Hidden symmetries in holographic conformal correlators

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Introduction

Motivation

AdS/CFT Correspondence

CFT on AdS boundary \Leftrightarrow Quantum gravity in AdS



Figure: AdS/CFT Correspondence

Motivation

AdS/CFT Correspondence

CFT on AdS boundary \Leftrightarrow Quantum gravity in AdS

$$\mathcal{N} = 4 \quad SYM \iff Type \ IIB \ strings \ on \ AdS_5 \times S^5 \\ \downarrow Introduce \ \mathcal{N} = 2 \ Hyper-multiplet \quad \downarrow Introduce \ probe \ D7-branes \\ \mathcal{N} = 2 \ CFT \iff Super \ gluons \ living \ on \ AdS_5 \times S^3$$

Motivation: hidden conformal symmetry

Hidden conformal symmetry in various background

Uplifting the distances x_{ij}^2 in simplest cases to higher-dimensional distances $x_{ij}^2 - t_{ij}$ and obtain the results of correlators with general external dimensions

$$\mathcal{H}_{2222}^{(1)}\left(x_{ij}^{2}\right) \to \mathcal{H}_{p_{1}p_{2}p_{3}p_{4}}^{(1)}\left(x_{ij}^{2}, t_{ij}\right)$$

• $AdS_5 \times S^5$, the 10d distances [Caron-Huot, Trinh '18] • $AdS_5 \times S^3$, the 8d distances [Alday, Behan, Ferrero, Zhou '21]

Such a higher-dimensional structure surprisingly exists beyond this regime.

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Motivation: hidden conformal symmetry



Figure: Map of the parameter space (N_c : rank of gauge group; λ : 't Hooft coupling) of $\mathcal{N} = 4$ SYM or strings on $AdS_5 \times S^5$. [Beisert, Ahn, Alday, Bajnok, Drummond, et al '10]

From weak to strong coupling

Weakly coupled regime

The correlators can be evaluated from the reduced integrands

$$G_{p_1p_2p_3p_4}^{(\ell)} \propto R_{1234}^{\mathcal{N}=4} \left(2x_{12}^2 x_{13}^2 x_{14}^2 x_{23}^2 x_{23}^2 x_{34}^2 \right) \int \prod_i \frac{d^4 x_{4+i}}{\pi^2} \mathcal{H}_{p_1p_2p_3p_4}^{(\ell)}.$$

Hidden symmetry in weak coupling

The 10-dimensional symmetry could be turned around to recover the generic correlator from the simplest case [Caron-Huot, Coronado '21]

$$\mathcal{H}_{2222}^{(\ell)}\left(x_{ij}^{2}\right) \to \mathcal{H}_{2222}^{(\ell)}\left(x_{ij}^{2} - t_{ij}\right) = \sum_{p_{i}=2}^{\infty} \mathcal{H}_{p_{1}p_{2}p_{3}p_{4}}^{(\ell)}\left(x_{ij}^{2}, t_{ij}\right).$$

We found the similar 8d structures in $\mathcal{N}=2$ theories [Du, Huang, Wang, Yuan, Zhou '24].

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From weak to strong coupling

From weak to strong coupling



Figure: Map of the parameter space (N_c : rank of gauge group; λ : 't Hooft coupling) of $\mathcal{N} = 4$ SYM or strings on $AdS_5 \times S^5$. [Beisert, Ahn, Alday, Bajnok, Drummond, et al '10]

From weak to strong coupling

From weak to strong coupling



Figure: From weakly to strongly coupled regime in $\mathcal{N} = 4$ SYM.

Strongly coupled Region

Hidden symmetry at four-point

The tree-level supergraviton/supergluon enjoys the higher-dimensional hidden symmetry. For example, the gluon amplitude can be written as [Drummond, Glew, Santagata '22]

$$M_4 = R_{1234} \circ \widetilde{M}_4, \qquad \widetilde{M}_4 = \frac{1}{(\rho_{12} - 1)(\rho_{14} - 1)}.$$

Extend hidden symmetry beyond four-point functions?

Strongly coupled Region

Hidden symmetry at five-point

We give the first concrete confirmation for the existence of the hidden eight-dimensional symmetries at the level of five points [Huang, Wang, Yuan, Zhang '24]

$$M_5 = R^{(1)} \circ \widetilde{M}_5^{(1)} + R^{(2)} \circ \widetilde{M}_5^{(2)} + (\text{cyclic}), \qquad (1)$$

where

$$\begin{split} \widetilde{M}_5^{(1)} &= -\frac{1}{5\,(\rho_{12}-1)(\rho_{23}-1)(\rho_{34}-1)}\,,\\ \widetilde{M}_5^{(2)} &= -\frac{2}{5\,(\rho_{12}-1)(\rho_{23}-1)(\rho_{45}-1)}\,. \end{split}$$



Figure: Four-point correlators at strong coupling in $\mathcal{N} = 4$ [Heslop '22].

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Hidden symmetry beyond tree-level

There is nontrivial evidence for the persistence of the hidden conformal symmetry at one loop [Alday, Zhou '19]

$$\widetilde{M}_{22pp}^{(2)} = \hat{\Delta}^{(8)} \circ \hat{\mathcal{D}}_{22pp} \circ \mathcal{L}_{2222} \,.$$

We study the analytic behavior of supergluons and supergravitons with arbitrary external dimensions and find some hints for this hidden conformal symmetry.

All N²E one-loop correlators from hidden symmetry

We bootstrap all of the next-next-to-extremal one-loop four-point correlators of supergravitons and supergluons in AdS_5 using a differential representation [Huang, Wang, Yuan '24]



Figure: A correlator is written as differential operators acting on certain seed functions in this representation.



Figure: The universal pole structure of supergluons and supergravitons [Huang, Wang, Yuan, Zhou '23]; [Huang, Wang, Yuan 'work in progress].

Outlook

Outlook

- \blacksquare We found the hidden symmetries in the weakly coupled regime for $\mathcal{N}=2$ theories.
- We gave the first concrete confirmation for the existence of the hidden eight-dimensional symmetries at the level of five points.
- We generalized the one-loop result to N²E using a novel representation and studied the hidden symmetry for correlators with arbitrary external dimensions.

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Thanks