

BESIII 上粲介子半轻衰变的研究

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第十届手征有效场论研讨会

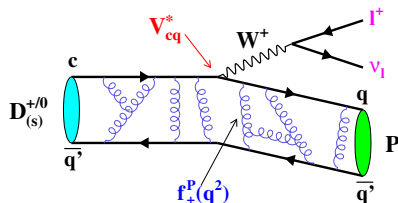
南京师范大学

2025 年 10 月 19 日

Outline

- 1 Motivation
- 2 BESIII dataset and double-tag method
- 3 Recent results at BESIII
- 4 Summary and Prospect

Motivation



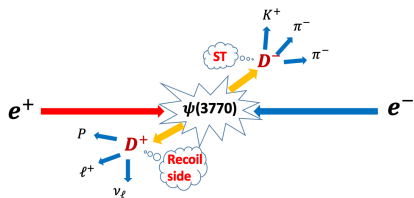
$$\frac{d\Gamma}{dq^2} \propto |V_{cq}|^2 |f_+(q^2)|^2$$

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Uncertainties dominated by $|V_{cs}|$ and $|V_{cd}|$

- Semi-leptonic decays of charm mesons are important for determining CKM matrix elements $|V_{cs(d)}|$, calibrating LQCD, testing LFU, *et al.*
- **FF measurement $\Rightarrow$ Calibrate LQCD calculations**
- $|V_{cq}|$ measurement $\Rightarrow$ **Test CKM matrix unitarity**
- **BF ratios $\Rightarrow$ Test lepton flavor universality (LFU)**

BESIII dataset and double-tag method



- e^+e^- annihilations data near threshold
 $\Rightarrow$ Double-tag method & Clean environment
- Undetectable neutrinos $\Rightarrow$ extract the semileptonic signals
 $U_{\text{miss}} = E_{\text{miss}} - |\vec{p}_{\text{miss}}|$, $M_{\text{miss}}^2 = E_{\text{miss}}^2 - |\vec{p}_{\text{miss}}|^2$
- BF with double-tag method: $\mathcal{B} = \frac{N_{\text{DT}}}{N_{\text{ST}} \epsilon_{\text{DT}} / \epsilon_{\text{ST}}}$
 $\Rightarrow$ Systematic uncertainties on the ST mostly canceled

Data sample	E_{cm} (GeV)	$\mathcal{L}_{\text{int}}$ (fb^{-1})	Single tag yields ($\times 10^6$)
$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$	3.773	20.3	$\bar{D}^0 \sim 16.9$; $D^- \sim 11.0$
$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	4.128-4.226	7.33	$D_s^- \sim 0.8$
$e^+e^- \rightarrow D_s^{*-+} D_s^{*-}$	4.237-4.669	10.64	$D_s^- \sim 0.12$

$$D_{(s)} \rightarrow P(S)\ell^+\nu_\ell$$

Theoretical expression of differential decay rate:

- Point-like: $D_{(s)} \rightarrow P\ell^+\nu_\ell$ ($P = K, \pi, \eta, \eta'$) [PRD101(2020)013004]

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 |V_{cq}|^2}{24\pi^3} \frac{(q^2 - m_\ell^2)^2 |\vec{p}_P|}{q^4 m_D^2} \left(1 + \frac{m_\ell^2}{2q^2}\right) m_D^2 |\vec{p}_P|^2 |f_+(q^2)|^2$$

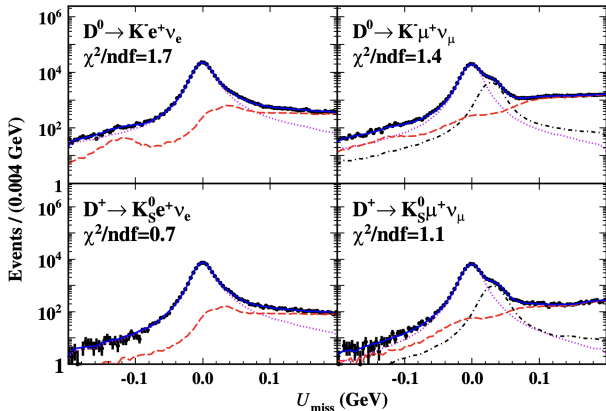
- Consider resonance's width: $D_{(s)} \rightarrow S\ell^+\nu_\ell$ ($S = a_0(980), f_0(980), f_0(500)$)
[PRD102(2020)016022, PLB759(2016)501]

$$\frac{d^2\Gamma}{dq^2 ds} = \frac{G_F^2 |V_{cq}|^2}{192\pi^4 m_D^3} \lambda^{1/2}(m_D^2, s, q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left(1 + \frac{m_\ell^2}{2q^2}\right) \lambda(m_D^2, s, q^2) |f_+(q^2)|^2 P(s)$$

$$P(s) = \begin{cases} P(s) = \frac{g_1 \rho_{\pi\pi}}{|m_0^2 - s - i(g_1 \rho_{\pi\pi} + g_2 \rho_{K\bar{K}})|^2}, \text{Flatte for } a_0(980)/f_0(980) \\ \frac{m_{f_0} \Gamma(s)}{(s - m_{f_0})^2 + m_{f_0}^2 \Gamma^2(s)}, \text{RBW for } f_0(500) \end{cases}$$

$D^0 \rightarrow K^-\ell^+\nu_\ell$ and $D^+ \rightarrow \bar{K}^0\ell^+\nu_\ell$

PRD110(2024)112006



- Data: 7.93 fb^{-1} @ 3.773 GeV

- Improved measurement of BFs

$$\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e) = (3.521 \pm 0.009 \pm 0.016)\%$$

$$\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu) = (3.419 \pm 0.011 \pm 0.016)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = (8.864 \pm 0.039 \pm 0.082)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu) = (8.665 \pm 0.046 \pm 0.084)\%$$

- Most precision LFU test: Consistent with

$$\mathcal{R}_{\text{SM}} = 0.975 \pm 0.001$$

$$\frac{\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e)} = 0.971 \pm 0.004 \pm 0.006$$

