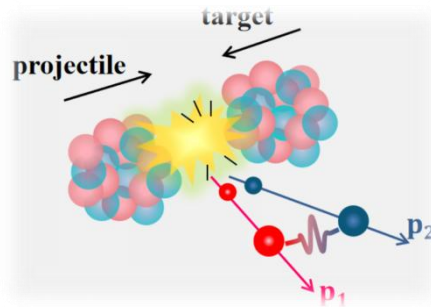




The 2nd International Workshop on Physics at High Baryon Density (PHD2025)

Extract the n-n interaction strength and the
space-time size of neutron emission source
using femtoscopic method



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Outline

1. Introduction: Motivation of the study
2. Experimental setup: CSHINE
3. Results and Discussions
 - ✓ n-n correlation function and (f_0^{nn}, d_0^{nn})
 - ✓ Preliminary p-p correlation function
4. Summary

Heavy Ion collisions and nuclear matter equation of state

01 Neutron Star

Properties, merging of NS is closely related to nEOS via TOV eqs.

Neutron Star

02 N-N Interactions

N-N interactions is the base of nEOS

03 Heavy Ion Collisions

HIC is the unique way to create dense nuclear matter in lab

HIC

N-N interactions

nEOS
 $E_{\text{sym}}(\rho)$

Complication of HIC

Measurement of N-N Interactions

Introduction

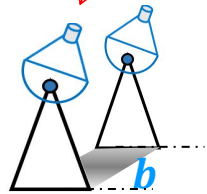
Two questions:

- ① Known from quantum mechanics, the interaction strength (scattering length and effective range) between particles can be measured by scattering experiment. But what if the particles are not stable?
- ② Heavy ion reaction is a violent femtoscopic process lasting for zeptoseconds, how can one measure the temporal-spatial size of such a process?

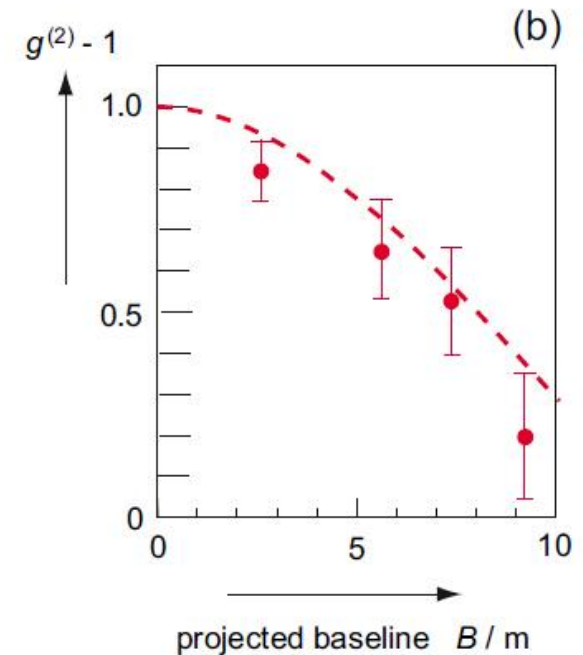
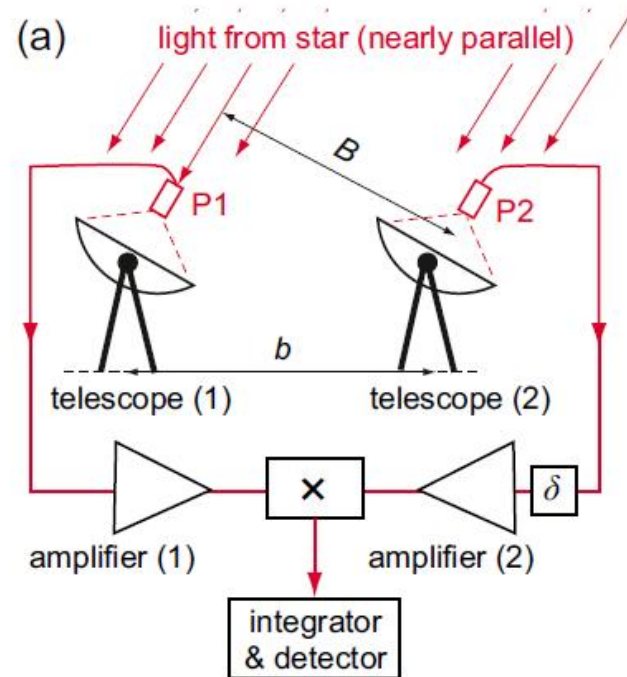
The answers to these two questions point to intensity interferometry!

What is the intensity interferometry (femtoscopic method)

- Invented by Hanbury Brown and Twiss in 1950s to determine the angular radius of Sirius.



$$C(q) = 1 + \frac{P(\mathbf{p}_1, \mathbf{p}_2)}{P(\mathbf{p}_1)P(\mathbf{p}_2)}$$



Hanbury Brown and Twiss, Nature **177**, 27 (1956)
 Hanbury Brown and Twiss, Nature **178**, 1046 (1956)

$$L/d \approx b/\lambda = 10^{7-9}$$

Application extends to nuclear physics

1960s, Goldhaber

π - π correlations

1977, S Koonin

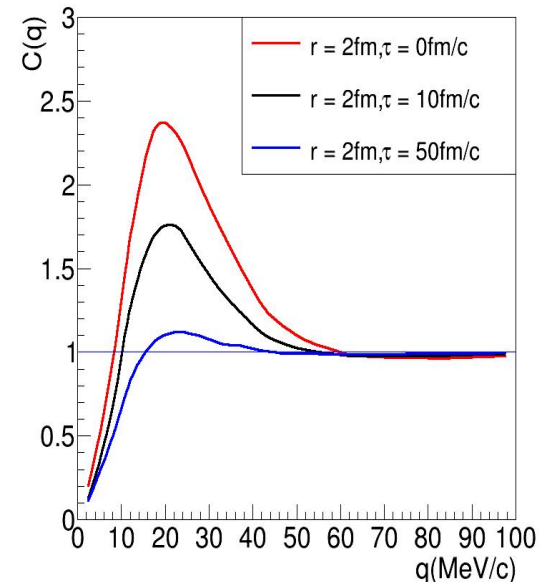
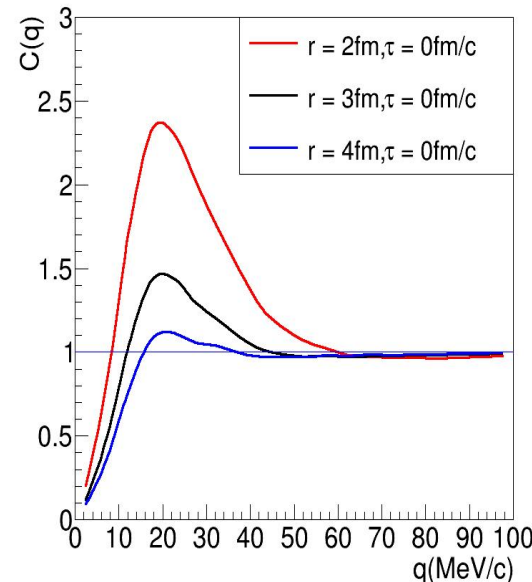
Formation the p-p correlation

1990s, enormously applied in HIC

IMF-IMF correlation functions

2000s, Imaging technique explored using pi-pi and p-p in relativistic HIC

S. Koonin, Phys. Lett. B70, 43 (1977)



Source distribution

$$\frac{1}{\sigma} \frac{d\sigma}{d\mathbf{p}_1 d\mathbf{p}_2} = \int dt_1 dt_2 \int d\mathbf{r}_1 d\mathbf{r}_2 D(\mathbf{r}_1 t_1, \mathbf{p}) D(\mathbf{r}_2 t_2, \mathbf{p}) \times \left\{ \frac{1}{4} |^1\Psi_{\mathbf{p}_1 \mathbf{p}_2}(\mathbf{r}'_1, \mathbf{r}_2)|^2 + \frac{3}{4} |^3\Psi_{\mathbf{p}_1 \mathbf{p}_2}(\mathbf{r}'_1, \mathbf{r}_2)|^2 \right\}$$

