





Emergence and quantification of collective effects across collision systems

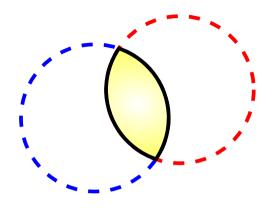
PRECISION FRONTIER OF QCD MATTER:
INFERENCE AND UNCERTAINTY
QUANTIFICATION. CCNU WUHAN
4.9.2025

Jasper Parkkila

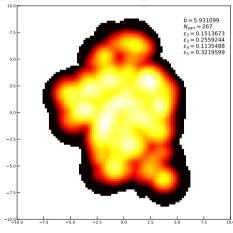
#### Talk ouline

- 1. Collective-like effects in heavy-ion collisions, theory and experiment
- 2. Transport properties from LHC and RHIC observables
- 3. Small system collective-like effects
- 4. Signatures of medium
- 4. Light-ion mid-point results

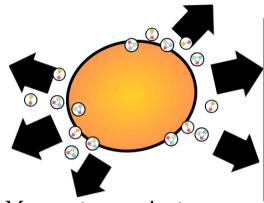
# Origin of collectivity in experiment and theory



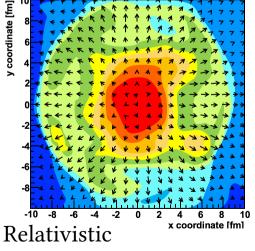
Spatial anisotropy



Initial condition models



Momentum anisotropy



hydrodynamics

#### ▶ Experiment

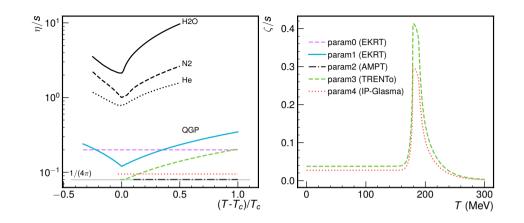
- Strongly-interacting **medium** is formed in collisions according to several experimental indicators
- This medium is fluid-like, implied by **anisotropic** particle momentum pattern of the hadronic products
- The anisotropic expansion is a result of **collective** behaviour, and is very prominent in heavy-ion system

#### ▶ Theory

- Hydrodynamics is a mainstream description of the medium
- The system undergoes a fluid-like expansion under the pressure gradients of the initial stage geometry
- Successful description of wide range of experimental observables
- Medium properties characterized by shear and bulk resistance to evolution over time

$$T^{\mu\nu}=eu^{\mu}u^{\nu}-(P+\Pi)\Delta^{\mu\nu}+\pi^{\mu\nu},\quad \sigma_{\mu}T^{\mu\nu}=0$$

# Transport properties of the hydrodynamic theory



#### ▶ Specific shear viscosity

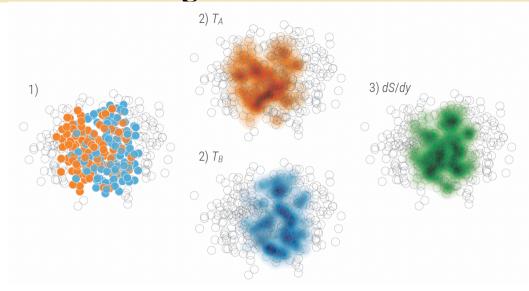
$$\frac{\eta}{s}(T) = \left(\frac{\eta}{s}\right)_{\min} + \left(\frac{\eta}{s}\right)_{\text{slope}} (T - T_{\text{c}}) \left(\frac{T}{T_{\text{c}}}\right)^{(\eta/s)_{\text{crv}}}$$

#### ▶ Specific bulk viscosity

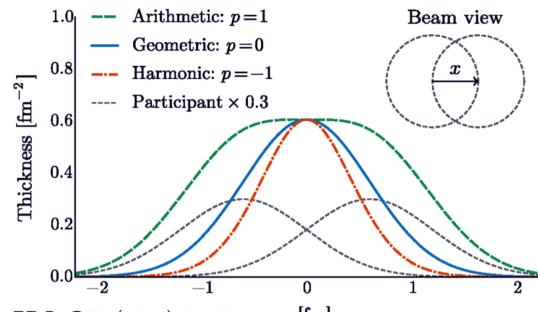
$$rac{\zeta}{s}(T) = rac{(\zeta/s)_{ ext{max}}}{1+\left(rac{T-(\zeta/s)_{ ext{T}_{ ext{peak}}}}{(\zeta/s)_{ ext{width}}}
ight)^2}$$

Parameter	Description	
$T_{ m c}$	Temperature of const. $\eta/s(T)$ , $T < T_{\rm c}$	
$n/s(T_{ m c})$	Minimum $\eta/s(T)$	
$(\eta/s)_{\mathrm{slope}}$	Slope of $\eta/s(T)$ above $T_{ m c}$	
$(\eta/s)_{ m crv}$	Curvature of $\eta/s(T)$ above $T_{ m c}$	
$(\zeta/s)_{T_{peak}}$	Temperature of maximum $\zeta/s(T)$	
$(\zeta/s)_{ m max}$	Maximum $\zeta/s(T)$	
$(\zeta/s)_{ m width}$	Width of $\zeta/s(T)$ peak	
$T_{ m switch}$	Switching / particlization temperature	
N(E)	Overall normalization for collision energy ${\cal E}$	
p	Entropy deposition parameter	
w	Nucleon width	
$\sigma_{ m k}$	Std. dev. of nucleon multiplicity fluctuations	
$d_{ m min}^3$	Minimum volume per nucleon	
$ au_{ m fs}$	Free-streaming time	

