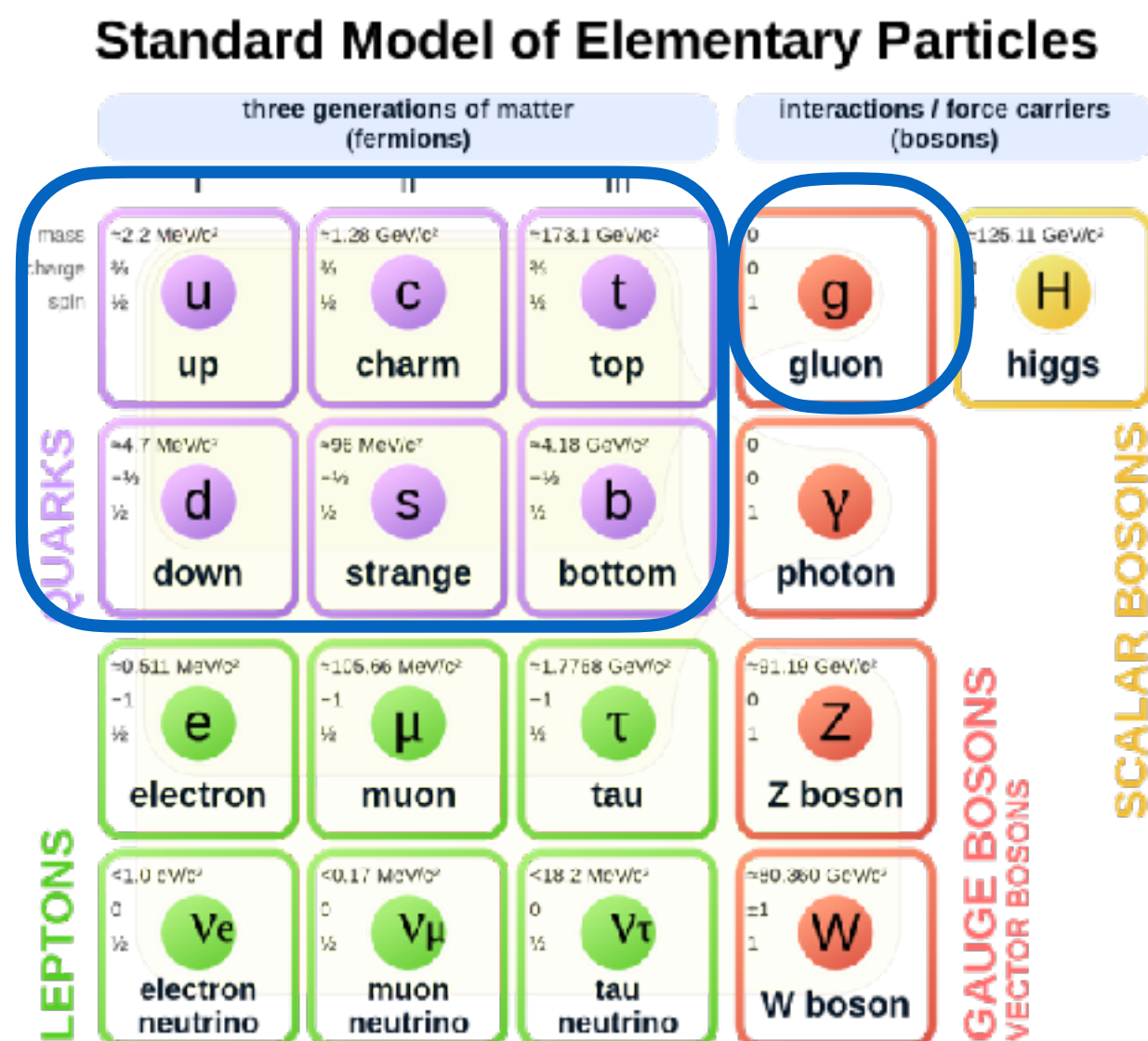


Discovery of a Glueball-like Particle $X(2370)$ @ BESIII

Yanping Huang

Institute of High Energy Physics, CAS

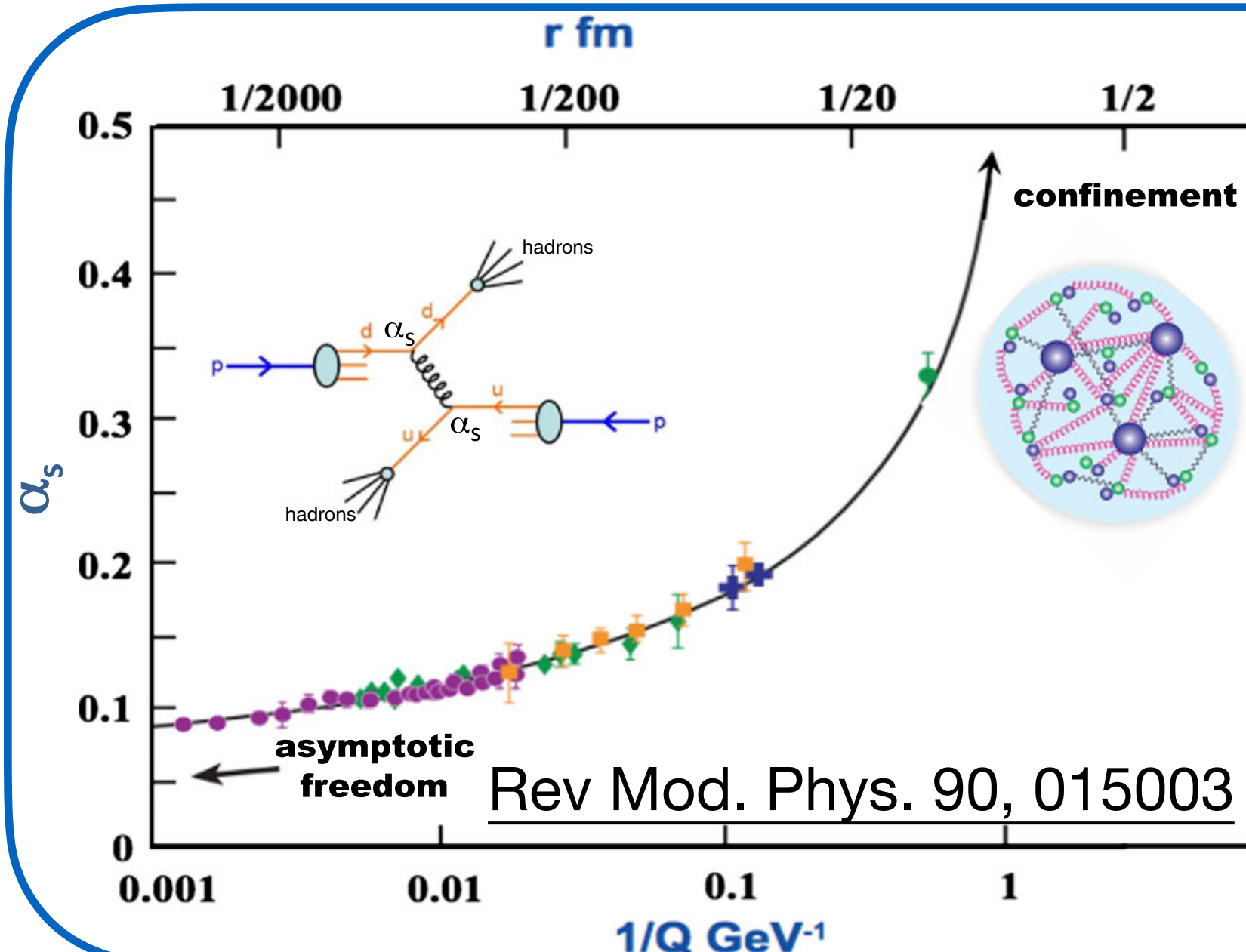
Fundamental Structure of Matters



◎ SM well describes fundamental structure of Matters, including EW and strong interactions

- **Gluons mediate strong interactions**
- **QCD (SU(3) non-Abel gauge theory) is the basic theory for strong interaction**

◎ Hadron spectroscopy can provide us clues for the understanding of fundamental structure via the hadron property study



QCD predictions

♦ High Energy:

- α_s running, widely confirmed experimentally (Nobel Prize 2004)

♦ Low Energy:

- Self-interaction of gluons → **Glueballs**

Glueballs

◆ **Special Importance of Glueballs:** **Glueballs to QCD** is just as important as **Higgs Boson to EW**

- ◆ Unique particle made of **pure force** (bosons)
- ◆ Direct proof of **self-interactions of gluons** — Direct proof of **non-Abel gauge interactions of QCD**
- ◆ Direct proof of **origin of mass** from strong interactions

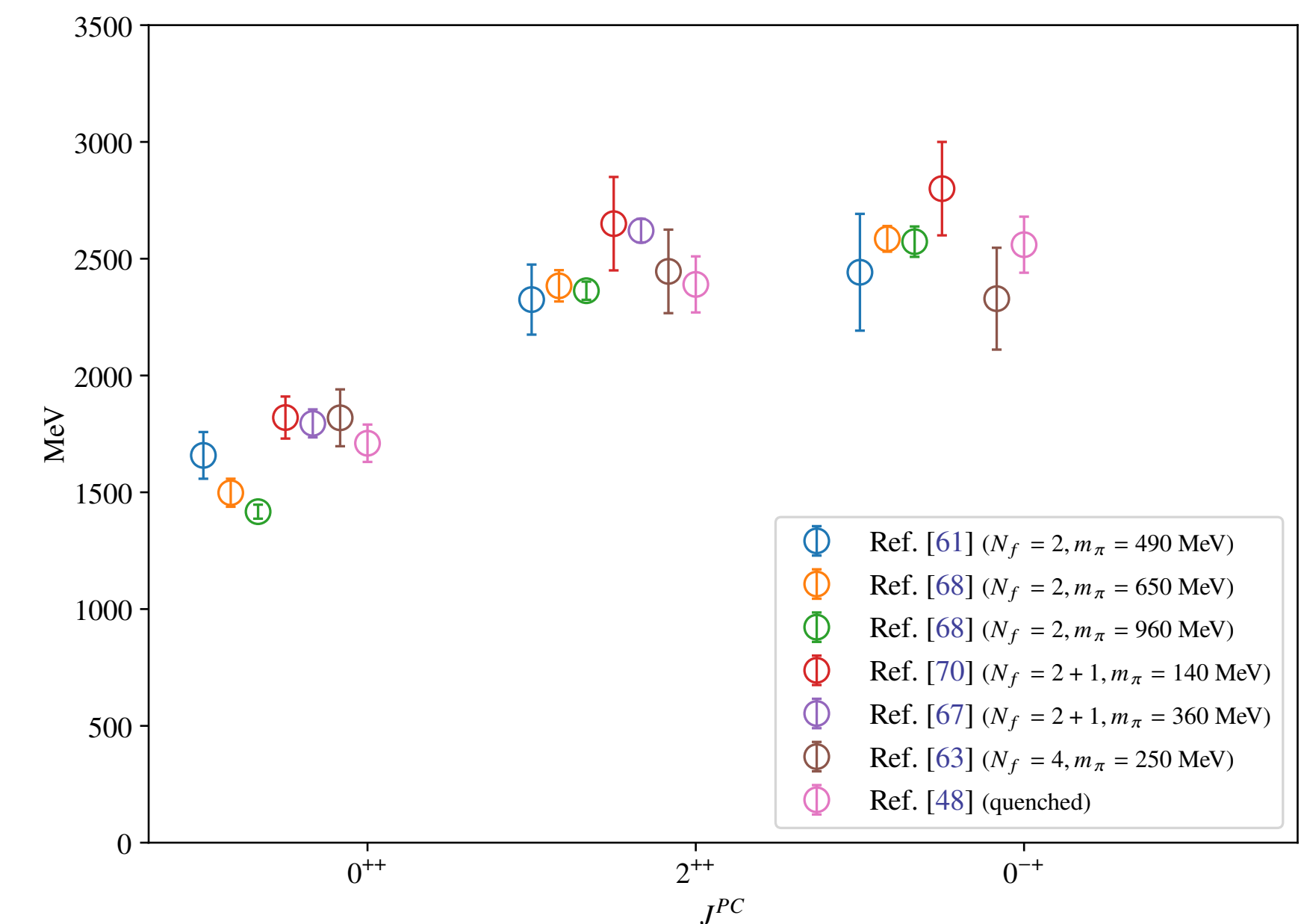
◆ **Lattice QCD** (LQCD) is a non-perturbative method from the first principles in theory.

◆ **Different lattice QCD groups** (including lattice simulations with dynamical quarks)

- ◆ Predictions on **masses and production rates** of pure glueballs
- ◆ Consistent results and expected to be reliable.

◆ **Lattice QCD predictions on glueball masses:**

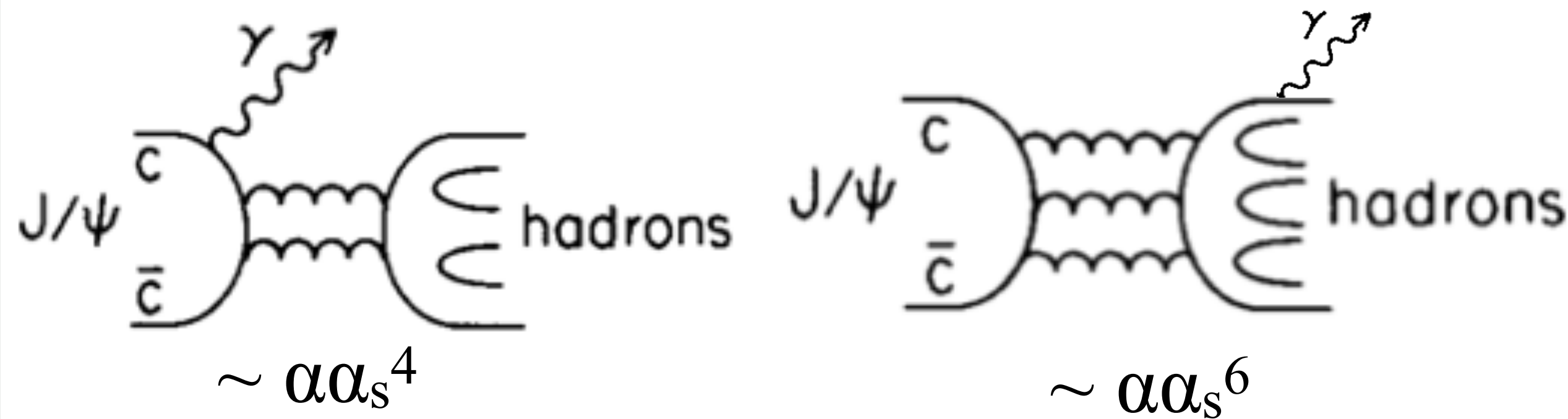
- ◆ **0^{++} ground state:** 1.5 - 1.7 GeV/c²
- ◆ **2^{++} ground state:** 2.3 - 2.4 GeV/c²
- ◆ **0^{-+} ground state:** 2.3 - 2.6 GeV/c²



arxiv:2305.04869

Glueball production in J/ψ Radiative decay

◆ Gluon rich environment



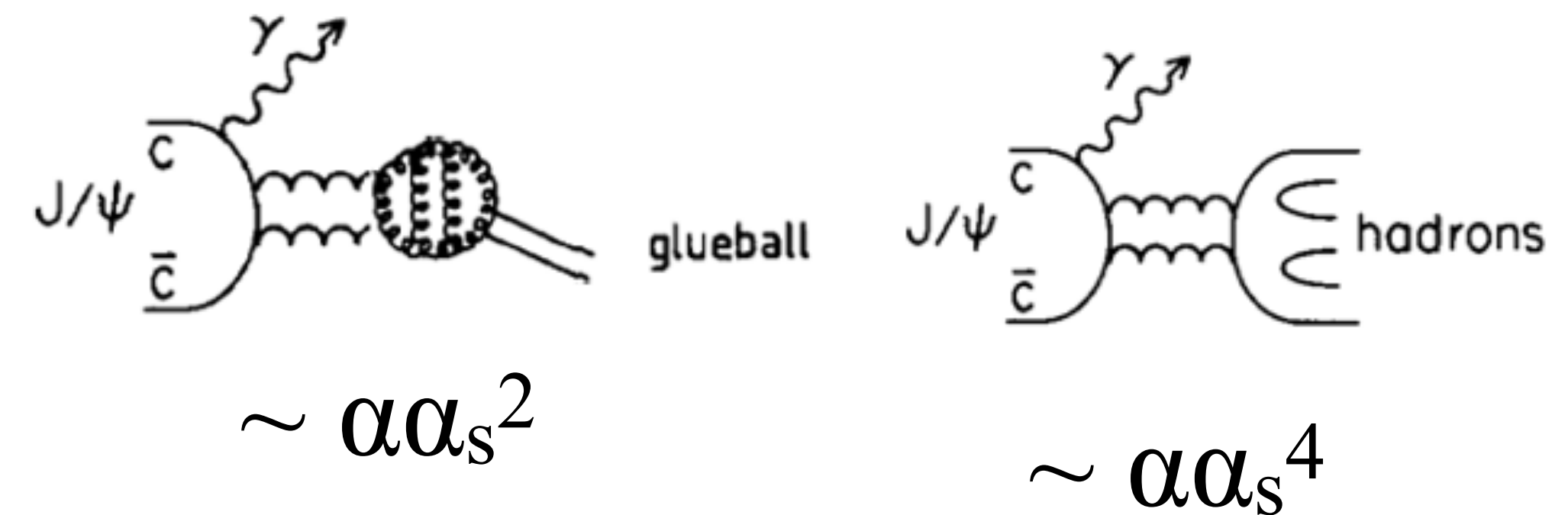
◆ **Isospin filter:** final states dominated by $I=0$ processes

