

Recent results of semi-leptonic D decays at BESIII

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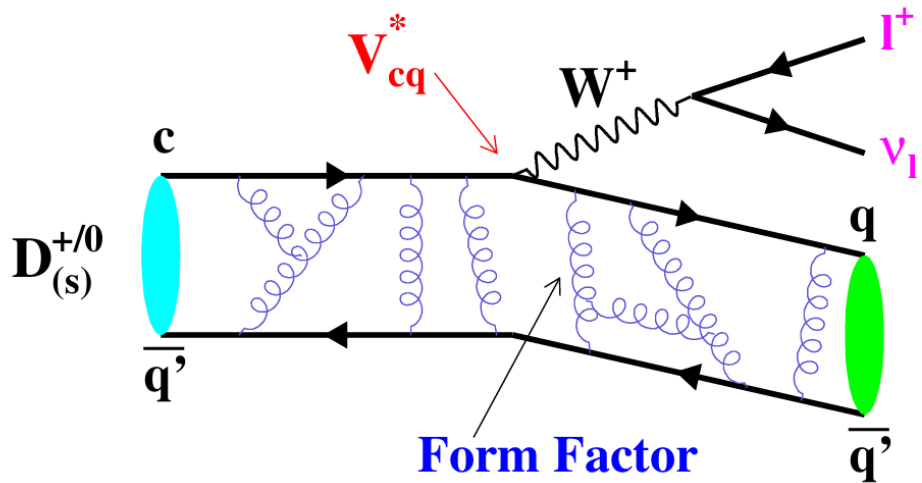
BESIII 粲强子研讨会2025, 兰州

Outline

- Motivations
- BESIII Experiment
- Pseudoscalar: $D \rightarrow P \ell^+ \nu_\ell$
- Scalar: $D \rightarrow S \ell^+ \nu_\ell$
- Vector: $D \rightarrow V \ell^+ \nu_\ell$
- Axial vector: $D \rightarrow A \ell^+ \nu_\ell$
- Summary & Outlook

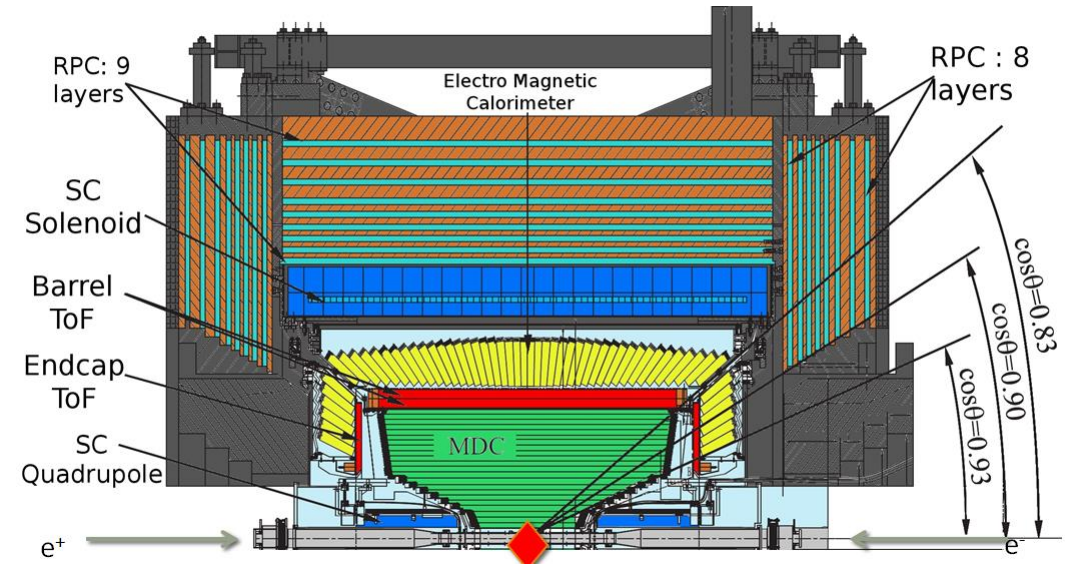
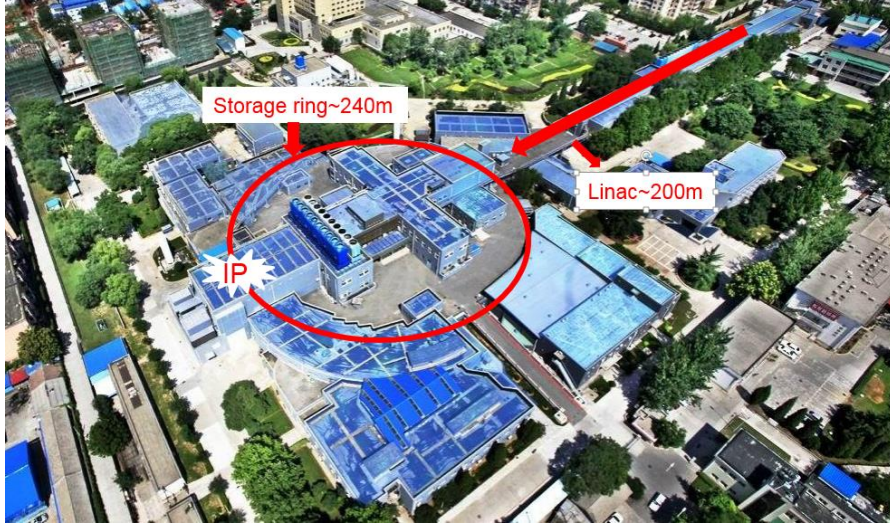
Motivations

$$M_{fi} = \frac{G_F}{\sqrt{2}} V_{cq} \times \langle P, S, V, A | q \gamma_\mu (1 - \gamma_5) c | D \rangle \times \bar{u}_\nu \gamma^\mu (1 - \gamma_5) \nu_{\ell^+}$$



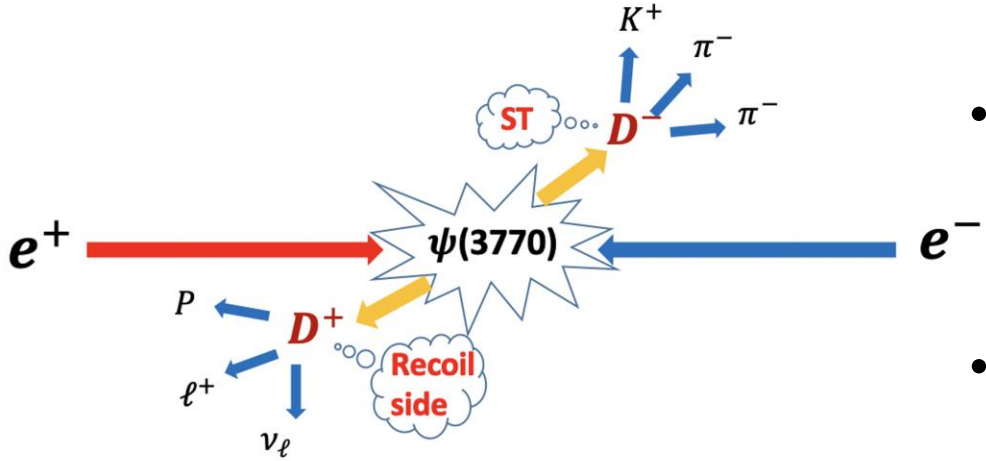
- **Determination of $|V_{cq}|$:** Validation of Unitarity of CKM matrix & Basic parameters of SM
- **Extraction of Form Factors:** Test & Calibrate various theoretical calculations, e.g. LQCD
- **Search for BSM:** lepton flavor universality & BSM scalar/vector/tensor contributions

BESIII experiment



- $\sqrt{s} = (1.85 - 4.95) \text{ GeV}$
- Peak luminosity: $1.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ @3.773 GeV
- MDC: $\sigma_p/P = 0.5\%$ @ 1 GeV; $\sigma_{dE/dx} = 6\%$
- TOF: $\sigma_T = 68(110) \text{ ps}$ for barrel(endcap); endcap upgraded in 2015 $\sigma_T = 110 \rightarrow 68 \text{ ps}$
- EMC: $\sigma_E/E = 2.5\%$ (5%) for barrel(endcap)

Dataset & Double tag method



- e^+e^- annihilations data near threshold $\rightarrow$ Double-tag method & Clean environment
- Undetectable neutrinos $\rightarrow$ extract the (semi-)leptonic signals with

$$U_{miss} = E_{miss} - |\vec{p}_{miss}|, M_{miss}^2 = E_{miss}^2 - |\vec{p}_{miss}|^2$$

