

# Recent Measurements of Hypernuclei Properties and Production from STAR BES II

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GSI

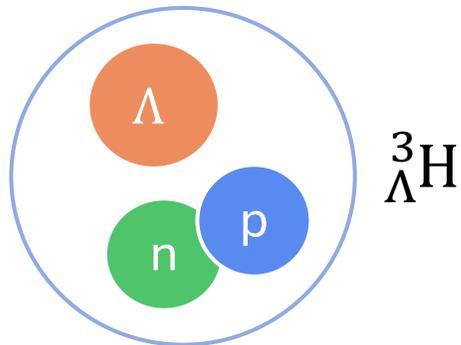
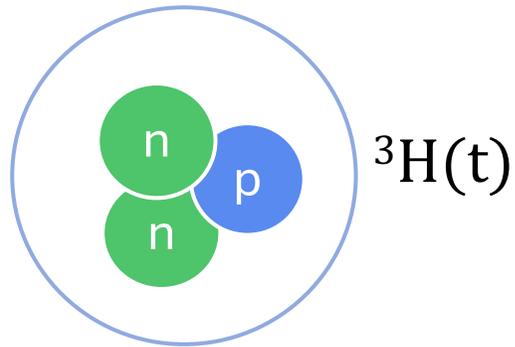
Jan 3<sup>rd</sup>, 2024, UCAS

# What are Hypernuclei?

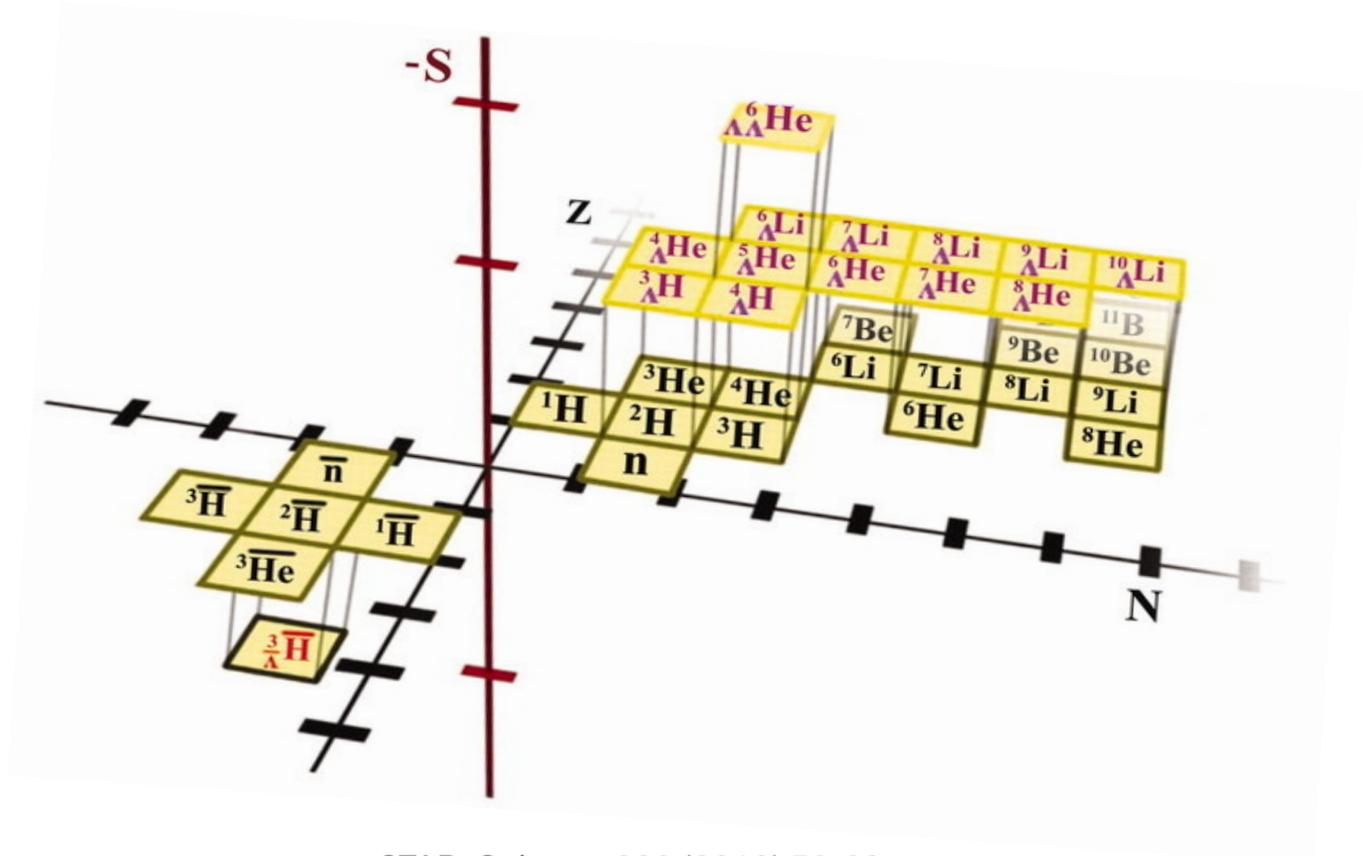
Hypernucleus: A bound system of nucleons with  $\geq 1$  hyperon.

Hyperon: A baryon with  $\geq 1$  strange quark (e.g.  $\Lambda$ ,  $\Xi$ ,  $\Omega$  etc).

Additional dimension in chart of nuclides



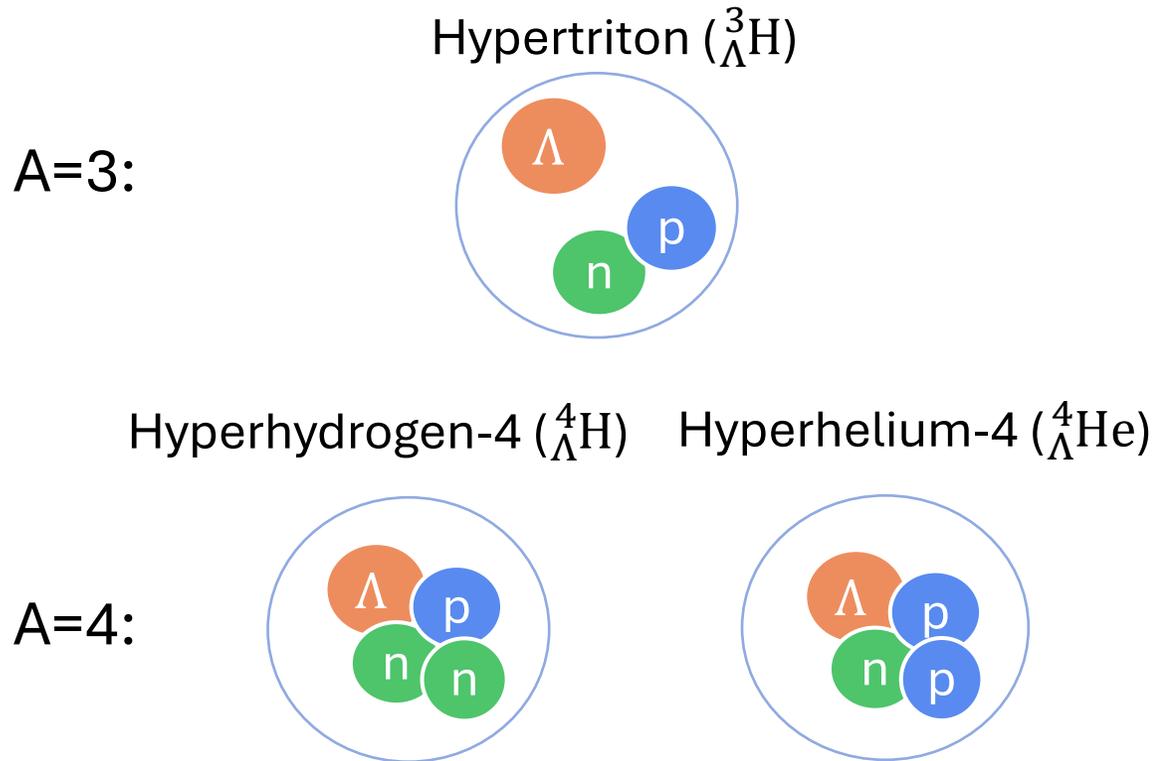
lightest hypernucleus



# Hypernuclei and Hyperon-Nucleon (Y-N) Interaction

## Hypernuclei -> probe to Y-N (Y-N-N) interaction

- Inner structure governed by interactions between nucleons (and hyperons)



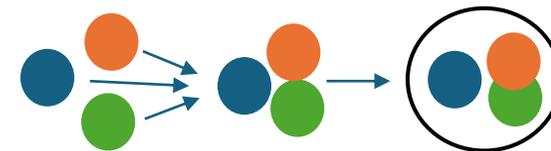
## Observables in heavy ion collisions

### Intrinsic Properties

- How tight they bind together
- Internal spin structure
- How they decay: lifetime, branching ratio

### Production mechanism

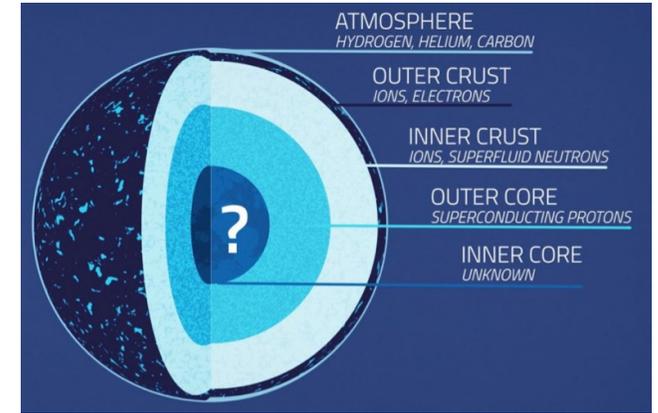
- How they form in heavy ion collisions
  - Collectivity, production yields



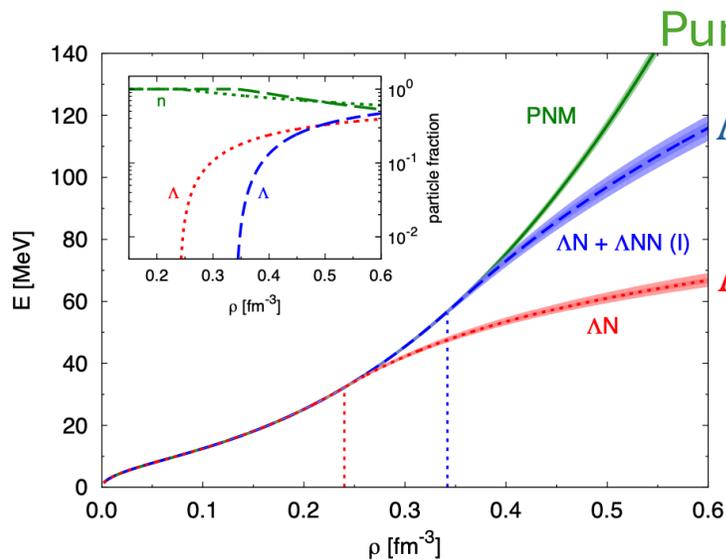
# Y-N Interaction, EoS and Astrophysics

- **Equation of State (EoS) in dense nuclear matter**
  - The strangeness degree of freedom in EoS at high baryon density region
- High baryon density nuclear matter
  - e.g. low energy HIC, neutron stars

Compact star



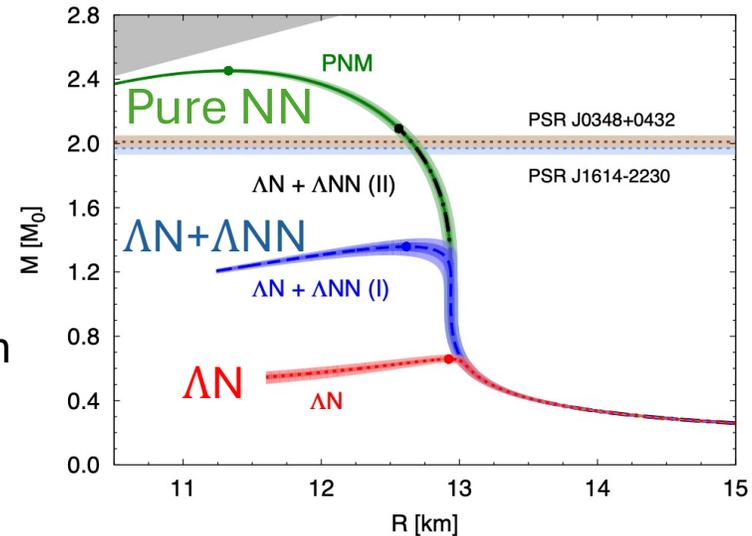
“Hyperon puzzle”



Nuclear matter EoS

D. Lonardoni, et al. PRL 114, 092301 (2015)

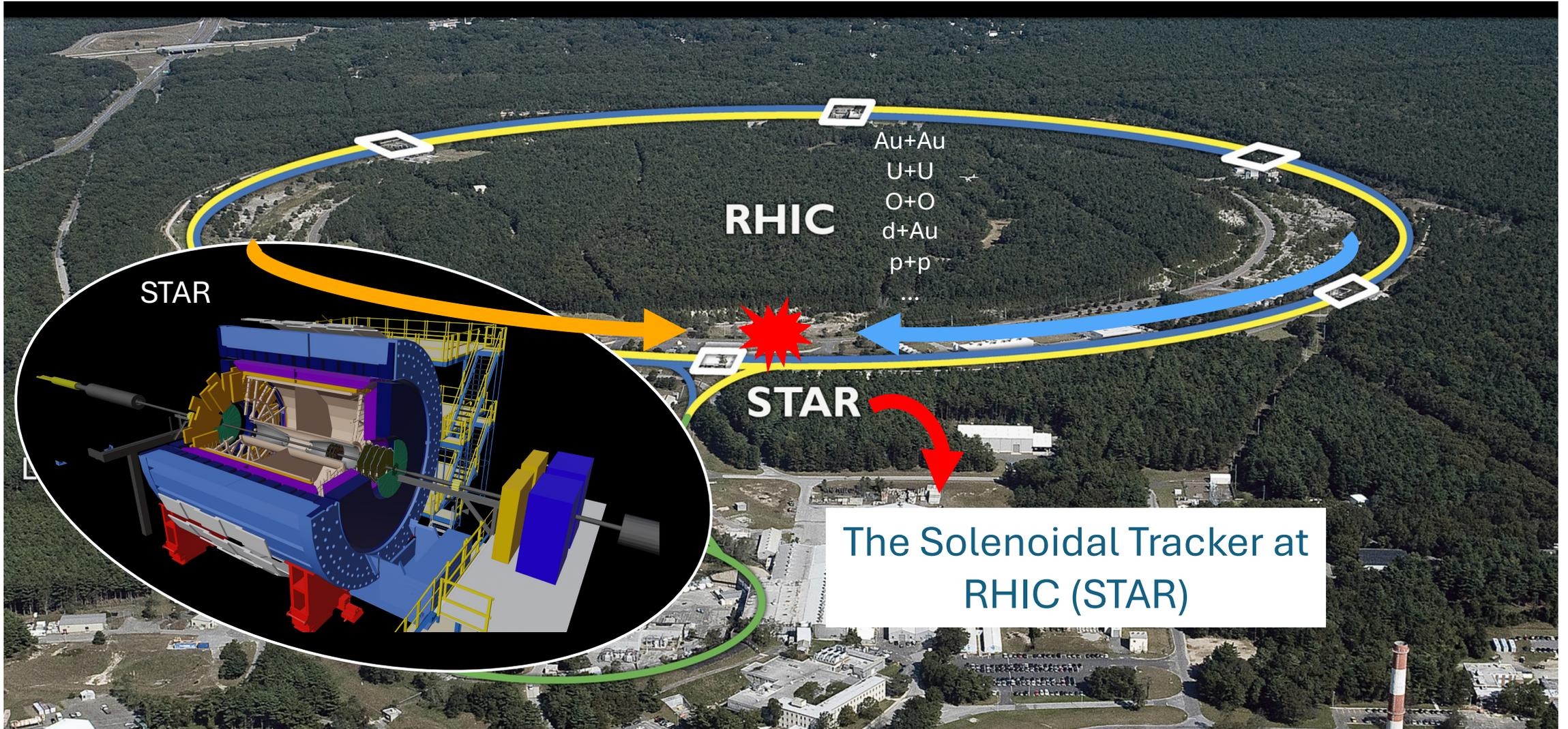
Presence of hyperon soften EoS



Mass vs R

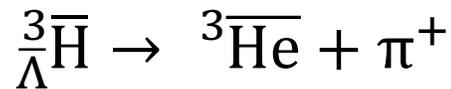
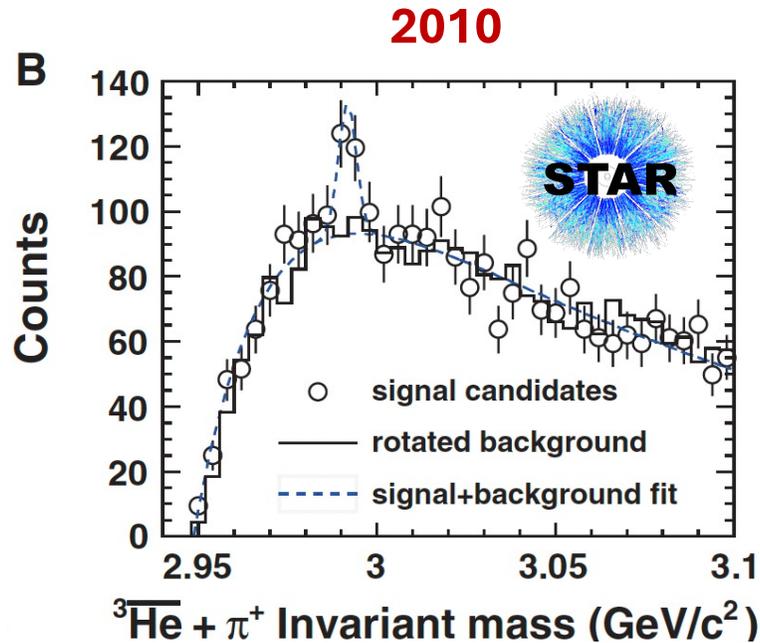
Observed heavy neutron stars

