Global Analyses of Collinear Fragmentation Functions from the NPC Collaboration

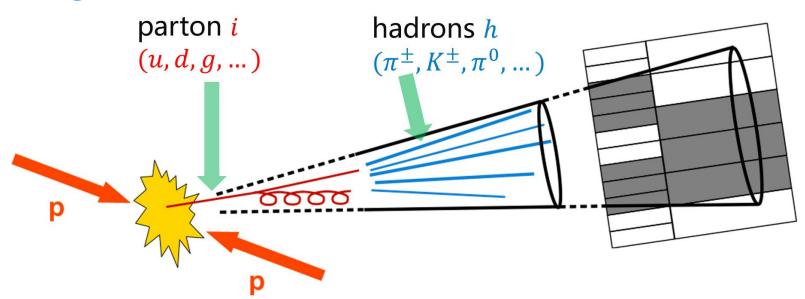
XiaoMin Shen(沈晓民) Institute of Modern Physics, CAS

On behalf of the Non-Perturbative Physics Collaboration (NPC)





Fragmentation Functions (FFs)



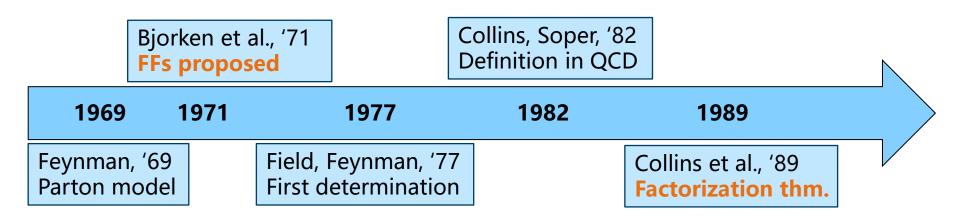
To describe hadronization parton i hadron h

$$D_{h/i}(z \equiv p_h^+/p_i^+) =$$

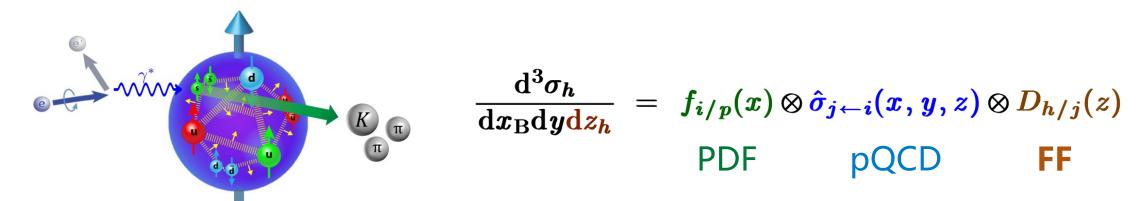
- the number density of hadron h
- carrying a fraction of momentum z
- of parton i



Why FFs: key ingredients of QCD factorization framework



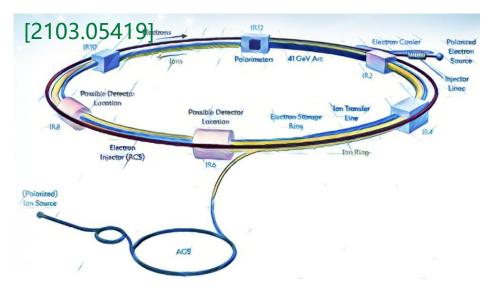
Semi-Inclusive DIS (SIDIS): e + N -> e + h + X

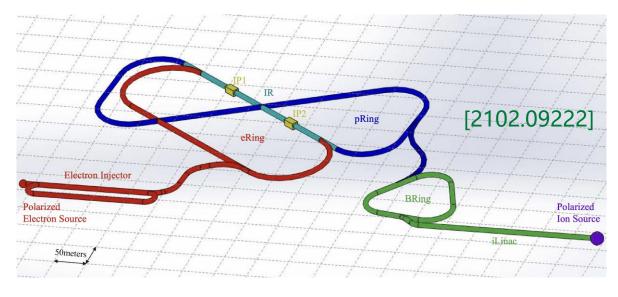


$$ightharpoonup e^+e^-
ightharpoonup h + X \quad pQCD \otimes FF$$

 $pp \rightarrow h + X$ PDF \otimes PDF \otimes pQCD \otimes FF

Why FFs: key role in the era of high-precision physics





- Electron-Ion Collider (EIC)
 - start operation in the early 2030s
 - unprecedented access to nucleon structure

- Electron-ion collider in China(EicC)
 - helicity structure of sea quarks
 [see Yuxiang's talk on Tuesday]

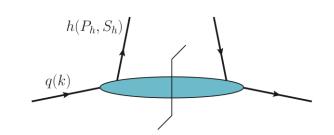


High-precision FFs will be key input to the EIC/EicC physics.

