

TDCPV in B_0 and B_s systems

17th International Conference on Heavy Quarks and Leptons

HQL 2025

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16/09/2025

Stefano Lacaprara

for the Belle II collaboration

INFN Padova

CPV in Standard Model: CKM matrix

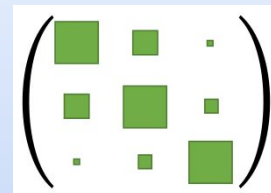
- a key for matter-antimatter asymmetry in the universe
 - In SM, only source is complex phase in CKM matrix
 - (and possible similar phase in PMNS matrix)



Dirac Medal 2010



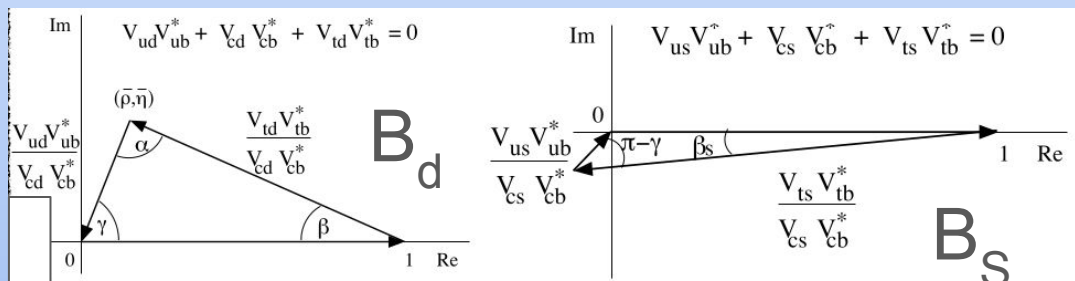
Nobel Prize 2008



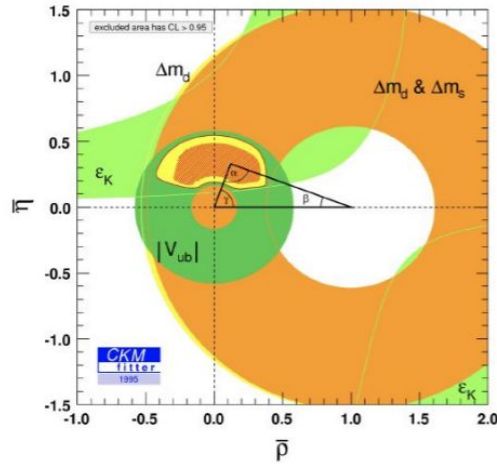
$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

- From CKM unitarity: $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \Rightarrow$ Triangles in complex plane

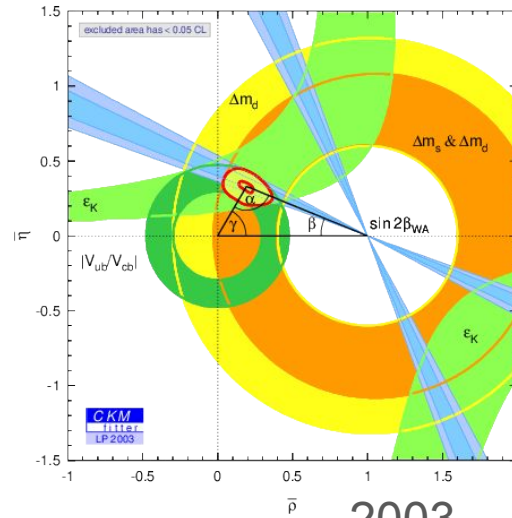
$$\begin{aligned} \phi_1 &= \beta \\ \phi_2 &= \alpha \\ \phi_3 &= \gamma \end{aligned}$$



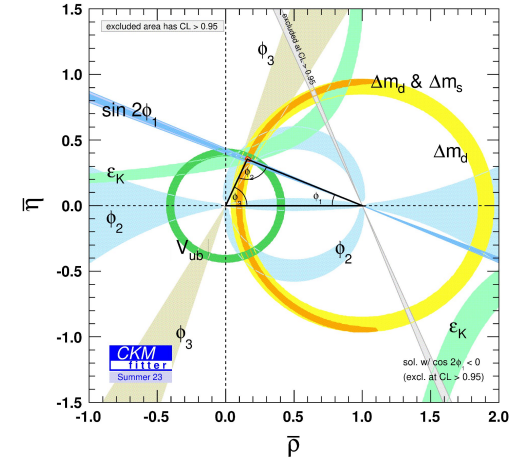
CPV and Unitarity Triangle



1995

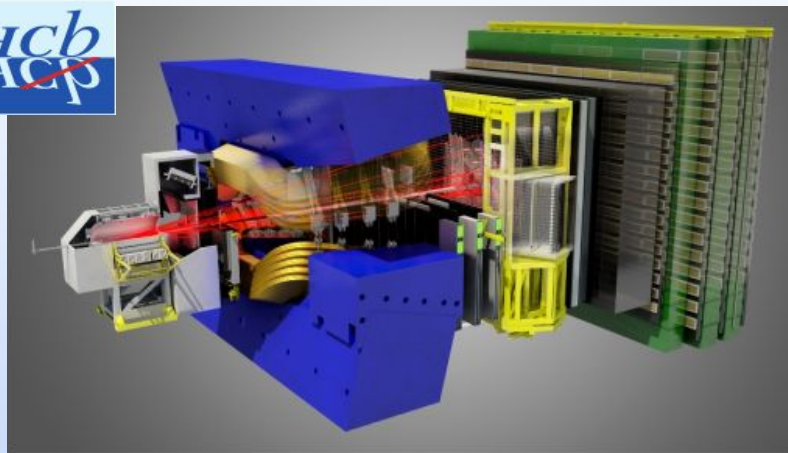
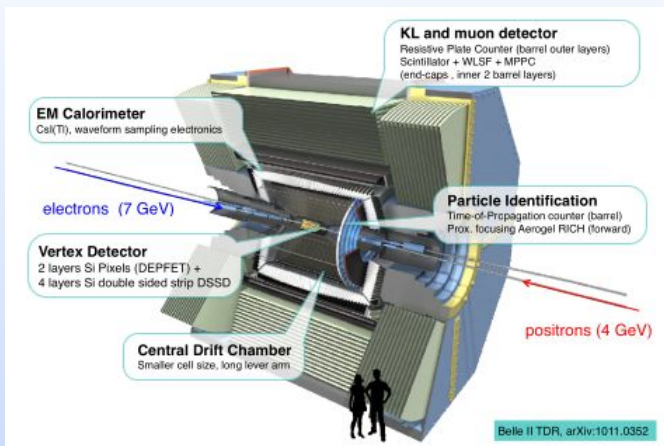


2003



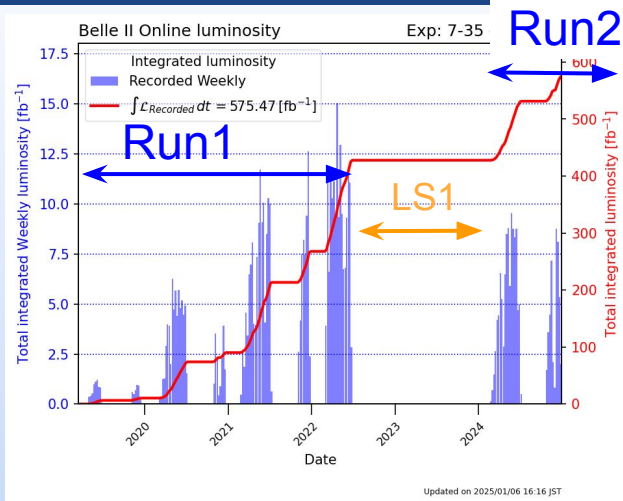
2023

- Precise test of SM by over constraining Unitarity Triangle
- Search for New Physics effects, especially in loop mediated diagrams
- Time Dependent CPV analysis is a powerful tool for precise angles measurements

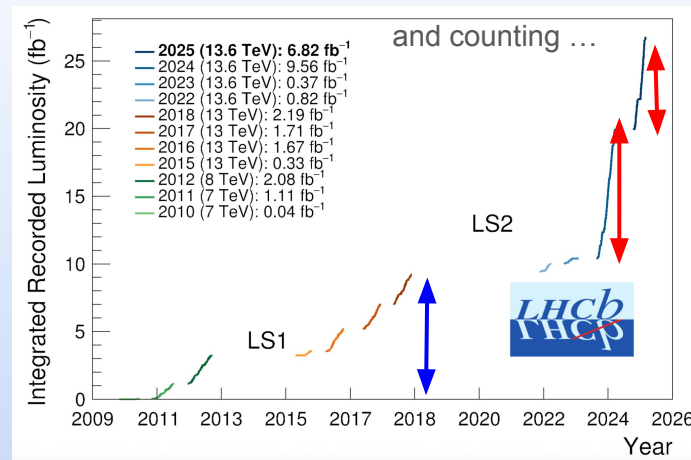


- e^+/e^- (4/7 GeV) at SuperKEK-B
 - Around $Y(4S)$ resonance
 - B-Bbar produced in coherent QM state
- Largely renovated wrt Belle
- Excellent neutral, electron reconstruction and hermeticity

- pp at LHC 13(.6) TeV
- Covering forward region
- Excellent performance (tracking, vertexing, PID), for B and D physics
- High pile-up, $O(100)$ tracks per event
- Complex trigger (now fully software)



- Luminosity record $5.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
 - **577 fb^{-1} collected: $\sim 500 \text{ fb}^{-1}$ at $\Upsilon(4S)$**
 - **Still less than foreseen**
 - **Hard work to improve luminosity and reduce beam backgrounds**
- Run2 data taking to resume from Nov '25
 - Long data taking until summer '26



- LHC performances are simply great
 - Max Luminosity levelled at $2.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
 - Integrated luminosity 2x in 2024
 - 2025 going great too

Belle II vs LHCb: summary

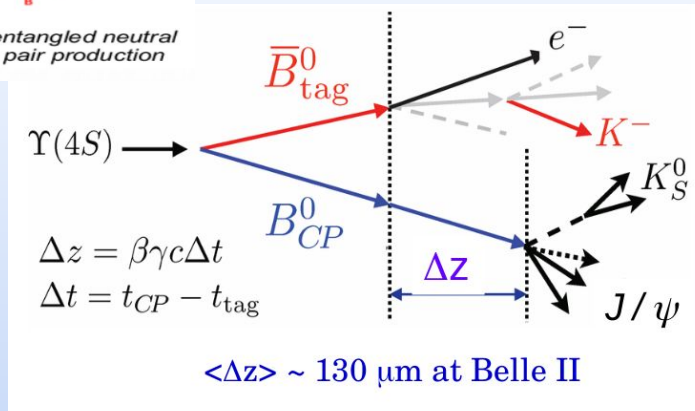


Feature	Belle II	LHCb
σ_{bb} [nb]	~1.1	~150 000
Int Lumi (goal)	multi 10 ab ⁻¹	50 fb ⁻¹ (phase I)
Background level	Low	High
Neutral efficiency	High	Low
Initial state	Well known	Mostly unknown
Decay-time resolution	Good	Excellent
Collision spot size	Tiny	Large
B-flavour tagging efficiency	~37%	4-8%