- Branching fraction with double tag method: $B = \frac{N_{DT}}{N_{ST}\epsilon_{DT}/\epsilon_{ST}}$
 $\rightarrow$ cancel most of systematic uncertainties due to ST

Data sample	E_{cm} (GeV)	$\mathcal{L}_{\text{int}}$ (fb $^{-1}$)	Single tag yields ($\times 10^6$)
$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$	3.773	20.3	$\bar{D}^0 \sim 16.9$; $D^- \sim 11.0$
$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	4.128-4.226	7.33	$D_s^- \sim 0.8$
$e^+e^- \rightarrow D_s^{*+} D_s^{*-}$	4.237-4.669	10.64	$D_s^- \sim 0.12$

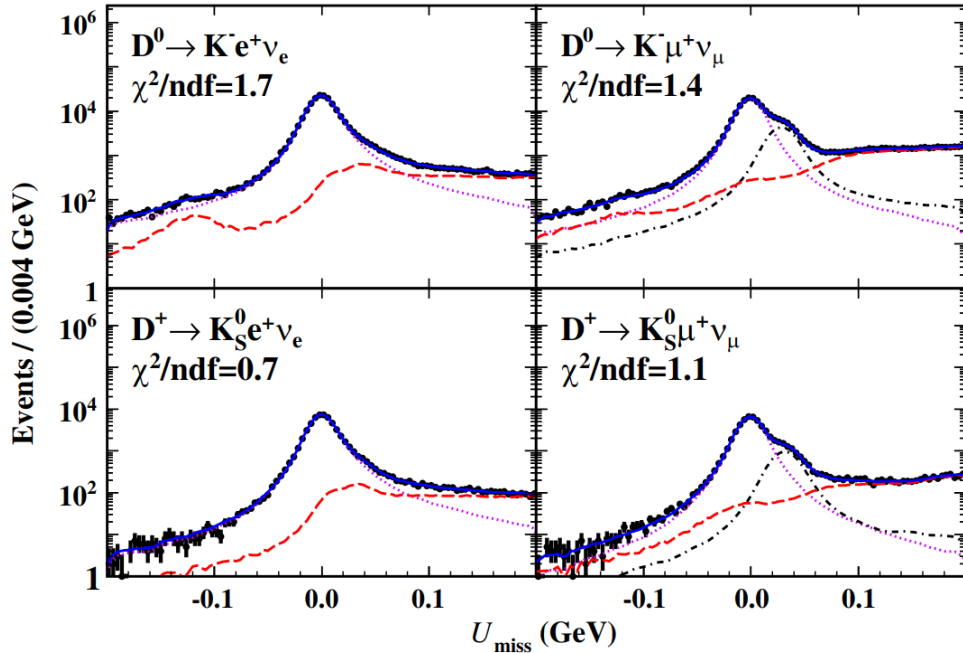
Decay formalism of $D \rightarrow P/S\ell^+\nu_\ell$

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 |V_{cq}|^2}{24\pi^3} \frac{(q^2 - m_\ell^2)^2 |p_X|}{q^4 m_D^2} \left[\left(1 + \frac{m_\ell^2}{2q^2} \right) m_D^2 |p_X|^2 |f_+^X(q^2)|^2 + \frac{3m_\ell^2}{8q^2} (m_D^2 - m_X^2)^2 |f_0^X(q^2)|^2 \right]$$

- X indicates (pseudo)-scalar particle
- Two FFs are included in $D \rightarrow P/S\ell^+\nu_\ell$: $f_+^X(q^2)$ & $f_0^X(q^2)$ with $f_+^X(0) = f_0^X(0)$
- Parametrization of q^2 -dependence:
 1. Single pole: $f(q^2) = f(0)/(1 - \frac{q^2}{M_{pole}^2})$
 2. Modified pole: $f(q^2) = f(0)/\left(1 - \frac{q^2}{M_{pole}^2}\right)\left(1 - \alpha \frac{q^2}{M_{pole}^2}\right)$
 3. Series expansion: $f(q^2) = \frac{1}{P(q^2)\Phi(q^2)} \sum a_k(t_0) [z(q^2, t_0)]^k$

Improved measurements of $D \rightarrow \bar{K} \ell^+ \nu_\ell$

- [Phys. Rev. D 110, 112006 \(2024\)](#)
- 7.93 fb^{-1} data sample @3.773 GeV
- $\sum N_{DT} \sim 0.44 \text{ M}$



- Branching fractions:

$$B(D^0 \rightarrow K^- e^+ \nu_e) = (3.521 \pm 0.009 \pm 0.016)\%$$

$$B(D^0 \rightarrow K^- \mu^+ \nu_\mu) = (3.419 \pm 0.011 \pm 0.016)\%$$

$$B(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = (8.864 \pm 0.039 \pm 0.082)\%$$

$$B(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu) = (8.665 \pm 0.046 \pm 0.084)\%$$

- LFU test: **consistent with SM: 0.975 ± 0.001**

$$\frac{B(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{B(D^0 \rightarrow K^- e^+ \nu_e)} = 0.971 \pm 0.004 \pm 0.006$$

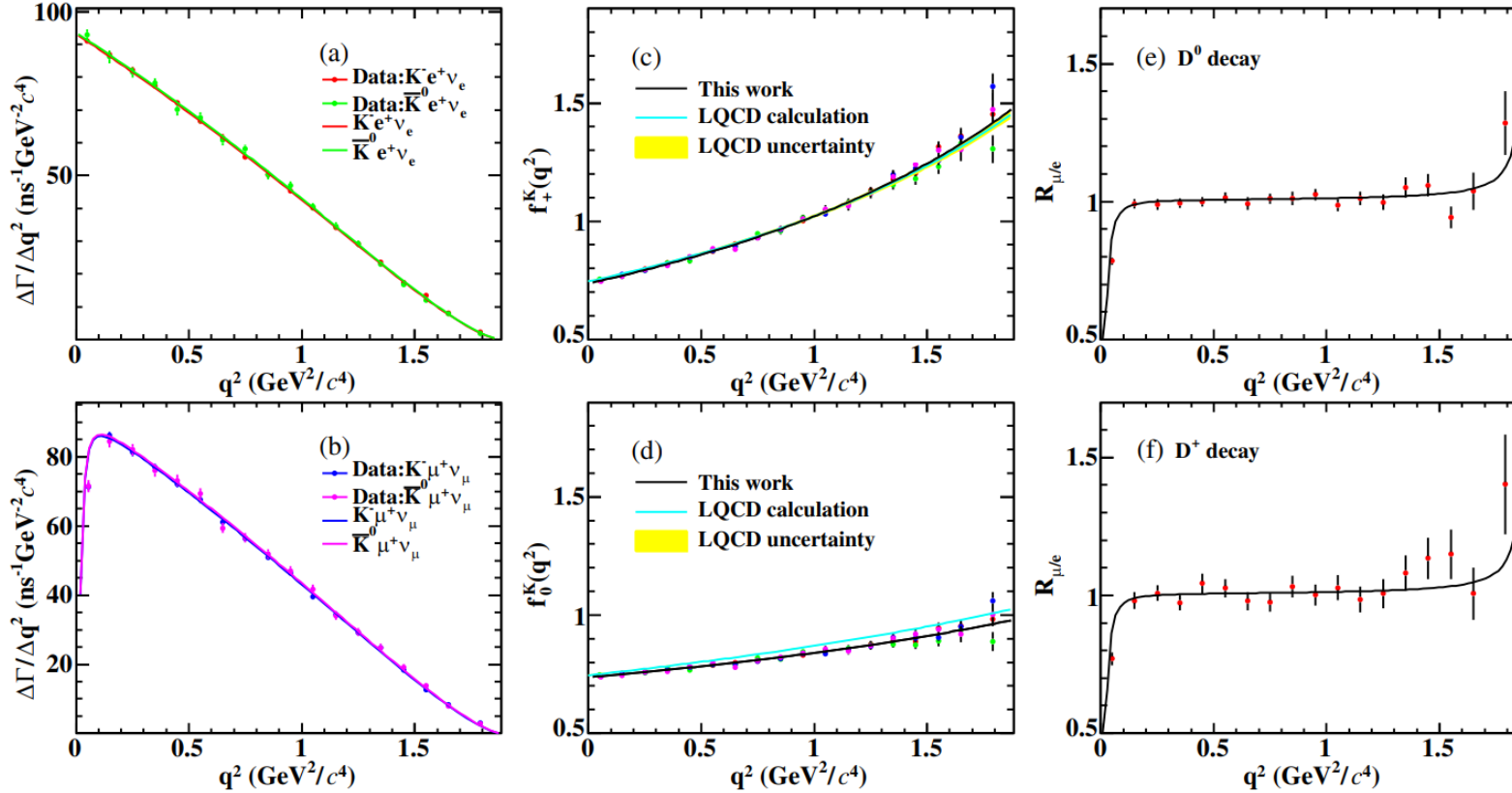
$$\frac{B(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)}{B(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 0.978 \pm 0.007 \pm 0.013$$

