



HFCPV2025

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THE 22nd NATIONAL SYMPOSIUM ON HEAVY FLAVOR PHYSICS AND CP VIOLATION

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Charm physics and Charmed-baryon decays at Belle II

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Belle and Belle II Experiments

- Asymmetric e^+e^- colliders
- Collisions mainly at 10.58 GeV , i.e at $\Upsilon(4S)$ resonance

KEKB

1999-2010

- e^+ (3.5 GeV) e^- (8 GeV)
- L_{peak} : $2.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ [achieved]

SuperKEKB

2019-current

- e^+ (4 GeV) e^- (7 GeV)

Target:

$$\int L dt = 50 \text{ ab}^{-1}$$

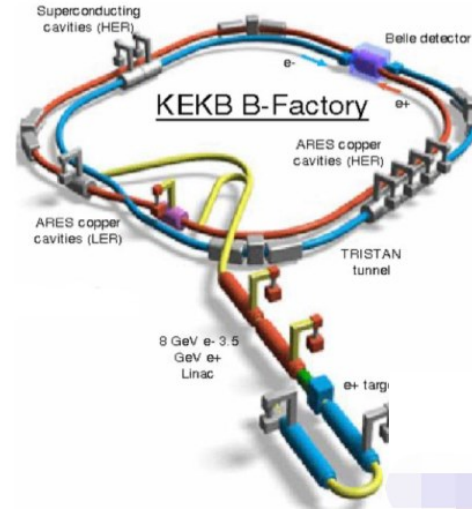
$$L_{peak} = 6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$$

Achieved:

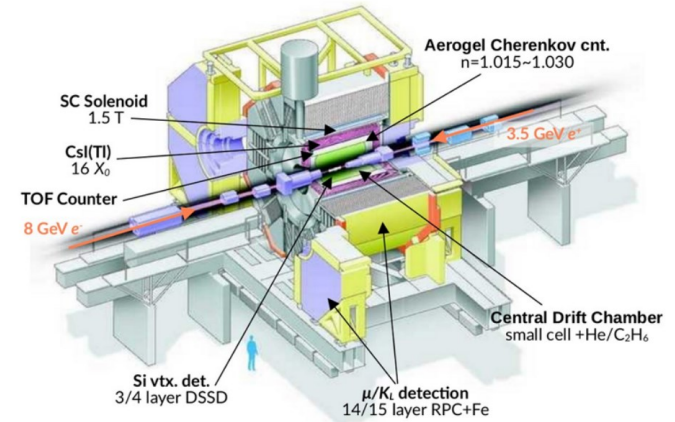
$$\int L dt > 530 \text{ fb}^{-1}$$

$$L_{peak} = 4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

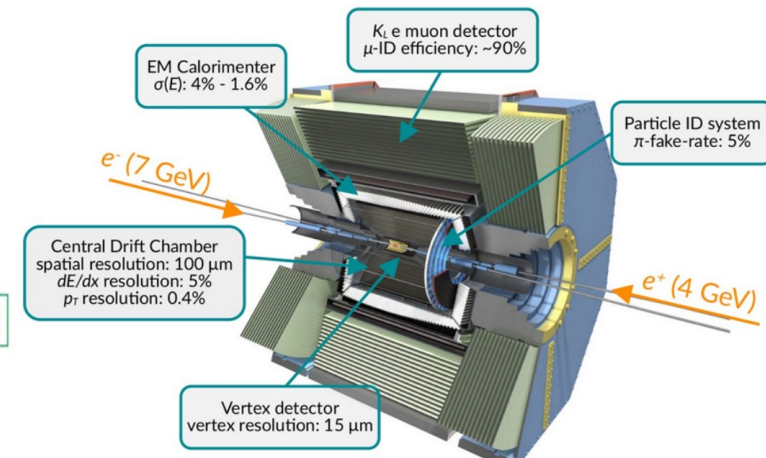
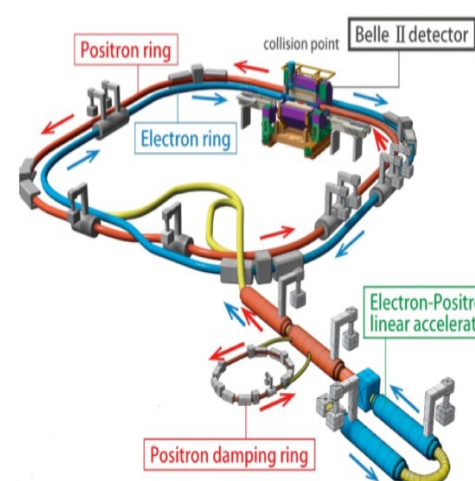
Current world record



BELLE @ KEKB



Belle II @ SuperKEKB



Charm physics at Belle and Belle II

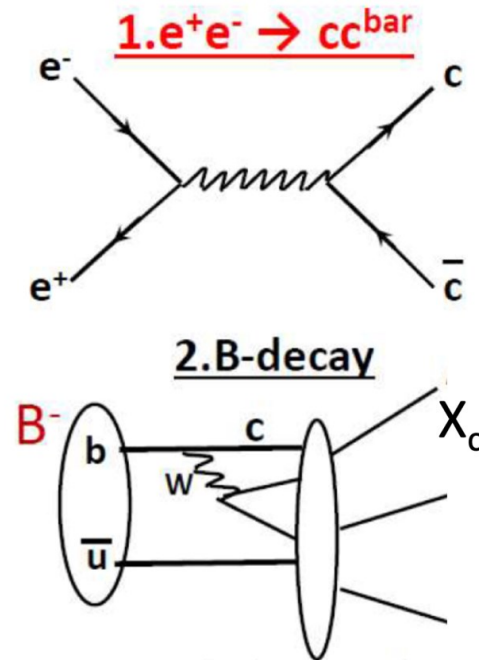
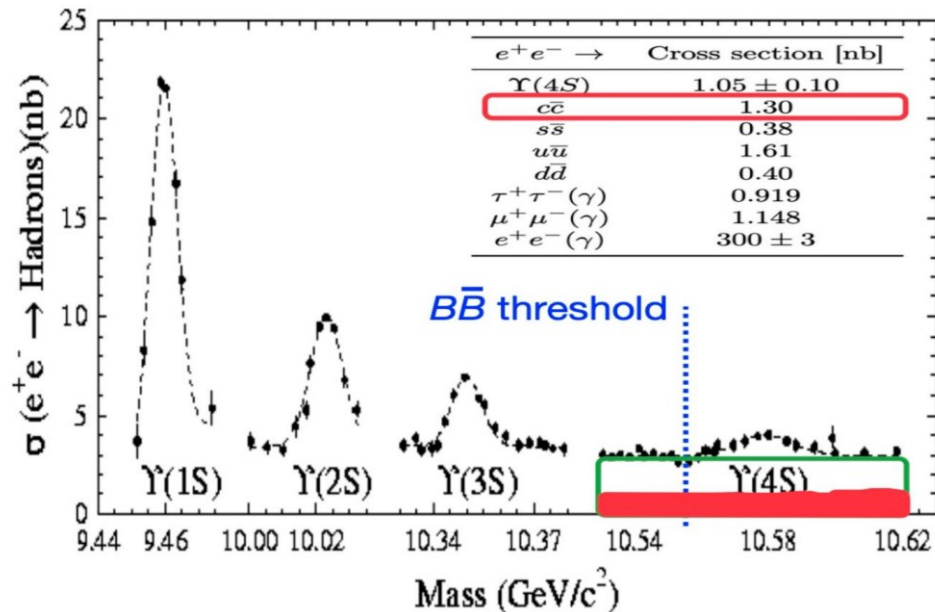
Two primary mechanisms for charm production at Belle/Belle II:

1. $e^+e^- \rightarrow c\bar{c} \rightarrow X_c$

- Absolute measurements not possible without reference
- Used for most analyses due to its simplicity compared to $B\bar{B}$ processes

2. $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B} \rightarrow X_c$

- Precise $B\bar{B}$ cross section allows for absolute measurements



CPV in Charm

CPV in $D \rightarrow \pi\pi$

- $D^0 \rightarrow \pi^+ \pi^-$:
 - the only channel with $> 3\sigma$ evidence of CPV in charm.
 - The SM generates CPV through interference of a tree-level and suppressed QCD loop amplitude $\Delta I = 1/2$ (I = isospin) [*Phys. Rev.D* 85, 114036 (2012)].
- $D^+ \rightarrow \pi^+ \pi^0$:
 - $I=2$ and can be reached from the $I=1/2$ initial state only via a $\Delta I = 3/2$ transition.
 - Therefore, any observation will confirm New Physics.
- $D^0 \rightarrow \pi^0 \pi^0$:
 - Can have $I=0$ or $I=2$ and hence can have nonzero direct CP asymmetries in SM.
 - Isospin sum rule:

$$R = \frac{a_{CP}(\pi^+ \pi^-)}{1 + \frac{\tau_{D^0}}{\mathcal{B}_{+-}} \left(\frac{\mathcal{B}_{00}}{\tau_{D^0}} - \frac{2}{3} \frac{\mathcal{B}_{+0}}{\tau_{D^+}} \right)} + \frac{a_{CP}(\pi^0 \pi^0)}{1 + \frac{\tau_{D^0}}{\mathcal{B}_{00}} \left(\frac{\mathcal{B}_{+-}}{\tau_{D^0}} - \frac{2}{3} \frac{\mathcal{B}_{+0}}{\tau_{D^+}} \right)} + \frac{a_{CP}(\pi^+ \pi^0)}{1 - \frac{3}{2} \frac{\tau_{D^+}}{\mathcal{B}_{+0}} \left(\frac{\mathcal{B}_{00}}{\tau_{D^0}} + \frac{\mathcal{B}_{+-}}{\tau_{D^0}} \right)}$$

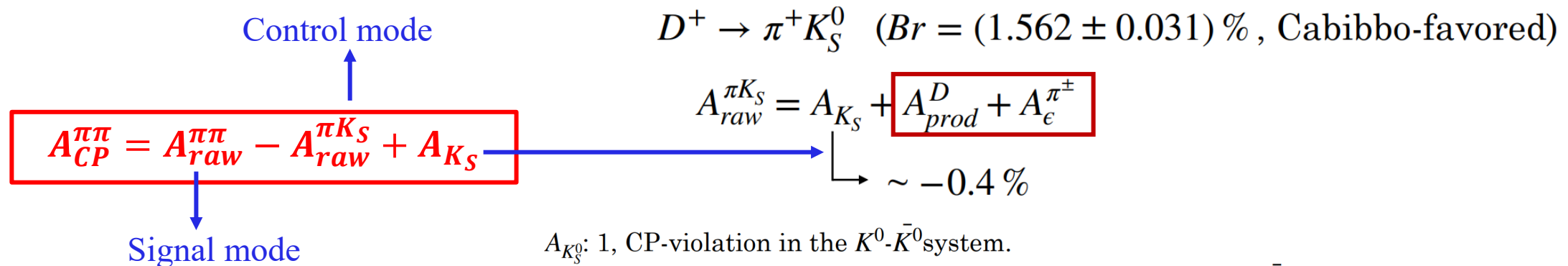
- $a_{CP} \neq 0, R=0$: CP violation from the $\Delta I=3/2$ amplitude (New Physics!!)
- $R = (0.93 \pm 3.1) \times 10^{-3}$, uncertainty is dominated by the $\pi^0 \pi^0$ mode HFLAV

- The physics variable that we are interested is $A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = \frac{\Gamma(D^+ \rightarrow \pi^+ \pi^0) - \Gamma(D^- \rightarrow \pi^- \pi^0)}{\Gamma(D^+ \rightarrow \pi^+ \pi^0) + \Gamma(D^- \rightarrow \pi^- \pi^0)}$
- But the variable easily accessed in exp is $A_{raw}^{\pi\pi} = \frac{N(D^+ \rightarrow \pi^+ \pi^0) - N(D^- \rightarrow \pi^- \pi^0)}{N(D^+ \rightarrow \pi^+ \pi^0) + N(D^- \rightarrow \pi^- \pi^0)}$
- $A_{raw}^{\pi\pi}$ is related by $A_{CP}^{\pi\pi} = A_{raw}^{\pi\pi} - (A_{prod}^D + A_{\epsilon}^{\pi}) \rightarrow$ **nuisance asymmetries**

A_{prod}^D : forward-backward asymmetric production in e^+e^- collisions of charm hadrons, due to $\gamma^* - Z^0$ interference and higher-order QED effects, is an odd function of $\cos\theta_{CM}(D^\pm)$.

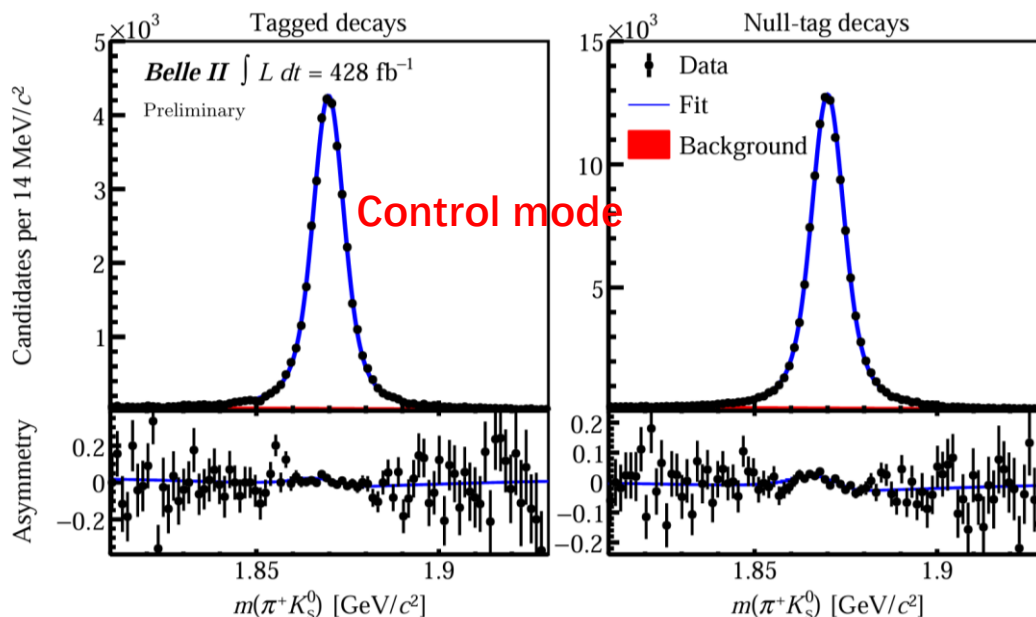
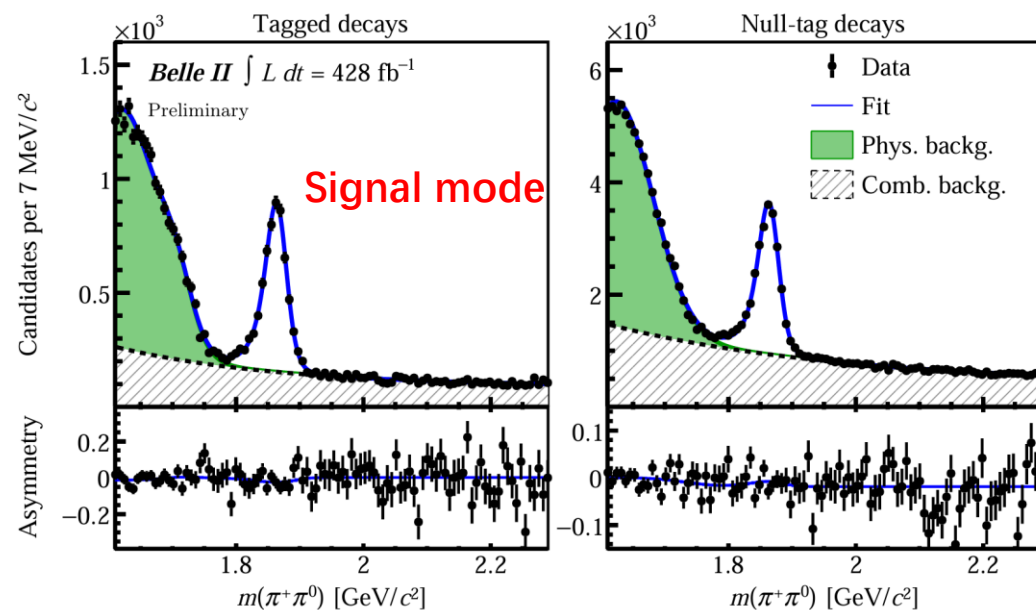
$A_{\epsilon}^{\pi^\pm}$: detection asymmetry of the low-momentum tagging pions.