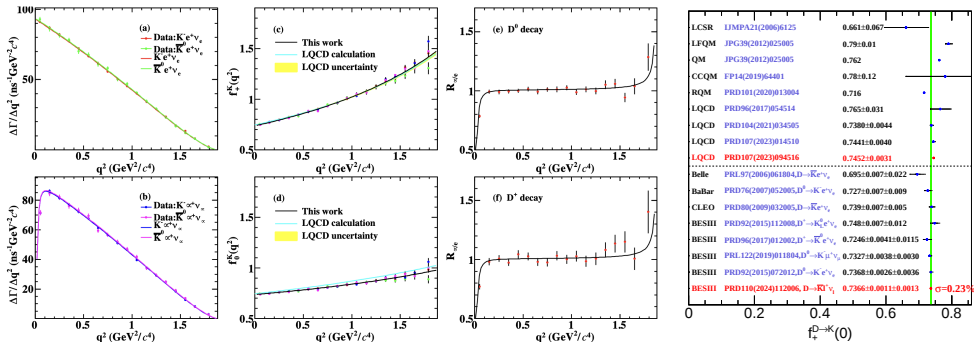
$$\frac{\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)}{\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 0.978 \pm 0.007 \pm 0.013$$

- Isospin test: Consistent with 1

$$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 1.000 \pm 0.007 \pm 0.012$$

$$\frac{\Gamma(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)} = 0.993 \pm 0.008 \pm 0.012$$

$$D^0 \rightarrow K^- \ell^+ \nu_\ell \text{ and } D^+ \rightarrow \bar{K}^0 \ell^+ \nu_\ell$$



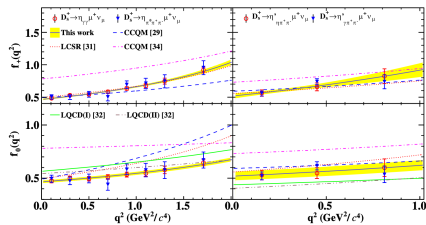
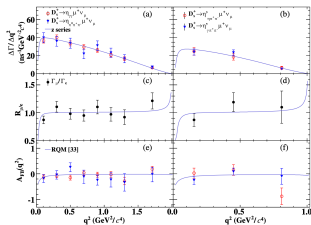
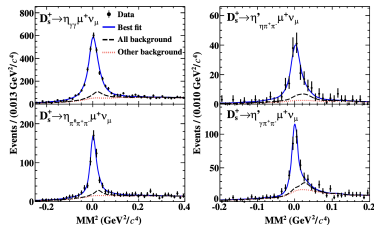
• Latest LQCD: $f_+^{D \rightarrow K}(0) = 0.7452(31)$ ($\sigma = 2.4\% \rightarrow 0.4\%$)

• Most precisions of FF $f_+^K(0)$ ($\sigma = 0.23\%$) and $|V_{cs}|$ ($\sigma = 0.48\%$)

$$f_+^K(0) = 0.7366 \pm 0.0011_{\text{stat}} \pm 0.0013_{\text{syst}}; |V_{cs}| = 0.9623 \pm 0.0015_{\text{stat}} \pm 0.0017_{\text{syst}} \pm 0.0040_{\text{LQCD}}$$

• Measured FF $f_+^K(0)$ is consistent with the LQCD calculations within 2.5 σ

$$D_s^+ \rightarrow \eta^{(\prime)} \mu^+ \nu_\mu$$



• Data: 7.33 fb^{-1} @ 4.128-4.226 GeV **PRL132(2024)091802**

• Precision of BFs are improved by a factor of ~ 6

$$\mathcal{B}(D_s^+ \rightarrow \eta \mu^+ \nu_\mu) = (2.235 \pm 0.051 \pm 0.052)\%$$

$$\mathcal{B}(D_s^+ \rightarrow \eta' \mu^+ \nu_\mu) = (0.801 \pm 0.055 \pm 0.028)\%$$

• First extraction of the FFs via semimuonic decays

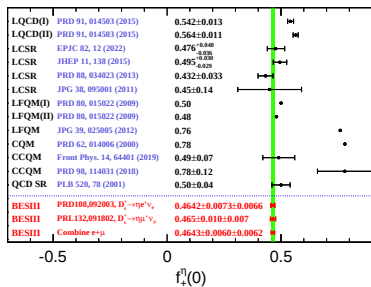
$$f_+^\eta(0) = 0.465 \pm 0.010 \pm 0.007; f_+^{\eta'}(0) = 0.518 \pm 0.038 \pm 0.012$$

• Most precision test of lepton flavor universality in D_s sector

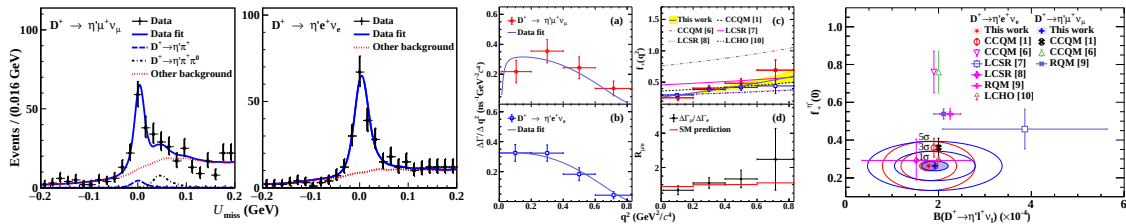
$$\mathcal{R}_{\mu/e}^\eta = 0.991 \pm 0.029 \pm 0.016; \mathcal{R}_{\mu/e}^{\eta'} = 0.988 \pm 0.082 \pm 0.031$$

• First extraction of the forward-backward asymmetry parameters

$$\langle A_{\text{FB}}^\eta \rangle = -0.059 \pm 0.031 \pm 0.005; \langle A_{\text{FB}}^{\eta'} \rangle = -0.064 \pm 0.079 \pm 0.006$$



$$D^+ \rightarrow \eta' \ell^+ \nu_\ell$$



• Data: 20.3 fb^{-1} @ 3.773 GeV PRL134(2025)111801

• **First observation of $D^+ \rightarrow \eta' \mu^+ \nu_\mu$ with significance of 8.6σ**