- Isospin test: **consistent with 1**

$$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 1.000 \pm 0.007 \pm 0.012$$

$$\frac{\Gamma(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)} = 0.993 \pm 0.008 \pm 0.012$$

Improved measurements of $D \rightarrow \bar{K} \ell^+ \nu_\ell$

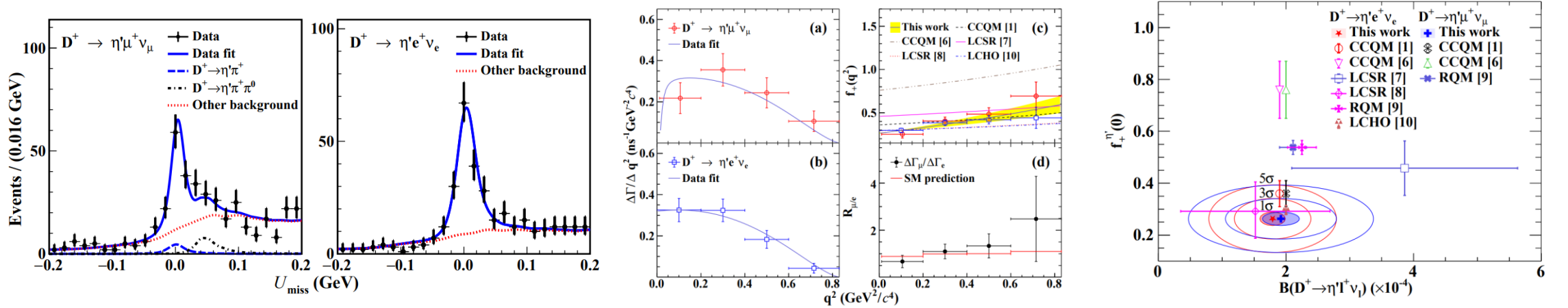


LCSR	Int. J. Mod. Phys. A 21, 6125 (2006)	0.661±0.067	
LFQM	J. Phys. G 39, 025005 (2012)	0.79±0.01	
CCQM	Front. Phys. 14, 64401 (2019)	0.78±0.12	
RQM	Phys.Rev.D 101, 013004 (2020)	0.716	
LQCD	Phys. Rev. D 96, 054514 (2017)	0.765±0.031	
LQCD	Phys.Rev.D 104, 034505 (2021)	0.7380±0.0044	
LQCD	Phys.Rev.D 107, 014510 (2023)	0.7441±0.0040	
LQCD	Phys.Rev.D 107, 094516 (2023)	0.7452±0.0031	
Belle	Phys.Rev.Lett. 97, 061804 (2006)	0.695±0.007±0.022	
BaBar	Phys.Rev.D 76, 052005 (2007)	0.727±0.007±0.009	
CLEO	Phys.Rev.D 80, 032005 (2009)	0.7365±0.0041±0.0041	
BESIII	Phys.Rev.D 92, 112008 (2015)	0.7478±0.0062±0.0113	
BESIII	Phys.Rev.D 96, 012002 (2017)	0.7245±0.0041±0.0115	
BESIII	Phys.Rev.Lett. 122, 011804 (2019)	0.7327±0.0039±0.0030	
BESIII	Phys.Rev.D 92, 072012 (2015)	0.7367±0.0026±0.0036	
This work	Simultaneous fit of $D \rightarrow \bar{K} \ell^+ \nu$	0.7366±0.0011±0.0013	

Simultaneous fit to $d\Gamma/dq^2$ to all four channels:

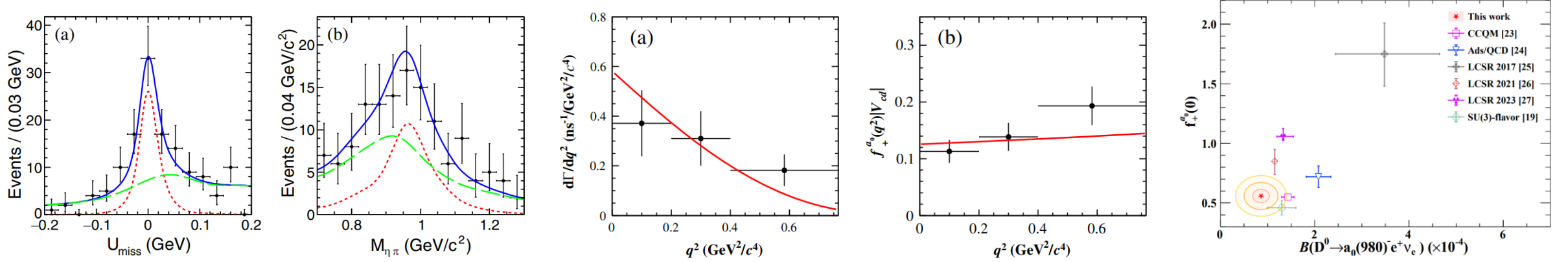
- $f_+^K(0) = 0.7366 \pm 0.0011_{stat.} \pm 0.0013_{syst.}$, precision 0.23%_{exp.}
- $|V_{cs}| = 0.9623 \pm 0.0015_{stat.} \pm 0.0017_{syst.} \pm 0.0040_{LQCD}$, precision 0.23%_{exp.} & 0.42%_{LQCD}

First study of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$ decay dynamics



- [Phys. Rev. Lett. 134, 111801 \(2025\)](#), based on 20.3 fb^{-1} data sample @3.773 GeV, $\sum N_{DT} \sim 240$
- First observation of $D^+ \rightarrow \eta' \mu^+ \nu_\mu$ decay with significance 8.6σ
- First extraction of FF of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$: $f_+^{\eta'}(0) = 0.263 \pm 0.025_{\text{stat.}} \pm 0.006_{\text{syst.}}$
- LFU test $R_{\mu/e}^\eta = 1.07 \pm 0.19_{\text{stat.}} \pm 0.03_{\text{syst.}}$, consistent with SM prediction.
- $\eta - \eta'$ mixing angle: $\cot^4 \phi_p = \frac{\Gamma(D_s^+ \rightarrow \eta' \ell^+ \nu_\ell)/\Gamma(D_s^+ \rightarrow \eta \ell^+ \nu_\ell)}{\Gamma(D^+ \rightarrow \eta' \ell^+ \nu_\ell)/\Gamma(D^+ \rightarrow \eta \ell^+ \nu_\ell)} \rightarrow \phi_p = (39.8 \pm 0.8 \pm 0.3)^\circ$

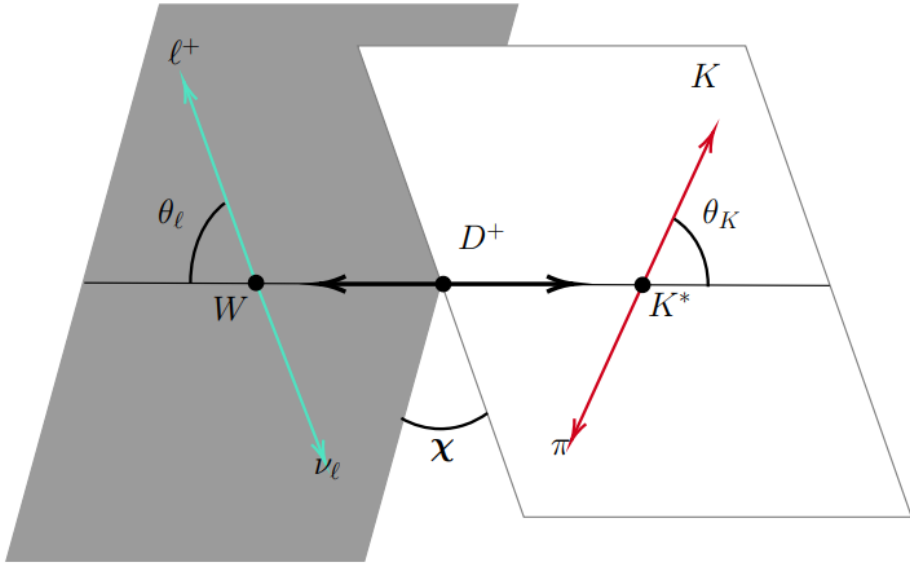
Updated measurement of $D^0 \rightarrow a_0(980)^- e^+ \nu_e$