$\downarrow$
use $D^+ \rightarrow \pi^+ K_S^0$ as a control mode to estimate this



$A_{K_S^0}$: 1, CP-violation in the $K^0 - \bar{K}^0$ system.

2, different nuclear-interaction cross-sections for K^0 and $\bar{K}^0$ mesons with detector.



Signal mode

	Tagged	Null-tag
Yield	5130 ± 110	18510 ± 240
A_{raw}	$(-2.9 \pm 1.8)\%$	$(-0.4 \pm 1.0)\%$

Control mode

	Tagged	Null-tag
Yield	39630 ± 300	123560 ± 500
A_{raw}	$(0.54 \pm 0.53)\%$	$(0.33 \pm 0.30)\%$

• Using 428 /fb, Belle II obtain:

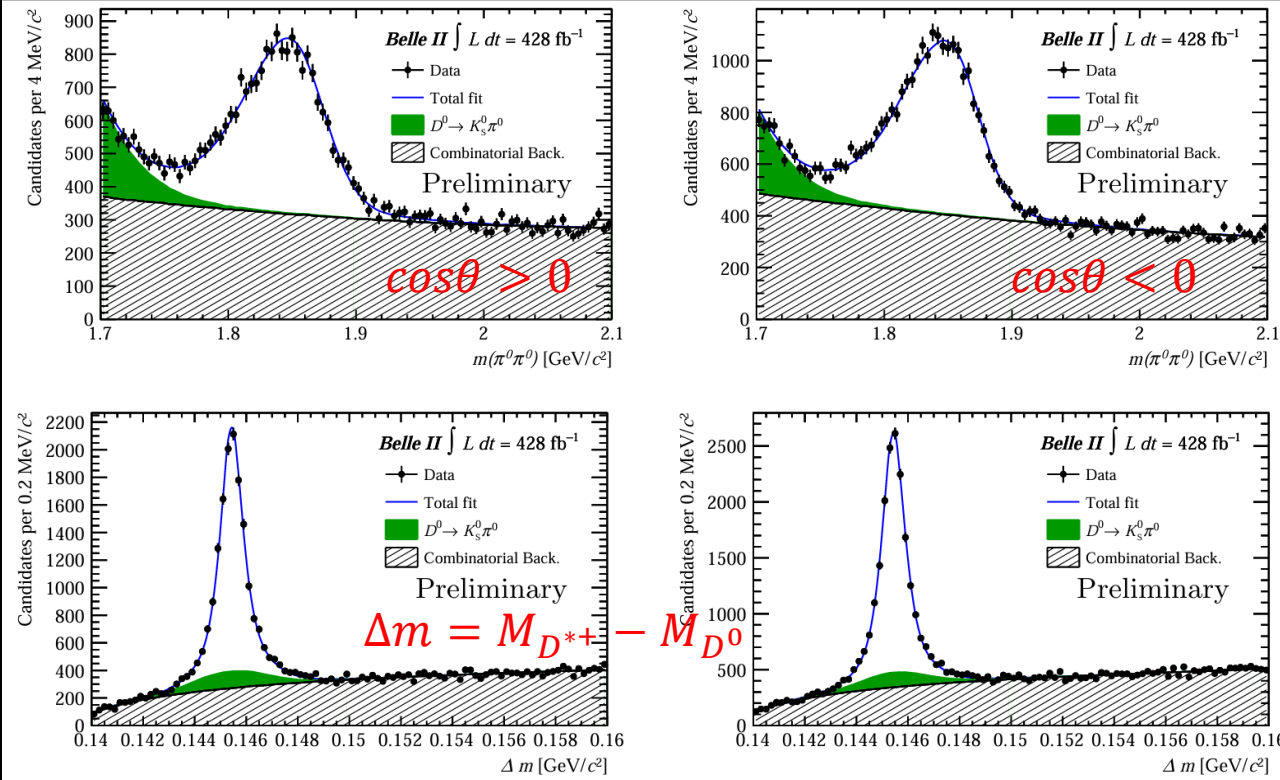
1. $A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = [-3.9 \pm 1.8(stat) \pm 0.2(syst)] \%$ for D^* -tagged sample;
2. $A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = [-1.1 \pm 1.0(stat) \pm 0.1(syst)] \%$ for null-tag sample.

• Combined:

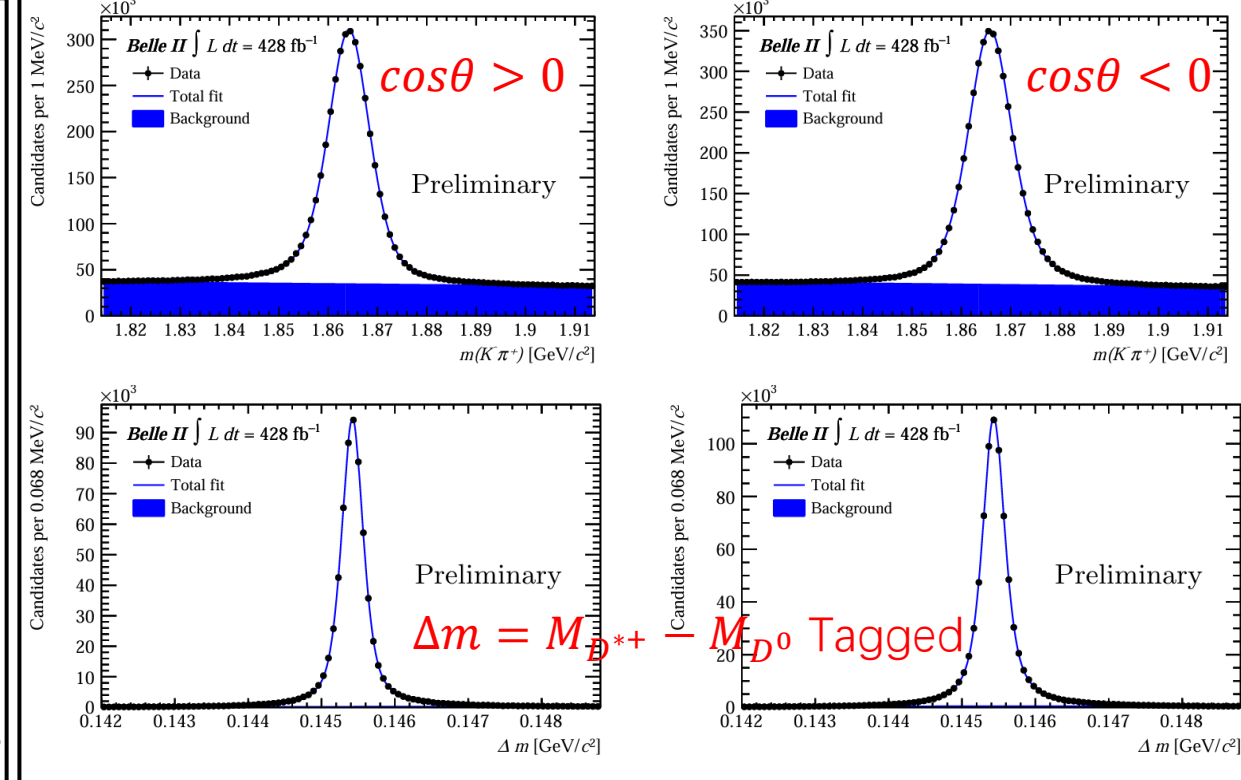
$$A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = [-1.8 \pm 0.9(stat) \pm 0.1(syst)] \%,$$

- most precise measurement
- improved precision compared to Belle's result: $(2.3 \pm 1.3 \pm 0.2)\%$ [*Phys. Rev. D* 97, 011101 (2018)]

Signal mode



Control mode



- $A_{CP}(D^0 \rightarrow \pi^0 \pi^0)$: $(0.30 \pm 0.72 \pm 0.20) \%$

- 15% less precise than the Belle measurement:
 $(0.030 \pm 0.64 \pm 0.10) \%$ [*Phys. Rev. Lett.* 112, 211601 (2014)]

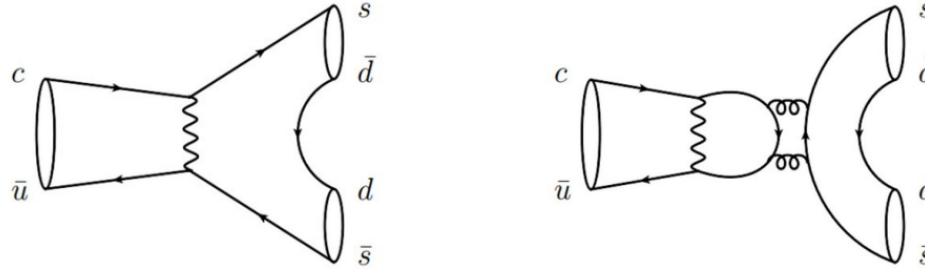
- $R = (1.5 \pm 2.5) \times 10^{-3}$, 20% improved precision.

- The improved precision per luminosity due to Belle II's better reconstruction π^0 .

- The CP asymmetry (SCS)

$$A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = \frac{\Gamma(D^0 \rightarrow K_S^0 K_S^0) - \Gamma(\bar{D}^0 \rightarrow K_S^0 K_S^0)}{\Gamma(D^0 \rightarrow K_S^0 K_S^0) + \Gamma(\bar{D}^0 \rightarrow K_S^0 K_S^0)},$$

- It may be enhanced to be an observable level ($\sim 1\%$) within the Standard Model, due to the interference of $c \rightarrow us\bar{s}$ and $c \rightarrow udd\bar{d}$ amplitudes. [[PRD 99, 113001 \(2019\)](#), [PRD 86, 014023 \(2012\)](#), [PRD 92, 054036 \(2015\)](#)]



- World average: $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-1.9 \pm 1.0) \%$ is dominated by

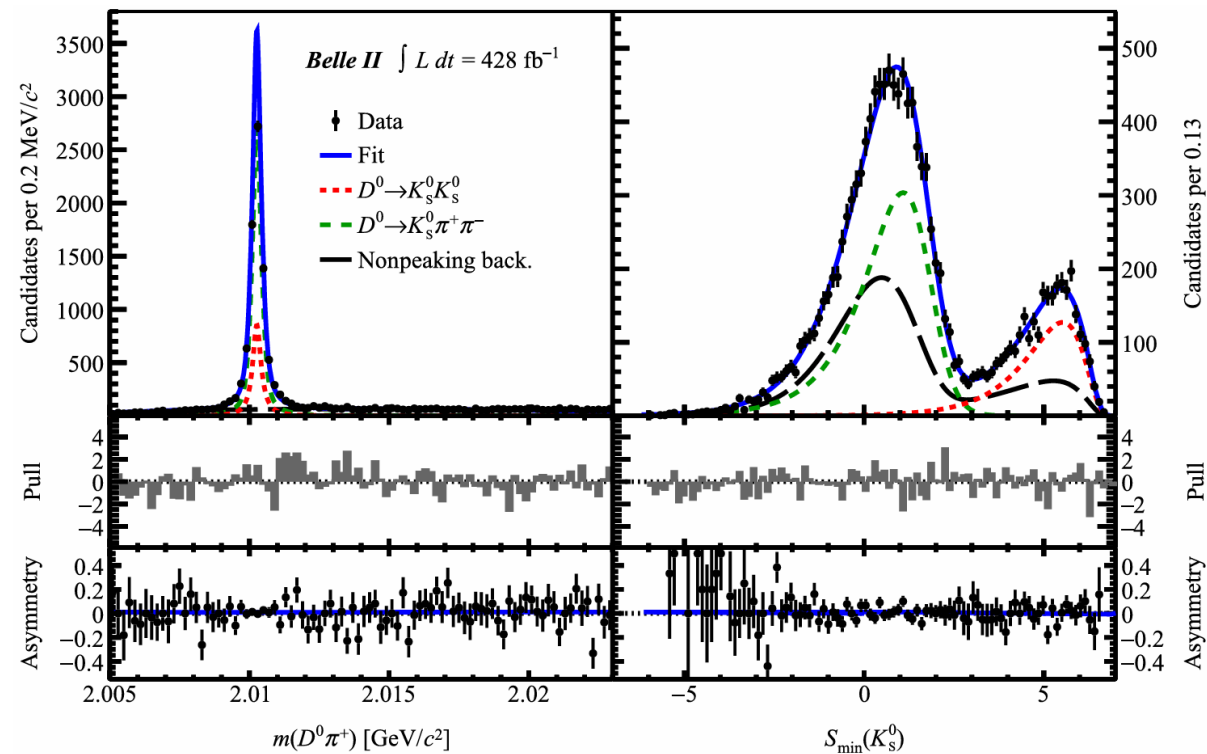
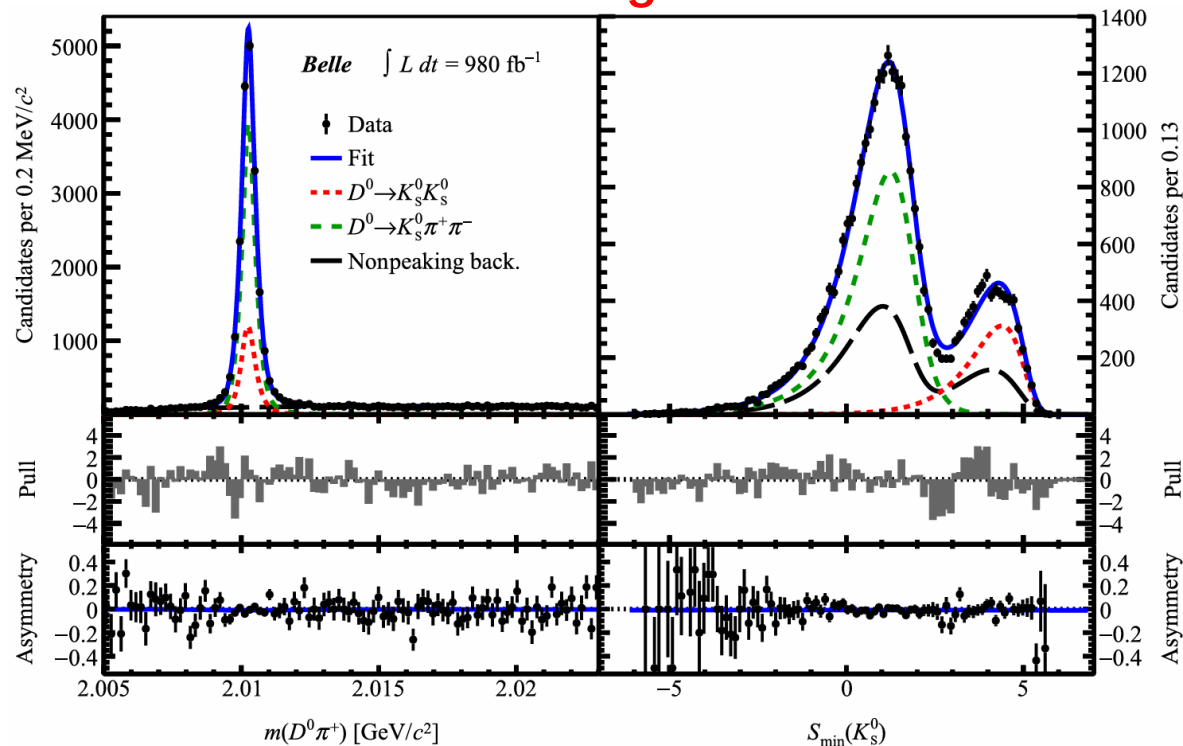
Belle (921 /fb): $A_{CP} = (-0.02 \pm 1.53 \pm 0.02 \pm 0.17) \%$, using $D^0 \rightarrow K_S^0 \pi^0$ as control mode. [PRL 119, 171801 \(2017\)](#)

LHCb (6 /fb): $A_{CP} = (-3.1 \pm 1.2 \pm 0.4 \pm 0.2) \%$, using $D^0 \rightarrow K^+ K^-$ as control mode. [PRD 104, L031102 \(2021\)](#)

CP asymmetry in $D^0 \rightarrow K_S^0 K_S^0$

PRD 111, 012015 (2025)

Signal mode



- Simultaneous 2D fit to $m(D^0 \pi^+)$ and $S_{\min}(K_S^0)$.

