

# Long lived Particle of Higgs sector

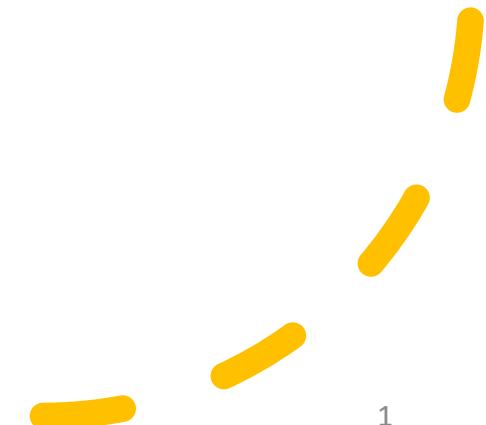
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2507.XXXX (XY Qi, HY Song, WS)



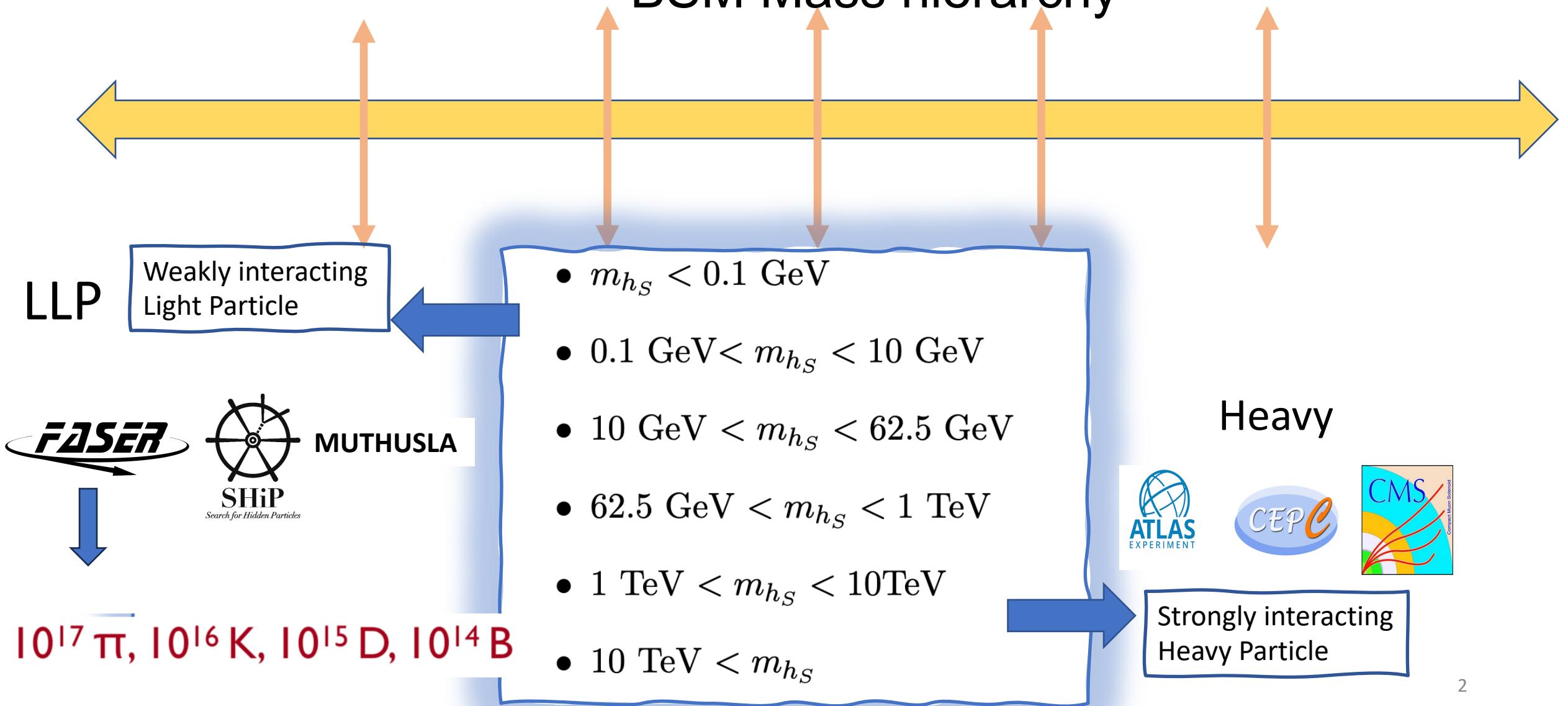
# outline

- Motivation: LLP and FASER
- 2HDM: complete Type-I study
- Study method: EFT and BMs
- Conclusion



# Motivation: LLP

## BSM Mass hierarchy



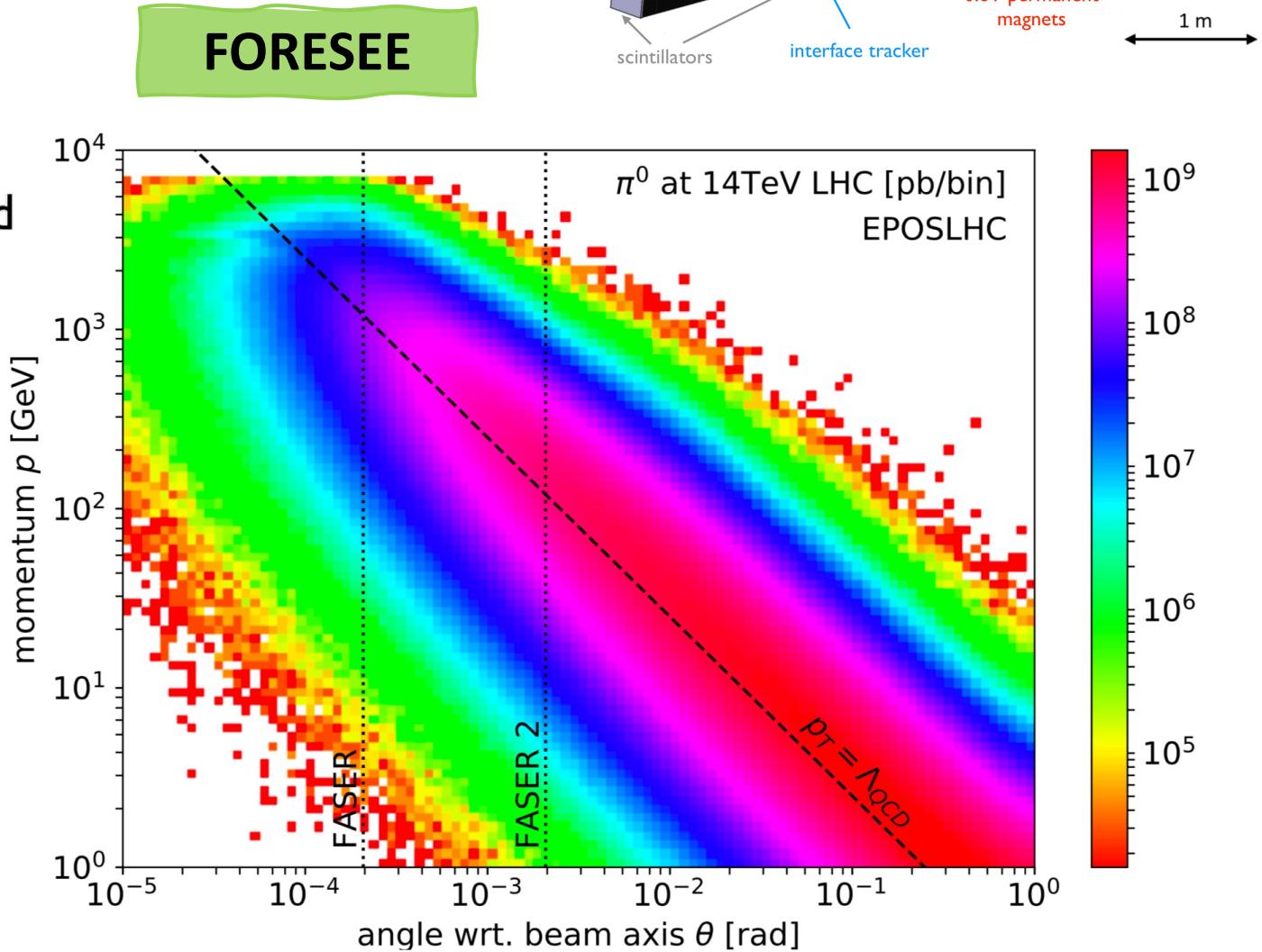
# Production

## Pion

boosted mesons highly collimated  
 $p \cdot \theta = p_T \sim \Lambda_{QCD}$

$$N_\pi = 10^{18} \text{ at } 3000 \text{ fb}^{-1}$$

FASER: radius R = 10 cm,  
length D = 1.5 m,  
FASER 2: radius R = 1m,  
length D = 5 m.



# Case study: 2HDM

- Two Higgs Doublet Model

$$\Phi_i = \begin{pmatrix} \phi_i^+ \\ (v_i + \phi_i^0 + iG_i)/\sqrt{2} \end{pmatrix}$$

$$v_u^2 + v_d^2 = v^2 = (246\text{GeV})^2$$

$$\tan \beta = v_u/v_d$$

$$\begin{pmatrix} H^0 \\ h^0 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \phi_1^0 \\ \phi_2^0 \end{pmatrix}, \quad A = -G_1 \sin \beta + G_2 \cos \beta$$

$$H^\pm = -\phi_1^\pm \sin \beta + \phi_2^\pm \cos \beta$$

	$\Phi_1$	$\Phi_2$
Type I	$u,d,l$	
Type II	$u$	$d,l$
lepton-specific	$u,d$	$l$
flipped	$u,l$	$d$

- Parameters (CP-conserving, Flavor Limit,  $Z_2$  Symmetry)

