



开放量子系统的退相干与重整化群

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复旦大学

第四届高能物理理论与实验融合发展研讨会

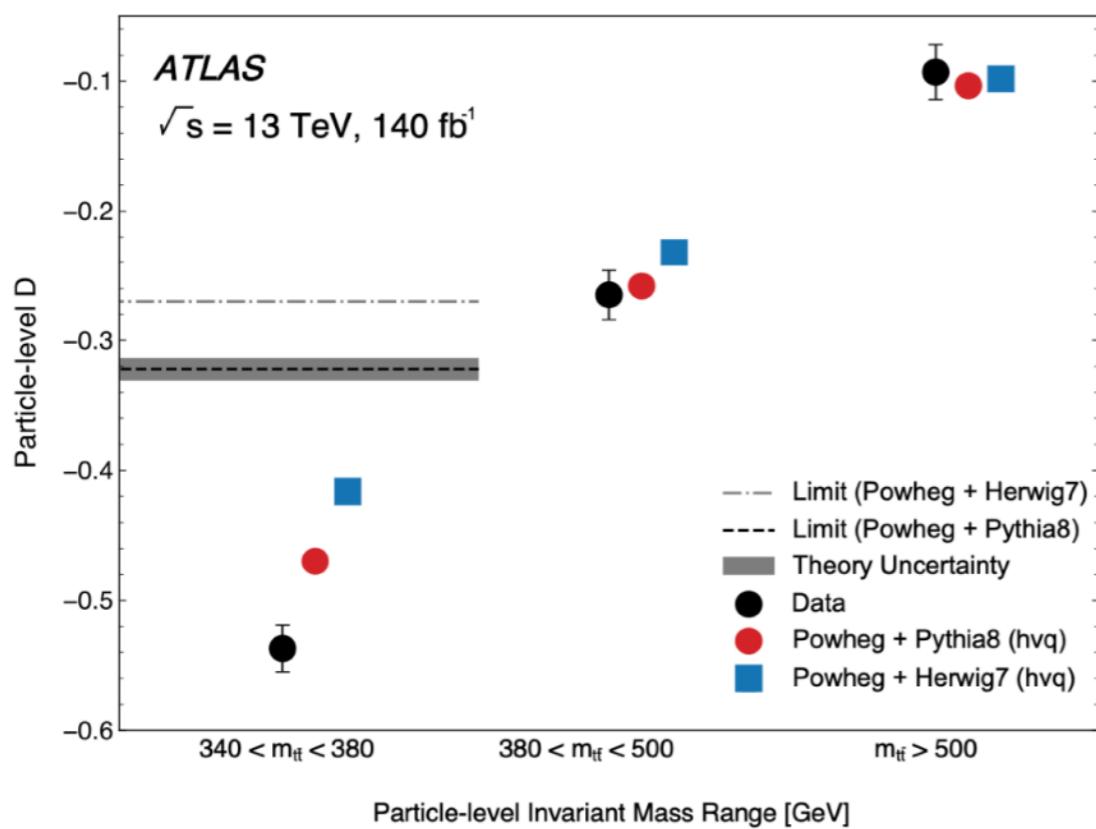
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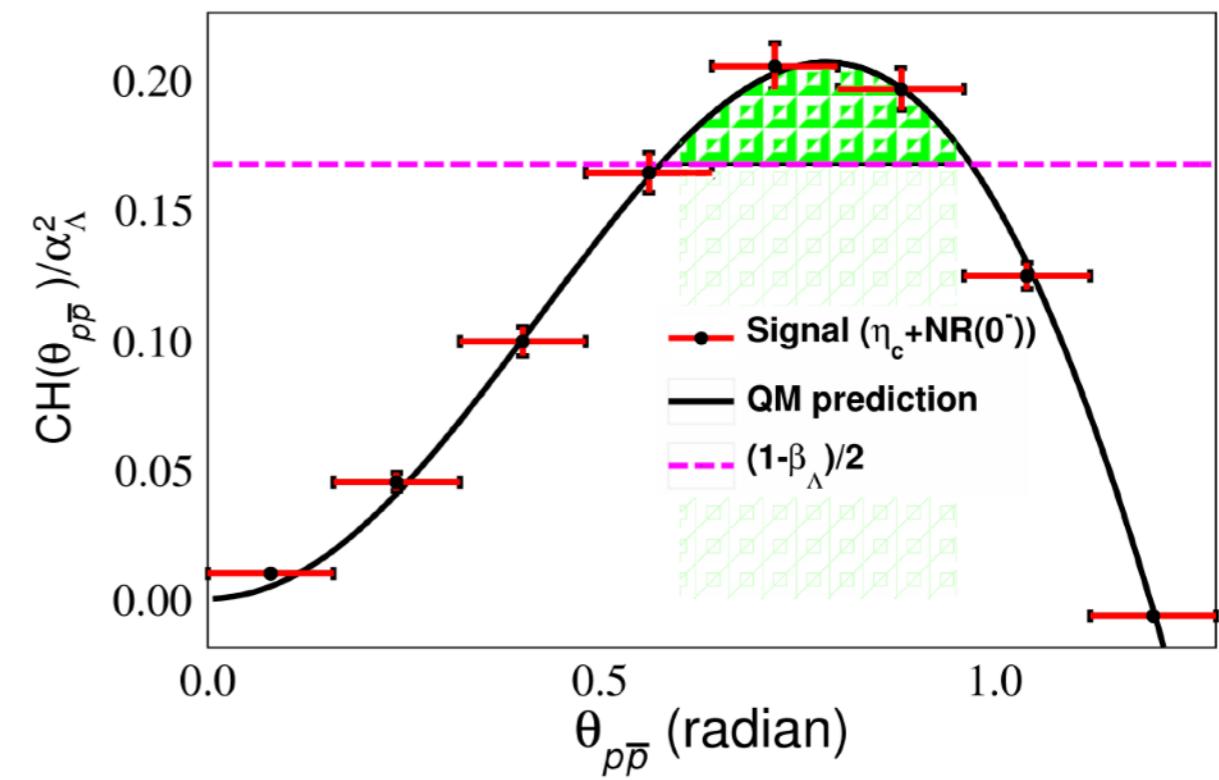
Quantum information science meets high energy physics

- The study of quantum information in high-energy collider physics is rapidly transitioning from a theoretical curiosity to an experimental reality. “Quantum Information meets High-Energy Physics: Input to the update of the European Strategy for Particle Physics”— A recent review 2504.00086
- Recent breakthroughs, such as the observation of spin entanglement in top-quark pairs, have established particle colliders as novel laboratories for studying quantum mechanics at unprecedented energy scales.

See Li and Yan's talks



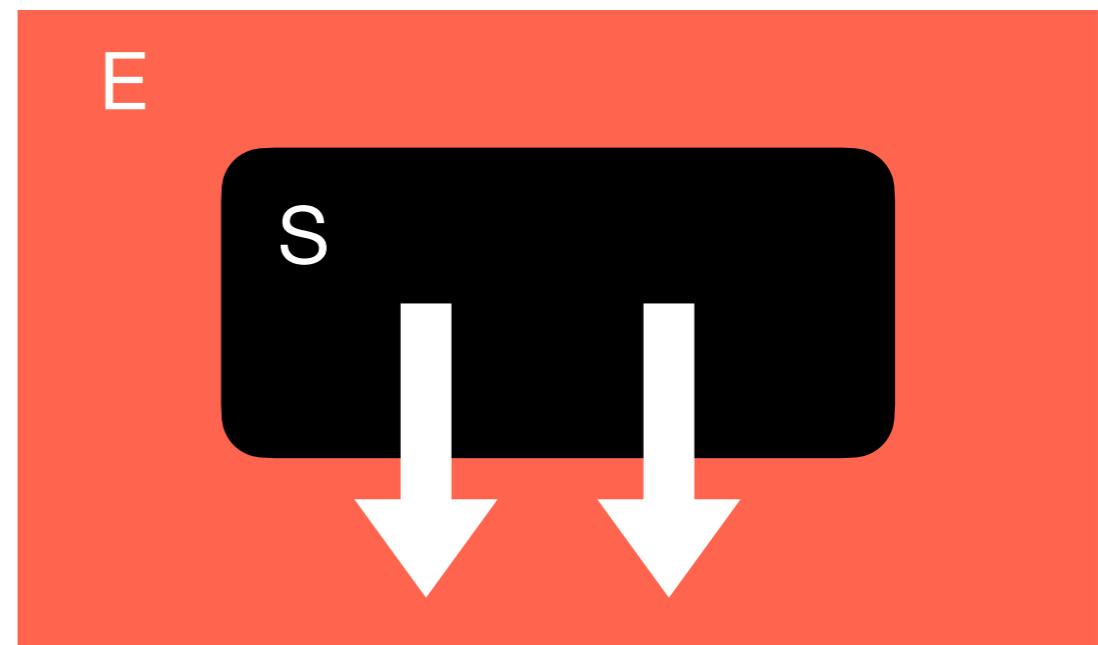
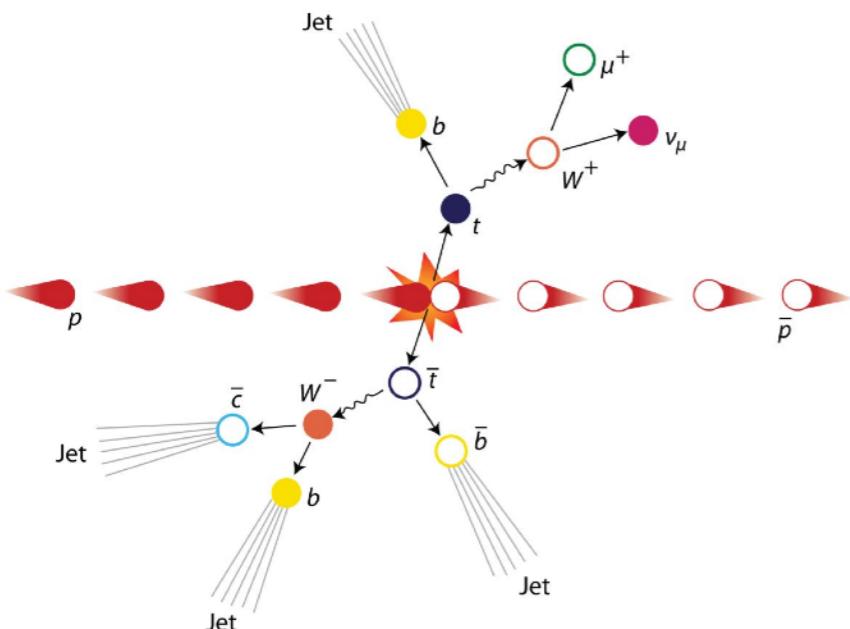
ATLAS Nature 2024