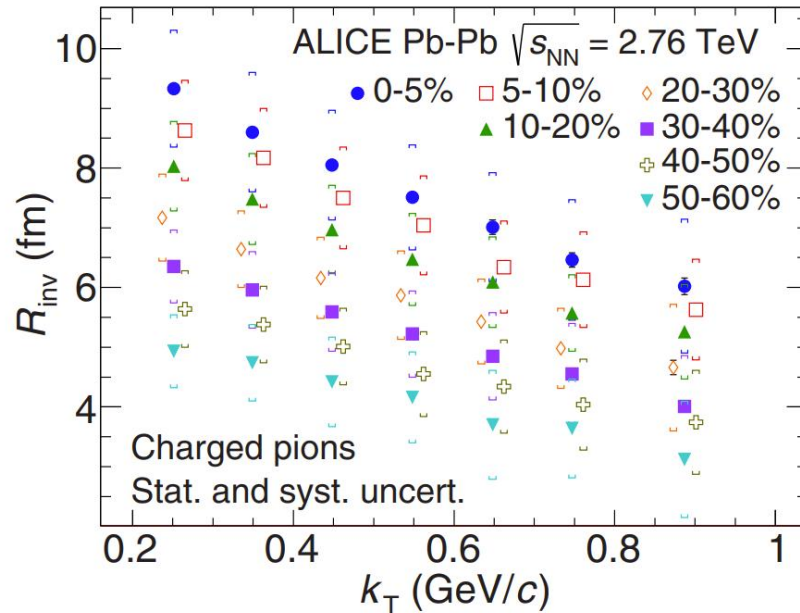
Propagation and p-p wave function of relative motion

$$D(\mathbf{r}, t, \mathbf{p}) = \frac{1}{\sigma} \frac{d\sigma}{d\mathbf{p}} \left[\frac{1}{\pi^{3/2} r_0^3} \exp(- (r - V_0 t)^2 / r_0^2) \right] \left[\frac{1}{\pi^{1/2} \tau} \exp(- t^2 / \tau^2) \right]$$

Correlation Function — To visualize the dynamic evolution of HIC

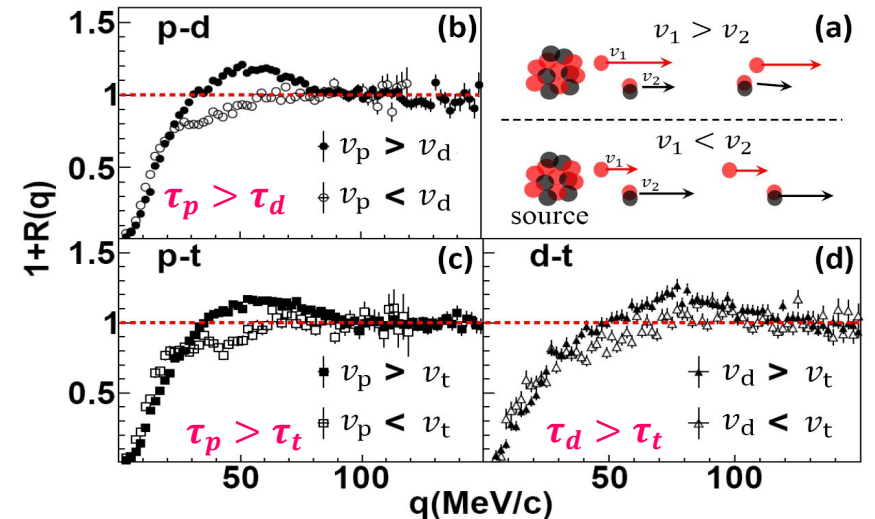
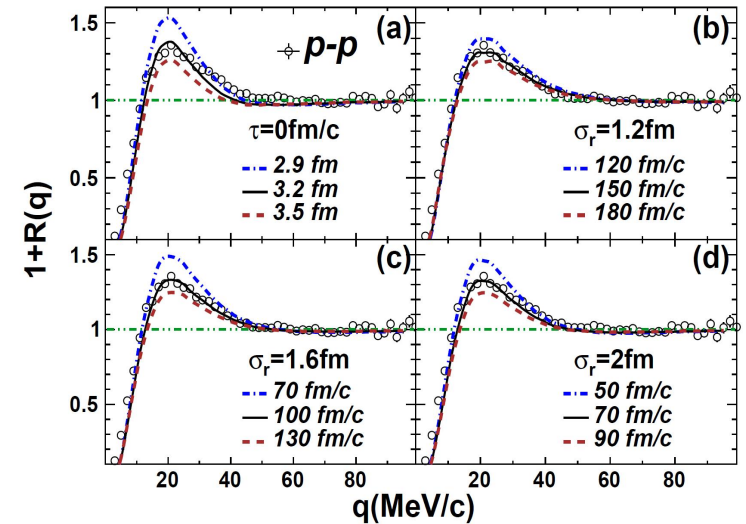
➤ CF carries the spatial-temporal information of the emission source, providing a good tool to constrain transport model as well.

ALICE: Pb+Pb at $\sqrt{s} = 2.76$ TeV



Phys. Rev. C 93,024905(2016)

CSHINE: Ar+Au at 30 MeV/u



Y. J. Wang et al., Phys. Lett. B 825, 136856 (2022)

Correlation Function — To measure the final state interaction of the particle pair

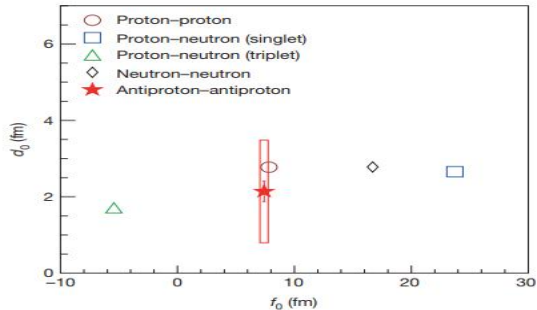
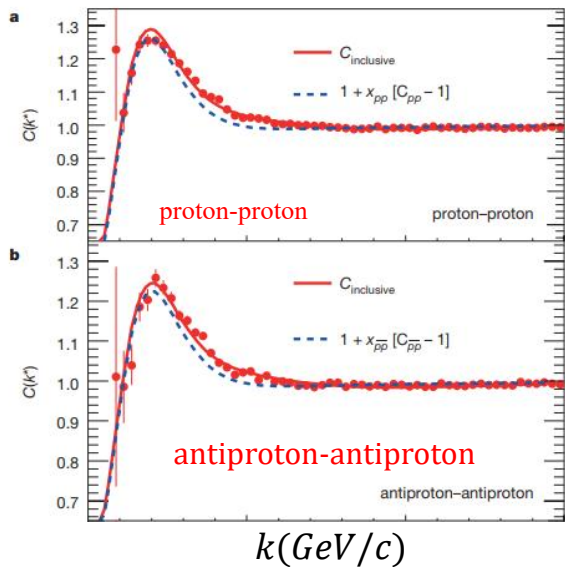
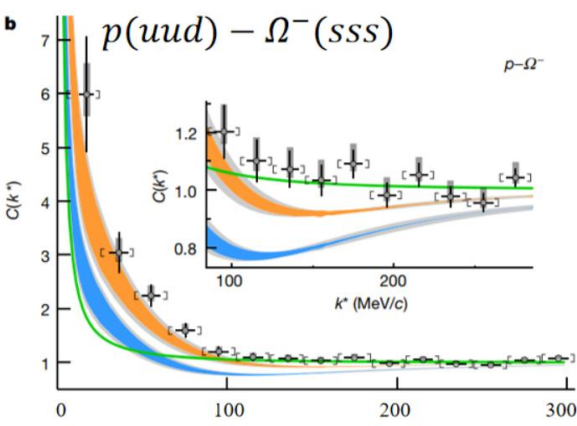
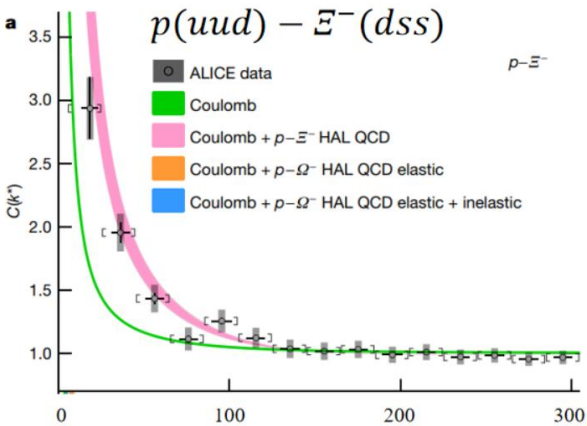
➤ CF measures the scattering length and effective range (f_0, d_0) of particle pair

Solving the Schrodinger equations at low energy(only s-wave), one get two constants (f_0, d_0)

$$\Psi(\vec{k}^*, \vec{r}) \approx e^{-i\vec{k}^* \vec{r}} + f_{k^*}(\theta) \frac{e^{ik^* r^*}}{r^*}$$

$$k \cot(\delta(k^*)) \approx \frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} + O(k^{*4})$$

$$f_{k^*}(\theta) \approx \frac{1}{2k^*_i} (e^{2i\delta} - 1) \approx (\frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - ik^*)^{-1}$$