◆ **Spin-parity filter:** C parity must be +, so $J^{PC}=0^{-+}, 0^{++}, 1^{++}, 2^{++}, 2^{-+} \dots$

◆ **Clean environment** in e^+e^- collision: very different from **p-p collision**

◆ Rich glueball production in J/ψ radiative decays:

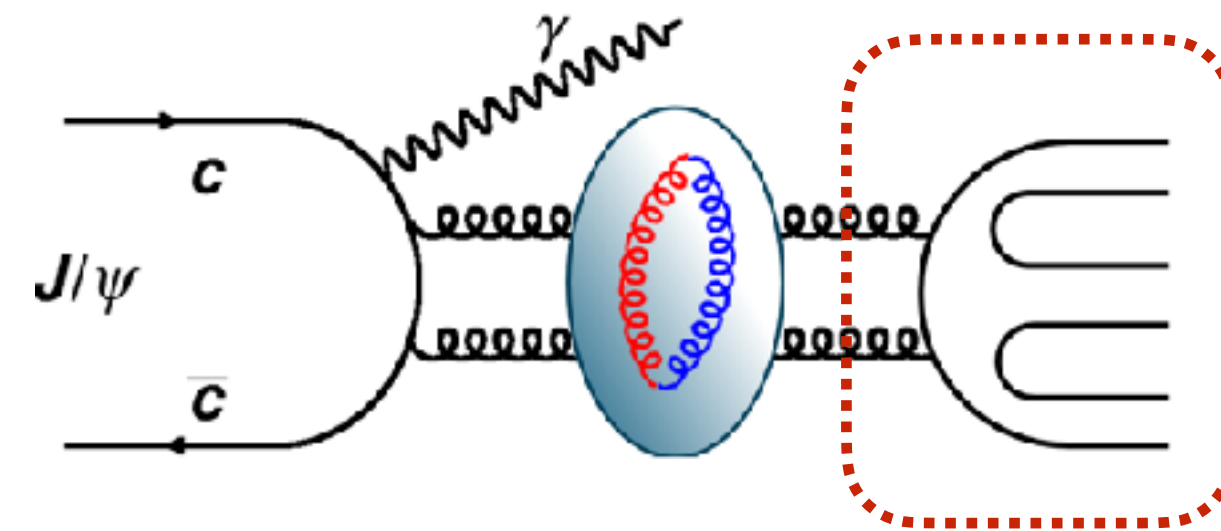
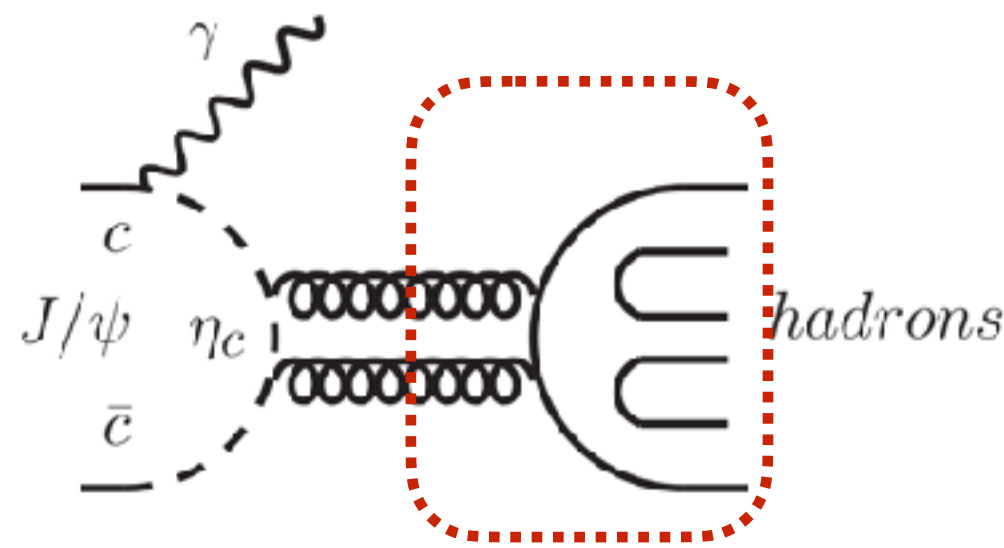
◆ **Glueball production rate** in J/ψ radiative decays could be **higher** than normal hadrons



➡ **J/ψ Radiative decay is an ideal place to search for glueballs**

Glueball Decays

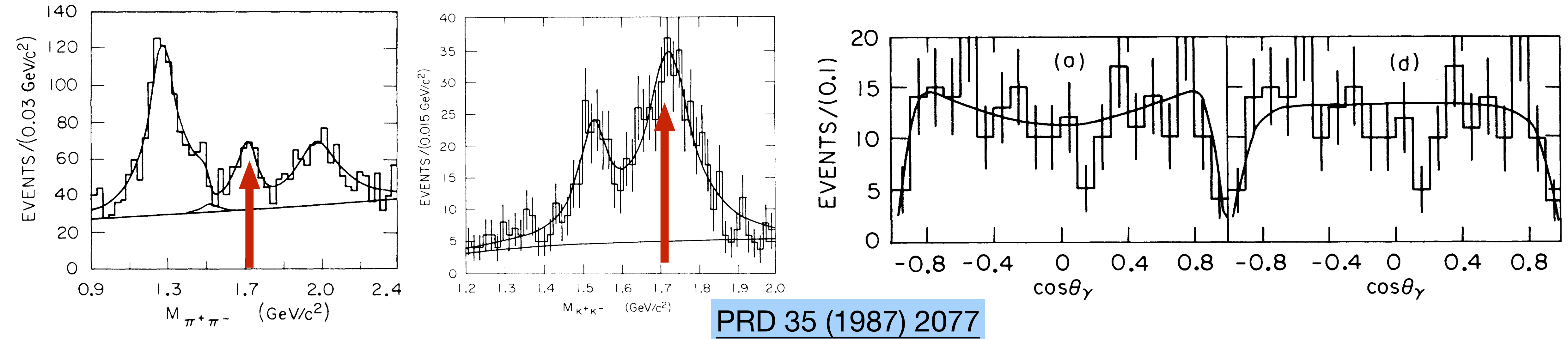
- ◆ **Flavor symmetric decays**
- ◆ **No rigorous predictions on decay patterns and their branching ratios**
- ◆ The glueball decays could be the analogy to **Charmonium decays** since they all decay via gluons (OZI suppression) [PLB 380 189(1996), Commu. Theor. Phys. 23.373 (1995)]
 - ◆ e.g. the 0^{-+} glueball could have similar decays of η_c



Historical Glueball Candidates

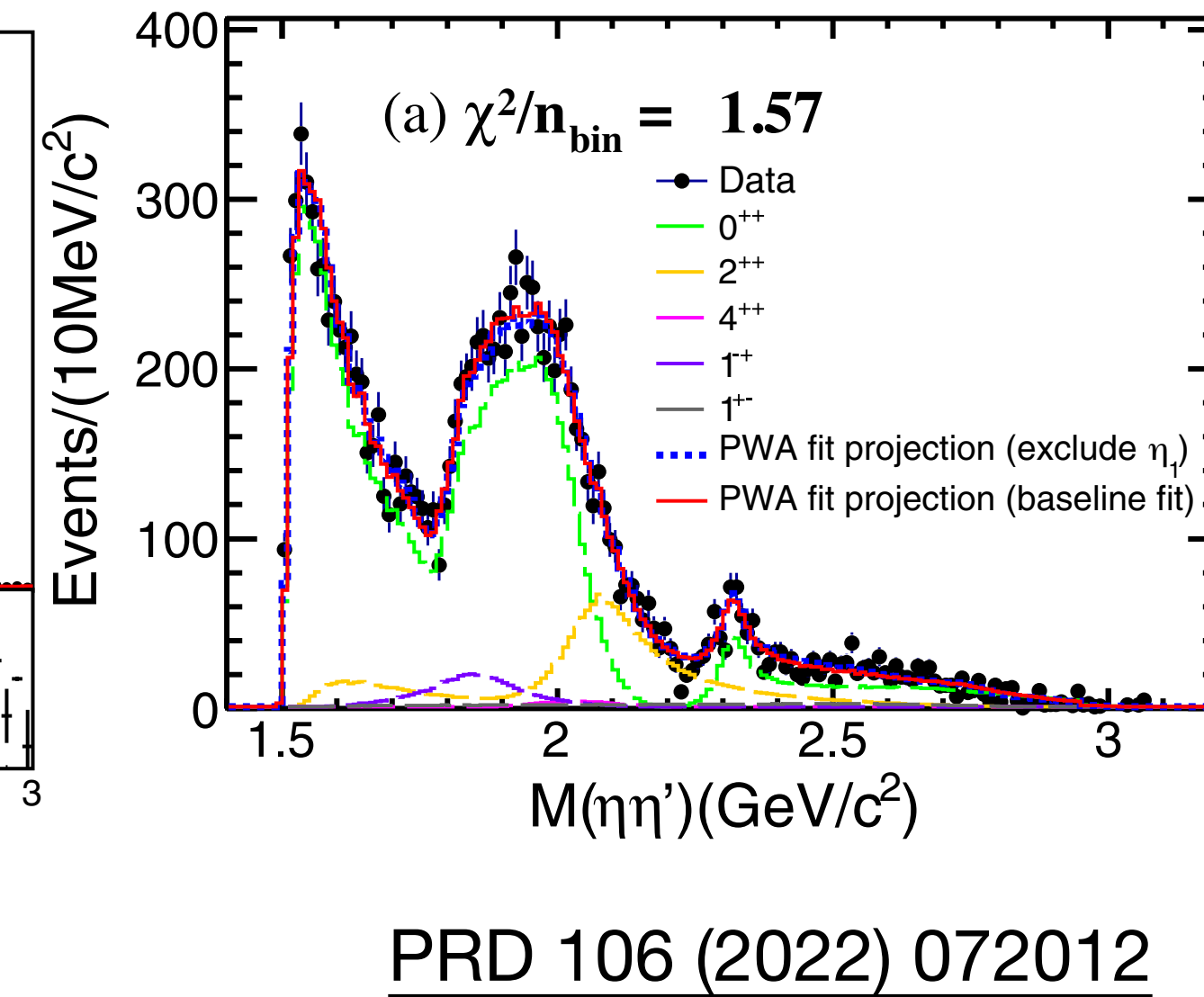
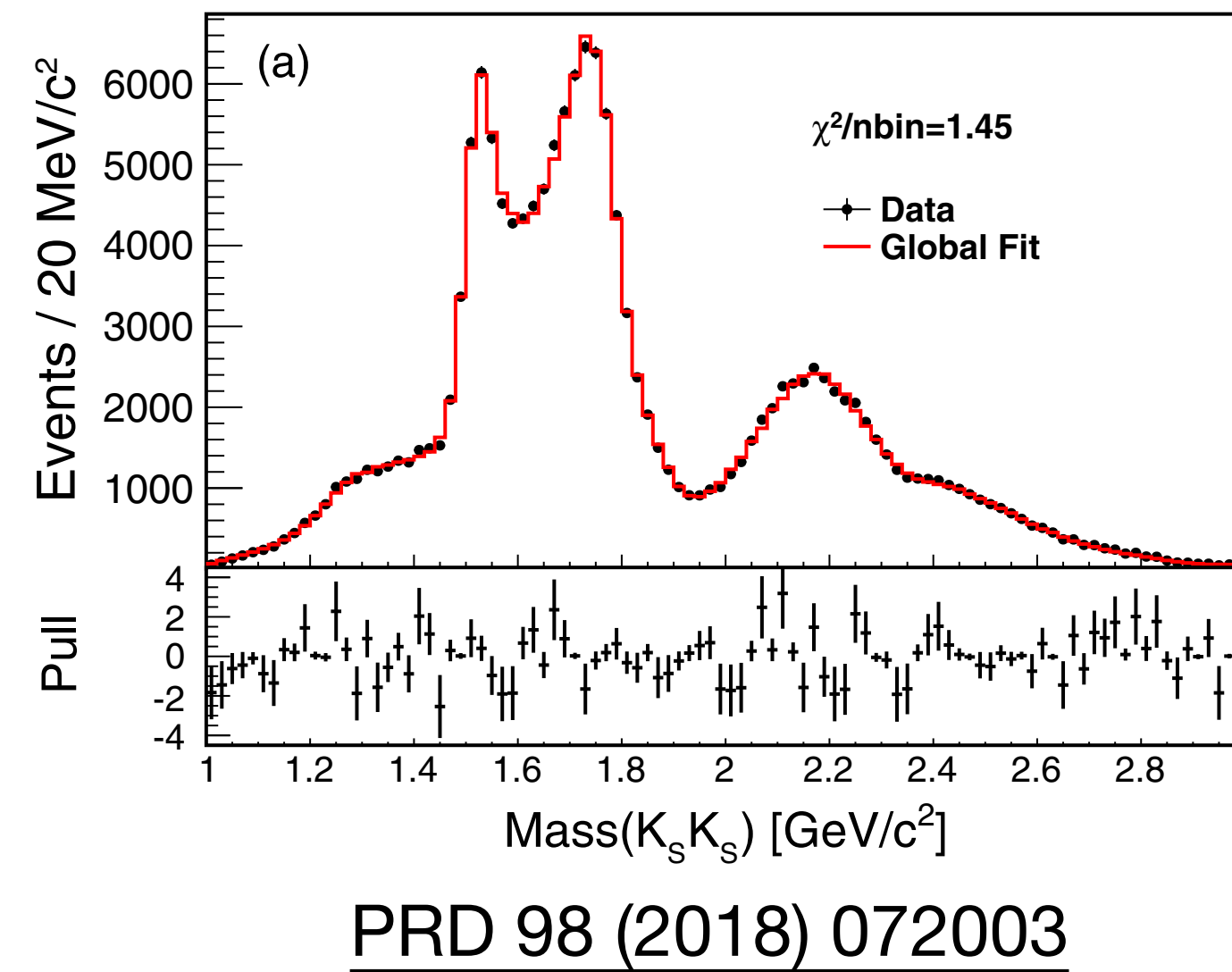
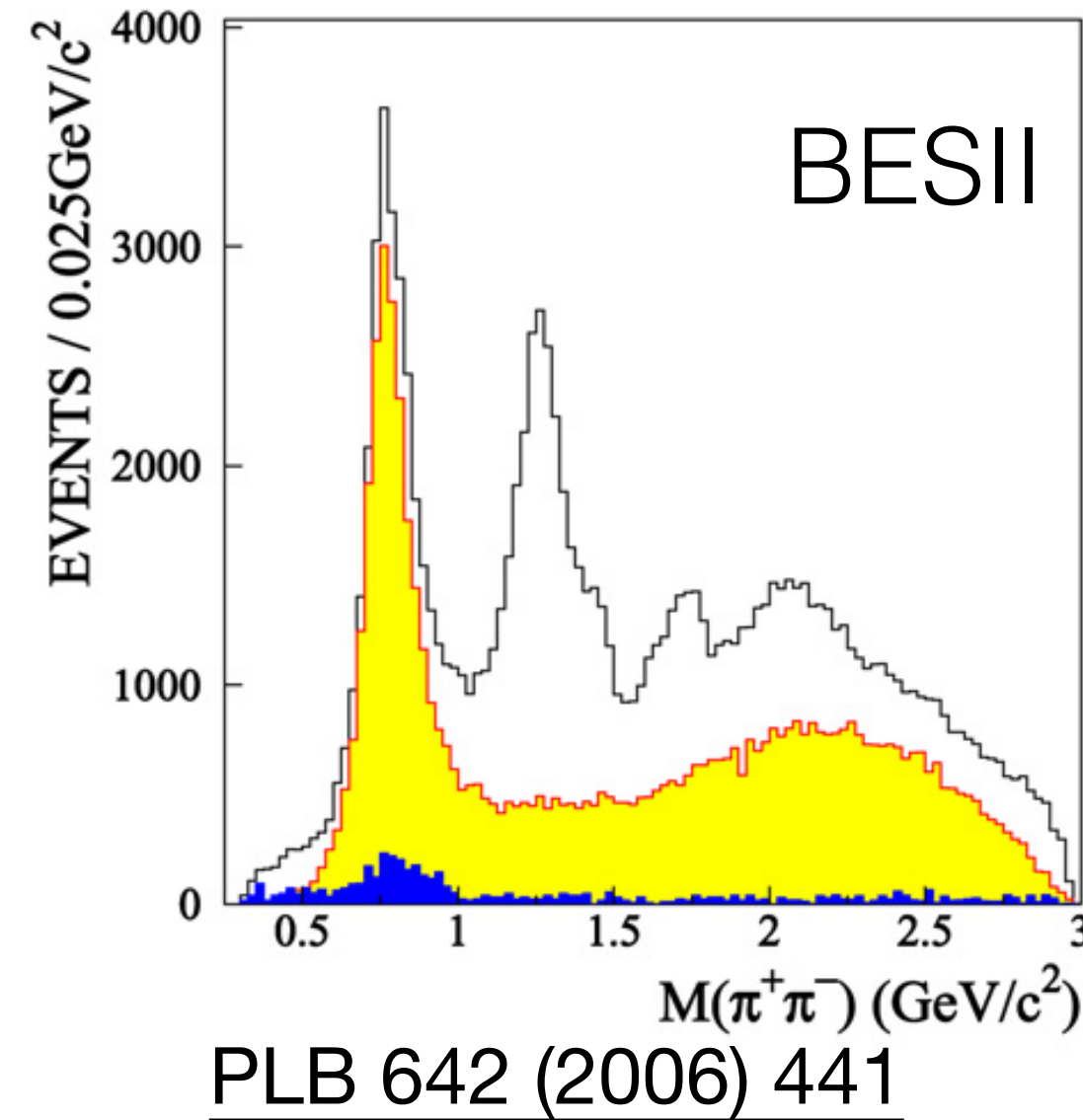
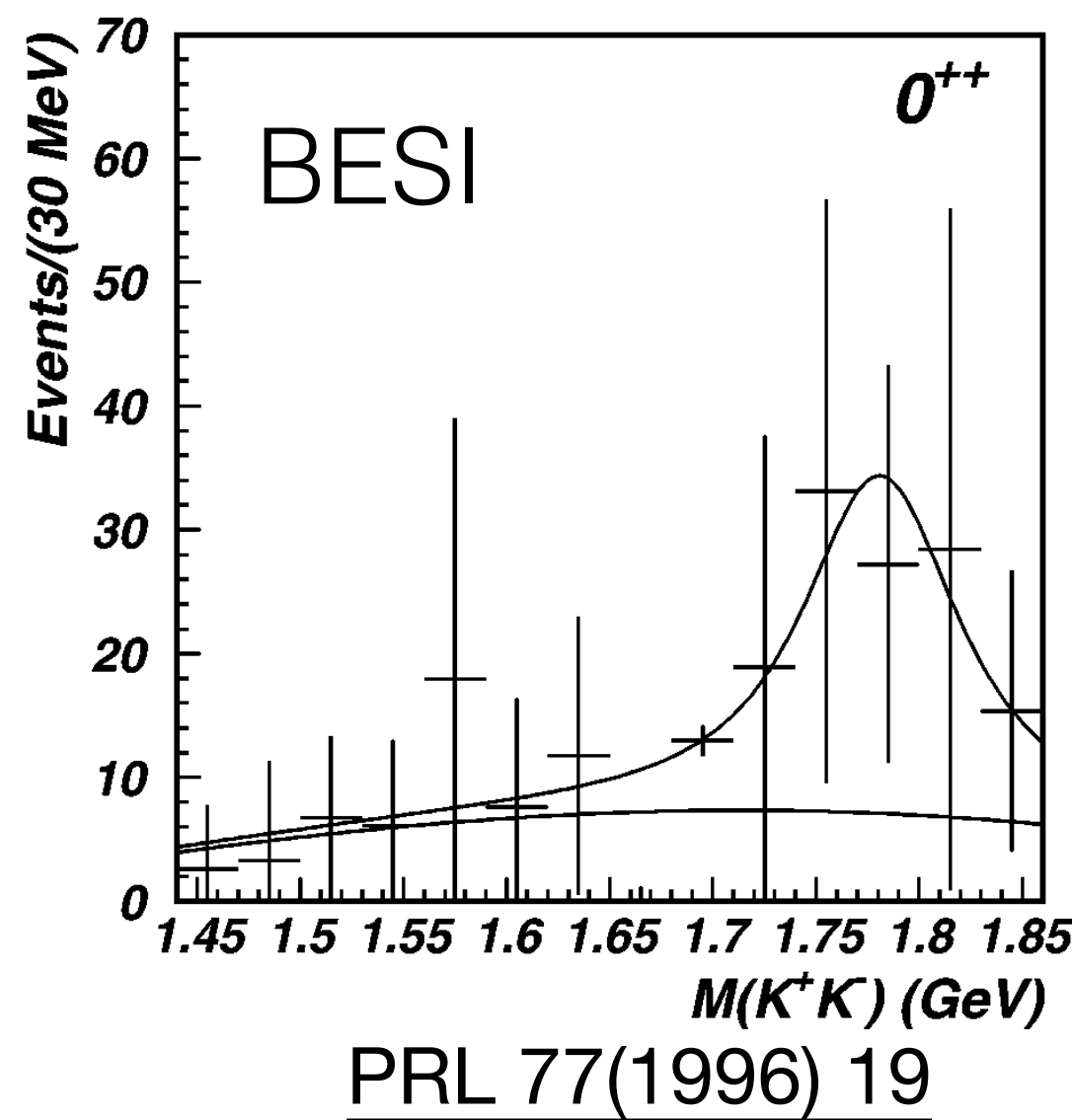
- ◆ Many experiments searched for glueballs over the past 4 decades
- ◆ Many historical glueball candidates, but with some difficulties/controversies.
 - ✦ Scalar Glueball candidate (0^{++}): $f_0(1500)$, $f_0(1710)$
 - ✦ Tensor Glueball candidate (2^{++}): $f_2(2340)$
 - ✦ Pseudoscalar Glueball candidate (0^{-+}): $\eta(1405)$

