

# DESI Dark Energy and Hubble tension

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暗物质暗能量研究现状发展趋势及对策专题研讨会  
2025-06-25 10:10-10:45

# References

{ 2505.22369 Jia-Le Ling, Guo-Hong Du, Tian-Nuo Li, Jing-Fei Zhang, Shao-Jiang Wang, Xin Zhang  
Model-independent cosmological inference after the DESI DR2 data with improved inverse distance ladder

This talk is mainly based on 2502.04212 Lu Huang (黃路), Rong-Gen Cai, Shao-Jiang Wang  
The DESI DR1/DR2 evidence for dynamical dark energy is biased by low-redshift supernovae

2410.06053 Lu Huang, Rong-Gen Cai, Shao-Jiang Wang, Jian-Qi Liu, Yan-Hong Yao  
Narrowing down the Hubble tension to the first two rungs of distance ladders  
Sci.China Phys.Mech.Astron. 68 (2025) 8, 280405

2401.14170 Lu Huang, Shao-Jiang Wang, Wang-Wei Yu  
No-go guide for the Hubble tension: Late-time or local-scale new physics  
Sci.China Phys.Mech.Astron. 68 (2025) 2, 220413

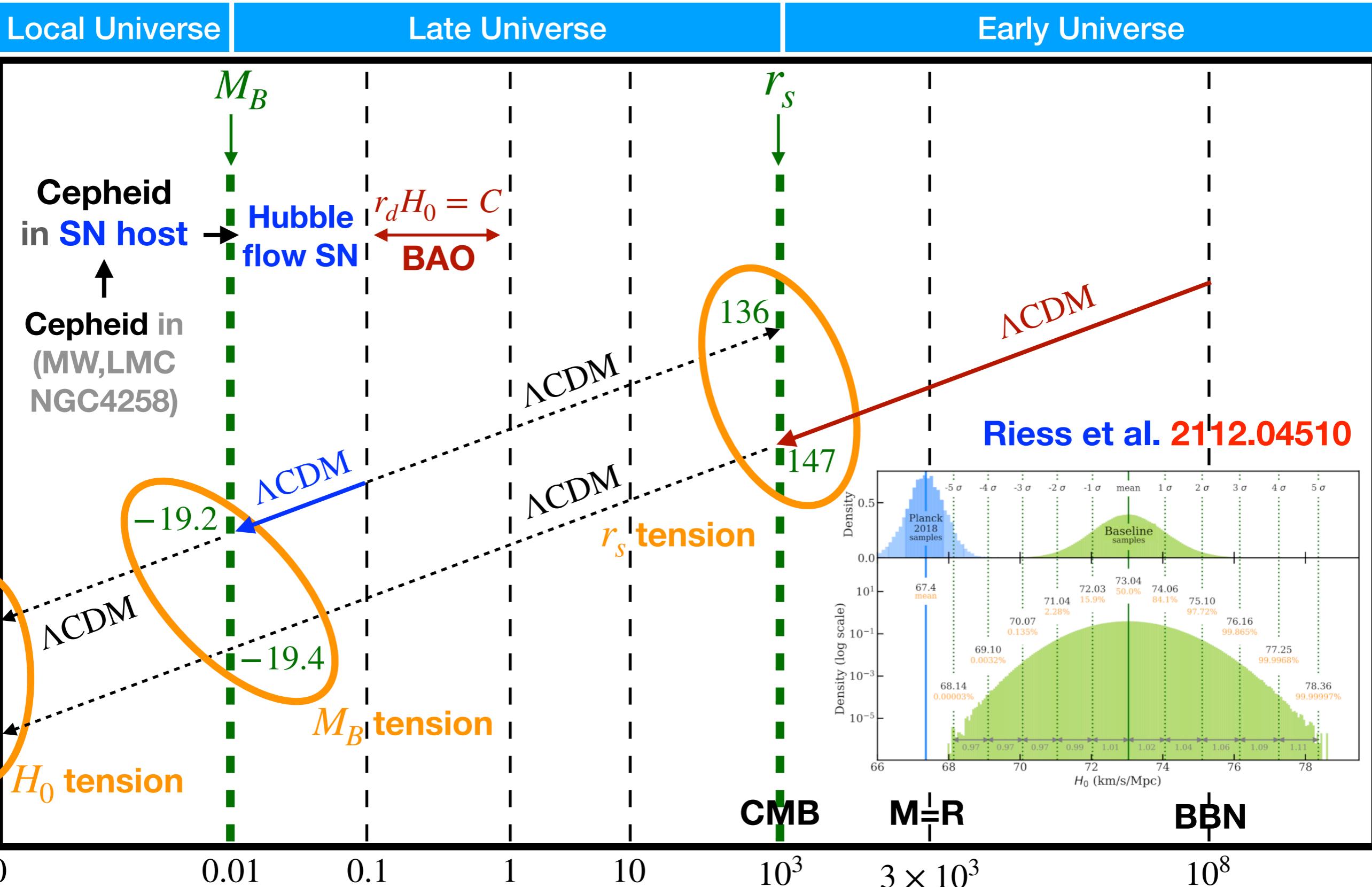
2202.12214 Rong-Gen Cai, Zong-Kuan Guo, Shao-Jiang Wang, Wang-Wei Yu, Yong Zhou  
No-go guide for late-time solutions to the Hubble tension: Matter perturbations  
Phys.Rev.D 106 (2022) 6, 063519

2107.13286 Rong-Gen Cai, Zong-Kuan Guo, Shao-Jiang Wang, Wang-Wei Yu, Yong Zhou  
No-go guide for the Hubble tension: Late-time solutions  
Phys.Rev.D 105 (2022) 2, L021301

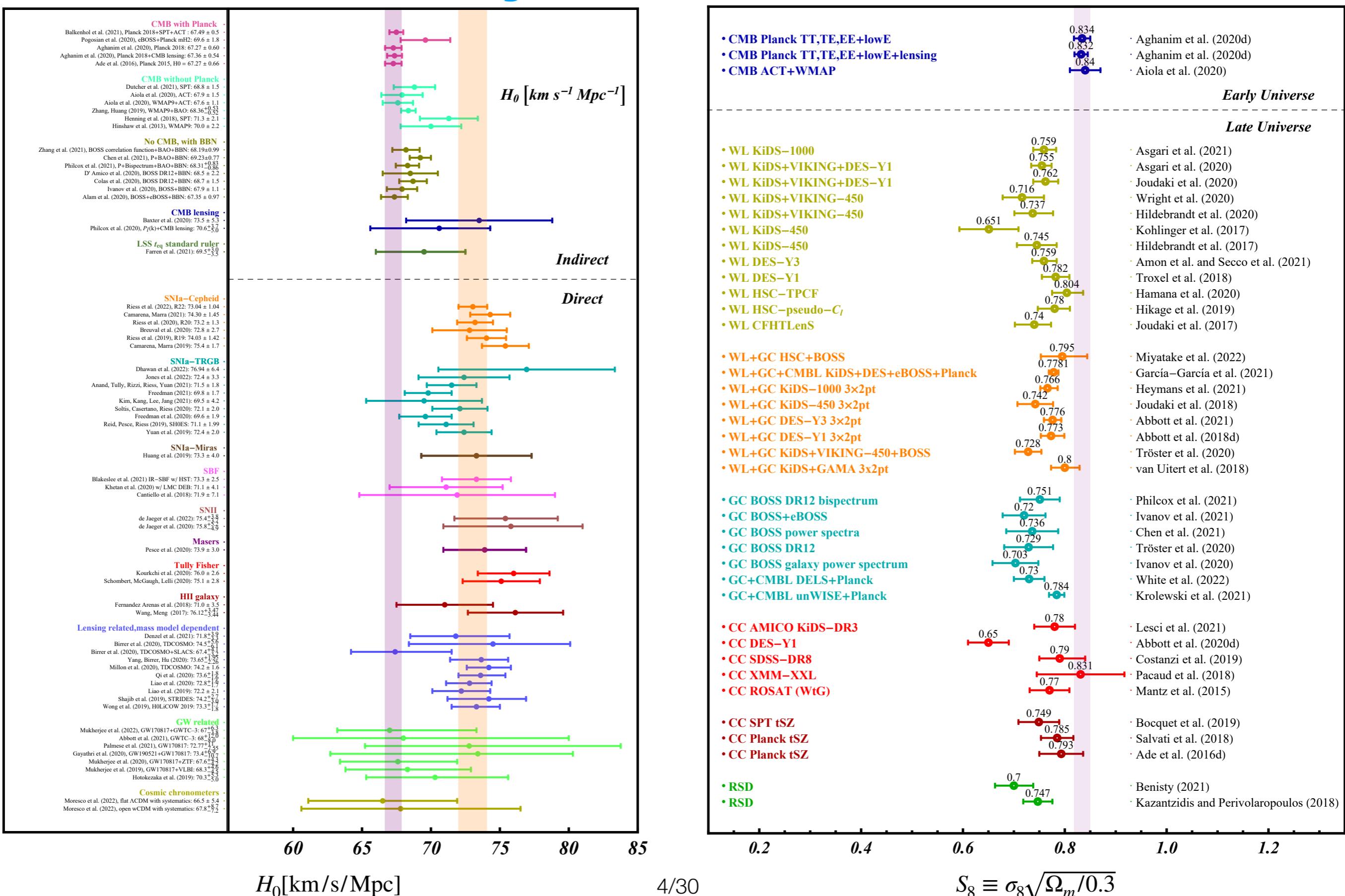
2102.02020 Rong-Gen Cai, Zong-Kuan Guo, Li Li, Shao-Jiang Wang, Wang-Wei Yu  
Chameleon dark energy can resolve the Hubble tension  
Phys.Rev.D 103 (2021) L121302

& 2209.14732 Wang-Wei Yu, Li Li, Shao-Jiang Wang First detection of the Hubble variation correlation and its scale dependence

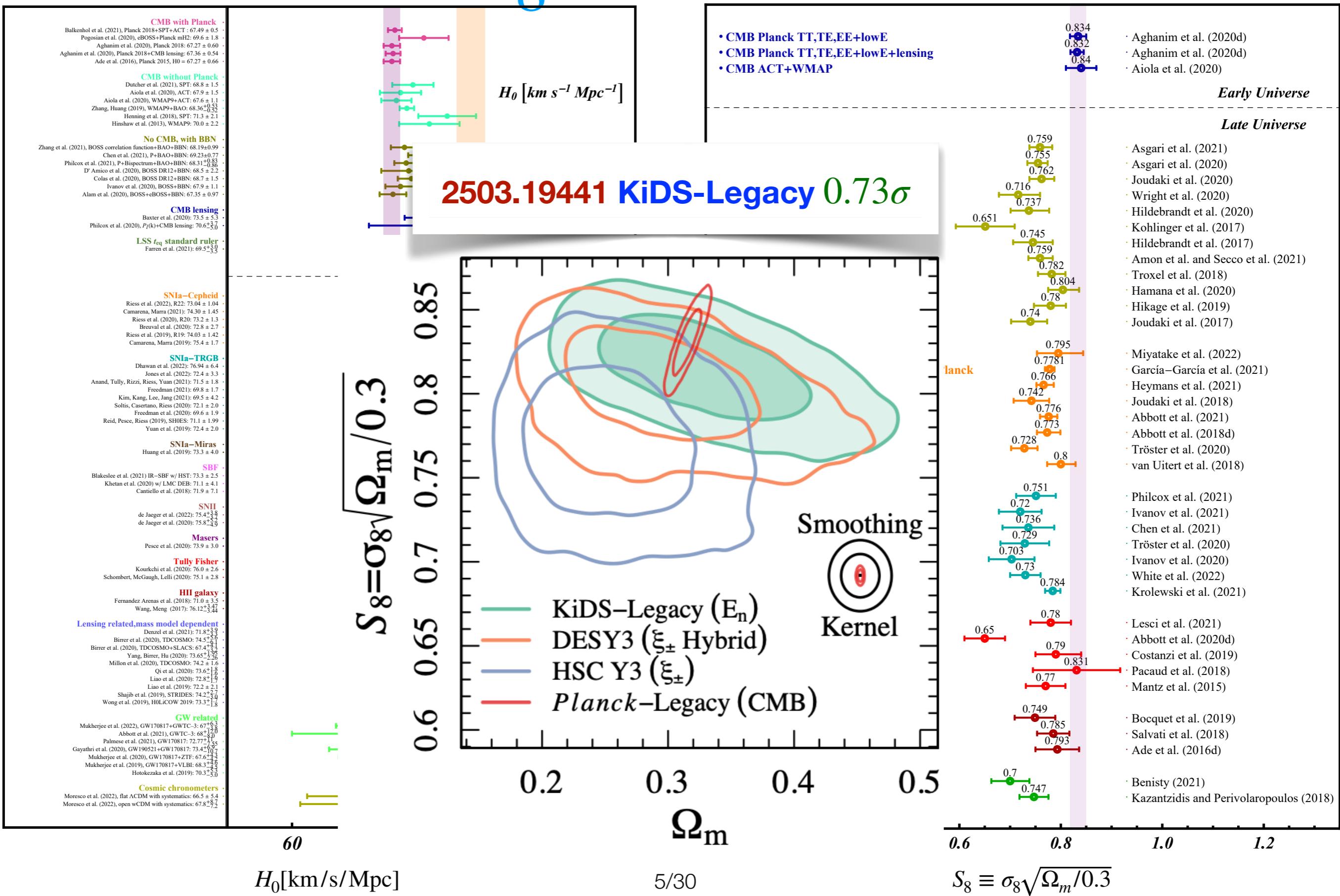
# $H_0$ tension



# Early-late tension



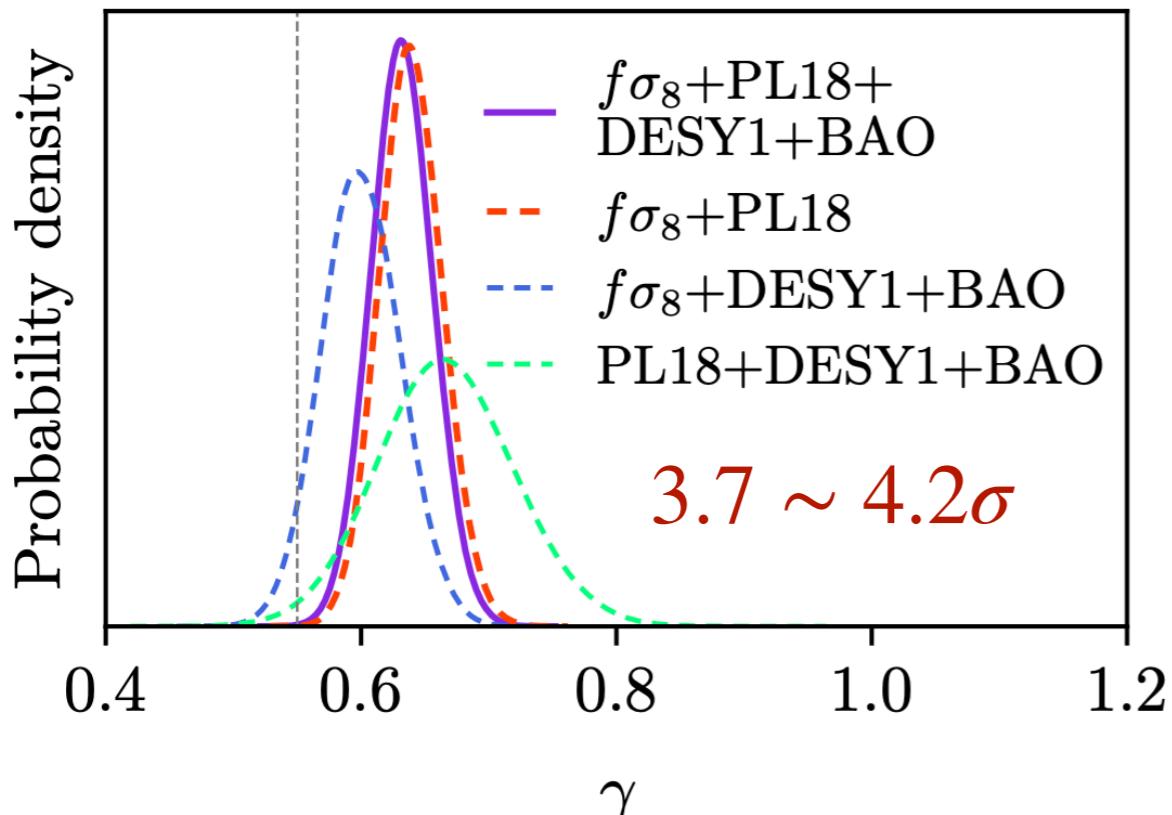
# $S_8$ tension?



# $\gamma$ tension!

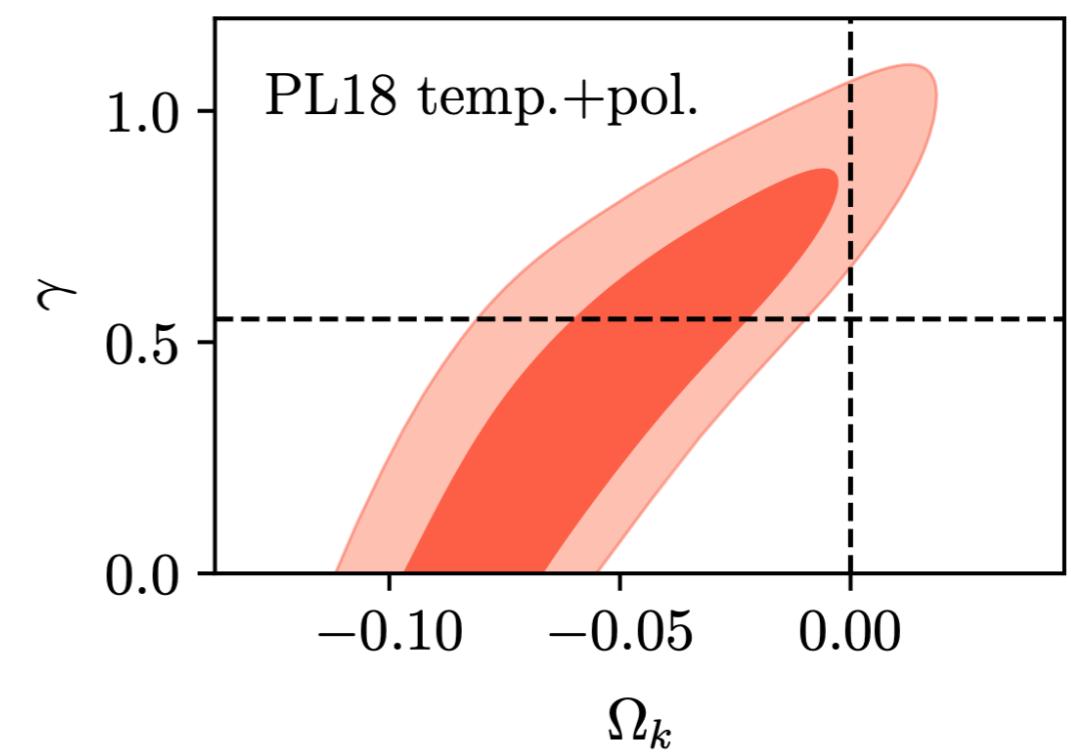
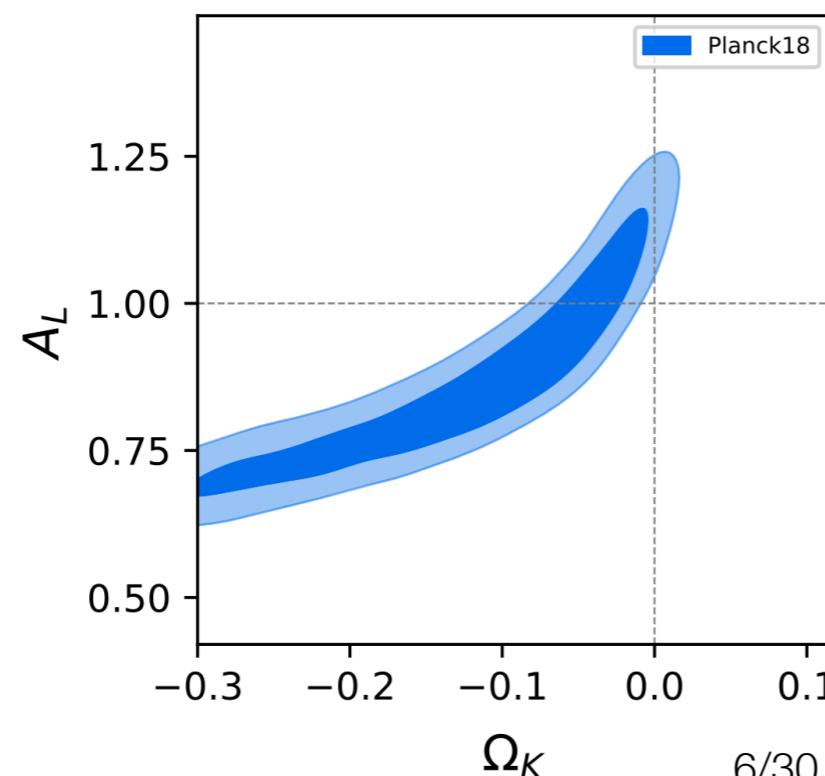
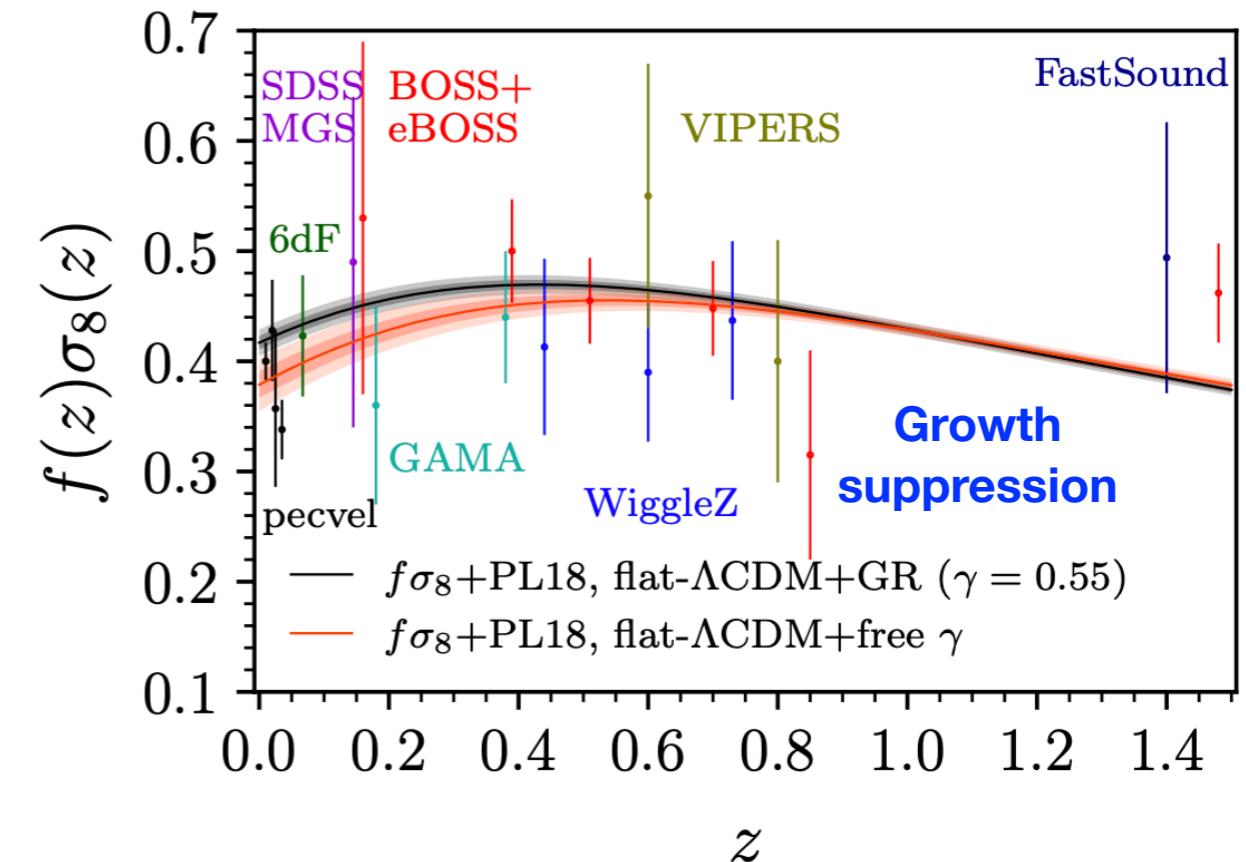
2302.01331 (PRL) growth index tension

$$D(a(t)) = \delta(t)/\delta(t_0) : f(a) = d \ln D/d \ln a = \Omega_m(a)^\gamma$$