Time-Dependent CPV analysis @Belle II



Quantum entangled neutral B meson pair production



$$\mathcal{A}_{CP}(\Delta t) = \frac{\Gamma(B_{\text{tag}=B^0}(\Delta t) \rightarrow f_{CP}) - \Gamma(B_{\text{tag}=\bar{B}^0}(\Delta t) \rightarrow f_{CP})}{\Gamma(B_{\text{tag}=B^0}(\Delta t) \rightarrow f_{CP}) + \Gamma(B_{\text{tag}=\bar{B}^0}(\Delta t) \rightarrow f_{CP})} =$$

$$= \boxed{S} \sin(\Delta m_d \Delta t) - \boxed{C} \cos(\Delta m_d \Delta t)$$

$S_{CP} = \sin(2\phi_i^{\text{eff}})$
 mixing induced CPV

$|B^0\rangle \rightarrow |f_{CP}\rangle$
 $|\bar{B}^0\rangle \rightarrow |f_{CP}\rangle$

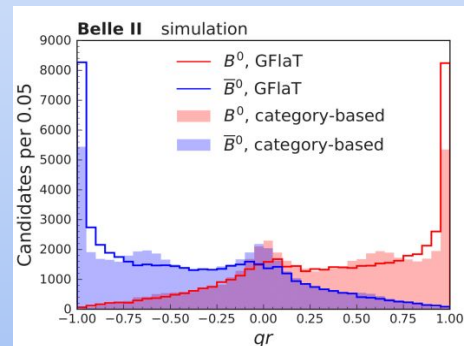
$\mathcal{A}_{CP} = -C_{CP}$
 Direct CPV

$|B\rangle \rightarrow |f\rangle$
 $|\bar{B}\rangle \rightarrow |f\rangle$

- B_{CP} fully reconstructed CP eigenstate
- B_{tag} vertex and flavour information
 - New **GFLaT** algorithm based on GNN
 - Improvement over previous (**C**ategory **B**ased) +18%

$$\varepsilon_{\text{tag}}^{\text{eff}}(\text{CB}) = (31.7 \pm 0.5 \pm 0.4) \%$$

$$\varepsilon_{\text{tag}}^{\text{eff}}(\text{GFLaT}) = (37.4 \pm 0.4 \pm 0.3) \%$$



Time-Dependent CPV analysis @LHCb



$$|B_{L,H}\rangle = |B_q^0\rangle q \pm |\bar{B}_q^0\rangle p$$

$$A_f = \langle f | H_W | B_{(s)}^0 \rangle$$

$$\bar{A}_f = \langle f | H_W | \bar{B}_{(s)}^0 \rangle$$

No CPV in mixing
 $|q/p| = 1$

$$A_{CP,f}(t) = \frac{\Gamma_{\bar{B}_{(s)}^0 \rightarrow f}(t) - \Gamma_{B_{(s)}^0 \rightarrow f}(t)}{\Gamma_{\bar{B}_{(s)}^0 \rightarrow f}(t) + \Gamma_{B_{(s)}^0 \rightarrow f}(t)} = \frac{S_f \sin(\Delta m_{d(s)} t) - C_f \cos(\Delta m_{d(s)} t)}{\cosh\left(\frac{\Delta \Gamma_{d(s)}}{2} t\right) + A_f^{\Delta \Gamma} \sinh\left(\frac{\Delta \Gamma_{d(s)}}{2} t\right)}$$

$$(q\bar{A}_f)/(pA_f) \equiv \lambda_f = |\lambda_f| e^{i\phi_{d(s)}^f}$$

$$(S_f)^2 + (C_f)^2 + (A_f^{\Delta \Gamma})^2 = 1$$

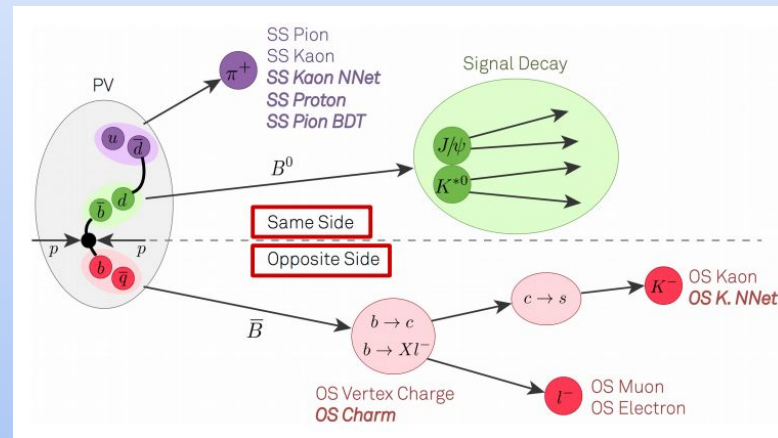
$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$$

CPV in the decay

$$S_{f_{CP}} = \frac{2\text{Im}[\lambda_{f_{CP}}]}{1 + |\lambda_{f_{CP}}|^2}$$

CPV in interference of mixing and decay

- Production of **B** and **B_s**
 - $\Delta \Gamma_s / \Gamma_s = 0.124 \pm 0.007$
- **Tagging** from Same and Opposite side:
 - Effective tagging efficiency: 4-8%
- Large boost + excellent vertex resolution
 - $\Rightarrow$ 60 fs time resolution



$$\phi_1/\beta$$

$\sin(2\phi_1/\beta)$ from $B \rightarrow J/\psi K_S$

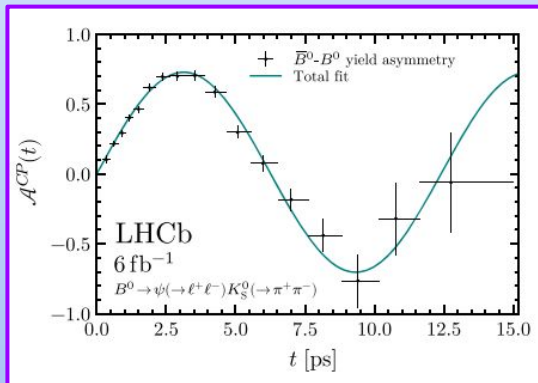
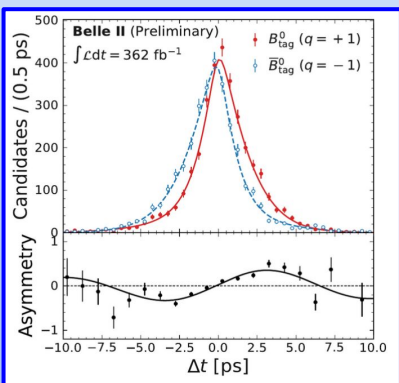
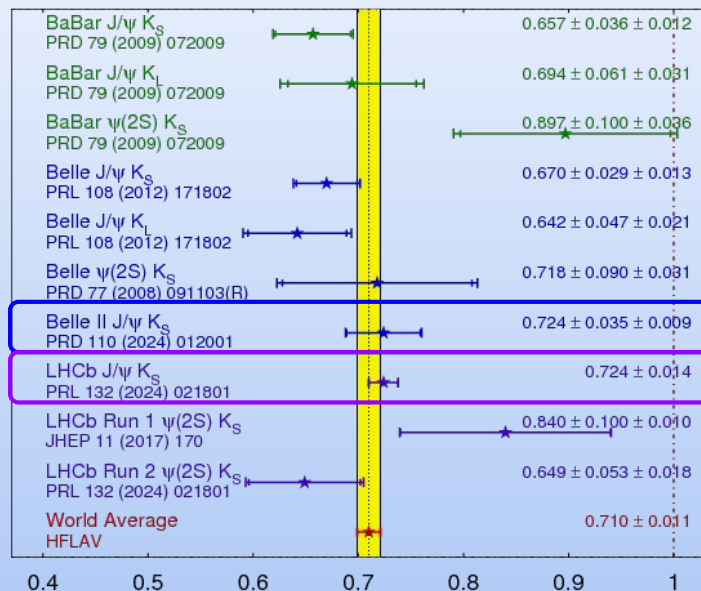
PRD 110 (2024), 12001
PRD 132 (2024), 0210801



- Golden channel, tree-dominated, little penguin pollution

	Belle II	LHCb
B-tagging eff.	~37%	4-6%
# candidates	~6.3k	~370k
Δt resolution	~1 ps	~60 fs
$\int \mathcal{L} dt$	362 fb ⁻¹	6 fb ⁻¹

$\sin(2\beta) \equiv \sin(2\phi_1)$ **HFLAV**
PDG 2025
PRELIMINARY

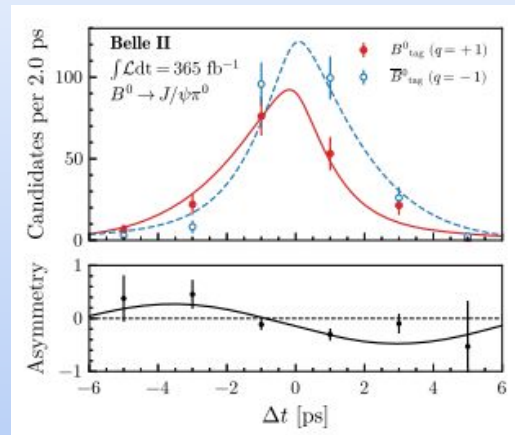
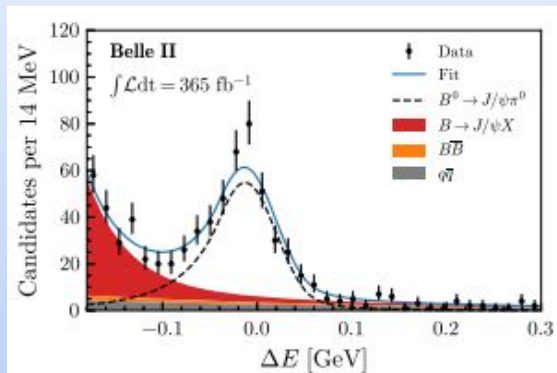
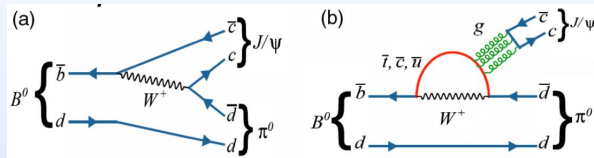