$$m_{11}^2, m_{22}^2, \lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5$$

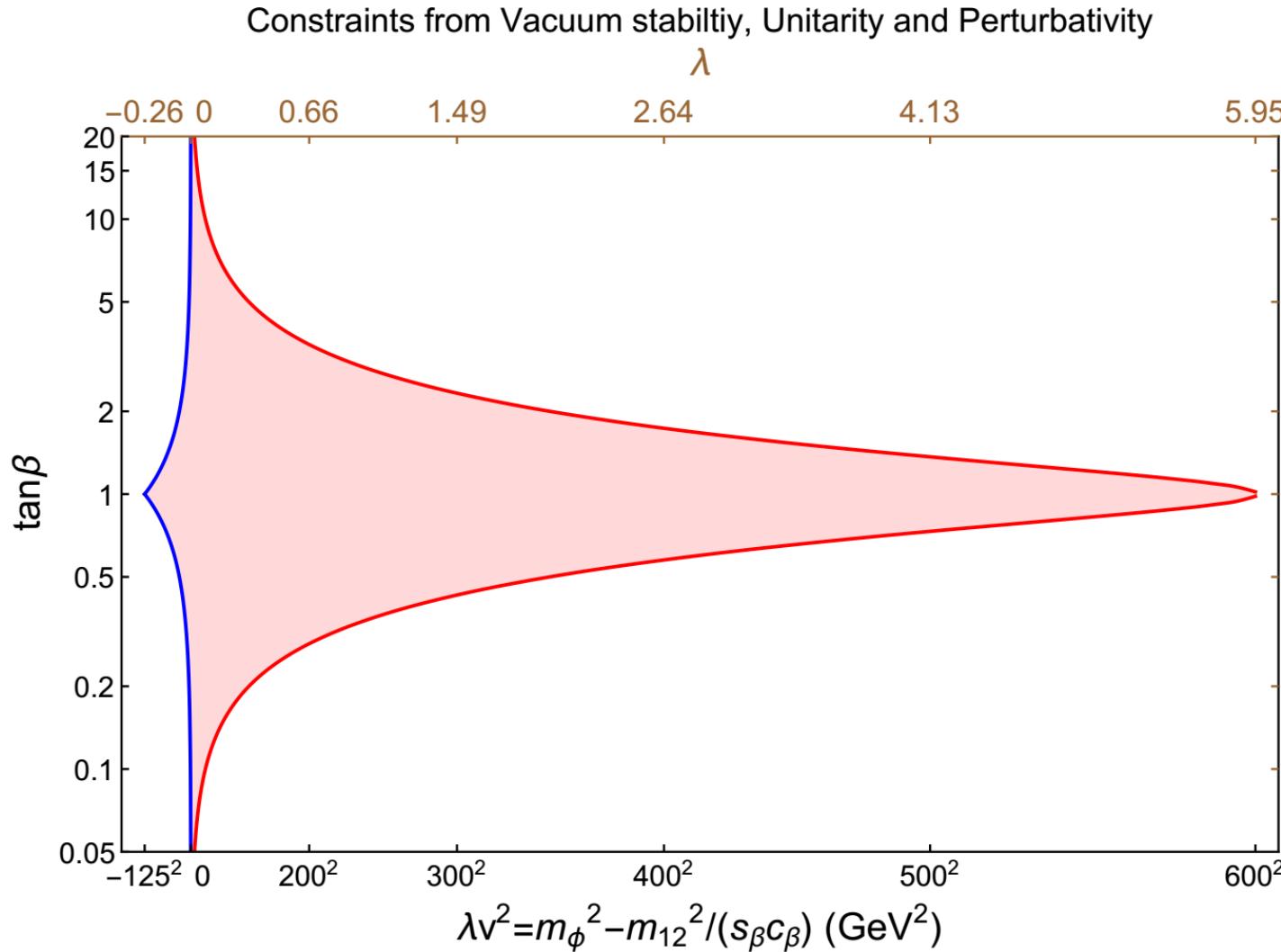


$$v, \tan \beta, \alpha, m_h, m_H, m_A, m_{H^\pm}$$

Soft  $Z_2$  symmetry breaking:  $m_{12}^2$

246 GeV      125. GeV      light

# Constraint



$$\cos(\beta - \alpha) = 0,$$
$$m_\Phi \equiv m_H = m_A = m_{H^\pm}$$

Theoretical constraints

$$\lambda v^2 \equiv m_\Phi^2 - m_{12}^2 / s_\beta c_\beta$$

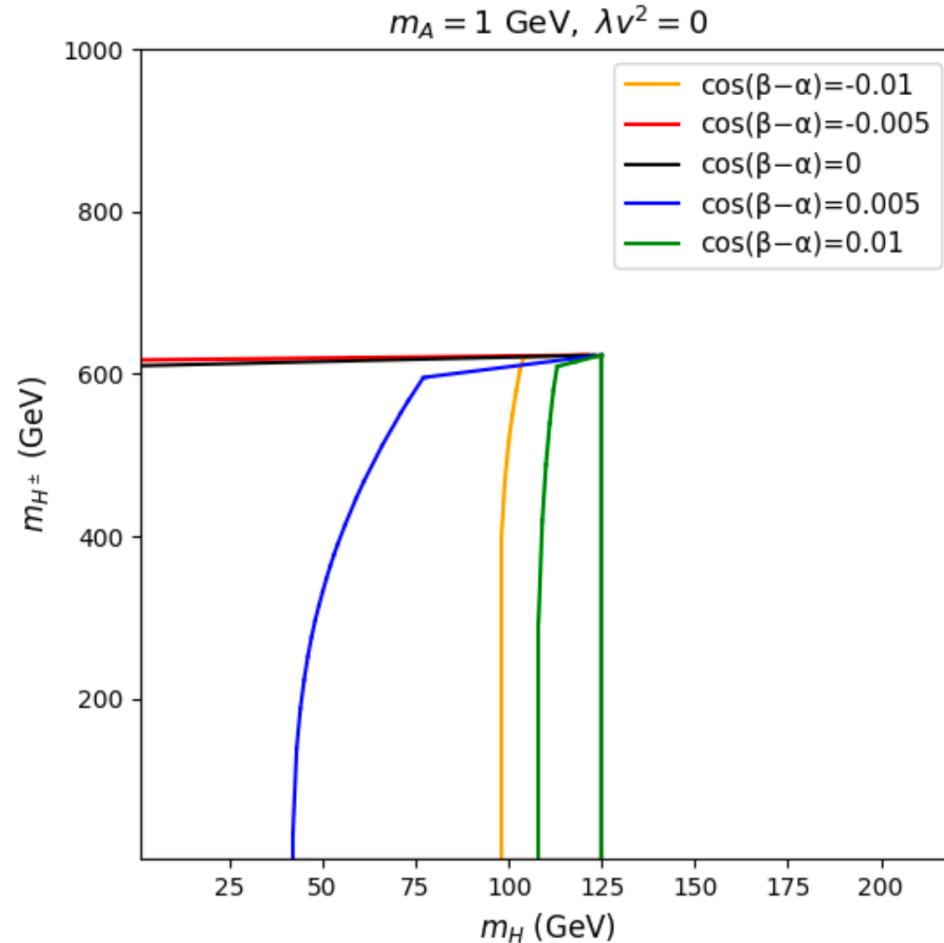
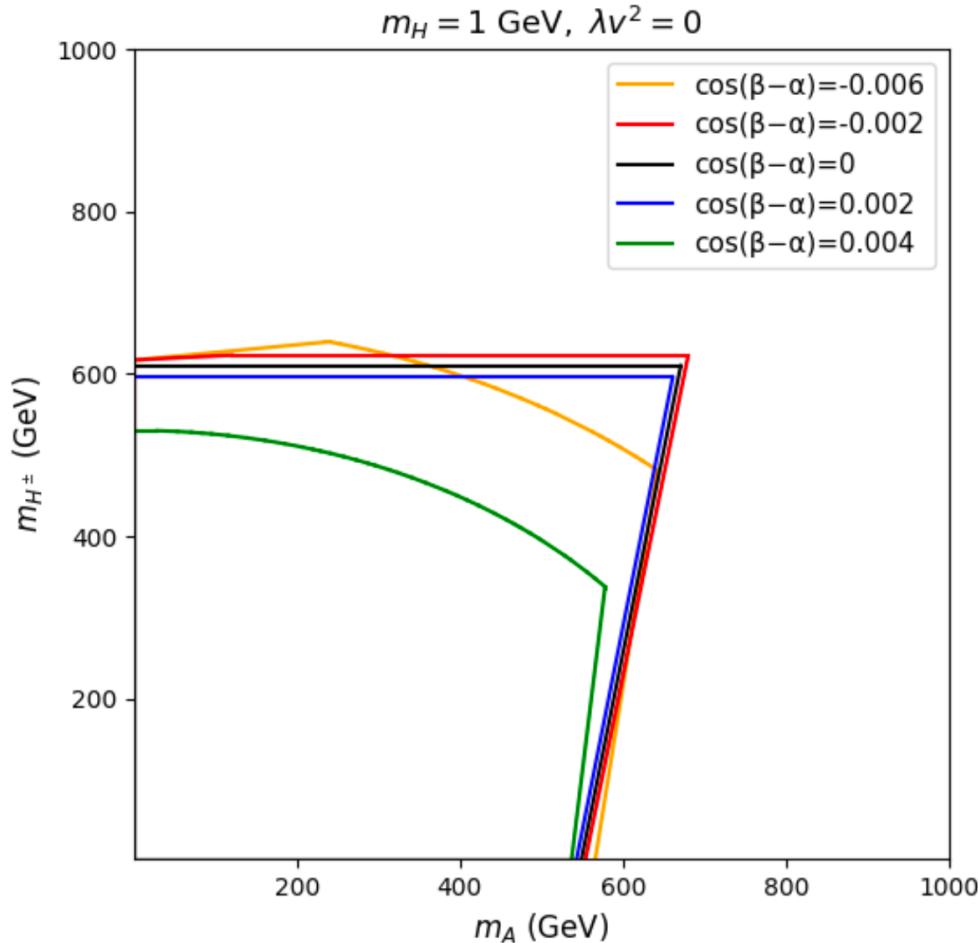
$$-125^2 \text{ GeV}^2 < \lambda v^2 < 600^2 \text{ GeV}^2$$

$$\lambda \in (-0.26, 5.95)$$
$$\lambda_4 = \lambda_5 = \lambda_3 - 0.258 = -\lambda$$

# Constraint

Theoretical constraints

$$\lambda v^2 \equiv m_H^2 - m_{12}^2 / s_\beta c_\beta = 0$$

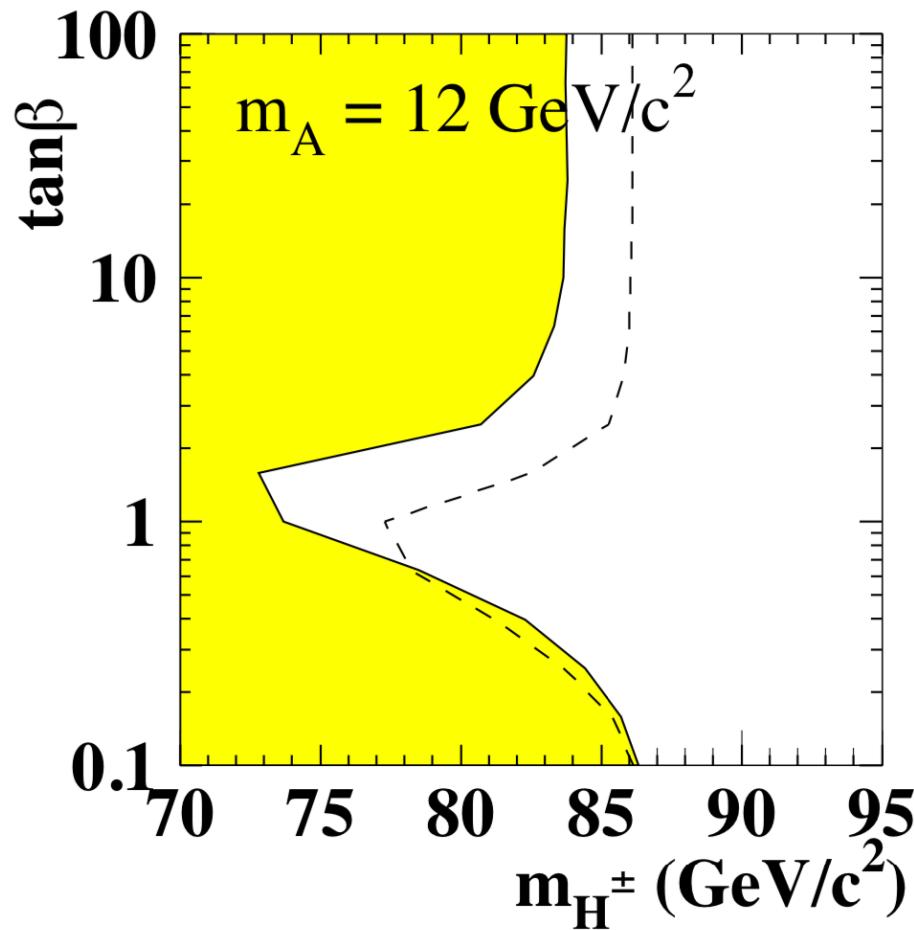


$$m_H \sim 0 : m_{A/H^\pm} \lesssim 600 \text{ GeV}$$

$$m_A \sim 0 : m_{H^\pm} \lesssim 600 \text{ GeV}, \quad m_H \lesssim m_h$$

# Constraint

Direct search at LEP



arXiv: 1301.6065

$$m_H \sim 0 : \quad m_A \sim m_{H^\pm} \lesssim 600 \text{ GeV}$$

$$m_A \sim 0 : \quad m_{H^\pm} \sim m_H \lesssim m_h$$

$$m_A \sim 10 \text{ GeV} : \quad 72 \text{ GeV} \lesssim m_{H^\pm} \sim m_H \lesssim 116 \text{ GeV}$$