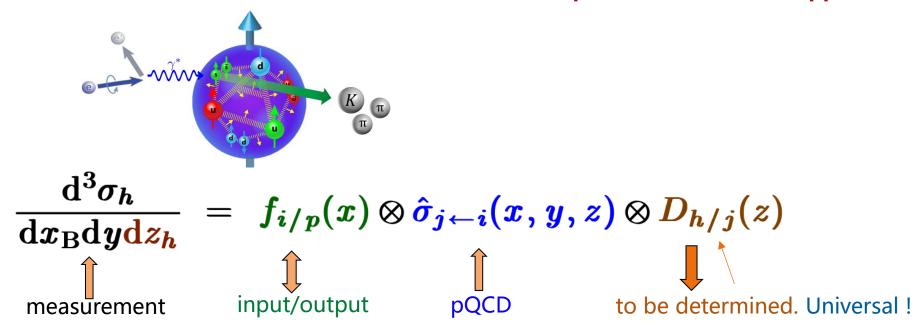
Determination of FFs from global data fit

❖ Field theory definiton of the collinear (integrated) quark FFs [Collins, Soper '82]

$$D_{h/q}(z) = \frac{z}{4} \sum_{X} \int \frac{d\xi^{+}}{2\pi} e^{iP_{h}^{-}\xi^{+}/z} \operatorname{Tr} \left[\langle 0 | \mathcal{W}(\infty^{+}, \xi^{+}) | \psi_{q}(\xi^{+}, 0^{-}, \vec{0}_{T}) | P_{h}, S_{h}; X \rangle \right] \times \langle P_{h}, S_{h}; X | \bar{\psi}_{q}(0^{+}, 0^{-}, \vec{0}_{T}) | \mathcal{W}(0^{+}, \infty^{+}) | 0 \rangle \gamma^{-}$$



❖ Global data fits based on factorization formula ep(SIDIS) + ee(SIA) + pp collisions





Outline

> Introduction

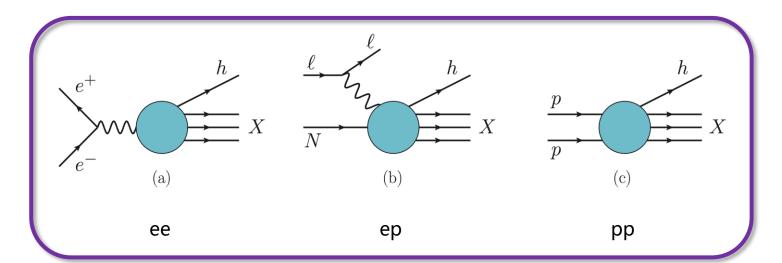
NPC=Non-Perturbative Physics Collaboration

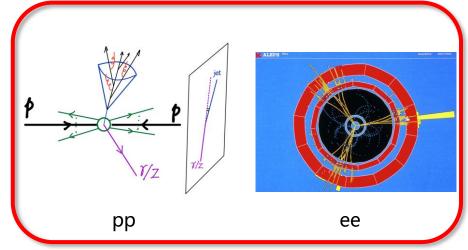
- ➤ Global fits of FFs at NLO from NPC
- > NPC analyses of FFs at NNLO

collaboration	NNFF	JAM	DSS+	BDSSV	MAP	NPC
SIA(ee)	✓	\checkmark	√	\checkmark	✓	
SIDIS (ep)	X	\checkmark	\checkmark	\checkmark	✓	\checkmark
pp incl. hadron	X	X	\checkmark	X	X	✓
hadron in jet	X	X	X	X	X	$\setminus \checkmark /$
FFs (charged h)	π^{\pm}, K^{\pm}, p	π^{\pm},K^{\pm}	π^{\pm}, K^{\pm}, p	π^\pm	$\pi^{\pm},\!K^{\pm}$	π^{\pm}, K^{\pm}, p
FFs (neutral h)			$\mid \eta \mid$			K^0,η,Λ
pQCD order	NNLO	NLO	NLO	appr. NNLO	appr. NNLO	NLO

Only some of the recent global analyses are shown here.