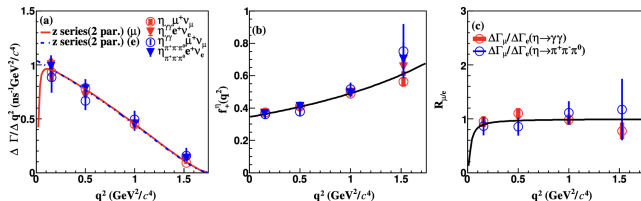
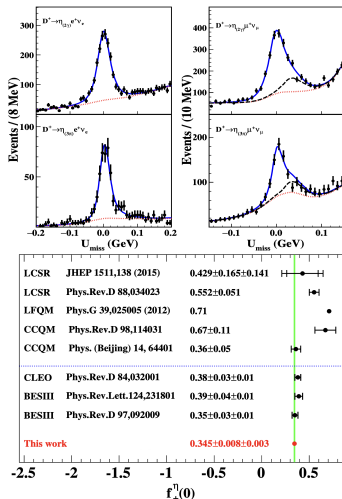
$$\mathcal{B}(D^+ \rightarrow \eta' \mu^+ \nu_\mu) = (1.92 \pm 0.28 \pm 0.08) \times 10^{-4}; \quad \mathcal{B}(D^+ \rightarrow \eta' e^+ \nu_e) = (1.79 \pm 0.19 \pm 0.07) \times 10^{-4}$$

• **First extraction of the FF of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$: $f_+^{\eta'}(0) = 0.263 \pm 0.025 \pm 0.006$**

• **LFU test: $\mathcal{R}_{\mu/e}^{\eta'} = 1.07 \pm 0.19 \pm 0.03$**

• **$\eta - \eta'$ mixing angle: $\phi_P = (39.8 \pm 0.8 \pm 0.3)^\circ$ ($\cot^4 \phi_P = \frac{\Gamma_{D_s^+ \rightarrow \eta' \ell^+ \nu_\ell} / \Gamma_{D_s^+ \rightarrow \eta \ell^+ \nu_\ell}}{\Gamma_{D^+ \rightarrow \eta' \ell^+ \nu_\ell} / \Gamma_{D^+ \rightarrow \eta \ell^+ \nu_\ell}}$)**

$$D^+ \rightarrow \eta \ell^+ \nu_\ell$$



- arXiv:2506.02521, submitted to JHEP

- Data: 20.3 fb⁻¹@3.773 GeV

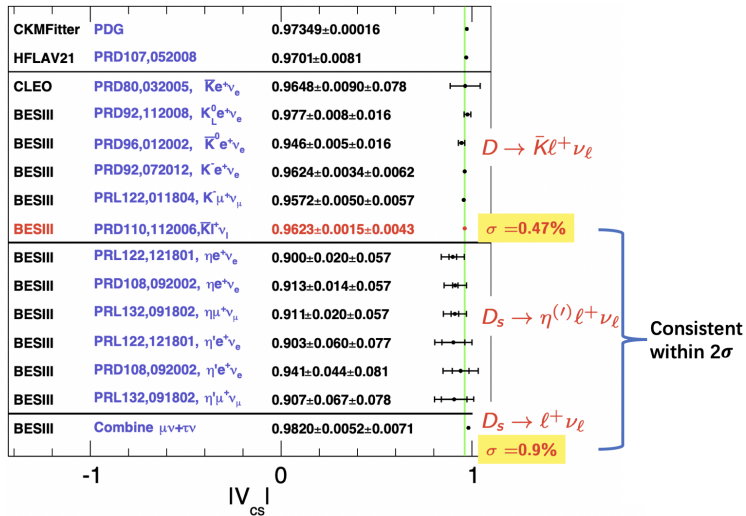
- Precisions of BF and FF are improved by $\sim 2\times$

$$\mathcal{B}(D^+ \rightarrow \eta \mu^+ \nu_\mu) = (9.08 \pm 0.35 \pm 0.23) \times 10^{-4}$$

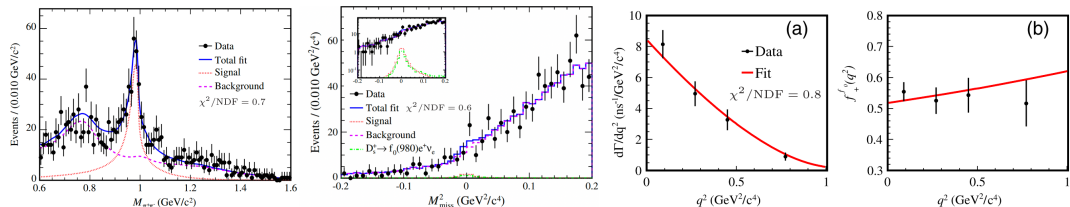
$$\mathcal{B}(D^+ \rightarrow \eta e^+ \nu_e) = (9.75 \pm 0.29 \pm 0.28) \times 10^{-4}$$

$$f_+^\eta(0) = 0.345 \pm 0.008 \pm 0.003$$

- LFU test: $\mathcal{R}_{\mu/e}^\eta = 0.93 \pm 0.05 \pm 0.02 \Rightarrow$ Consistent with SM

Comparison of $|V_{cs}|$ 

$D_s^+ \rightarrow f_0(980)e^+\nu_e$ via $f_0(980) \rightarrow \pi^+\pi^-$



• $7.33 \text{ fb}^{-1} @ 4.128\text{-}4.226 \text{ GeV}$ **PRL132(2024)141901**

• **Updated BF measurement**

$$\mathcal{B}(D_s^+ \rightarrow f_0(980)\pi^+\pi^- e^+\nu_e) = (1.72 \pm 0.13 \pm 0.10) \times 10^{-3}$$

