

Nuclear physics across energy scales

Imaging shapes of atomic nuclei from large to small via flow measurement

Chunjian Zhang

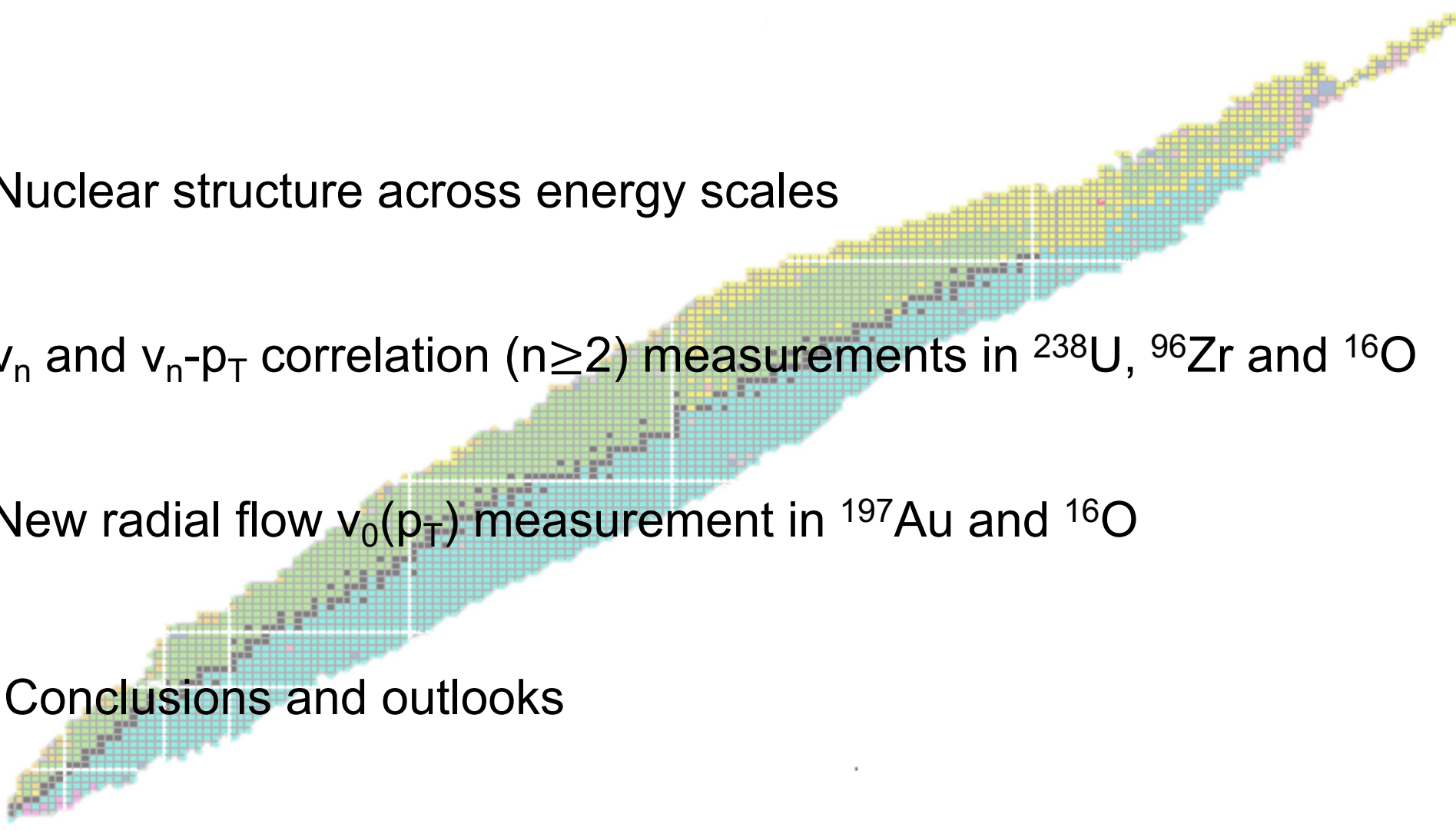
Fudan University

September 18-21, 2025, Wuhan



Central China
Center for Nuclear Theory
华中核理论中心

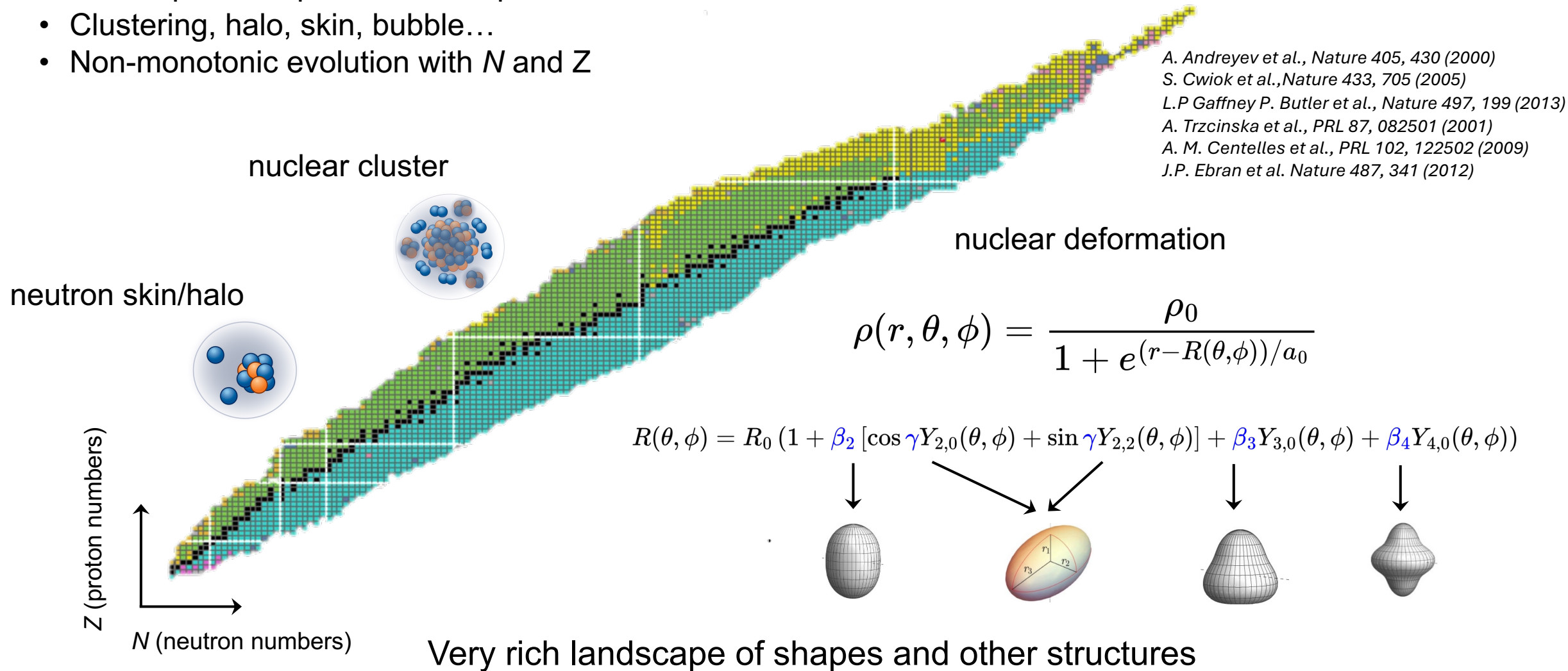
Outline

- 
- I. Nuclear structure across energy scales
 - II. v_n and v_n - p_T correlation ($n \geq 2$) measurements in ^{238}U , ^{96}Zr and ^{16}O
 - III. New radial flow $v_0(p_T)$ measurement in ^{197}Au and ^{16}O
 - IV. Conclusions and outlooks

Shape of atomic nuclei

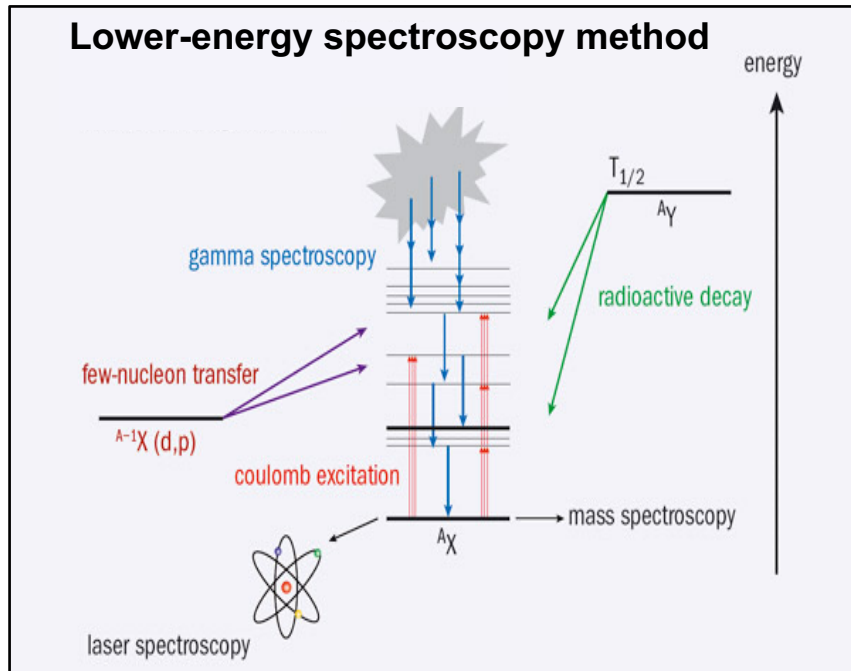
Emergent phenomena of the many-body quantum system, govern by short-range strong nuclear force

- Quadrupole/octupole/hexadecapole deformations
- Clustering, halo, skin, bubble...
- Non-monotonic evolution with N and Z



A. Andreyev et al., *Nature* 405, 430 (2000)
 S. Cwiok et al., *Nature* 433, 705 (2005)
 L.P Gaffney P. Butler et al., *Nature* 497, 199 (2013)
 A. Trzcinska et al., *PRL* 87, 082501 (2001)
 A. M. Centelles et al., *PRL* 102, 122502 (2009)
 J.P. Ebran et al. *Nature* 487, 341 (2012)

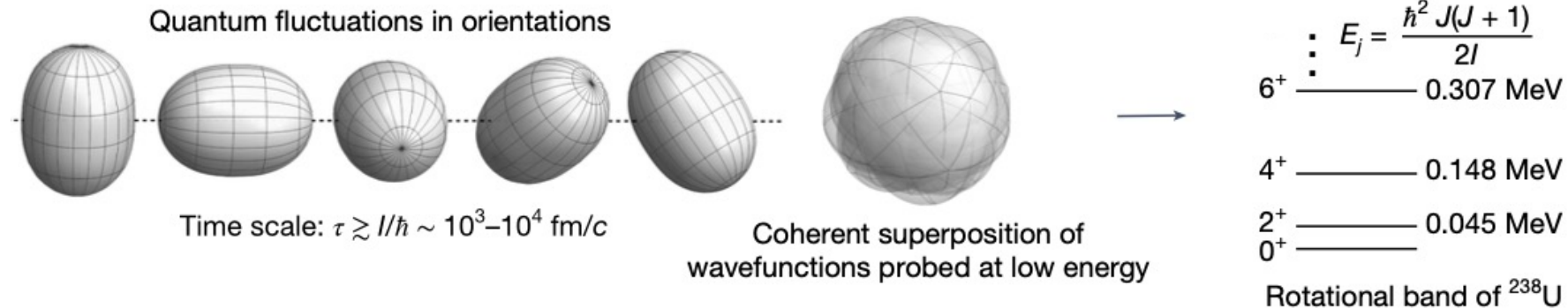
Nuclear shape at low energy: long exposure



Traditional imaging method taken before destruction

- Low energy spectroscopic methods probe a superposition of these fluctuations.
- Instantaneous shapes not directly seen, but inferred from model comparison.

Each DOF has zero-point fluctuations within certain timescales.



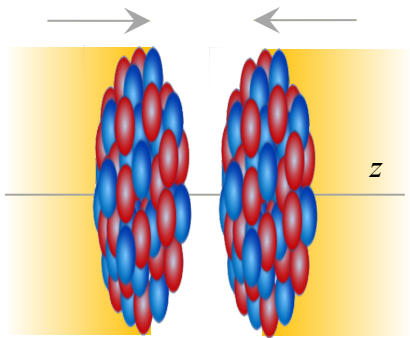
Imaging by smashing method

Take a snapshot

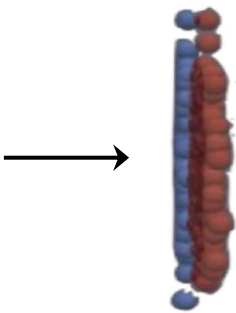
Evolution

Measurement

Nuclei collisions



$$T_{\mu\nu}(\tau = 0)$$

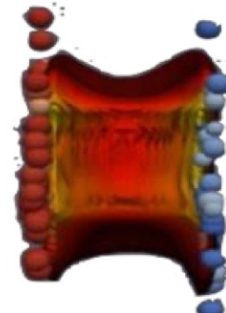


$$\tau \sim 2R_0/\Gamma \sim 0.1\text{fm}/c$$

exposure

Pressure-driven expansion of
Quark-gluon plasma (QGP)

$$\partial_\mu T^{\mu\nu} = 0, \text{ EOS, viscosity...}$$

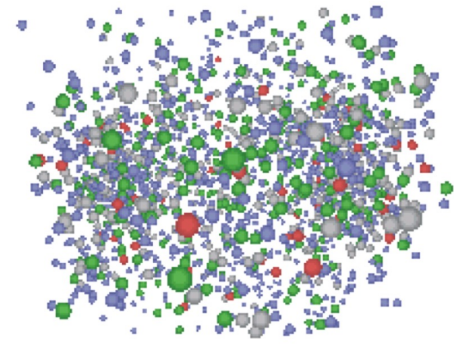


$$\tau \sim 10\text{fm}/c$$

expansion

free-streaming

$$T_{\mu\nu}(\tau = \infty)$$



$$\tau \sim 10^{15}\text{fm}/c$$

detection

$$\rho(r, \theta, \phi) = \frac{\rho_0}{1 + e^{(r-R(\theta, \phi))/a_0}}$$

$\beta_2 \rightarrow$ quadrupole deformation

$\beta_3 \rightarrow$ octupole deformation

$\gamma \rightarrow$ triaxiality

$a_0 \rightarrow$ surface diffuseness

$R_0 \rightarrow$ nuclear size

ab initio theory/shell model/DFT

J. Jia et al., Nucl. Sci. Tech 35, 220 (2024)

Imaging by smashing method

Take a snapshot

Evolution

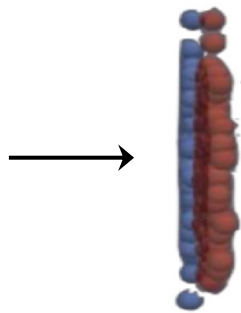
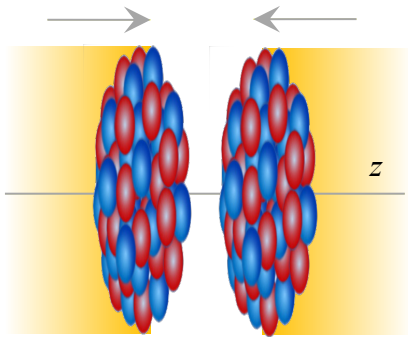
Measurement

Nuclei collisions

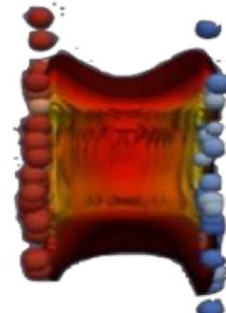
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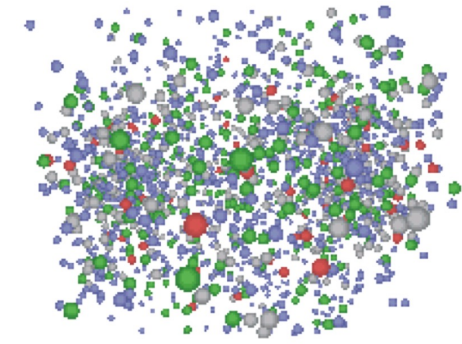
$$T_{\mu\nu}(\tau = \infty)$$



Pressure-driven expansion of
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$\tau \sim 2R_0/\Gamma \sim 0.1\text{fm}/c$
exposure

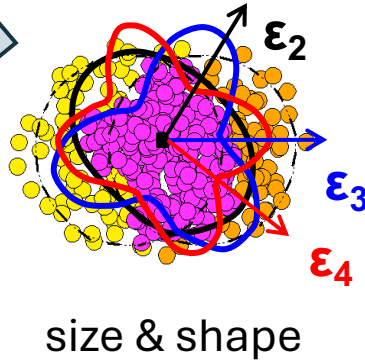
$\tau \sim 10\text{fm}/c$
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- $\beta_2 \rightarrow$ quadrupole deformation
- $\beta_3 \rightarrow$ octupole deformation
- $\gamma \rightarrow$ triaxiality
- $a_0 \rightarrow$ surface diffuseness
- $R_0 \rightarrow$ nuclear size

ab initio theory/shell model/DFT



size & shape

J. Jia et al., Nucl. Sci. Tech 35, 220 (2024)

$$R_\perp^2 \propto \langle r_\perp^2 \rangle \quad \mathcal{E}_n \propto \langle r_\perp^n e^{in\phi} \rangle$$

$$R_0 \quad a_0 \quad \beta_n$$

$$\text{Observables } \frac{d^2 N}{d\phi dp_T} = N(p_T) \left(\sum_n V_n e^{-in\phi} \right)$$

Event-by-event linear responses:

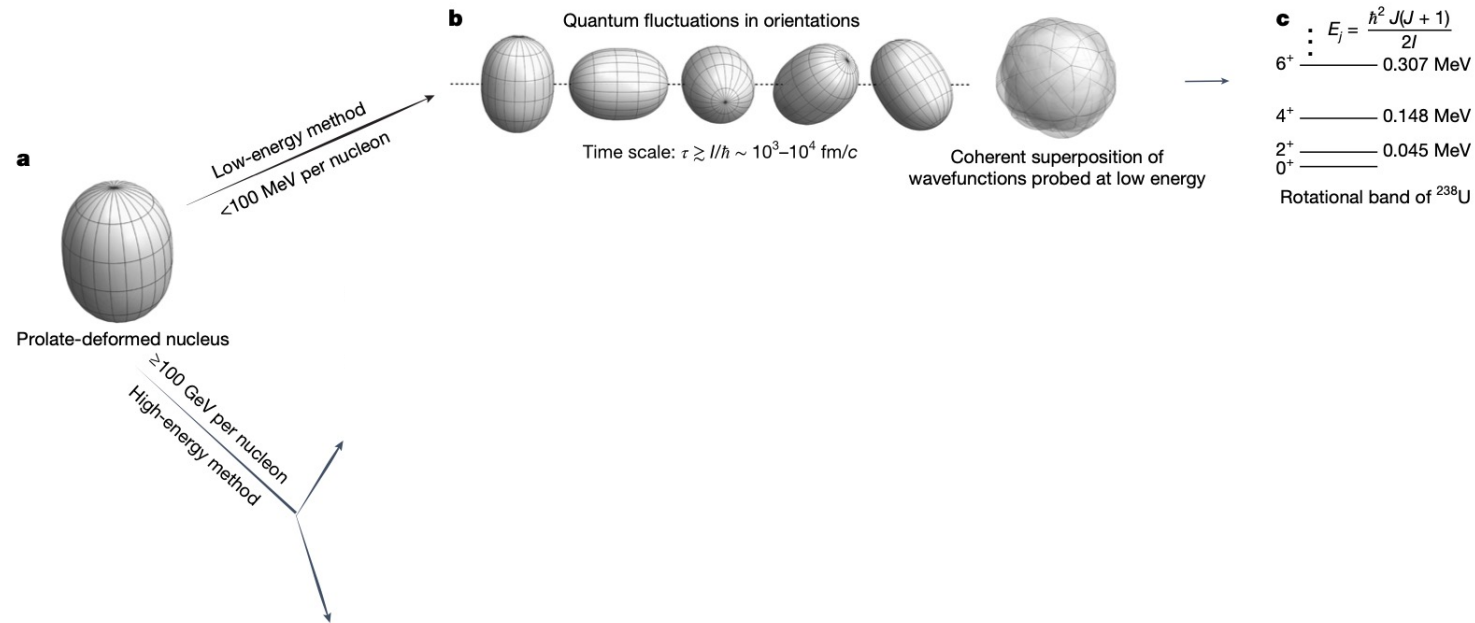
$$\frac{\delta[p_T]}{[p_T]} \propto -\frac{\delta R_\perp}{R_\perp} \quad V_n \propto \mathcal{E}_n$$