# RHIC and The STAR Detector

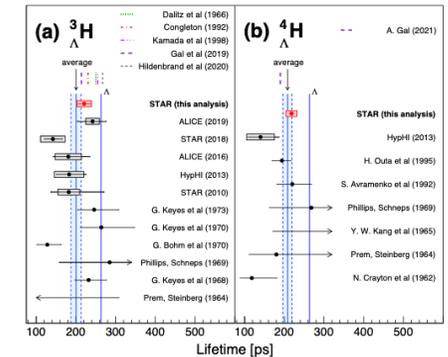
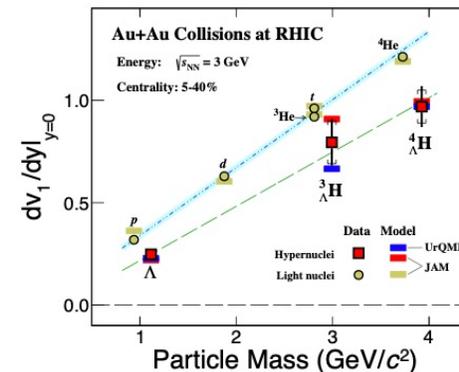
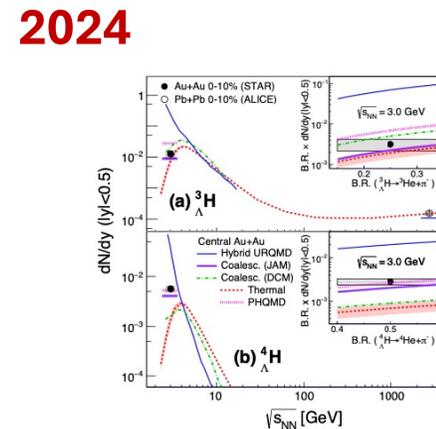
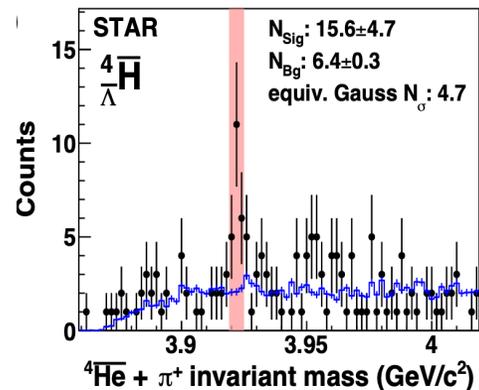
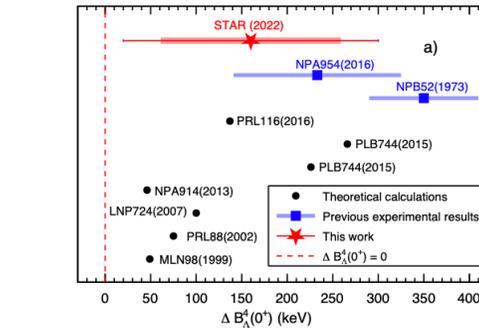


# Previous Hypernuclei Measurements at STAR

- STAR observed  $\frac{3}{\Lambda}\overline{\text{H}}$  in 2010
  - Starting of hypernuclei measurements at STAR



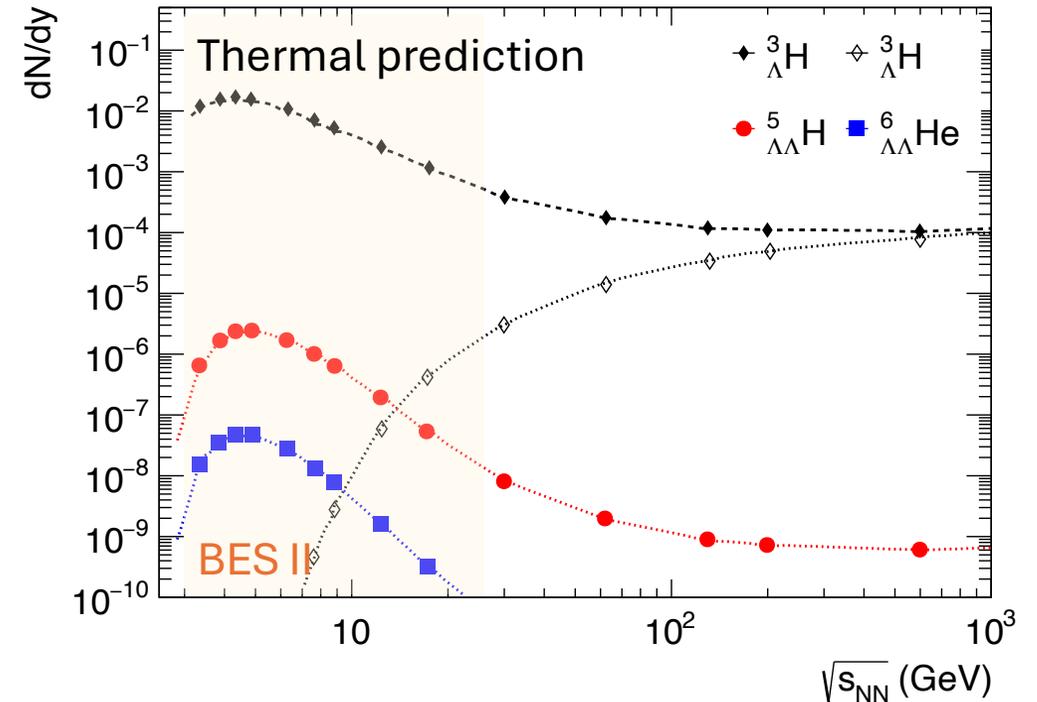
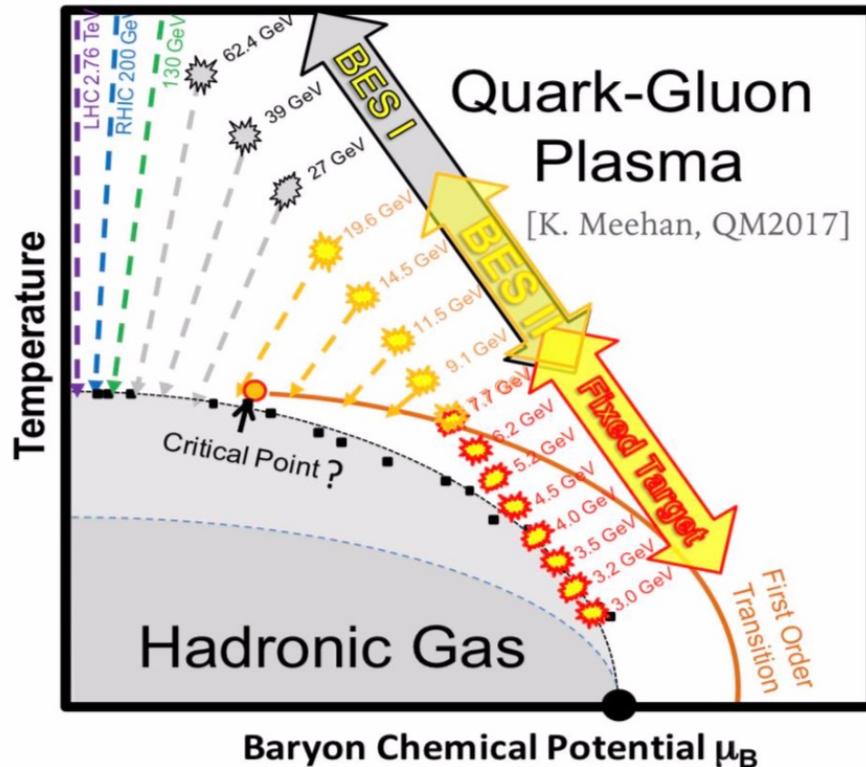
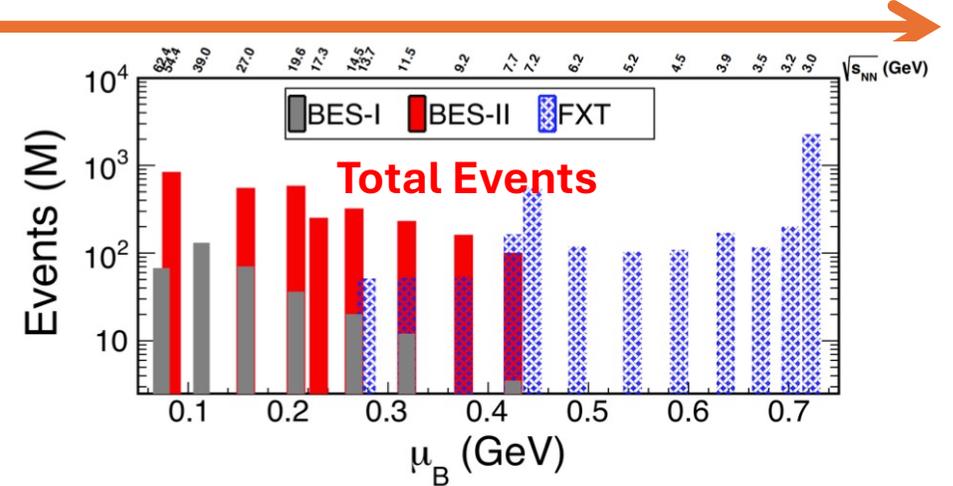
Science 328 (2010) 58-62



Today's talk would focus on hypernuclei production yields measurements.

# STAR Beam Energy Scan II (BES II)

- Mapping the QCD diagram in the region of  $200 < \mu_B \leq \sim 750 \text{ MeV}$ 
  - Collisions species: Au+Au
  - Collider mode:  $\sqrt{s_{NN}} = 7.7 - 27 \text{ GeV}$
  - Fixed-Target mode:  $\sqrt{s_{NN}} = 3.0 - 7.7 \text{ GeV}$



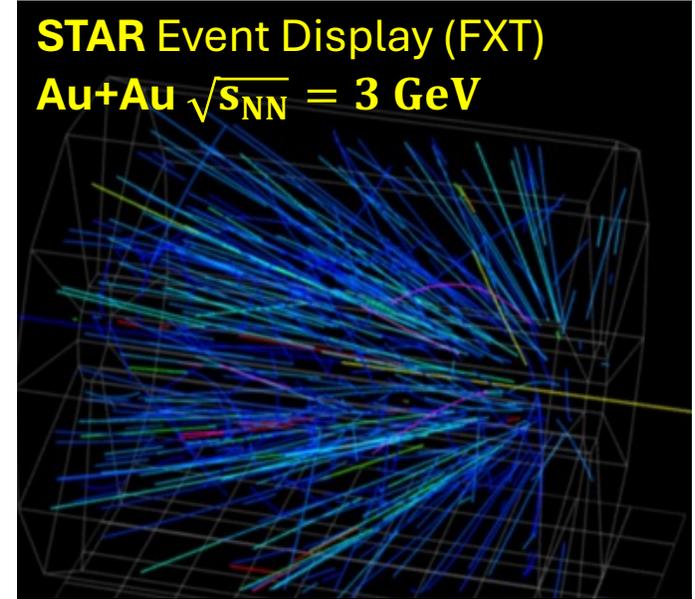
Thermal model: B. Dönigus, Eur. Phys. J. A 56:280 (2020)  
A. Andronic et al, PLB 697, 203 (2011)

# Fixed-Target Setup at STAR

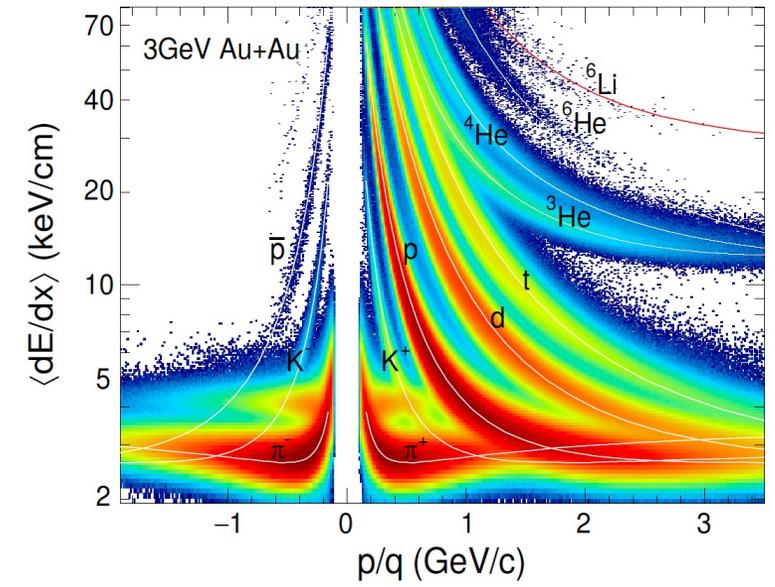
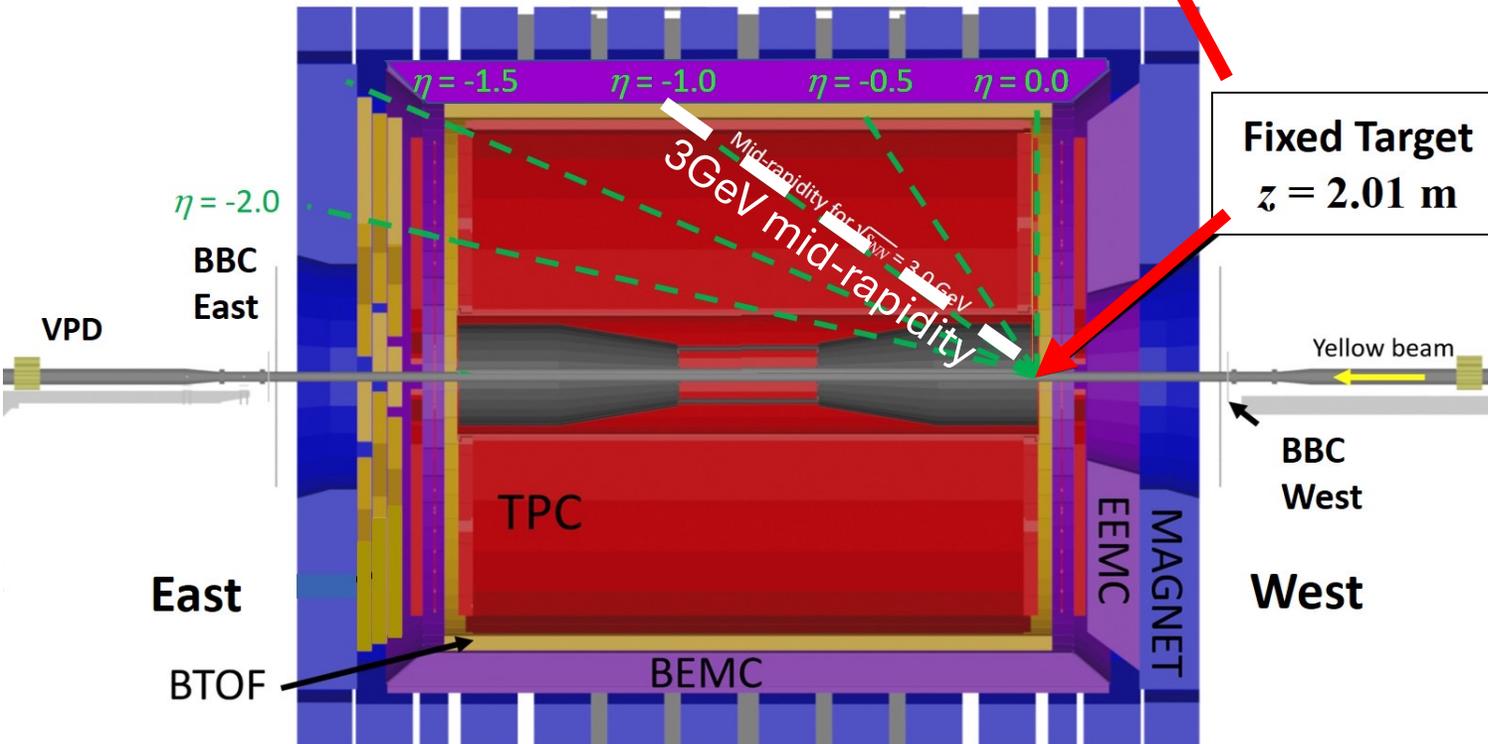
Gold foil,  
250  $\mu\text{m}$  thick



STAR Event Display (FXT)  
Au+Au  $\sqrt{s_{NN}} = 3 \text{ GeV}$



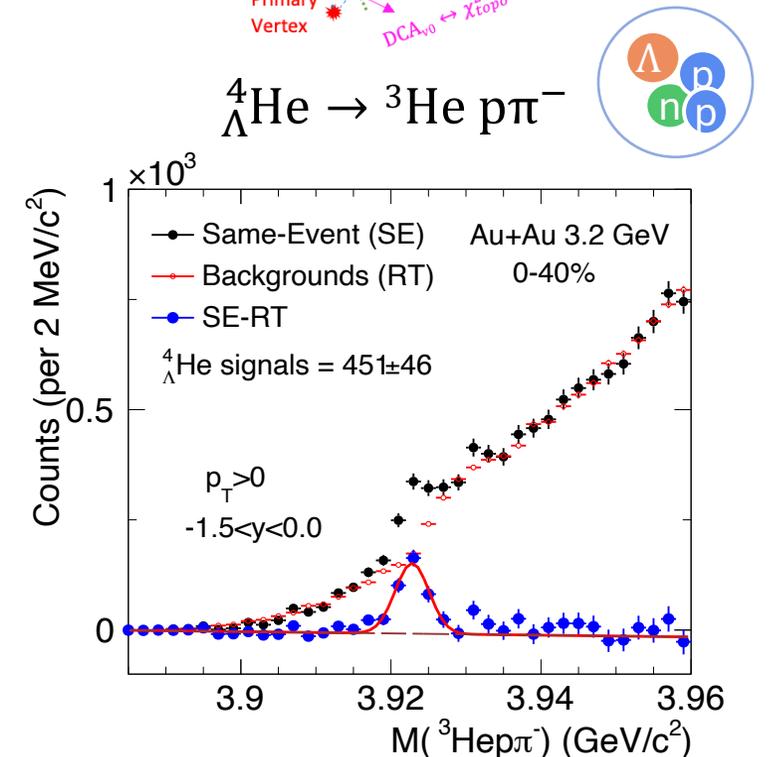
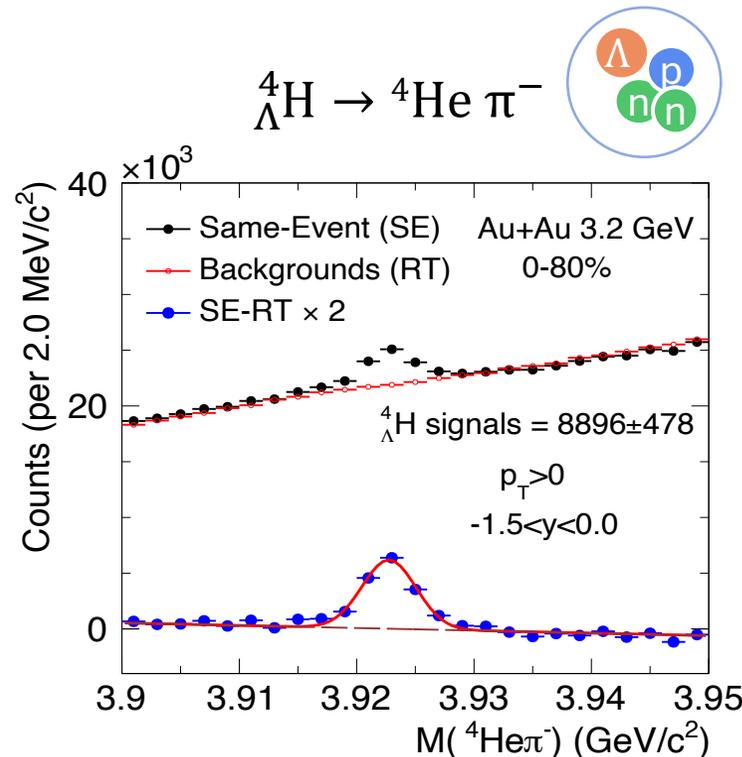
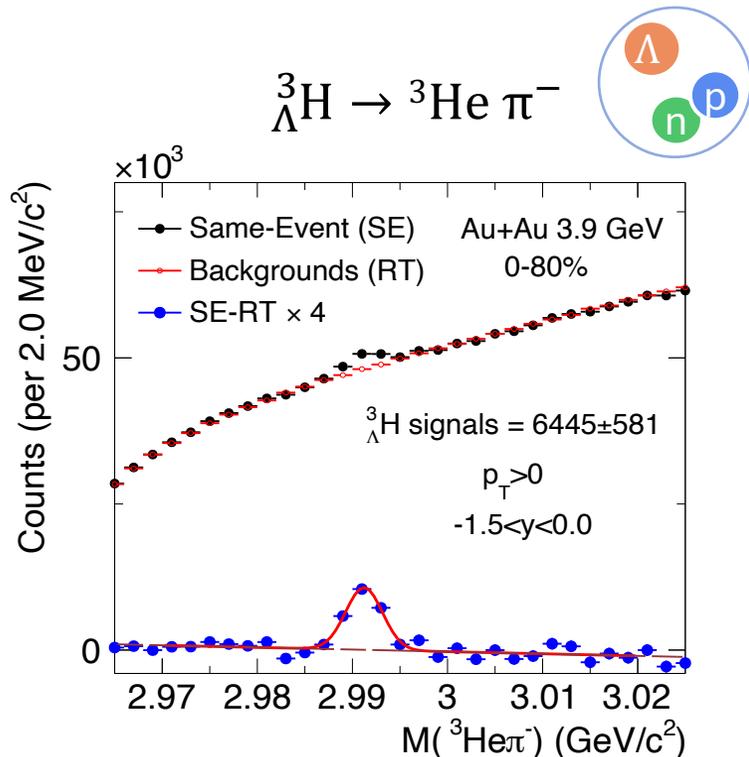
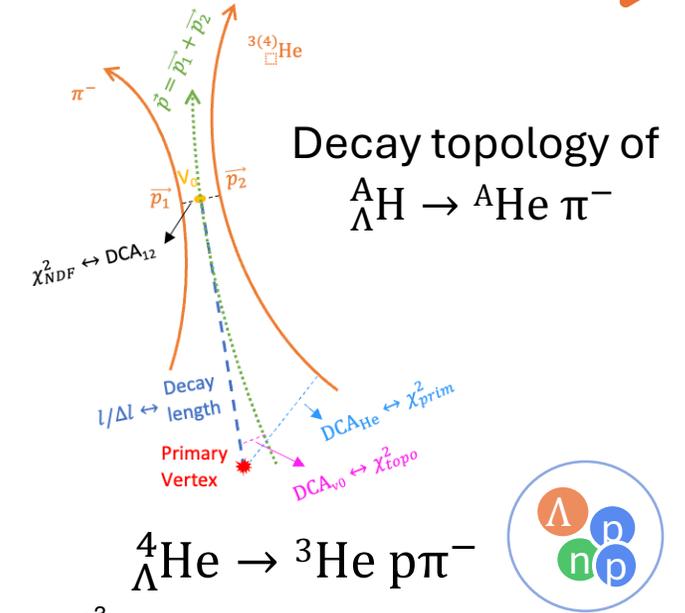
Fixed Target  
 $z = 2.01 \text{ m}$