CPV in $B \rightarrow J/\psi\pi^0$

PRD 111 (2024), 12011
Belle II 365 fb⁻¹



- Color-suppressed $b \rightarrow c\bar{c}d$ $B \rightarrow J/\psi\pi^0$ constraint small penguin pollution in $B \rightarrow J/\psi K_S$
 - Relevant with increasing precision
- $\phi_d^{\text{eff}} = 2\phi_1 + \Delta\phi_d$, with $\Delta\phi_d \approx 0.5^\circ$
- Using both $\mu\mu$ and ee
- Challenges:
 - π^0 reconstruction
 - $J/\psi X$ background
- BR uncertainty at level of Belle with half dataset
- First $>5\sigma$ observation of mixing-induced CPV



$$\begin{aligned}
 N_{\text{sig}}(\mu\mu) &= 204 \pm 17 \\
 N_{\text{sig}}(ee) &= 188 \pm 17 \\
 \text{BR} &= (2.00 \pm 0.12 \pm 0.09) 10^{-5}
 \end{aligned}$$

$$\begin{aligned}
 S &= -0.88 \pm 0.17 \pm 0.03 \\
 C &= +0.13 \pm 0.12 \pm 0.03
 \end{aligned}$$

$$B \rightarrow K_S \pi^0 \gamma$$

PRL 134, 011802 (2025)

Belle II 362 fb⁻¹



- $B^0 \rightarrow K_S \pi^0 \gamma$ is expected to have small/none mixing induced CPV in SM
 - $b \rightarrow s \gamma_R$ is helicity suppressed (m_s/m_b) wrt $b \rightarrow s \gamma_L$
 - $B^0 \rightarrow s \gamma_L$ vs $B^0 \rightarrow \bar{B}^0 \rightarrow s \gamma_R$
- Vertex from $K_S \rightarrow \pi^+ \pi^-$ and IP constraint
- Measured separately for **resonant** $K^{*0}(\rightarrow K_S \pi^0) \gamma$

$$S = 0.00^{+0.27}_{-0.26}^{+0.03}_{-0.04}$$

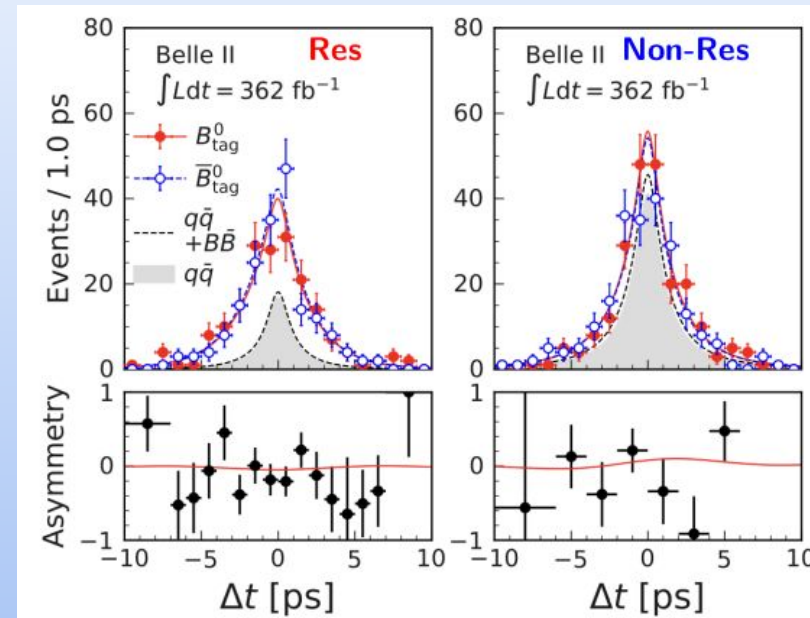
$$C = 0.10 \pm 0.13 \pm 0.03$$

- and inclusive (**non resonant**) decay $K_S \pi^0 \gamma$

$$S = 0.04^{+0.45}_{-0.44} \pm 0.10$$

$$C = -0.06 \pm 0.25 \pm 0.07$$

Most precise result so far



$$B \rightarrow K_S \pi^+ \pi^- \gamma$$

new

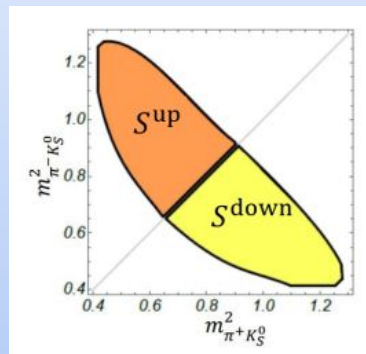
Belle + Belle II 711+365 fb⁻¹



- Also helicity suppressed m_s/m_b
- Sensitive to NP
 - Only $(K_S \rho) \gamma$ are true CP eigenstate
 - Other intermediate resonance (eg $K^* \pi$) requires full amplitude analysis (not done)

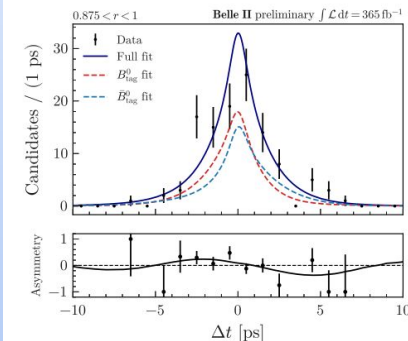
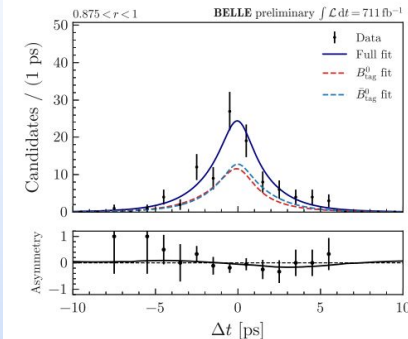
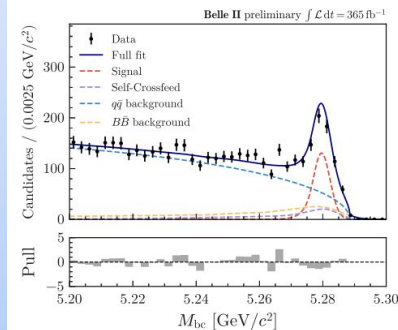
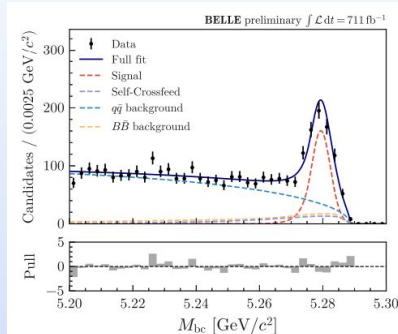
$$S^\pm = S^{\text{up}} \pm S^{\text{down}}$$

- Help in constraining C_7/C'_7
- [\[JHEP09\(2019\)034\]](#)



$$\begin{aligned} C &= -0.17 \pm 0.09 \pm 0.04 \\ S &= -0.29 \pm 0.11 \pm 0.05 \\ S^+ &= -0.57 \pm 0.23 \pm 0.10 \\ S^- &= 0.31 \pm 0.24 \pm 0.05 \end{aligned}$$

x2 smaller uncertainty than Belle or BaBar

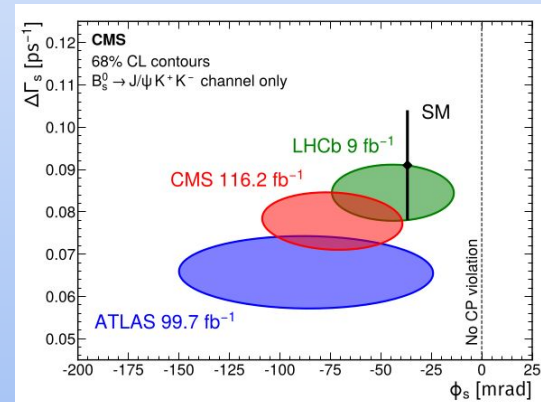
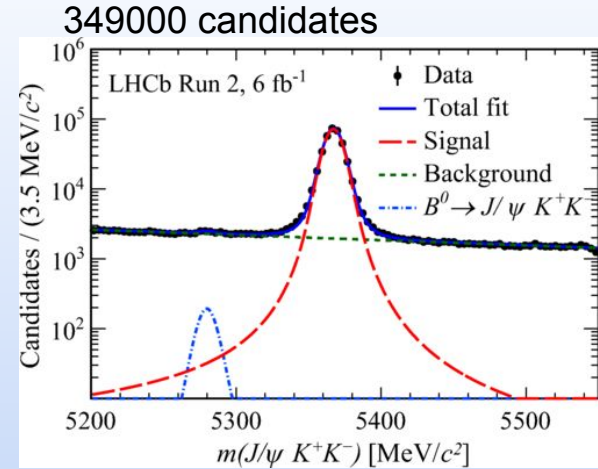


CPV in $B_s \rightarrow J/\psi \phi$

PRL 132 (2024) 051802
LHCb Run2 6 fb⁻¹



- $\phi_s \simeq -2\beta_s = -2\arg\left(-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right)$
- Precise determination from indirect from SM fit
 - $\phi_s = -0.0368^{+0.0008}_{-0.0006}$
 - NP can significantly change ϕ_s [\[RevModPhys.88.045002\]](#)
 - Excellent NP probe
- Combine angular and t fit to cope with $P \rightarrow VV$ decay
 - Disentangle CP-odd/CP-even polarization
- LHCb
 - Most precise measurement to date
 - Combination with other LHCb measurement:
 - $\phi_s = -0.031 \pm 0.018 \text{ rad}$
- Nice results also from CMS/ATLAS
 - Xin Chen's talk after this

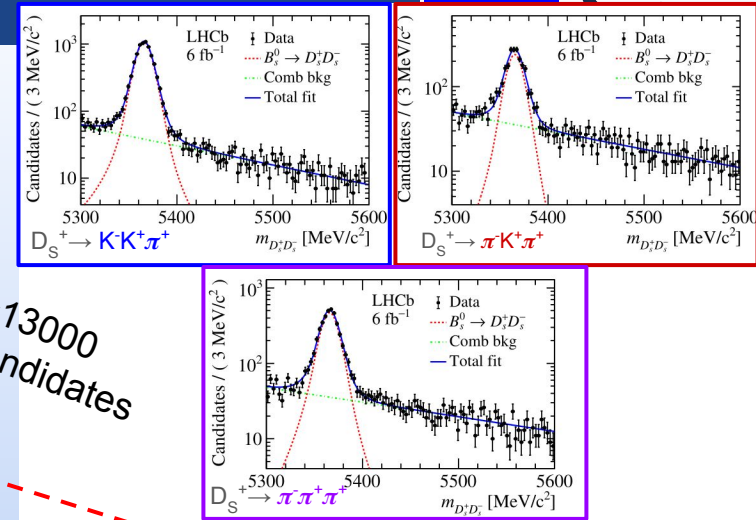


CPV in $B_s \rightarrow D_s^+ D_s^-$

JHEP 01 (2025) 61 LHCb Run2 6 fb⁻¹



- Together $B_0 \rightarrow D^+ D^-$
 - One $D_s^\pm \rightarrow KK\pi$ and other $D_s^\pm \rightarrow K^- K^+ \pi^+ / \pi^- K^+ \pi^+ / \pi^- \pi^+ \pi^+$
 - $D^+ \rightarrow K^- \pi^+ \pi^+$: Critical K- π separation, using MVA
 - Fit to $m(D_s^+ D_s^-)$ to extract signal
 - S-weighted time distribution fit
- B_s results consistent with no CP asymmetry