G. Giacalone et al., PRC 103, 024909 (2021); H. Niemi et al., PRC 87, 054901 (2013)

Key: 1) fast snapshot, 2) linear response, 3) large multiplicity for many-body correlation

Imaging nuclear shape in high-energy snapshot

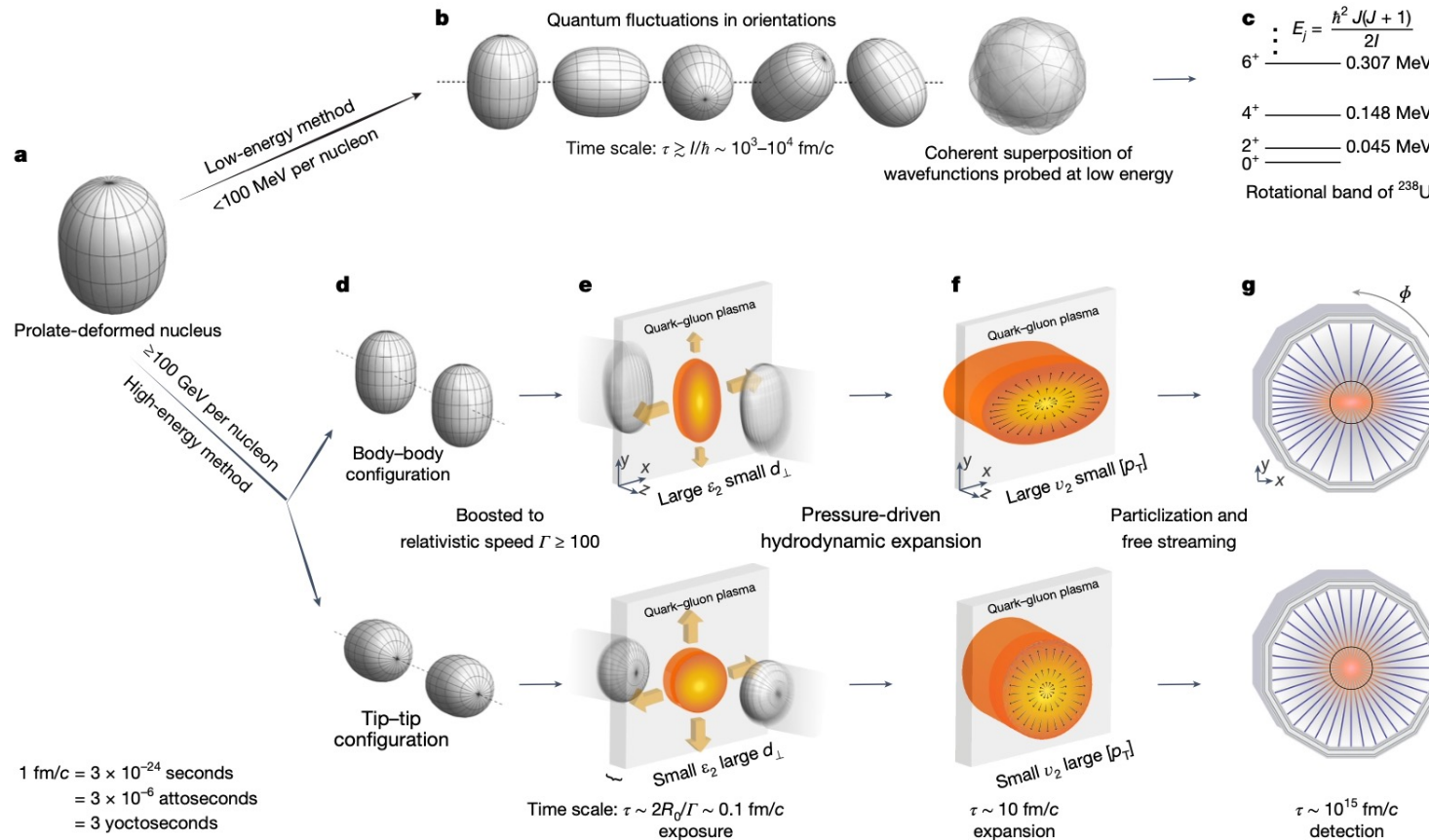
- Nuclear shape in intrinsic (body-fixed) frame not directly visible in the lab frame
--Mainly inferred from non-invasive spectroscopy methods.



$1 \text{ fm/c} = 3 \times 10^{-24} \text{ seconds}$
 $= 3 \times 10^{-6} \text{ attoseconds}$
 $= 3 \text{ yoctoseconds}$

Imaging nuclear shape in high-energy snapshot

- Nuclear shape in intrinsic (body-fixed) frame not directly visible in the lab frame
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STAR, *Nature* 635, 67-72 (2024)

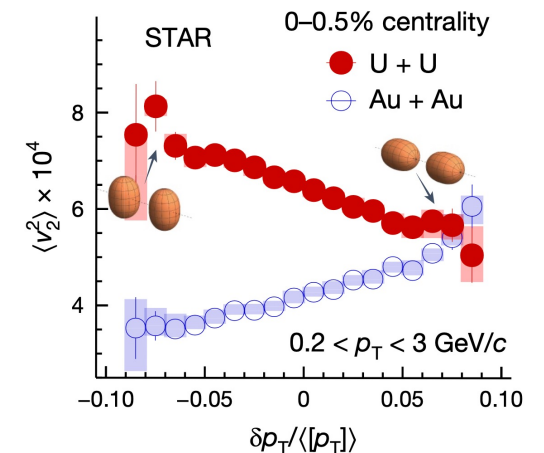
<https://www.nature.com/articles/s41586-024-08097-2>

Body-body: large-eccentricity large-size

$v_2 \nearrow$ $p_T \searrow$

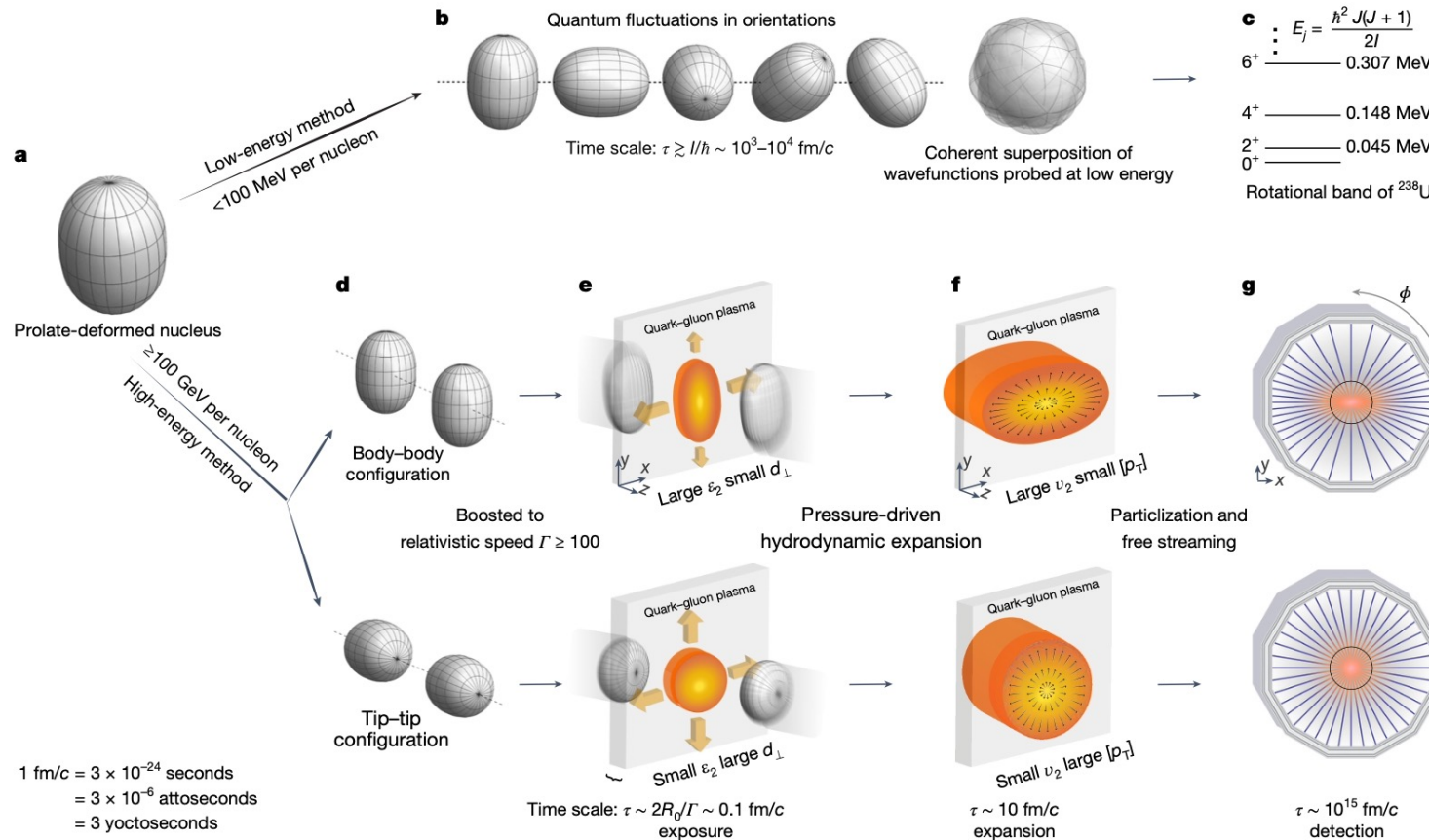
Tip-tip : small-eccentricity small-size

$v_2 \searrow$ $p_T \nearrow$



Imaging nuclear shape in high-energy snapshot

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--Mainly inferred from non-invasive spectroscopy methods.



STAR, *Nature* 635, 67-72 (2024)
<https://www.nature.com/articles/s41586-024-08097-2>

across energy scales

Body-body: large-eccentricity large-size

$v_2 \nearrow$ $p_T \searrow$

Tip-tip : small-eccentricity small-size

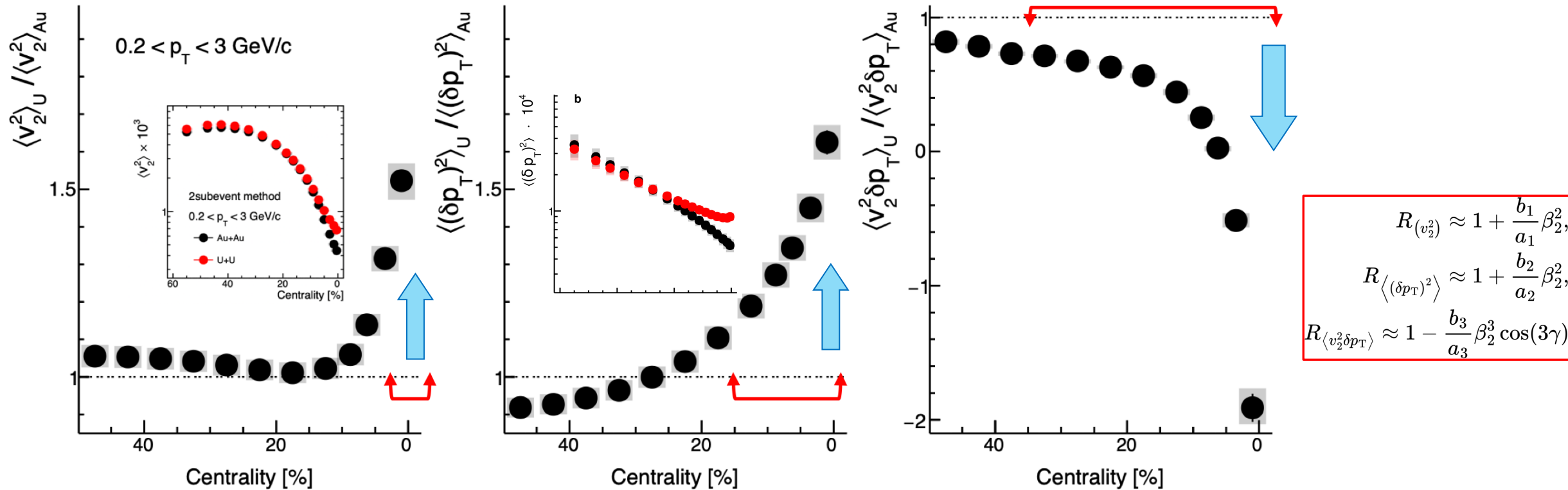
$v_2 \searrow$ $p_T \nearrow$

$$\begin{aligned} \langle v_2^2 \rangle &= a_1 + b_1 \beta_2^2, \\ \langle (\delta p_T)^2 \rangle &= a_2 + b_2 \beta_2^2, \\ \langle v_2^2 \delta p_T \rangle &= a_3 - b_3 \beta_2^3 \cos(3\gamma). \end{aligned}$$

G. Giacalone, J. Jia, C. Zhang, *PRL* 127, 242301(2021)

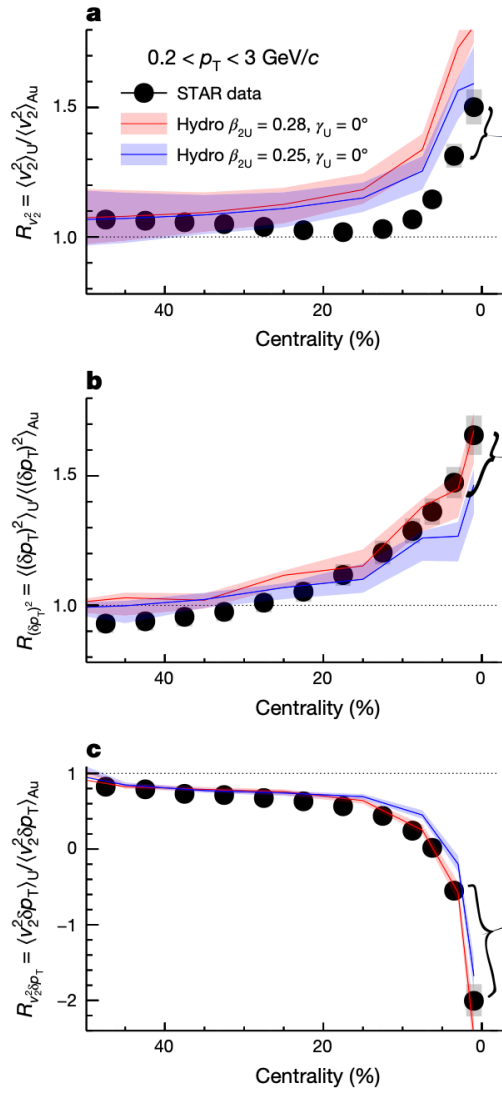
Shape-frozen like a snapshot during nuclear crossing ($10^{-25}\text{s} \ll$ rotational time scale 10^{-21}s)
probe entire mass distribution in the intrinsic frame via multi-point correlations

Ratio of observables

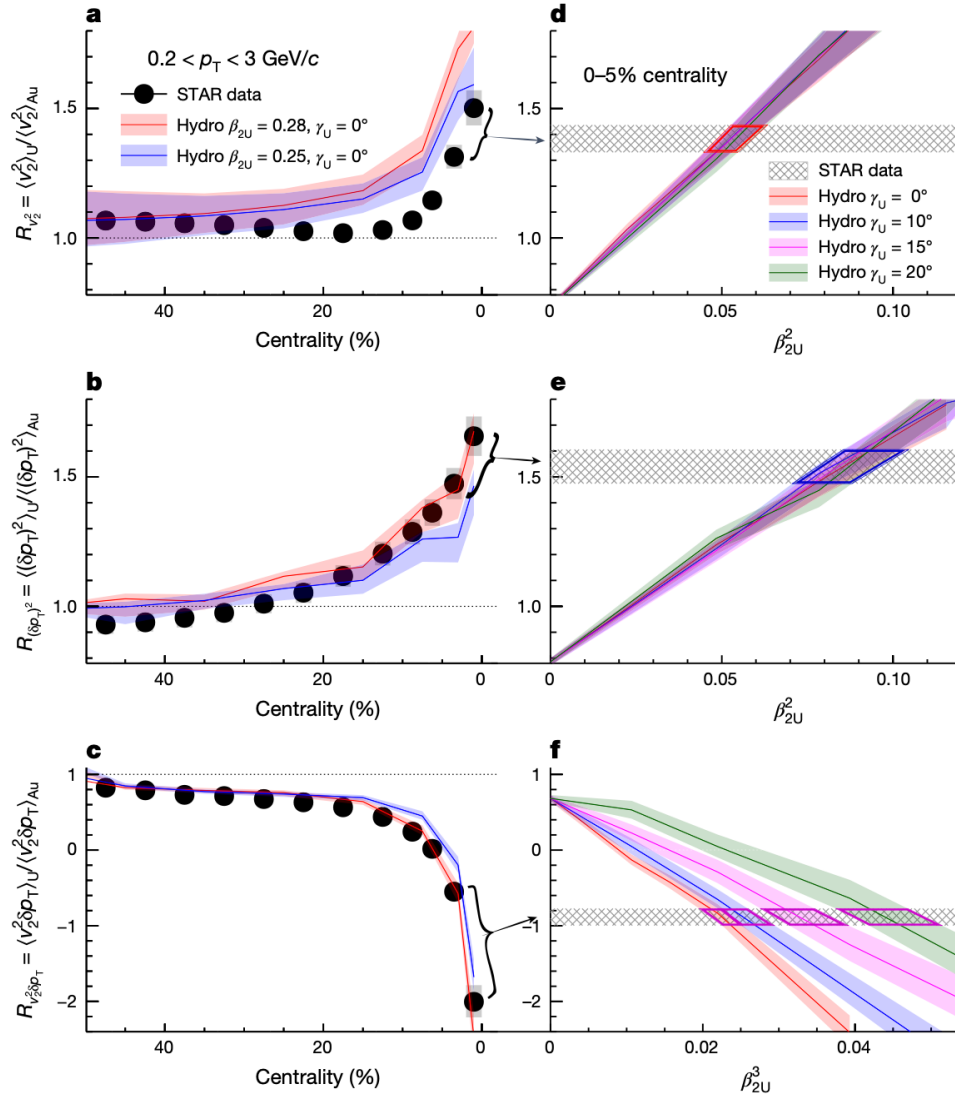


- Elliptic flow and size fluctuation are enhanced by the nuclear deformation effect.
- Ratios cancel final state effects and isolate the effects of initial state/nuclear structures.
→ U deformation dominates the ultra-central collisions (UCC)