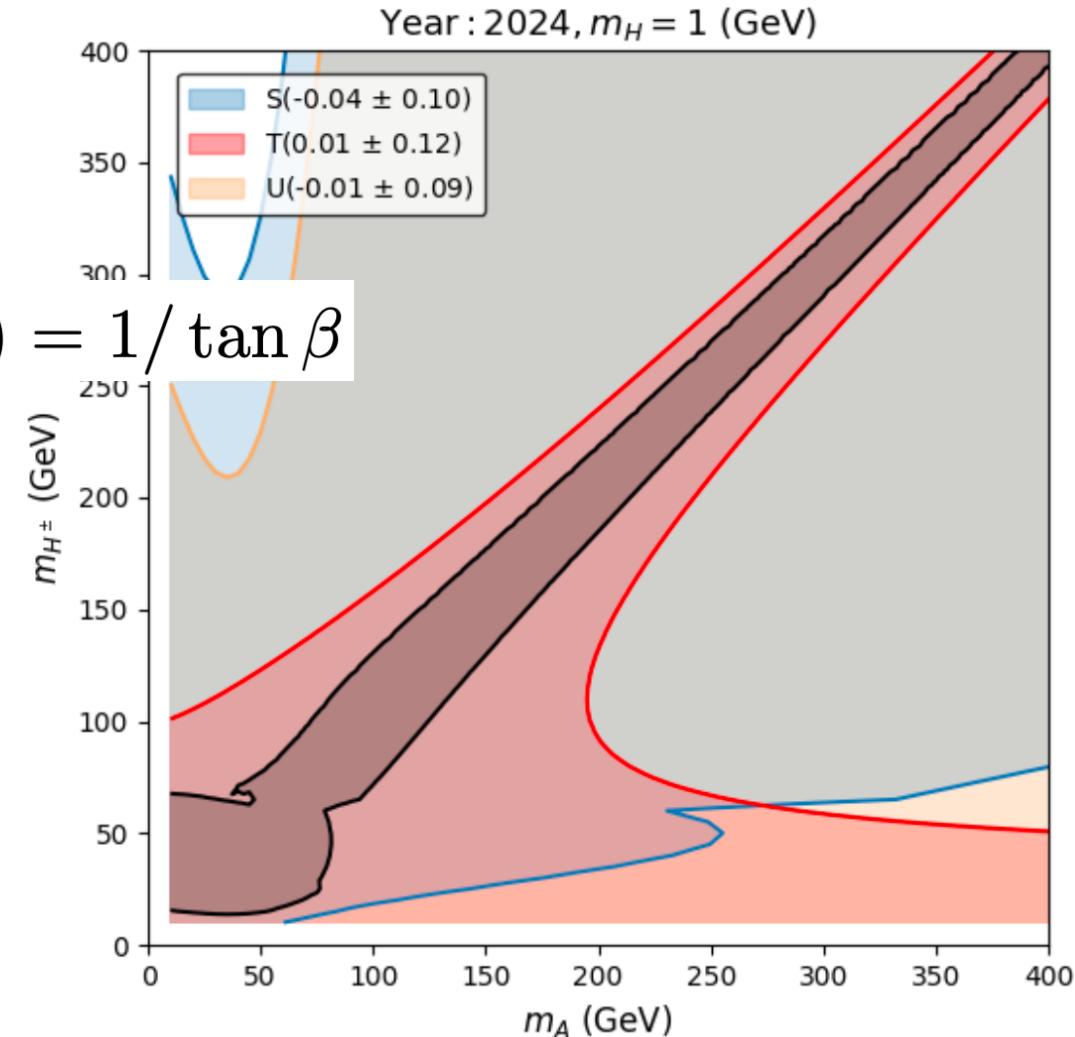
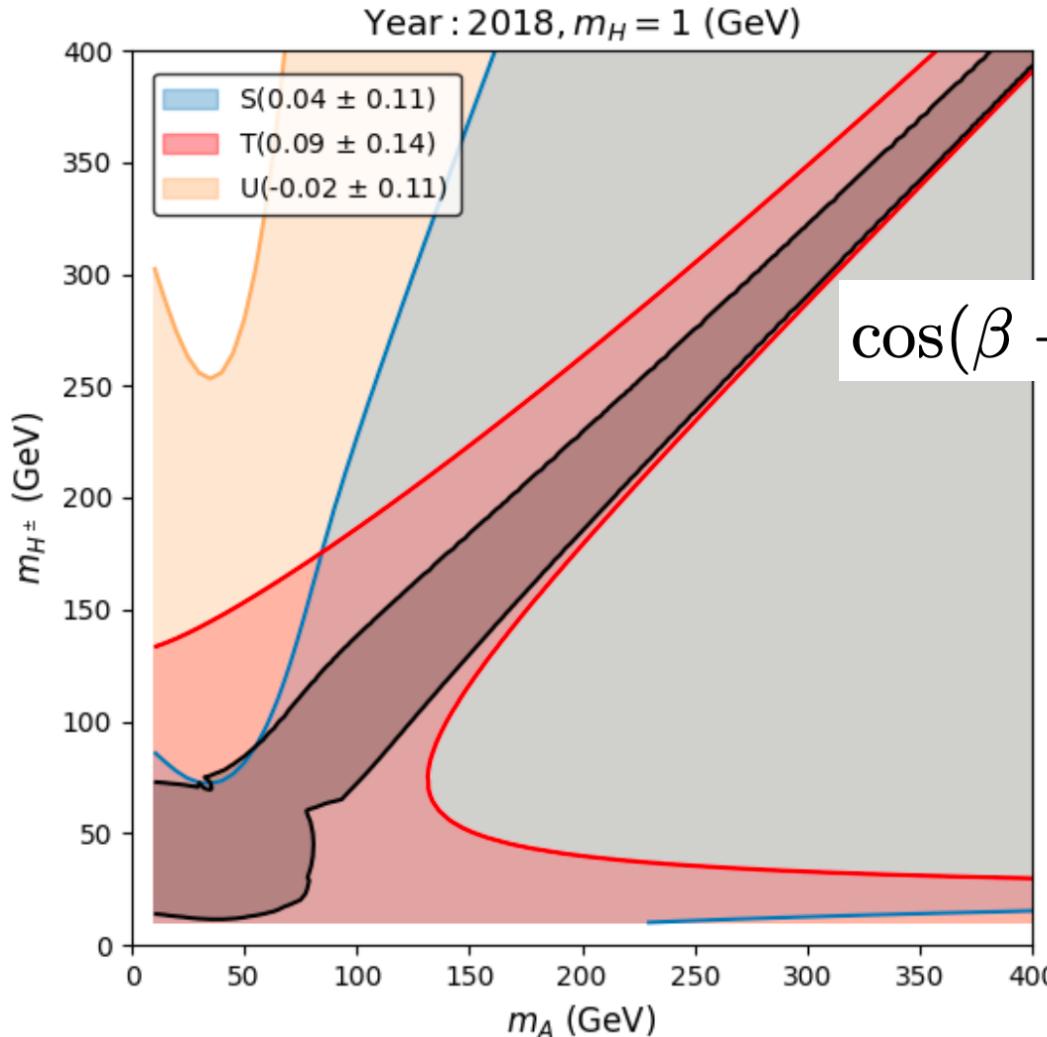
# Constraint

## Oblique constraints: Z pole

	2018 [96]			2024 [99]				
$\sigma$	correlation			$\sigma$	correlation			
	$S$	$T$	$U$		$S$	$T$	$U$	
$S$	$0.04 \pm 0.11$	1	$0.92$	$-0.68$	$-0.04 \pm 0.10$	1	$0.93$	$-0.70$
$T$	$0.09 \pm 0.14$	—	1	$-0.87$	$0.01 \pm 0.12$	—	1	$-0.87$
$U$	$-0.02 \pm 0.11$	—	—	1	$-0.01 \pm 0.09$	—	—	1