Historical Glueball Candidates — Scalar $f_0(1710)$



- ◆ The $f_0(1710)$ was discovered in $J/\psi \rightarrow \gamma \pi^+ \pi^-$ and $J/\psi \rightarrow \gamma K^+ K^-$ by MarkIII in 1987 as $\theta_2(1720)$
- ◆ $J^{PC} = 2^{++}$ from a simple fit to the angular distribution
- ◆ The significance of 2^{++} state is $\sim 3\sigma$ better than 0^{++} assumption

Historical Glueball Candidates — Scalar $f_0(1710)$



◆ The $f_0(1710)$ was firstly changed to be 0^{++} from a full PWA of $J/\psi \rightarrow \gamma KK$ @ BES I. Lots of studies at Mark II, DM2, BES I, BES II, BES III

◆ The $f_0(1710)$ favors to be **a scalar glueball or large glueball content: controversy of dynamic mixing mechanism**

◆ **High production rate of $J/\psi \rightarrow \gamma f_0(1710)$**

$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma \pi \pi] = (4.0 \pm 1.0) \times 10^{-4}$$

BES II: PLB 642 (2006) 441

$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma K_s^0 K_s^0] = (2.00^{+0.03}_{-0.02} {}^{+0.31}_{-0.10}) \times 10^{-4}$$

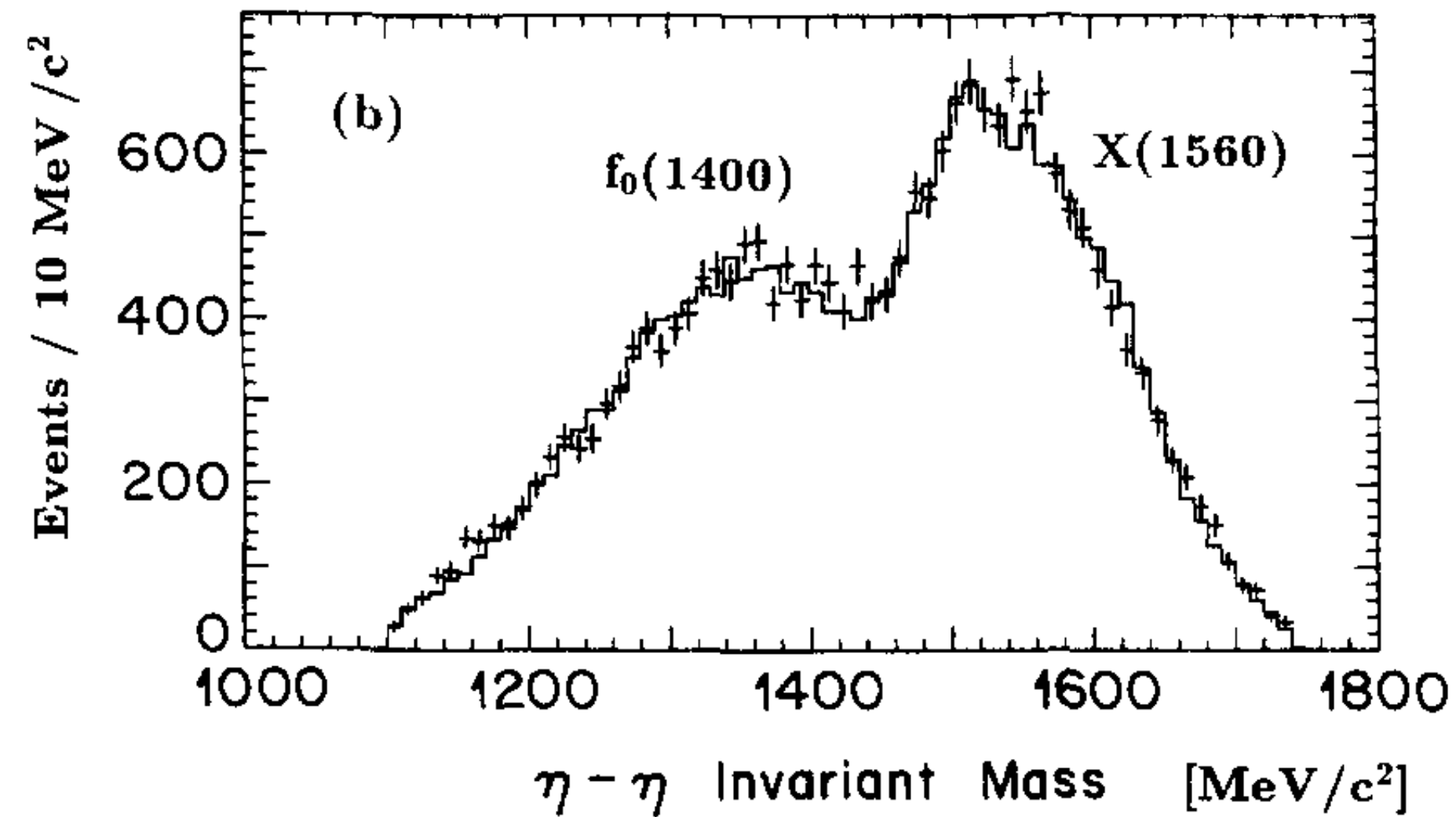
BES III: PRD 98 (2018) 072003

◆ **Decay suppression in $f_0(1710) \rightarrow \eta \eta'$**

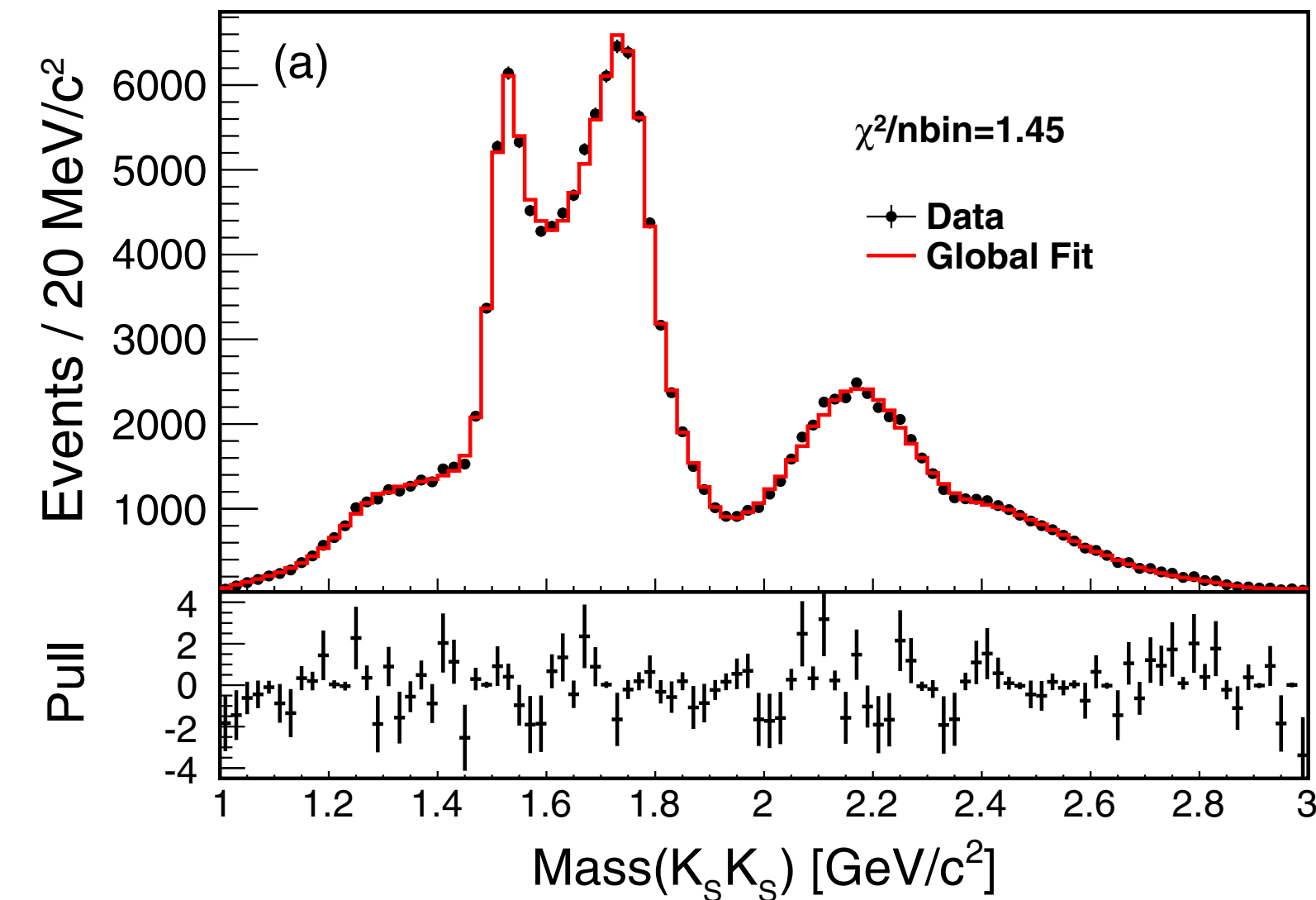
$$B[f_0(1710) \rightarrow \eta \eta' / f_0(1710) \rightarrow \pi \pi] < (2.9 \pm {}^{+1.1}_{-0.9}) \times 10^{-3}$$

BES III: PRD 106 072012(2022)

Historical Glueball Candidates — Scalar $f_0(1500)$



PLB 291 (1992) 347



PRD 98 (2018) 072003

- ◆ The $f_0(1500)$ was discovered by Crystal Barrel in 1992
- ◆ An unique 0^{++} candidate since $f_0(1710)$ was f_2 at that time

◆ Disfavors to its interpretation of a scalar glueball

◆ Lower production rate of $J/\psi \rightarrow \gamma f_0(1500)$

$$B[J/\psi \rightarrow \gamma f_0(1500) \rightarrow \gamma K_s^0 K_s^0] = (1.59^{+0.16}_{-0.16} \quad {}^{+0.18}_{-0.56}) \times 10^{-5}$$

$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma K_s^0 K_s^0] = (2.00^{+0.03}_{-0.02} \quad {}^{+0.31}_{-0.10}) \times 10^{-4}$$