Using D^* tag method

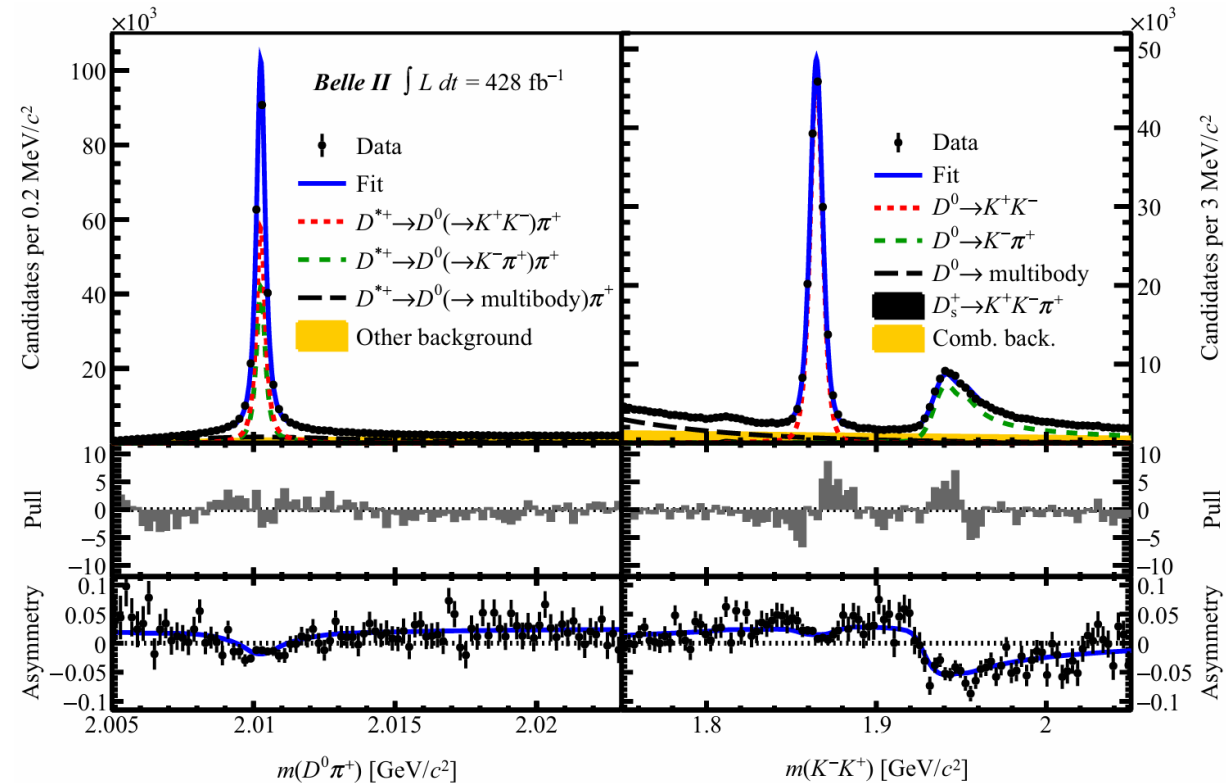
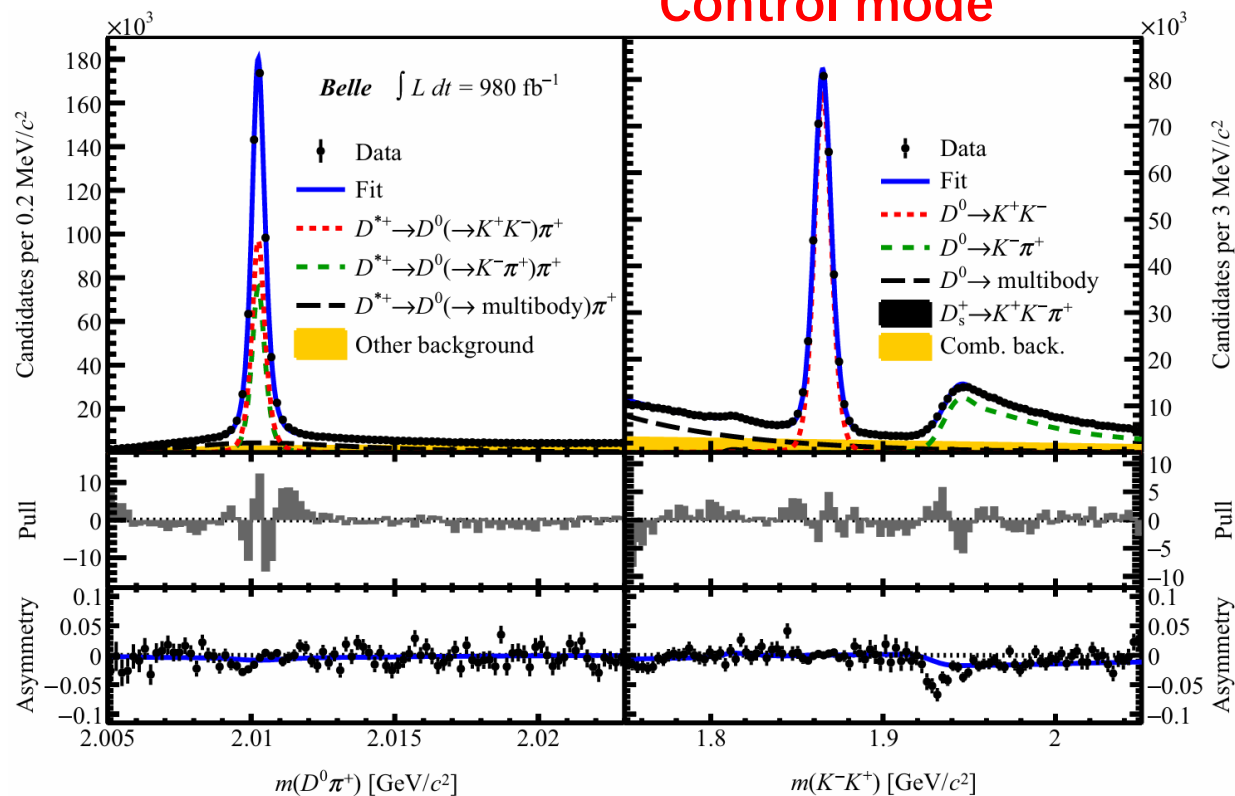
- **Signal** and **Physics background** ($D^0 \rightarrow K_S^0 \pi^+ \pi^-$) peak at the same position in $m(D^0 \pi^+)$ but different in $S_{\min}(K_S^0)$.

$$A_{\text{raw}}^{K_S^0 K_S^0} = (-1.0 \pm 1.6) \% \text{ in Belle; } A_{\text{raw}}^{K_S^0 K_S^0} = (-0.6 \pm 2.3) \% \text{ in Belle II.}$$

CP asymmetry in $D^0 \rightarrow K_S^0 K_S^0$

PRD 111, 012015 (2025)

Control mode



$$A_{raw}^{K^+ K^-} = (0.17 \pm 0.19) \% \text{ in Belle}; A_{raw}^{K^+ K^-} = (1.61 \pm 0.27) \% \text{ in Belle II.}$$

- Combined Belle and Belle II (1.4 /ab), $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-1.4 \pm 1.3 \pm 0.1) \%$, comparable to the best existing measurement (LHCb).
 - Factor of two smaller systematic uncertainty as compared to Belle result: $(-0.02 \pm 1.53 \pm 0.02 \pm 0.17) \%$ [Phys. Rev. Lett. 119, 171801 (2017)]
 - Comparable with world's best measurement by LHCb: $(-3.1 \pm 1.2 \pm 0.4 \pm 0.2) \%$ [Phys. Rev. D 104, L031102 (2021)].

CP asymmetry in $D^0 \rightarrow K_S^0 K_S^0$

PRD 112, 012017 (2025)

Using charm
flavor tagger

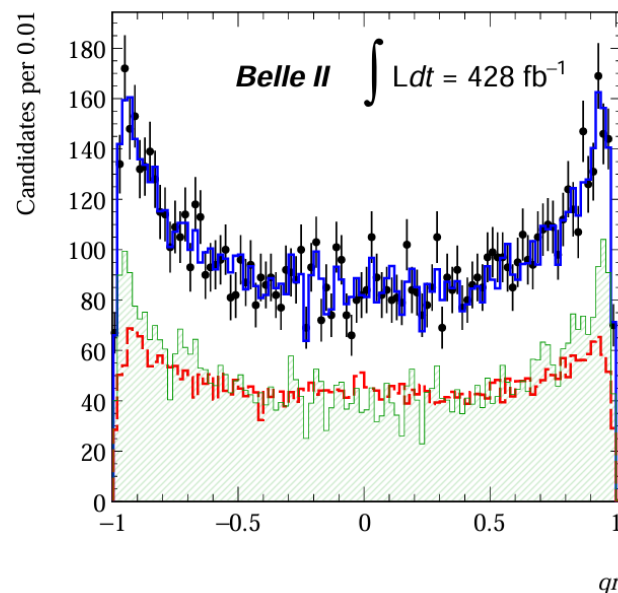
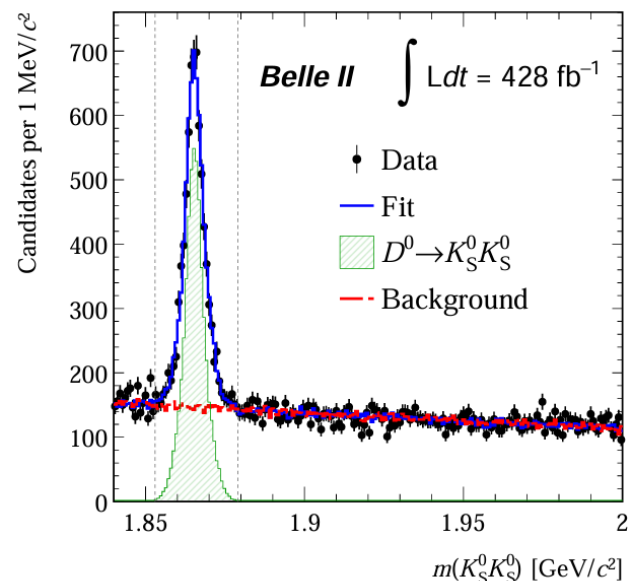
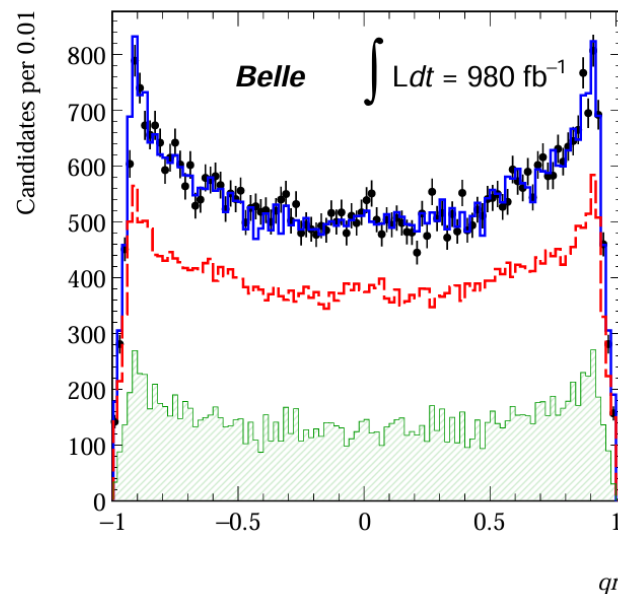
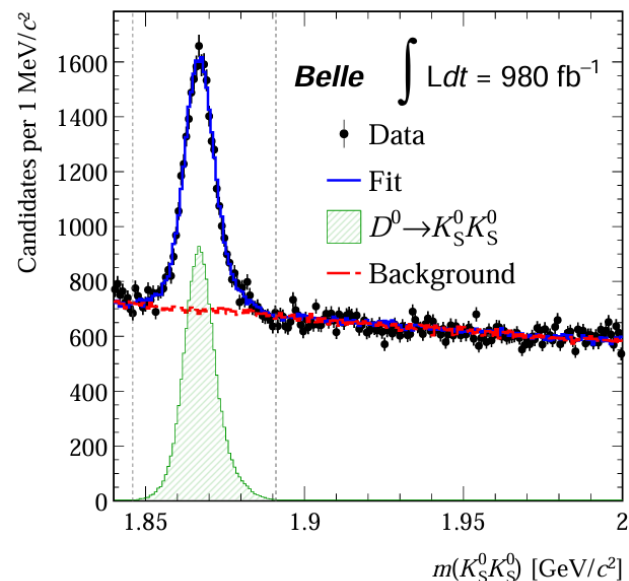
- Events used in the previous analysis are removed.
- $D^0 \rightarrow K_S \pi^+ \pi^-$ suppressed using $S_{\min}(K_S)$.