BESIII Nature Communications 2025

Decoherence in high energy collisions

- We assume QFT is the underlying description and do not address debates concerning tests of local hidden variable theories at colliders Li, Shen, Yang '24; Bechtle, Breuning, Dreiner, Duhr '25; Abel, Dreiner, Sengupta, Ubaldi '25 ...
- In the above measurements at the LHC, entangled top quark pairs can not be treated as a **closed system**
- Top quarks may radiate gluons or photons in the short period of time before decaying, leading to a reduction in quantum spin information, i.e., **decoherence**.
- Decoherence can be studied by recognizing that realistic quantum systems are always embedded in some environment.
- This interaction with the system results in ‘leakage of information’ to the environment, **decreasing the entanglement between the components of the system**.



Some decoherence effects in open system

- **K0 K0bar system (Bertlmann '04) $\Lambda \Lambda\bar{b}$ ar system (Wu, Qian, Yang, Wang '24)**
- **“Infrared quantum information” Soft radiation decrease momentum entanglement (Carney, Chaurette, Neuenfeld, Semenof '17)**
- **Decoherence and precision calculation (Aoude, Barr, Maltoni, Satrioni '25)**
- **Decoherence and renormalization group flow (Lin, Liu, DYS, Wei '25, Gu, Lin, DYS, Yang, Wang in progress)**
- **Decoherence and decoupling in effective field theory (Burgess, Colas , Holman, Kaplanek '25)**
- **Black hole horizons decohere superpositions (Biggs, Maldacena '24)**

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Open Quantum Systems: Dissipative Dynamics from Quarks to the Cosmos
December 1, 2025 - December 12, 2025

ORGANIZERS

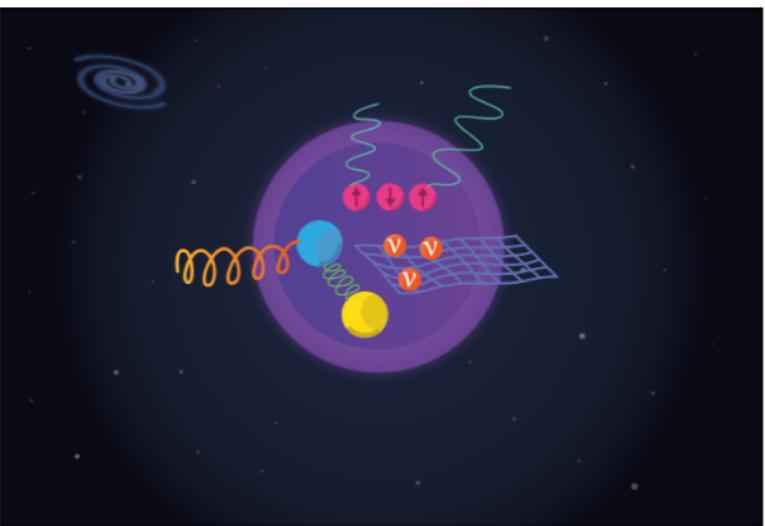
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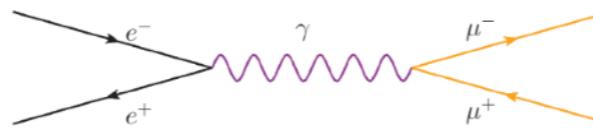
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The application deadline for this event has passed.

Concurrence at LO (closed system)

- Consider QED process $e^+e^- \rightarrow f\bar{f}$



- The spin state of a lepton pair can be characterized by a two-qubit density operator

$$\hat{\rho} = \frac{1}{4} (\hat{I}_2 \otimes \hat{I}_2 + B_i^+ \hat{\sigma}_i \otimes \hat{I}_2 + B_i^- \hat{I}_2 \otimes \hat{\sigma}_i + C_{ij} \hat{\sigma}_i \otimes \hat{\sigma}_j)$$

↑
Spin correlation matrix

- At the LO

$$\rho_{\text{LO}} = \frac{1}{4} \left(\hat{I}_2 \otimes \hat{I}_2 + \frac{\sin^2 \theta}{1 + \cos^2 \theta} \hat{\sigma}_1 \otimes \hat{\sigma}_1 + \frac{\sin^2 \theta}{1 + \cos^2 \theta} \hat{\sigma}_2 \otimes \hat{\sigma}_2 - \hat{\sigma}_3 \otimes \hat{\sigma}_3 \right)$$

- To probe entanglement, one can calculate the concurrence C

$$C[\rho_{\text{LO}}] = \frac{\sin^2 \theta}{1 + \cos^2 \theta}$$

- Maximum entanglement $\cos \theta = 0$

$$C[\rho_{\text{LO}}] = 1$$

$$\frac{1}{\sqrt{2}}(|+-\rangle + |-+\rangle)$$

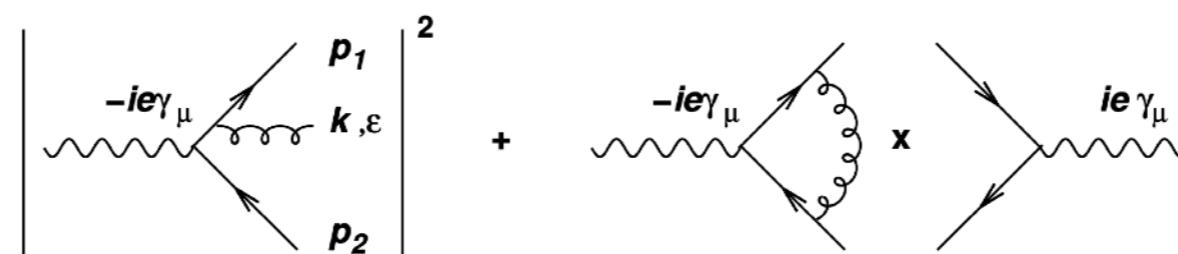
Quantum maps for open systems and perturbative calculation

Aoude, Barr, Maltoni, Satrioni '25

- The evolution of an open system can be represented by a quantum map (channel)

$$\mathcal{E}[\rho] = \sum_j K_j \rho K_j^\dagger, \quad \sum_j K_j^\dagger K_j = \mathbb{1},$$

Kraus operators: Kraus representation theorem



- The virtual corrections lead to the same final state Hilbert space while the real emission leads to the extra Hilbert space of the environment.
- To obtain the reduced density matrix, we need to trace over the emitted radiation

$$\rho_{\text{LO+NLO}}^{\text{red}} = p_{\text{LO}} \mathbb{1} \rho_{\text{LO}} \mathbb{1} + \bar{\mathcal{E}}_V[\rho_{\text{LO}}] + \bar{\mathcal{E}}_R[\rho_{\text{LO}}]$$

$$\bar{\mathcal{E}}_V[\rho_{\text{LO}}] = p_V \mathbb{1} \rho_{\text{LO}} \mathbb{1}$$

Virtual

$$\bar{\mathcal{E}}_R[\rho_{\text{LO}}] = \sum_j K_j \rho_{\text{LO}} K_j^\dagger$$