~13000 candidates

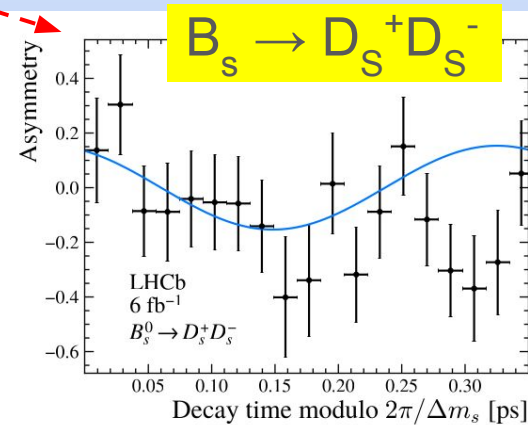
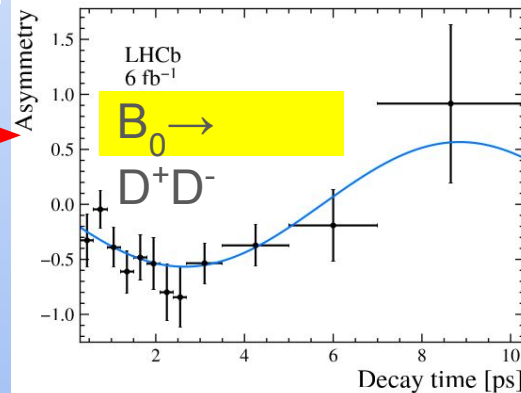
$$\phi_s = -0.055 \pm 0.090 \text{ (stat)} \pm 0.021 \text{ (syst)} \text{ rad,}$$

$$|\lambda_{D_s^+ D_s^-}| = 1.054 \pm 0.099 \text{ (stat)} \pm 0.020 \text{ (syst),}$$

- B_0 results show CPV at 6σ

$$S_{D^+ D^-} = -0.552 \pm 0.100 \text{ (stat)} \pm 0.010 \text{ (syst),}$$

$$C_{D^+ D^-} = 0.128 \pm 0.103 \text{ (stat)} \pm 0.010 \text{ (syst).}$$



$$\phi_2/\alpha$$

- Tree level $b \rightarrow u \bar{d}$ for $B \rightarrow \pi\pi/\pi\rho/\rho\rho$
 - Weak phase ϕ_2
 - Small $b \rightarrow d$ loop amplitudes contributes with additional $\Delta\phi_2$
 - $S = \sqrt{(1 - C^2)} \sin(2\phi_2 + \Delta\phi_2)$

Challenges:

- reconstruct $2\pi^0$
- Angular analysis to measure polarization in $P \rightarrow VV$ decay

$$\mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) = (2.89^{+0.23}_{-0.22}) \times 10^{-5},$$

$$f_L = 0.921^{+0.024}_{-0.025},$$

$$S = -0.26 \pm 0.19$$

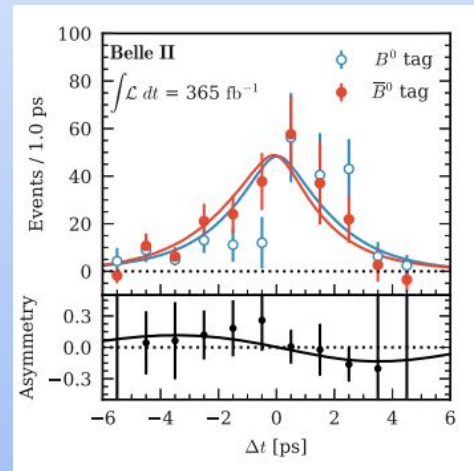
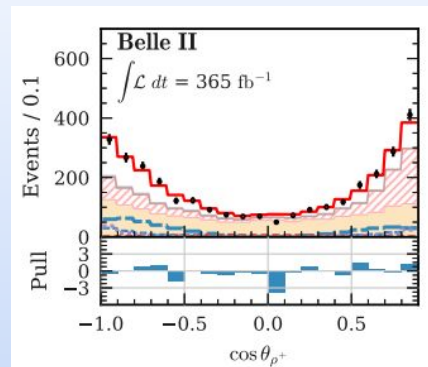
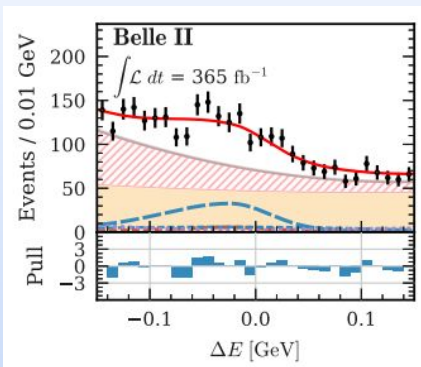
$$C = -0.02 \pm 0.12,$$

- Results in $\sim 8\%$ improvement on ϕ_2 from $B \rightarrow \rho\rho$ using isospin analysis

$B^0 \rightarrow \pi^0 \pi^0$ results in Nakao-san's talk

$$\phi_2 = (92.6^{+4.5}_{-4.7})^\circ$$

$$\Delta\phi_2 = (2.4^{+3.8}_{-3.7})^\circ$$



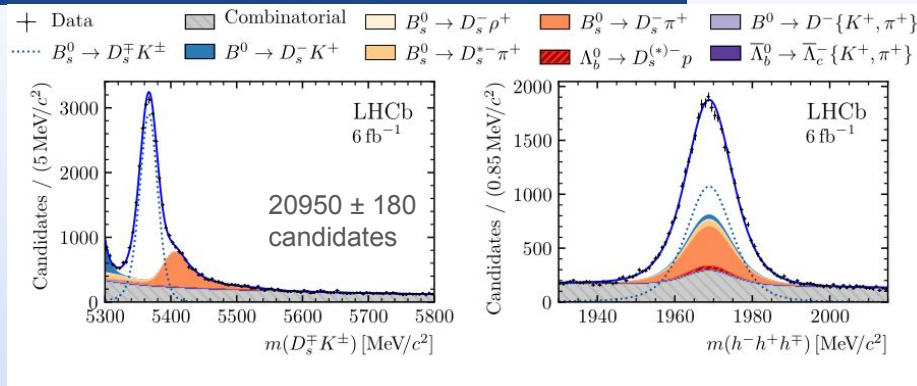
ϕ_3/γ

LHCb: γ/ϕ_3 with $B_s \rightarrow D_s^\mp K^\pm$ decays

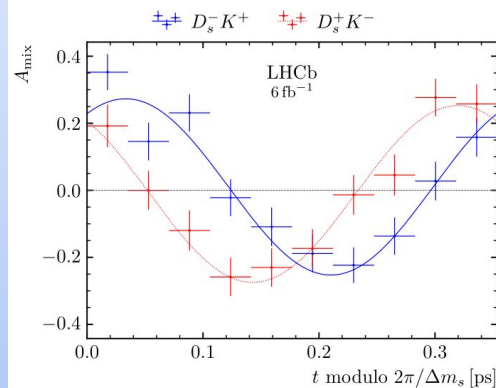
JHEP 03 (2025) 139
LHCb 6 fb⁻¹



- Tree-level decay
 - Sensitive to $(\gamma - 2\beta_s)$ phase
 - $r_{D_s K} \approx 0.4$ ($r_{DK} \approx 0.02$)
 - $A(b \rightarrow c\bar{s}u) \sim A(b \rightarrow u\bar{c}s) \sim O(\lambda^3)$
- $D_s \rightarrow KK\pi/K\pi\pi/\pi\pi\pi$
- 2D mass fit to get signal (*sPlot*)
- Flavor-tag 6.1% OS/SS
- External input (ϕ_s , production and detection asymmetries)
- Combined with Run1



$$\begin{aligned}\gamma &= (81^{+12}_{-11})^\circ, \\ \delta &= (347.6 \pm 6.3)^\circ \\ r_{D_s K} &= 0.318^{+0.034}_{-0.033}.\end{aligned}$$



Used for LHCb γ combination (not competitive)

$\gamma/\phi_3 = (64.6 \pm 2.8)^\circ$ [LHCb-CONF-2024-004](#)

Combination Belle/BelleII $\phi_3 = (78.6 \pm 7.3)^\circ$

Few ab⁻¹ needed to compete with LHCb results

[JHEP 10 2024, 143 \(2024\)](#)

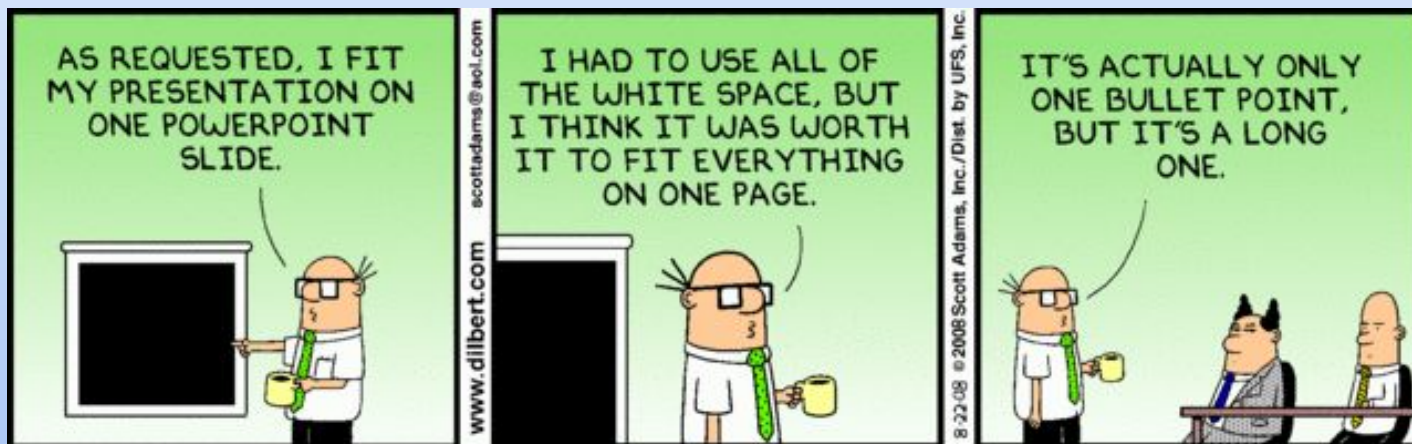
Summary and future



- Time Dependent CPV measurements presented for B and B_s
 - LHCb dominating the scene, CMS/ATLAS contributing for β_s
 - BelleII leading in final states with neutral and in α/ϕ_2
- Future projection as input to EPPSU: [arXiv:2503.24346v2](https://arxiv.org/abs/2503.24346v2)
 - ATLAS/CMS/LHCb/BelleII
 - Measurement mostly statistically limited
- Complementarity and cross check in different environments is essential

