

D_s 多体衰变振幅分析

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2025. 08 贵阳

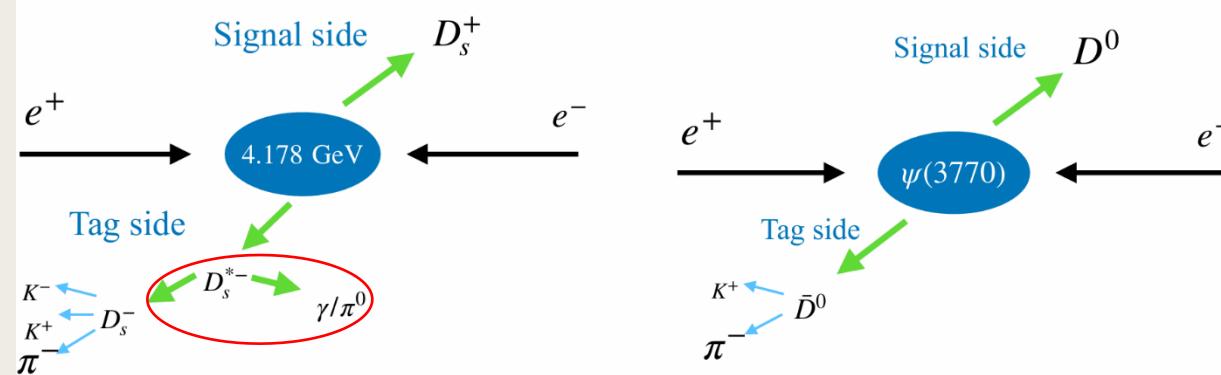
Theory under Topological Diagram Approach

PhysRevD.109.073008, Phys. Rev. D 104, 073003 (2021)

Cabbibo Favored							Singly Cabbibo Suppressed			
$D_s^+ \rightarrow VP$	$\bar{K}^{*0} K^+$	$\lambda_{sd}(C_P + A_V)$	3.79 ± 0.09	3.80 ± 0.10	3.79 ± 0.09	$D_s^+ \rightarrow \pi^+ K^{*0}$	2.55 ± 0.35^a	2.06 ± 0.06	1.58 ± 0.05	
	$K_S^0 K^{*+}$	$\frac{1}{\sqrt{2}}[\lambda_{sd}(C_V + A_P) - \lambda_{ds}(T_P + C_V)]$	0.77 ± 0.07^a	0.79 ± 0.04	0.78 ± 0.03	$D_s^+ \rightarrow \pi^0 K^{*+}$	0.75 ± 0.25^b	0.71 ± 0.03	0.67 ± 0.03	
	$\rho^+ \pi^0$	$\frac{1}{\sqrt{2}}\lambda_{sd}(A_P - A_V)$...	0.012 ± 0.003	0.011 ± 0.002	$D_s^+ \rightarrow K^+ \rho^0$	2.17 ± 0.25	1.01 ± 0.03	1.11 ± 0.03	
	$\rho^+ \eta$	$\lambda_{sd}[\frac{1}{\sqrt{2}}(A_P + A_V) \cos \phi - T_P \sin \phi]$	8.9 ± 0.8	9.25 ± 0.35	8.75 ± 0.31	$D_s^+ \rightarrow K^0 \rho^+$	5.46 ± 0.95^b	7.54 ± 0.27	7.30 ± 0.26	
	$\rho^+ \eta'$	$\lambda_{sd}[\frac{1}{\sqrt{2}}(A_P + A_V) \sin \phi + T_P \cos \phi]$	5.8 ± 1.5	3.24 ± 0.11	3.60 ± 0.11	$D_s^+ \rightarrow \eta K^{*+}$...	0.37 ± 0.07	0.39 ± 0.09	
	$\pi^+ \rho^0$	$\frac{1}{\sqrt{2}}\lambda_{sd}(A_V - A_P)$	0.0112 ± 0.0013^b	0.011 ± 0.003	0.011 ± 0.002	$D_s^+ \rightarrow \eta' K^{*+}$...	0.40 ± 0.02	0.42 ± 0.02	
	$\pi^+ \omega$	$\frac{1}{\sqrt{2}}\lambda_{sd}(A_V + A_P)$	0.238 ± 0.015^c	0.24 ± 0.01	0.24 ± 0.01	$D_s^+ \rightarrow K^+ \omega$	0.99 ± 0.15	1.16 ± 0.03	1.17 ± 0.03	
	$\pi^+ \phi$	$\lambda_{sd}T_V$	4.50 ± 0.12	4.49 ± 0.11	4.50 ± 0.11	$D_s^+ \rightarrow K^+ \phi$	0.18 ± 0.04	0.11 ± 0.01	0.29 ± 0.02	
	$D_s^+ \rightarrow K^{*+} K^0$	$\lambda_{ds}(T_P + C_V)$...				1.47 ± 0.09		1.44 ± 0.11	
$D_s \rightarrow SP$	$D_s^+ \rightarrow K^{*0} K^+$	$\lambda_{ds}(T_V + C_P)$		0.90 ± 0.51			0.20 ± 0.02		0.11 ± 0.02	
	$D_s^+ \rightarrow a_0^+ \pi^0$	$\frac{1}{\sqrt{2}}\lambda_{sd}(A - A')$				$\frac{1}{\sqrt{2}}\lambda_{sd}(A - A' + \bar{T})$				
	$\rightarrow a_0^0 \pi^+$	$\frac{1}{\sqrt{2}}\lambda_{sd}(-A + A')$				$\frac{1}{\sqrt{2}}\lambda_{sd}(-A + A' - \bar{T})$				
$D_s^+ \rightarrow a_0(980)^+ \pi^0 + a_0(980)^0 \pi^+ \rightarrow \pi^+ \pi^0 \eta$				-	$(1.6-3.0) \times 10^{-2}^a$		$(1.46 \pm 0.27)\%^b$			
$D_s \rightarrow VV$	$D_s^+ \rightarrow \bar{K}^{*0} K^{*+}$	$\lambda_{sd}(C_h + A_h)$			$D_s^+ \rightarrow \rho^+ \rho^0$		0			
	$D_s^+ \rightarrow \rho^+ \omega$	$\frac{1}{\sqrt{2}}\lambda_{sd}A_h$			$D_s^+ \rightarrow \rho^+ \phi$		$\lambda_{sd}T_h$			
	$D_s^+ \rightarrow \rho^+ K^{*0}$	$\lambda_d T_h + \lambda_s A_h$			$D_s^+ \rightarrow \rho^0 K^{*+}$		$\frac{1}{\sqrt{2}}(\lambda_d C_h - \lambda_s A_h)$			
	$D_s^+ \rightarrow K^{*+} \omega$	$\frac{1}{\sqrt{2}}(\lambda_d C_h + \lambda_s A_h)$			$D_s^+ \rightarrow K^{*+} \phi$		$\lambda_s(T_h + C_h + A_h)$			
	$D_s^+ \rightarrow K^{*+} K^{*0}$	$\lambda_{ds}(T_h + C_h)$								

$$|T_P| > |T_V| > |C_P| > |E_P| > |C_V| \gtrsim |E_V| > |A_{P,V}|$$

数据集



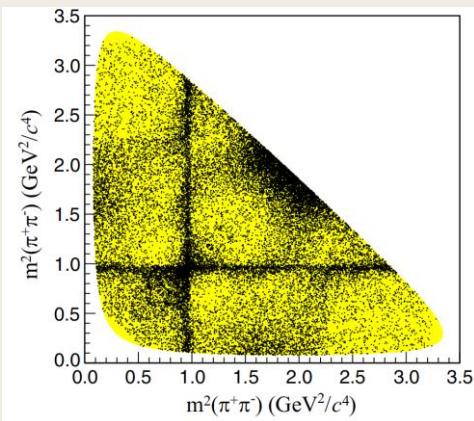
$e^+ e^- \rightarrow D_s^{*\pm} D_s^{\mp}$: **7.33 fb⁻¹** @4.128-4.226 GeV

样本	年份	亮度 (pb ⁻¹)
4130	2019	401.5
4160	2019	408.7
4180	2016	3189.0
4190	2012, 2017	570.0
4200	2017	526.0
4210	2013, 2017	572.0
4220	2013, 2017	569.2
4230	2012, 2013	1091.8

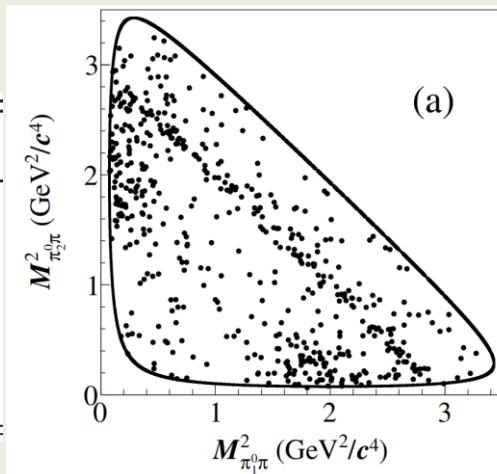
$$D_s^+ \rightarrow \pi^+ \pi^+ \pi^- \quad \& \quad D_s^+ \rightarrow \pi^+ \pi^0 \pi^0$$

$D_s^+ \rightarrow \pi^+ \pi^+ \pi^-$ Phys. Rev. D 106, 112006 (2022)
13797 events with $\sim 80\%$ purity