#### Phenomelogical initial conditions



[			
Parameter	Description		
N(E)	Overall normalization for collision energy $E$		
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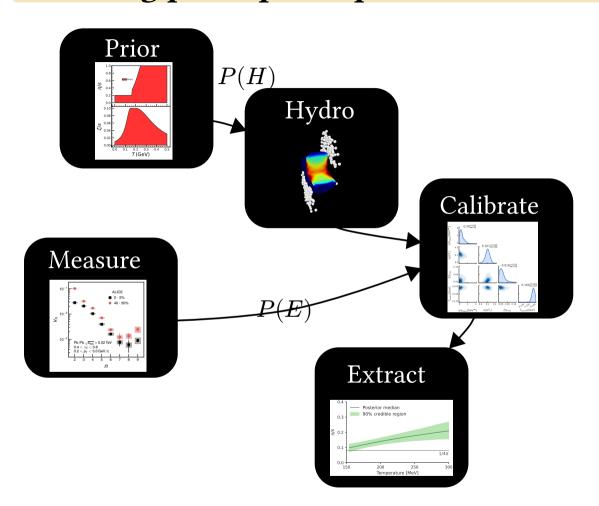
PRC. **C92** (2015) 011901 **x** [fm]

$$rac{\mathrm{d}E}{\mathrm{d}x_{\perp}\,\mathrm{d}\eta_{s}} = \mathrm{Norm} imes \left(rac{T_{\mathrm{A}} + T_{\mathrm{B}}}{2}
ight)^{1/p}$$

$$T_{
m A,B} = \int {
m d}z 
ho_{
m A,B}(x\pm b/2,y,z)$$

$$\rho_{\rm nucleon}(x) = \frac{1}{\left(2\pi w^2\right)^{3/2}} \exp(-|x|^2/2w^2)$$

### Working principle of parameter estimation



#### Bayes' theorem

$$P(H|E) = \frac{P(E|H) \cdot P(H)}{P(E)}$$

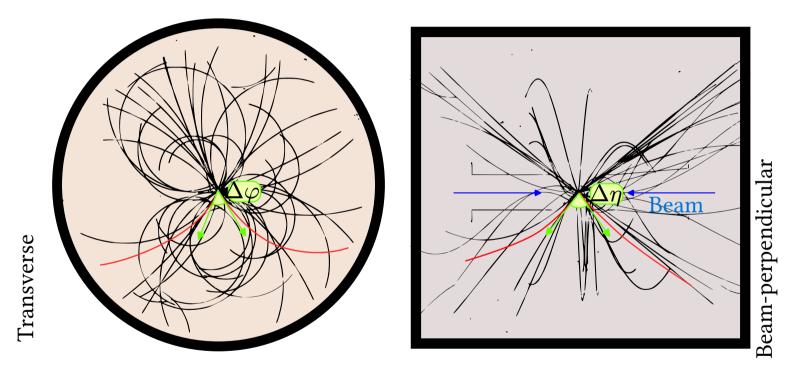
$$P(E) = \sum_{i=1}^{n} P(E|H_i)P(H_i)$$

Posterior: P(H|E): prob. of H given E (experimental data)

- Find optimal set of model parameters that best reproduce the experimental data.
- Utilize constraints, such as flow observables, to help narrow down the  $\eta/s(T)$  etc.
- Massive computational cost: need to probe the entire 14-parameter space with sufficient statistics

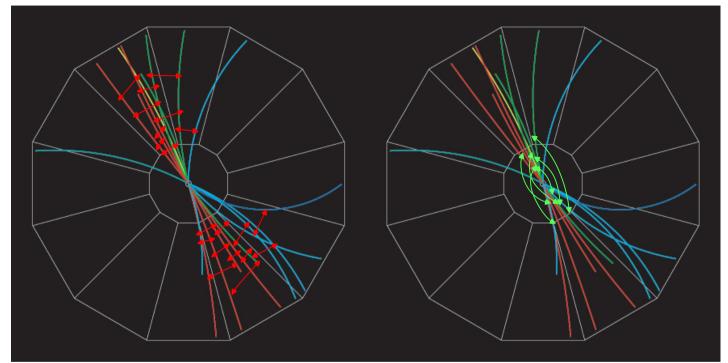
### **Experimental quantification**

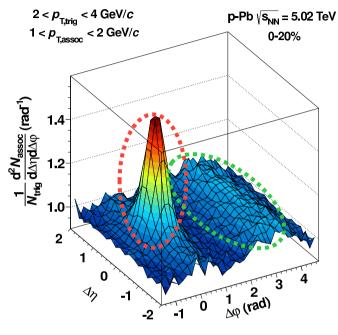
- Experimentally, only final-stage particles and their attributes can be measured
- How can the collective-like effects be experimentally quantified?



• Two-particle azimuthal correlations: measurement of the polar angle  $\Delta \varphi$  and pseudorapidity  $\Delta \eta$  between all pairs of charged particles coming from the collision. What sort of correlations can be observed?