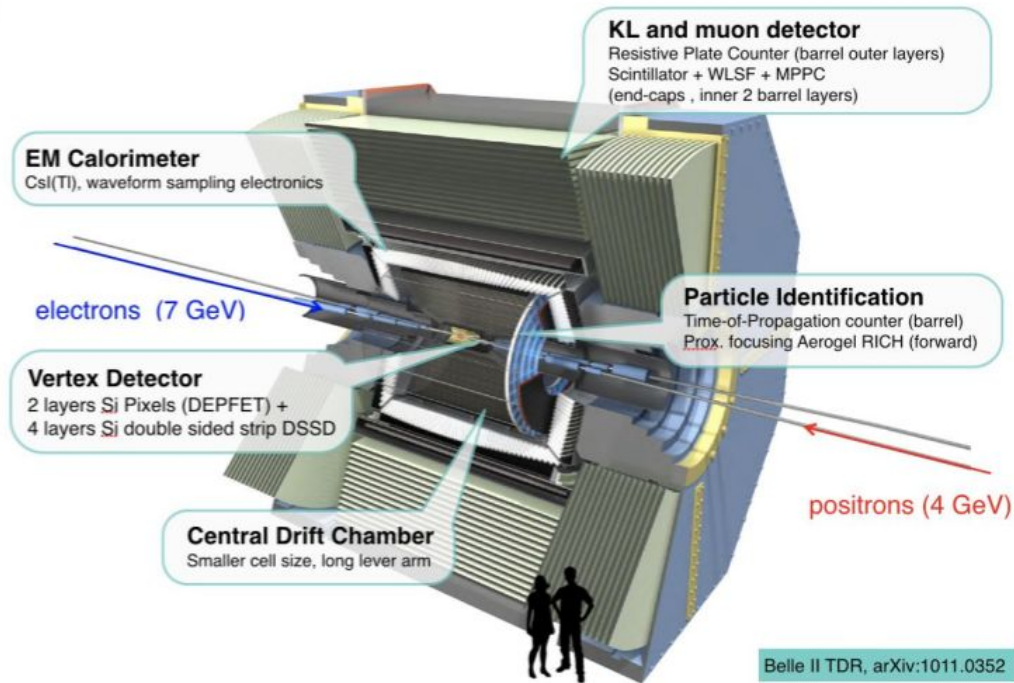
Experiment Assumed data sample	LHCb 50 fb ⁻¹	Belle II 10 ab ⁻¹
CKM angles		
β	0.20°	0.4°
α	—	2.5°
γ	0.8°	2.2°
ϕ_s [mrad]	8	—
CP violation in loop-dominated decays		
$S(B^0 \rightarrow \eta' K_S^0)$	—	0.023
$\phi_s(B_s^0 \rightarrow \phi\phi)$ [mrad]	22	—
$\phi_s(B_s^0 \rightarrow K^{*0} \bar{K}^{*0})$ [mrad]	20	—

Backup

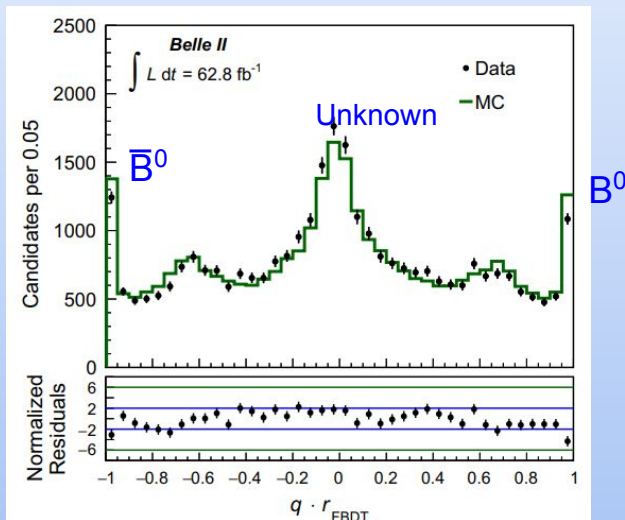


Luminosity Frontier experiment

- Asymmetric e^+e^- colliders- B factories, also charm and τ factories
- Belle Belle II: e^+ (3.5 GeV) e^- (8 GeV) e^+ (4 GeV) e^- (7 GeV)
- Improved vertex resolution allows lower boost
- 424 fb^{-1} (362 fb^{-1} at $Y(4S)$) collected at Belle II so far; Goal: 50 ab^{-1}



- Used to determine the quark-flavour of B_{tag}
- Many different final states considered, combined with two layers of MVA discriminators.
 - Developed also a **Deep Neural Network** with similar performance



Categories	Targets
Electron	e^-
Intermediate Electron	e^+
Muon	μ^-
Intermediate Muon	μ^+
KinLepton	e^-
Intermediate KinLepton	ℓ^+
Kaon	K^-
KaonPion	K^-, π^+
SlowPion	π^+
FastHadron	π^-, K^-
MaximumP	ℓ^-, π^-
FSC	ℓ^-, π^+
Lambda	Λ
Total= 13	

Performance measured on data using $B^0 \rightarrow D^{(*)} h^+$ decays

- Effective efficiency:

$$\varepsilon_{eff} = \sum_i \varepsilon_i (1 - 2w_i)^2$$

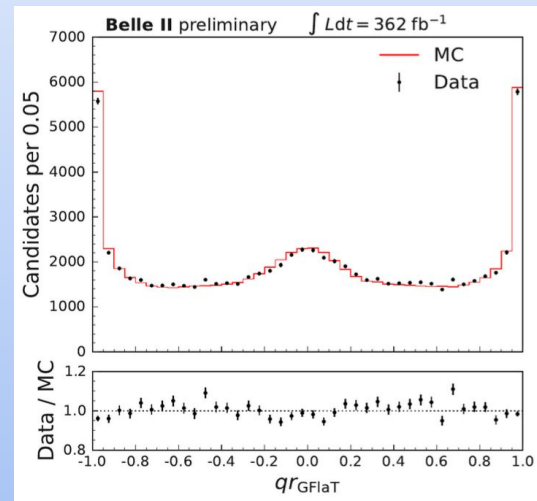
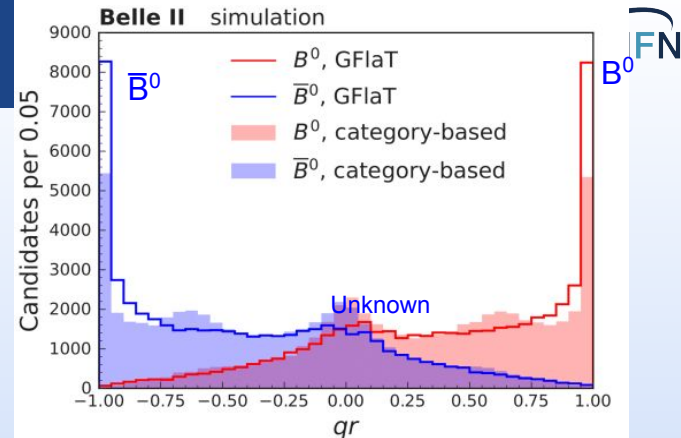
$$= (30.0 \pm 1.2 \pm 0.4)\%$$

B flavour tagging: GFlaT

arXiv:2402.17260
PRD 110 (2024). 12001

- CPV analysis in Belle II used a category-based (CB) algorithm [[Eur. Phys. J 82, 283 \(2022\)](#)]
- A more advanced algorithm GFlaT, based on graph convolutional neural network (GNN), was developed
 - Using 25 variables for each track from the B_{tag} decay
- Performance evaluated on data using self-tagging $B^0 \rightarrow D^{(*)}\pi^+$ decays
- Significant improvement in performance
 - **+18%** (relative)

$$\begin{aligned}\varepsilon_{\text{tag}}(\text{CB}) &= (31.7 \pm 0.5 \pm 0.4) \% \\ \varepsilon_{\text{tag}}(\text{GFlaT}) &= (37.4 \pm 0.4 \pm 0.3) \%\end{aligned}$$



Measurement of ϕ_2/α

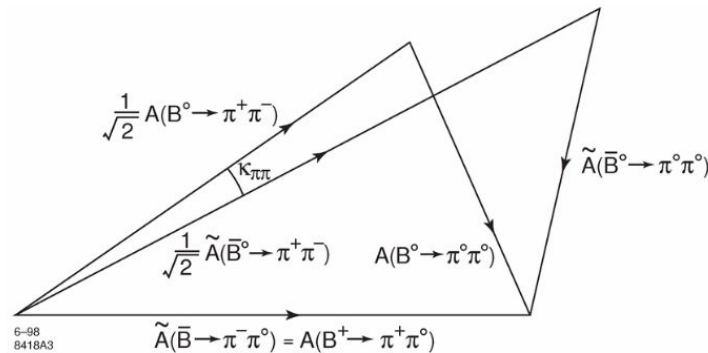
- The measurement of ϕ_2 from $B \rightarrow \pi\pi$ (or $B \rightarrow \rho\rho$) final states comes from an isospin analysis:

The following equalities hold:

$$\frac{1}{\sqrt{2}}A^{+-} + A^{00} = A^{+0}$$

$$\frac{1}{\sqrt{2}}\tilde{A}^{+-} + \tilde{A}^{00} = \tilde{A}^{+0}$$

$$A^{+0} = \tilde{A}^{+0}$$

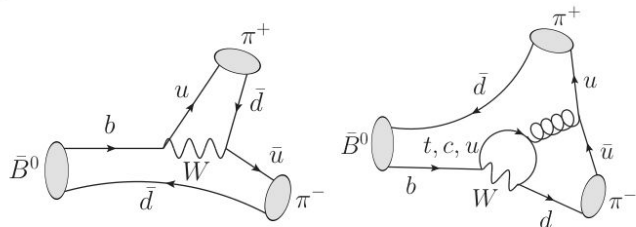


M. Gronau and D. London,
PRL 65 (1990), 3381

- Observables (for e.g. $B \rightarrow \pi\pi$):
 - branching fractions of: $B^0 \rightarrow \pi^+\pi^0, \pi^+\pi^-, \pi^0\pi^0$;
 - direct (time-independent) CP asymmetries: C^{+-}, C^{00} ;
 - time-dependent CP asymmetries: S^{+-}, S^{00} .
- Belle II will be able to measure all these observables;
- We expect to push the sensitivity to α to $\sim 1^\circ$.

