



D 介子四体末态振幅分析

“粲强子衰变和标准模型的精确测量”2025夏季年会

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研究背景和目的

利用振幅分析研究粲介子多体强子衰变，有助于理解其强、弱衰变动力学机制，检验及刻度非微扰QCD理论模型

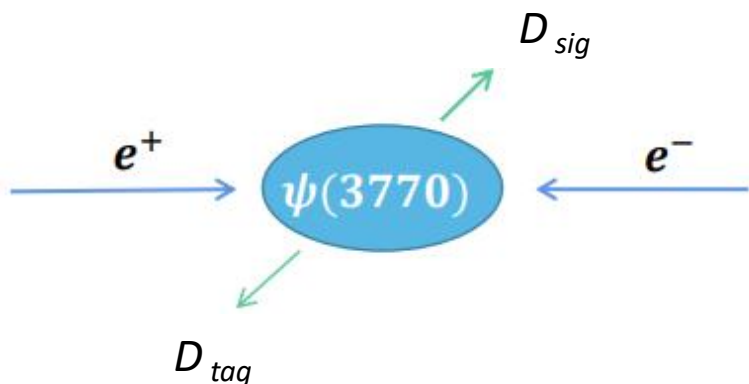
相较于三体衰变，四体衰变通常分支比更小，数据统计量低，同时中间过程复杂，振幅分析难度更大，相关研究较为匮乏

通过振幅分析，提供衰变中间共振态信息，针对特定过程进行研究：

- $D \rightarrow VV$ ：粲介子重要强子衰变过程，分支比大，同时包含三种角动量态，为解决重介子极化疑难提供关键信息
- $D \rightarrow AP$ ：研究轴矢量介子的重要途径，如 $K_1(1270)$, $a_1(1260)$, $K_1(1400)$ 等
- $D \rightarrow VS$ ：研究标量介子如 $a_0(980)$ ，结合理论模型判断其夸克组成
- $D \rightarrow PP$ ：研究激发态赝标量介子 $\eta(1405)$, $\eta(1475)$ 等
- $D \rightarrow VP$ ：研究含 $\omega / \phi (\rightarrow \pi^+ \pi^- \pi^0)$ 的过程

研究方法

利用双标记法重建 D 介子



构造振幅模型，通过最大似然拟合寻找最佳解

- **Total amplitude:** The sum over all the partial wave amplitudes $\mathcal{M}_{D^0}(p_j) = \sum_n c_n \mathcal{A}_n(p_j)$,
 $\mathcal{A}_n(p_j) = P_n^1 P_n^2 S_n F_n^1 F_n^2 F_n^{D^0}$
 - $c_n = \rho_n e^{i\phi_n}$: complex coefficient
 - $\mathcal{A}_n(p)$: the n^{th} intermediate process amplitude
 - $P_n^{1,2}(m)$: propagator
 - $S_n(p_j)$: spin factor
 - $F_n^{1,2}(F_n^{D^0})$: the Blatt-Weisskopf barriers of the intermediate resonance and D_0 meson.
- **PDF** is calculated by following formula

$$\text{PDF}(p_j) = \omega_{\text{sig}} \frac{\varepsilon(p_j) |\mathcal{M}(p_j)|^2 R_4(p_j)}{\int \varepsilon(p_j) |\mathcal{M}(p_j)|^2 R_4(p_j) dp_j} + (1 - \omega_{\text{sig}}) \frac{B(p_j) R_4(p_j)}{\int B(p_j) R_4(p_j) dp_j}$$

- $B(p_j)$: background shape
- $\mathcal{M}(p_j)$: total amplitude
- ω_{sig} : fraction of signal
- $R_4(p_j)$: phase space

研究方法

helicity振幅 $D \rightarrow VV \rightarrow (P_1 P_2)(P_3 P_4)$

$$H_{\lambda_{V_1}, \lambda_{V_2}} = F_{\lambda_{V_1}, \lambda_{V_2}}^{J_D} D_{\lambda_D, \lambda_{V_1} - \lambda_{V_2}}^{J_D}(\phi_{V_1}, \theta_{V_1}, 0) \cdot P_{V_1} F_{\lambda_{P_1}, \lambda_{P_2}}^{J_{V_1}} D_{\lambda_{V_1}, \lambda_{P_1} - \lambda_{P_2}}^{J_{V_1}}(\phi_{P_1}, \theta_{P_1}, 0) \cdot P_{V_2} F_{\lambda_{P_3}, \lambda_{P_4}}^{J_{V_2}} D_{\lambda_{V_2}, \lambda_{P_3} - \lambda_{P_4}}^{J_{V_2}}(\phi_{P_3}, \theta_{P_3}, 0).$$

$$J_D = 0 \Rightarrow \lambda_{V_1} = \lambda_{V_2} \quad \therefore |A|^2 = \left| \sum_{\lambda_{V_1} \lambda_{V_2}} H_{\lambda_{V_1} \lambda_{V_2}} \right|^2 = |H_{11} + H_{-1-1} + H_{00}|^2$$

$$F_{\pm 1 \pm 1}^{J_D} = \sqrt{\frac{1}{3}} g_{00} \pm \sqrt{\frac{1}{2}} W r g_{11} + \sqrt{\frac{1}{6}} r^2 g_{22} \quad , \quad F_{00}^{J_D} = \gamma_1 \gamma_2 \left(-\sqrt{\frac{1}{3}} g_{00} + \sqrt{\frac{2}{3}} r^2 g_{22} \right) \quad r = 2|q|$$

$|q|$: momentum of V in D rest frame γ : Lorentz factor of V in D rest frame W : mass of D (m)

$$f_L = \frac{|H_{00}|^2}{|H_{11} + H_{-1-1} + H_{00}|^2}$$

The transformation is based on the references [JHEP06\(2023\)039](#) and [Phys.Rev.D 57 \(1998\) 431-442](#) .