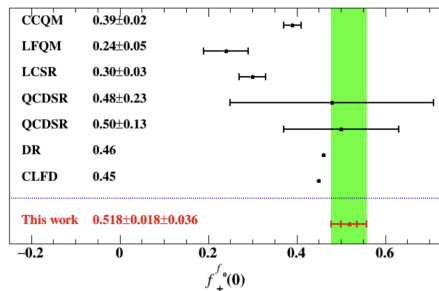
• **$q\bar{q}$ mixing angle:** $\sin\phi(1/\sqrt{2})(u\bar{u} + d\bar{d}) + \cos\phi s\bar{s}$

$$\phi = (19.7 \pm 12.8)^\circ \Rightarrow \text{red } s\bar{s} \text{ component dominates}$$

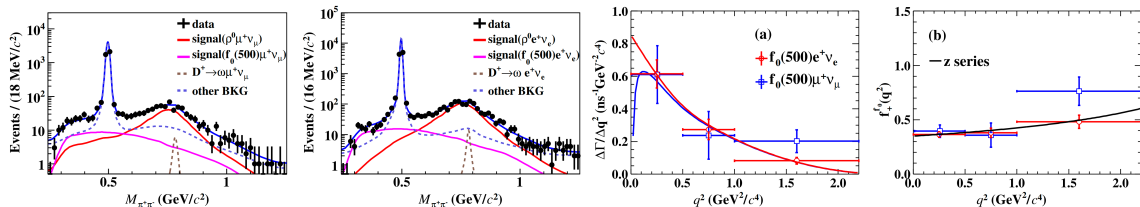
• **First FF measurement:** $f_+^{f_0(980)}(0) = 0.518 \pm 0.018 \pm 0.036$

• **First search of $D_s^+ \rightarrow f_0(500)e^+\nu_e$ ($M_{\pi^+\pi^-} < 0.45 \text{ GeV}/c^2$)**

$$\mathcal{B}(D_s^+ \rightarrow f_0(500)\pi^+\pi^- e^+\nu_e) < 3.3 \times 10^{-4} @ 90\% \text{ C. L.}$$



$D^+ \rightarrow f_0(500)\mu^+\nu_\mu$ and $D^+ \rightarrow \pi^+\pi^-\ell^+\nu_\ell$



• 2.93 fb^{-1} @ 3.773 GeV PRD110(2024)092008

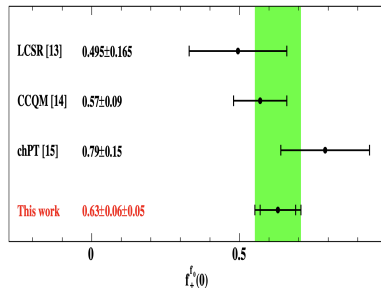
• **First observation of $D^+ \rightarrow f_0(500)\mu^+\nu_\mu$**

$$\mathcal{B}_{D^+ \rightarrow f_0(500)\pi^+\pi^-\mu^+\nu_\mu} = (0.72 \pm 0.13 \pm 0.10) \times 10^{-3}$$

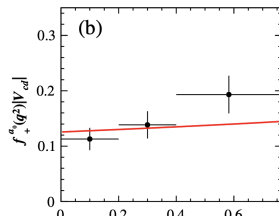
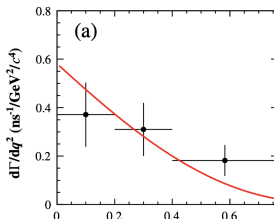
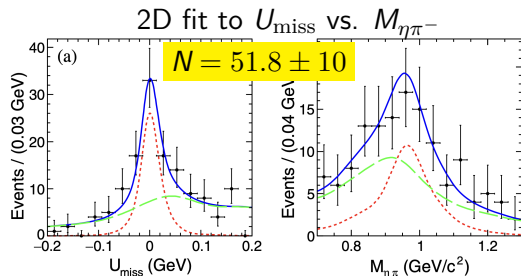
$$\mathcal{B}_{D^+ \rightarrow \rho^0\pi^+\pi^-\mu^+\nu_\mu} = (1.64 \pm 0.13 \pm 0.11) \times 10^{-3}$$

• **First FF measurement:** $f_+^{f_0(500)}(0) = 0.63 \pm 0.06 \pm 0.05$

• $\mathcal{R}_{\mu/e}^{\rho^0} = 0.88 \pm 0.10$ (SM ~ 0.96), $\mathcal{R}_{\mu/e}^{f_0(500)} = 1.14 \pm 0.28$ (SM ~ 0.90)



$D^0 \rightarrow a_0(980)^- e^+ \nu_e$ via $a_0(980)^- \rightarrow \eta\pi^-$



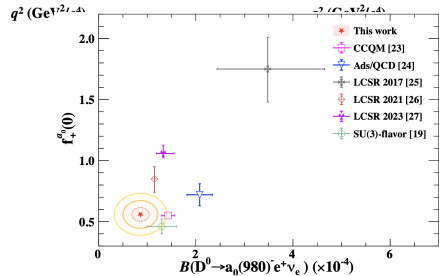
• Data: 7.93 fb^{-1} @ 3.773 GeV PRD111(2025)L091501

• **Improve measurement of BF**

$$\mathcal{B}(D^0 \rightarrow a_0(980)^- e^+ \nu_e, a_0(980)^- \rightarrow \eta\pi^-) = (0.86 \pm 0.17 \pm 0.05) \times 10^{-4}$$

• **First extraction of the FF**

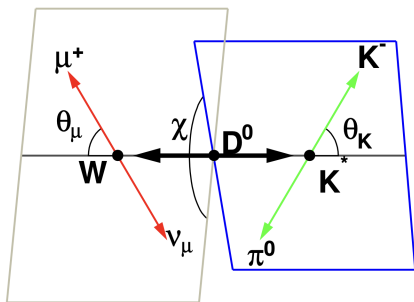
$$f_+^{a_0(980)}(0) = 0.559 \pm 0.056 \pm 0.013$$



$$D \rightarrow V\ell^+\nu_\ell \quad (V = K^*(892), \rho, \omega, \phi)$$

$$\Gamma(D \rightarrow V\ell^+\nu_\ell) \propto |V_{cd(s)}|^2 \mathcal{I}(A_1(q^2), A_2(q^2), V(q^2)...) dm^2 dq^2 d\cos(\theta_h) \cos(\theta_\ell) d\chi$$

