

momentum dependence of $K^*(892)$'s ρ_{00} at BESIII

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Outline

- 1 Motivation
- 2 Data sets and event selection
- 3 Spin alignment of K^* (892)
- 4 Systematic uncertainty
- 5 Summary
- 6 BACKUP
 - fit for data
 - fit for luarlw

Spin density matrix of vector meson

- 1 The spin state of a vector state is described by 3×3 spin density matrix

- ρ_{mm} : probability to be in $|s; s_z = m\rangle$ state

$$\begin{pmatrix} \rho_{-1,-1} & \rho_{-1,0} & \rho_{-1,1} \\ \rho_{-1,0}^* & \rho_{00} & \rho_{01} \\ \rho_{-1,1}^* & \rho_{01}^* & \rho_{11} \end{pmatrix}$$

- 2 The polarization vector is related to some elements of spin density matrix

$$\vec{\mathcal{P}} = [\mathcal{P}_1, \mathcal{P}_2, \mathcal{P}_3] = [\sqrt{2}\text{Re}(\rho_{-1,0} + \rho_{01}), \sqrt{2}\text{Im}(\rho_{-1,0} + \rho_{01}), (\rho_{11} - \rho_{-1,-1})]$$

- 3 Angular of decay particle (kaon) at K^{*0} helicity frame

- extract some elements, e.g. ρ_{00}

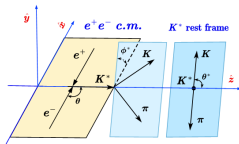
- 4 Vector meson are polarized or not by comparing of ρ_{00} and $1/3$

- $\rho_{00} \neq 1/3$: spin alignment

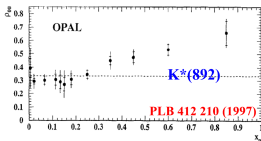
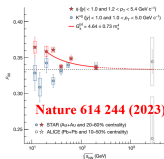
- 5 The angle distribution for the decay particle in the rest frame:

$$W(\theta^*, \phi^*) = \frac{3}{4\pi} \left[\frac{1}{2}(1 - \rho_{00}) + \frac{1}{2}(3\rho_{00} - 1) \cos^2 \theta^* \right]$$

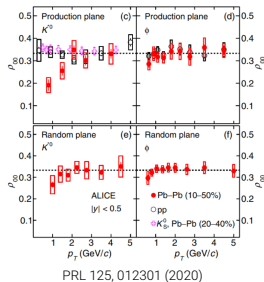
$$\begin{aligned} & -\text{Re}\rho_{1,-1} \sin^2 \phi^* \cos 2\phi^* - \frac{1}{\sqrt{2}} \text{Re}(\rho_{10} - \rho_{0,-1}) \sin 2\theta^* \cos \phi^* \\ & + \text{Im}\rho_{1,-1} \sin^2 \theta^* \sin 2\phi^* + \frac{1}{\sqrt{2}} \text{Im}(\rho_{10} - \rho_{0,-1}) \sin 2\theta^* \sin \phi^* \end{aligned}$$



ρ_{00} of vector meson

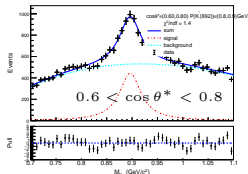


- 1 Heavy ion collision: contribution from QGP(Quark-Gluon Plasma) & fragmentation
 - STAR: for ϕ **unexpectedly large** than 1/3 (with respect to reaction plane)
- 2 e^+e^- collision: contribution from **fragmentation**, Z^0 energy
 - $x_p < 0.3$, consistent with 1/3; $x_p > 0.3$, larger than 1/3
- 3 pp collision: contribution from PDF function & fragmentation.
 - ALICE: ρ_{00} for ϕ and K^* are consistent with 1/3.
- 4 BESIII: e^+e^- collision: **fragmentation**, γ^* dominant
 - BAM-00884, unbinned ρ_{00} @ $\sqrt{s}=3.5$ GeV.
 - How about momentum dependence of ρ_{00} ?

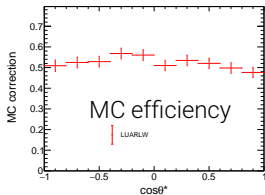


How to determine ρ_{00} at BESIII

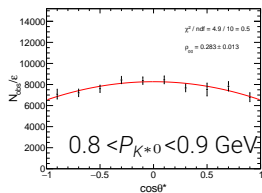
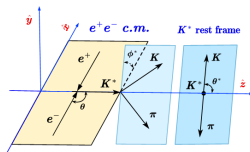
- 1 Hadronic selection to select hadrons
- 2 Extract K^{*0} signals from hadrons
 - fit to the spectrum of $M_{K^{\pm}\pi^{\mp}}$



$0.8 < P_{K^{*0}} < 0.9$ GeV



- 3 MC for the correction efficiency.
- 4 Get ρ_{00} component from fitting the **efficiency corrected signal events**.



$$W(\theta^*) = \frac{3}{4} [(1 - \rho_{00}) + (3\rho_{00} - 1) \cos^2 \theta^*]$$

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Data sets

- Boss version: 703
- Data sets:

| | \sqrt{s} (GeV) | Run number | \mathcal{L} (pb^{-1}) |
|------------|------------------|---------------|------------------------------------|
| chic1 scan | 3.4900 | 47467 – 47493 | 12.11 |
| | 3.5080 | 51657 – 51893 | 181.79 |
| | 3.5097 | 51584 – 51656 | 39.29 |
| | 3.5104 | 51894 – 52090 | 183.64 |
| | 3.5146 | 52298 – 52332 | 40.92 |

- Hadronic MC samples:

LUARLW, 10M events each point.(nominal)

HYBRID, 10M events each point.

- QED MC:

$e^+e^- \rightarrow e^+e^- / \mu^+\mu^- / \gamma\gamma$: **Babayaga3.5**

$e^+e^- \rightarrow e^+e^- + X$ (X:leptons and hadrons): **DIAG36,EKHARA,GALUGA2.0**

Hadronic event selection

- Same as R-value analysis published in PRL 128, 062004 (2022)

Track Level

- **Veto Bhabha and Di-gamma events**
 - $N_{\text{shower}} \geq 2$
 - $E_1 \geq E_2 \geq 0.65E_{\text{beam}}$
 - $|\Delta\theta| = |\theta_1 + \theta_2 - 180^\circ| < 10^\circ$
- **Isolated photon**
 - Energy deposition should be larger than 0.1 GeV
 - Angle from the nearest charged track should be larger than 20°
 - $0 < T_{\text{EMC}} < 700$ ns
- **Good charged hadronic tracks**
 - $|V_x| < 0.5$ cm, $|V_z| < 5.0$ cm, $|\cos\theta| < 0.93$
 - $p_{\text{track}} < 0.94p_{\text{beam}}$, where $p_{\text{beam}} \approx E_{\text{beam}}$
 - $\chi_{\text{prob.}} = (dE/dx_{\text{measure}} - dE/dx_{\text{proton}}) / \sigma_{\text{proton}} > 10$
 - Remove charged tracks when $E/p > 0.8$ and $p > 0.65p_{\text{beam}}$
 - Veto γ -conversions when $M(e^+e^-) < 0.1$ GeV and $\theta_{ee} < 15^\circ$