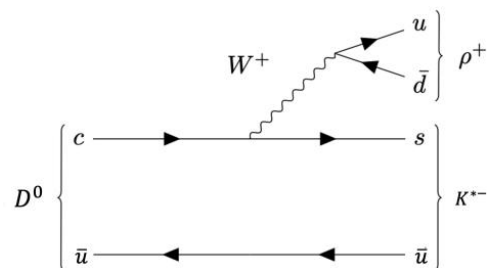
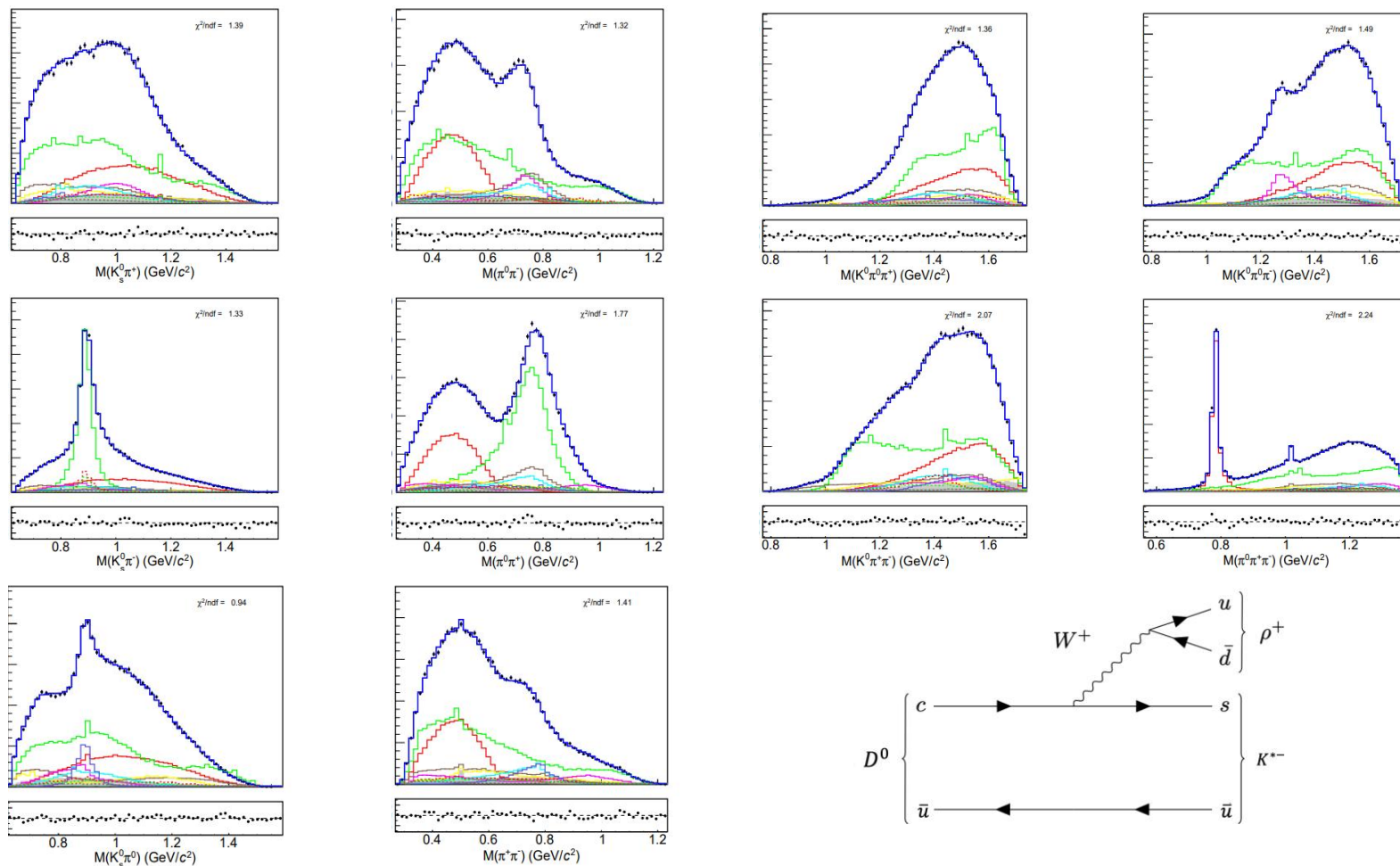
研究现状

$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	(Feng Yutong)
$D^0 \rightarrow K_S^0 \pi^0 \pi^0 \pi^0$	(Rong Shaoshi)
$D^0 \rightarrow K_S^0 K^+ \pi^- \pi^0$	(Li Zhenxuan)
$D^0 \rightarrow K_S^0 K^- \pi^+ \pi^0$	(Li Zhenxuan)
$D^0 \rightarrow K^+ K^- \pi^0 \pi^0$	(Wang Jiahao)
$D^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$	(Wang Jiahao)
$D^+ \rightarrow K^+ K^- \pi^+ \pi^0$	(Lu Yu)
$D^0 \rightarrow K^- K^- K^+ \pi^+$	(Shi Jialei)

$D^0 \rightarrow K_L^0 \pi^+ \pi^- \pi^0$	(Feng Yutong)
$D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^-$	(Li Shuo)
$D^0 \rightarrow K^- \pi^+ \pi^+ \eta$	(Zeng Xin)
$D^0 \rightarrow K^- \pi^+ \pi^0 \eta$	(Zhou Shuai)
$D^0 \rightarrow K_S^0 \pi^+ \pi^- \eta$	(Liu Xinghan)
$D^+ \rightarrow \pi^+ \pi^+ \pi^- \pi^0$	(Li Xu)
$D^0 \rightarrow \pi^+ \pi^- \pi^0 \pi^0$	(Shan Xinyu)
$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	(Shan Xinyu)

$$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$$

BAM-01025



- CP-even fractions
- longitudinal polarization fraction of $D^0 \rightarrow K^{*-} \rho^+$ and $D^0 \rightarrow \bar{K}^{*0} \rho^0$.
- $D^0 \rightarrow K^{*-} \rho^+$ 纵向极化0.5左右
- $D^0 \rightarrow \bar{K}^{*0} \rho^0$ 横向极化主导