NPC FFs analyses incorporate various types of data





single-inclusive hadron production

hadron in jet measurements

> Hadron-in-jet data provides direct probe of z dependence

$$\frac{p_{T,h}}{p_{T,j}} \stackrel{\mathrm{LO}}{\longrightarrow} z$$

All theoretical predictions calculated with FMNLO.

[Liu, XS, Zhou, Gao, 2305.14620 (JHEP)]



figure credit: A. Metz, A. Vossen,1607.02521; ALEPH Collaboration

Experiments	N_{pt}	χ^2	χ^2/N_{pt}
ATLAS jets †	446	350.8	0.79
ATLAS Z/γ + jet [†]	15	31.8	2.12
CMS Z/γ + jet [†]	15	17.3	1.15
LHCb Z + jet	20	30.6	1.53
ALICE inc. hadron	147	150.6	1.02
STAR inc. hadron	60	42.2	0.70
pp sum	703	623.3	0.89
TASSO	8	7.0	0.88
TPC	12	11.6	0.97
OPAL	20	16.3	0.81
OPAL (202 GeV) †	17	24.2	1.42
ALEPH	42	31.4	0.75
DELPHI	78	36.4	0.47
DELPHI (189 GeV)	9	15.3	1.70
SLD	198	211.6	1.07
SIA sum	384	353.8	0.92
H1 [†]	16	12.5	0.78
H1 (asy.) [†]	14	12.2	0.87
ZEUS †	32	65.5	2.05
COMPASS (061)	124	107.3	0.87
COMPASS $(16p)$	97	56.8	0.59
SIDIS sum	283	254.4	0.90
Global total	1370	1231.5	0.90

NPC23 π^{\pm} , K^{\pm} , p FFs fit

collaboration	year	$\sqrt{s}[\mathrm{GeV}]$	χ^2	$N_{ m pt}$	$\chi^2/N_{ m pt}$
TASSO	1985	14	5.65	9 9	0.63
TASSO	1985	22	5.87	6	0.98
TASSO	1985	34	16.03	13	1.23
TASSO	1990	14.8	12.56	9	1.40
TASSO	1990	21.5	3.78	6	0.63
TASSO	1990	34.5	17.51	13	1.35
TASSO	1990	35	14.76	13	1.14
TASSO	1990	42.6	33.60	13	2.58
TPC	1984	29	2.75	8	0.34
MARK II	1985	29	12.65	17	0.74
HRS	1987	29	33.16	12	2.76
CELLO	1990	35	2.71	9	0.30
TOPAZ	1995	58	0.29	4	0.07
OPAL	1991	91.2	7.75	7	1.11
OPAL	1995	91.2	13.63	16	0.85
OPAL	2000	91.2	8.62	16	0.54
ALEPH	1998	91.2	6.39	16	0.40
ALEPH	2000	91.2	12.72	14	0.91
ALEPH jet 1	2000	91.2	14.91	12	1.24
ALEPH jet 2	2000	91.2	8.21	13	0.63
ALEPH jet 3	2000	91.2	8.55	11	0.78
DELPHI	1995	91.2	7.55	13	0.58
SLD	1999	91.2	7.39	9	0.82
SLD c -tagged	1999	91.2	17.44	9	1.94
SLD <i>b</i> -tagged	1999	91.2	11.12	9	1.24
SIA sum			285.60	277	1.03
ZEUS $Q^2 \in 160,640 \mathrm{GeV^2}$	2012	318	4.41	5	0.88
ZEUS $Q^2 \in 640, 2560 \mathrm{GeV}^2$	2012	318	3.26	5	0.65
ZEUS $Q^2 \in 2560, 10240 \mathrm{GeV^2}$	2012	318	2.74	2	1.37
SIDIS sum			10.41	12	0.87
ALICE $N_{K_S^0}^{13\mathrm{TeV}}/N_{K_S^0}^{7\mathrm{TeV}}$	2021	13000 & 7000	2.88	10	0.29
ALICE $N_{K^0_S}/N_{\pi^\pm}$	2021	13000	5.79	15	0.39
pp sum			8.67	25	0.35
total sum			304.68	314	0.97