Combine Belle and Belle II:

$$A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (1.3 \pm 2.0 \pm 0.3)\%$$

Method	A_{CP} [%]
D^* -tag	$-1.4 \pm 1.3 \pm 0.1$
CFT-tag	$1.3 \pm 2.0 \pm 0.3$
Combination	$-0.6 \pm 1.1 \pm 0.1$

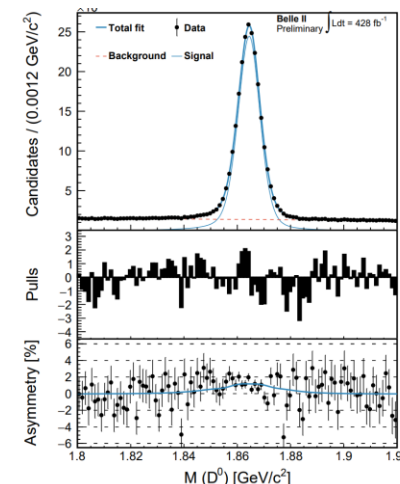
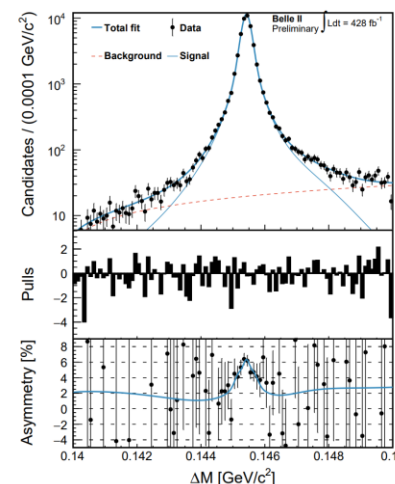
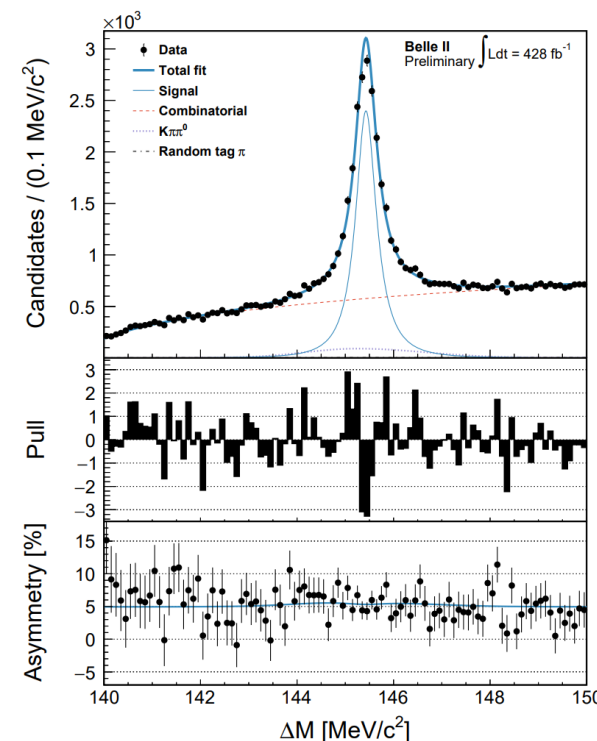
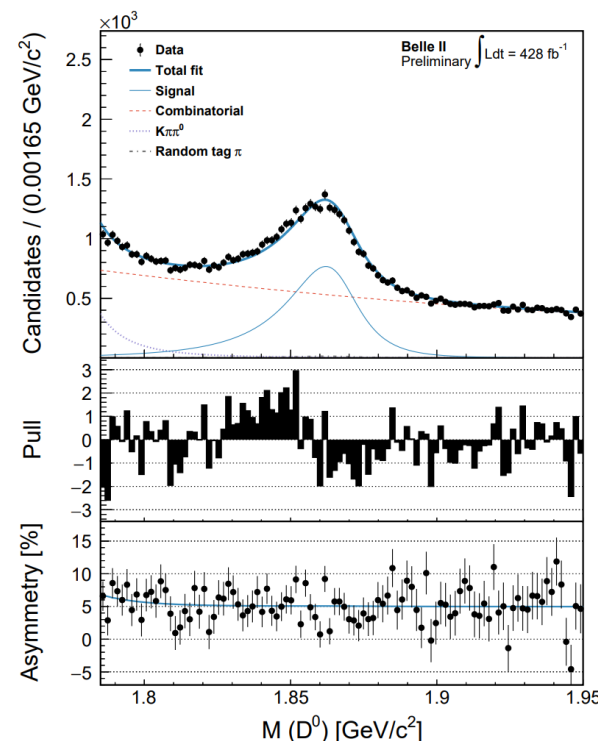
○ Most precise determination till date.



CP asymmetry in $D^0 \rightarrow \pi^+ \pi^- \pi^0$

Preliminary result

- SCS three-body decay, interference of several amplitude
- Signal: D^{*+} tagged sample for $D^0 \rightarrow \pi^+ \pi^- \pi^0$.
- Control mode: tagged and untagged $D^0 \rightarrow K^- \pi^+$
- Simultaneous fit to $(\Delta m, m(\pi^+ \pi^- \pi^0))$ in 8 bins of $\cos\theta_{\text{CM}}$, averaged symmetrically around 0 to remove the production asymmetry
- $A_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^- \pi^0): (0.29 \pm 0.27 \pm 0.13) \%$
 - Most precise measurement till date
 - 34% more precise than BABAR with just 10% more statistics



CP asymmetry in $\Xi_c^+ \rightarrow \Sigma^+ h^+ h^-$ and $\Lambda_c^+ \rightarrow p h^+ h^-$

Preliminary result

First measurement of A_{CP} in SCS three-body charm baryon decays.

$$A_{CP}(X_c^+ \rightarrow f^+) \equiv \frac{\Gamma(X_c^+ \rightarrow f^+) - \Gamma(\bar{X}_c^- \rightarrow \bar{f}^-)}{\Gamma(X_c^+ \rightarrow f^+) + \Gamma(\bar{X}_c^- \rightarrow \bar{f}^-)}.$$

Measured A_{CP} :

$$A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-) = (3.7 \pm 6.6 \pm 0.6)\%,$$

$$A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-) = (9.5 \pm 6.8 \pm 0.5)\%,$$

$$A_{CP}(\Lambda_c^+ \rightarrow p K^+ K^-) = (3.9 \pm 1.7 \pm 0.7)\%,$$

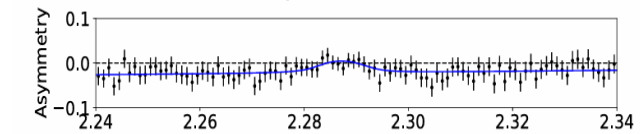
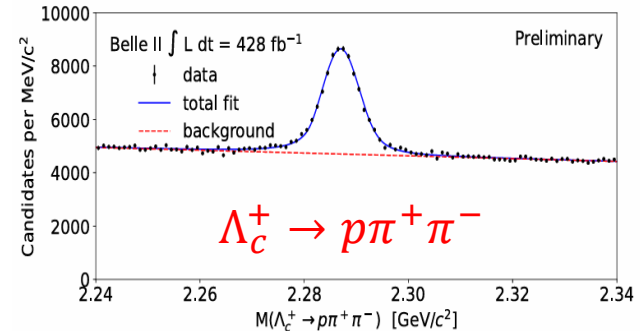
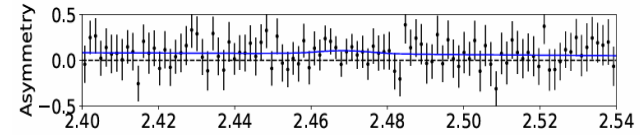
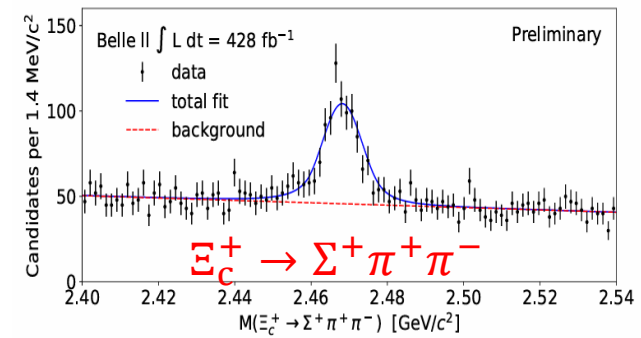
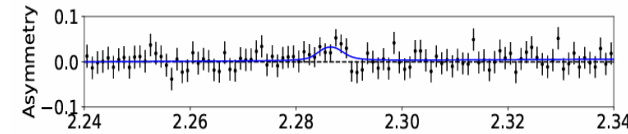
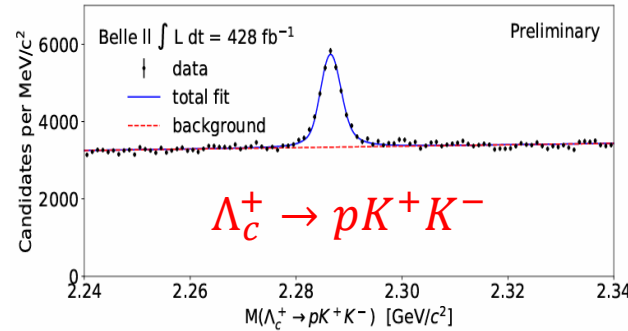
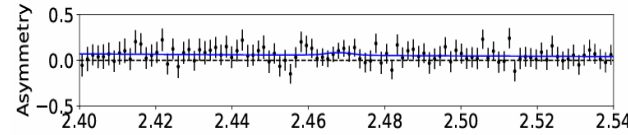
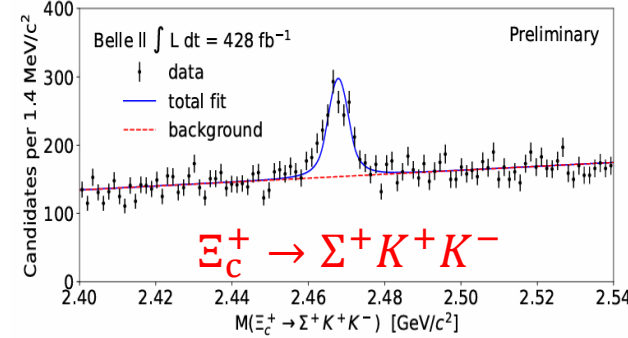
$$A_{CP}(\Lambda_c^+ \rightarrow p \pi^+ \pi^-) = (0.3 \pm 1.0 \pm 0.2)\%,$$

U-spin symmetry with 7% precision:

$$A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-) + A_{CP}(\Lambda_c^+ \rightarrow p K^+ K^-) = (13.4 \pm 7.0 \pm 0.9)\%,$$

$$A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-) + A_{CP}(\Lambda_c^+ \rightarrow p \pi^+ \pi^-) = (4.0 \pm 6.6 \pm 0.7)\%,$$

- Their uncertainties are mainly statistical.
- Future measurements using more data collected by will be important for CP violation and testing U spin.



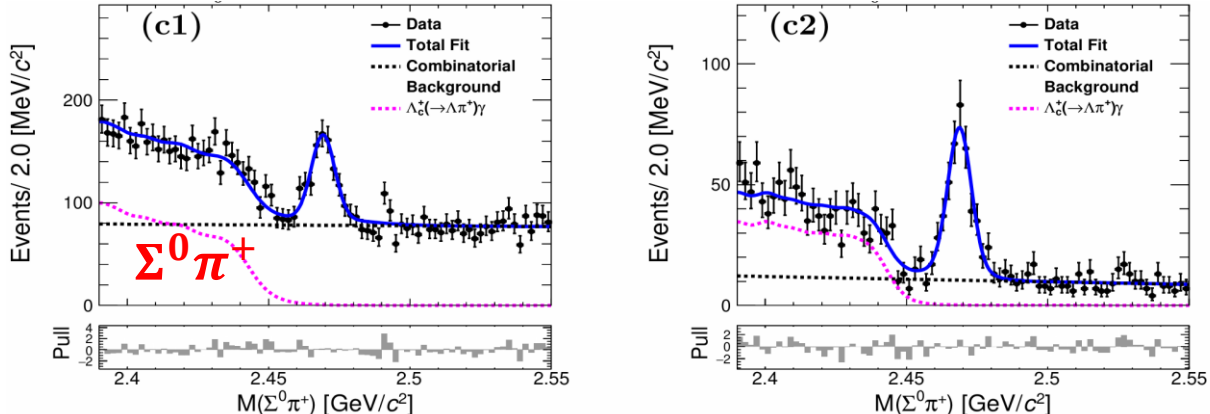
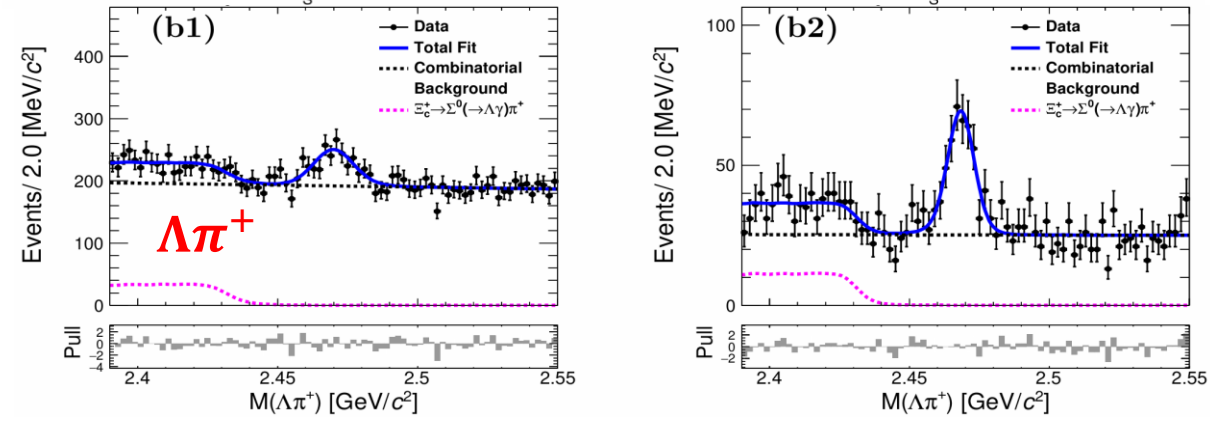
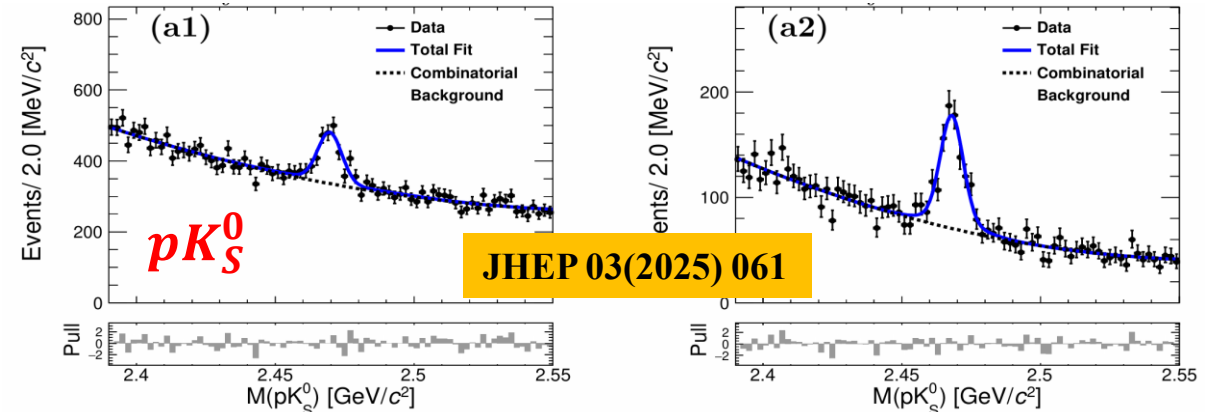
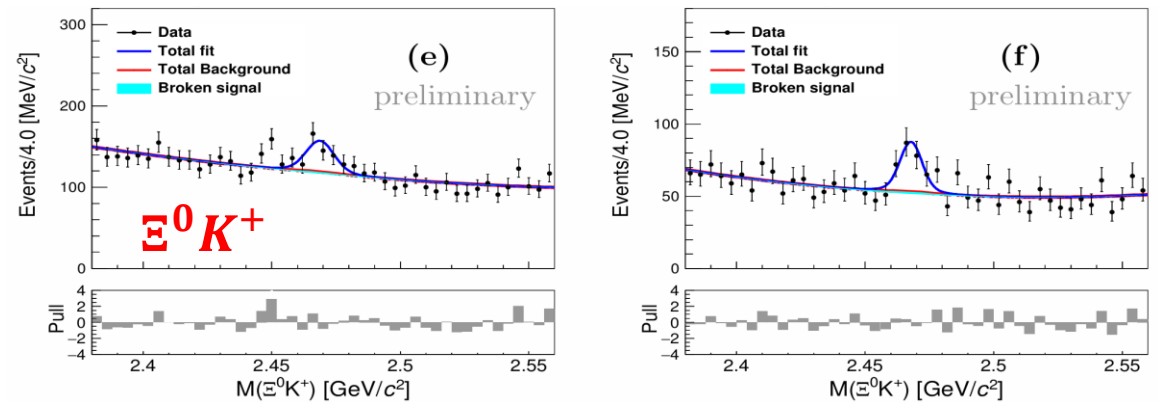
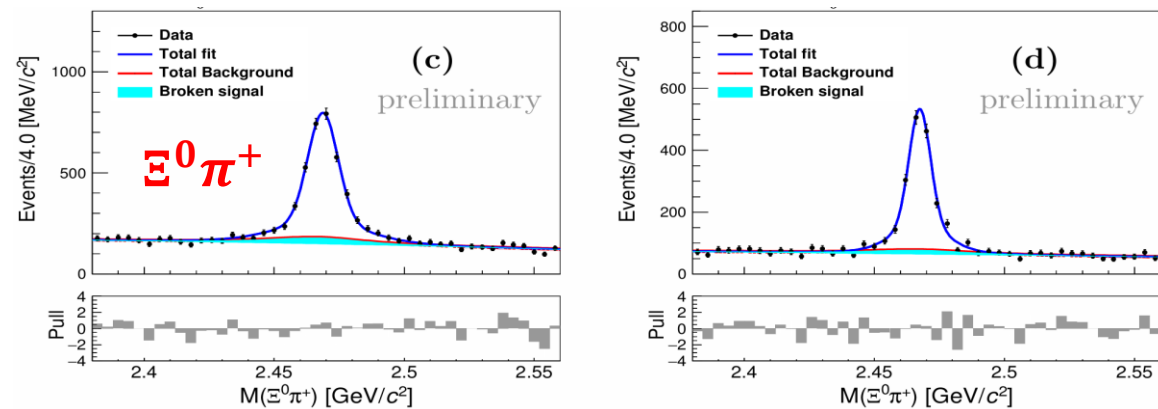
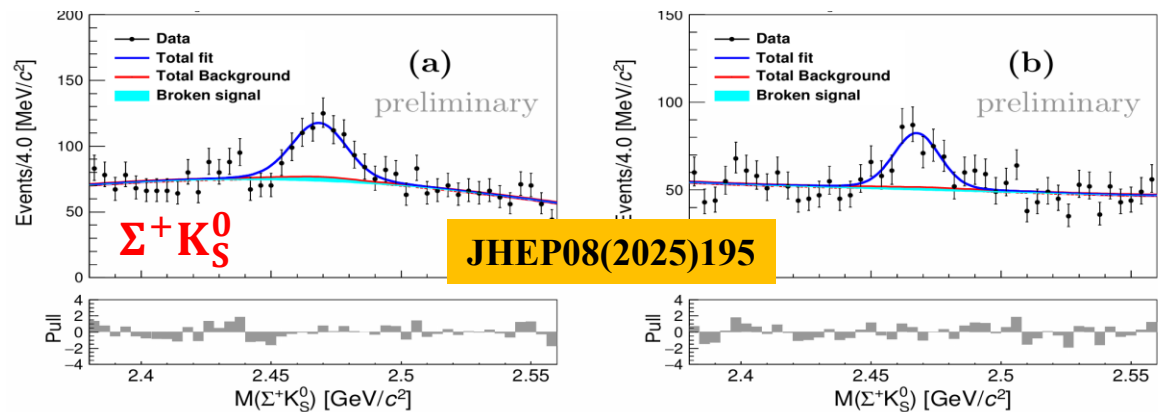
Summary of CPV in charm