Event Level

At least 2 good charged hadronic tracks

- **Number of good charged hadronic tracks = 2:**
 - $|\Delta\theta| = |\theta_1 + \theta_2 - 180^\circ| > 10^\circ$ or $|\Delta\phi| = ||\phi_1 - \phi_2| - 180^\circ| > 15^\circ$
 - At least 2 isolated photons
- **Number of good charged hadronic tracks = 3:**
 - The two highest momentum tracks are required not back-to-back: $|\Delta\theta| = |\theta_1 + \theta_2 - 180^\circ| < 10^\circ$ or $|\Delta\phi| = ||\phi_1 - \phi_2| - 180^\circ| < 15^\circ$
 - (number of track with $E/p > 0.8$) ≤ 1
 - (number of track with PID ratio > 0.25) ≤ 1 , where the PID ratio is defined as $r_{\text{PID}} = \frac{\text{Prob.}(e)}{\text{Prob.}(p)+\text{Prob.}(K)+\text{Prob.}(\pi)+\text{Prob.}(e)}$
- **Number of good charged hadronic tracks ≥ 4 :**
No additional requirements

Reconstruction of $K^*(892)$ via $K^*(892) \rightarrow K\pi$

1 PID ($dE/dx + \text{ToF}$)

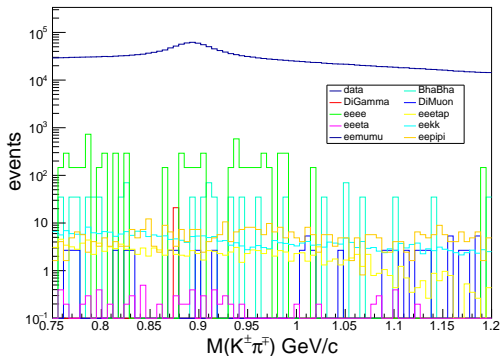
- $\text{Prob.}(K) > \text{Prob.}(\pi), \text{Prob.}(K) > \text{Prob.}(p)$ and $\text{Prob}(K) > 0.001$
- $\text{Prob.}(\pi) > \text{Prob.}(K), \text{Prob.}(\pi) > \text{Prob.}(p)$ and $\text{Prob}(\pi) > 0.001$

2 combine all $K^\pm \pi^\mp$

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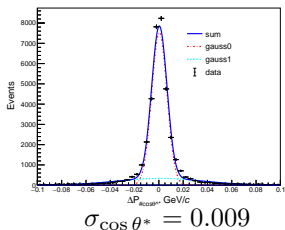
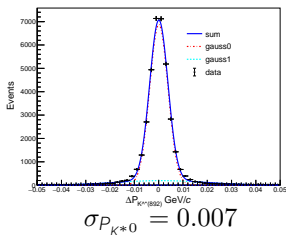
QED Background MC



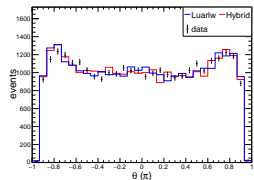
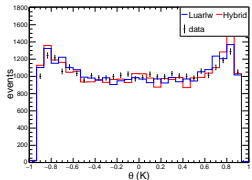
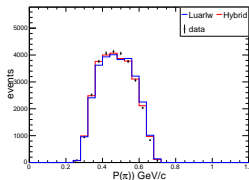
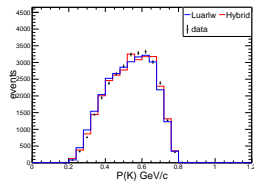
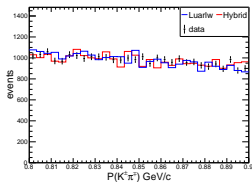
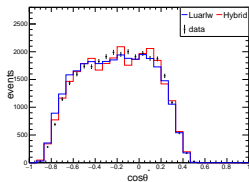
- 1 QED background: Bhabha, di-gamma, di-muon, and two-photon events.
- 2 All QED process can be well described by **polynomial function**.

Binning determination

- 1 The **resolution** of $\cos \theta^*$ and P_{K^*0} :
 - Obtained by **LUARLW MC**, and fitted with **double Gaussian function**
- 2 The candidate events are divided into **10 intervals** of $\cos \theta^*$
 - $\Delta \cos \theta^* = 0.2 > 5\sigma_{\cos \theta^*}$
- 3 The momentum intervals is set at 0.1 GeV, ranging from 0.4 to 1.6 GeV.
 - $\Delta P_{K^*0} = 0.1 > 5\sigma_{P_{K^*0}}$



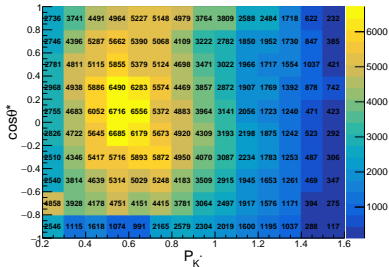
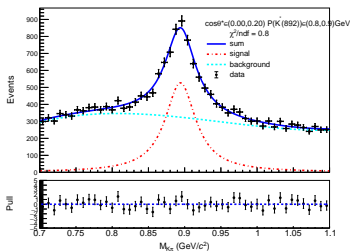
The difference between data and MC



The MC fits with the data well.

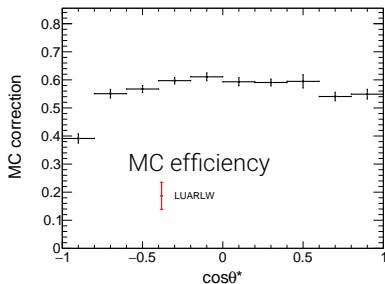
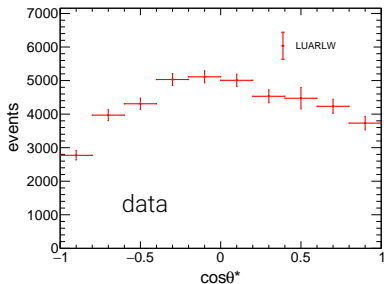
Extract $K^{*0}(892)$ signals

- Unbinned maximum likelihood fit method is used to extract signals from $M(K^\pm\pi^\mp)$ in each (p vs. $\cos\theta^*$) bin.
- Signal:** Breit-Wigner \otimes Gaussian
- Background:** 3th-order Chebyshev polynomial
- The parameter of the Breit-Wigner function is fixed to the $K^*(892)$'s PDG values.