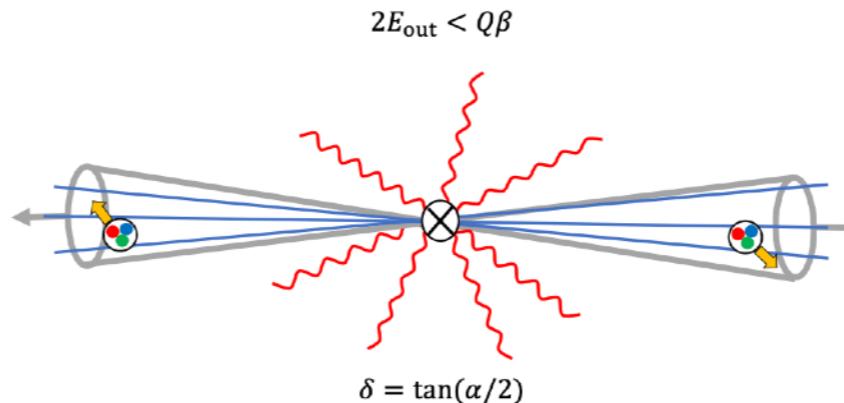
Real: hard, collinear, soft

Effective field theory for decoherence

J.Y. Gu, S.J. Lin (林士佳), DYS, L.T. Wang, S.X. Yang (杨斯翔) 2509.XXXXX

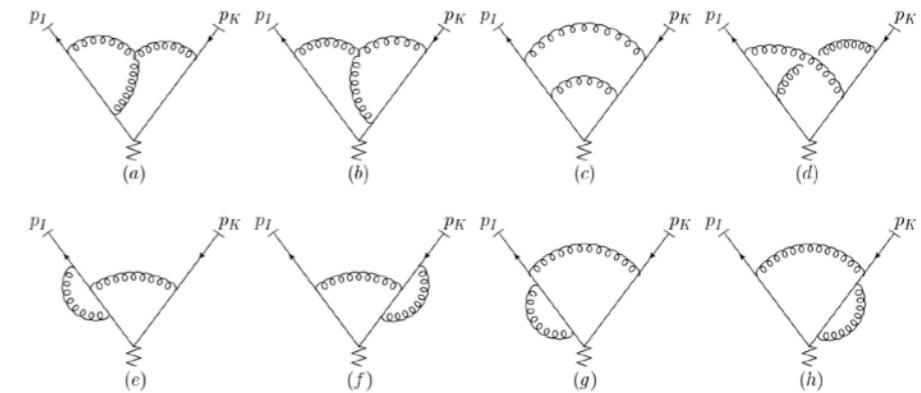
- Radiation should be considered **unresolvable** if either **soft** or **collinear**
- We introduce the energy and angular resolution parameters, which is similar to Sterman-Weinberg cone jet definition (Sterman, Weinberg '77)

Two fermion events:



- We apply soft collinear effective theory (SCET) + Jet Effective Theory (JET) (Becher, Neubert, Rothen, DYS '16 PRL)
- The initial spin state generated by the short-distance hard scattering $\hat{\rho}_{\text{hard}}(Q, \mu)$
- Apply a standard multiplicative renormalization scheme to regularize both UV and IR divergences

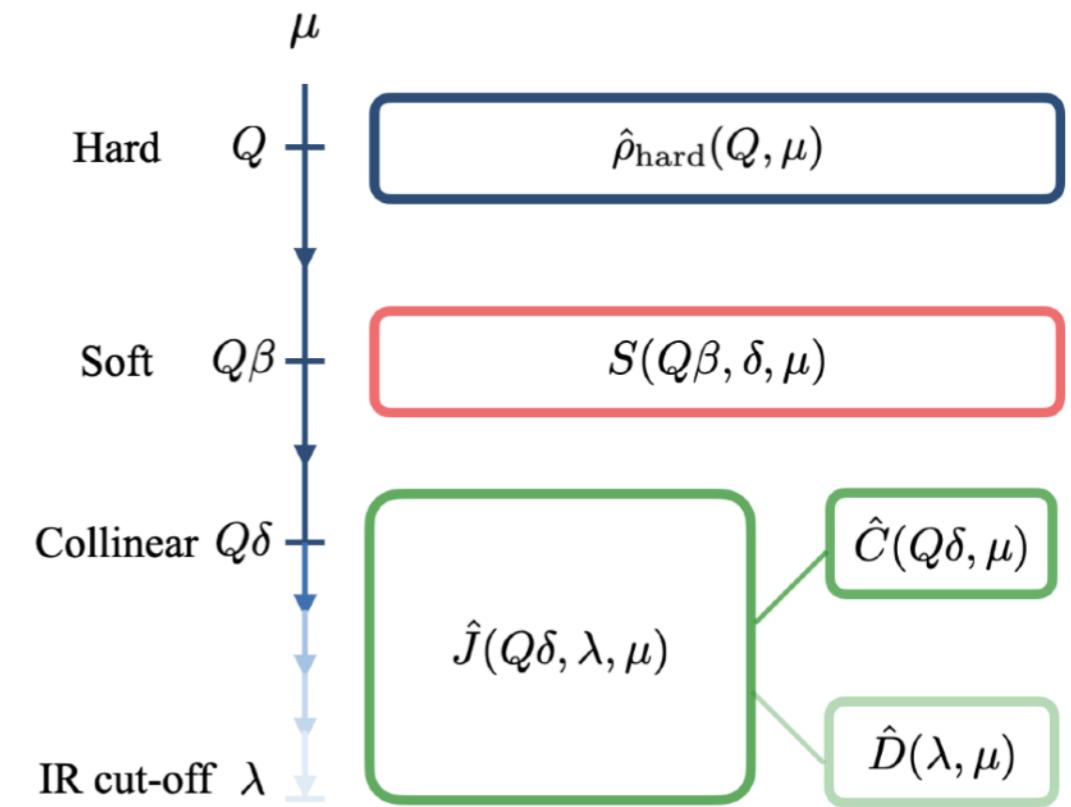
$$\hat{\rho}_{\text{hard}}(Q, \mu) = \frac{1}{4} \left(\hat{I} \otimes \hat{I} + P_i^+ \hat{\sigma}_i \otimes \hat{I} + P_j^- \hat{I} \otimes \hat{\sigma}_j + C_{ij} \hat{\sigma}_i \otimes \hat{\sigma}_j \right)$$



Factorization of the density operator

- This jet definition allows us to apply the factorization theorems of SCET
- Soft function **S** accounts for large-angle soft radiation. At the leading power, soft emissions are spin-independent and thus **do not induce decoherence**
- The fragmenting jet operators **J_f** project the hard scattering state onto the Hilbert space of the observed particles. This effectively traces over unobserved collinear radiation, and **induces decoherence**

$$\sum_X \langle 0 | \psi | fX \rangle \langle fX | \bar{\psi} | 0 \rangle$$



Spin decomposition

$$\hat{J}_f = \mathcal{J}_f^U \hat{I} \otimes \hat{I} + \mathcal{J}_f^L \hat{\sigma}_z \otimes \hat{\sigma}_z + \mathcal{J}_f^T (\hat{\sigma}_x \otimes \hat{\sigma}_x + \hat{\sigma}_y \otimes \hat{\sigma}_y)$$

- J^U : unpolarized
- J^L : longitudinal polarized
- J^T : transverse polarized

Factorization of the density operator

- Refactorization via an operator product expansion

$$\hat{J}(Q\delta, \lambda, \mu) = \hat{C}(Q\delta, \mu) \hat{D}(\lambda, \mu)$$

Fragmentation operator

- Define a scale-dependent effective production matrix

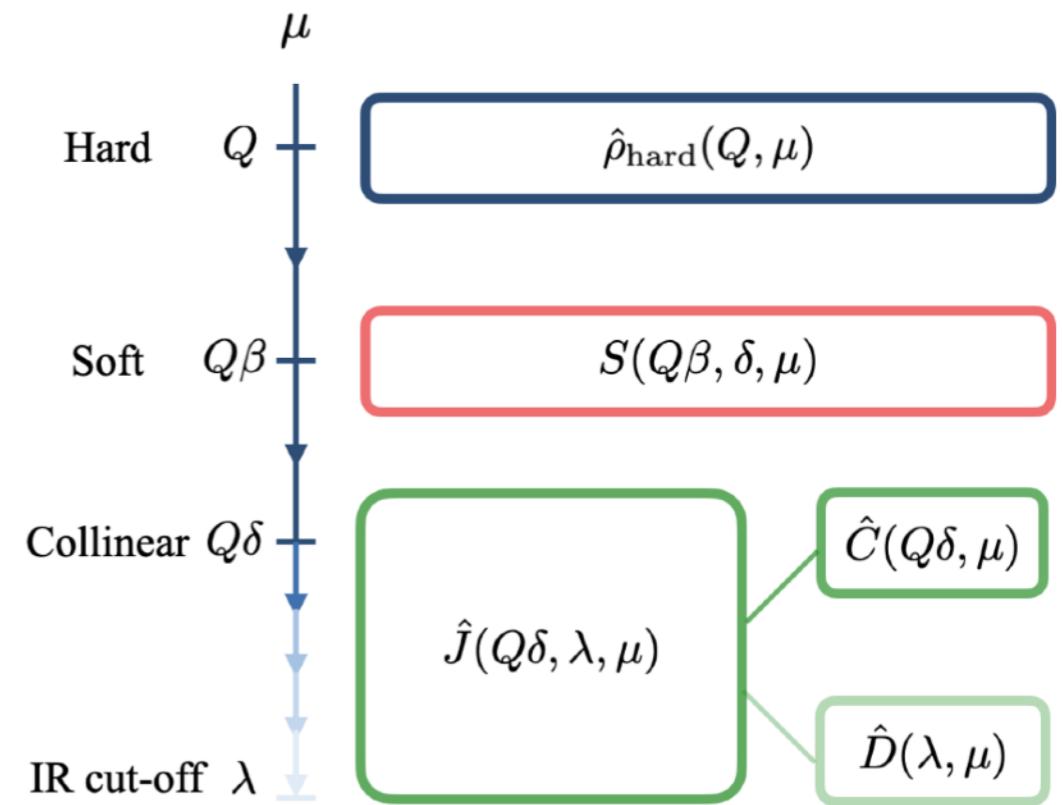
$$\hat{R}_{\text{eff}}(\mu) \equiv S(Q\beta, \delta, \mu) \hat{C}_f(Q\delta, \mu) \hat{R}_{\text{hard}}(Q, \mu) \hat{C}_{\bar{f}}(Q\delta, \mu)$$