Channel	A_{CP}	References
$D^0 \rightarrow \pi^0 \pi^0$	$(+0.3 \pm 0.7 \pm 0.2)\%$	PRD 112, 012006 (2025)
$D^+ \rightarrow \pi^+ \pi^0$	$(-1.8 \pm 0.9 \pm 0.1)\%$	PRD 112, L031101 (2025)
$D^0 \rightarrow \pi^+ \pi^- \pi^0$	$(0.3 \pm 0.3 \pm 0.1)\%$	Preliminary result
$D^0 \rightarrow K_S^0 K_S^0$	$(-0.6 \pm 1.1 \pm 0.1)\%$	PRD 111, 012015 (2025), PRD 112, 012017 (2025)
$D^+, D_s^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$	$(+3.9 \pm 4.5 \pm 1.1)\%, (-0.2 \pm 2.5 \pm 1.1)\%$	JHEP 04 (2025) 036
$\Lambda_c^+ \rightarrow \Lambda K^+, \Sigma^0 K^+$	$(+2.1 \pm 2.6 \pm 0.1)\%, (+2.5 \pm 5.4 \pm 0.4)\%$	Sci. Bull. 68 (2023) 583
$\Lambda_c^+ \rightarrow p K^+ K^-, p \pi^+ \pi^-$	$(+3.9 \pm 1.7 \pm 0.7)\%, (+0.3 \pm 1.0 \pm 0.2)\%$	Preliminary result
$\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-, \Sigma^+ \pi^+ \pi^-$	$(+3.7 \pm 6.6 \pm 0.6)\%, (+9.5 \pm 6.8 \pm 0.5)\%$	Preliminary result

2025 Published and to be published!

Charm baryon decays

$$\Xi_c^+ \rightarrow \Sigma^+ K_S^0, \Xi^0 \pi^+, \Xi^0 K^+, p K_S^0, \Lambda \pi^+, \Sigma^0 \pi^+$$

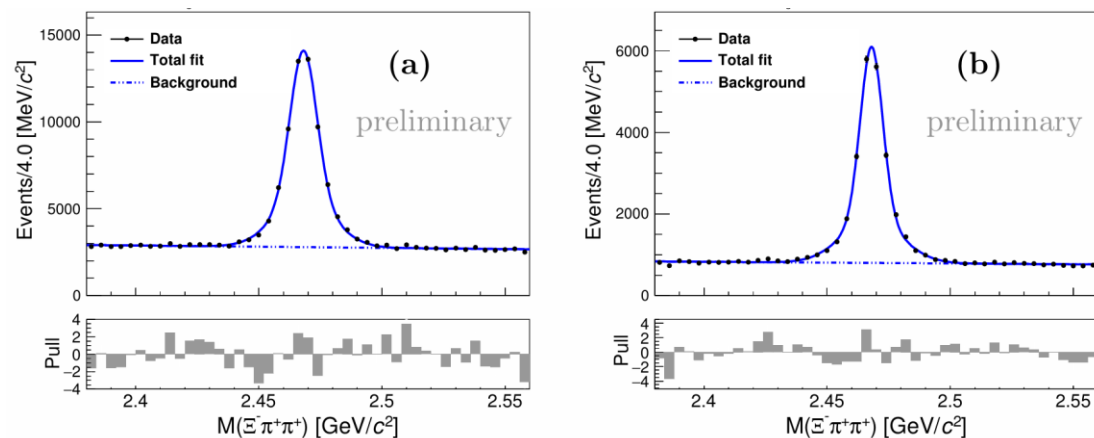


$$\Xi_c^+ \rightarrow \Sigma^+ K_S^0, \Xi^0 \pi^+, \Xi^0 K^+, p K_S^0, \Lambda \pi^+, \Sigma^0 \pi^+$$

Ratio of BF between signal and reference mode:

$$\frac{B_{sig}}{B_{ref}} = \frac{y_{sig} \times B'_{sig}}{y_{ref} \times B'_{ref}}$$

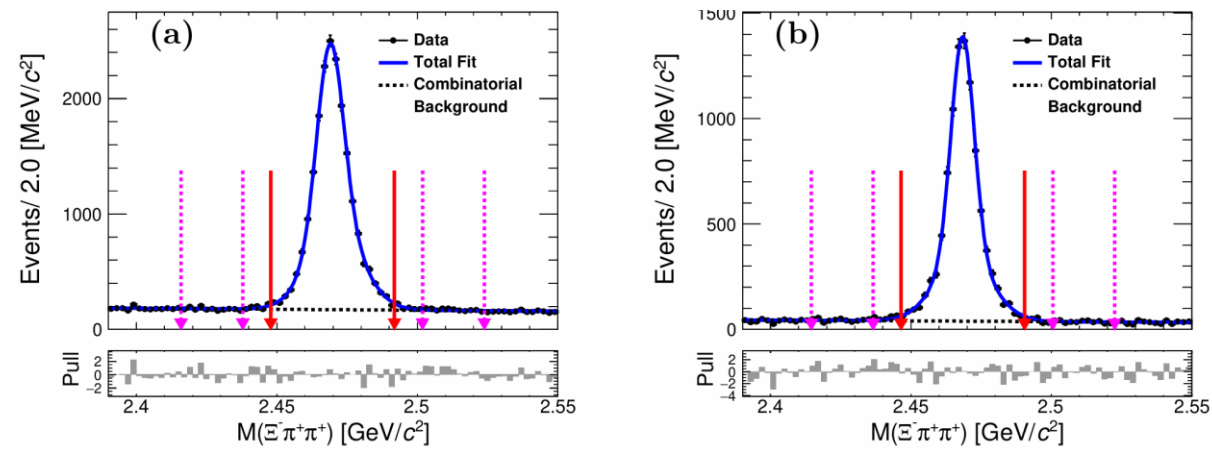
JHEP08(2025)195



$$\begin{aligned} \mathcal{B}(\Xi_c^+ \rightarrow \Sigma^+ K_S^0) &= (0.194 \pm 0.021 \pm 0.009 \pm 0.087)\%, \\ \mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+) &= (0.719 \pm 0.014 \pm 0.024 \pm 0.322)\%, \\ \mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 K^+) &= (0.049 \pm 0.007 \pm 0.002 \pm 0.022)\%, \end{aligned}$$

Improved precision
For the first time

JHEP 03(2025) 061



$$\begin{aligned} \mathcal{B}(\Xi_c^+ \rightarrow p K_S^0) &= (7.16 \pm 0.46 \pm 0.20 \pm 3.21) \times 10^{-4}, \\ \mathcal{B}(\Xi_c^+ \rightarrow \Lambda \pi^+) &= (4.52 \pm 0.41 \pm 0.26 \pm 2.03) \times 10^{-4}, \\ \mathcal{B}(\Xi_c^+ \rightarrow \Sigma^0 \pi^+) &= (1.20 \pm 0.08 \pm 0.07 \pm 0.54) \times 10^{-3}. \end{aligned}$$

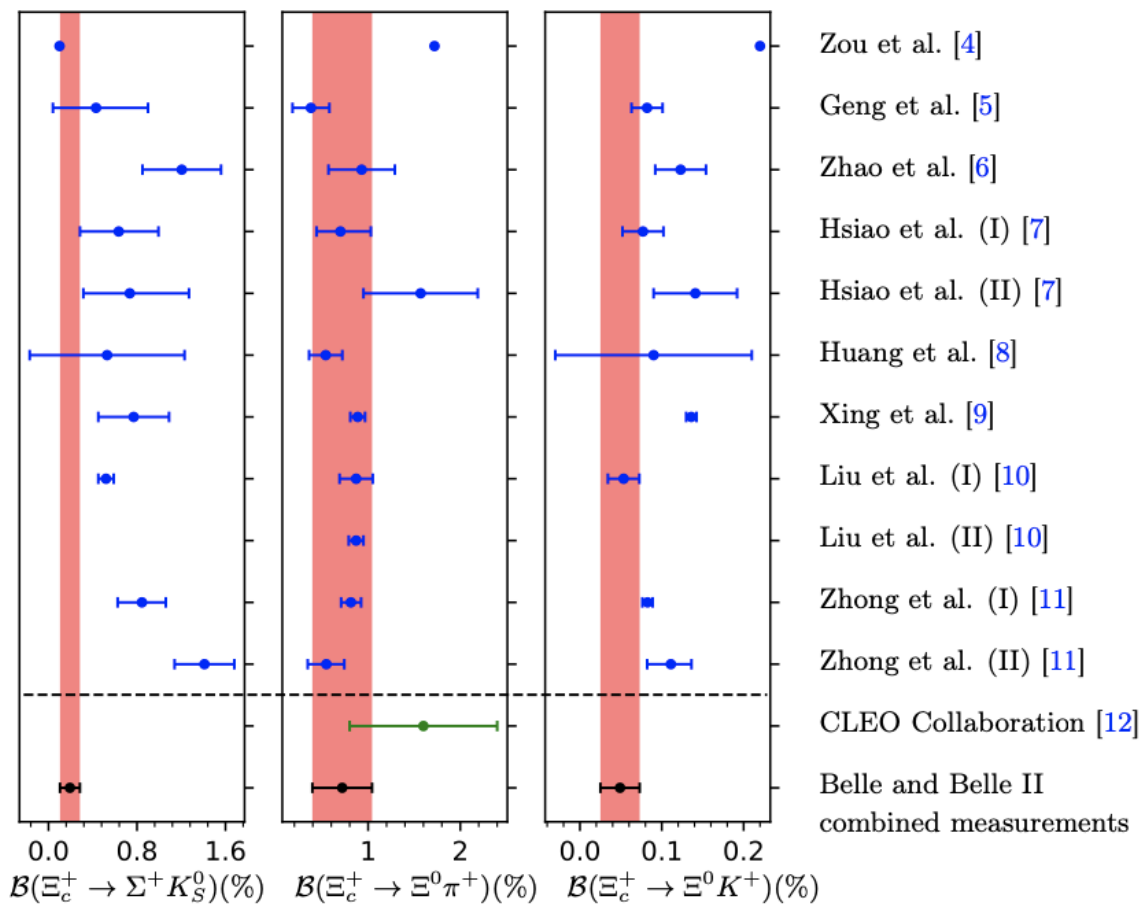
For the first time

$$\Xi_c^+ \rightarrow \Sigma^+ K_S^0, \Xi^0 \pi^+, \Xi^0 K^+, p K_S^0, \Lambda \pi^+, \Sigma^0 \pi^+$$

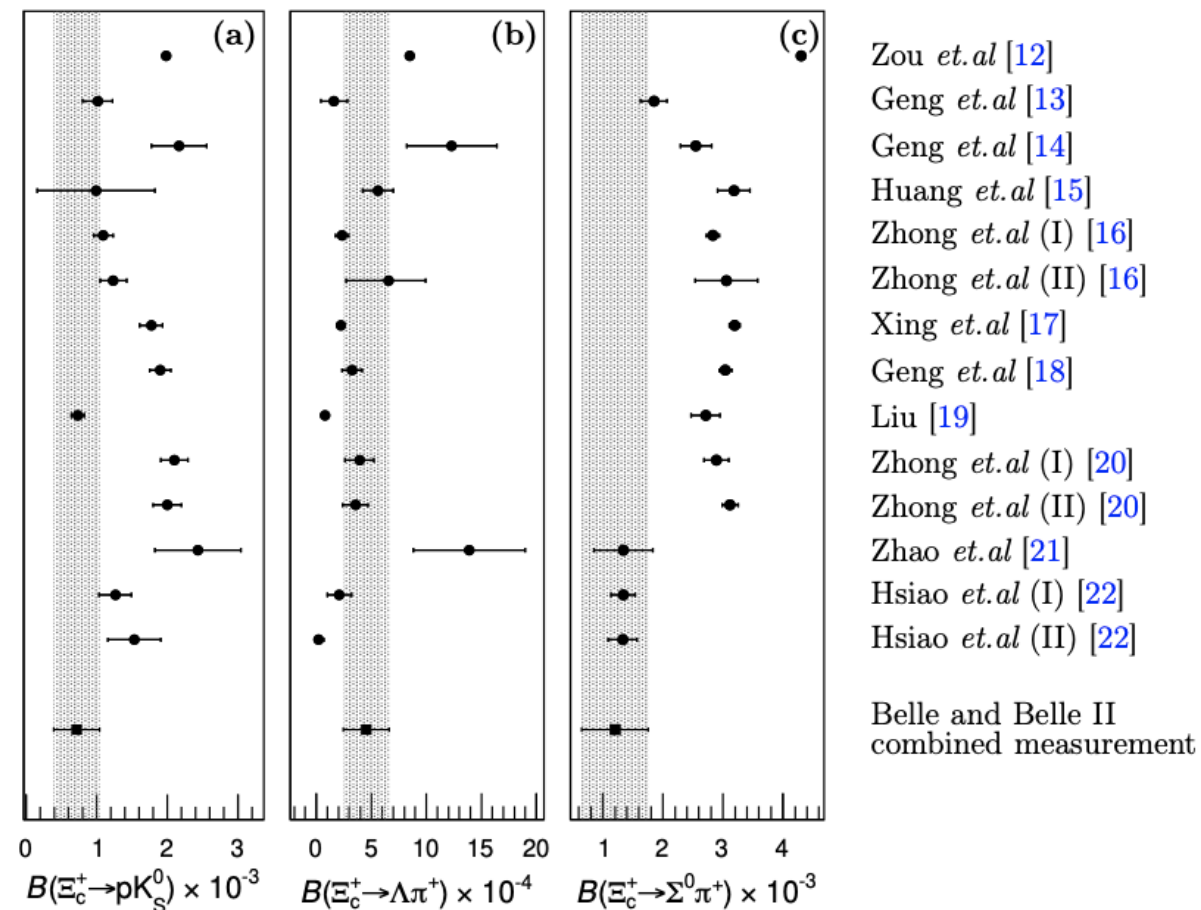
First or most precise measurements!