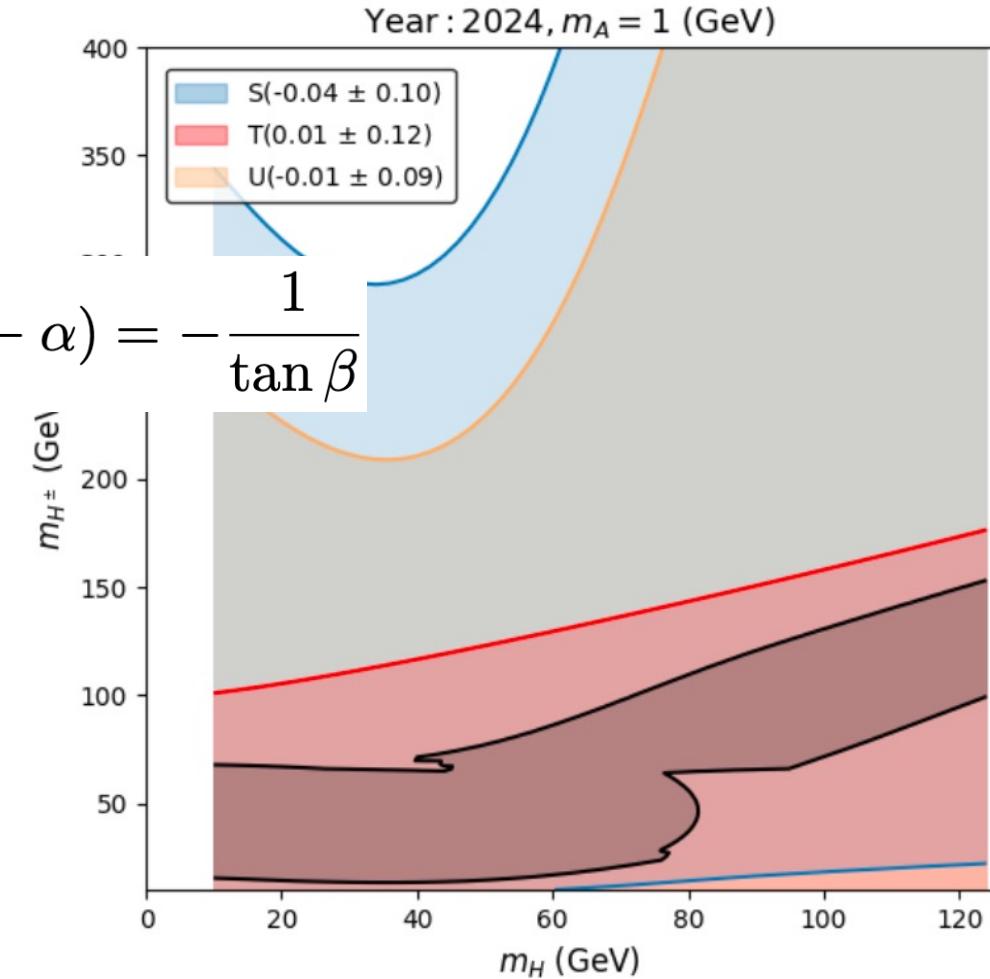
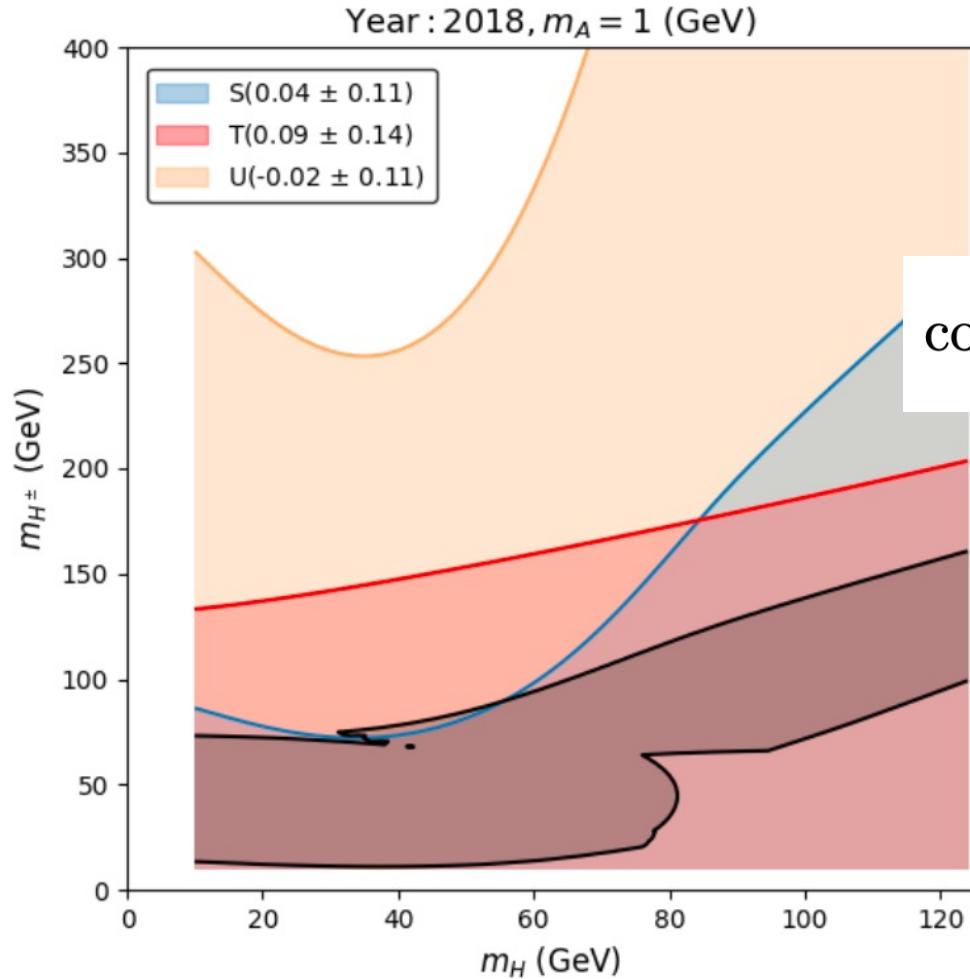
# Constraint

## Oblique constraints: Z pole



# Constraint

## Oblique constraints: Z pole



# Constraint

## Invisible Higgs decays

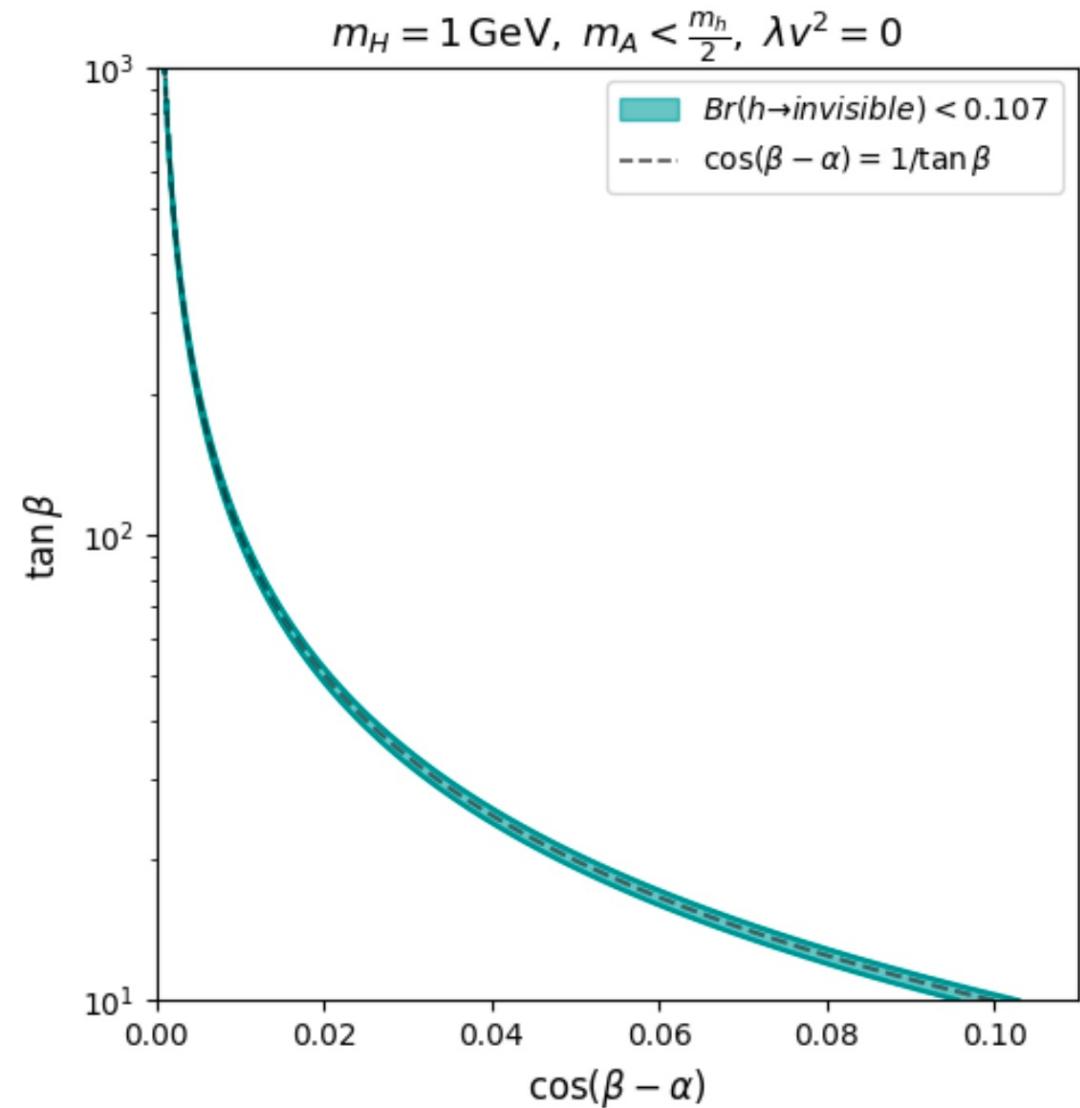
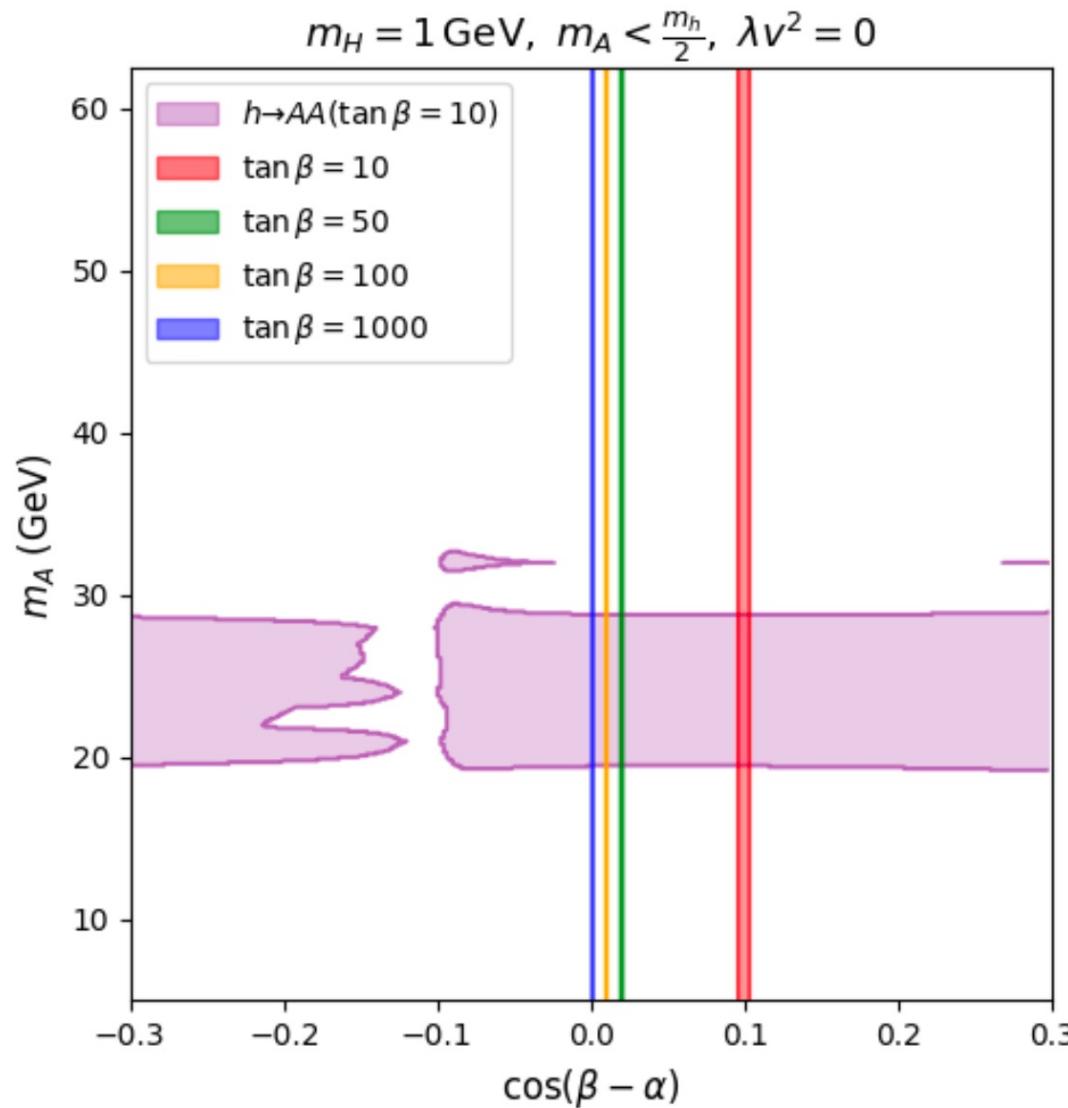
$$\text{Br}(h \rightarrow \phi\phi) = \frac{\Gamma(h \rightarrow \phi\phi)}{\Gamma_h} \approx \frac{1}{\Gamma_h^{\text{SM}}} \frac{g_{h\phi\phi}^2}{8\pi m_h^2} \left(1 - \frac{4m_H^2}{m_h^2}\right)^{1/2} \simeq 4700 \cdot \left(\frac{g_{h\phi\phi}}{v}\right)^2 < 0.107$$

$$g_{hHH} = \frac{s_{\beta-\alpha}}{2v} \left[ (m_H^2 - 3\lambda v^2 - m_h^2) \left( 2t_{2\beta}^{-1} s_{\beta-\alpha} c_{\beta-\alpha} - c_{\beta-\alpha}^2 + s_{\beta-\alpha}^2 \right) + (\lambda v^2 - m_H^2) \right],$$

$$g_{hAA} = \frac{1}{2v} \left[ (2m_H^2 - 2\lambda v^2 - 2m_A^2 - m_h^2) s_{\beta-\alpha} + 2(m_H^2 - \lambda v^2 - m_h^2) t_{2\beta}^{-1} c_{\beta-\alpha} \right].$$