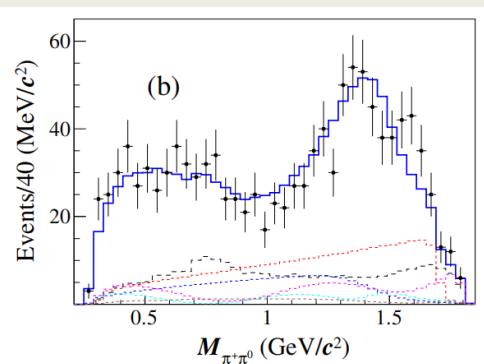
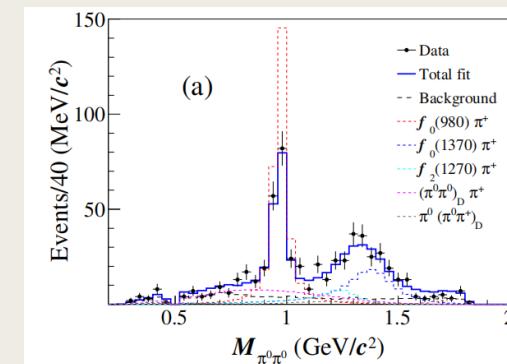
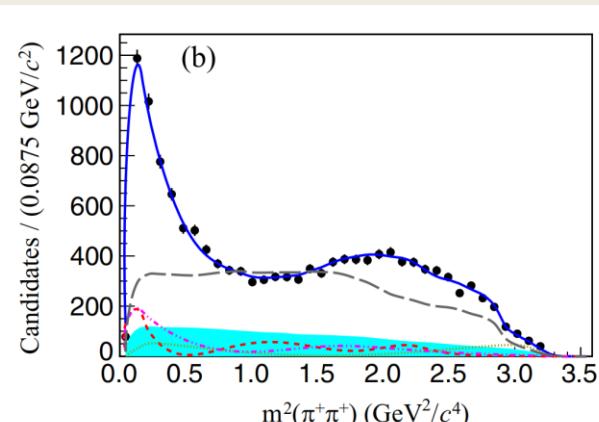
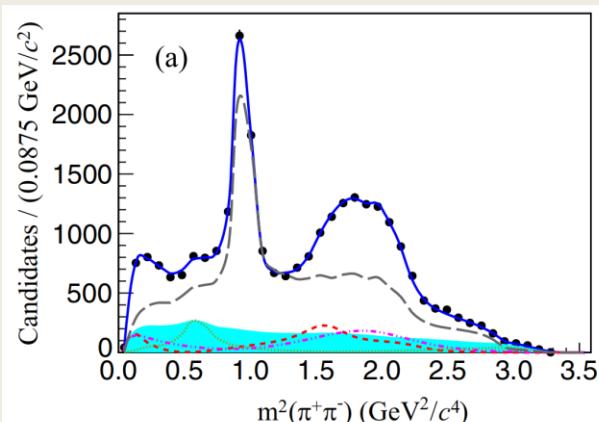
$D_s^+ \rightarrow \pi^+ \pi^0 \pi^0$ JHEP01(2022)052
572 events with $\sim 78\%$ purity



Decay mode	Fit fraction (%)
$f_2(1270)\pi^+$	$10.5 \pm 0.8 \pm 1.1$
$\rho(770)\pi^+$	$0.9 \pm 0.4 \pm 0.5$
$\rho(1450)\pi^+$	$1.3 \pm 0.4 \pm 0.5$
S wave	$84.2 \pm 0.8 \pm 1.2$
$\sum_i \mathcal{F}_i$	$96.8 \pm 2.4 \pm 3.3$



Amplitude	FF (%)	
$D_s^+ \rightarrow f_0(980)\pi^+$	$55.4 \pm 6.8 \pm 7.3$	
$D_s^+ \rightarrow f_0(1370)\pi^+$	$25.5 \pm 5.1 \pm 9.3$	
$D_s^+ \rightarrow f_2(1270)\pi^+$	$9.7 \pm 2.9 \pm 6.0$	
$D_s^+ \rightarrow \pi^+(\pi^0)_D\pi^0$	$21.8 \pm 6.8 \pm 3.6$	
$D_s^+ \rightarrow (\pi^+\pi^0)_D\pi^0$	$5.7 \pm 2.6 \pm 2.0$	



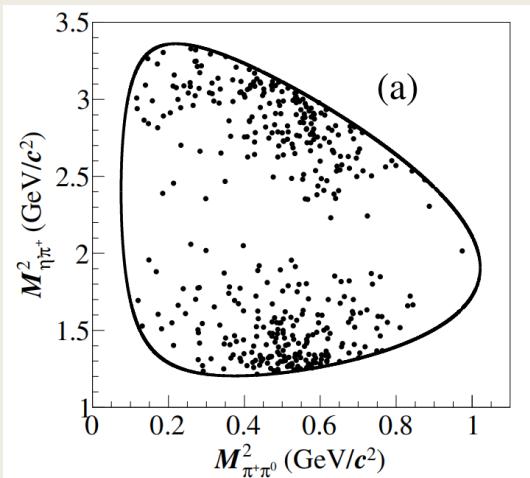
$$\frac{f_{0(2)} \rightarrow \pi^+ \pi^-}{f_{0(2)} \rightarrow \pi^0 \pi^0} \sim 2$$

$$D_s^+ \rightarrow \pi^+ \pi^0 \eta' \text{ & } D_s^+ \rightarrow \pi^+ \pi^0 \eta$$

$$\frac{1}{\sin \phi} \mathcal{A}(D_s^+ \rightarrow \pi^+ \omega) = \frac{\cos \phi}{\sin \phi} \mathcal{A}(D_s^+ \rightarrow \rho^+ \eta) + \mathcal{A}(D_s^+ \rightarrow \rho^+ \eta').$$

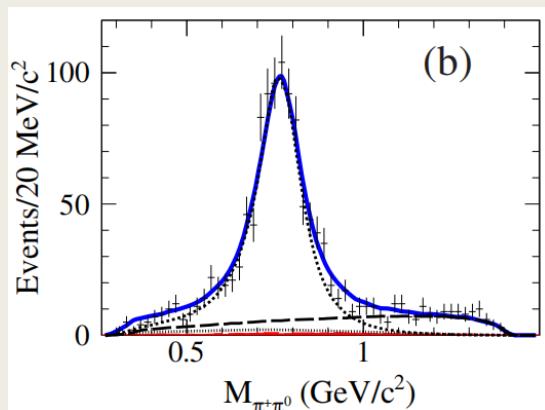
$\blacktriangleright 1.6\% < \mathcal{B}(D_s^+ \rightarrow \rho^+ \eta') < 3.9\%$

411 events with ~96% purity

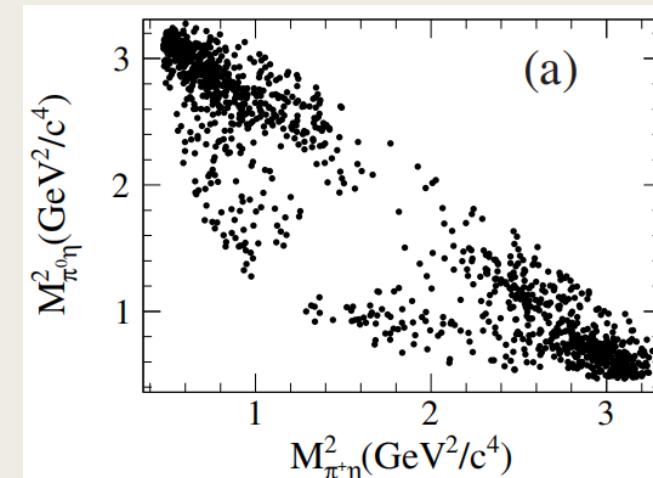


Phys. Rev. Lett. 123, 112001 (2019)