BESIII: PRD 98 (2018) 072003

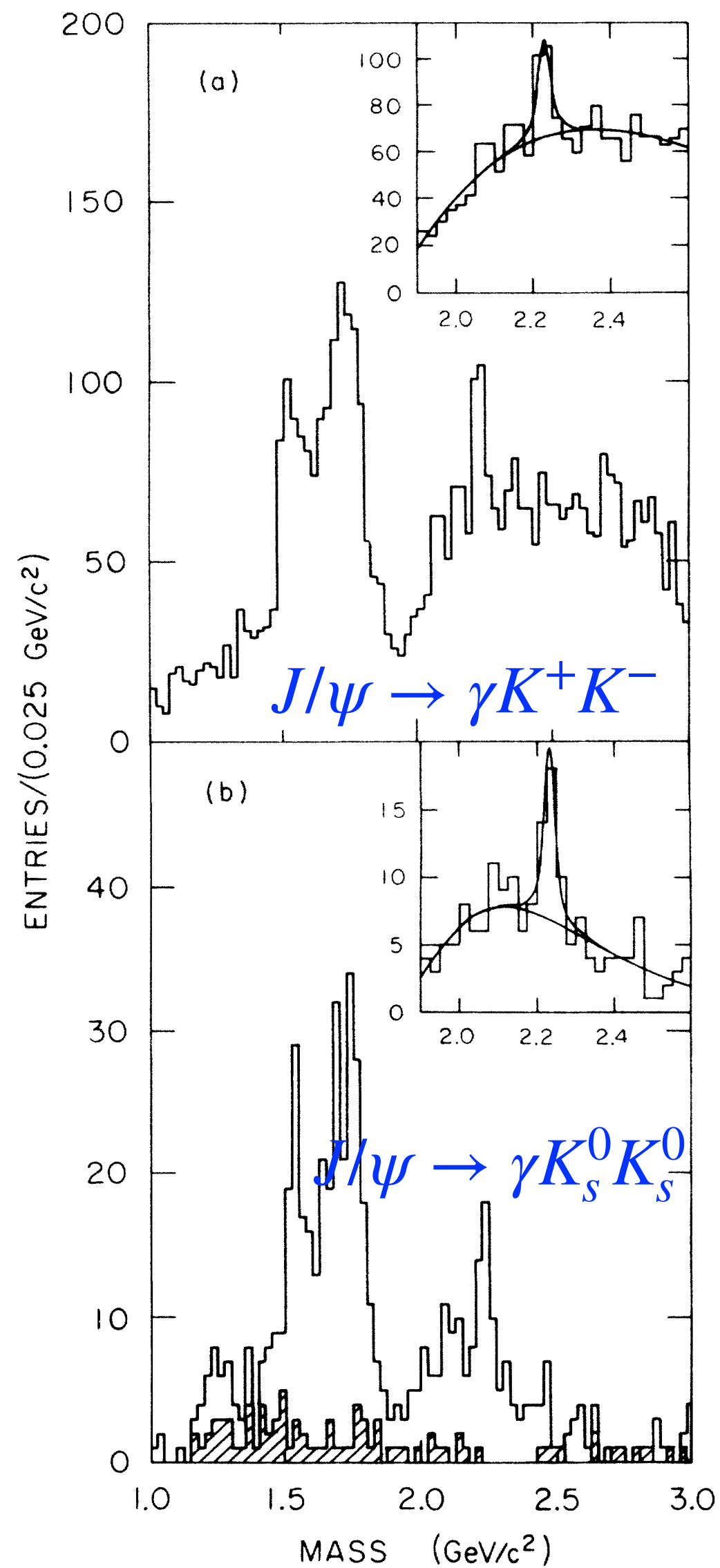
◆ No strong suppression in $f_0(1500) \rightarrow \eta\eta'$

$$B[f_0(1500) \rightarrow \eta\eta'/f_0(1500) \rightarrow \pi\pi] = (1.66 \pm {}^{+0.42}_{-0.40}) \times 10^{-1}$$

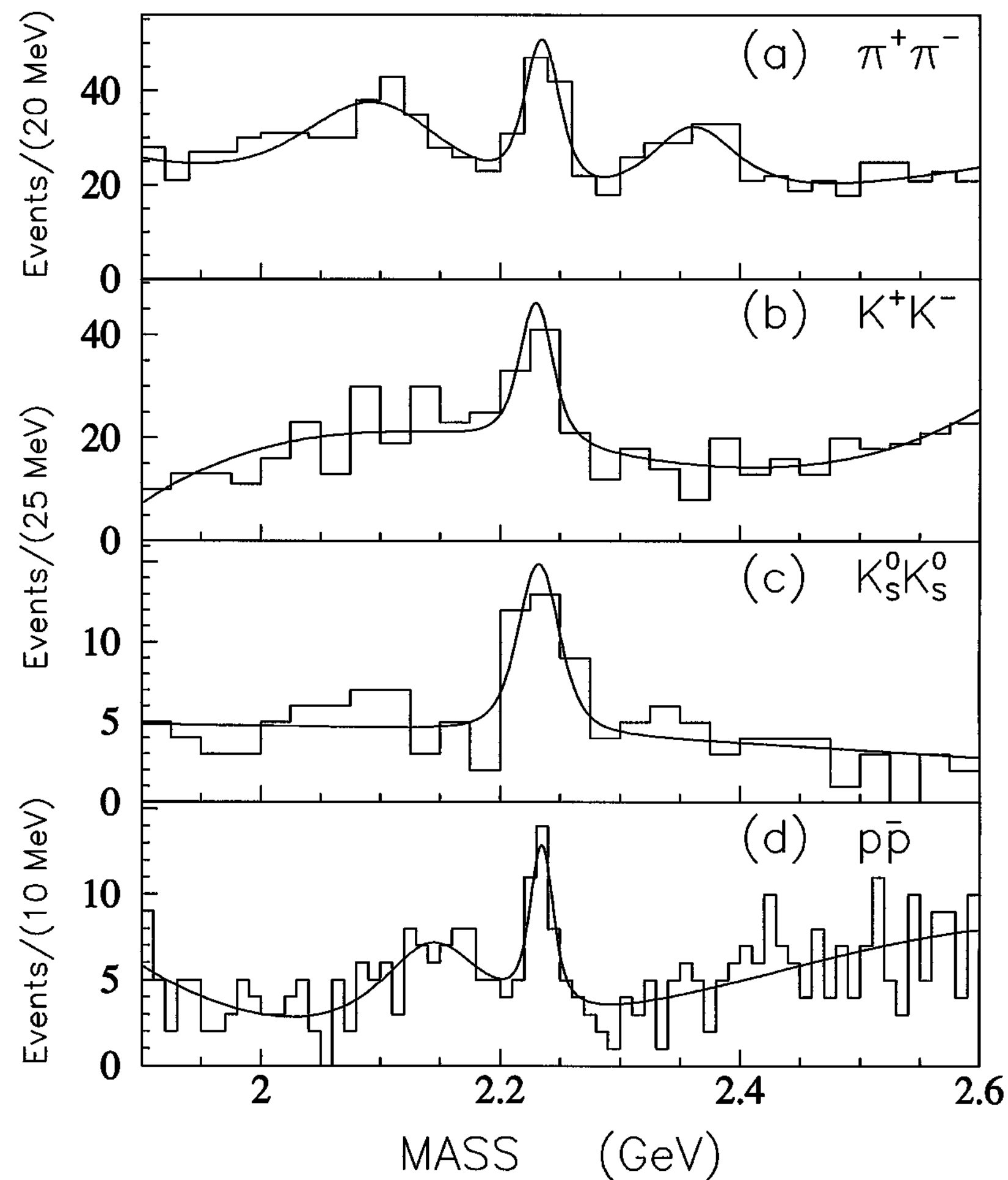
$$B[f_0(1710) \rightarrow \eta\eta'/f_0(1710) \rightarrow \pi\pi] < (2.9 \pm {}^{+1.1}_{-0.9}) \times 10^{-3}$$

BESIII: PRD 106 072012(2022)

Historical Glueball Candidates — Tensor $\xi(2230)$



PRL 56 (1986) 107



PRL 76 (1996) 3502

- ◆ First observed by MarkIII is $J/\psi \rightarrow \gamma K K$ in 1980's, then by BES I in 1990's in $J/\psi \rightarrow \gamma K K$, $\gamma \pi \pi$, $\gamma p \bar{p}$ with very narrow mass peak.
- ◆ It was a tensor glueball candidate due to good flavor symmetric decay property.
- ◆ Difficulty: it was not confirmed by BES II, nor BES III with much higher statistics.

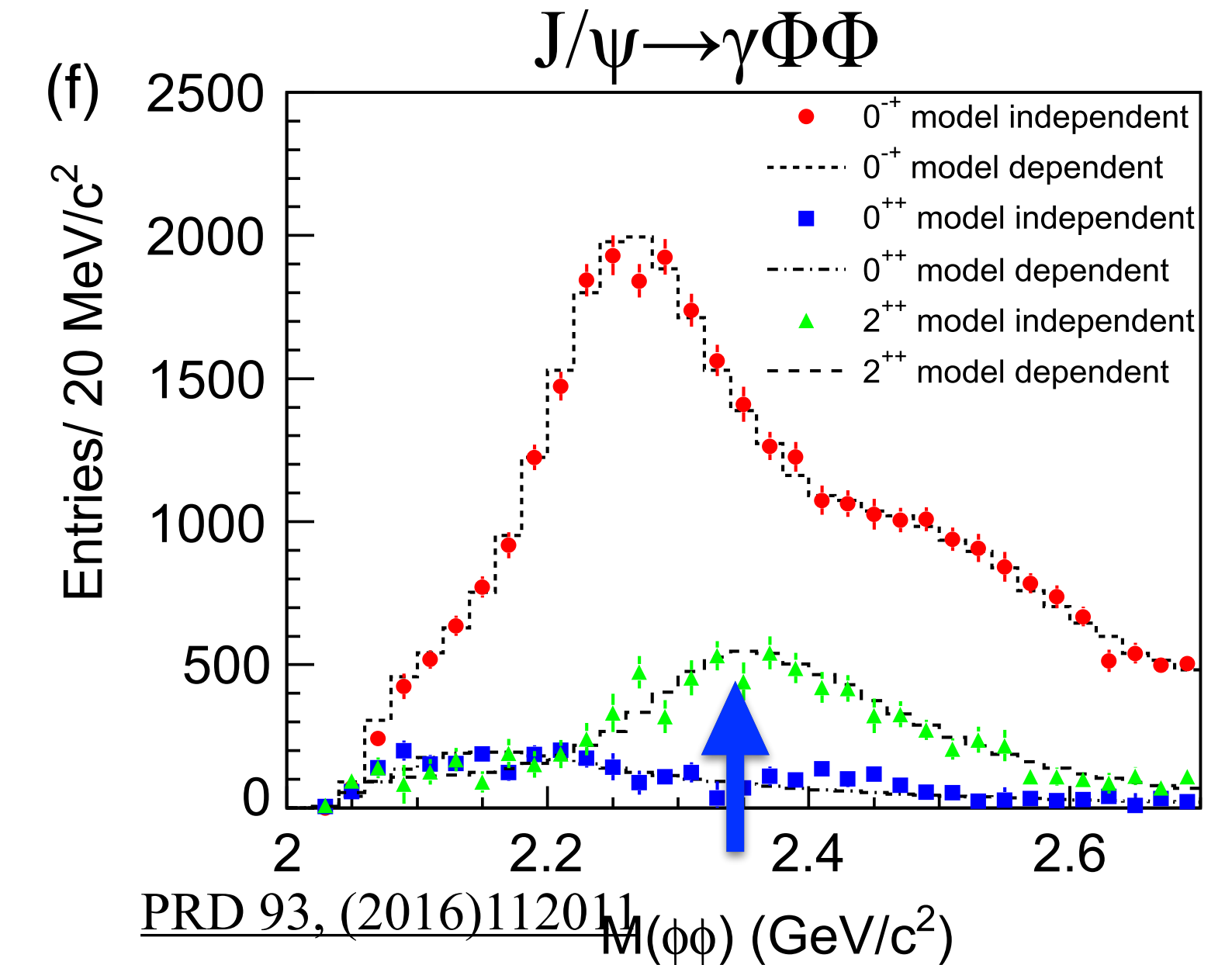
Historical Glueball Candidates — Tensor $f_2(2340)$

$$\Gamma(J/\psi \rightarrow \gamma G_{2+}) = 1.01(22) \text{ keV}$$

$$\Gamma(J/\psi \rightarrow \gamma G_{2+})/\Gamma_{tot} = 1.1 \times 10^{-2}$$

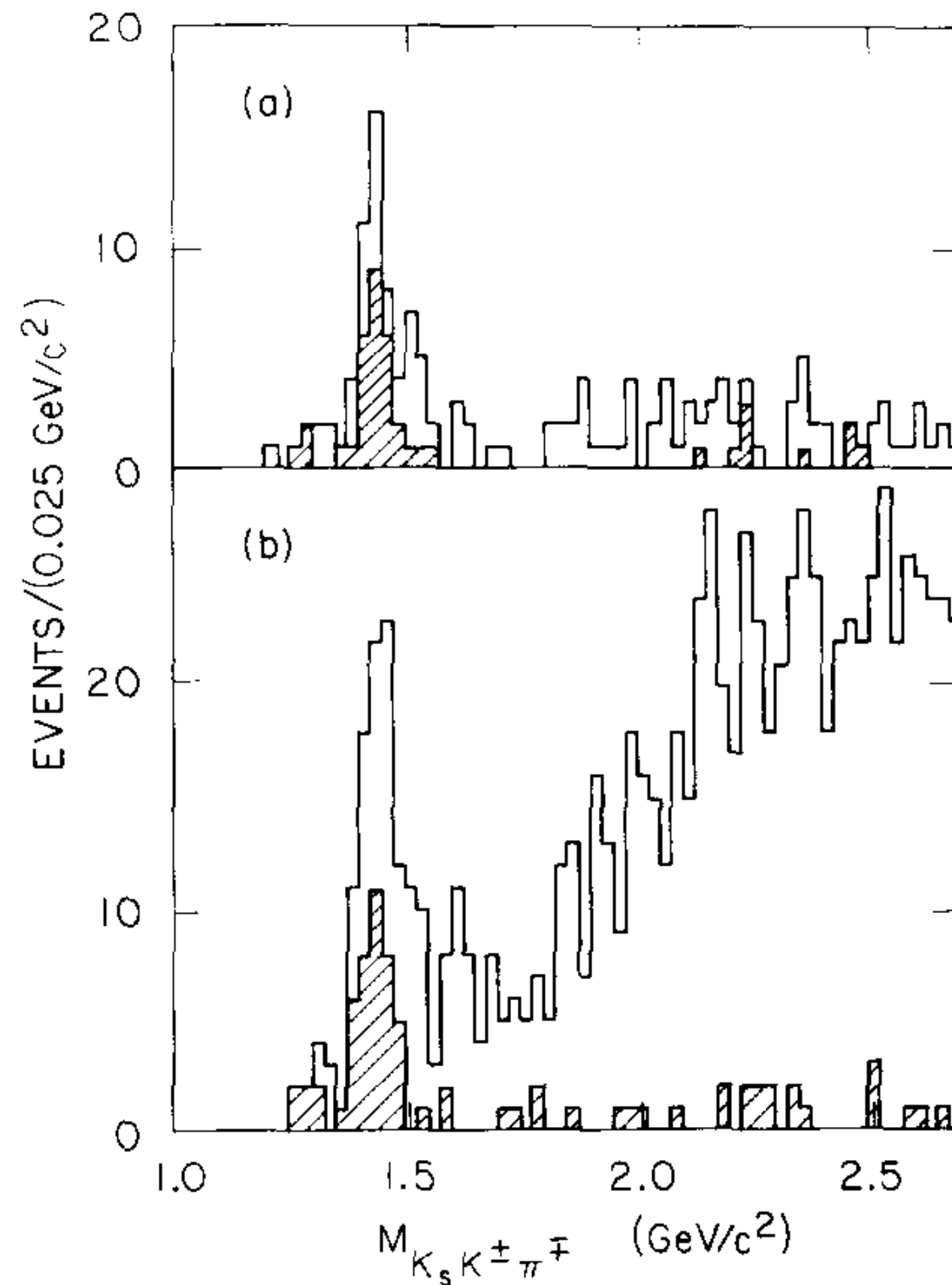
CLQCD, Phys. Rev. Lett. 111, 091601 (2013)

- ◆ **Large production rate of $f_2(2340)$ in $J/\psi \rightarrow \gamma(KK/\eta\eta/\eta'\eta'/\phi\phi)$:**
substantially lower than the LQCD prediction for tensor glueball
- ◆ $B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma \eta\eta) = (3.8^{+0.62}_{-0.66} \text{ } ^{+2.37}_{-2.07}) \times 10^{-5}$ (PRD 87,2013,092009)
- ◆ $B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma \phi\phi) = (1.91 \pm 0.14^{+0.72}_{-0.73}) \times 10^{-4}$ (PRD 93,2016,112011)
- ◆ $B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma K_s K_s) = (5.54^{+0.34}_{-0.40} \text{ } ^{+3.82}_{-1.49}) \times 10^{-5}$ (PRD 98,2018,072003)
- ◆ $B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma \eta'\eta') = (8.67 \pm 0.70^{+0.16}_{-1.67}) \times 10^{-6}$ (PRD 105,2022,072002)
- ◆ **Difficulty: Many wide tensor mesons and large overlaps in the mass region of 2.3 GeV** (2^{++} glueball mass from the LQCD predictions)
- ◆ Studies are strongly model dependent.