The fit result and MC efficiency

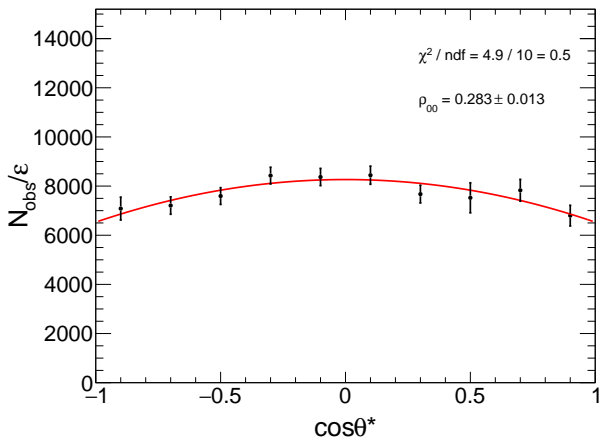
$$0.8 < P_{K^*} < 0.9 \text{ GeV}/c$$



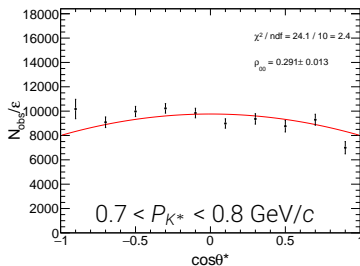
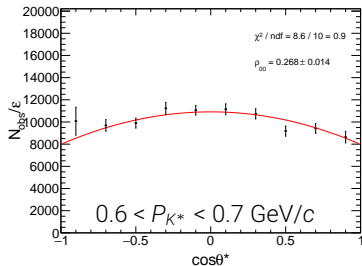
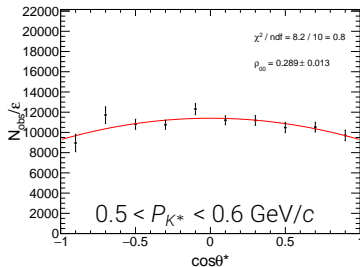
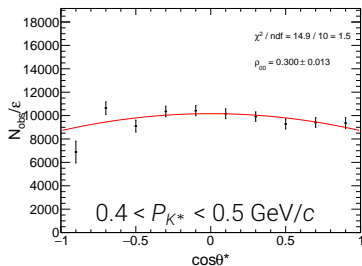
- The signal yields of data is shown in left figure.

ρ_{00} result while $P_\phi \in (0.8, 0.9)$ GeV/c

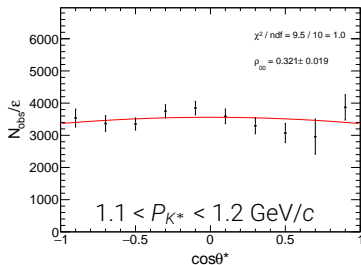
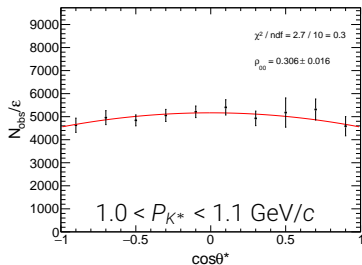
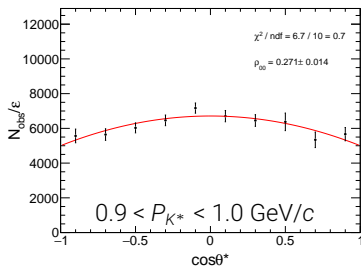
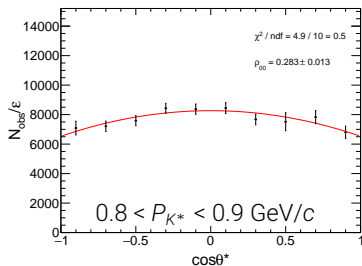
$$W(\theta^*) = \frac{3}{4} [(1 - \rho_{00}) + (3\rho_{00} - 1) \cos^2 \theta^*]$$



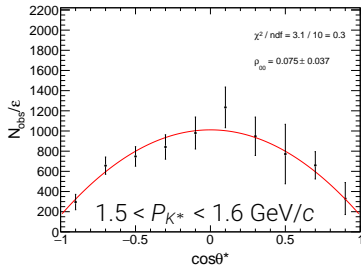
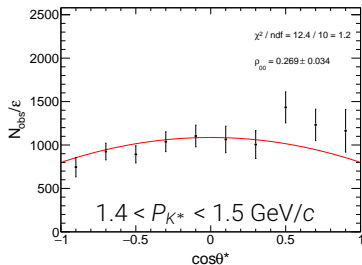
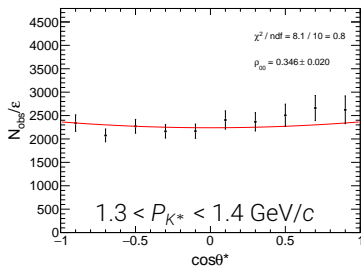
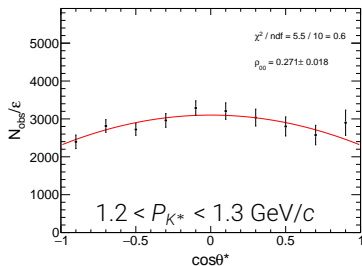
ρ_{00} result in each momentum bin



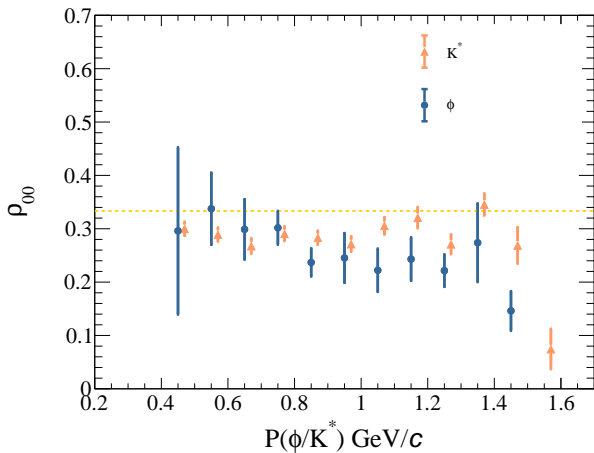
ρ_{00} result in each momentum bin



ρ_{00} result in each momentum bin



ρ_{00} result at $\sqrt{s} = 3.5 \text{ GeV}/c^2$



K^{*0} come from resonance decay

- At BESIII, K^{*0} may come from **fragmentation** or by **resonance decay**.
 - The helicity distribution of the resonance decay to K^{*0} may **influence** the decay angle of K^{*0}
- List table show that the number of K^{*0} decayed by **resonance**(by topology)

| source | percent(%) |
|------------------|------------|
| $K_2^{*+}(1430)$ | 1.74 |
| $K_1^0(1400)$ | 1.46 |
| $K_1^+(1400)$ | 0.75 |
| $K_2^{*0}(1430)$ | 0.61 |
| $K_1^+(1270)$ | 0.31 |