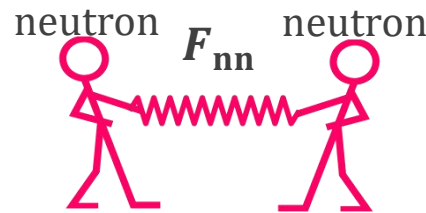
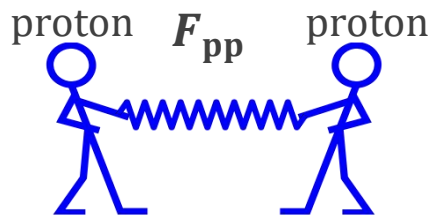


Matter and antimatter Symmetry of the strong interaction

Why neutron-neutron correlation so special

- ① reveal the collision dynamics in terms of the Isospin DOF
- ② determine the n-n (f_0, d_0) — CSB of nuclear force

p-p: ($f_0^{pp} = -17.3 \pm 0.4, d_0^{pp} = 2.85 \pm 0.04$)
 n-n: ($f_0^{nn} = -18.9 \pm 0.4, d_0^{nn} = 2.75 \pm 0.11$)
 R. Machleidt., PRC 63, 024001 (2001)



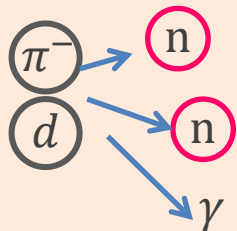
$$\Delta a_{\text{CSB}} = f_0^{pp} - f_0^{nn}$$

nuclear force CSB

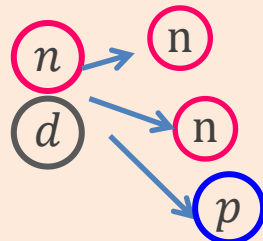
However, no n-n scattering data due to the unavailability of neutron target!

Indirect Scattering:

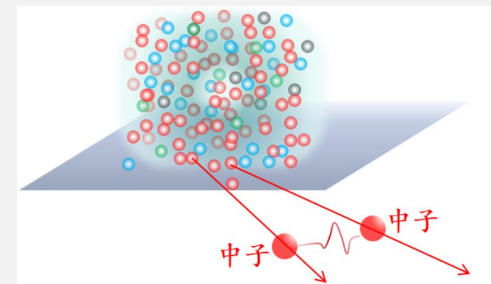
$d(\pi^-, \gamma)2n$



$d(n, p)2n$



Heavy Ion Collisions:



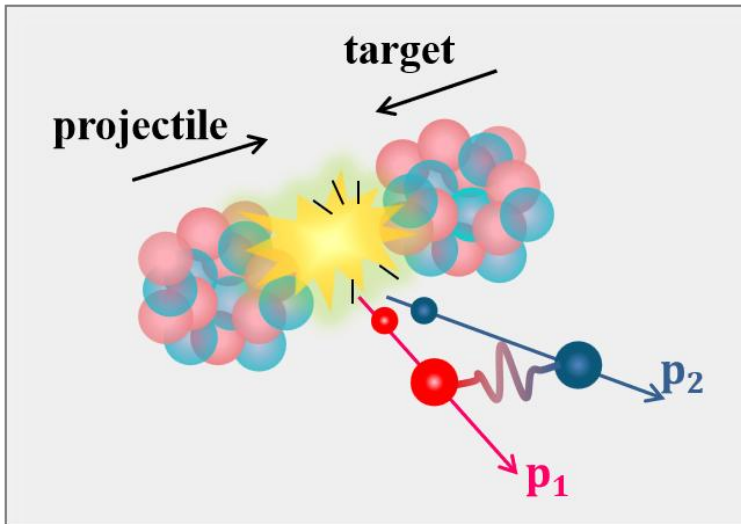
Lednicky and Lyuboshitz propose to extract (f_0^{nn}, d_0^{nn}) via the n-n CF in HIC

Lednický and Lyuboshitz method

Lednický and Lyuboshitz proposed to extract n-n FSI by measuring the n-n correlation function in heavy ion collisions.

Assuming:

- Incoherent emission source
- A smooth emission source
- Correlation beyond 3 bodies negligible



R. Lednický, et al. Sov. J. Nucl. Phys. 35 (1982) 770
 Ann. Rev. Nucl. Part. Sci. 55 (2005) 357-402
 Phys. Rev. C 102 (2020) 3, 034001

Definition

Original momentum CF definition

$$C(\mathbf{p}_1, \mathbf{p}_2) \equiv \frac{P(\mathbf{p}_1, \mathbf{p}_2)}{P(\mathbf{p}_1)P(\mathbf{p}_2)}$$

$\mathbf{p}_1, \mathbf{p}_2$ are the single particle momentum

Modeling

Describing the CF using K-P formula:

$$C(\mathbf{k}^*) = \int d^3r S(\mathbf{r}^*) |\psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

Source
function

Relative wave function
of the particle pair

Experiment

Experimentally using mixture event method to subtract the background:

$$C(\mathbf{k}^*) = \mathcal{N} \frac{A(\mathbf{k}^*)}{B(\mathbf{k}^*)}$$

Signal

Background

$\mathbf{k}^*$: Relative momentum in pair rest frame

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✓ n-n correlation function and (f_0^{nn}, d_0^{nn})

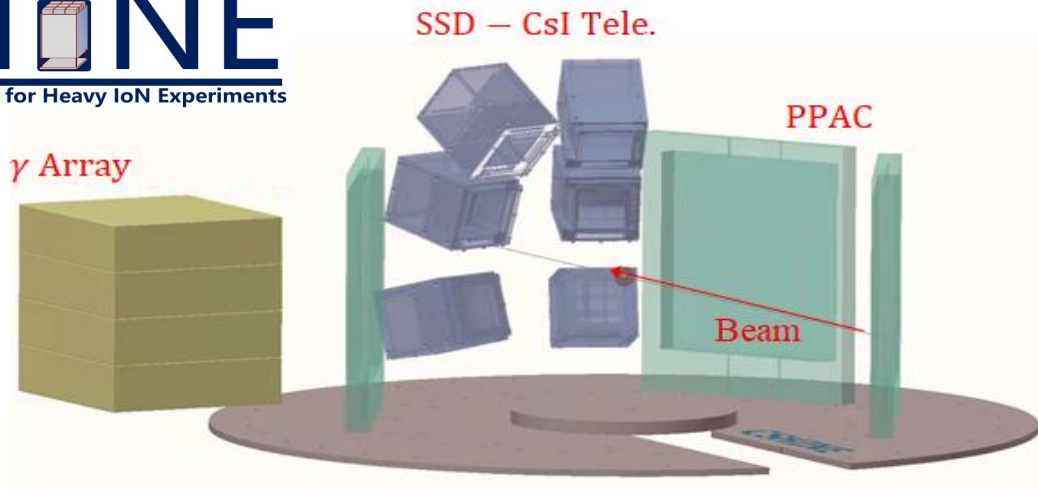
✓ Preliminary p-p correlation function

4. Summary

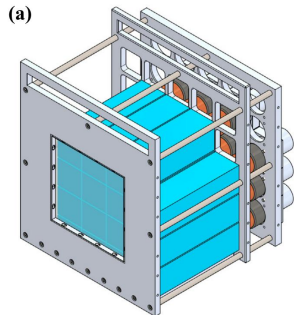
2. Experiment Setup and data analysis

Compact Spectrometer for Heavy Ion Experiment
installed at the Radioactive Ion Beam Line at Lanzhou, HIRFL

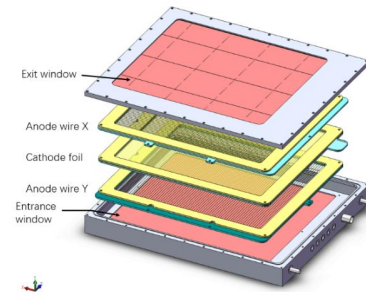
CSHINE
Compact Spectrometer for Heavy Ion Experiments



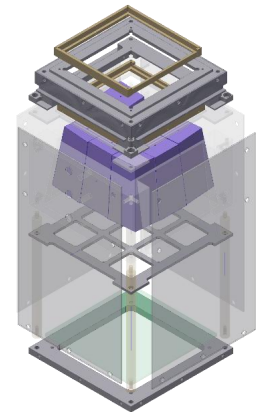
Total channels: ~400, starting from 2014