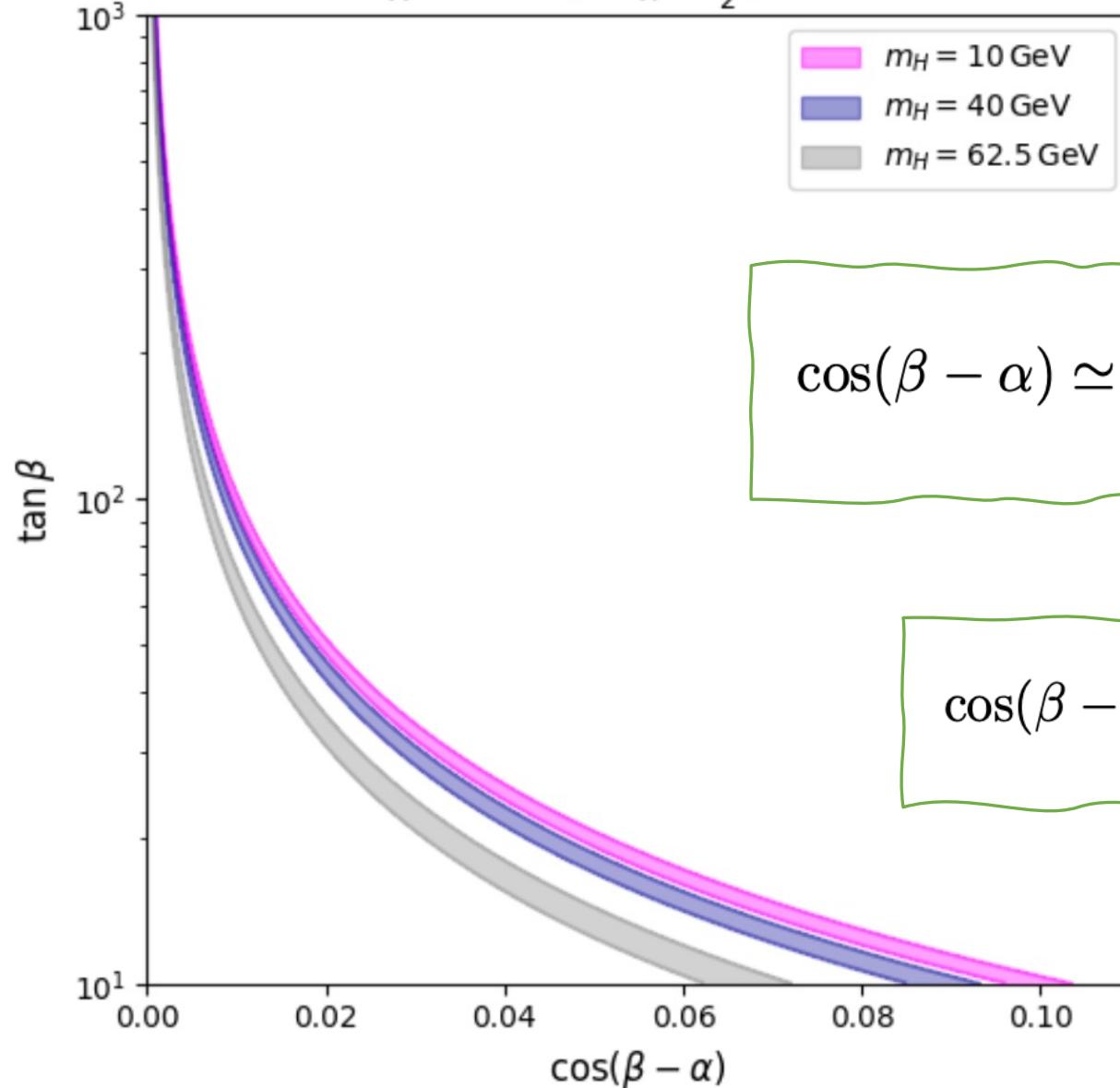
## Light H

$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta}, \quad m_A \in (54, 600) \text{ GeV}, \quad m_{H^\pm} \sim m_A, \quad \lambda v^2 = 0.$$



# Light A: case-1

$\lambda \ll 1, m_H < \frac{m_h}{2}, \lambda v^2 = 0$



$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta} \frac{2m_H^2 - m_h^2}{m_H^2 - m_h^2}, \quad m_H \in \left(5, \frac{m_h}{2}\right) \text{ GeV.}$$

$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta}, \quad m_H \in (5, 25) \text{ GeV.}$$



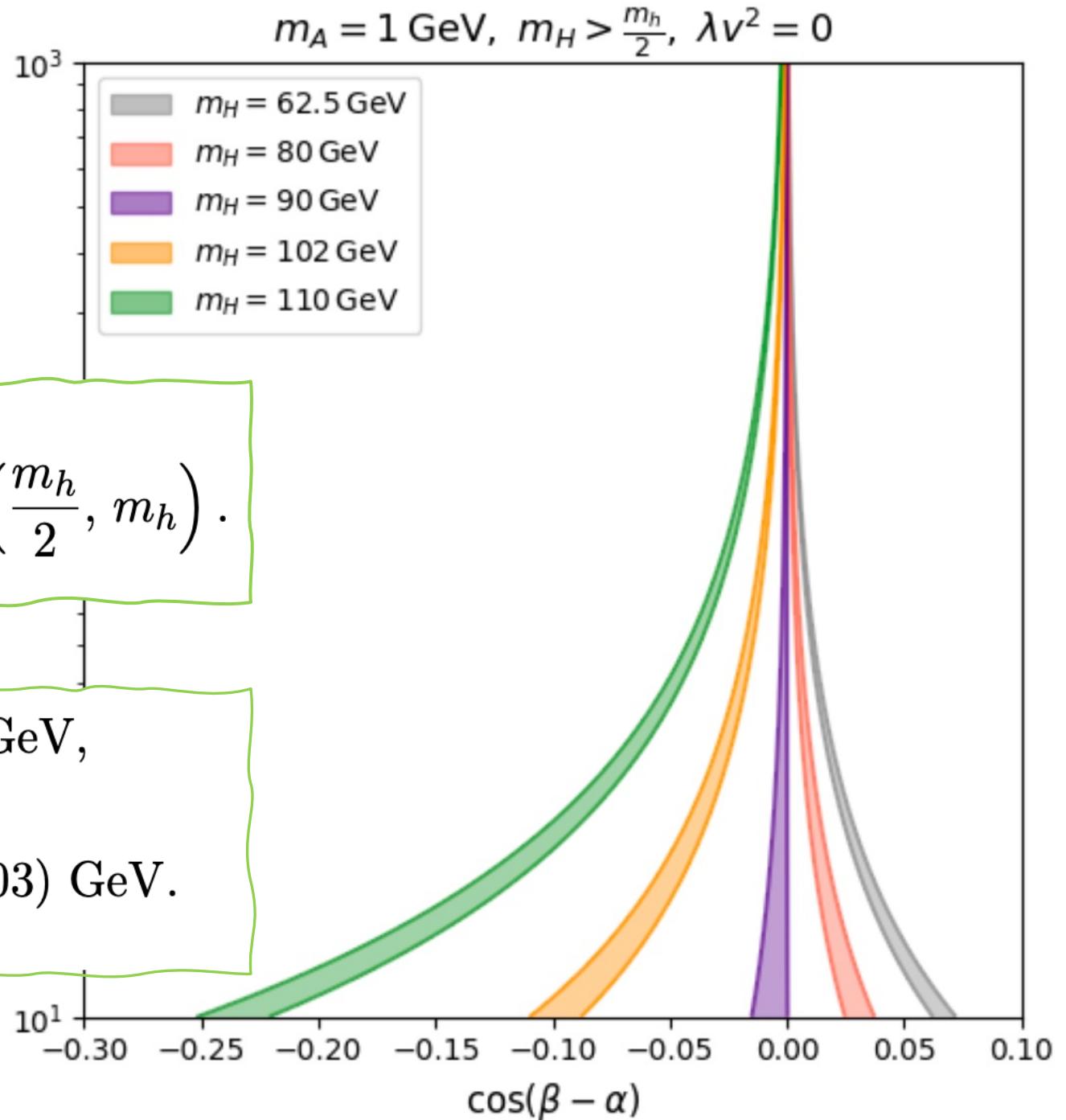
## Light A: case-2

$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta} \frac{2m_H^2 - m_h^2}{m_H^2 - m_h^2}, \quad m_H \in \left( \frac{m_h}{2}, m_h \right).$$



$$\cos(\beta - \alpha) \simeq 0, \quad m_H \in (86.9, 90) \text{ GeV},$$

$$\cos(\beta - \alpha) \simeq -\frac{1}{\tan \beta}, \quad m_H \in (101.2, 103) \text{ GeV}.$$