Amplitude

ωK_S^0
ϕK_S^0
$\omega(1420)$
$\omega(1650)$
$K(1410)^- \pi^+ [K(1410) \rightarrow K_S^0 \rho(770)]$
$\bar{K}^*(1680)^0 \pi^0$
$K^*(1680)^- \pi^+$
$K^*(1680)^+ \pi^-$
$\pi(1300) K_S^0$
$\bar{K}(1460)^0 \pi^0$
$K(1460)^- \pi^+$
$h_1(1170) K_S^0$
$a_1(1260) K_S^0$
$a_1(1640) K_S^0$
$K_1(1270)^- \pi^+$
$\bar{K}_1(1270)^0 \pi^0$
$\bar{K}_1(1400)^0 \pi^0$
$K_1(1400)^- \pi^+$
$\bar{K}_1(1650)^0 \pi^0$
$K_1(1650)^- \pi^+$
$a_2(1320) K_S^0$
$K_2^*(1430)^- \pi^+$
$\bar{K}_2^*(1430)^0 \pi^0$
$K^*(892)^- \rho(770)^+$
$\bar{K}^*(892)^0 \rho(770)^0$
$K^*(892)^- \rho(1450)^+$
$\bar{K}^*(892)^0 \rho(1450)^0 [D]$
$K^*(1680)^- \rho(770)^+ [S]$
$\rho(1450)^0 (K_S^0 \pi^0)^{L=1}$
$\bar{K}^*(892)^0 f_2(1270)$

$$D^0 \rightarrow K_S^0 \pi^0 \pi^0 \pi^0$$

memo review

- 末态包含三个全同 π^0 ，振幅分析难度较大
- 不含 ρ ，中间态较少

Amplitude

$$D^0 \rightarrow \bar{K}_1(1400)^0 \pi^0, \bar{K}_1(1400)^0 \rightarrow \bar{K}^*(892)^0 \pi^0$$

$$D^0 \rightarrow \bar{K}_1(1270)^0 \pi^0, \bar{K}_1(1270)^0 \rightarrow \bar{K}^*(892)^0 \pi^0$$

$$D^0 \rightarrow \bar{K}(1460) \pi^0, \bar{K}(1460) \rightarrow \bar{K}^*(892)^0 \pi^0$$

$$D^0 \rightarrow \bar{K}(1460) \pi^0, \bar{K}(1460) \rightarrow \bar{K}^0(\pi^0 \pi^0)_{S\text{-wave}}$$

f_{KK}

β_0

β_1

$$D^0 \rightarrow \bar{K}_S^0 \pi(1300), \pi(1300) \rightarrow (\pi^0 \pi^0)_{S\text{-wave}} \pi^0$$

$f_{\pi\pi}$

β_0

β_1

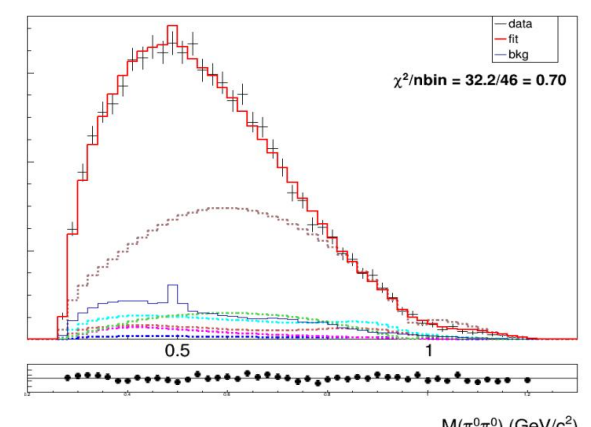
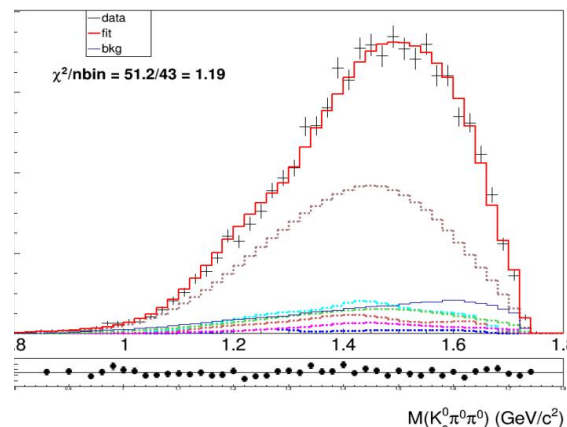
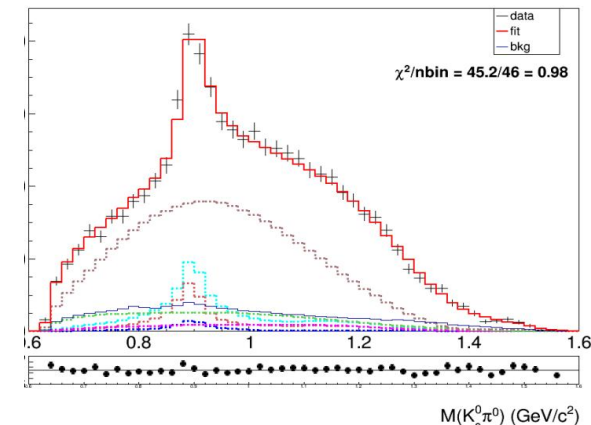
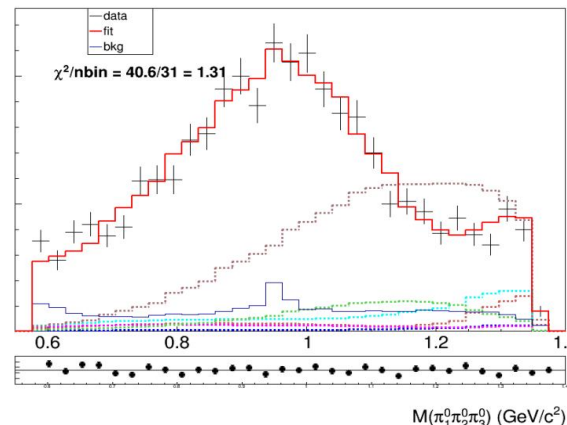
$$D^0 \rightarrow (K_S^0 \pi^0)_{S\text{-wave}} (\pi^0 \pi^0)_{S\text{-wave}}$$