CsI hodoscope for
high energy γ



PPAC for fission
fragments



SSDT for LCP
and IMFs

Operation of CSHINE

02 2018

30 MeV/u $^{40}\text{Ar}+^{197}\text{Au}$

04 2022

25 MeV/u $^{86}\text{Kr}+^{124}\text{Sn}$

30 MeV/u* $^{40}\text{Ar}+^{197}\text{Au}$

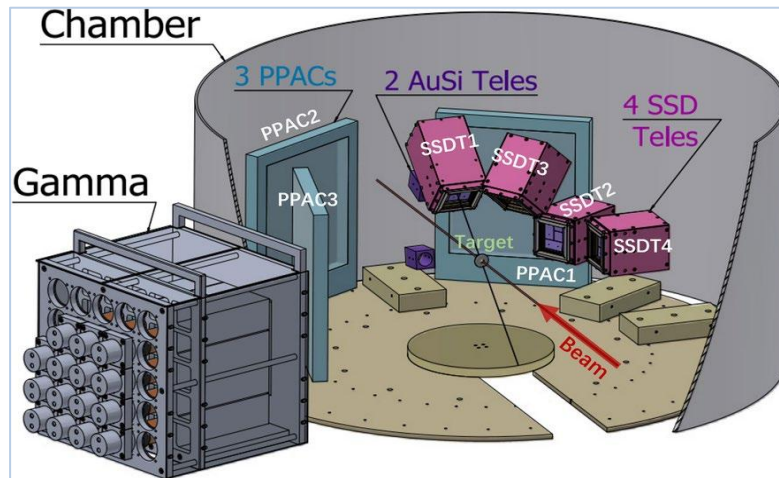
01 2014

25 MeV/u $^{86}\text{Kr}+^{208}\text{Pb}$

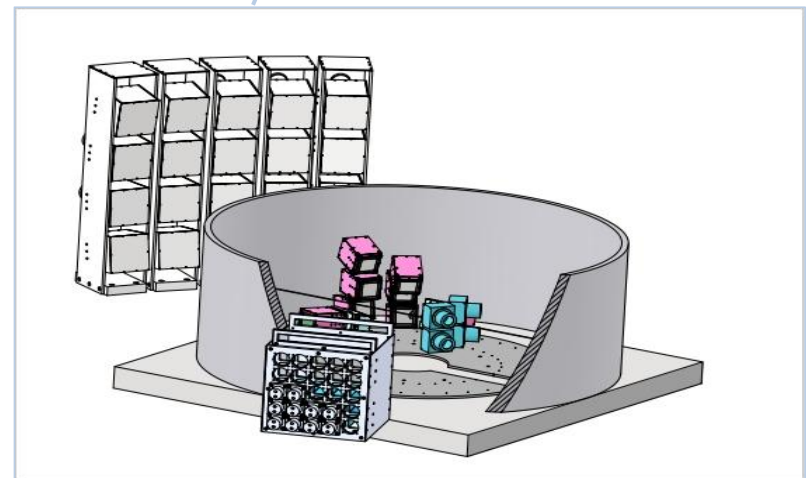
03 2019

25 MeV/u $^{124}\text{Sn}+^{124}\text{Sn}$

05 2024



4th run: 2022 CSHINE-Gamma



5th run: 2024 CSHINE-Neutron Wall

Technique and Physics Programs of CSHINE

Detection Techniques:

› Neutron Wall Construction

NIMA 1070,170055 (2025)

› High Energy γ array

NIMA 1053 168330 (2023) ,
NIMA 1080, 170787 (2025)

› FPGA Trigger System

NST 33, 162(2022)

› PPACs for Fission Fragments

NST 33, 40 (2022)

› Silicon Strip Detectors for LCPs

NIMA 1029, 166461 (2022),
NIMA 1011, 165592 (2021) ,
NST 32, 4 (2021), NST 36, 132 (2025)

Physics Studies:

› Bremsstrahlung γ and SRC

PLB 850,138514 (2024)

PLB 857,139009 (2025)

arXiv 2504.13929; arXiv 2508.04550

› n-n CF and (f_0^{nn}, d_0^{nn})

PRL 134,222301 (2025)

› t/ ^3He ratio and ^3He -puzzle

PRC 107, L041601 (2023)

NST 36,155 (2025)

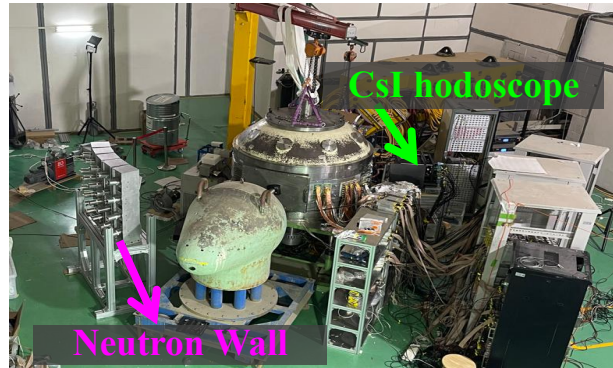
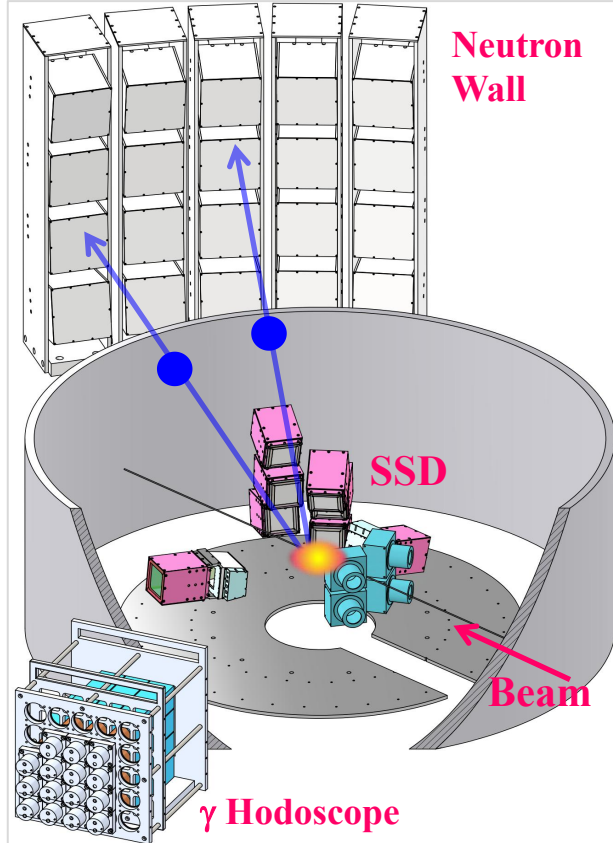
› Isospin Chronology

PLB 825, 136856 (2022)

› Constraint of $E_{\text{sym}}(\rho)$ near $\rho \approx \rho_0$

PRC 95, 041602R (2017)

25 MeV/u $^{124}\text{Sn}+^{124}\text{Sn}$ Experiment (in April 2024)

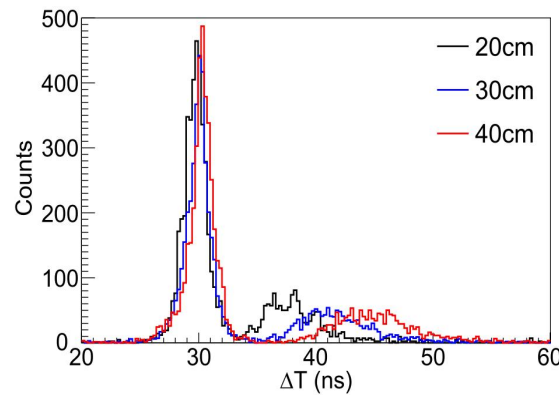


Detector Setup:

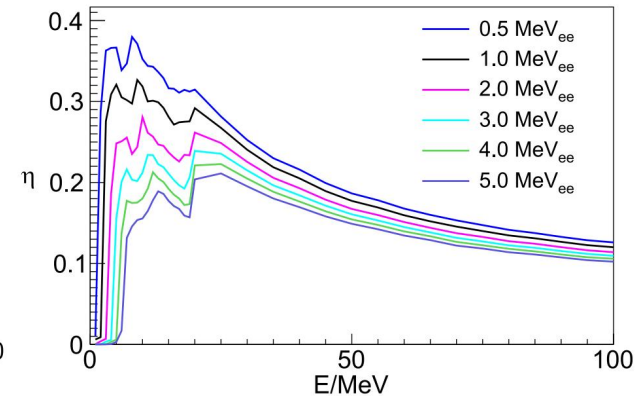
- A 4×5 array for neutrons
- 6 SSD telescopes for LCPs
- A 15-unit CsI(Tl) hodoscope for Bremsstrahlung γ rays
- A small CsI wall for centrality determination

Neutron Wall Parameters and Performance:

- unit size: $15\text{cm} \times 15\text{cm} \times 15\text{cm}$
- Intrinsic time resolution 200 ps, $L \approx 220\text{cm}$
- 20 units: Covering $21^\circ < \theta_{\text{lab}} < 53^\circ$ in Lab



n- γ coincidence in ^{252}Cf test



Efficiency curve in G4 simulation

Outline

1. Introduction: Motivation of the study

2. Experimental setup: CSHINE

3. Results and Discussions

✓ **n-n correlation function and (f_0^{nn}, d_0^{nn})**

✓ **Preliminary p-p correlation function**

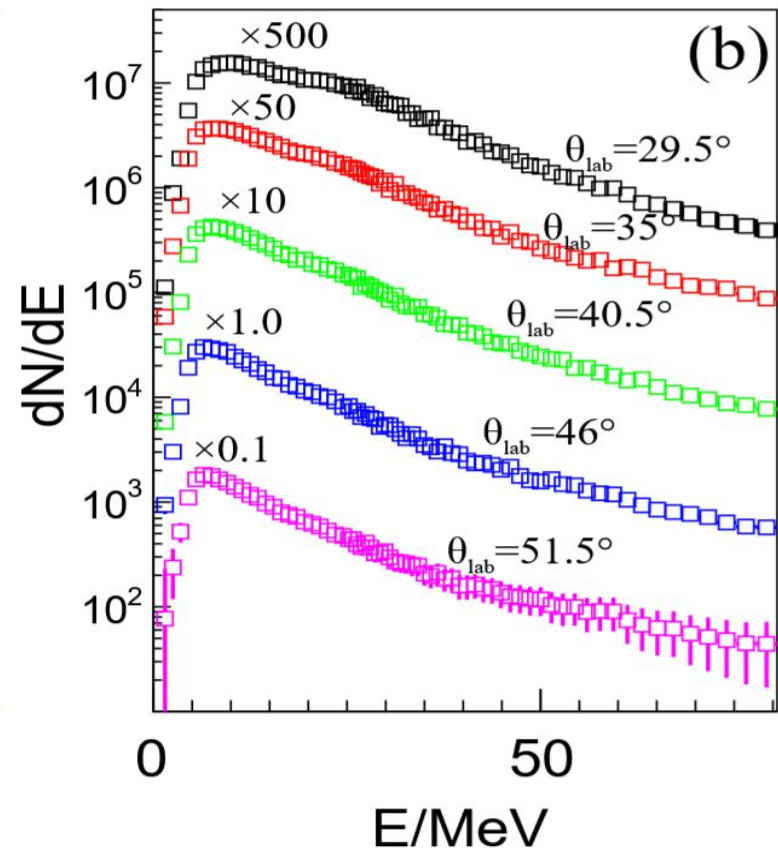
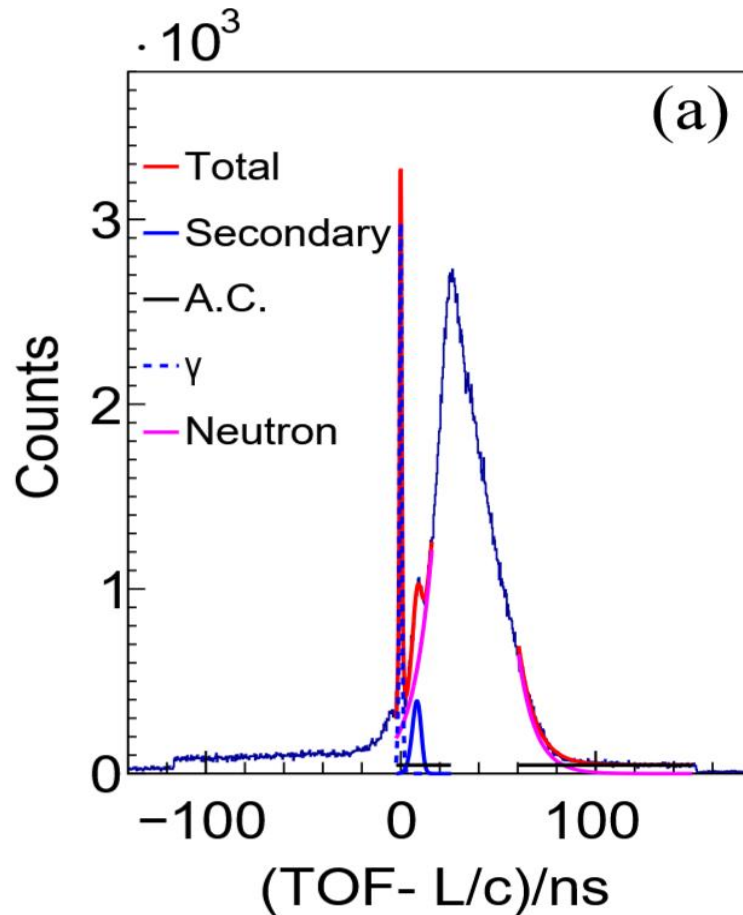
4. Summary

n-n correlation function and (f_0^{nn}, d_0^{nn})

Neutron spectra:

n- γ discrimination by TOF method

Neutrons, γ -rays, secondaries and backgrounds are distinguished.

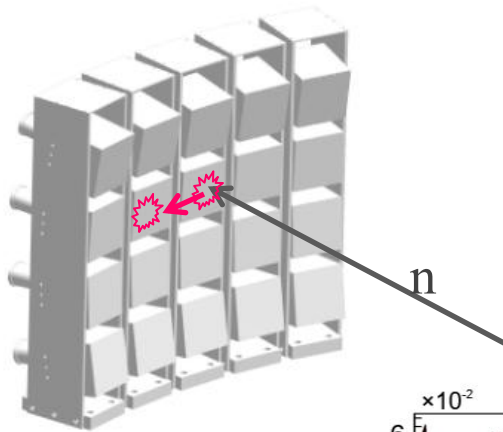


Cross-talk corrections and systematic uncertainties

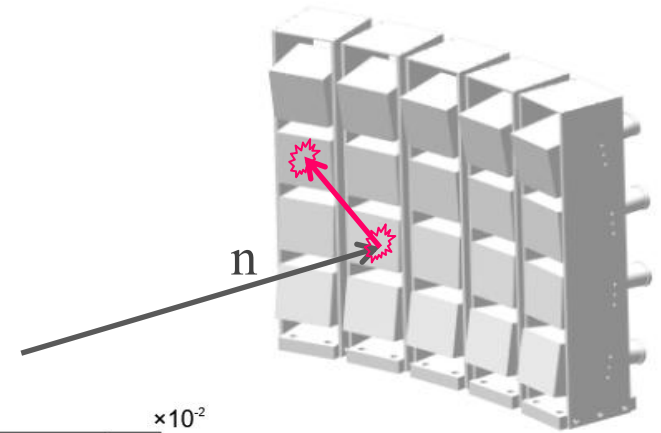
Cross-talk is the most influential effect to be corrected!

Using Geant 4 simulation to reproduce the cross-talk pattern

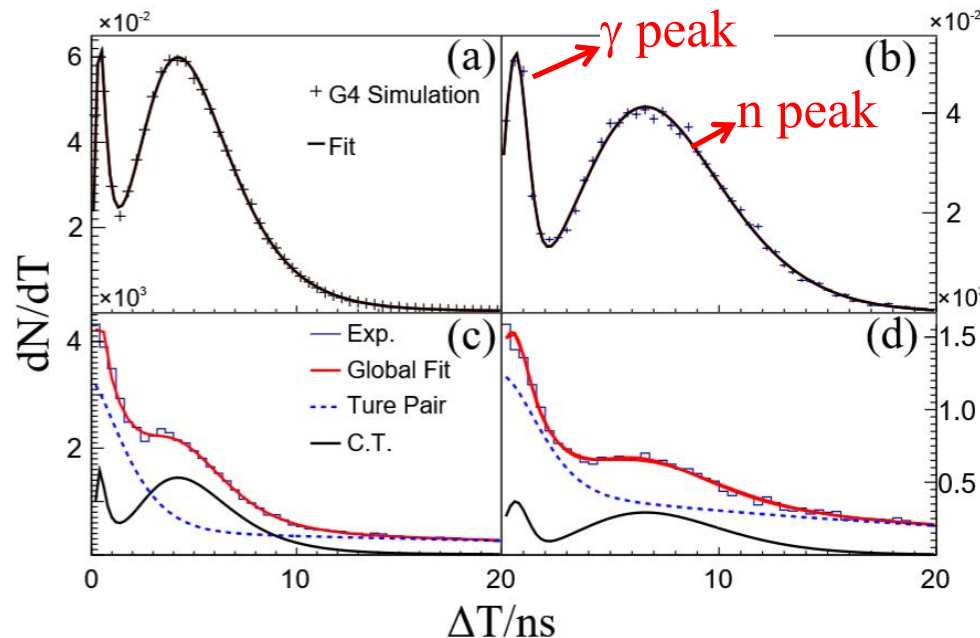
Doing global fit to decompose and subtract the cross-talk



