



Interference and Phase Study on the Omega Pseudoscalar Processes in the Vicinity of Narrow Charmonium Resonances

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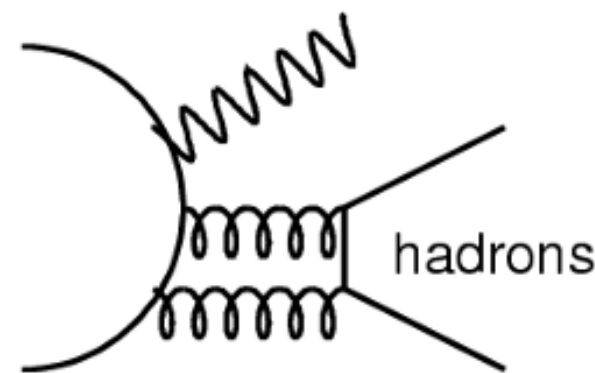


Motivations



- There are mainly three J/ψ hadronic decay modes:

- $J/\psi \rightarrow \gamma^* \rightarrow h$ (purely electromagnetic),
- $J/\psi \rightarrow ggg$ (purely strong),
- $J/\psi \rightarrow \gamma gg$ (mixed).

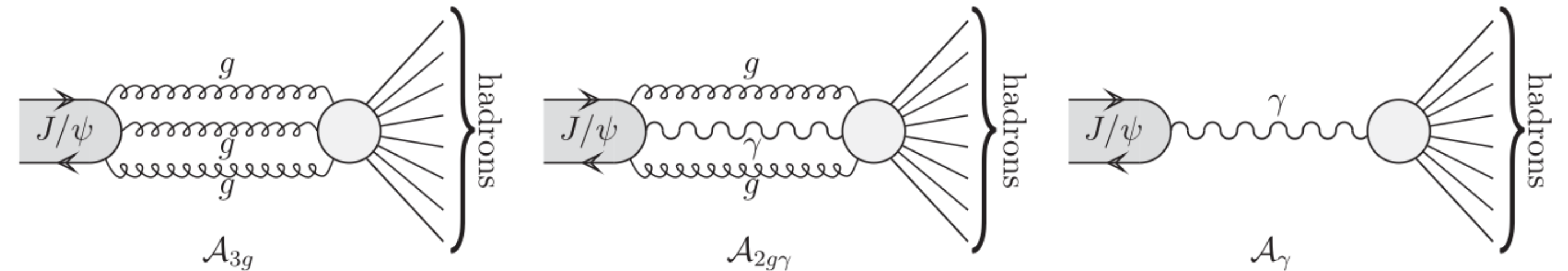


$J/\psi(1S)$ DECAY MODES

Mode		Fraction (Γ_i / Γ)
Γ_1	hadrons	$(87.7 \pm 0.5) \%$
Γ_2	virtual $\gamma \rightarrow$ hadrons	$(13.46 \pm 0.07) \%$
Γ_3	ggg	$(64.1 \pm 1.0) \%$
Γ_4	γgg	$(8.8 \pm 1.1) \%$

- We believe the existence of $J/\psi \rightarrow \gamma gg$ mixed decay mode because of J/ψ radiative decays.
- The decay $J/\psi \rightarrow \gamma gg$ is not explicitly forbidden in J/ψ hadronic decays, but its experimental observation is highly challenging.
- For example, the total decay amplitude of a $J/\psi \rightarrow (2n + 1)\pi$ is a sum of three main intermediate states.

- $A = A_\gamma + A_{\gamma gg} + A_{ggg}$
- $|A_{ggg}| \gg |A_\gamma|, |A_{\gamma gg}|$



- $J/\psi \rightarrow (2n + 1)\pi$ is G -parity conserved.

- Strong interaction preserves G -parity because of charge conjugation and isospin conservation.
- $J/\psi(\psi')$ has negative G -parity: $C_{J/\psi} = -1, I_{J/\psi} = 0 \Rightarrow G_{J/\psi} = C_{J/\psi}(-1)^{I_{J/\psi}} = -1$.
- G -parity is multiplicative quantum number: $G_{n\pi} = (-1)^n$.



Motivations



- The strong and electromagnetic amplitudes had been separated for $J/\psi \rightarrow 5\pi$.
- BESII collaboration, PLB(2019) **791** 375
- P. Wang et al., PRD(2004) **69** 057502
- $A_{\text{cont.}} = \mathcal{F}_{n\pi}(W)e^{i\phi_{\text{cont.}}}$, the amplitude of the continuum background from $e^+e^- \rightarrow \text{odd } n\pi$

$$A_\gamma(W) = \frac{3W\Gamma_{ee}}{\alpha(W^2 - M^2 + iM\Gamma)} \mathcal{F}_{n\pi}(W)e^{i\phi_\gamma}$$

$$A_{ggg}(W) = C_{ggg}e^{i\phi_{ggg}}A_\gamma(W)$$

$$\text{Similarly, } A_{\gamma gg}(W) = C_{\gamma gg}e^{i\phi_{\gamma gg}}A_\gamma(W)$$

$$A_{n\pi} = A_{\text{cont.}} + A_\gamma + A_{\gamma gg} + A_{ggg}$$

$$\sigma_{n\pi}^{\text{Born}}(W) = \frac{4\pi\alpha^2}{W^3} |A_{n\pi}|^2 P_{n\pi}(W) \text{ with } P_{n\pi}(W) = \frac{q_{n\pi}^3}{3}$$

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BESIII Collaboration / Physics Letters B 791 (2019) 375–384

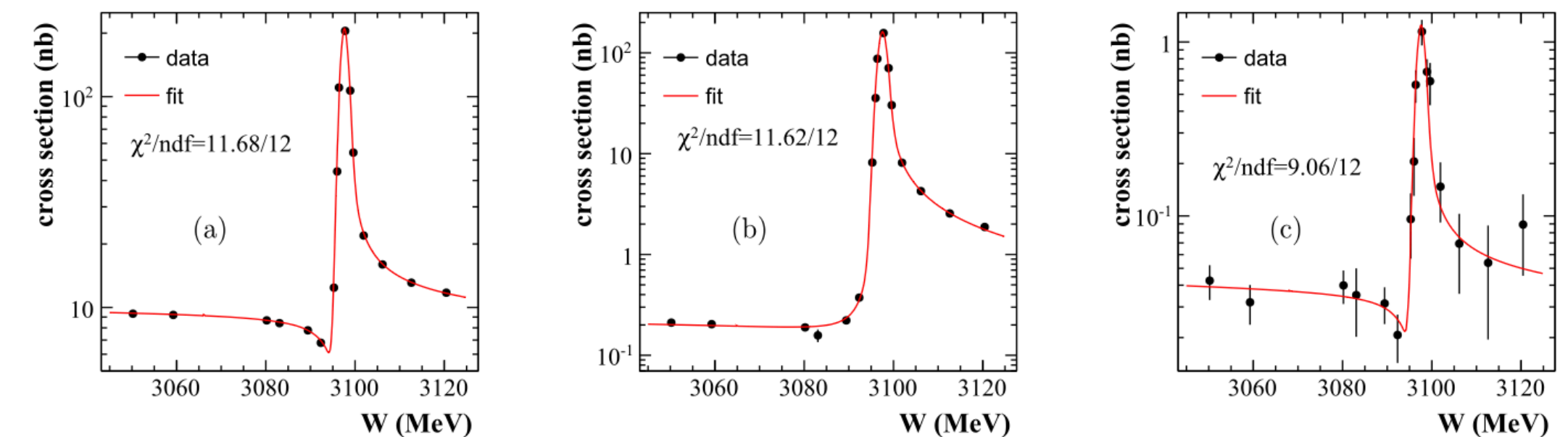


Fig. 3. The lineshapes of e^+e^- annihilates to (a) $\mu^+\mu^-$, (b) 5π , and (c) $\eta\pi^+\pi^-$. The black points with error bars are data, and the solid lines show the fit results.



Motivations



- The dressed cross section which includes the vacuum-polarization effects is

$$\begin{aligned}\sigma^{\text{dre}} &= \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{n\pi}}{W^2} \right)^2 q_{n\pi}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} e^{i\phi_{\text{cont.}}} + \frac{3W\Gamma_{ee}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1e^{i\phi_\gamma} + C_{\gamma gg} e^{i\phi_{\gamma gg}} + C_{ggg} e^{i\phi_{ggg}} \right) \right|^2 \\ &= \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{n\pi}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1e^{i\phi_{\gamma,\text{cont.}}} + C_{ggg} e^{i\phi_{\gamma gg,\text{cont.}}} + C_{\gamma gg} e^{i\phi_{ggg,\text{cont.}}} \right) \right|^2 \\ &\simeq \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{n\pi}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee} e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{ggg} e^{i\phi_{\gamma gg,\gamma}} \right) \right|^2\end{aligned}$$

- The “bare” resonance mass M , total and electron widths Γ and Γ_{ee} are replaced by the physical ones, respectively.
- $\phi_{\gamma,\text{cont.}} = \phi_\gamma - \phi_{\text{cont.}}$; $\phi_{\gamma gg,\text{cont.}} = \phi_{\gamma gg} - \phi_{\text{cont.}}$; $\phi_{\gamma gg,\gamma} = \phi_{\gamma gg} - \phi_\gamma$
- Usually, $A_{\gamma gg}$ is **ignored** because $|A_{ggg}| \gg |A_{\gamma gg}| \Rightarrow C_{ggg} \gg C_{\gamma gg}$



Motivations



- If we want to experimentally observe the **mixed γgg decay mode** in J/ψ hadronic decay, the **purely strong ggg decay mode** must be **suppressed**.
- For an isospin violated decay, the purely strong amplitude A_{ggg} is **suppressed** by the dimensionless factor $|m_u - m_d|/\sqrt{q^2}$.
- As it has been mentioned that strong interaction preserves G -parity.
 - Electromagnetic and weak interactions can be G -parity and isospin violated.
- $J/\psi(\psi') \rightarrow 2n\pi$ is G -parity violated.
- The decays of $J/\psi(\psi') \rightarrow \omega P(\pi^0, \eta, \eta')$ can have exclusive $2n\pi$ final states:
 - $\omega \rightarrow \pi^+\pi^-\pi^0 \Rightarrow J/\psi(\psi') \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-2\pi^0$
 - $\eta \rightarrow \pi^+\pi^-\pi^0 \Rightarrow J/\psi(\psi') \rightarrow \omega\eta \rightarrow 2(\pi^+\pi^-\pi^0)$
 - $\eta \rightarrow 3\pi^0 \Rightarrow J/\psi(\psi') \rightarrow \omega\eta \rightarrow \pi^+\pi^-4\pi^0$
 - $\eta' \rightarrow \eta\pi^+\pi^- \Rightarrow J/\psi(\psi') \rightarrow \omega\eta' \rightarrow 3(\pi^+\pi^-)2\pi^0$ or $J/\psi(\psi') \rightarrow \omega\eta' \rightarrow 2(\pi^+\pi^-)4\pi^0$
- $J/\psi \rightarrow \gamma gg$ **might be** experimentally observed in the J/ψ hadronic resonance decay $J/\psi \rightarrow \omega P \rightarrow 2n\pi$.



Motivations



- For a $J/\psi \rightarrow \omega P \rightarrow 2n\pi$ decay, the isospin violation is driven by either **electromagnetic effects** or **quark mass differences**.
- $J/\psi(\psi') \rightarrow \omega\pi^0$ is G -parity and isospin violated which is driven by **electromagnetic effects**.
 - $I_{J/\psi} = 0; \quad G_{J/\psi} = -1$
 - $I_\omega = 0, I_{\pi^0} = 1 \Rightarrow I_{\omega\pi^0} = 1; \quad G_\omega = -1, G_{\pi^0} = -1 \Rightarrow G_{\omega\pi^0} = +1$
 - $I_\omega = 0, I_{\eta(\eta')} = 0 \Rightarrow I_{\omega\eta(\eta')} = 0; \quad G_\omega = -1, G_{\eta(\eta')} = +1 \Rightarrow G_{\omega\eta(\eta')} = -1$
- $J/\psi \rightarrow \omega\eta$ is G -parity and isospin conserved.
 - It is well known that $\eta \rightarrow \pi^+\pi^-\pi^0$ or $\eta \rightarrow 3\pi^0$ is G -parity and isospin violated which is driven by **quark mass differences** where the electromagnetic contribution vanishes at leading order of the chiral perturbation series
 - $\mathcal{L}_{\text{QCD}}^{\Delta m} = -\frac{1}{2}(m_u - m_d)(\bar{u}u - \bar{d}d)$
 - $\text{Br}(\eta \rightarrow 3\pi^0) = (32.56 \pm 0.21) \%, \text{Br}(\eta \rightarrow \pi^+\pi^-\pi^0) = (23.02 \pm 0.25) \%$
 - $\text{Br}(\eta \rightarrow 2\gamma) = (39.36 \pm 0.18) \%$
- Similarly, $J/\psi \rightarrow \omega\eta'$ is G -parity and isospin conserved.
 - $\eta' \rightarrow \eta\pi^+\pi^-$ is the main decay mode which is G -parity conserved
 - $\eta' \rightarrow \pi^+\pi^-\pi^0$ is rare because of isospin violation.



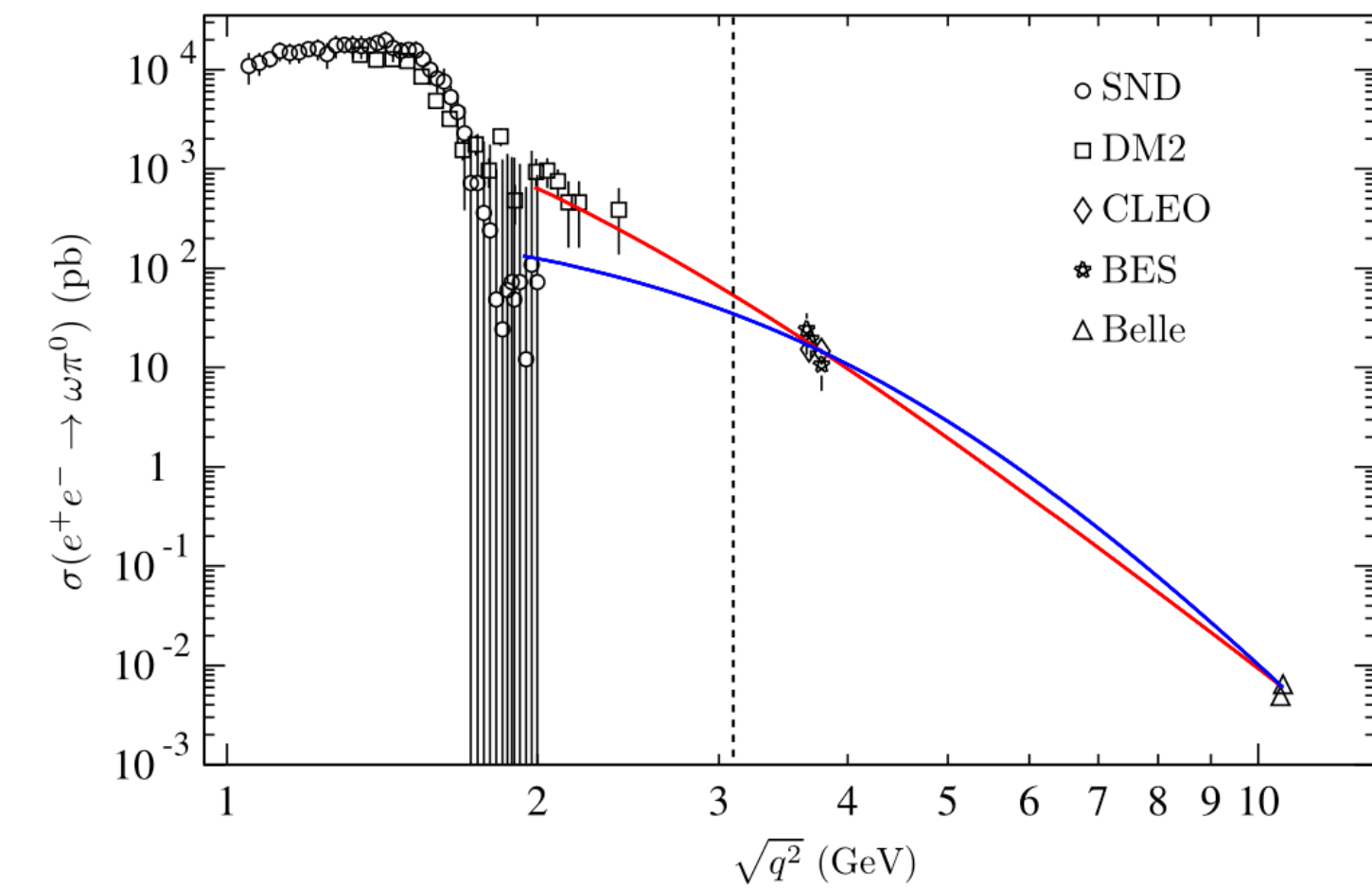
Motivations



- Therefore, $J/\psi \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-2\pi^0$ is the **golden channel** to experimentally observe the mixed decay mode $J/\psi \rightarrow \gamma gg$ in J/ψ hadronic resonance decay.
- Rinaldo Baldini Ferroli et al., [PRD(2017) **95**, 034038] interpolated the cross section $\sigma(e^+e^- \rightarrow \omega\pi^0)$ to $\sqrt{q^2} = M_{J/\psi}$ with DM2 and SND experiments data at lower energy regions $q^2 \in [1.05, 2.00]$ GeV and higher energy region BES, CLEO and Belle data at $\psi(3686)$, $\psi(3770)$ and $\Upsilon(4S)$ to obtain the branching ratio of the purely electromagnetic process.

$$\bullet \quad B_\gamma(J/\psi \rightarrow \omega\pi^0) = \begin{cases} (3.53 \pm 0.18) \times 10^{-4} \\ (2.29 \pm 0.40) \times 10^{-4} \end{cases}$$

$$\bullet \quad B_{\text{PDG}}(J/\psi \rightarrow \omega\pi^0) = (4.5 \pm 0.5) \times 10^{-4}$$





Motivations



- R. B. Ferroli et al., [PLB(2019) **799**, 135041; PRD(2021) **103**, 016005] also discussed the amplitudes separation in J/ψ and ψ' baryon decays by using an effective strong Lagrangian density and considering $B\bar{B}$ spin-1/2 SU(3) octet.
- Unfortunately, the $A_{\gamma gg}$ amplitude is zero in the A_{ggg} suppressed decay channel

Table 12

Purely strong (second column), purely EM (third column) and mixed (fourth column) BRs in the case of a complex ratio R .