Resonance	M (MeV/ c^2)	Γ (MeV/ c^2)	B.F. ($\times 10^{-4}$)	Sig.
$\eta(2225)$	2216^{+4+21}_{-5-11}	185^{+12+43}_{-14-17}	$(2.40 \pm 0.10^{+2.47}_{-0.18})$	28σ
$\eta(2100)$	2050^{+30+75}_{-24-26}	$250^{+36+181}_{-30-164}$	$(3.30 \pm 0.09^{+0.18}_{-3.04})$	22σ
$X(2500)$	$2470^{+15+101}_{-19-23}$	230^{+64+56}_{-35-33}	$(0.17 \pm 0.02^{+0.02}_{-0.08})$	8.8σ
$f_0(2100)$	2101	224	$(0.43 \pm 0.04^{+0.24}_{-0.03})$	24σ
$f_2(2010)$	2011	202	$(0.35 \pm 0.05^{+0.28}_{-0.15})$	9.5σ
$f_2(2300)$	2297	149	$(0.44 \pm 0.07^{+0.09}_{-0.15})$	6.4σ
$f_2(2340)$	2339	319	$(1.91 \pm 0.14^{+0.72}_{-0.73})$	11σ
0^{-+} PHSP			$(2.74 \pm 0.15^{+0.16}_{-1.48})$	6.8σ

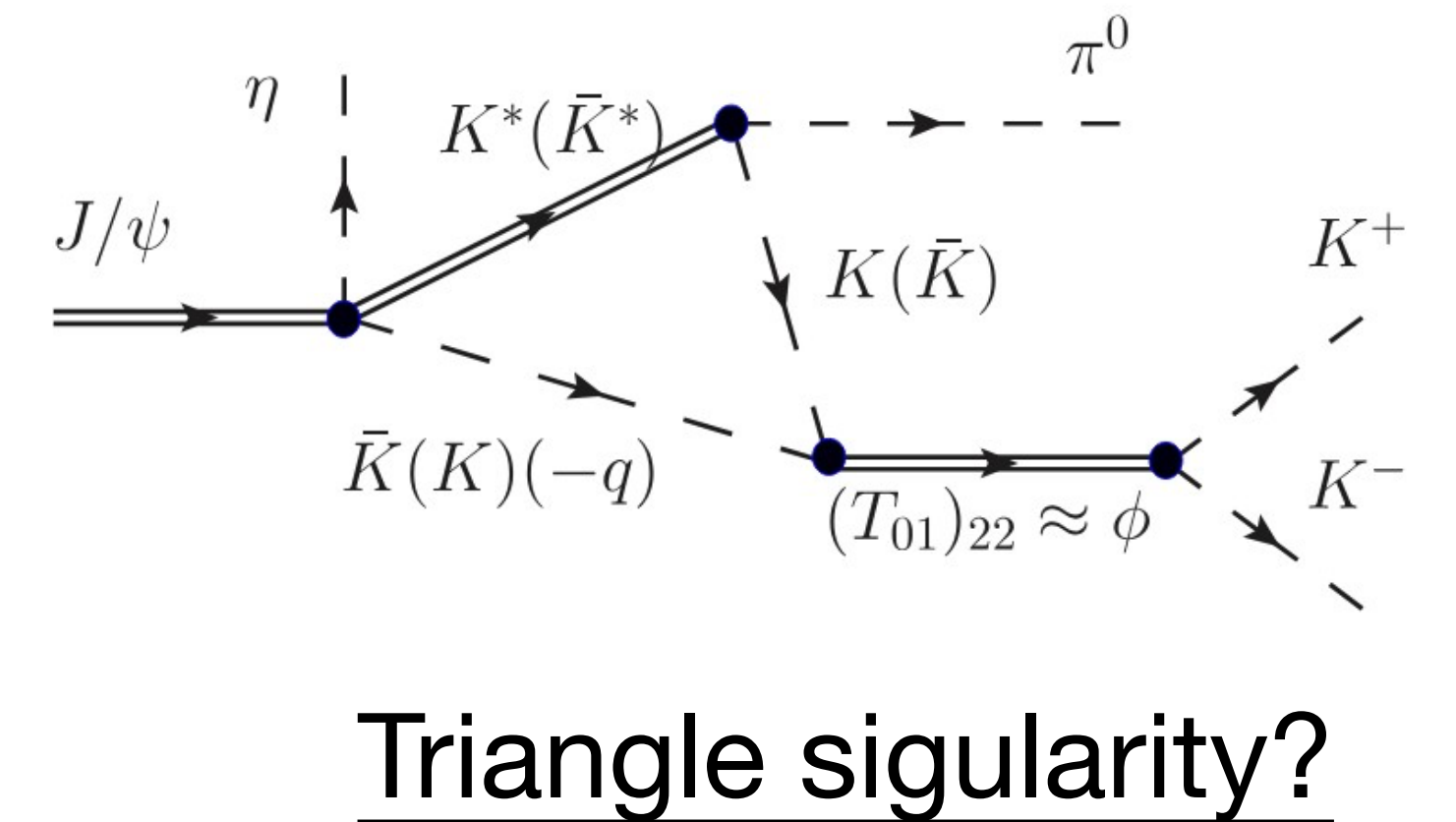
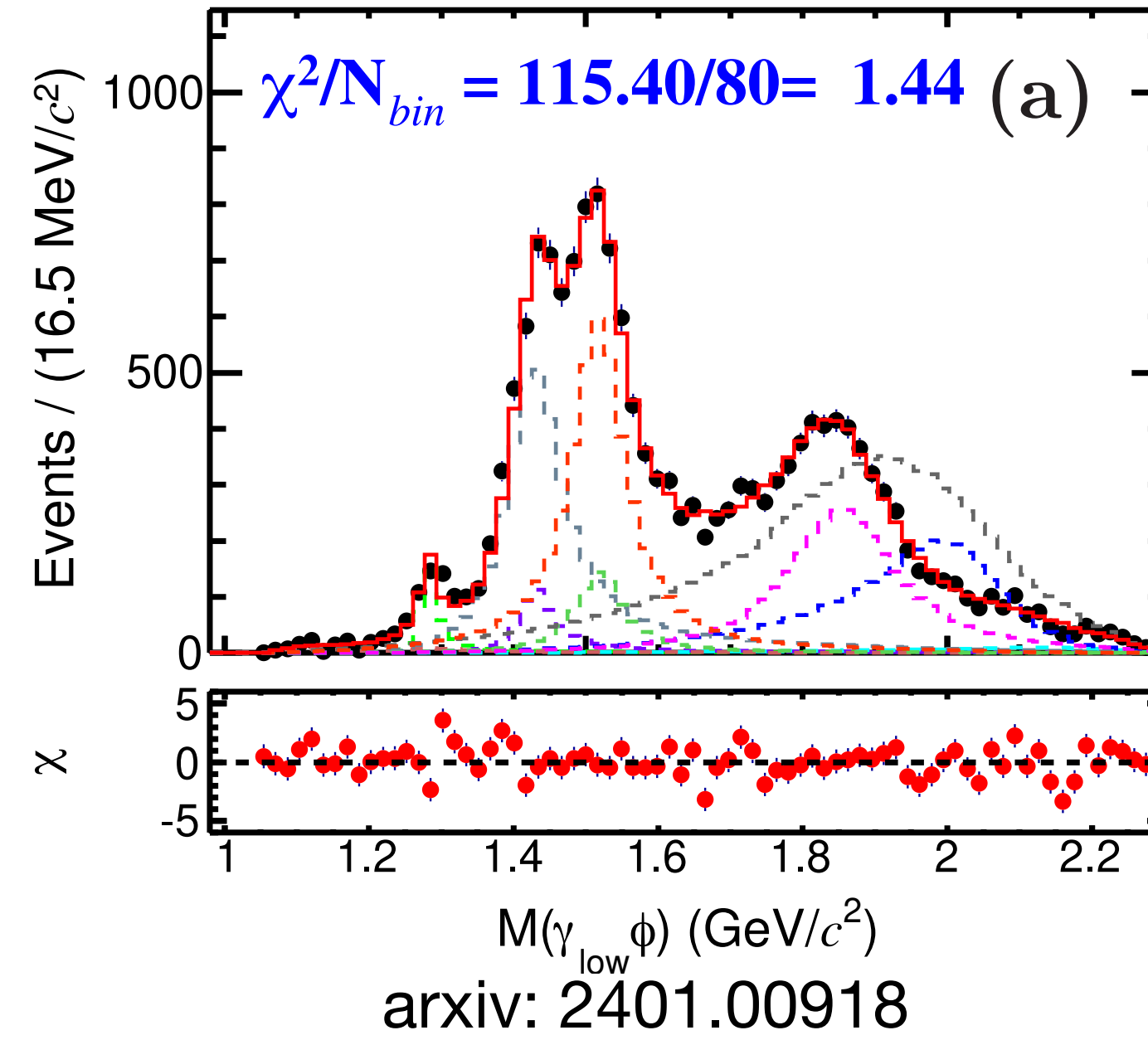
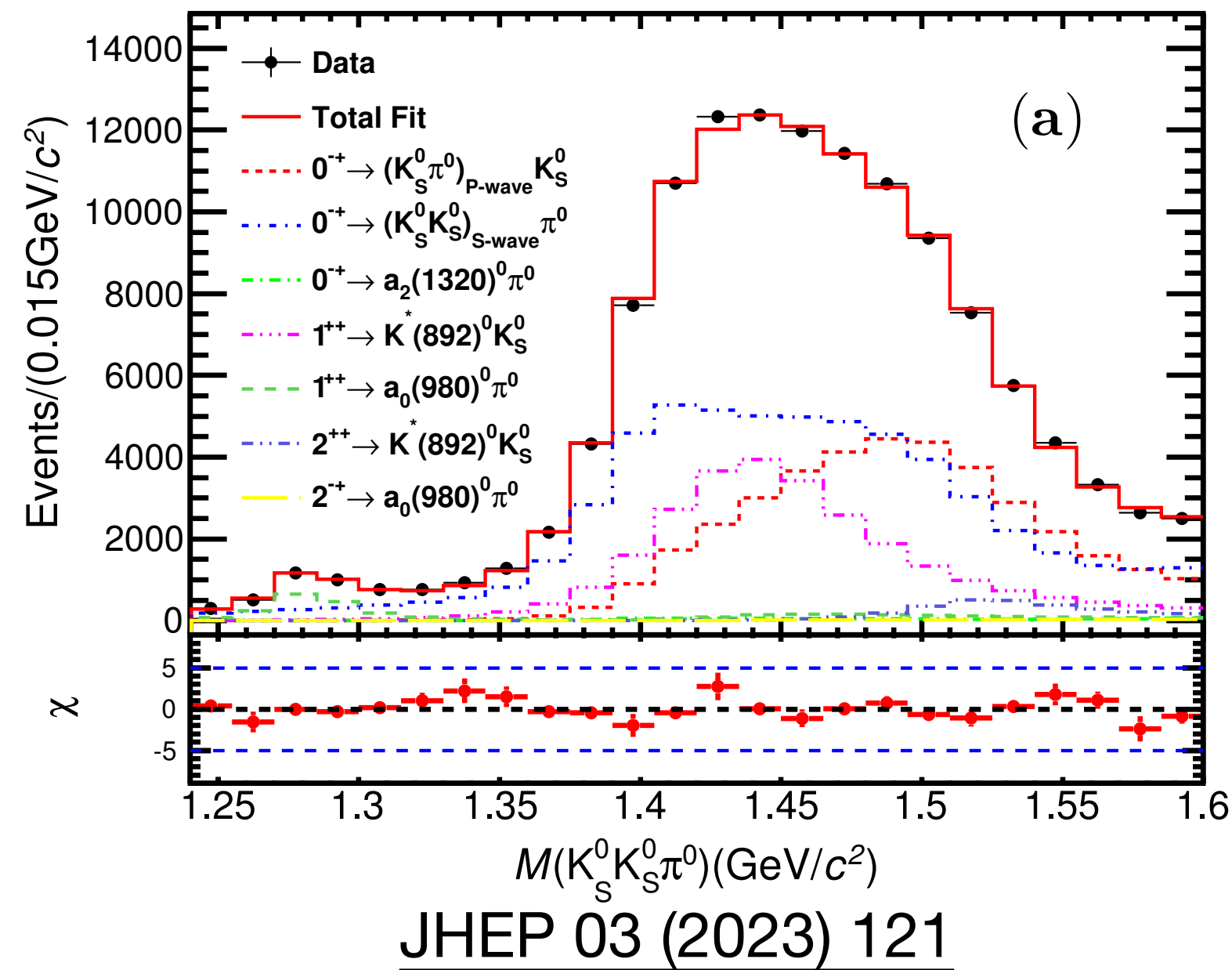
Historical Glueball Candidates — Pseudoscalar $\eta(1405)$



Phys. Lett. 97B (1980) 2

- ◆ First discovered by MarkII in 1980, named as $\eta(1440)$ with complicated structures.
- ◆ Believed as the first glueball candidate due to its large production rate in J/ψ radiative decays
- ◆ Lots of studies at MarkII, MarkIII, DM2 and BES:
 - ◆ **No longer a 0^{-+} glueball candidate due to its large different mass from latest LQCD prediction (Lack of reliable LQCD predictions in 1980's)**