- [Phys. Rev. D 111, L091501 \(2025\)](#), based on 7.93 fb^{-1} data sample @3.773 GeV, $N_{DT} \sim 50$
- $B(D^0 \rightarrow a_0(980)^- e^+ \nu_e) \times B(a_0(980)^- \rightarrow \eta\pi^-) = (0.86 \pm 0.17 \pm 0.05) \times 10^{-4}$
- **First extraction of the FF:** $f_+^{a_0(980)}(0) = 0.559 \pm 0.056 \pm 0.013$
- Pin down the nature of $a_0(980)$ by comparing with theoretical calculations

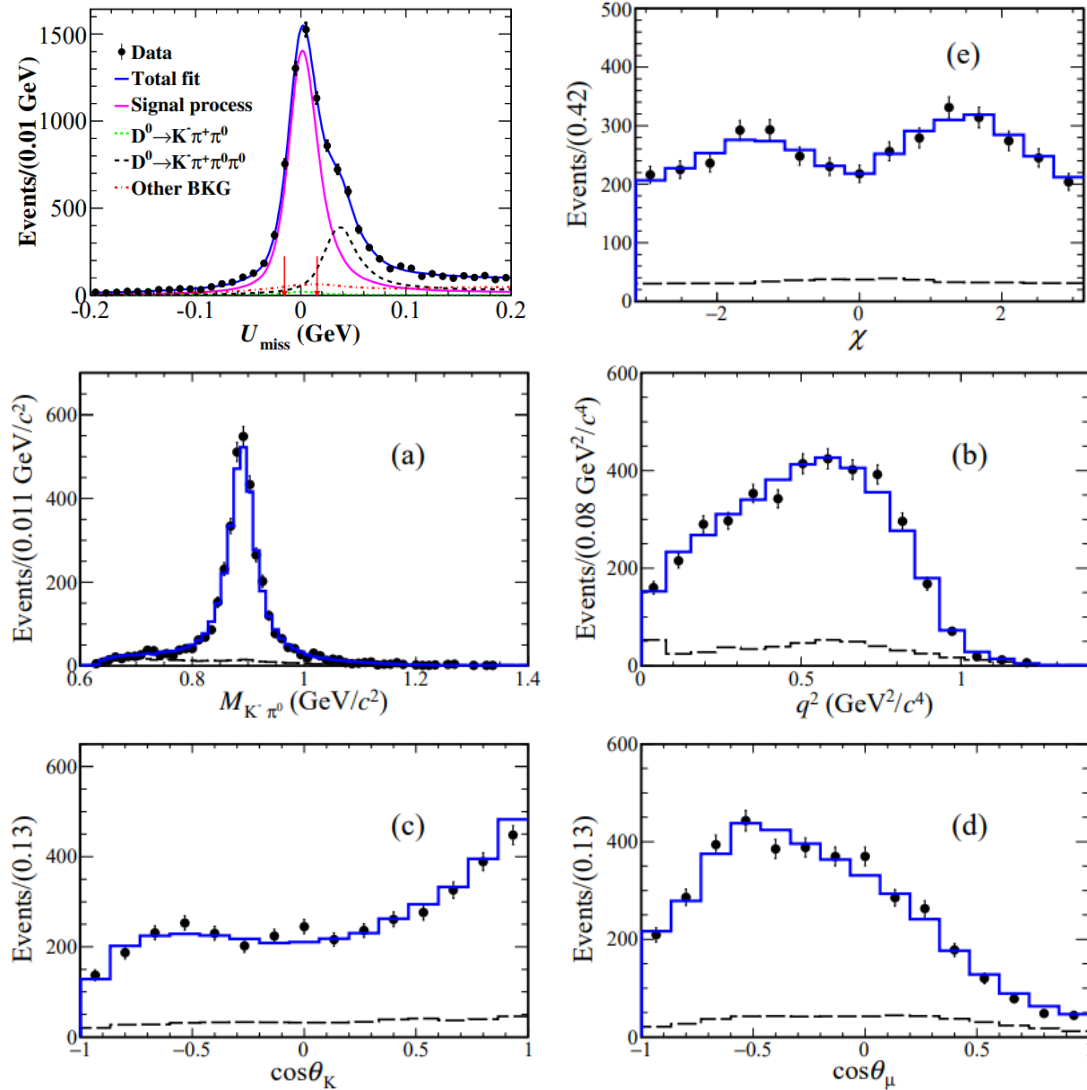
Decay formalism of $D \rightarrow V \ell^+ \nu_\ell, V \rightarrow P_1 P_2$

$$d^5\Gamma = \frac{G_F^2 |V_{cq}|^2}{(4\pi)^6 m_D^3} X \beta \beta_l I(S_{p_1 p_2}, q^2, \theta_K, \theta_l, \chi) dS_{p_1 p_2} dq^2 d\cos\theta_{p_1} d\cos\theta_l d\chi$$



- Formalism based on [Phys. Rev. D 46 5040 \(1992\)](#)
- Five kinematic variables: $S_{p_1 p_2}, q^2, \theta_K, \theta_l, \chi$
- Decay intensity: $I = \sum_1^9 I_i(\theta_K, q^2, S_{p_1 p_2}) \times f_i(\theta_l, \chi)$
- The detailed expressions of I_i are given in reference.
- Three FFs: $A_{1,2}(q^2)$ & $V(q^2) \rightarrow r_2 = \frac{A_2(0)}{A_1(0)}$ & $r_V = \frac{V(0)}{A_1(0)}$

An example: $D^0 \rightarrow K^- \pi^0 \mu^+ \nu_\mu$



- [PRL 134 011803 \(2025\)](#), based on 7.93 fb^{-1} data sample @3.773 GeV, $N_{DT} \sim 6.4 \text{ K}$
- FFs described with single pole model
- Component $K^*(892) + (K\pi)_{s\text{-wave}}$
- Stringent test of various theoretical works.

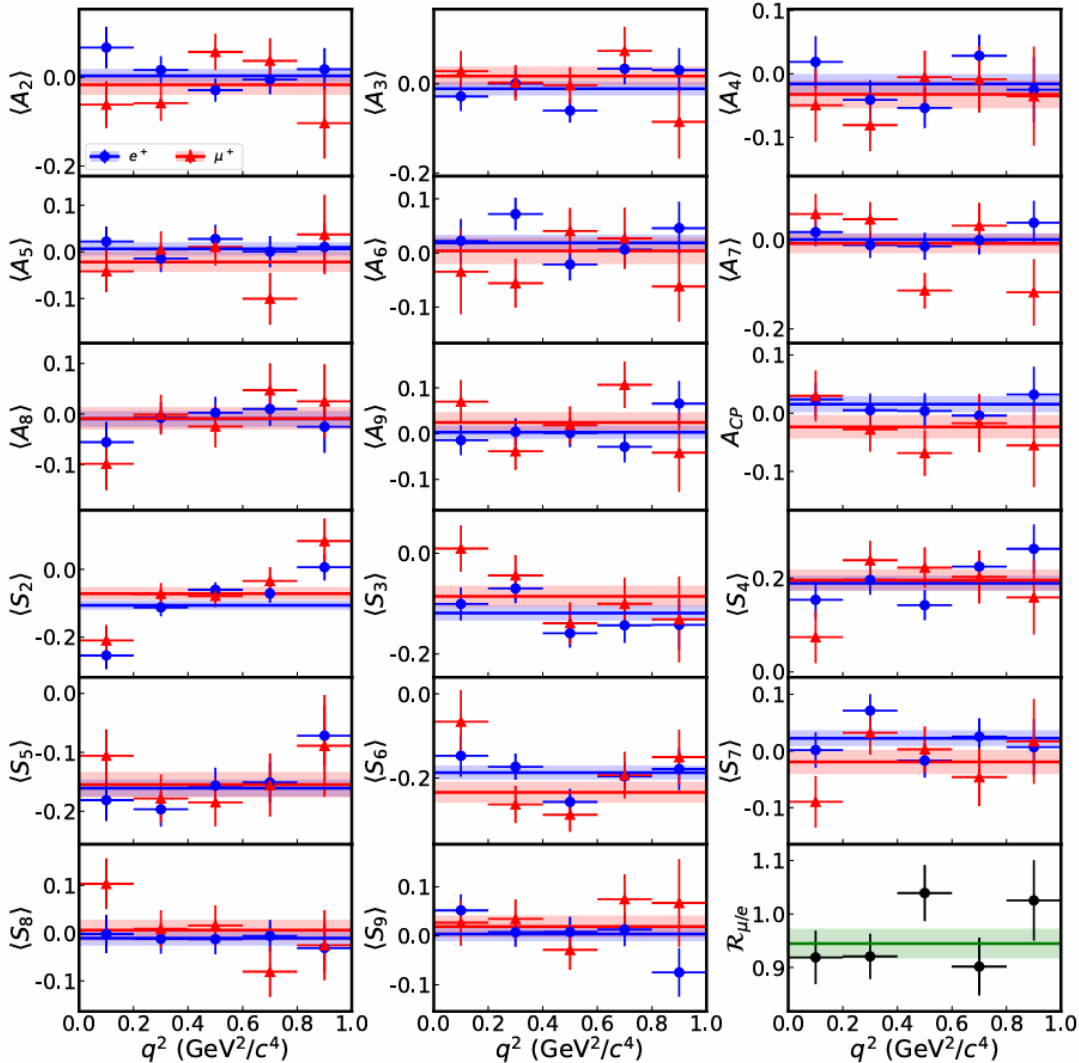
Theory	$\mathcal{B}(\%)$	r_V	r_2
LCSR [7, 16]	$2.01^{+0.09}_{-0.08}$	1.39	0.60
χ UA [17]	1.98	...	...
CCQM [6]	2.80	1.22 ± 0.24	0.92 ± 0.18
CQM [8, 18]	3.09	1.56	0.74
LFQM [9]	...	1.36	0.83
HM $_\chi$ T [10]	...	1.60	0.50
Experiments	$\mathcal{B}(\%)$	r_V	r_2
BESIII [39]	...	$1.46 \pm 0.07 \pm 0.02$	$0.67 \pm 0.06 \pm 0.01$
FOCUS [11]	1.89 ± 0.24	$1.71 \pm 0.68 \pm 0.34$	$0.91 \pm 0.37 \pm 0.10$
This work	$2.073 \pm 0.039 \pm 0.032$	$1.37 \pm 0.09 \pm 0.03$	$0.76 \pm 0.06 \pm 0.02$