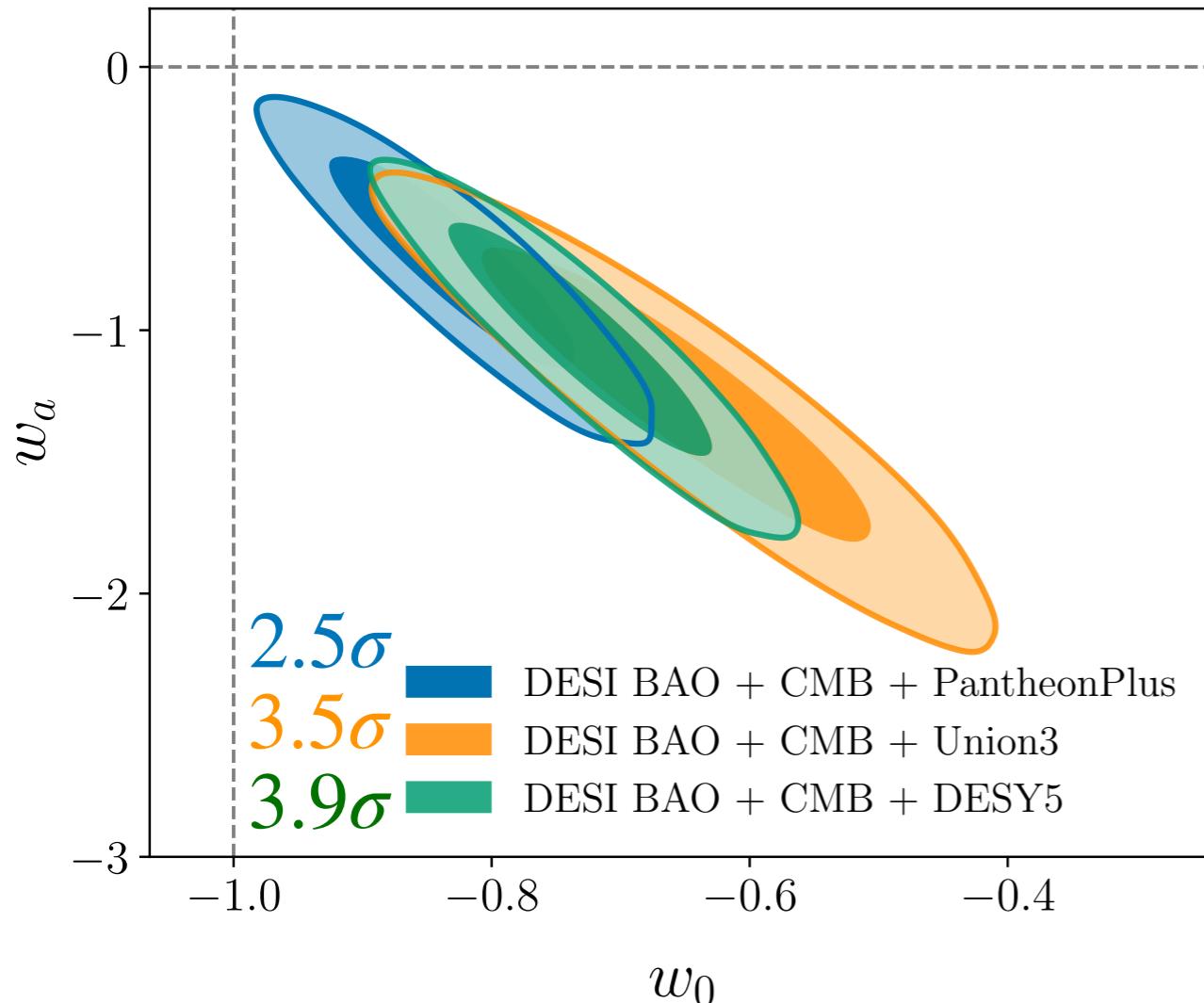
**A larger  $\gamma$  reproduces the flat Universe that is otherwise closed with  $A_L = 1$  from 1911.02087**

Nature Astron

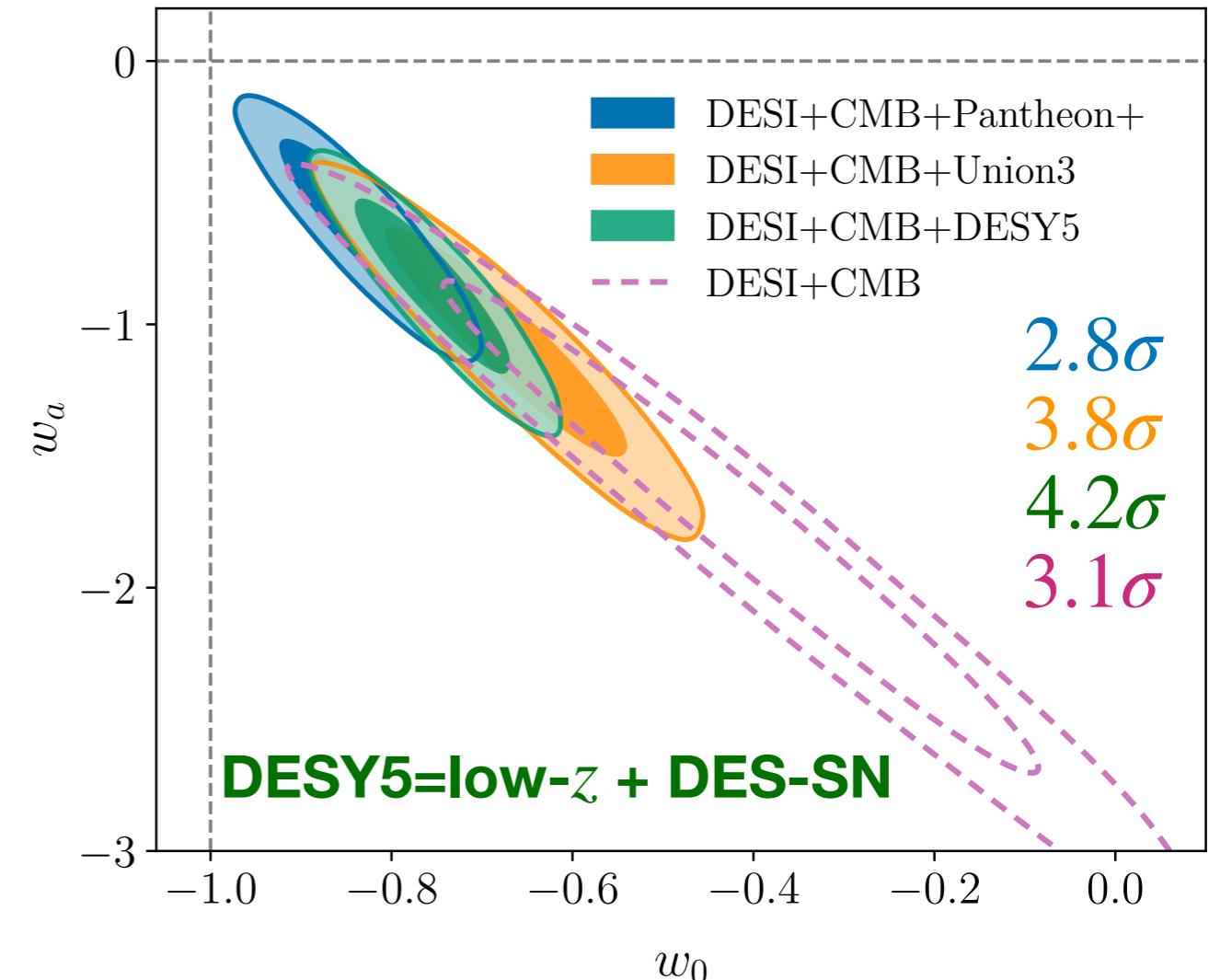


# DESI-BAO+Planck-CMB+SNe

**2404.03002 DESI DR1 Y1 BAO**



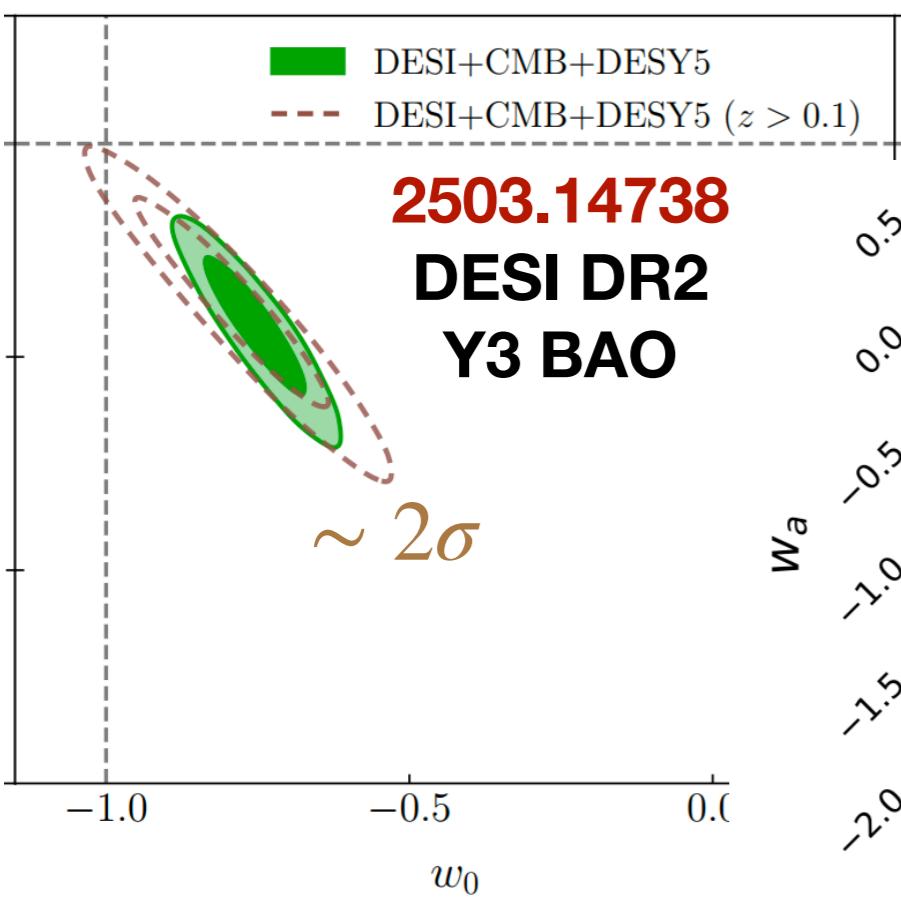
**2503.14738 DESI DR2 Y3 BAO**



**2408.07175 George Efstathiou**  
**"Evolving dark energy or supernovae systematics?"**  
**MNRAS 538 (2025) 2, 875-882**

**2505.02658 George Efstathiou**  
**"Baryon Acoustic Oscillations from a Different Angle"**

# DESI-BAO+Planck-CMB+SNe

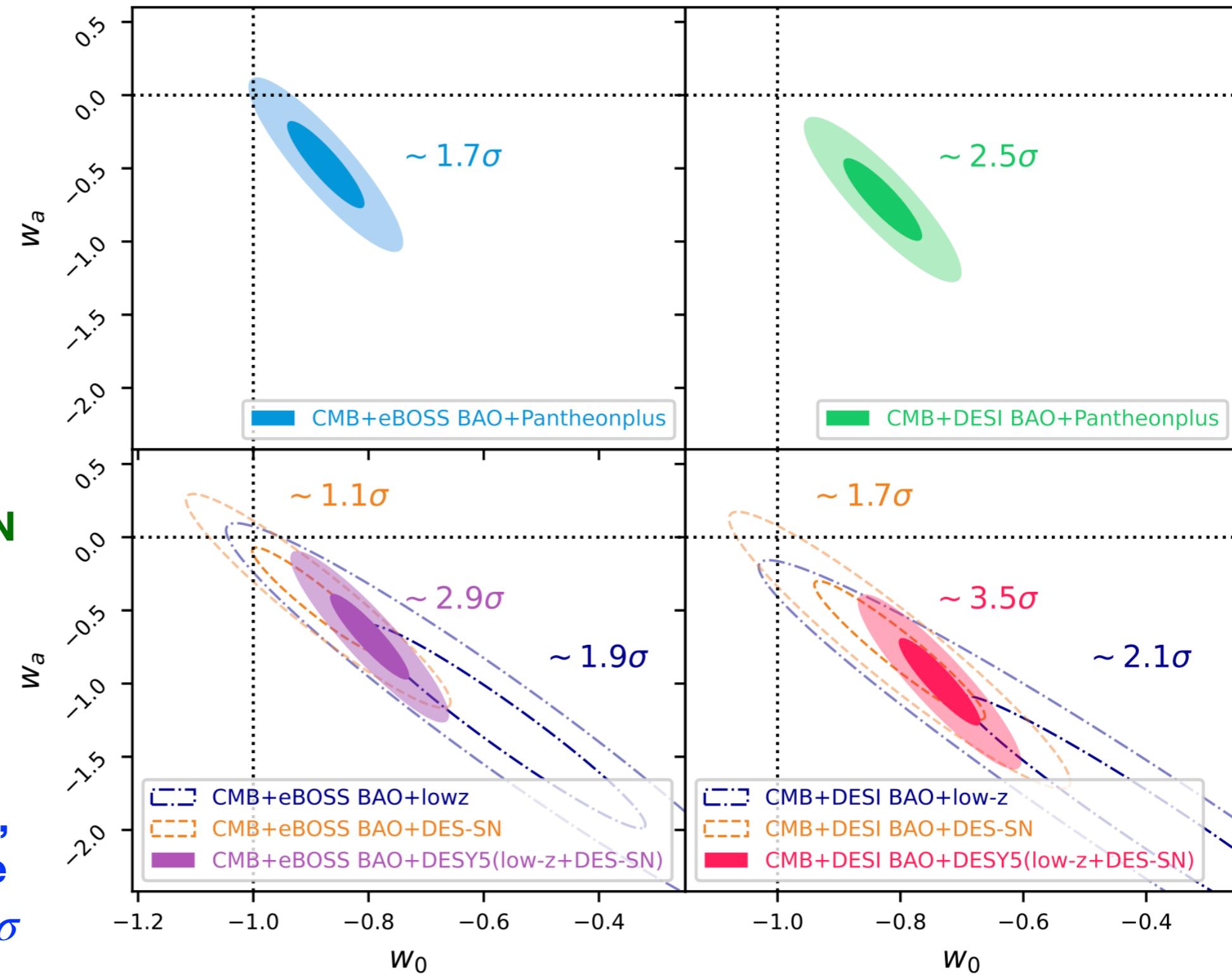


**2502.04212** Huang, Cai, SJW "The DESI DR1/DR2 evidence for dynamical dark energy is biased by low-redshift supernovae"

**DESY5=low- $z$  + DES-SN**

**Low- $z$  sample  
dominates the  
deviation from  $\Lambda$ CDM**

**Without low- $z$  sample,  
the deviation from the  
 $\Lambda$ CDM is only about  $2\sigma$**



# Distance ladder

$$\mu \equiv m_B - M_B \equiv 5 \lg \frac{D_L}{10 \text{pc}} \equiv 5 \lg d_L + 5 \lg \frac{c/H_0}{\text{Mpc}} + 25$$

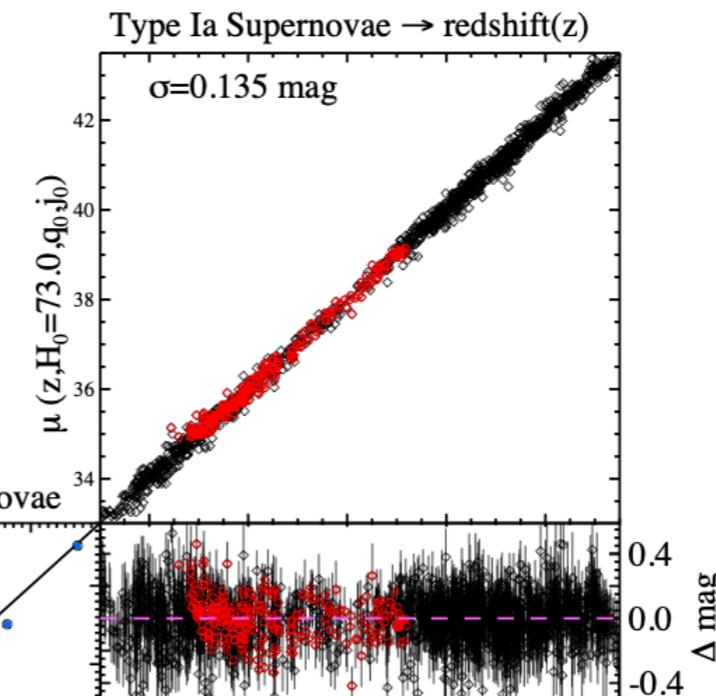
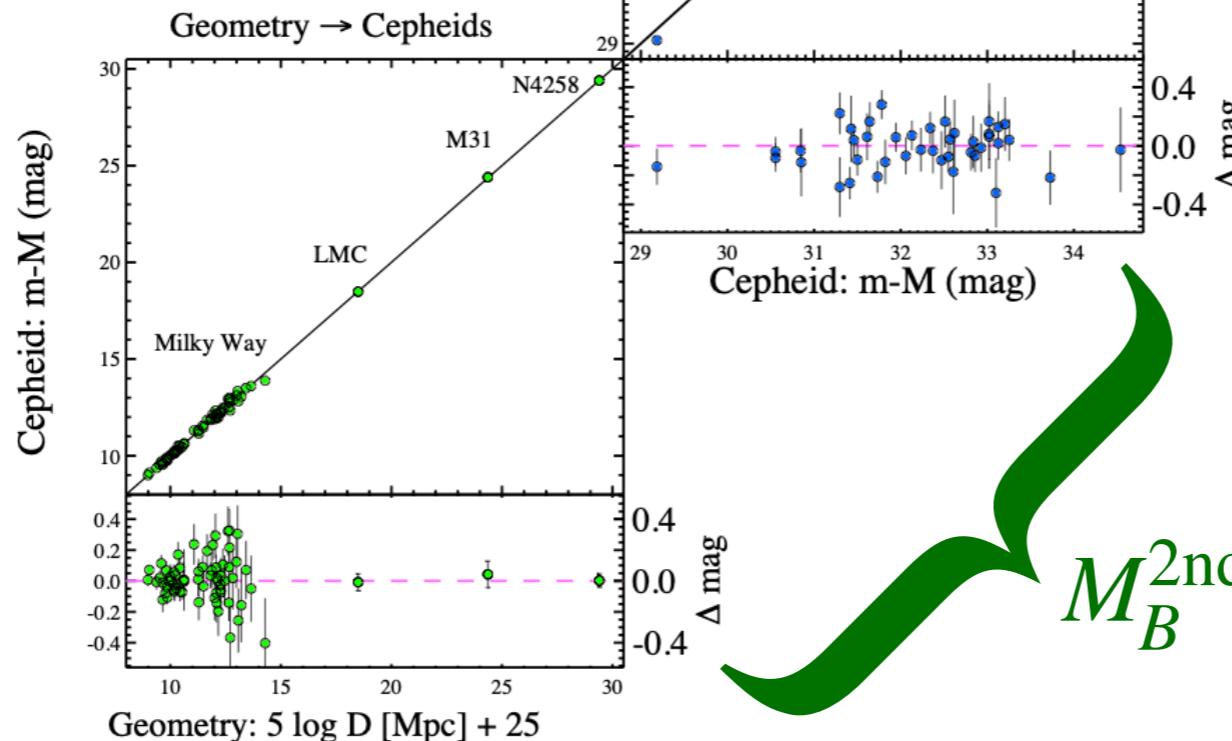
$$\Lambda\text{CDM} : E(z) \equiv H(z)/H_0 = \sqrt{\Omega_m(1+z)^3 + (1-\Omega_m)}$$

$$d_L(z) = \frac{D_L(z)}{c/H_0} = (1+z) \int_0^z \frac{dz'}{E(z')}$$

$$m_B = 5 \lg d_L(z) - 5a_B$$

$$-5a_B \equiv M_B + 5 \lg \frac{c/H_0}{\text{Mpc}} + 25$$

**1. 1st & 2nd rungs inter-calibrations systematics**



**2. 3rd-rung statistical systematics**

$a_B^{3\text{rd}}$

**3. No intrinsic SN systematics**

$$M_B^{2\text{nd}} = M_B^{3\text{rd}} \text{ & } a_B^{3\text{rd}} \Rightarrow H_0$$