NPC23 K⁰ FFs fit

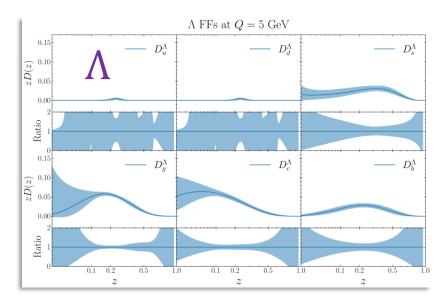


The NPC FF sets at NLO

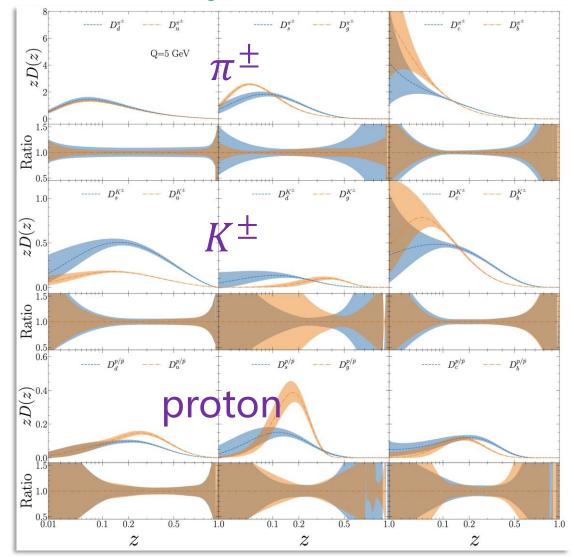
NPC FF sets are publicly available

LHAPDF 6,5,5

Main page	PDF sets	Class hierarchy	Examples	More				
2070000	NPC23_	Plp_nlo			(tarball) (info file)	127	
2070200	NPC23_	_KAp_nlo			(tarball	(info file)	127	
2070400	NPC23_	PRp_nlo			(tarball	(info file)	127	
2070600	NPC23_	Plm_nlo			(tarball) (info file)	127	
2070800	NPC23_	_KAm_nlo			(tarball	(info file)	127	
2071000	NPC23_	PRm_nlo			(tarball	(info file)	127	
2071200	NPC23_	NPC23_Plsum_nlo (tarball) (info file)						
2071400	NPC23_	_KAsum_nlo			(tarball	(info file)	127	
2071600	NPC23_	PRsum_nlo			(tarball	(info file)	127	
2071800	NPC23_	_CHHAp_nlo			(tarball) (info file)	127	
2072000	NPC23_	_CHHAm_nlo			(tarball	(info file)	127	
2072200	NPC23_	CHHAsum_nlo			(tarball) (info file)	127	



Gao, Liu, **XS**, Xing, Zhao, *PRL 132, 261903,* '24 Gao, Liu, **XS**, Xing, Zhao, *PRD 110, 114019,* '24 (Editors' suggestion) Gao, Liu, Li, **XS**, Xing, Zhao, Zhou, *PRD 112, 054045, '25*





Both charged and neutral hadron FFs determined

collaboration	NNFF	JAM	$\mathrm{DSS}+$	BDSSV	MAP	NPC
SIA(ee)	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
SIDIS (ep)	X	\checkmark	\checkmark	✓	\checkmark	√
pp incl. hadron	X	X	\checkmark	X	X	\checkmark
hadron in jet	X	X	X	X	X	\checkmark
FFs (charged h)	π^{\pm}, K^{\pm}, p	π^{\pm},K^{\pm}	π^{\pm}, K^{\pm}, p	π^\pm	$\pi^{\pm},\!K^{\pm}$	$\pi^{\pm},\!K^{\pm},\!p$
FFs (neutral h)			η			K^0,η,Λ
pQCD order	NNLO	NLO	NLO	appr. NNLO	appr. NNLO	NLO

- > FFs determination at NLO from Nonperturbative Physics Collaboration (NPC)
 - NPC23 FFs to light charged hadrons:

Gao, Liu, **XS**, Xing, Zhao, *PRL 132, 261903,* '24 Gao, Liu, **XS**, Xing, Zhao, *PRD 110, 114019,* '24 (Editors' suggestion)

NPC23 FFs to light neutral hadrons:

Gao, Liu, Li, XS, Xing, Zhao, Zhou, PRD 112, 054045, '25



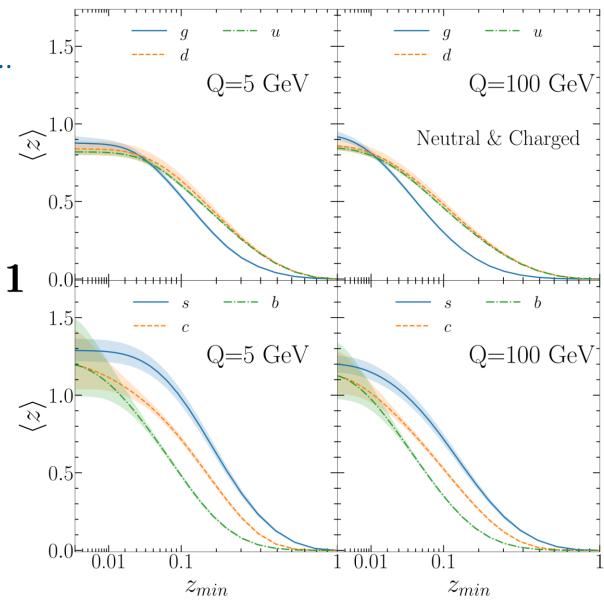
Test sum rule using neutral + charged hadron FFs

parton i hadrons $h = \pi^{\pm}, \pi^{0}, K^{\pm}, K^{0}, \cdots$

> The momentum sum rule:

$$\lim_{z_{\min} \to 0} \sum_{h} \int_{z_{\min}}^{1} \left[z D_{h/i}(z) \right] dz = 1 \quad 0.0$$

Gao, Liu, **XS**, Xing, Zhao, *PRL 132, 261903,* '24 Gao, Liu, Li, **XS**, Xing, Zhao, Zhou, *PRD 112, 054045, '25*



IMP.

Outline

- > Introduction
- > NPC analyses of FFs at NLO
- ➤ NPC analyses of FFs at NNLO + constraints on PDFs

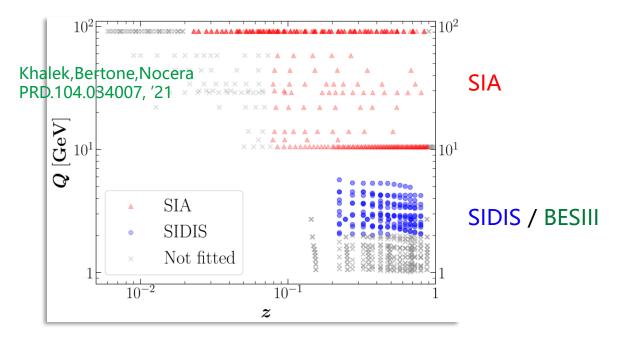
collaboration	NNFF	JAM	$\mathrm{DSS} +$	BDSSV	MAP	NPC	NPC
SIA(ee)	✓	√	√	√	√	✓	√
SIDIS (ep)	X	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	✓
pp incl. hadron	X	X	✓	X	X	\checkmark	X
hadron in jet	X	X	X	X	X	✓	X
FFs	π^{\pm},K^{\pm},p	$\pi^{\pm},\!K^{\pm}$	$\pi^{\pm}, K^{\pm}, p, h^{\pm}$	π^\pm	$\pi^{\pm},\!K^{\pm}$	$\pi^{\pm},\!K^{\pm},\!p,\!h^{\pm}$	$\pi^{\pm},\!K^{\pm}$
			η			K^0,η,Λ	
pQCD order	NNLO	NLO	NLO	appr. NNLO	appr. NNLO	NLO	NNLO

Global analysis of FFs at full NNLO: the datasets

$SIA(e^+e^-)$ data used in the fit:

	/= /O.V	1 ()		C1 -4-4	la a durana
\exp .	$\sqrt{s}/{ m GeV}$	$ \operatorname{lum.}(n_Z) $	year	final states	hadrons
DELPHI	189	157.7 pb^{-1}	2002	inc. had.	π^{\pm}, K^{\pm}
OPAL	m_Z	780 000	1994	$Z\! o qar q$	π^{\pm}, K^{\pm}
ALEPH	m_Z	520 000	1995	$Z\! o qar q$	π^{\pm}, K^{\pm}
DELPHI	m_Z	1 400 000	1998	$Z\! ightarrow qar q$	π^{\pm}, K^{\pm}
				$Z\! o\! bar b$	π^{\pm},K^{\pm}
				$Z\! ightarrow qar q$	π^{\pm},K^{\pm}
SLD	m_Z	400 000	2004	$Z\! o\! bar b$	π^{\pm}, K^{\pm}
				$Z \rightarrow c\bar{c}$	π^{\pm}, K^{\pm}
TASSO	44	34 pb^{-1}	1989	inc. had.	π^{\pm},π^0
TASSO	34	77 pb^{-1}	1989	inc. had.	π^{\pm}, K^{\pm}
$\mathrm{TPC}/2\gamma$	29	70 pb^{-1}	1988	inc. had.	π^{\pm}, K^{\pm}
Belle	10.52	$68 \; {\rm fb^{-1}}$	2013	inc. had.	π^{\pm}, K^{\pm}
BaBar	10.54	$0.91 \; \mathrm{fb^{-1}}$	2013	inc. had.	π^{\pm}, K^{\pm}
BESIII	2.0-3.671	253 pb^{-1}	2025	inc. had.	π^{\pm}, K^{\pm}