- Renormalization group eqn $t \equiv \log(Q\delta/\mu)$

$$\hat{R}_{\text{eff}}(t) = \hat{U}_f(t, 0) \hat{R}_{\text{eff}}(0) \hat{U}_{\bar{f}}(t, 0)$$

$$U^{\mathcal{P}}(t, 0) = \exp \left(\int_0^t dt \gamma^{\mathcal{P}} \right)$$

$\gamma^{\mathcal{P}} \equiv \frac{\alpha}{\pi} P_{ff}^{\mathcal{P}}$ 1st Mellin moment of splitting function



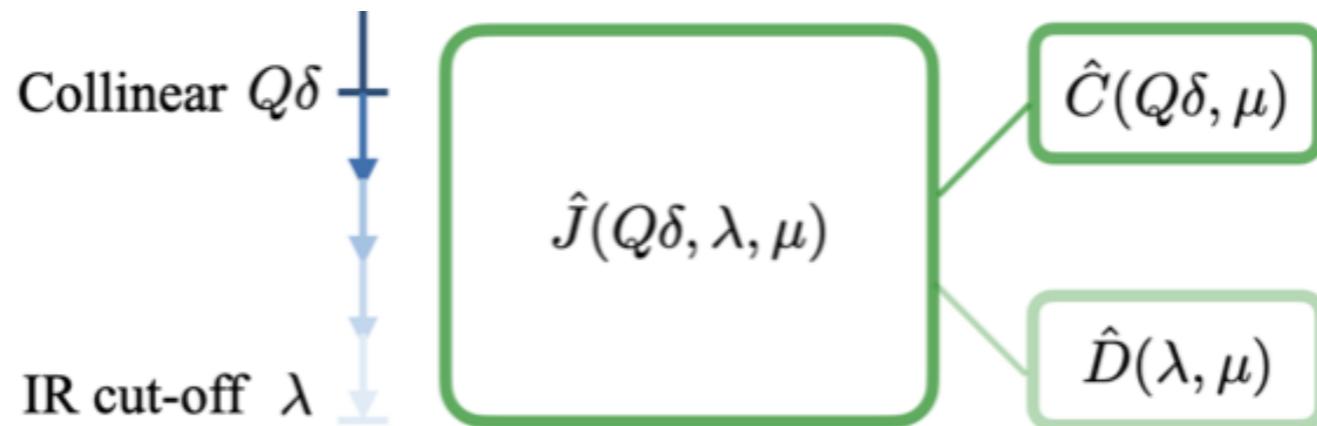
decoherence = RG flow
 anomalous dimensions determine
 the information loss

Measurement operator

- The final stage of the process is the projection of the evolved spin state onto a definite experimental outcome
- Define spin-dependent measurement operators $\hat{M}_f(\mathbf{S}_f) \equiv \hat{D}_f \hat{P}_f$

$$d\sigma(\mathbf{S}_f, \mathbf{S}_{\bar{f}}) \propto \text{Tr} \left[\hat{M}_f(\mathbf{S}_f, t) \hat{R}_{\text{eff}}(t) \hat{M}_{\bar{f}}(\mathbf{S}_{\bar{f}}, t) \right]$$

- Physics at different scales separated
 - Decoherence from collinear radiation are encapsulated in the RGE of the effective density matrix
 - Infrared physics of the final-state projection is contained entirely within the measurement operators (e.g. fragmentation function in QCD)



Kraus operator and Lindblad master equation

- We use QED as an example: IR cut-off = lepton mass $\lambda = m$
- The Kraus operators in QED

$$\hat{K}_{(i,j)} = \hat{K}_i^{\ell^-} \otimes \hat{K}_j^{\ell^+}$$

$$\hat{K}_0^{\ell^-} = \hat{K}_0^{\ell^+} = \sqrt{1 - p^2} \mathbb{I},$$

$$\hat{K}_1^{\ell^-} = \hat{K}_1^{\ell^+} = p \hat{\sigma}_3, \quad p = \sqrt{\frac{1}{2} \left[1 - \exp \left(-\frac{\alpha}{2\pi} t \right) \right]}$$

- Lindblad equation and jump operator

$$\frac{d\hat{\rho}_{\text{eff}}}{dt} = -\frac{\alpha}{2\pi} \hat{\rho}_{\text{eff}} + \frac{\alpha}{4\pi} [(\hat{\sigma}_3 \otimes \mathbb{I}) \hat{\rho}_{\text{eff}} (\hat{\sigma}_3 \otimes \mathbb{I}) + (\mathbb{I} \otimes \hat{\sigma}_3) \hat{\rho}_{\text{eff}} (\mathbb{I} \otimes \hat{\sigma}_3)]$$

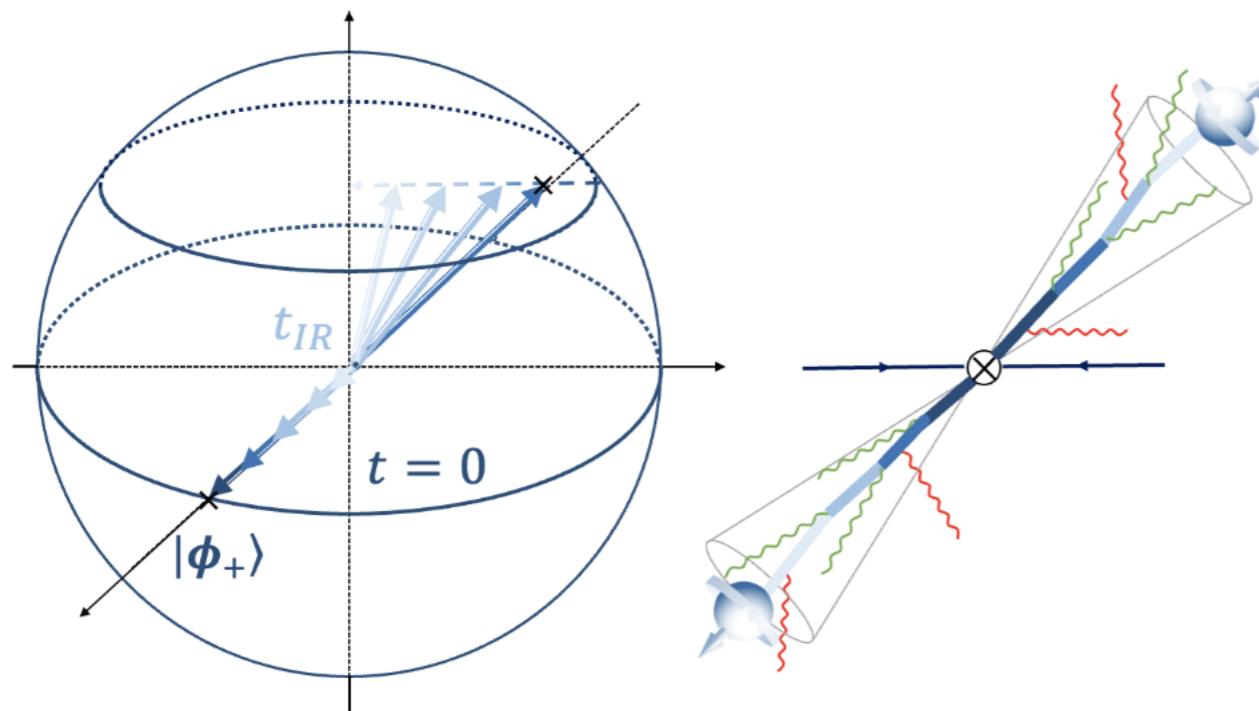
$$\hat{L}_1 = \sqrt{\alpha/4\pi} \hat{\sigma}_3 \otimes \mathbb{I} \quad \hat{L}_2 = \sqrt{\alpha/4\pi} \mathbb{I} \otimes \hat{\sigma}_3$$

- Quantum trajectory interpretation: each "jump" corresponds to an unresolved collinear photon emission from either of the fermion legs, which induces a stochastic **phase-flip**
- Decay of all off-diagonal terms