$M_B^{2\text{nd}}$

**4. No apparent SN systematics**

$$a_B^{3\text{rd}} = a_B^{2\text{nd}} \text{ & } M_B^{2\text{nd}} \Rightarrow H_0$$

# Distance ladder

THE ASTROPHYSICAL JOURNAL, 935:83 (19pp), 2022 August 20

<https://doi.org/10.3847/1538-4357/ac80bd>

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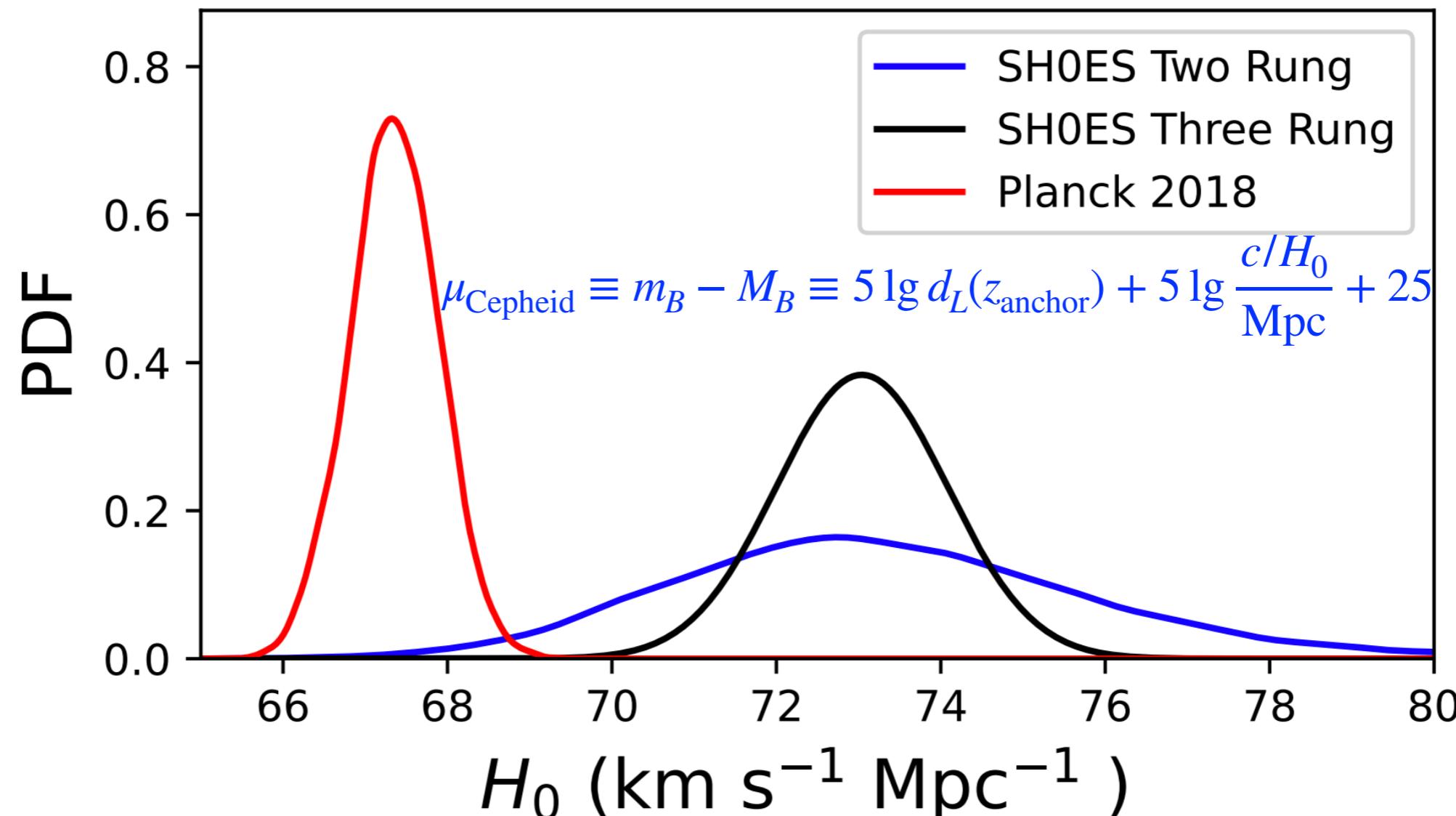
2204.10866



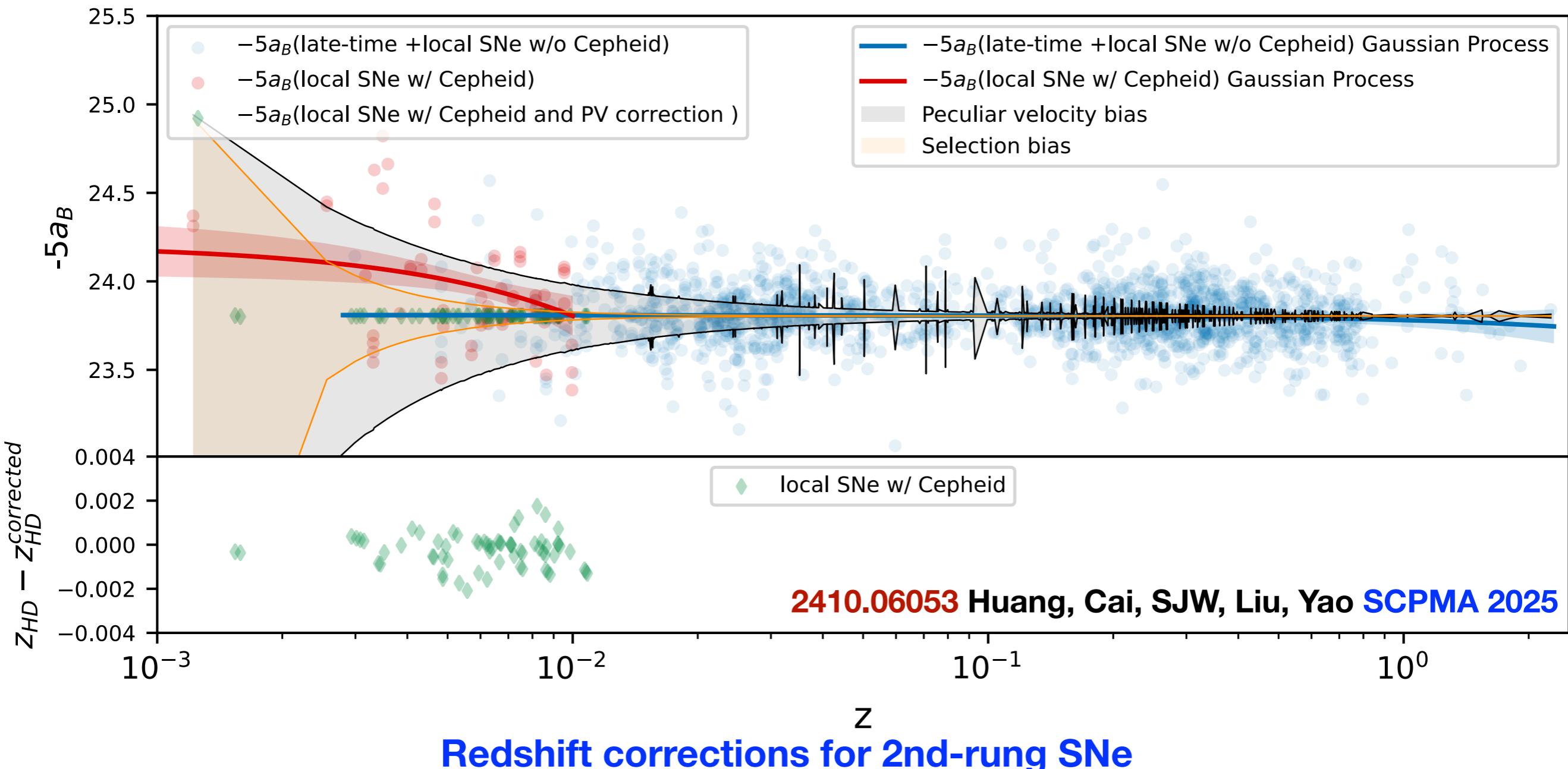
CrossMark

## Measurements of the Hubble Constant with a Two-rung Distance Ladder: Two Out of Three Ain't Bad

W. D'Arcy Kenworthy<sup>1</sup> , Adam G. Riess<sup>1</sup> , Daniel Scolnic<sup>2</sup> , Wenlong Yuan<sup>1</sup> , José Luis Bernal<sup>1</sup> , Dillon Brout<sup>3,7</sup> , Stefano Casertano<sup>4</sup>, David O. Jones<sup>5,7</sup> , Lucas Macri<sup>6</sup> , and Erik R. Peterson<sup>2</sup>



# $a_B$ tension around $z \sim 0.01$ ?



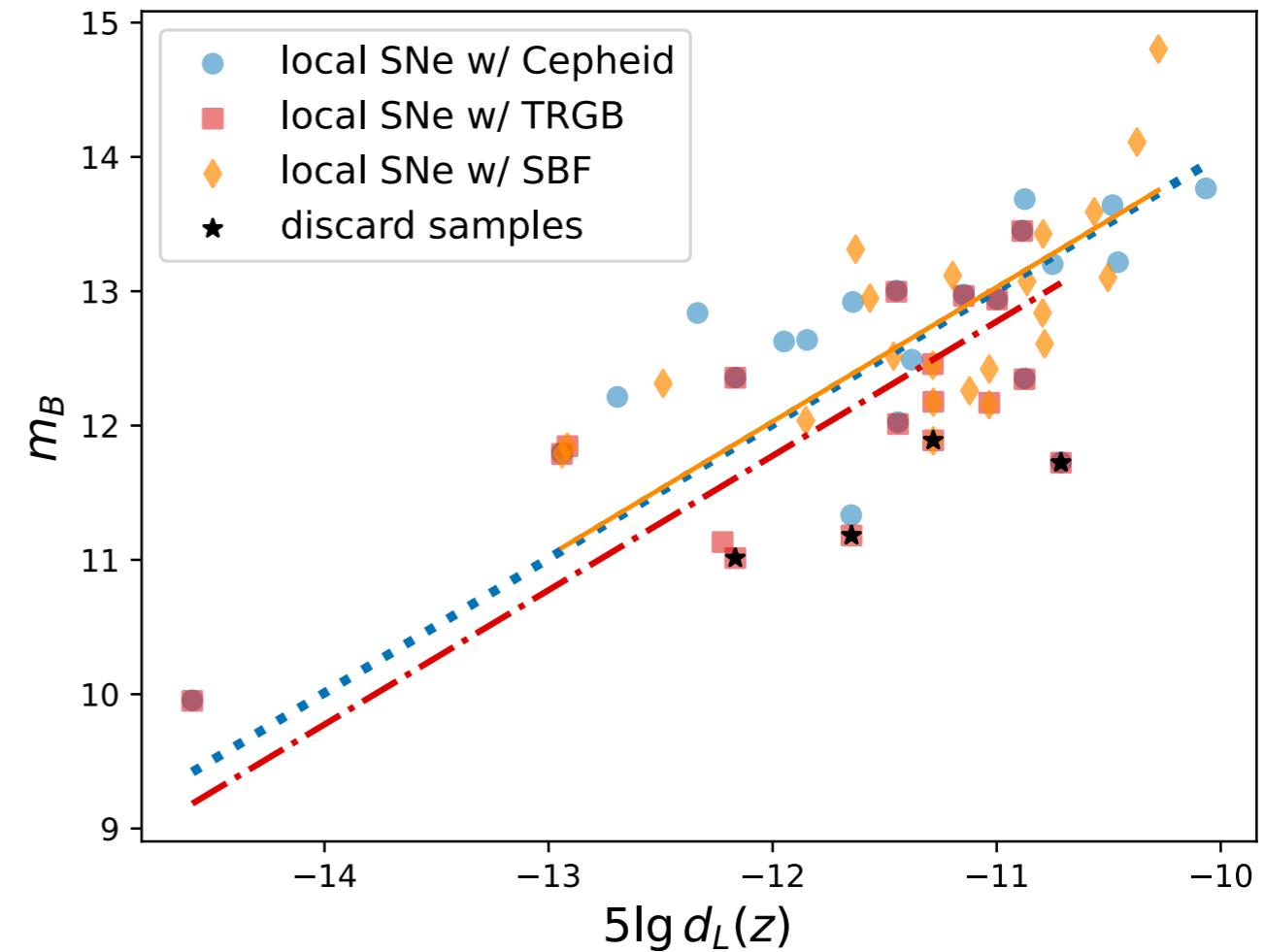
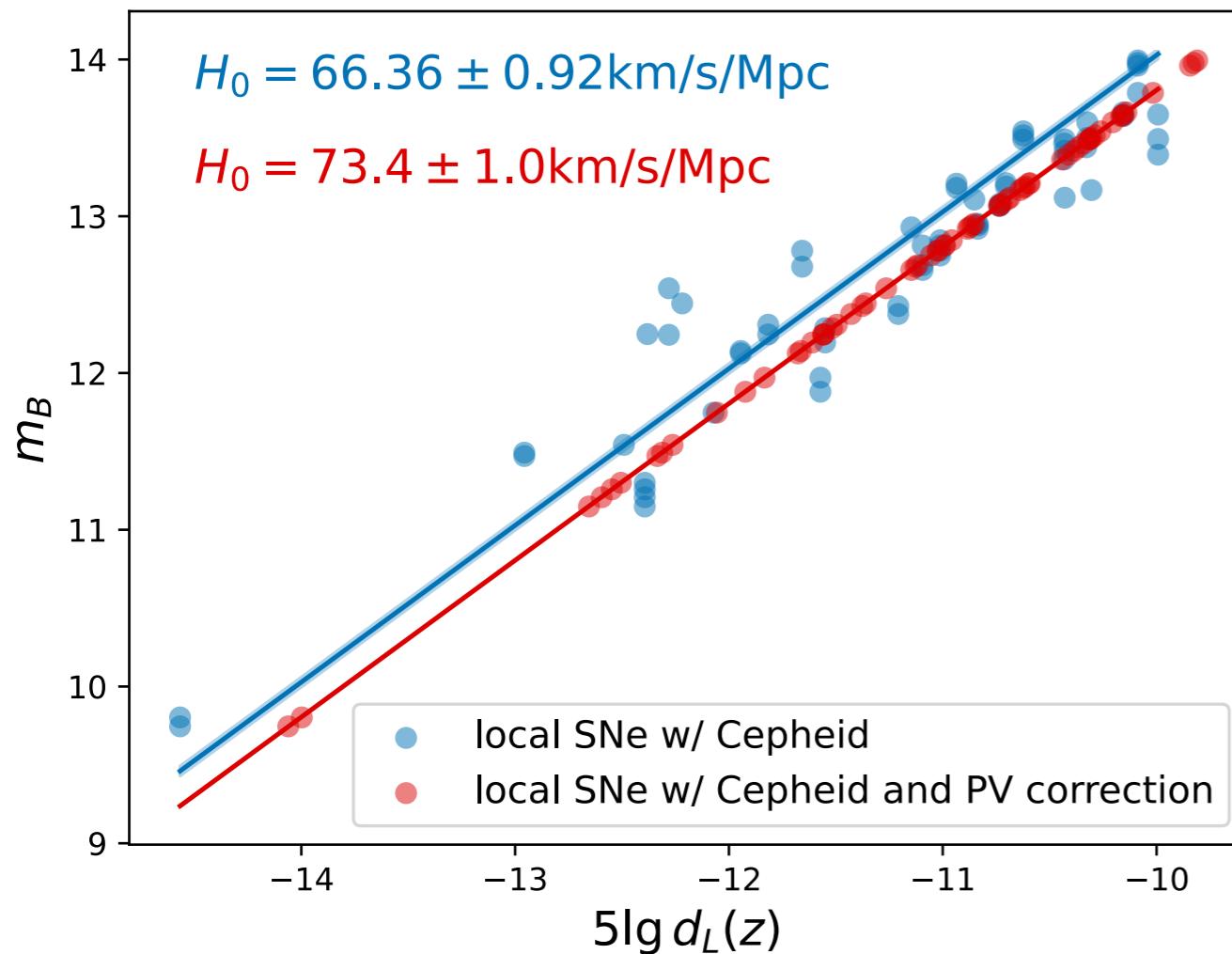
Rigorous approach: SH0ES 2204.10866

PV corrections directly from reconstructions of density field and velocity field from 2M++/2MRS

Efficient approach: Ours 2410.06053

Redshift corrected from minimizing difference of  $a_{B,i} = \lg d_L(z_i) - 0.2m_{B,i}$  to Planck-calibrated late-time SNe

# $a_B$ consistency around $z \sim 0.01$



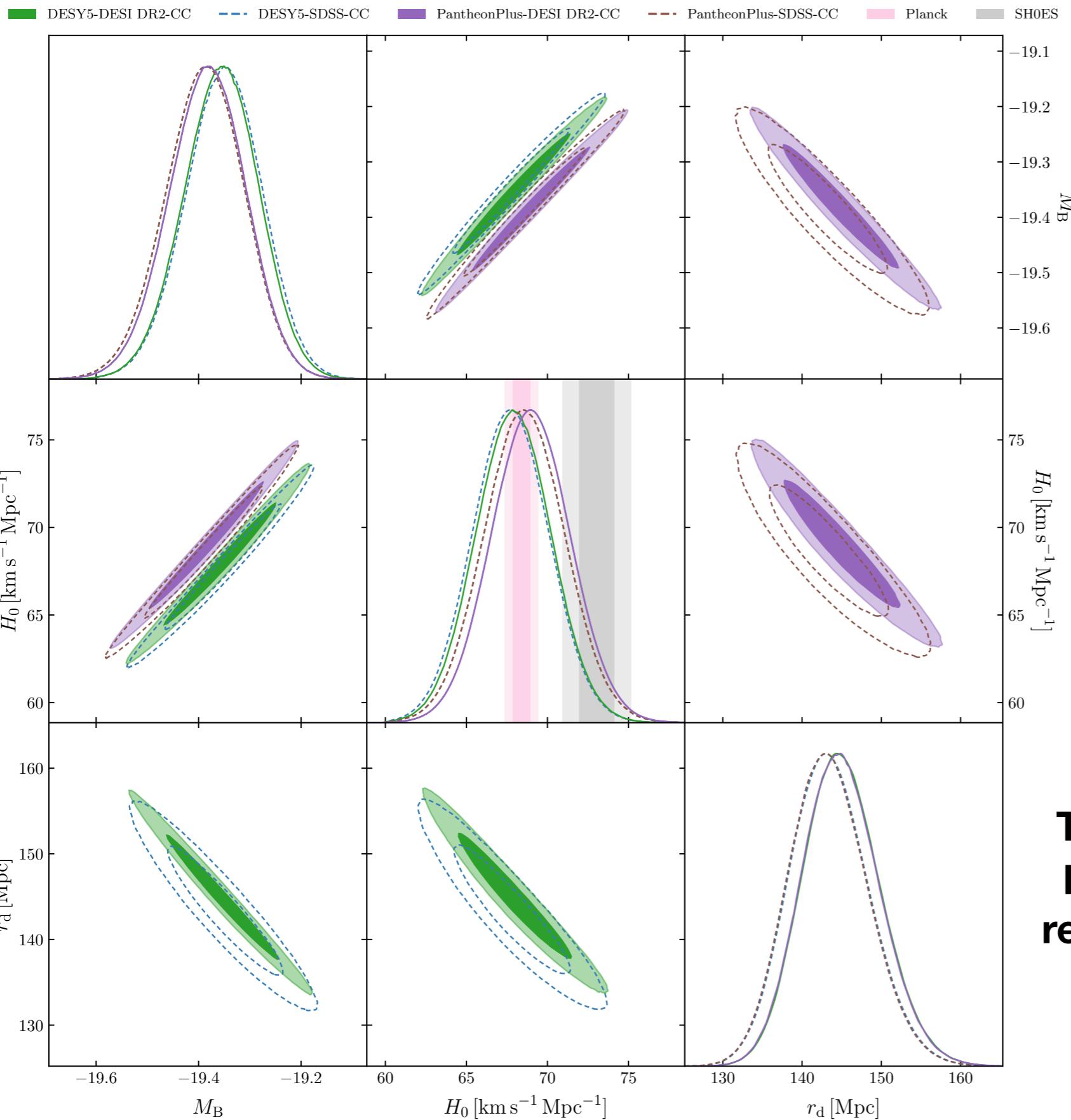
**Our first two-rung distance ladder result**

**SH0ES first two-rung distance ladder:**  
supports our redshift correction  
  
**SH0ES three-rung distance ladder:**  
no third-rung SN systematics

$$H_0 = \begin{cases} 73.1 \pm 2.4 \text{ km/s/Mpc}, & z_{\text{CSP}} + \mu_{\text{Cepheid}}, \\ 74.5 \pm 3.5 \text{ km/s/Mpc}, & z_{\text{CSP}} + \mu_{\text{TRGB}}, \\ 72.1 \pm 2.3 \text{ km/s/Mpc}, & z_{\text{CSP}} + \mu_{\text{SBF}}. \end{cases}$$

**There is no more disagreement between Riess and Freedman**

# $a_B$ tension around $z \sim 0.1$ ?



2505.22369 Jia-Le Ling, Guo-Hong Du, Tian-Nuo Li, Jing-Fei Zhang, Shao-Jiang Wang, Xin Zhang  
**Model-independent cosmological inference after the DESI DR2 data with improved inverse distance ladder**