[Phys. Rev. 137, B438 (1965), Phys. Rev. D 46,5040 (1992)]



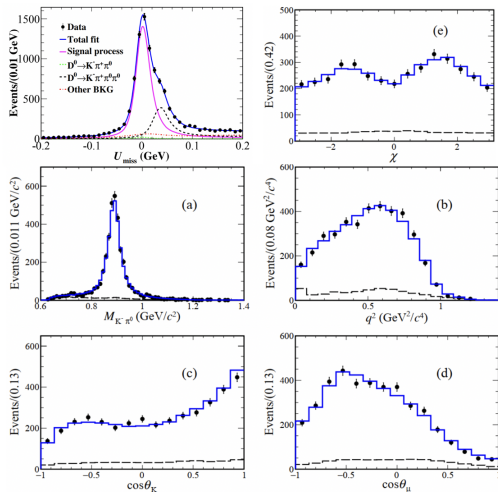
- Decay intensity $\mathcal{I}$ include S, P, D wave components
- Five kinematic variables: $m, q^2, \theta_K, \theta_\mu, \chi$
- Three FF parameterization (single pole)

$$A_{1,2}(q^2) = \frac{A_{1,2}(0)}{1 - q^2/M_A^2}; \quad V(q^2) = \frac{V(0)}{1 - q^2/M_V^2}$$

$$r_V = \frac{V(0)}{A_1(0)}; \quad r_2 = \frac{A_2(0)}{A_1(0)}$$
- Un-binned maximum likelihood

$$-\ln\mathcal{L} = (-\ln\mathcal{L}_{\text{data}}) - (-\ln\mathcal{L}_{\text{bkg}})$$

$D^0 \rightarrow K^*(892)^-\mu^+\nu_\mu$ via $K^*(892)^- \rightarrow K^-\pi^0$



PRL134(2025)011803

- Data: 7.9 fb^{-1} @ $3.773 \text{ GeV} \Rightarrow N_{\text{DT}} = 6436 \pm 119$
- **First measurement of BF**
 $\mathcal{B}(D^0 \rightarrow K^-\pi^0\mu^+\nu_\mu) = (0.729 \pm 0.014 \pm 0.011)\%$
 $\mathcal{B}(D^0 \rightarrow K^*(892)^-\mu^+\nu_\mu) = (2.062 \pm 0.039 \pm 0.032)\%$
- **LFU test ($\mathcal{R}_{\text{SM}} \sim 0.92 - 0.99$) Consistent**

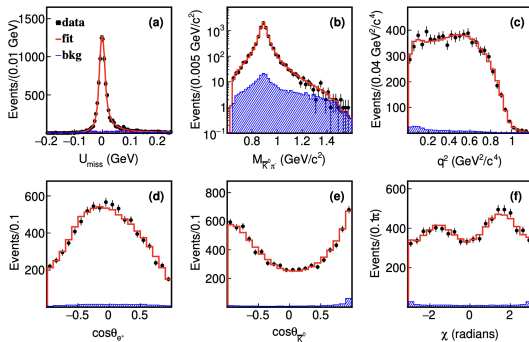
$$\mathcal{R}_{\mu/e} = \frac{\mathcal{B}(D^0 \rightarrow K^*(892)^-\mu^+\nu_\mu)}{\mathcal{B}(D^0 \rightarrow K^*(892)^-e^+\nu_e)} = 1.020 \pm 0.030 \pm 0.028$$

- **First FF measurement**

$$r_V = \frac{V(0)}{A_1(0)} = 1.37 \pm 0.09 \pm 0.03$$

$$r_2 = \frac{A_2(0)}{A_1(0)} = 0.76 \pm 0.06 \pm 0.02$$

$D^0 \rightarrow K^*(892)^- e^+ \nu_e$ via $K^*(892)^- \rightarrow \bar{K}^0 \pi^-$



- Data: $7.9 \text{ fb}^{-1} @ 3.773 \text{ GeV} \Rightarrow N_{\text{DT}} = 8752 \pm 132$ **JHEP03(2025)197**

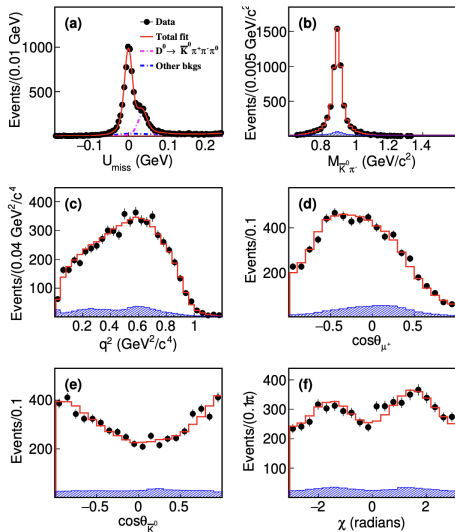
- **Updated measurement of BF**

$$\mathcal{B}(D^0 \rightarrow \bar{K}^0 \pi^0 e^+ \nu_e) = (1.444 \pm 0.022 \pm 0.024)\%; \mathcal{B}(D^0 \rightarrow K^*(892)^- e^+ \nu_e) = (2.039 \pm 0.032 \pm 0.034)\%$$

- **Updated FF measurement**

$$r_V = \frac{V(0)}{A_1(0)} = 1.48 \pm 0.05 \pm 0.02; r_2 = \frac{A_2(0)}{A_1(0)} = 0.70 \pm 0.04 \pm 0.02; A_1(0) = 0.610 \pm 0.007 \pm 0.004$$

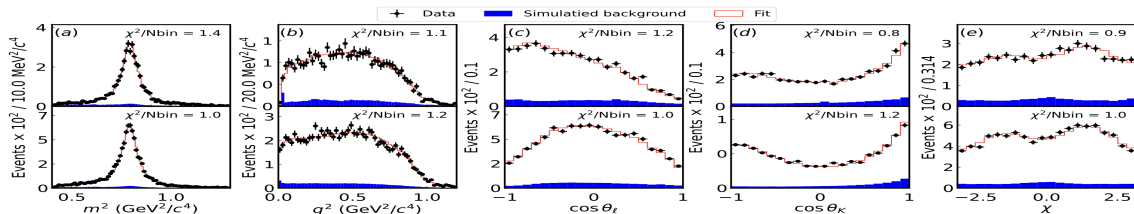
$D^0 \rightarrow K^*(892)^-\mu^+\nu_\mu$ via $K^*(892)^- \rightarrow \bar{K}^0\pi^-$