$$\mathcal{B}(D_s^+ \rightarrow \rho^+ \eta) = (7.44 \pm 0.52 \pm 0.38)\%$$

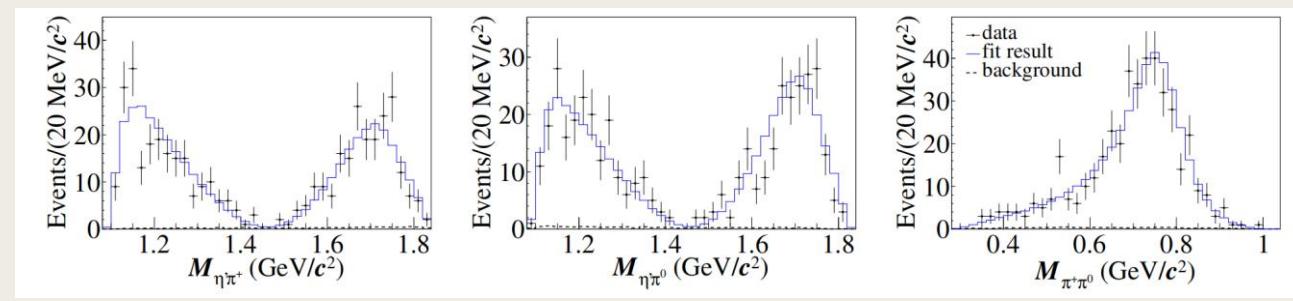


1239 events with ~98% purity



JHEP04(2022)058

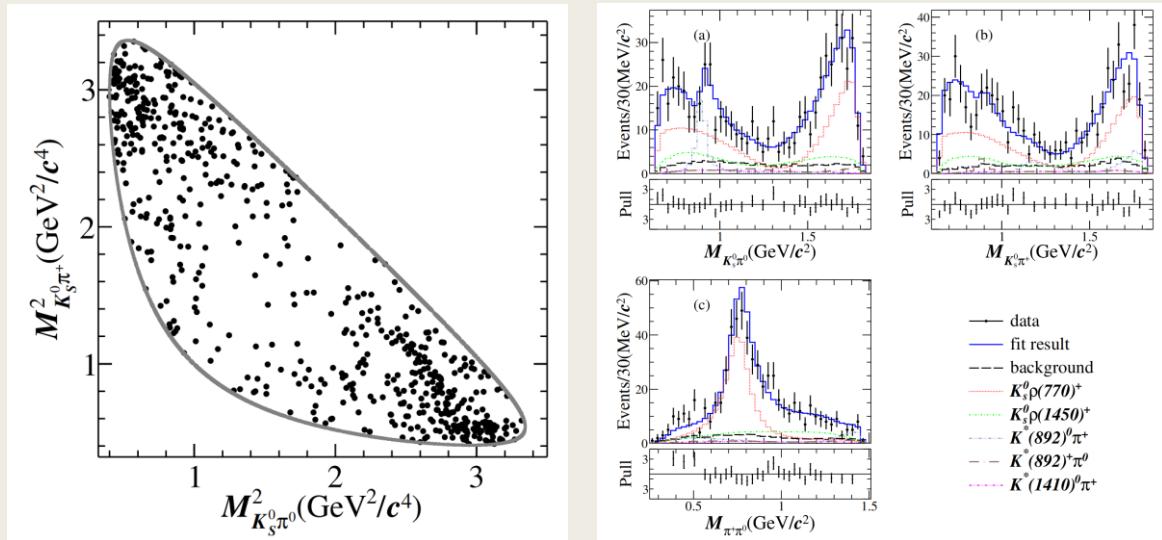
$$\mathcal{B}(D_s^+ \rightarrow \rho^+ \eta') = (6.15 \pm 0.25 \pm 0.18)\%$$



$$D_s^+ \rightarrow K_S^0 \pi^+ \pi^0 \text{ & } D_s^+ \rightarrow K^+ \pi^+ \pi^-$$

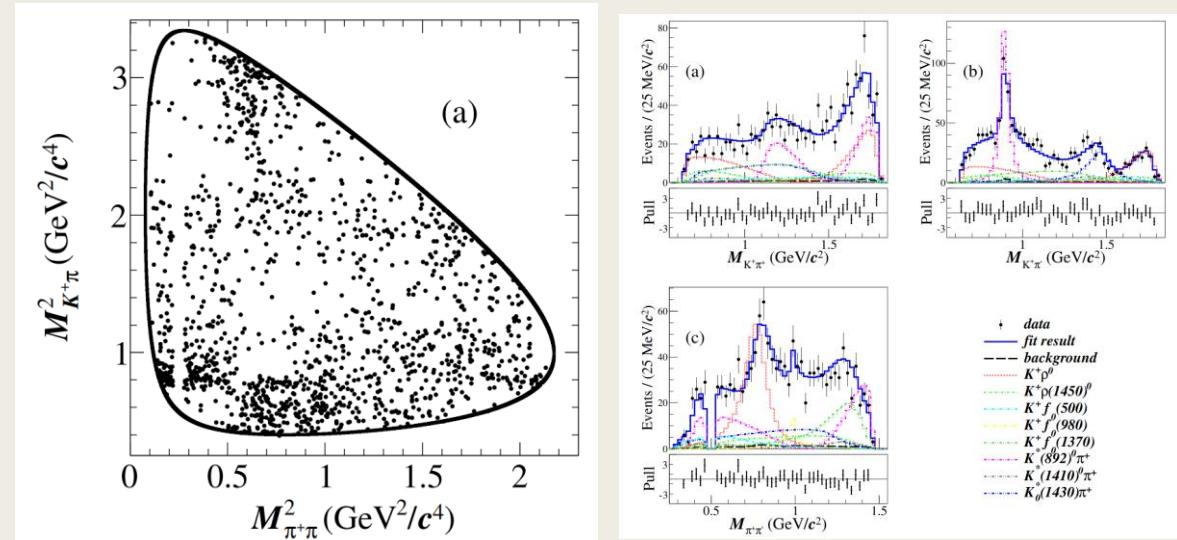
609 events with ~85% purity

JHEP06(2021)181



1356 events with ~95% purity

JHEP08(2022)196



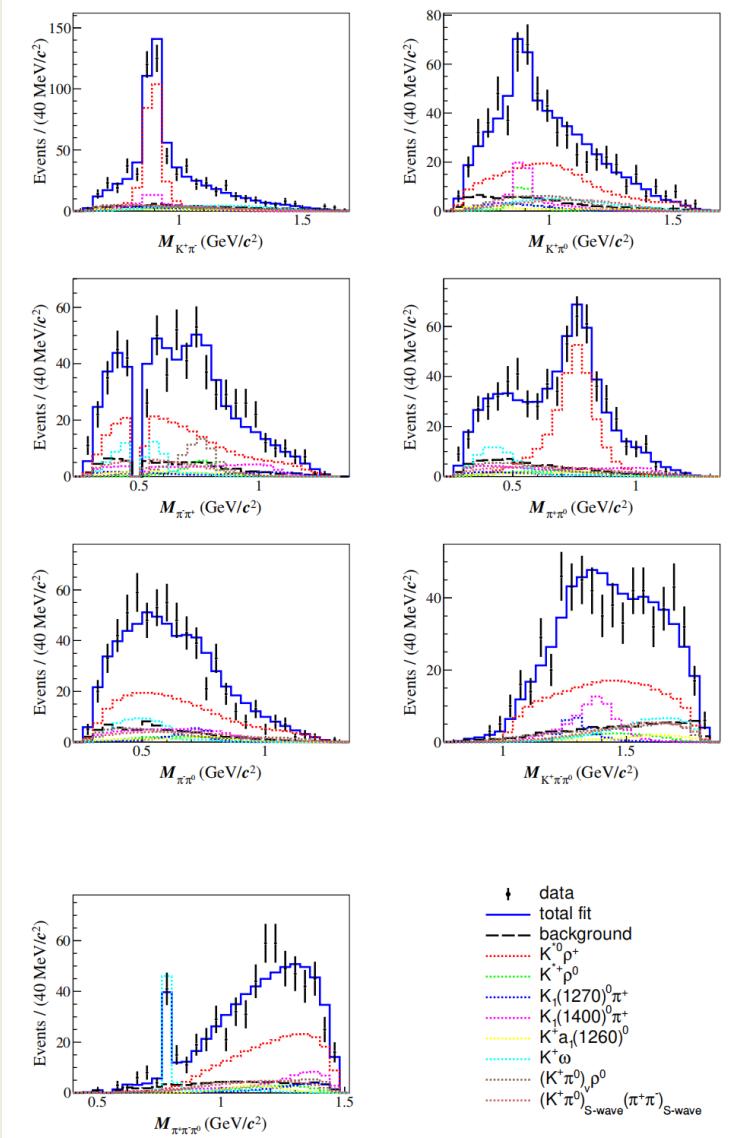
Intermediate process	BF (10^{-3})
$D_s^+ \rightarrow K_S^0 \rho^+$	$2.73 \pm 0.42 \pm 0.22$
$D_s^+ \rightarrow K_S^0 \rho(1450)^+$	$1.11 \pm 0.24 \pm 0.24$
$D_s^+ \rightarrow K^*(892)^0 \pi^+$	$0.45 \pm 0.12 \pm 0.05$
$D_s^+ \rightarrow K^*(892)^+ \pi^0$	$0.25 \pm 0.08 \pm 0.02$
$D_s^+ \rightarrow K^*(1410)^0 \pi^+$	$0.18 \pm 0.09 \pm 0.03$