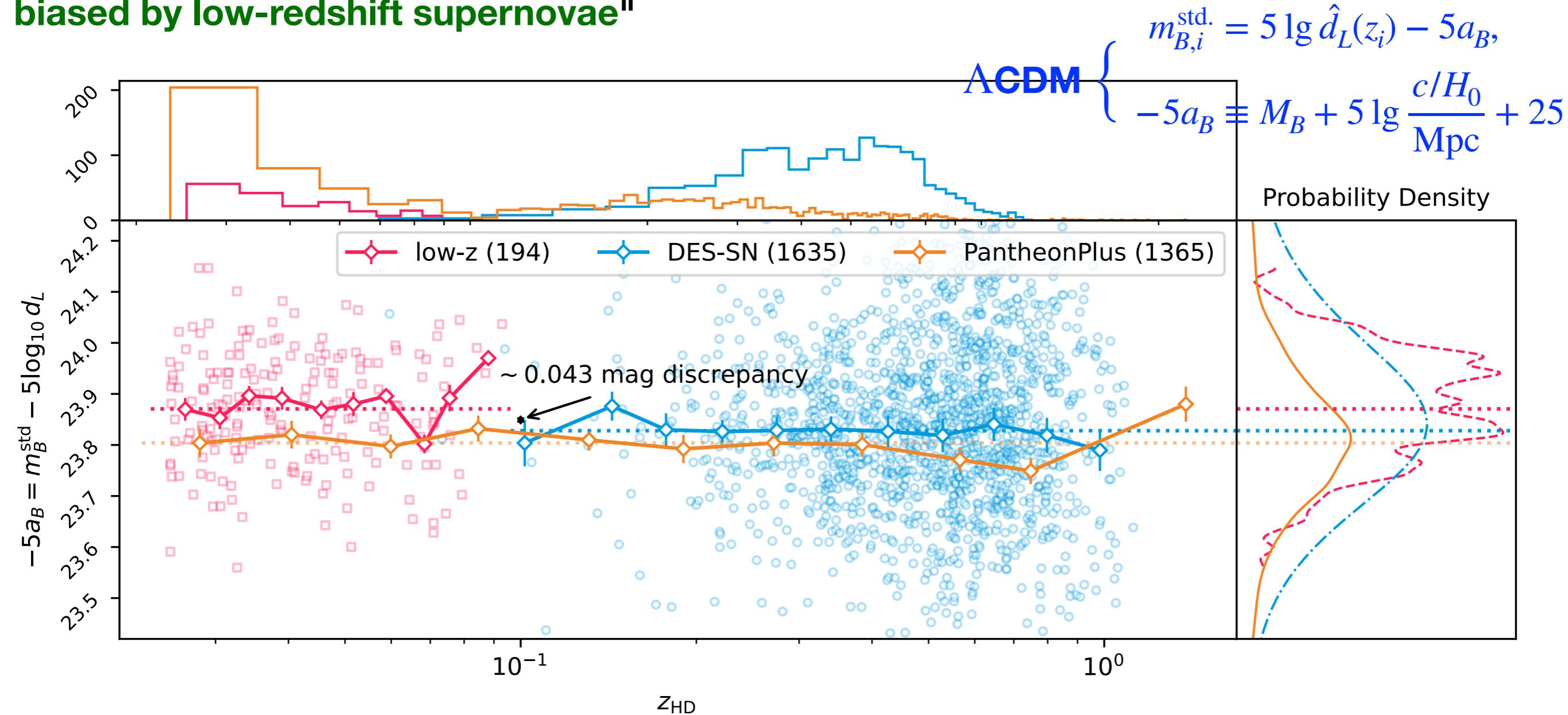
$$m_B = 5 \lg d_L(z) - 5a_B$$

$$-5a_B \equiv M_B + 5 \lg \frac{c/H_0}{\text{Mpc}} + 25$$

**There is an  $a_B$  tension between DESY5 and PantheonPlus SNe regardless of DESI DR2/SDSS or CMB/CC and  $\Lambda$ CDM/PAge !**

# $a_B$ tension around $z \sim 0.1$ ?

2502.04212 Huang, Cai, SJW "The DESI DR1/DR2 evidence for dynamical dark energy is biased by low-redshift supernovae"



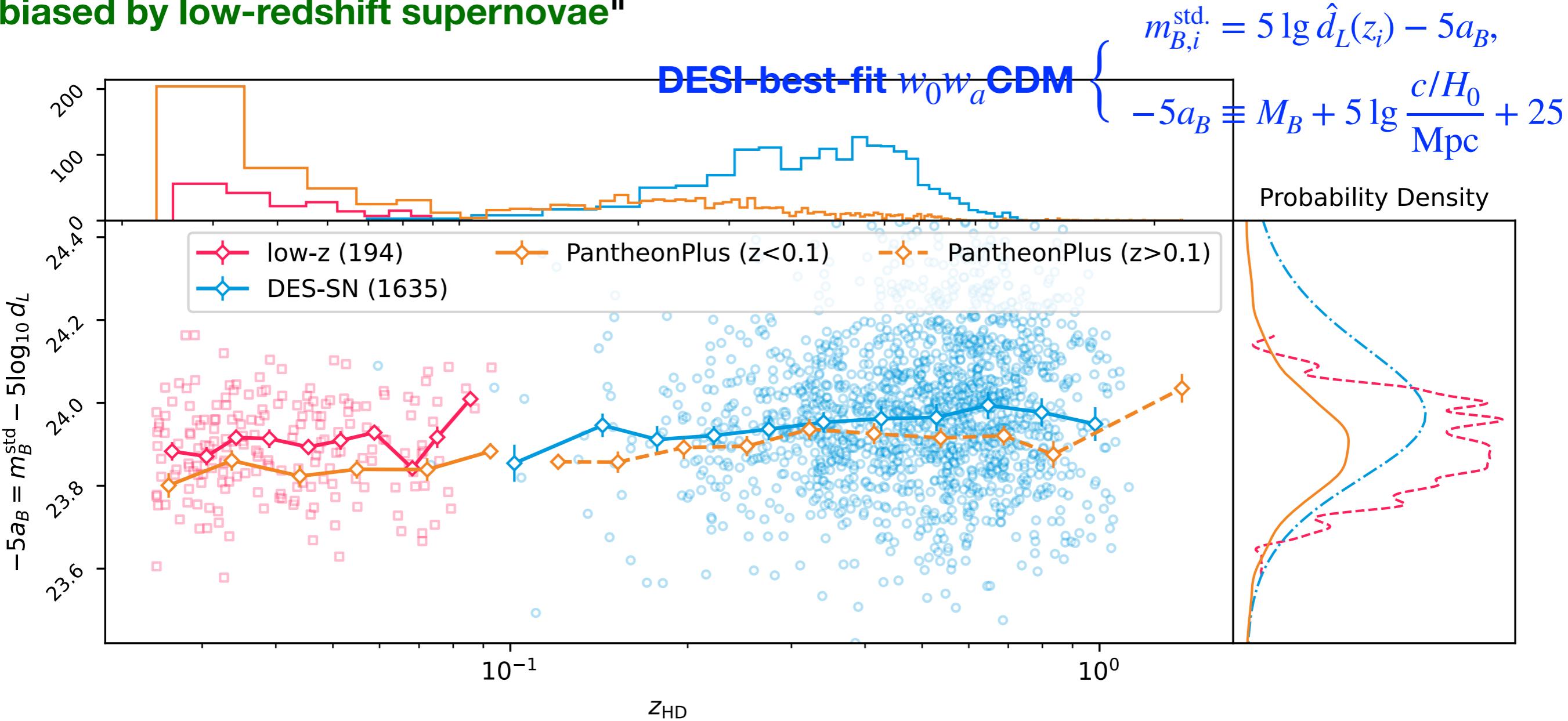
Intercept  $-5a_B$  is the degeneracy direction of  $H_0$  and  $M_B$  and more sensitive to systematics in  $m$  and  $z$

Its measured value is more reliable at high redshifts than low redshift, less affected by peculiar velocity

DESY5=low-z+DES-SN admits  $a_B$  discrepancy between low-z and DES-SN, unlike uniform PantheonPlus

# $a_B$ tension around $z \sim 0.1$ ?

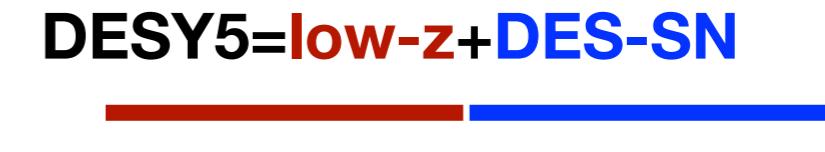
2502.04212 Huang, Cai, SJW "The DESI DR1/DR2 evidence for dynamical dark energy is biased by low-redshift supernovae"



$\Lambda$ CDM: DESY5=low-z+DES-SN

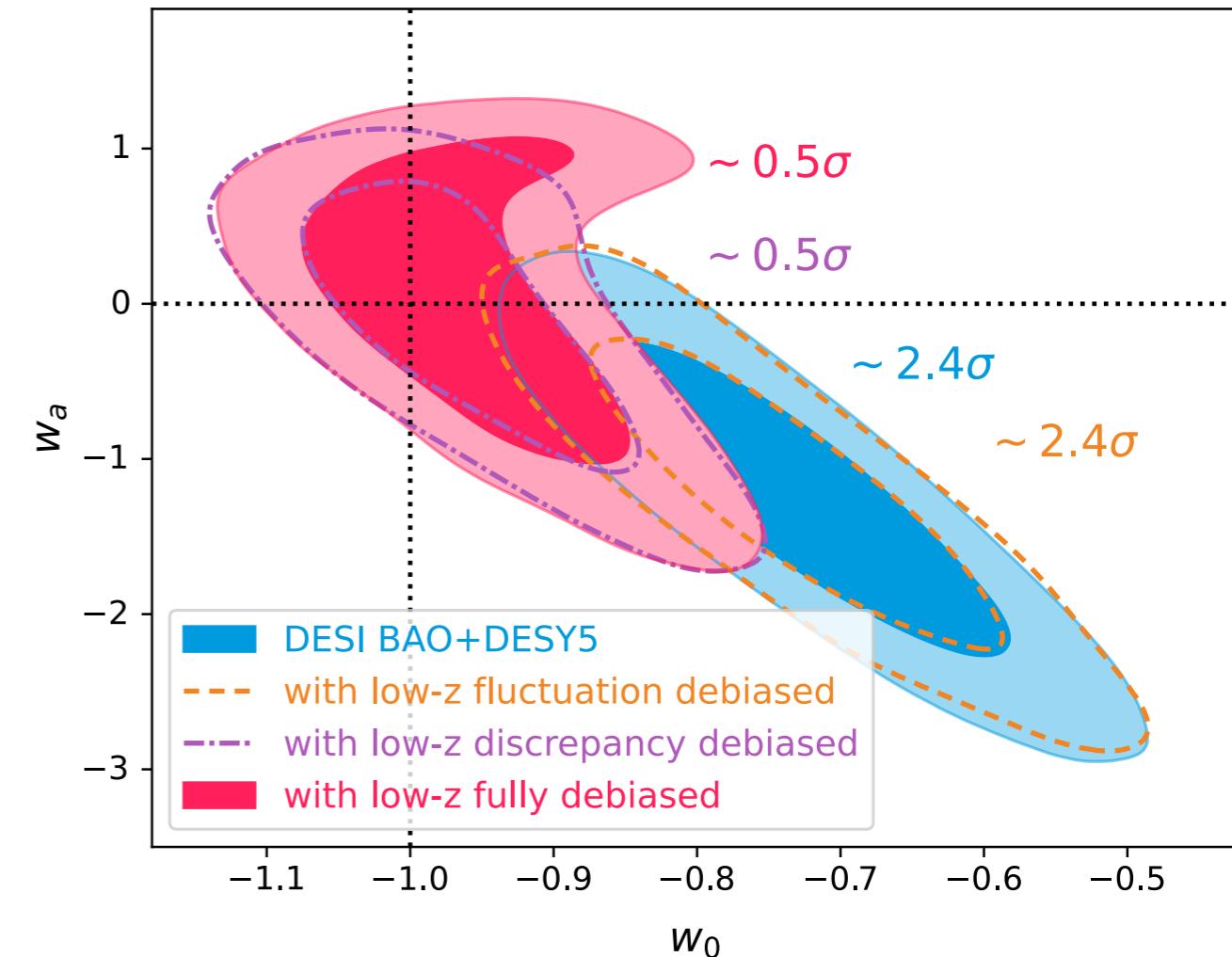
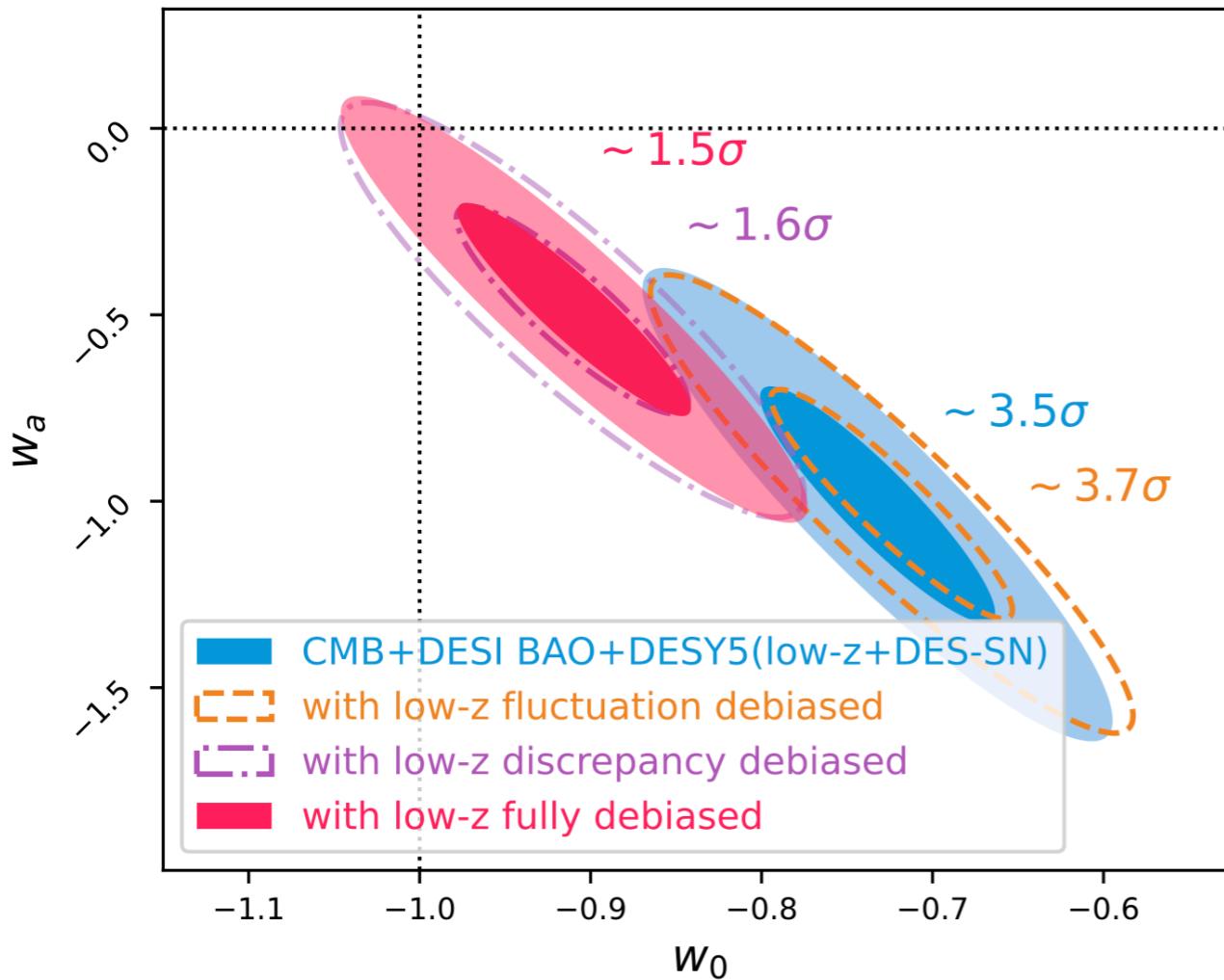


Other model:



# $a_B$ consistency around $z \sim 0.1$

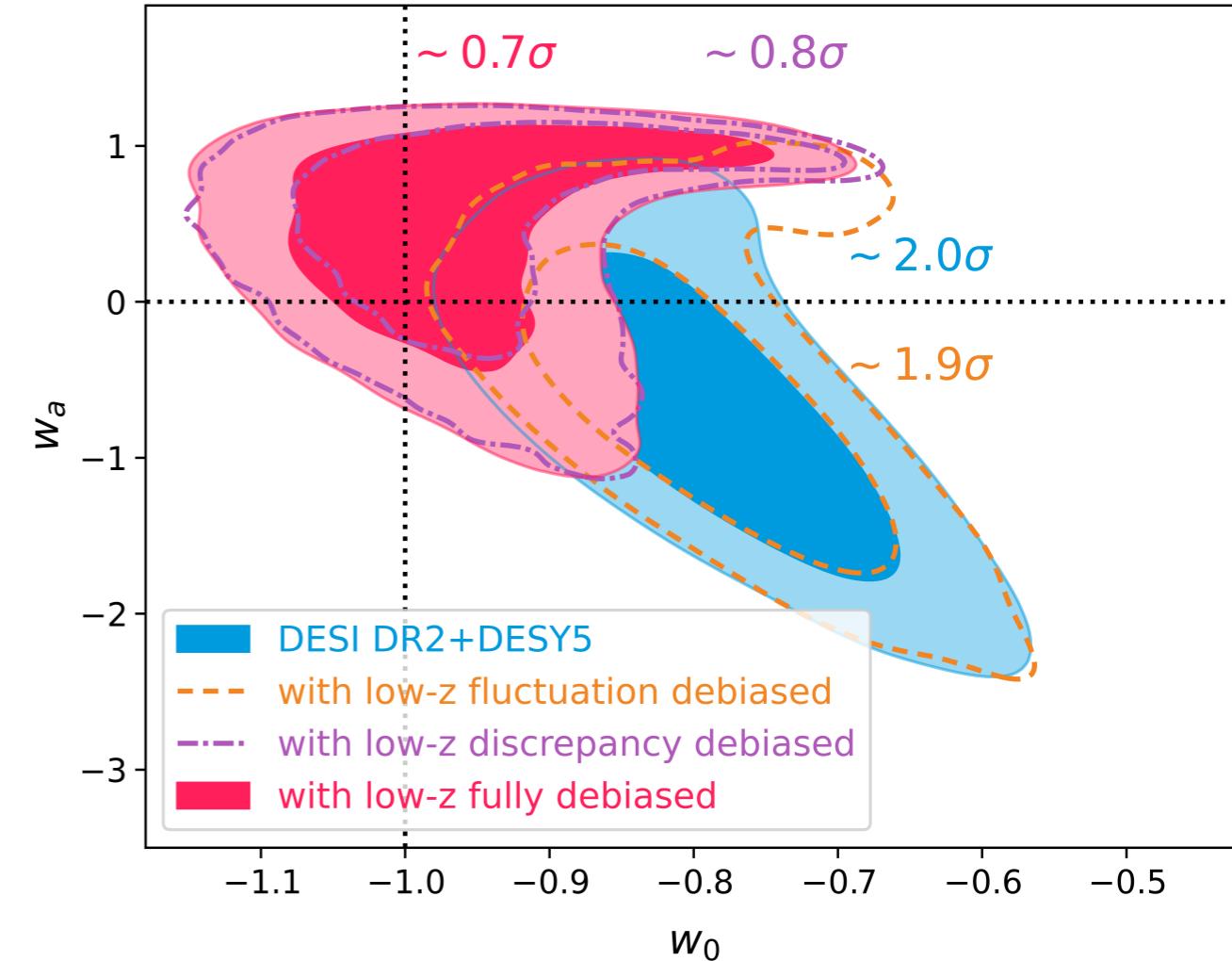
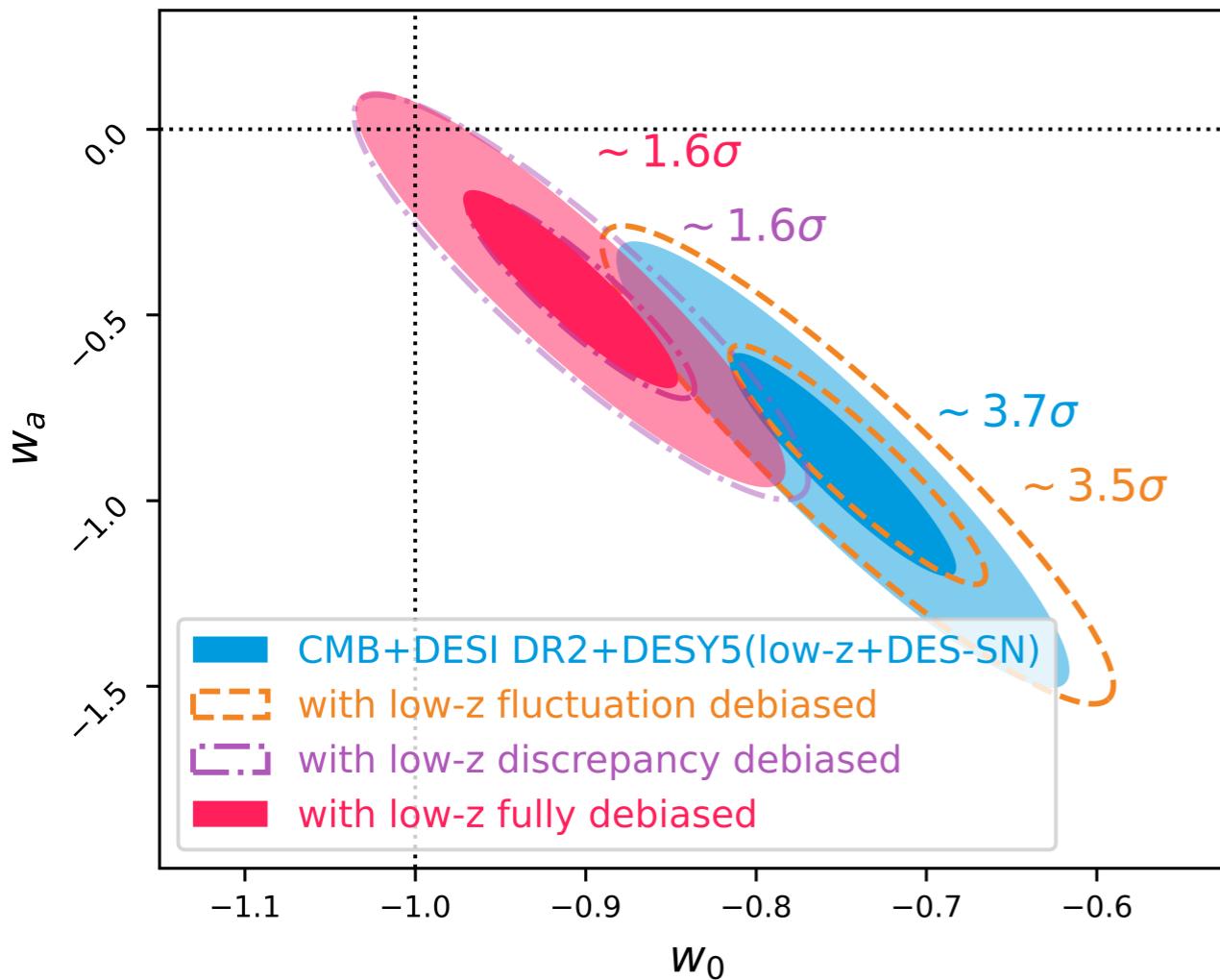
2502.04212 Huang, Cai, SJW "The DESI DR1/DR2 evidence for dynamical dark energy is biased by low-redshift supernovae"