Constraining the ground-state ^{238}U : β_2 and γ



Constraining the ground-state ^{238}U : β_2 and γ



Sufficient precision is achieved from ratios in ultra-central collisions

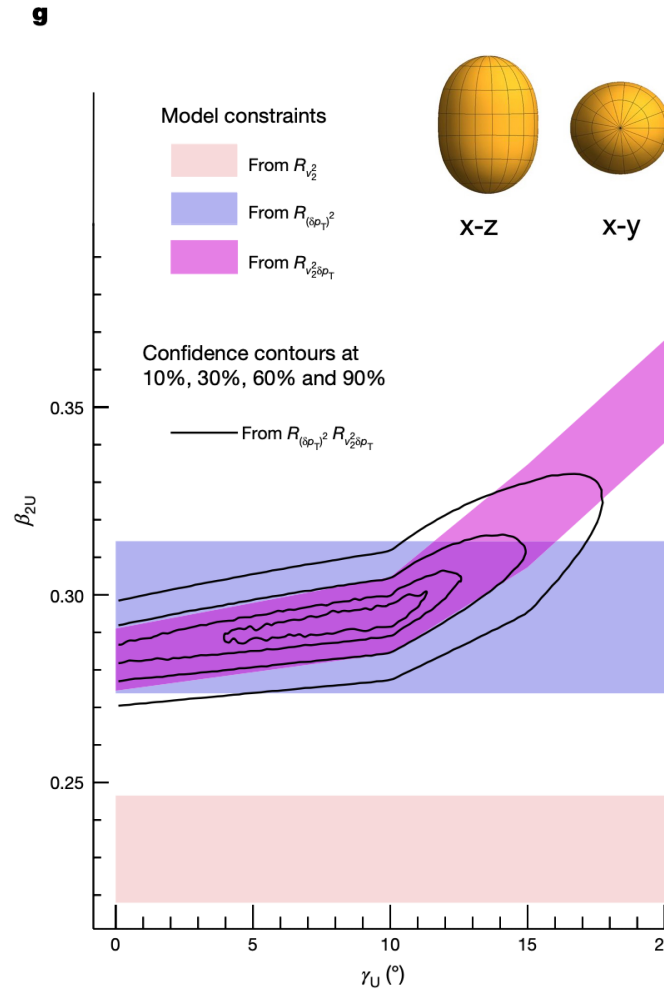
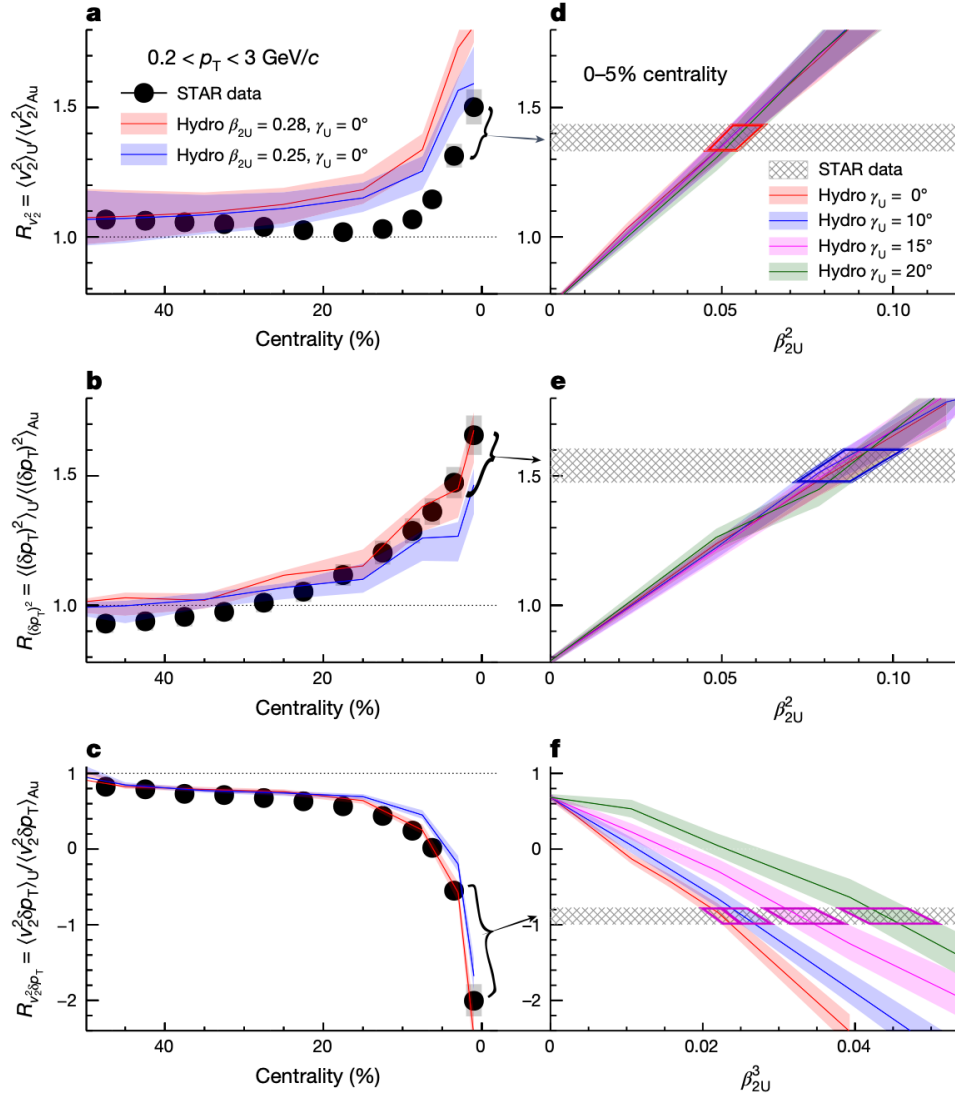
Relation confirmed from hydro

$$R_{(v_2^2)} \approx 1 + \frac{b_1}{a_1} \beta_2^2,$$

$$R_{\langle (\delta p_T)^2 \rangle} \approx 1 + \frac{b_2}{a_2} \beta_2^2,$$

$$R_{\langle v_2^2 \delta p_T \rangle} \approx 1 - \frac{b_3}{a_3} \beta_2^3 \cos(3\gamma)$$

Constraining the ground-state ^{238}U : β_2 and γ



Sufficient precision is achieved from ratios in ultra-central collisions

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$$R_{\langle v_2^2 \delta p_T \rangle} \approx 1 - \frac{b_3}{a_3} \beta_2^3 \cos(3\gamma)$$

High-energy estimate:

$$\beta_{2U} = 0.286 \pm 0.025$$

$$\gamma_U = 8.5^\circ \pm 4.8^\circ$$

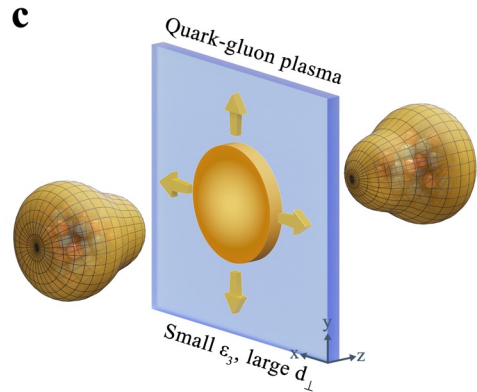
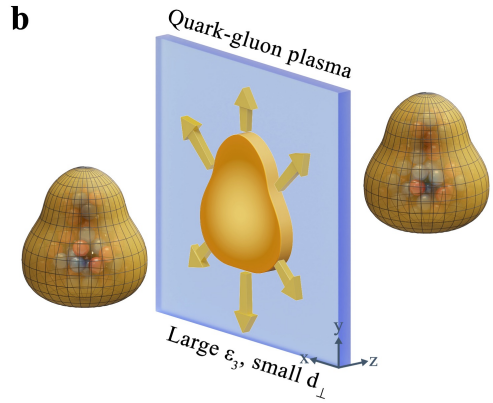
low-energy estimate:

$$\beta_{2U} = 0.287 \pm 0.007$$

$$\gamma_U = 6^\circ - 8^\circ$$

A large deformation with a slight deviation from axial symmetry in the nuclear ground-state

Evidence of octupole deformation $\beta_{3,U}$



However, v_3 is fluctuation driven, expect in central

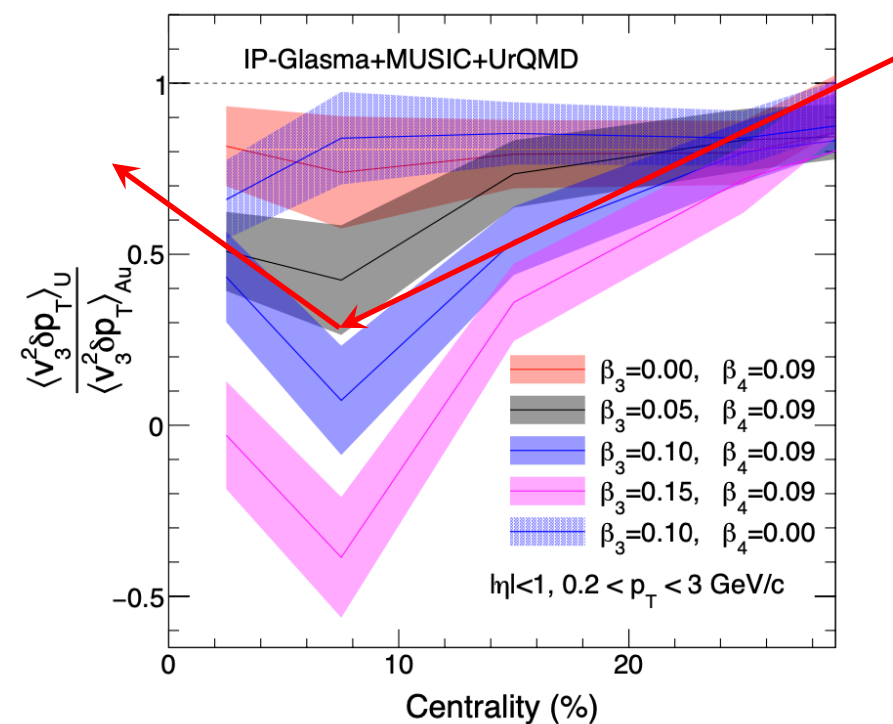
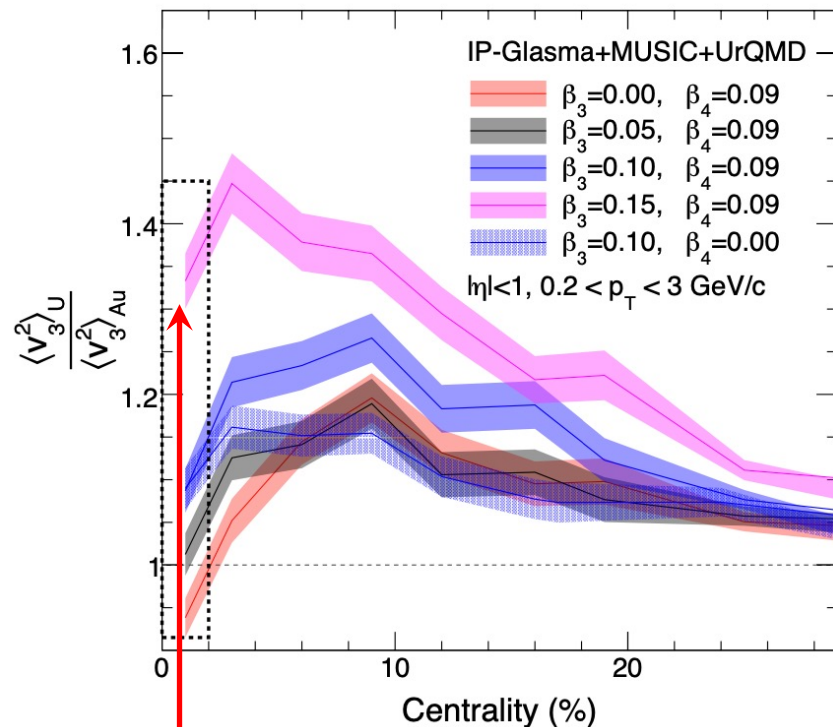
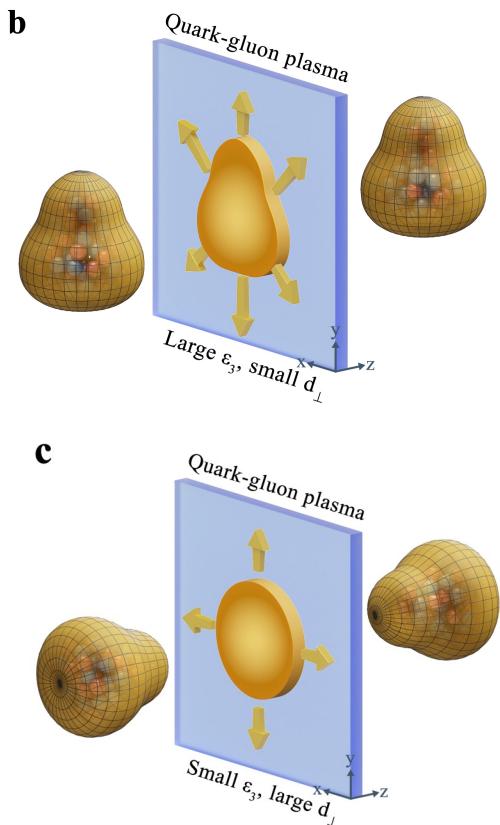
$$\langle v_3^2 \rangle \propto \langle \epsilon_3^2 \rangle \sim 1/A$$

mass number ↗

Evidence of octupole deformation $\beta_{3,U}$

IP-Glasma+MUSIC calculations

C. Zhang, J. Jia, J. Chen, C. Shen, L. Liu, arXiv: 2504.15245



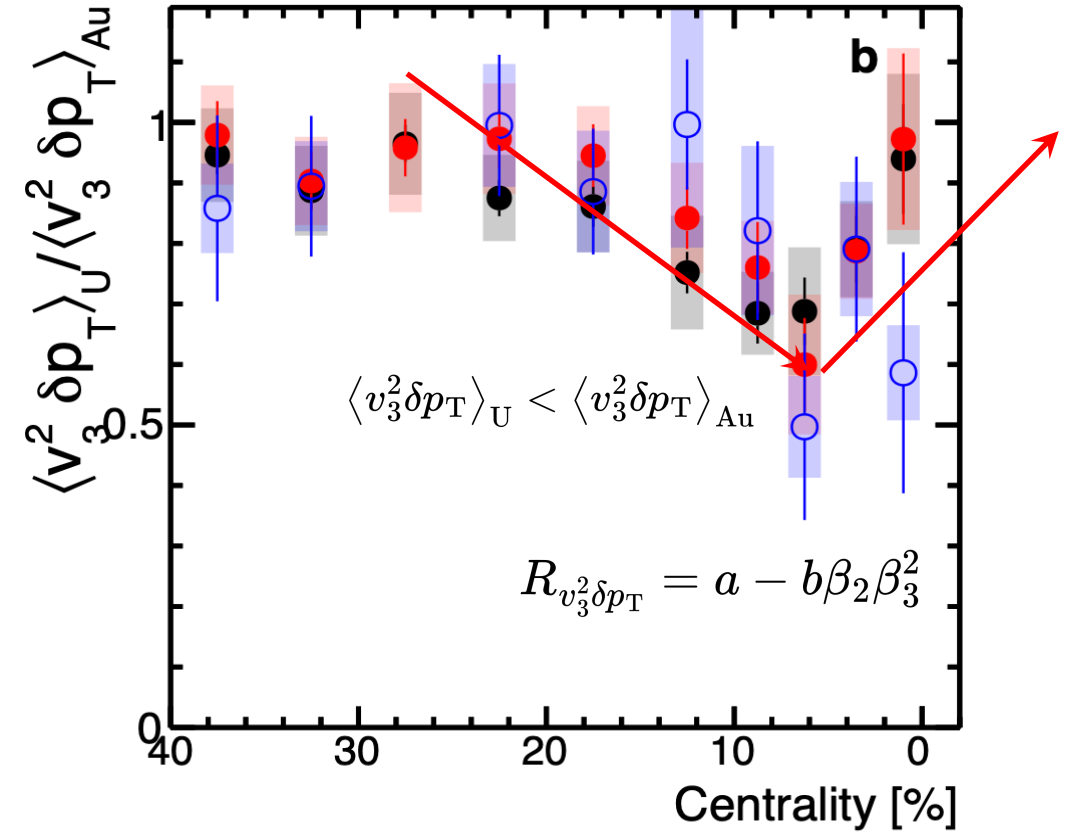
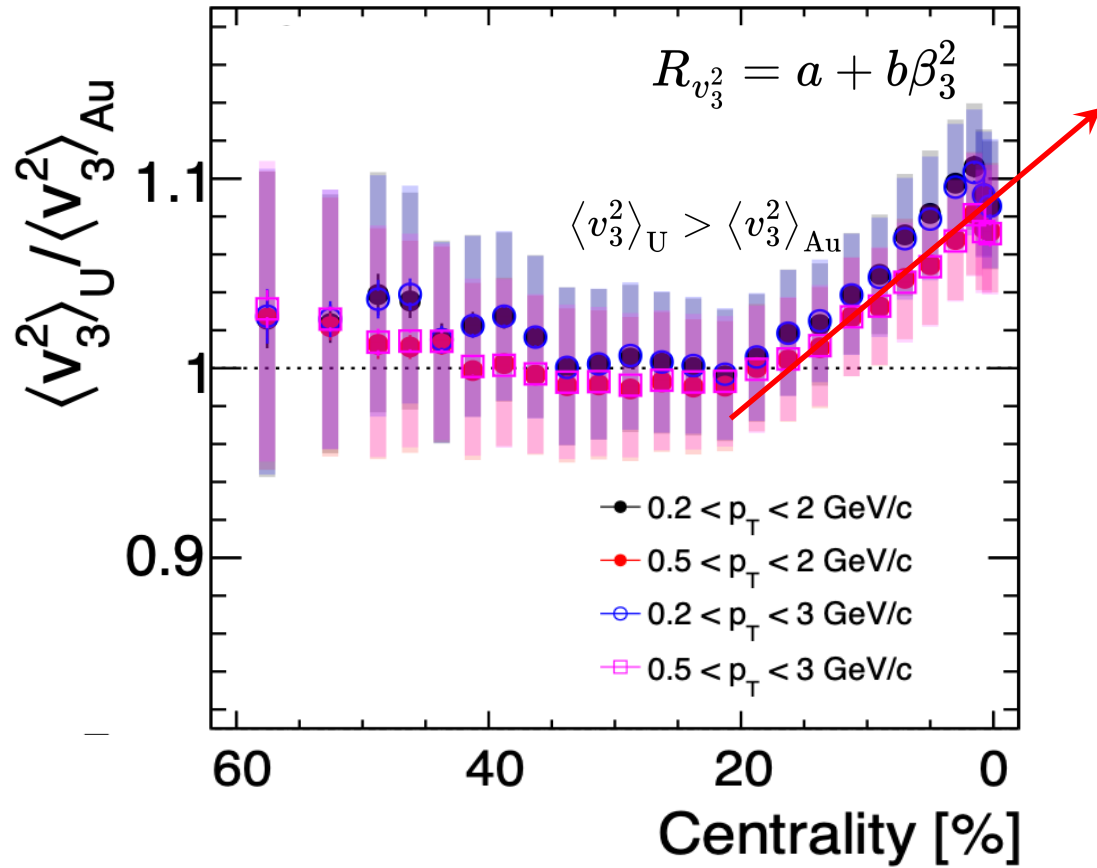
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mass number

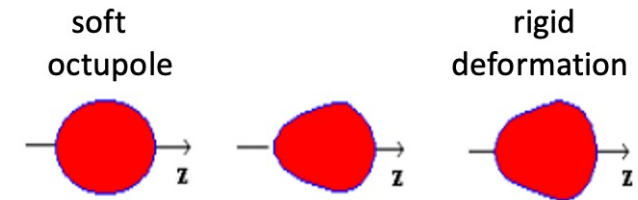
$\langle v_3^2 \rangle$ follows a linear increase with β_3^2 ,

Characteristic anticorrelation in $\langle v_3^2 \delta p_T \rangle$ shows a pronounced β_3 -dependent suppression.



