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# PRECISE PREDICTIONS ON HIGGS DECAYS TO BOTTOM QUARKS AND GLUONS

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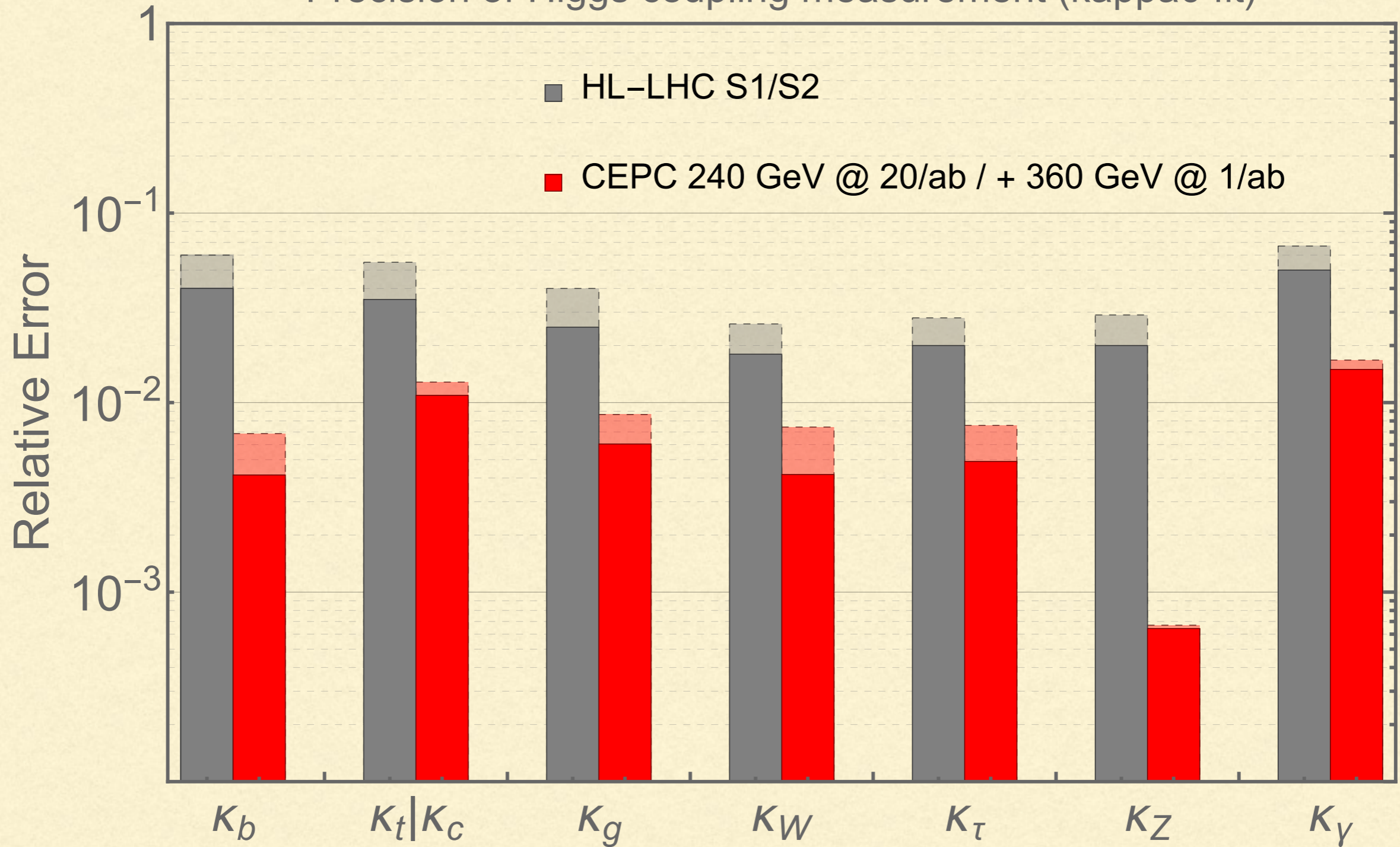
arXiv: 2310.20514, 2411.07493, 2503.22169  
with Xing Wang, Yefan Wang, Da-Jiang Zhang

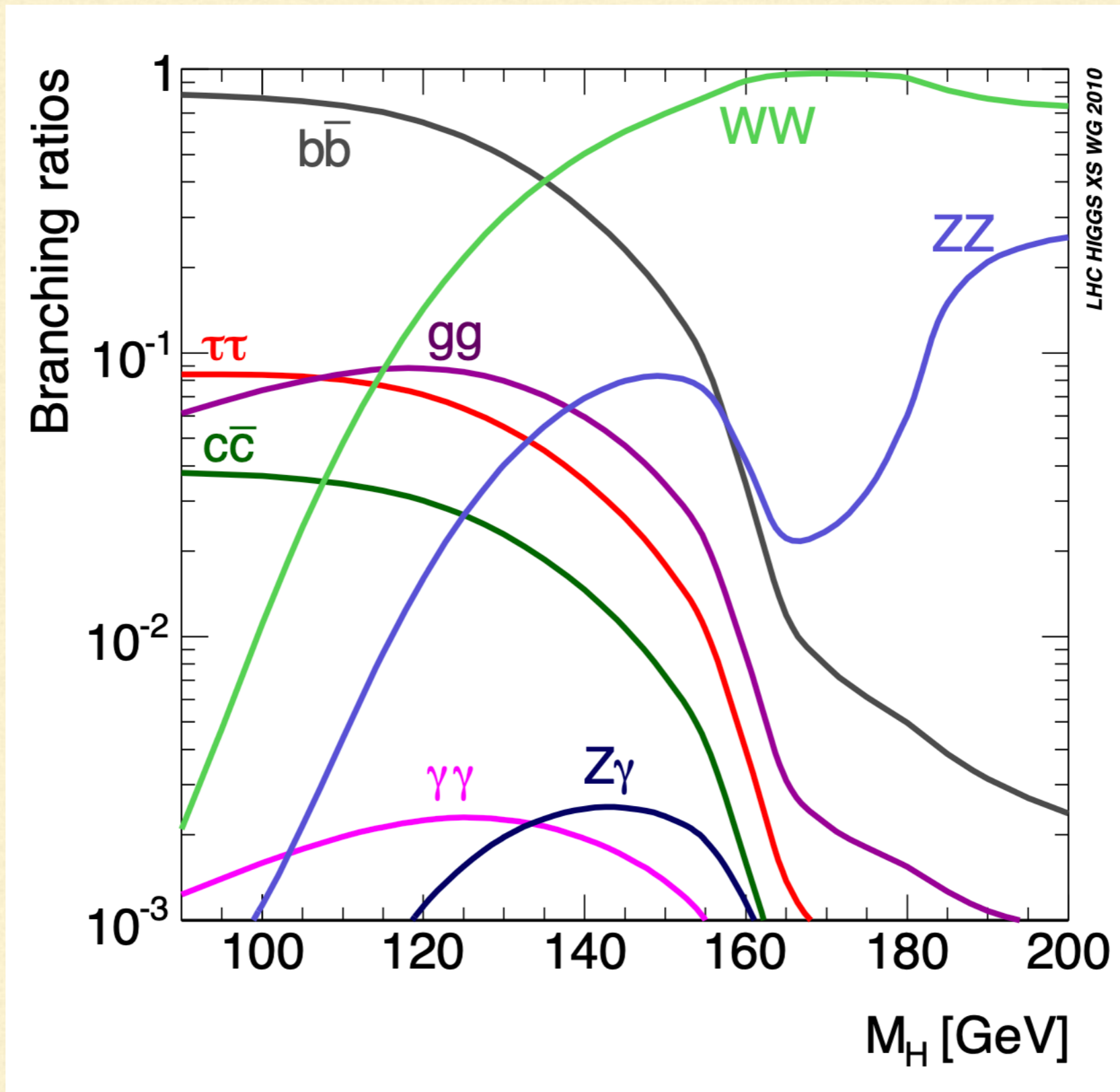
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	240 GeV, 20 ab <sup>-1</sup>		360 GeV, 1 ab <sup>-1</sup>		
	ZH	vvH	ZH	vvH	eeH
inclusive	<b>0.26%</b>		<b>1.40%</b>	\	\
H→bb	<b>0.14%</b>	<b>1.59%</b>	<b>0.90%</b>	<b>1.10%</b>	<b>4.30%</b>
H→cc	<b>2.02%</b>		<b>8.80%</b>	<b>16%</b>	<b>20%</b>
H→gg	<b>0.81%</b>		<b>3.40%</b>	<b>4.50%</b>	<b>12%</b>
H→WW	<b>0.53%</b>		<b>2.80%</b>	<b>4.40%</b>	<b>6.50%</b>
H→ZZ	<b>4.17%</b>		<b>20%</b>	<b>21%</b>	
$H \rightarrow \tau\tau$	<b>0.42%</b>		<b>2.10%</b>	<b>4.20%</b>	<b>7.50%</b>
$H \rightarrow \gamma\gamma$	<b>3.02%</b>		<b>11%</b>	<b>16%</b>	
$H \rightarrow \mu\mu$	<b>6.36%</b>		<b>41%</b>	<b>57%</b>	
$H \rightarrow Z\gamma$	<b>8.50%</b>		<b>35%</b>		
$\text{Br}_{upper}(H \rightarrow inv.)$	<b>0.07%</b>				
$\Gamma_H$	<b>1.65%</b>		<b>1.10%</b>		