Intermediate process	BF(10^{-3})
$D_s^+ \rightarrow K^+ \rho^0$	$1.96 \pm 0.19 \pm 0.23$
$D_s^+ \rightarrow K^+ \rho(1450)^0$	$0.80 \pm 0.19 \pm 0.18$
$D_s^+ \rightarrow K^*(892)^0 \pi^+$	$1.85 \pm 0.12 \pm 0.13$
$D_s^+ \rightarrow K^*(1410)^0 \pi^+$	$0.27 \pm 0.13 \pm 0.15$
$D_s^+ \rightarrow K_0^*(1430)^0 \pi^+$	$1.13 \pm 0.16 \pm 0.16$
$D_s^+ \rightarrow K^+ f_0(500)$	$0.44 \pm 0.13 \pm 0.27$
$D_s^+ \rightarrow K^+ f_0(980)$	$0.27 \pm 0.08 \pm 0.07$
$D_s^+ \rightarrow K^+ f_0(1370)$	$1.22 \pm 0.18 \pm 0.57$

$$D_s^+ \rightarrow K^+ \pi^+ \pi^- \pi^0$$

630 events with $\sim 85\%$ purity

JHEP09(2022)242



Intermediate process	BF (10^{-3})
$D_s^+[S] \rightarrow K^*(892)^0 \rho^+$	$1.41 \pm 0.23 \pm 0.07$
$D_s^+[P] \rightarrow K^*(892)^0 \rho^+$	$2.53 \pm 0.28 \pm 0.12$
$D_s^+ \rightarrow K^*(892)^0 \rho^+$	$3.95 \pm 0.35 \pm 0.17$
$D_s^+[P] \rightarrow K^*(892)^+ \rho^0$	$0.42 \pm 0.16 \pm 0.06$
$D_s^+ \rightarrow K^+ \omega$	$0.95 \pm 0.12 \pm 0.06$
$D_s^+ \rightarrow K_1(1270)^0 \pi^+, K_1(1270)^0 [S] \rightarrow K^+ \rho^-$	$0.39 \pm 0.12 \pm 0.06$
$D_s^+ \rightarrow K_1(1400)^0 \pi^+, K_1(1400)^0 [S] \rightarrow K^*(892)^+ \pi^-$	$0.55 \pm 0.09 \pm 0.03$
$D_s^+ \rightarrow K_1(1400)^0 \pi^+, K_1(1400)^0 [S] \rightarrow K^*(892)^0 \pi^0$	$0.59 \pm 0.09 \pm 0.02$
$D_s^+ \rightarrow K_1(1400)^0 \pi^+, K_1(1400)^0 [S] \rightarrow K^*(892) \pi$	$1.10 \pm 0.19 \pm 0.04$
$D_s^+ \rightarrow a_1(1260)^0 K^+, a_1(1260)^0 [S] \rightarrow \rho^+ \pi^-$	$0.19 \pm 0.07 \pm 0.09$
$D_s^+ \rightarrow a_1(1260)^0 K^+, a_1(1260)^0 [S] \rightarrow \rho^- \pi^+$	$0.19 \pm 0.07 \pm 0.09$
$D_s^+ \rightarrow a_1(1260)^0 K^+, a_1(1260)^0 [S] \rightarrow \rho \pi$	$0.32 \pm 0.12 \pm 0.15$
$D_s^+[S] \rightarrow (K^+ \pi^0)_V \rho^0$	$1.01 \pm 0.20 \pm 0.06$
$D_s^+ \rightarrow (K^+ \pi^0)_{S-wave} (\pi^+ \pi^-)_{S-wave}$	$0.93 \pm 0.22 \pm 0.09$

$$D_s^+ \rightarrow K^+ \rho^0, D_s^+ \rightarrow K^+ \omega \sim \text{Diagram C}$$

TDA: ~ 1

FAT: ~ 30

Experiment: ~ 2

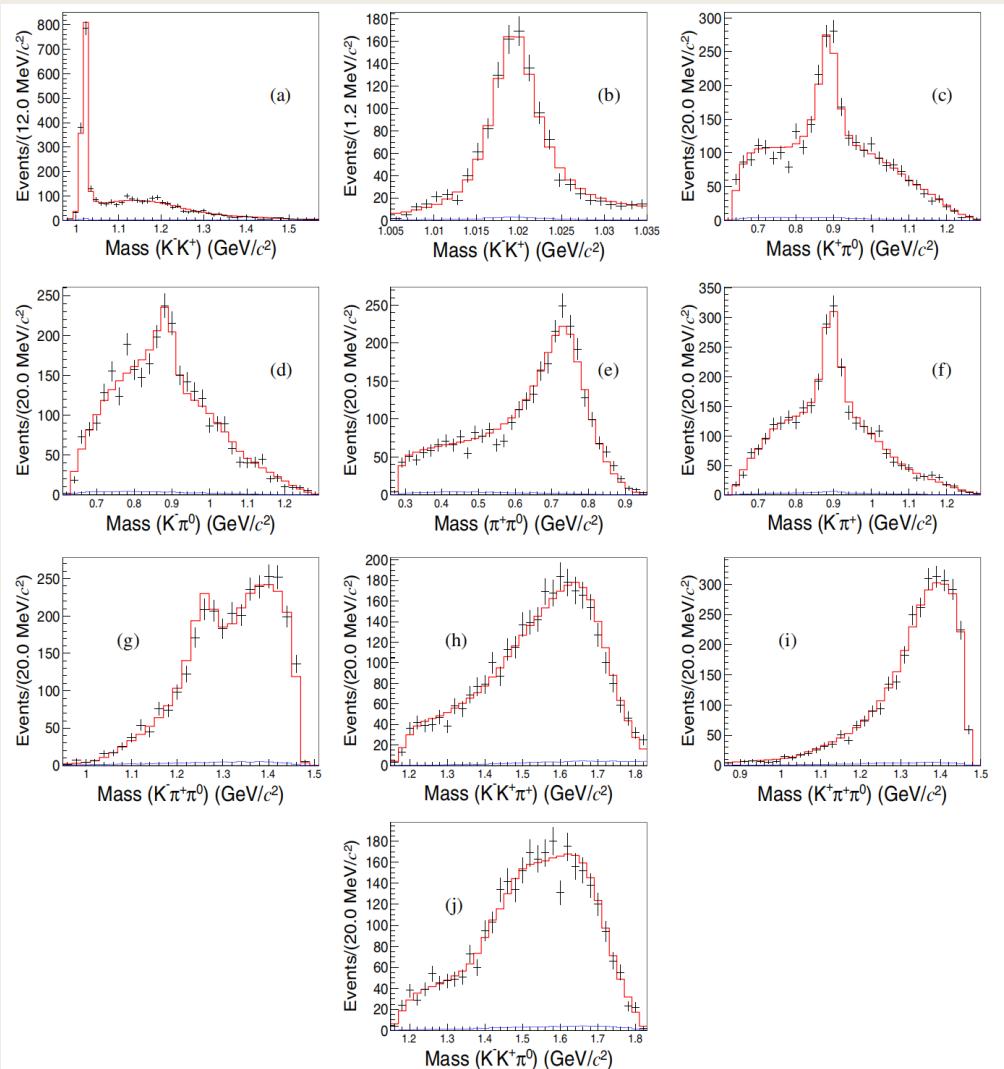
PhysRevD.109.073008

PhysRevD.89.054006

$D_s^+ \rightarrow K^+ K^- \pi^+ \pi^0$

3088 events with $\sim 97\%$ purity

Phys. Rev. D 104, 032011 (2021)



Process	BF (%)
$D_s^+[S] \rightarrow \phi\rho^+$	$2.10 \pm 0.09 \pm 0.13$
$D_s^+[P] \rightarrow \phi\rho^+$	$0.52 \pm 0.05 \pm 0.02$
$D_s^+[D] \rightarrow \phi\rho^+$	$0.18 \pm 0.04 \pm 0.02$
$D_s^+ \rightarrow \phi\rho^+$	$2.75 \pm 0.07 \pm 0.15$
$D_s^+[S] \rightarrow \bar{K}^{*0}K^{*+}$	$0.88 \pm 0.05 \pm 0.03$
$D_s^+[P] \rightarrow \bar{K}^{*0}K^{*+}$	$0.37 \pm 0.03 \pm 0.02$
$D_s^+[D] \rightarrow \bar{K}^{*0}K^{*+}$	$0.18 \pm 0.03 \pm 0.01$
$D_s^+ \rightarrow \bar{K}^{*0}K^{*+}$	$1.25 \pm 0.05 \pm 0.06$
$D_s^+ \rightarrow \bar{K}_1^0(1270)K^+, \bar{K}_1^0(1270) \rightarrow K^-\rho^+$	$0.57 \pm 0.05 \pm 0.04$
$D_s^+ \rightarrow \bar{K}_1^0(1270)K^+, \bar{K}_1^0(1270)[S] \rightarrow K^*\pi$	$0.21 \pm 0.04 \pm 0.03$
$D_s^+ \rightarrow \bar{K}_1^0(1270)K^+, \bar{K}_1^0(1270)[D] \rightarrow K^*\pi$	$0.07 \pm 0.02 \pm 0.01$
$D_s^+ \rightarrow \bar{K}_1^0(1270)K^+, \bar{K}_1^0(1270) \rightarrow K^*\pi$	$0.29 \pm 0.04 \pm 0.04$
$D_s^+ \rightarrow \bar{K}_1^0(1400)K^+, \bar{K}_1^0(1400) \rightarrow K^*\pi$	$0.44 \pm 0.06 \pm 0.07$
$D_s^+ \rightarrow a_0^0(980)\rho^+$	$0.19 \pm 0.03 \pm 0.03$
$D_s^+ \rightarrow f_1(1420)\pi^+, f_1(1420) \rightarrow K^{*\mp}K^\pm$	$0.13 \pm 0.02 \pm 0.01$
$D_s^+ \rightarrow f_1(1420)\pi^+, f_1(1420) \rightarrow a_0^0(980)\pi^0$	$0.04 \pm 0.01 \pm 0.01$
$D_s^+ \rightarrow \eta(1475)\pi^+, \eta(1475) \rightarrow a_0^0(980)\pi^0$	$0.07 \pm 0.02 \pm 0.02$

LHCb: J. High Energy Phys. 02 (2019) 126.