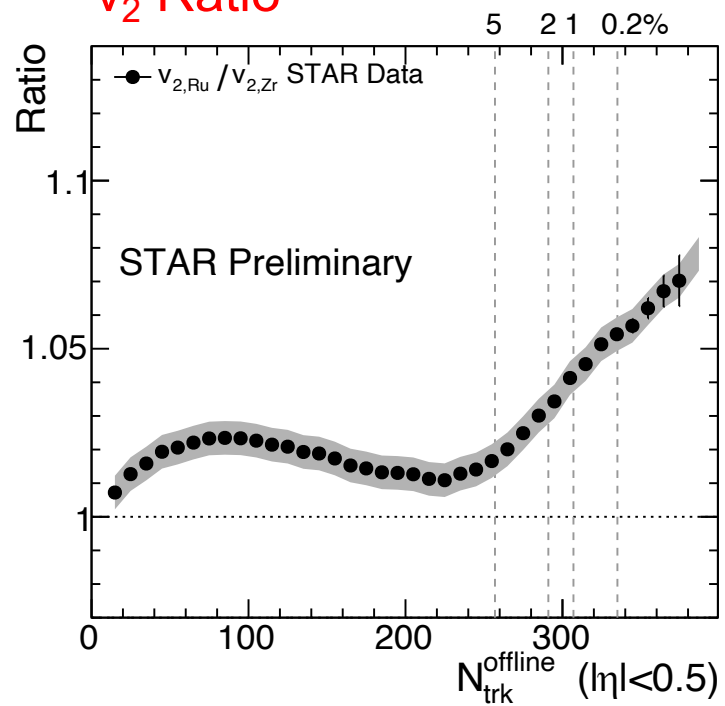
Order of v_3 and v_3 - p_T reversed by considering non-zero $\beta_{3,U}$, $\beta_{4,U}$.

An evidence and modest $\beta_{3,U} \sim 0.08$ - 0.10 are confirmed.

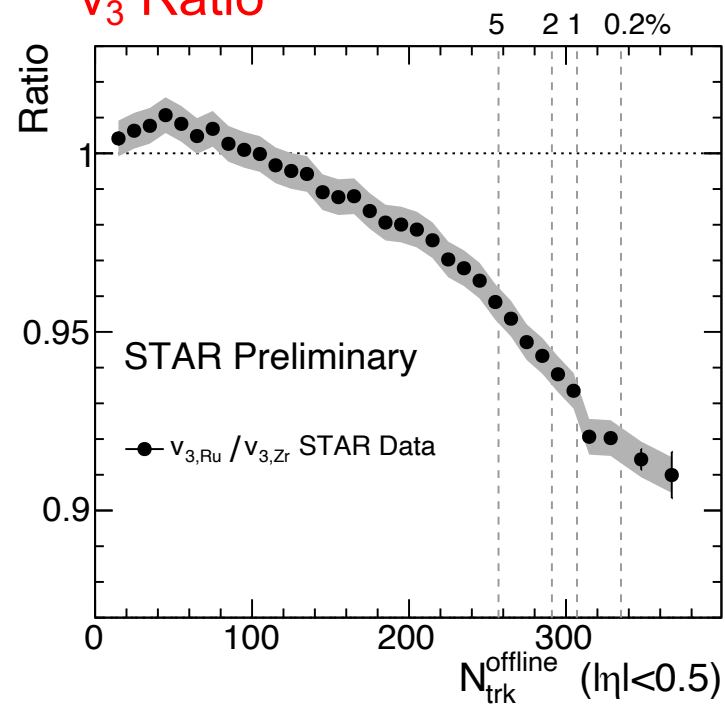


Nuclear structure via $^{96}\text{Ru}/^{96}\text{Zr}$ v_n ratio

v_2 Ratio

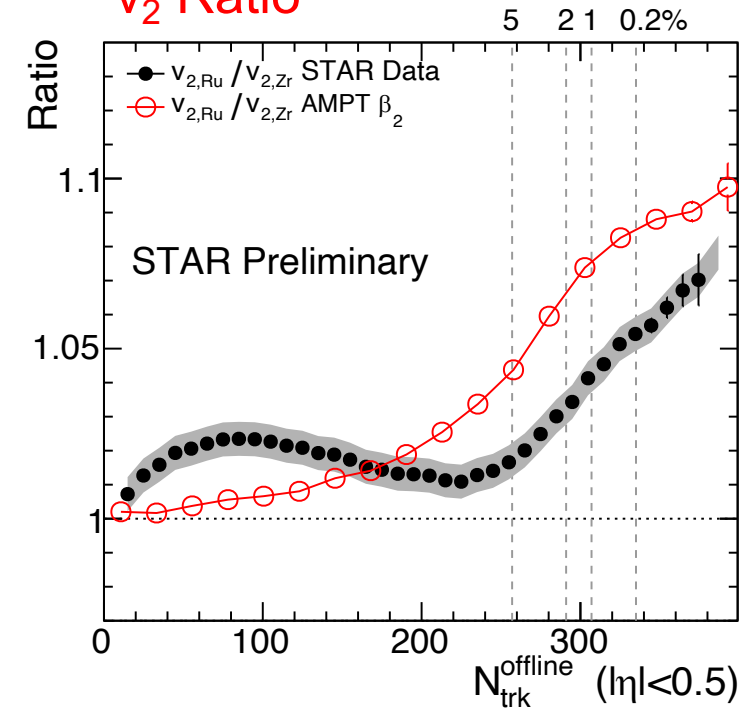


v_3 Ratio

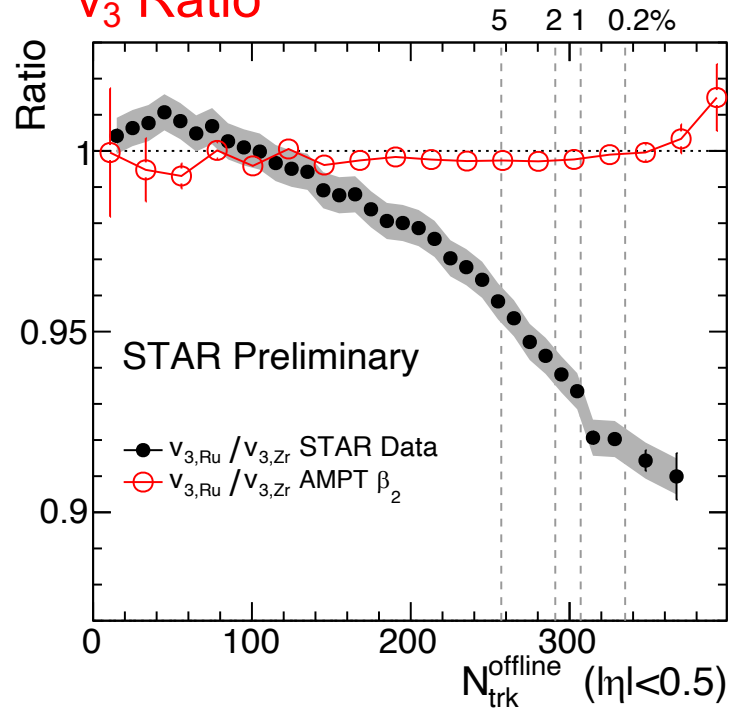


Nuclear structure via $^{96}\text{Ru}/^{96}\text{Zr}$ v_n ratio

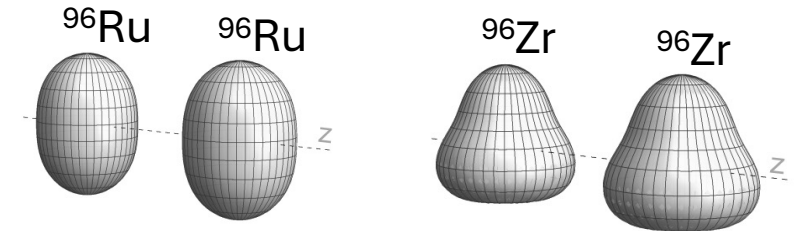
v_2 Ratio



v_3 Ratio



$\beta_{2,\text{Ru}} \sim 0.16$ increase v_2 , no influence on v_3 ratio



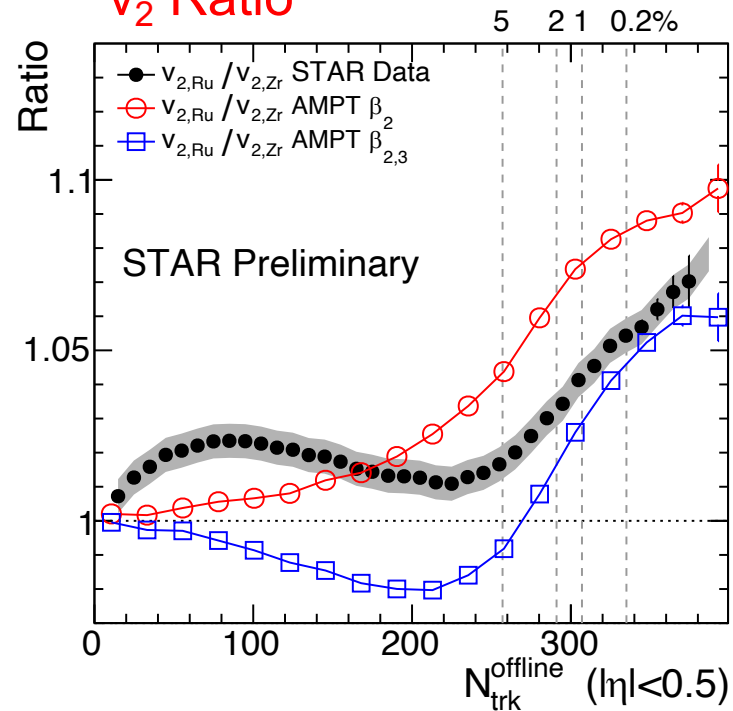
$$\beta_{2,\text{Ru}} = 0.16 \pm 0.02$$

difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 fm	0.07 fm

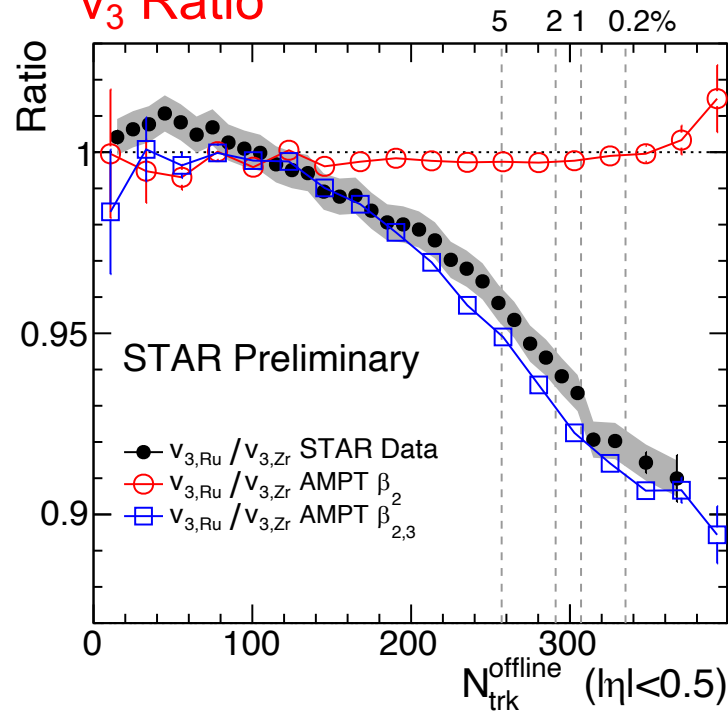
Current estimation is from transport model

Nuclear structure via $^{96}\text{Ru}/^{96}\text{Zr}$ v_n ratio

v_2 Ratio

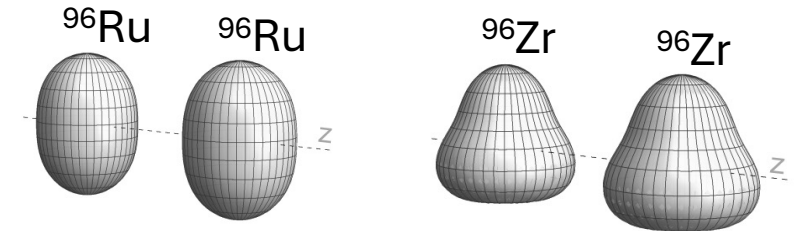


v_3 Ratio



$\beta_{2,\text{Ru}} \sim 0.16$ increase v_2 , no influence on v_3 ratio

$\beta_{3,\text{Zr}} \sim 0.2$ decrease v_2 in mid-central, decrease v_3 ratio



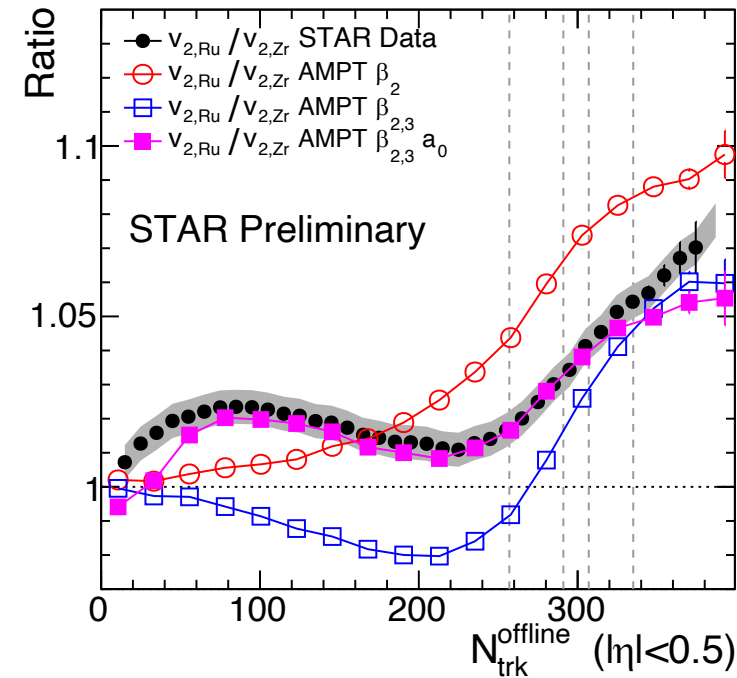
$$\beta_{2,\text{Ru}} = 0.16 \pm 0.02 \quad \beta_{3,\text{Zr}} = 0.20 \pm 0.02$$

difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 fm	0.07 fm

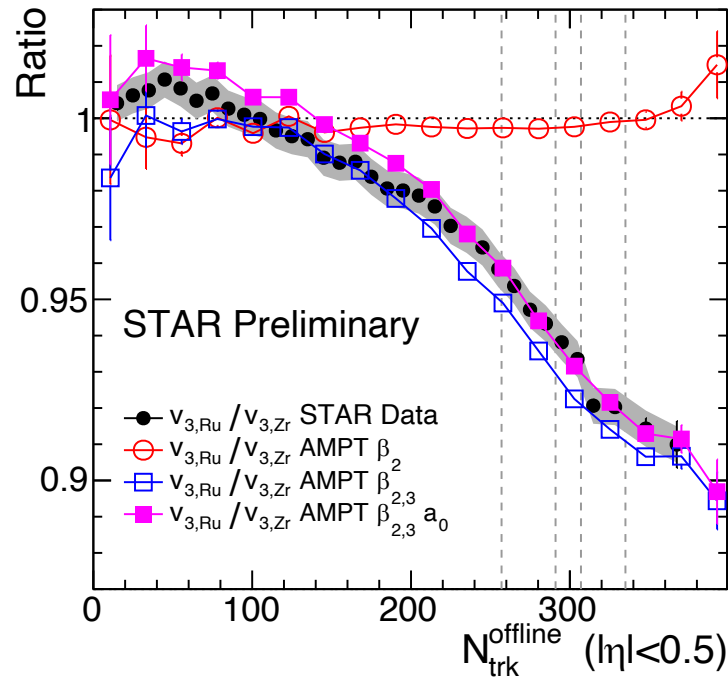
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Nuclear structure via $^{96}\text{Ru}/^{96}\text{Zr}$ v_n ratio

v_2 Ratio



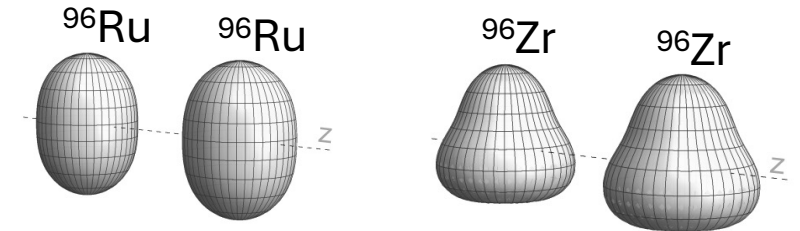
v_3 Ratio



$\beta_{2,\text{Ru}} \sim 0.16$ increase v_2 , no influence on v_3 ratio

$\beta_{3,\text{Zr}} \sim 0.2$ decrease v_2 in mid-central, decrease v_3 ratio

$\Delta a_0 = -0.06$ fm increase v_2 mid-central, small impact on v_3



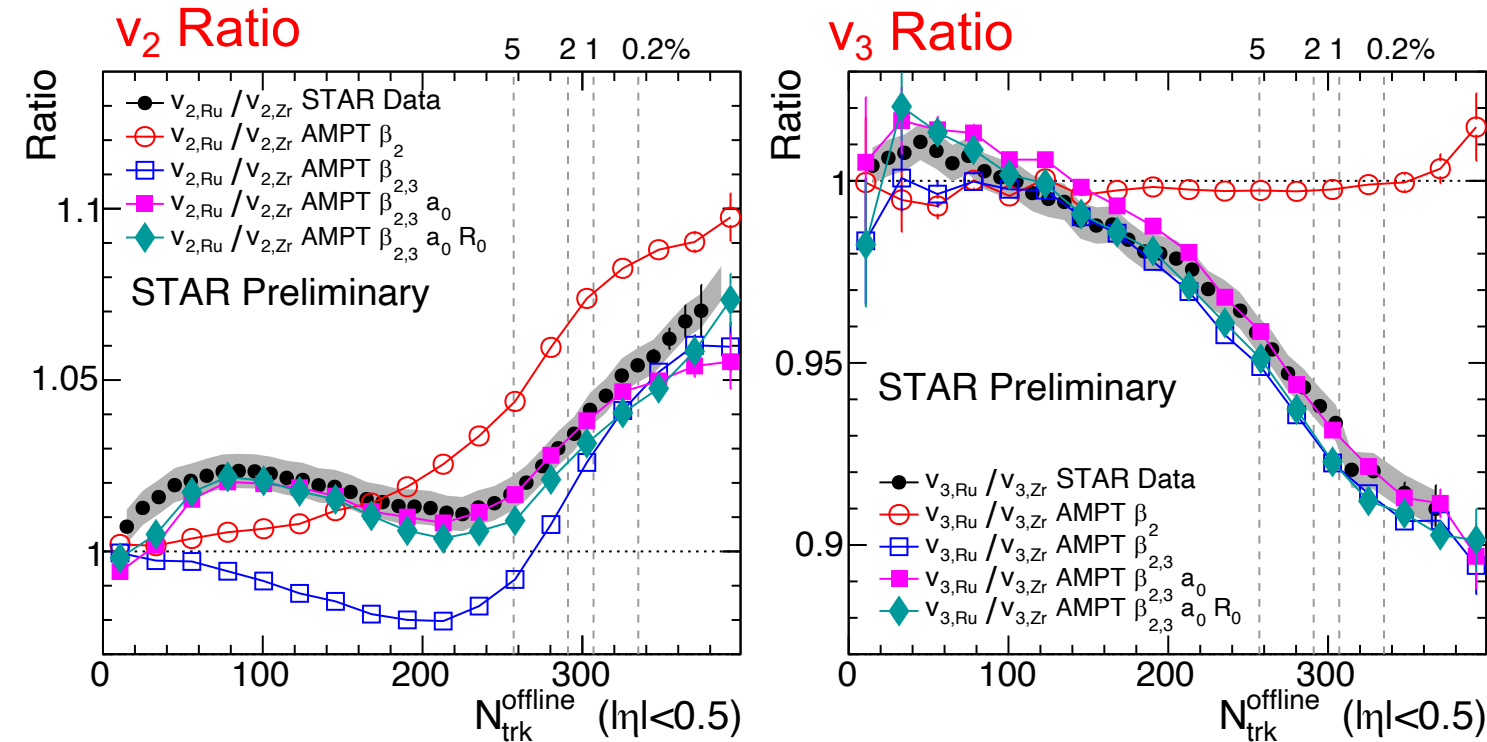
$$\beta_{2,\text{Ru}} = 0.16 \pm 0.02 \quad \beta_{3,\text{Zr}} = 0.20 \pm 0.02$$

difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 fm	0.07 fm

Current estimation is from transport model

- Direct observation of octupole deformation in ^{96}Zr nucleus
- Imply the neutron skin difference between ^{96}Ru and ^{96}Zr