[BESIII, **PRL**135, 151901, 2025]



- Kinematic cuts in our analyses:
 - Q > 3 GeV (SIA)
 - Q > 2 GeV(SIDIS)
 - z > 0.01, $E_h > E_{h,min}$ (0.8 GeV by default)



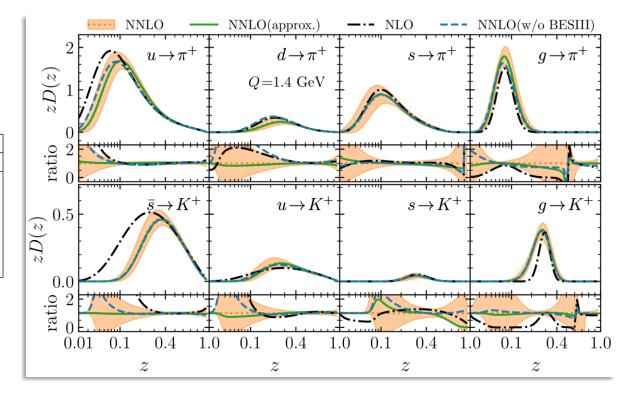
the first test on universality of FFs at Q~3 GeV using both ee and SIDIS data

Global analysis of FFs at full NNLO: results

> Fit quality of the NNLO analyses

	В	ESIII	CO	MPASS	B-fa	actories	H	E-SIA		globa	1
$E_{h,\min}[\mathrm{GeV}]$	$N_{ m pt}$	$\chi^2/N_{ m pt}$	$N_{ m pt}$	χ^2	$\chi^2/N_{ m pt}$						
0.5	242	1.26	358	1.65	233	1.06	426	1.19	1259	1650.2	1.31
0.6	212	1.21	290	1.59	228	0.92	423	0.97	1153	1338.8	1.16
0.7	182	1.11	214	1.47	223	0.61	413	0.84	1032	997.2	0.97
0.8	152	0.98	142	1.30	218	0.53	407	0.82	919	781.8	0.85
0.9	122	1.05	94	1.29	213	0.52	407	0.80	836	687.1	0.82
1.0	98	1.14	54	0.97	209	0.49	403	0.80	764	587.2	0.77

energy cut of the identified hadron



LHAgrids of our FFs have been submitted to the LHAPDF repository.

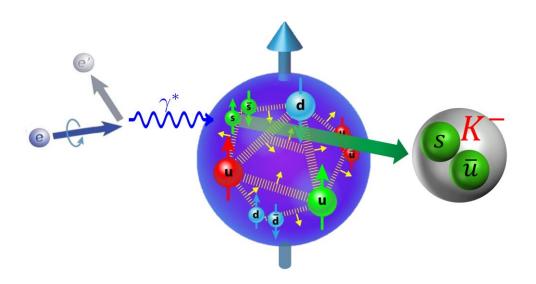
https://www.lhapdf.org/pdfsets.html



Application: constraining proton PDFs at NNLO

SIDIS may also constrain PDFs:

$$rac{\mathrm{d}^3\sigma_h}{\mathrm{d}x_\mathrm{B}\mathrm{d}y\mathrm{d}z_h} = f_{i/p}(x)\otimes\hat{\sigma}_{j\leftarrow i}(x,y,z)\otimes D_{h/j}(z)$$
 unpolarized PDF FF



➤ LO xsec of SIDIS off an isoscalar target (COMPASS)

$$\frac{\mathrm{d}\sigma^{K^{+}}}{\mathrm{d}x\mathrm{d}y\mathrm{d}z} - \frac{\mathrm{d}\sigma^{K^{-}}}{\mathrm{d}x\mathrm{d}y\mathrm{d}z}$$

$$\sim 2\left(u_{v}(x) + d_{v}(x)\right)\left(D_{u}^{K^{+}}(z) - D_{\bar{u}}^{K^{+}}(z)\right)$$

$$+ \left(s(x) - \bar{s}(x)\right)\left(D_{s}^{K^{+}}(z) - D_{\bar{s}}^{K^{+}}(z)\right) + \cdots$$
PDF