Consistent with different predictions.

JHEP08(2025)195



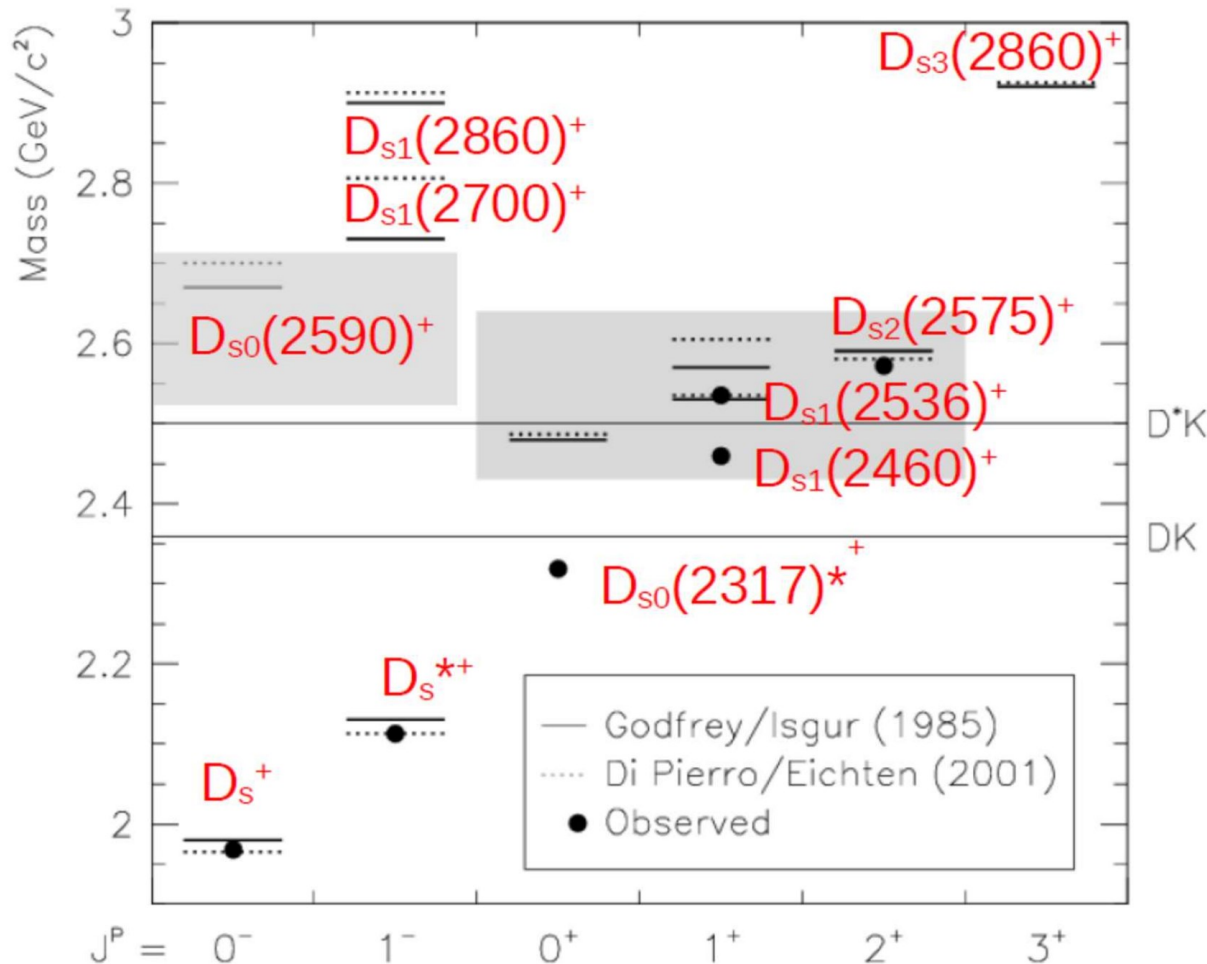
JHEP 03(2025) 061



Spectroscopy

First observation of $D_{s0}^*(2317)^+ \rightarrow D_s^{*+} \gamma$

Preliminary result



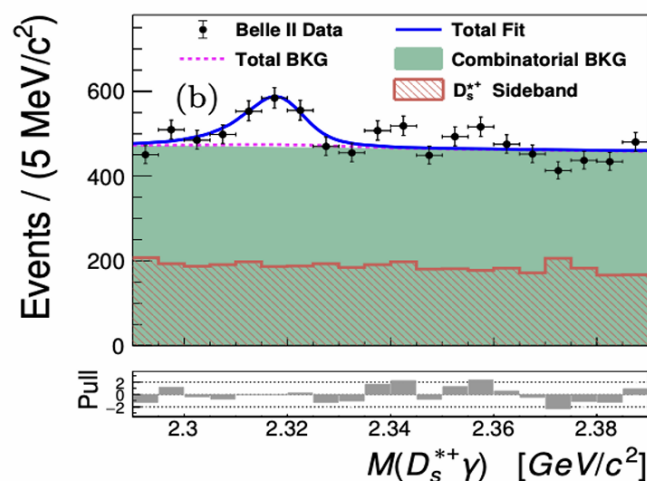
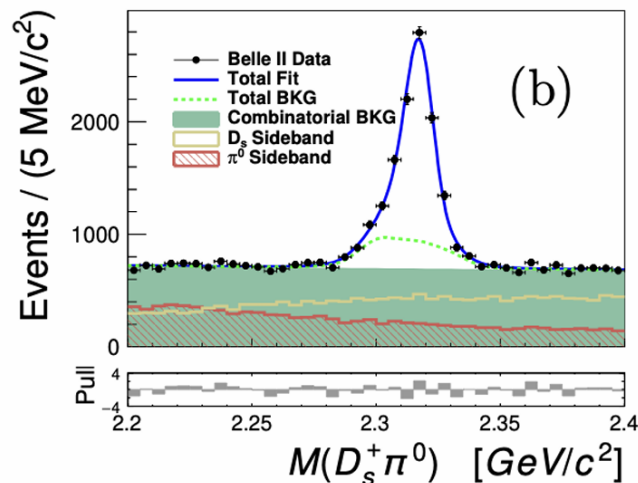
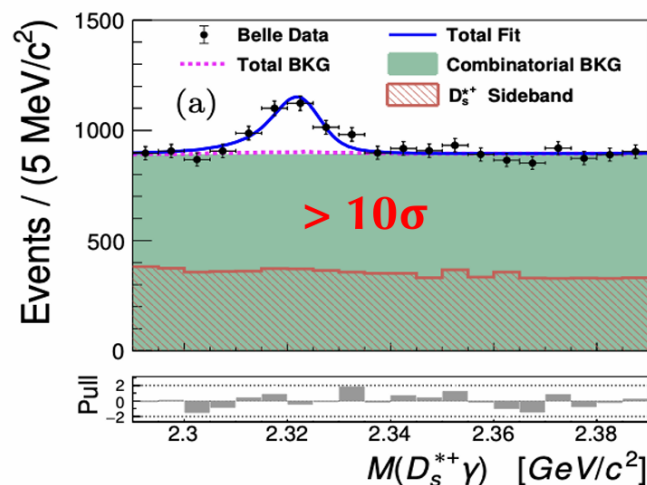
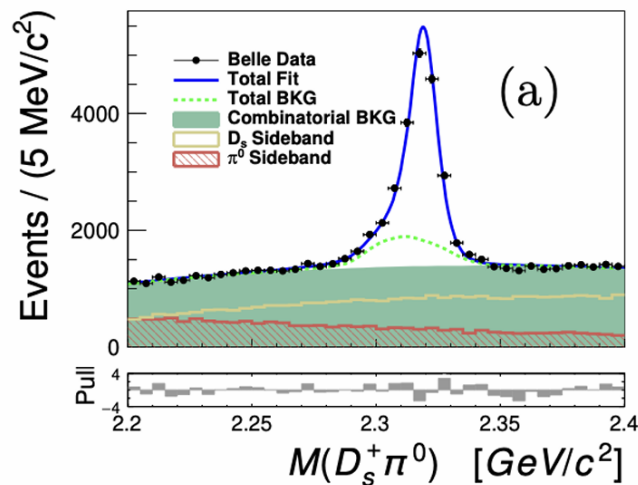
- $D_{s0}^*(2317)$ draws significant attention as its mass is significantly lower than expectation
- Its radiative transition will provide a direct experimental constraint on various theoretical models.

First observation of $D_{s0}^*(2317)^+ \rightarrow D_s^{*+} \gamma$

Preliminary result

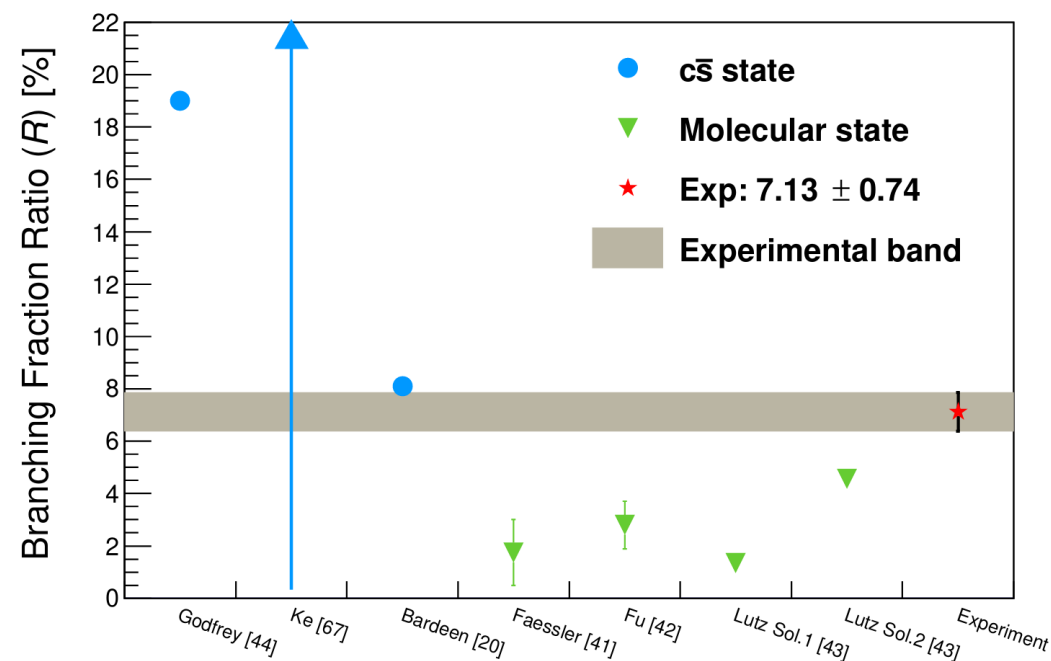
- Target: $D_{s0}^*(2317)^+ \rightarrow D_s^{*+} \gamma$
- Control channel: $D_{s0}^*(2317)^+ \rightarrow D_s^+ \pi^0$ ($\text{Br} = (100_{-20}^{+0})\%$)

Partial decay widths:
unique in discriminating between various models



$$\mathcal{R} = \frac{\mathcal{B}(D_{s0}^*(2317)^+ \rightarrow D_s^{*+} \gamma)}{\mathcal{B}(D_{s0}^*(2317)^+ \rightarrow D_s^+ \pi^0)}$$

$$= [7.14 \pm 0.70(\text{stat.}) \pm 0.23(\text{syst.})]\%$$



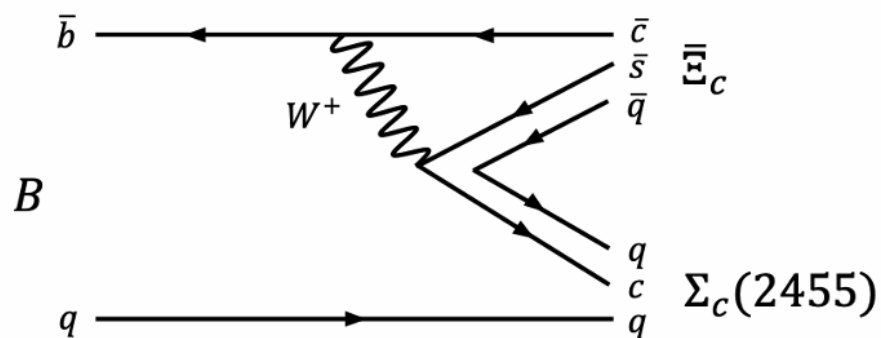
$D_{s0}(2317)^+$ could be the mixture state of pure $c\bar{s}$ state and molecular state.

BF of $B^{+,0} \rightarrow \Sigma_c(2455)^{++,0} \bar{\Sigma}_c^{-,0}$

PRD 112 L051101 (2025)

- BF predicted to be 4×10^{-3} (sum rule) [NPB 345, 137 (1990)] or of the order 10^{-4} (di-quark model) [ZPC 51, 445 (1991)].

These two decays proceed through a purely internal W-emission:



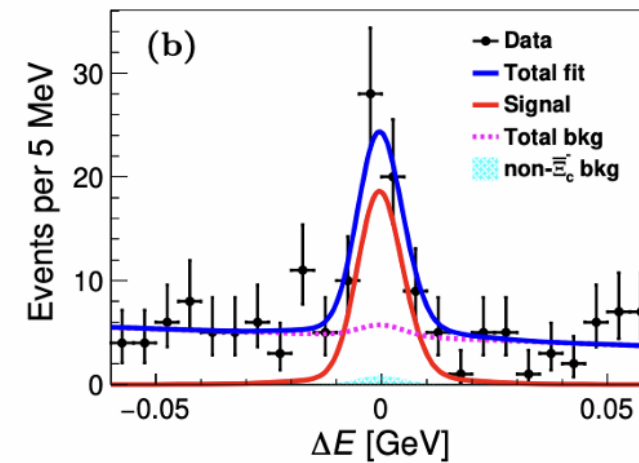
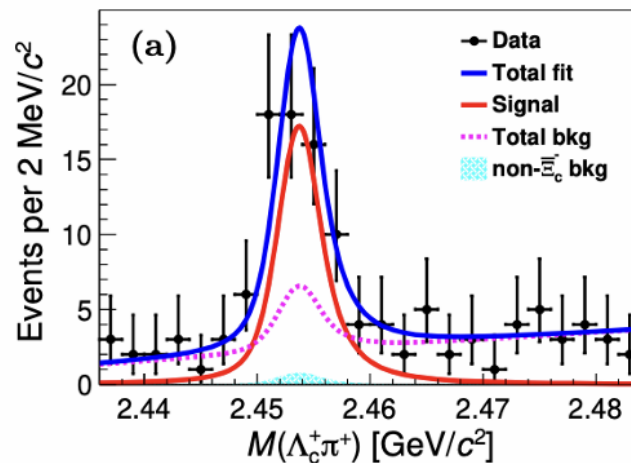
To date, no B decays into charmed baryon pairs containing both a sextet and an antitriplet have been observed.

$$\mathcal{B}(B^+ \rightarrow \Sigma_c^{++} \bar{\Sigma}_c^-) = (5.74 \pm 1.11 \pm 0.42^{+2.47}_{-1.53}) \times 10^{-4}$$