$B\bar{B}$	$\text{BR}_{B\bar{B}}^{ggg} \times 10^3$	$\text{BR}_{B\bar{B}}^{\gamma} \times 10^5$	$\text{BR}_{B\bar{B}}^{gg\gamma} \times 10^5$
$\Sigma^0 \bar{\Sigma}^0$	1.100 ± 0.017	0.903 ± 0.061	0
$\Lambda \bar{\Lambda}$	2.010 ± 0.024	0.982 ± 0.066	0
$\Lambda \bar{\Sigma}^0 + \text{c.c.}$	0	2.83 ± 0.19	0
$p \bar{p}$	2.210 ± 0.043	8.47 ± 0.43	2.97 ± 0.87
$n \bar{n}$	2.210 ± 0.043	4.50 ± 0.30	0
$\Sigma^+ \bar{\Sigma}^-$	1.100 ± 0.017	6.82 ± 0.35	1.49 ± 0.44
$\Sigma^- \bar{\Sigma}^+$	1.090 ± 0.017	0.500 ± 0.094	1.47 ± 0.43
$\Xi^0 \bar{\Xi}^0$	1.260 ± 0.027	2.99 ± 0.20	0
$\Xi^- \bar{\Xi}^+$	1.240 ± 0.026	0.410 ± 0.077	1.67 ± 0.49

TABLE I. Parametrizations of the $B\bar{B}$ decay amplitudes.

$B\bar{B}$	$\mathcal{A}_{B\bar{B}}^{ggg}$	$\mathcal{A}_{B\bar{B}}^{gg\gamma}$	$\mathcal{A}_{B\bar{B}}^{\gamma}$
$p \bar{p}$	$(G_0 - D_m + F_m)e^{i\varphi}$	$\mathcal{A}_{p\bar{p}}^{ggg} R$	$D_e + F_e$
$n \bar{n}$	$(G_0 - D_m + F_m)e^{i\varphi}$	0	$-2D_e$
$\Lambda \bar{\Sigma}^0 + \text{c.c.}$	0	0	$\sqrt{3}D_e$
$\Lambda \bar{\Lambda}$	$(G_0 - 2D_m)e^{i\varphi}$	0	$-D_e$
$\Sigma^+ \bar{\Sigma}^-$	$(G_0 + 2D_m)e^{i\varphi}$	$\mathcal{A}_{\Sigma^+\bar{\Sigma}^-}^{ggg} R$	$D_e + F_e$
$\Sigma^- \bar{\Sigma}^+$	$(G_0 + 2D_m)e^{i\varphi}$	$\mathcal{A}_{\Sigma^-\bar{\Sigma}^+}^{ggg} R$	$D_e - F_e$
$\Sigma^0 \bar{\Sigma}^0$	$(G_0 + 2D_m)e^{i\varphi}$	0	D_e
$\Xi^0 \bar{\Xi}^0$	$(G_0 - D_m - F_m)e^{i\varphi}$	0	$-2D_e$
$\Xi^- \bar{\Xi}^+$	$(G_0 - D_m - F_m)e^{i\varphi}$	$\mathcal{A}_{\Xi^-\bar{\Xi}^+}^{ggg} R$	$D_e - F_e$

TABLE VI. Strong (second column), EM (third column) and mixed (fourth column) BRs for the $\psi(2S)$ meson.

$B\bar{B}$	$\text{BR}_{B\bar{B}}^{ggg} \times 10^4$	$\text{BR}_{B\bar{B}}^{\gamma} \times 10^6$	$\text{BR}_{B\bar{B}}^{gg\gamma} \times 10^6$
$p \bar{p}$	3.20 ± 0.12	1.34 ± 0.17	1.3 ± 1.0
$n \bar{n}$	3.20 ± 0.12	0.99 ± 0.11	0
$\Lambda \bar{\Lambda}$	3.61 ± 0.13	0.229 ± 0.026	0
$\Sigma^+ \bar{\Sigma}^-$	2.30 ± 0.10	1.19 ± 0.15	0.94 ± 0.73
$\Sigma^- \bar{\Sigma}^+$	2.29 ± 0.10	0.028 ± 0.022	0.94 ± 0.73
$\Sigma^0 \bar{\Sigma}^0$	2.30 ± 0.10	0.219 ± 0.024	0
$\Xi^0 \bar{\Xi}^0$	3.19 ± 0.11	0.807 ± 0.089	0
$\Xi^- \bar{\Xi}^+$	3.17 ± 0.11	0.026 ± 0.020	1.28 ± 0.98

$$J/\psi \rightarrow B\bar{B}$$

$$\psi' \rightarrow B\bar{B}$$

$$\text{Br}_{B\bar{B}}^{\gamma}(\psi' \rightarrow \Lambda \bar{\Sigma}^0 + \text{c.c.}) = (1.6 \pm 0.7) \times 10^{-6}$$

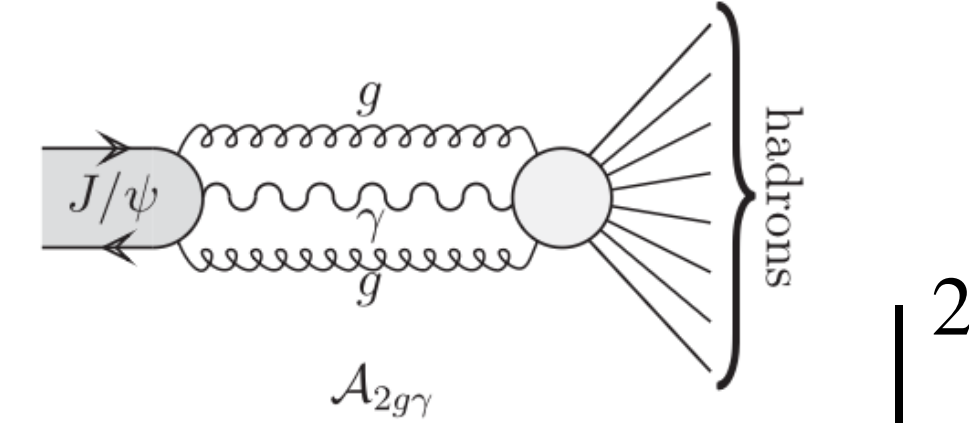
BESIII Collaboration, PRD(2021) **103**, 112004



Motivations

BESIII

- Including $J/\psi \rightarrow \gamma g g \rightarrow \omega \pi^0$, the dressed cross section for $J/\psi \rightarrow \omega \pi^0$ is



$$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{\omega\pi^0}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} e^{i\phi_{\text{cont.}}} + \frac{3W\Gamma_{ee}}{\alpha (W^2 - M^2 + iM\Gamma)} \left(1 e^{i\phi_\gamma} + C_{\gamma gg} e^{i\phi_{\gamma gg}} \right) \right|^2$$

$$= \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{\omega\pi^0}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee} e^{i\phi_{\gamma, \text{cont.}}}}{\alpha (W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma gg} e^{i\phi_{\gamma gg, \gamma}} \right) \right|^2$$

- If $C_{\gamma gg}$ is non-zero, we will observe the **mixed** $J/\psi \rightarrow \gamma g g \rightarrow \omega \pi^0$ decay mode.
- BESIII have collected data at 24 energies around J/ψ resonance and 11 energies around $\psi(3686)$ resonance.



Motivations



- For e^+e^- annihilation, initial state radiation (ISR) effect must be considered. [E. A. Kuraev and V. S. Fadin, SJNP(1985) **41**, 466]

- $$\sigma^{\text{ISR}}(W) = \int_0^{1 - \left(\frac{W_{\text{min}}}{W}\right)^2} dx F(x, W) \times \sigma^{\text{dre}}(W\sqrt{1-x})$$

- $$F(x, W) = \beta x^{\beta-1} (1 + \delta) - \beta \left(1 - \frac{x}{2}\right) + \frac{1}{8} \beta^2 \left[4(2-x) \times \log \frac{1}{x} - \frac{1 + 3(1-x)^2}{x} \log(1-x) - 6 + x \right]$$

- $$\delta = \frac{3}{4} \beta + \frac{\alpha}{\pi} \left(\frac{\pi^2}{3} - \frac{1}{2} \right) + \beta^2 \left(\frac{9}{32} - \frac{\pi^2}{12} \right), \beta = \frac{2\alpha}{\pi} \left(2 \log \frac{W}{m_e} - 1 \right)$$

- Since the decay widths of J/ψ and $\psi(3686)$ are much smaller than the c.m. energy spreads S_E of BEPCII, the experimentally observed cross section is the Gaussian convolution with the dressed cross section.

- $$\sigma^{\text{exp}}(W) = \int_{W-nS_E}^{W+nS_E} \frac{1}{\sqrt{2\pi}S_E} \exp\left(\frac{-(W-W')^2}{2S_E^2}\right) \sigma^{\text{ISR}}(W') dW'$$

- Y. N. Wang, Y. D. Wang, P. Wang, CPC (2024) **48**, 113103; B. X. Liu, Z. Y. Zhang, X. Zhou, PRD (2024) **110**, 053010



$e^+e^- \rightarrow \omega\pi^0$ around J/ψ resonance



- $e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-\pi^0$ with $\omega \rightarrow \pi^+\pi^-\pi^0$ and $\pi^0 \rightarrow 2\gamma$
- Data sets of 3.097 GeV
 - 2009, 2012, 2018, 2019
 - Total 10 billion
- Scan energy data sets from 3.050 GeV to 3.120 GeV
 - 2012, [jpsiscan](#)
 - 2018, [tauscan](#)



W (GeV)	3.05	3.059	3.083	3.087	3.089	3.092
L (pb ⁻¹)	1.4919 ± 0.161	15.060 ± 0.161	4.769 ± 0.055	2.470 ± 0.020	15.558 ± 0.165	14.910 ± 0.160
W (GeV)	3.0952	3.096	3.0957	3.0962	3.0964	3.09699
L (pb ⁻¹)	2.143 ± 0.025	1.816 ± 0.021	2.920 ± 0.020	4.980 ± 0.030	2.135 ± 0.025	3.100 ± 0.020
W (GeV)	3.097	3.0972	3.0976	3.0978	3.0987	3.0989
L (pb ⁻¹)	2962.720 ± 0.430	1.680 ± 0.010	4.660 ± 0.030	2.096 ± 0.026	2.203 ± 0.025	5.640 ± 0.030
W (GeV)	3.0996	3.101	3.104	3.106	3.112	3.12
L (pb ⁻¹)	0.756 ± 0.011	1.612 ± 0.021	5.720 ± 0.030	2.106 ± 0.025	1.720 ± 0.021	1.264 ± 0.016

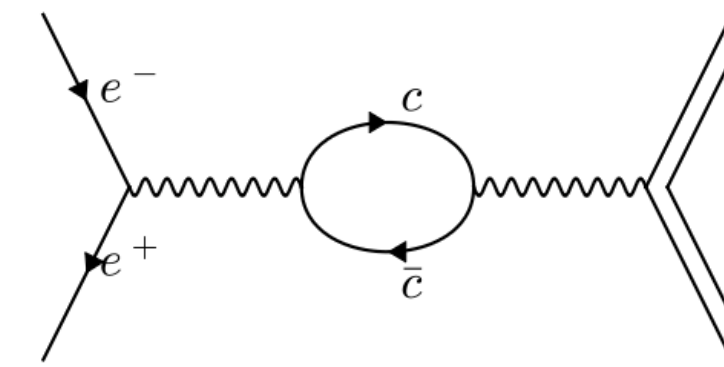
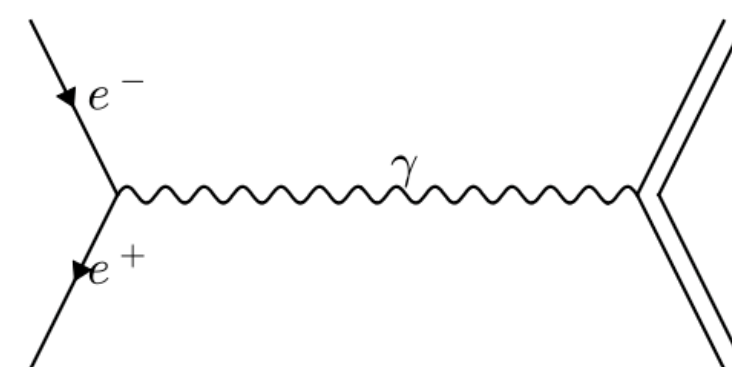


$e^+e^- \rightarrow \omega\pi^0$ around J/ψ resonance

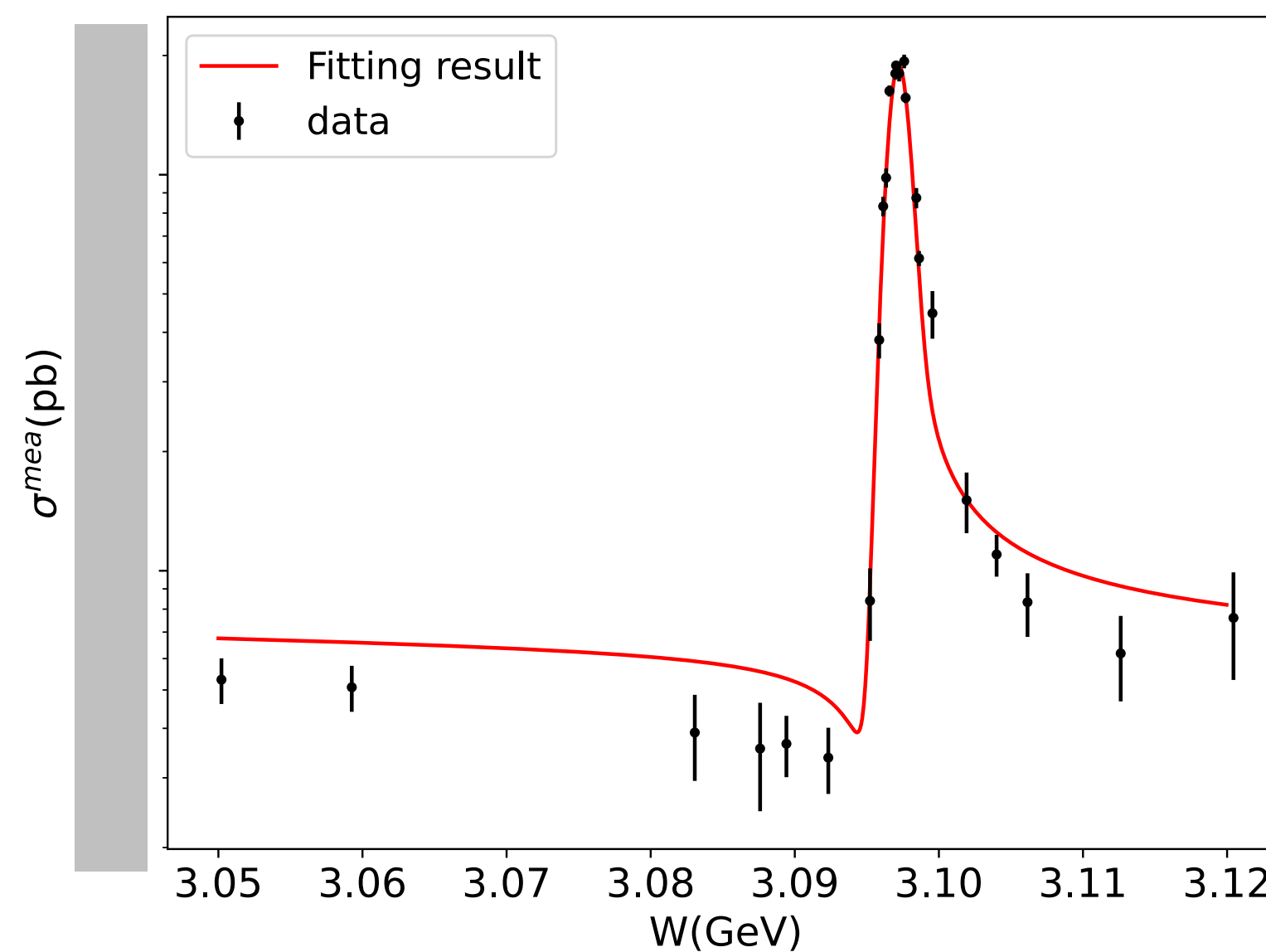
- Firstly, we try to only consider the **purely electromagnetic** mode γ^*

- $e^+e^- \rightarrow \omega\pi^0$

- $e^+e^- \rightarrow J/\psi \rightarrow \gamma^* \rightarrow \omega\pi^0$



- $$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{\omega\pi^0}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}}{\alpha(W^2 - M^2 + iM\Gamma)} e^{i\phi_{\gamma,\text{cont.}}} \right|^2$$