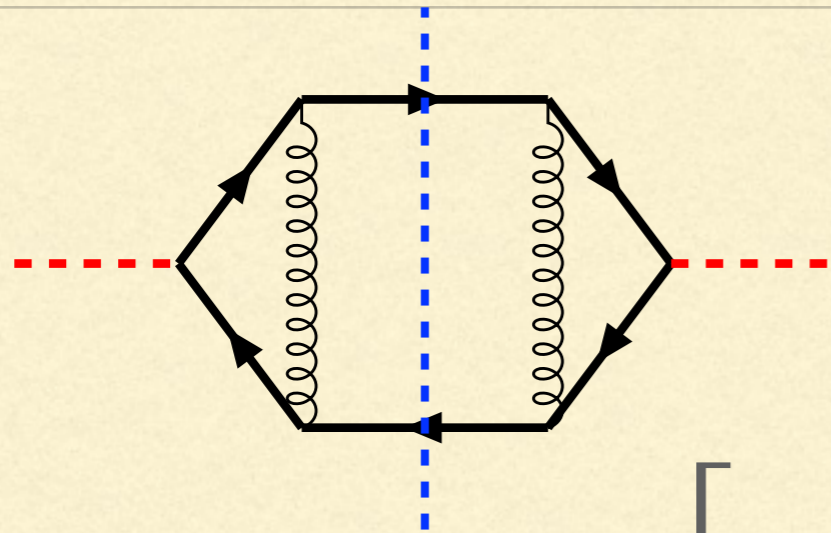
Precision of Higgs coupling measurement (kappa0 fit)







# HIGGS DECAYS TO $b\bar{b} + X$



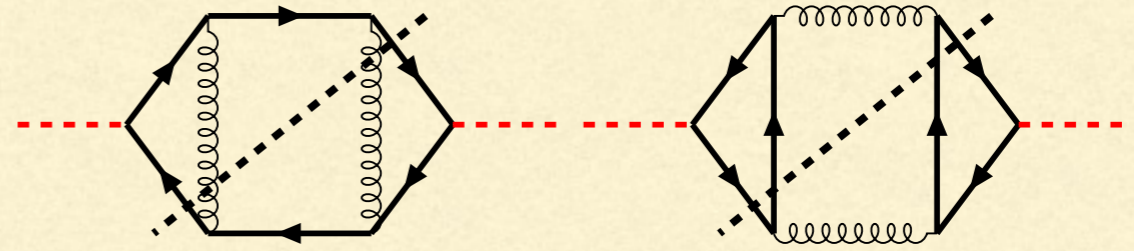
The decay rate is proportional to  $y_b^2$ .

$$\Gamma(H \rightarrow b\bar{b}) = \Gamma_{\text{LO}} \left[ 1 + \frac{\alpha_s(\mu)}{\pi} X_1^{y_b y_b} + \left( \frac{\alpha_s(\mu)}{\pi} \right)^2 (X_2^{y_b y_b} + X_2^{y_b y_t}) \right]$$

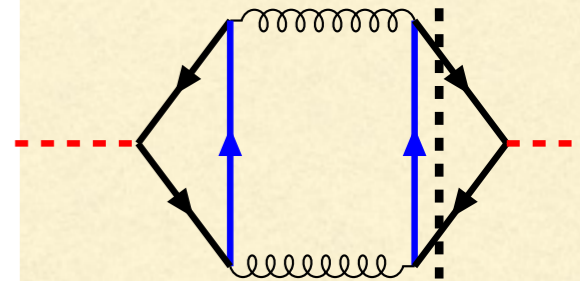
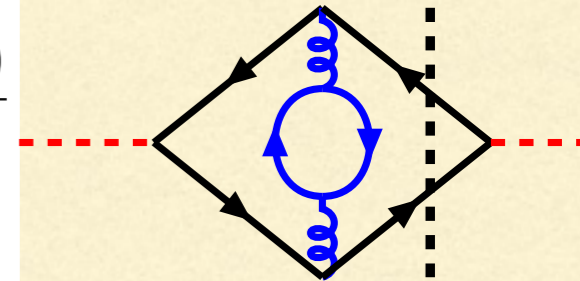
$$\Gamma_{\text{LO}} = \frac{N_c}{16\pi} \bar{y}_b^2 m_H \left( 1 - \frac{4}{z} \right)^{3/2}, \quad z \equiv \frac{m_H^2}{m_b^2}$$

$$X_1^{y_b y_b} = 2 \log \left( \frac{\mu^2}{m_H^2} \right) + \frac{17}{3} + \frac{12 \log(z) + 10}{z} + \mathcal{O}(z^{-2})$$

$$X_2^{y_b y_b} = \tilde{X}_{2, b\bar{b}}^{y_b y_b} + X_{2, b\bar{b}b\bar{b}}^{y_b y_b}$$



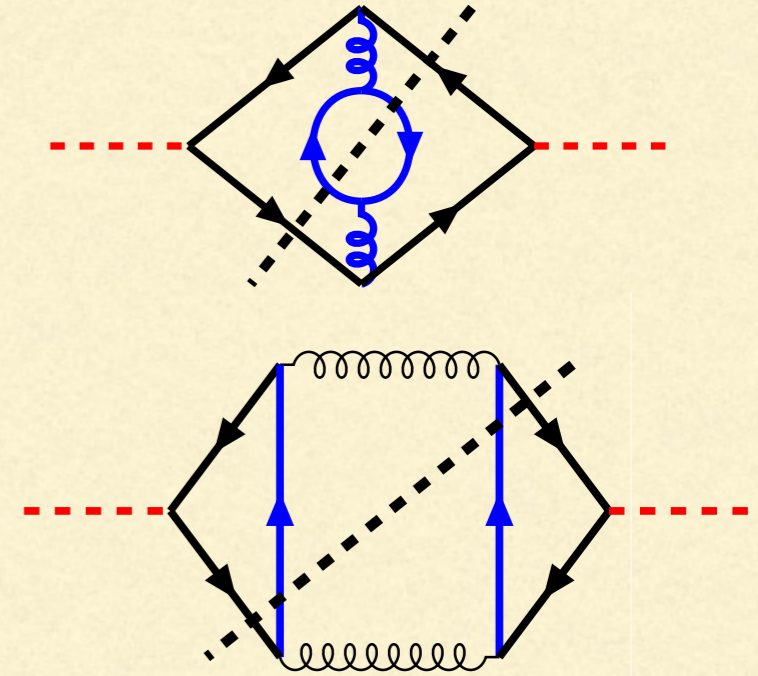
$$\begin{aligned} \tilde{X}_{2, b\bar{b}}^{y_b y_b} \Big|_{z \rightarrow \infty} = & -\frac{\log^3(z)}{27} + \frac{19 \log^2(z)}{54} + \frac{2\zeta(3) \log(z)}{9} + \frac{\pi^2 \log(z)}{54} \\ & - \frac{503 \log(z)}{324} + \frac{55 - 2n_l}{12} \log^2\left(\frac{\mu^2}{m_H^2}\right) + \frac{307 - 11n_l}{9} \log\left(\frac{\mu^2}{m_H^2}\right) + \frac{2(3n_l - 86)\zeta(3)}{9} \\ & + \frac{(3n_l - 98)\pi^2}{54} - \frac{19\pi^4}{1620} + \frac{2 \log(2)\pi^2}{9} + \frac{98681 - 3510n_l}{1296} \\ & + \frac{1}{z} \left( -\frac{5 \log^4(z)}{36} + \frac{\log^3(z)}{18} + \frac{\pi^2 \log^2(z)}{18} - \frac{(2n_l - 9) \log^2(z)}{2} - \frac{7\pi^2 \log(z)}{54} \right. \\ & \left. - (2n_l - 55) \log(z) \log\left(\frac{\mu^2}{m_H^2}\right) - \frac{(117n_l - 3625) \log(z)}{27} - 4\zeta(3) \log(z) \right. \\ & \left. - \frac{71\pi^4}{540} + \frac{4\pi^2 \log(2)}{3} - \frac{5(2n_l - 55)}{6} \log\left(\frac{\mu^2}{m_H^2}\right) + \frac{430\zeta(3)}{9} - \frac{(9n_l - 175)\pi^2}{9} \right. \\ & \left. + \frac{36829 - 1548n_l}{324} \right) + \mathcal{O}(z^{-2}), \end{aligned} \tag{5.}$$