Measurement of ϕ_2/α

Two amplitudes of comparable size with different weak phase:



Penguin in $B^0 \rightarrow \pi^+ \pi^-$, $\pi^0 \pi^0$, but not in $B^\pm \rightarrow \pi^\pm \pi^0$

$$\phi_2 = (\bar{A}^{+0}, A^{+0}), \phi_2^{eff} = (\bar{A}^{+-}, A^{+-})$$

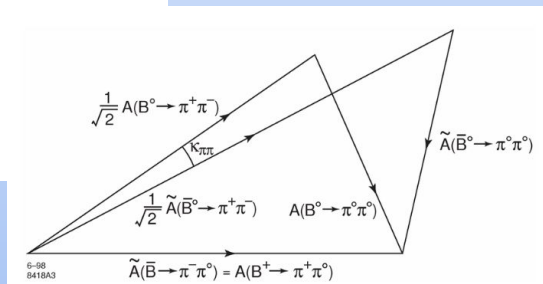
Isospin analysis [Gronau-London PRL, 64 3381 (1990)]: constraints

B^0 and $B^\pm$ amplitudes:

$$A^{+0} = A^{+-}/\sqrt{2} + A^{00}$$

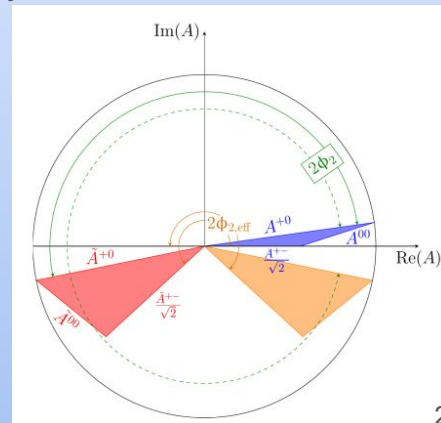
$$\bar{A}^{+0} = \bar{A}^{+-}/\sqrt{2} + \bar{A}^{00}$$

$$|A^{+0}| = |\bar{A}^{+0}|$$



Similar for $B \rightarrow \rho \rho$

- Need all branching fractions;
- Direct CP asymmetries: C^{+-} , C^{00} ;
- TD CP asymmetries: S^{+-} , S^{00} ;
 - S^{00} reduces folding ambiguities
- Belle II will be able to measure all these observables
 - Final sensitivity $\sim 1^\circ$



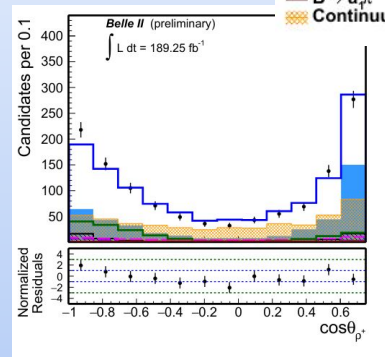
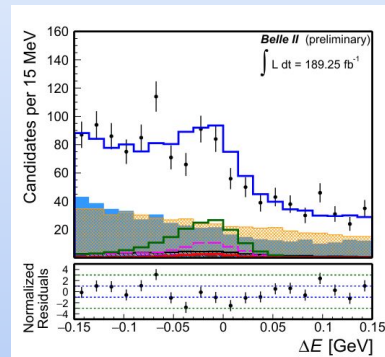
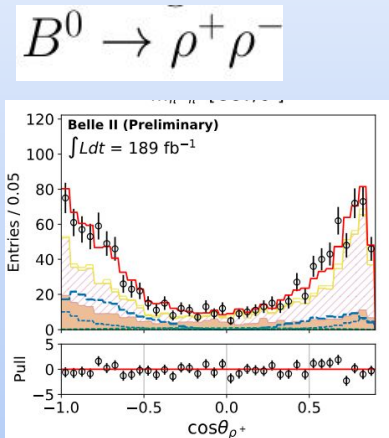
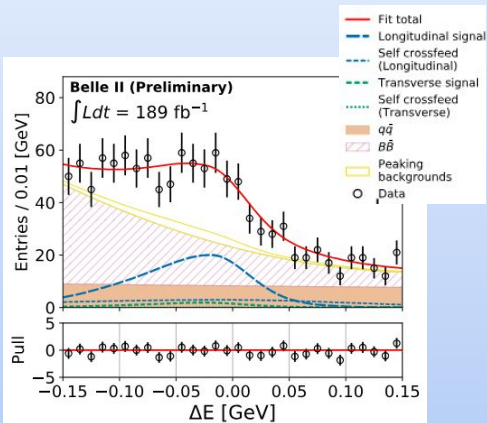
Toward ϕ_2/α : $B \rightarrow \rho\rho$

[arxiv:2208.03554](https://arxiv.org/abs/2208.03554)
[arxiv:2206.12362](https://arxiv.org/abs/2206.12362)



- Broad resonances of vector mesons, π^0 in final state
 - multiple non-negligible peaking background contributions
- CP analysis requires measurement of longitudinal polarization:
 - angular analysis using helicity angles of ρ 's

$$B^+ \rightarrow \rho^+ \rho^0$$



$$\begin{aligned} \mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) &= [2.67 \pm 0.28 (\text{stat}) \pm 0.28 (\text{syst})] \times 10^{-5}, \\ f_L &= 0.956 \pm 0.035 (\text{stat}) \pm 0.033 (\text{syst}), \end{aligned}$$

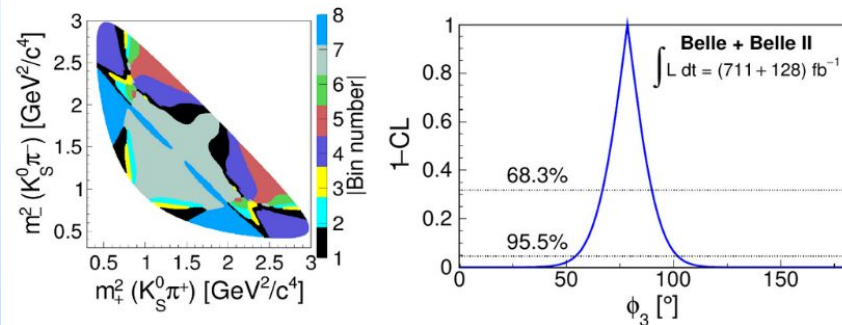
$$\mathcal{B}(B^+ \rightarrow \rho^+ \rho^0) = [23.2_{-2.1}^{+2.2} (\text{stat}) \pm 2.7 (\text{syst})] \times 10^{-6},$$

$$f_L = 0.943_{-0.033}^{+0.035} (\text{stat}) \pm 0.027 (\text{syst}),$$

$$\mathcal{A}_{CP} = -0.069 \pm 0.068 (\text{stat}) \pm 0.060 (\text{syst}).$$

- Best sensitivity from the BPGGSZ method, exploiting the interference in the $D^0 \rightarrow K_S \pi^+ \pi^-$ Dalitz plot:

J. Hikasa, [J. High Energ. Phys. 2022, 63 \(2022\)](#)



$$\begin{aligned} \phi_3 &= (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ, \\ r_B^{DK} &= 0.129 \pm 0.024 \pm 0.001 \pm 0.002, \\ \delta_B^{DK} &= (124.8 \pm 12.9 \pm 0.5 \pm 1.7)^\circ, \\ r_B^{D\pi} &= 0.017 \pm 0.006 \pm 0.001 \pm 0.001, \\ \delta_B^{D\pi} &= (341.0 \pm 17.0 \pm 1.2 \pm 2.6)^\circ. \end{aligned}$$

- GLW method [[Phys.Lett.B 253 \(1991\) 483-488](#), [Phys.Lett.B 265 \(1991\) 172-176](#)]: consider decays of the D^0 to odd (-) and even (+) CP eigenstates and measure the observables:

$$\mathcal{A}_{CP\pm} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)} \quad \mathcal{R}_{CP\pm} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{\text{flav}} K^-) + \mathcal{B}(B^+ \rightarrow D_{\text{flav}} K^+)}$$

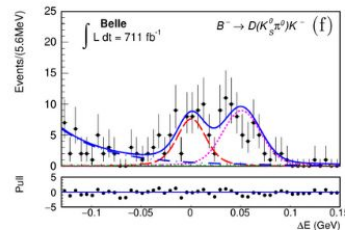
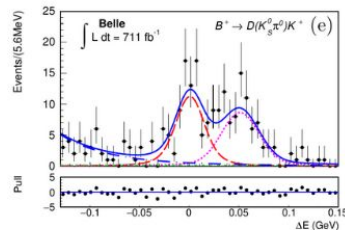
which are related to ϕ_3 :

$$\begin{aligned} \mathcal{R}_{CP\pm} &= 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \phi_3 \\ \mathcal{A}_{CP\pm} &= \pm 2r_B \sin \delta_B \sin \phi_3 / \mathcal{R}_{CP\pm} \end{aligned}$$

Belle/BelleII combined results on γ/ϕ_3

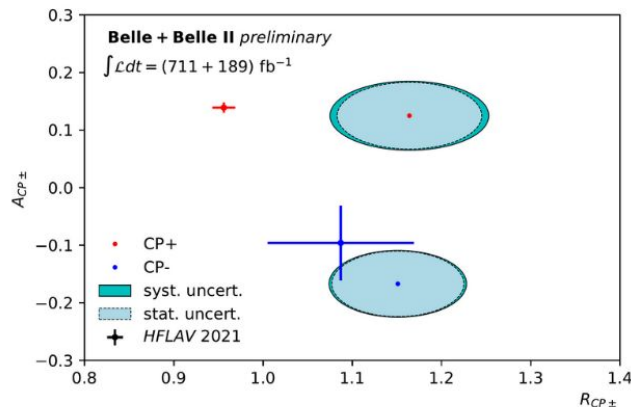
- Considering $D^0 \rightarrow K^+K^-$ as CP+, $D^0 \rightarrow K_S\pi^0$ as CP-, and $D^0 \rightarrow K^-\pi^+$ as flavor specific final state, we measure (on the Belle + Belle II data set):

$$\begin{aligned}\mathcal{R}_{CP+} &= 1.164 \pm 0.081 \pm 0.036, \\ \mathcal{R}_{CP-} &= 1.151 \pm 0.074 \pm 0.019, \\ \mathcal{A}_{CP+} &= (+12.5 \pm 5.8 \pm 1.4)\%, \\ \mathcal{A}_{CP-} &= (-16.7 \pm 5.7 \pm 0.6)\%.\end{aligned}$$



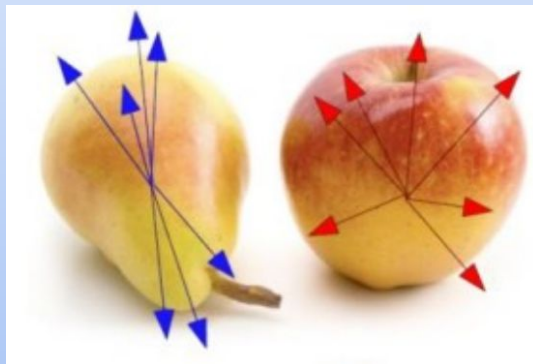
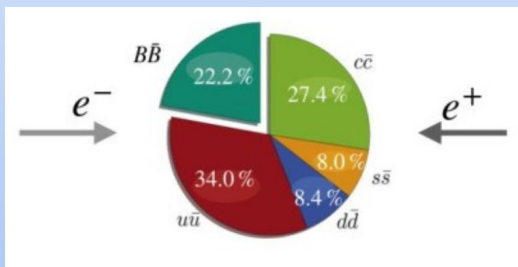
- The $\mathcal{A}_{CP}$'s differ from each other at $\sim 3.5\sigma$;
- This translates into constraints on ϕ_3 :