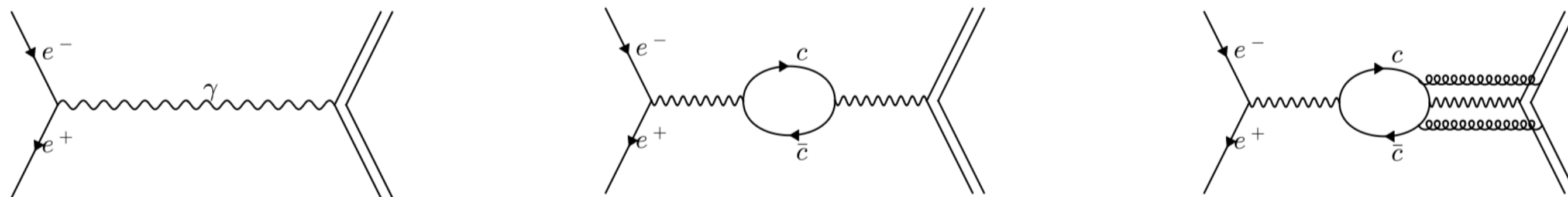


$e^+e^- \rightarrow \omega\pi^0$ around J/ψ resonance

BESIII

- Then, we include the **mixed mode** γgg

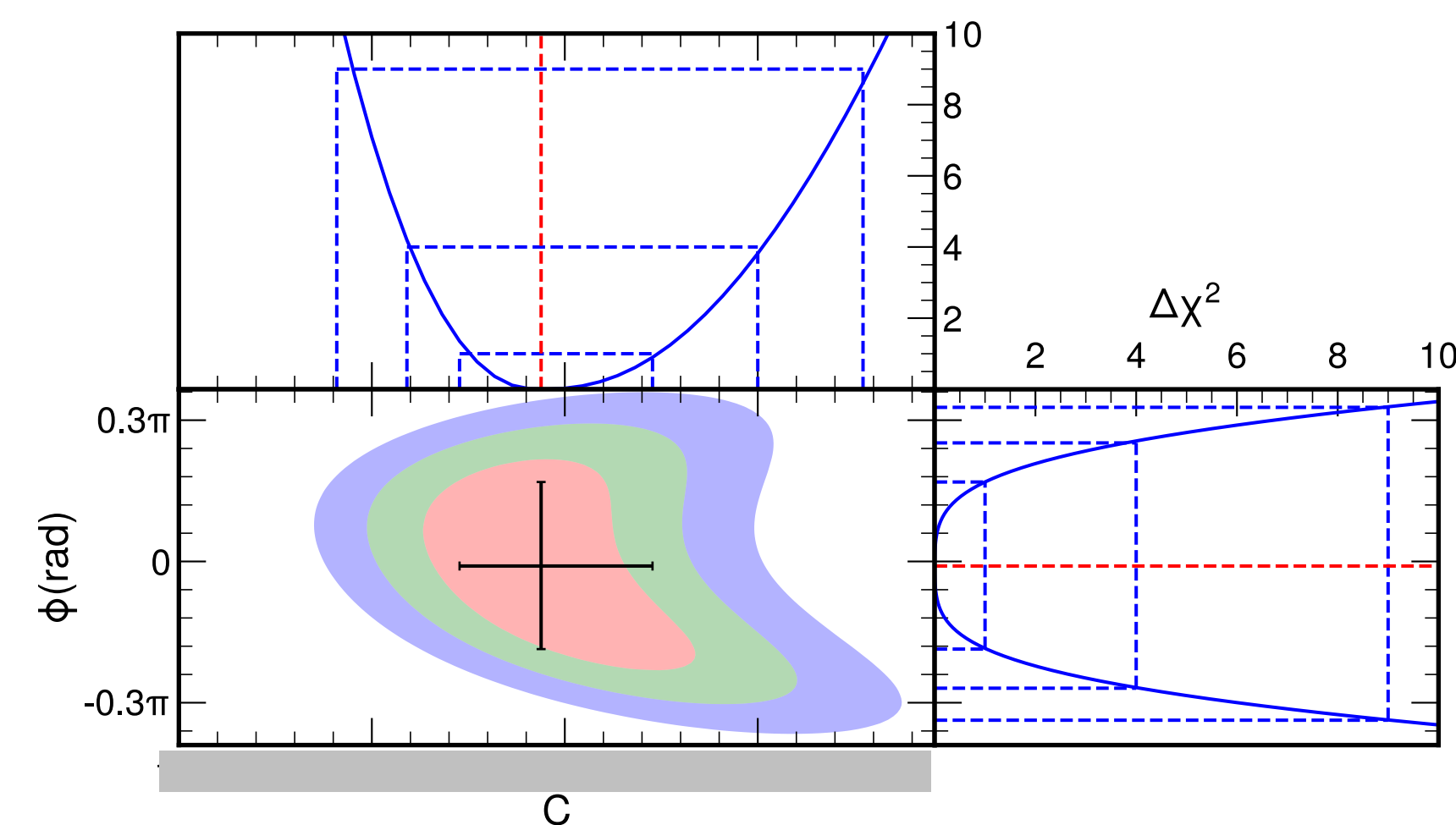
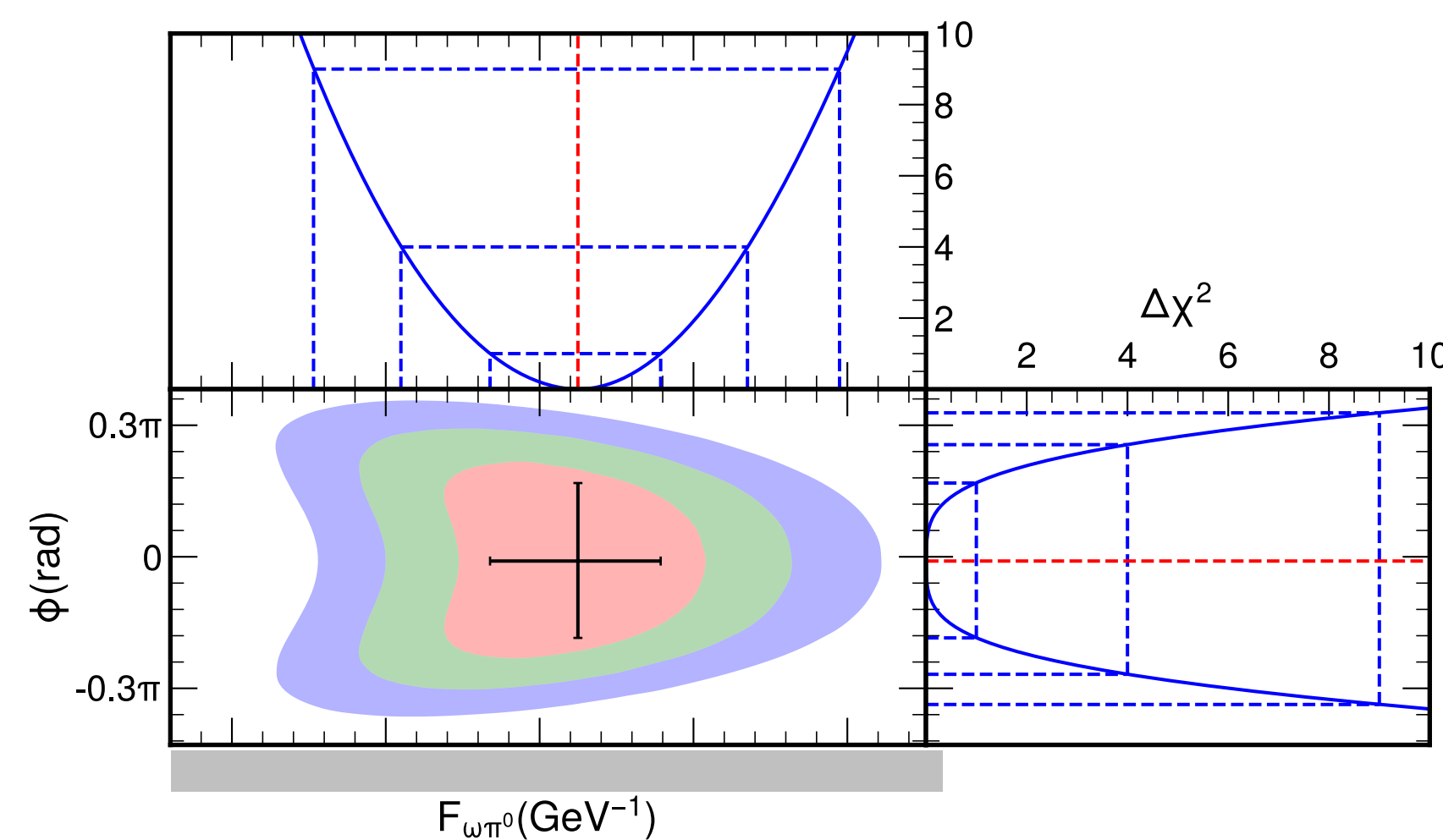
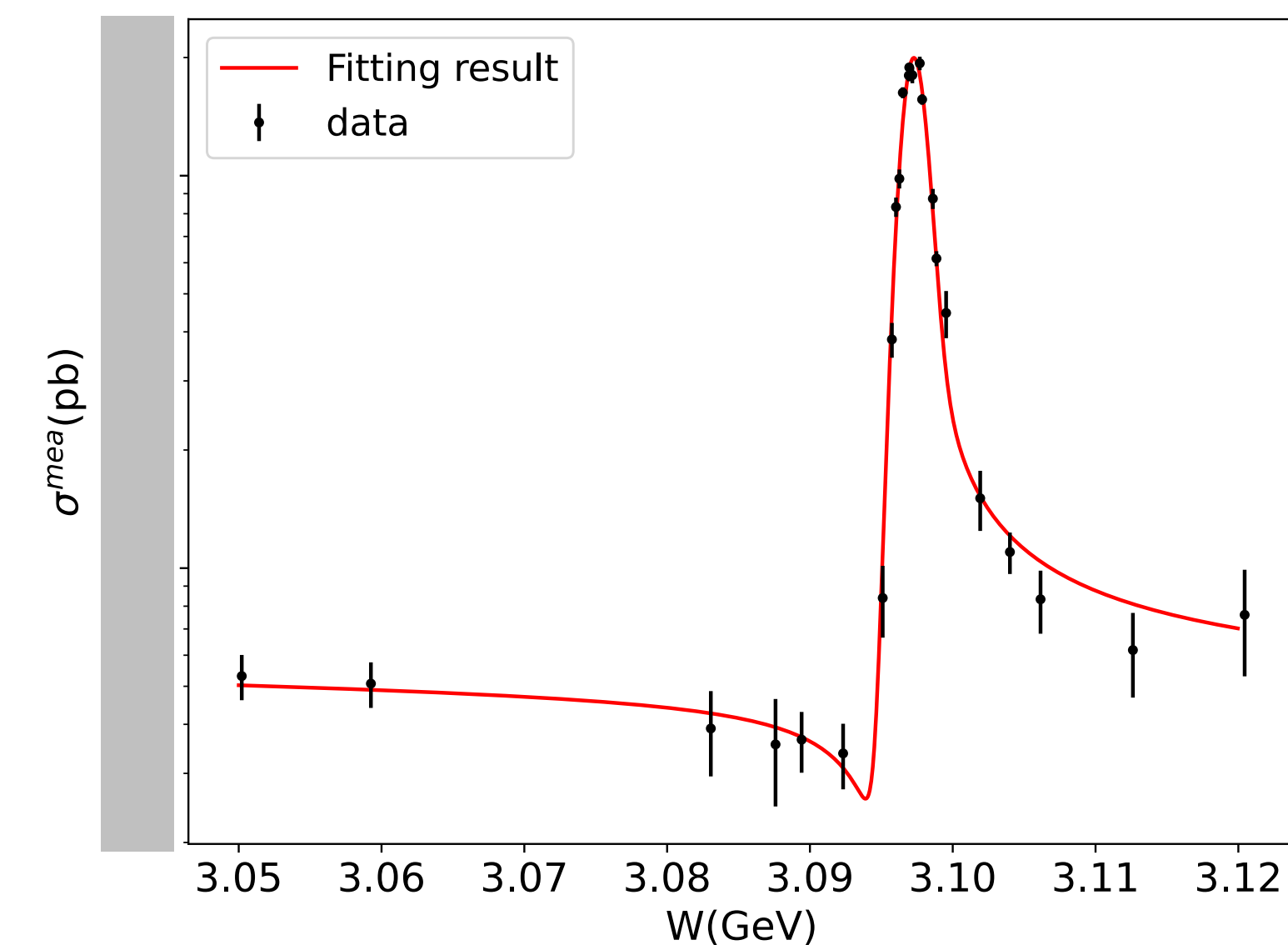
- $e^+e^- \rightarrow \omega\pi^0$
- $e^+e^- \rightarrow J/\psi \rightarrow \gamma^* \rightarrow \omega\pi^0$
- $e^+e^- \rightarrow J/\psi \rightarrow \gamma gg \rightarrow \omega\pi^0$



$$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{\omega\pi^0}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} \right) \right|^2$$

$$Ce^{i\phi} = \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} \right) e^{i\phi_{\gamma,\text{cont.}}}$$

Parameter	Result
$M(\text{MeV})$	3097.15 ± 0.03
$\mathcal{F}_{\omega\pi^0}(\text{GeV}^{-1})$	$(\text{shaded box}) \pm 0.13 \times 10^{-1}$
C	$\text{shaded box} \pm 0.07$
$\Phi(^{\circ})$	$\text{shaded box} \pm 34.9$
$S_E(\text{MeV})$	0.844 ± 0.024



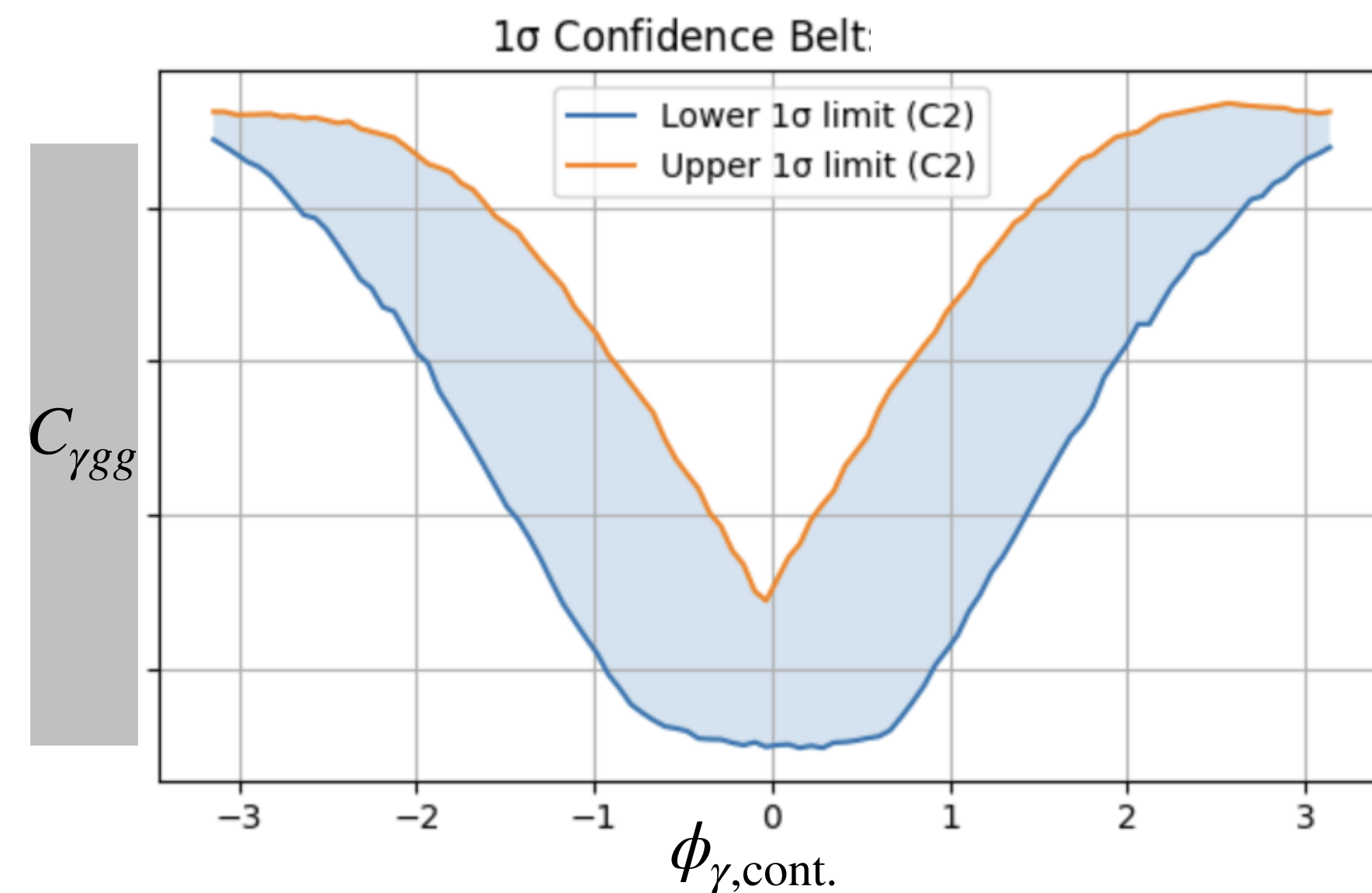
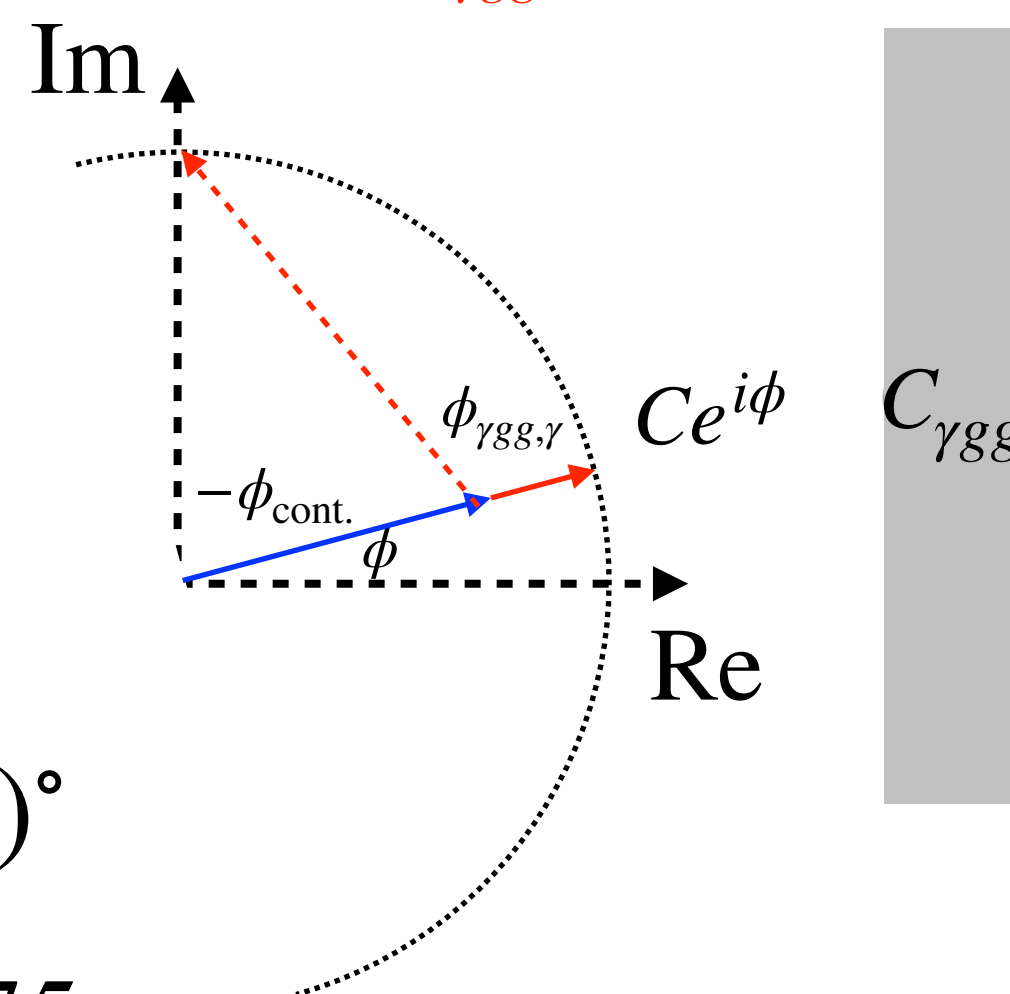