The DDE evidence from Planck-CMB+DESI Y1 BAO+DESY5(low-z+DES-SN) is reduced from  $3.5\sigma$  to  $1.5\sigma$  after our bias correction, and the pure late-Universe data without Planck-CMB deviates from  $\Lambda$ CDM only at  $0.5\sigma$

# $a_B$ consistency around $z \sim 0.1$

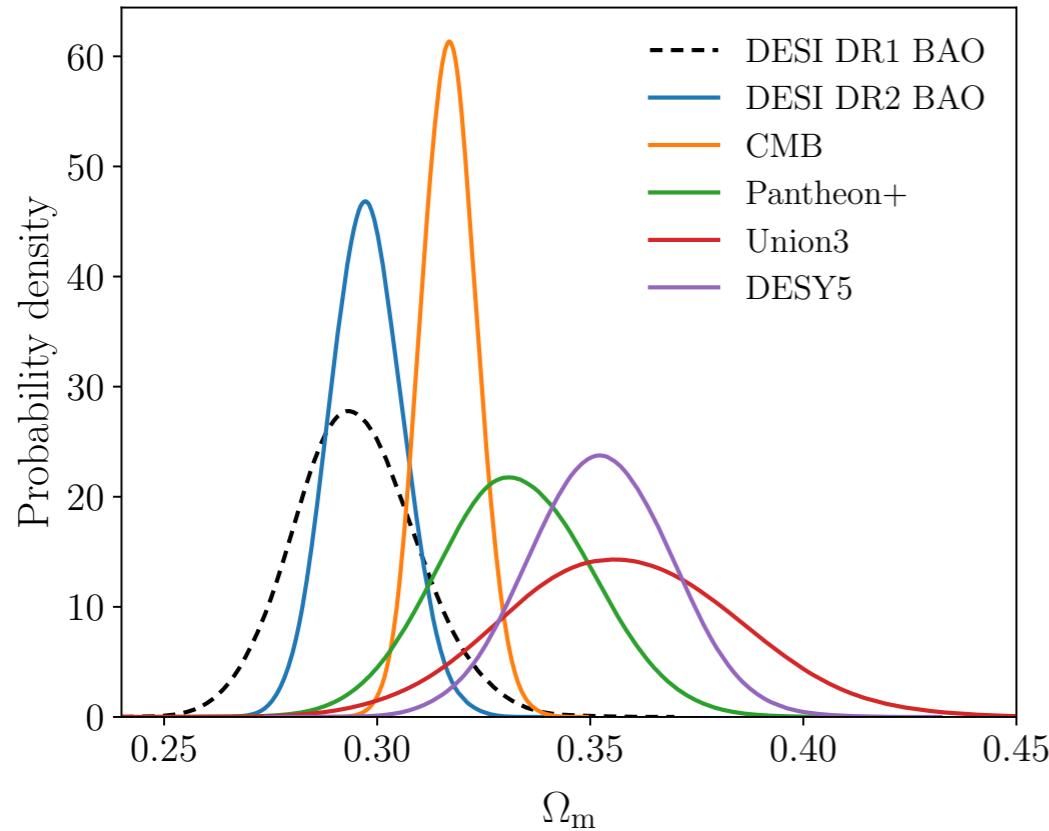
2502.04212 Huang, Cai, SJW "The DESI DR1/DR2 evidence for dynamical dark energy is biased by low-redshift supernovae"



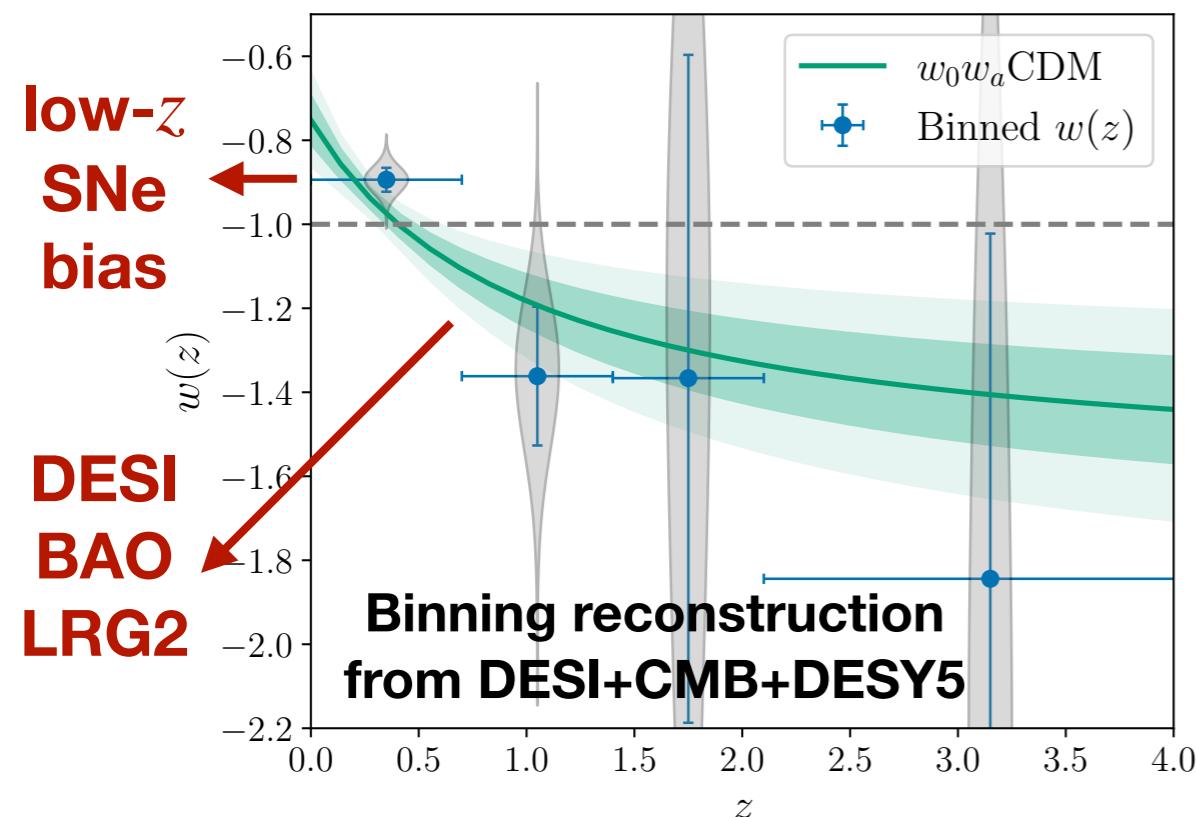
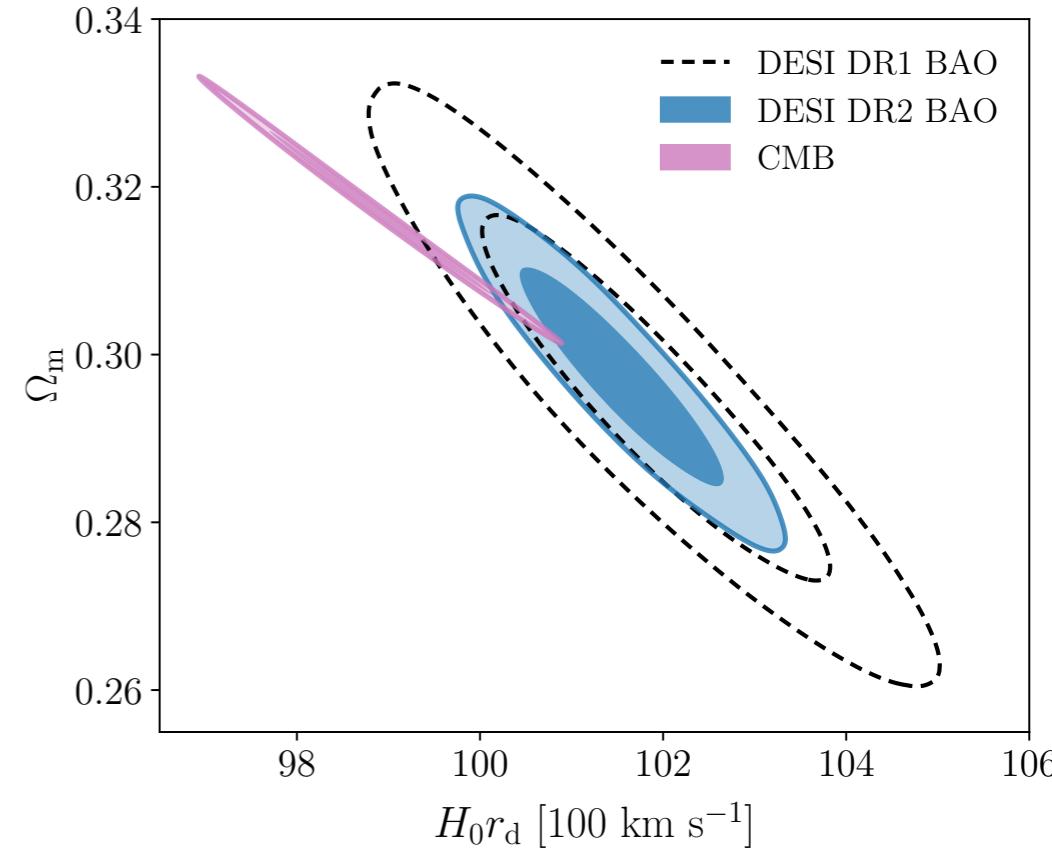
The DDE evidence from Planck-CMB+DESI Y3 BAO+DESY5(low-z+DES-SN) is reduced from  $3.7\sigma$  to  $1.6\sigma$  after our bias correction, and the pure late-Universe data without Planck-CMB deviates from  $\Lambda$ CDM only at  $0.7\sigma$

# DESI-BAO VS Planck-CMB

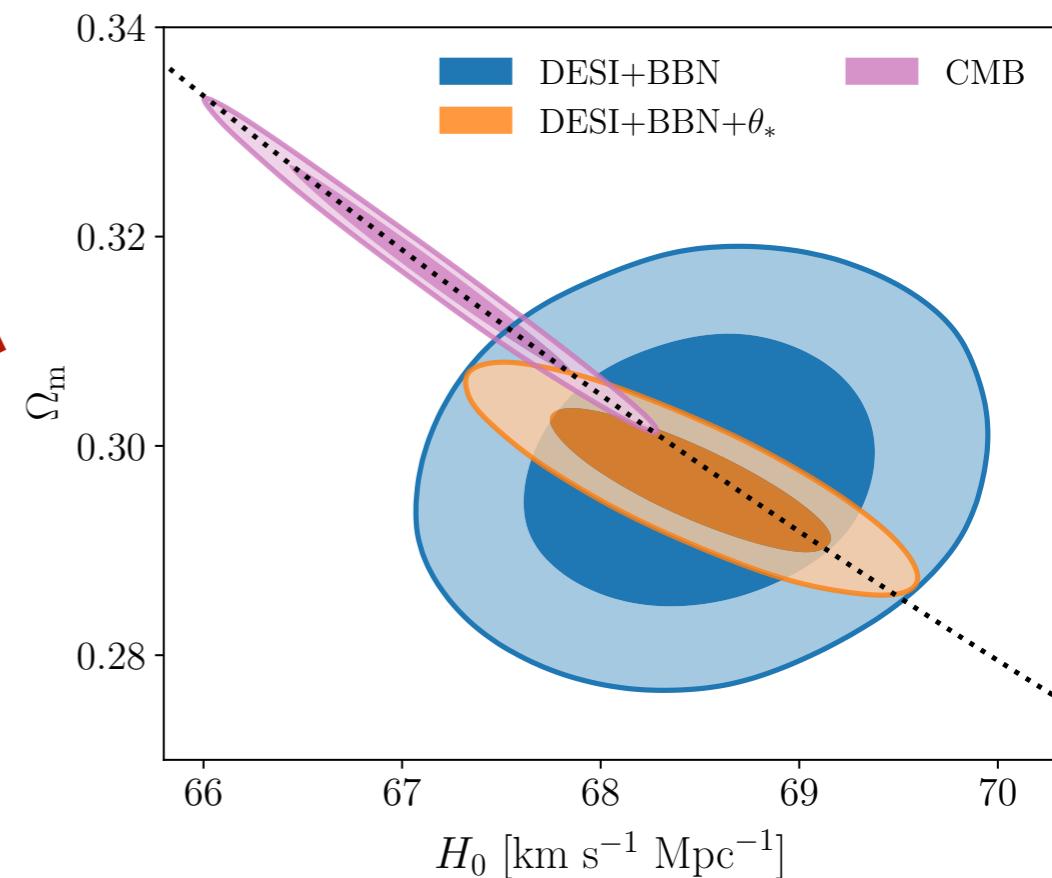
2503.14738 DESI DR2 Y3 BAO What DESI DR2 truly want to tell us is  $\Omega_m$  tension with Planck-CMB within  $\Lambda$ CDM



$\Omega_m$  tension!

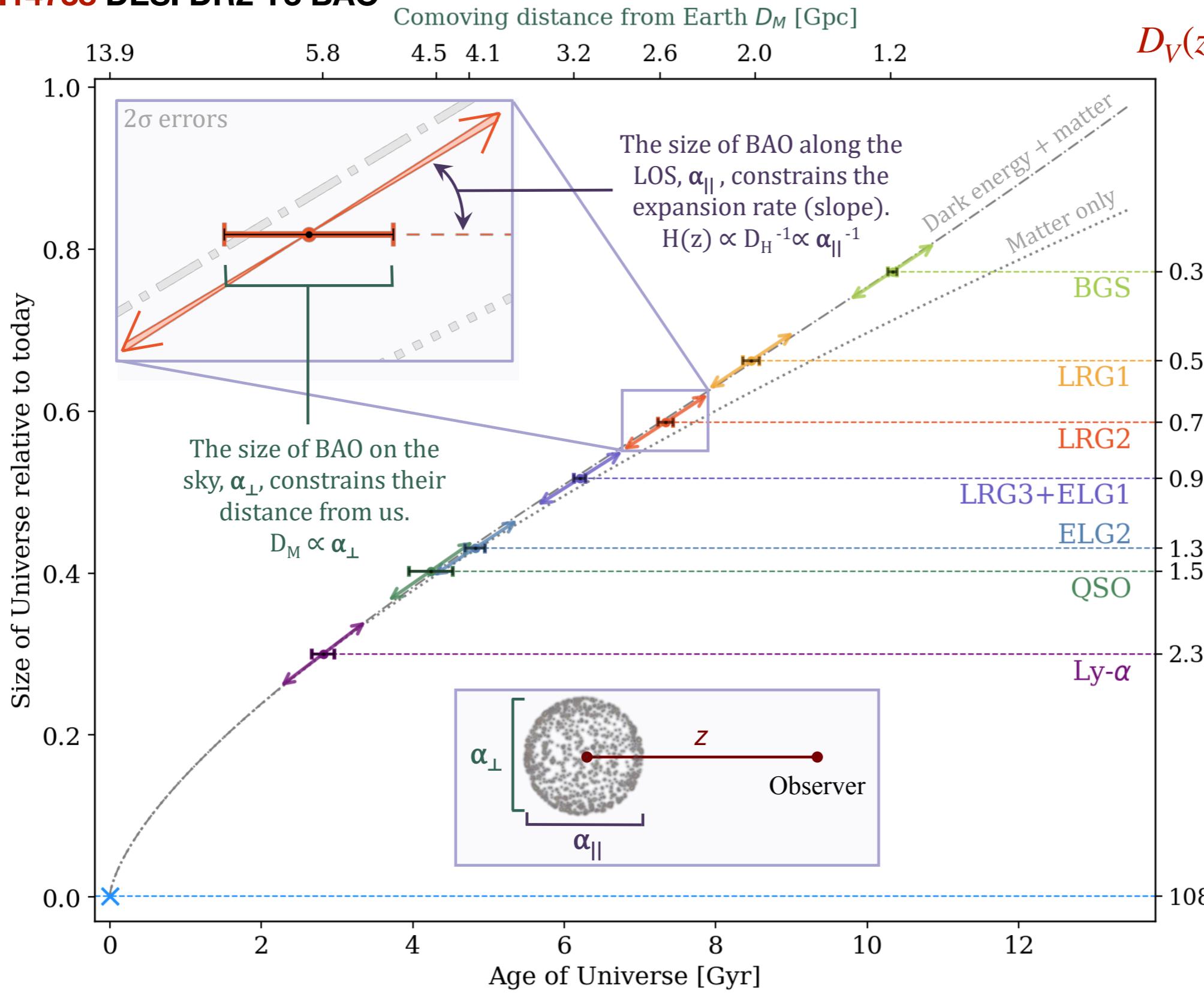


Dynamical  
dark energy  
with phantom  
crossing



# DESI BAO

2503.14738 DESI DR2 Y3 BAO



$$D_V(z) = (z D_M^2(z) D_H(z))^{1/3}$$

$$D_H(z) = \frac{c}{H(z)}$$

$$D_M(z) = \int_0^{z'} \frac{cdz'}{H(z')}$$

$$r_d = \int_{z_d}^{\infty} \frac{c_s(z)dz}{H(z)}$$

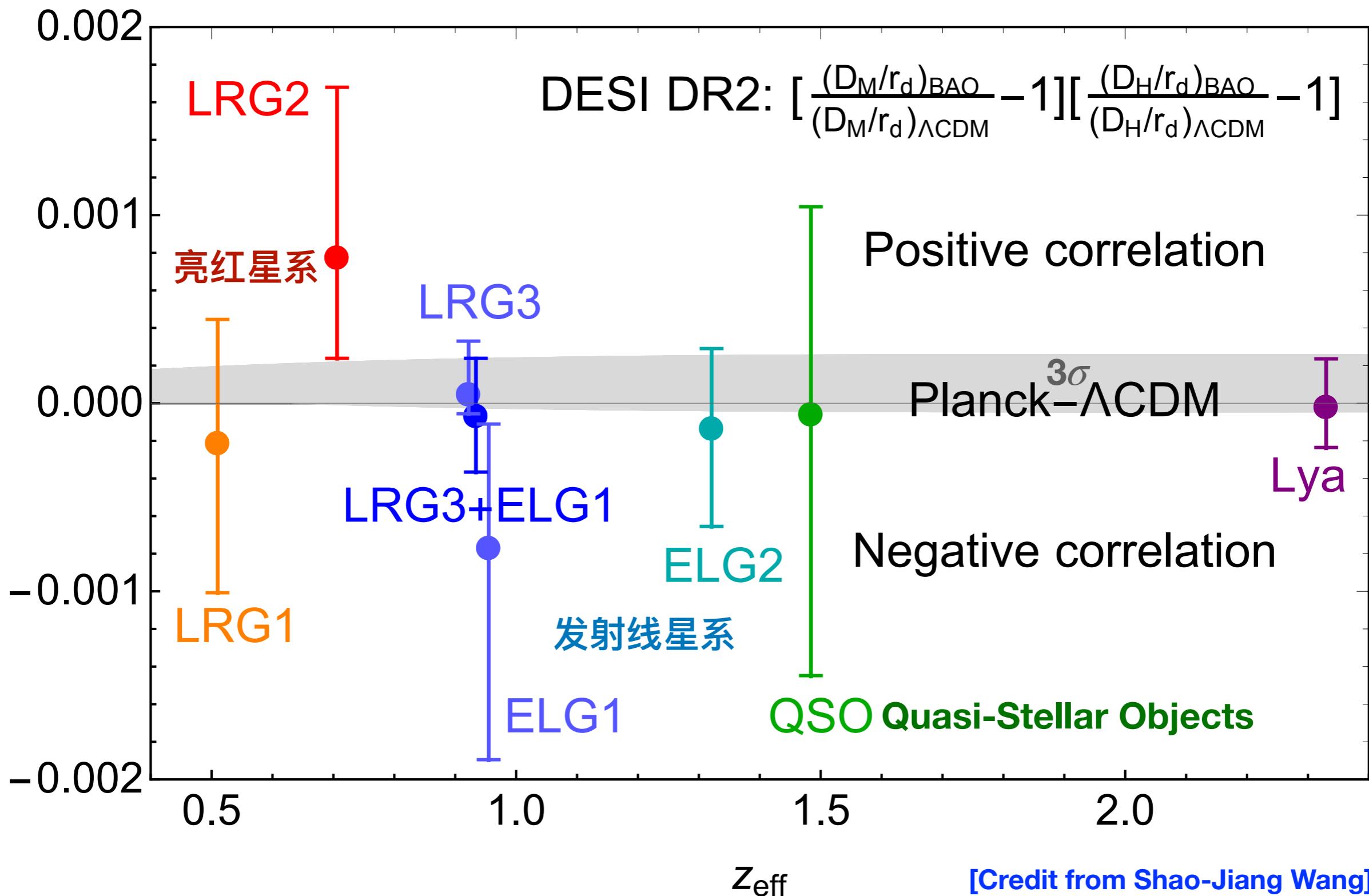
$$\alpha_{\parallel}(z) = \frac{D_H(z)/r_d}{D_H^{\text{fid}}(z)/r_d^{\text{fid}}}$$