The Collection of $D \rightarrow \bar{K}\pi\ell^+\nu_\ell$ works

Similar works of isospin channels are listed here.

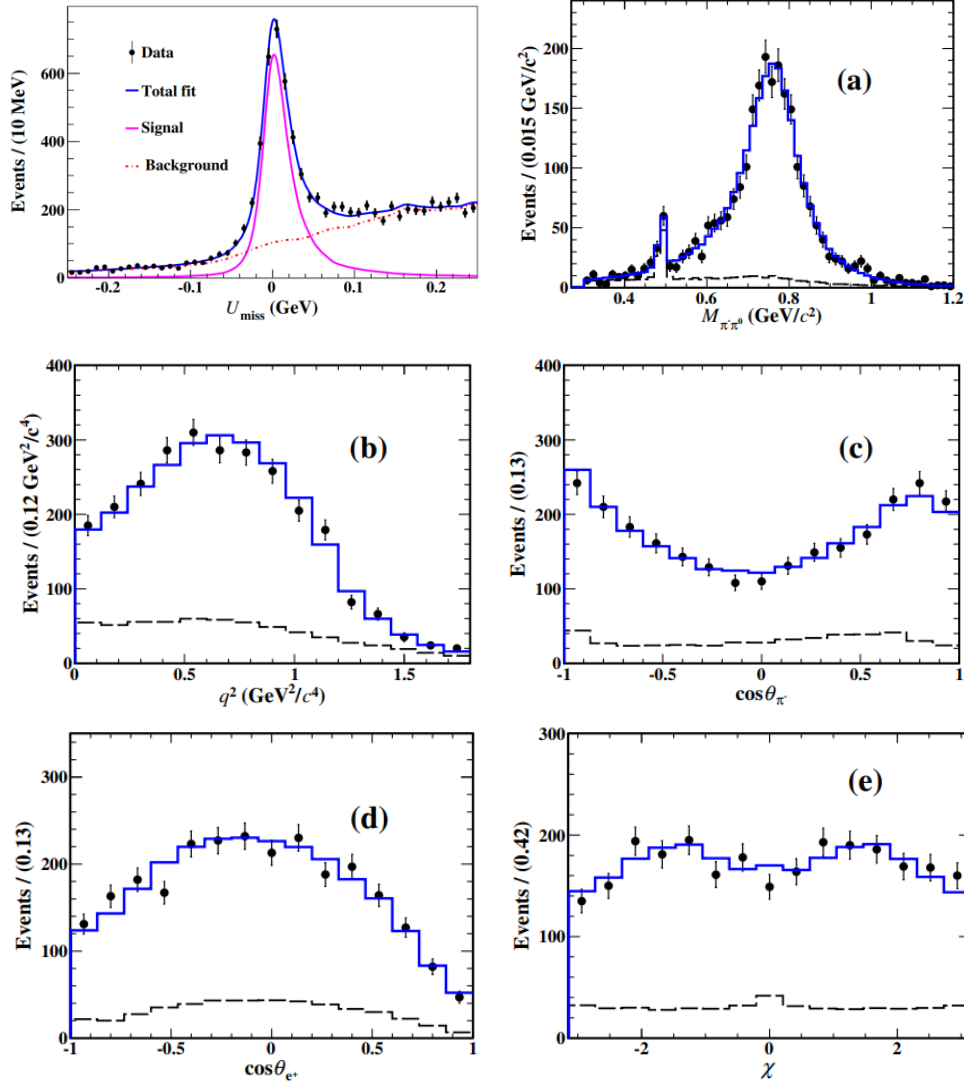
	$D^0 \rightarrow \bar{K}^0\pi^-e^+\nu_e$	$D^0 \rightarrow \bar{K}^0\pi^-\mu^+\nu_\mu$	$D^0 \rightarrow K^-\pi^0\mu^+\nu_\mu$	$D^+ \rightarrow \bar{K}^0\pi^0\ell^+\nu_\ell$
Ref	JHEP 03 197 (2025)	arXiv:2504.10867	PRL 134 011803 (2025)	arXiv:2506.05761
Data Set (fb^{-1})	7.93	7.93	7.93	20.3
$B(D \rightarrow \bar{K}\pi\ell^+\nu_\ell)$ (%)	$1.444 \pm 0.022 \pm 0.024$	$1.373 \pm 0.020 \pm 0.023$	$0.773 \pm 0.014 \pm 0.012$	$\mu: 0.896 \pm 0.017 \pm 0.008$ $e: 0.943 \pm 0.012 \pm 0.010$
$B(D \rightarrow \bar{K}^*\ell^+\nu_\ell)$ (%)	$2.039 \pm 0.032 \pm 0.034$	$1.948 \pm 0.033 \pm 0.036$	$2.073 \pm 0.039 \pm 0.032$	$\mu: 4.99 \pm 0.10 \pm 0.05$ $e: 5.29 \pm 0.07 \pm 0.06$
r_V	$1.48 \pm 0.05 \pm 0.02$	$1.46 \pm 0.11 \pm 0.04$	$1.37 \pm 0.09 \pm 0.03$	$1.42 \pm 0.03 \pm 0.02$
r_2	$0.70 \pm 0.04 \pm 0.02$	$0.71 \pm 0.08 \pm 0.03$	$0.76 \pm 0.06 \pm 0.02$	$0.75 \pm 0.03 \pm 0.01$
N_{obs} (K)	8.7	6.8	6.4	17.9
$R_{\mu/e}$ of $K^*/K\pi$	$0.96 \pm 0.02 \pm 0.02$		$1.02 \pm 0.03 \pm 0.03$	$0.94 \pm 0.02 \pm 0.01$

Investigation of Angular info in $D \rightarrow \bar{K}\pi\ell^+\nu_\ell$



- NP contributions may result CPV or LFV in $D \rightarrow \bar{K}\pi\ell^+\nu_\ell$
- LFV can be test via: integrated and q^2 -binned $R_{\mu/e}$
- CPV can be test via: A_{cp} and a full set of angular observables $\langle A_i \rangle$ & $\langle S_i \rangle$
- In SM model, all $\langle A_i \rangle$ & A_{cp} & $\langle S_{6,7,8} \rangle$ are zero.
- In [arXiv:2506.05761](https://arxiv.org/abs/2506.05761), all these variables are measured, and no deviation from SM is seen.