$e^+e^- \rightarrow \omega\pi^0$ around J/ψ resonance



- $Ce^{i\phi} = \left(1 + C_{\gamma gg} e^{i\phi_{\gamma gg, \gamma}}\right) e^{i\phi_{\gamma, \text{cont.}}}$
- To get $C_{\gamma gg}$, we need $\phi_{\gamma, \text{cont.}}$
- $\phi_{\gamma, \text{cont.}} = 0$ or $\pm\pi$?
- The study of $e^+e^- \rightarrow \mu^+\mu^-$ around J/ψ resonance shows that $\phi_{\gamma, \text{cont.}} = (3.0 \pm 5.7)^\circ$
- BESII collaboration, PLB(2019) 791 375
- Francesco Rosini: $\phi_{\gamma, \text{cont.}} = \pm\pi$

$$Ce^{i\phi} e^{-i\phi_{\gamma, \text{cont.}}} = 1 + C_{\gamma gg} e^{i\phi_{\gamma gg, \gamma}}$$



• Three contributions: continuum + $\psi \rightarrow \gamma^* \rightarrow K^+K^- + \psi \rightarrow 3g \rightarrow K^+K^-$.

$$A_{\text{cont}} = eJ_\mu^e \frac{-i}{q^2} F_K(q^2) C^\mu$$

$$e^+e^- \rightarrow \gamma^* \rightarrow K^+K^-$$

$$A_\gamma = eJ_\mu^e \frac{-i}{q^2} \frac{-i(g_\psi^\gamma)^2(q^2/M^2)}{q^2 - M^2 + iM\Gamma} \frac{-i}{q^2} F_K(q^2) C^\mu$$

$$e^+e^- \rightarrow \gamma^* \rightarrow \psi \rightarrow \gamma^* \rightarrow K^+K^-$$

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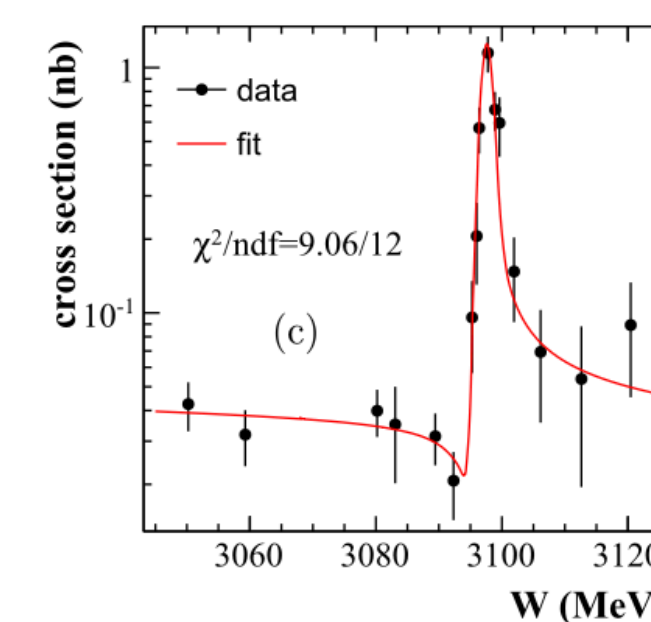
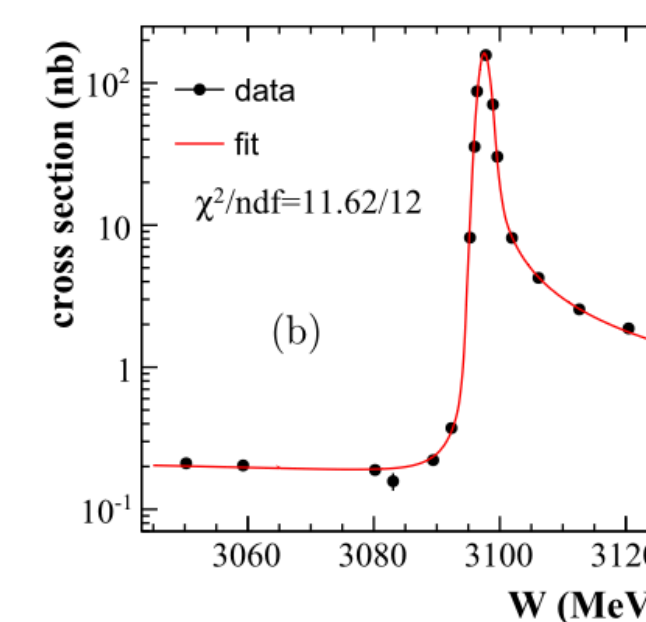
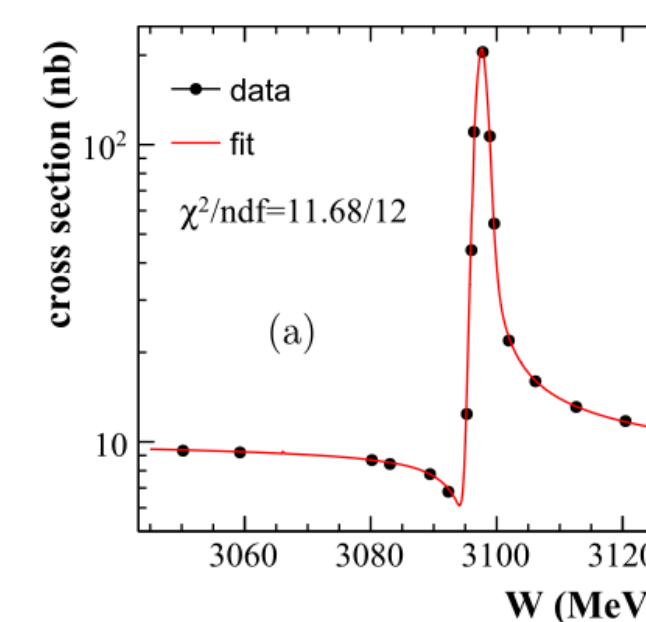


Fig. 3. The lineshapes of e^+e^- annihilates to (a) $\mu^+\mu^-$, (b) 5π , and (c) $\eta\pi^+\pi^-$. The black points with error bars are data, and the solid lines show the fit results.

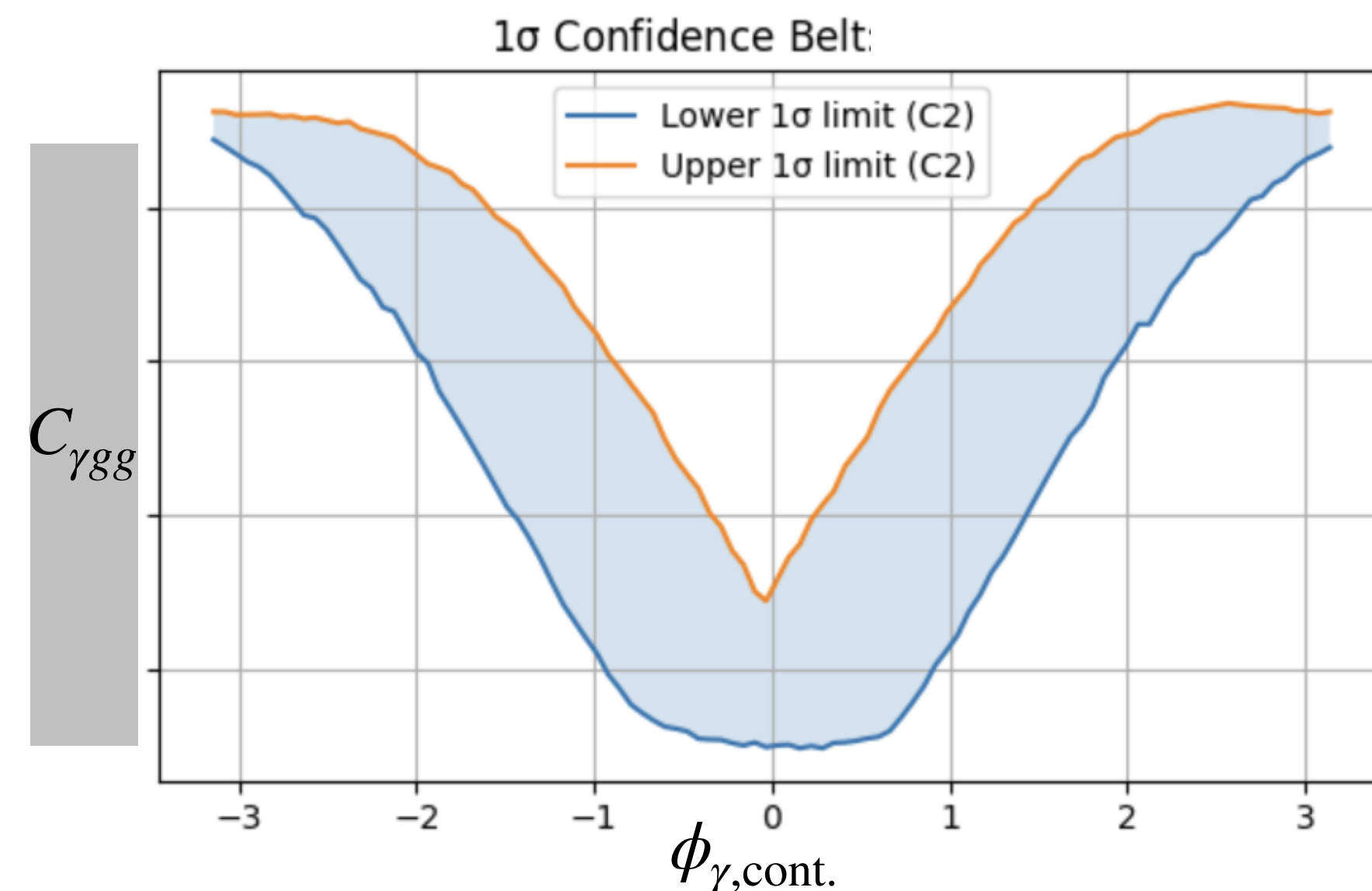
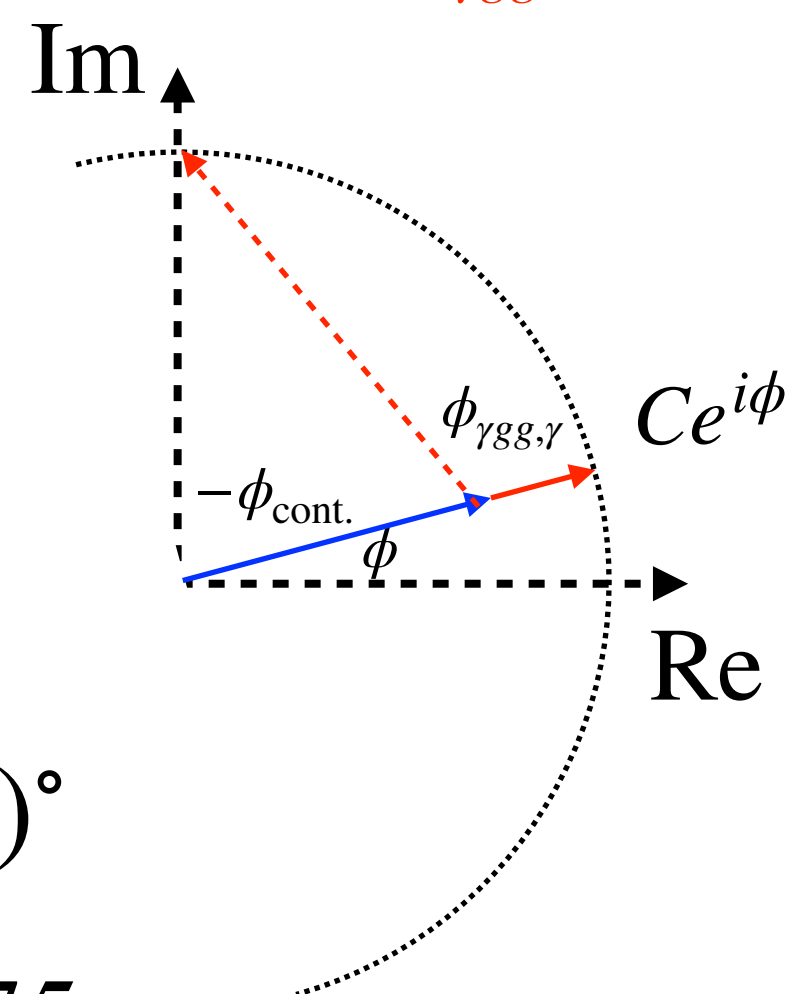


$e^+e^- \rightarrow \omega\pi^0$ around J/ψ resonance



- $Ce^{i\phi} = \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg, \gamma}}\right)e^{i\phi_{\gamma, \text{cont.}}}$
- To get $C_{\gamma gg}$, we need $\phi_{\gamma, \text{cont.}}$
- $\phi_{\gamma, \text{cont.}} = 0$ or $\pm\pi$?
- The study of $e^+e^- \rightarrow \mu^+\mu^-$ around J/ψ resonance shows that $\phi_{\gamma, \text{cont.}} = (3.0 \pm 5.7)^\circ$
- BESII collaboration, PLB(2019) 791 375
- Francesco Rosini: adding i before g_ψ^γ

$$Ce^{i\phi}e^{-i\phi_{\gamma, \text{cont.}}} = 1 + C_{\gamma gg}e^{i\phi_{\gamma gg, \gamma}}$$



$$A_{\text{cont}} = eJ_\mu^e \frac{-i}{s} F_K(s) (p_+^\mu - p_-^\mu),$$

$$A_\gamma = eJ_\mu^e \frac{-i}{s} \frac{-i(i g_\psi^\gamma)^2 (s/M^2)}{s - M^2 + iM\Gamma} \frac{-i}{s} F_K(s) (p_+^\mu - p_-^\mu)$$