$\alpha_{3/2}$

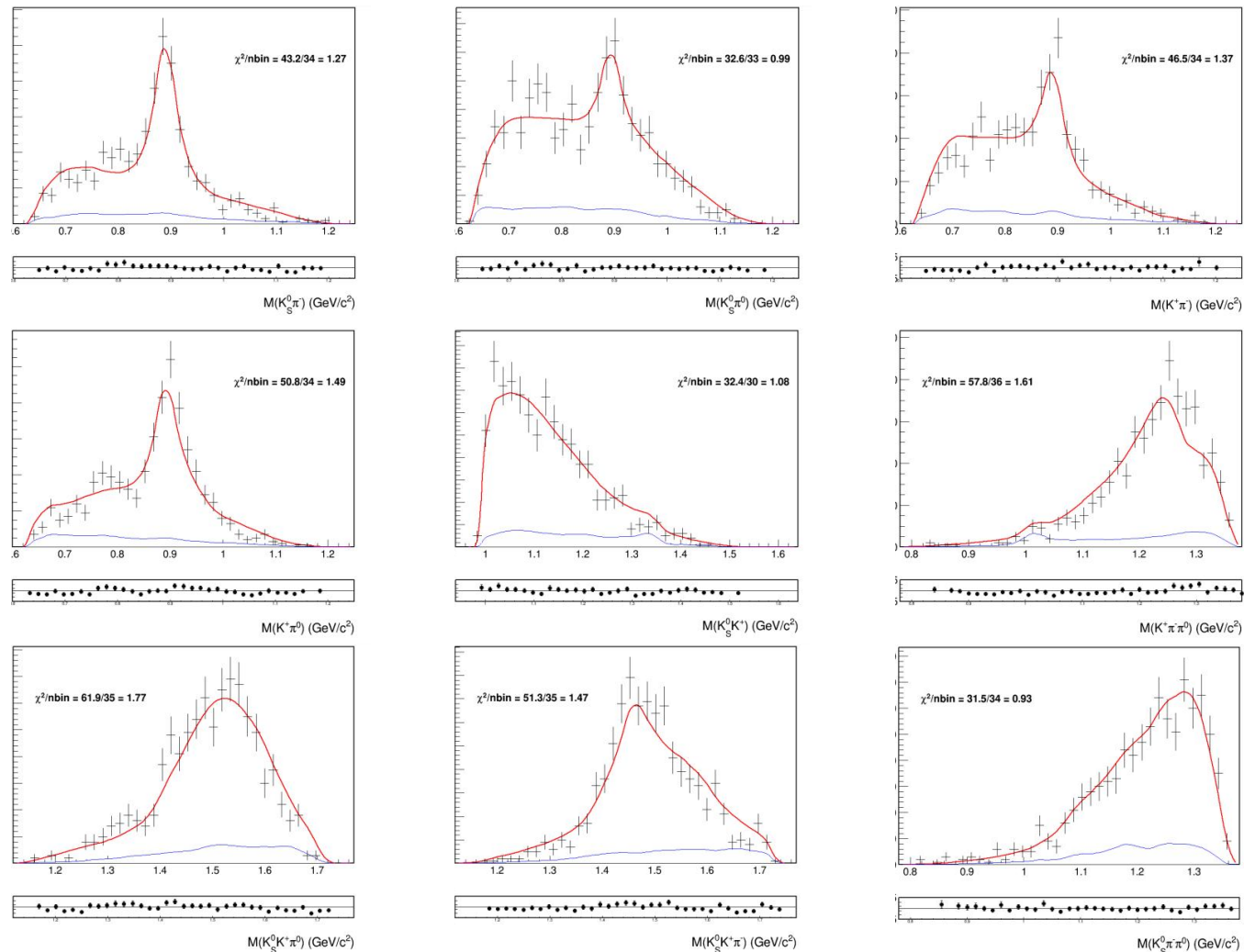
$\alpha_{K\eta'}$

β_1

$f_{\pi\pi}$



- 为 $K_1(1270)/K_1(1400)$ 混合角的确定提供实验测量



Amplitude

$$D^0[S] \rightarrow K^{*+} K^{*-}$$

$$D^0[P] \rightarrow K^{*+} K^{*-}$$

$$D^0 \rightarrow K^{*+} K^{*-}$$

$$D^0[S] \rightarrow \bar{K}^{*0} K^{*0}$$

$$D^0[D] \rightarrow \bar{K}^{*0} K^{*0}$$

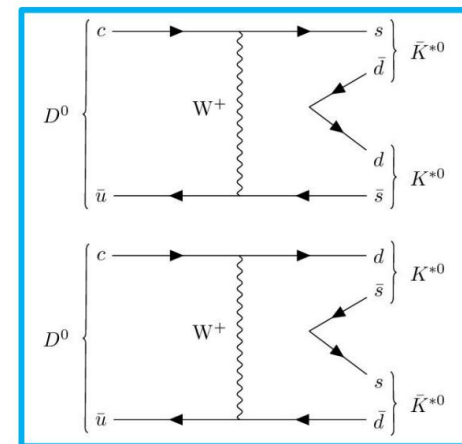
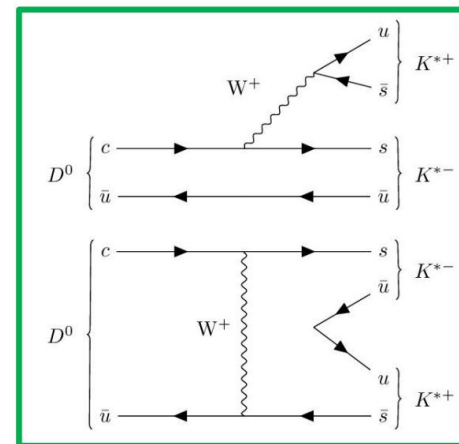
$$D^0 \rightarrow K^{*0} K^{*0}$$

$$D^0 \rightarrow K_1^-(1400)[S](\rightarrow K^* \pi) K^+$$

$$D^0 \rightarrow K_1^0(1270)[S](\rightarrow K^+ \rho^-) K_S^0$$

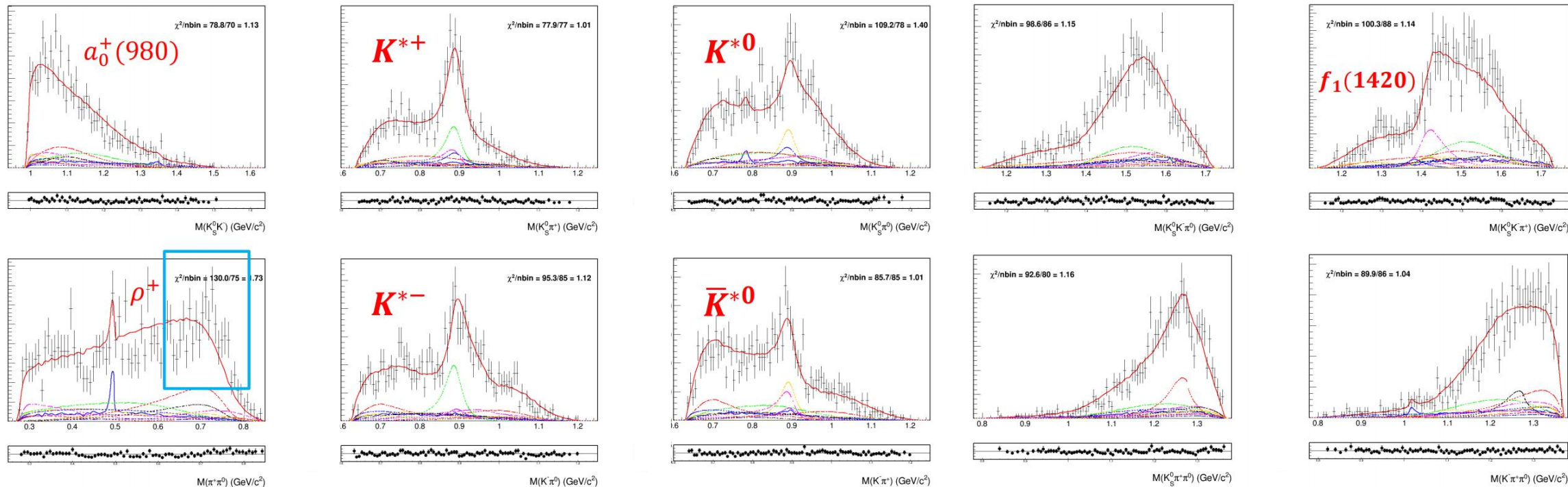
$$D^0 \rightarrow \eta(1475)(\rightarrow K^* K) \pi^0$$