# All constraints: allowed LLP at Type-I 2HDM

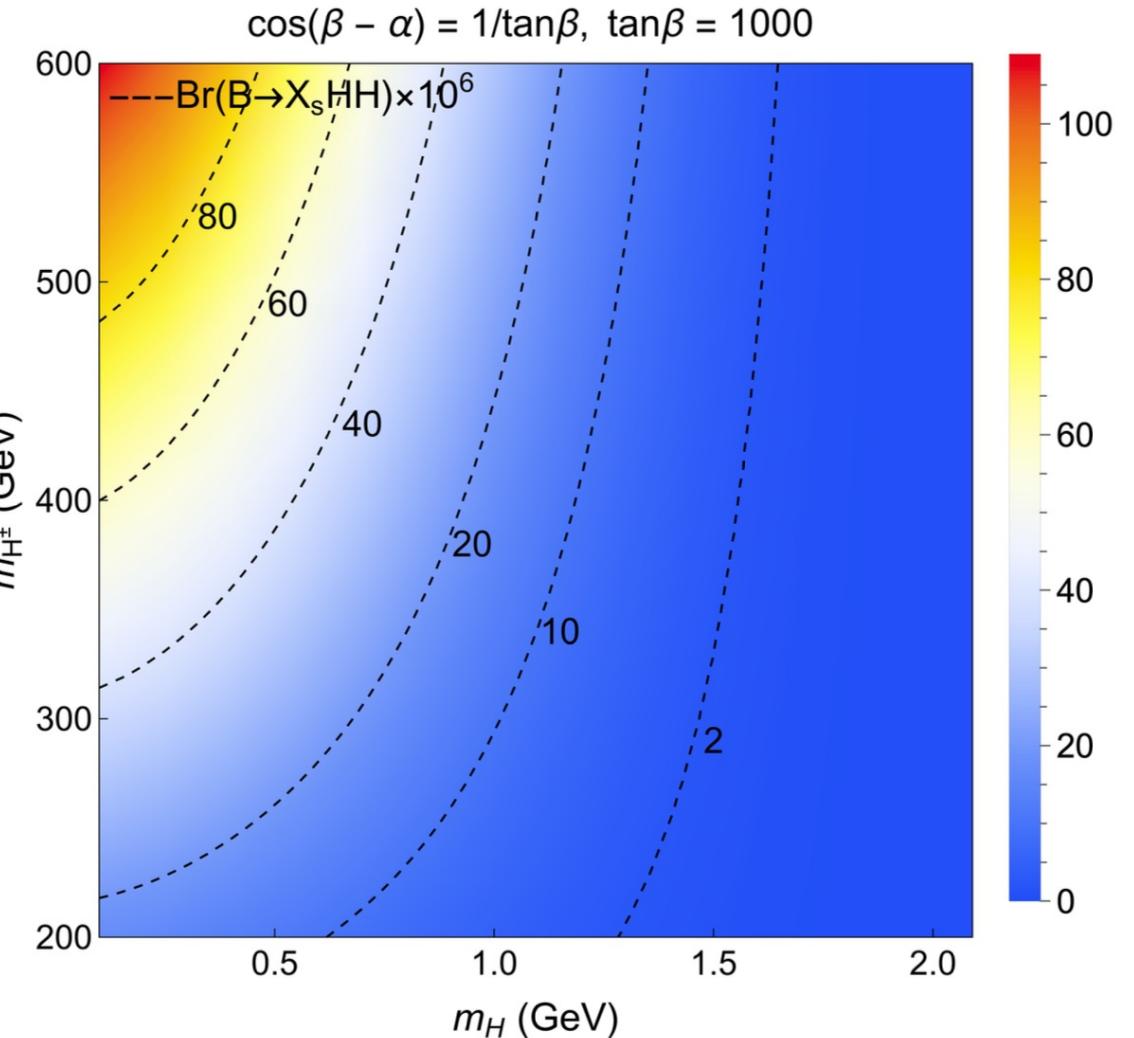
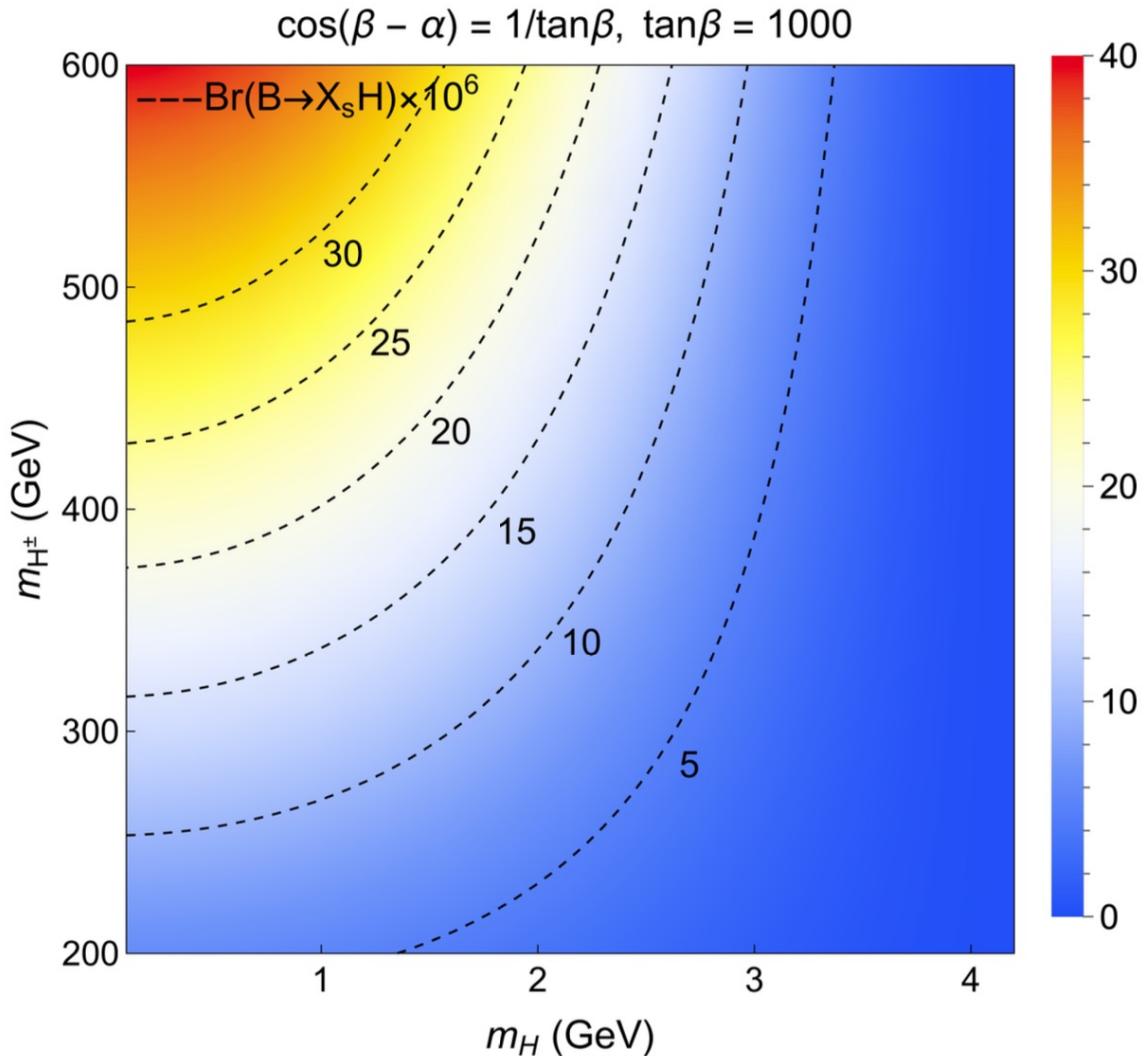
$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta}, \quad m_A \in (54, 600) \text{ GeV}, \quad m_{H^\pm} \sim m_A, \quad \lambda v^2 = 0.$$

$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta} \frac{2m_H^2 - m_h^2}{m_H^2 - m_h^2}, \quad m_H \in (54, m_h) \text{ GeV}, \quad m_{H^\pm} \sim m_A, \quad \lambda v^2 = 0.$$

$$\cos(\beta - \alpha) = 0, \quad m_H \in (86.9, 90) \text{ GeV}, \quad m_{H^\pm} \sim m_H, \quad \lambda v^2 = 0,$$

$$\cos(\beta - \alpha) = -\frac{1}{\tan \beta}, \quad m_H \in (101.2, 103) \text{ GeV}, \quad m_{H^\pm} \sim m_H, \quad \lambda v^2 = 0.$$

# Collider analysis



# Production: CP even scalar

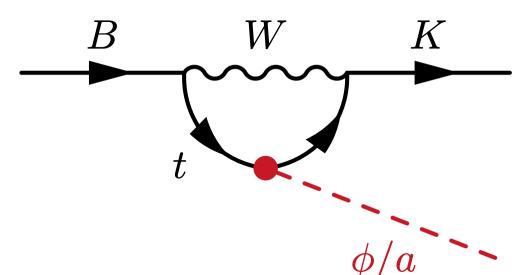
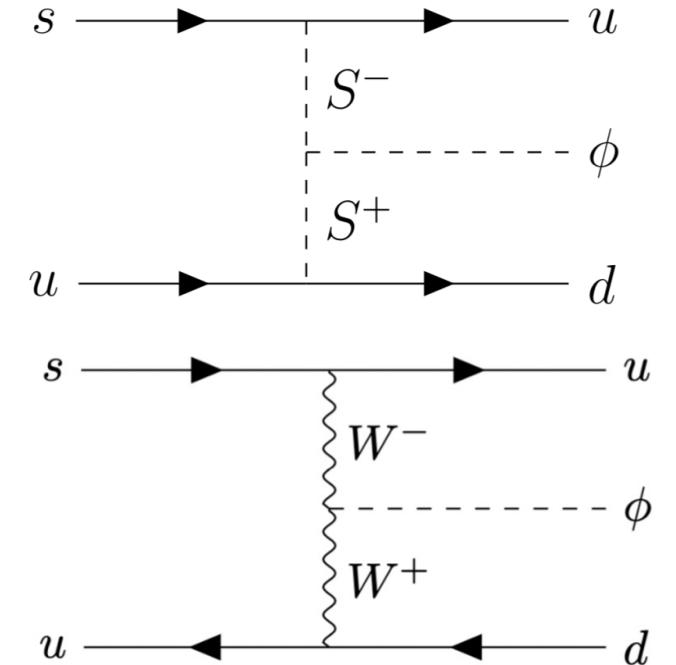
$$\mathcal{L} = -\frac{1}{2}m_\phi^2\phi^2 - \sum_f \xi_\phi^f \frac{m_f}{v} \phi \bar{f}f + \xi_\phi^W \frac{2m_W^2}{v} \phi W^\mu{}^+ W_\mu^- + \xi_\phi^Z \frac{m_Z^2}{v} \phi Z^\mu Z_\mu \\ + \xi_{\phi\phi}^W \frac{g^2}{4} \phi \phi W^\mu{}^+ W_\mu^- + \xi_{\phi\phi}^Z \frac{g^2}{8 \cos^2 \theta_W} \phi \phi Z^\mu Z_\mu + \xi_\phi^g \frac{\alpha_s}{12\pi v} \phi G_{\mu\nu}^a G^{a\mu\nu} + \xi_\phi^\gamma \frac{\alpha_{ew}}{4\pi v} \phi F_{\mu\nu} F^{\mu\nu}$$

$$\text{Br}(K^\pm \rightarrow \pi^\pm \phi) = \frac{1}{\Gamma_{K^\pm}} \frac{2p_\phi^0}{m_{K^\pm}} \frac{|\mathcal{M}|^2}{16\pi m_{K^\pm}}, \quad \boxed{\text{Main contribution}}$$

$$\mathcal{M}(K^\pm \rightarrow \pi^\pm \phi) = G_F^{1/2} 2^{1/4} \xi_\phi^W \left[ \frac{7\lambda(m_{K^\pm}^2 + m_{\pi^\pm}^2 - m_\phi^2)}{12} - \frac{7Am_{K^\pm}^2}{12} \right] + \frac{\xi_\phi^{ds}}{2\pi} m_s \frac{m_{K^\pm}^2 - m_{\pi^\pm}^2}{m_s - m_d} f_0^{K^\pm \pi^\pm}(q^2)$$

$$\frac{\text{Br}(B \rightarrow X_s \phi)}{\text{Br}(B \rightarrow X_c e \nu)} = \frac{\Gamma(b \rightarrow s \phi)}{\Gamma(b \rightarrow c e \nu)} = \frac{12\pi^2 v^2}{m_b^2} (1 - \frac{m_\phi^2}{m_b^2})^2 \frac{1}{f(m_c^2/m_b^2)} \left| \frac{\xi_\phi^{bs}}{V_{cb}} \right|^2$$

b: 4.18 GeV, B: around 5.3 GeV,



# Decay: CP even scalar

$$\Gamma_{\pi\pi} = \frac{3G_F}{16\sqrt{2}\pi m_\Phi} \beta_\pi \left| \xi_\Phi^{gg} \frac{2}{27} (\Theta_\pi - \Gamma_\pi - \Delta_\pi) + \frac{m_u \xi_\Phi^u + m_d \xi_\Phi^d}{m_u + m_d} \Gamma_\pi + (\xi_\Phi^s) \Delta_\pi \right|^2$$

$$\Gamma_{KK} = \frac{G_F}{4\sqrt{2}\pi m_\Phi} \beta_K \left| \xi_\Phi^{gg} \frac{2}{27} (\Theta_K - \Gamma_K - \Delta_K) + \frac{m_u \xi_\Phi^u + m_d \xi_\Phi^d}{m_u + m_d} \Gamma_K + (\xi_\Phi^s) \Delta_K \right|^2$$

$$\Gamma_\pi = \langle \pi\pi | m_u \bar{u}u + m_d \bar{d}d | 0 \rangle, \quad \Delta_\pi = \langle \pi\pi | m_s \bar{s}s | 0 \rangle, \quad \Theta_\pi = \langle \pi\pi | \Theta_\mu^\mu | 0 \rangle$$