CLEO: Phys. Rev. D 85, 122002 (2012).

$$R_{K_1(1270)} = \frac{B(K_1^0 \rightarrow K^*\pi)}{B(K_1^0 \rightarrow K\rho)} = 0.99 \pm 0.15 \pm 0.18$$

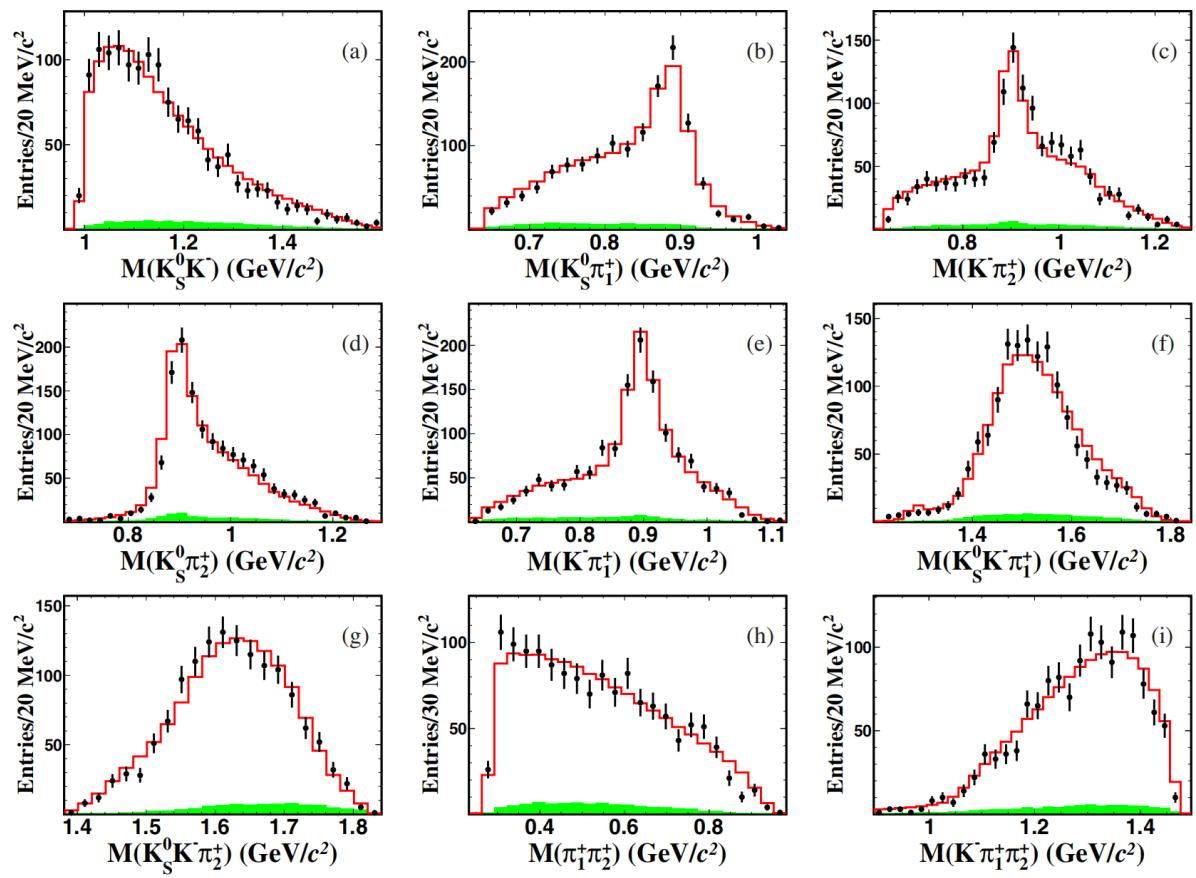
BESIII via $D^{+/0} \rightarrow K_1(1270)e^+\nu_e$: $(0.203 \pm 0.021 \pm 0.087)$

2503.02196

$$D_s^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$$

1318 events with $\sim 95\%$ purity

Phys. Rev. D 103, 092006 (2021)



Process	BF(10^{-3})	
	This analysis	PDG
$D_s^+[S] \rightarrow K^*(892)^+ \bar{K}^*(892)^0$	$5.01 \pm 0.49 \pm 0.78$	
$D_s^+[P] \rightarrow K^*(892)^+ \bar{K}^*(892)^0$	$1.10 \pm 0.16 \pm 0.10$	
$D_s^+[D] \rightarrow K^*(892)^+ \bar{K}^*(892)^0$	$0.65 \pm 0.12 \pm 0.10$	
$D_s^+ \rightarrow K^*(892)^+ \bar{K}^*(892)^0$	$5.93 \pm 0.47 \pm 0.74$	
$D_s^+ \rightarrow K^*(892)^+ (K^- \pi^+)_{S\text{-wave}}$	$0.73 \pm 0.17 \pm 0.15$	
$D_s^+ \rightarrow \bar{K}^*(892)^0 (K_S^0 \pi^+)_{S\text{-wave}}$	$1.06 \pm 0.16 \pm 0.13$	
$D_s^+ \rightarrow \eta(1475) \pi^+, \eta(1475) \rightarrow a_0(980)^- \pi^+$	$1.57 \pm 0.39 \pm 0.76$	
$D_s^+ \rightarrow \eta(1475) \pi^+, \eta(1475) \rightarrow \bar{K}^*(892)^0 K_S^0$	$0.32 \pm 0.10 \pm 0.10$	
$D_s^+ \rightarrow \eta(1475) \pi^+, \eta(1475) \rightarrow K^*(892)^+ K^-$	$0.32 \pm 0.10 \pm 0.10$	
$D_s^+ \rightarrow \eta(1475) \pi^+, \eta(1475) \rightarrow K^*(892) K$	$0.72 \pm 0.21 \pm 0.14$	
$D_s^+ \rightarrow \eta(1475) \pi^+, \eta(1475) \rightarrow (K_S^0 \pi^+)_{S\text{-wave}} K^-$	$3.44 \pm 0.54 \pm 1.10$	
$D_s^+ \rightarrow f_1(1285) \pi^+, f_1(1285) \rightarrow a_0(980)^- \pi^+$	$0.33 \pm 0.08 \pm 0.10$	
$D_s^+ \rightarrow (K^*(892)^+ K^-)_P \pi^+, (K^*(892)^+ K^-)_P \rightarrow K^*(892)^+ K^-$	$1.58 \pm 0.28 \pm 0.26$	
$D_s^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$	$14.60 \pm 0.46 \pm 0.48$	16.50 ± 1.00

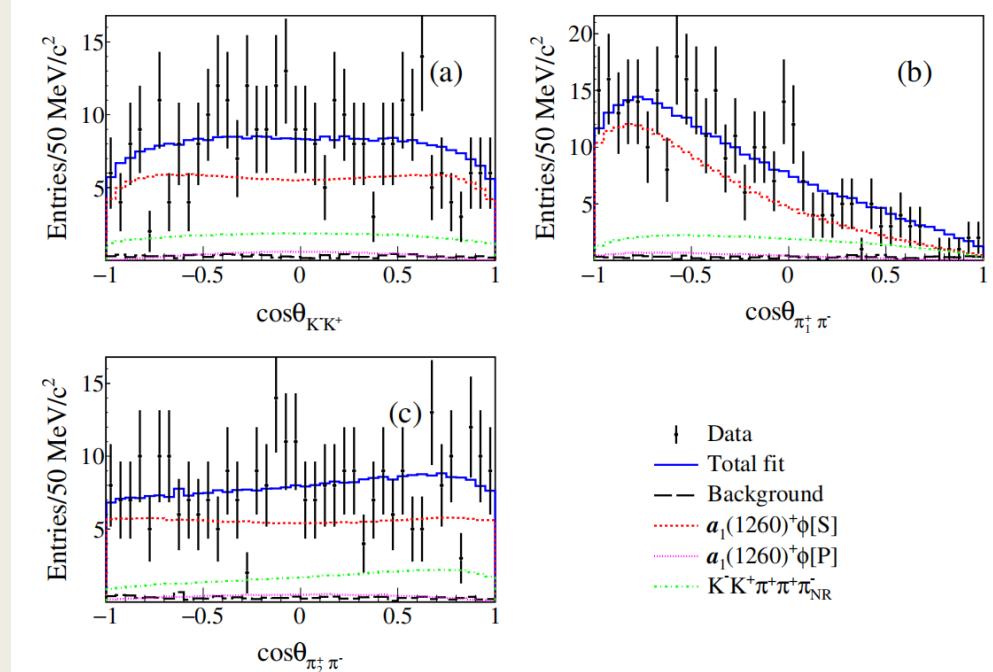
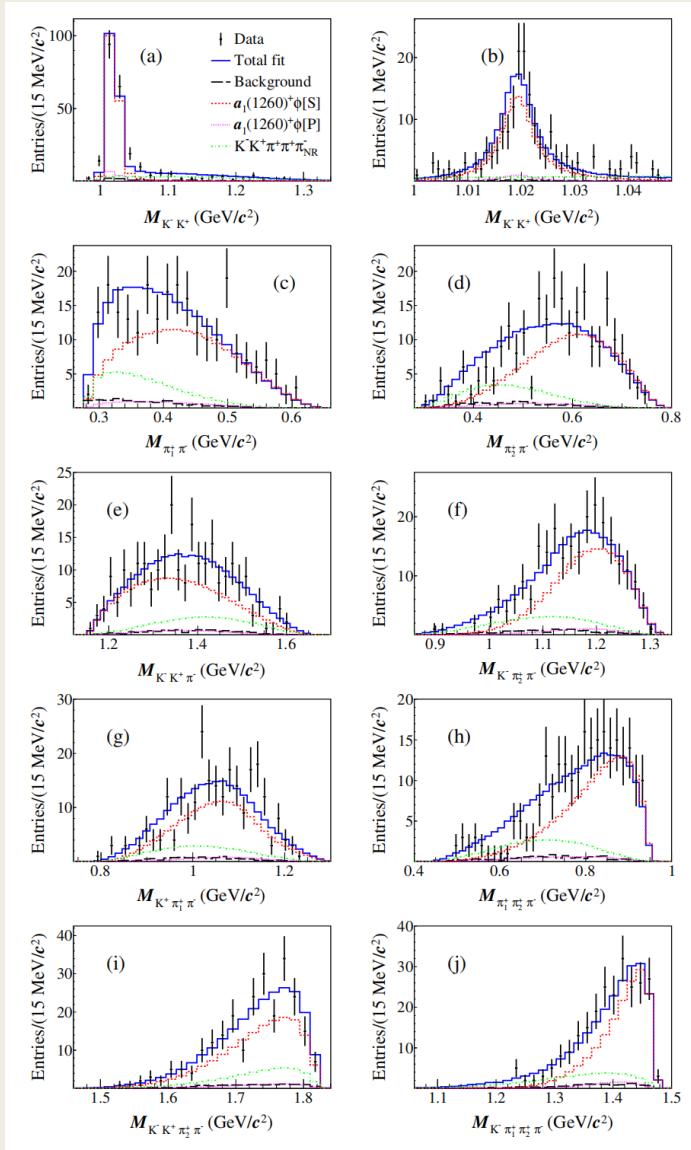
$$D_s^+ \rightarrow \bar{K}^{*0} K^{*+} = (5.64 \pm 0.23 \pm 0.27)\% \text{ from } D_s^+ \rightarrow K^+ K^- \pi^+ \pi^0$$