$$D^0 \rightarrow a_0^+(980) \rho^-$$


 同时测量到 $D^0 \rightarrow K^{*-} K^{*+}$, $D^0 \rightarrow \bar{K}^{*0} K^{*0}$ 的极化

$$D^0 \rightarrow K_S^0 K^- \pi^+ \pi^0$$

分会报告



Amplitude

$$D^0[S] \rightarrow K^{*+} K^{*-}$$

$$D^0[P] \rightarrow K^{*+} K^{*-}$$

$$D^0[D] \rightarrow K^{*+} K^{*-}$$

$$D^0 \rightarrow K^{*+} K^{*-}$$

$$D^0[S] \rightarrow \bar{K}^{*0} K^{*0}$$

$$D^0[P] \rightarrow \bar{K}^{*0} K^{*0}$$

$$D^0[D] \rightarrow \bar{K}^{*0} K^{*0}$$

$$D^0 \rightarrow \bar{K}^{*0} K^{*0}$$

$$D^0 \rightarrow K_1^+(1270)[S](\rightarrow K_S^0 \rho^+) K^-$$

$$D^0 \rightarrow K_1^+(1400)[S](\rightarrow K^* \pi) K^-$$

$$D^0 \rightarrow \bar{K}_1^0(1270)[S](\rightarrow K^- \rho^+) K_S^0$$

$$D^0 \rightarrow \bar{K}_1^0(1400)[S](\rightarrow K^* \pi) K_S^0$$

$$D^0 \rightarrow f_1(1420)[S](\rightarrow K^* K) \pi^0$$

$$D^0 \rightarrow f_1(1420)(\rightarrow a_0^-(980) \pi^+) \pi^0$$

$$D^0 \rightarrow \eta(1405)(\rightarrow a_0^-(980) \pi^+) \pi^0$$

$$D^0 \rightarrow a_0^-(980) \rho^+$$

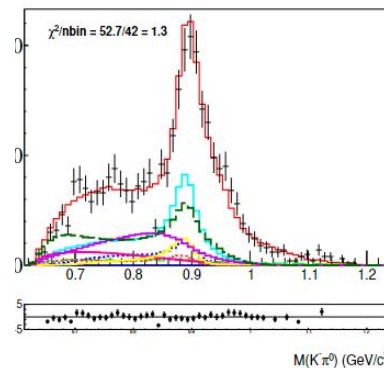
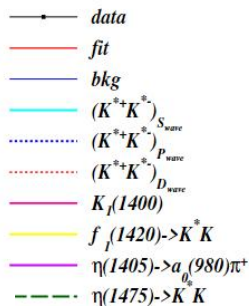
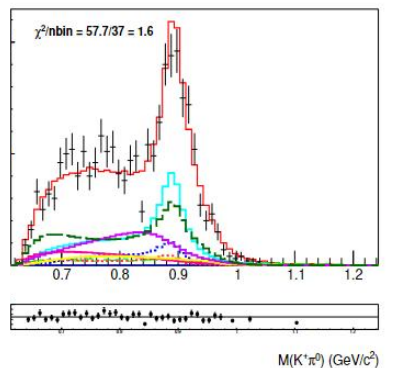
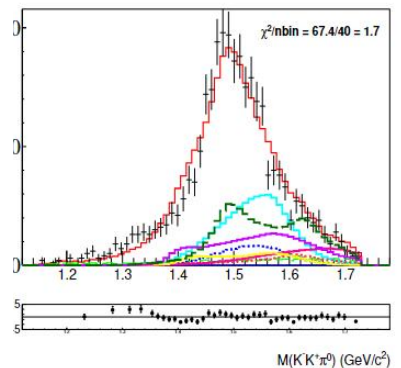
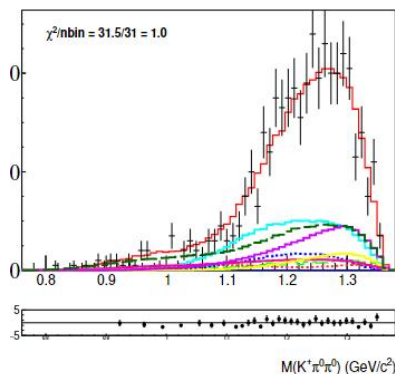
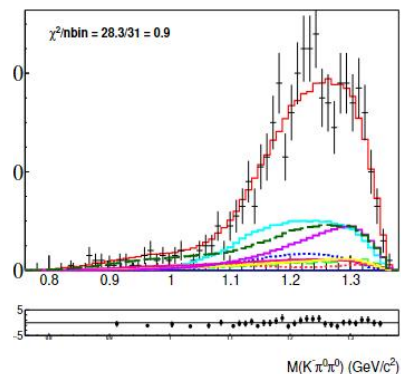
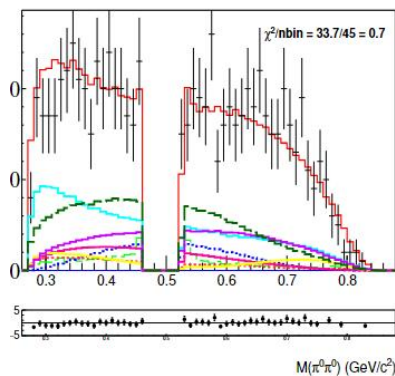
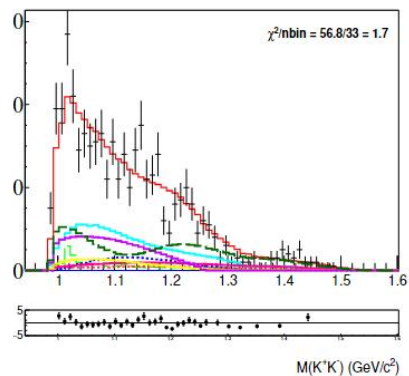
- 同时测量 $D^0 \rightarrow K^{*-} K^{*+}$, $D^0 \rightarrow \bar{K}^{*0} K^{*0}$ 的极化