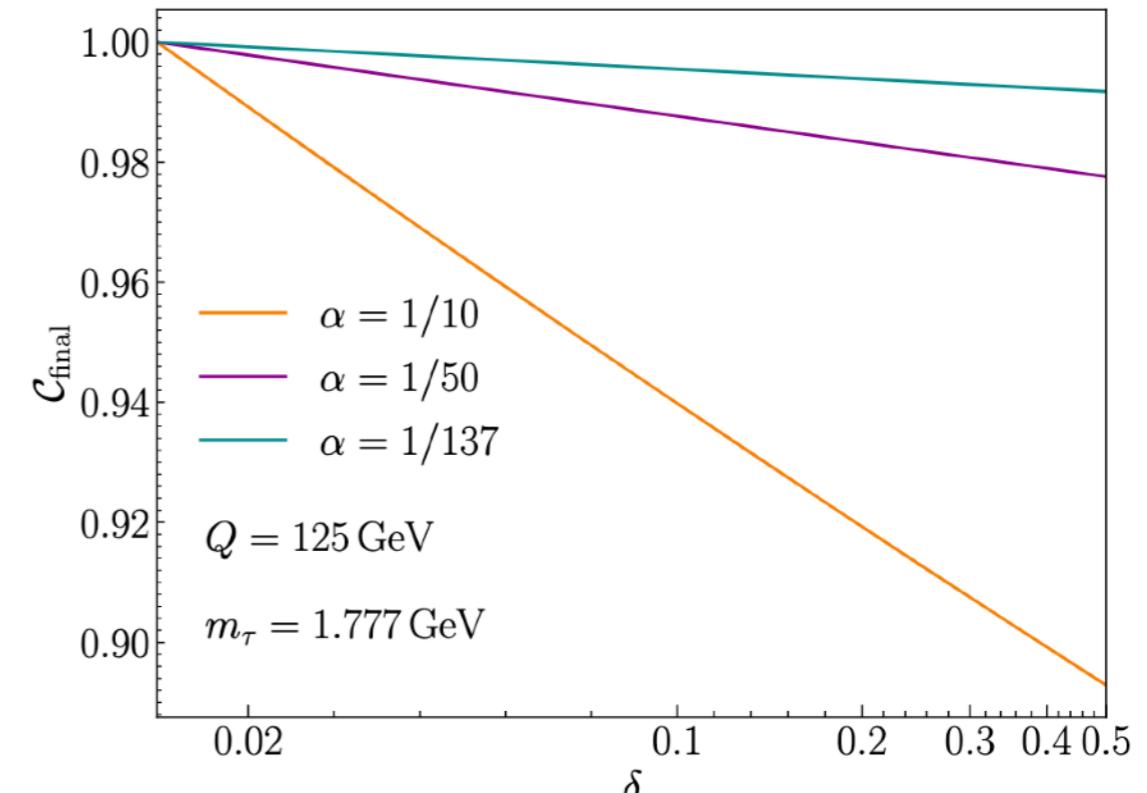
$$\frac{\hat{\rho}_{\text{eff}}^{ij}(t)}{\hat{\rho}_{\text{eff}}^{ij}(0)} = \begin{cases} 1 & i = j \text{ (diagonal),} \\ e^{-\frac{\alpha}{\pi}t} & ij = 14, 23, 32, 41 \text{ (anti-diagonal),} \\ e^{-\frac{\alpha}{2\pi}t} & \text{else.} \end{cases}$$

RG flow as a phase-flip channel

- Concurrence in QED $\mathcal{C}(t) = \mathcal{C}(0)e^{-\frac{\alpha}{\pi}t}$



$$|\phi_+\rangle = (\left|+-\right\rangle + \left|-\right.\left.+\right\rangle)/\sqrt{2}$$



- The concurrence after passage through a two-sided channel is bounded

$$C[(\$_1 \otimes \$_2) \rho_0] \leq C[(\$_1 \otimes \mathbb{1}) |\phi^+\rangle \langle \phi^+|] C[(\mathbb{1} \otimes \$_2) |\phi^+\rangle \langle \phi^+|] C(\rho_0)$$

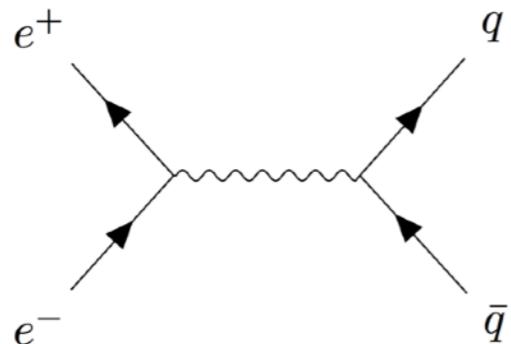
Konrad *et.al.* Nature Physics 2007

- For the most general case, we have an **inequality**

$$\mathcal{C}_{\text{final}} \leq \mathcal{C}(0) \left(\frac{Q\delta}{m} \right)^{-\frac{\alpha}{\pi}}$$

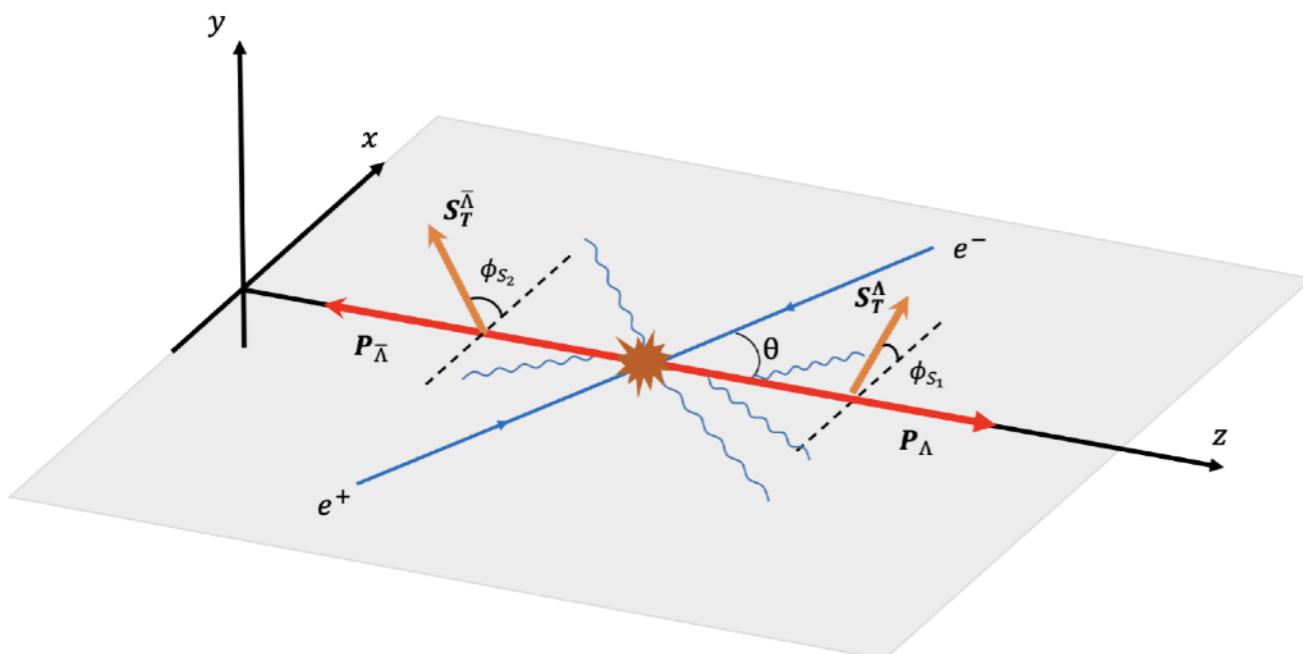
Spin correlation in Λ pair production with a thrust cut

S.J. Lin (林士佳), M.J. Liu (刘铭钧), DYS, S.Y. Wei '25



Bell variable
Parton-level

$$\mathcal{B}_+^{q\bar{q}} = \frac{2 \sin^2 \theta}{1 + \cos^2 \theta}$$



Bell variable
Hadron-level

$$\mathcal{B}_+^{\Lambda\bar{\Lambda}} = \frac{2 d\sigma^T}{d\sigma^U}$$

Parton model:

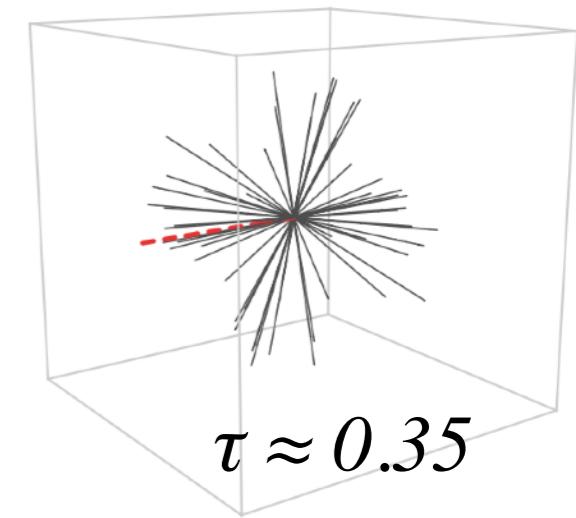
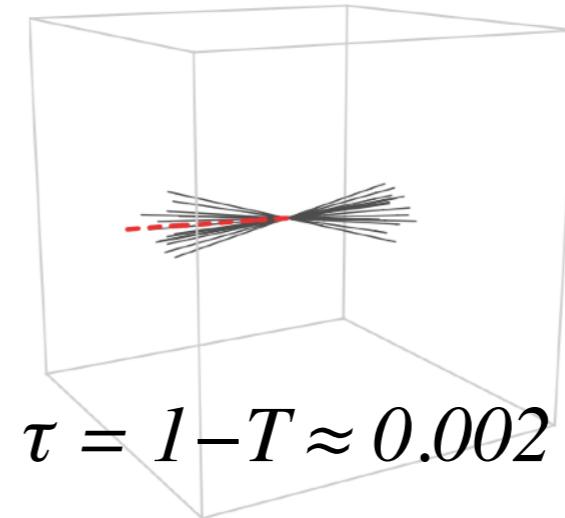
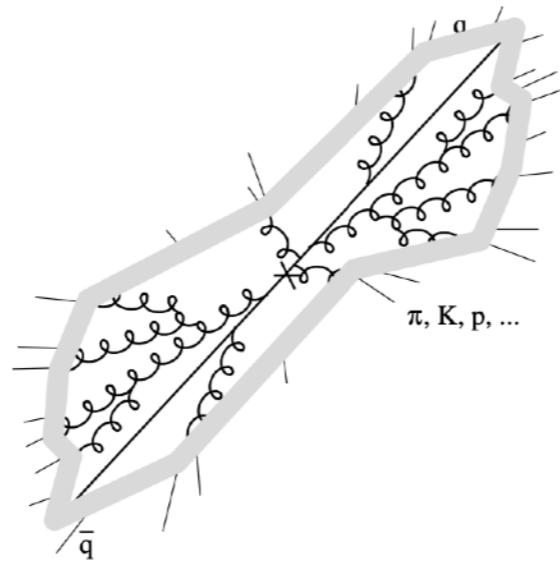
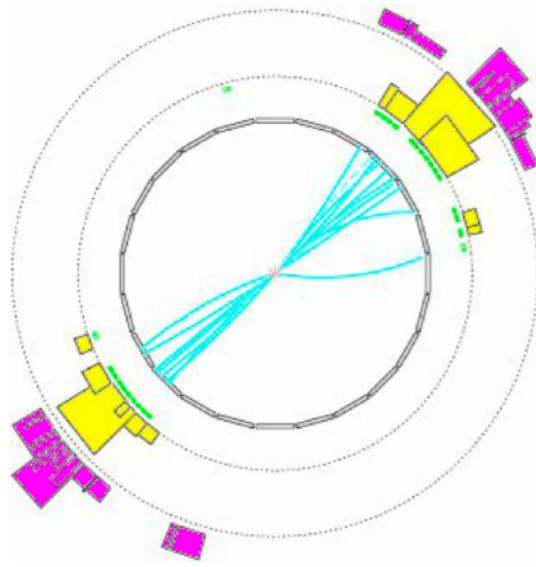
$$\begin{aligned} \frac{d\sigma(S^\Lambda, S^{\bar{\Lambda}})}{dz_1 dz_2 d\Omega} = & \sum_q e_q^2 \left[\frac{d\sigma_0^U}{d\Omega} \mathcal{D}_{\Lambda/q}^U(z_1, \mu) \mathcal{D}_{\bar{\Lambda}/\bar{q}}^U(z_2, \mu) + P_z^\Lambda P_z^{\bar{\Lambda}} \frac{d\sigma_0^L}{d\Omega} \mathcal{D}_{\Lambda/q}^L(z_1, \mu) \mathcal{D}_{\bar{\Lambda}/\bar{q}}^L(z_2, \mu) \right. \\ & \left. + |S_T^\Lambda| |S_T^{\bar{\Lambda}}| \cos(\phi_{S_1} + \phi_{S_2}) \frac{d\sigma_0^T}{d\Omega} \mathcal{D}_{\Lambda/q}^T(z_1, \mu) \mathcal{D}_{\bar{\Lambda}/\bar{q}}^T(z_2, \mu) \right] \end{aligned}$$