- Generate MC to consider the effect from those resonances.(ongoing)

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Systematic uncertainty (still ongoing)

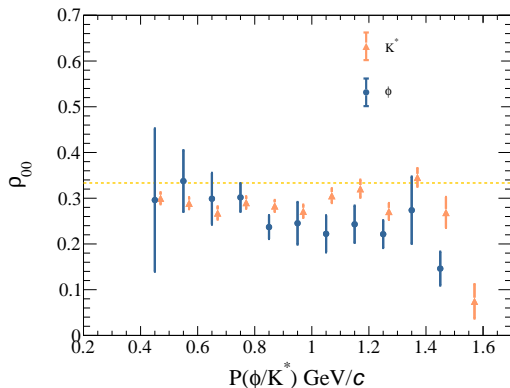
- 1 **MC model:** LUARLW \rightarrow HYBRID.
 - The difference between two MC model results.
- 2 **Event selection**
 - Same as **R-value analysis**.
- 3 **Fit method**
 - **Signal pdf & background pdf**
- 4 **Beam associated background**
 - N_{beam} is estimate by sideband method.

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Summary and outlook

- 1 Spin alignment of inclusive K^* is studied with $\mathcal{L} = 457.75 \text{ pb}^{-1}$ at $\sqrt{s} = 3.5 \text{ GeV}$.
- 2 ρ_{00} for K^* deviates from $1/3$, ϕ is more polarized than K^* does.



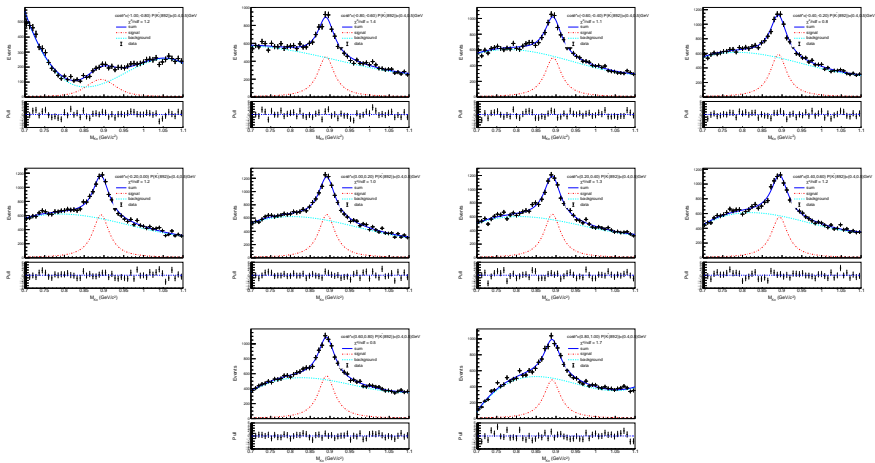
Next to do:

- Finish **systematic uncertainty** for $\sqrt{s} = 3.5 \text{ GeV}$.
- Other energy points (3.65 GeV and 3.08 GeV).

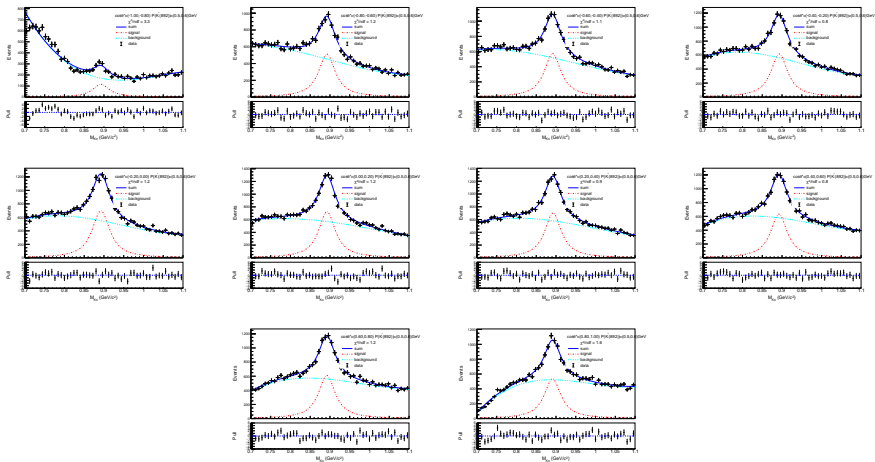
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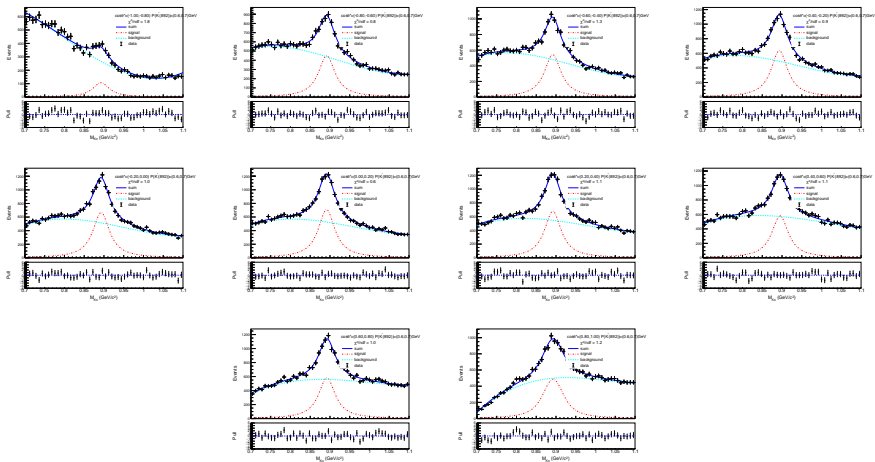
data result on $0.4 < P_{K^*} < 0.5$ GeV



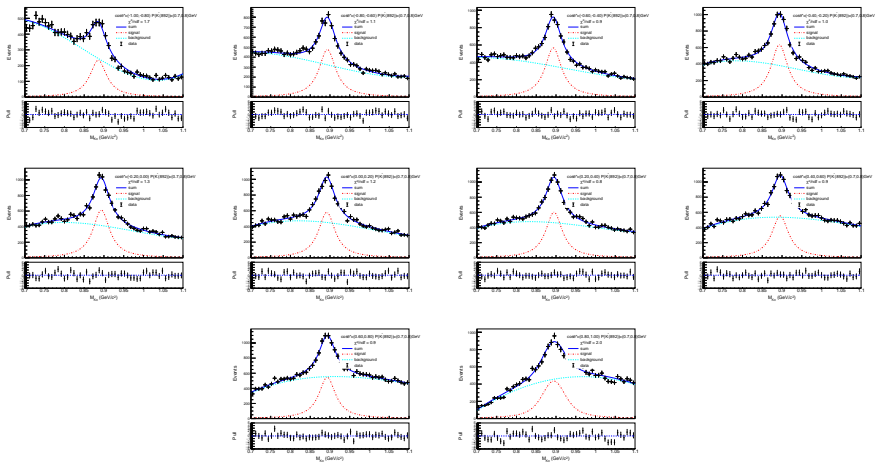
data result on $0.5 < P_{K^*} < 0.6$ GeV