Nuclear structure via $^{96}\text{Ru}/^{96}\text{Zr}$ v_n ratio

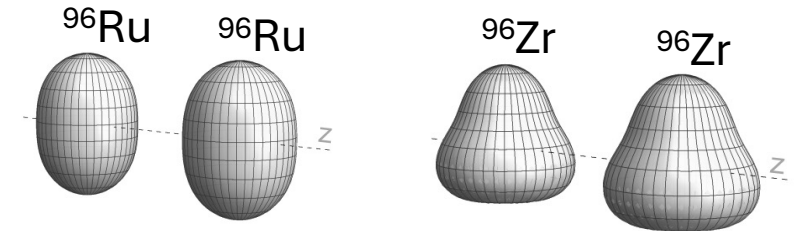


$\beta_{2,\text{Ru}} \sim 0.16$ increase v_2 , no influence on v_3 ratio

$\beta_{3,\text{Zr}} \sim 0.2$ decrease v_2 in mid-central, decrease v_3 ratio

$\Delta a_0 = -0.06$ fm increase v_2 mid-central, small impact on v_3

Radius $\Delta R_0 = 0.07$ fm only slightly affects v_2 and v_3 ratio.



$$\beta_{2,\text{Ru}} = 0.16 \pm 0.02 \quad \beta_{3,\text{Zr}} = 0.20 \pm 0.02$$

difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 fm	0.07 fm

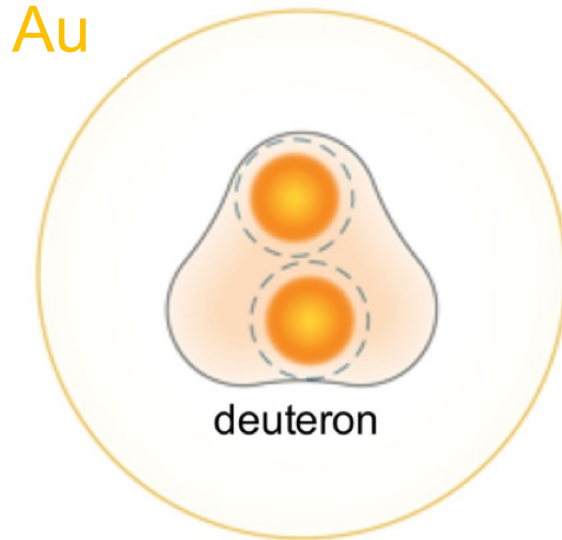
Current estimation is from transport model

$$R_{\mathcal{O}} \equiv \frac{\mathcal{O}_{\text{Ru}}}{\mathcal{O}_{\text{Zr}}} \approx 1 + c_1 \Delta\beta_2^2 + c_2 \Delta\beta_3^2 + c_3 \Delta R_0 + c_4 \Delta a_0$$

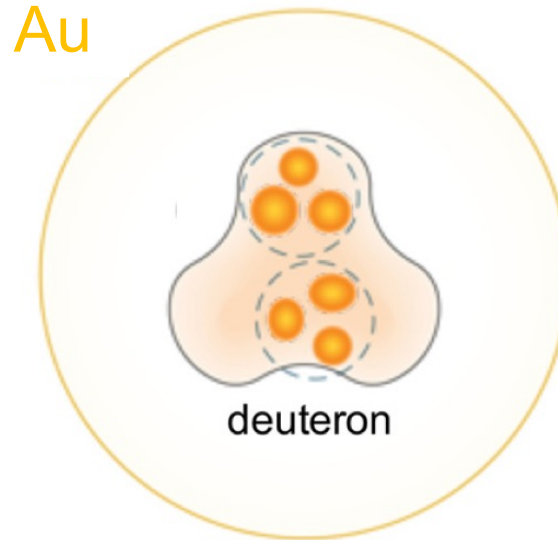
- Direct observation of octupole deformation in ^{96}Zr nucleus
- Imply the neutron skin difference between ^{96}Ru and ^{96}Zr
- Simultaneously constrain parameters using Bayesian analysis

Light nuclear geometry and nucleon nucleon correlations

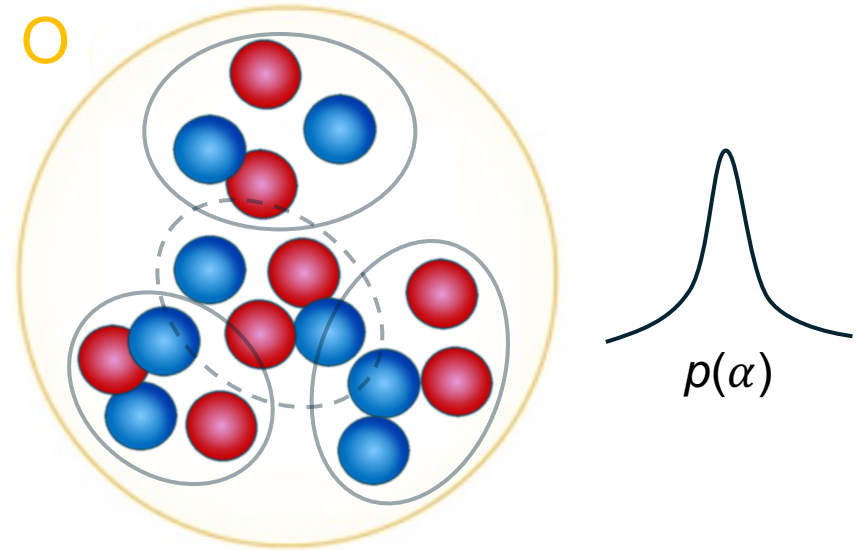
Nucleon fluctuation



Nucleon & subnucleon fluctuation



Nucleon-nucleon correlation



ab initio calculations

STAR, PRL 130, 242301 (2023)

STAR, PRC 110, 064902 (2024)

W. He, Y. Ma et al., PRL 113, 032506 (2014);...

C. Zhang, J. Chen, G. Giacalone, S. Huang, J. Jia, Y. Ma, PLB 862, 139322 (2025)

S. Huang, J. Jia, C. Zhang, 2507.16162

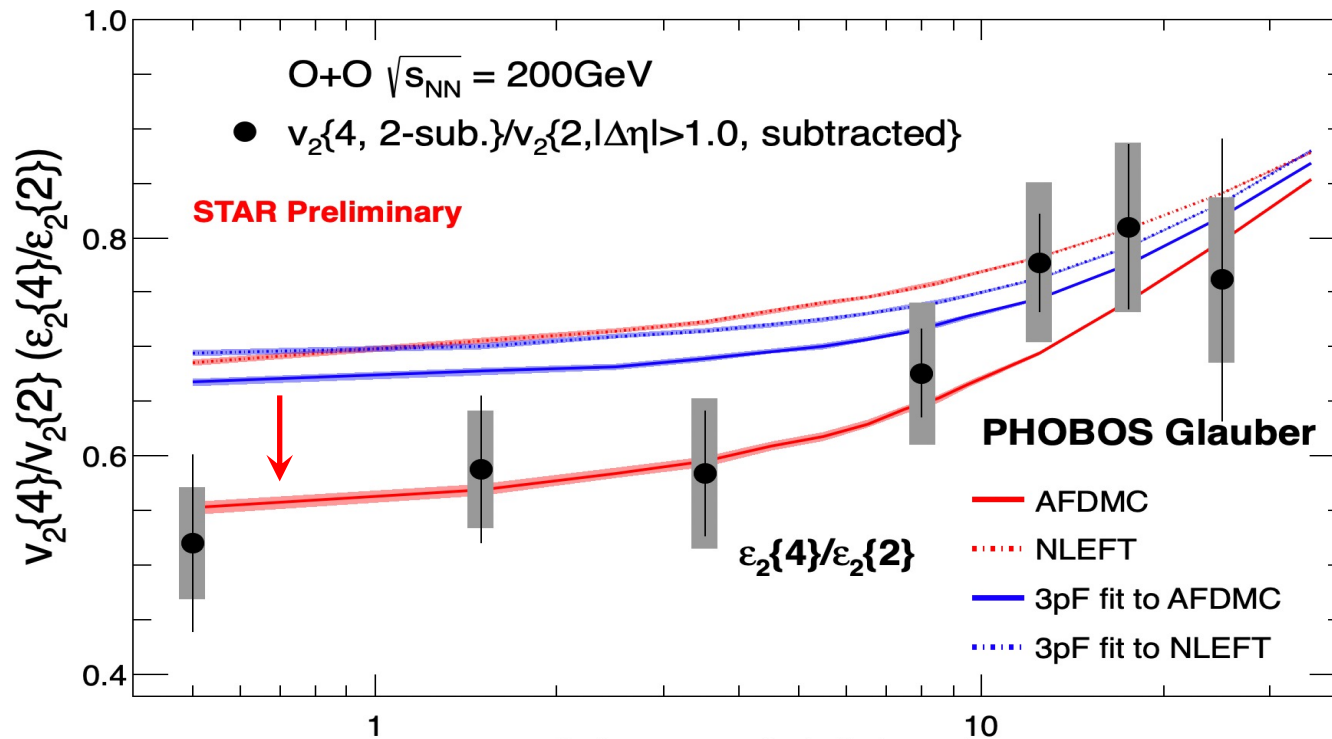
d+Au collision, 200 GeV

Nearly same N_{ch}

O+O collision, 200 GeV

STAR paper is in Collaboration Review

More details in Jiangyong's talk



$\epsilon_2\{4\} / \epsilon_2\{2\}$ from three models:

1. **WS is away from STAR data.**

2. **VMC and EFT have a visible difference.**

Can many-nucleon correlations significantly impact the eccentricity fluctuations? YES!

VMC and EFT theory have visible differences describing the $v_2\{4\}/v_2\{2\}$. **The interplay between sub-nucleon fluctuation and many-nucleon correlation.**

STAR, PRL 130, 242301 (2023)

$$(v_n\{2\})^2 = c_n\{2\} = \langle v_n^2 \rangle$$

$$(v_n\{4\})^4 = -c_n\{4\} = 2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle$$

$$\epsilon_2\{2\}^2 = \langle \epsilon_2^2 \rangle$$

$$\epsilon_2\{4\}^4 = 2\langle \epsilon_2^2 \rangle^2 - \langle \epsilon_2^4 \rangle$$

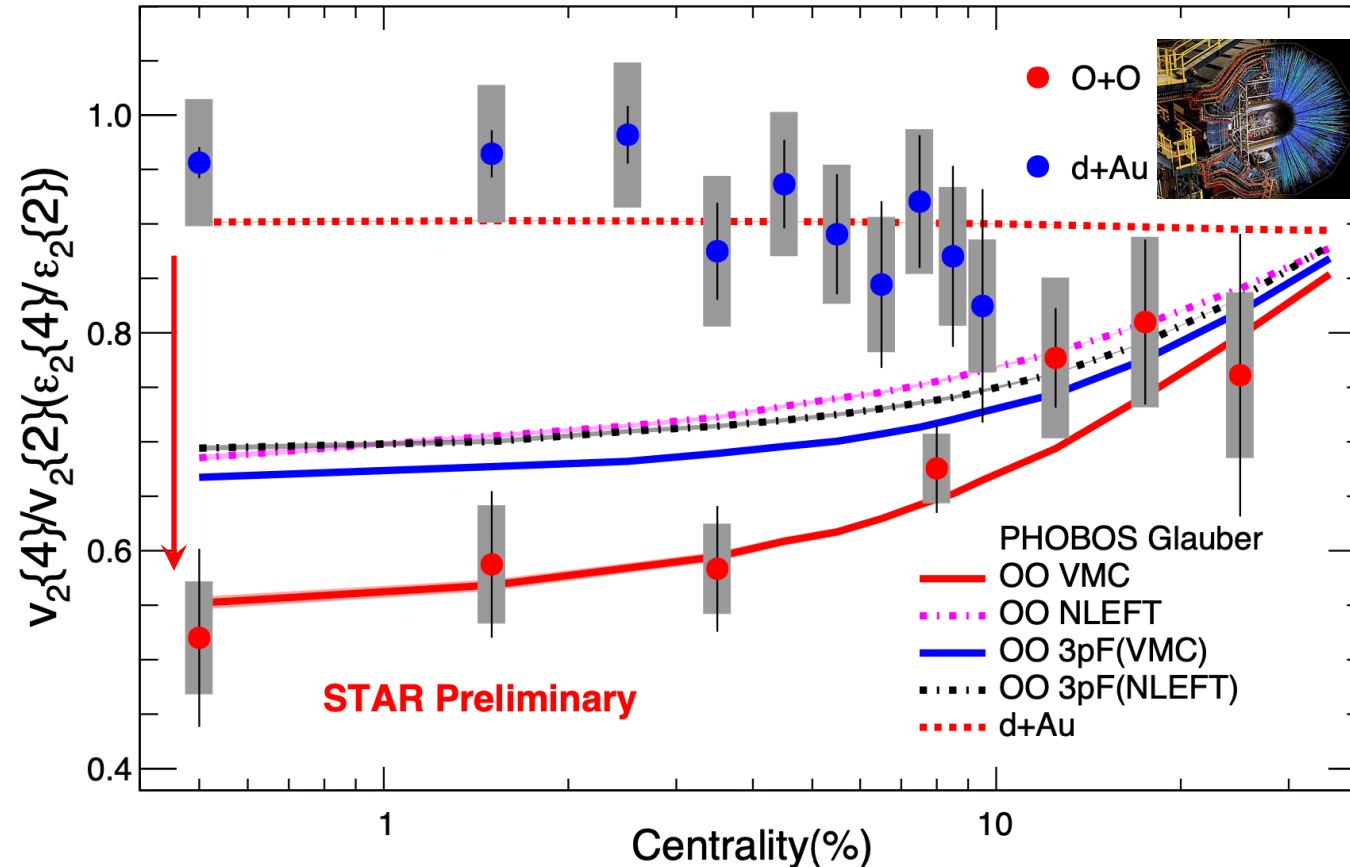
Y. Ma, S. Zhang, Handbook of Nuclear Physics (2022); W. He, Y. Ma et al, PRL 113, 032506 (2014)

G. Giacalone, G. Nijs et al., PRL135, 012302 (2025), G. Giacalone, W. Zhao et al., PRL134, 082301 (2025); C. Zhang, J. Chen, G. Giacalone, S. Huang, J. Jia, Y. Ma, PLB 862, 139322 (2025)

Y. Wang, S. Zhao, B. Cao, H. Xu, H. Song, PRC 109, L051904 (2024); X. Zhao, G. Ma. Y. Zhou, Z. Lin, C. Zhang, 2404.09780; S. Jahan, Roch, C. Shen, 2507. 11394

STAR paper is in Collaboration Review

More details in Jiangyong's talk



$\epsilon_2\{4\}/\epsilon_2\{2\}$ from three models:

1. **WS** is away from **STAR** data.

2. **VMC** and **EFT** have a visible difference.

Can many-nucleon correlations significantly impact the eccentricity fluctuations? **YES!**

VMC and EFT theory have visible differences describing the $v_2\{4\}/v_2\{2\}$. The interplay between sub-nucleon fluctuation and many-nucleon correlation.

STAR, PRL 130, 242301 (2023)

Geometric scan elucidates nuclear tomography and strong nuclear force?