$$D_s^+ \rightarrow \bar{K}^{*0} K^{*+} = (5.34 \pm 0.39 \pm 0.64)\%$$

$$D_s^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$$

243 events with $\sim 96\%$ purity

JHEP07(2022)051

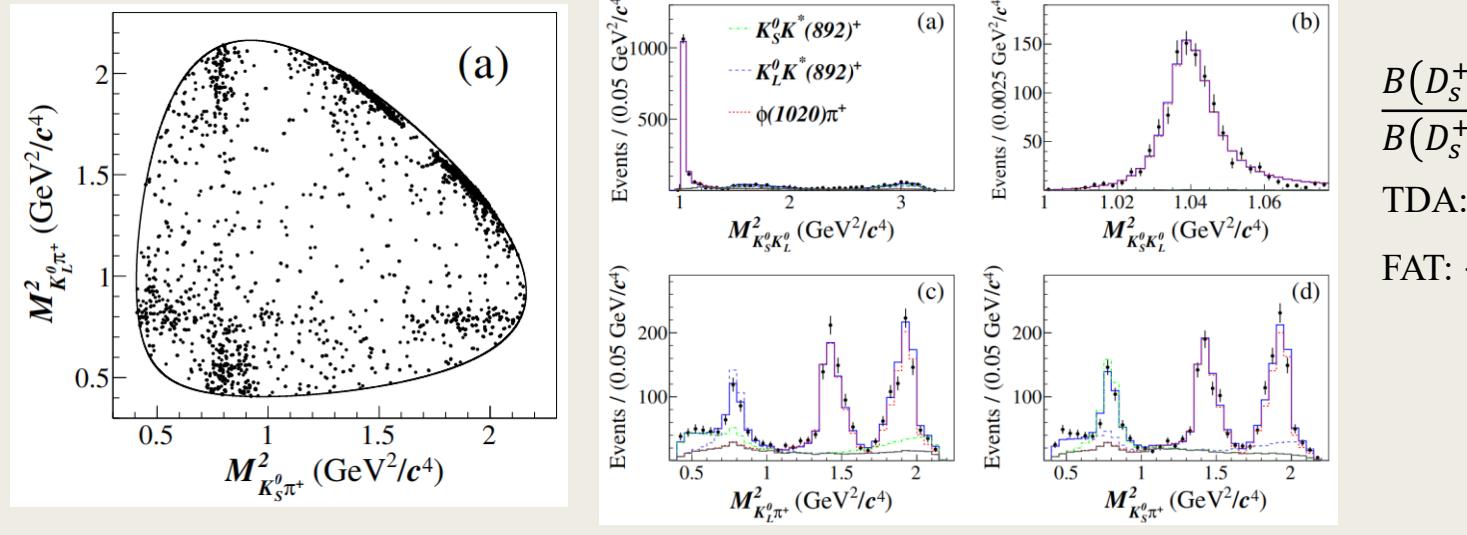


Intermediate process	BF (10^{-3})	PDG (10^{-3})
$D_s^+[S] \rightarrow a_1(1260)^+ \phi, a_1(1260)^+[S] \rightarrow \rho^0 \pi^+$	$4.82 \pm 0.40 \pm 0.29$	
$D_s^+[P] \rightarrow a_1(1260)^+ \phi, a_1(1260)^+[S] \rightarrow \rho^0 \pi^+$	$0.34 \pm 0.11 \pm 0.05$	
$D_s^+ \rightarrow a_1(1260)^+ \phi$	$5.15 \pm 0.41 \pm 0.32$	7.4 ± 1.2
$D_s^+ \rightarrow (K^- K^+ \pi^+ \pi^+ \pi^-)_{NR}$	$1.44 \pm 0.22 \pm 0.10$	0.9 ± 0.7

$$D_s^+ \rightarrow K_S^0 K_L^0 \pi^+$$

2310 events with $\sim 78\%$ purity

arXiv:2503.11383

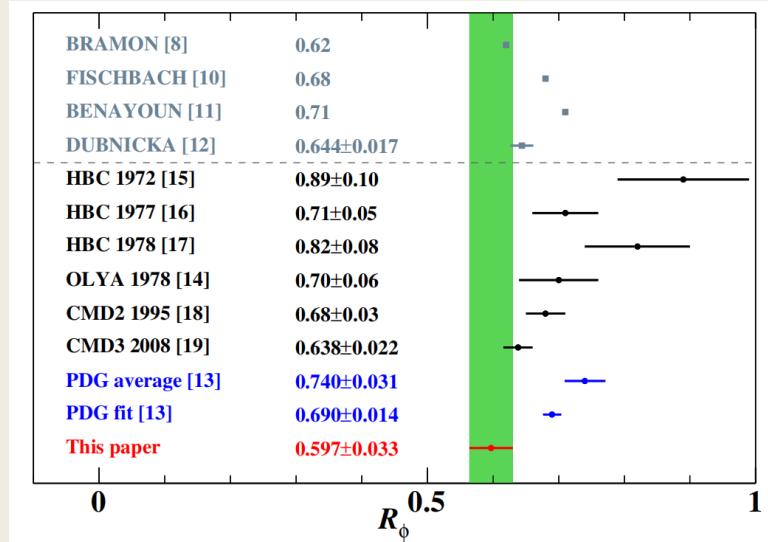


Amplitude	Phase (rad)	FF (%)	BF (%)	σ
$D_s^+ \rightarrow \phi \pi^+$	0.0(fixed)	$70.9 \pm 1.3 \pm 1.5$	$1.32 \pm 0.05 \pm 0.04$	>10
$D_s^+ \rightarrow K_L^0 K^*(892)^+$	$0.68 \pm 0.17 \pm 0.21$	$22.8 \pm 1.3 \pm 1.5$	$0.42 \pm 0.03 \pm 0.03$	>10
$D_s^+ \rightarrow K_S^0 K^*(892)^+$	$-2.40 \pm 0.18 \pm 0.31$	$17.4 \pm 1.2 \pm 0.9$	$0.31 \pm 0.02 \pm 0.02$	>10

$$\frac{B(D_s^+ \rightarrow K_S^0 K^*) - B(D_s^+ \rightarrow K_L^0 K^*)}{B(D_s^+ \rightarrow K_S^0 K^*) + B(D_s^+ \rightarrow K_L^0 K^*)} = (-13.4 \pm 5.0 \pm 3.4)\%$$