Shed new lights on $\eta(1405)/\eta(1475)$ puzzle



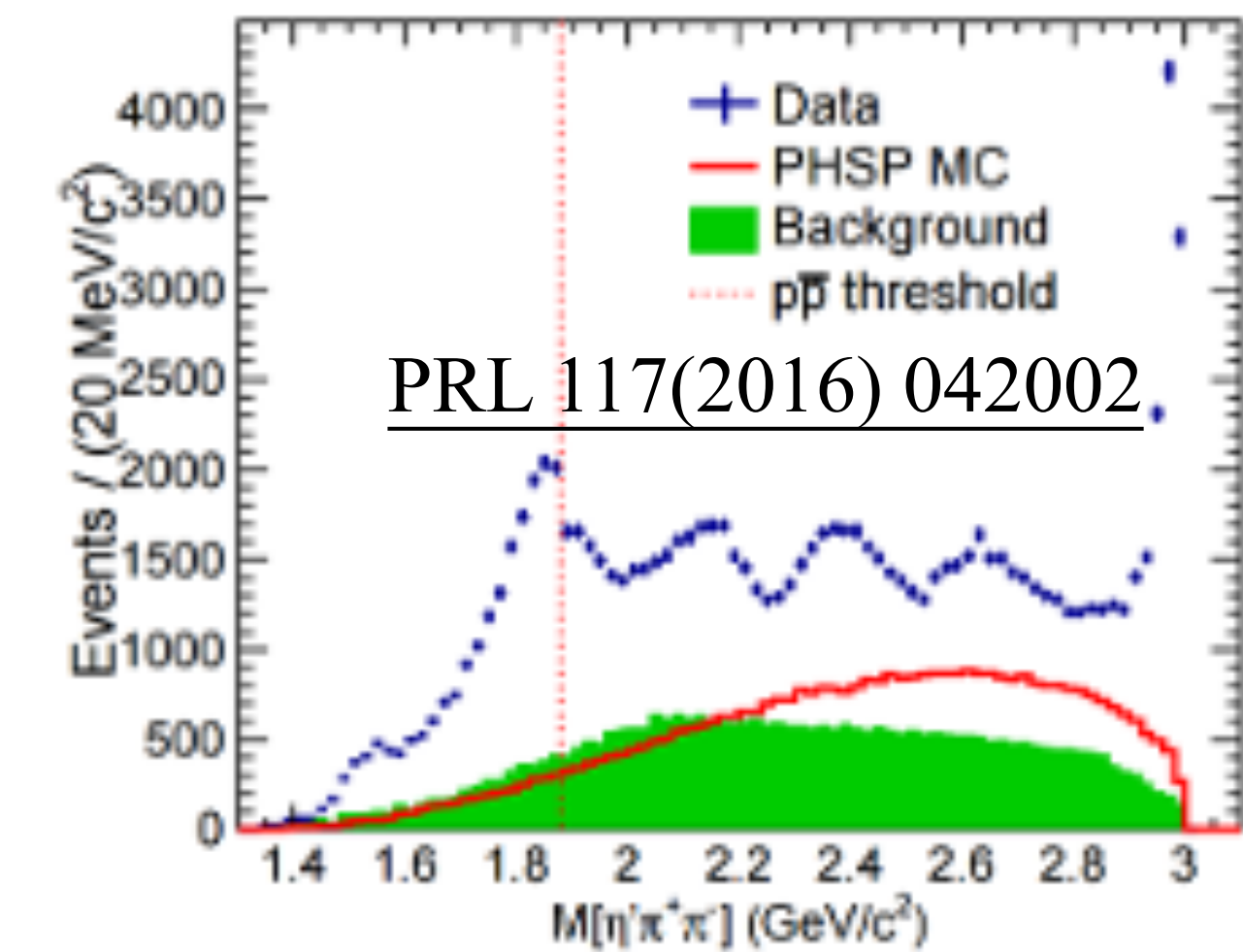
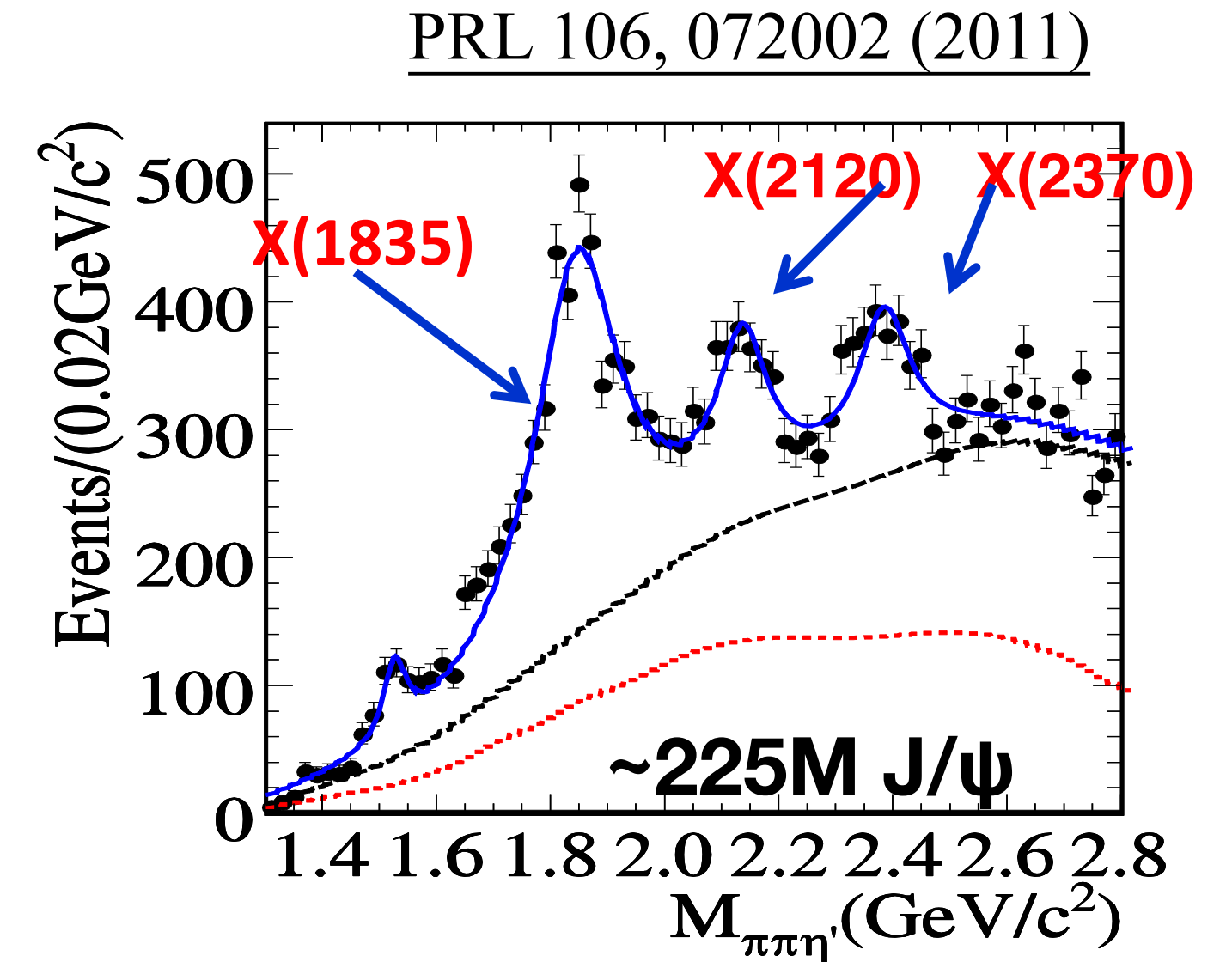
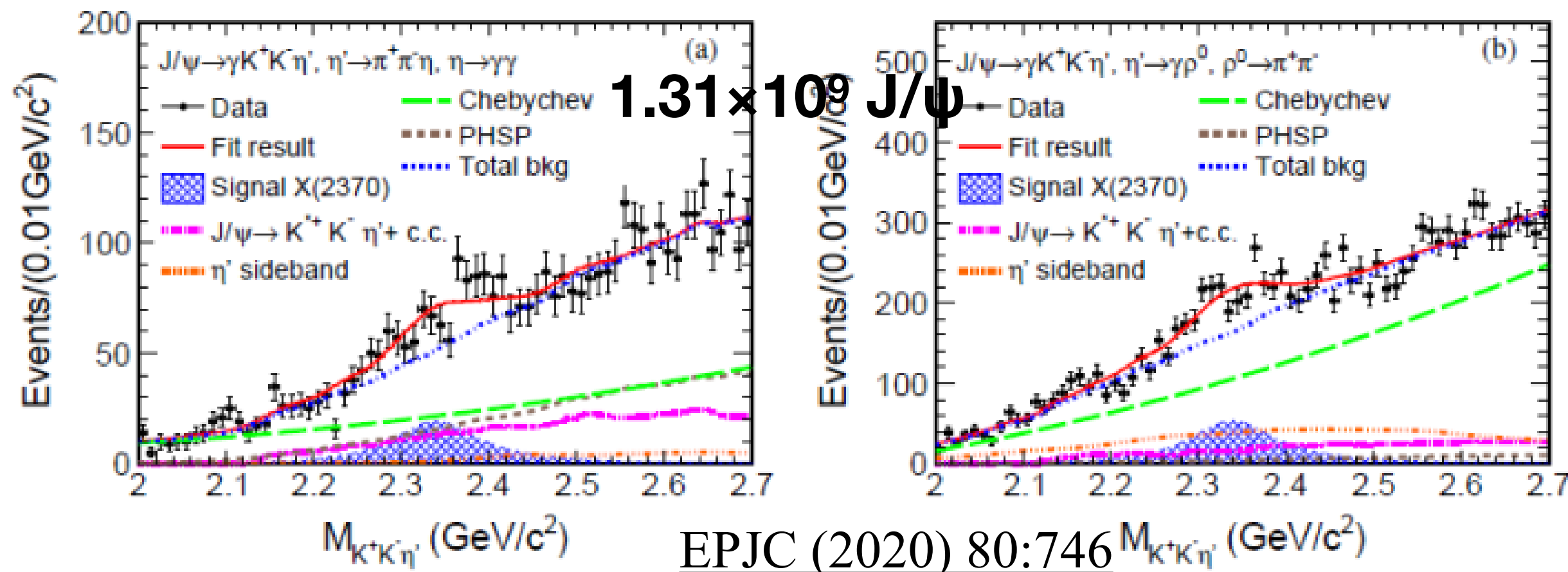
- ◆ $\eta(1295)$ and $\eta(1475)$ are generally assigned to be the first radial excitation of the ground states of η and η'
- ◆ $\eta(1405)$ - $\eta(1475)$ puzzle :Whether or not the $\eta(1405)$ - $\eta(1475)$ are 1 or 2 states?
- ◆ PWA of $J/\psi \rightarrow \gamma K_S K_S \pi^0$: Two isoscalar states $\eta(1405)$ and $\eta(1475)$ around 1.4 GeV can well fit data
- ◆ PWA of $J/\psi \rightarrow \gamma \gamma \Phi$: observed $\eta(1405)$ with 18.9σ , while $\eta(1475)$ can not be excluded (3.9σ)

X(2370)

◆ Discovered by BESIII in $J/\psi \rightarrow \gamma\pi^+\pi^-\eta'$ in 2011

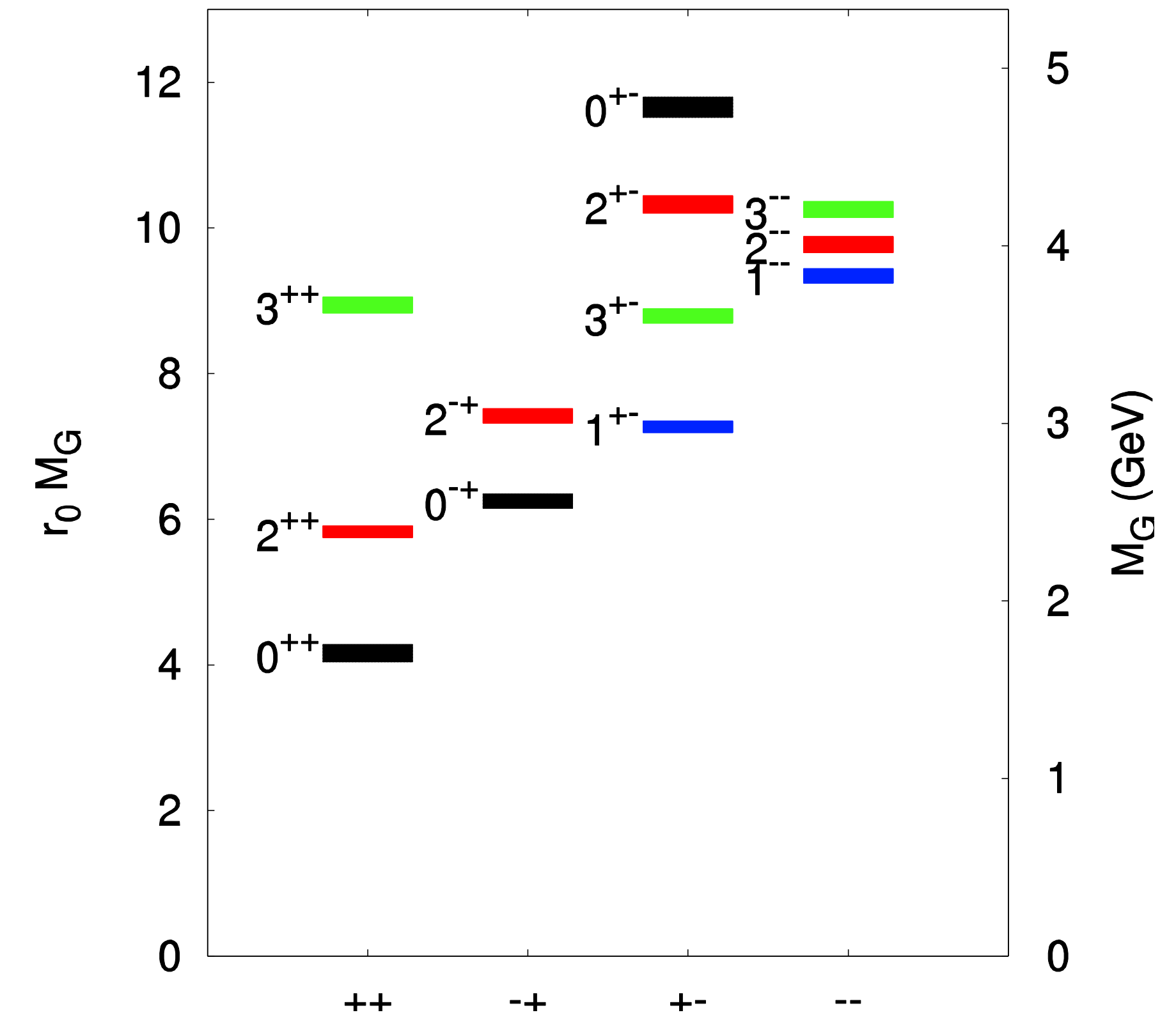
	M(MeV/c ²)	Γ (MeV/c ²)	Sig.
X(1835)	$1836.5 \pm 3.0^{+5.6}_{-2.1}$	$190.1 \pm 9.0^{+38}_{-36}$	$>20\sigma$
X(2120)	$2122.4 \pm 6.7^{+4.7}_{-2.7}$	$83 \pm 16^{+31}_{-11}$	7.2σ
X(2370)	$2376.3 \pm 8.7^{+3.2}_{-4.3}$	$83 \pm 17^{+44}_{-6}$	6.4σ

◆ Confirmed by BESIII in $J/\psi \rightarrow \gamma\pi^+\pi^-\eta'$ and $J/\psi \rightarrow \gamma K\bar{K}\eta'$ (new mode)

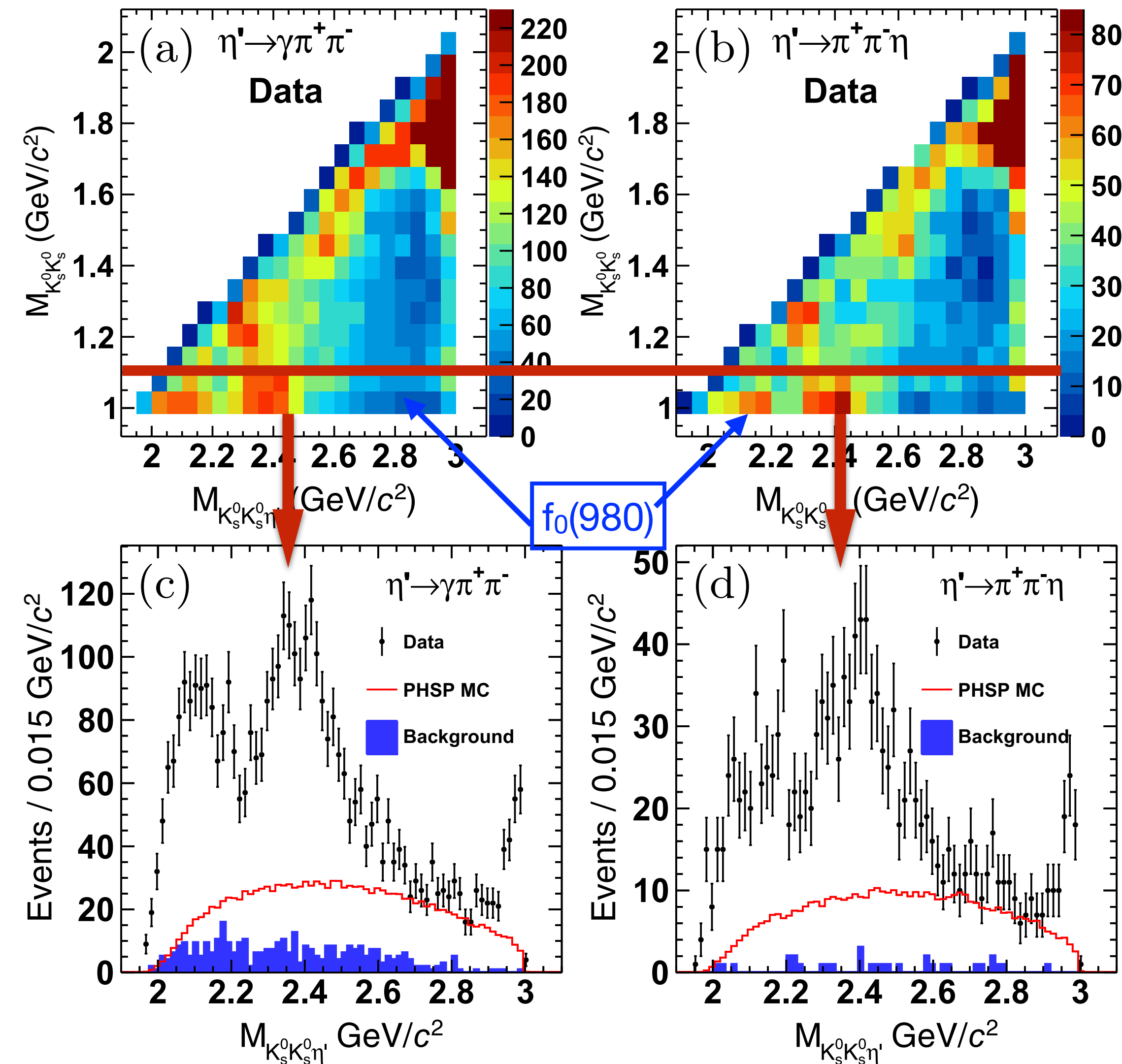


X(2370) - good candidate of 0^{-+} glueball

- ◆ Its mass is consistent with LQCD prediction on the 0^{-+} glueball
- ◆ Produced in the gluon-rich J/ψ radiative decays
- ◆ Observed in flavor symmetric decay modes of $\pi^+\pi^-\eta'$ and $K\bar{K}\eta'$ — favorite decay modes of 0^{-+} glueball
- ◆ Determination of its spin-parity is crucial