Boer, Jakob, Mulders '97

Spin correlation in Λ pair production with a thrust cut

S.J. Lin (林士佳), M.J. Liu (刘铭钧), DYS, S.Y. Wei '25

- We apply the event shape thrust (T) to select two-jet configuration $T = \frac{1}{Q} \max_{\vec{n}_T} \sum_i |\vec{n}_T \cdot \vec{p}_i|$



- The resummation predictions on the polarized cross section

$$\frac{d\sigma^{\mathcal{P}}(\tau_{\text{cut}})}{dz_1 dz_2 d\Omega} = \int_0^{\tau_{\text{cut}}} d\tau \frac{d\sigma^{\mathcal{P}}}{d\tau dz_1 dz_2 d\Omega},$$

$$\begin{aligned}
 &= \frac{d\sigma_0^{\mathcal{P}}}{d\Omega} \exp [4C_F S(\mu_h, \mu_J) + 4C_F S(\mu_s, \mu_J) - 2A_H(\mu_h, \mu_s) + 4A_J(\mu_J, \mu_s)] \left(\frac{Q^2}{\mu_h^2} \right)^{-2C_F A_{\text{cusp}}(\mu_h, \mu_J)} \\
 &\quad \times H(Q^2, \mu_h) \tilde{S}_T(\partial_\eta, \mu_s) \\
 &\quad \times \sum_q e_q^2 \tilde{\mathcal{G}}_{\Lambda/q}^{\mathcal{P}} \left(z_1, \ln \frac{\mu_s Q}{\mu_J^2} + \partial_\eta, \mu_J \right) \tilde{\mathcal{G}}_{\bar{\Lambda}/\bar{q}}^{\mathcal{P}} \left(z_2, \ln \frac{\mu_s Q}{\mu_J^2} + \partial_\eta, \mu_J \right) \left(\frac{\tau_{\text{cut}} Q}{\mu_s} \right)^\eta \frac{e^{-\gamma_E \eta}}{\Gamma(1 + \eta)} \Bigg|_{\eta=4C_F A_{\text{cusp}}(\mu_J, \mu_s)}.
 \end{aligned}$$

$$\mu_h = Q, \quad \mu_J = Q\sqrt{\tau_{\text{cut}}}, \quad \mu_s = Q\tau_{\text{cut}}.$$

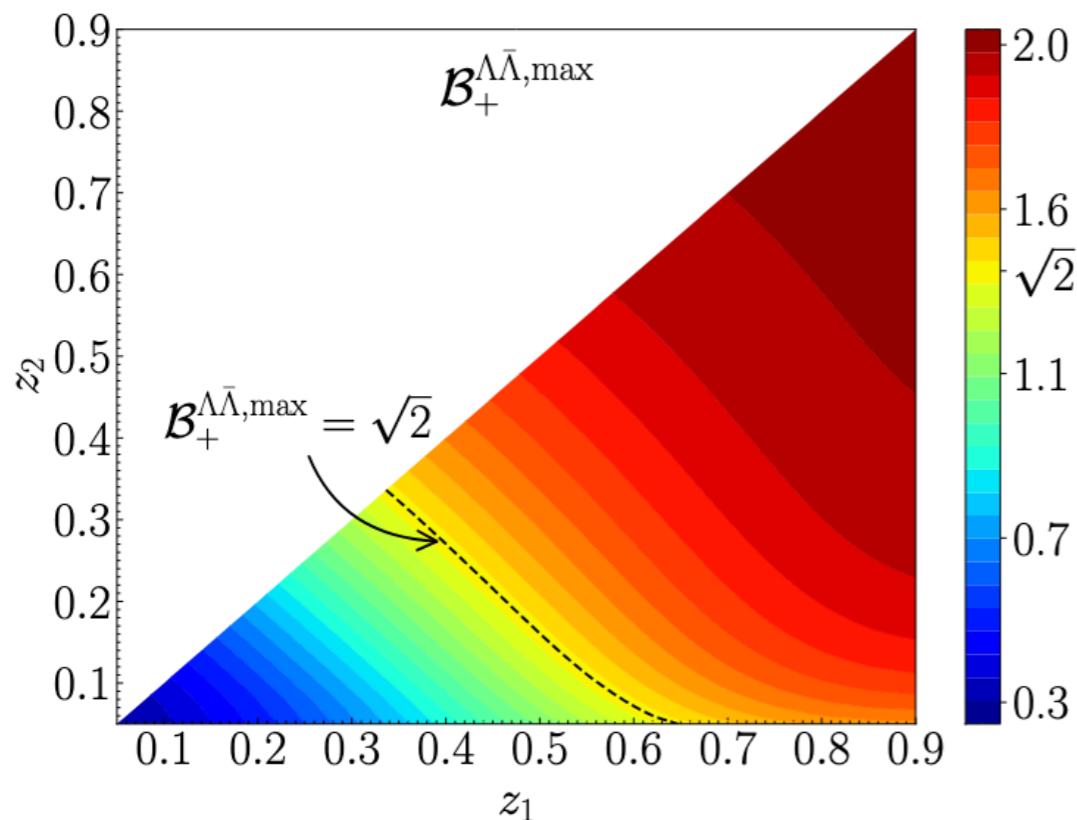
Bell nonlocality and decoherence

S.J. Lin (林士佳), M.J. Liu (刘铭钧), DYS, S.Y. Wei '25

- For the non-perturbative Λ FFs, we employ the DSV parameterization for the unpolarized Λ FF (de Florian, Stratmann, Vogelsang '97)
- We can utilize theoretical positivity bounds to define their maximal contribution (Soffer '94; Vogelsang '97)

$$|\mathcal{D}^L(z, \mu_0)| \leq \mathcal{D}^U(z, \mu_0), \quad |\mathcal{D}^T(z, \mu_0)| \leq \frac{1}{2} [\mathcal{D}^U(z, \mu_0) + \mathcal{D}^L(z, \mu_0)]$$

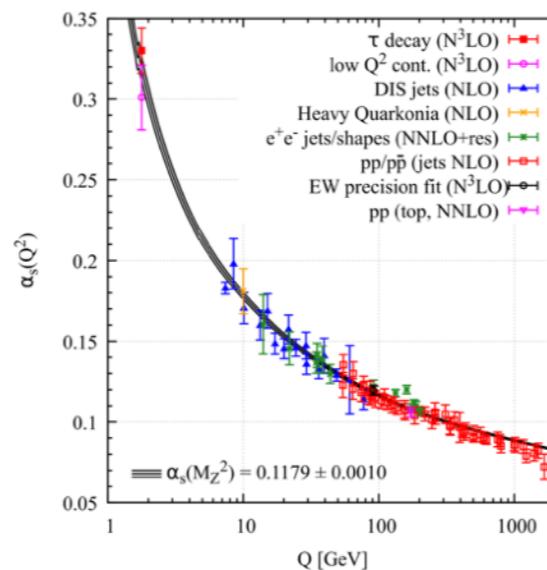
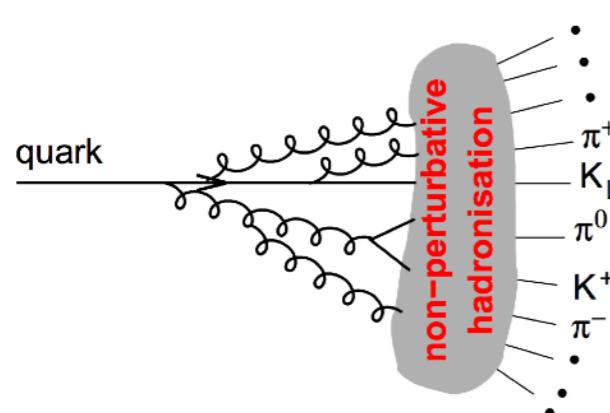
- We start from the ideal partonic baseline of a maximally entangled $\mathcal{B}_+^{q\bar{q}} = 2$