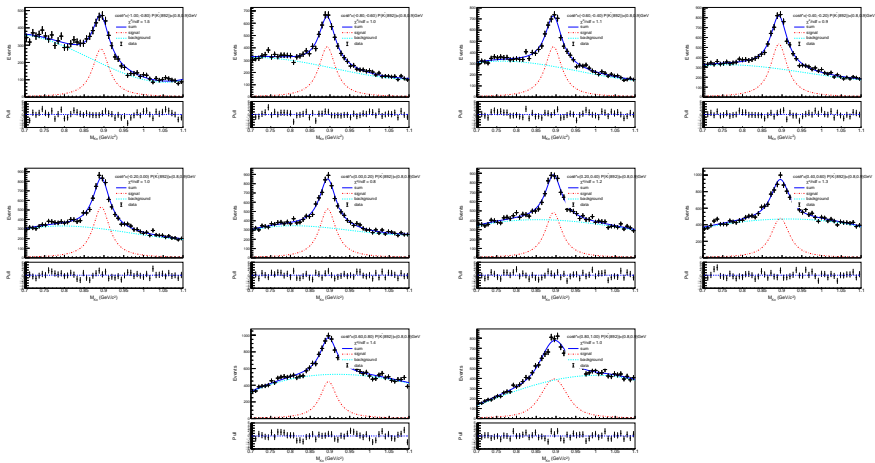
data result on $0.6 < P_{K^*} < 0.7$ GeV



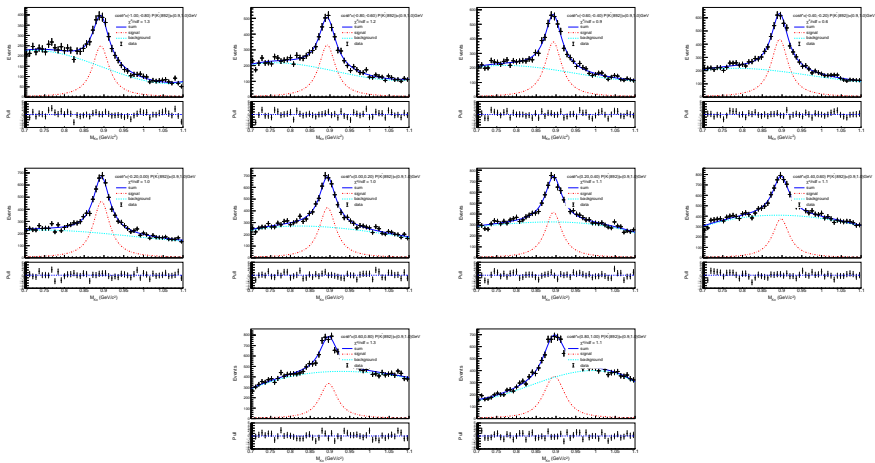
data result on $0.7 < P_{K^*} < 0.8$ GeV



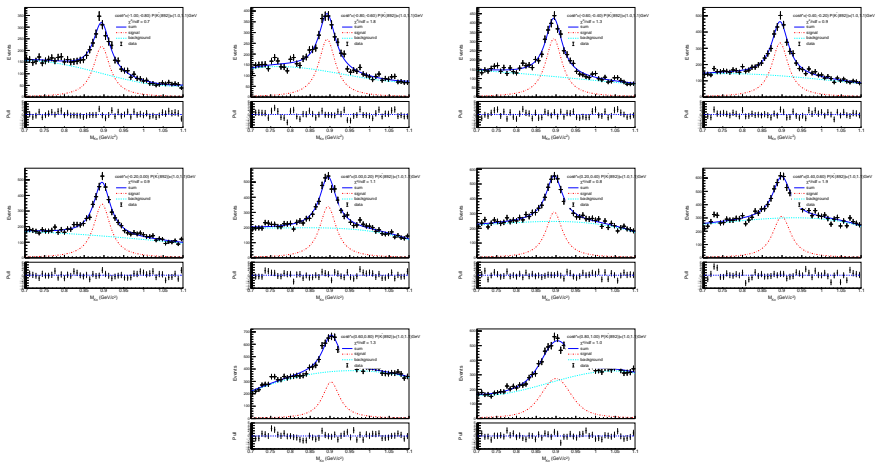
data result on $0.8 < P_{K^*} < 0.9$ GeV



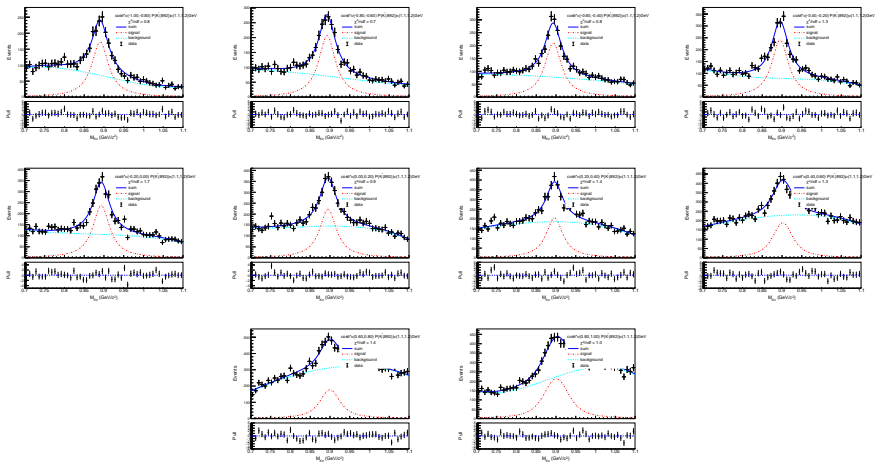
data result on $0.9 < P_{K^*} < 1.0$ GeV