It is divergent in the massless limit!



$$\begin{aligned}
X_{2,bbbb}^{y_b y_b} \Big|_{z \rightarrow \infty} &= \frac{\log^3(z)}{27} - \frac{19 \log^2(z)}{54} - \frac{2\zeta(3) \log(z)}{9} - \frac{\pi^2 \log(z)}{54} + \frac{503 \log(z)}{324} \\
&+ \frac{19\pi^4}{1620} - \frac{2 \log(2)\pi^2}{9} + \frac{5\zeta(3)}{18} + \frac{31\pi^2}{108} - \frac{2491}{648} \\
&+ \frac{1}{z} \left( \frac{\log^4(z)}{18} - \frac{\log^3(z)}{18} - \frac{2\pi^2 \log^2(z)}{9} + \frac{7\pi^2 \log(z)}{54} - \frac{\log^2(z)}{3} + 4\zeta(3) \log(z) \right. \\
&\left. + \frac{211 \log(z)}{54} + \frac{13\pi^4}{270} - \frac{7\zeta(3)}{9} + \frac{19\pi^2}{18} - \frac{8353}{324} \right) + \mathcal{O}(z^{-2}).
\end{aligned}$$

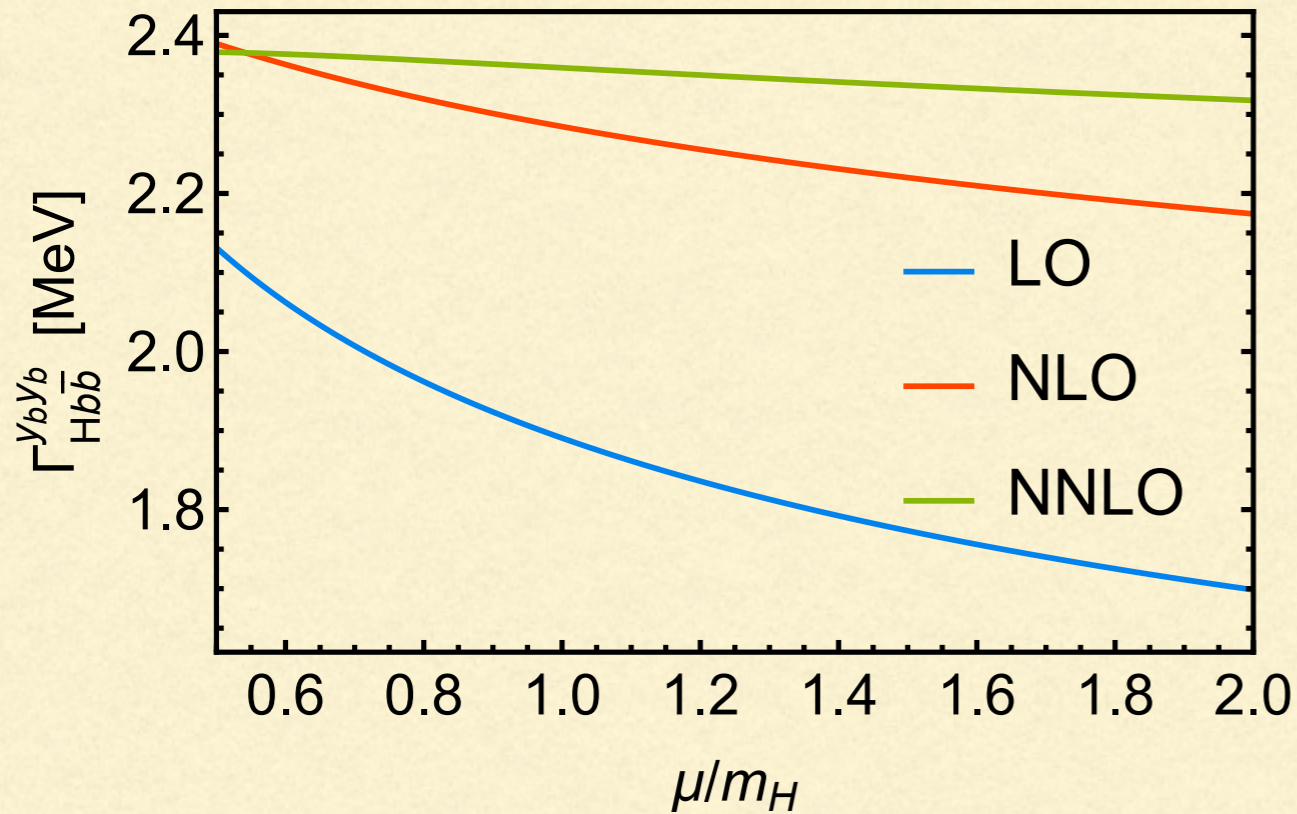


$$\begin{aligned}
X_2^{y_b y_b} \Big|_{z \rightarrow \infty (m_b^2 \rightarrow 0)} &= \frac{55 - 2n_l}{12} \log^2 \left( \frac{\mu^2}{m_H^2} \right) + \frac{307 - 11n_l}{9} \log \left( \frac{\mu^2}{m_H^2} \right) + \frac{(4n_l - 113)\zeta(3)}{6} \\
&+ \frac{(2n_l - 55)\pi^2}{36} + \frac{10411 - 390n_l}{144} + \frac{1}{z} \left( -\frac{\log^4(z)}{12} - \frac{\pi^2 \log^2(z)}{6} - \frac{(6n_l - 25) \log^2(z)}{6} \right. \\
&- \frac{(26n_l - 829) \log(z)}{6} - (2n_l - 55) \log(z) \log \left( \frac{\mu^2}{m_H^2} \right) - \frac{5(2n_l - 55)}{6} \log \left( \frac{\mu^2}{m_H^2} \right) - \frac{\pi^4}{12} \\
&\left. + \frac{4\pi^2 \log(2)}{3} + 47\zeta(3) - \frac{(2n_l - 41)\pi^2}{2} + \frac{791 - 43n_l}{9} \right) + \mathcal{O}(z^{-2}). \tag{5.12}
\end{aligned}$$