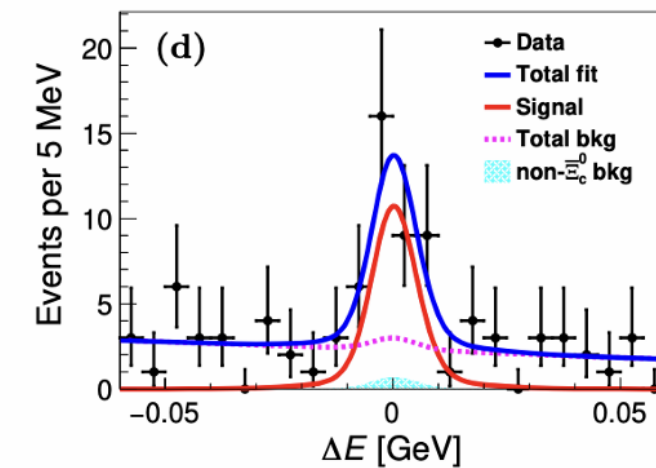
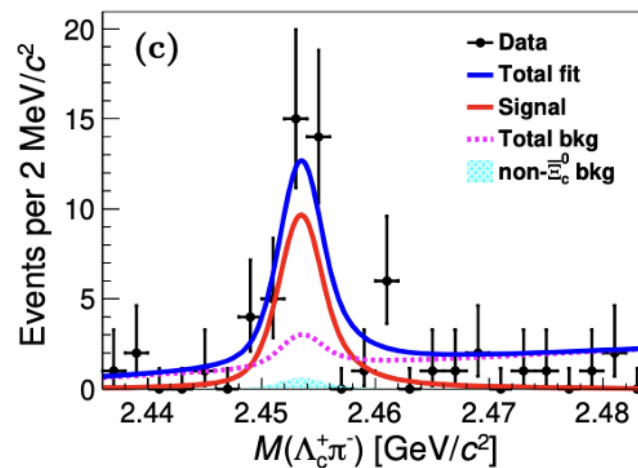
$$\mathcal{B}(B^0 \rightarrow \Sigma_c^0 \bar{\Sigma}_c^0) = (4.83 \pm 1.12 \pm 0.37^{+0.72}_{-0.60}) \times 10^{-4}$$

First observations!

$$B^+ \rightarrow \Sigma_c^{++} \bar{\Sigma}_c^-$$



$$B^0 \rightarrow \Sigma_c^0 \bar{\Sigma}_c^0$$



Summary

- Belle II collected 575 fb^{-1} of data + Belle $1 \text{ ab}^{-1} \approx 1.5 \text{ ab}^{-1}$
- Presented recent measurements of CP asymmetries in charm:
 - Consistent with CP symmetries.
 - Most precise measurement of $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ and $A_{CP}(D^0 \rightarrow \pi^+ \pi^- \pi^0)$
 - First measurement of A_{CP} in SCS three-body charm baryon decays
- Presented BF measurement of charmed baryons and study of the $D_{s0}^*(2317)$
- First observation of B meson decay to a sextet and an antitriplet charmed baryon pair.
- Belle II resumes operations in November. Stay tuned for more results!!

Thanks for your attention!

Backup

Comparison of available charm samples

Experiment	Machine	C.M.	Luminosity	N_{prod}	Efficiency	Characters
	BEPC-II (e^+e^-)	3.77 GeV 4.18-4.23 GeV 4.6-4.7 GeV	2.9 (8 $\rightarrow$ 20) fb^{-1} 7.3 fb^{-1} 4.5 fb^{-1}	$D^{0,+}$: $10^7 (\rightarrow 10^8)$ D_s^+ : 5×10^6 Λ_c^+ : 0.8×10^6 ★☆☆	★★★★	☺ extremely clean environment ☺ quantum coherence ☹ no boost, no time-dept analysis
	SuperKEKB (e^+e^-)	10.58 GeV	0.4 ($\rightarrow$ 50) ab^{-1}	D^0 : $6 \times 10^8 (\rightarrow 10^{11})$ $D_{(s)}^+$: $10^8 (\rightarrow 10^{10})$ Λ_c^+ : $10^7 (\rightarrow 10^9)$		☺ high-efficiency detection of neutrals ☺ good trigger efficiency ☺ time-dependent analysis
	KEKB (e^+e^-)	10.58 GeV	1 ab^{-1}	$D^{0,+}, D_s^+$: 10^9 Λ_c^+ : 10^8 ★★★☆☆	$\mathcal{O}(1-10\%)$ ★★	☹ smaller cross-section than LHCb
	LHC (pp)	7+8 TeV 13 TeV	1+2 fb^{-1} 6 fb^{-1} ($\rightarrow$ 23 $\rightarrow$ 50) fb^{-1}	5×10^{12} 10^{13} ★★★★★	★	☺ very large production cross-section ☺ large boost, excellent time resolution ☹ dedicated trigger required

Here uses $\sigma(D^0\bar{D}^0@3.77\text{ GeV})=3.61\text{ nb}$, $\sigma(D^+D^-@3.77\text{ GeV})=2.88\text{ nb}$, $\sigma(D_s^*D_s@4.17\text{ GeV})=0.967\text{ nb}$; $\sigma(c\bar{c}@10.58\text{ GeV})=1.3\text{ nb}$ where each $c\bar{c}$ event averagely has 1.1/0.6/0.3 $D^0/D^+/D_s^+$ yields; $\sigma(D^0@CDF)=13.3\text{ }\mu\text{b}$, and $\sigma(D^0@LHCb)=1661\text{ }\mu\text{b}$, mainly from *Int. J. Mod. Phys. A* **29**(2014)24,14300518.

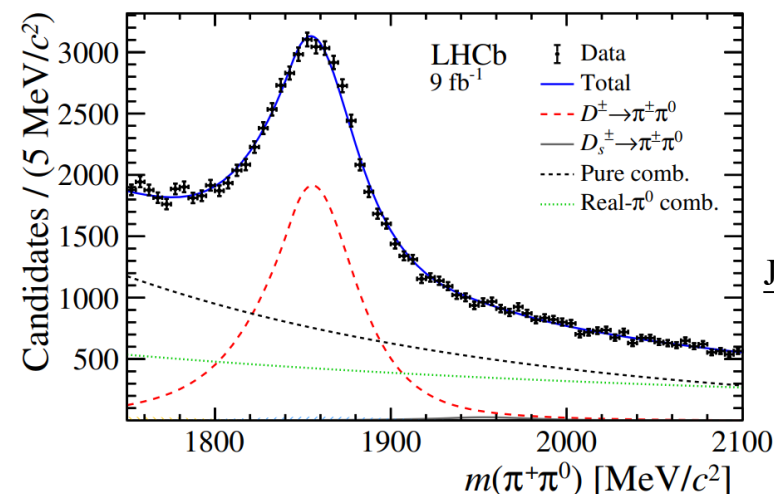
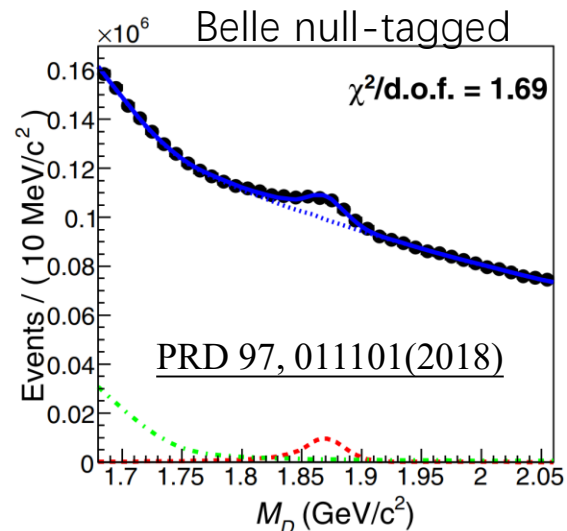
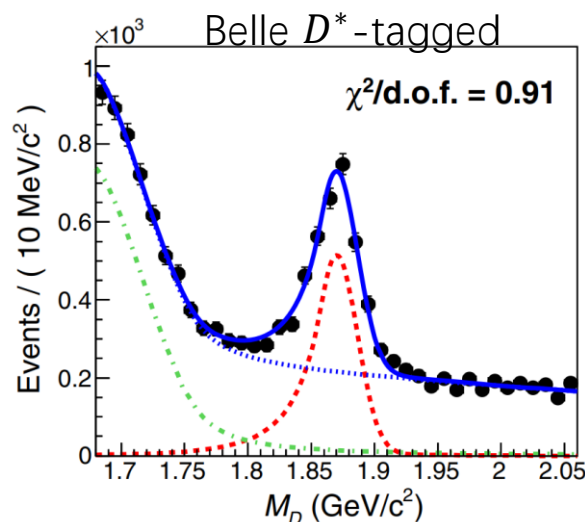
- BESIII, Belle II, and LHCb experiments have their advantages for charm studies.
- They all are continuously collecting more datasets with increased luminosity in the foreseeable future.

- A 3.8σ CPV in the pionic mode $D^0 \rightarrow \pi^+ \pi^-$.
 - Unclear if observed CP violation can be described by the SM or not, due to large hadronic uncertainties
PRL 131, 051802 (2023) PRD 108, 036026 (2023) PRD 109, 033011 (2024)
- Isospin-related modes $D^+ \rightarrow \pi^+ \pi^0$ can reduce hadronic uncertainty.
- In addition, $D^+ \rightarrow \pi^+ \pi^0$ ($I = 2$) is expected to **have no CPV in SM**
 - since it does not receive QCD penguin ($\Delta I = 1/2$) contribution and has suppressed electroweak penguin contribution.

History of $A_{cp}(D^+ \rightarrow \pi^+ \pi^0)$:

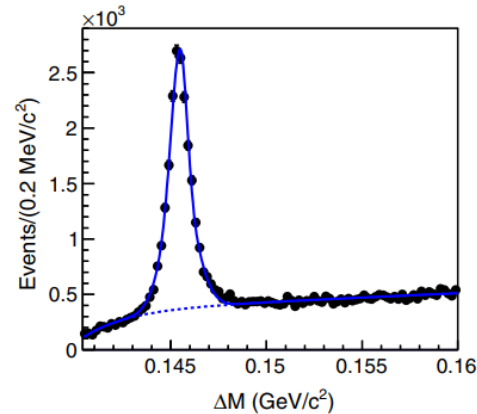
Belle: $A_{cp}(D^+ \rightarrow \pi^+ \pi^0) = (2.31 \pm 1.24 \pm 0.23)\%$

LHCb: $A_{cp}(D^+ \rightarrow \pi^+ \pi^0) = (-1.3 \pm 0.9 \pm 0.6)\%$



JHEP 06, 019 (2021)

- Belle reported $A_{CP}(D^0 \rightarrow \pi^0 \pi^0) = (-0.03 \pm 0.64 \pm 0.10)\%$ using 980 fb^{-1} datasets.

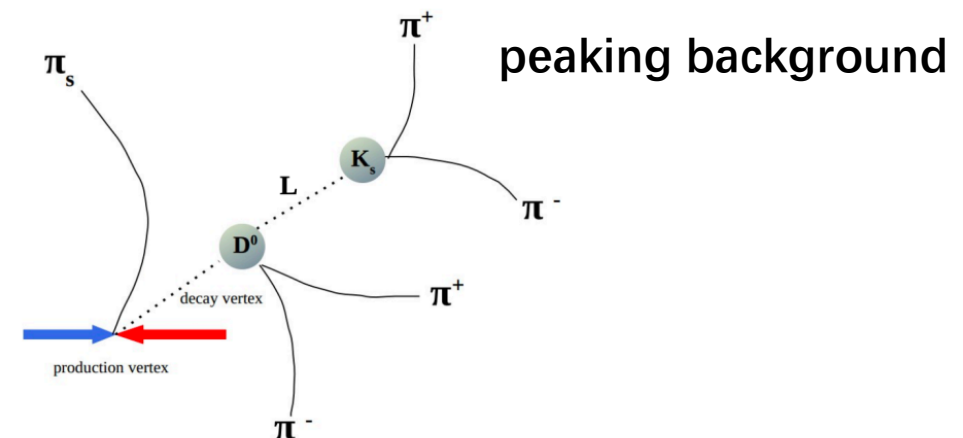
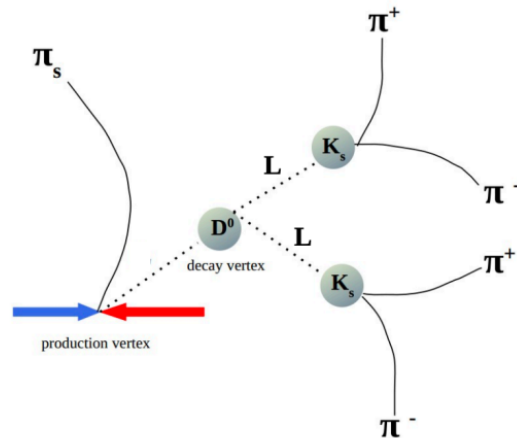


PRL 112, 211601 (2014)

- Signal mode: $A_{raw}^{\pi^0 \pi^0} = A_{CP}^{\pi^0 \pi^0} + A_{prod}^{D^*} + A_{\epsilon}^{\pi_s}$; control modes: D^* -tagged $D^0 \rightarrow K^- \pi^+$, untagged $D^0 \rightarrow K^- \pi^+$.
 - $A_{raw}^{K\pi, tag} = A_{prod}^{D^*}(D^0 \rightarrow K^- \pi^+) + A_{\epsilon}^{\pi_s}(D^0 \rightarrow K^- \pi^+) + A_{\epsilon}^{K\pi}(D^0 \rightarrow K^- \pi^+)$
 - $A_{raw}^{K\pi, untag} = A_{prod}^{D^0}(D^0 \rightarrow K^- \pi^+) + A_{\epsilon}^{K\pi}(D^0 \rightarrow K^- \pi^+)$
- ➔
- Using $A'_{raw} = \frac{A_{raw}(\cos\theta_{CM} < 0) + A_{raw}(\cos\theta_{CM} > 0)}{2}$, the **Production Asymmetry** is averaged out.
(odd function of $\cos\theta_{CM}$)
 - $A_{CP}(D^0 \rightarrow \pi^0 \pi^0) = A'_{raw}^{\pi^0 \pi^0} - (A'_{raw}^{K\pi, tag} - A'_{raw}^{K\pi, untag})$

$A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ using D^* -tagged sample

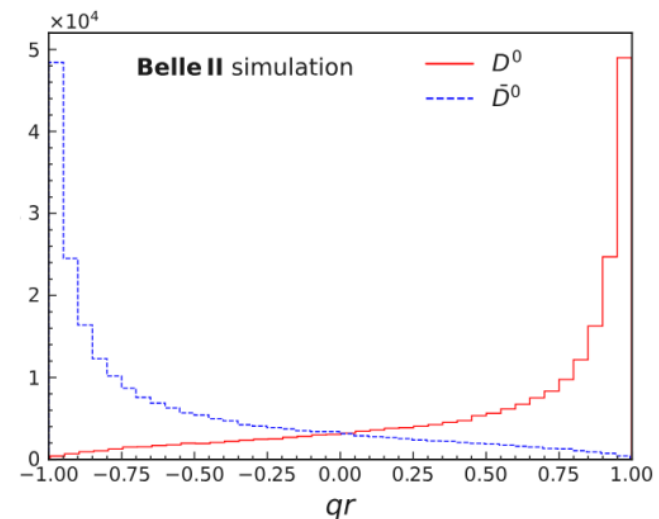
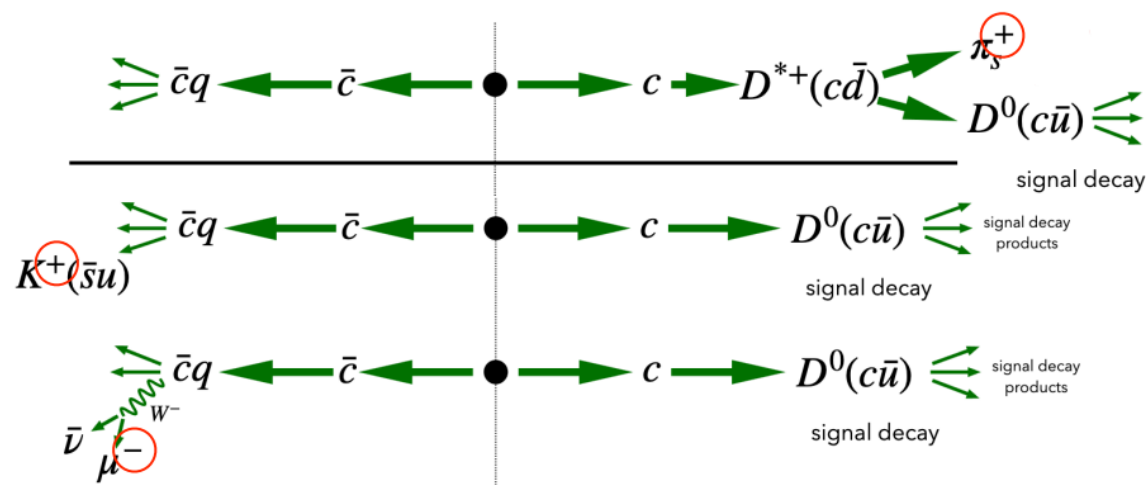
- Measure $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ based on $D^{*+} \rightarrow D^0 \pi^+$ sample at Belle + Belle II (1.4 /ab).
- $A_{CP}^{K_S^0 K_S^0} = (A_{raw}^{K_S^0 K_S^0} - A_{raw}^{K^+ K^-}) + A_{CP}^{K^+ K^-}$ assuming nuisance asymmetries are made identical by kinematics weighting.
- Main background from same-final-state $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ decays. Separate with K_S^0 flight distance significance L/σ : $S_{min}(K_S^0) = \log[\min(L1/\sigma1, L2/\sigma2)]$.