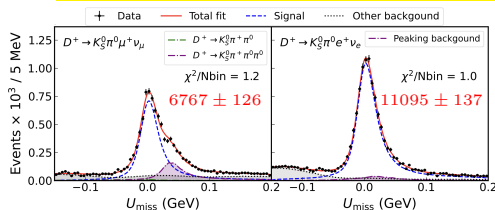
PRL135(2025)111803

- Data: 7.9 fb^{-1} @ $3.773 \text{ GeV} \Rightarrow N_{\text{DT}} = 6796 \pm 98$
- **First measurement of BF**
 $\mathcal{B}(D^0 \rightarrow \bar{K}^0\pi^0\mu^+\nu_\mu) = (1.373 \pm 0.020 \pm 0.023)\%$
 $\mathcal{B}(D^0 \rightarrow K^*(892)^-\mu^+\nu_\mu) = (1.948 \pm 0.033 \pm 0.036)\%$
- **LFU test ($\mathcal{R}_{\text{SM}} \sim 0.92 - 0.99$) Consistent**
 $\mathcal{R}_{\mu/e} = \frac{\mathcal{B}(D^0 \rightarrow K^*(892)^-\mu^+\nu_\mu)}{\mathcal{B}(D^0 \rightarrow K^*(892)^-e^+\nu_e)} = 0.955 \pm 0.020 \pm 0.017$
 $\mathcal{R}_{\mu/e} = \frac{\mathcal{B}(D^0 \rightarrow \bar{K}^0\pi^-\mu^+\nu_\mu)}{\mathcal{B}(D^0 \rightarrow \bar{K}^0\pi^-e^+\nu_e)} = 0.951 \pm 0.020 \pm 0.016$
- **First FF measurement**
 $r_V = \frac{V(0)}{A_1(0)} = 1.46 \pm 0.11 \pm 0.04$
 $r_2 = \frac{A_2(0)}{A_1(0)} = 0.71 \pm 0.08 \pm 0.03$
 $A_1(0) = 0.623 \pm 0.008 \pm 0.008$

$$D^+ \rightarrow \bar{K}^*(892)^0 \ell^+ \nu_\ell \text{ via } \bar{K}^*(892)^0 \rightarrow K_S^0 \pi^0$$



arXiv:2506.05761, Accepted by PRL



Data: 20.3 fb $^{-1}$ @3.773 GeV

• First observation of $D^+ \rightarrow K_S^0 \pi^0 \mu^+ \nu_\mu$

$$\mathcal{B}(D^+ \rightarrow K_S^0 \pi^0 \mu^+ \nu_\mu) = (0.896 \pm 0.017 \pm 0.008)\%$$

$$\mathcal{B}(D^+ \rightarrow K_S^0 \pi^0 e^+ \nu_e) = (0.943 \pm 0.012 \pm 0.010)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^*(892)^0 \mu^+ \nu_\mu) = (5.00 \pm 0.10 \pm 0.06)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^*(892)^0 e^+ \nu_e) = (5.29 \pm 0.07 \pm 0.06)\%$$

• LFU test ($\mathcal{R}_{\text{SM}} \sim 0.92 - 0.95$) Consistent

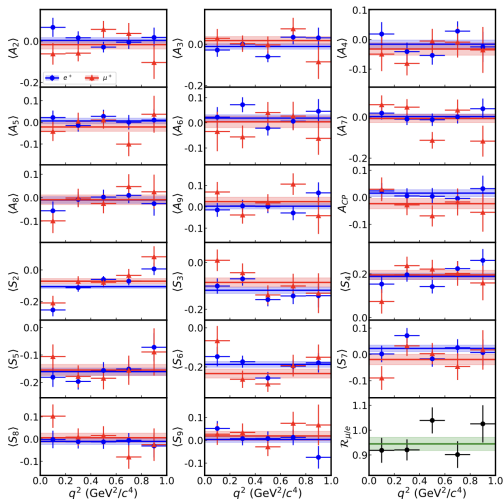
$$\mathcal{R}_{\mu/e} = \frac{\mathcal{B}(D^+ \rightarrow \bar{K}^*(892)^0 \mu^+ \nu_\mu)}{\mathcal{B}(D^+ \rightarrow \bar{K}^*(892)^0 e^+ \nu_e)} = 0.94 \pm 0.02 \pm 0.01$$

• Improved FF measurement

$$r_V = \frac{V(0)}{A_1(0)} = 1.42 \pm 0.03 \pm 0.02$$

$$r_2 = \frac{A_2(0)}{A_1(0)} = 0.75 \pm 0.03 \pm 0.01$$

$$D^+ \rightarrow \bar{K}^*(892)^0 \ell^+ \nu_\ell \text{ via } \bar{K}^*(892)^0 \rightarrow K_S^0 \pi^0$$



- NP contributions may result CPV or LFV in $D \rightarrow K_S^0 \pi^0 \ell^+ \nu_\ell$
- LFV can be test via: integrated and q^2 -binned $\mathcal{R}_{\mu/e}$
- CPV can be test via: A_{CP} and a full set of angular observables $\langle A_i \rangle$ and $\langle S_i \rangle$
- In SM model, all $\langle A_i \rangle$, A_{CP} and $\langle S_{7,8,9} \rangle$ are zero.
- No deviation from SM is seen.