Side-by-side cross-talk

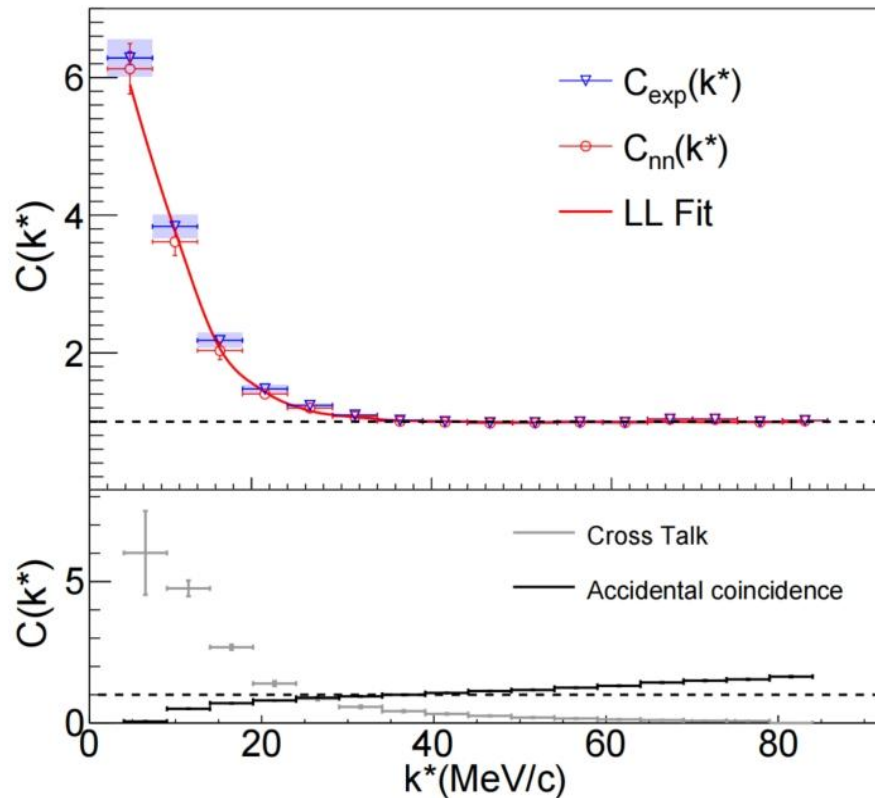


Corner-to-corner cross-talk



n-n correlation function and (f_0^{nn}, d_0^{nn})

After the correction of TOF resolution, cross-talk and accidental coincidence, one obtains the n-n correlation function:



$$C_{\text{nn}}(k^*) = A_{\text{nn}} \frac{N_{\text{nn}}^{\text{same}}(k^*)}{N_{\text{exp}}^{\text{mix}}(k^*)}$$

$$= \frac{A_{\text{nn}}}{1 - \lambda_{\text{ct}} - \lambda_{\text{ac}}} \left(\frac{C_{\text{exp}}(k^*)}{A_{\text{exp}}} - \lambda_{\text{ct}} \frac{N_{\text{ct}}^{\text{mix}}(k^*)}{N_{\text{exp}}^{\text{mix}}(k^*)} - \lambda_{\text{ac}} \frac{N_{\text{ac}}^{\text{same}}(k^*)}{N_{\text{exp}}^{\text{mix}}(k^*)} \right)$$

$\Delta\text{TOF Fit}$ TOF Fit

G4 Simulation

Cross-talk and accidental coincidence partly cancel each other.

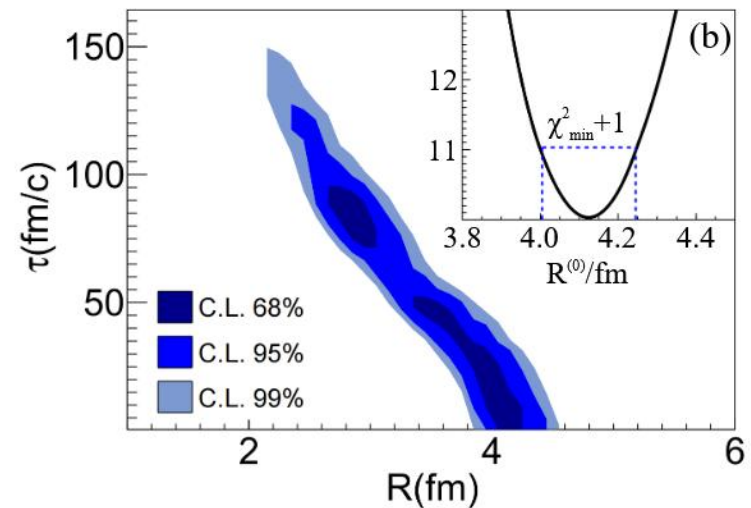
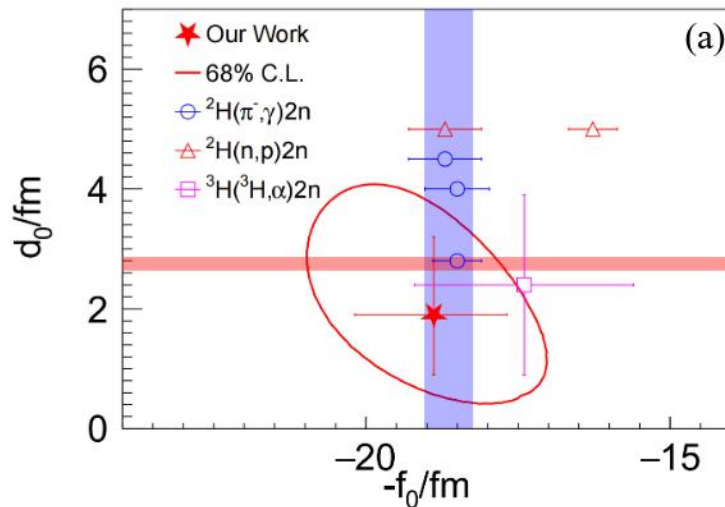
Extraction of (f_0^{nn}, d_0^{nn})

- ✓ (f_0^{nn}, d_0^{nn}) is extracted from 25 MeV/u $^{124}\text{Sn} + ^{124}\text{Sn}$ reactions:

$$f_0^{nn} = 18.9_{-1.2}^{+1.3} \text{ fm}, d_0^{nn} = 1.9_{-1.0}^{+1.3} \text{ fm}$$

[Better control of the uncertainty still demanded for CSB studies.]

- ✓ Simultaneously, the temporal-spatial source size is extracted: $R^{(0)} = 4.1 \pm 0.1 \text{ fm}$

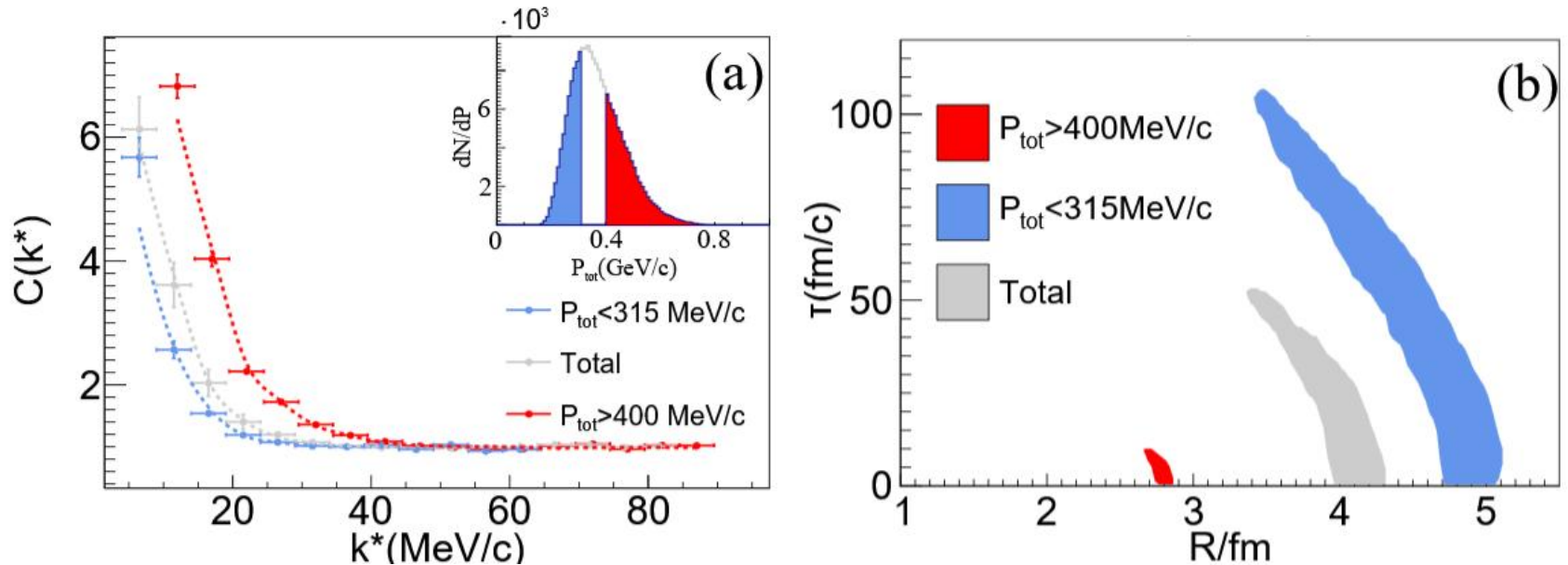


Here we assume a Gaussian source function :

$$S \propto \exp(-r^2/R^2 - t^2/\tau^2)$$

Dependence of source size on nn pair momentum

- ✓ n-n CF Showing dependence on the pair-momentum
- ✓ For the low momentum, space-volume is larger (larger space, longer time), correlation becomes weaker.