- 结合上个分析, 可以测 $r_{+/-} = \frac{B(D^0 \rightarrow a_0^+ \rho^-)}{B(D^0 \rightarrow a_0^- \rho^+)}$

为确定 a_0 结构提供信息

$D^0 \rightarrow K^+ K^- \pi^0 \pi^0$

BAM-0998&Draft



Amplitude

$$D^0[S] \rightarrow K^{*+}(892)K^{*-}(892)$$

$$D^0[P] \rightarrow K^{*+}(892)K^{*-}(892)$$

$$D^0[D] \rightarrow K^{*+}(892)K^{*-}(892)$$

$$D^0 \rightarrow K^{*+}(892)K^{*-}(892)$$

$$D^0 \rightarrow K_1(1400)^+(\rightarrow K^*(892)^+\pi^0)K^-$$

$$D^0 \rightarrow f_1(1420)(\rightarrow K^*(892)^+K^-)\pi^0$$

$$D^0 \rightarrow f_1(1420)(\rightarrow K^*(892)^-K^+)\pi^0$$

$$D^0 \rightarrow f_1(1420)\pi^0$$

$$D^0 \rightarrow \eta(1405)(\rightarrow a_0(980)\pi^0)\pi^0$$

$$D^0 \rightarrow \eta(1475)(\rightarrow K^{*-}(892)K^+)\pi^0$$

$$D^0 \rightarrow \eta(1475)(\rightarrow K^{*+}(892)K^-)\pi^0$$

$$D^0 \rightarrow \eta(1475)\pi^0$$

- 主要过程: $D \rightarrow VV$
- 横向极化主导
- $D^0 \rightarrow K^{*+}K^{*-}$ 分支比测量

Amplitude	$\mathcal{B}(D^0 \rightarrow K^*(892)^+ K^*(892)^-) (\times 10^{-3})$
NRCQM with FSI [13]	9.92 ± 0.34
NRCQM without FSI [13]	5.86
flavor SU(3) symmetry model [9]	2.4
factorization approach [41]	7.3

$$D^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$$

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Amplitude

$$D^+[S] \rightarrow \bar{K}^*(892)^0 K^*(892)^-$$

$$D^+[P] \rightarrow \bar{K}^*(892)^0 K^*(892)^-$$

$$D^+[D] \rightarrow \bar{K}^*(892)^0 K^*(892)^-$$

$$D^+ \rightarrow f_1(1285)\pi^+, f_1(1285) \rightarrow a_0(980)\pi^+$$

$$D^+ \rightarrow f_1(1420)\pi^+, f_1(1420) \rightarrow K^*(892)^+ K^-$$

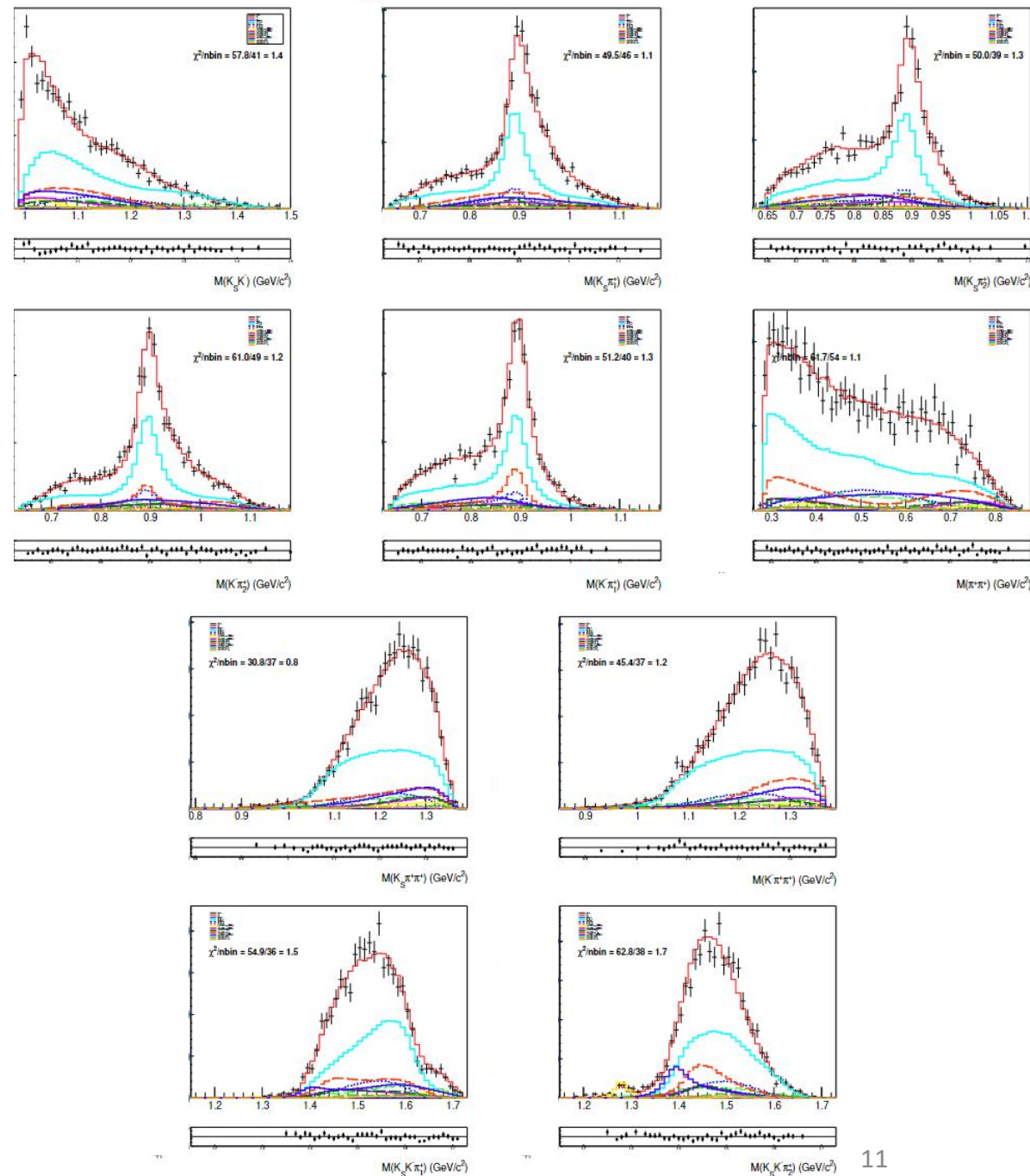
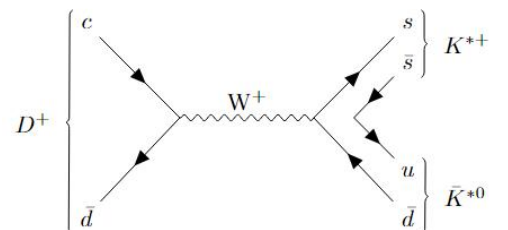
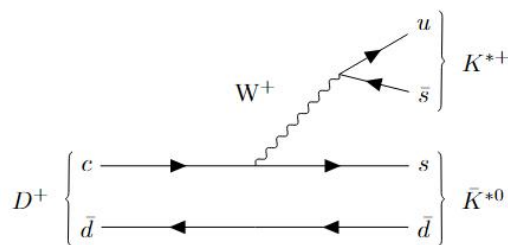
$$D^+ \rightarrow f_1(1420)\pi^+, f_1(1420) \rightarrow K^*(892)^0 K_S$$