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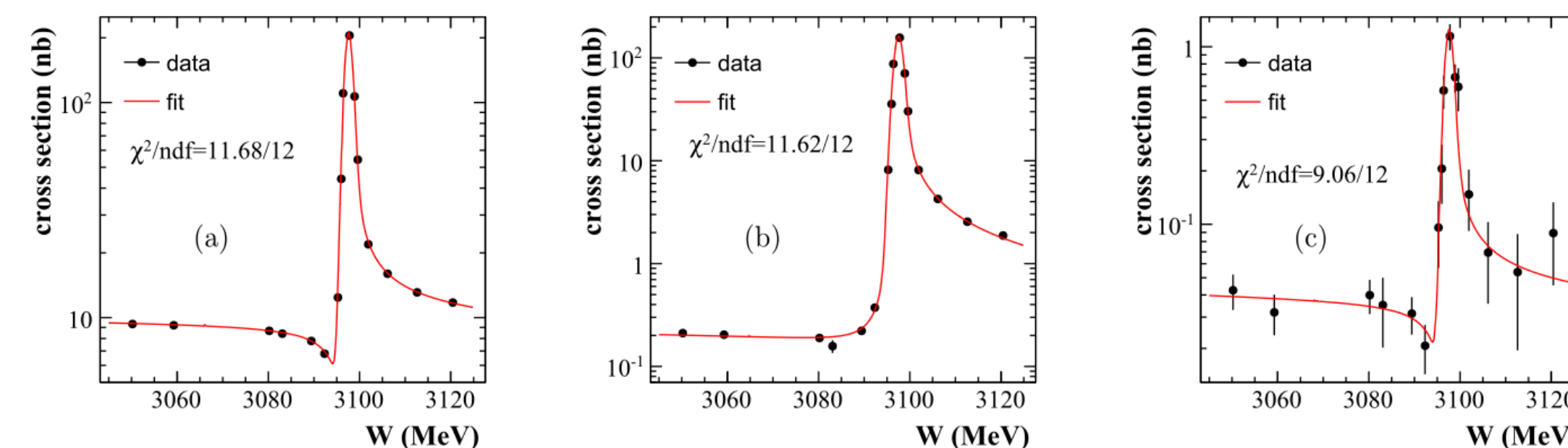


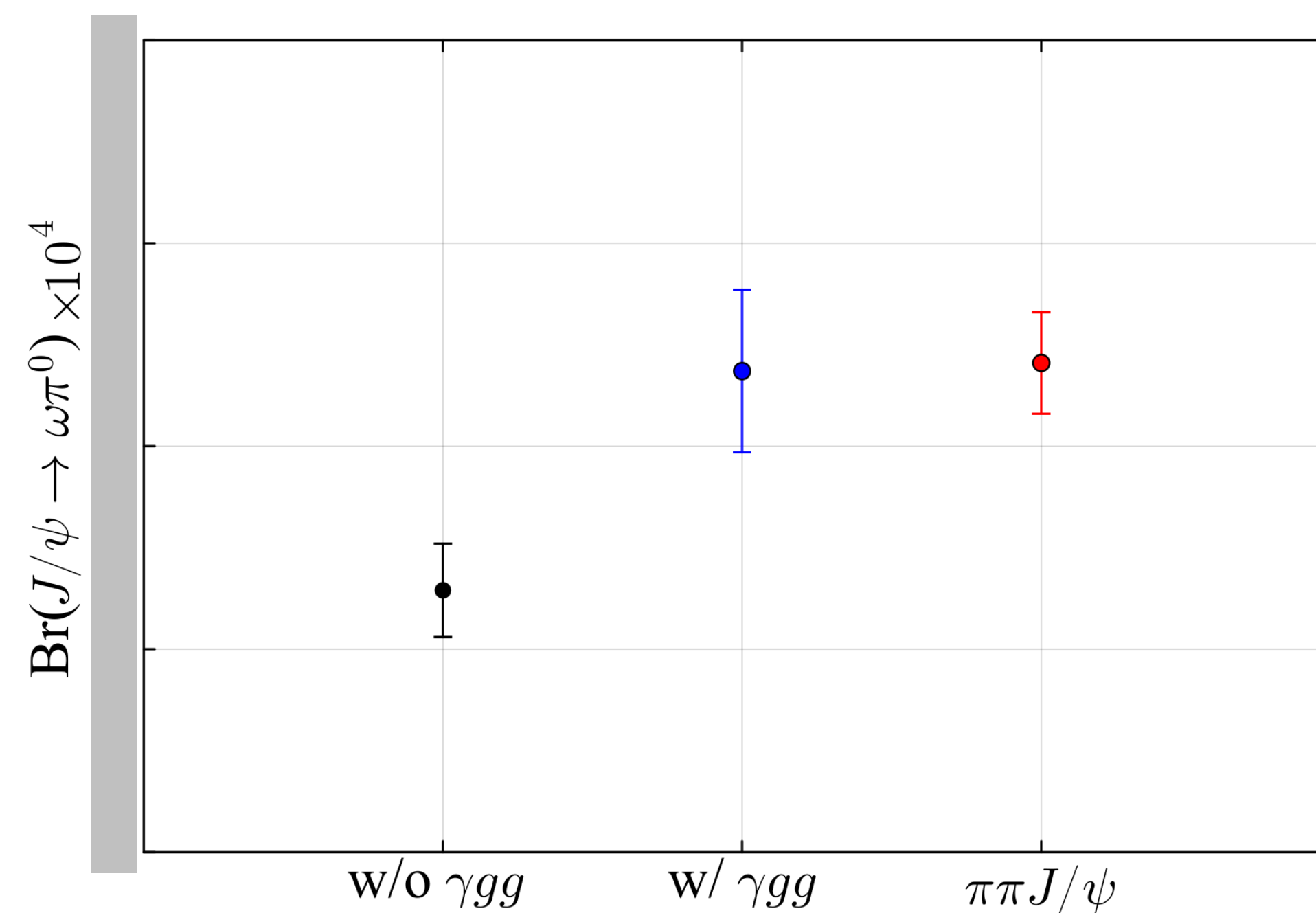
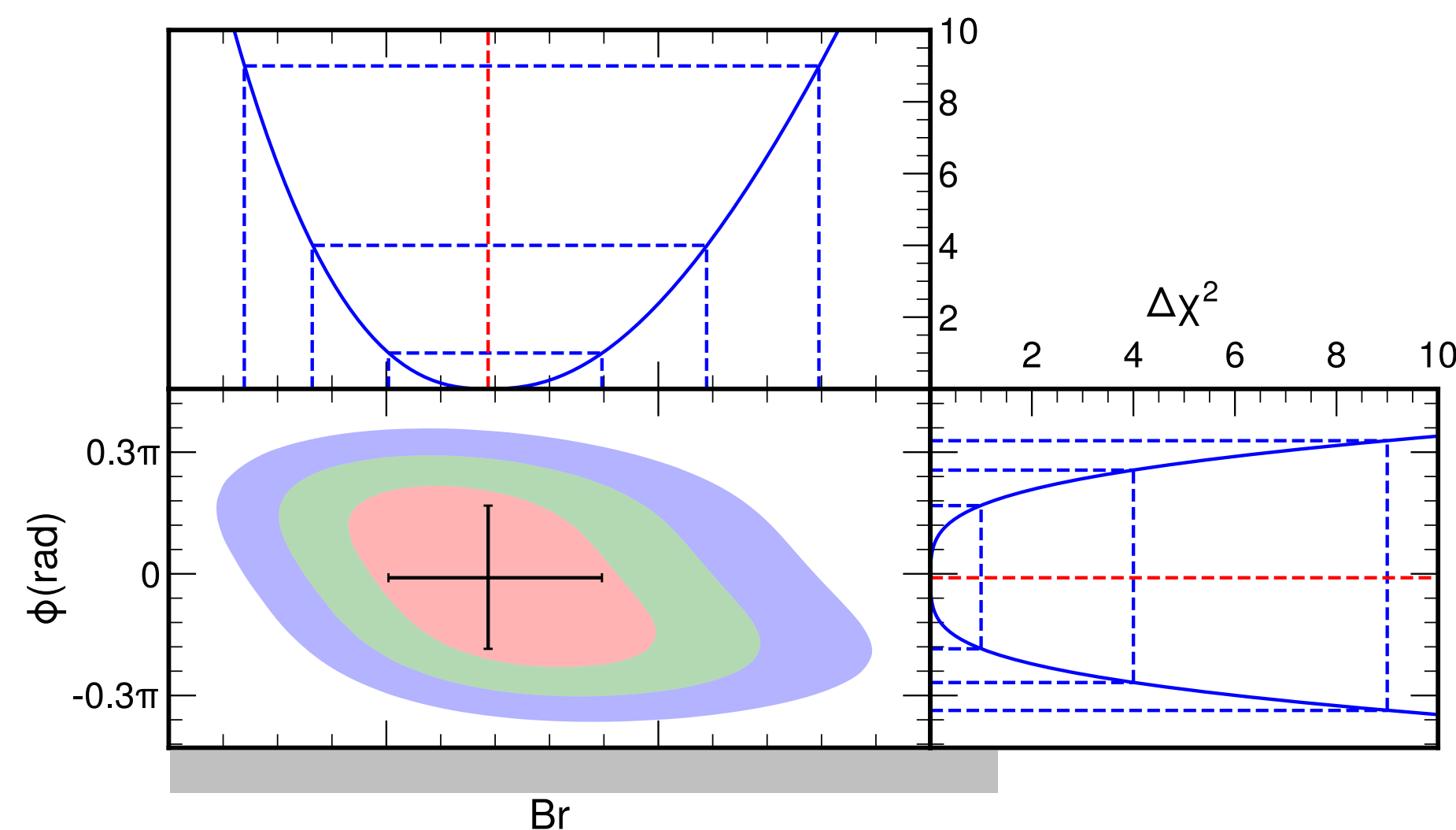
Fig. 3. The lineshapes of e^+e^- annihilates to (a) $\mu^+\mu^-$, (b) 5π , and (c) $\eta\pi^+\pi^-$. The black points with error bars are data, and the solid lines show the fit results.



$e^+e^- \rightarrow \omega\pi^0$ around J/ψ resonance



- $\text{Br}(J/\psi \rightarrow \omega\pi^0) = \frac{C^2 \mathcal{F}_{\omega\pi^0}^2 \Gamma_{ee} q_{\omega\pi^0}^3(M)}{M^4 \Gamma}$
- Branching ratio passed cross check from $\psi(3686) \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \omega\pi^0$.
 - Jiabao Gong and Gang Li
- We plan to give a combination result in future.





$e^+e^- \rightarrow \omega\eta$ around J/ψ resonance



- As we have mentioned $J/\psi \rightarrow \omega\eta$ is G -parity and isospin conserved
- $\eta \rightarrow 3\pi$ is isospin violated which is driven by **quark mass differences**.
- We expect that $J/\psi \rightarrow ggg$ is predominant in $J/\psi \rightarrow \omega\eta$: $|A_{ggg}| \gg |A_{\gamma gg}|, |A_\gamma|$.
- We use the exclusive decay $\eta \rightarrow 2\gamma$ so that $J/\psi \rightarrow \omega\eta \rightarrow \pi^+\pi^-4\gamma$ has the same final decay particles with $J/\psi \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-4\gamma$.

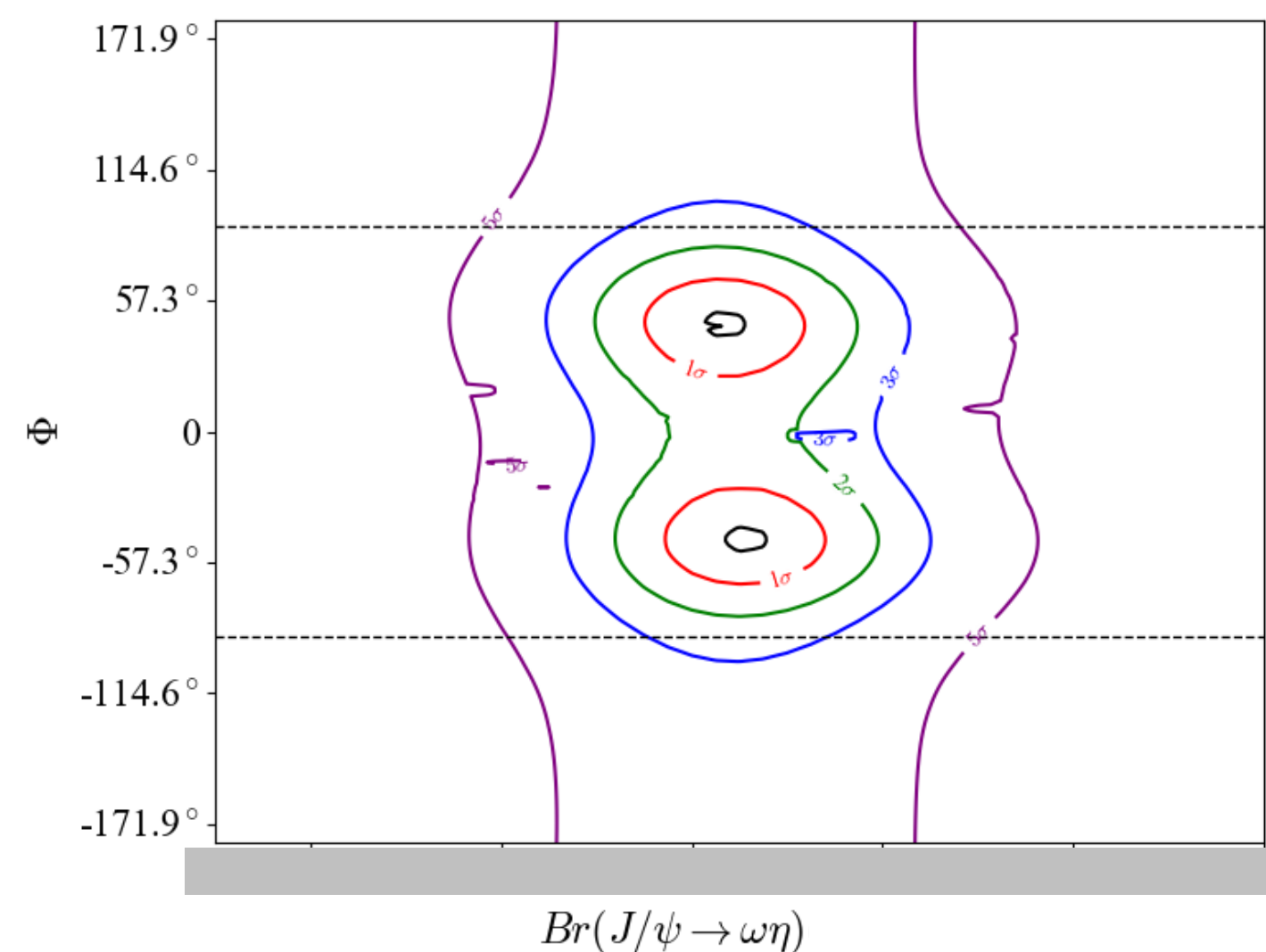
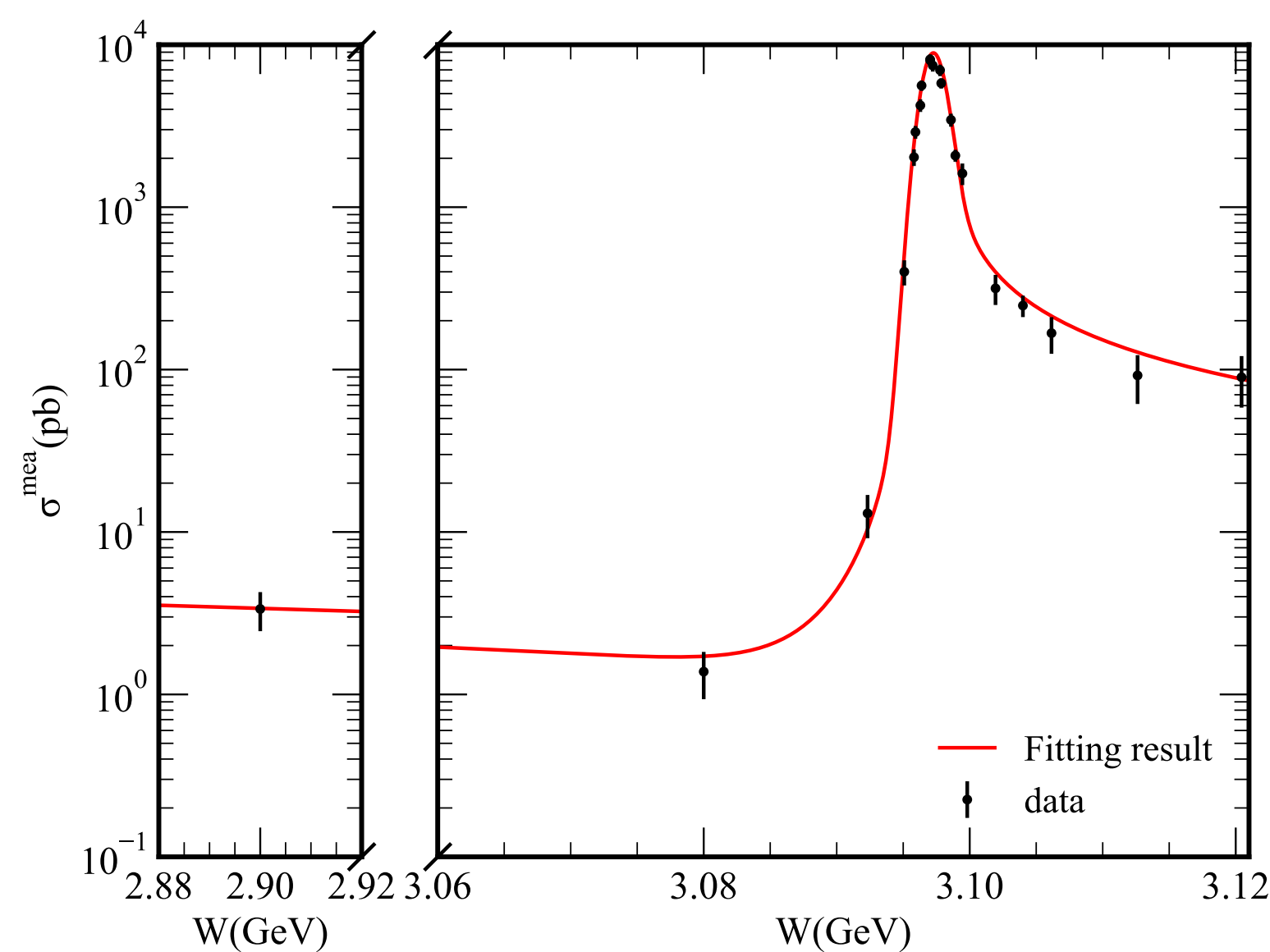
- $$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\eta}}{W^2} \right)^2 q_{\omega\eta}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} + C_{ggg}e^{i\phi_{ggg,\gamma}} \right) \right|^2$$