# Two-particle correlation: typical general features in $(\Delta \eta, \Delta \varphi)$





ALICE, PLB. 719 (2013) 29-41

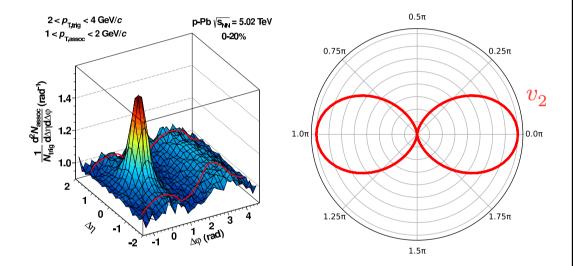
Particles from the same jet at low  $\Delta\eta\Delta\varphi$  form the near-side peak

Particles from back-to-back jets at  $\Delta \varphi \sim \pi$  form the away-side ridge

pp event in STAR experiment

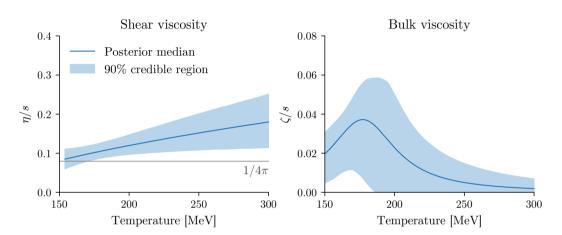
# Long-range correlations

 Collective-like effects manifest themselves as the double-ridge structure in the long-range correlations



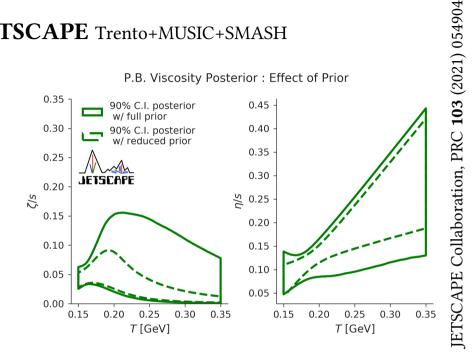
• The double-ridge emerges when a large *elliptic* harmonic component is present: characterizes the elliptic expansion

Modes of expansion are chacterized through the flow coefficients  $v_n$ :  $\frac{\mathrm{d}N}{\mathrm{d}\Delta\varphi} \propto 1 + \sum_{n=1}^{\infty} v_n^2 \cos(\Delta\varphi).$ 10-**ALICE** 0 - 5% 40 - 50%  $10^{-3}$ Pb-Pb  $\sqrt{s_{NN}}$  = 5.02 TeV  $0.4 < |\eta| < 0.8$  $0.2 < p_T < 5.0 \, \text{GeV/c}$ n



Steffen A. Bass et al., Nature Physics (2019)

#### **JETSCAPE** Trento+MUSIC+SMASH

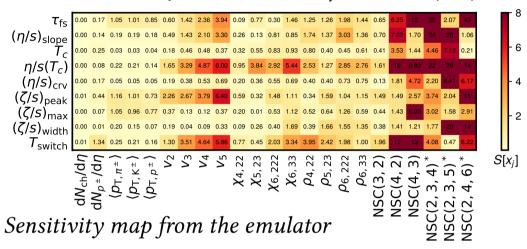


- A number of studies done by 2021 utilizing mostly low-harmonic and 2.76 TeV observables
- Still rather large uncertainty for both  $\eta/s(T)$  and  $z\eta/s(T)$ . Can uncertainty be improved?
- Duke and JETSCAPE provide open source setups for hydrodynamics and bayesian parameter estimation good starting point phenomelogy work
- Started with JETSCAPE, soon move over to Duke setup

#### Our arsenal of observables from ALICE

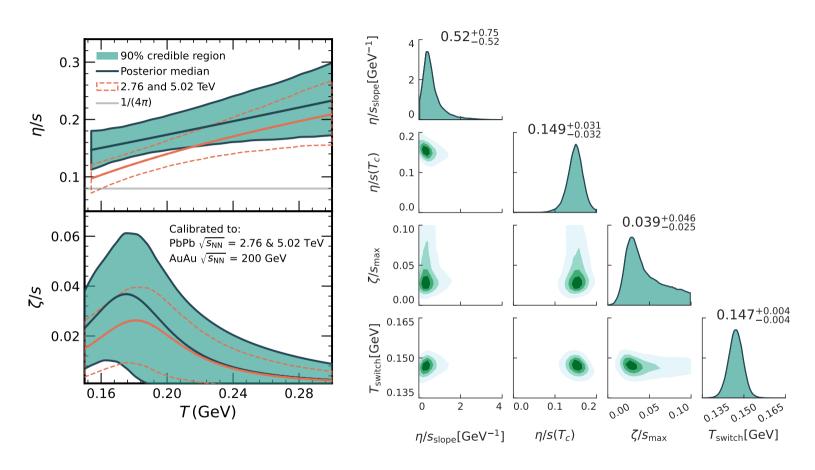
Name	Symbol	Sensitivity- stochastic approach
(High harmonic) Flow coefficients	$v_n$	Average $\langle \eta/s \rangle$ , $\langle \zeta/s \rangle$
Non-linear flow mode coefficients	$\chi_{n,mk}$	$\eta/s(T)$ at the freeze-out
Symmetry-plane correlations	$ ho_{n,mk}$	$\eta/s(T)$ temperature dependence
(Normalized) symmetric cumulants	$\begin{array}{c} \text{(N)SC}(k,l,m) \\ \langle v_m^2 v_n^2 \rangle \end{array}$	
Asymmetric cumulants	$\begin{array}{c} \mathrm{AC}_{\mathbf{a},\mathbf{b}}(k,l,m) \\ \langle v_m^{2\cdot\mathbf{a}}v_n^{2\cdot\mathbf{b}} \rangle \end{array}$	
$N_{ m ch}$ spectra and avg. transverse momentum	$N_{p^\pm}/\mathrm{d}\eta, \langle p_\mathrm{T} angle$	$T_{ m switch}$ and $ au_{ m fs}$

J.E. Parkkila, et. al, Phys. Lett. B 835 (2022) 137485



- More advanced multi-particle observables beyond the  $v_n$  present unique sensitivity to various stages of the evolution
- More sensitive observables have more constraining power
- Observables should be independent of from other

### Parameter estimation using advanced azimuthal correlations



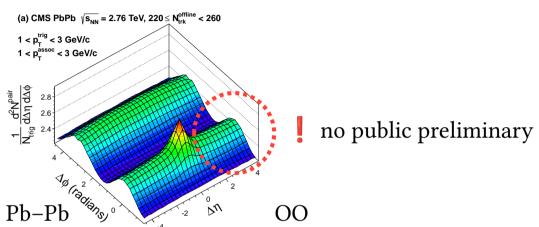
Our latest calibration includes data from LHC Pb–Pb at 5.02 + 2.76 TeV and RHIC Au–Au at 200 GeV.