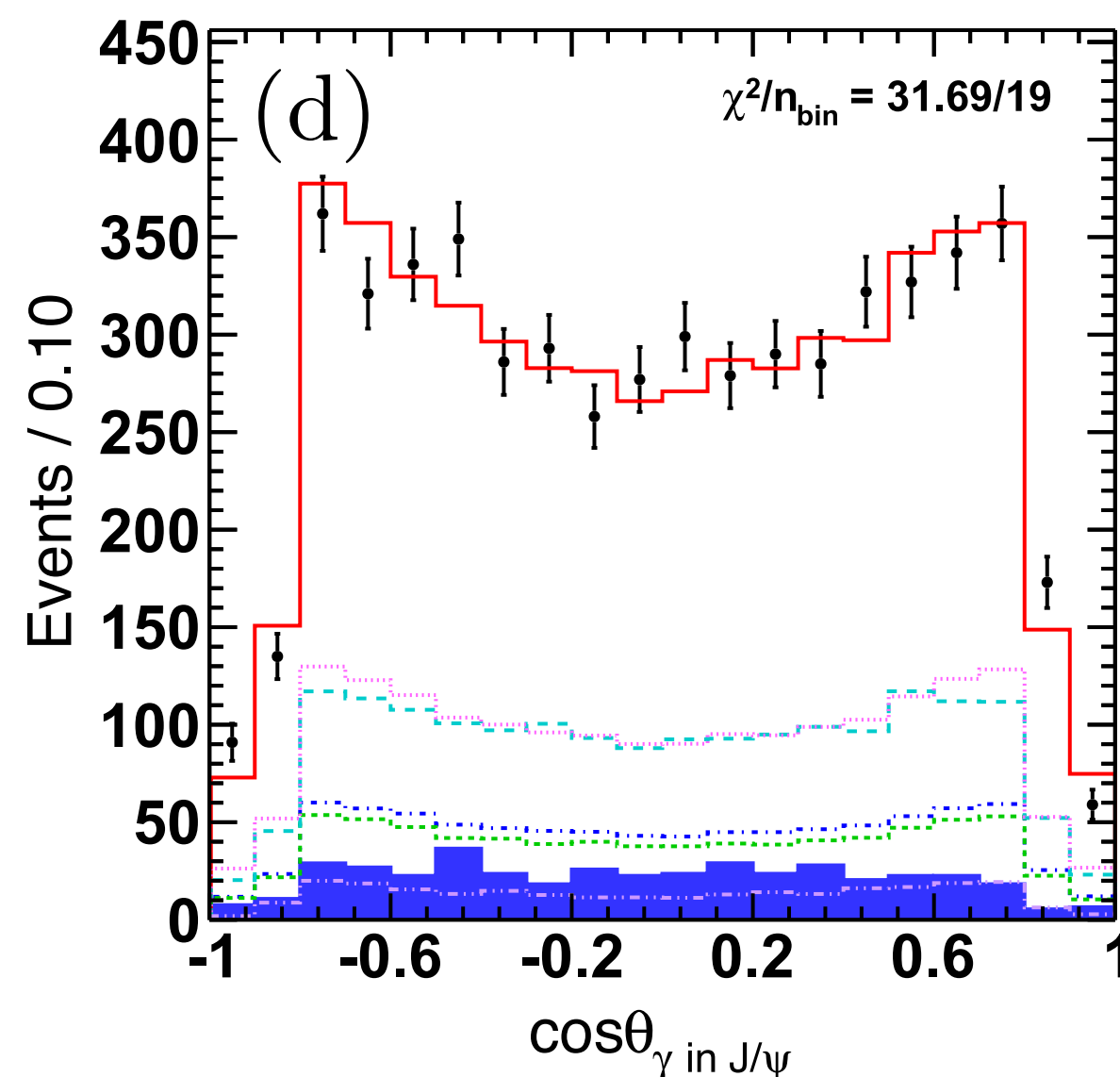
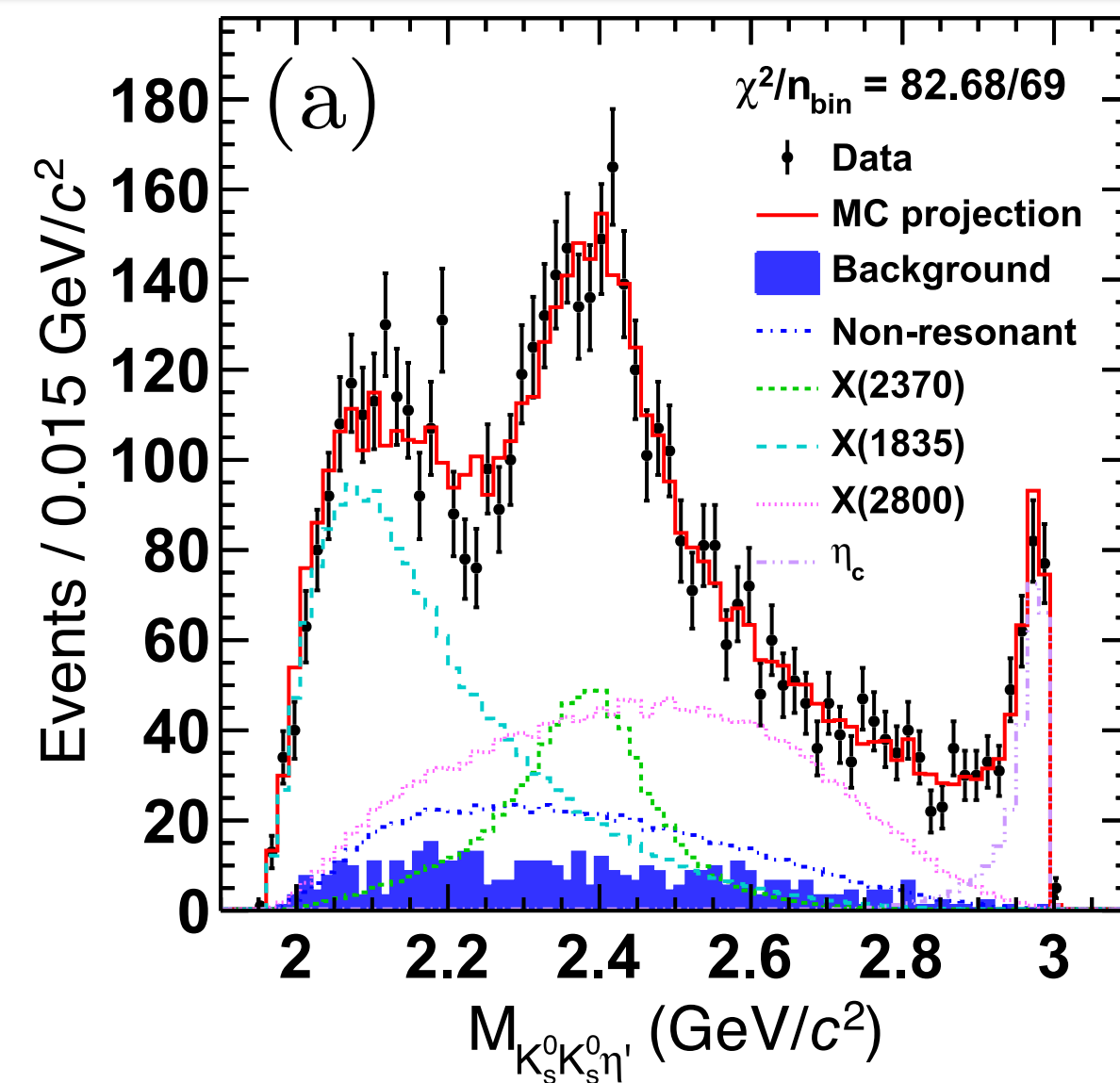


Spin-Parity determination of the $X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$



- ◆ Analysis advantage of $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$:
 - ◆ Almost background free channel (exchange symmetry and C-parity conservation)
 - ◆ 10 billion J/ψ data
 - ◆ Very good BESIII detector performance
- ◆ Similar structures in $\eta' \rightarrow \pi^+ \pi^- \eta$ / $\gamma \pi^+ \pi^-$ modes:
 - ◆ Evident $f_0(980)$ in $K_s^0 K_s^0$ mass threshold
 - ◆ Clear signal of $X(1835), X(2370), \eta_c$ with $f_0(980)$ selection
- ◆ Best PWA fit can well describe the data:
 - ◆ **Spin-parity of the $X(2370)$ is determined to be 0^- with significance larger than 9.8σ w.r.t. other J^{PC} assumptions**

Spin-Parity determination of the $X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$



PRL 132 (2024) 181901

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 - ◆ **Spin-parity of the $X(2370)$ is determined to be 0^{-+} with significance larger than 9.8σ w.r.t. other J^{PC} assumptions**

Compared with LQCD prediction on Lightest 0^{-+} Glueball

X(2370) measurements:

PRL 132 (2024) 181901

$J^{PC} = 0^{-+}$ with significance $>9.8\sigma$

$M = 2395 \pm 11^{+26}_{-94}$ MeV

$\Gamma = 188^{+18}_{-17}{}^{+124}_{-33}$ MeV

**$B(J/\psi \rightarrow \gamma X(2370))B(X(2370) \rightarrow f_0(980)\eta')B(f_0(980) \rightarrow K^0_s K^0_s)$
 $= (1.31 \pm 0.22^{+2.85}_{-0.84}) \times 10^{-5}$**

LQCD prediction on lightest pseudoscalar glueball:

$J^{PC} = 0^{-+}$

$M = 2395 \pm 14$ MeV

$B(J/\psi \rightarrow \gamma G_{0^{-+}}) = (2.31 \pm 0.80) \times 10^{-4}$

PRD 100 (2019) 054511

- ◆ The measurements are in a good agreement with the predictions on **lightest pseudoscalar glueball**
- ◆ **The spin-parity of the X(2370) is determined to be 0^{-+} for the first time**
- ◆ **Mass is in a good agreement with LQCD predictions**
- ◆ The estimation on $B(J/\psi \rightarrow \gamma X(2370))$ and prediction on $B(J/\psi \rightarrow \gamma G_{0^{-+}})$ are consistent within errors (assuming $\sim 5\%$ decay rate, $B(J/\psi \rightarrow \gamma X(2370)) = (10.7^{+22.8}_{-7}) \times 10^{-4}$)

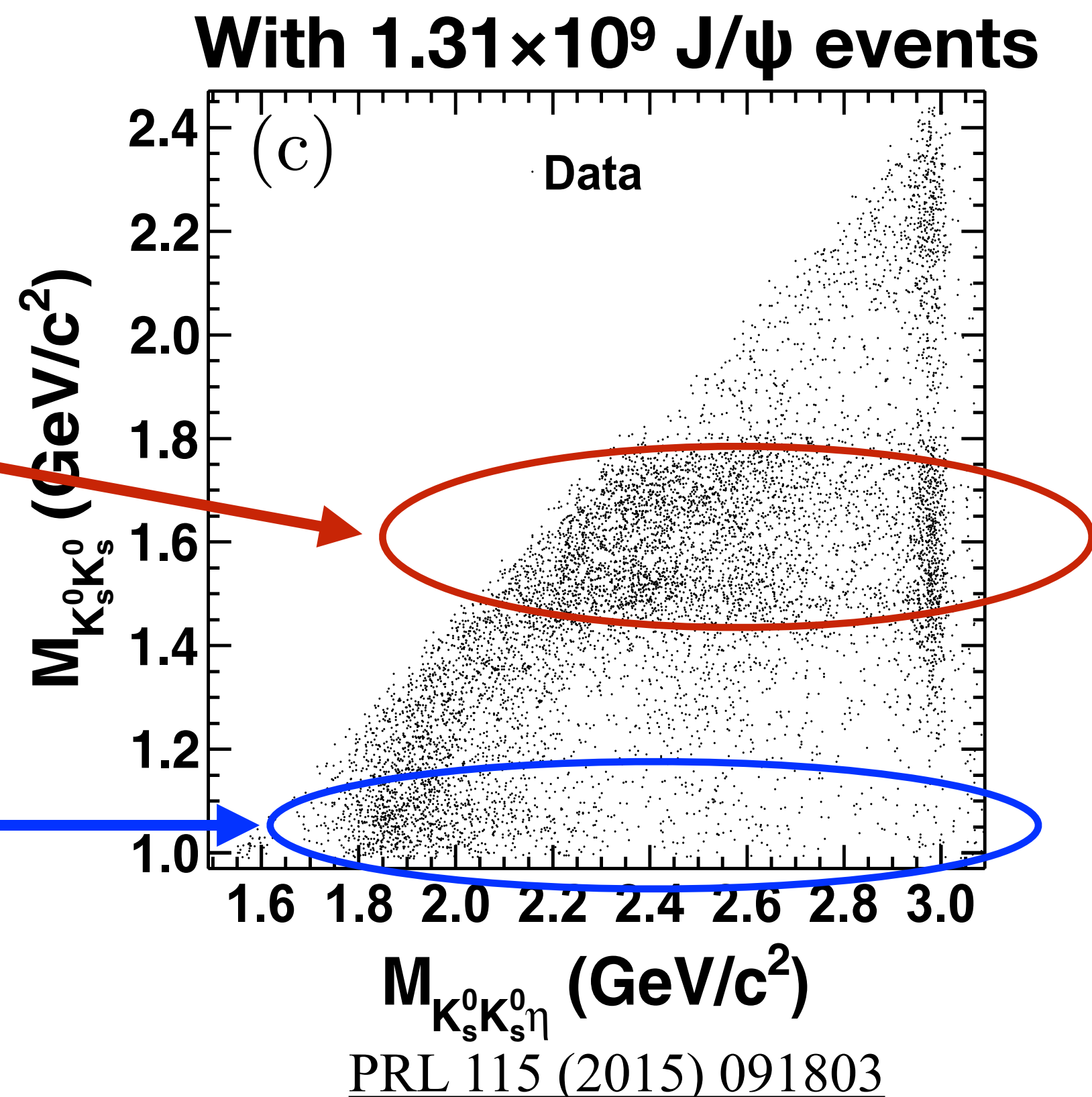
$X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta$

Observation and Spin-Parity Determination of the $X(1835)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta$

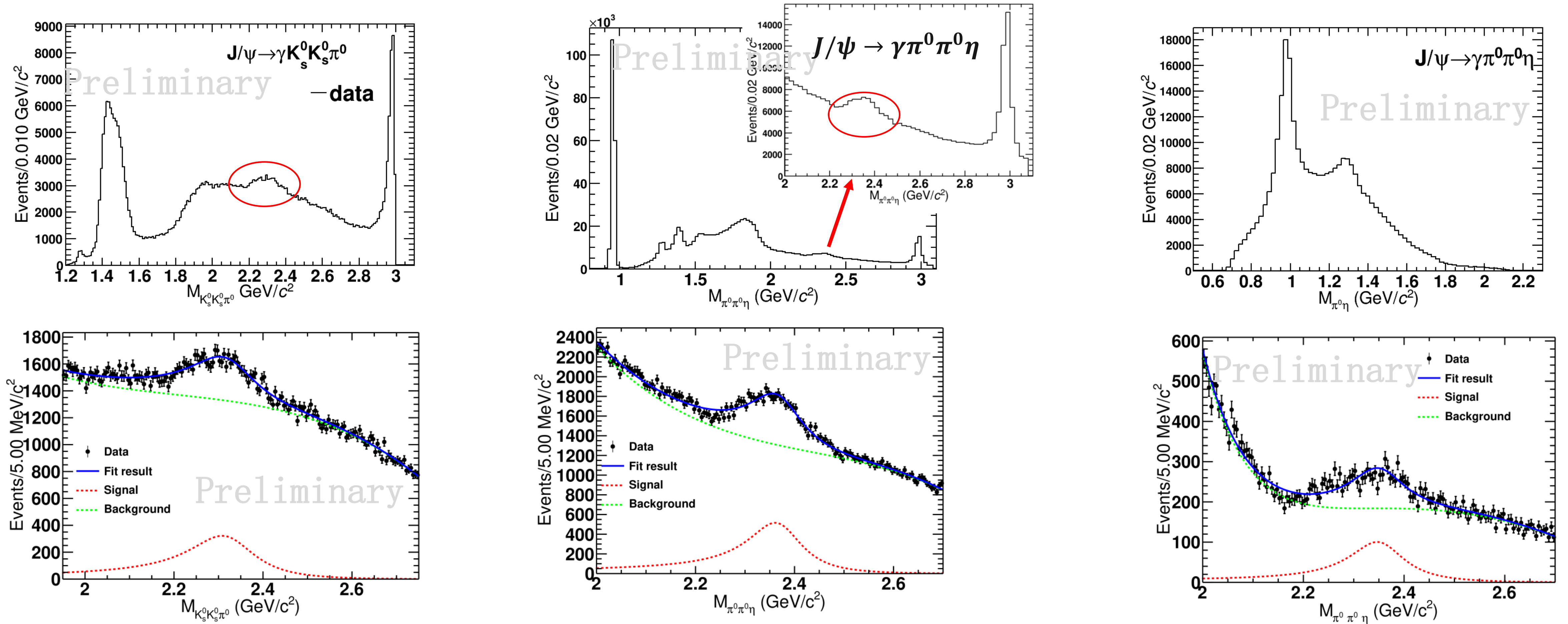
Qualitatively, we can clearly observe: similar decay patterns of the $X(2370)$ and η_c if phase space allows