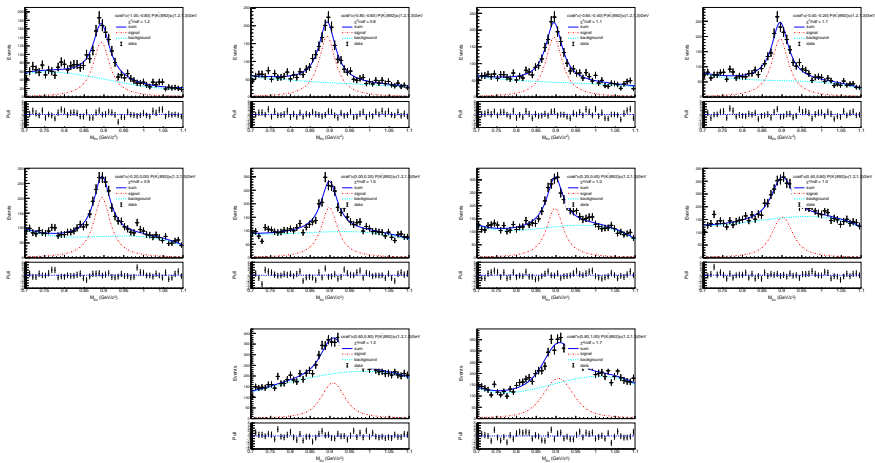
data result on $1.0 < P_{K^*} < 1.1$ GeV



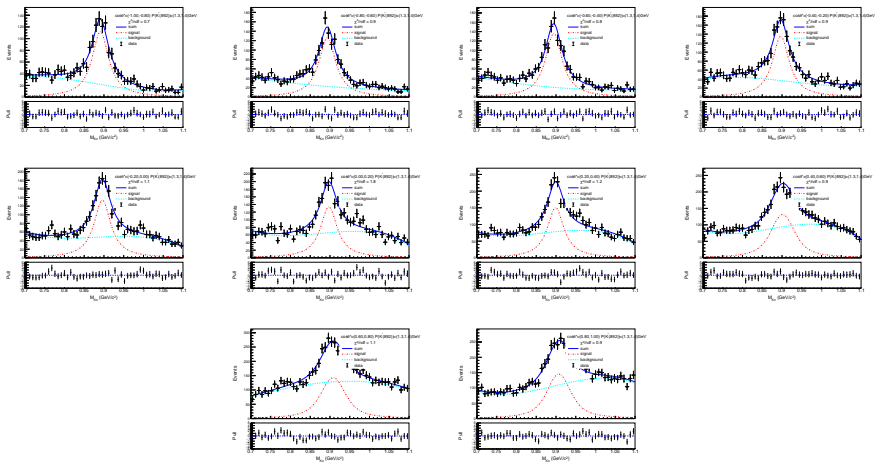
data result on $1.1 < P_{K^*} < 1.2$ GeV



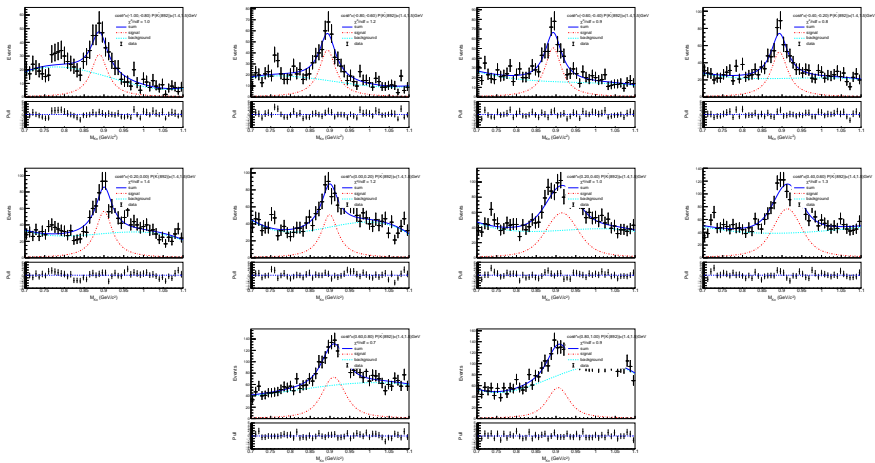
data result on $1.2 < P_{K^*} < 1.3$ GeV



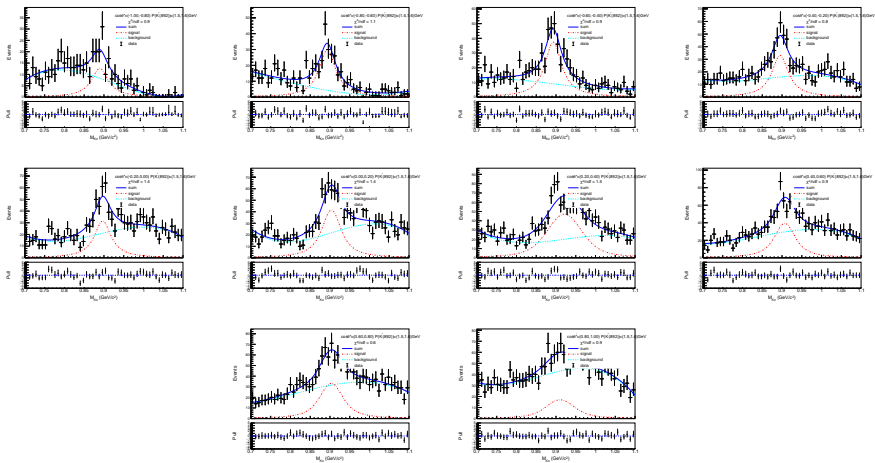
data result on $1.3 < P_{K^*} < 1.4$ GeV



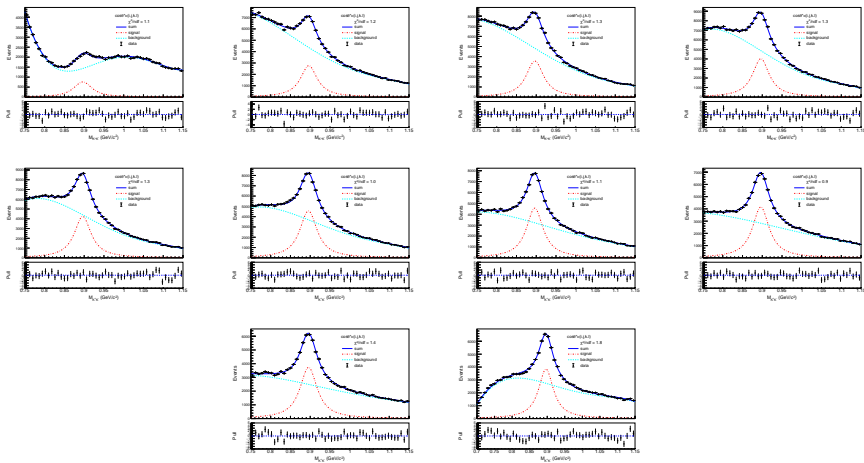
data result on $1.4 < P_{K^*} < 1.5$ GeV