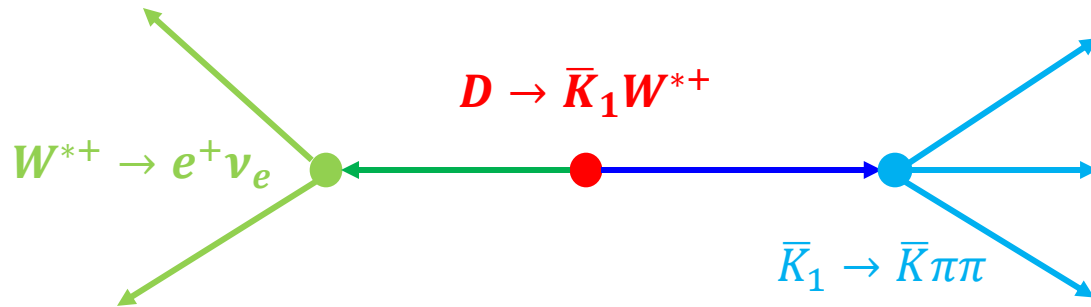
Updated measurement of $D^0 \rightarrow \rho^- e^+ \nu_e$



- [PRD 110, 112018\(2024\)](#), based on 7.93 fb^{-1} data sample @3.773 GeV, $N_{DT} \sim 3.3$ K
- $B(D^0 \rightarrow \rho^- e^+ \nu_e) = (1.439 \pm 0.033 \pm 0.027) \times 10^{-3}$
- The only component is $\rho(770)$
- $r_V = 1.548 \pm 0.079 \pm 0.041$, $r_2 = 0.823 \pm 0.056 \pm 0.026$, improved by a factor 1.6.

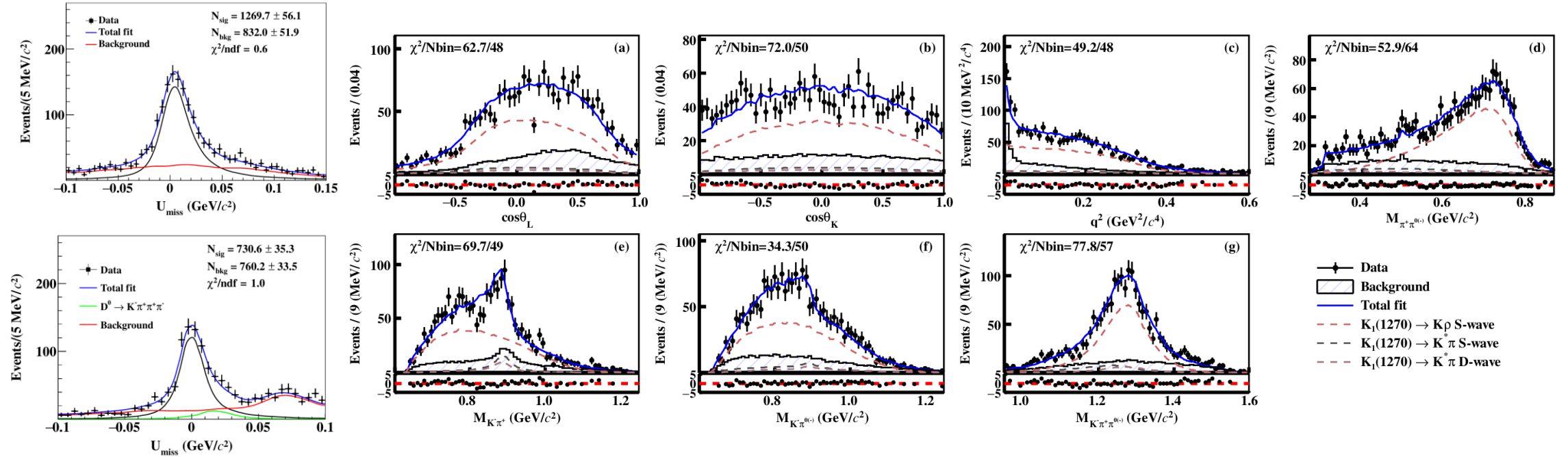
Decay formalism of $D \rightarrow Ae^+ \nu_e, A \rightarrow P_1 P_2 P_3$

$$M = (V - A)^{\mu\eta} \cdot \left[\sum_{\lambda_{W^*}} \epsilon^*(\lambda_{W^*})_\mu \epsilon(\lambda_{W^*})_\rho \right] \cdot \left[\sum_{\lambda_{\bar{K}_1}} \epsilon^*(\lambda_{\bar{K}_1})_\eta \epsilon(\lambda_{\bar{K}_1})_\sigma \right] \cdot R_{\bar{K}_1} \cdot J^\sigma \cdot [\bar{u}_\nu \gamma^\rho (1 - \gamma_5) \nu_l]$$



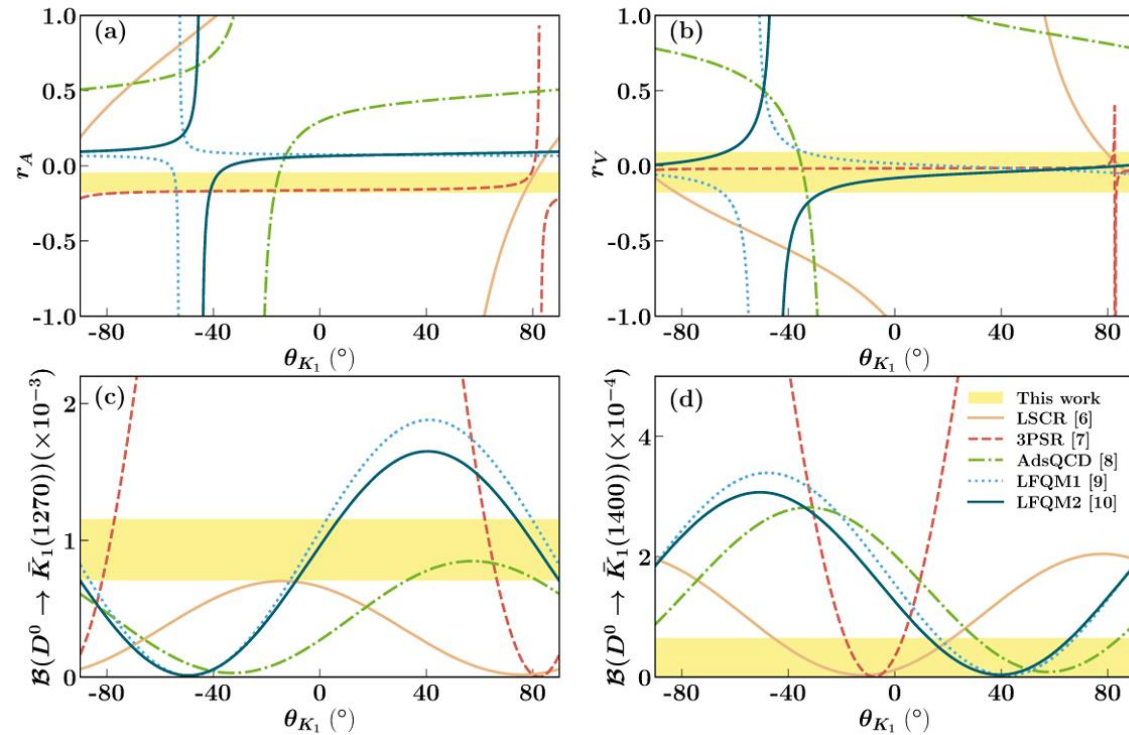
- More independent kinematic variables of **five body** semi-leptonic decay $\rightarrow$ general formalism is required!
- $D \rightarrow \bar{K}_1 W^{*+}$: $\langle \bar{K}_1 | s \gamma_\mu (1 - \gamma_5) | D \rangle$, cited from [PRD 104, 053003 \(2021\)](#) $\rightarrow V_{1,2}$ & $A \rightarrow r_A = \frac{A(0)}{V_1(0)}$ & $r_V = \frac{V_2(0)}{V_1(0)}$
- $\bar{K}_1 \rightarrow \bar{K} \pi \pi$: Constructed in covariant tensor formalism, following [Eur. Phys. J. A 16, 537\(2003\)](#)
- $m_e \rightarrow 0$: $q^\mu [\bar{u}_\nu \gamma_\mu (1 - \gamma_5) \nu_l] = 0$ is used.