# Hypernuclei reconstruction at STAR

- Signals are reconstructed by KFParticle package.
  - Combinatorial backgrounds reconstructed by rotation of  ${}^3({}^4)\text{He}$  tracks.

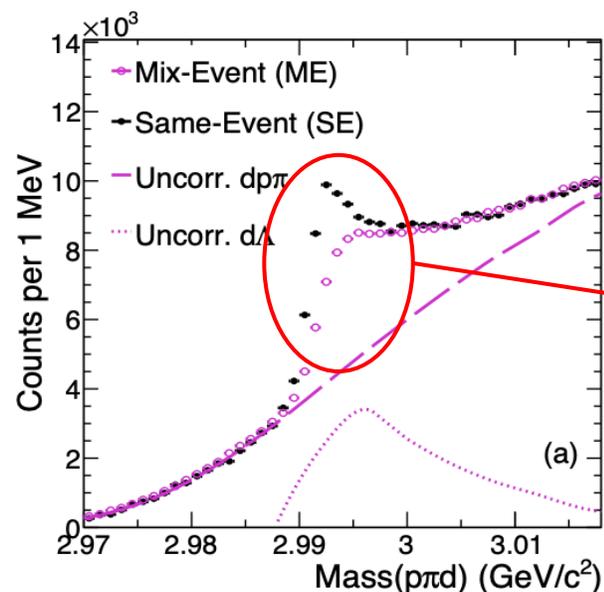
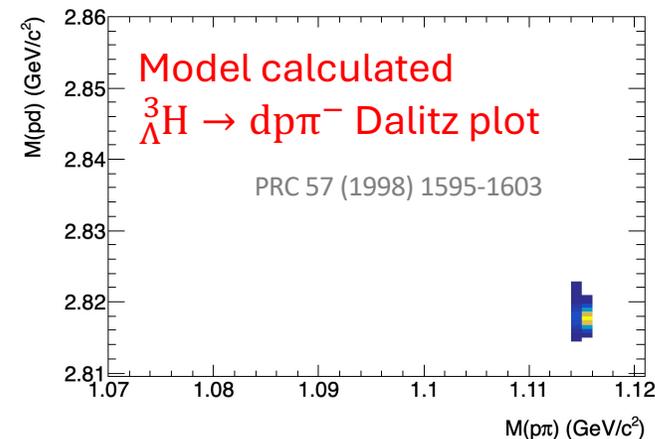
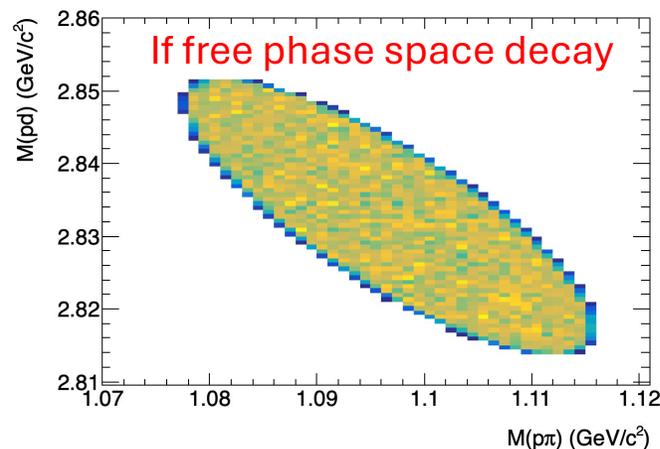
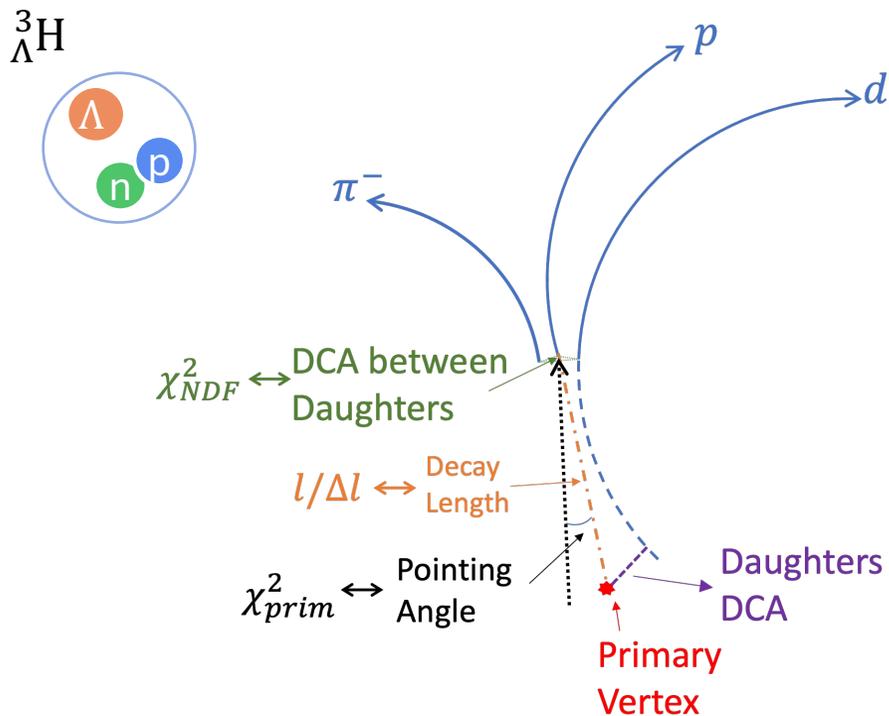
X. Ju et al. Nucl. Sci. Tech. 34, 10, 158 (2023)



# ${}^3_{\Lambda}\text{H}$ reconstruction via 3-body channel

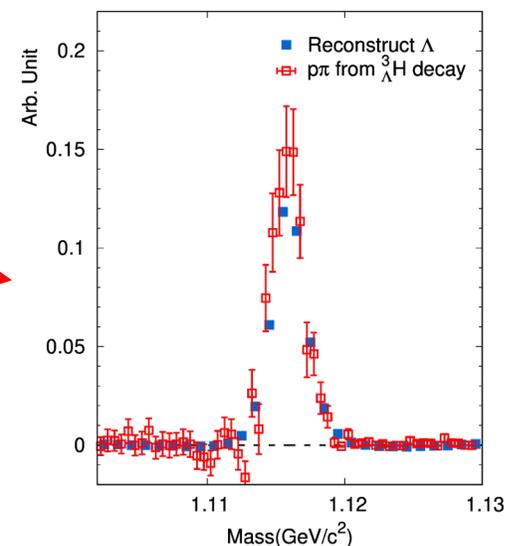
${}^3_{\Lambda}\text{H} \rightarrow dp\pi^{-}$ , B.R.  $\sim 40\text{-}50\%$   
 ${}^3_{\Lambda}\text{H} \rightarrow {}^3\text{He}\pi^{-}$ , B.R.  $\sim 15\text{-}25\%$

- ${}^3_{\Lambda}\text{H}$ : Simplest hypernuclei system
- ${}^3_{\Lambda}\text{H}$  decay topological distribution very similar as  $\Lambda+d$



Au+Au  $\sqrt{s_{NN}}=3$  GeV  
 0-50%  
 $-1 < y < 0$   
 $1 < p_T < 3$  GeV/c

Real  $\Lambda$  and  $(p\pi)$  from  ${}^3_{\Lambda}\text{H}$  decay



# Correlated $\Lambda d$ contamination in ${}^3_{\Lambda}\text{H} \rightarrow d p \pi^-$ signal

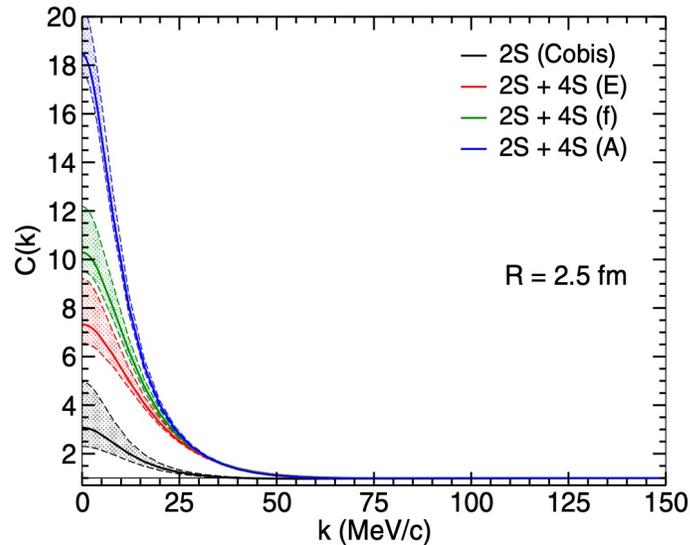
- $\Lambda d$  may have kinematic correlations according to theory calculation.

$$C(k^*) = \frac{P(\Lambda d)}{P(\Lambda)P(d)}, \text{ p is the possibility of finding particle}$$

No correlation  $\rightarrow C(k^*)=1$ .

$k^* \rightarrow$  relative momentum between  $\Lambda$  and  $d$ .

PRC 102, 034001 (2020)



Model predicts peak structure in  $C(k^*)$  at  $k^* \rightarrow 0$ .

When  $k^*=0$ , in  $\Lambda$  and  $d$  pair CMS framework:

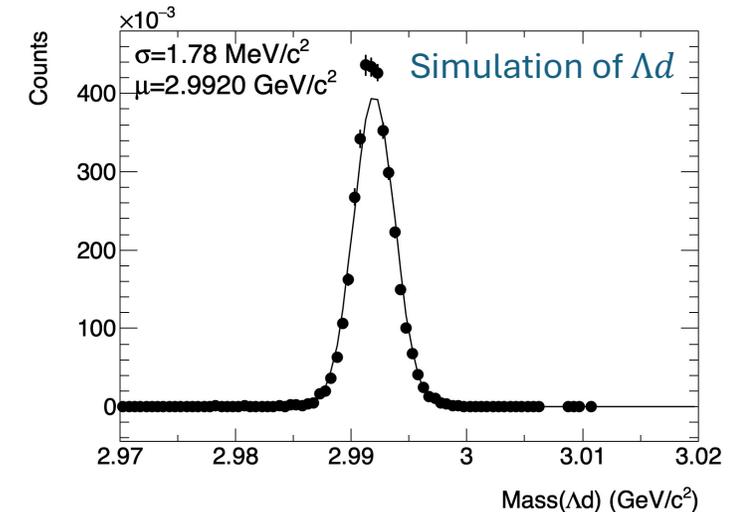
$$p_{\Lambda} = -p_d = 0$$

$$P(\Lambda) : (p_{\Lambda}, E_{\Lambda}) = (0, m_{\Lambda})$$

$$P(d) : (p_d, E_d) = (0, m_d)$$

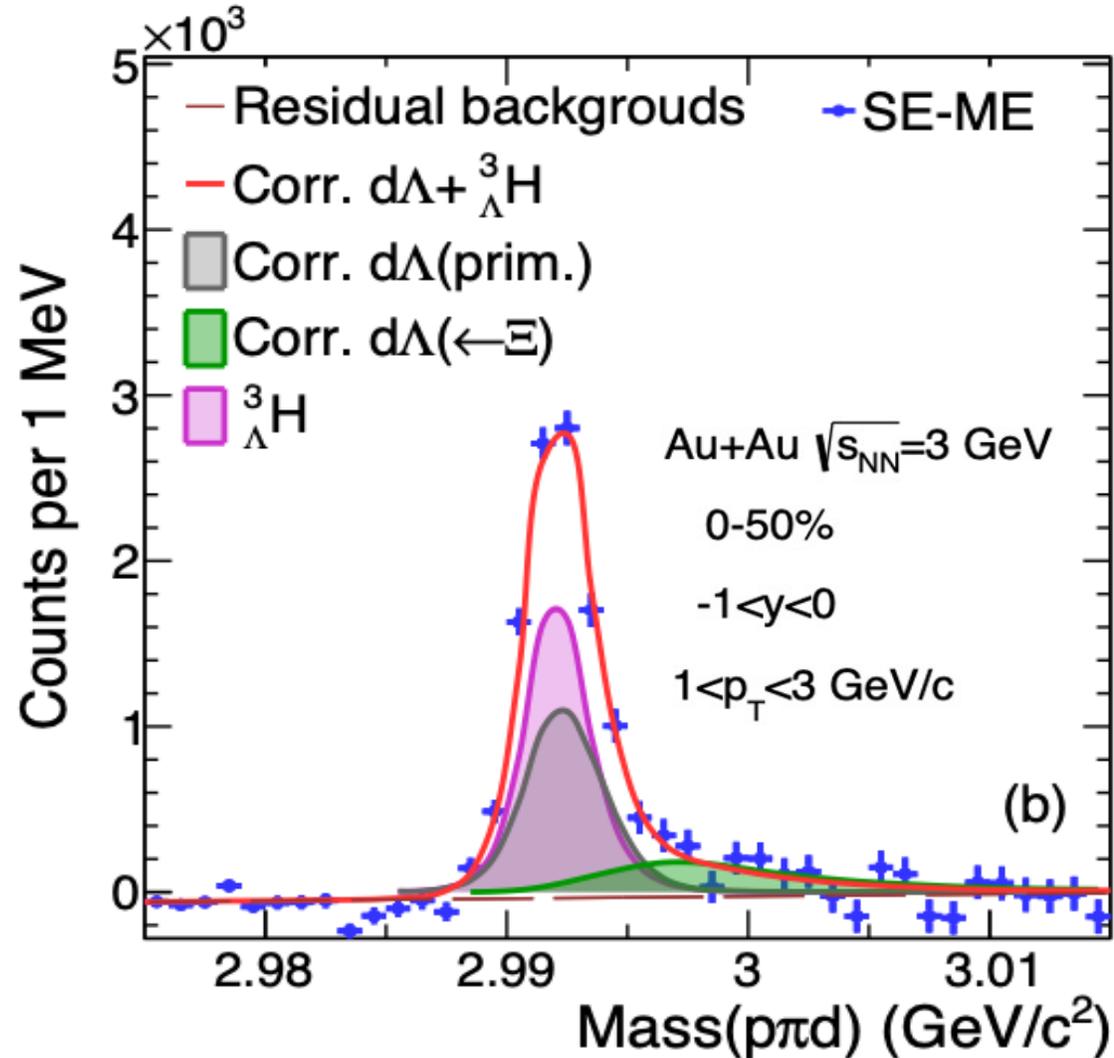
$$\rightarrow P(\Lambda d) : (p_{\Lambda} + p_d, E_{\Lambda} + E_d) = (0, m_{\Lambda} + m_d)$$

Set  $C(k^*)$  weight on uncorrected  $\Lambda$  and  $d$



- Correlated  $\Lambda d$  could form a peak near  $M({}^3_{\Lambda}\text{H})$  even after subtracting combinatorial background.
  - $M(\Lambda) + M(d) \sim 2.9913 \text{ GeV}/c^2$ ,  $M({}^3_{\Lambda}\text{H}) \sim 2.991 \text{ GeV}/c^2$ .