- We observe that under these ideal hadronization assumptions, the Bell variable is suppressed below the partonic maximum of 2
- As expected, this decoherence is reduced at large z , where the hadron carries most of the parent parton's spin information

Quantum information theory for hadronization

Parton (quark or gluon) fragmentation and hadronization



Jets are emergent property of QCD

- Soft-collinear singularity
- Asymptotic freedom
- Color string breaks

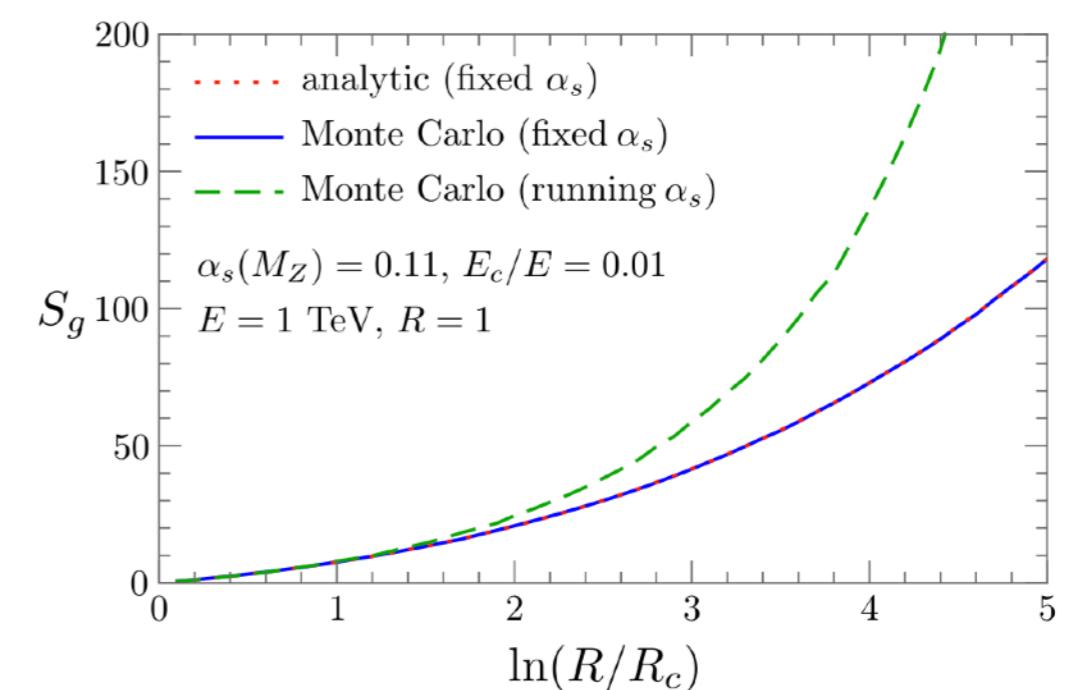
Dynamics of jets formation: from short to long distance in quantum field theory

E.g. Jet entropy Neill, Waalewijn '19 PRL

Reduced density matrix

$$\rho = \sum_{n=1}^{\infty} \int_H d\Pi_n(p_J) \frac{1}{\sigma} \frac{d\sigma}{d\Pi_n} |p_1, p_2, \dots, p_n\rangle \langle p_1, p_2, \dots, p_n|,$$

Renyi entropy $S_\alpha = \frac{\ln \text{tr}[\rho^\alpha]}{1-\alpha} = \frac{1}{1-\alpha} \ln \sum_{n=0}^{\infty} \text{tr}[\rho_n^\alpha]$



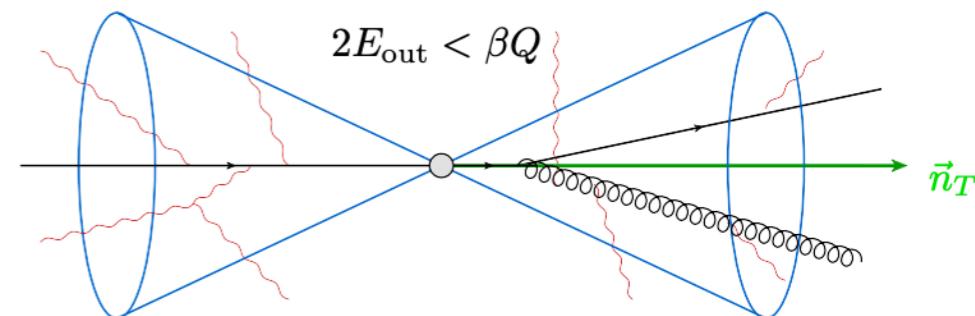
Gap fraction and open quantum system evolution

Becher, Neubert, Rothen, DYS '16 PRL

EFT contains two modes:

$$\text{hard: } p_h \sim Q(1, 1, 1)$$

$$\text{soft: } p_s \sim Q\beta(1, 1, 1)$$

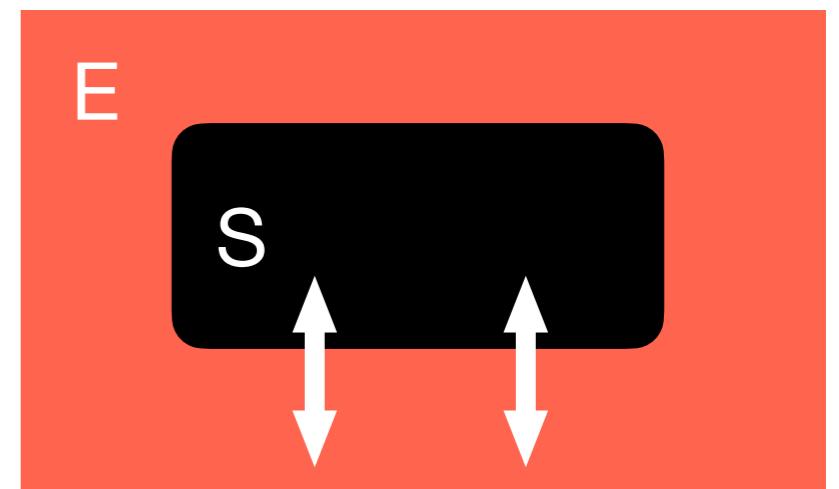


1. no collinear singularity, only single logs
2. method of region to verify at two-loop level

Hard parton described by collinear field

gauge invariant: $\chi_i(0) = W_i^\dagger(\bar{n}_i) \frac{\not{n}_i \not{\bar{n}}_i}{4} \psi_i(0)$

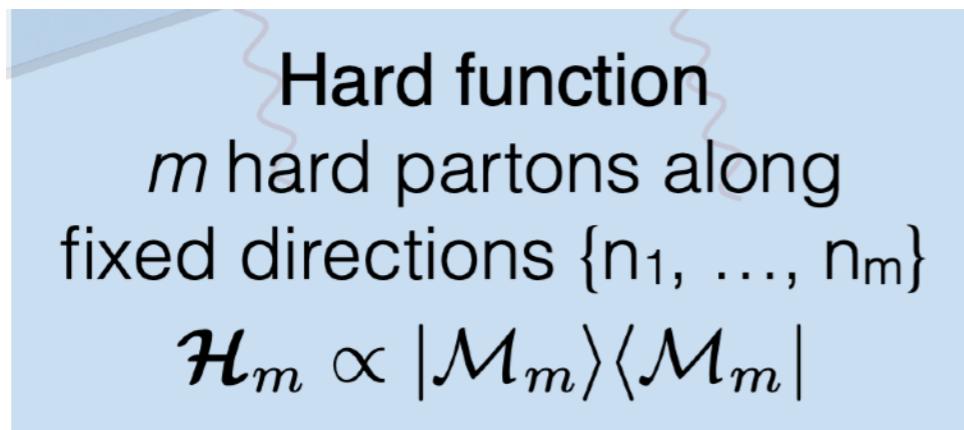
Perform decoupling transformation: $\Phi_i = S_i(n_i) \Phi_i^{(0)}$



$$S_i(n_i) = \mathbf{P} \exp \left(ig_s \int_0^\infty ds n_i \cdot A_s^a(s n_i) T_i^a \right)$$