$$\alpha_{\perp}(z) = \frac{D_M(z)/r_d}{D_M^{\text{fid}}(z)/r_d^{\text{fid}}}$$

$$\alpha_{\text{iso}} = (\alpha_{\parallel} \alpha_{\perp}^2)^{1/3}$$

$$\alpha_{\text{AP}} = \alpha_{\parallel}/\alpha_{\perp}$$

# DESI BAO

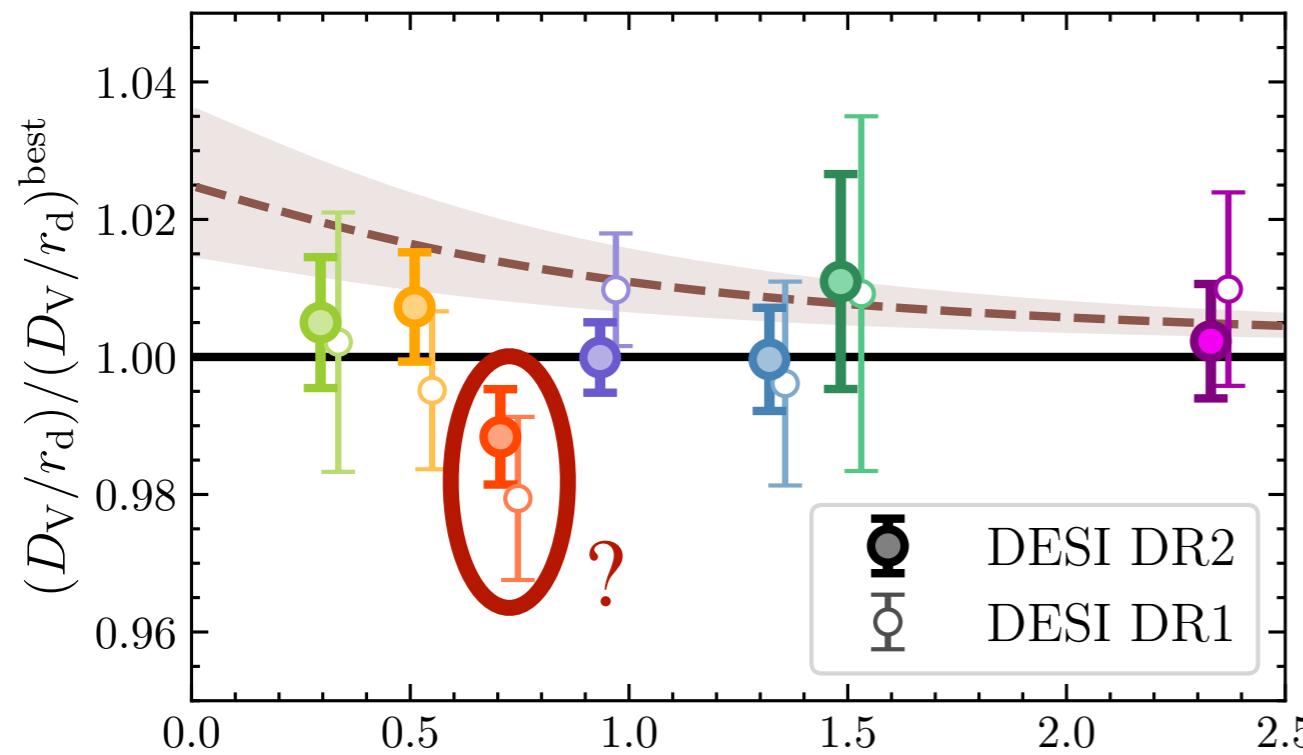


LRG2 is among the largest deviation from  $\Lambda$ CDM for a positive correlation between  $D_M/r_d$  and  $D_H/r_d$

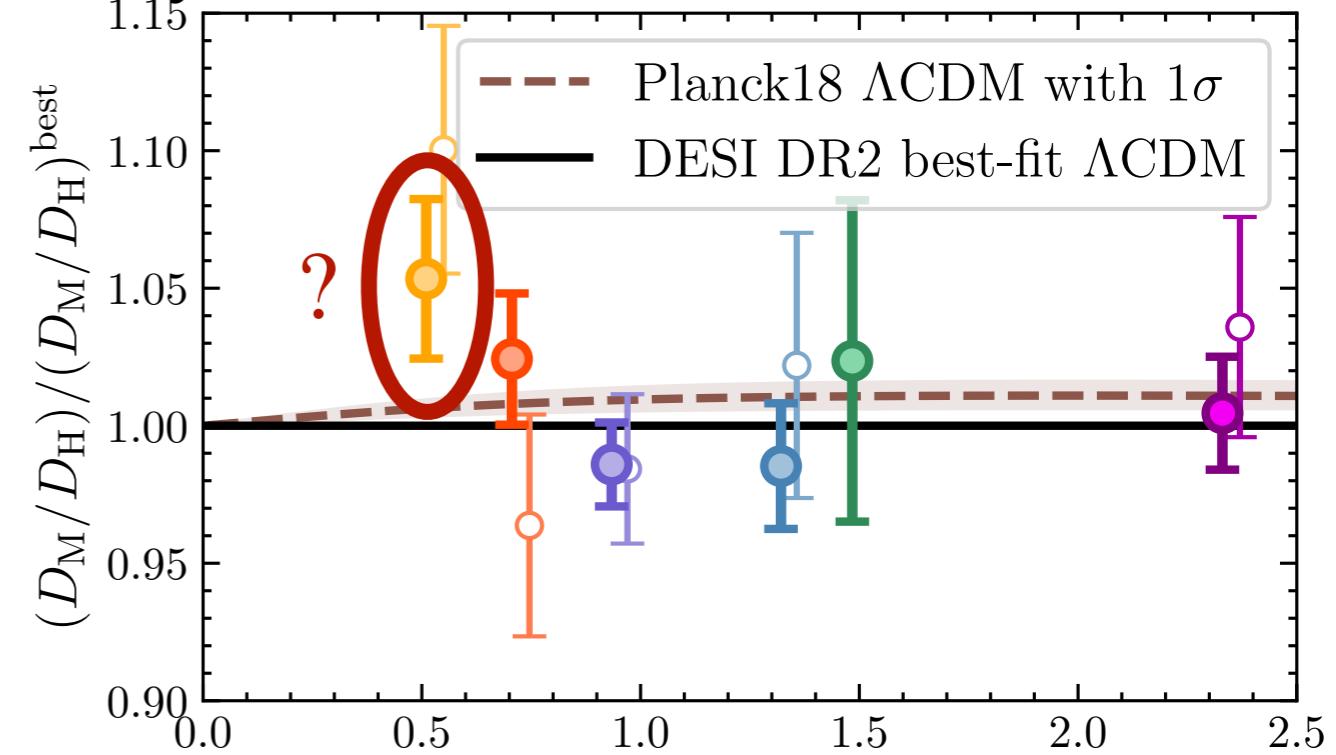
# DESI BAO

**2503.14738 DESI DR2 Y3 BAO**

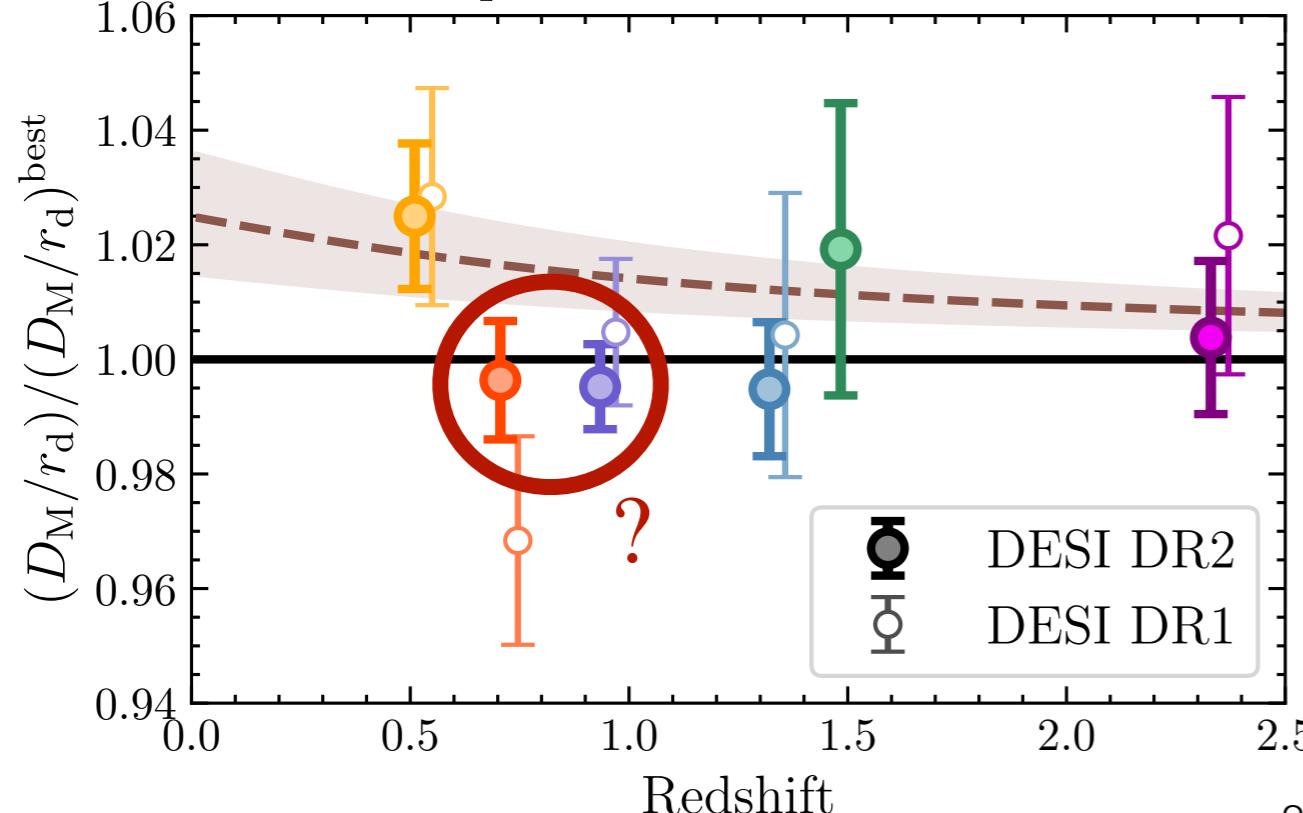
Isotropic BAO Distance



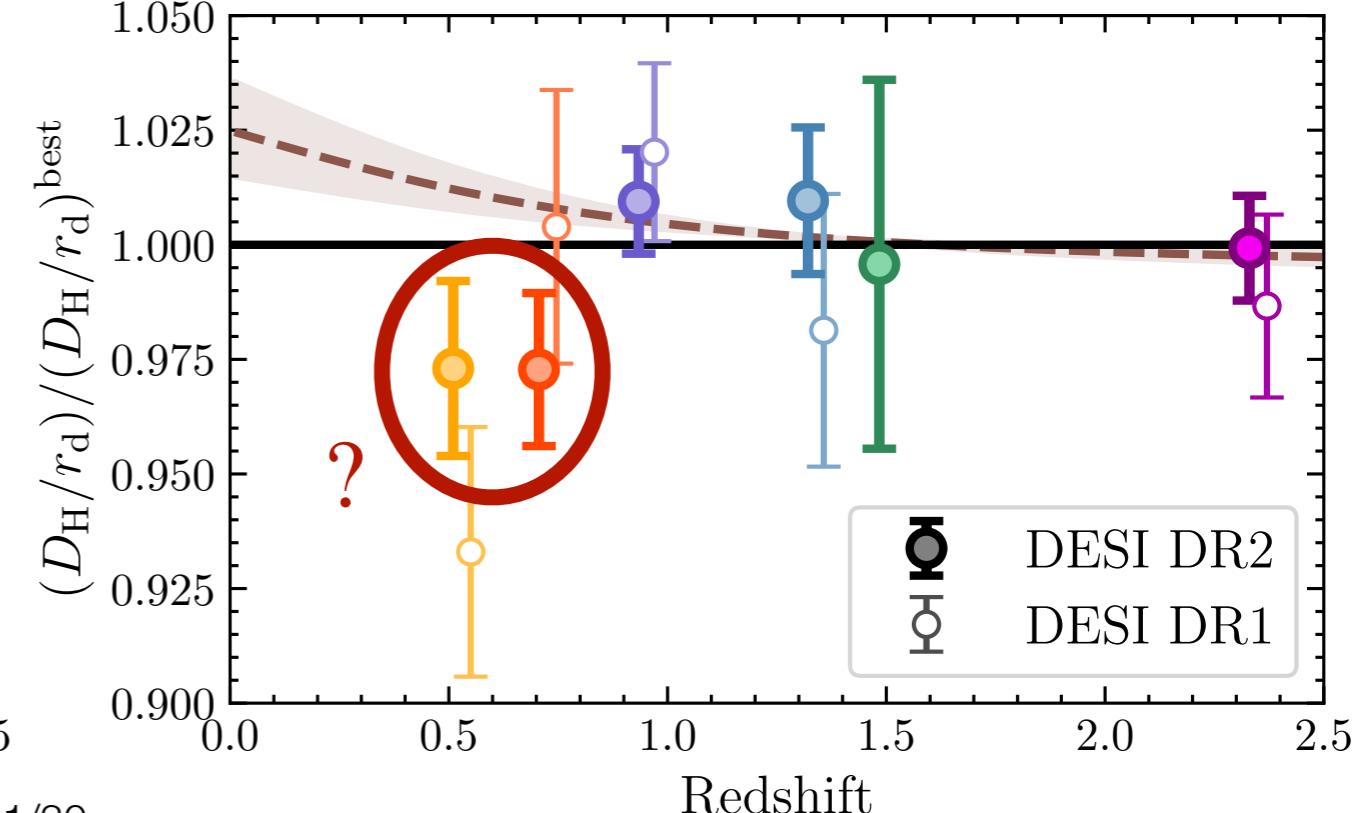
BAO Distance Ratio



Perpendicular BAO Distance



Parallel BAO Distance



# DESI BAO

2503.14738 DESI DR2 Y3 BAO

**DESI BAO seems to indeed imply a phantom-to-quintessence transition to lower redshifts**

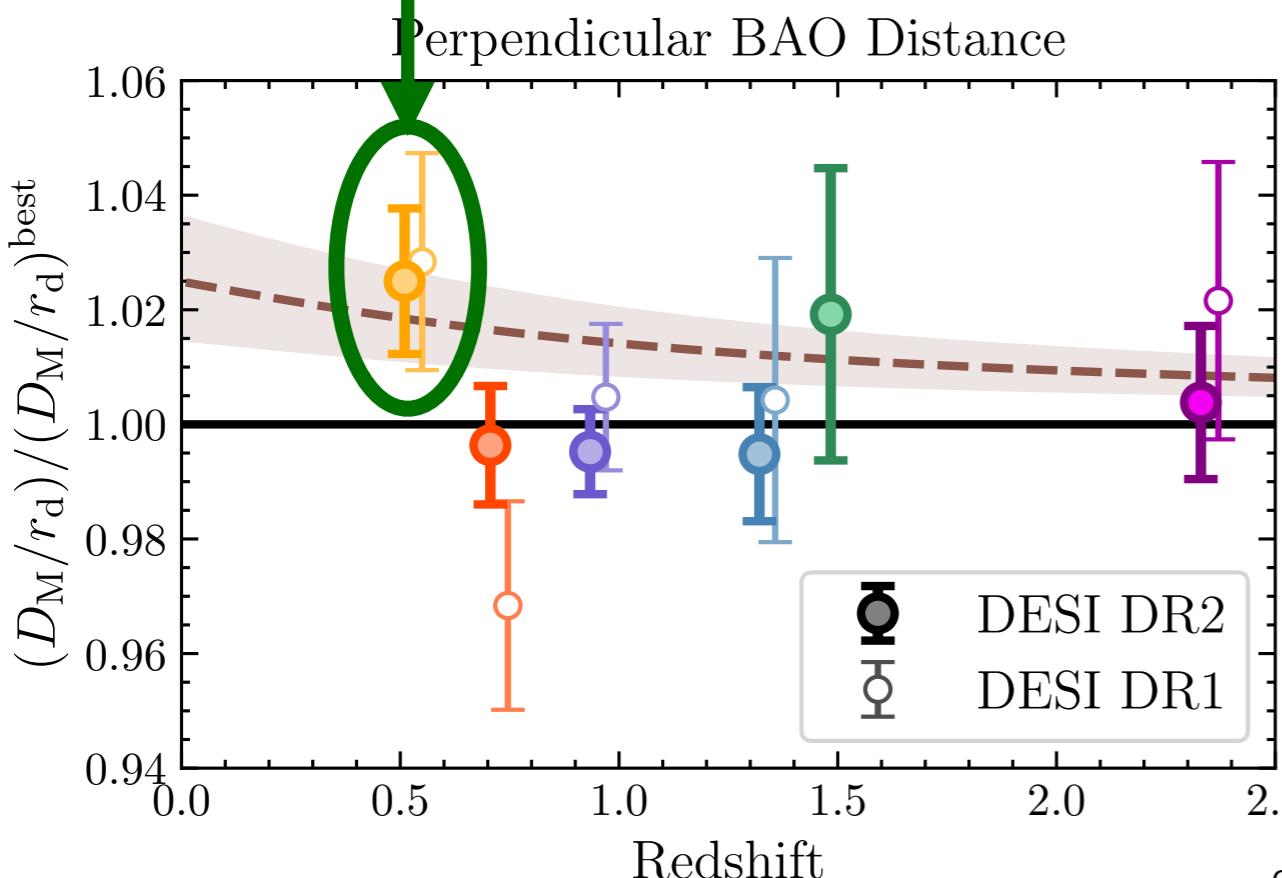
$$D_M(z) = \int_0^{z'} \frac{cdz'}{H(z')}$$

So that the integral of  $D_H(z)$  within

$$D_H(z) = \frac{c}{H(z)}$$

**LRG could be lifted up at low- $z$**

$$D_M^{\text{DESI}}(z_{\text{LRG1}}) > D_M^{\Lambda\text{CDM}}(z_{\text{LRG1}})$$