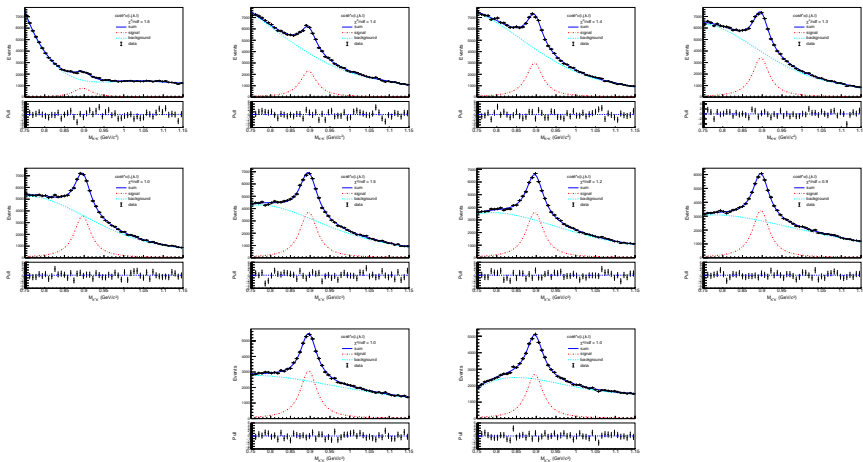
data result on $1.5 < P_{K^*} < 1.6$ GeV