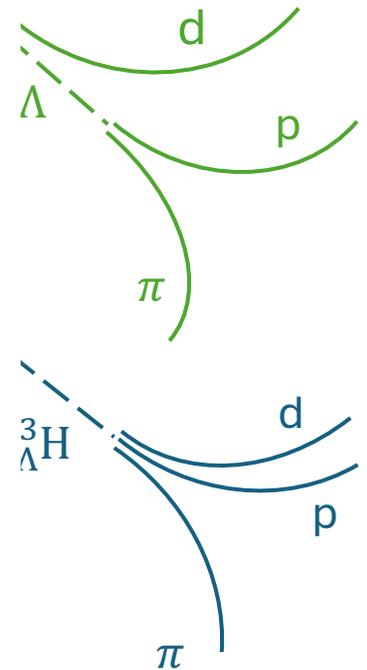
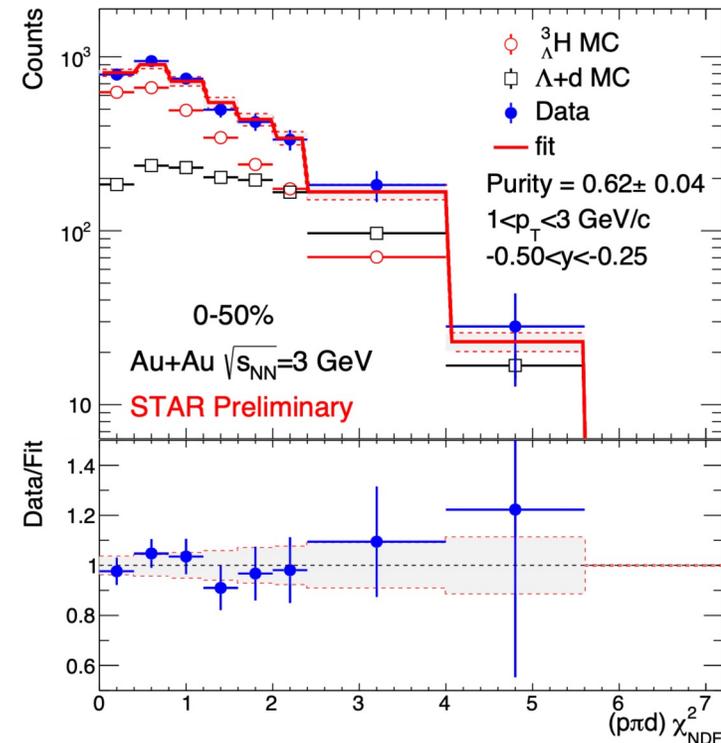
# ${}^3\Lambda$ H reconstruction via 3-body channel

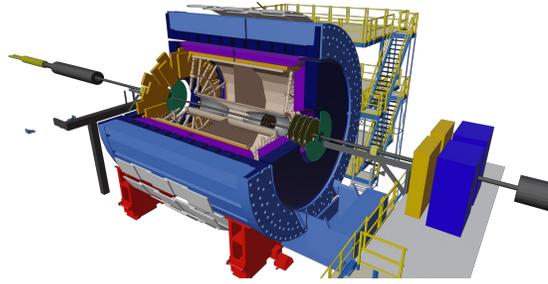
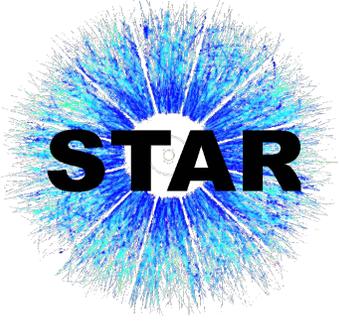


- Template fit method to estimate  ${}^3\Lambda$  H purity statistically.

- $\chi_{NDF \Lambda d}^2, \chi_{NDF {}^3\Lambda}^2$  template estimated from simulations.

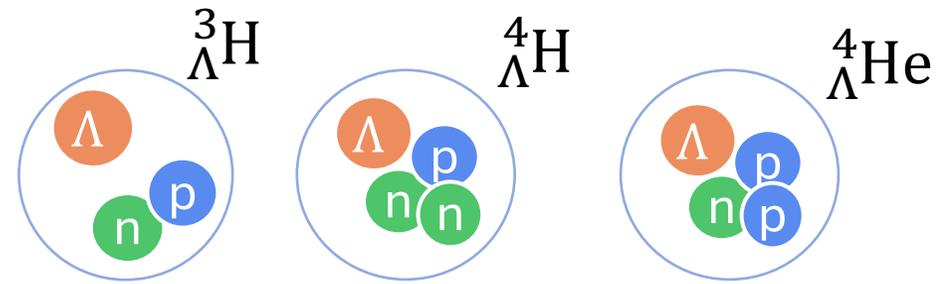
$$\chi_{NDF Data}^2 = p_0 \cdot (\chi_{NDF \Lambda d}^2 + p_1 \cdot \chi_{NDF {}^3\Lambda}^2)$$





# Measurements on Hypernuclei

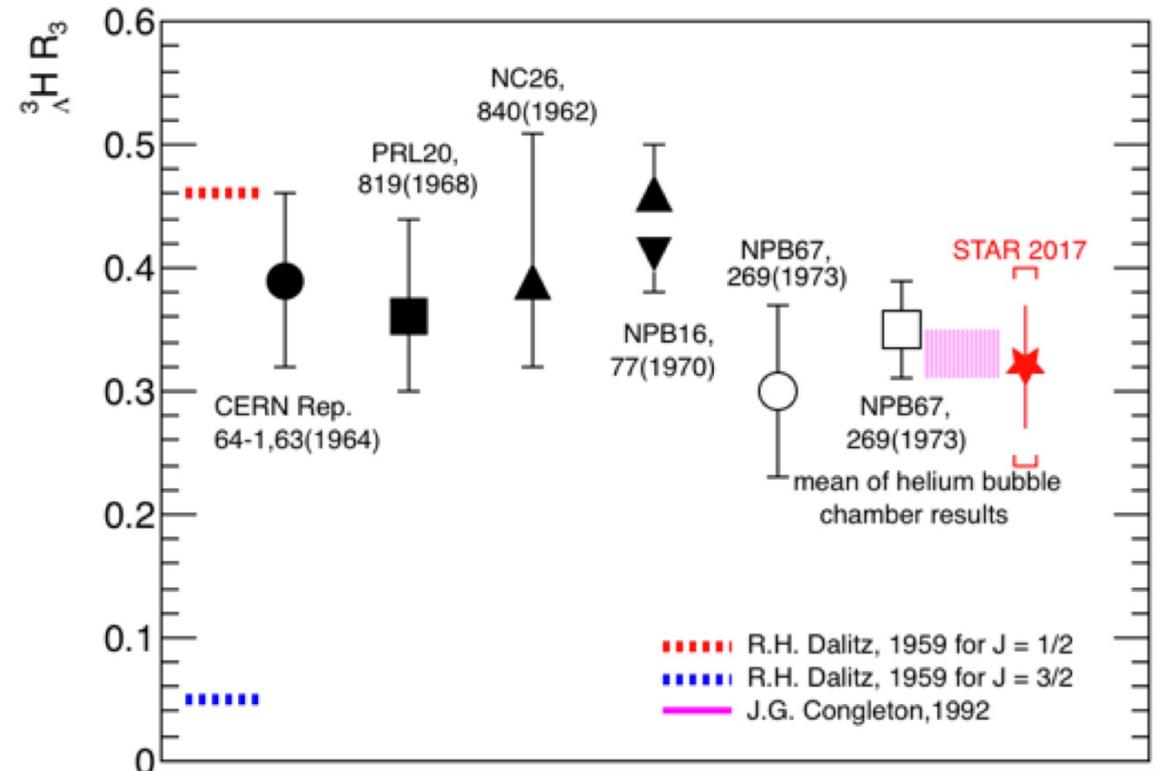
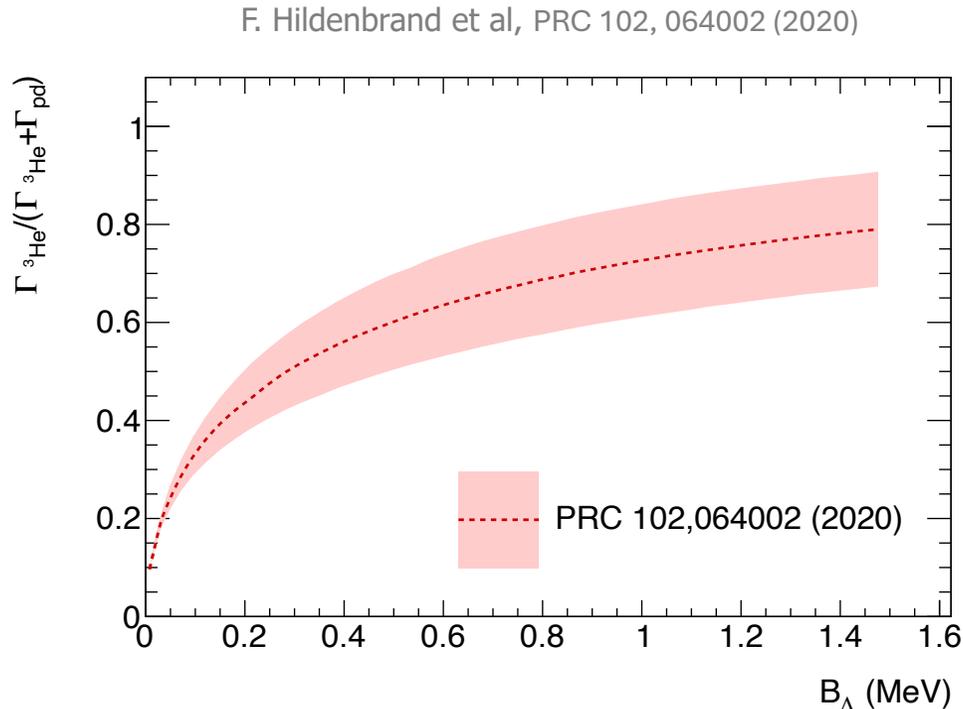
## Branching ratio



# ${}^3_{\Lambda}\text{H}$ Branching Ratio $R_3$

- Calculations propose that  ${}^3_{\Lambda}\text{H}$   $R_3$  may be sensitive to  $\Lambda$  separation energy  $B_{\Lambda}$ 
  - ${}^3_{\Lambda}\text{H}$   $B_{\Lambda} = M(d) + M(\Lambda) - M({}^3_{\Lambda}\text{H})$
- Sensitive to  ${}^3_{\Lambda}\text{H}$  spin states
- Global uncertainty for yields measurements

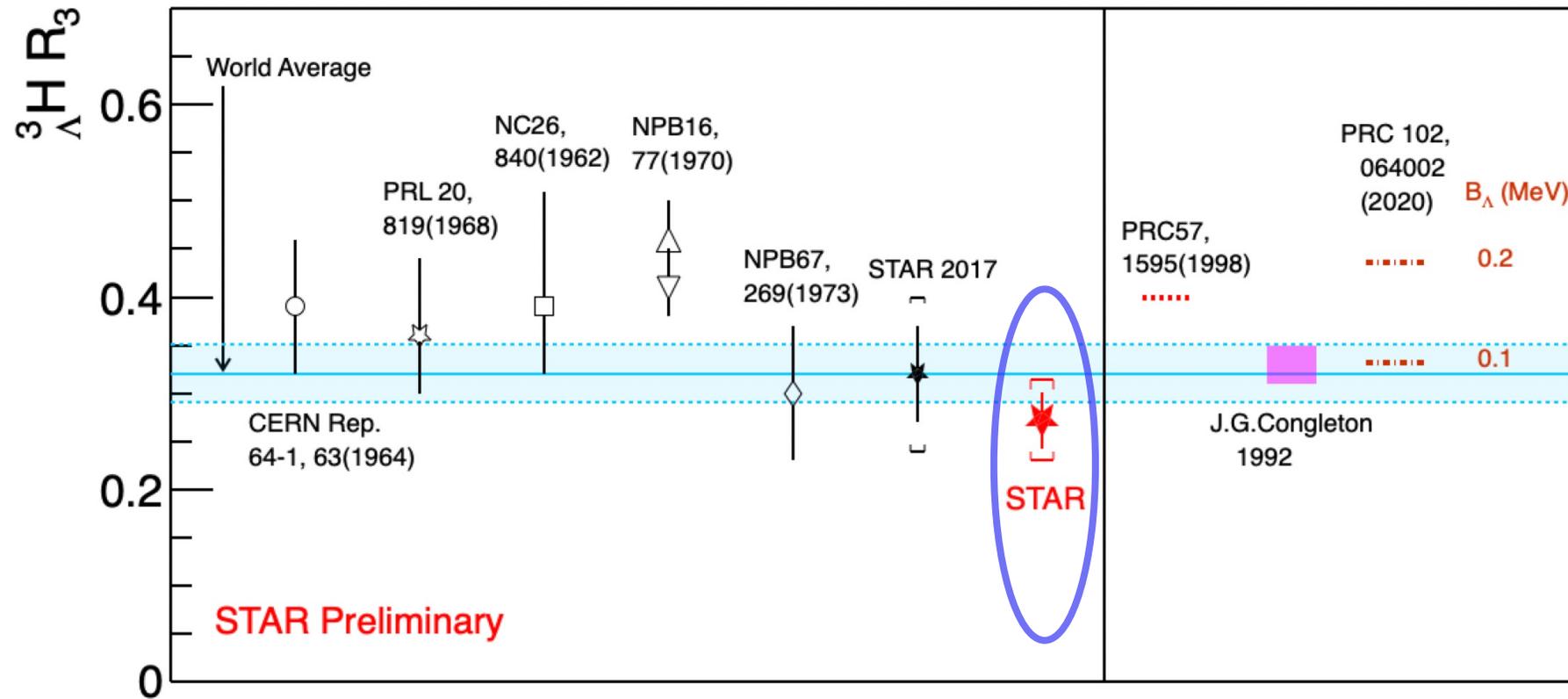
$$R_3 = \frac{\text{B. R. } ({}^3_{\Lambda}\text{H} \rightarrow 3\text{He}\pi^-)}{\text{B. R. } ({}^3_{\Lambda}\text{H} \rightarrow \text{pd}\pi^-) + \text{B. R. } ({}^3_{\Lambda}\text{H} \rightarrow 3\text{He}\pi^-)}$$



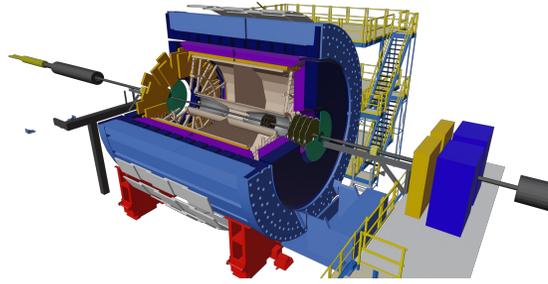
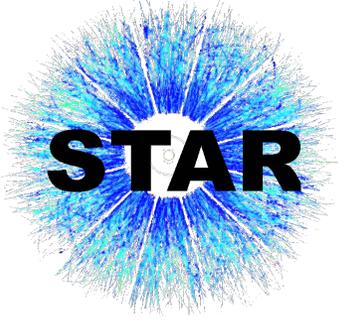
# ${}^3_{\Lambda}\text{H}$ Branching Ratio $R_3$

$$R_3 = \frac{\text{B. R. } ({}^3_{\Lambda}\text{H} \rightarrow 3\text{He}\pi^-)}{\text{B. R. } ({}^3_{\Lambda}\text{H} \rightarrow \text{pd}\pi^-) + \text{B. R. } ({}^3_{\Lambda}\text{H} \rightarrow 3\text{He}\pi^-)}$$

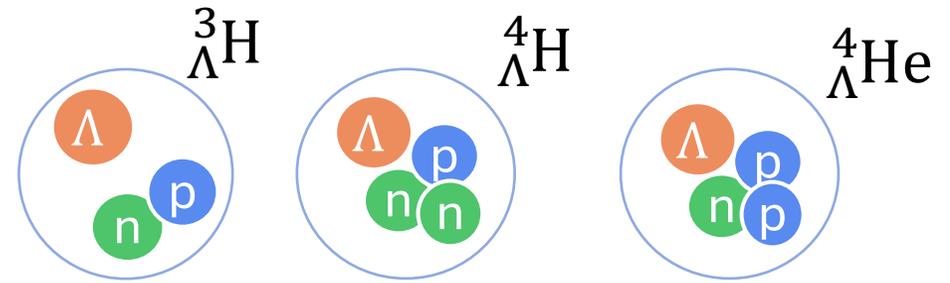
STAR:  $R_3 = 0.272 \pm 0.030 \pm 0.042$



- STAR new  $R_3$  data favors small binding energy of hypertriton.



# Measurements on Hypernuclei Production at STAR



# Hypernuclei Production in HIC

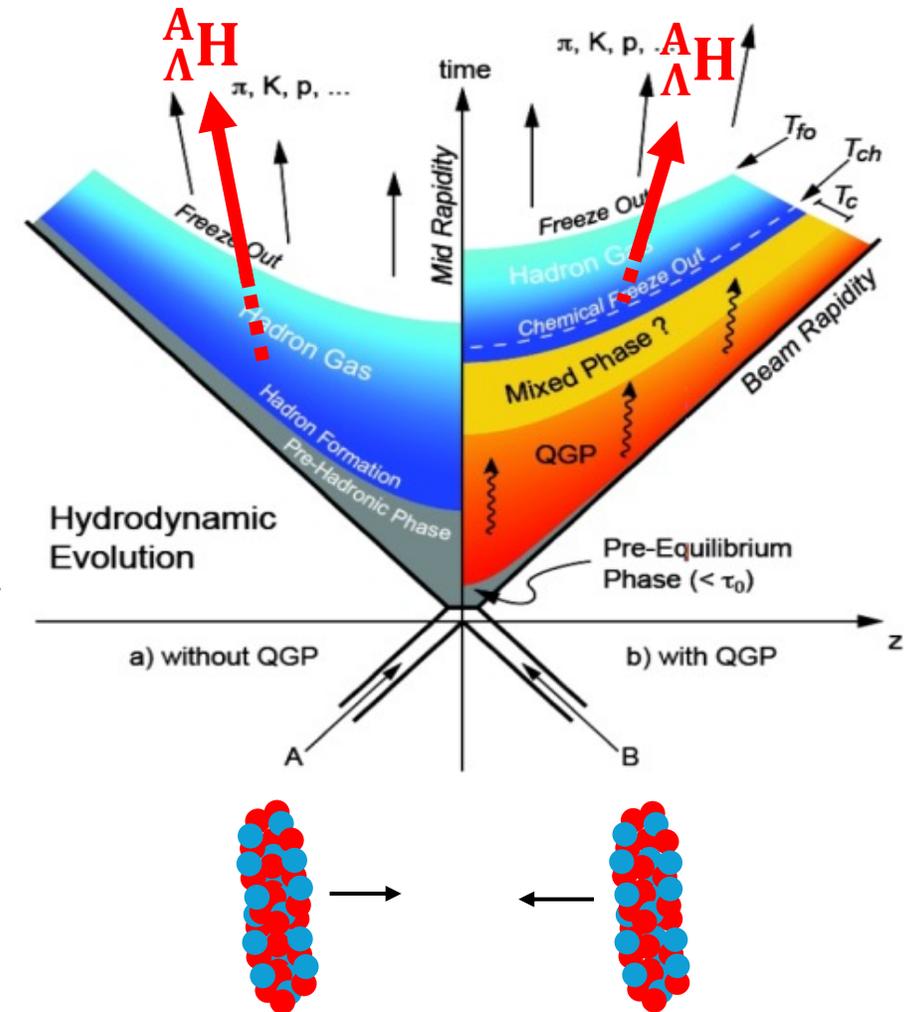
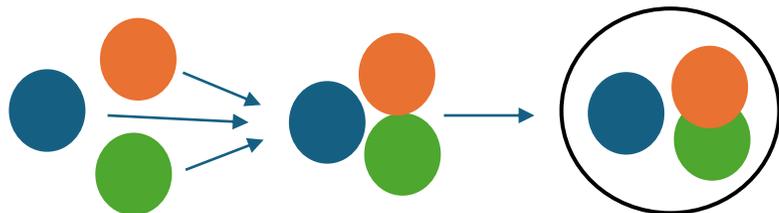
## Models at mid-rapidity

### Thermal model

- Hadron **chemical freeze out**  $T_{ch}$  and  $\mu_B$ 
  - $\frac{dN}{d^3 p} \sim \exp\left(-\frac{E-\mu_B}{T}\right)$
- Assuming the conserved baryon entropy after hadron chemical freeze-out

### Coalescence formation

- Baryons / nuclei very close in phase space  $(\vec{p}, \vec{r})$ .
  - Any experimental evidence?
  - The role of  $Y$ - $N$  interaction?