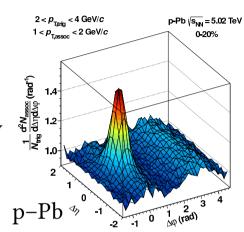
- Parameters well constrained despite 3 collision systems and many observables
- Larger uncertainty than
   Pb-Pb alone (2022 study)
- Model limitations, choice of centrality etc.

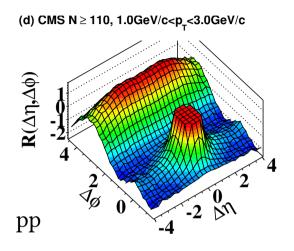
- M. Virta, J.E. Parkkila, D.J. Kim, PRC. 111 (2025) 044903
- J.E. Parkkila, **et. al**, Phys. Lett. B **835** (2022) 137485

# Collective-like effects in various collision systems

• This signal is present across various collision system sizes

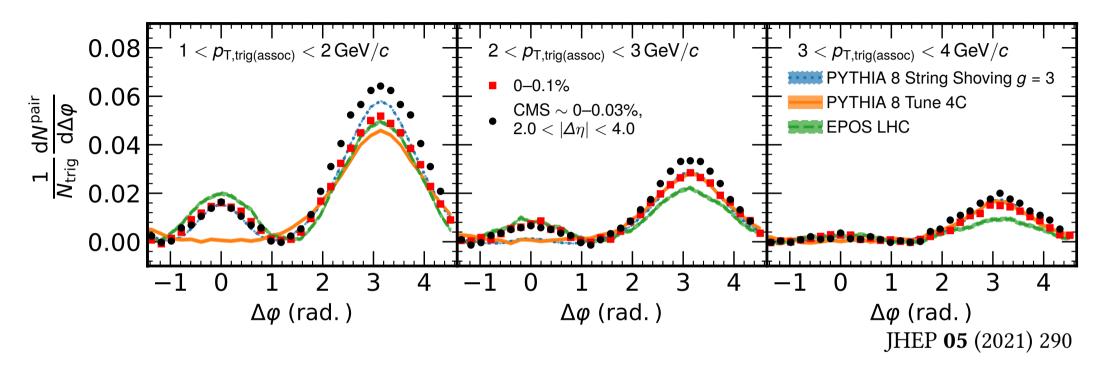






- Long-range correlation emerges during the early stages
- In heavy-ion systems this is the medium response to initial stage geometry
- Light-ion: likely medium response
- p-Pb and pp: medium-like, but might be something else
- In small systems the origin is unclear (QGP? Multi-parton scattering? Ropes? Initial-stage effect?)

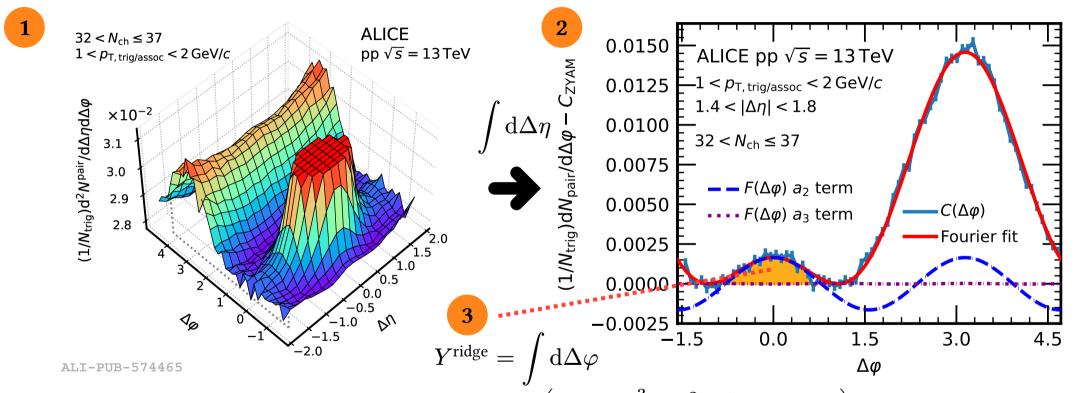
# Long-range correlations in pp: basic findings



- Prominent long-range near-side ridge in high multiplicity ( $N_{\rm ch} > 110$ ) collisions
- Small signal in minimum bias (0–100%)
- How small can the system get and still exhibit these signals?
- Several theoretical approaches with or without medium

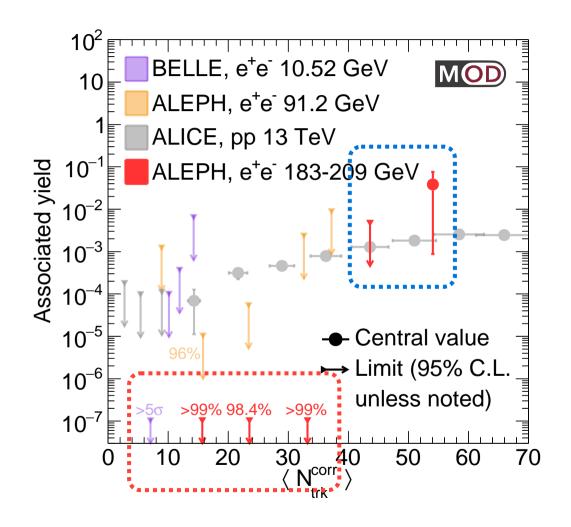
# Ridge-yield as quantification for collective-like effects