First study of $D^{0(+)} \rightarrow K^- \pi^+ \pi^0(-) e^+ \nu_e$



- [arXiv:2503.02196](https://arxiv.org/abs/2503.02196), based on 20.3 fb^{-1} data sample @3.773 GeV, $\sum N_{DT} \sim 2.0 \text{ K}$
- Improve BFs measurement of $D \rightarrow \bar{K}_1(1270)e^+\nu_e$ & **First upper limit on $D \rightarrow \bar{K}_1(1400)e^+\nu_e$**
 $B(D^+ \rightarrow \bar{K}_1^0(1270)e^+\nu_e) = (2.27 \pm 0.11 \pm 0.07 \pm 0.07) \times 10^{-3}$; $B(D^+ \rightarrow \bar{K}_1^0(1400)e^+\nu_e) < 1.4 \times 10^{-4}$
 $B(D^0 \rightarrow K_1^-(1270)e^+\nu_e) = (1.02 \pm 0.06 \pm 0.06 \pm 0.03) \times 10^{-3}$; $B(D^0 \rightarrow K_1^-(1400)e^+\nu_e) < 0.7 \times 10^{-4}$
- **First FFs measurement:** $r_A = (-11.2 \pm 1.0 \pm 0.9) \times 10^{-2}$ & $r_V = (-4.3 \pm 1.0 \pm 2.5) \times 10^{-2}$
- Component: **$K\rho(770)$ & $K^*(892)\pi$** $\rightarrow B(K_1(1270) \rightarrow K^*\pi)/B(K_1(1270) \rightarrow K\rho) = (20.3 \pm 2.1 \pm 8.7)\%$

First study of $D^{0(+)} \rightarrow K^- \pi^+ \pi^{0(-)} e^+ \nu_e$



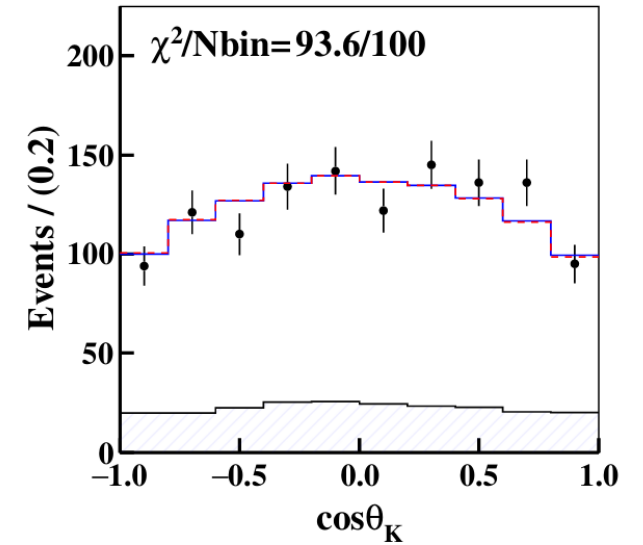
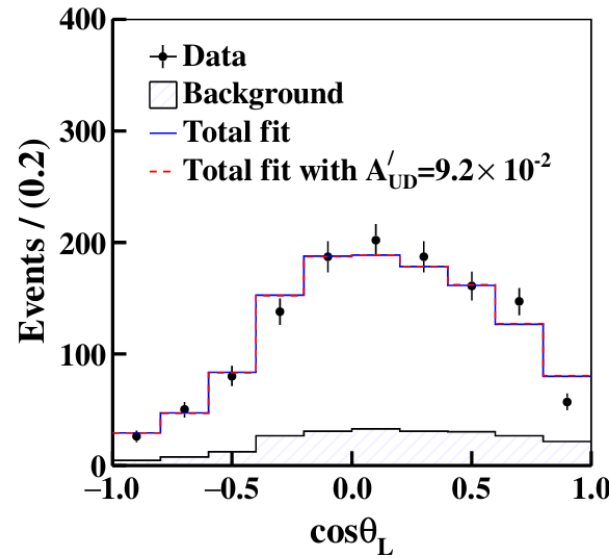
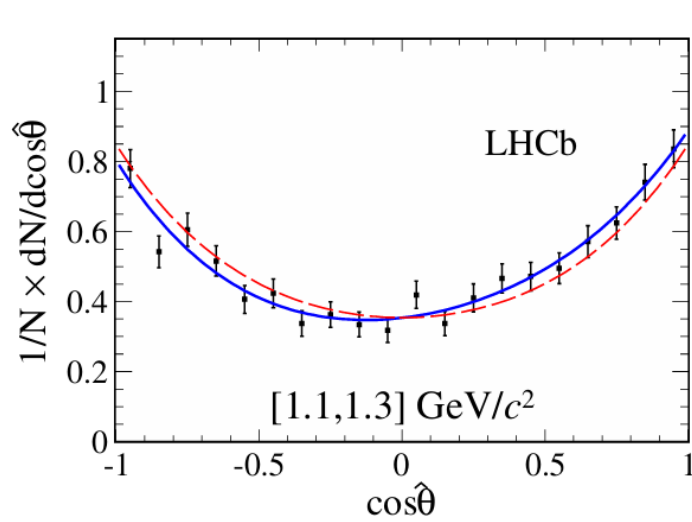
- K_{1A} (1P_1) & K_{1B} (3P_1) mix into $K_1(1270)$ & $K_1(1400)$
- FFs are sensitive to the mixing angle θ_{K_1} :

$$f_{K_1(1270)} = f_{K_{1A}} \sin \theta_{K_1} + f_{K_{1B}} \cos \theta_{K_1}$$

$$f_{K_1(1400)} = f_{K_{1A}} \cos \theta_{K_1} - f_{K_{1B}} \sin \theta_{K_1}$$

- Three unknown pars. ($f_{K_{1A}}, f_{K_{1B}}, \theta_{K_1}$) & Two equations
→ Determine θ_{K_1} requires one parameter input!
- However, for all theoretical predictions, we have **four observables to give stringent test** on them without assuming the value of θ_{K_1} .

First study of $D^{0(+)} \rightarrow K^- \pi^+ \pi^{0(-)} e^+ \nu_e$

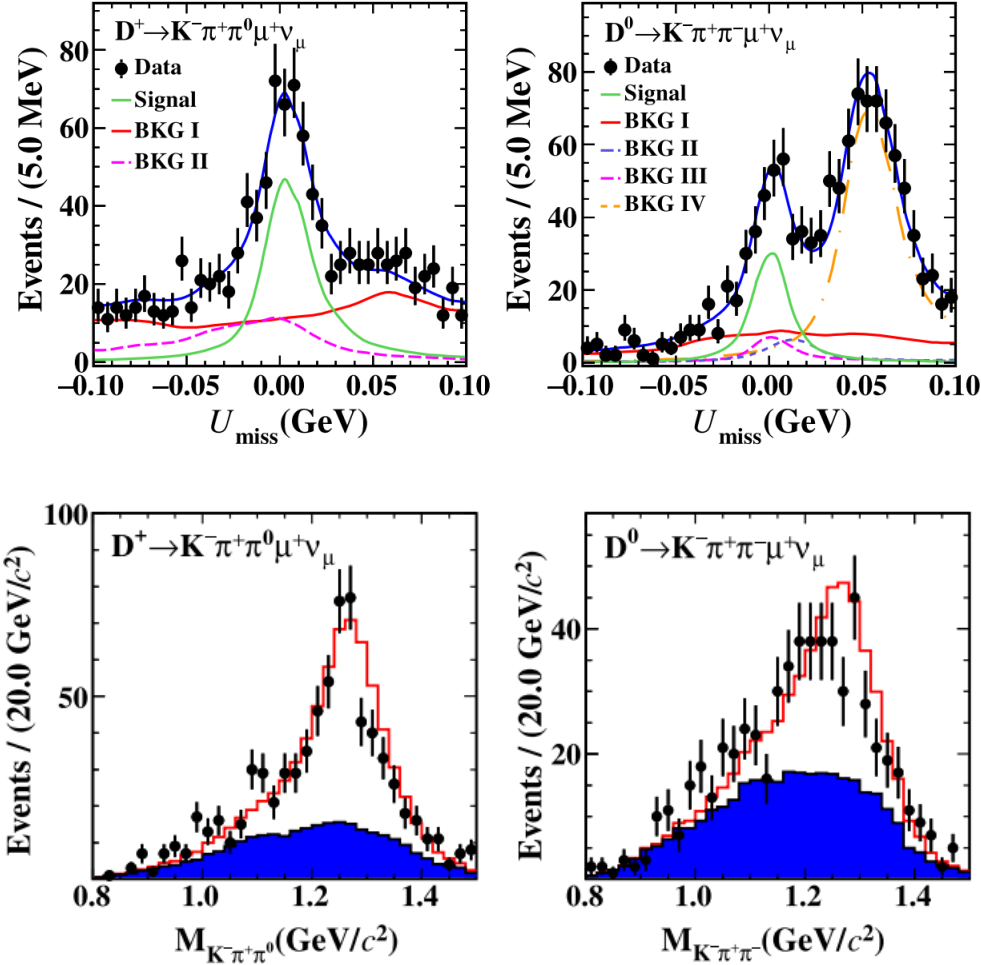


- $\bar{b} \rightarrow \bar{s} \gamma$: polarization of photon $\lambda_\gamma \sim +1$, any deviation indicates NP effects
- LHCb observed photon polarization in $B^+ \rightarrow K_1^+(1270)(\rightarrow K\pi\pi)\gamma$ with up-down asymmetry