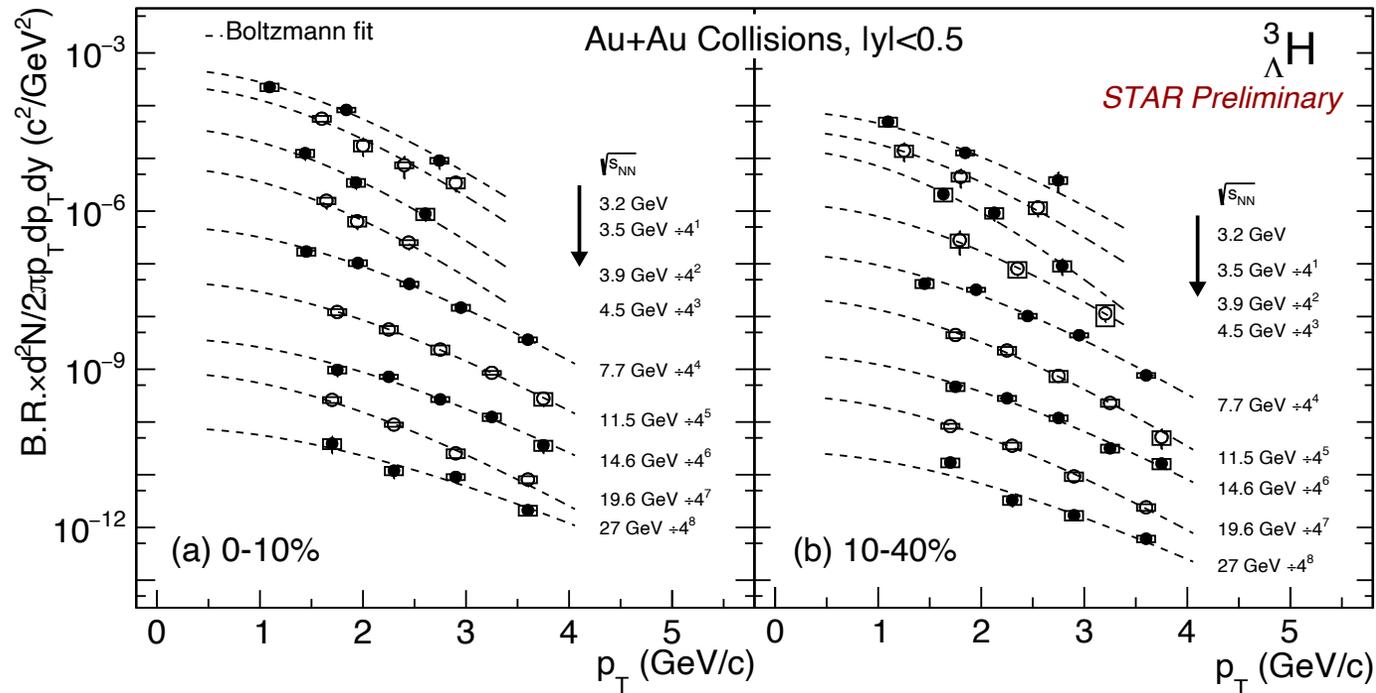


# Fruitful Results from STAR BES II

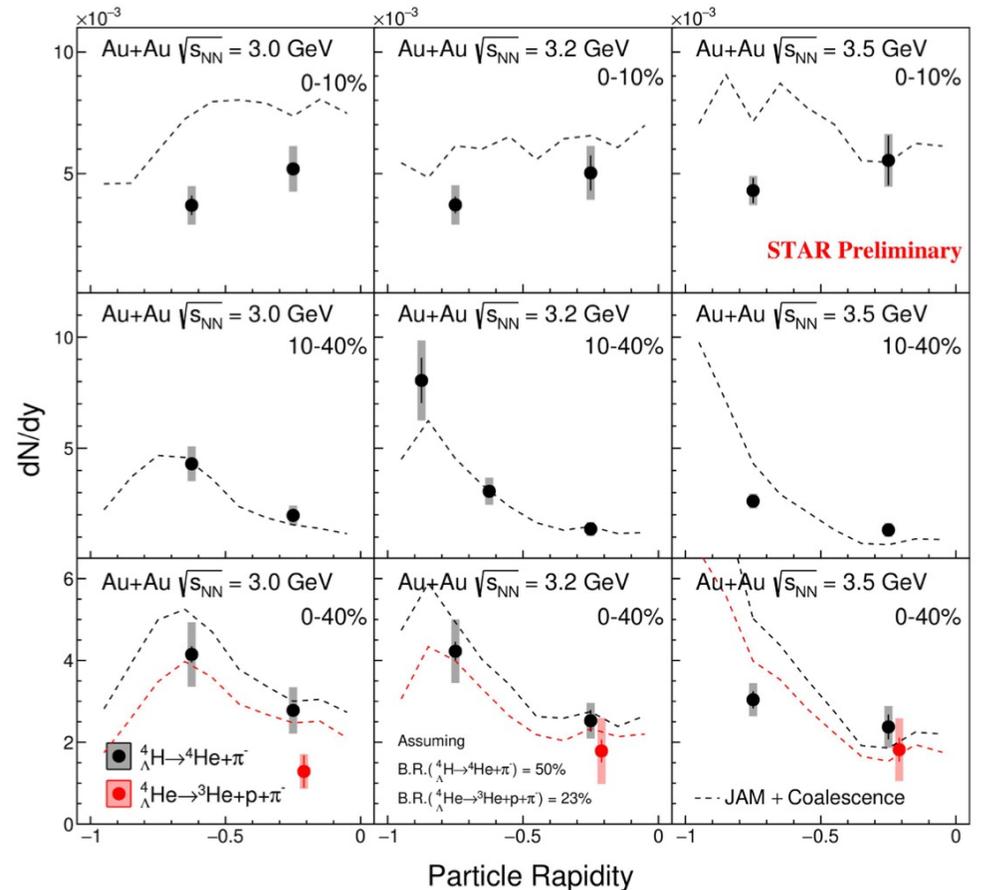
- Utilizing BES II datasets, we measure:

- ${}^3_{\Lambda}\text{H}$   $p_T$  spectra,  $dN/dy$ ,  $\langle p_T \rangle$  in Au+Au collisions at  $\sqrt{s_{NN}} = 3-27$  GeV
- ${}^4_{\Lambda}\text{H}$ ,  ${}^4_{\Lambda}\text{He}$   $p_T$  spectra,  $dN/dy$ ,  $\langle p_T \rangle$  in Au+Au collisions at  $\sqrt{s_{NN}} = 3-3.5$  GeV

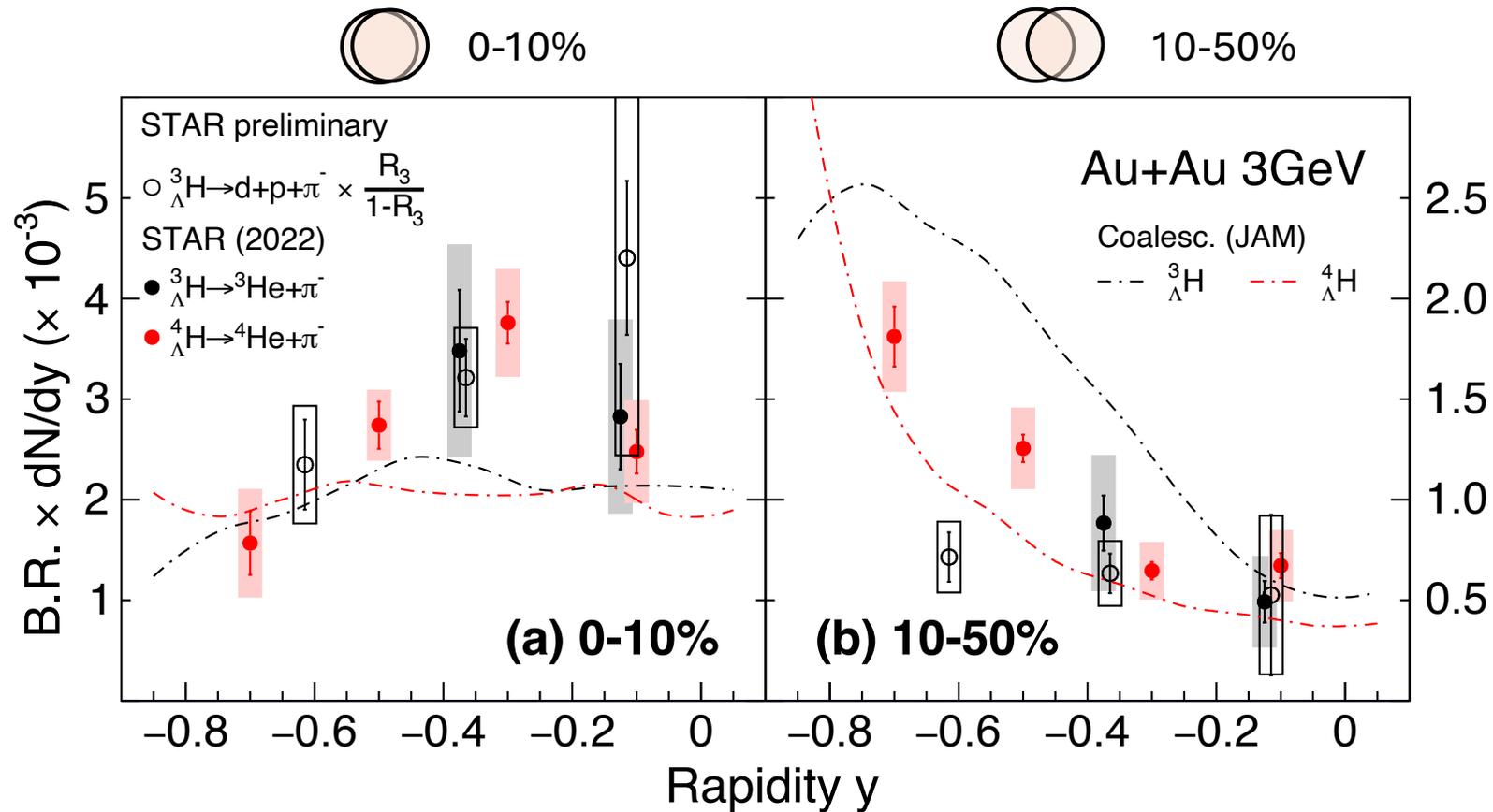
A=3:  ${}^3_{\Lambda}\text{H}$  (Au+Au  $\sqrt{s_{NN}} = 3-27$  GeV)



A=4:  ${}^4_{\Lambda}\text{H}$ ,  ${}^4_{\Lambda}\text{He}$  (Au+Au  $\sqrt{s_{NN}} = 3-3.5$  GeV)



# ${}^3_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{H}$ $dN/dy$ in Au+Au collisions at 3 GeV

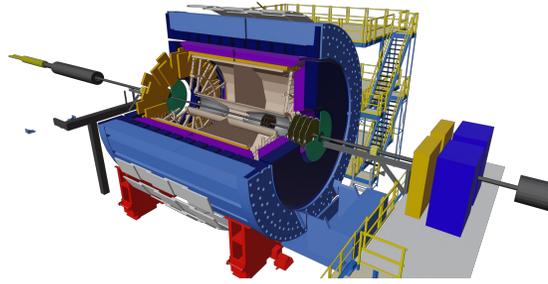
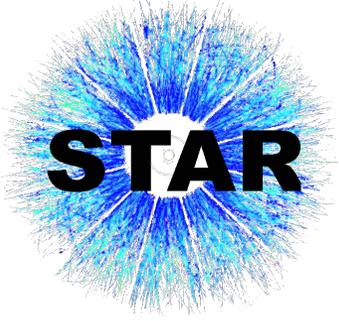


## JAM+Coal.

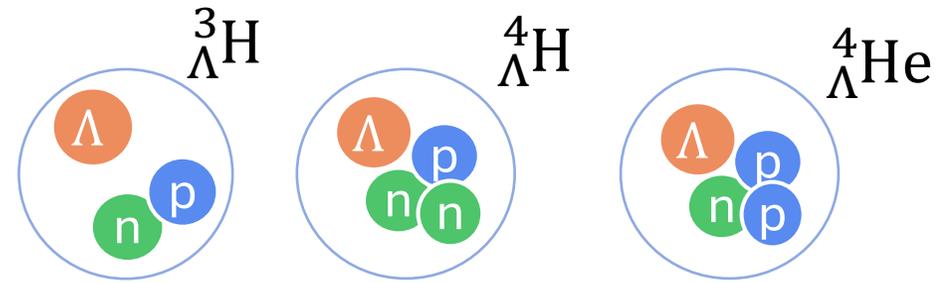
- Tuned to match proton and  $\Lambda$  spectra from data;
- Instant coalescence after kinetic freeze-out
- Two body coalescence:  $d/t+\Lambda$

3 GeV  ${}^3(4)_{\Lambda}\text{H} \rightarrow {}^3(4)\text{He} + \pi^-$ :  
 PRL 128, 202301 (2022)

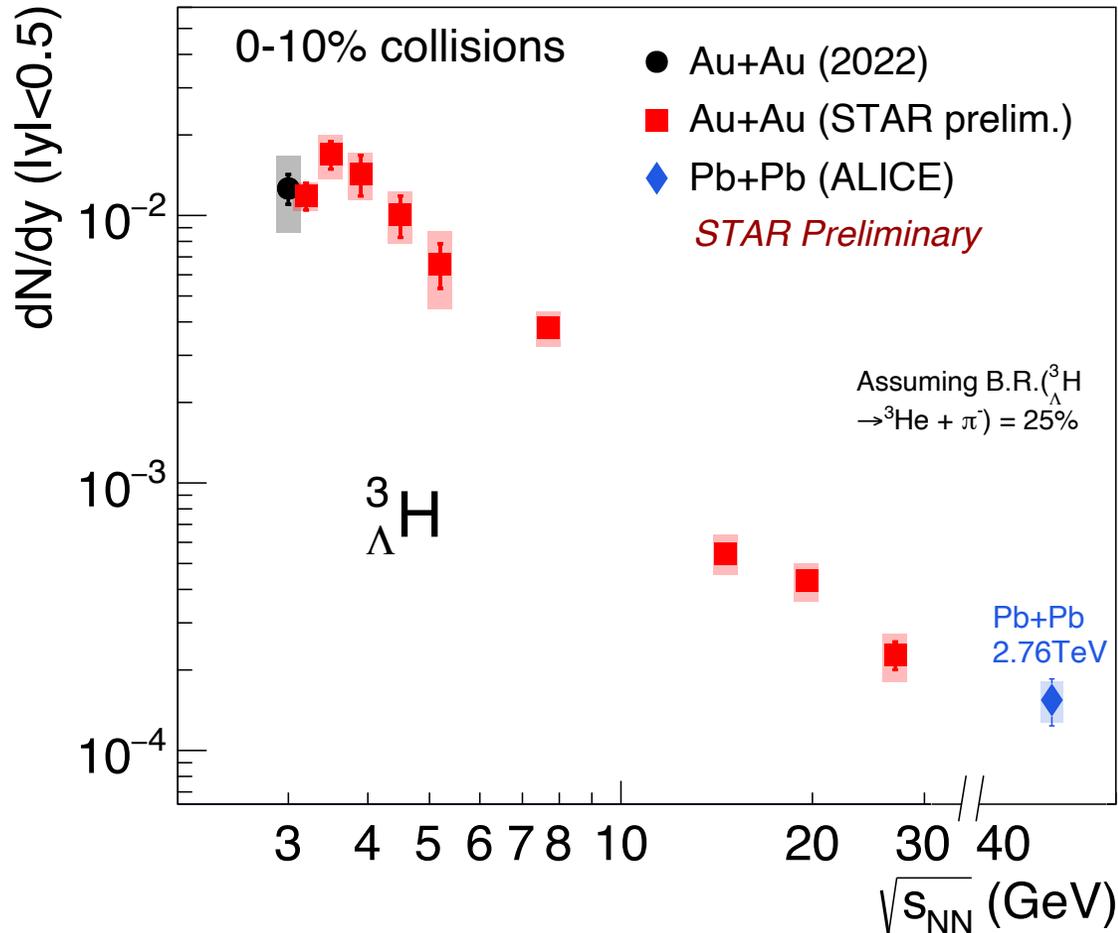
- Coalescence models with tuned parameters:
  - Qualitatively describe the trend of  ${}^4_{\Lambda}\text{H}$  yields versus rapidity.
  - Fail to describe the  ${}^3_{\Lambda}\text{H}$  tendency in 10-50% centralities.