$e^+e^- \rightarrow \omega\eta$ around J/ψ resonance



- $$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\eta}}{W^2} \right)^2 q_{\omega\eta}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} + C_{ggg}e^{i\phi_{ggg,\gamma}} \right) \right|^2$$
- $$Ce^{i\phi} = \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} + C_{ggg}e^{i\phi_{ggg,\gamma}} \right) e^{i\phi_{\gamma,\text{cont.}}}$$



As we expect:

$$C_{ggg} \gg 1 \Rightarrow |A_{ggg}| \gg |A_{\gamma}|, |A_{\gamma gg}|$$

Parameter	Result
$M(\text{MeV})$	3097.18 ± 0.03
$\mathcal{F}_{\omega\eta}(\text{GeV}^{-1})$	$(\text{shaded}) \pm 1.09 \times 10^{-2}$
$\mathcal{C}$	$\text{shaded} \pm 1.56$
$\Phi(^{\circ})$	$\text{shaded} \pm 12.9$



$e^+e^- \rightarrow \omega\pi^0(\eta)$ around $\psi(3686)$ resonance BESIII

- $e^+e^- \rightarrow \omega\pi^0(\eta) \rightarrow \pi^+\pi^-\pi^0 4\gamma$ with $\omega \rightarrow \pi^+\pi^-\pi^0$ and $\pi^0(\eta) \rightarrow 2\gamma$
- Data sets of 3.686 GeV
 - 2009, 2012, 2021
 - Total 2.7 billion
- Data sets of 3.65 GeV and 3.682 GeV
 - 2022
- Scan energy data sets from 3.58 GeV and 3.71 GeV
 - 2018, psipscan



W (GeV)	3.65	3.67016	3.68014	3.682	3.68275	3.68422
L (pb ⁻¹)	410 ± 4.10	83.58 ± 0.08	83.06 ± 0.08	404 ± 4.04	28.18 ± 0.05	27.84 ± 0.05
W (GeV)	3.68526	3.686	3.68650	3.69136	3.70976	
L (pb ⁻¹)	25.34 ± 0.05	3877 ± 38.77	24.45 ± 0.05	68.65 ± 0.08	69.33 ± 0.08	



$e^+e^- \rightarrow \omega\pi^0(\eta)$ around $\psi(3686)$ resonance BESIII

- As we know that:
 - $\text{Br}_{\text{PDG}}(J/\psi \rightarrow \omega\pi^0) = (4.5 \pm 0.5) \times 10^{-4}$; $\text{Br}_{\text{PDG}}(\psi(3686) \rightarrow \omega\pi^0) = (2.1 \pm 0.6) \times 10^{-5}$
 - $\text{Br}_{\text{PDG}}(J/\psi \rightarrow \omega\eta) = (1.74 \pm 0.20) \times 10^{-3}$; $\text{Br}_{\text{PDG}}(\psi(3686) \rightarrow \omega\eta) < 1.1 \times 10^{-5}$
- What do we expect for $\text{Br}_{\text{PDG}}(\psi(3686) \rightarrow \omega\pi^0)$ and $\text{Br}_{\text{PDG}}(\psi(3686) \rightarrow \omega\eta)$?
- According to the 12% rule
 - $\frac{\text{Br}_\gamma(\psi(3686) \rightarrow \gamma^* \rightarrow \omega\pi^0)}{\text{Br}_\gamma(J/\psi \rightarrow \gamma^* \rightarrow \omega\pi^0)} \simeq 12\% \Rightarrow \text{Br}(\psi(3686) \rightarrow \omega\pi^0) \sim 10^{-5}$
 - Is there the **mixed mode γgg** in $\psi(3686) \rightarrow \omega\pi^0$?
 - $\frac{\text{Br}_\gamma(\psi(3686) \rightarrow ggg \rightarrow \omega\eta)}{\text{Br}_\gamma(J/\psi \rightarrow ggg \rightarrow \omega\eta)} \simeq 12\% \Rightarrow \text{Br}(\psi(3686) \rightarrow \omega\eta) \sim 10^{-4} \gg 1.1 \times 10^{-5}$

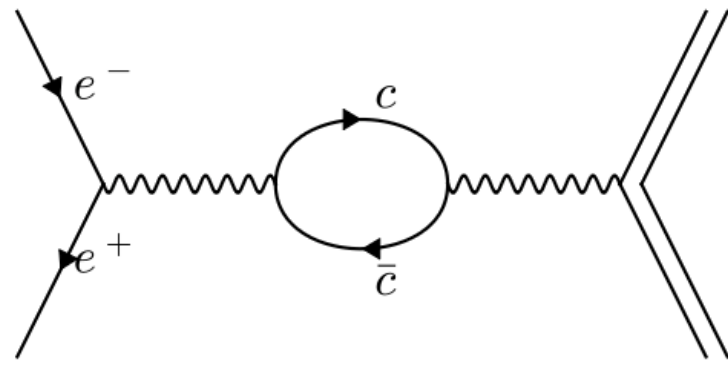
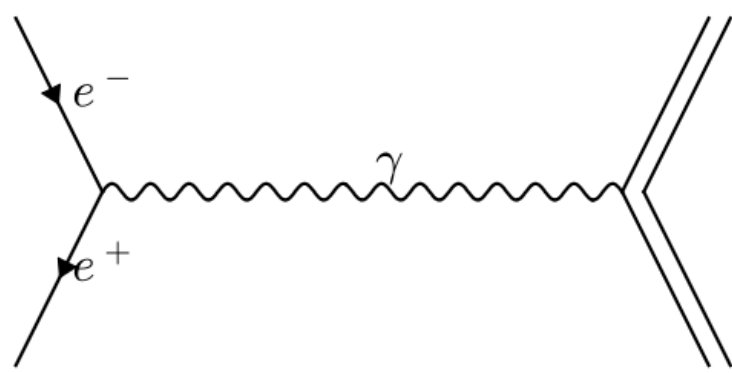


$e^+e^- \rightarrow \omega\pi^0$ around $\psi(3686)$ resonance BESIII

• Firstly, we try to only consider the **purely electromagnetic** mode

• $e^+e^- \rightarrow \omega\pi^0$

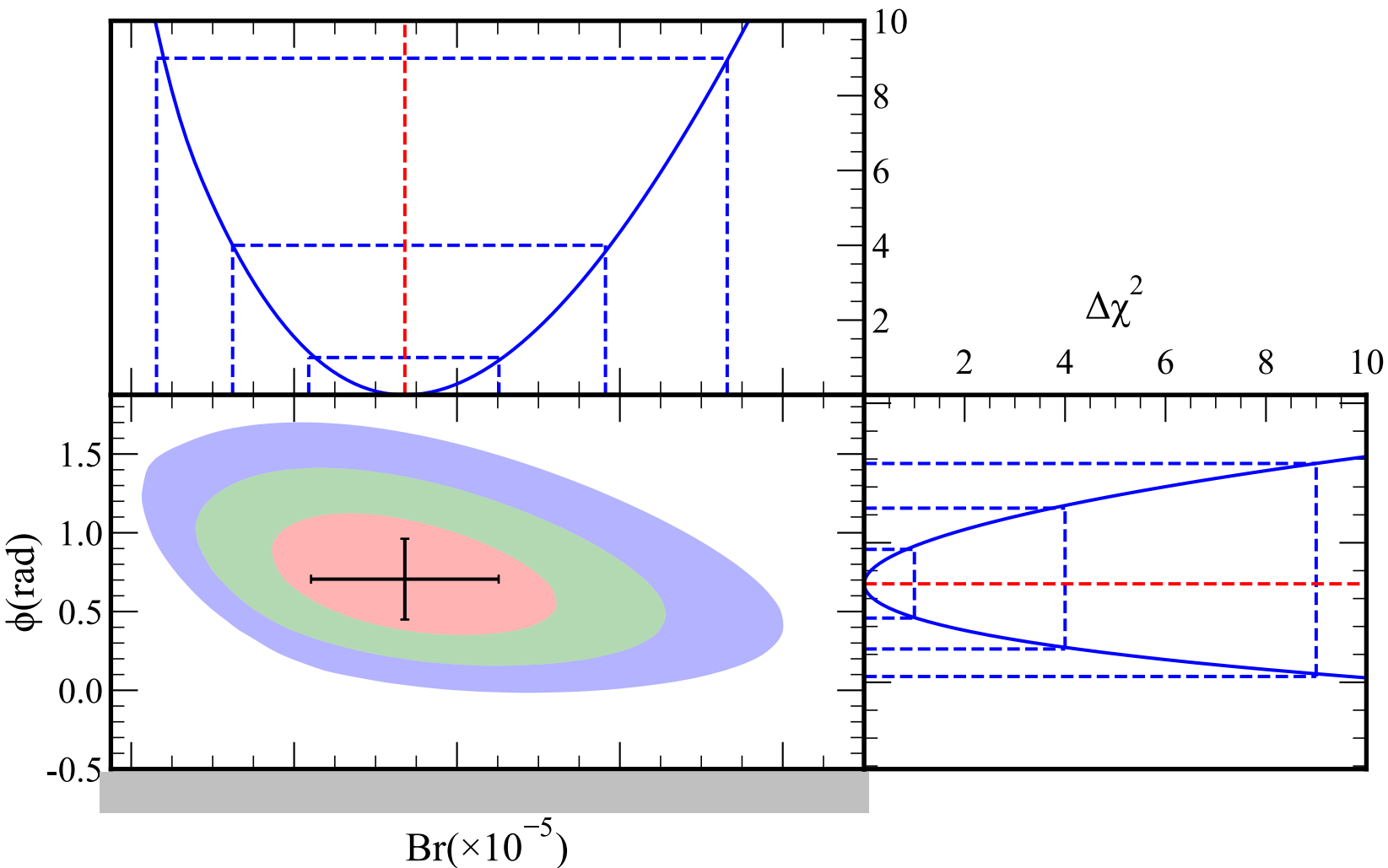
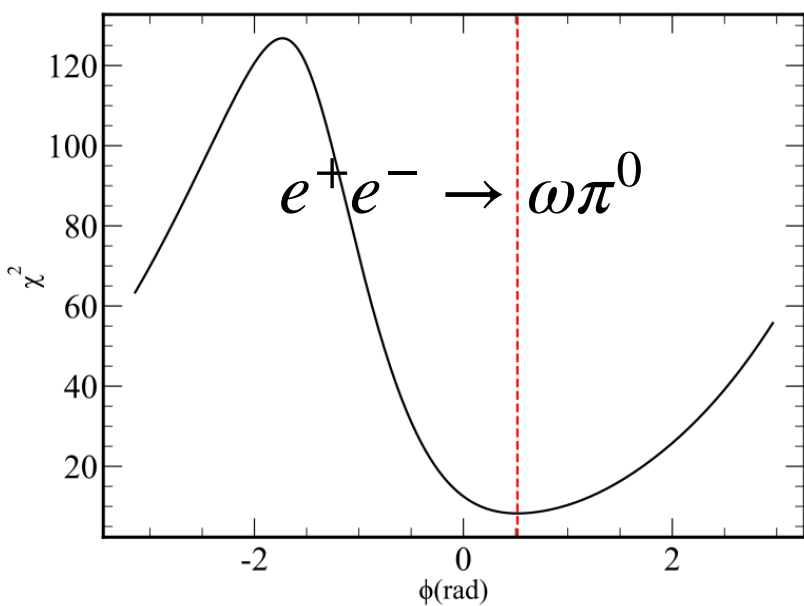
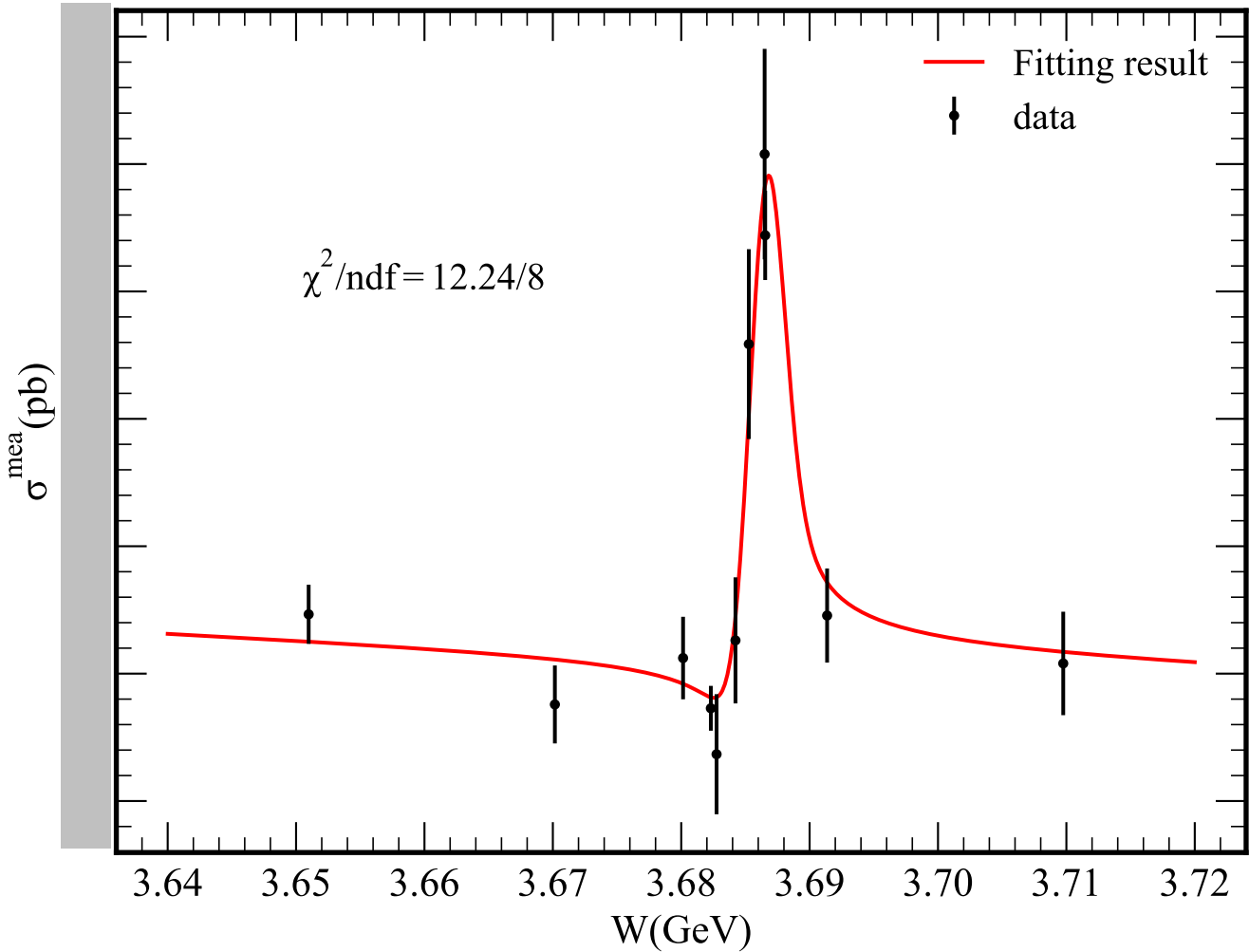
• $e^+e^- \rightarrow \psi(3686) \rightarrow \gamma^* \rightarrow \omega\pi^0$



•
$$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{\omega\pi^0}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}}{\alpha (W^2 - M^2 + iM\Gamma)} \right|^2 e^{i\phi_{\gamma, \text{cont.}}}$$

$$\text{Br}(\psi(2S) \rightarrow \omega\pi^0) = \frac{\mathcal{F}_{\omega\pi^0}^2 \Gamma_{ee} q_{\omega\pi^0}^3(M)}{M^4 \Gamma}$$

Parameter	$\phi(\text{rad})$	$M(\text{MeV})$	$\mathcal{F}_{\omega\pi^0}^2(\text{GeV}^4)$
Fitting result	$\pm 0.21 \pm 0.25$	$3686.18 \pm 0.29 \pm 0.23$	$\pm 0.03 \pm 0.05$





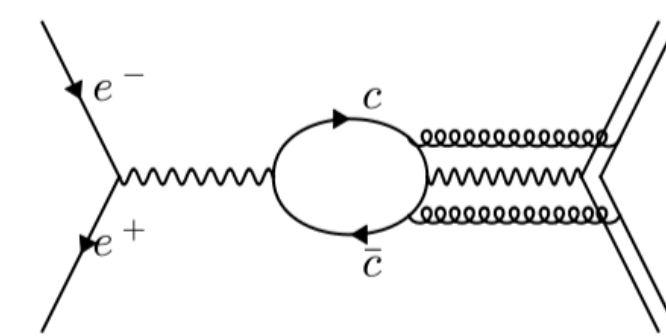
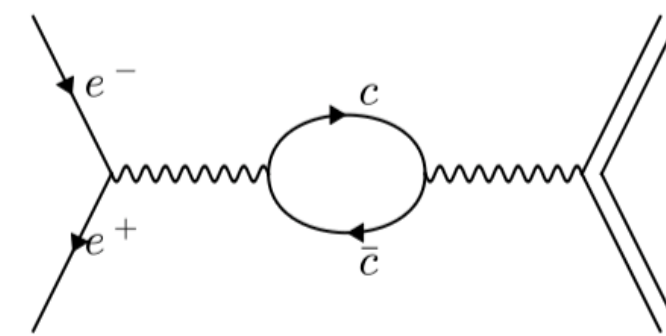
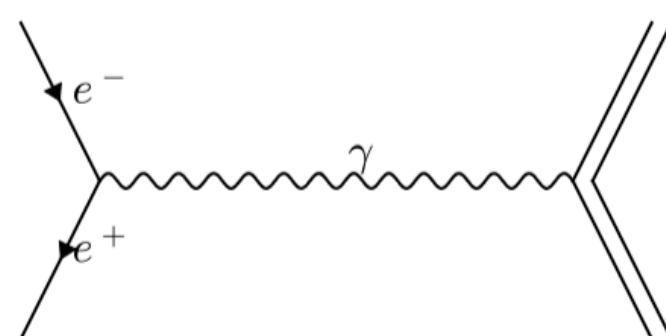
$e^+e^- \rightarrow \omega\pi^0$ around $\psi(3686)$ resonance BESIII