FF

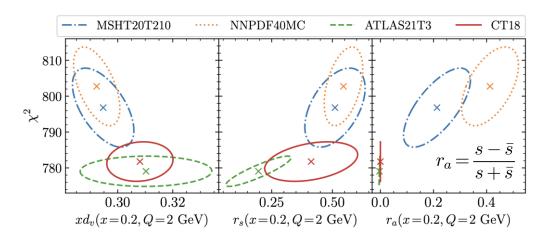
is sensitive to strangeness asymmetry

$$r_a = \frac{s - \bar{s}}{s + \bar{s}}$$



Application: constraining proton PDFs at NNLO

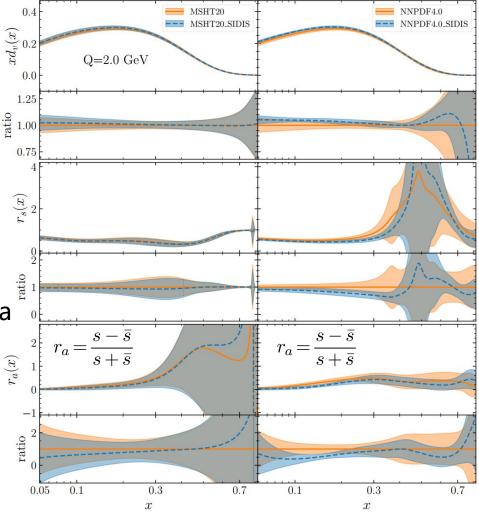
 \triangleright Correlation between χ^2 and PDFs



Modified PDFs which reflect the impact of SIDIS data

- Reweighting of the NNPDF4.0 PDF set
- Profiling of the MSHT20 PDF set

[Gao, XS, Xing, Zhao, Zhou, PRL 135, 041902, 2025]



PDF sets before and after reweighting/profiling

Summary

- > NPC collaboration has delivered precise and comprehensive FF sets at NLO.
- > We present the **first** global (SIA+SIDIS) FFs determination at full NNLO.
- > FFs studies may also contribute to nucleon structure analyses.

collaboration	NPC	NPC
SIA(ee)	\checkmark	\checkmark
SIDIS (ep)	\checkmark	\checkmark
pp incl. hadron	\checkmark	X
hadron in jet	\checkmark	X
FFs	π^{\pm},K^{\pm},p	$\pi^{\pm},\!K^{\pm}$
	K^0,η,Λ	
pQCD order	NLO	NNLO

FF sets from NPC: https://www.lhapdf.org/pdfsets.html
NLO charged hadron:

Gao, Liu, **XS**, Xing, Zhao, *PRL 132, 261903*, 2024

Gao, Liu, **XS**, Xing, Zhao, PRD 110, 114019, 2024

NLO neutral hadron:

Gao, Liu, Li, **XS**, Xing, Zhao, Zhou, *PRD 112, 054045,* 2025

NNLO:

Gao, XS, Xing, Zhao, Zhou, PRL 135, 041902, 2025

Thank you for your attention!



Backup slides

NPC collaboration gathering on July 19th 2025

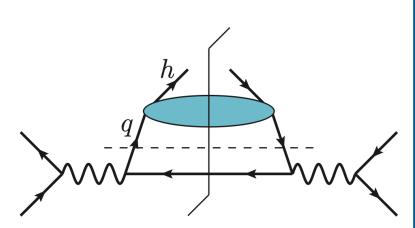




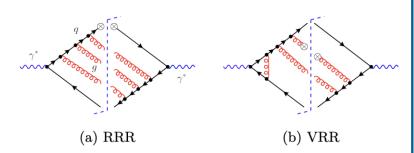
in neighborhood of Huizhou city (host of EICc)

Jun Gao, ChongYang Liu, Meng Yang Li, XiaoMin Shen, HongXi Xing, YuXiang Zhao, Bin Zhou, YiYu Zhou Shanghai JiaoTong Univ., South China Normal Univ., Institute of Modern Physics, CAS