# Energy Dependence of Hypernuclei Production



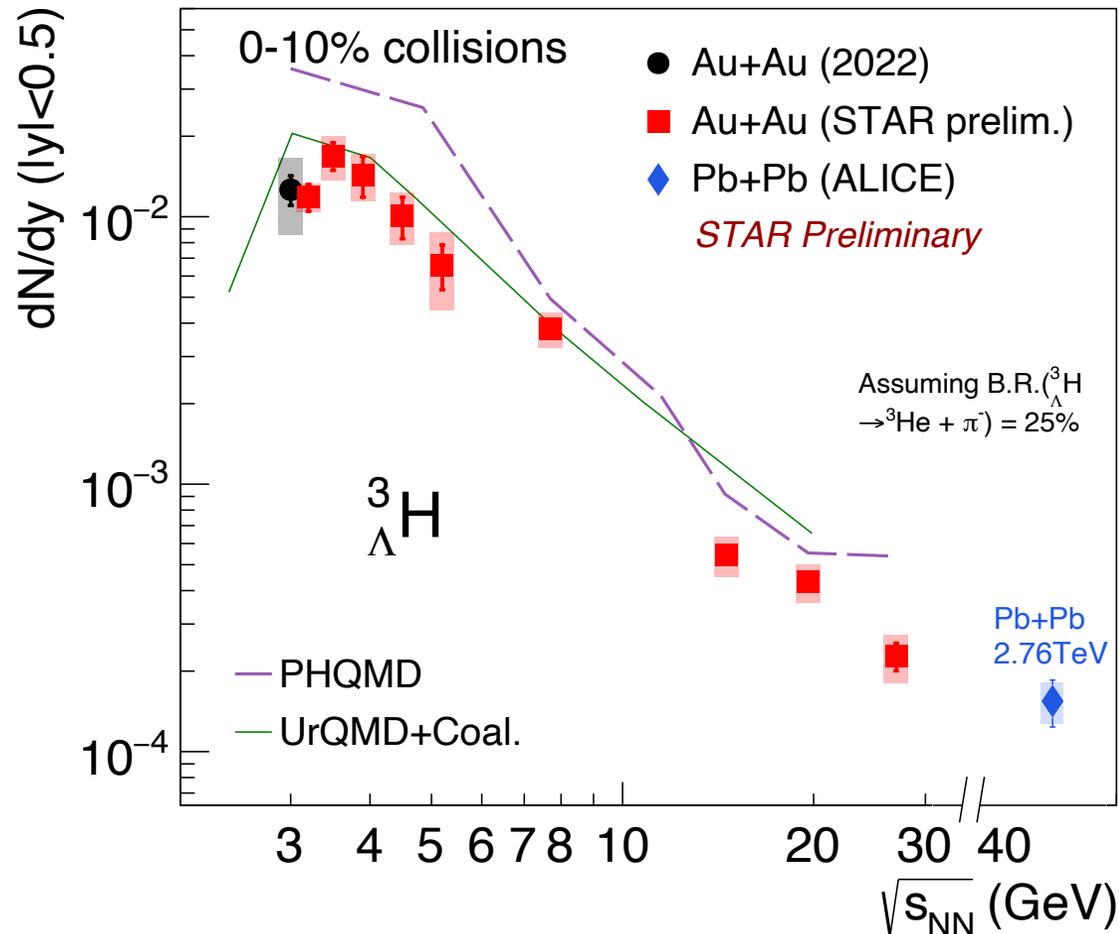
# Energy Dependence of ${}^3_{\Lambda}\text{H}$ Production



${}^3_{\Lambda}\text{H}$  production yields reaches peak at around 3-4 GeV.

- Increase steeply from 27 to 3 GeV as  $\sqrt{s_{NN}}$  goes lower
- Interplay between:
  - $\sqrt{s_{NN}} \downarrow$ , **baryon density**  $\uparrow$ , yields  $\uparrow$
  - Hyperon production

# Energy Dependence of ${}^3_{\Lambda}\text{H}$ Production



Coal. (UrQMD): T. Reichert et al. PRC 107 (2023) 1, 014912  
 PHQMD: S. Gläsel et al. PRC 105, 014908 (2022),  
 V. Kireyeu et al. arXiv:1911.09496  
 Pb+Pb: ALICE, PLB 754, 360 (2016)  
 STAR at 3 GeV: PRL 128, 202301 (2022)

## UrQMD + Instant coal.

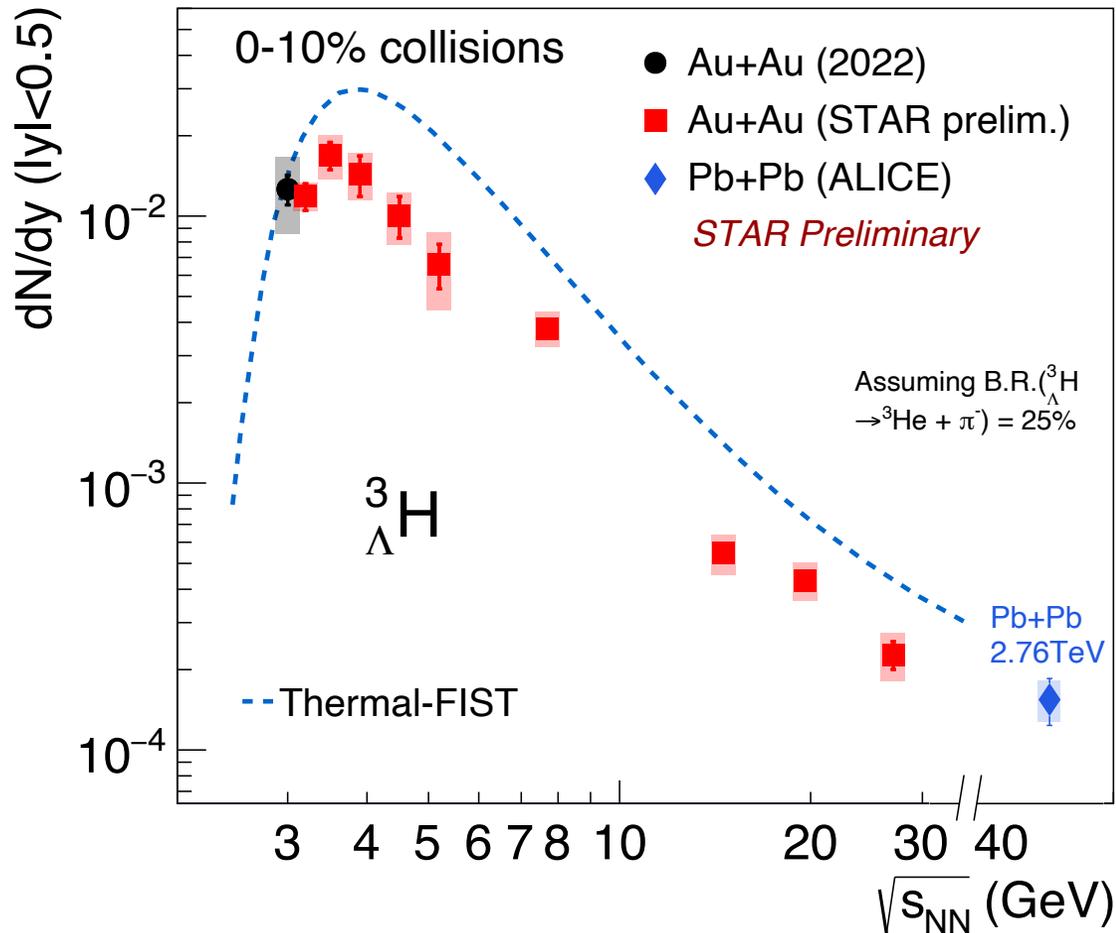
- Describe data from 3-10 GeV
- Instant coalescence after hadron kinetic freeze-out
- Coalescence condition:
  - $|\vec{p}_1 - \vec{p}_2| < \Delta P, |\vec{r}_1 - \vec{r}_2| < \Delta R$

## PHQMD

- Transport model + dynamical cluster formation.
- Cluster can be formed before hadron kinetic freeze out.
- Future developments
  - Momentum dependent EoS
  - Y-N potential

Details see: [Elena Bratkovskaya SQM2024](#)

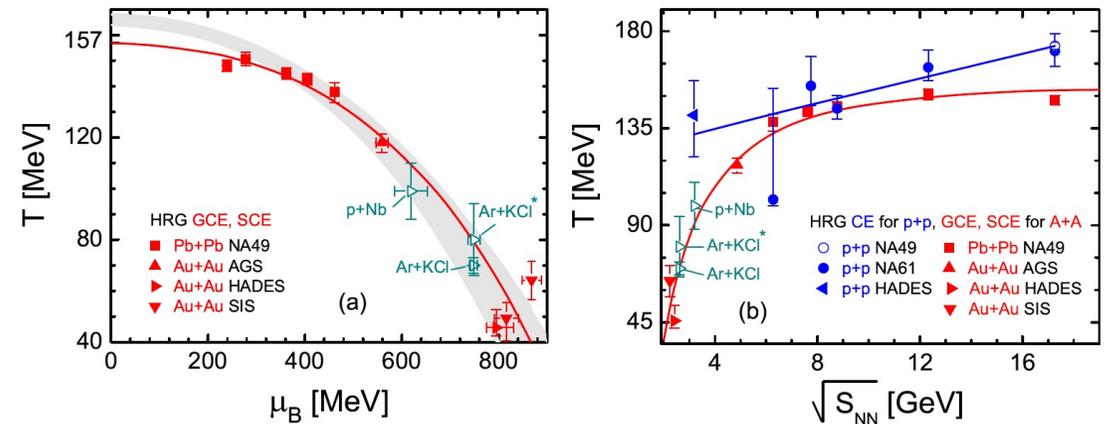
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Thermal-FIST: T. Reichert et al, PRC 107, 014912 (2023)  
 Pb+Pb: ALICE, PLB 754, 360 (2016)  
 Au+Au: STAR, PRL 128, 202301 (2022)

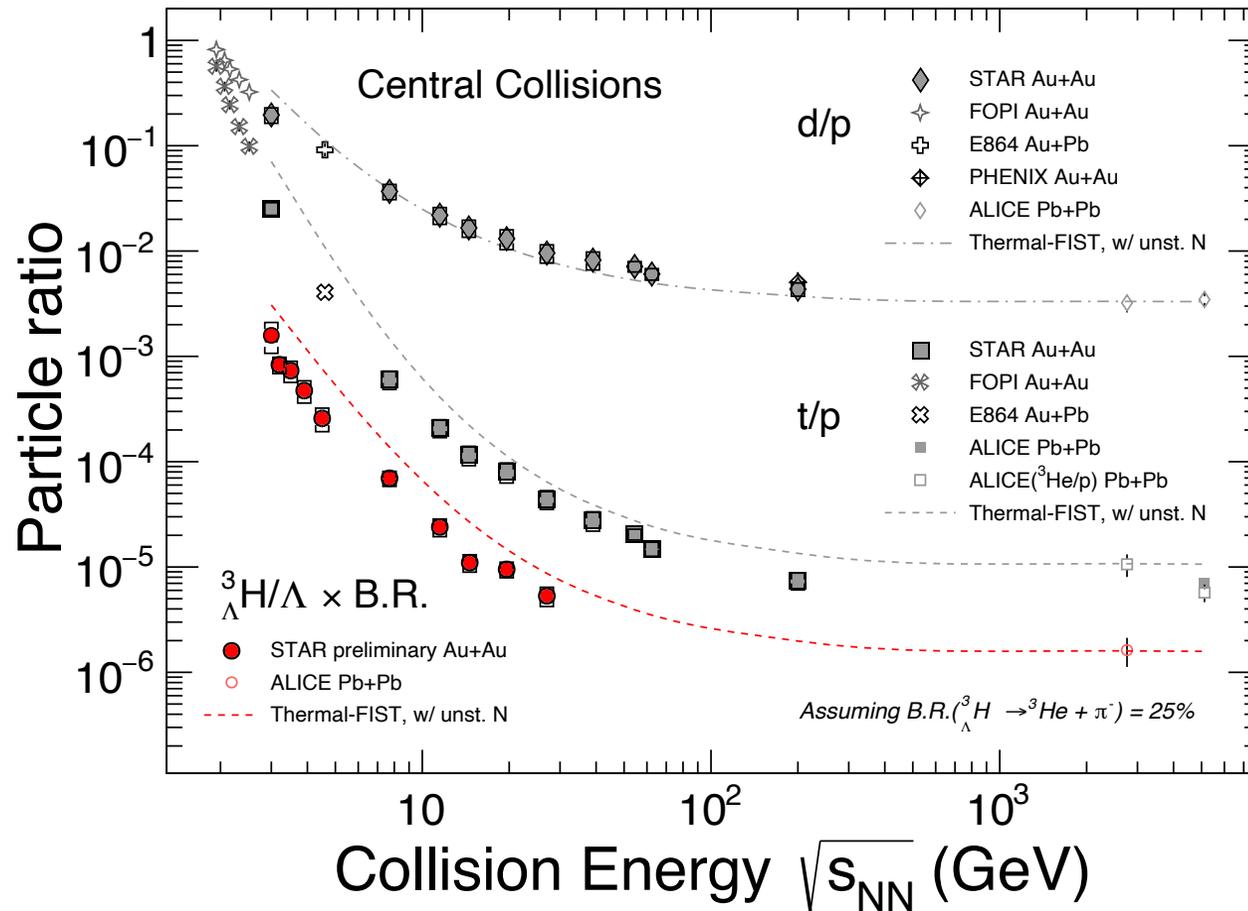
## Thermal-FIST model

- Hadron chemical freeze-out  $T$  and  $\mu_B$ 
  - $\frac{dN}{d^3p} \sim \exp\left(-\frac{E-\mu_B}{T}\right)$
- Strangeness canonical ensemble in low energies
- $\sim 2$  times larger than the data



Phys. Rev. C 93, 064906 (2016)

# ${}^3_{\Lambda}\text{H}/\Lambda$ Compared to Thermal Model



Thermal-FIST:

- Hadron chemical freeze-out  $T$  and  $\mu_B$ .

T. Reichert et al, PRC 107, 014912 (2023)

${}^3_{\Lambda}\text{H}/\Lambda$ : Cancel strangeness canonical suppression and volume size

Thermal model at RHIC energies:

$A=2$  ( $d$ ): Overall consistent

$A=3$  ( $t$  and  ${}^3_{\Lambda}\text{H}$ ):  $\sim 2x$  higher than data

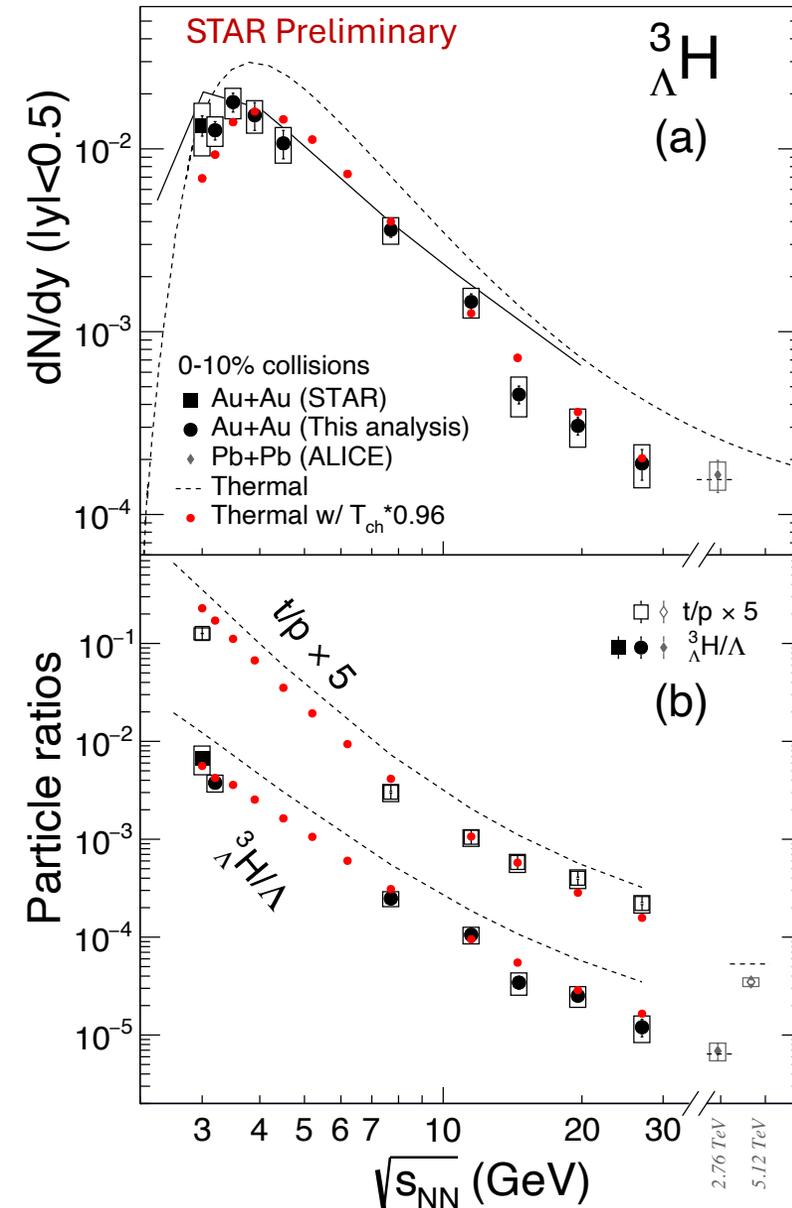
- ${}^3_{\Lambda}\text{H}$  (and  $t$ ) maybe not in equilibrium at hadron chemical freeze out.

# What happened if we decrease the temperature

- t and  ${}^3\Lambda\text{H}$  -> default  $\mu_B$  and  $0.96*T$
- Proton and  $\Lambda$  -> default T and  $\mu_B$
- The tuned Thermal-FIST with  $0.96*T$  seems able to describe the data
- Note that:
  - The t and  ${}^3\Lambda\text{H}$  yields modifies dramatically with the changes of temperature:

yields  $\sim C * \exp[-1 * (m_T - \mu_B) / T]$   
 $m_T \sim 3 \text{ GeV}$  for t and  ${}^3\Lambda\text{H}$   
 $\mu_B \sim 0.7 - 0.14 \text{ GeV}$  (from 3-27 GeV)  
 $T \sim 0.085 - 0.155 \text{ GeV}$  (from 3-27 GeV)

- Because triton and  ${}^3\Lambda\text{H}$  are heavy, so the impact from  $\mu_B$  become less significant

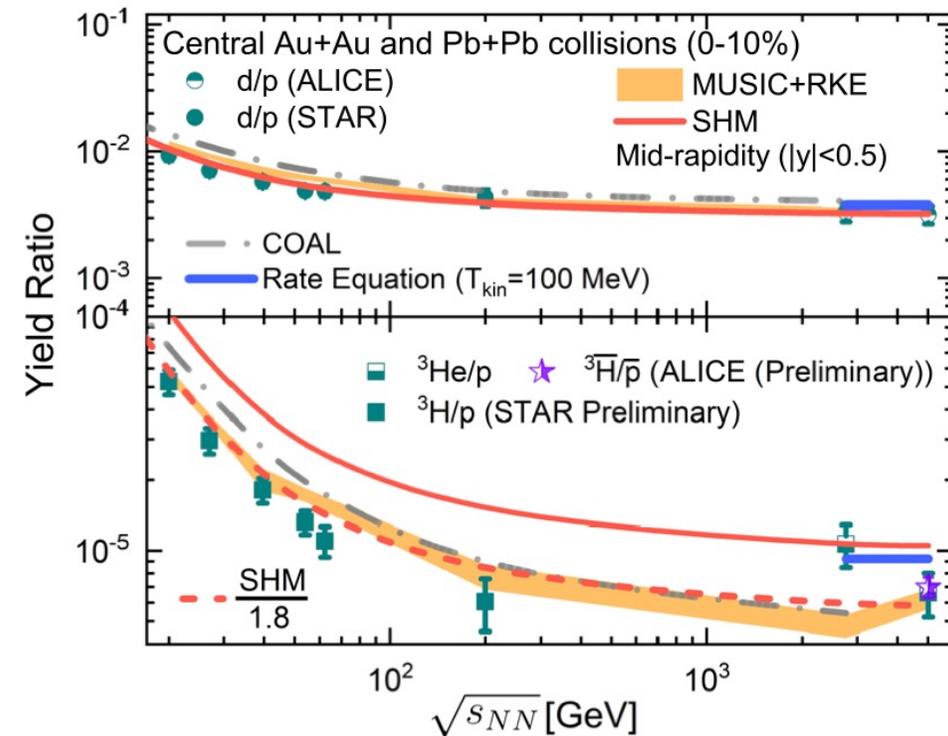
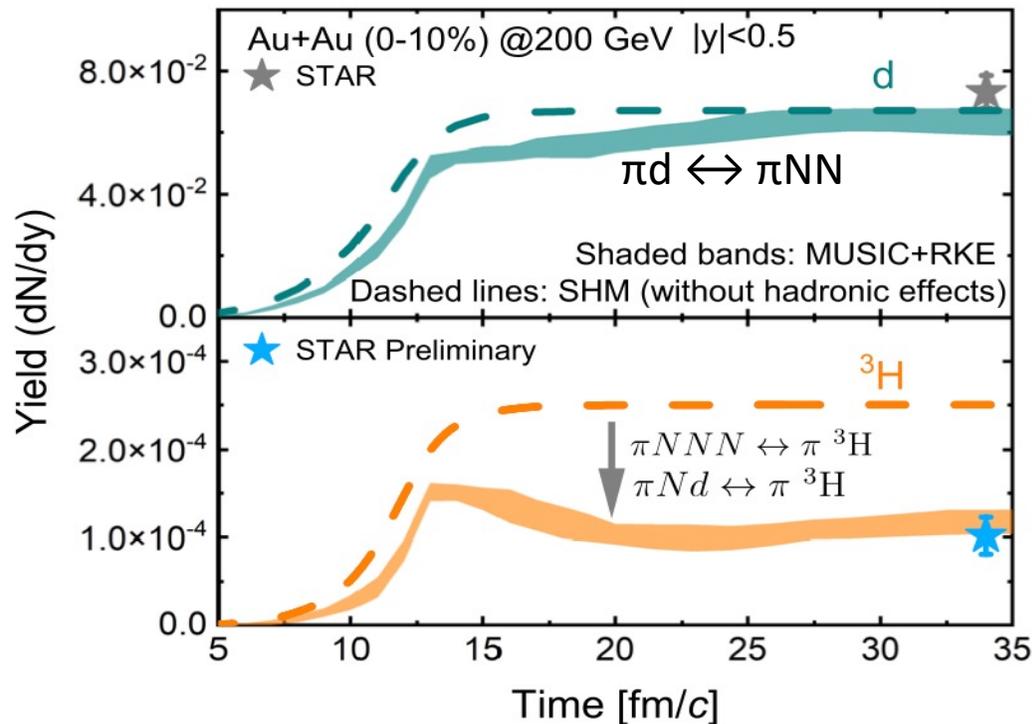


# Other possible model: kinetic approach

- Relativistic kinetic equation (RKE) to include hadronic re-scattering processes.
  - Close connection to Coal. via final state interaction close to kinetic freeze-out.