$A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ using opposite side charm-flavor tagger

PRD 107, 112010 (2023)

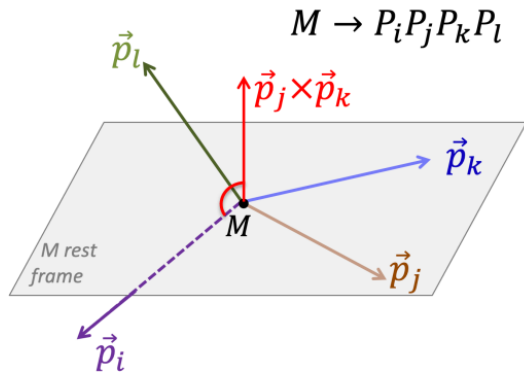
- Charm flavor tagger: novel method to tag flavor of D^0 meson from other collision products ($K^\pm/\mu^\pm$ from other charm hadron) $\rightarrow$ new CFT-tag independent sample.
- $q = \pm 1$, the predicted flavor
- ω , per-event wrong-tag probability
- Define dilution $r = 1-2\omega$. Use product qr to measure A_{CP} .
- Calibrate r value using self-tagged decays ($D^0 \rightarrow K^- \pi^+$) in data.
- Use Belle + Belle II data sets (1.4 /ab), **excluding D^* -tagged sample**.
- Larger background wrt D^* -tag: train BDT with kinematic information.
- Cut on BDT output and $S_{\min}$ reduce $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ significantly.



Search for CPV in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$

JHEP 04 (2025) 036

- $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$ has a dominant intermediate process: $D_{(s)}^+ \rightarrow \bar{K}^{*0} K^{*+}$ (tree, annihilation, penguin.)
These amplitudes interfere with one another, potentially giving rise to CPV
- Unlike time-integrated CPV, which is proportional to $\sin\delta \cdot \sin\phi$, CPV via kinematic observables (e.g. triple-product) is proportional to $\cos\delta \cdot \sin\phi$. (δ strong phase difference, ϕ weak phase difference)



$$X = C_{TP} \equiv (\vec{p}_j \times \vec{p}_k) \cdot \vec{p}_i$$

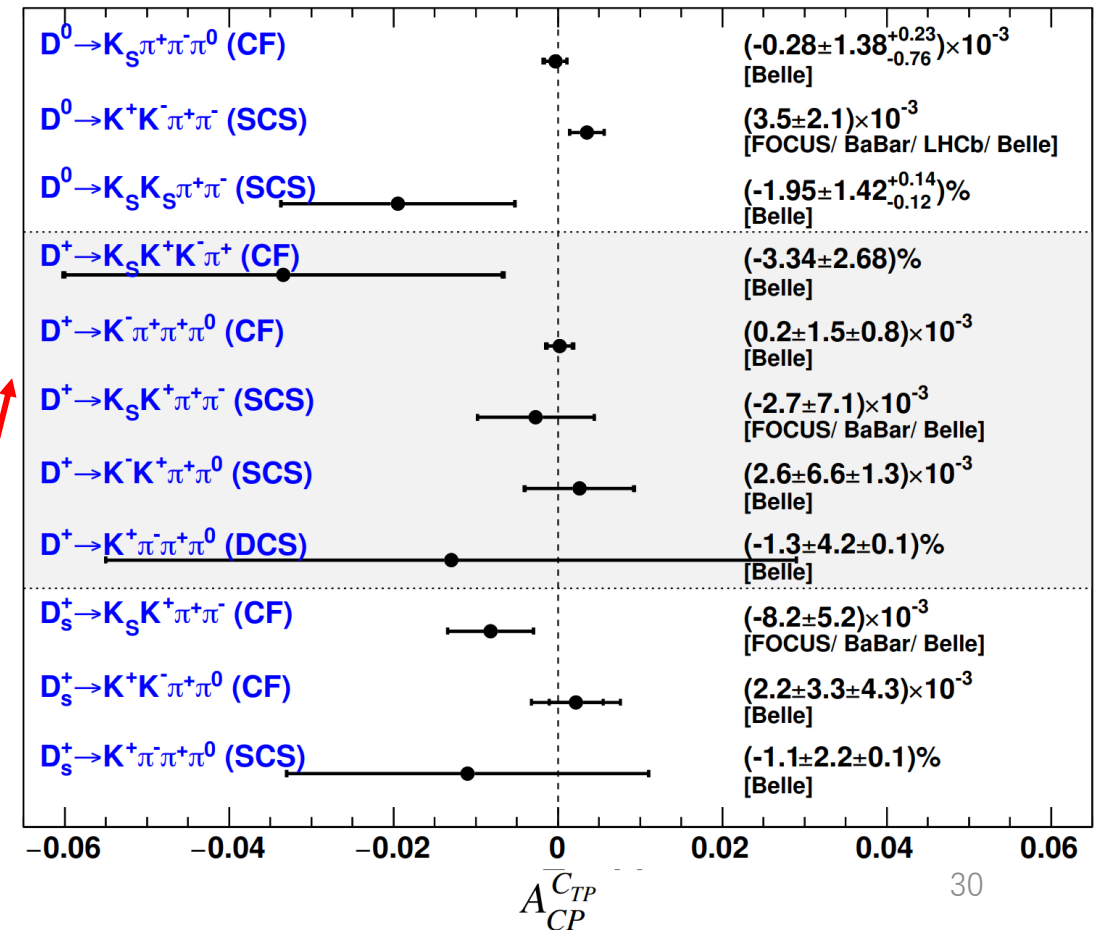
$$A_X(D_{(s)}^+) = \frac{N_+(X > 0) - N_+(X < 0)}{N_+(X > 0) + N_+(X < 0)}; A_{\bar{X}}(D_{(s)}^-) = \frac{N_-(\bar{X} > 0) - N_-(\bar{X} < 0)}{N_-(\bar{X} > 0) + N_-(\bar{X} < 0)}$$

• N is obtained from fit.

$\bar{X}$ is CP-conjugate of X

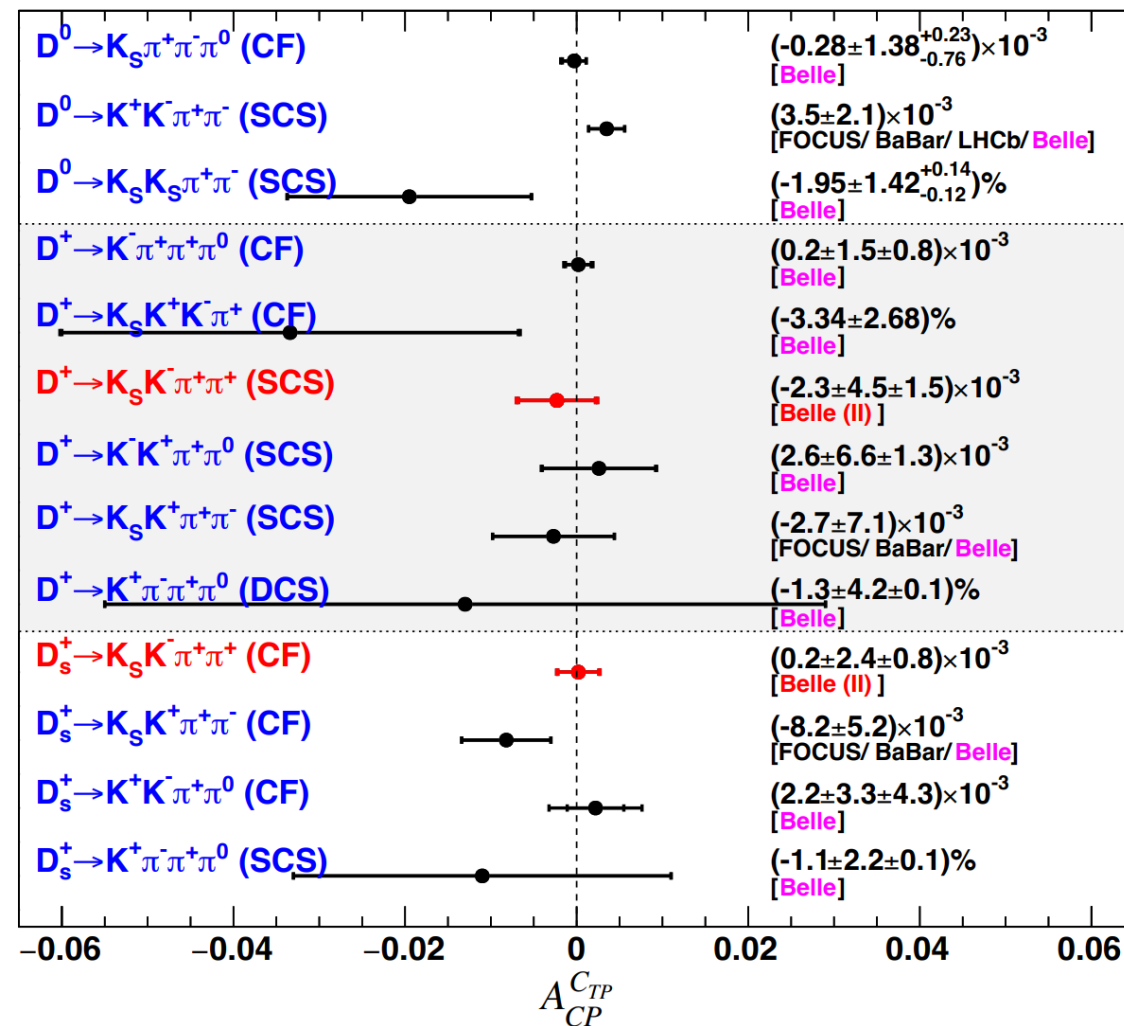
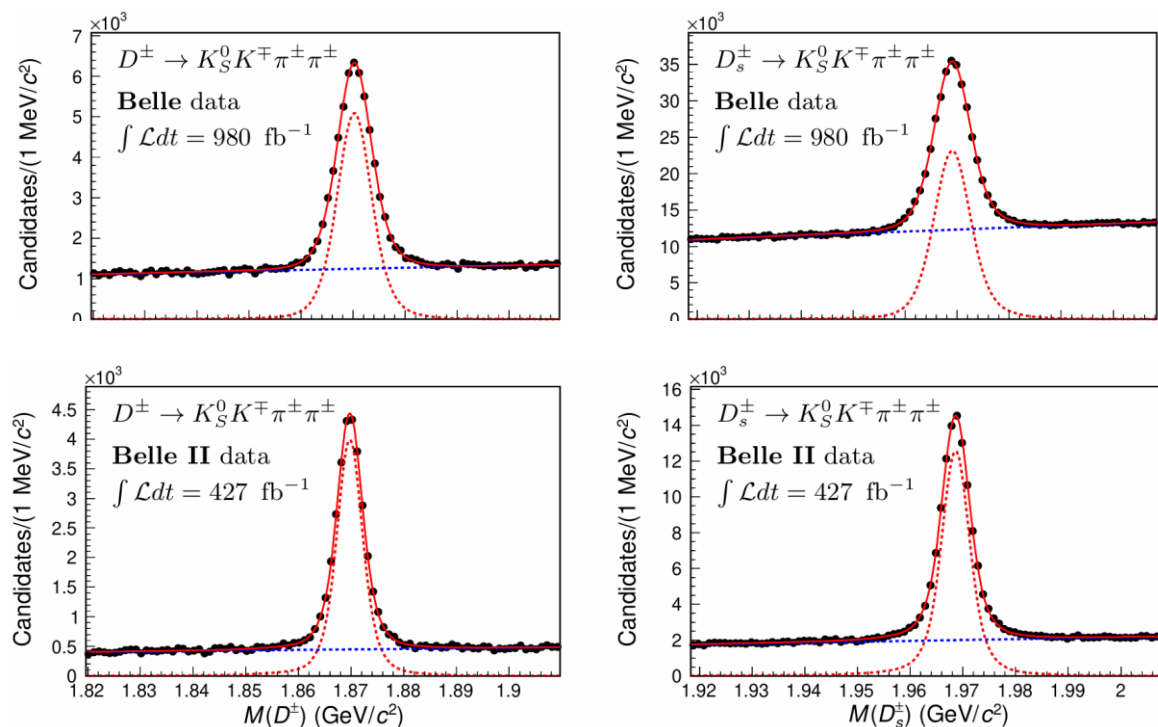
$$A_{CP}^X = \frac{1}{2}(A_X(D_{(s)}^+) - A_{\bar{X}}(D_{(s)}^-))$$

- A couple of 4-body decays searched using this technique.
- First time on $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$, whose $\mathcal{B} = 0.23\%$ (1.53%).



Search for CPV in $D_{(s)}^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$

JHEP 04 (2025) 036



$$A_{cp}^{CP}(D^+) = (-2.3 \pm 4.5 \pm 1.5) \times 10^{-3}$$

$$A_{cp}^{CP}(D_s^+) = (0.2 \pm 2.4 \pm 0.8) \times 10^{-3}$$

No evidence for CPV found!

CP asymmetry in $\Xi_c^+ \rightarrow \Sigma^+ h^+ h^-$ and $\Lambda_c^+ \rightarrow p h^+ h^-$

Preliminary result

- There is a U-spin sum rule equivalent to the one that connects $D^0 \rightarrow KK, \pi\pi$, links the SCS decays $\Xi_c^+ \rightarrow \Sigma^+ h^+ h^-$ and $\Lambda_c^+ \rightarrow p h^+ h^-$ ($h = K, \pi$) [PRD 99,032005(2019)]:

$$\begin{aligned} A_{CP}^{dir}(\Lambda_c^+ \rightarrow p K^+ K^-) + A_{CP}^{dir}(\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-) &= 0 \\ A_{CP}^{dir}(\Lambda_c^+ \rightarrow p \pi^+ \pi^-) + A_{CP}^{dir}(\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-) &= 0 \end{aligned}$$

- Assuming U-spin symmetry:

$$\begin{aligned} A_{CP}(\Lambda_c^+ \rightarrow p K^+ K^-) + A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-) &= 0 \\ A_{CP}(\Lambda_c^+ \rightarrow p \pi^+ \pi^-) + A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-) &= 0 \end{aligned}$$

- Measurement by LHCb [JHEP03(2018)182]:

$$\Delta A_{CP}^{wgt} = A_{CP}(p K^- K^+) - A_{CP}^{wgt}(p \pi^- \pi^+) = (0.30 \pm 0.91 \pm 0.61)$$