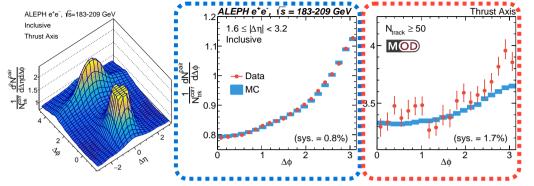
• Near-side ridge clearly visible in high-multiplicity events



- Find the baseline and  $|\Delta \varphi_{\min}|$  by fitting  $F(\Delta \varphi) = A \Big(1 + 2 \sum_{n=1}^3 v_n^{2, \mathrm{cent}} \cos(n \Delta \varphi)\Big) + C_{\mathrm{ZYAM}}$  to the signal
- Measured in  $1.4 < |\Delta \eta| < 1.8$  to suppress the short-range non-flow correlations
- $p_{\rm T}>1.0~{
  m GeV}/c$  (trig and assoc) to avoid near-side jet broadening into  $|\Delta\eta|>1.4$

# Ridge yield in e<sup>+</sup>e<sup>-</sup> collisions

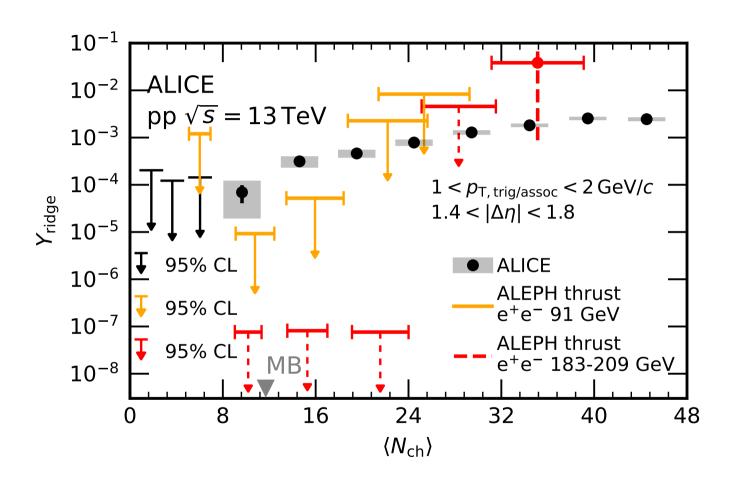




pp system details are intricate. Study the simpler processes involved in e<sup>+</sup>e<sup>-</sup> annihilations (point-like collision: no uncertainties on initial geometry or parton distribution function description)

- No yield in the lowest multiplicities  $N_{
  m ch} < 10$
- Would we get similarly small values in pp as in  $e^+e^-$  or are the two systems intrinsically different?

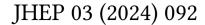
# Ridge yield in low-multiplicity pp

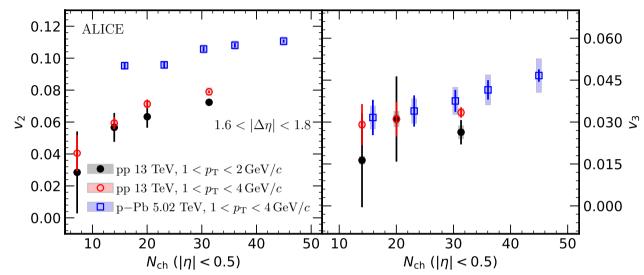


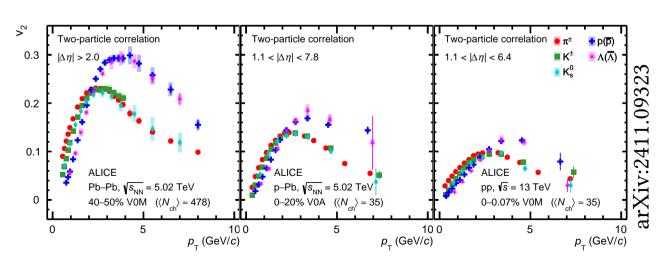
PRL. **132** (2024) 172302

- Non-zero yield even in very low multiplicity collisions (95% C.L)
- First quantitative constraints of yield in smallest hadronic collisions
- 5–6 $\sigma$  larger yield in pp compared to  $e^+e^-$  collisions
- A comparison to e<sup>+</sup>e<sup>-</sup> can provide insight to what processes might or do not contribute to the yield
- A reference point-like collision can also help understand the magnitude of initial stage effects

# Flow in pp



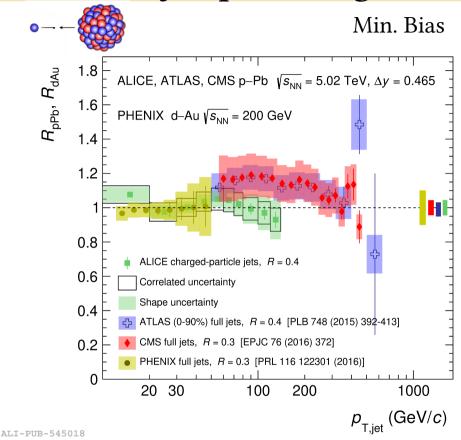




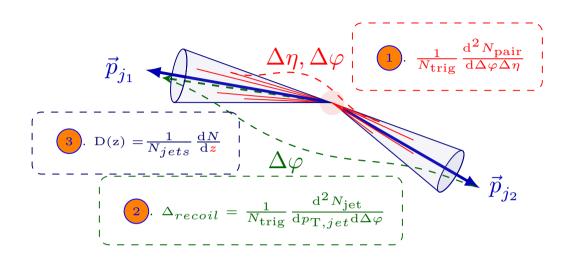
- Significant flow  $v_2$  and  $v_3$  measured in pp and pPb
- Even mass ordering is observed
- Evident that everything from small to large systems flows