Need more low-energy model inputs.

$$\begin{aligned} (v_n\{2\})^2 &= c_n\{2\} = \langle v_n^2 \rangle & \epsilon_2\{2\}^2 &= \langle \epsilon_2^2 \rangle \\ (v_n\{4\})^4 &= -c_n\{4\} = 2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle & \epsilon_2\{4\}^4 &= 2\langle \epsilon_2^2 \rangle^2 - \langle \epsilon_2^4 \rangle \end{aligned}$$

Y. Ma, S. Zhang, Handbook of Nuclear Physics (2022); W. He, Y. Ma et al, PRL 113, 032506 (2014)

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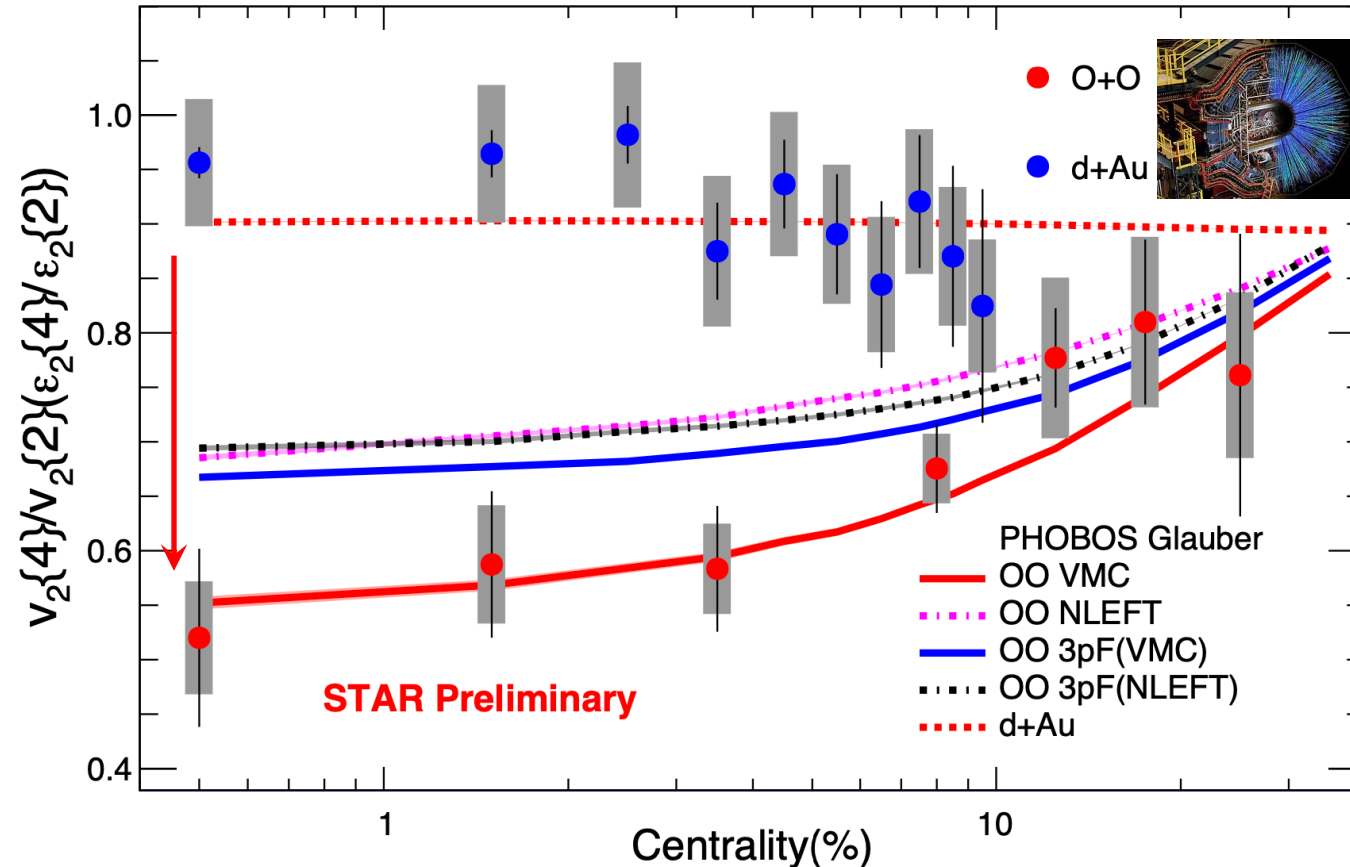
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Benchmarking geometric tomography of ^{16}O nucleus

New

STAR paper is in Collaboration Review

More details in Jiangyong's talk



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LHC (ALICE, ATLAS, CMS, LHCb) released the O+O/Ne+Ne!!!
Shape imaging method for light ions (New avenue)

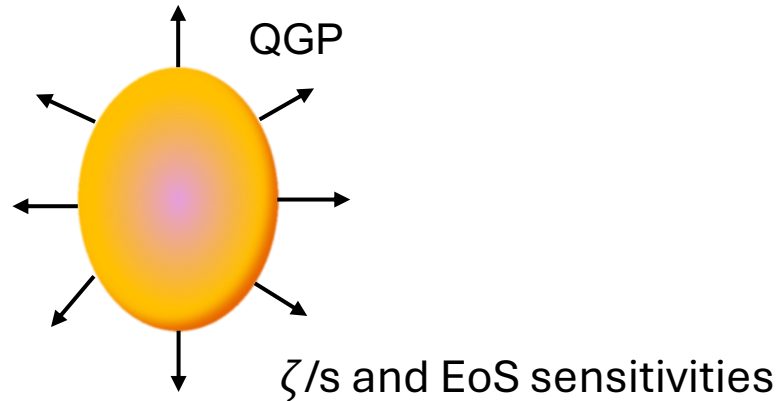
Y. Ma, S. Zhang, Handbook of Nuclear Physics (2022); W. He, Y. Ma et al, PRL 113, 032506 (2014)

G. Giacalone, G. Nijs et al., PRL135, 012302 (2025); G. Giacalone, W. Zhao et al., PRL134, 082301 (2025); C. Zhang, J. Chen, G. Giacalone, S. Huang, J. Jia, Y. Ma, PLB 862, 139322 (2025)

Y. Wang, S. Zhao, B. Cao, H. Xu, H. Song, PRC 109, L051904 (2024); X. Zhao, G. Ma. Y. Zhou, Z. Lin, C. Zhang, 2404.09780; S. Jahan, Roch, C. Shen, 2507. 11394

New radial flow $v_0(p_T)$ measurement in 200 GeV

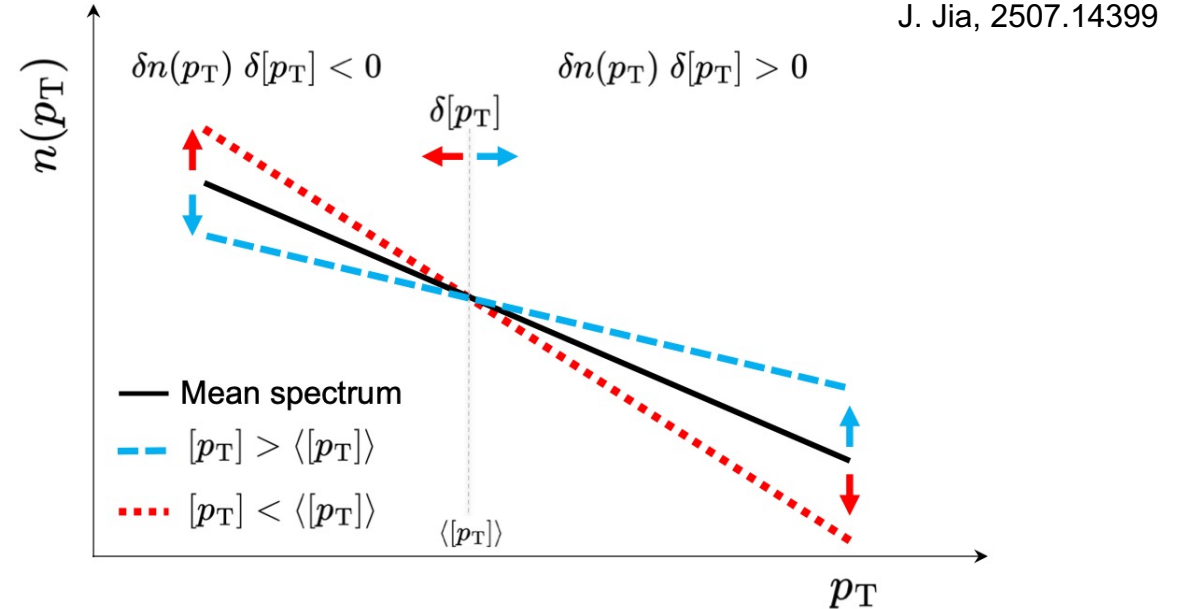
Radial expansion: the $n=0$ modulation



Spectra slope quantified by $[p_T]$ in each event:
Fluctuation in $[p_T]$ $\rightarrow$ Fluctuation in spectra.

Quantify the correlation induced by radial flow using
covariance between $n(p_T)$ and $[p_T]$: $\langle \delta n(p_T) \delta [p_T] \rangle$

B. Schenke, C. Shen, D. Teaney, PRC 102, 034905 (2020)
 T. Parida, R. Samanta, J.Y. Ollitrault, PLB 857, 138985 (2024)
 S. A. Jahan, H. Roch, C. Shen. arXiv: 2507.11394
 L. Du, 2508.07184



J. Jia, 2507.14399

Calculated within a reference range, p_T -independent.

$$v_0(p_T) = \frac{\langle \delta n(p_T) \delta [p_T] \rangle}{\langle n(p_T) \rangle \langle [p_T] \rangle} \times \frac{1}{v_{0,int}}$$

Pearson Correlations between local possibility of particle yield and reference mean p_T from spectra

Remove influence from global fluctuations

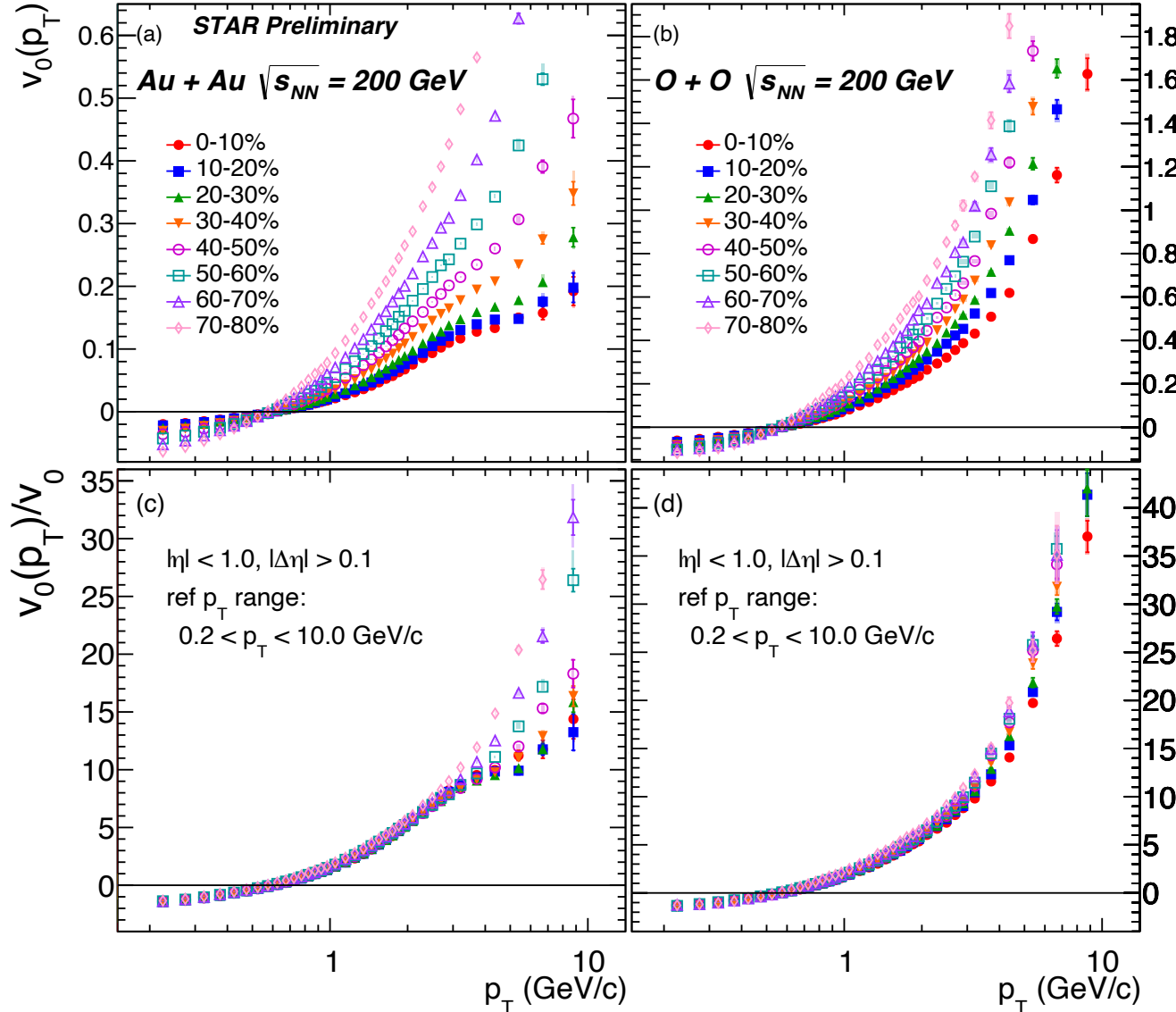
$$v_{0,int} \equiv \frac{\sqrt{\langle (\delta [p_T])^2 \rangle}}{\langle [p_T] \rangle}$$

This allows us to verify the signatures of collectivity for radial flow, like for anisotropic flow

Radial flow $v_0(p_T)$ in system-size comparison

Au+ Au vs. O+O

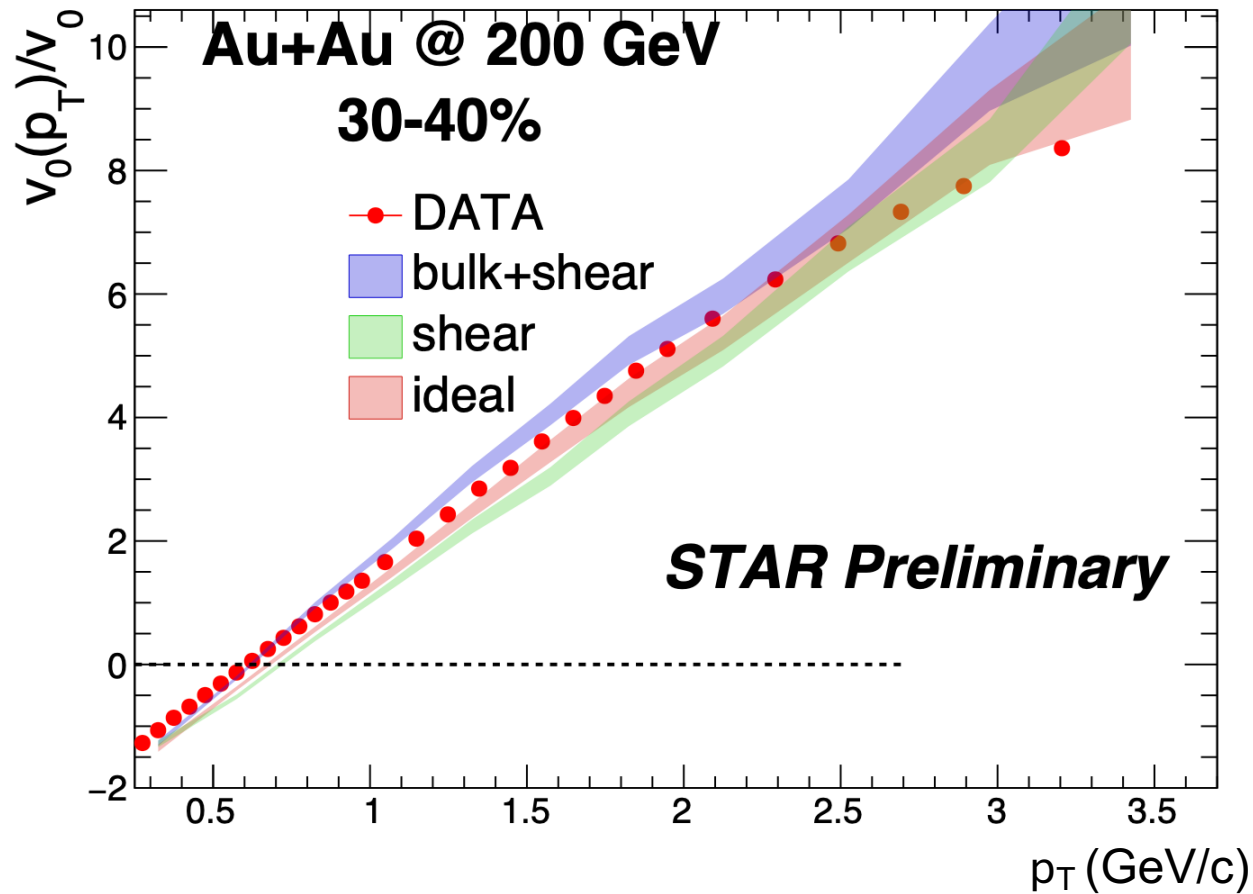
First measurement at RHIC --- Zaining Wang (Fudan & Stony Brook), IS 2025



Increase with p_T
Exhibiting a strong centrality dependence.
The zero-crossing point coincides with $\langle [p_T] \rangle$,
where fluctuations vanish

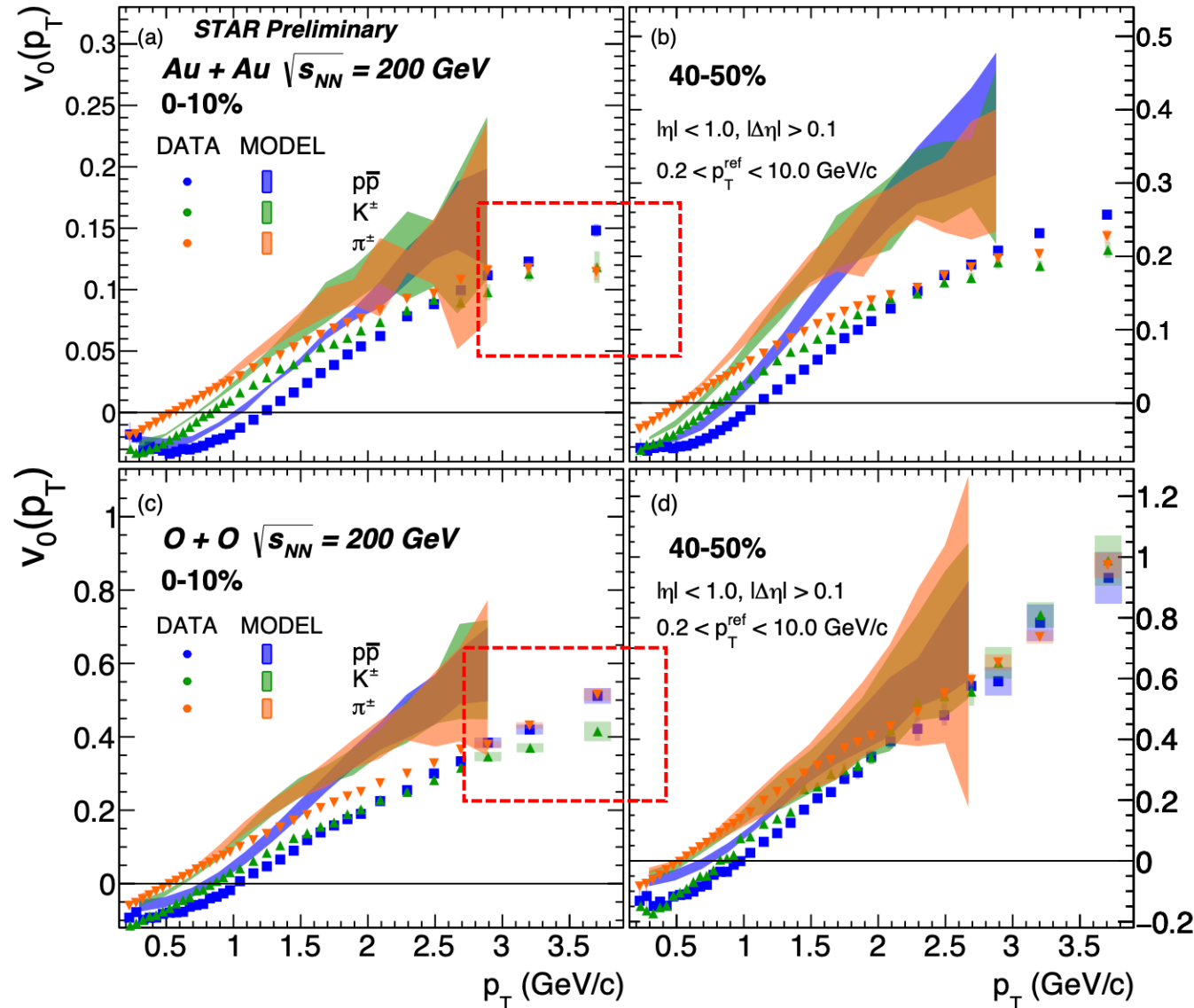
After normalization, all centralities collapse onto a single trend, indicating a hydrodynamic collective response to global fluctuations

$$v_0(p_T) = \frac{\langle \delta n(p_T) \delta [p_T]_{p_T^{\text{ref}}} \rangle}{\langle \delta n(p_T) \rangle (\langle \delta [p_T] \rangle v_0)_{p_T^{\text{ref}}}}$$



It demonstrated to have a strong bulk viscosity

Only a weak dependence on shear viscosity, which is suggested by comparison in models (need to check more)