	68.3% CL	95.4% CL
ϕ_3 (°)	[8.7, 20.5] [83.8, 96.1] [163.4, 173.1]	[4.7, 175.8]
r_B	[0.282, 0.489]	[0.069, 0.560]



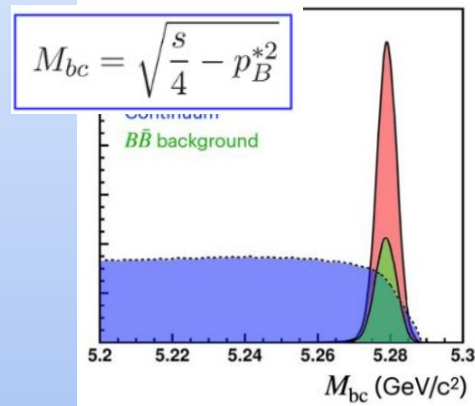
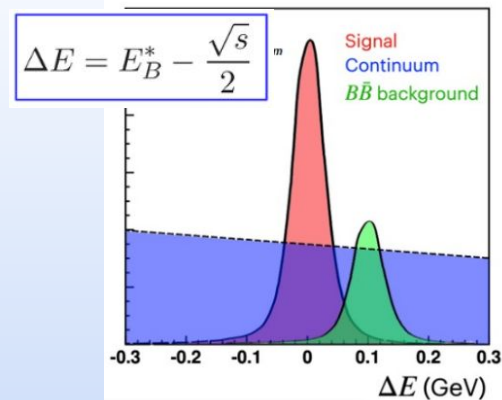
B-Factory variables

- Two key variables to discriminate fully reconstructed (hadronic) signal from background
 - Background from continuum ($q\bar{q}$ -bar) and from $B\bar{B}$
- Discrimination against continuum ($q\bar{q}$ -bar) background using event-shape variables via a multivariate classifier



$q\bar{q}$ events

$B\bar{B}$ events

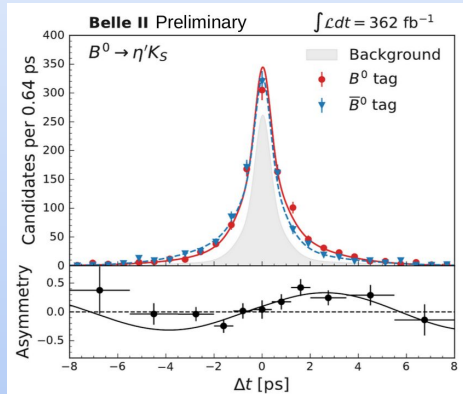


TDCPV in Charmless B decay



- $B \rightarrow \eta' K_S$
 - $\eta' \rightarrow \eta (\rightarrow \gamma\gamma) \pi^+ \pi^-$
 - $\eta' \rightarrow \rho \gamma$
- High $\mathcal{B}$, theoretically clean
 - ~800 signal events

[arXiv:2402.03713](https://arxiv.org/abs/2402.03713)

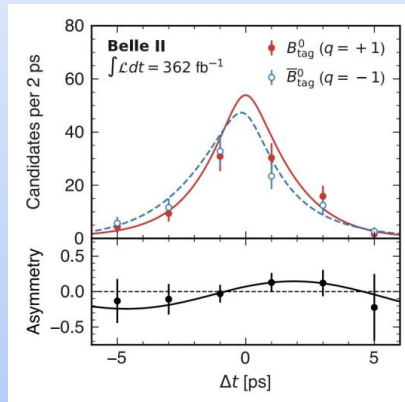


$$S = 0.67 \pm 0.10 \pm 0.04$$

$$C = -0.19 \pm 0.08 \pm 0.03$$

- $B \rightarrow \phi K_S$
 - ~160 signal events
- Challenge: non resonant background with opposite-CP
 - ~160 signal events

[PRD 108, 072012 \(2023\)](https://arxiv.org/abs/2403.02590)



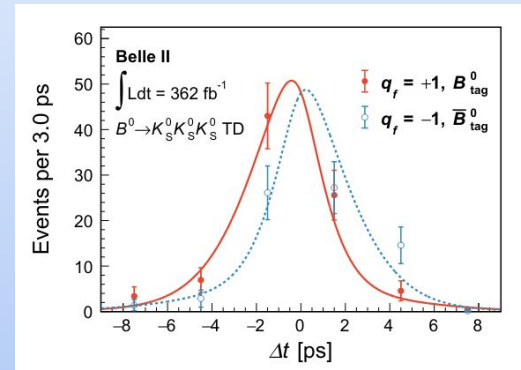
$$S = 0.54 \pm 0.26^{+0.06}_{-0.08}$$

$$C = -0.31 \pm 0.20 \pm 0.05$$

- $B \rightarrow K_S K_S K_S$
 - ~160 signal events
- Challenge: no prompt tracks from B vertex
 - Use $K_S \rightarrow \pi^+ \pi^-$ extrapolated to IP

[arXiv:2403.02590](https://arxiv.org/abs/2403.02590)

Accepted by PRD



$$S = -1.37^{+0.35}_{-0.45} \pm 0.03$$

$$C = -0.07 \pm 0.20 \pm 0.05$$

$\sin(2\phi_1/\beta)$ from $B \rightarrow J/\psi K_S$

arXiv:2402.17260
PRD 110 (2024), 12001



- Golden channel, almost background free
- Updated results using improved GFlaT flavour tagger
- Fit ΔE distribution to subtract background
- Fit background-subtracted Δt distribution to extract CPV parameters

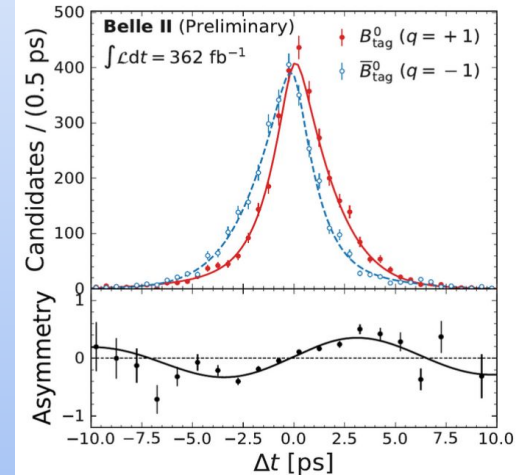
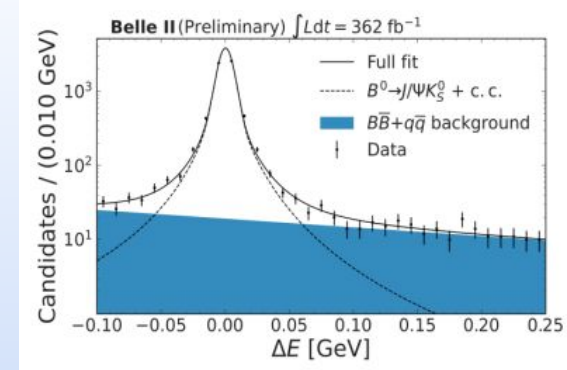
$$S = 0.724 \pm 0.035 \pm 0.014$$
$$C = -0.035 \pm 0.026 \pm 0.013$$

World average (K_S mode only):

$$S_{CP} = 0.695 \pm 0.019$$

$$A_{CP} = 0.000 \pm 0.020$$

- Statistical uncertainties **8%** smaller than with category-based Flavour Tagger

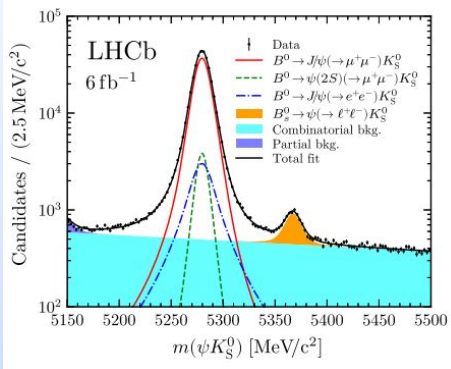


sin 2 β measurement @ LHCb

PRD 132 (2024), 0210801

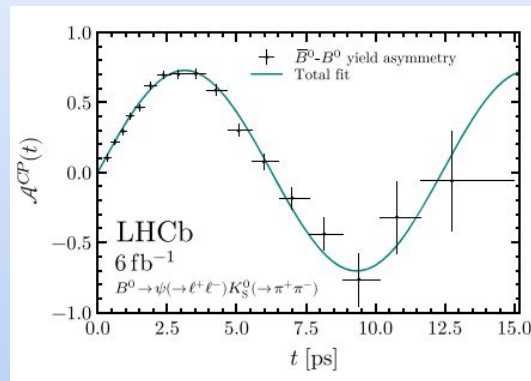
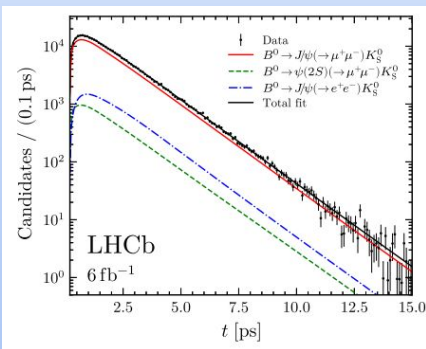


6 fb⁻¹ collected in Run2



Channel	$\epsilon_{\text{tag}}(\%)$	$\mathcal{D}^2(\%)$
$B^0 \rightarrow J/\psi(\rightarrow \mu^+\mu^-)K_S^0$	85.34 ± 0.05	4.661 ± 0.013
$B^0 \rightarrow J/\psi(\rightarrow e^+e^-)K_S^0$	92.20 ± 0.08	6.462 ± 0.032
$B^0 \rightarrow \psi(2S)(\rightarrow \mu^+\mu^-)K_S^0$	84.81 ± 0.15	4.59 ± 0.04

372 350 tagged events



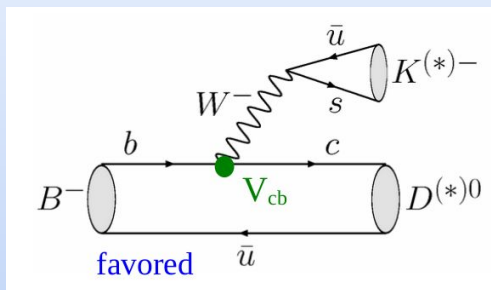
$$S_{\psi K_S^0}^{\text{Run 1\&2}} = 0.724 \pm 0.014(\text{stat} + \text{syst}),$$

$$C_{\psi K_S^0}^{\text{Run 1\&2}} = 0.004 \pm 0.012(\text{stat} + \text{syst}),$$