The large logarithms at subleading power:  $\log^4(z) = 1688$

$$\overline{m}_b(m_H) = 2.78 \text{ GeV}$$

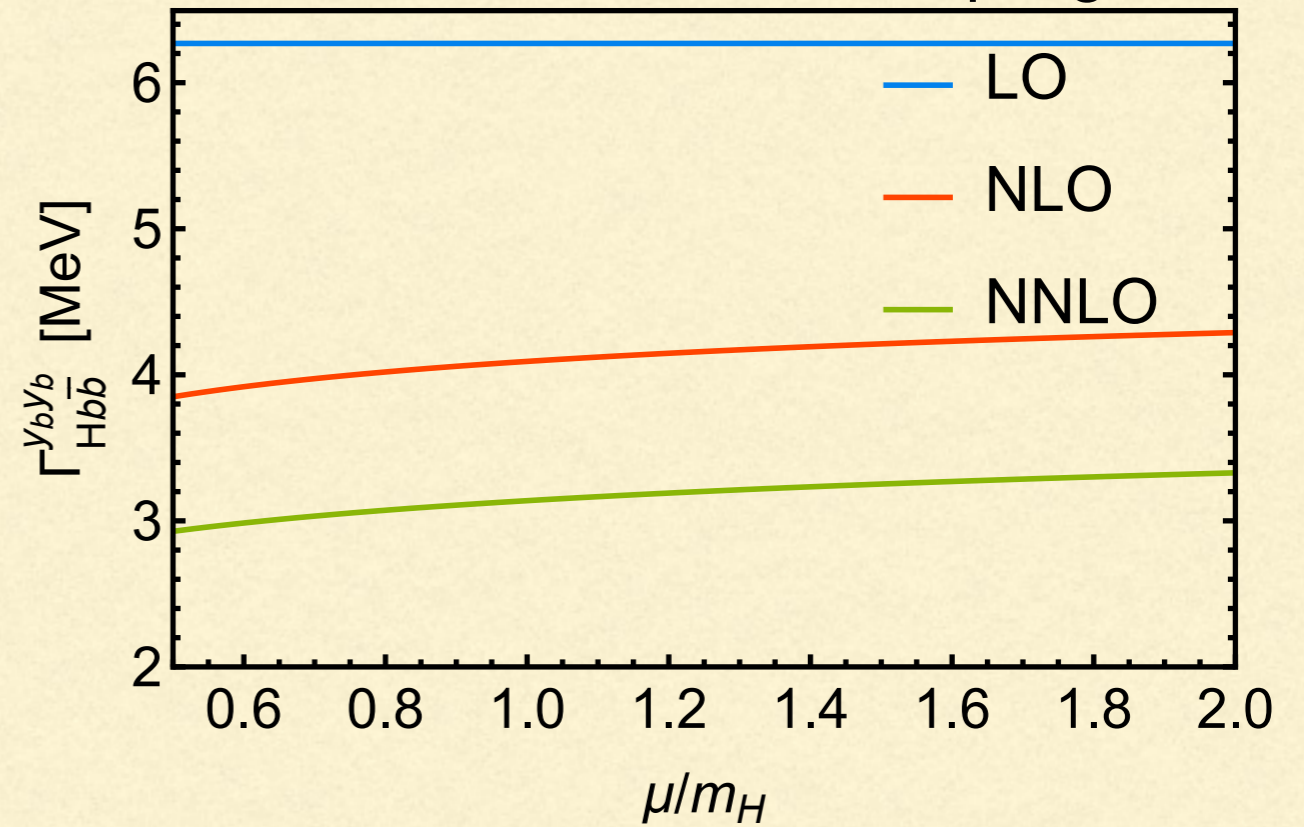
$\overline{\text{MS}}$  Yukawa Coupling



LO unc.  $\sim 23\%$   
 NLO unc.  $\sim 9\%$   
 NNLO unc.  $\sim 3\%$   
 NLO/LO = 1.12-1.28  
 NNLO/NLO = 0-1.07

$$m_b = 5.07 \text{ GeV}$$

On-shell Yukawa Coupling



NLO unc.  $\sim 11\%$   
 NNLO unc.  $\sim 13\%$   
 NLO/LO = 0.65  
 NNLO/NLO = 0.78



width	LO	NLO	NNLO( $y_b^2$ )	NNLO( $y_b y_t$ )	NNNLO( $y_b^2$ )	NNNNLO( $y_b^2$ )
$\overline{\text{MS}}$	$1.891^{+0.241}_{-0.192}$	$2.285^{+0.105}_{-0.110}$	$2.359^{+0.020}_{-0.041}$	$2.376^{+0.026}_{-0.046}$	$2.379^{+0.005}_{-0.015}$	$2.377^{+0.006}_{-0.006}$
on-shell	6.269	$4.092^{+0.197}_{-0.242}$	$3.138^{+0.191}_{-0.210}$	$3.193^{+0.181}_{-0.197}$	$2.804^{+0.112}_{-0.096}$	$2.649^{+0.065}_{-0.049}$

Larin et al, hep-ph/9506465

Chetyrkin hep-ph/9608318,

Baikov et al, hep-ph/0511063,

Herzog et al, 1707.01044

The results in  $\overline{\text{MS}}$  scheme become stable quickly.

Scale unc.  $\sim 0.3\%$ .

In onshell scheme,  $N3\text{LO}/N2\text{LO}=0.88$ ,  $N4\text{LO}/N3\text{LO}=0.95$ .

Scale unc.  $\sim 2\%$ .

$$\mathcal{L}_{\text{eff}} = -\frac{H}{v} (C_1 \mathcal{O}_1^R + C_2 \mathcal{O}_2^R) + \mathcal{L}_{\text{QCD}}$$

$$\mathcal{O}_1 = (G_{a,\mu\nu}^0)^2, \quad \mathcal{O}_2 = m_b^0 \bar{b}^0 b^0$$

$$C_1 = -\left(\frac{\alpha_s}{\pi}\right) \frac{1}{12} - \left(\frac{\alpha_s}{\pi}\right)^2 \frac{11}{48} - \left(\frac{\alpha_s}{\pi}\right)^3 \left[ \frac{2777}{3456} + \frac{19}{192} L_t - n_f \left( \frac{67}{1152} - \frac{1}{36} L_t \right) \right] + \mathcal{O}(\alpha_s^4),$$

$$C_2 = 1 + \left(\frac{\alpha_s}{\pi}\right)^2 \left[ \frac{5}{18} - \frac{1}{3} L_t \right] + \left(\frac{\alpha_s}{\pi}\right)^3 \left[ -\frac{841}{1296} + \frac{5}{3} \zeta(3) - \frac{79}{36} L_t - \frac{11}{12} L_t^2 + n_f \left( \frac{53}{216} + \frac{1}{18} L_t^2 \right) \right] + \mathcal{O}(\alpha_s^4),$$

The relative error of using this EFT is below 1%.

The correction to the total decay width is below 0.01%.

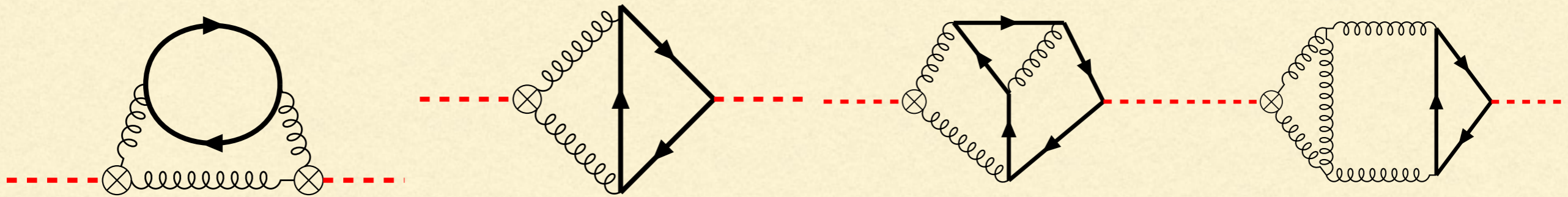


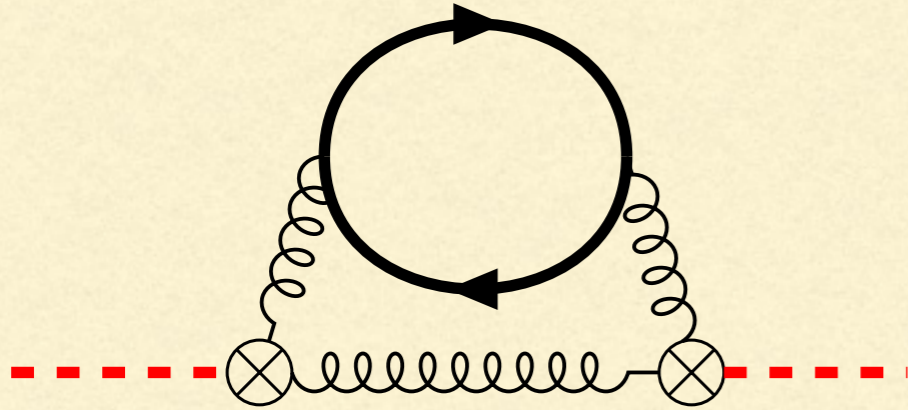
$$\Gamma_{H \rightarrow b\bar{b}} = \Gamma_{H \rightarrow b\bar{b}}^{C_2 C_2} + \Gamma_{H \rightarrow b\bar{b}}^{C_1 C_2} + \Gamma_{H \rightarrow b\bar{b}}^{C_1 C_1}$$