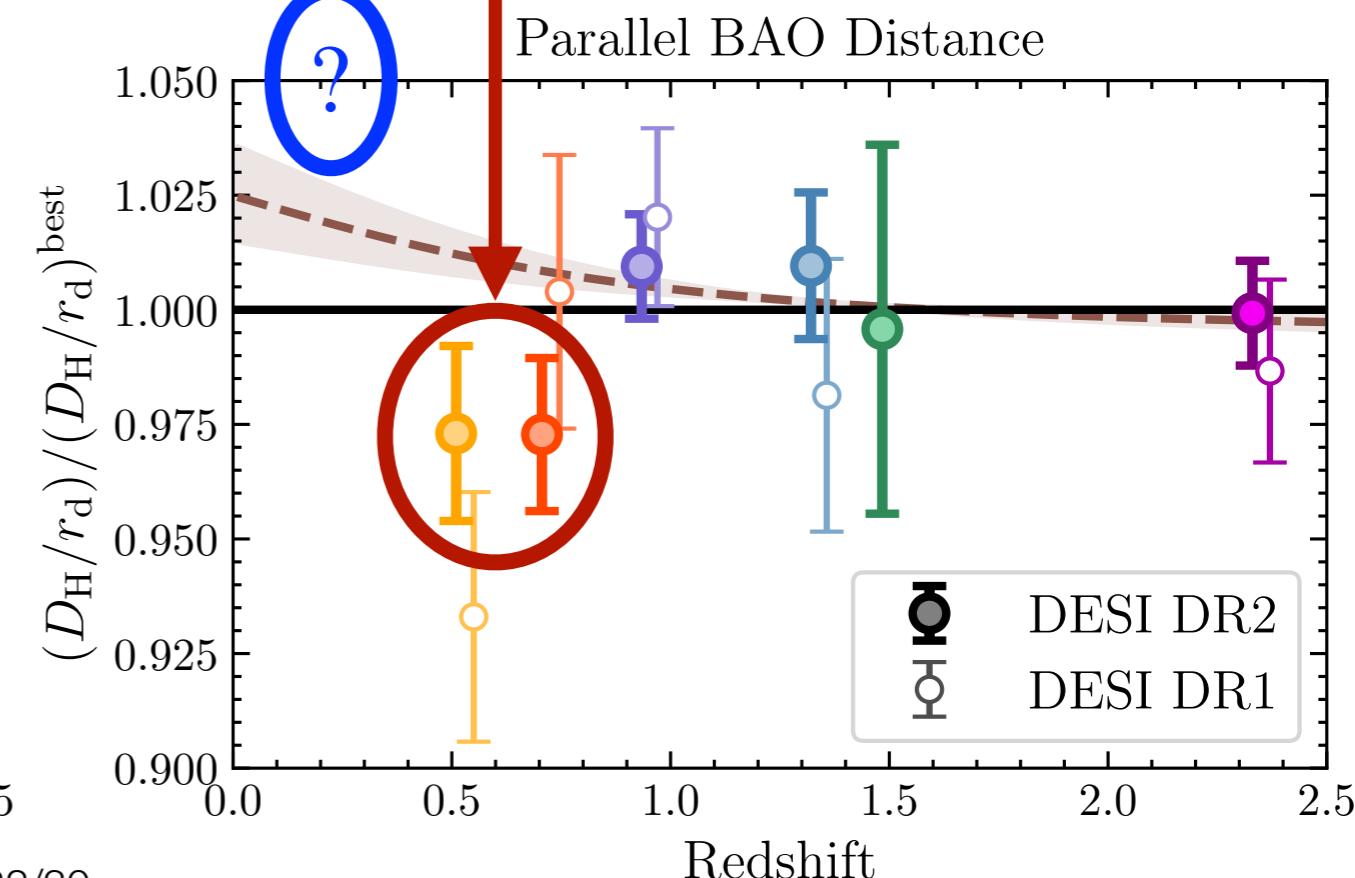


**Quintessential DE at low redshifts**

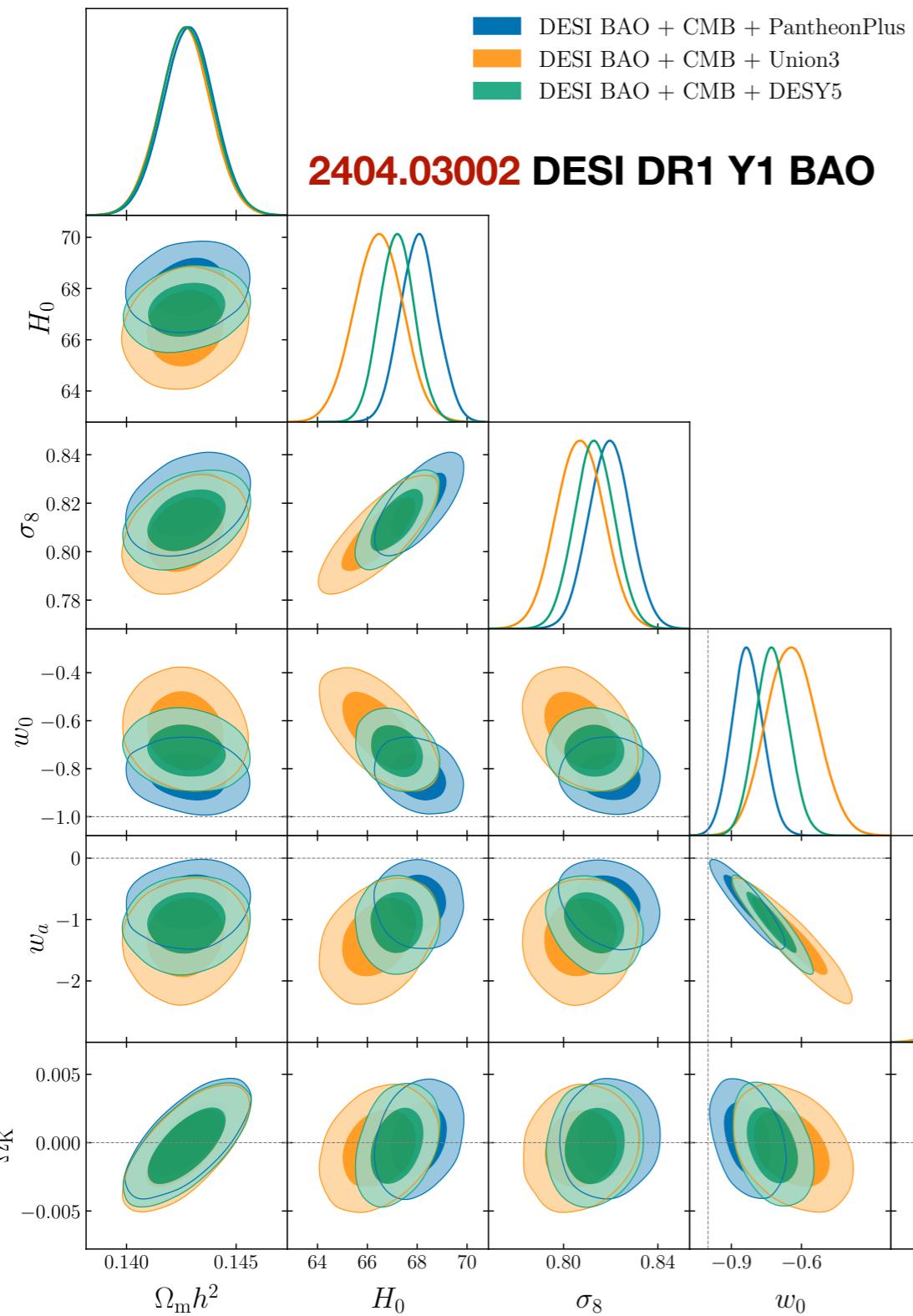
$$D_H^{\text{QDE}}(z_{\text{low}}) > D_H^{\Lambda\text{CDM}}(z_{\text{low}})$$

**Phantom DE at high redshifts**

$$D_H^{\text{PDE}}(z_{\text{high}}) < D_H^{\Lambda\text{CDM}}(z_{\text{high}})$$



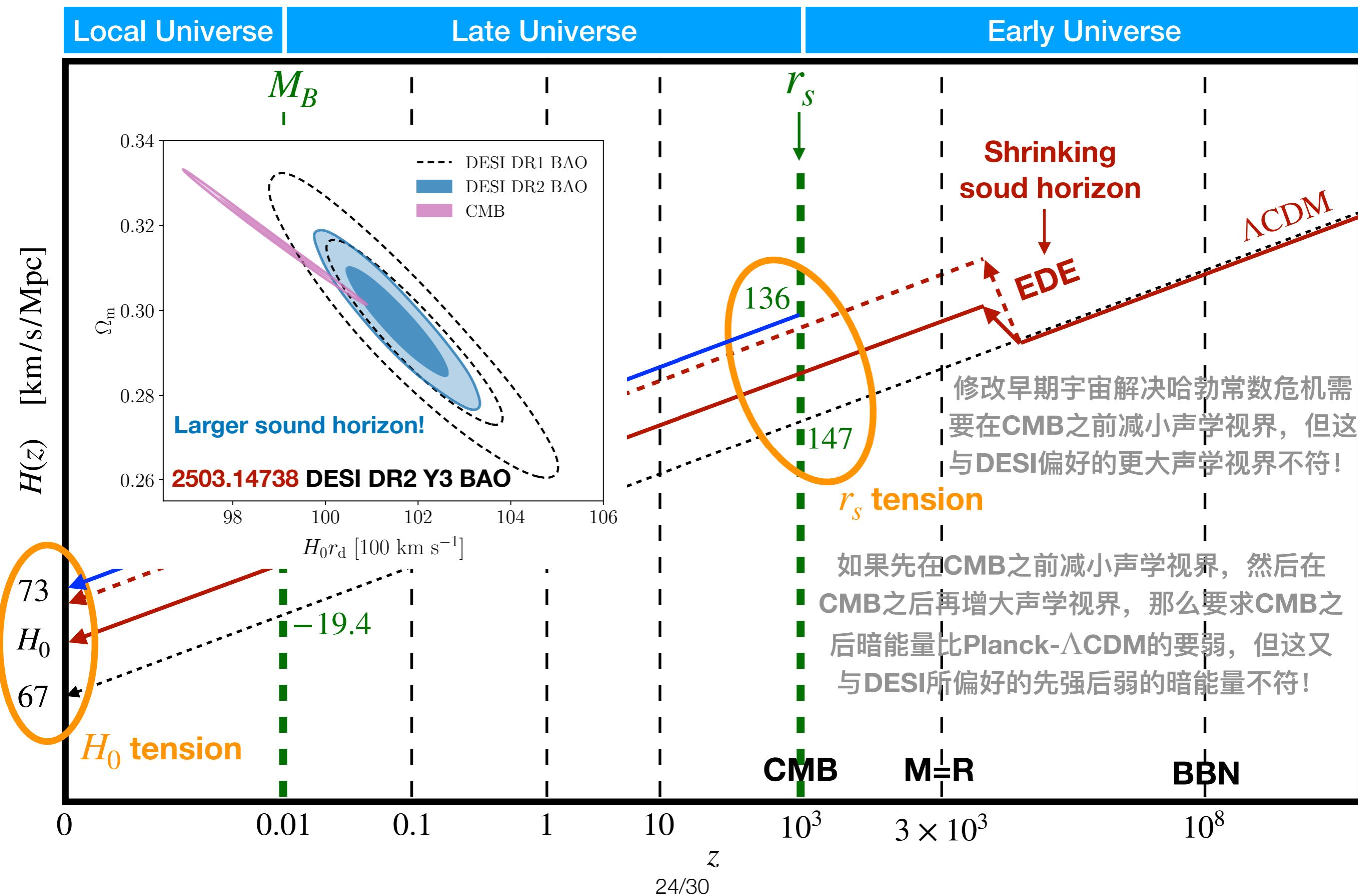
# DESI tension with Hubble tension



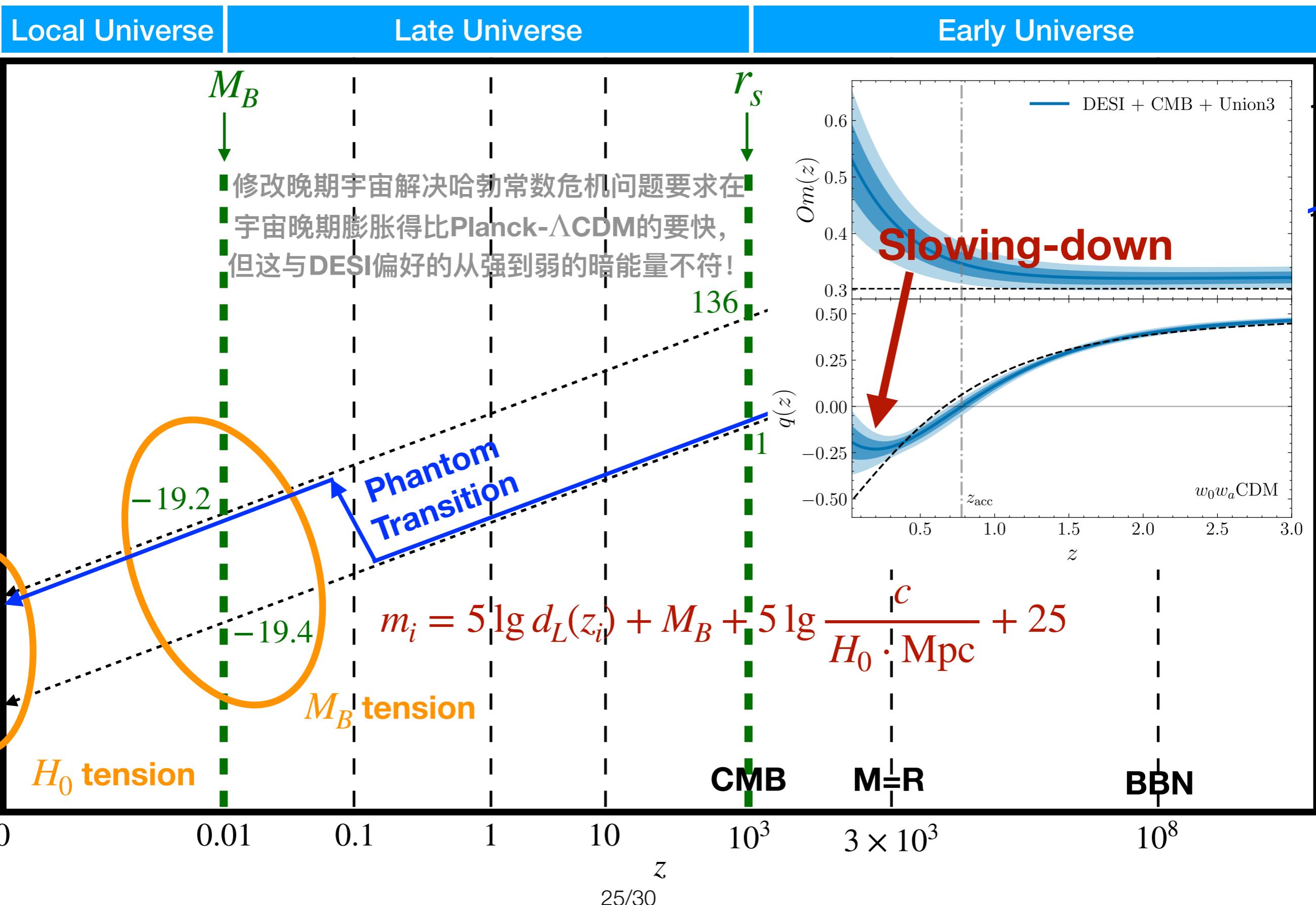
Hubble tension is worsen!

Model/Dataset	$\Omega_m$	$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]
$\Lambda$ CDM <b>2503.14738 DESI DR2 Y3 BAO</b>		
CMB	$0.3169 \pm 0.0065$	$67.14 \pm 0.47$
DESI	$0.2975 \pm 0.0086$	—
DESI+BBN	$0.2977 \pm 0.0086$	$68.51 \pm 0.58$
DESI+BBN+ $\theta_*$	$0.2967 \pm 0.0045$	$68.45 \pm 0.47$
DESI+CMB	$0.3027 \pm 0.0036$	$68.17 \pm 0.28$
$w_0 w_a$ CDM <b>2503.14738 DESI DR2 Y3 BAO</b>		
CMB	$0.220^{+0.019}_{-0.078}$	$83^{+20}_{-6}$
DESI	$0.352^{+0.041}_{-0.018}$	—
DESI+Pantheon+	$0.298^{+0.025}_{-0.011}$	—
DESI+Union3	$0.328^{+0.019}_{-0.014}$	—
DESI+DESY5	$0.319^{+0.017}_{-0.011}$	—
DESI+( $\theta_*, \omega_b, \omega_{bc}$ )CMB	$0.353 \pm 0.022$	$63.7^{+1.7}_{-2.2}$
DESI+CMB (no lensing)	$0.352 \pm 0.021$	$63.7^{+1.7}_{-2.1}$
DESI+CMB	$0.353 \pm 0.021$	$63.6^{+1.6}_{-2.1}$
DESI+CMB+Pantheon+	$0.3114 \pm 0.0057$	$67.51 \pm 0.59$
DESI+CMB+Union3	$0.3275 \pm 0.0086$	$65.91 \pm 0.84$
DESI+CMB+DESY5	$0.3191 \pm 0.0056$	$66.74 \pm 0.56$
DESI+DESY3 (3×2pt)+Pantheon+	$0.3140 \pm 0.0091$	—
DESI+DESY3 (3×2pt)+Union3	$0.333 \pm 0.012$	—
DESI+DESY3 (3×2pt)+DESY5	$0.3239 \pm 0.0092$	—

# DESI tension with early Hubble solutions



# DESI tension with late Hubble solutions

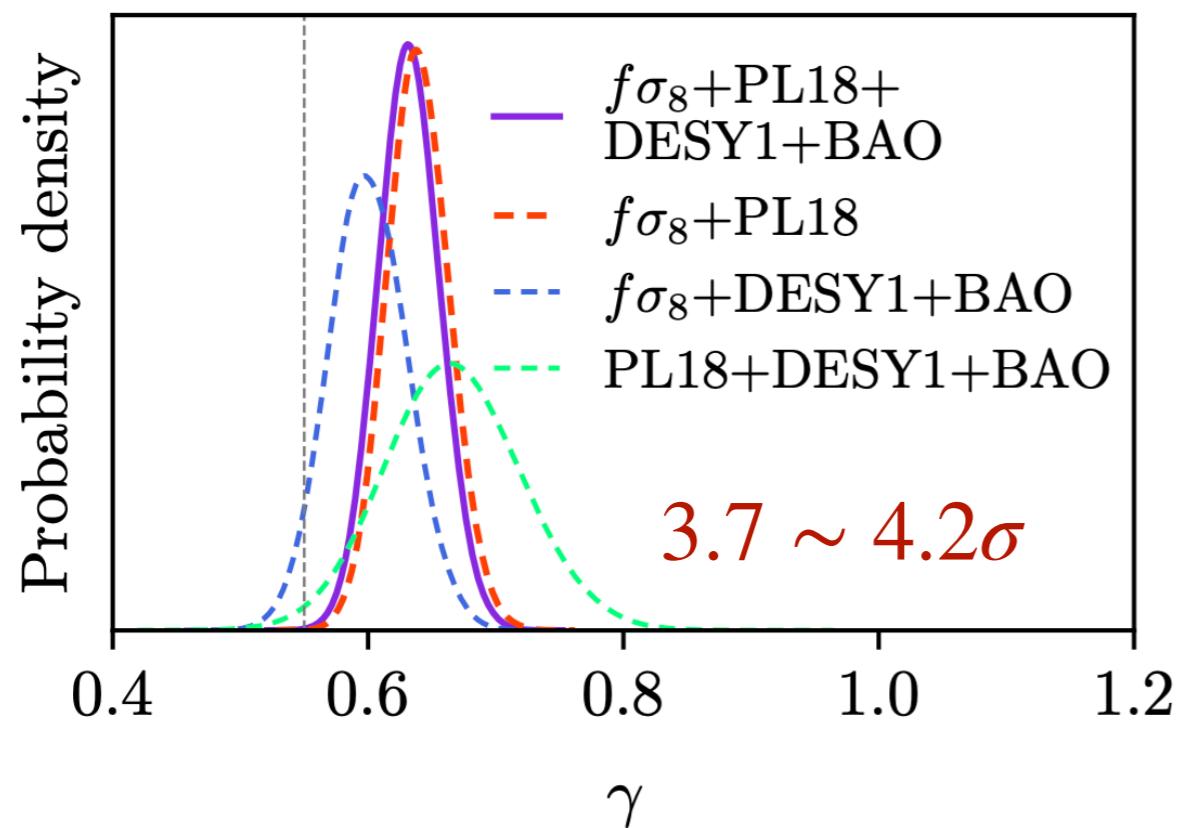


# DESI tension with $\gamma$ tension

2302.01331 (PRL) growth index tension

GR + linear  $\delta \equiv \frac{\rho - \bar{\rho}}{\rho} \ll 1$  regime

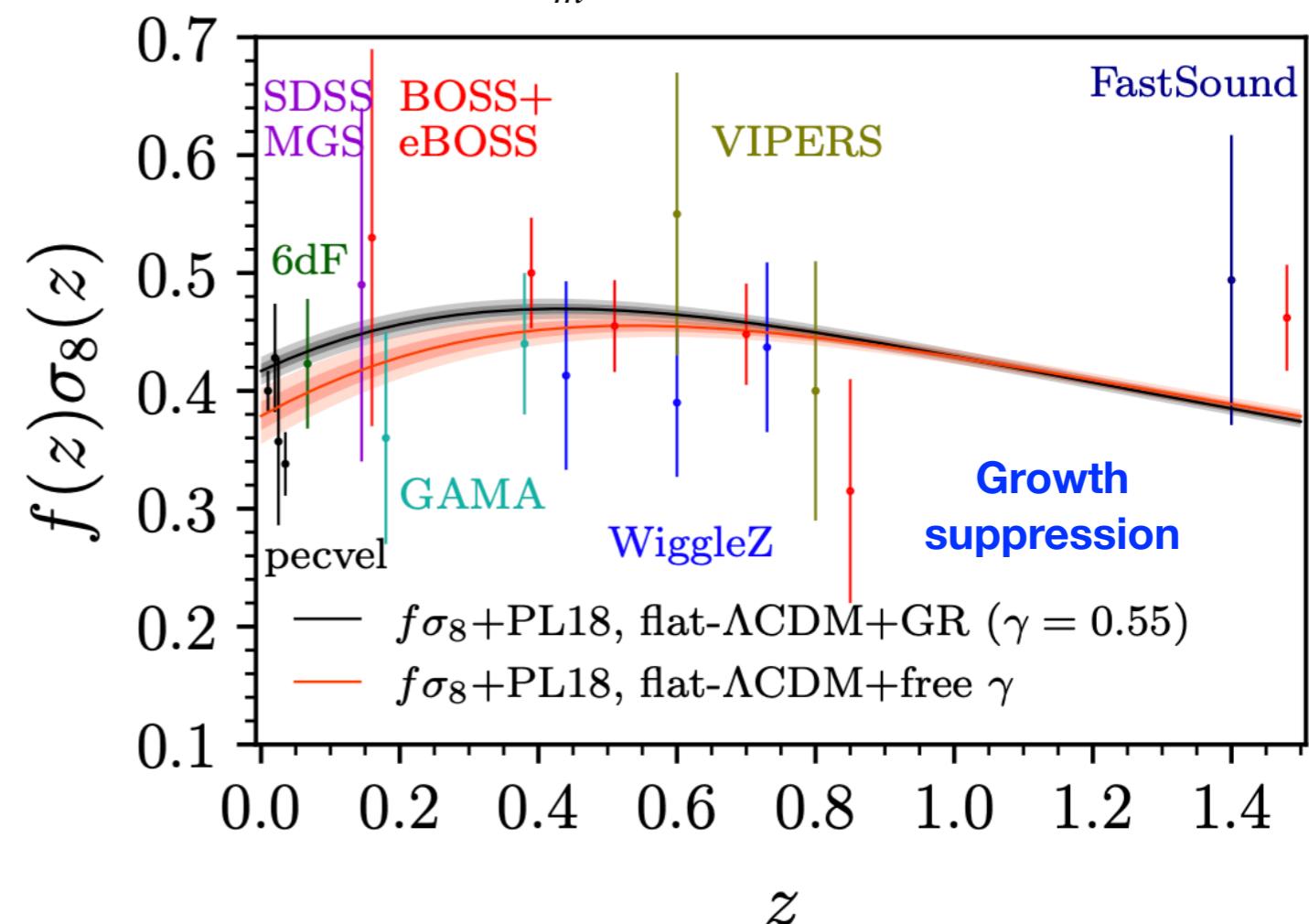
$0.0003h/\text{Mpc} \simeq H_0 \lesssim k \lesssim 0.1h/\text{Mpc}$



$$\ddot{\delta}(\mathbf{k}, t) + 2H\dot{\delta}(\mathbf{k}, t) - 4\pi G\bar{\rho}\delta(\mathbf{k}, t) = 0$$

