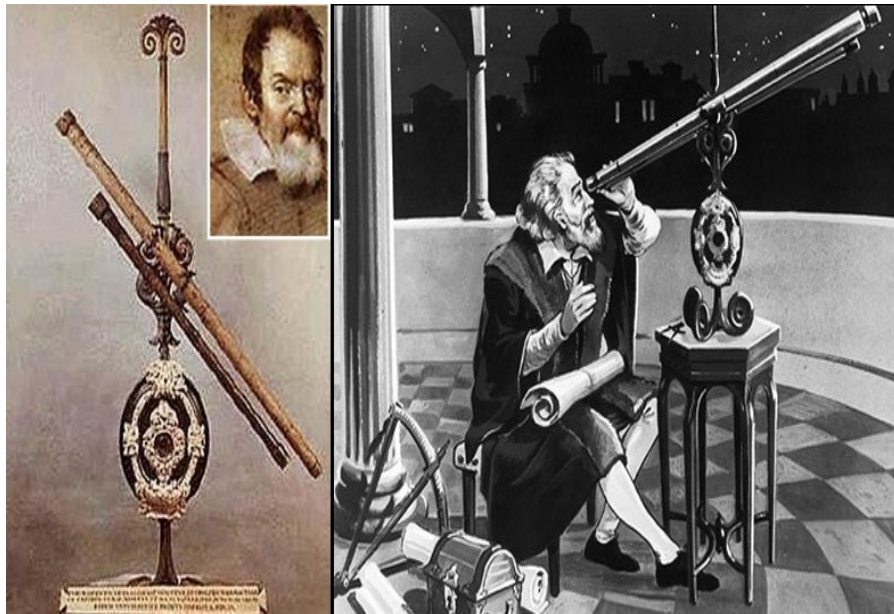
Modified gravity roadmap



5000 years of observations 500 years of organized observations



We are approaching a Revolution!

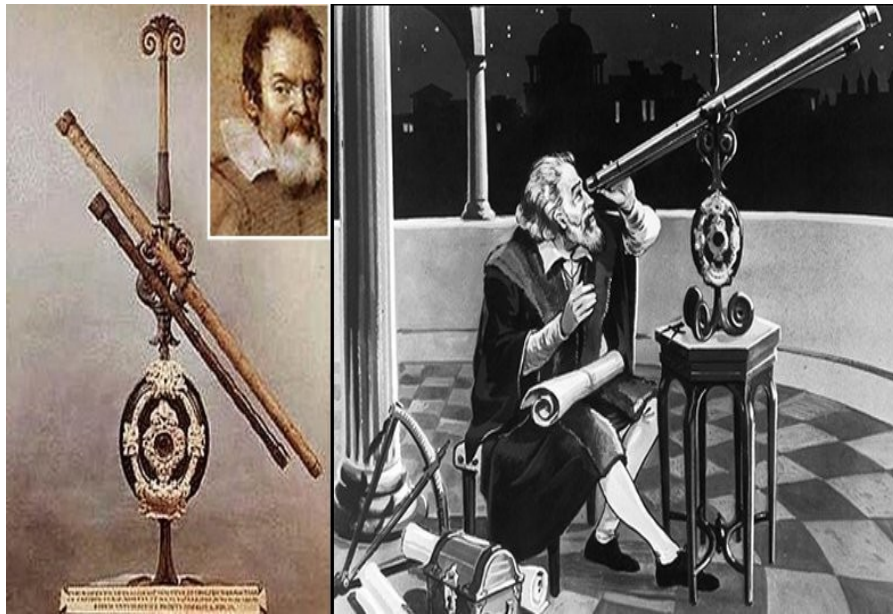


EM observations: 400 years



GW observations: 10 years

We are approaching a Revolution!



EM observations: 400 years

GW observations: 10 years

Thank you!