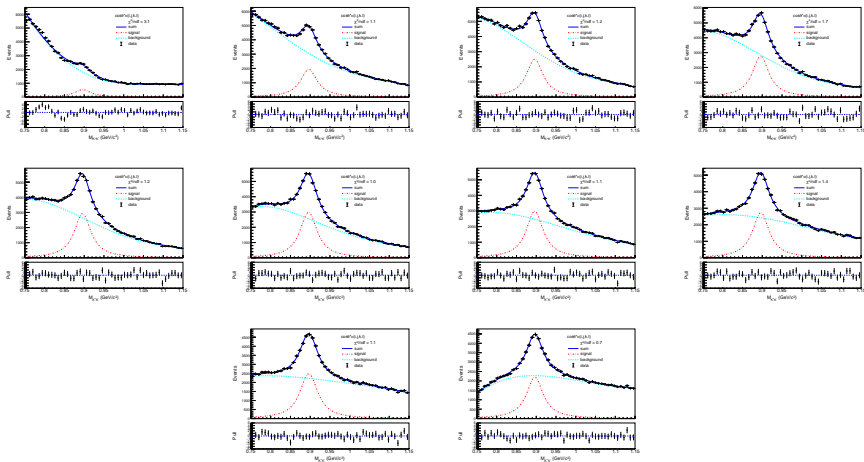
Ion result on $0.4 < P_{K^*} < 0.5$ GeV



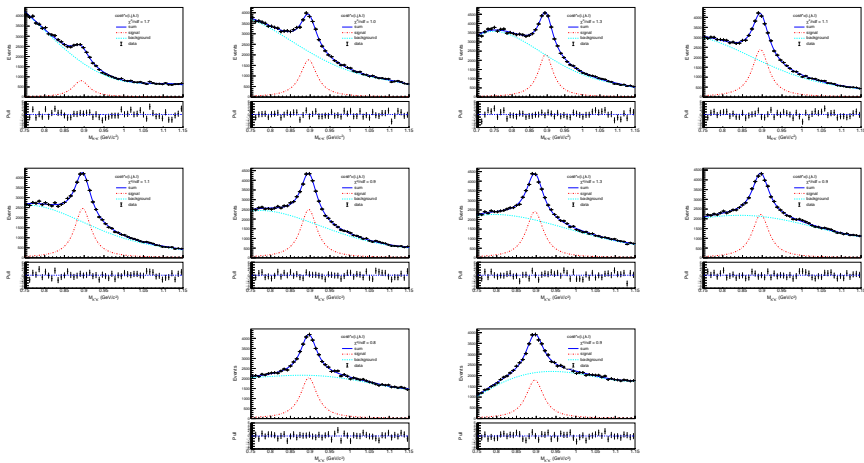
Ion result on $0.5 < P_{K^*} < 0.6$ GeV



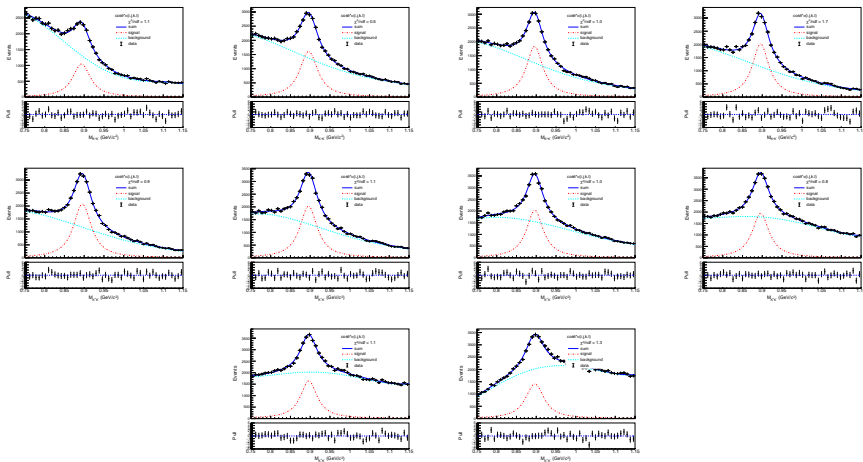
Ion result on $0.6 < P_{K^*} < 0.7$ GeV



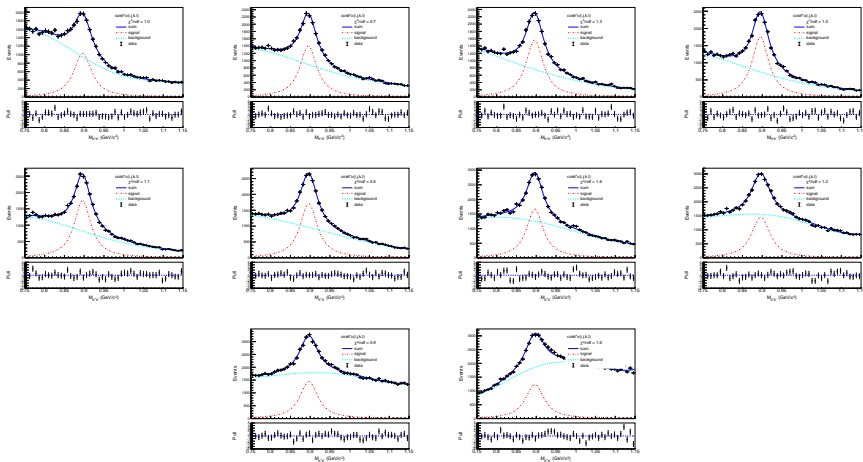
Ion result on $0.7 < P_{K^*} < 0.8$ GeV



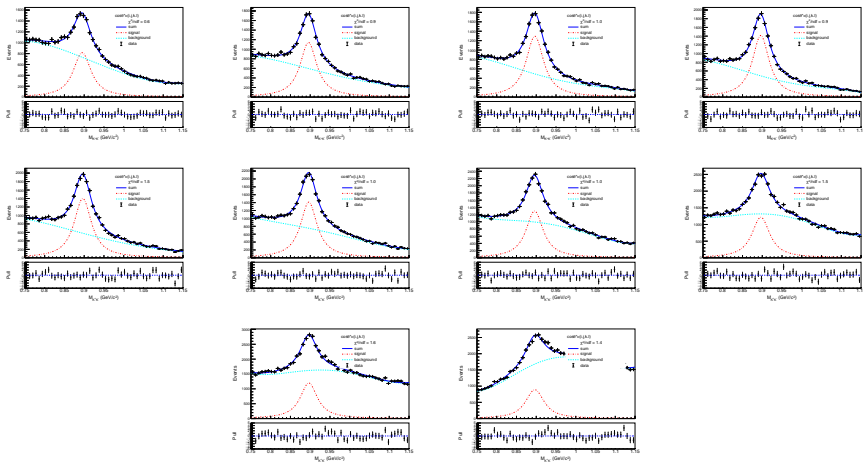
Ion result on $0.8 < P_{K^*} < 0.9$ GeV



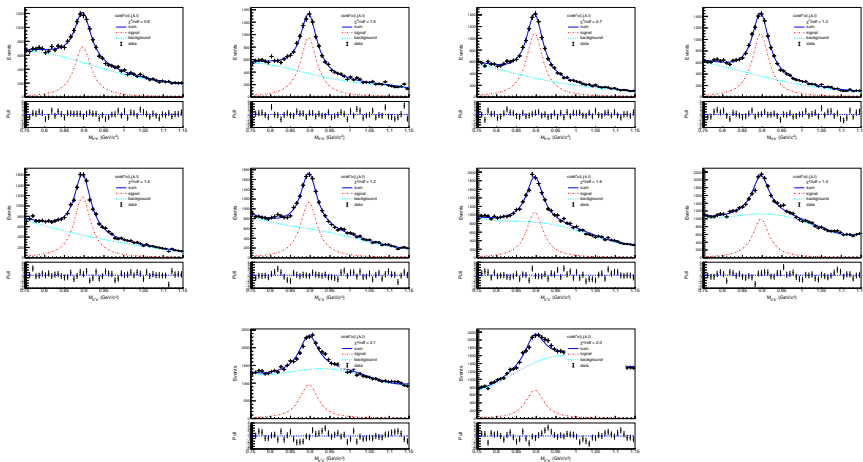
Ion result on $0.9 < P_{K^*} < 1.0$ GeV



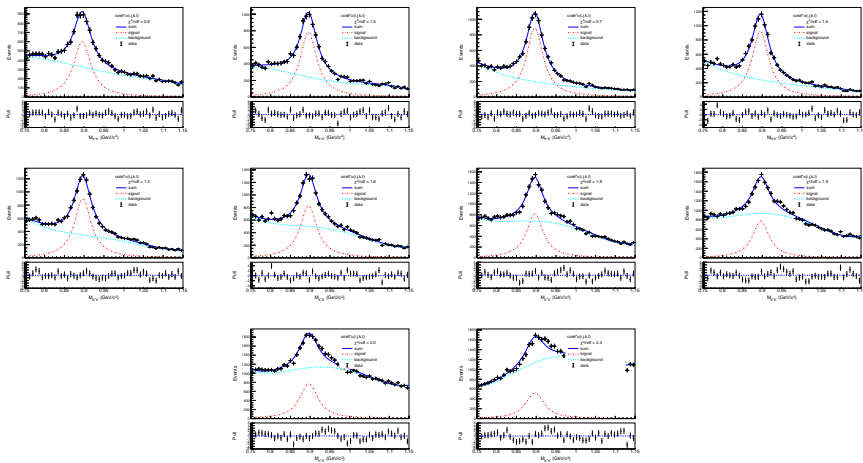
Ion result on $1.0 < P_{K^*} < 1.1$ GeV



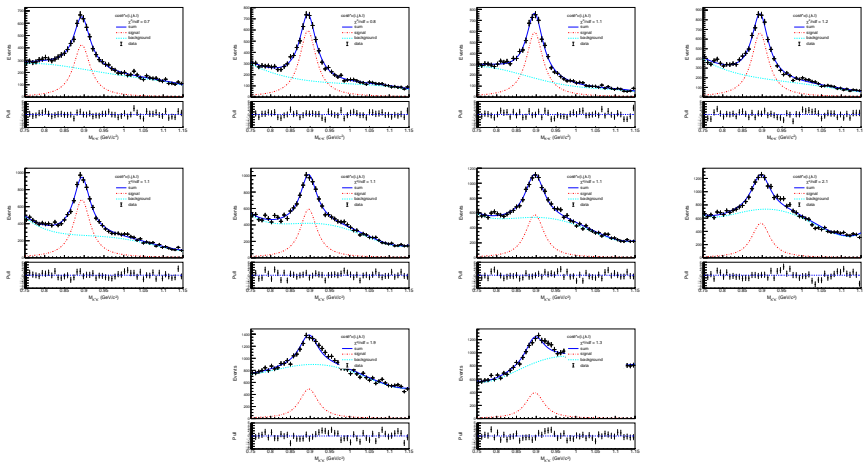
Ion result on $1.1 < P_{K^*} < 1.2$ GeV



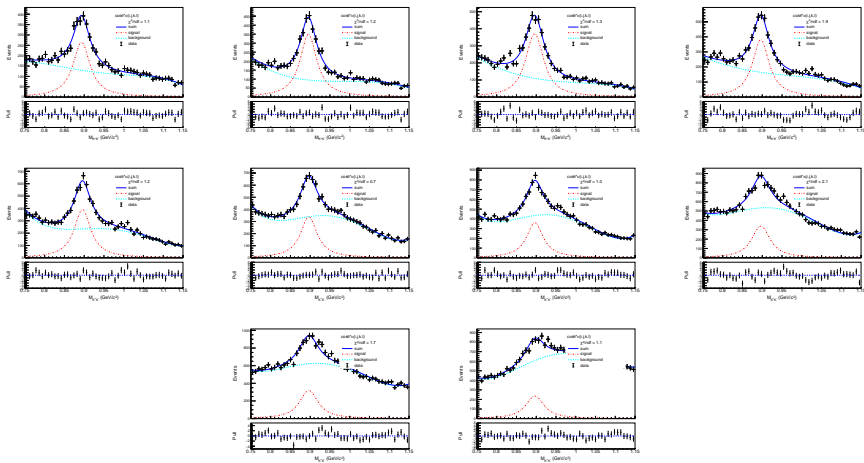
Ion result on $1.2 < P_{K^*} < 1.3$ GeV



Ion result on $1.3 < P_{K^*} < 1.4$ GeV



Ion result on $1.4 < P_{K^*} < 1.5$ GeV



Ion result on $1.5 < P_{K^*} < 1.6$ GeV