$$A_{ud} = f_h \lambda_\gamma = (6.9 \pm 1.7) \times 10^{-2}$$

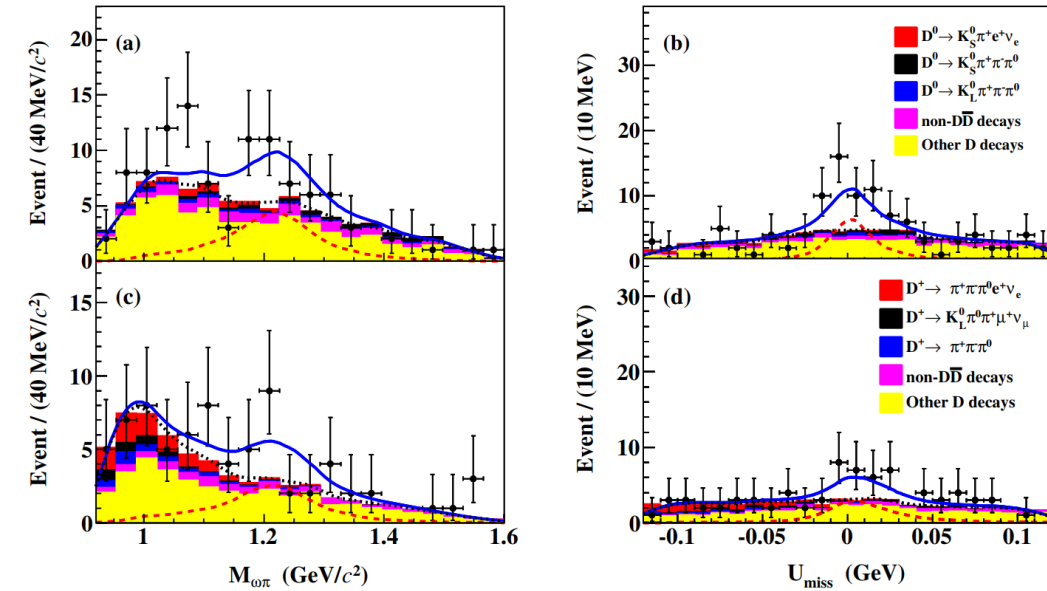
- Theoretical calculation of f_h suffers from limited knowledge of current J^μ in $K_1 \rightarrow K\pi\pi$.
- [PRL 125 051802 \(2020\)](#) suggests up-down asymmetry in $D \rightarrow K_1(1270)e^+\nu_e$: $A'_{ud} = \frac{4}{3} f_h$
- 2D Angular fit $\rightarrow A'_{ud} = 0.01 \pm 0.11$, consistent with SM prediction $\frac{4}{3} A_{ud} = (0.092 \pm 0.022)$

Observation of $D \rightarrow \bar{K}_1(1270)\mu^+\nu_\mu$



- [PRD 111, L071101 \(2025\)](#), based on 7.93 fb^{-1} data sample @3.773 GeV, $N_{DT} \sim 0.6 \text{ K}$
- $B(D^+ \rightarrow \bar{K}_1^0(1270)\mu^+\nu_\mu) = (2.36 \pm 0.20_{-0.27}^{+0.18} \pm 0.48) \times 10^{-3}$,
 $B(D^0 \rightarrow K_1^-(1270)\mu^+\nu_\mu) = (0.78 \pm 0.11_{-0.09}^{+0.05} \pm 0.15) \times 10^{-3}$
- LFU test: $R_{D^0} = 0.74 \pm 0.13_{-0.13}^{+0.08}$, $R_{D^+} = 1.03 \pm 0.14_{-0.15}^{+0.11}$
- Isospin test: $1.22 \pm 0.10_{-0.09}^{+0.06}$

Observation of $D \rightarrow b_1(1235)e^+\nu_e$



- [arXiv:2407.20551](https://arxiv.org/abs/2407.20551), based on 7.93 fb^{-1} data sample @3.773 GeV, $N_{DT} \sim 60$
- First observation of $D \rightarrow b_1(1235)e^+\nu_e$
- $B(D^0 \rightarrow b_1(1235)^- e^+ \nu_e) \times B(b_1(1235)^- \rightarrow \omega \pi^-) = (0.72 \pm 0.18^{+0.06}_{-0.08}) \times 10^{-4}$
- $B(D^+ \rightarrow b_1(1235)^0 e^+ \nu_e) \times B(b_1(1235)^0 \rightarrow \omega \pi^0) = (1.16 \pm 0.44 \pm 0.16) \times 10^{-4}$

Outlook of $D \rightarrow \bar{K} \ell^+ \nu_\ell$: Angular info. & BSM search

- With 20.3 fb^{-1} @ 3.773 GeV: $\sum N_{DT}$: 0.44 M $\rightarrow$ **1.12 M**

- Forward-backward asymmetry measurement:

$$A_{FB}(q^2) = \frac{d\Gamma(\cos \theta_W > 0) - d\Gamma(\cos \theta_W < 0)}{d\Gamma(\cos \theta_W > 0) + d\Gamma(\cos \theta_W < 0)}$$

- BSM search: including BSM operators,

$$(\bar{s} \gamma_\mu P_L c)(\bar{\nu}_\ell \gamma^\mu P_L \ell) + (\bar{s} [\mathbf{C}_R P_R + \mathbf{C}_L P_L] c)(\bar{\nu}_\ell P_R \ell)$$

$D \rightarrow \bar{K} \ell^+ \nu_\ell$: Combined fit to $d\Gamma/dq^2$ & $A_{FB}(q^2) \rightarrow C_S = C_R + C_L$

$D_S \rightarrow \ell^+ \nu_\ell$: Compare measured and LQCD calculated BF $\rightarrow C_P = C_R - C_L$

$\rightarrow$ **Most stringent constrain on scalar current in charm sector!**

Outlook of $D \rightarrow \bar{K}\pi\ell^+\nu_\ell$: Precision & New

- The expected signal yields of all channels: > 0.3 M
- Search for **more excited kaon** in $D \rightarrow K_l^*(1410,1430,1680)\ell^+\nu_\ell$
- **Combined fit for more precise r_A & r_V** , currently is still statistical uncertainty dominated
- Measure **$r_{A,V}(q^2)$ in different q^2 region** $\rightarrow$ Model independent extraction
- Search for **NP contributions** via massive angular observables
- **Extraction of $|V_{cs}|$** : Limited by theoretical uncertainty...

Summary & Outlook

$$M_{fi} = \frac{G_F}{\sqrt{2}} V_{cq} \times \langle P, S, V, A | q \gamma_\mu (1 - \gamma_5) c | D \rangle \times \bar{u}_\nu \gamma^\mu (1 - \gamma_5) \nu_{\ell^+}$$

- **$|V_{cq}|$ related:** Unprecedented precision $\sim 0.23\%$ of $f_+^K \cdot |V_{cs}|$ has been achieved in $D \rightarrow K \ell^+ \nu_\ell$ measurement
- **FFs related:** precise measurements of FFs in $D \rightarrow (K, K^*, \rho) \ell^+ \nu_\ell$, first measurements of FFs in $D \rightarrow (\eta', a_0(980), K_1(1270)) \ell^+ \nu_\ell$
- **BFs related:** Observation of $D \rightarrow K_1(1270) \mu^+ \nu_\mu, b_1(1235) e^+ \nu_e$, upper limit of $D \rightarrow K_1(1400) e^+ \nu_e$
- **NP related:** LFU test, Angular/CPV observable in $D \rightarrow K \pi \ell^+ \nu_\ell$, up-down asymmetry in $D \rightarrow K_1(1270) e^+ \nu_e$
- **Outlook:** More Precise & More decay modes & Search for NP with 20.3 fb^{-1} data!