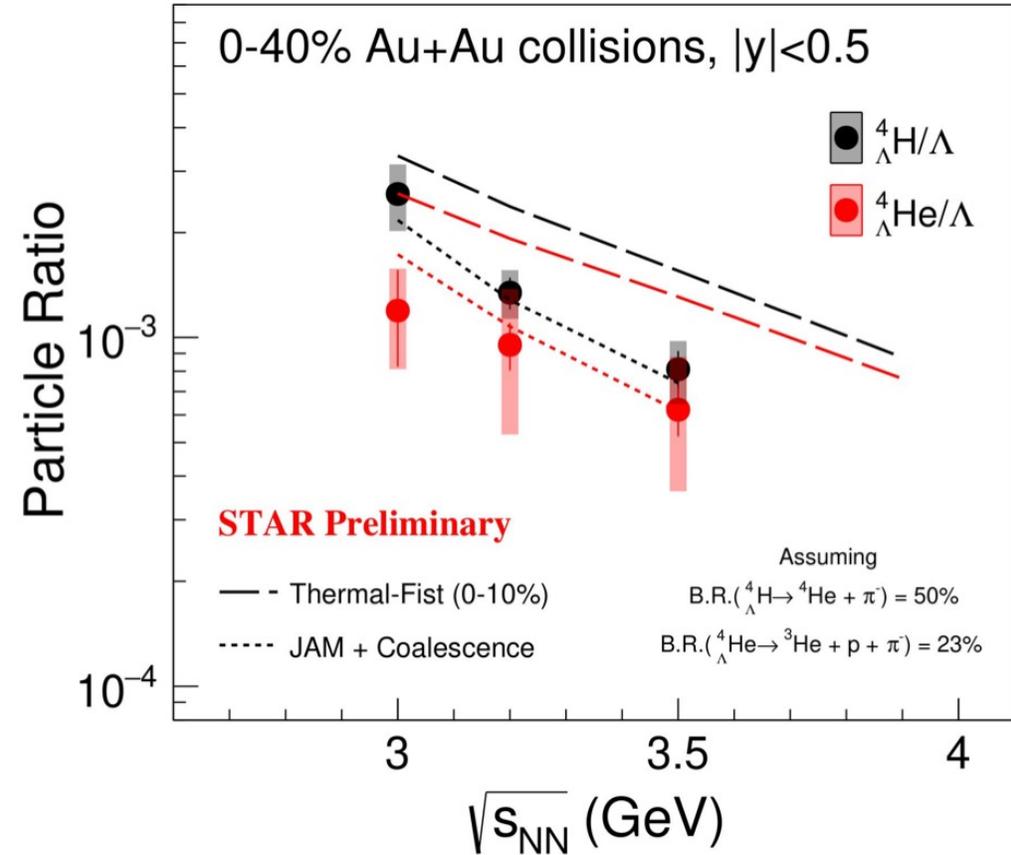
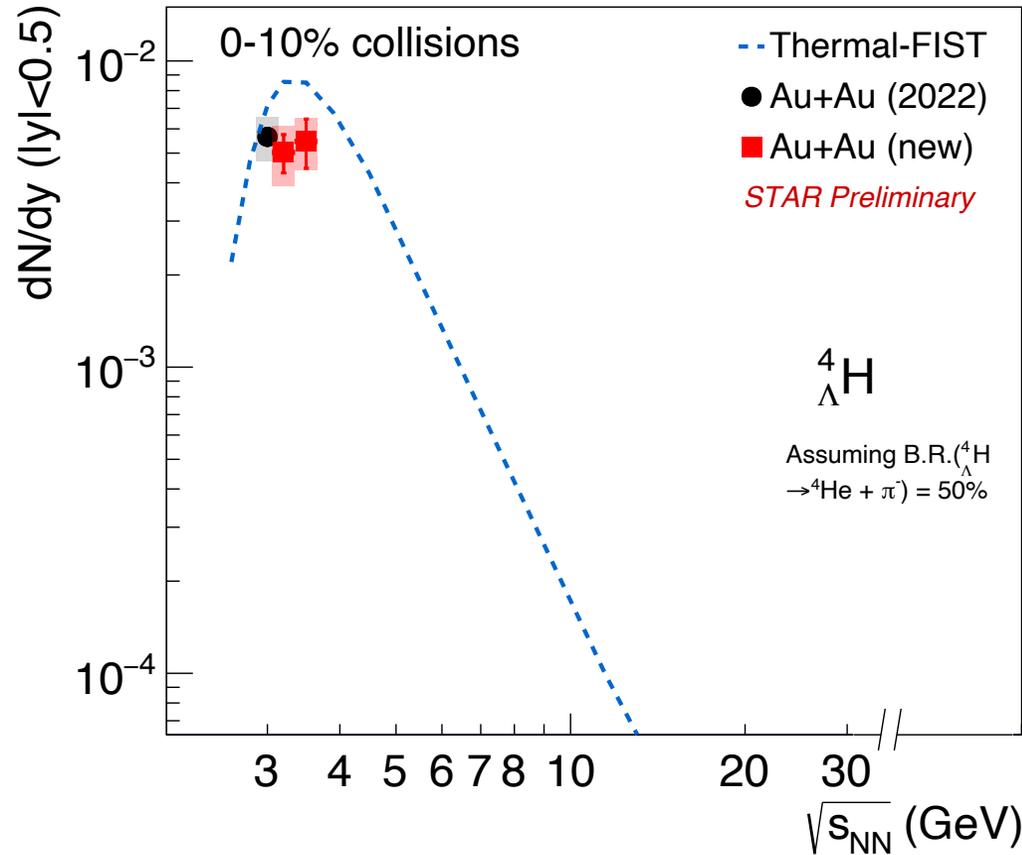
*P. Danielewicz et al. NPA 533 (1991) 712-748*

*Kaijia Sun et al, Nature Commun. 15 (2024) 1, 1074*



# Production of ${}^4_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{He}$

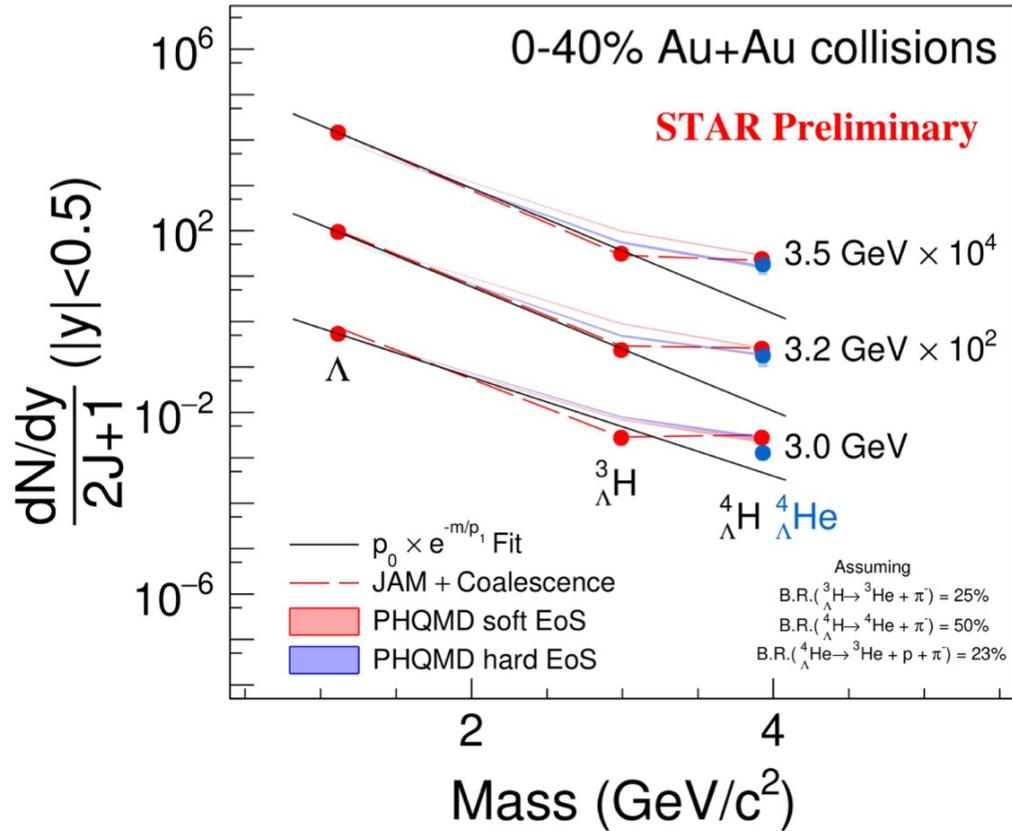
${}^4_{\Lambda}\text{He}$ : Chenlu Hu, SQM2024



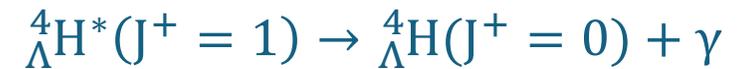
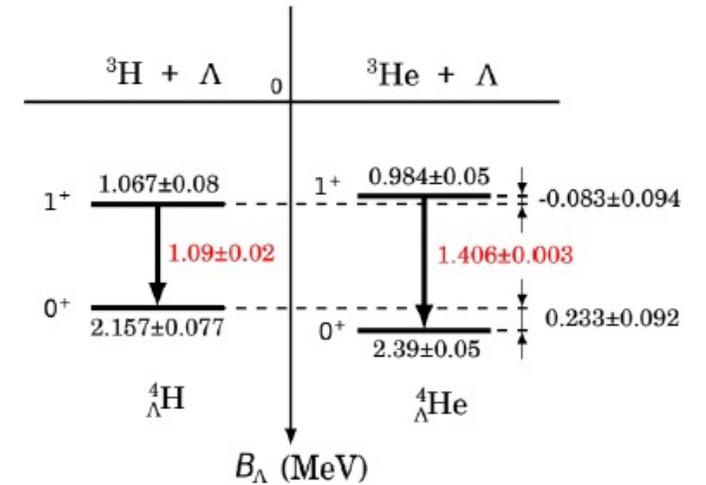
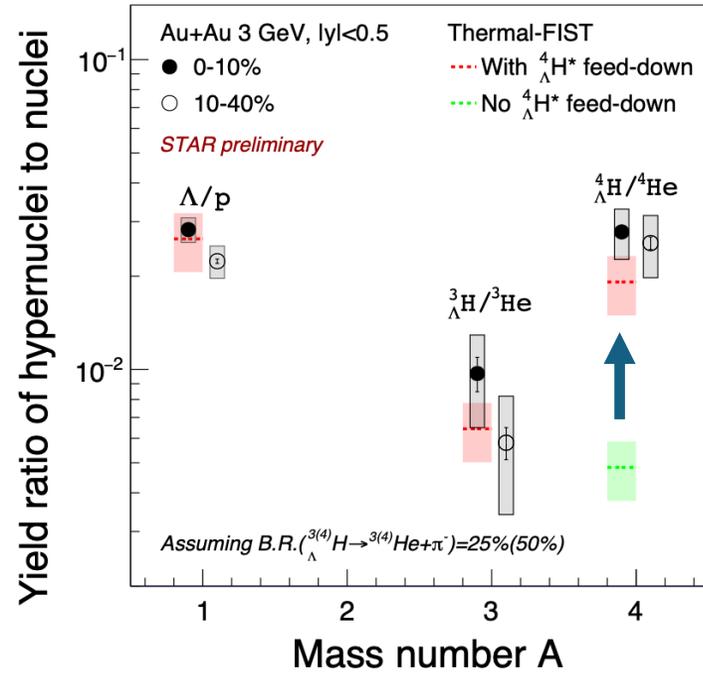
- Thermal model also over-predict  ${}^4_{\Lambda}\text{H}$  and  ${}^4_{\Lambda}\text{He}$  yields while JAM+coal. describes the data.

# Production of ${}^4_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{He}$

Thermal expectation:  $\frac{dN}{dy} \sim \exp\left(-\frac{m}{T}\right)$

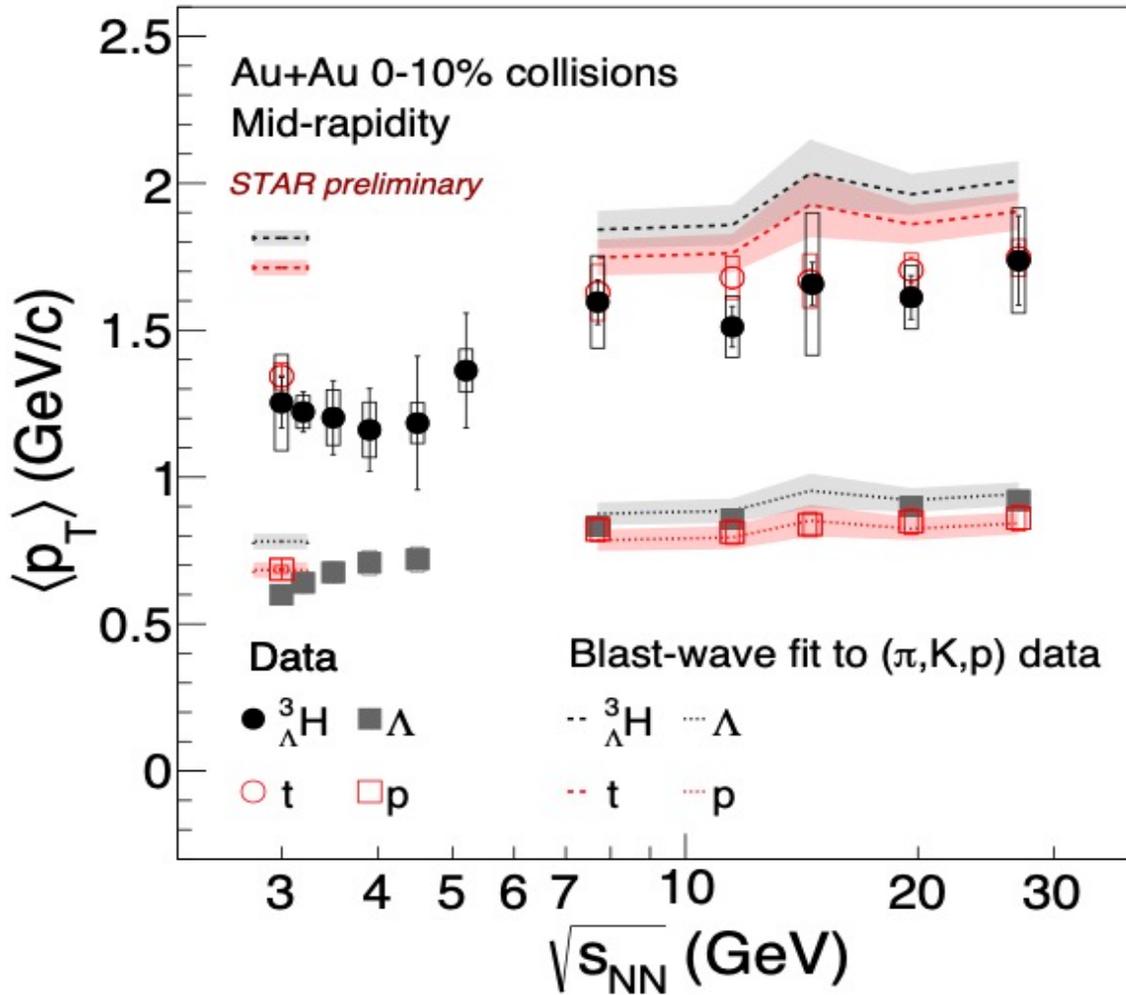


PHQMD: S. Gläsel et al. PRC 105, 014908 (2022)



- Evidence of the formation of  ${}^4_{\Lambda}\text{H}$  and  ${}^4_{\Lambda}\text{He}$  excited states in 3-4 GeV collisions.

# Energy Dependence of ${}^3\Lambda\text{H}$ $\langle p_T \rangle$



- ${}^3\Lambda\text{H}$  and  $t$   $\langle p_T \rangle < \langle p_T \rangle^{BW}$  at 3 GeV
- Hint of  ${}^3\Lambda\text{H}$  and  $t$   $\langle p_T \rangle < \langle p_T \rangle^{BW} > 7.7$  GeV
  - $\langle p_T \rangle^{BW}$ : Blast-wave (BW) expectation calculated using **kinetic freeze-out parameters** from measured light hadron ( $\pi$ , K, p) spectra.