$$D^+ \rightarrow f_1(1420)\pi^+, f_1(1420) \rightarrow a_0(980)\pi^+$$

$$D^+ \rightarrow \eta(1405)\pi^+, \eta(1405) \rightarrow a_0(980)\pi^+$$

$$D^+ \rightarrow \eta(1475)\pi^+, \eta(1475) \rightarrow K^*(892)^+ K^-$$

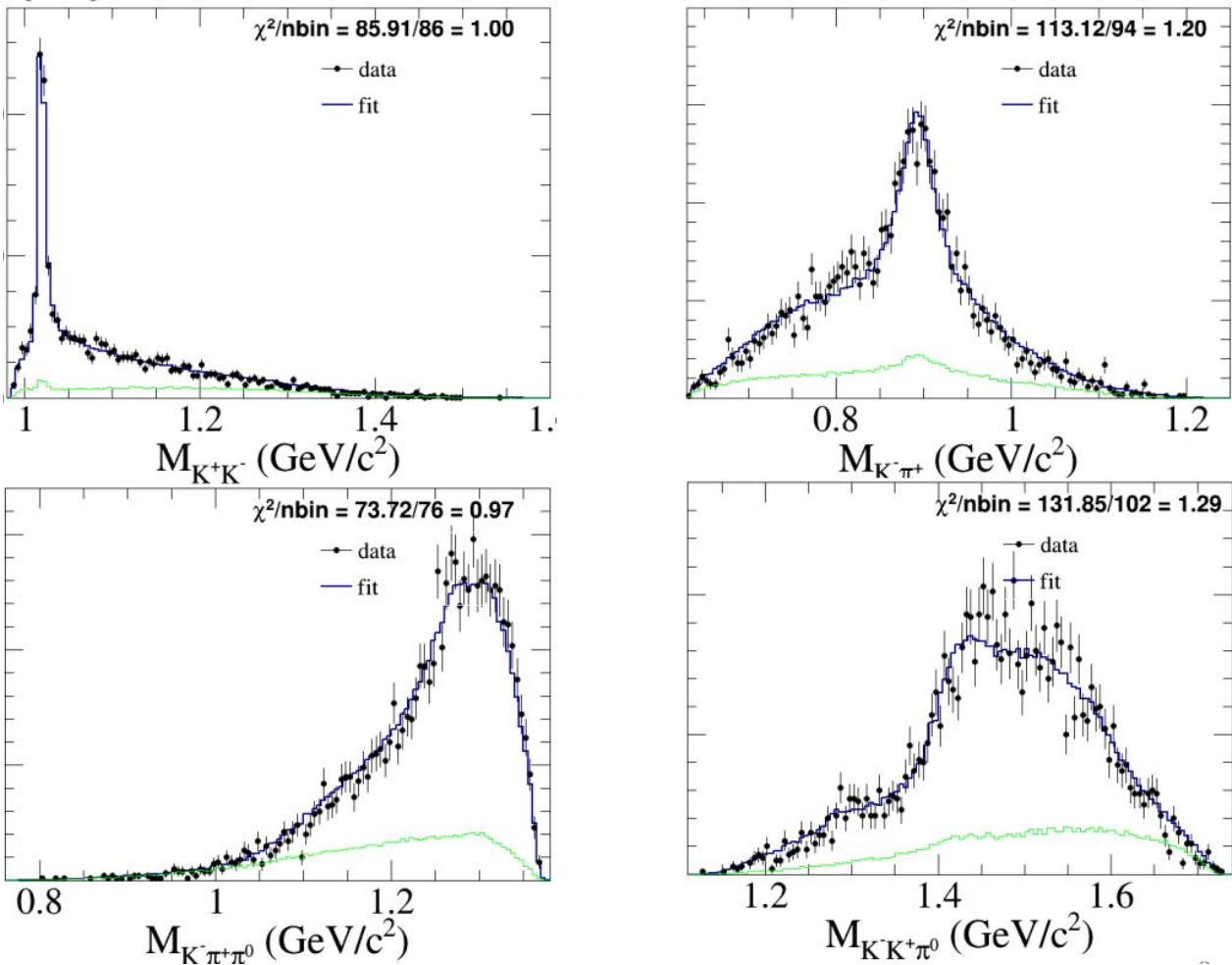
$$D^+ \rightarrow \eta(1475)\pi^+, \eta(1475) \rightarrow K^*(892)^0 K_S$$