Leading order chiral perturbation theory

$$\Gamma_\pi^0 = m_\pi^2,$$

$$\Delta_\pi^0 = 0,$$

$$\Theta_\pi^0 = s + 2m_\pi^2$$

$$\Gamma_K^0 = \frac{1}{2} m_\pi^2,$$

$$\Delta_K^0 = m_K^2 - \frac{1}{2} m_\pi^2,$$

$$\Theta_K^0 = s + 2m_K^2$$

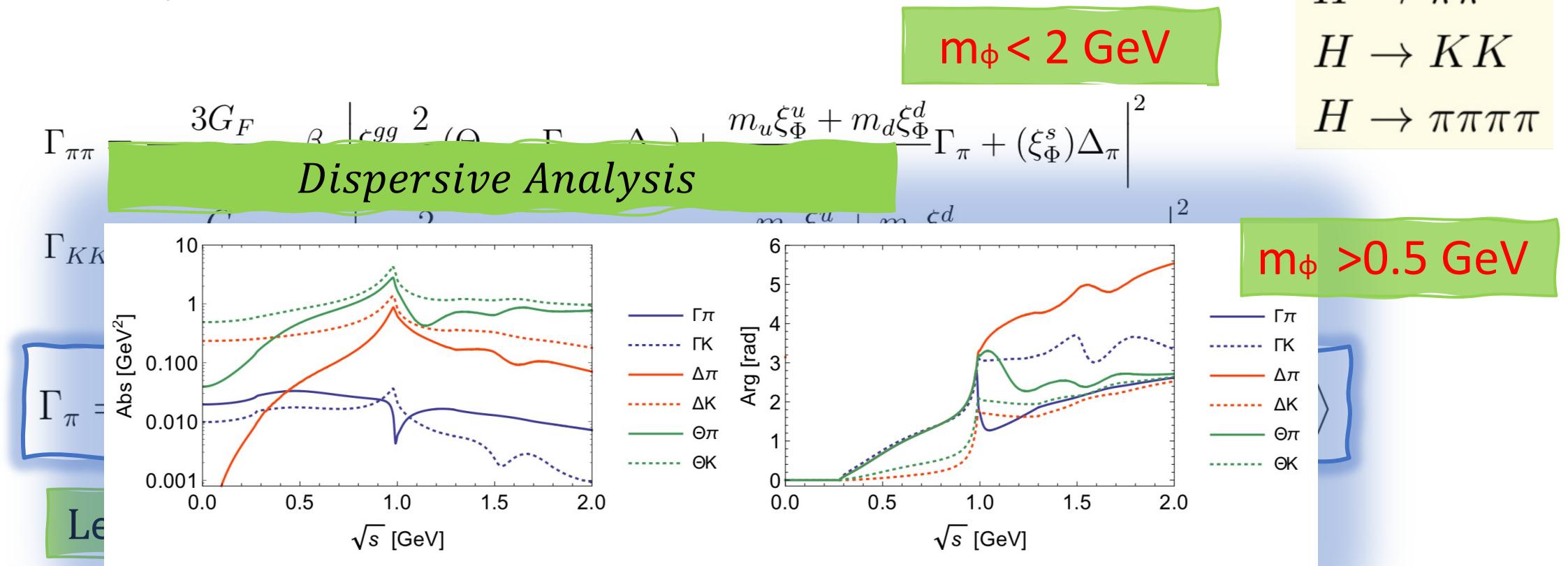
$m_\Phi < 0.5 \text{ GeV}$

$H \rightarrow \pi\pi$

$H \rightarrow KK$

$H \rightarrow \pi\pi\pi\pi$

# Decay: CP even scalar



$$\Gamma_\pi^0 = m_\pi^2,$$

$$\Delta_\pi^0 = 0,$$

$$\Theta_\pi^0 = s + 2m_\pi^2$$

$$\Gamma_K^0 = \frac{1}{2}m_\pi^2,$$

$$\Delta_K^0 = m_K^2 - \frac{1}{2}m_\pi^2,$$

$$\Theta_K^0 = s + 2m_K^2$$

[https://github.com/shiggs90/Light\\_scalar\\_decay.git](https://github.com/shiggs90/Light_scalar_decay.git)

# BMs

For light  $H$ :

$$\cos(\beta - \alpha) = \frac{1}{\tan \beta}, \quad m_A = 200 \text{ GeV}, \quad m_{H^\pm} = 222.35 \pm 0.95 \text{ GeV}, \quad \lambda v^2 = 0,$$

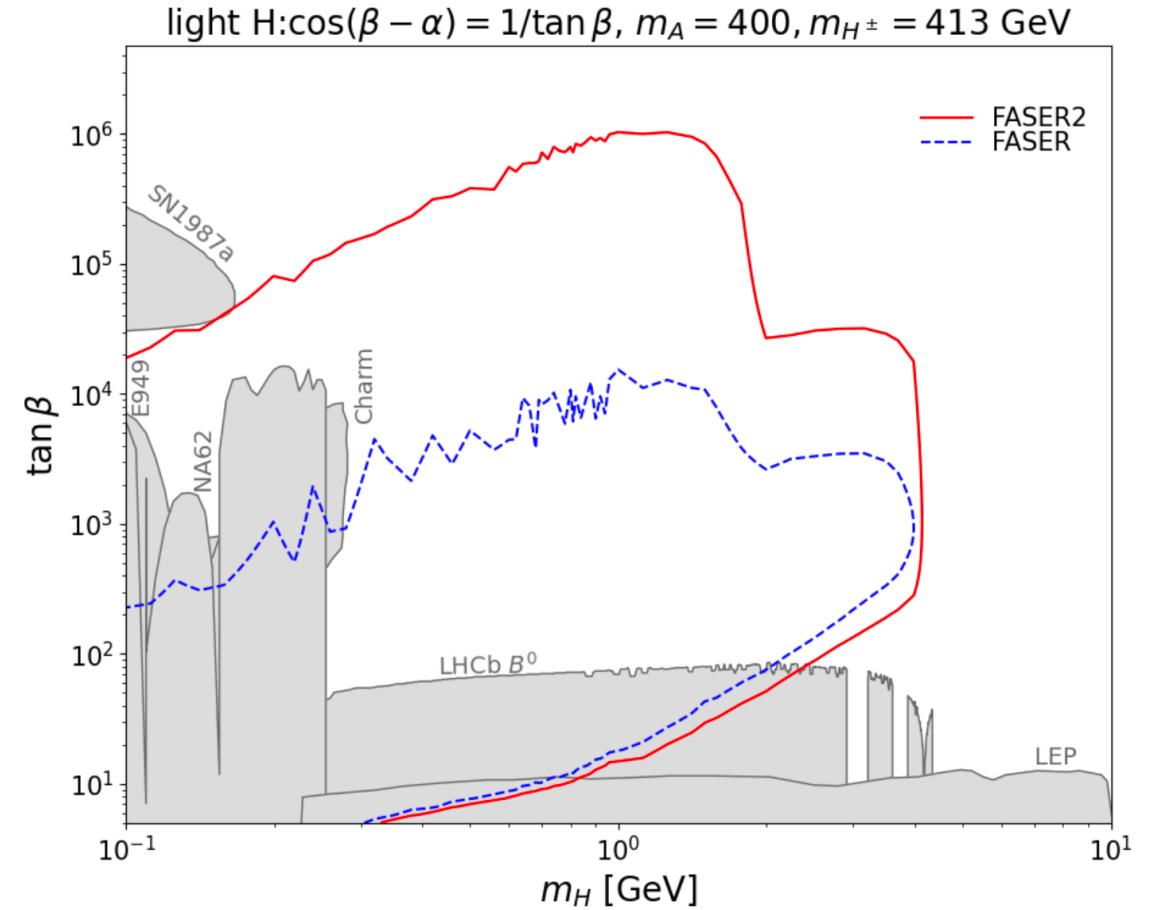
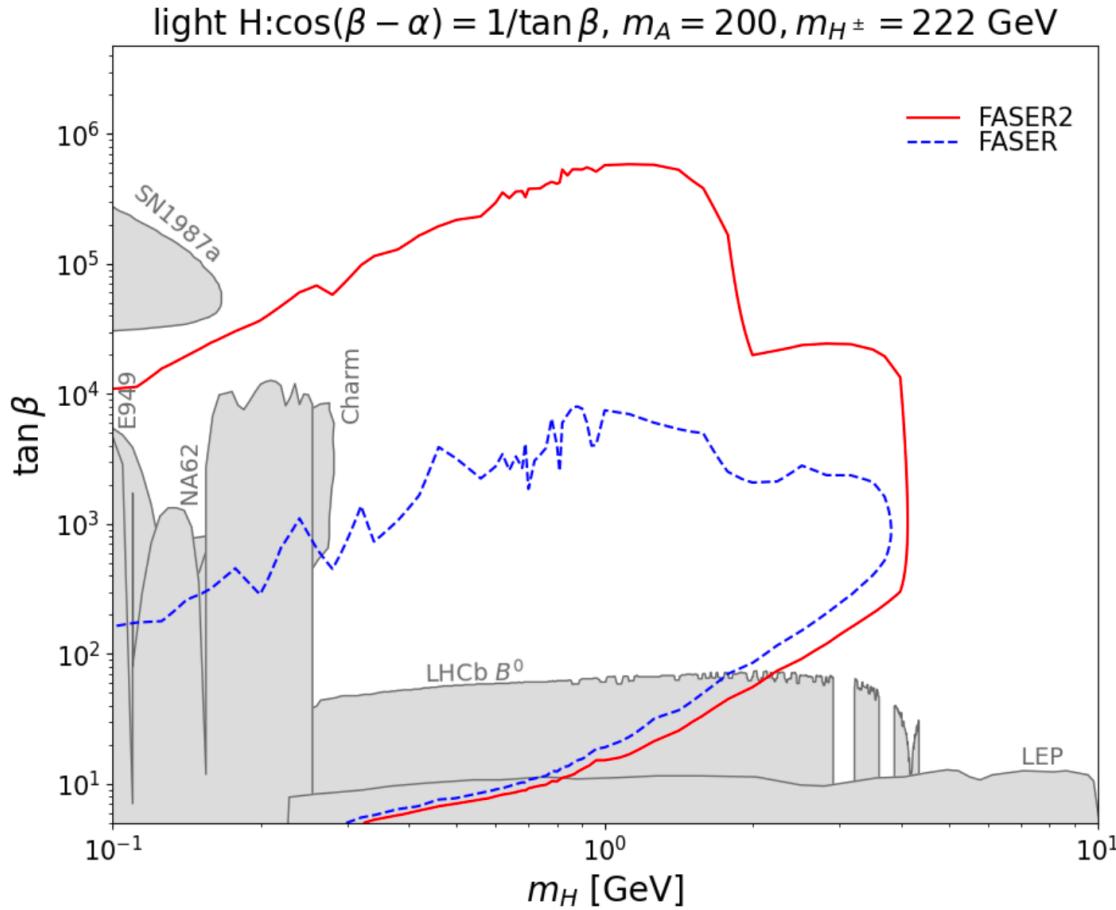
$$\cos(\beta - \alpha) = \frac{1}{\tan \beta}, \quad m_A = 400 \text{ GeV}, \quad m_{H^\pm} = 413.15 \pm 0.45 \text{ GeV}, \quad \lambda v^2 = 0,$$