Factorization for gap between jets in e+e-

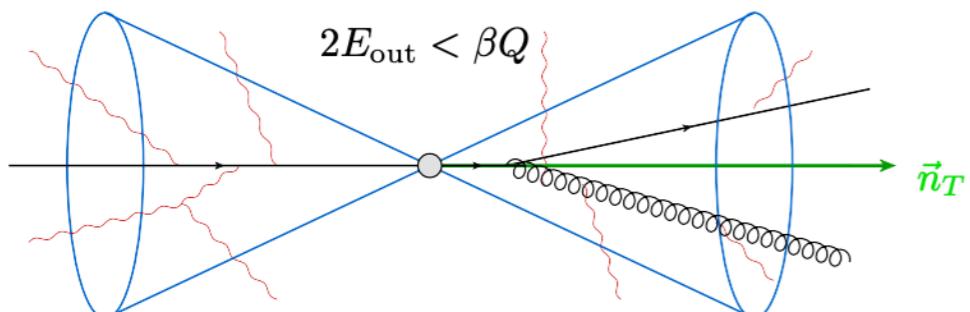
(Becher, Neubert, Rothen, DYS, '15 PRL, '16 JHEP; Caron-Huot '15 JHEP)



$$\text{Tr}[\rho \mathcal{O}]$$



$$\sigma(Q, Q_\Omega) \sim \sum_{m=2}^{\infty} \prod_{i=1}^m \int \frac{d\Omega(\vec{n}_i)}{4\pi} \text{Tr}_c [\mathcal{H}_m(\{\vec{n}_1, \dots, \vec{n}_m\}, Q, \mu) \mathcal{S}_m(\{\vec{n}_1, \dots, \vec{n}_m\}, Q_\Omega, \mu)]$$



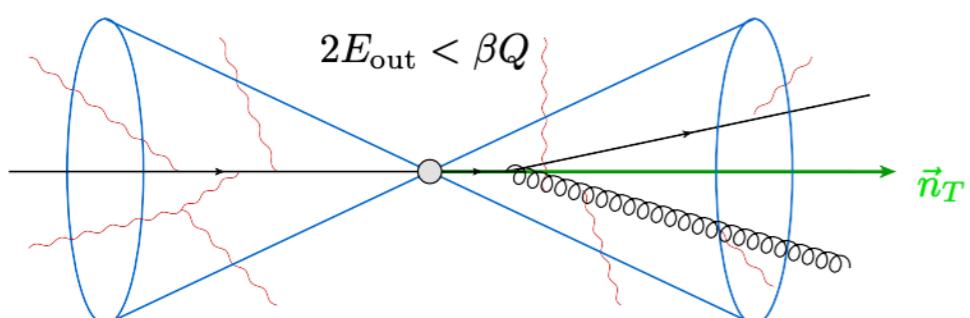
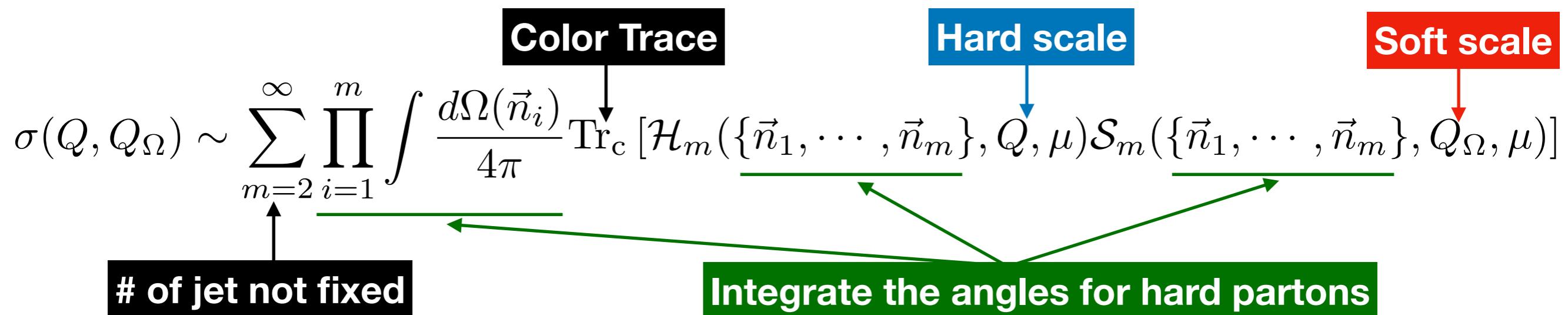
Factorization for gap between jets in e+e-

(Becher, Neubert, Rothen, DYS, '15 PRL, '16 JHEP; Caron-Huot '15 JHEP)

Hard function
 m hard partons along
fixed directions $\{\mathbf{n}_1, \dots, \mathbf{n}_m\}$
 $\mathcal{H}_m \propto |\mathcal{M}_m\rangle\langle\mathcal{M}_m|$

$$\text{Tr}[\rho \mathcal{O}]$$

Soft function
squared amplitude
with m Wilson lines



All-order evolution of leading Super-Leading Logs

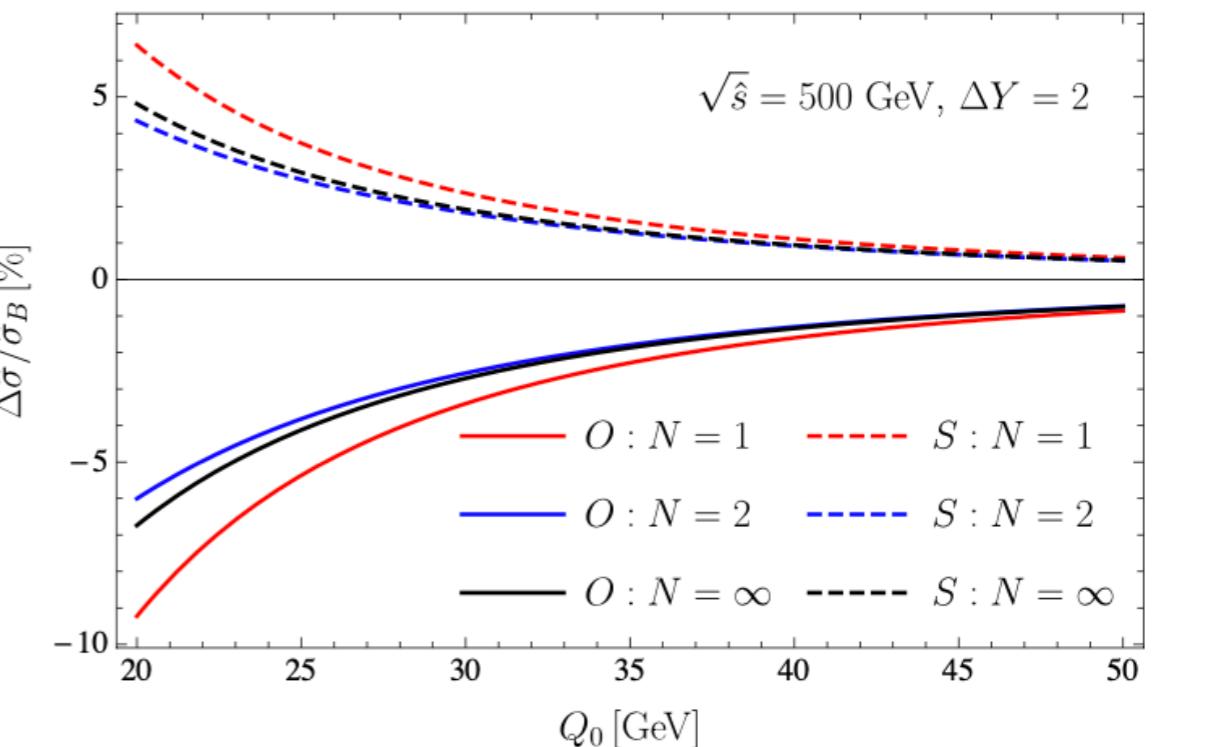
(Becher, Neubert, DYS '21 PRL + Stillger'23 JHEP)

All-order structure: Kampe de Feriet function (a two-variable generalization of the generalized hypergeometric series, the general sextic equation can be solved in terms of it)

$$\begin{aligned}\Sigma(v, w) &= \sum_{m=0}^{\infty} \sum_{r=0}^{\infty} \frac{(1)_{m+r} (1)_m (\frac{1}{2})_r}{(2)_{m+r} (\frac{5}{2})_{m+r}} \frac{(-w)^m (-vw)^r}{m! r!} \\ &= {}^{1+1}F_{2+0} \left(\begin{matrix} 1 : 1, \frac{1}{2}; \\ 2, \frac{5}{2}: \end{matrix} ; -w, -vw \right) \quad w = \frac{N_c \alpha_s(\bar{\mu})}{\pi} \ln^2 \left(\frac{\mu_h}{\mu_s} \right)\end{aligned}$$

Sudakov suppression of the superleading logarithms is weaker than the one present for global observables

$$\begin{array}{ccc} \text{Global logs} & \longrightarrow & e^{-\omega} \\ \\ \text{Superleading logs} & \xrightarrow{\omega \rightarrow \infty} & \frac{1}{\omega} \end{array}$$



Red: Four loop

Blue: Five loop

Black: all order

Summary and outlooks

- We have established a systematic framework for calculating spin decoherence by unifying SCET with the formalism of open quantum systems.
- Our central finding is that the renormalization group evolution constitutes a quantum channel, where the RG flow parameter, rather than time, drives a Markovian loss of quantum coherence.
- We work under the assumption that the process is Markovian to a good approximation. At the same time, there could be important non-Markovian effects $\hat{L} \propto \hat{\sigma}_i \otimes \hat{\sigma}_j$
- Quantum information science meets Lorentzian fragmentation

In the FUTURE

Perturbative: Amplitudes, Amplitudes, Amplitudes...

Numerical: Hamiltonian Truncation, Q-Computers

Lorentzian-fragmentation, diffraction,...



Thank you