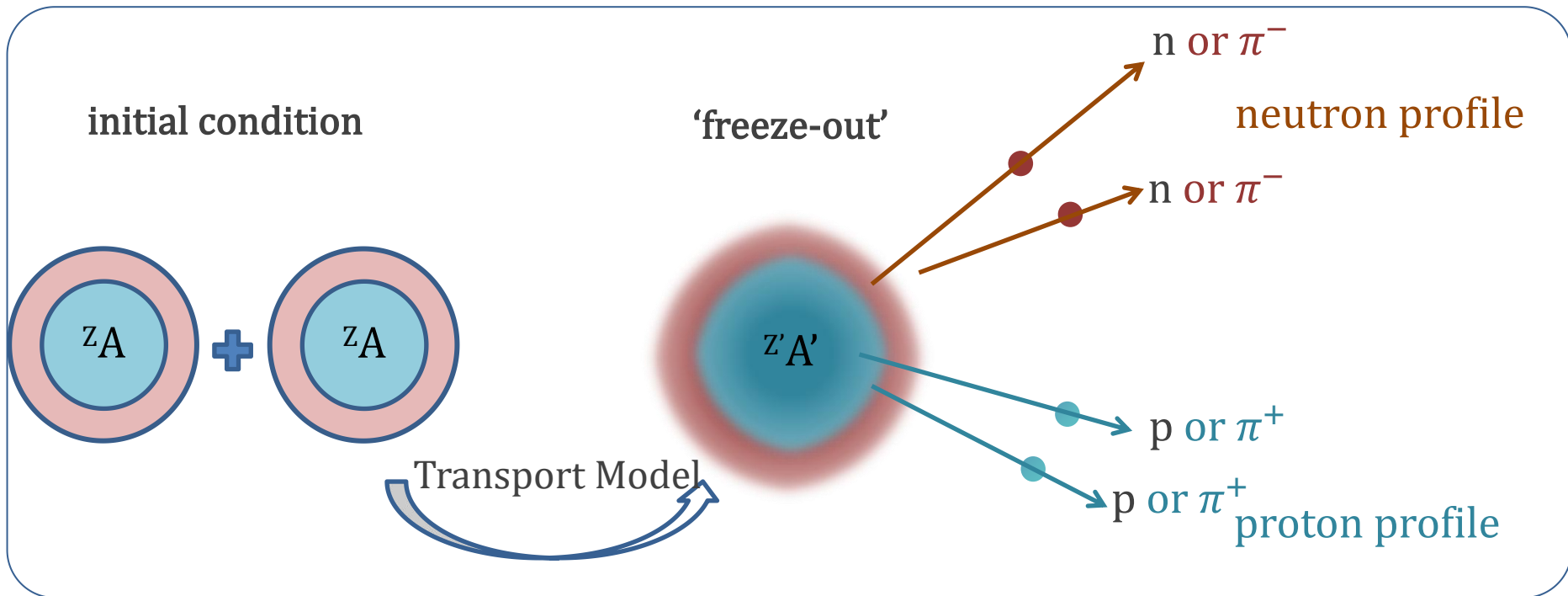


3.2 Preliminary p-p correlation function

Apparently, in order to

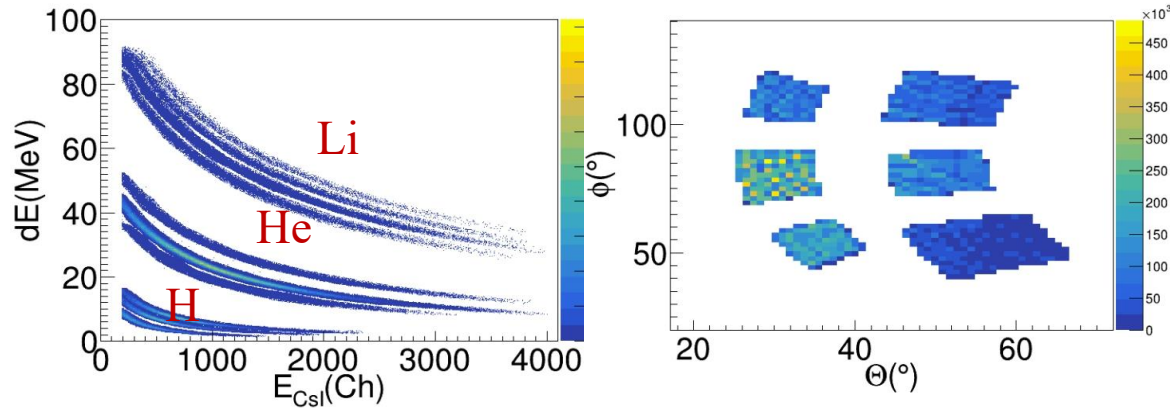
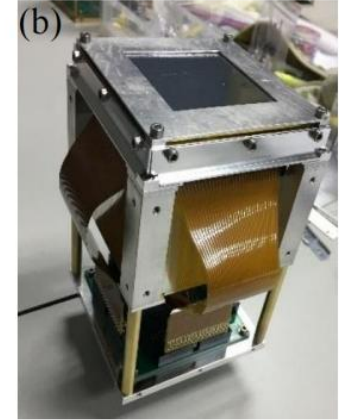
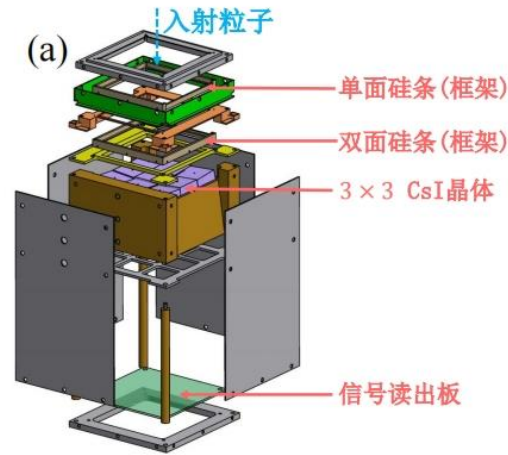
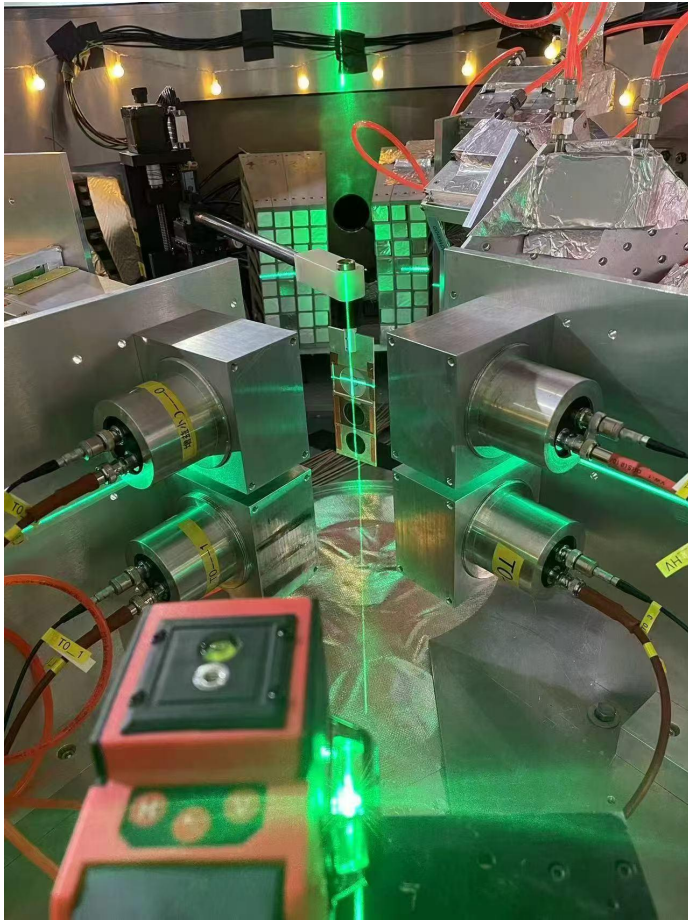
- ① reveal the collision dynamics in terms of the Isospin DOF
- ② investigate the CSB of nuclear force