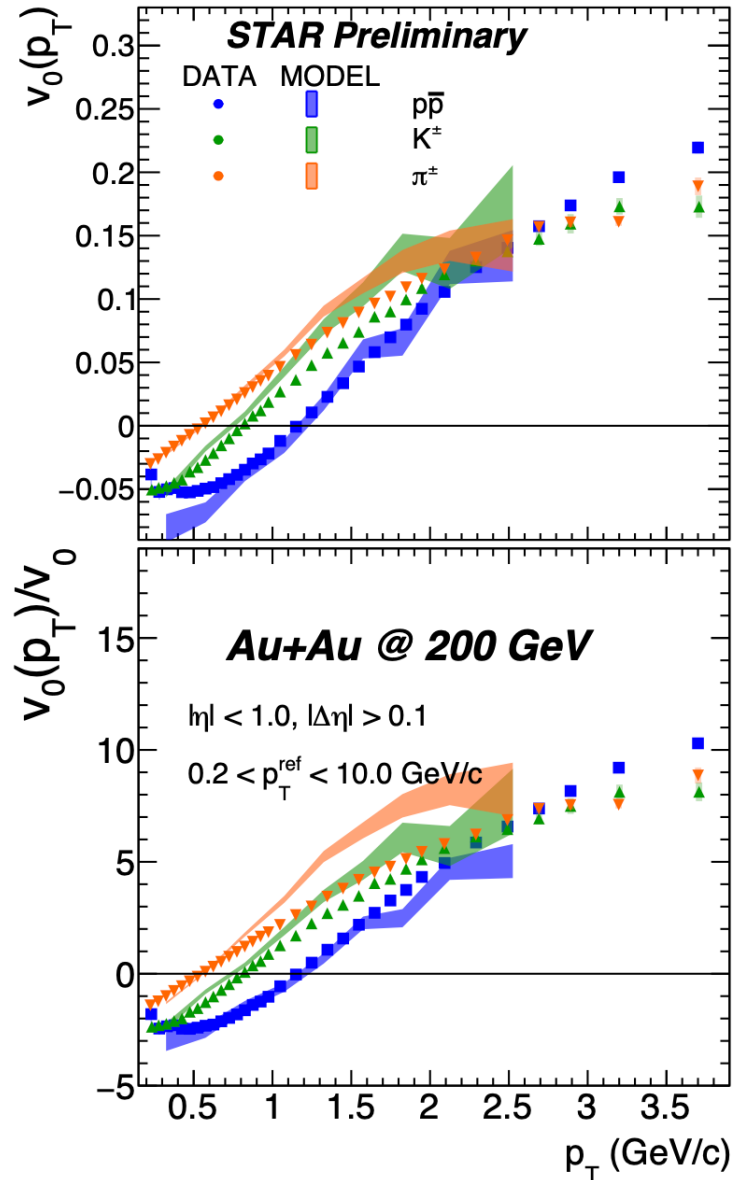


$$v_0(p_T) = \frac{\langle \delta n(p_T) \delta [p_T]_{p_T^{ref}} \rangle}{\langle \delta n(p_T) \rangle (\langle \delta [p_T] \rangle v_0)_{p_T^{ref}}}$$

The stronger boost experienced by heavier particles gives rise to a clear mass ordering

Meson-baryon splitting are observed

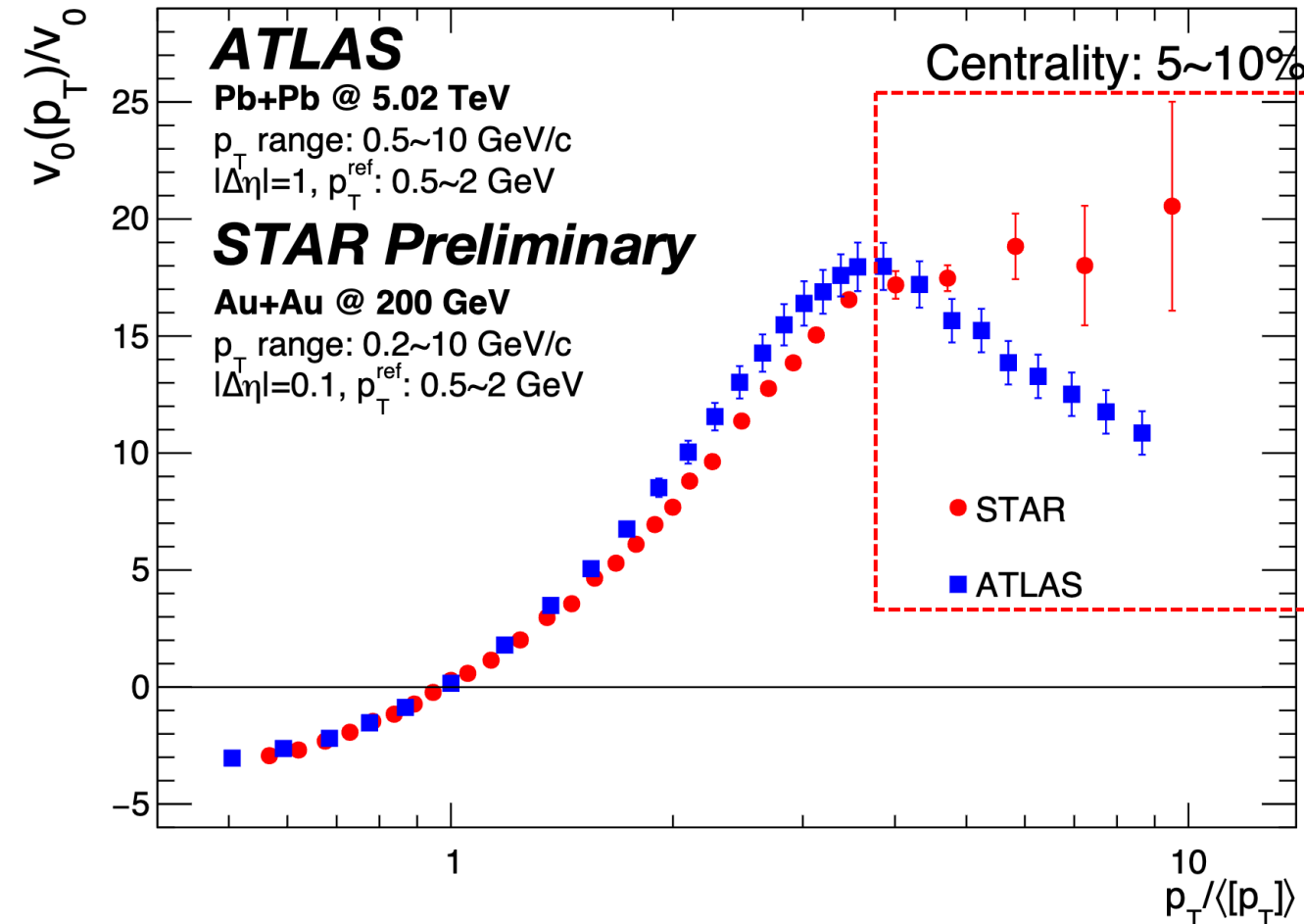
3D-Glauber+MUSIC+UrQMD model also show clear mass ordering, but seems deviate from data



$$v_0(p_T) = \frac{\langle \delta n(p_T) \delta [p_T]_{p_T^{ref}} \rangle}{\langle \delta n(p_T) \rangle (\langle \delta [p_T] \rangle v_0)_{p_T^{ref}}}$$

TRENTTo+free-streaming+MUSIC+iSS+SMASH show good comparison

More model calculations are needed to tune for fitting this new observables at RHIC energies.



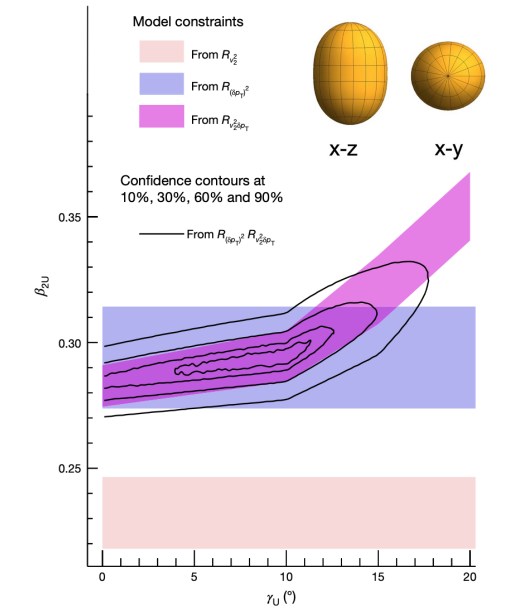
1) Will add the ALICE, ATLAS, and STAR together. 2) Would also expect nuclear structure features in $n=0$ modulations? U+U/Au+Au, Ru+Ru/Zr+Zr, ...

Future system- and energy-scans are interesting and useful for understanding radial flow

IV. Conclusions and Outlooks

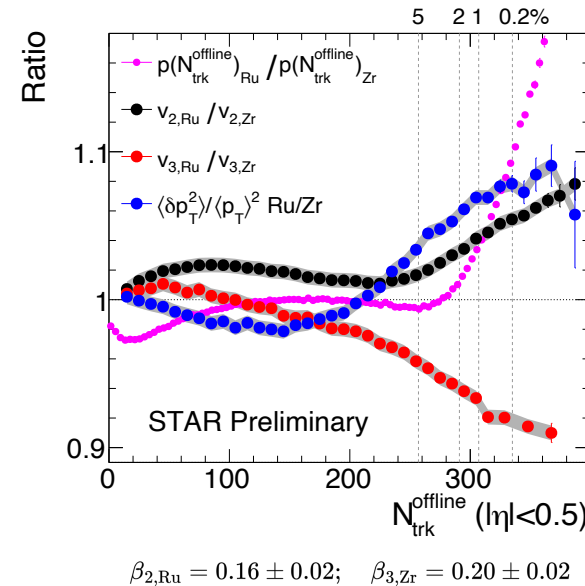
1. The signatures of nuclear structure in nuclear collisions are ubiquitous:

STAR, Nature 635, 67-72 (2024); 2506.17785

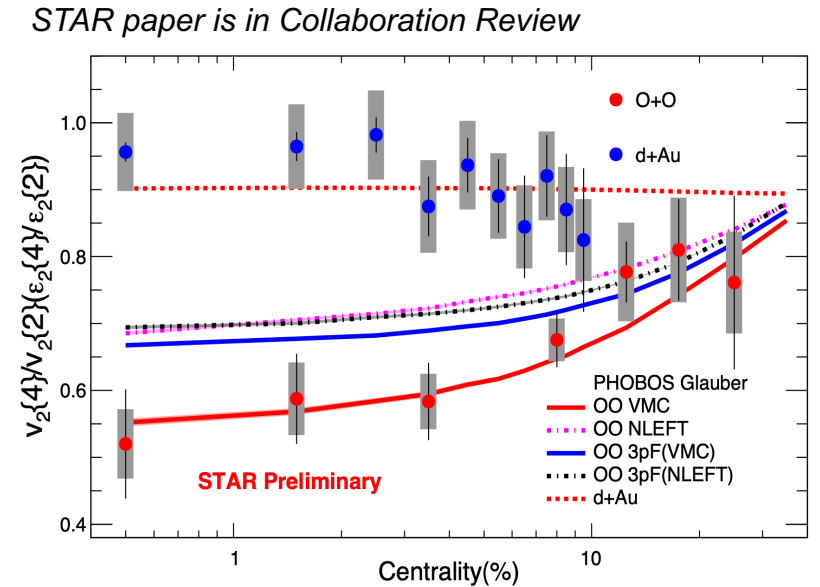


$$\beta_{2\text{U}} = 0.286 \pm 0.025; \quad \gamma_{\text{U}} = 8.5^\circ \pm 4.8^\circ$$

$$\beta_{3\text{U}} = 0.08 - 0.1; \quad \beta_{3\text{U}} \sim \beta_{4\text{U}}$$



difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 <i>fm</i>	0.07 <i>fm</i>



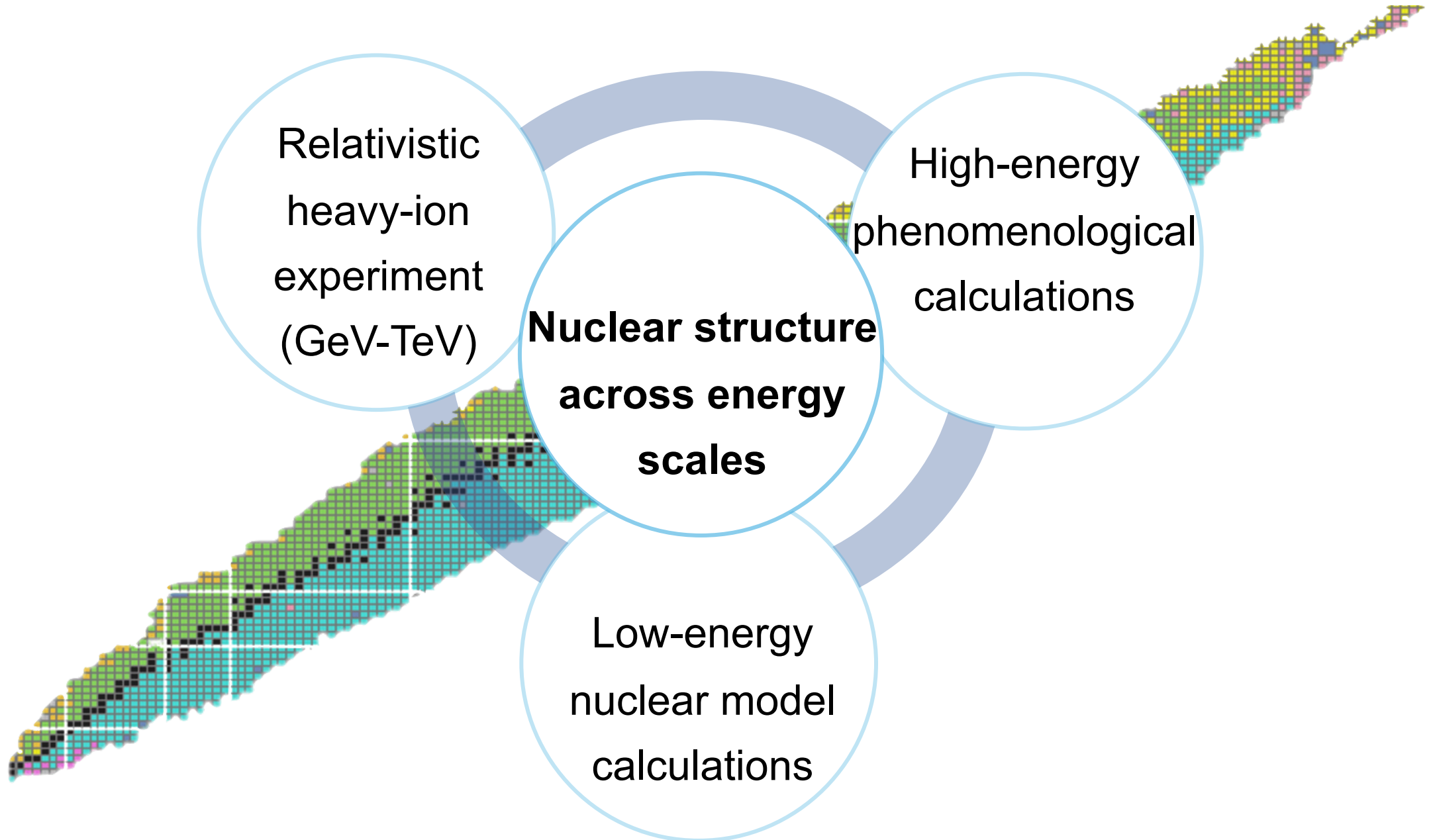
Nucleon-nucleon correlation is remarkable

2. Many potential applications from large to small collision systems :

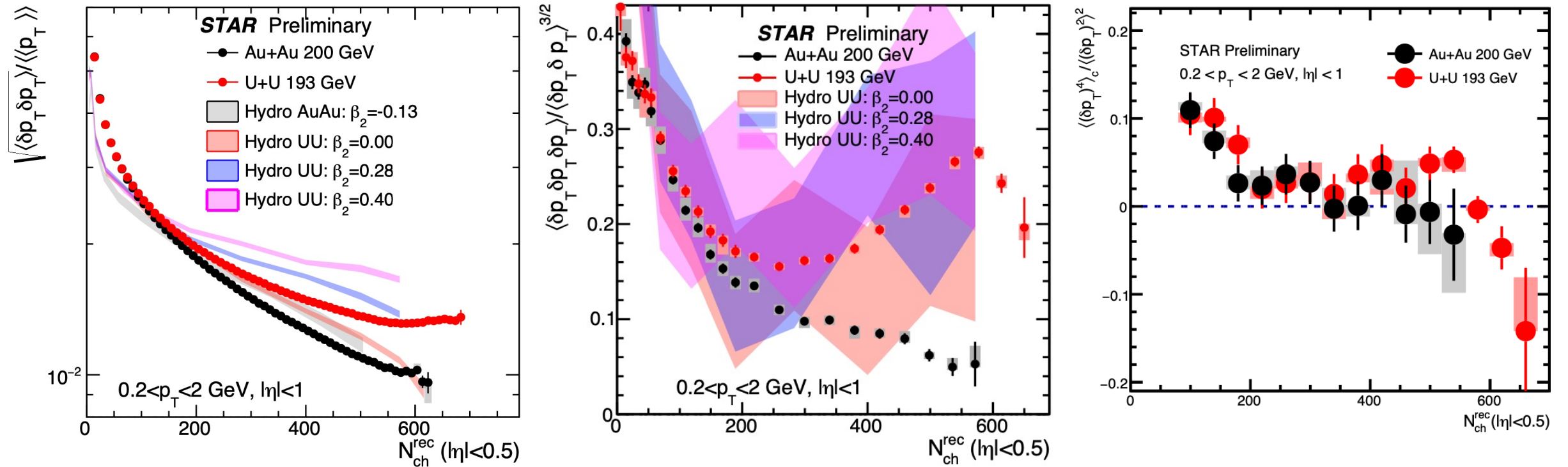
Nuclear mass number (A)

- Nucleosynthesis, nuclear fission, $0\nu\beta\beta$
- Rigid and soft β_n and γ (shape fluctuations/coexistence)
- Neutron skin
- Energy evolution between GeV/TeV and MeV in even-and odd-A nuclei

IV. Conclusions and Outlooks



[p_T] fluctuations as other novel tool



Au+Au: variance and skewness follow independent source scaling $1/N_s^{n-1}$ within power-law decrease

U+U: large enhancement in normalized variance and skewness and sign-change in normalized kurtosis
→ size fluctuations enhanced