For light  $A$ :

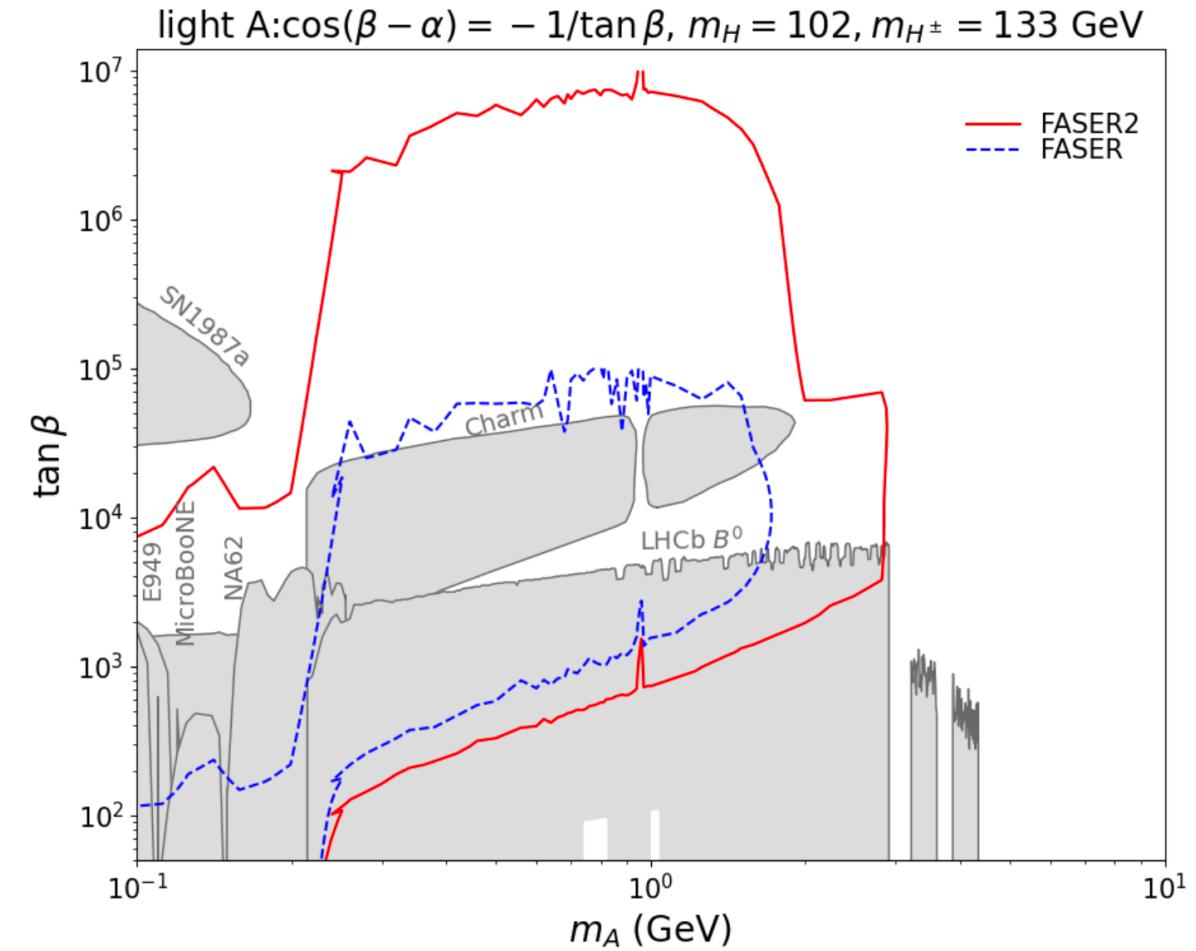
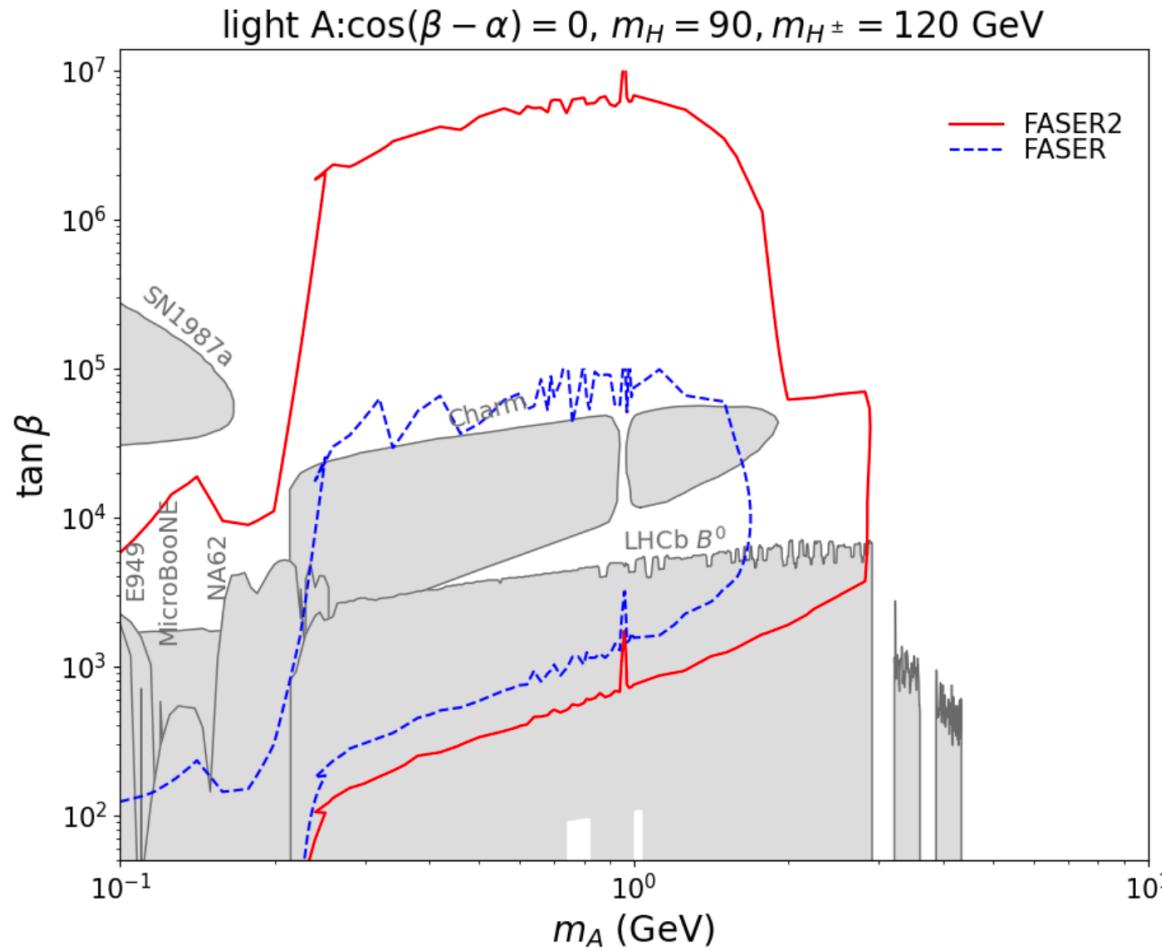
$$\cos(\beta - \alpha) = 0, \quad m_H = 90 \text{ GeV}, \quad m_{H^\pm} = 118.75 \pm 2.25 \text{ GeV}, \quad \lambda v^2 = 0,$$

$$\cos(\beta - \alpha) = -\frac{1}{\tan \beta}, \quad m_H = 102 \text{ GeV}, \quad m_{H^\pm} = 131.05 \pm 1.95 \text{ GeV}, \quad \lambda v^2 = 0.$$

# BMs



# BMs

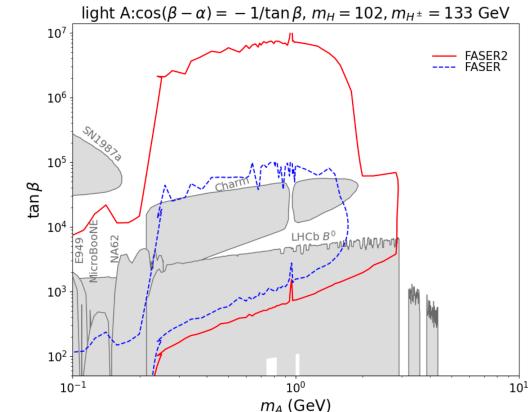
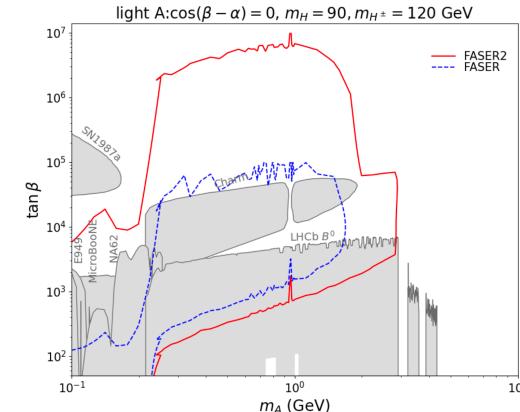
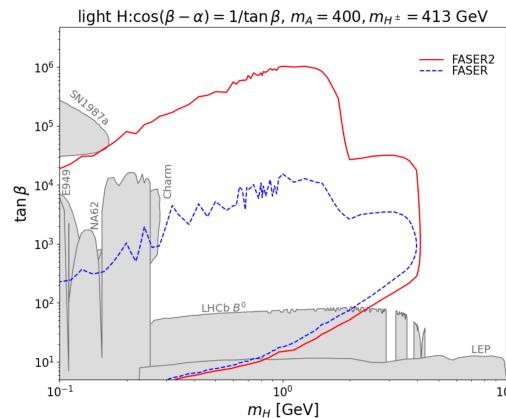
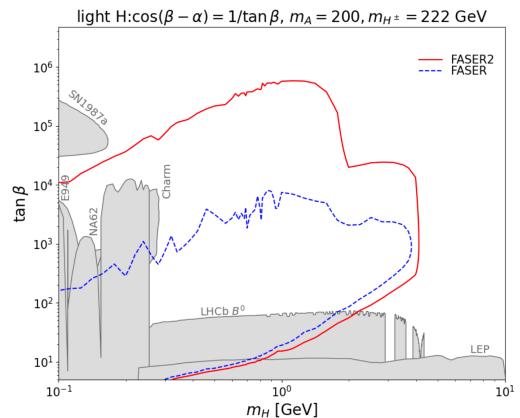


# Conclusion

- Complete allowed LLP at Type-I 2HDM

$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta}, \quad m_A \in (54, 600) \text{ GeV}, \quad m_{H^\pm} \sim m_A, \quad \lambda v^2 = 0.$$

$$\cos(\beta - \alpha) \simeq \frac{1}{\tan \beta} \frac{2m_H^2 - m_h^2}{m_H^2 - m_h^2}, \quad m_H \in (54, m_h) \text{ GeV}, \quad m_{H^\pm} \sim m_A, \quad \lambda v^2 = 0.$$



Thanks !