- Then, we include the **mixed mode**

- $e^+e^- \rightarrow \omega\pi^0$

- $e^+e^- \rightarrow J/\psi \rightarrow \gamma^* \rightarrow \omega\pi^0$

- $e^+e^- \rightarrow J/\psi \rightarrow \gamma gg \rightarrow \omega\pi^0$



- $$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\pi^0}}{W^2} \right)^2 q_{\omega\pi^0}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} \right) \right|^2$$

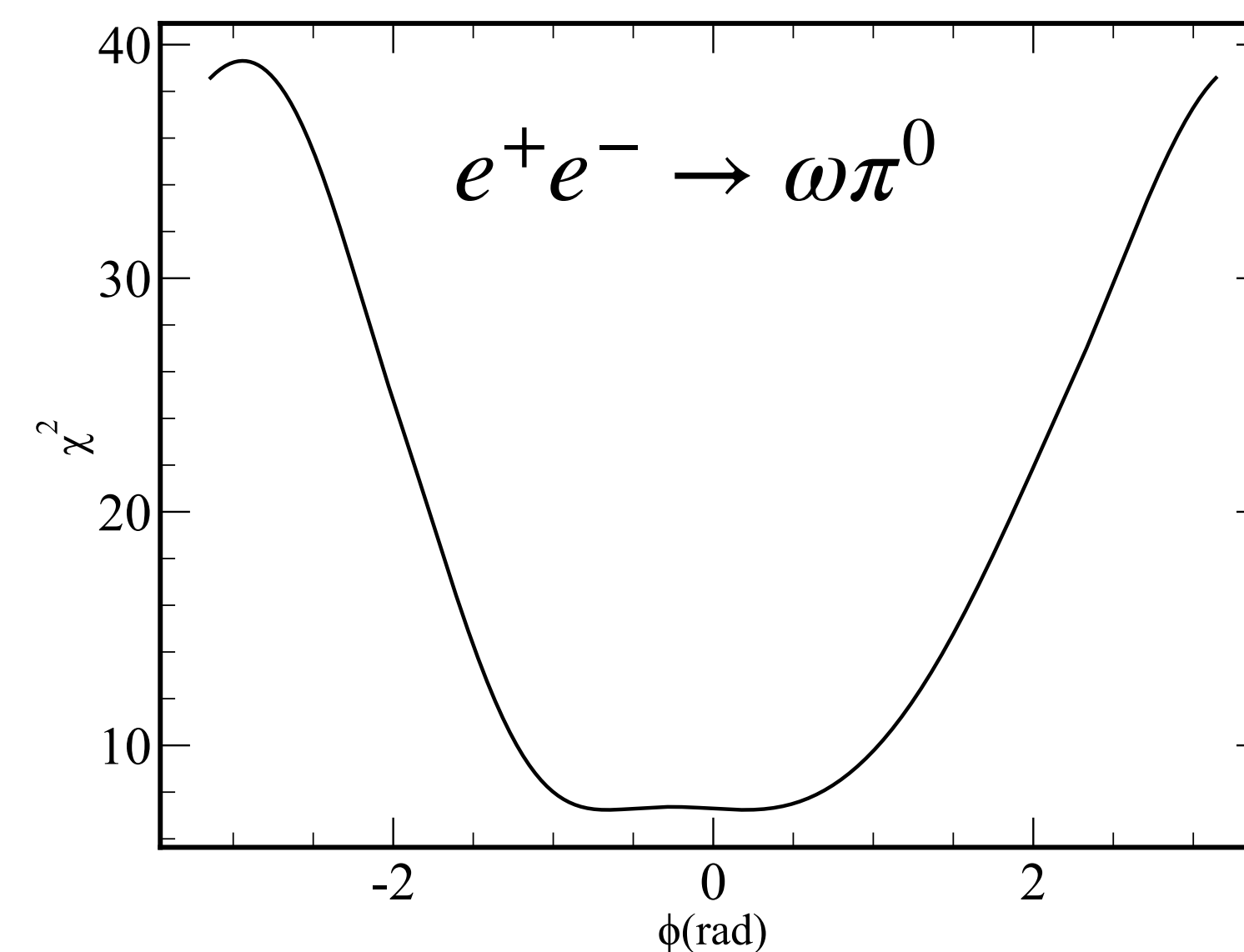
- $$Ce^{i\phi} = \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} \right) e^{i\phi_{\gamma,\text{cont.}}}$$

- There seems two solutions

- $\Delta\chi^2$ barrier is too low or $\Delta\chi^2$ is flat around $\chi_{\min}^2$

- Large uncertainty of ϕ causes large uncertainty of Br

- Lower statistics? Or $|A_{\gamma gg}| \ll |A_{\gamma}| \Rightarrow C_{\gamma gg} \simeq 0$?





$e^+e^- \rightarrow \omega\eta$ around $\psi(3686)$ resonance



- $$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\eta}}{W^2} \right)^2 q_{\omega\eta}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma\gamma\gamma}e^{i\phi_{\gamma\gamma\gamma,\gamma}} + C_{ggg}e^{i\phi_{ggg,\gamma}} \right) \right|^2$$

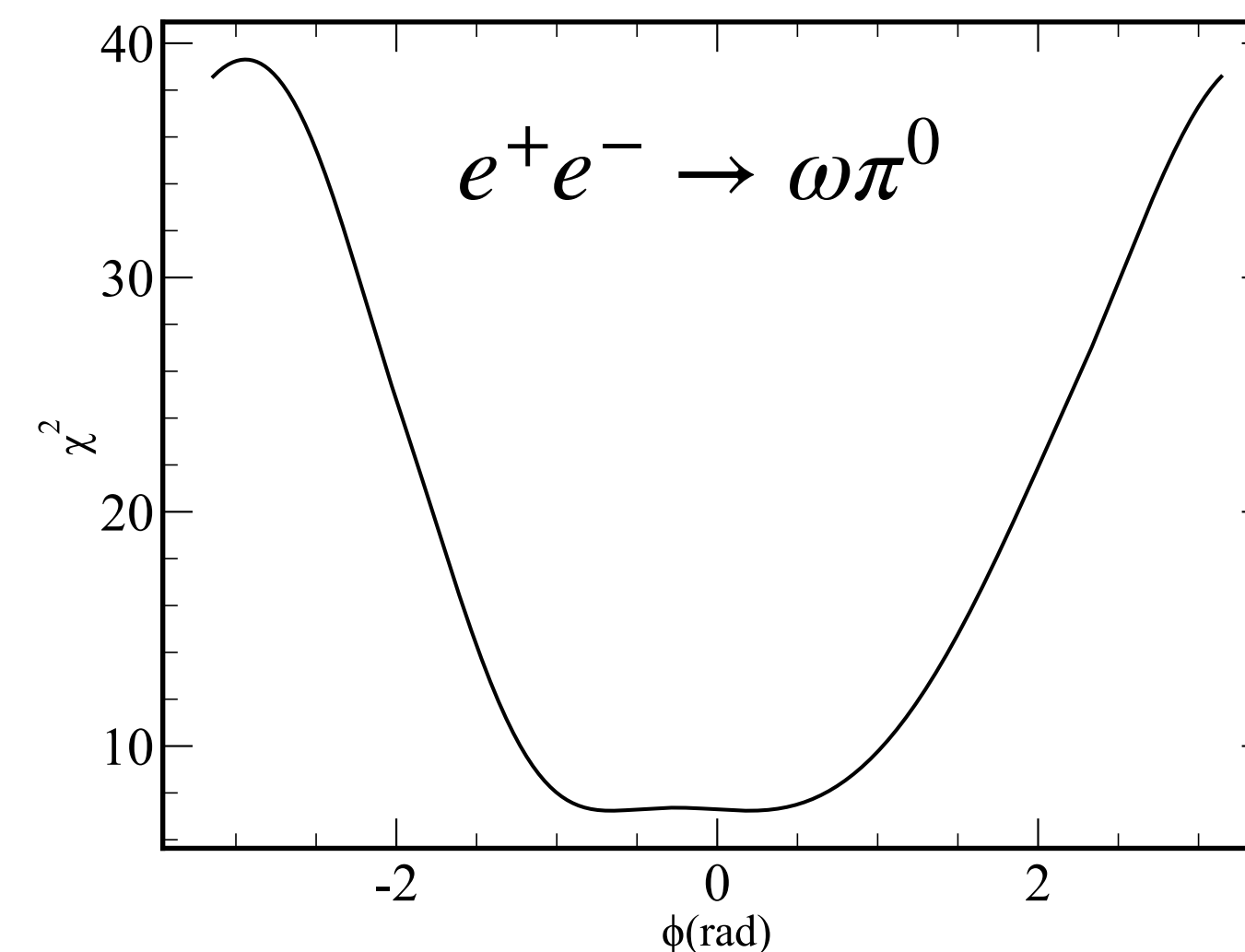
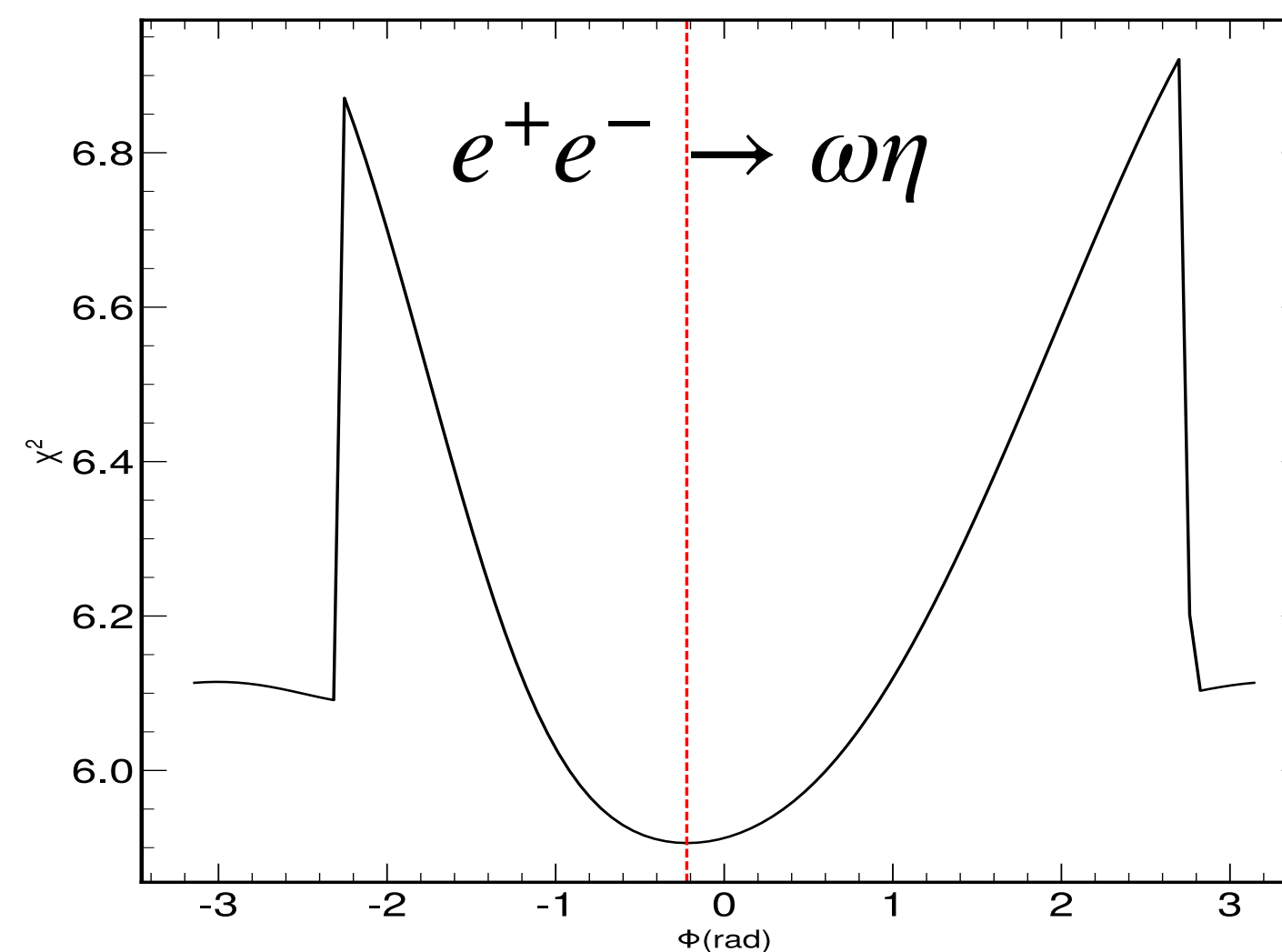
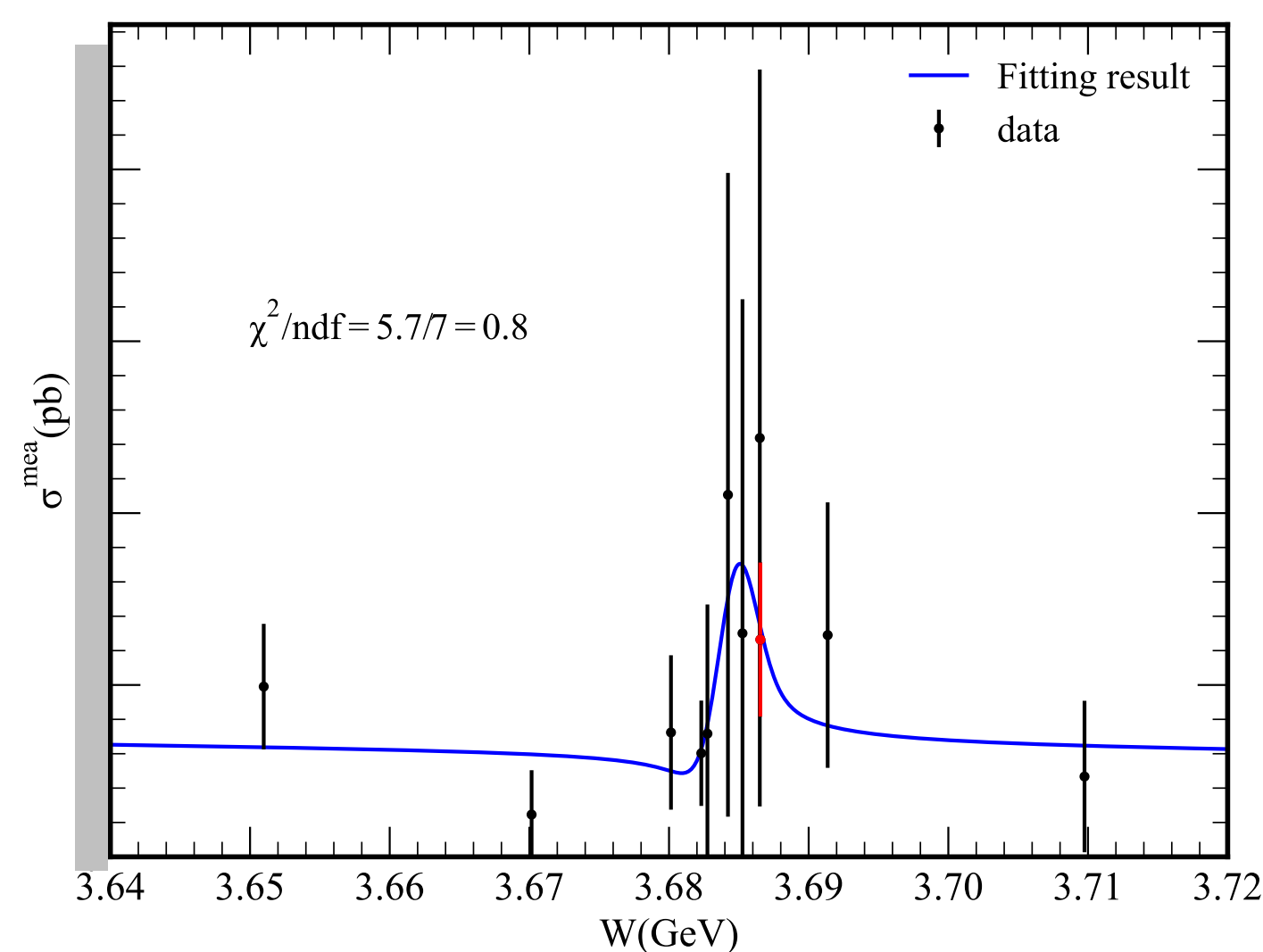
- $$Ce^{i\phi} = \left(1 + C_{\gamma\gamma\gamma}e^{i\phi_{\gamma\gamma\gamma,\gamma}} + C_{ggg}e^{i\phi_{ggg,\gamma}} \right) e^{i\phi_{\gamma,\text{cont.}}}$$

- $$\text{Br}(\psi(3686) \rightarrow \omega\eta) = \frac{C^2 \mathcal{F}_{\omega\eta}^2 \Gamma_{ee} q_{\omega\eta}^3(M)}{M^4 \Gamma}$$