In the upper KK mass band of 1.5-1.7 GeV range, clear signals of both $X(2370)$ and η_c

In the lower KK mass band of $f_0(980)$, no $X(2370)$, nor η_c



Observation of new decay modes of the X(2370)



First observation of $X(2370) \rightarrow K_s^0 K_s^0 \pi^0$, $X(2370) \rightarrow \pi^0 \pi^0 \eta$ and $X(2370) \rightarrow a(980) \eta$ with **significances $\gg 5\sigma$** and accompanied with η_c

Observation of the X(2370) in the 5 golden decay modes

5 major η_c decay modes (from PDG)
— 5 “Golden” modes in 0^{-+} glueball traditional searches

Decays involving hadronic resonances

Γ_1	$\eta'(958)\pi\pi$	(1.87 ± 0.26) %
Γ_2	$\eta'(958)K\bar{K}$	(1.61 ± 0.25) %

Decays into stable hadrons

Γ_{34}	$K\bar{K}\pi$	(7.0 ± 0.4) %
Γ_{35}	$K\bar{K}\eta$	(1.32 ± 0.15) %
Γ_{36}	$\eta\pi^+\pi^-$	(1.7 ± 0.5) %

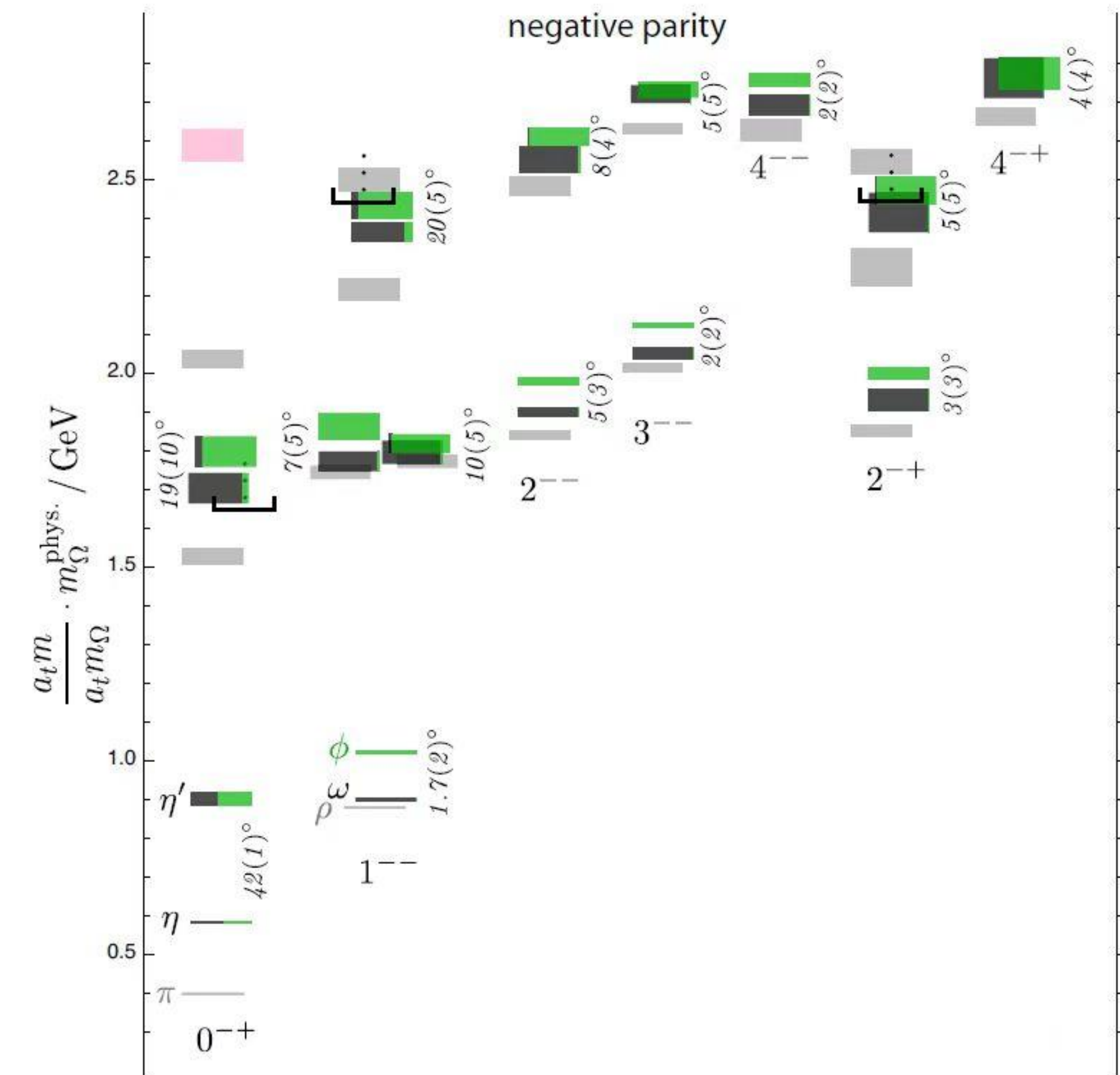
◆ The 0^{-+} glueball decays could be the analogy to η_c decays

- Decay modes of $X(2370) \rightarrow \pi\pi\eta', K\bar{K}\eta', K\bar{K}\pi, \pi\pi\eta, K\bar{K}\eta, a(980)\pi$ observed, consistent with 0^{-+} glueball

Such high similarity between the X(2370) and η_c decay modes strongly supports the glueball interpretation of the X(2370)

Discussion on X(2370) decay properties

- ◆ Normal $q\bar{q}$ mesons, hybrids and multiquark states can hardly explain all 5 decay modes ($\pi\pi\eta'$, $KK\eta'$, $\pi\pi\eta$, $KK\eta$, $KK\pi$) with different quark flavor combinations.
- ◆ e.g., LQCD calculation shows that mixing between $u\bar{u} + d\bar{d}$ and $s\bar{s}$ components should be very small for 0^{-+} $q\bar{q}$ meson at $\sim 2\text{GeV}$
- ◆ The high similarities between X(2370) and η_c decay modes strongly suggest it decays via gluons



PRD 83 (2011) 11502

Narrow Decay Partial Widths of the X(2370)

- ◆ For 5 golden PPP decay modes: similar number of events under the X(2370) peak
 - No dominant decay modes, similar to η_c
- ◆ Naive estimation on the BR of each mode ~5-10%, i.e., partial width of each decay modes is ~10MeV
- ◆ This would be very hard to be explained if there were quark content ($q\bar{q}$, qqg , multiquark) in X(2370) for OZI allowed decays
 - ✦ Typically OZI allowed decay partial width ~100MeV
 - ✦ OZI allowed decays usually have dominant decay modes
- ◆ X(2370) decays should be OZI suppressed decays as η_c , i.e., via gluons!

Discussion on X(2370) properties — Production

- ◆ Richly produced in J/ψ radiative decays — just as glueball expectation
- ◆ In the above 2.3GeV mass region as LQCD 0^{-+} glueball prediction, X(2370) is the **unique** 0^{-+} particle produced in these “5 golden modes” and in J/ψ radiative decays, i.e., no other 0^{-+} particles in this mass region can be called as “richly produced” if they have not shown up in 10 billion such a huge J/ψ data sample.
- ◆ **The production property shows that we only have one qualified candidate X(2370) for 0^{-+} glueball**
- ◆ **We are facing a situation: Either we finally identify X(2370) as 0^{-+} glueball, or LQCD may face a big challenge in the glueball predictions — — similar to the situation before the Higgs boson discovery**

Summary

- ◆ **Glueballs are important predictions from LQCD:**
 - ✦ **Unique particles formed** by gluons (force carriers) due to non-Abelian Gauge self-interactions of gluons
- ◆ **The X(2370) observed in J/ψ radiative decays is the first particle consistent with 0^{-+} glueball**
 - ✦ **Spin-parity quantum numbers** are determined to be $J^{pc} = 0^{-+}$
 - ✦ Measurements and predictions on **mass and rich production rate** are consistent within errors
 - ✦ **Decay properties:** observation of 5 golden decay modes of $\pi\pi\eta', K\bar{K}\eta', K\bar{K}\pi, \pi\pi\eta, K\bar{K}\eta, a(980)\pi$ (in analogy to η_c)
 - **Glueball-like particle, X(2370) is discovered by BESIII**

Golden decay modes in 0^{-+} glueball search

- ◆ Typically, PPP (3 pseudoscalar mesons, such as $\pi\pi\eta$, $\pi\pi\eta'$, $KK\pi$) modes are believed as golden decay modes in 0^{-+} glueball searches
 - ◆ S wave decays for 0^{-+} mesons, no suppression factor, dominant decay modes
 - ◆ PPP modes are strongly suppressed in 0^{++} , 2^{++} meson decays — spin-parity filter
- ◆ PP (2 pseudoscalar mesons) modes are mostly forbidden for 0^{-+} mesons
- ◆ VV (2 vector mesons, such as $\omega\omega$, $\phi\phi$, $\rho\rho$, K^*K^*)
 - ◆ P wave decays for 0^{-+} mesons — suppressed decays, especially near mass threshold
 - ◆ All J^{PC} mesons allowed, not a spin-parity filter
- ◆ Baryon modes
 - ◆ All J^{PC} mesons allowed, not a spin-parity filter

Interpretation

	X(2370)	η_c	Interpretation on the X(2370)
$f_0(980)\eta'$	✓	✓	Disfavors $q\bar{q}$ meson with pure $u\bar{u}/d\bar{d}$ component
$f_0(980)\eta$	Suppressed	Suppressed	Disfavors $q\bar{q}$ meson with pure $s\bar{s}$ component
$f_0(1500)\eta$	✓	✓	Disfavors $q\bar{q}$ meson with pure $s\bar{s}$ component

◆ **The X(2370) decay properties observed:** **disfavor the interpretation of $q\bar{q}$ meson**

- ◆ Observed decay modes (η_c dominant decays) and suppressed decay modes are consistent between the X(2370) and η_c
- ◆ A good agreement with the glueball interpretation

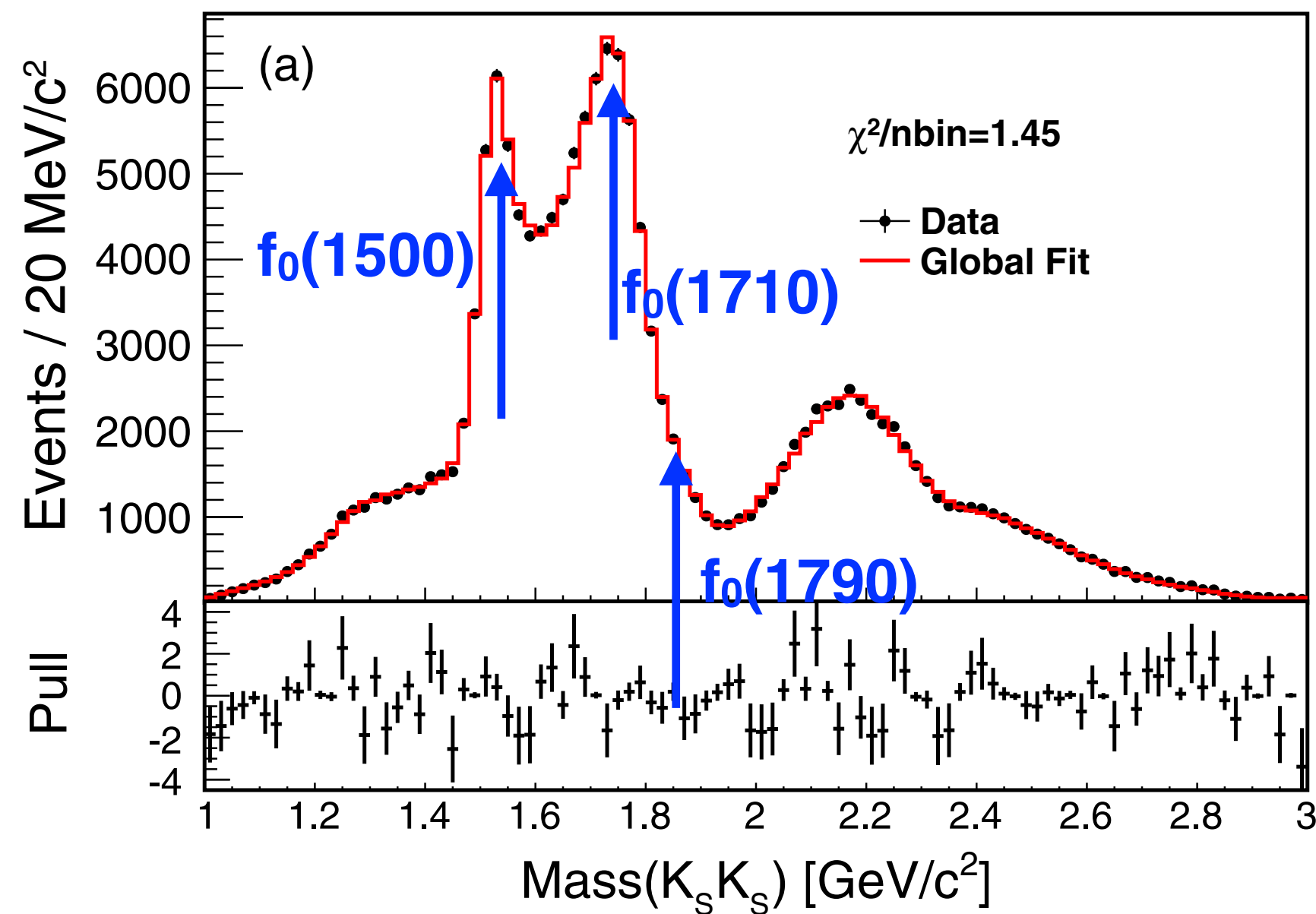
◆ **The X(2370) production properties observed:**

- ◆ richly produced in J/ψ radiative decays as the glueball expectation

◆ **Mass, spin-parity:** consistent with 0^{-+} glueball prediction

In the mass region larger than 2GeV, the only particle X(2370) for the 0^{-+} glueball candidate in J/ψ radiative decays and five golden decay modes ($\pi\pi\eta', K\bar{K}\eta', K\bar{K}\pi, \pi\pi\eta, K\bar{K}\eta$)

Historical Glueball Candidates — Scalar $f_0(1710)$



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$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma \pi \pi] = (4.0 \pm 1.0) \times 10^{-4}$$

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$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma K_s^0 K_s^0] = (2.00^{+0.03}_{-0.02} \quad {}^{+0.31}_{-0.10}) \times 10^{-4}$$

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- ◆ **Controversy:** with PS subtraction, $\Gamma(f_0(1710) \rightarrow \pi\pi:KK) = 1:2.43$, in contrast to the flavor symmetry property of a pure glueball
- ◆ **Difficulty:** needs to be understood from **first principle of QCD** (not just phenomenological understanding)
 - ◆ What causes the **flavor symmetric breaking**?
 - ◆ **Dynamic mixing mechanism:** mixing between $f_0(1500)/f_0(1710)$, or even with $f_0(1790)$

Improved situation in Glueball Searches

◆ Experimentally:

- ◆ **World largest J/ψ data sample : ~10 billion**
- ◆ **Physics channels with few background**
- ◆ **GPU technique helps to speed up PWA** [J.Phys.Conf. Ser. 219, 042031]
 - ◆ It takes a long time in PWA for the complicated interference and comprehensive test of different combinations

◆ Theoretically:

- ◆ **Guidance from η_c decays**
- ◆ Now we have prediction on **glueball production rate from LQCD**: $B(J/\psi \rightarrow \gamma G_{0-+}) = 2.31 \pm 0.80 \times 10^{-4}$
- ◆ Luckily, for the $X(2370)$, there is **no other 0^{-+} resonance nearby** (in $\sim 200\text{MeV}$ range) in J/ψ radiative decays

Many thanks to the efficient work:

**The BESIII detector maintenance and offline software teams, computing center
The BEPCII accelerator operation team which provide stable detector operation**