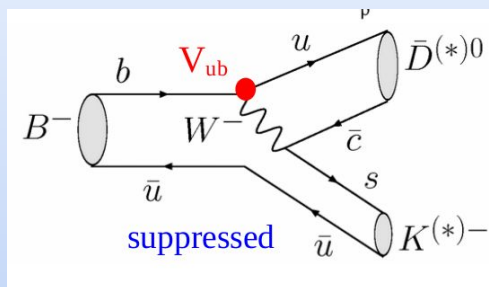
~60 fs time resolution

Results on γ/ϕ_3

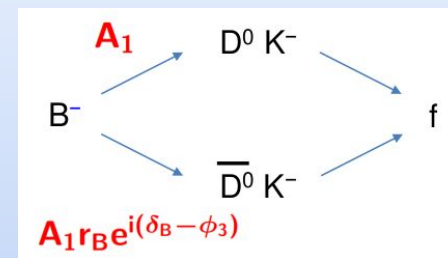
- γ/ϕ_3 from interference of tree level amplitudes:
 - Fundamental input of CKM UT fit
- ϕ_3 can be measured using interference $B \rightarrow DK$ and $B \rightarrow \bar{D}K$ (or D^*K^* , $D\pi$)



$$B^- \rightarrow D^0 K^- \approx V_{cb} V_{us}^* A_1$$



$$B^- \rightarrow \bar{D}^0 K^- \approx V_{ub} V_{cs}^* A_1 r_B e^{i(\delta_B - \phi_3)}$$



- Amplitude ratio r_B and strong phase δ_B are mode-dependent

- Several methods used

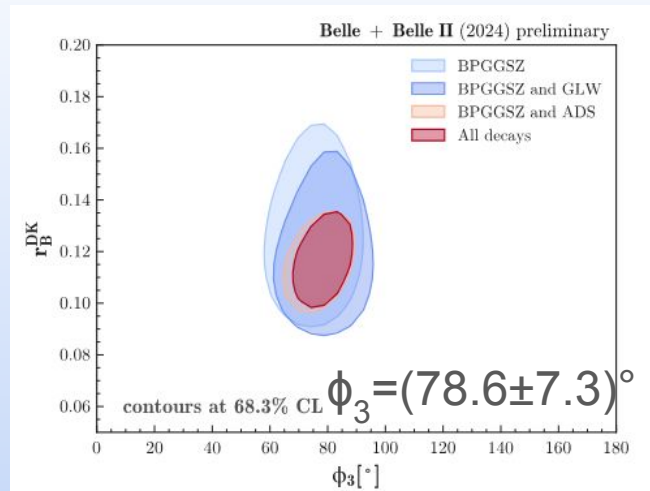
- GLW $B^\pm \rightarrow D^0_{CP} K^\pm$ [arXiv:2308.05048 \[hep-ex\]](https://arxiv.org/abs/2308.05048)
 - Use CP eigenstate of D meson
- ADS [PRL 78 \(1997\) 3257](https://arxiv.org/abs/1907.03257)
 - Enhancement of CP violation by using doubly Cabibbo suppressed decays.
- BPGGSZ $D^0 \rightarrow K_S h^+ h^-$ [JHEP 2022\(2022\). 63](https://arxiv.org/abs/2202.063)
 - Different amplitude and strong phase in different region of Dalitz plot.
- GLS $D^0 \rightarrow K_S K\pi$ [JHEP 09\(2023\)146](https://arxiv.org/abs/2309.146)

- D-decay strong phase from CLEO-c & BESIII

- Need improvement by BESIII

LHCb: $\phi_3 = (64.6 \pm 2.8)^\circ$ [LHCb-CONF-2024-004](https://arxiv.org/abs/2404.004)

Few ab^{-1} needed for a meaningful comparison



- Likelihood with 60 input observables
 - including 15 auxiliary inputs (D-decay)
 - 16 free parameters
- $r_B(\delta_B)$ with little high-fluctuation
 - Worse precision with WA values

Belle + Belle II Combined γ/ϕ_3

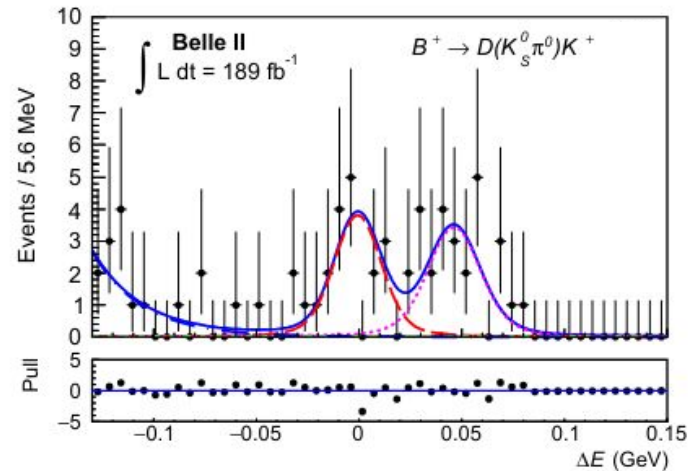
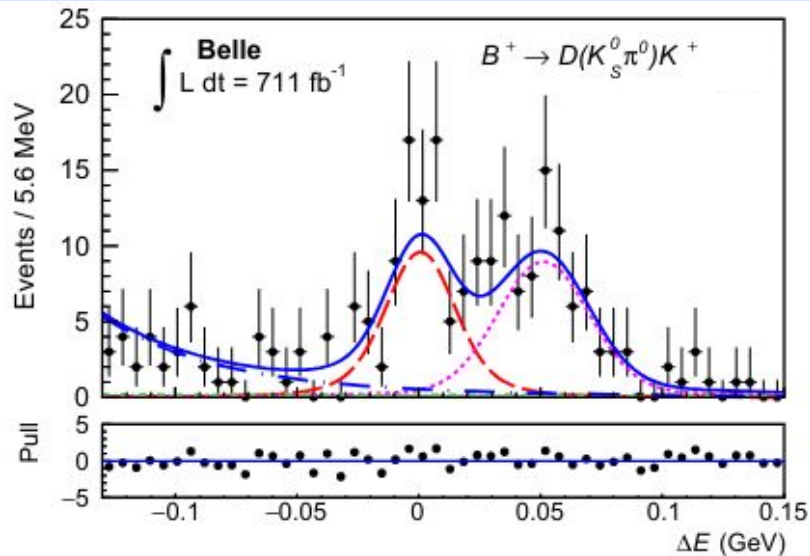
arXiv:2308.05048
Belle II 189 fb⁻¹



• Example:

- $B^\pm \rightarrow D_{CP} K^\pm$ (GLW)
- CP-odd $D_{CP} \rightarrow K_S \pi^0$: only in Belle(II)
- Combined Belle and BelleII analysis

B decay	D decay	Method	Data set (Belle + Belle II) [fb ⁻¹]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^0, K^- K^+$	GLW	711 + 189
$B^+ \rightarrow Dh^+$	$D \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 K^- \pi^+$	GLS	711 + 362
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \rightarrow K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega,$ $K^- K^+, \pi^- \pi^+$	GLW	210 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \gamma, D \rightarrow K_S^0 \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0



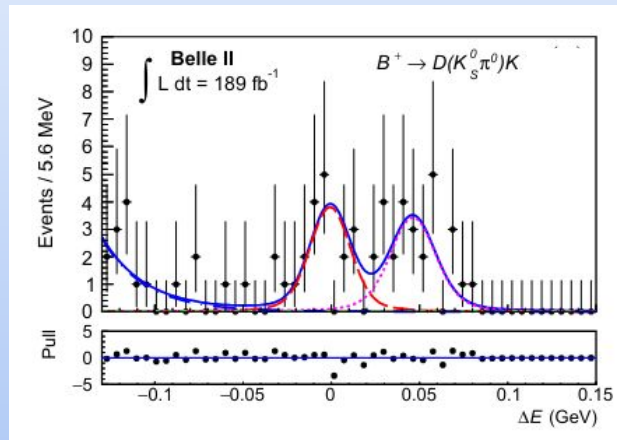
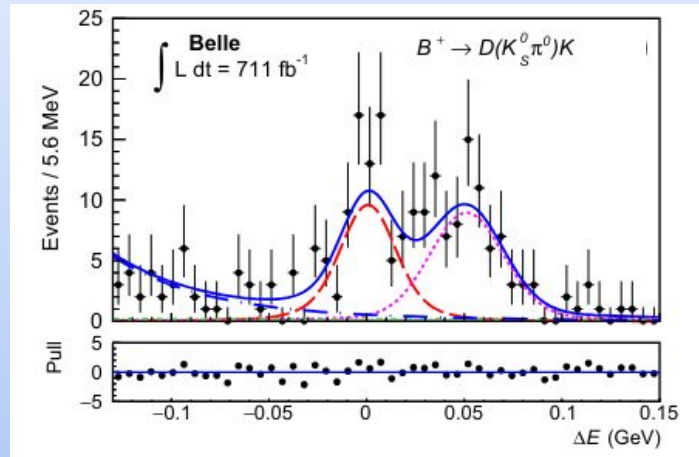
Belle + Belle II Combined γ/ϕ_3

arXiv:2308.05048
Belle II 189 fb⁻¹



- An example (not TD)
 - $B^\pm \rightarrow D_{CP} K^\pm$ (GLW)
 - CP-odd $D_{CP} \rightarrow K_S \pi^0$: only in Belle(II)
 - Combined Belle and BelleII analysis

B decay	D decay	Method	Data set (Belle + Belle II) [fb ⁻¹]
$B^+ \rightarrow D h^+$	$D \rightarrow K_S^0 \pi^0, K^- K^+$	GLW	711 + 189
$B^+ \rightarrow D h^+$	$D \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0
$B^+ \rightarrow D h^+$	$D \rightarrow K_S^0 K^- \pi^+$	GLS	711 + 362
$B^+ \rightarrow D h^+$	$D \rightarrow K_S^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128
$B^+ \rightarrow D h^+$	$D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \rightarrow K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega,$ $K^- K^+, \pi^- \pi^+$	GLW	210 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \gamma, D \rightarrow K_S^0 \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0



Combinazione $\phi_3 = (78.6 \pm 7.3)^\circ$ [JHEP 10 2024, 143 \(2024\)](#)

Few ab⁻¹ needed for a meaningful comparison with LHCb results

Experiment Assumed data sample	ATLAS 20.3-99.7 fb ⁻¹	CMS 116-140 fb ⁻¹	LHCb 2-9 fb ⁻¹	Belle II 364-1075 fb ⁻¹
CKM angles				
β	—	—	0.57° [15]	1.2° [16]
α	—	—	—	6.6° [17]
γ	—	—	2.8° [18]	13° [17]
ϕ_s [mrad]	42 [19]	23 [20]	20 [21]	—
<i>CP</i> violation in loop-dominated decays				
$S(B^0 \rightarrow \eta' K_S^0)$	—	—	—	0.087 [17]
$\phi_s(B_s^0 \rightarrow \phi\phi)$ [mrad]	—	—	69 [22]	—
$\phi_s(B_s^0 \rightarrow K^{*0}\bar{K}^{*0})$ [mrad]	—	—	130 [23]	—