J.E. Parkkila

# Search for jet quenching effects in small systems



• Even though flow signatures are observed, no sign of jet quenching in small systems (ALICE, JHEP **05** (2024) 041)



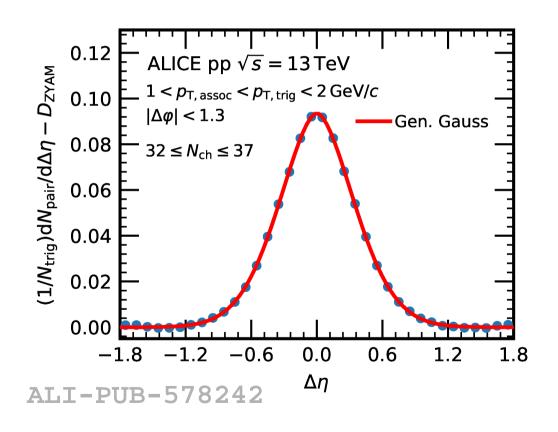
How about multiplicity dependence in pp collisions?

- 1. hadron-hadron correlations? (presented today)
- 2. hadron-jet correlations (JHEP **05** (2024) 229)
- 3. intra-jet correlations (Eur.Phys.J **C84** (2024) 1079)
- ▶ Multiplicity dependence of di-hadron correlations

Robust test against Pb-Pb reference

# Quantification of jet modification

Aim to quantify the modification of the jet correlation shape over various multiplicity bins.



Fit a generalized Gaussian over  $\Delta \eta$ -projection of the correlation function over  $\Delta \varphi \in [-1.3, 1.3]$ .

$$A + \frac{1}{2\alpha\Gamma(1/\beta)} \exp\left[-\left(\frac{|x|}{\alpha}\right)^{\beta}\right],$$

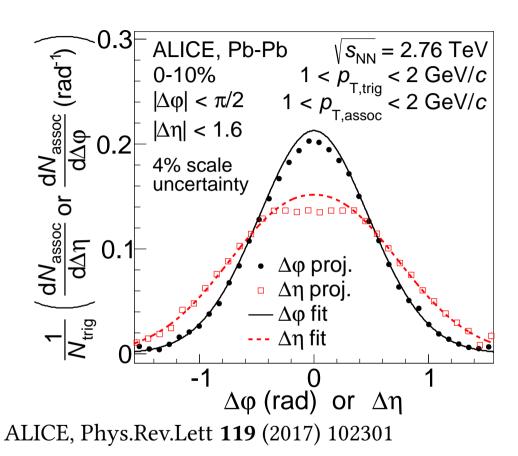
where

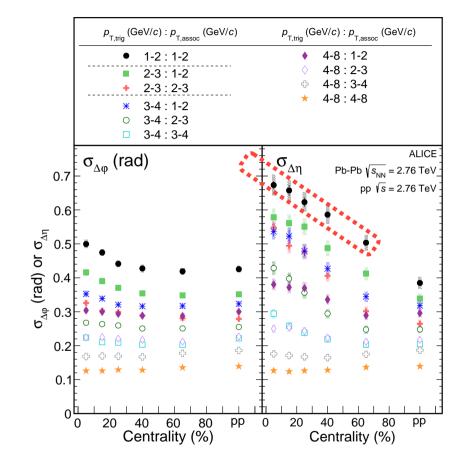
$$\sigma = \sqrt{\frac{\alpha^2 \Gamma(3/\beta)}{\Gamma(1/\beta)}}$$

#### Broadening

Greater  $\sigma_{\Delta\eta}$  toward larger (higher multiplicity) collisions. This can signal the presence of jet quenching, and therefore, likely medium.

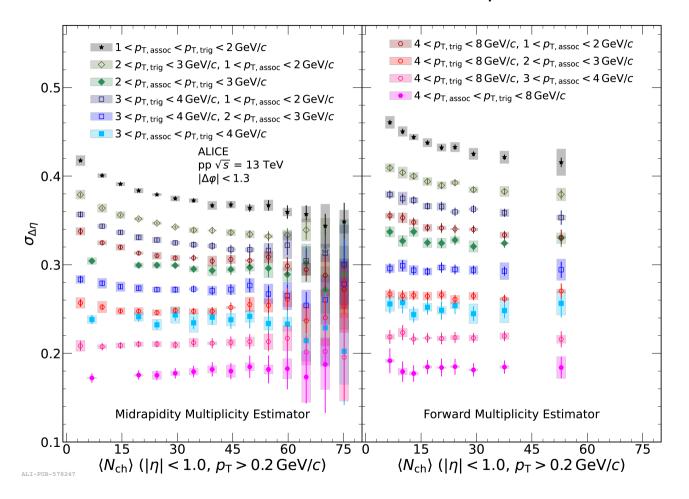
### Broadening of jets in Pb-Pb collisions





- Broadening of the jet fragmentation peak in various kinematic regions observed in heavy-ion collisions.
- Abnormal and wider in  $\Delta\eta$  direction than  $\Delta\varphi$