Parameter	Result
$M(\text{MeV})$	3684.81 ± 0.91
$\mathcal{C}$	± 0.95
$\Phi(\text{rad})$	± 2.39
$\mathcal{B}(\psi(2S) \rightarrow \omega\eta)$	$(\pm) \times 10^{-6}$

- Large uncertainty of ϕ causes large uncertainty of Br

- $\Delta\chi^2$ is flat around $\chi_{\min}^2$ (déjà vu)





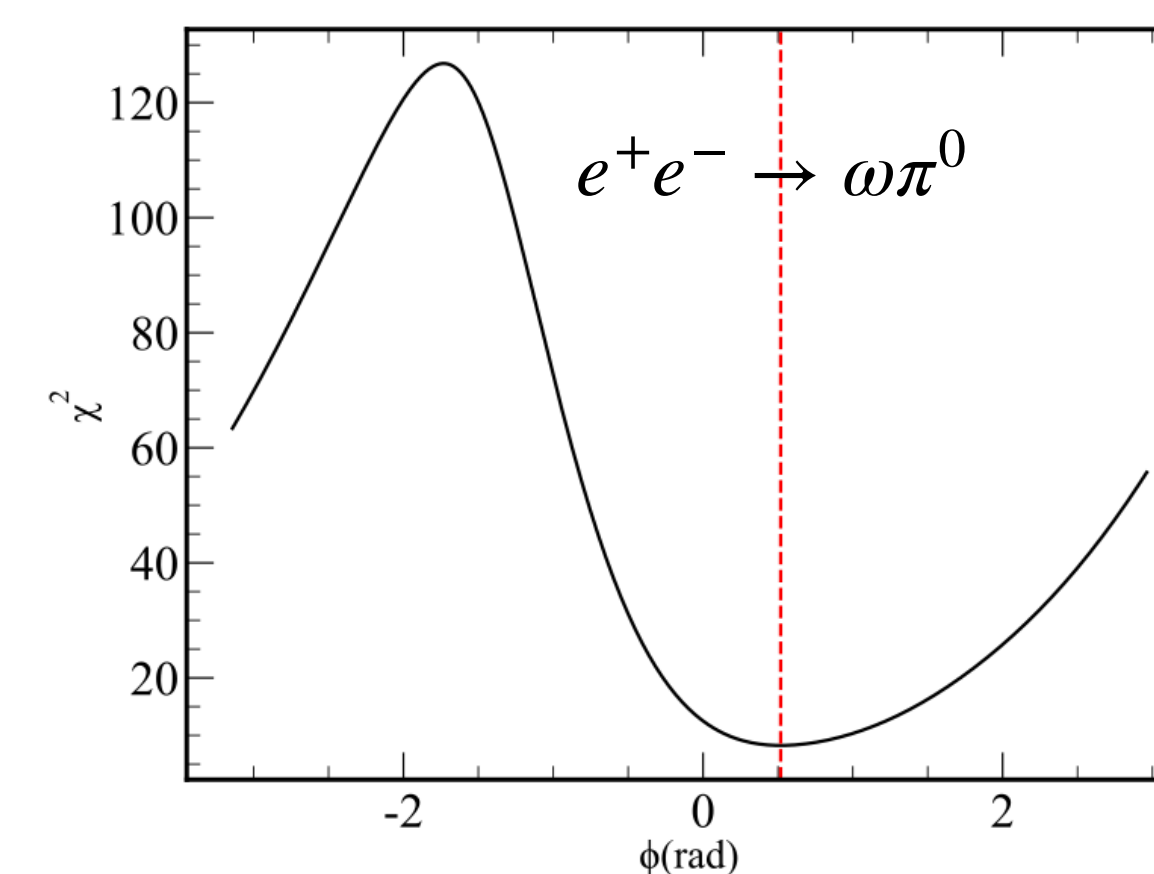
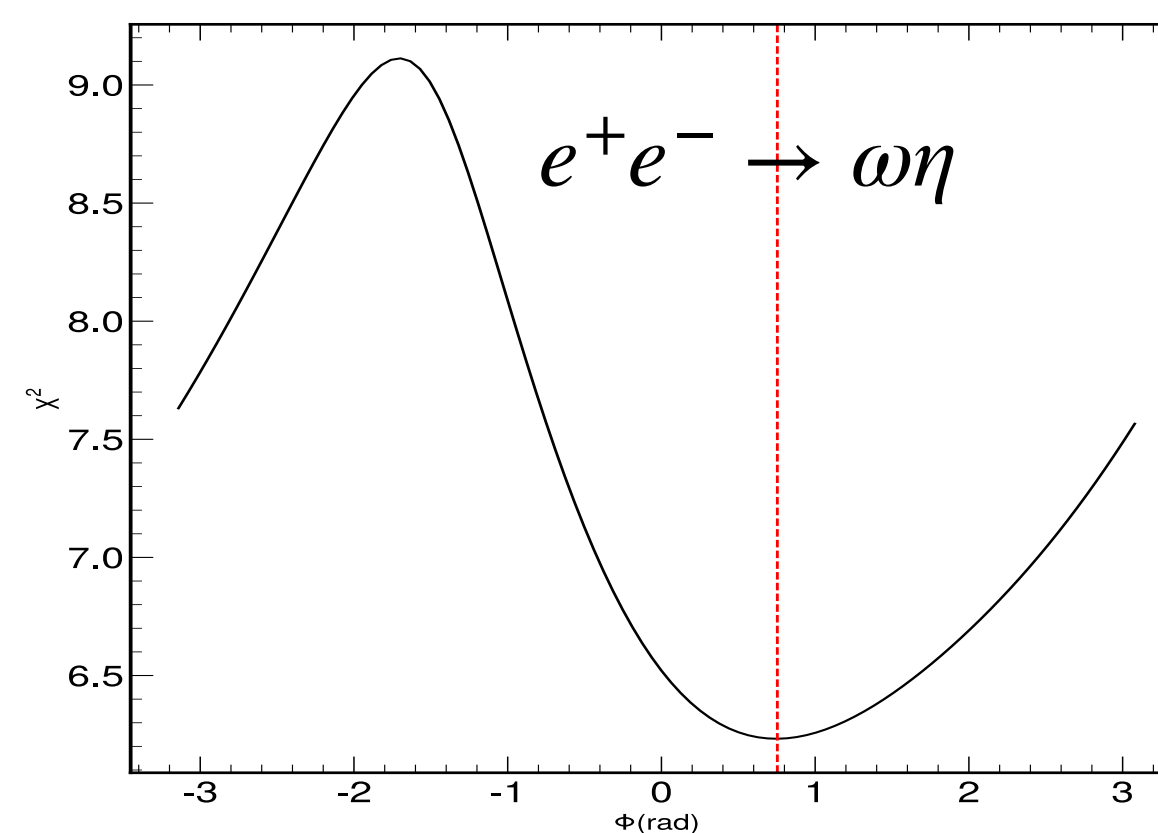
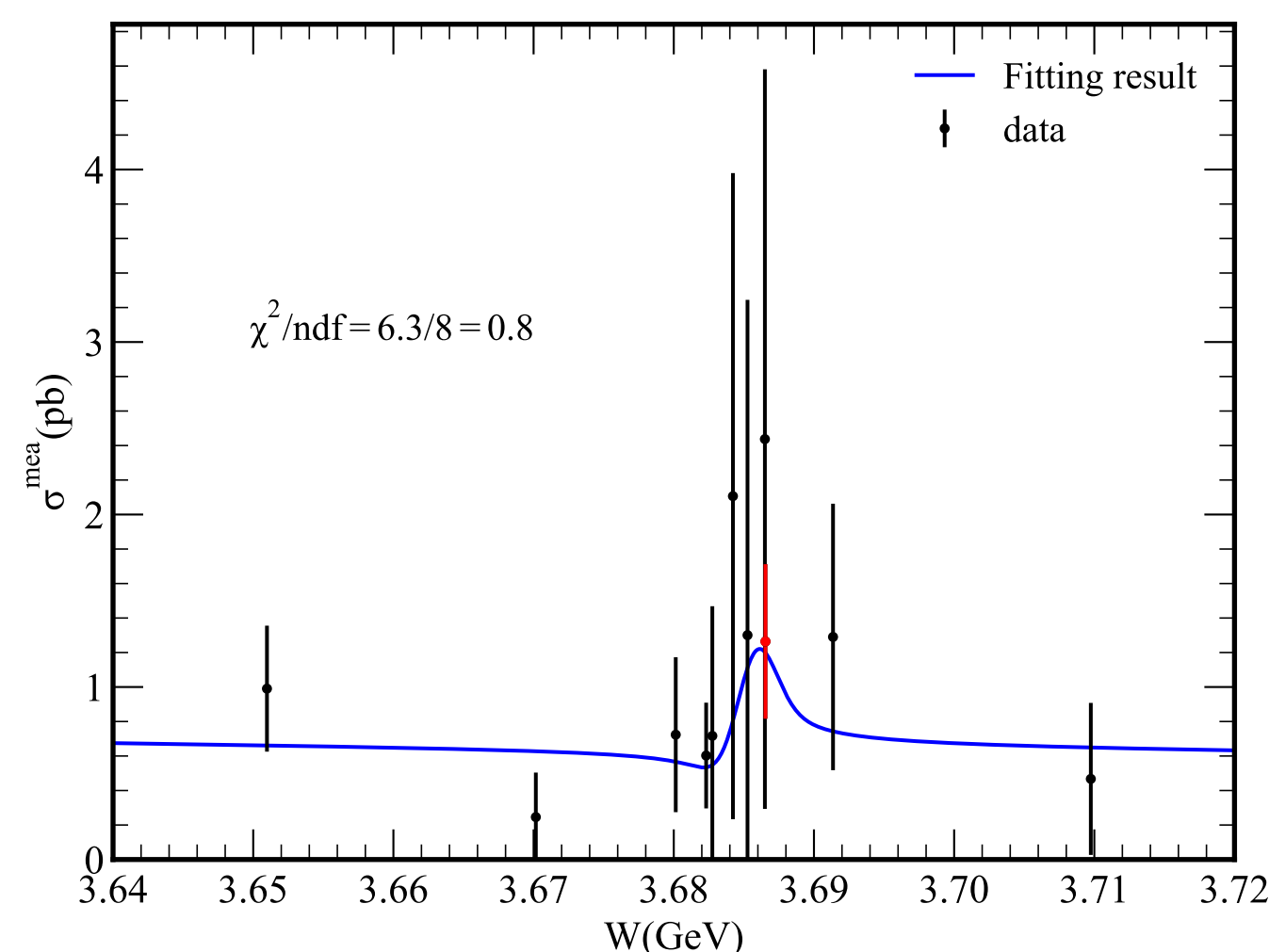
$e^+e^- \rightarrow \omega\eta$ around $\psi(3686)$ resonance



- $\text{Br}_{\text{PDG}}(\psi(3686) \rightarrow \omega\eta)$ does not follow the 12% rule
- “ $\rho\pi$ ” puzzle, Q. Zhao, et al., CPC(2010) **34**, 299
 - “The strong decay of $\psi(3686)$ receives relatively larger destructive interfaces from the intermediate meson loop transitions.”
- We try to only consider the **purely electromagnetic** mode

Parameter	Result
$M(\text{MeV})$	3685.37 ± 1.61
$\Phi(\text{rad})$	± 1.47
$\text{B}(\psi(2S) \rightarrow \omega\eta)$	$(\pm 1.65) \times 10^{-7}$

$$\sigma^{\text{dre}} = \frac{4\pi\alpha^2}{3W^2} \left(\frac{\mathcal{F}_{\omega\eta}}{W^2} \right)^2 q_{\omega\eta}^3(W) \left| \frac{1}{|1 - \Pi_0(W)|} + \frac{3W\Gamma_{ee}e^{i\phi_{\gamma,\text{cont.}}}}{\alpha(W^2 - M^2 + iM\Gamma)} \left(1 + C_{\gamma gg}e^{i\phi_{\gamma gg,\gamma}} - C_{ggg}e^{i\phi_{ggg,\gamma}} \right) \right|^2$$





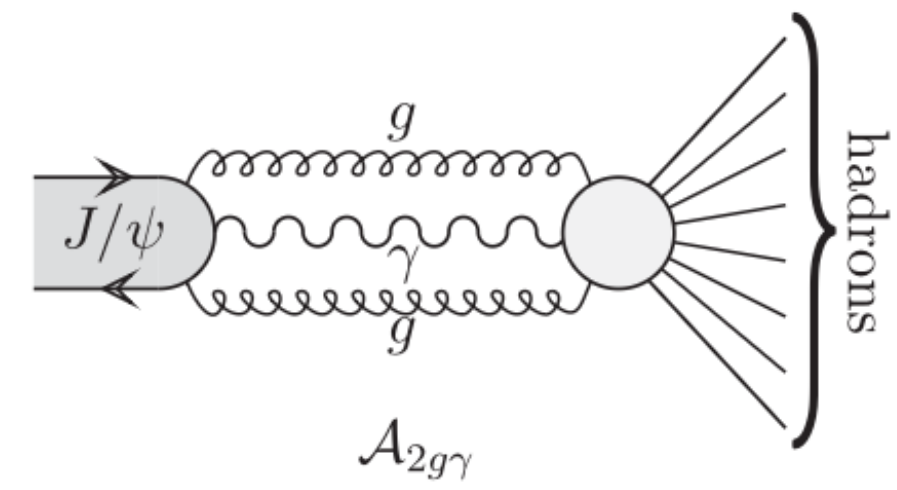
$$J/\psi(\psi') \rightarrow \omega\eta'$$

- $\text{Br}_{\text{PDG}}(J/\psi \rightarrow \omega\eta') = (1.89 \pm 0.18) \times 10^{-4}$; $\text{Br}_{\text{PDG}}(\psi(3686) \rightarrow \omega\eta') = (3.2^{+2.5}_{-2.1}) \times 10^{-5}$
- J/ψ and $\psi(3686)$ scan data lack sufficient statistics to measure the cross sections of $e^+e^- \rightarrow \omega\eta'$ around J/ψ and $\psi(3686)$.
- We expect that $J/\psi \rightarrow ggg$ is predominant in $J/\psi \rightarrow \omega\eta'$.
 - $\text{Br}_{\text{PDG}}(J/\psi \rightarrow \omega\eta') \sim \text{Br}_{\text{PDG}}(J/\psi \rightarrow \omega\pi^0) = (4.5 \pm 0.5) \times 10^{-4}$
 - The exclusive branching ratio and detector efficiency of $\omega\eta'$ is smaller than those of $\omega\pi^0$.
 - $\text{Br}_{\text{PDG}}(J/\psi \rightarrow \omega\eta') \gg \text{Br}_{\text{PDG}}(\psi(2S) \rightarrow \omega\pi^0) = (2.1 \pm 0.6) \times 10^{-5}$
 - The luminosities of scan data around J/ψ are smaller than those around $\psi(3686)$.
- We expect that $J/\psi \rightarrow ggg$ is suppressed in $\psi(3686) \rightarrow \omega\eta'$.
 - Even if $\psi(3686) \rightarrow \omega\eta'$ follows 12% rule, $\text{Br}(\psi(3686) \rightarrow \omega\eta') \sim 10^{-5}$.
- Therefore, we have only measured the branching ratios of $J/\psi(\psi') \rightarrow \omega\eta'$ by using the J/ψ and $\psi(3686)$ data sets.
 - Both passed group review, BESIII memos



Summary



- We have measured the cross sections of $e^+e^- \rightarrow \omega\pi^0(\eta)$ around J/ψ and $\psi(3686)$.
- Due to lack sufficient statistics, not cross sections but $\text{Br}(J/\psi(\psi') \rightarrow \omega\eta')$ has been measured.
- We firstly experimentally observe the **mixed γgg decay mode** in $J/\psi \rightarrow \omega\pi^0$.

$\mathcal{A}_{2g\gamma}$
- Branching ratio of $J/\psi \rightarrow \omega\pi^0$ has passed the cross check from that of $\psi(3686) \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \omega\pi^0$.
- We observe the predominant **purely strong ggg decay mode** in $J/\psi \rightarrow \omega\eta$.
- $|A_{ggg}| \gg |A_\gamma|, |A_{\gamma gg}|$ as we expect.



Summary



- We find that cross section data are **insensitive** to including the **mixed γgg decay mode** in $\psi(3686) \rightarrow \omega\pi^0$, that is, $|A_{\gamma gg}| \ll |A_\gamma|$ in $\psi(3686) \rightarrow \omega\pi^0$.
- Normal or abnormal?
- We find that cross section data are **insensitive** to including the **strong ggg decay mode** in $\psi(3686) \rightarrow \omega\eta$.
- Can we believe that the purely electromagnetic γ^* decay mode is predominant?
 - $|A_{ggg}|, |A_{\gamma gg}| \ll |A_\gamma|$ in $\psi(3686) \rightarrow \omega\eta$?





Thanks



- Pioneers: Ping Wang, Yadi Wang, Rinaldo Baldini Ferroli et al. Looking for the phase angle between strong and EM mechanisms in J/ψ decay

Yadi Wang^{1,4}, Ping Wang³, Rinaldo Baldini Ferroli¹, Marco Destefanis²,
Monica Bertani¹, Marco Maggiora², Adriano Zallo¹, Alessandro Calcaterra¹

- WHU

- Zhenyu Zhang, Zhefei Tian, Baoxin Liu, Yanning Wang, Yiqi Du, Wenhao Ya, Zikun Xi et al.

- LNU

- Xiaoshen Kang, Li Gong

- USTC

- Xiaorong Zhou, Hailin Song

- IHEP

- In memory of **Bingxin Zhang** (张丙新)

- Gang Li, Jiabao Gong