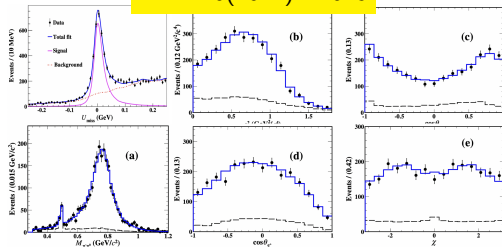
Summary of $D \rightarrow \bar{K}\pi\ell^+\nu_\ell$

	$D^0 \rightarrow \bar{K}^0\pi^-e^+\nu_e$	$D^0 \rightarrow \bar{K}^0\pi^-\mu^+\nu_\mu$	$D^0 \rightarrow K^-\pi^0\mu^+\nu_\mu$	$D^+ \rightarrow K^0\pi^0\ell^+\nu_\ell$
Reference	JHEP03(2025)197	PRL135(2025)111803	PRL134(2025)011803	arXiv:2506.05761 Accepted by PRL
Data Set (fb^{-1})	7.93	7.93	7.93	20.3
Signal yields	8752 ± 132	6796 ± 98	6436 ± 119	$e : 11095 \pm 137$ $\mu : 6767 \pm 126$
$\mathcal{B}(D \rightarrow \bar{K}\pi\ell^+\nu_\ell)(\%)$	$1.444 \pm 0.022 \pm 0.024$	$1.373 \pm 0.020 \pm 0.023$	$0.729 \pm 0.014 \pm 0.011$	$e : 0.943 \pm 0.012 \pm 0.010$ $\mu : 0.896 \pm 0.017 \pm 0.008$
$\mathcal{B}(D \rightarrow \bar{K}^*\ell^+\nu_\ell)(\%)$	$2.039 \pm 0.032 \pm 0.034$	$1.948 \pm 0.033 \pm 0.036$	$2.062 \pm 0.039 \pm 0.032$	$e : 5.29 \pm 0.07 \pm 0.06$ $\mu : 5.00 \pm 0.10 \pm 0.06$
r_V	$1.48 \pm 0.05 \pm 0.02$	$1.46 \pm 0.11 \pm 0.04$	$1.37 \pm 0.09 \pm 0.03$	$1.42 \pm 0.03 \pm 0.02$
r_2	$0.70 \pm 0.04 \pm 0.02$	$0.71 \pm 0.08 \pm 0.03$	$0.76 \pm 0.06 \pm 0.02$	$0.75 \pm 0.03 \pm 0.01$
$\mathcal{R}_{\mu/e}^{K^*}$	$0.955 \pm 0.020 \pm 0.017$		$1.020 \pm 0.030 \pm 0.028$	$0.94 \pm 0.02 \pm 0.01$

Studies of $D^+ \rightarrow K^-\pi^+\ell^+\nu_\ell$ are ongoing

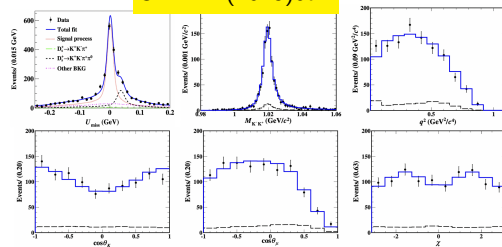
$D^0 \rightarrow \rho(770)^- e^+ \nu_e$ and $D_s^+ \rightarrow \phi \mu^+ \nu_\mu$

PRD110(2024)112018



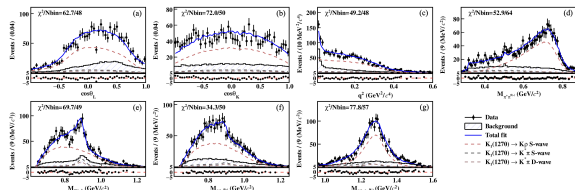
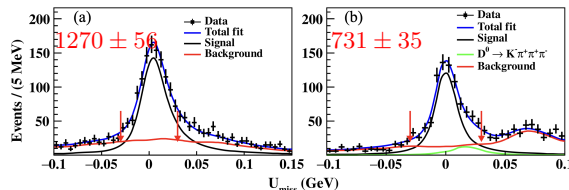
- Data: $7.9 \text{ fb}^{-1} @ 3.773 \text{ GeV} \Rightarrow N = 3337 \pm 77$
- **Precision of BF is improved by $1.6\times$**
 $\mathcal{B}(D^0 \rightarrow \rho^- e^+ \nu_e) = (1.439 \pm 0.033 \pm 0.027) \times 10^{-3}$
- **Updated FF measurement**
 $r_V = 1.548 \pm 0.079 \pm 0.041; r_2 = 0.823 \pm 0.056 \pm 0.026$

JHEP12(2023)072

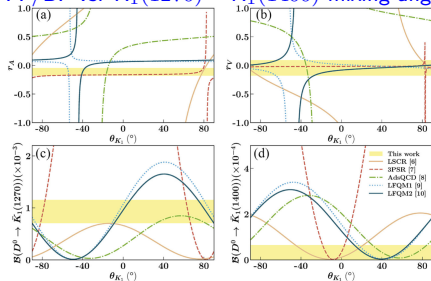


- Data: $7.33 \text{ fb}^{-1} @ 4.128\text{-}4.226 \text{ GeV} \Rightarrow N = 1725 \pm 68$
- **Precision of BF is improved by $4.3\times$**
 $\mathcal{B}(D_s^+ \rightarrow \phi \mu^+ \nu_\mu) = (2.25 \pm 0.09 \pm 0.07)\%$
- **Updated FF measurement**
 $r_V = 1.58 \pm 0.17 \pm 0.02; r_2 = 0.71 \pm 0.14 \pm 0.02$
- **LFU test:** $\mathcal{R}_{\mu/e}^\phi = 0.94 \pm 0.08$

$$D^{0(+)} \rightarrow \bar{K}_1(1270)e^+\nu_e \text{ via } \bar{K}_1(1270) \rightarrow K^-\pi^+\pi^0(-)$$



FF/BF vs. $K_1(1270) - K_1(1400)$ mixing angle θ_{K_1}



• Data: 20.3 fb^{-1} @ 3.773 GeV **PRL135(2025)091801**

• Improved measurement of BF

$$\mathcal{B}(D^+ \rightarrow \bar{K}_1(1270)^0 e^+ \nu_e) = (2.27 \pm 0.11 \pm 0.10) \times 10^{-3}$$

$$\mathcal{B}(D^0 \rightarrow K_1(1270)^- e^+ \nu_e) = (1.02 \pm 0.06 \pm 0.07) \times 10^{-3}$$