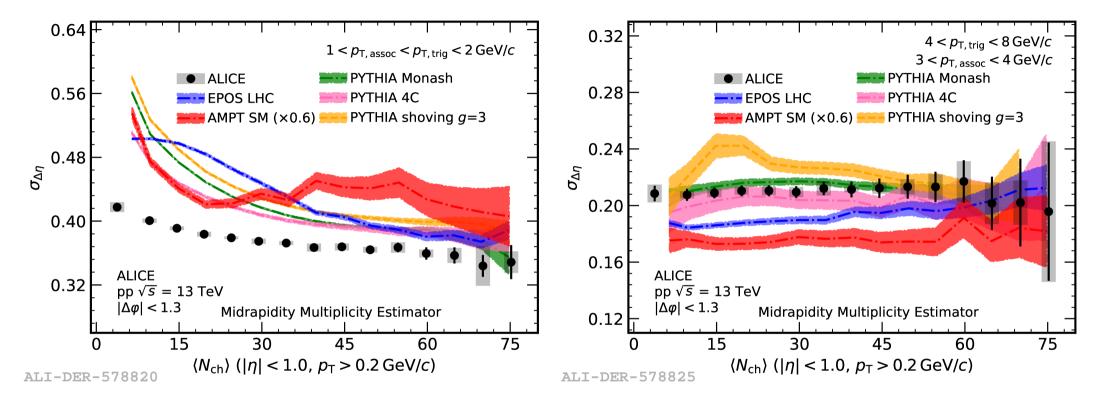
# Multiplicity dependence of $\sigma_{\Delta_i}$ in pp 13 TeV: width comparison



- Multiplicity dependence decreases for higher  $p_{\rm T}$  and higher multiplicity
  - But could it be because of multiplicity estimator bias?
- Forward multiplicity estimator results have broader jets and weaker multiplicity dependence across almost all  $p_{\rm T}$ -bins
- Clear ordering in the magnitude  $\rightarrow$  narrower peaks towards higher  $p_{\rm T}$
- No signs of jet quenching in pp

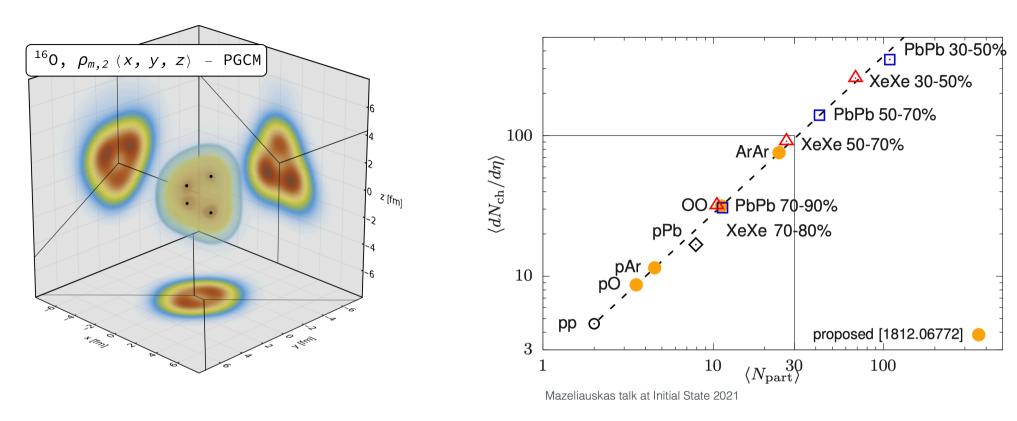
JHEP **03** (2025) 194

#### Model comparisons in pp



- Models overestimate for the lower- $p_{\mathrm{T}}$  but better description for higher- $p_{\mathrm{T}}$
- Trend is captured by most models
- The multiplicity dependence is weaker for higher- $p_T$
- Non-trivial  $p_{\rm T}$  and multiplicity dependence in the models which contains "Jets" + "Flow"
- Caution with your interpretation, introduced biases while producing flow (e.g, EPOS and PYTHIA8-Shoving)
- Not trivial to extract flow from some models (see S. Ji et al., PRC 108 (2023) 034909)

# Jet quenching in light-ion systems: 00?



Expect p–Pb and OO fall into transition region  $\tau_{\rm Hydro}/R \approx 1$  where system is expected to encounter final state interactions, but is also out-of-equilibrium for a significant part of its lifetime. No hint in p–Pb but a sweet spot to oberve jet quenching signal in OO.

# Centrality dependent jet-shape modification in OO

No public preliminary

Jet-shape modification in OO – comparison to Pb-Pb

No public preliminary

Jet-shape modification in OO - comparison to pp reference

No public preliminary

# **Summary**

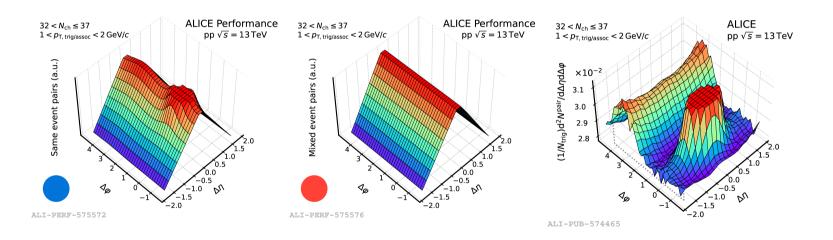
- QGP is created in heavy-ion collisions at the LHC and its evolution governed by relativistic hydrodynamics
- Higher harmonic and independent advanced multi-particle correlations can improve the parameter estimation outcomes
- Flow-like signals are measured even in the smallest collision systems
- However, no jet quenching signals observed in pp

# Backup

### Two-particle correlations: experimental representation

**Two-particle correlation function** between trigger and associated particles  $(p_{T, \rm trig} > p_{T, \rm assoc})$ 

$$\frac{1}{N_{\rm trig}^*} \frac{\mathrm{d}^2 N_{\rm pair}}{\mathrm{d}\Delta\eta\Delta\varphi}(\Delta\eta,\Delta\varphi) = N_{\rm pair}^{*,\rm mixed}(0,0) \frac{N_{\rm pair}^{*,\rm same}(\Delta\eta,\Delta\varphi)}{N_{\rm pair}^{*,\rm mixed}(\Delta\eta,\Delta\varphi)}.$$



(Same- and Mixed-event correlation function, and the corrected outcome.)