One need measuring n-n and p-p correlation functions simultaneously



Ongoing activities: p-p correlations

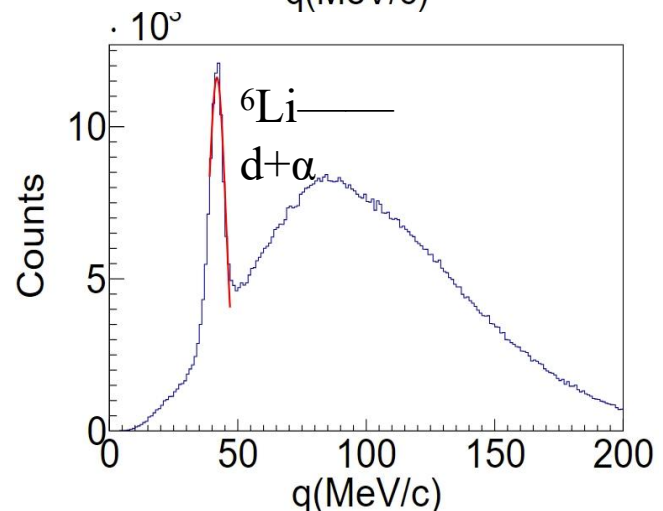
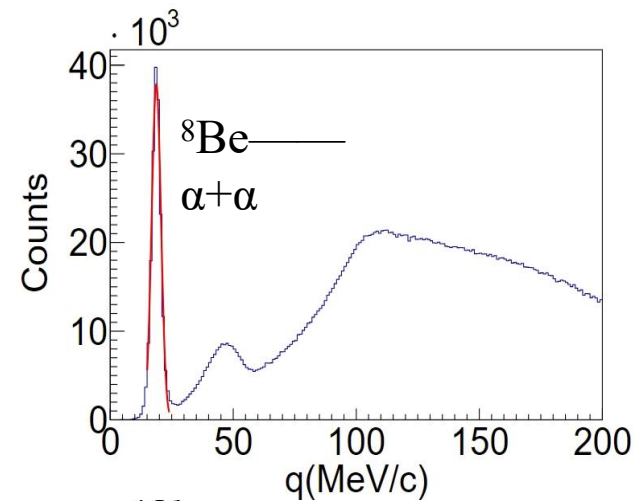
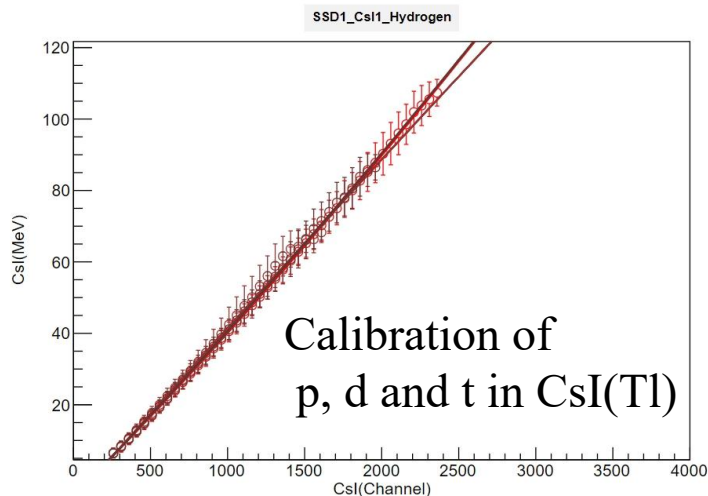
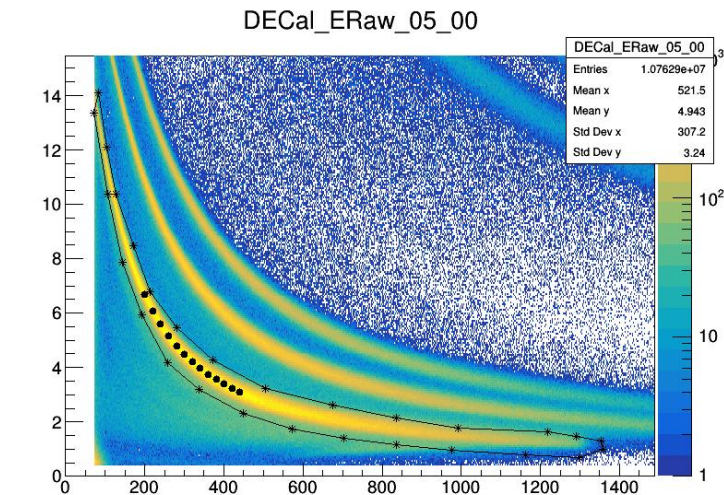
Protons are measured by the silicon strip detector telescopes (SSDT).



F.H.Guan et al., NIMA 1011, 165592 (2021) ,
Y. J. Wang et al., NST 32, 4 (2021), cover story
X. B. Wei et al., NST 36, 132 (2025), cover story

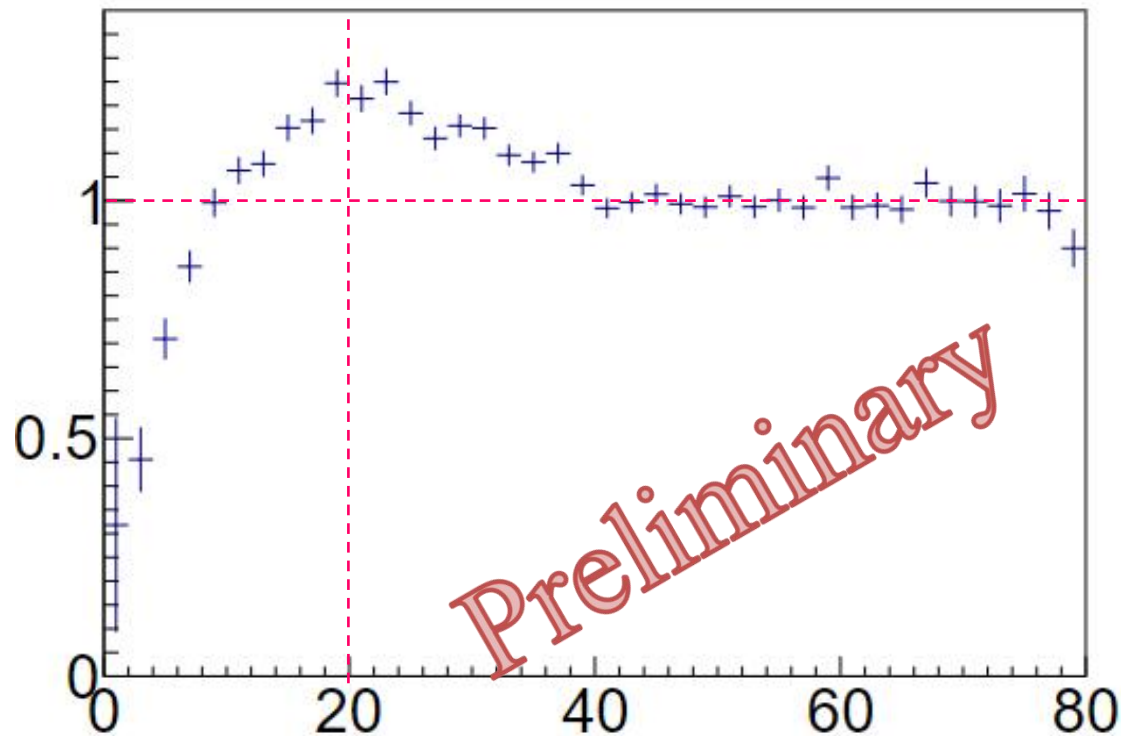
Calibration check for 25 MeV/u $^{124}\text{Sn}+^{124}\text{Sn}$

- SSD calibration by α source+pulser
- CsI calibration by energy loss match
- Calibration check by the know correlation peaks



Preliminary p-p correlation function

- p-p correlation functions obtained preliminarily
 - correlation peak well located!
 - Due to insufficient statistics, no selection on impact parameter is done



Efficiency curve optimization and systematics analysis on going, stay tuned!

4 Summary

❶ With the newly built neutron wall on CSHINE, the n-n correlation function in the reactions of $^{124}\text{Sn} + ^{124}\text{Sn}$ at 25 MeV/u has been measured.

- Geant 4 simulation is applied to do the cross talk correction.
- The nn CF has been fitted by LL model assuming a Gaussian source.

$$f_0^{nn} = 18.9_{-1.2}^{+1.3} \text{fm}, d_0^{nn} = 1.9_{-1.0}^{+1.3} \text{fm}, R^{(0)} = 4.1 \pm 0.1 \text{fm}$$

❷ p-p correlation function analysis is ongoing ...

❸ The results demonstrate the feasibility to pin down the CSB with femtoscopy correlation at improved resolution, and highlight the perspective of the future studies on isospin dynamics and CIB, using n-n, p-p and n-p correlation functions with better uncertainty control.

Stay tuned ...

Thank you for your attention!