- 主要过程: $D \rightarrow VV$
- 横向极化主导
- $D^+ \rightarrow K^{*0} K^{*+}$ 分支比首次测量

$$D^+ \rightarrow K^+ K^- \pi^+ \pi^0$$

已过组内审核

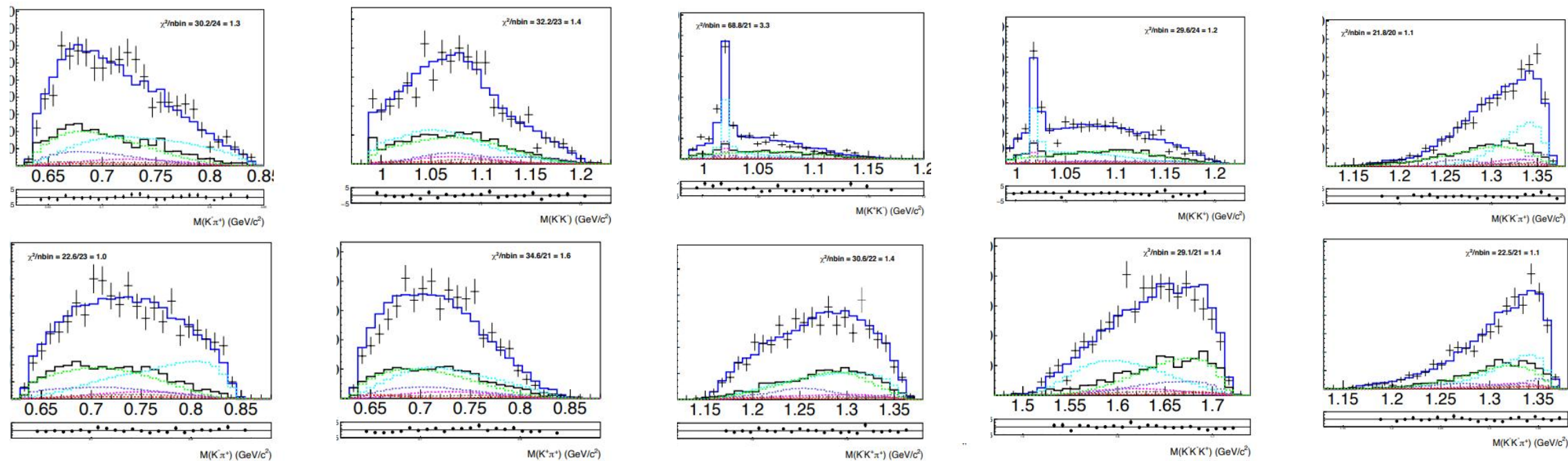


同时测量 $D^+ \rightarrow K^{*0} K^{*+}$, $D^+ \rightarrow \phi \rho^+$ 的极化

$D^+ \rightarrow \phi \rho^+$	S
	P
	D
$D^+ \rightarrow \bar{K}^{*0} K^+$	S
	P
	D
$D^+ \rightarrow \bar{K}_1(1270)^0 (\rho^+ K^-) K^+$	S
$D^+ \rightarrow \bar{K}_1(1400)^0 (\bar{K}^* \pi) K^+$	S
$D^+ \rightarrow a_0(980)^0 \rho^+$	
$D^+ \rightarrow f_1(1420) (K^* K) \pi^+$	S
$D^+ \rightarrow f_1(1285) (K^* K) \pi^+$	S
$D^+ \rightarrow \eta(1405) (a_0(980) \pi^0) \pi^+$	
$D^+ \rightarrow \eta(1405) (K^* K) \pi^+$	

$D^0 \rightarrow K^- K^- K^+ \pi^+$

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$$D^0[S] \rightarrow \phi \bar{K}^{*0}$$

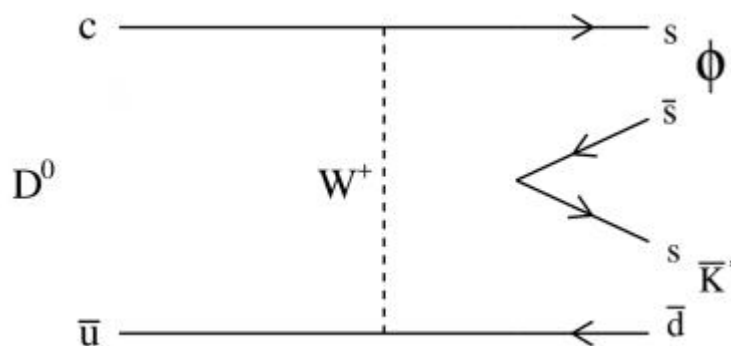
$$D^0[P] \rightarrow \phi \bar{K}^{*0}$$

$$D^0[D] \rightarrow \phi \bar{K}^{*0}$$

$$D^0 \rightarrow \phi \bar{K}^{*0}$$

$$D^0 \rightarrow (K^- \pi^+)_s \phi$$

$$D^0 \rightarrow (K^- K^+)_s \bar{K}^{*0}$$



Other ongoing analysis....

$D^0 \rightarrow K_L^0 \pi^+ \pi^- \pi^0$	(Feng Yutong)	初步结果
$D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^-$	(Li Shuo)	2024.12 合作组会分会报告
$D^+ \rightarrow K^- \pi^+ \pi^+ \eta$	(Zeng Xin)	初步结果
$D^0 \rightarrow K^- \pi^+ \pi^0 \eta$	(Zhou Shuai)	初步结果
$D^0 \rightarrow K_S^0 \pi^+ \pi^- \eta$	(Liu Xinghan)	2025.4 Workshop分会报告
$D^+ \rightarrow \pi^+ \pi^+ \pi^- \pi^0$	(Li Xu)	2023.12 合作组会分会报告
$D^0 \rightarrow \pi^+ \pi^- \pi^0 \pi^0$	(Shan Xinyu)	2.93fb ⁻¹ 已发表
$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	(Shan Xinyu)	2.93fb ⁻¹ 已发表 在更新20.3fb ⁻¹ 中

总结

对 D 介子四体衰变的振幅分析研究积累了丰富的成果

- 对 $D \rightarrow VV$ 过程有了更深入的了解, 包括 $D^0 \rightarrow K^{*-}K^{*+}$, $D^0 \rightarrow \bar{K}^{*0}K^{*0}$, $D^0 \rightarrow K^{*-}\rho^+$, $D^0 \rightarrow \bar{K}^{*0}\rho^+$, $D^+ \rightarrow K^{*0}K^{*+}$, $D^+ \rightarrow \phi\rho^+$ 等
- 测量到大量 $D \rightarrow AP$ 过程, 为研究轴矢量介子性质及衰变方式提供重要信息
- 在部分衰变道的研究中, 观测到实验值与理论预期不符的情况, 如 $D^0 \rightarrow \bar{K}^{*0}\rho^0$ 的极化情况、 $D^0 \rightarrow K^{*-}K^{*+}$ 的分支比、 $D \rightarrow a_0\rho$ 系统中的 $r_{+/-}$ 、 $r_{+/0}$ 值等

谢谢！