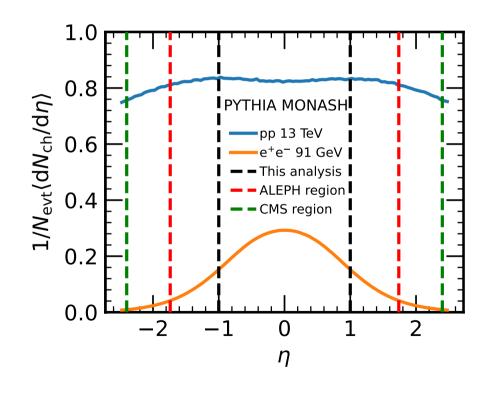
The two-particle correlation method is used to study azimuthal angle distributions of the emitted charged particles, and in turn probe collective-like effects and jet fragmentation interplay with potential medium.

# Conversion of ALEPH multiplicity

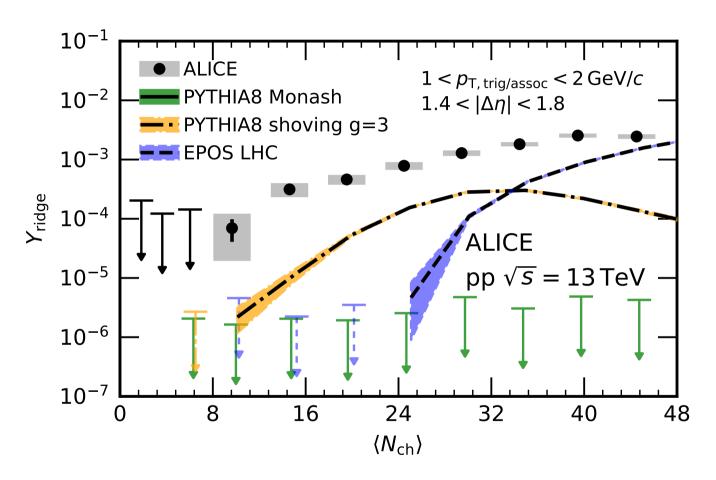
- Estimate the limits of uncertainty on the conversion of the multiplicity
- Target: multiplicity defined by accepted particles within  $|\eta|<1.0,\,p_{\rm T}>0.2\frac{\rm GeV}{c}$
- Multiplicity conversion between different systems and experiments is done using PYTHIA
  - 1. Simulate pp at  $\sqrt{s}=13$  TeV in both experimental acceptances. Multiplicity ratio to obtain  $\alpha_{\rm A}$
  - 2. Simulate e<sup>+</sup>e<sup>-</sup> at  $\sqrt{s}=91$  GeV in both experimental acceptances. Multiplicity ratio to obtain  $\alpha_{\rm B}$

Method	Experiment	Corr. factor $\alpha_{\text{A/B}}$
PYTHIA	ALEPH pp 13 TeV, ALEPH e <sup>+</sup> e <sup>-</sup> 91 GeV	0.57 (A) 0.78 (B)
Flat $dN/d\eta$	ALEPH	0.63

Experiment	$ \eta_{ m max} $	$p_{ m T,min}$	$\sqrt{s}$
ALICE pp	1.0	0.2	13 TeV
ALEPH e <sup>+</sup> e <sup>-</sup>	1.738	0.2	91 GeV



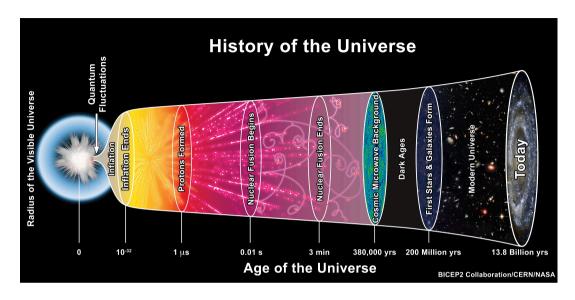
### Low multiplicity pp ridge yield model comparisons

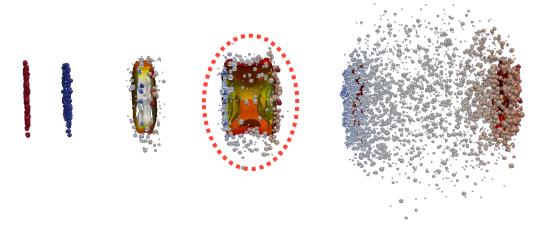


- No ridge from Monash, as expected
- Models with collectivity mechanisms underestimate the ridge yield
- Model ridge yield calculated at large  $2<|\Delta\eta|<4$  to avoid the over-estimated jet fragmentation width

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### Matter in early universe





- Early Universe immediately after Big Bang: free quarks and gluons not confined to hadrons
- Can be created small nuclei-sized droplets at the LHC in heavy-ion collisions
- Study of this matter can improve the understanding on a strongly-interacting system as well as the conditions in early Universe