$$\Gamma_{H \rightarrow b\bar{b}}^{C_2 C_2} = C_2 C_2 \left[ \Delta_{0, b\bar{b}}^{C_2 C_2} + \left(\frac{\alpha_s}{\pi}\right) \Delta_{1, b\bar{b}}^{C_2 C_2} + \left(\frac{\alpha_s}{\pi}\right)^2 \Delta_{2, b\bar{b}}^{C_2 C_2} + \left(\frac{\alpha_s}{\pi}\right)^3 \Delta_{3, b\bar{b}}^{C_2 C_2} + \mathcal{O}(\alpha_s^4) \right]$$

$$\Gamma_{H \rightarrow b\bar{b}}^{C_1 C_2} = C_1 C_2 \left[ \left(\frac{\alpha_s}{\pi}\right) \Delta_{1, b\bar{b}}^{C_1 C_2} + \left(\frac{\alpha_s}{\pi}\right)^2 \Delta_{2, b\bar{b}}^{C_1 C_2} + \mathcal{O}(\alpha_s^3) \right],$$

$$\Gamma_{H \rightarrow b\bar{b}}^{C_1 C_1} = C_1 C_1 \left[ \left(\frac{\alpha_s}{\pi}\right) \Delta_{1, b\bar{b}}^{C_1 C_1} + \mathcal{O}(\alpha_s^2) \right],$$



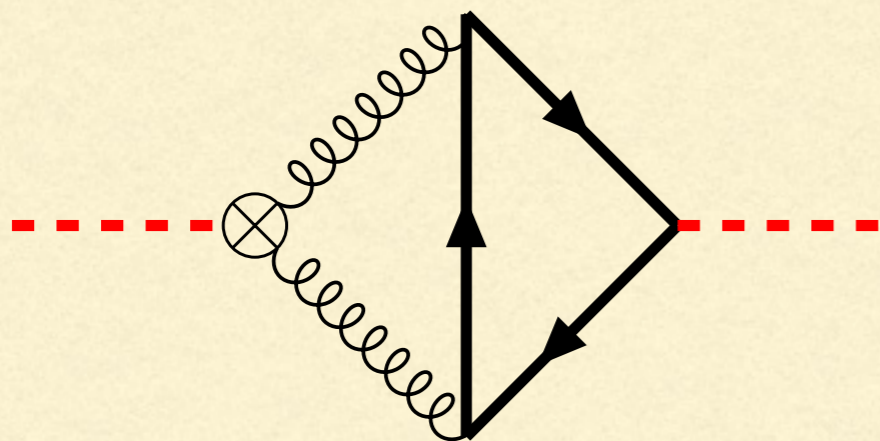


$$\Delta_{1,b\bar{b}}^{C_1 C_1} \Big|_{z \rightarrow \infty} = \frac{m_H^3}{\pi v^2} C_A C_F \left[ \frac{1}{6} \log(z) - \frac{7}{12} + \frac{3}{z} \right] + \mathcal{O}(z^{-2})$$

It is power enhanced and divergent in  $m_b \rightarrow 0$  limit.

The extraction of  $y_b$  is highly non-trivial after considering such contributions.





$$\Delta_{1,b\bar{b}}^{C_1 C_2} |_{z \rightarrow \infty} = \frac{m_H m_b \bar{m}_b(\mu)}{\pi v^2} C_A C_F \left[ -\frac{1}{8} \log^2(z) - \frac{3}{4} \log\left(\frac{\mu^2}{m_H^2}\right) + \frac{\pi^2}{8} - \frac{19}{8} \right. \\ \left. + \frac{1}{2} \frac{\log^2(z)}{z} + 2 \frac{\log(z)}{z} + \frac{9}{2z} \log\left(\frac{\mu^2}{m_H^2}\right) - \frac{\pi^2}{2z} + \frac{15}{2z} \right] + \mathcal{O}(z^{-2}),$$

The double logarithm dominates.

It is induced by soft massive quarks, different from traditional Sudakov double logarithms.

$$-\frac{m_H m_b \bar{m}_b(\mu)}{8\pi v^2} C_A C_F \log^2(z) \times \frac{1}{24} (C_A - C_F) \log^2(z)$$

$$\begin{aligned}
\Gamma_{H \rightarrow b\bar{b}} = & \frac{3m_H \bar{m}_b^2}{8v^2\pi} \left\{ 1 + \left(\frac{\alpha_s}{\pi}\right) \frac{17}{3} \right. \\
& + \left(\frac{\alpha_s}{\pi}\right)^2 \left[ \frac{1}{9} \log^2(\bar{z}) - \frac{2}{3} \log(x) - \frac{97\zeta(3)}{6} - \frac{17\pi^2}{12} + \frac{9235}{144} \right] \\
& + \left(\frac{\alpha_s}{\pi}\right)^3 \left[ \frac{5}{648} \log^4(\bar{z}) + \frac{59}{324} \log^3(\bar{z}) - \frac{31\pi^2}{324} \log^2(\bar{z}) + \frac{989}{648} \log^2(\bar{z}) \right. \\
& + \frac{32\zeta(3)}{27} \log(\bar{z}) - \frac{41\pi^2}{324} \log(\bar{z}) + \frac{137}{216} \log(\bar{z}) - \frac{23}{18} \log^2(x) - \frac{49}{6} \log(x) \\
& \left. + \frac{1945\zeta(5)}{36} - \frac{13\pi^4}{3240} - \frac{81239\zeta(3)}{216} - \frac{81239\zeta(3)}{216} - \frac{22291\pi^2}{648} + \frac{37434709}{46656} \right] \left. \right\} \\
& + \frac{m_H^3}{v^2\pi} \left(\frac{\alpha_s}{\pi}\right)^3 \left[ \frac{\log(\bar{z})}{216} - \frac{7}{432} \right] + \mathcal{O}(\bar{z}^{-1}) + \mathcal{O}(x) + \mathcal{O}(\alpha_s^4)
\end{aligned}$$



	[MeV]	$\mu = \frac{1}{2}m_H$	$\mu = m_H$	$\mu = 2m_H$
$\mathcal{O}(\alpha_s^0)$	$\Gamma_{Hb\bar{b}}^{C_2C_2}$	2.1314	1.8905	1.6985
$\mathcal{O}(\alpha_s^1)$	$\Gamma_{Hb\bar{b}}^{C_2C_2}$	0.25813	0.39409	0.47563
$\mathcal{O}(\alpha_s^2)$	$\Gamma_{Hb\bar{b}}^{C_2C_2}$	-0.0043084	0.076819	0.143670
	$\Gamma_{Hb\bar{b}}^{C_1C_2}$	0.027078	0.024746	0.022608
$\mathcal{O}(\alpha_s^3)$	$\Gamma_{Hb\bar{b}}^{C_2C_2}$	-0.015360	0.0048336	0.038198
	$\Gamma_{Hb\bar{b}}^{C_1C_2}$	0.010314	0.013585	0.015170
	$\Gamma_{Hb\bar{b}}^{C_1C_1}$	0.0088676	0.0064617	0.0048595

MS scheme

NLO/LO=20%

NNLO/NLO=4%

1% correction!