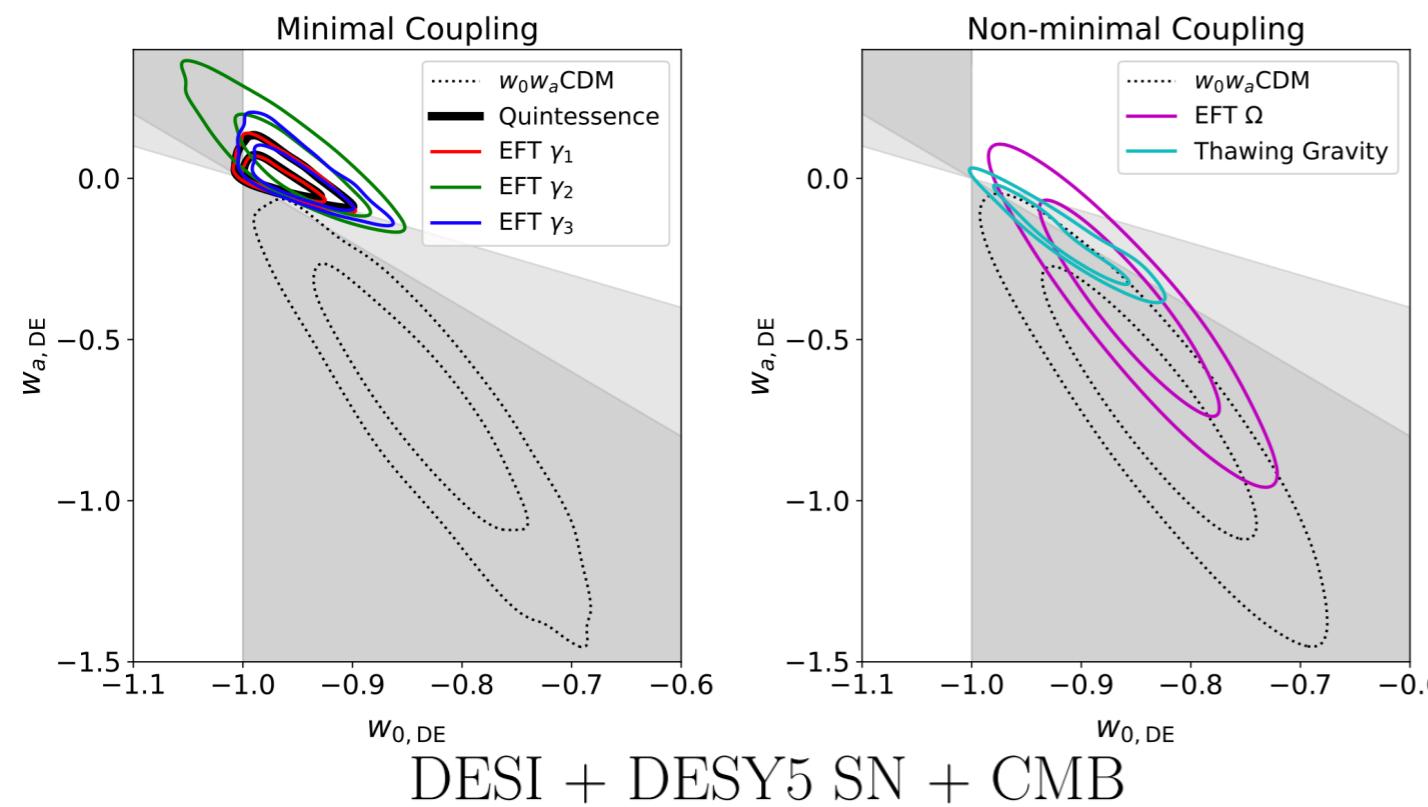
$$D(t) \equiv \frac{\delta(t)}{\delta(t_0)}, \quad f(a) \equiv \frac{d \ln D(a)}{d \ln a}$$

$$f(a) = \Omega_m^\gamma(a), \quad \gamma \approx 0.55, \quad \text{flat } \Lambda\text{CDM}$$



Since the Hubble expansion suppresses the matter perturbation growth, a weakening DE compared to the cosmological constant will less suppress matter perturbation growth, leading to faster growth than  $\Lambda\text{CDM}$

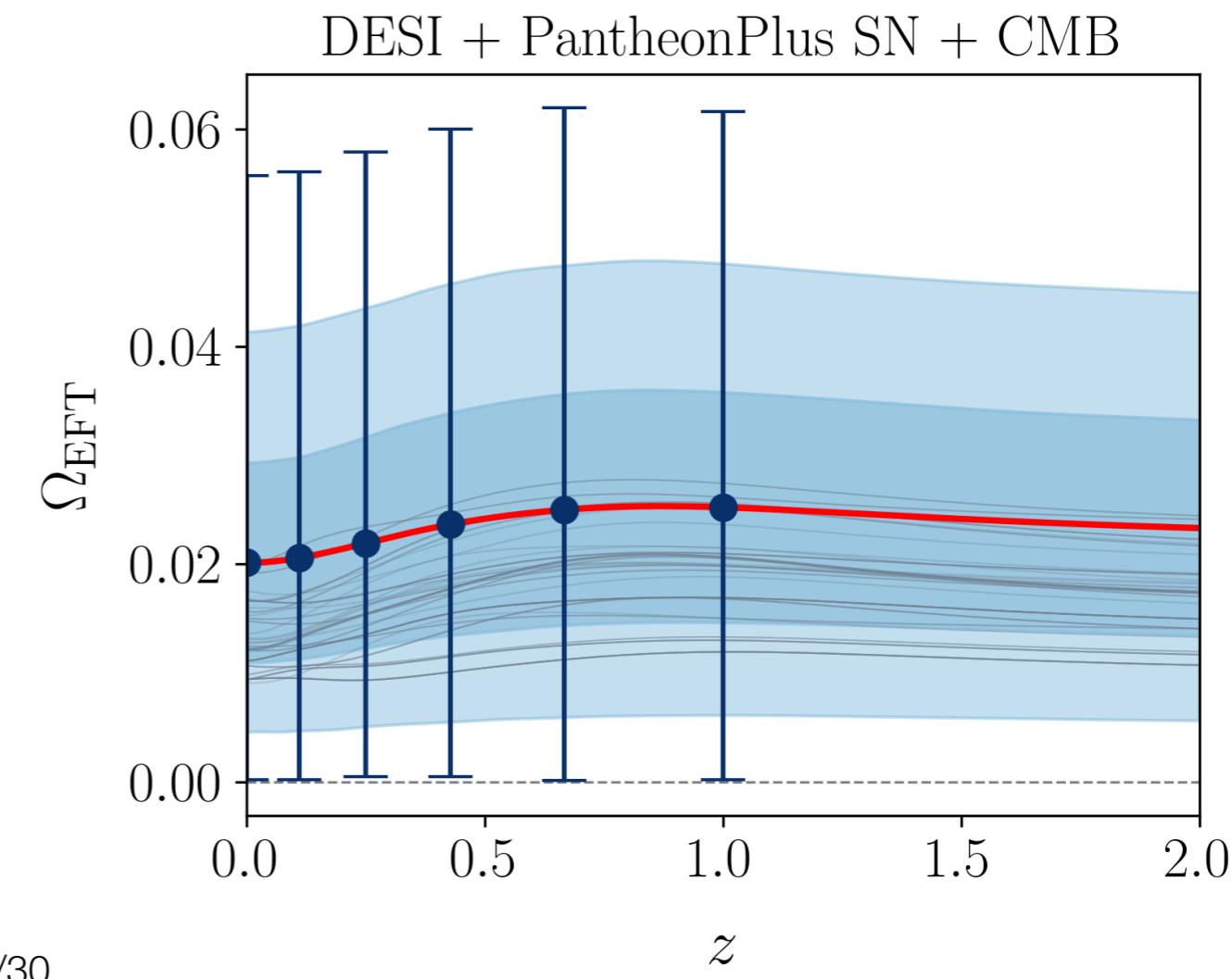
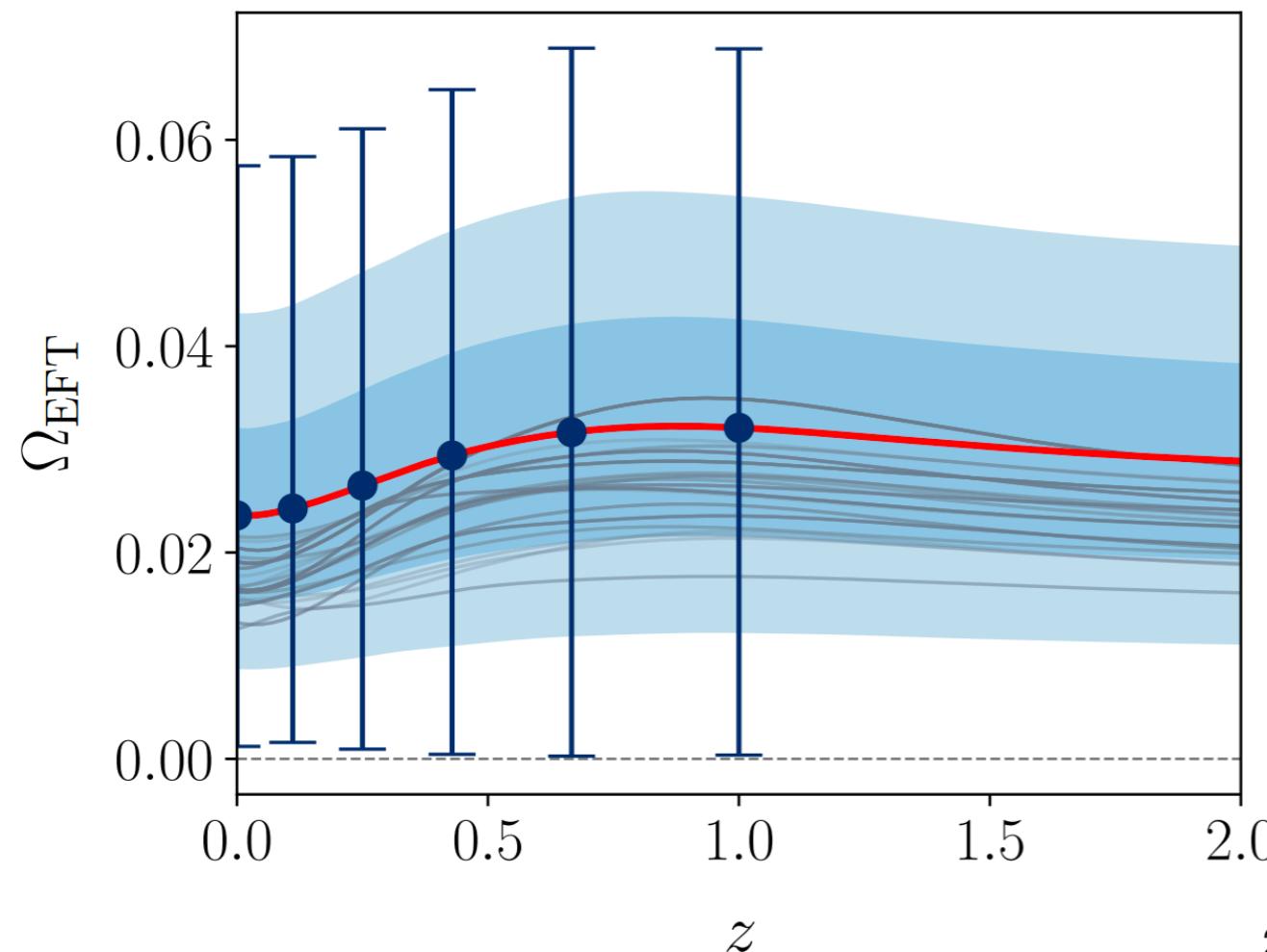
# Non-minimal coupling



2407.15832 Gen Ye, Matteo Martinelli, Bin Hu, Alessandra Silvestri, "Non-minimally coupled gravity as a physically viable fit to DESI 2024 BAO" PRL 134 (2025) 181002

均偏好一个非最小耦合的引力

2503.19898 Jiaming Pan, Gen Ye, "Non-minimally coupled gravity constraints from DESI DR2 data"



# Non-minimal coupling

$$S = \int d^4x \sqrt{-g} \left[ \frac{M_{\text{Pl}}^2}{2}(R - 2\Lambda) - \frac{1}{2}g^{\mu\nu}\nabla_\mu\phi\nabla_\nu\phi - V(\phi) + \mathcal{L}_{\text{SM}}[g_{\mu\nu}, \psi_{\text{SM}}] \right] + \int d^4x \sqrt{-\tilde{g}} \mathcal{L}_{\text{DM}}[\tilde{g}_{\mu\nu} \equiv \Omega(\phi)^2 g_{\mu\nu}, \psi_{\text{DM}}]$$

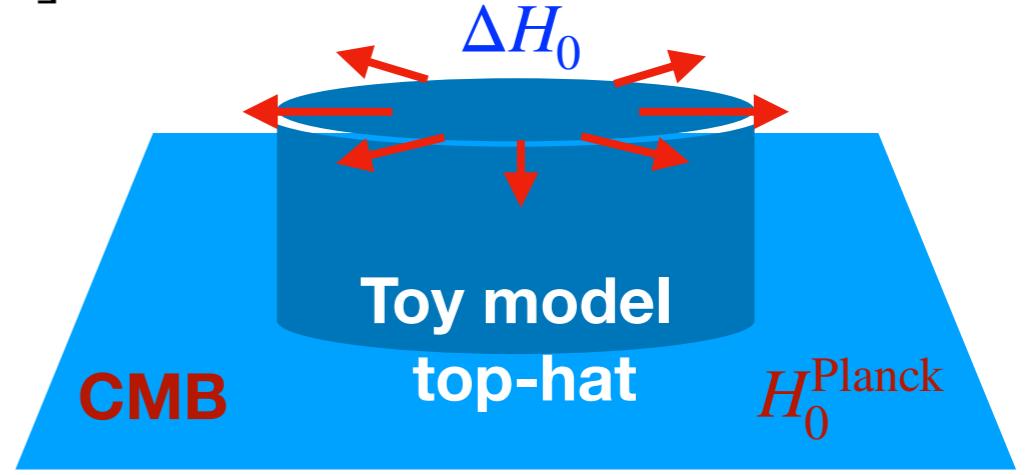
**Effective potential**      **Peebles-Ratra potential**

$$V_{\text{eff}}(\phi) = V(\phi) + \Omega(\phi)\hat{\rho}_m \quad \text{Matter density}$$

**Chameleon**

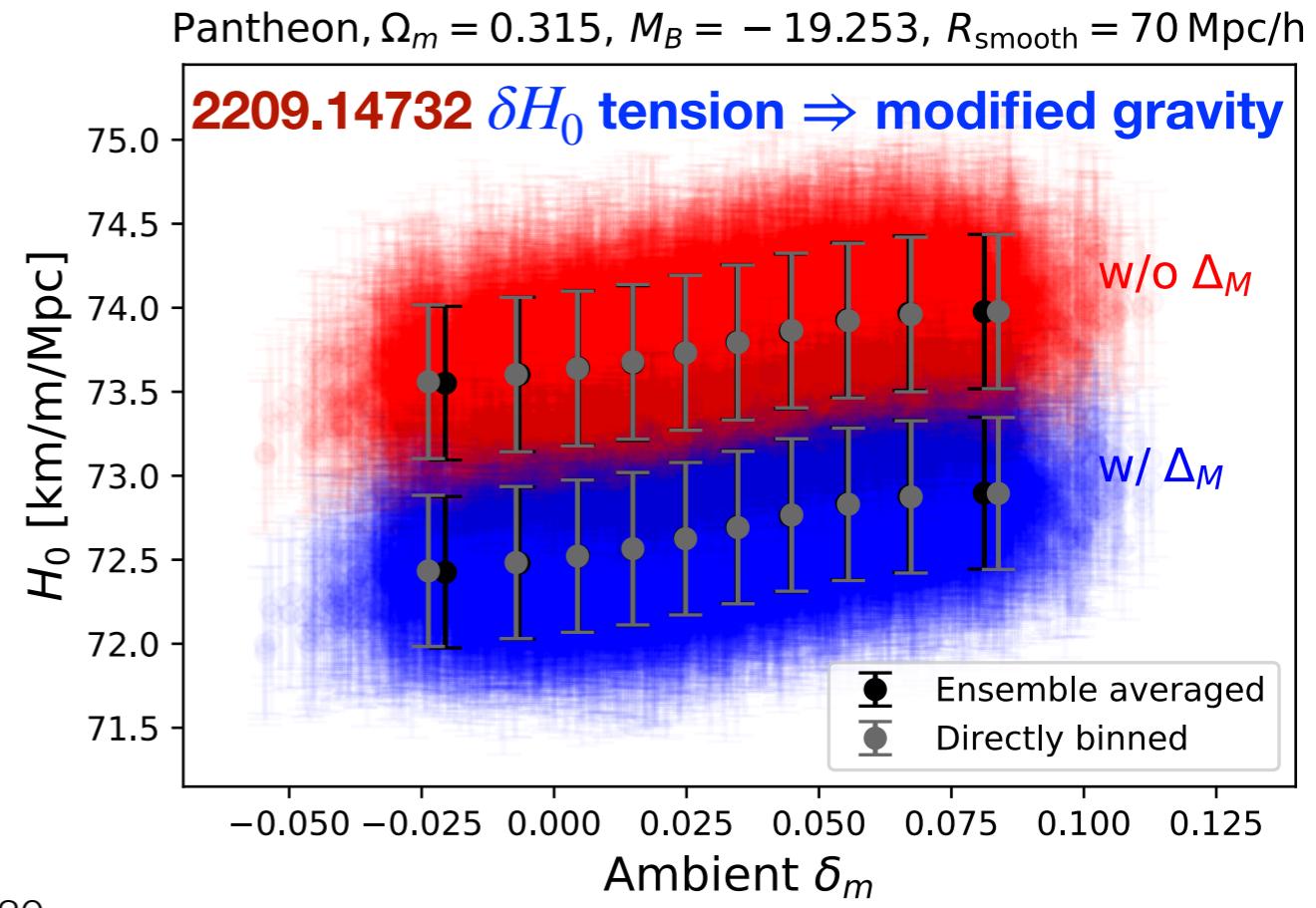
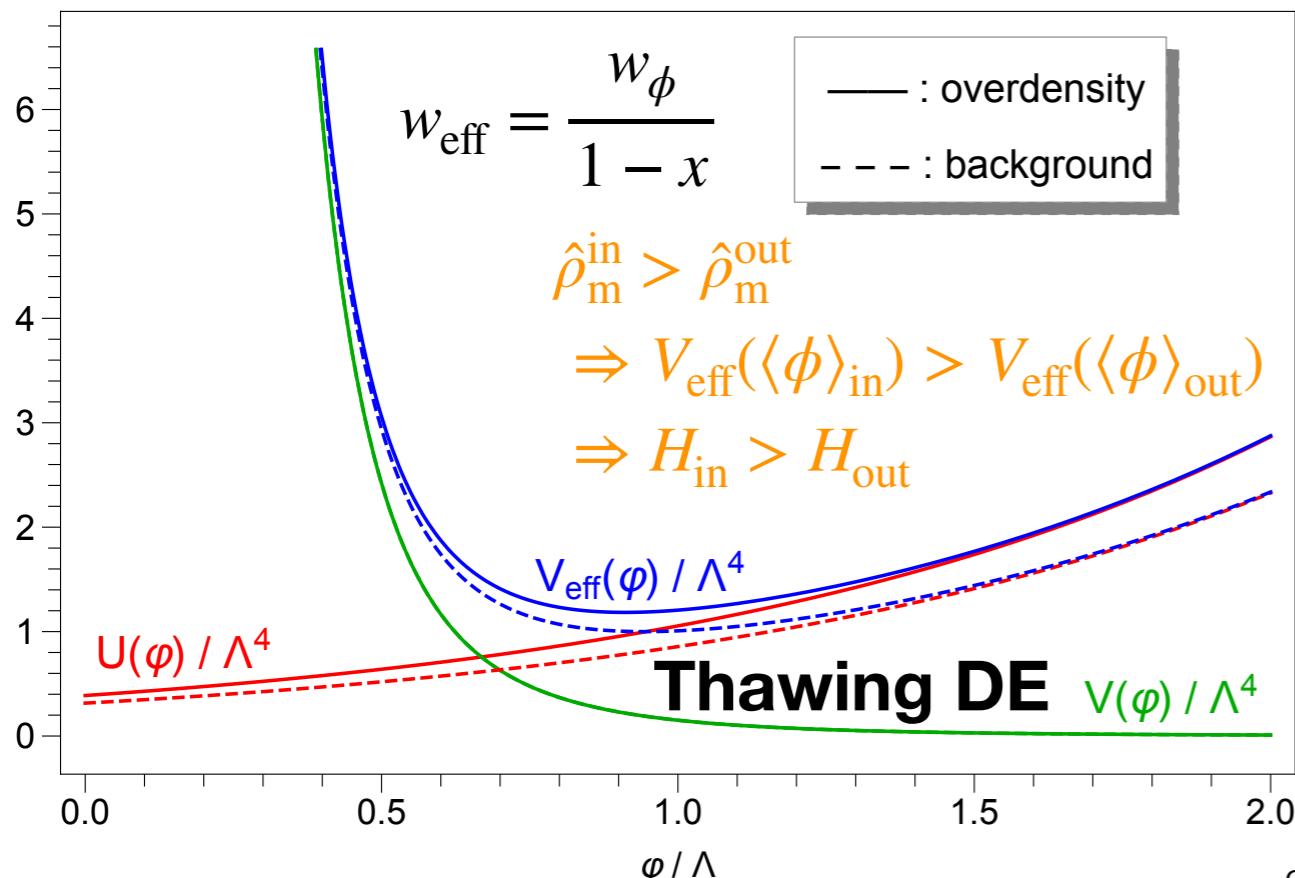
$$\Omega(\phi) = \exp\left(\frac{\phi}{\Lambda}\right)$$

$$V(\phi) = \alpha\Lambda^4 \left(\frac{\Lambda}{\phi}\right)^n$$



**Cai, Guo, Li, SJW, Yu (PRD Letter 2021)**

**Effective cosmological constant**  $V_{\text{eff}}(\langle\phi\rangle)$



# Conclusions and discussions



It is indeed the critical time from  $\Lambda$ CDM to something different

$\left\{ \begin{array}{l} \text{MG/DDE: crossing?} \\ \text{MG&DDE: thawing?} \end{array} \right.$



What DESI BAO really want to tell us is the disagreement with Planck-CMB on  $\Omega_m$  if  $\Lambda$ CDM is assumed

Whatever left can be interpreted diversely, e.g. MG /& DDE, but the crossing crucially depends on low-z SNe

Phenomenological?



DESI DDE is not only in tension with  $H_0$  tension (in tension with both early/late solutions to  $H_0$  tension)  
but also the way out of it has already ruled out its preferred phantom crossing from  $w_{\text{DE}} < -1$  to  $w_{\text{DE}} > -1$



DESI DDE is not only in tension with  $H_0$  tension but also in tension with  $S_8$  tension,  $\gamma$  tension, and  $\delta H_0$  tension

The beyond- $\Lambda$ CDM new physics might be thawing dark energy from modified gravity with coupling to matter



Such a non-minimal coupling of scalar field to gravity might be naturally motivated from UV completed theory, e.g. modular field from string compactifications and 2007.04396

Thank you

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