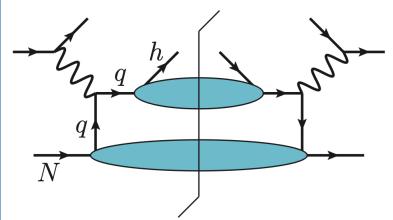
Recent progresses from pQCD



$SIA(e^+e^-)$ at N3LO



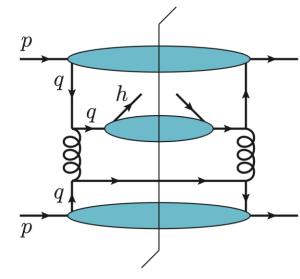
[He, Xing, Yang, Zhu, PRL.135.101901(2025)]



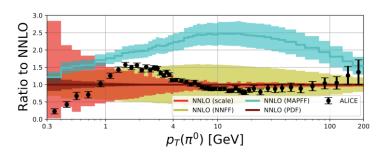
SIDIS(ep) at NNLO

[Bonino, Gehrmann, et al. & Goyal, Moch, et al.

PRL.132.251901, '24, PRL.132.251902, '24, PRL.133.211904, '24, PRL.133.211905, '24, 2504.05376]



pp at NNLO



[Czakon, Generet, Mitov, Poncelet, 2503.11489]



Figure credit: A. Metz, A. Vossen, 1607.02521

Global analysis of FFs at full NNLO: theoretical prediction

FFs at starting scale $Q_0 = 1.4 \text{ GeV}$

parameterized as

$$zD_i^h(z, Q_0) = z^{\alpha_i^h} (1-z)^{\beta_i^h} \exp\left(\sum_{n=0}^m a_{i,n}^h z^{n/2}\right)$$

charge/isospin symmetries suppress number of free parameters (54 in total)

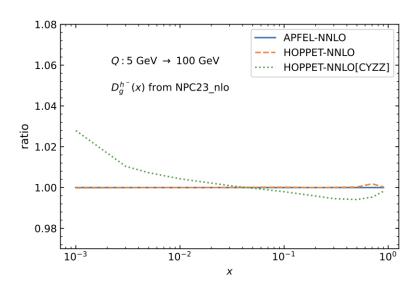
$$D_{u\to\pi^+}(z,Q) = D_{\bar{u}\to\pi^-}(z,Q)$$

$$D_{u\to\pi^+}(z,Q_0) = D_{\bar{d}\to\pi^+}(z,Q_0)$$

FFs at arbitrary energy scale $(Q_0 \rightarrow Q)$

3-loop timelike DGLAP evolution [Mitov, Moch, Vogt, Almasy]

 \rightarrow + $P_{qg}^{T(2)}$ correction[Chen, Yang, Zhu, Zhu, '20]

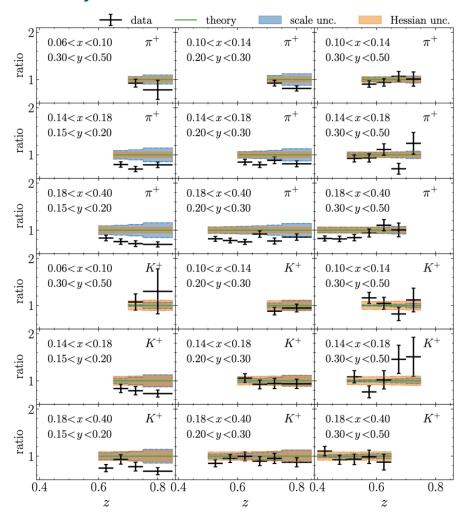


> Heavy quark FFs are frozen below mass threshold.

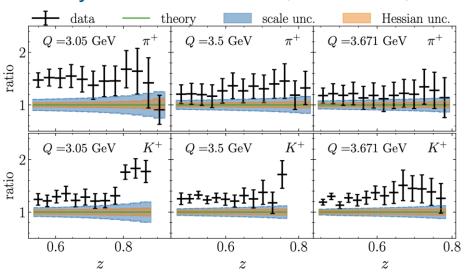


Test on leading-twist collinear factorization at low Q

Theory v.s. data for COMPASS06 (SIDIS: 2~5GeV)



Theory v.s. data for BESIII (SIA: ~3GeV)



- Kinematic cuts in our analyses:
 - Q > 3 GeV (SIA)
 - Q > 2 GeV(SIDIS)
 - $z > 0.01, E_h > 0.8 \text{ GeV}$



the first test on universality of FFs at Q~3 GeV using ee and SIDIS data