• First extraction of FF [cited from PRD104(2021)053003]

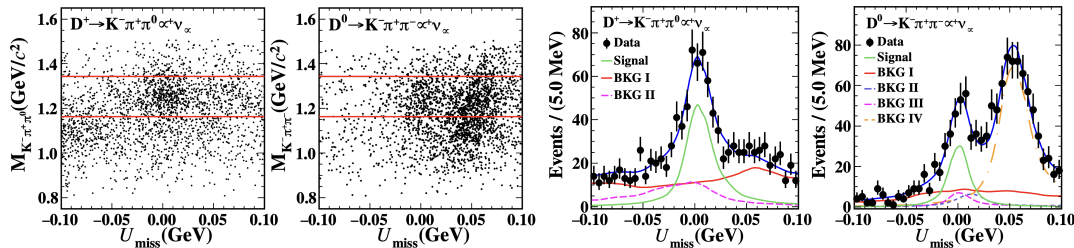
$$r_A = (-11.2 \pm 1.0 \pm 0.9) \times 10^{-2}$$

$$r_V = (-4.3 \pm 0.10 \pm 2.5) \times 10^{-2}$$

• No evidence of $D \rightarrow \bar{K}_1(1400)e^+\nu_e$; UL is set at 90% C.L.

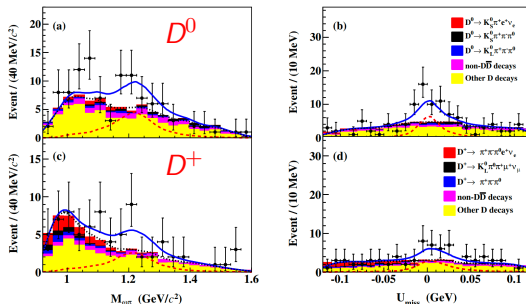
$$\mathcal{B}(D^{0(+)} \rightarrow \bar{K}_1(1400)e^+\nu + e) < 1.4 \times 10^{-4} (0.7 \times 10^{-4})$$

$$D^{0(+)} \rightarrow \bar{K}_1(1270)\mu^+\nu_\mu \text{ via } \bar{K}_1(1270) \rightarrow K^-\pi^+\pi^{0(-)}$$



- Data: 7.9 fb^{-1} @ 3.773 GeV PRD111(2025)L071101
- **Observation of $D^+ \rightarrow \bar{K}_1(1270)^0 \mu^+ \nu_\mu$ (12.5σ) and $D^0 \rightarrow K_1(1270)^- \mu^+ \nu_\mu$ (6.0σ)**
 $\mathcal{B}(D^+ \rightarrow \bar{K}_1(1270)^0 \mu^+ \nu_\mu) = (2.36 \pm 0.20_{-0.27}^{+0.18} \pm 0.48) \times 10^{-3}$
 $\mathcal{B}(D^0 \rightarrow K_1(1270)^- \mu^+ \nu_\mu) = (0.78 \pm 0.11_{-0.09}^{+0.05} \pm 0.15) \times 10^{-3}$
- **LFU test:** $\mathcal{R}_{\mu/e}^{D^+} = 1.03 \pm 0.14_{-0.15}^{+0.11}$; $\mathcal{R}_{\mu/e}^{D^0} = 0.74 \pm 0.13_{-0.13}^{+0.08}$
- **Isospin conservation:** $\frac{\Gamma(D^+ \rightarrow \bar{K}_1(1270)^0 \mu^+ \nu_\mu)}{\Gamma(D^0 \rightarrow K_1(1270)^- \mu^+ \nu_\mu)} = 1.22 \pm 0.10_{-0.09}^{+0.06}$

$D^{0(+)} \rightarrow b_1(1235)e^+\nu_e$ via $b_1(1235) \rightarrow \omega\pi$



- Data: 7.9 fb^{-1} @ 3.773 GeV [arXiv:2407.20551](https://arxiv.org/abs/2407.20551), submitted to PRL
- **First observation of $D^0 \rightarrow b_1(1235)e^+\nu_e$ (5.2σ); Evidence of $D^+ \rightarrow b_1(1235)^0e^+\nu_e$ (3.1σ)**
 $\mathcal{B}(D^0 \rightarrow b_1(1235)^- e^+ \nu_e, b_1(1235)^- \rightarrow \omega\pi^-) = (0.72 \pm 0.18^{+0.06}_{-0.08}) \times 10^{-4}$
 $\mathcal{B}(D^+ \rightarrow b_1(1235)^0 e^+ \nu_e, b_1(1235)^0 \rightarrow \omega\pi^0) = (1.16 \pm 0.44 \pm 0.16) \times 10^{-4}$
- **Isospin test:** $\frac{\Gamma(D^0 \rightarrow b_1^- e^+ \nu_e)}{2\Gamma(D^+ \rightarrow b_1^0 e^+ \nu_e)} = 0.78 \pm 0.19 \pm 0.05$, consistent with 1

Summary and Prospect

Summary:

- Recent results of semileptonic decays of charm meson at BESIII are reported:
 - Precisions of $|V_{cs}|$ and $f_+^{D \rightarrow \bar{K}}(0)$ have been reduced to 0.5% and 0.25%, respectively!
 - No evidence of $\mu - e$ LFU violation is found (especially for $D^{0(+)} \rightarrow \bar{K} \ell^+ \nu_\ell$ $\sigma = 0.7\%(1.5\%)$)
 - Precision measurements of BF and FF for $D_{(s)} \rightarrow \eta^{(\prime)} \ell^+ \nu_\ell$ and $D \rightarrow \bar{K}^* \ell^+ \nu_\ell$
 - Study the nature of light hadrons in semi-leptonic decay (a_0 , f_0 , b_1 and K_1)

Prospect:

- 20.3 fb^{-1} data @3.773 GeV is ready at Jul. 2024, more precision measurements, searching for rare semileptonic decays, and jointed measurements of multiple channels will be presented;
- Additional 3 fb^{-1} data @4.178 GeV in future [CPC44(2020)040001] will further improve the precisions in D_s sector.

Thank you