For C1C2, NNLO/NLO=55%

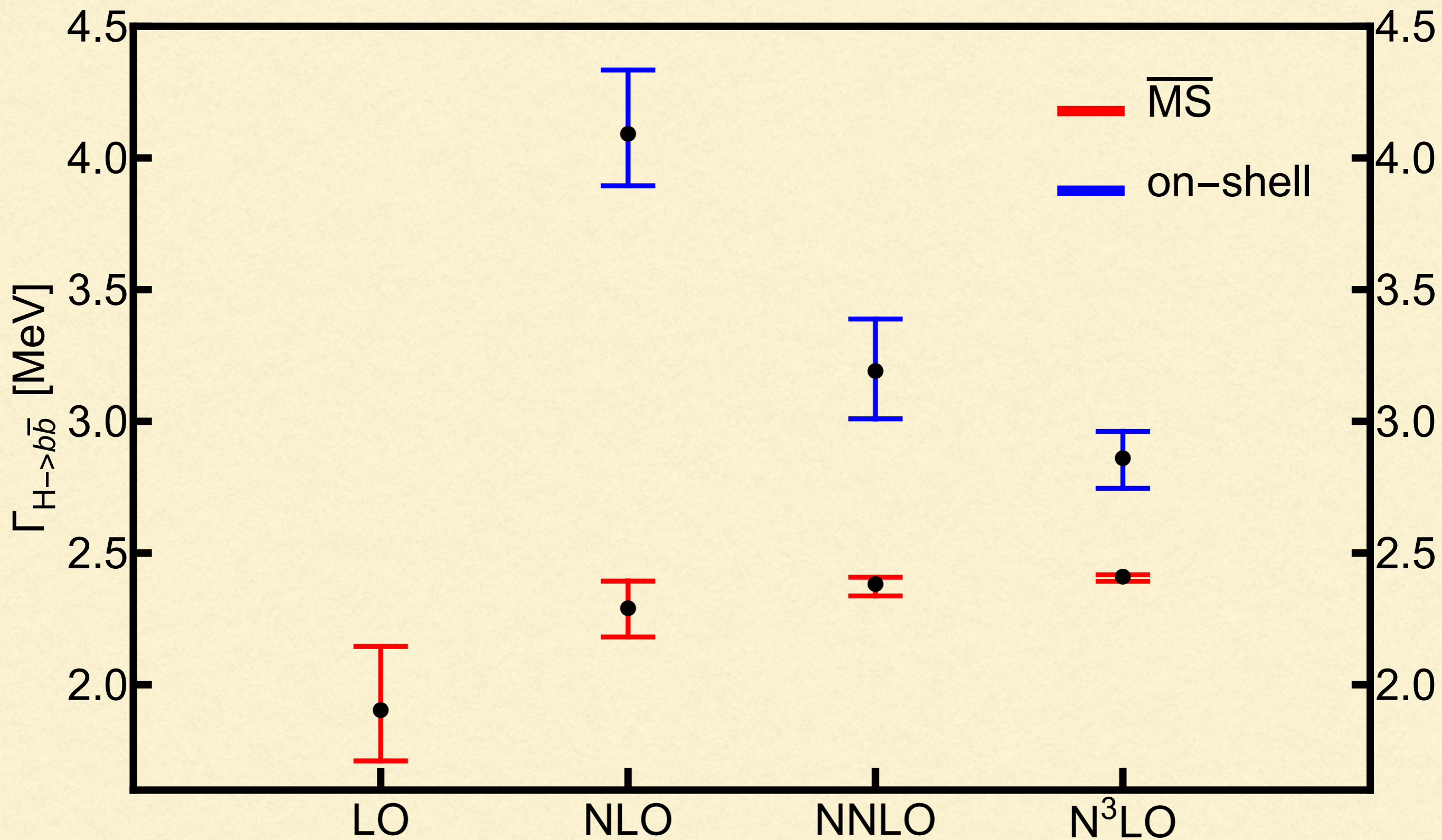
Fortunately, the C1C1 contribution is not large.

	[MeV]	$\mu = \frac{1}{2}m_H$	$\mu = m_H$	$\mu = 2m_H$
$\Gamma_{H \rightarrow b\bar{b}} (\overline{\text{MS}})$	$\mathcal{O}(\alpha_s^0)$	2.1454	1.9036	1.7108
	$\mathcal{O}(\alpha_s^1)$	0.24806	0.38682	0.47051
	$\mathcal{O}(\alpha_s^2)$	0.014742	0.091773	0.15580
	$\mathcal{O}(\alpha_s^3)$	0.0092203	0.028117	0.055816
$\Gamma_{H \rightarrow b\bar{b}} (\text{OS})$	$\mathcal{O}(\alpha_s^0)$	6.2687	6.2687	6.2687
	$\mathcal{O}(\alpha_s^1)$	-2.4192	-2.1770	-1.9797
	$\mathcal{O}(\alpha_s^2)$	-0.85590	-0.90061	-0.91641
	$\mathcal{O}(\alpha_s^3)$	-0.23550	-0.33107	-0.39831

$$\Gamma_{H \rightarrow b\bar{b}}^{\text{N}^3\text{LO QCD}} (\overline{\text{MS}}) = 2.410_{-0.017}^{+0.007} \text{ MeV}$$

$$\Gamma_{H \rightarrow b\bar{b}}^{\text{N}^3\text{LO QCD+NLO EW}} (\overline{\text{MS}}) = 2.382_{-0.017}^{+0.007} \text{ MeV}$$





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# HIGGS DECAYS TO GLUONS

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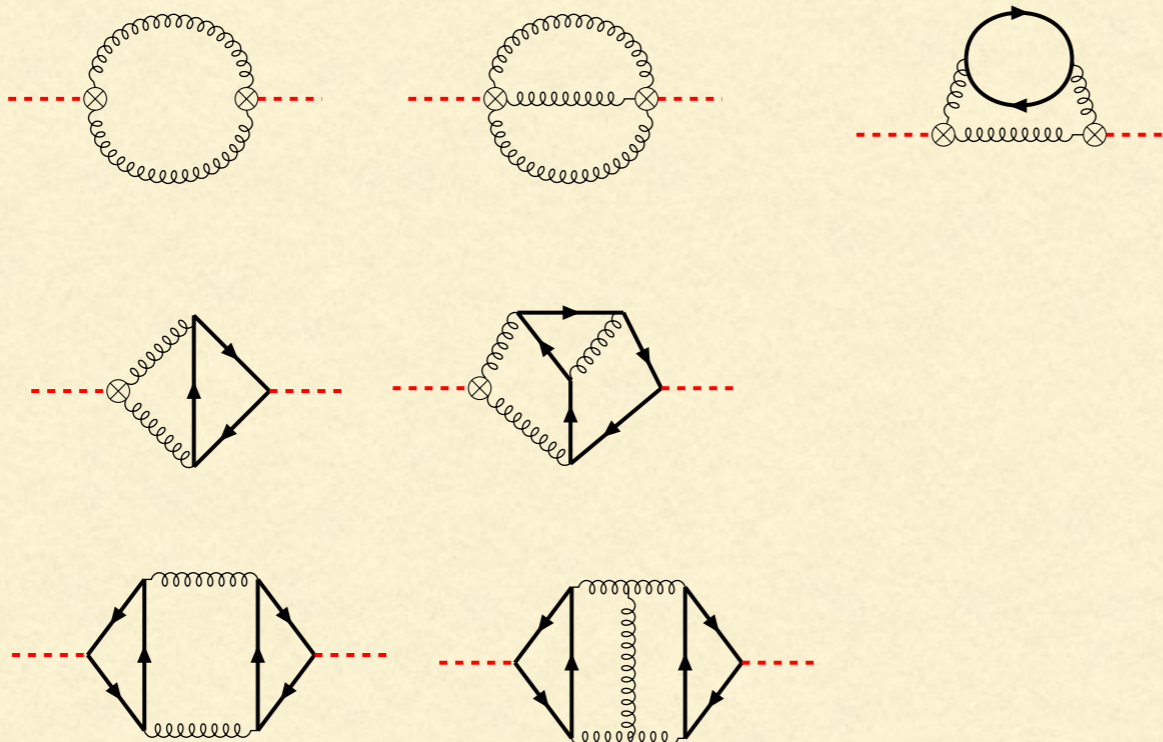


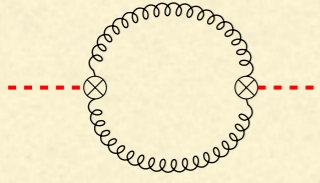
$$\Gamma_{H \rightarrow gg} = \Gamma_{H \rightarrow gg}^{C_1 C_1} + \Gamma_{H \rightarrow gg}^{C_1 C_2} + \Gamma_{H \rightarrow gg}^{C_2 C_2}$$

$$\Gamma_{H \rightarrow gg}^{C_1 C_1} = C_1 C_1 \left[ \Delta_{0,gg}^{C_1 C_1} + \left( \frac{\alpha_s}{\pi} \right) \Delta_{1,gg}^{C_1 C_1} + \mathcal{O}(\alpha_s^2) \right],$$