TDA: $-0.164 \pm 0.032 / -0.159 \pm 0.028$

FAT: -0.066 ± 0.191

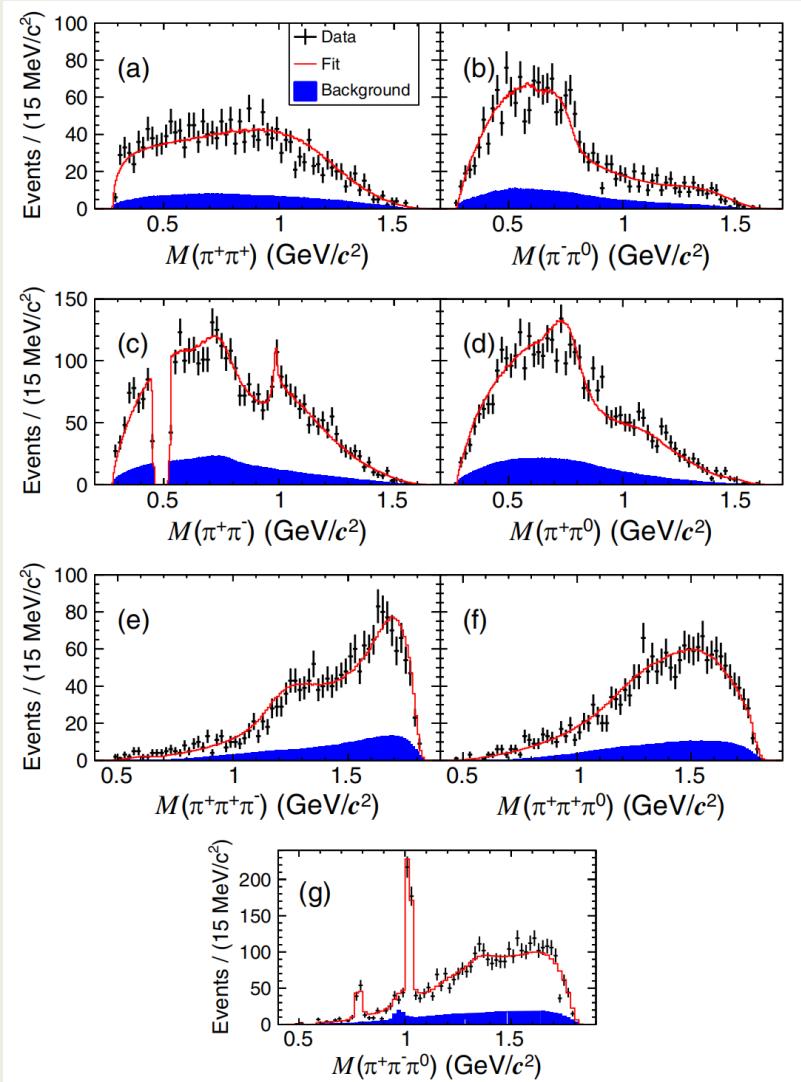


$$R_\phi = B(\phi \rightarrow K_S^0 K_L^0) / B(\phi \rightarrow K^+ K^-)$$

$D_s^+ \rightarrow \pi^+ \pi^+ \pi^- \pi^0$

1552 events with ~80% purity

Phys. Rev. Lett. 134, 011904 (2025)



Component	Phase (rad)	FF (%)	BF (10 ⁻³)
$f_0(1370)\rho^+$	0.0(fixed)	$24.9 \pm 3.8 \pm 2.1$	$5.08 \pm 0.80 \pm 0.43$
$f_0(980)\rho^+$	$3.99 \pm 0.13 \pm 0.07$	$12.6 \pm 2.1 \pm 1.0$	$2.57 \pm 0.44 \pm 0.20$
$f_2(1270)\rho^+$	$1.11 \pm 0.10 \pm 0.10$	$9.5 \pm 1.7 \pm 0.6$	$1.94 \pm 0.36 \pm 0.12$
$(\rho^+\rho^0)_S$	$1.10 \pm 0.18 \pm 0.10$	$3.5 \pm 1.2 \pm 0.6$	$0.71 \pm 0.25 \pm 0.12$
$[\rho(1450)^+\rho^0]_S$	$0.43 \pm 0.18 \pm 0.17$	$4.6 \pm 1.3 \pm 0.8$	$0.94 \pm 0.27 \pm 0.16$
$[\rho^+\rho(1450)^0]_P$	$4.58 \pm 0.16 \pm 0.09$	$8.6 \pm 1.3 \pm 0.4$	$1.75 \pm 0.27 \pm 0.08$
$\phi[(\rho\pi) \rightarrow \pi^+\pi^-\pi^0]\pi^+$	$2.90 \pm 0.15 \pm 0.18$	$24.9 \pm 1.2 \pm 0.4$	$5.08 \pm 0.32 \pm 0.10$
$\omega[(\rho\pi) \rightarrow \pi^+\pi^-\pi^0]\pi^+$	$3.22 \pm 0.21 \pm 0.09$	$6.9 \pm 0.8 \pm 0.3$	$1.41 \pm 0.17 \pm 0.06$
$a_1^+(\rho^0\pi^+)\pi^0$	$3.78 \pm 0.16 \pm 0.12$	$12.5 \pm 1.6 \pm 1.0$	$2.55 \pm 0.34 \pm 0.20$
$a_1^0[(\rho\pi)_S \rightarrow \pi^+\pi^-\pi^0]\pi^+$	$4.82 \pm 0.15 \pm 0.12$	$6.3 \pm 1.9 \pm 1.2$	$1.29 \pm 0.39 \pm 0.24$
$\pi(1300)^0[(\rho\pi)_P \rightarrow \pi^+\pi^-\pi^0]\pi^+$	$2.22 \pm 0.14 \pm 0.08$	$11.7 \pm 2.3 \pm 2.2$	$2.39 \pm 0.48 \pm 0.45$

- $R_\phi = \mathcal{B}(D_s^+ \rightarrow \phi(\rightarrow \pi^+\pi^-\pi^0)\pi^+)/\mathcal{B}(D_s^+ \rightarrow \phi(\rightarrow K^+K^-)\pi^+)$
 $= \mathcal{B}(\phi \rightarrow \pi^+\pi^-\pi^0)/\mathcal{B}(\phi \rightarrow K^+K^-) = 0.230 \pm 0.014 \pm 0.010$

R_ϕ (PDG) = 0.313 ± 0.010

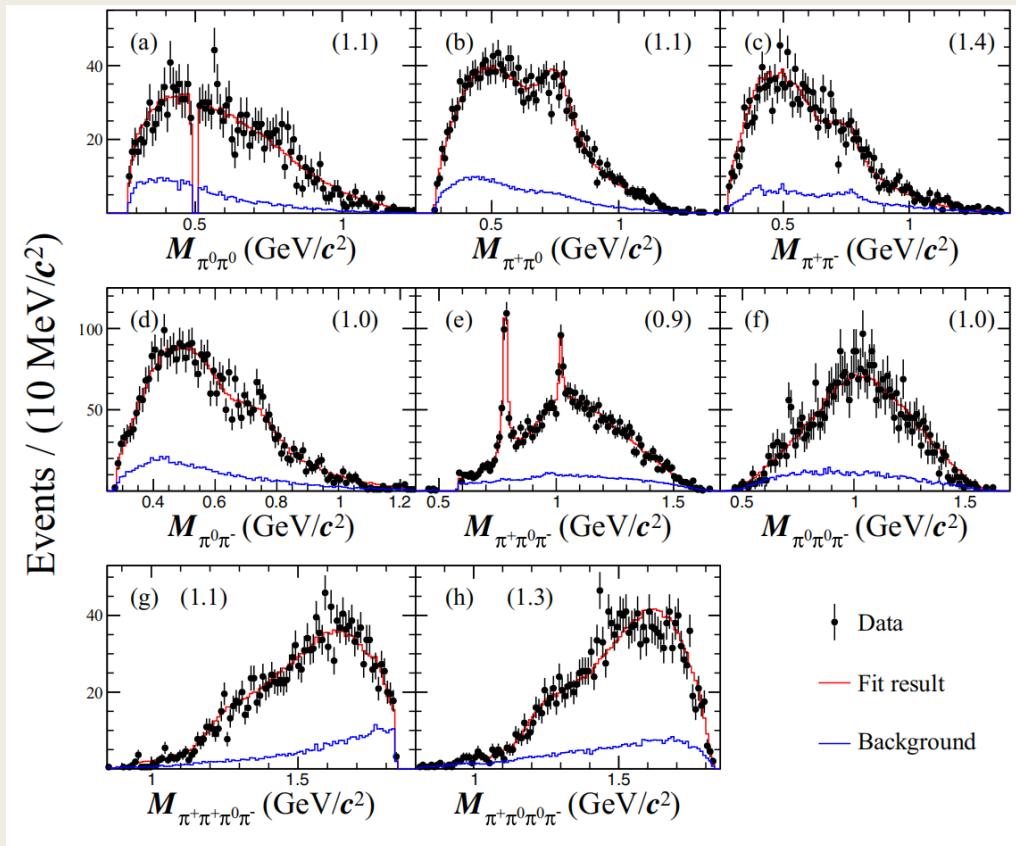
大于4倍标准偏差

- $D_s^+ \rightarrow f_0(980)\rho^+$ --- W -外发射过程主导
- $D_s^+ \rightarrow \omega\pi^+$ --- 纯 W -湮灭过程

$$D_s^+ \rightarrow \pi^+ \pi^+ \pi^- \pi^0 \pi^0$$

1888 events with ~80% purity

Phys. Rev. Lett. 134, 201902 (2025)



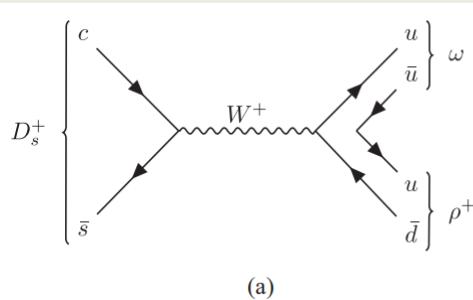
$$R_\phi = \mathcal{B}(D_s^+ \rightarrow \phi(\rightarrow \pi^+ \pi^- \pi^0) \rho^+) / \mathcal{B}(D_s^+ \rightarrow \phi(\rightarrow K^+ K^-) \rho^+)$$

$$= \mathcal{B}(\phi \rightarrow \pi^+ \pi^- \pi^0) / \mathcal{B}(\phi \rightarrow K^+ K^-) = 0.222 \pm 0.019 \pm 0.016$$