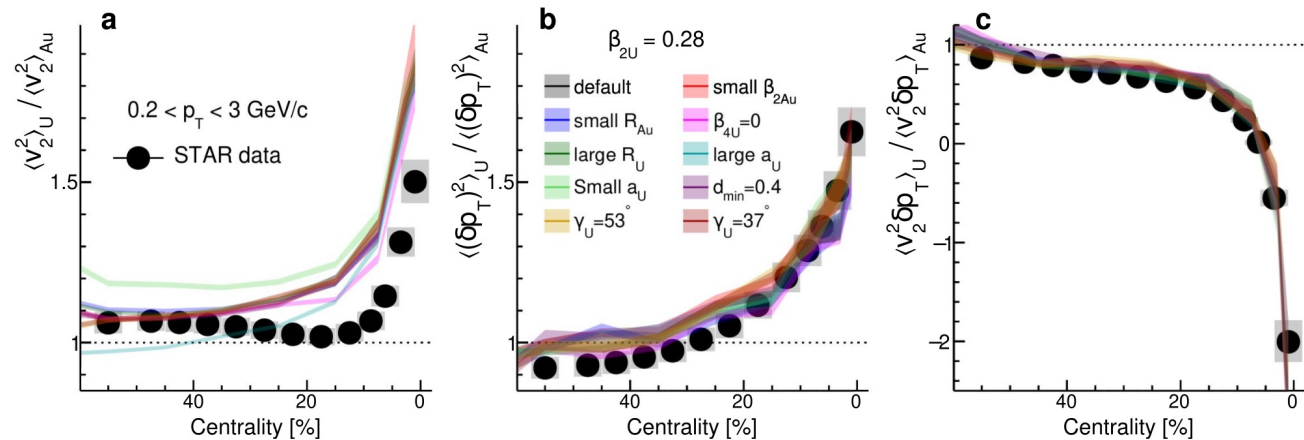
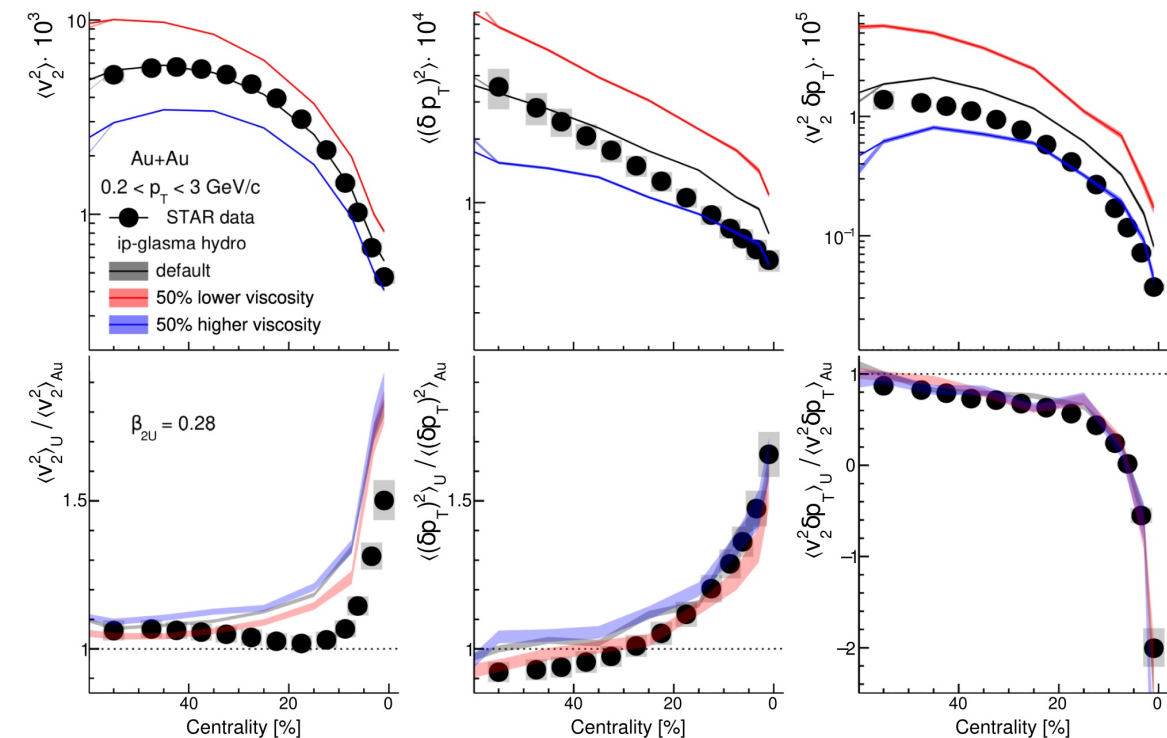
The nuclear deformation role is further confirmed by hydro calculations. But we need more statistics.

[p_T] fluctuations also serve as a good observable to explore the role of nuclear deformation.

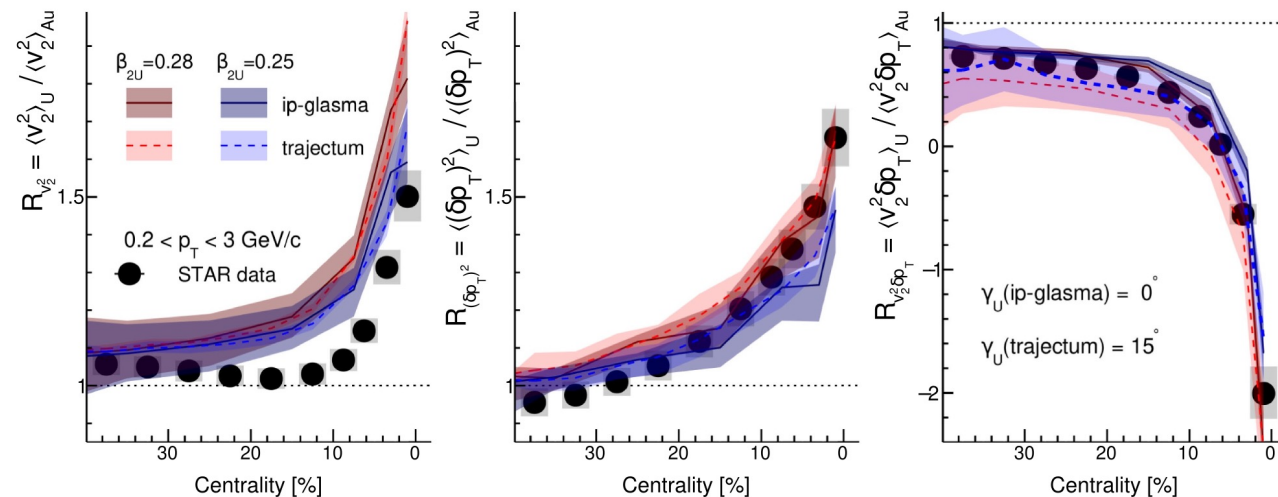
Viscosity, nuclear parameters, and model variations

2) Effect from nuclear parameters are small, included as model systematics.

1) Taking the ratios cancels the viscosity effects.



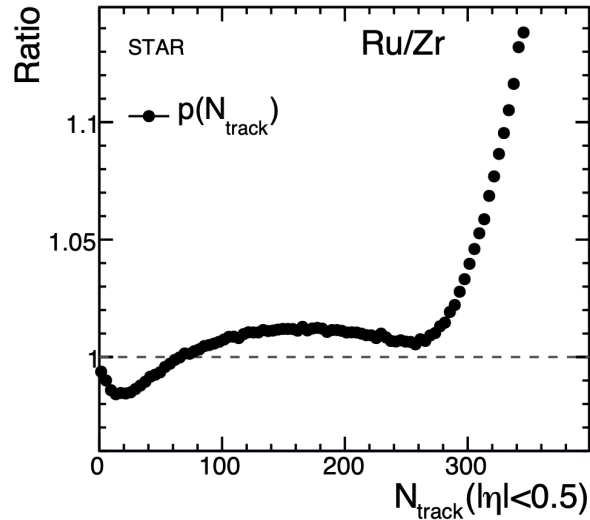
3) Another hydrodynamics model, Trajectum, shows rather consistent extractions even if it was not tuned to RHIC data.



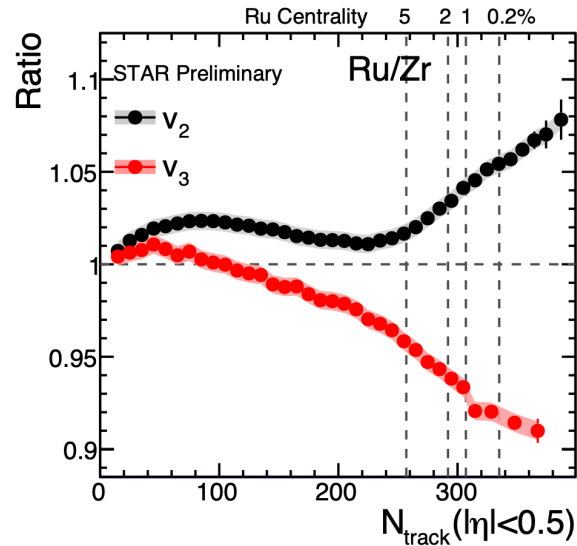
Extracted $\beta_{2,U}$ and γ_U values are robust.

Nuclear structure is inherent of heavy-ion probes

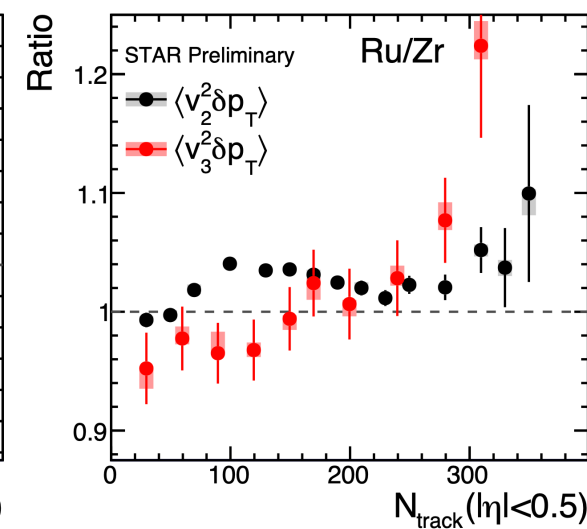
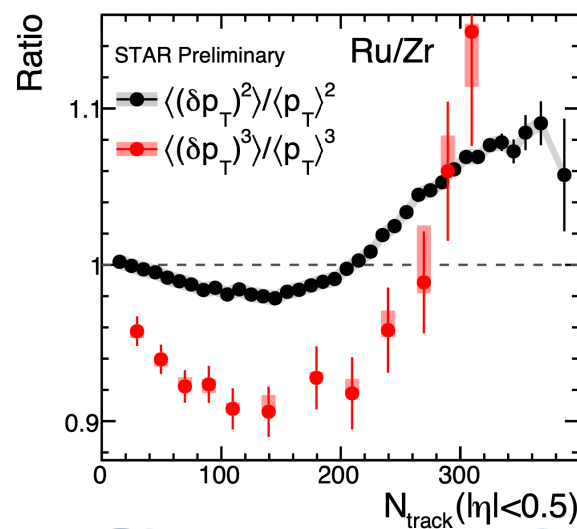
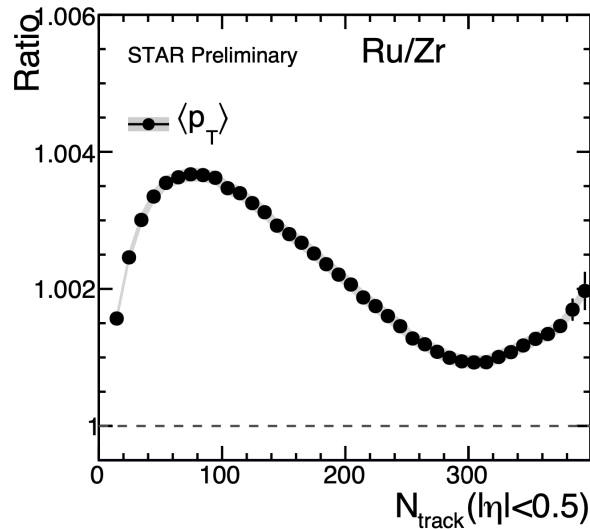
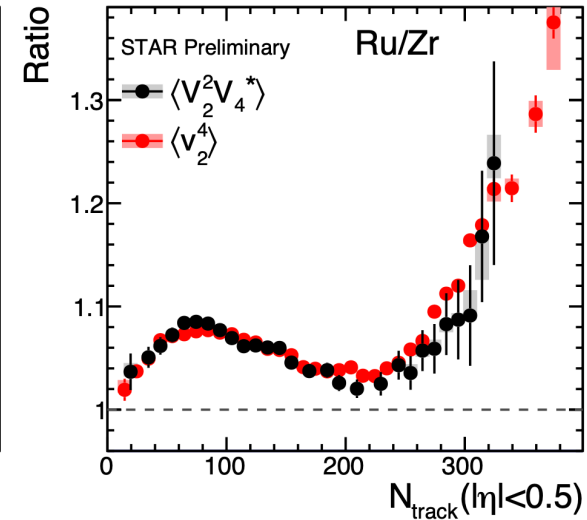
one-body distribution



two-body correlations



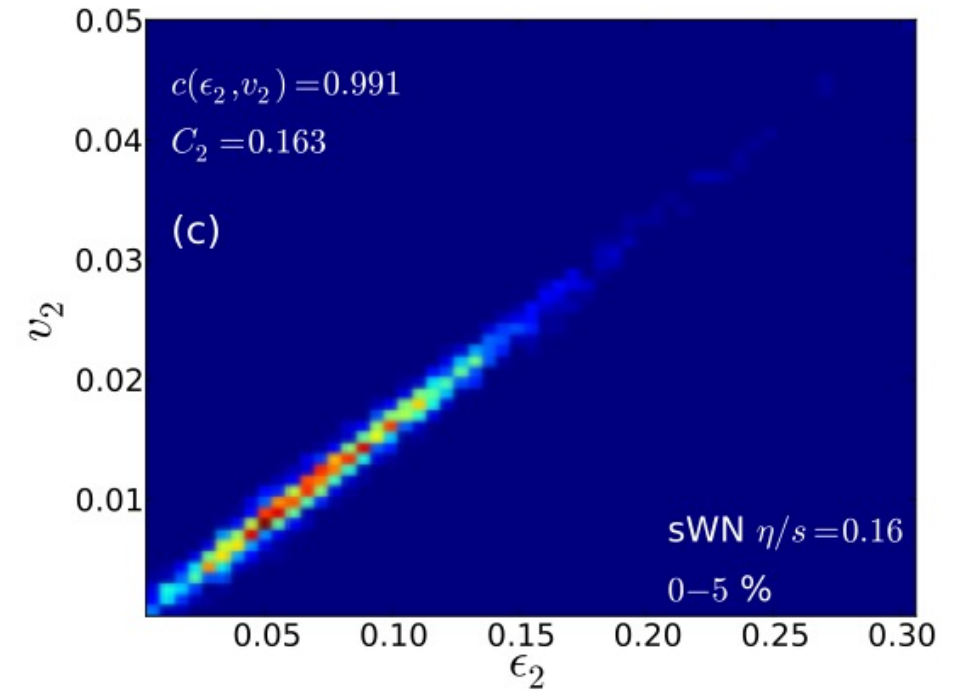
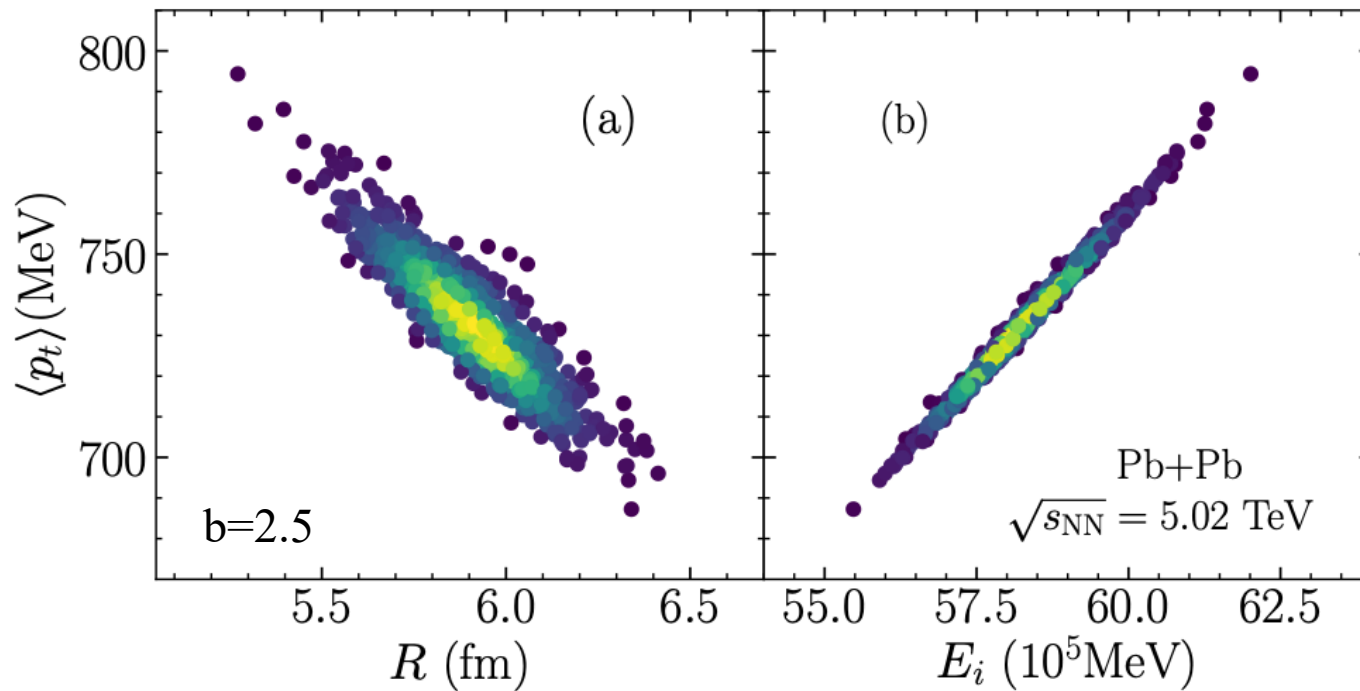
three-body correlations



Linear response in ultra-central collisions

$$\frac{\delta[p_T]}{[p_T]} \propto -\frac{\delta R_{\perp}}{R_{\perp}}$$

$$V_n \propto \mathcal{E}_n$$

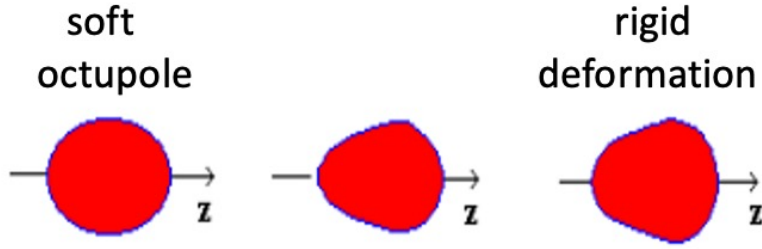


G. Giacalone, F. Gardim, J. Hostler, J. Ollitrault, et al, PRC 103, 024909 (2021)

H. Niemi, G. Denicol, H. Holopainen, P. Huovinen, PRC 87, 054901 (2013)

Probe $\beta_{3,U}$ and its fluctuation

Octupole collectivity



$$\langle \beta_3^2 \rangle = \bar{\beta}_3^2 + \sigma_{\beta_3}^2$$

$$c_{n,\epsilon}\{2\} = \langle \epsilon_n^2 \rangle \approx \langle \epsilon_{n,0}^2 \rangle + \langle p_n p_n^* \rangle \langle \beta_n^2 \rangle$$

$$\begin{aligned} c_{n,\epsilon}\{4\} &= \langle \epsilon_n^4 \rangle - 2\langle \epsilon_n^2 \rangle^2 \\ &\approx \langle \epsilon_{n,0}^4 \rangle - 2\langle \epsilon_{n,0}^2 \rangle^2 + \langle p_n^2 p_n^{2*} \rangle \langle \beta_n^4 \rangle - 2\langle p_n p_n^* \rangle^2 \langle \beta_n^2 \rangle^2 \end{aligned}$$

Four-particle correlation is linearly scaled to $\langle \beta_{3,U}^4 \rangle$.

A way to discriminate between static and dynamic collective modes in high-energy nuclear collisions

L. Liu, C. Zhang, J. Chen, J. Jia, X. Huang, Y. Ma, 2509.09376