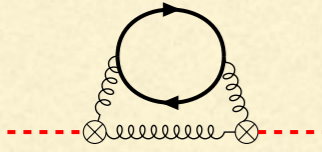
$$\Gamma_{H \rightarrow gg}^{C_1 C_2} = C_1 C_2 \left[ \left( \frac{\alpha_s}{\pi} \right) \Delta_{1,gg}^{C_1 C_2} + \left( \frac{\alpha_s}{\pi} \right)^2 \Delta_{2,gg}^{C_1 C_2} + \mathcal{O}(\alpha_s^3) \right],$$

$$\Gamma_{H \rightarrow gg}^{C_2 C_2} = C_2 C_2 \left[ \left( \frac{\alpha_s}{\pi} \right)^2 \Delta_{2,gg}^{C_2 C_2} + \left( \frac{\alpha_s}{\pi} \right)^3 \Delta_{3,gg}^{C_2 C_2} + \mathcal{O}(\alpha_s^4) \right],$$

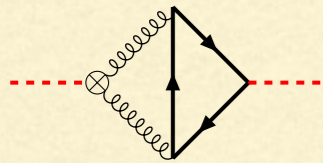
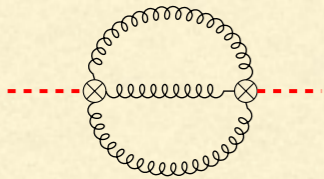




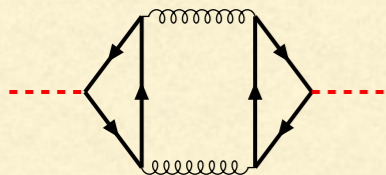
$$\Delta_{0,gg}^{C_1 C_1} = \frac{C_A C_F m_H^3}{2\pi v^2}$$



$$\Delta_{1,gg}^{C_1 C_1} = \frac{m_H^3}{\pi v^2} C_A C_F \left( \left[ -\frac{1}{6} \log(z) - \frac{1}{6} \log\left(\frac{\mu^2}{m_H^2}\right) \right] \right. \\ \left. + C_A \left[ \frac{11}{12} \log\left(\frac{\mu^2}{m_H^2}\right) + \frac{73}{24} \right] + n_l \left[ -\frac{1}{6} \log\left(\frac{\mu^2}{m_H^2}\right) - \frac{7}{12} \right] \right)$$



$$\Delta_{1,gg}^{C_1 C_2} \Big|_{z \rightarrow \infty} = \frac{m_H m_b \bar{m}_b}{\pi v^2} C_A C_F \times \\ \left[ \frac{1}{8} \log^2(z) - \frac{\pi^2}{8} - \frac{1}{2} - \frac{1}{2} \frac{\log^2(z)}{z} - \frac{1}{2} \frac{\log(z)}{z} + \frac{\pi^2}{2z} + \mathcal{O}(z^{-2}) \right]$$



$$\Delta_{2,gg}^{C_2 C_2} \Big|_{z \rightarrow \infty} = \frac{m_b^2 \bar{m}_b^2}{\pi v^2 m_H} C_A \times \\ \left[ \frac{(\log^2(z) - 4 \log(z) + \pi^2 + 4) (\log^2(z) + 4 \log(z) + \pi^2 + 4)}{96} + \mathcal{O}(z^{-1}) \right]$$



$$\begin{aligned}
\Gamma_{H \rightarrow gg} = & \frac{m_H^3}{v^2 \pi} \left\{ \left( \frac{\alpha_s}{\pi} \right)^2 \frac{1}{72} + \left( \frac{\alpha_s}{\pi} \right)^3 \left[ -\frac{1}{216} \log(\bar{z}) + \frac{229}{864} \right] \right\} \\
& + \frac{m_H \bar{m}_b^2}{v^2 \pi} \left\{ \left( \frac{\alpha_s}{\pi} \right)^2 \left[ -\frac{1}{24} \log^2(\bar{z}) + \frac{\pi^2}{24} + \frac{1}{6} \right] \right. \\
& + \left( \frac{\alpha_s}{\pi} \right)^3 \left[ -\frac{5}{1728} \log^4(\bar{z}) - \frac{59}{864} \log^3(\bar{z}) + \frac{31\pi^2}{864} \log^2(\bar{z}) - \frac{989}{1728} \log^2(\bar{z}) \right. \\
& - \frac{4\zeta(3)}{9} \log(\bar{z}) + \frac{41\pi^2}{864} \log(\bar{z}) - \frac{137}{576} \log(\bar{z}) - \frac{137\pi^4}{8640} - \frac{29\zeta(3)}{36} \\
& \left. \left. + \frac{1277\pi^2}{1728} + \frac{17275}{3456} \right] + \mathcal{O}(\bar{z}^{-1}) \right\}
\end{aligned}$$

$$\begin{aligned}
\Gamma_{H \rightarrow \text{hadrons}} = & \frac{m_H^3}{v^2 \pi} \left\{ \left( \frac{\alpha_s}{\pi} \right)^2 \frac{1}{72} + \left( \frac{\alpha_s}{\pi} \right)^3 \frac{215}{864} + \mathcal{O}(\bar{z}^{-1}) \right\} \\
& + \frac{3m_H \bar{m}_b^2}{8v^2 \pi} \left\{ 1 + \left( \frac{\alpha_s}{\pi} \right) \frac{17}{3} + \left( \frac{\alpha_s}{\pi} \right)^2 \left[ -\frac{2}{3} \log(x) - \frac{97\zeta(3)}{6} - \frac{47\pi^2}{36} + \frac{9299}{144} \right] \right. \\
& + \left( \frac{\alpha_s}{\pi} \right)^3 \left[ -\frac{23}{18} \log^2(x) - \frac{49}{6} \log(x) + \frac{1945\zeta(5)}{36} - \frac{5\pi^4}{108} - \frac{81703\zeta(3)}{216} \right. \\
& \left. \left. - \frac{10507\pi^2}{324} + \frac{38056609}{46656} \right] + \mathcal{O}(\bar{z}^{-1}) \right\}
\end{aligned}$$

Agree with Davies et al, 1703.02988

		on-shell scheme			$\overline{\text{MS}}$ scheme		
[MeV]		$\mu = \frac{m_H}{2}$	$\mu = m_H$	$\mu = 2m_H$	$\mu = \frac{m_H}{2}$	$\mu = m_H$	$\mu = 2m_H$
$\mathcal{O}(\alpha_s^2)$	$\Gamma_{H \rightarrow gg}^{C_2 C_2}$	0.003208	0.002598	0.002148	0.0006336	0.0004269	0.0002994
	$\Gamma_{H \rightarrow gg}^{C_1 C_2}$	-0.03018	-0.02444	-0.02021	-0.01601	-0.01200	-0.00925
	$\Gamma_{H \rightarrow gg}^{C_1 C_1}$	0.2269	0.1837	0.1520	0.2269	0.1837	0.1520
$\mathcal{O}(\alpha_s^3)$	$\Gamma_{H \rightarrow gg}^{C_2 C_2}$	-	-	-	-	-	-
	$\Gamma_{H \rightarrow gg}^{C_1 C_2}$	-0.009250	-0.01140	-0.01208	-0.01088	-0.01054	-0.009632
	$\Gamma_{H \rightarrow gg}^{C_1 C_1}$	0.1052	0.1117	0.1104	0.1019	0.1091	0.1082

The C1C1 contributions are dominant.