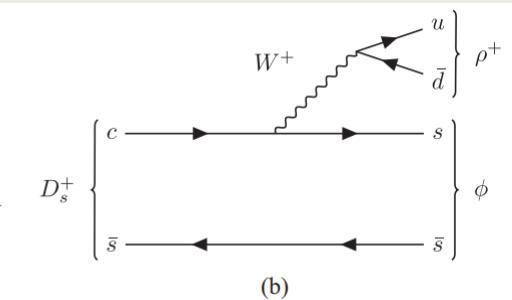
$$R_\phi (\text{PDG}) = 0.313 \pm 0.010$$

大于3倍标准偏差

纯W-湮灭过程



纯W-外发射过程



Amplitude	Phase ϕ (rad)	FF (%)	BF (%)	Significance
$D_s^+[S] \rightarrow \omega\rho^+$	0.0 (fixed)	$6.12 \pm 1.34^{+0.44}_{-0.52}$	$0.30 \pm 0.07^{+0.02}_{-0.03}$	$> 10\sigma$
$D_s^+[P] \rightarrow \omega\rho^+$	$2.92 \pm 0.13^{+0.05}_{-0.07}$	$5.05 \pm 0.86^{+0.83}_{-0.79}$	$0.25 \pm 0.04^{+0.04}_{-0.04}$	6.1σ
$D_s^+[D] \rightarrow \omega\rho^+$	$4.91 \pm 0.09^{+0.04}_{-0.09}$	$10.36 \pm 1.26^{+0.70}_{-1.45}$	$0.52 \pm 0.07^{+0.04}_{-0.07}$	$> 10\sigma$
$D_s^+ \rightarrow \omega\rho^+$...	$19.98 \pm 1.40^{+0.92}_{-1.20}$	$0.99 \pm 0.08^{+0.05}_{-0.07}$...
$D_s^+[S] \rightarrow \phi\rho^+$	$0.72 \pm 0.11^{+0.06}_{-0.09}$	$11.62 \pm 0.94^{+0.46}_{-0.39}$	$3.32 \pm 0.29^{+0.19}_{-0.17}$	$> 10\sigma$
$D_s^+[P] \rightarrow \phi\rho^+$	$1.34 \pm 0.15^{+0.07}_{-0.30}$	$2.22 \pm 0.42^{+0.15}_{-0.20}$	$0.63 \pm 0.12^{+0.05}_{-0.06}$	$> 10\sigma$
$D_s^+ \rightarrow \phi\rho^+$...	$13.86 \pm 1.03^{+0.47}_{-0.35}$	$3.98 \pm 0.33^{+0.21}_{-0.19}$...
$D_s^+ \rightarrow \rho(1450)^+\pi^0, \rho(1450)^+ \rightarrow \omega\pi^+$	$1.55 \pm 0.11^{+0.06}_{-0.08}$	$7.84 \pm 0.83^{+0.49}_{-0.58}$	$0.39 \pm 0.04^{+0.03}_{-0.03}$	6.3σ
$D_s^+[S] \rightarrow a_1(1260)^0\rho^+, a_1(1260)^0[S] \rightarrow \rho^+\pi^-$	$4.61 \pm 0.10^{+0.14}_{-0.15}$	$5.19 \pm 0.50^{+0.22}_{-0.21}$	$0.23 \pm 0.02^{+0.01}_{-0.01}$	$> 10\sigma$
$D_s^+[P] \rightarrow a_1(1260)^0\rho^+, a_1(1260)^0[S] \rightarrow \rho^+\pi^-$	$0.06 \pm 0.10^{+0.14}_{-0.15}$	$6.25 \pm 0.52^{+0.23}_{-0.25}$	$0.50 \pm 0.04^{+0.02}_{-0.02}$	$> 10\sigma$
$D_s^+ \rightarrow a_1(1260)^0\rho^+, a_1(1260)^0 \rightarrow \rho^+\pi^-$...	$11.43 \pm 0.67^{+0.35}_{-0.35}$	$0.50 \pm 0.04^{+0.02}_{-0.02}$...
$D_s^+[S] \rightarrow a_1(1260)^0\rho^+, a_1(1260)^0[S] \rightarrow \rho^-\pi^+$	$4.61 \pm 0.10^{+0.14}_{-0.15}$	$3.64 \pm 0.35^{+0.17}_{-0.17}$	$0.16 \pm 0.02^{+0.01}_{-0.01}$	$> 10\sigma$
$D_s^+[P] \rightarrow a_1(1260)^0\rho^+, a_1(1260)^0[S] \rightarrow \rho^-\pi^+$	$0.06 \pm 0.10^{+0.14}_{-0.15}$	$3.76 \pm 0.31^{+0.20}_{-0.20}$	$0.17 \pm 0.01^{+0.01}_{-0.01}$	$> 10\sigma$
$D_s^+ \rightarrow a_1(1260)^0\rho^+, a_1(1260)^0 \rightarrow \rho^-\pi^+$...	$7.39 \pm 0.44^{+0.26}_{-0.26}$	$0.33 \pm 0.02^{+0.02}_{-0.02}$...
$D_s^+[S] \rightarrow a_1(1260)^+\rho^0, a_1(1260)^+[S] \rightarrow \rho^+\pi^0$	$1.85 \pm 0.11^{+0.18}_{-0.19}$	$9.43 \pm 1.14^{+1.13}_{-1.13}$	$0.41 \pm 0.05^{+0.05}_{-0.05}$	9.2σ
$D_s^+[P] \rightarrow a_1(1260)^+\rho^0, a_1(1260)^+[S] \rightarrow \rho^+\pi^0$	$3.52 \pm 0.12^{+0.20}_{-0.21}$	$7.10 \pm 0.88^{+0.51}_{-0.51}$	$0.31 \pm 0.04^{+0.02}_{-0.02}$	$> 10\sigma$
$D_s^+ \rightarrow a_1(1260)^+\rho^0, a_1(1260)^+ \rightarrow \rho^+\pi^0$...	$16.53 \pm 1.37^{+1.52}_{-1.52}$	$0.73 \pm 0.07^{+0.07}_{-0.07}$...
$D_s^+ \rightarrow b_1(1235)^+\pi^0, b_1(1235)^+[S] \rightarrow \omega\pi^+$	$4.27 \pm 0.10^{+0.05}_{-0.06}$	$10.79 \pm 0.98^{+0.68}_{-0.68}$	$0.53 \pm 0.05^{+0.03}_{-0.03}$	9.7σ
$D_s^+ \rightarrow b_1(1235)^0\pi^+, b_1(1235)^0[S] \rightarrow \omega\pi^0$	$1.22 \pm 0.09^{+0.04}_{-0.06}$	$14.60 \pm 1.20^{+0.52}_{-0.49}$	$0.72 \pm 0.06^{+0.05}_{-0.05}$	$> 10\sigma$

$D > S > P!$

总结

- D_s^+ 介子强子末态衰变是研究 W -湮灭过程的良好环境
 - $D_s^+ \rightarrow \rho^0 \pi^+, a_0(980) \pi^+, \omega \rho^+ \dots$
- BESIII D_s^+ 强子衰变振幅分析硕果累累：已发表/在投17篇文章
 - 3 (1) PRL, 7 PRD, 6 JHEP
- 多个黄金标记道模型
 - $D_s^+ \rightarrow K^+ K^- \pi^+, D_s^+ \rightarrow K^+ K^- \pi^+ \pi^0, D_s^+ \rightarrow \pi^+ \pi^- \pi^0 \dots$
- 为轻标量介子研究提供许多重要信息
 - $a_0(980), \phi, a_0(1817) \dots$

▼ D_s^\pm Amplitude analyses
$D_s^+ \rightarrow K^+ K^- \pi^+$ partial wave analyses
$D_s^+ \rightarrow K^+ K_S \pi^0$ partial wave analyses
$D_s^+ \rightarrow 2 \pi^+ \pi^-$ partial wave analyses
$D_s^+ \rightarrow 2 \pi^+ \pi^- \pi^0$ partial wave analyses
$D_s^+ \rightarrow 2 \pi^+ \pi^- \eta$ partial wave analyses
$D_s^+ \rightarrow \pi^+ \pi^0 \eta'$ partial wave analyses.
$D_s^+ \rightarrow \pi^+ 2 \pi^0$ partial wave analyses.
$D_s^+ \rightarrow K^+ \pi^+ \pi^-$ partial wave analyses
$D_s^+ \rightarrow K_S^0 \pi^+ \pi^0$ partial wave analyses
$D_s^+ \rightarrow K^+ \pi^+ \pi^- \pi^0$ partial wave analyses
$D_s^+ \rightarrow 2 K_S^0 \pi^+$ partial wave analyses
$D_s^+ \rightarrow K_S^0 K^- 2 \pi^+$ partial wave analyses
$D_s^+ \rightarrow K^- K^+ \pi^+ \pi^0$ partial wave analyses
$D_s^+ \rightarrow K^- K^+ 2 \pi^+ \pi^-$ partial wave analyses

感谢您的垂听！