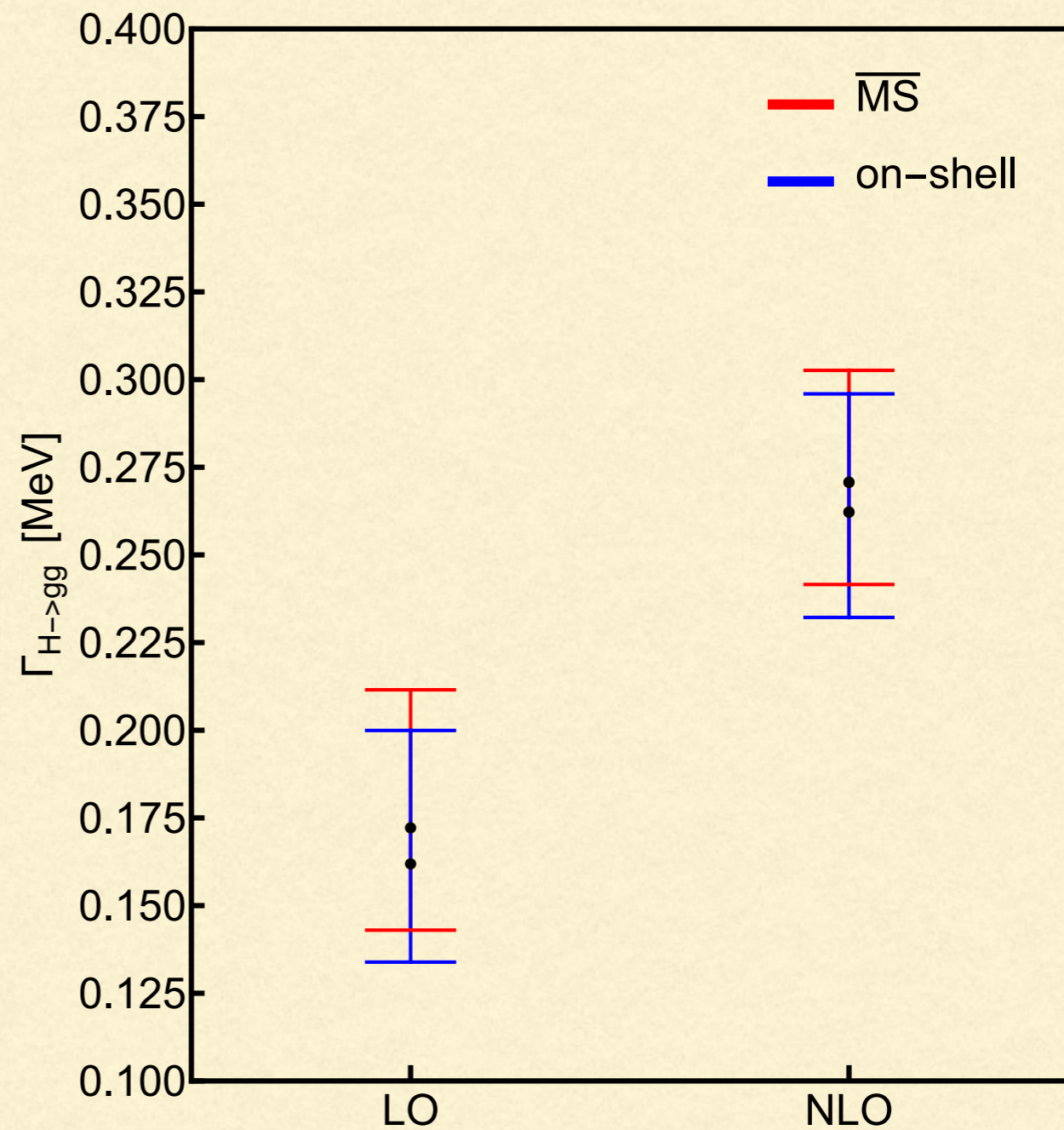
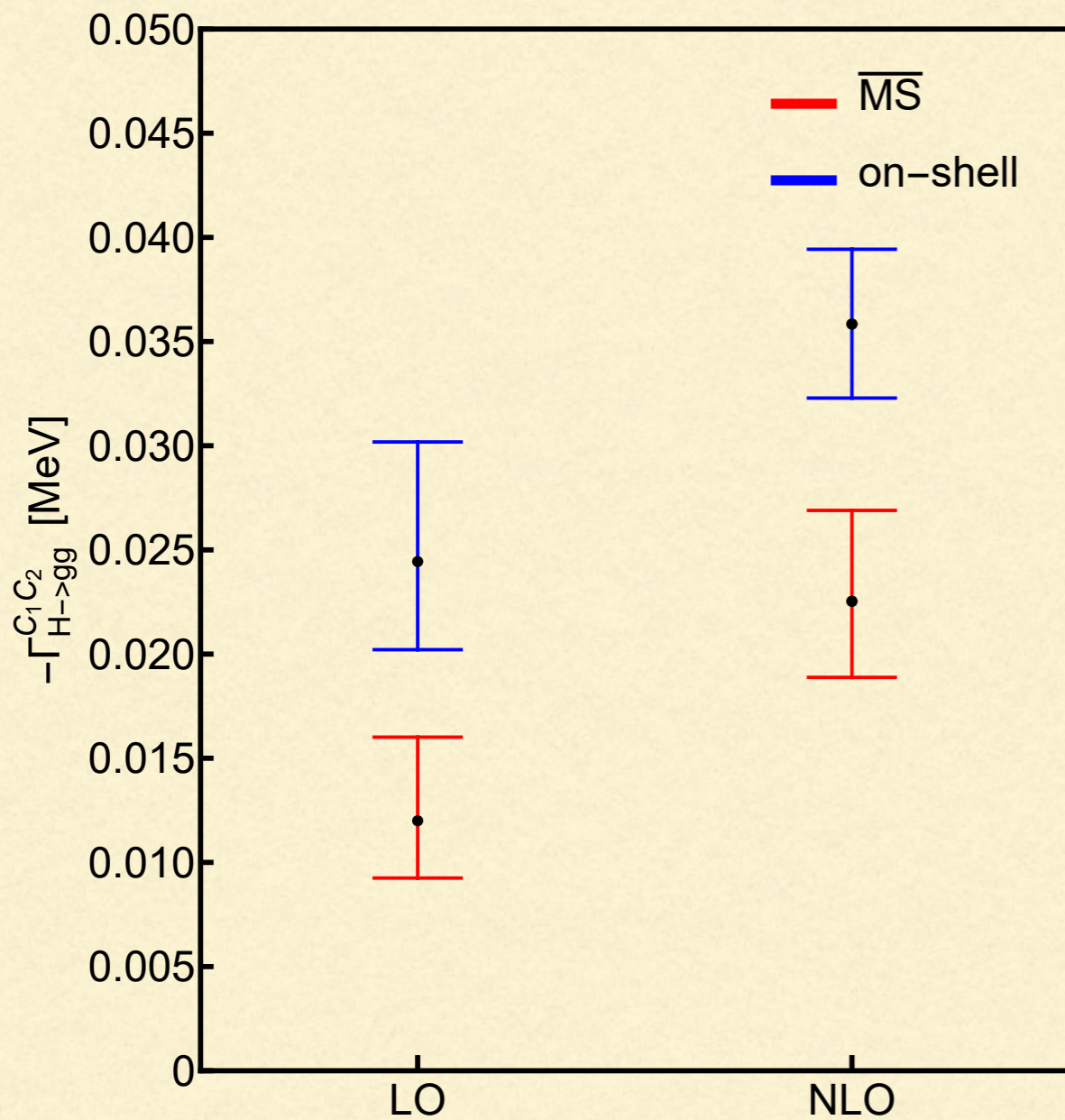
The C1C2 contributions are 13%, much larger than  $m_b^2/m_H^2$ .

The C2C2 contributions are only 1%.

The QCD correction in C1C1 is 61%.

The QCD correction in C1C2 is 47% (88%) in onshell (MS) scheme.





$$\Gamma_{H \rightarrow gg}^{\text{NLO}} (\text{on-shell}) = 0.278^{+0.038}_{-0.033} \text{ MeV}$$

$$\Gamma_{H \rightarrow gg}^{\text{NLO}} (\overline{\text{MS}}) = 0.289^{+0.034}_{-0.031} \text{ MeV}$$



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# CONCLUSIONS

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- Higgs decays to  $b\bar{b}$  and  $gg$  can be measured with an accuracy better than 1%.
  - Theoretical predictions are investigated with full dependence on the bottom quark mass.
  - Large corrections are found due to the logarithms  $\log(m_H^2/m_b^2)$ .
  - Extraction of the bottom quark Yukawa coupling is nontrivial after considering higher order corrections.
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**Thanks a lot for your attention!**

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