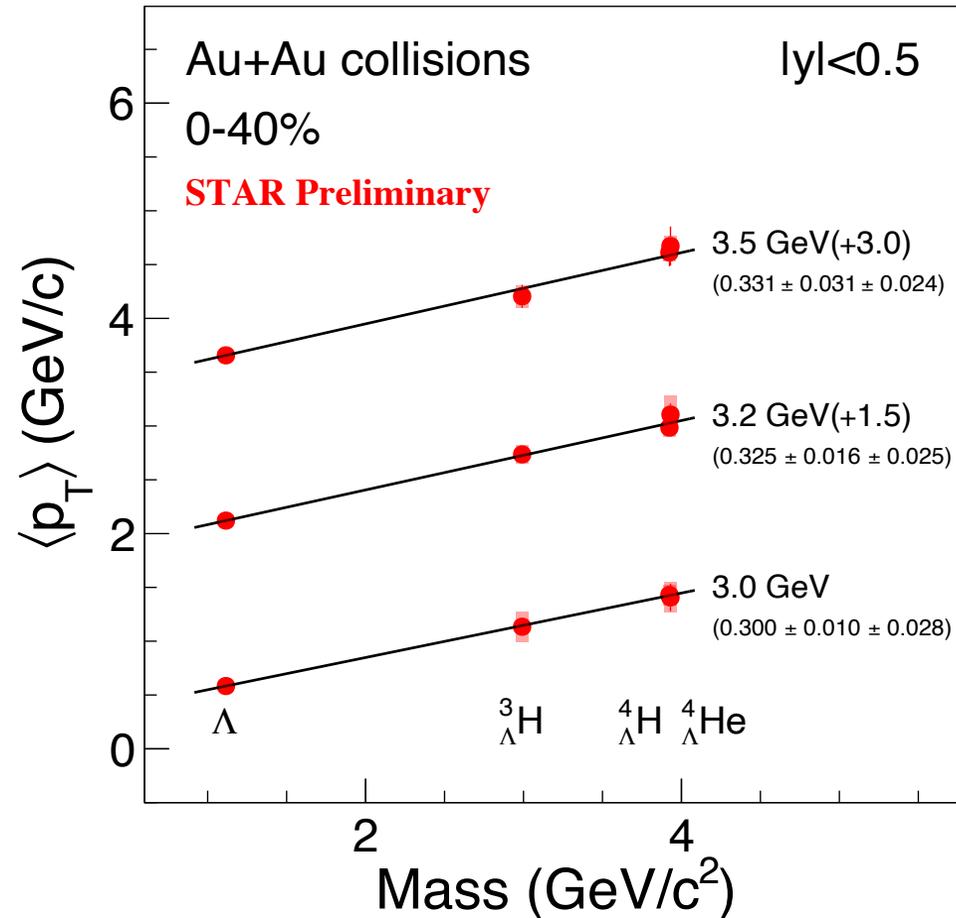
Blastwave function:

$$\frac{1}{2\pi p_T} \frac{d^2 N}{dp_T dy} \propto \int_0^R r dr m_T I_0 \left( \frac{p_T \sinh \rho(r)}{T_{kin}} \right) \times K_1 \left( \frac{m_T \cosh \rho(r)}{T_{kin}} \right)$$

${}^3\Lambda\text{H}$  and  $t$  might do not follow the same collective expansion as light hadrons.

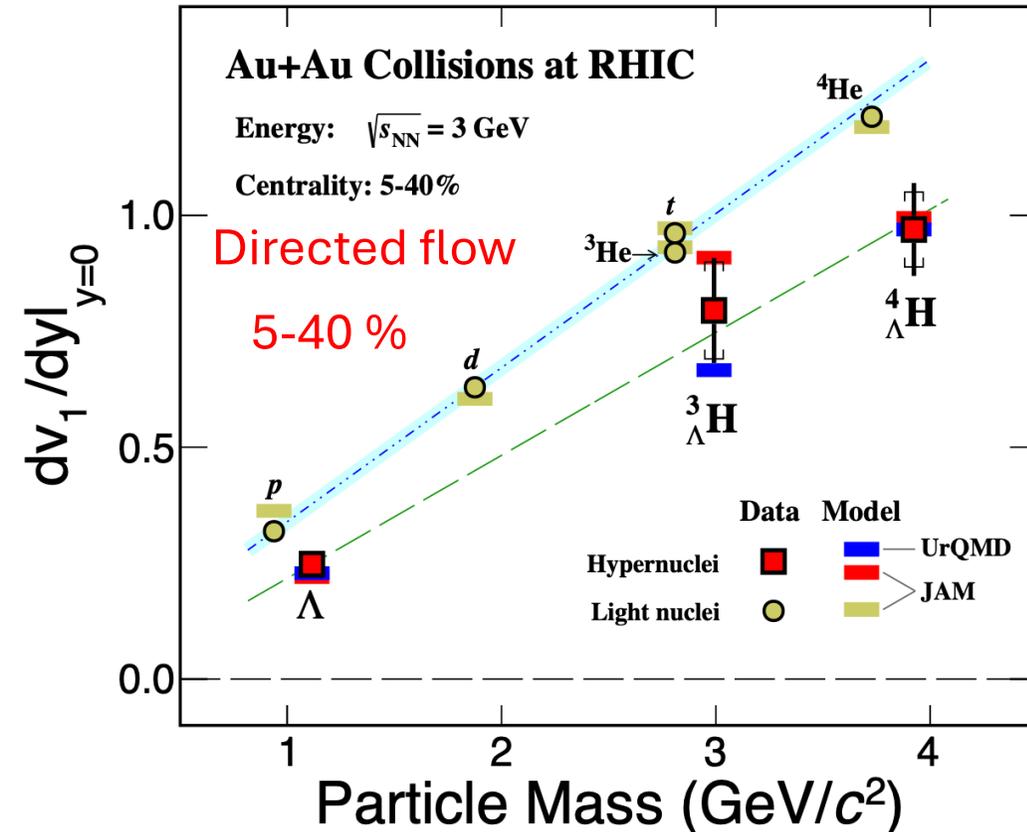
# Hypernuclei Collectivity versus Mass

$\langle p_T \rangle \rightarrow$  Radial flow contributions



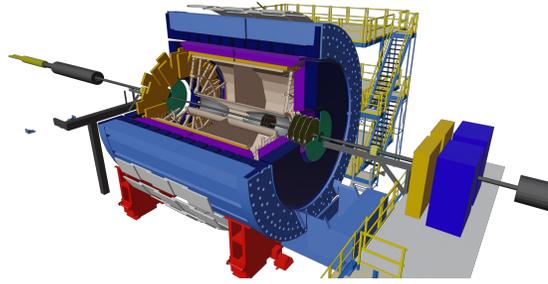
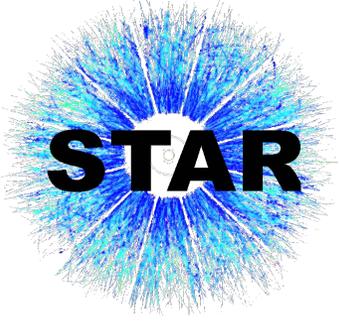
$v_1 \rightarrow$  Directed flow

$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left( 1 + \sum_1^\infty 2v_n \cos [n(\phi - \psi_{RP})] \right)$$

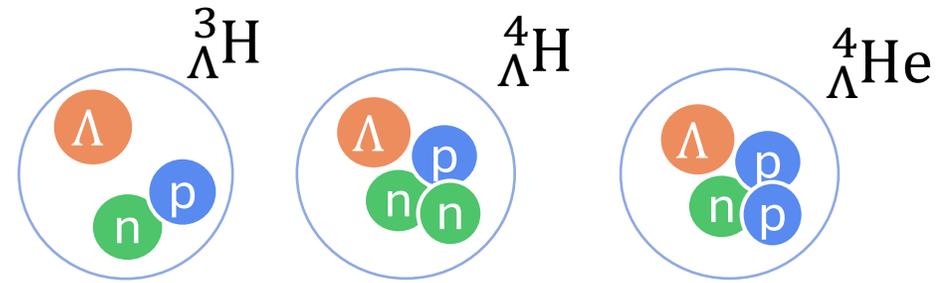


STAR, PRL 130 (2023) 212301

- Hypernuclei  $\langle p_T \rangle$  (and  $v_1$ ) show linear mass scaling from 3 to 3.5 GeV in mid-rapidity.
  - Consistent with **coalescence formation** picture.



# Multiplicity Dependence of Hypernuclei Production



# Strangeness Population Factor ( $S_A$ )

$$S_A = \frac{{}^A_{\Lambda}H(A \times p_T)}{{}^A\text{He}(A \times p_T) \times \frac{\Lambda}{p}(p_T)} = \frac{B_A({}^A_{\Lambda}H)(p_T)}{B_A({}^A\text{He})(p_T)}$$

S. Zhang et al, PLB 684, 224 (2010)

$$E_A \frac{d^3 N_A}{dp_A^3} = B_A \left( E_{p,n} \frac{d^3 N_{p,n}}{dp_{p,n}^3} \right)^A \Big|_{\vec{p}_p = \vec{p}_n = \frac{\vec{p}_A}{A}}$$

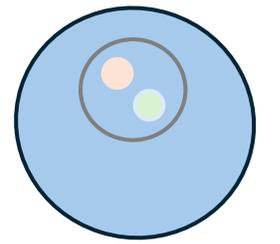
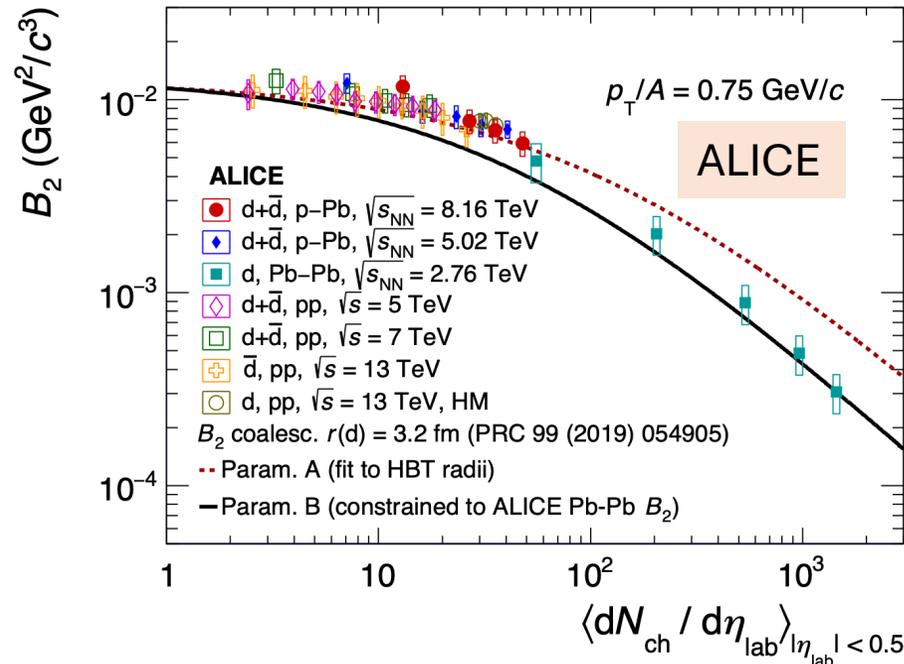
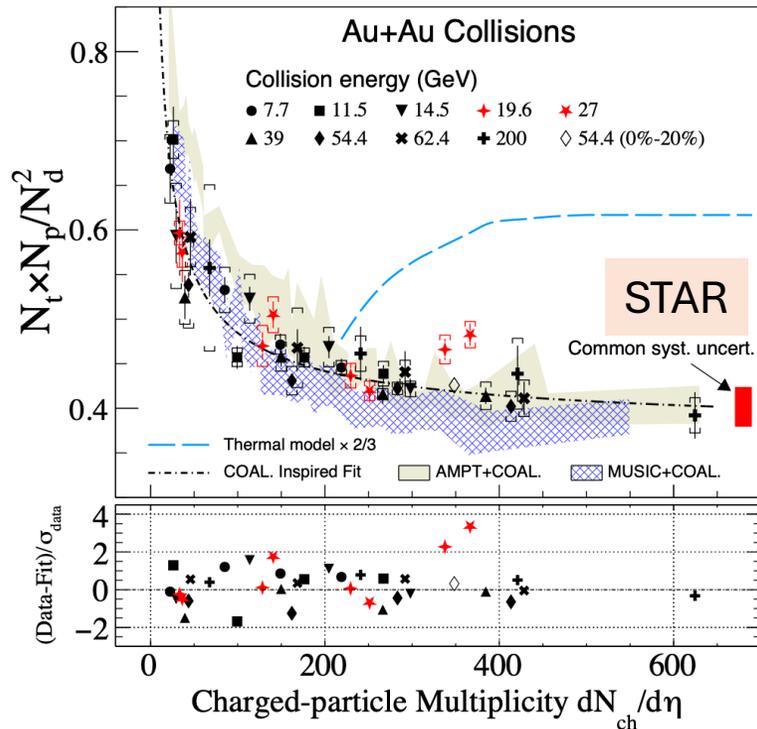
- $S_A$ : Direct connection to coalescence parameters  $B_A$

F. Bellini, PRC 99, 054905 (2019)

Under some coalescence scenarios:

$$B_A = \frac{2J_A + 1}{2^A} \frac{1}{\sqrt{A}} \frac{1}{m_T^{A-1}} \left( \frac{2\pi}{R^2 + (\frac{r_A}{2})^2} \right)^{\frac{3}{2}(A-1)}$$

Emit source size Radius



Emit source

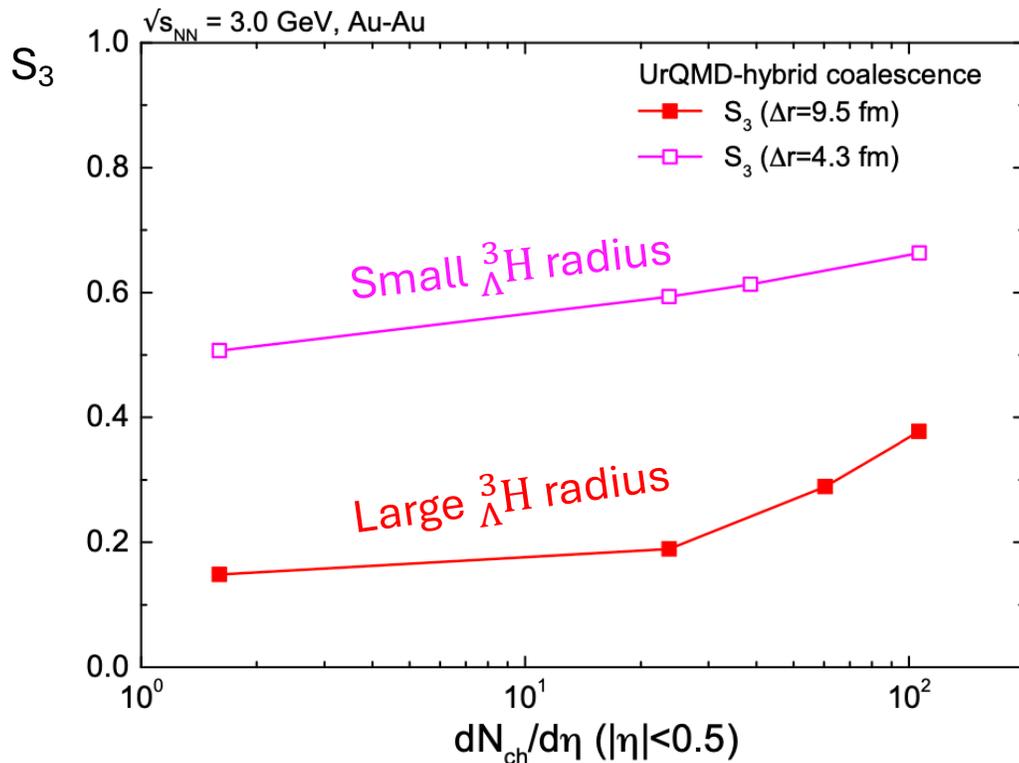
# Strangeness Population Factor ( $S_A$ )

$$S_A = \frac{{}^A_{\Lambda}\text{H}(A \times p_T)}{{}^A\text{He}(A \times p_T) \times \frac{\Lambda}{p}(p_T)} = \frac{B_A({}^A_{\Lambda}\text{H})(p_T)}{B_A({}^A\text{He})(p_T)}$$

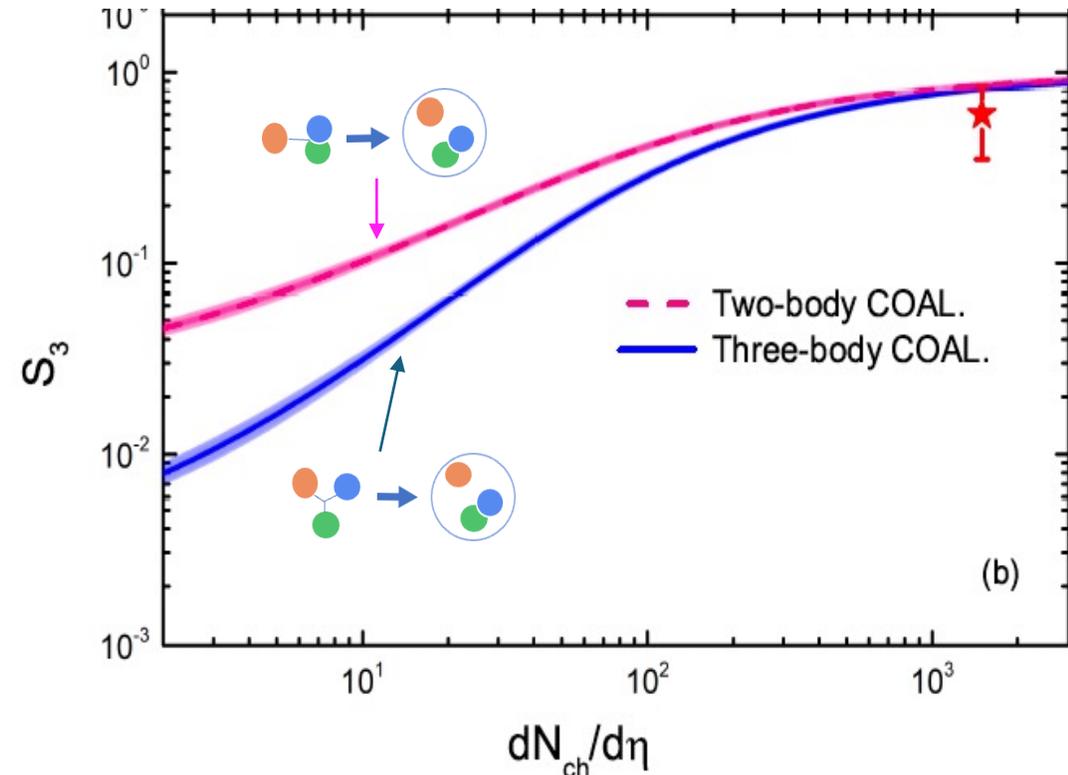
S. Zhang et al, PLB 684, 224 (2010)

- $S_A$ : Direct connection to coalescence parameters  $B_A$
- $S_3$  vs.  $dN_{ch}/d\eta$ : Possible insights to  ${}^3_{\Lambda}\text{H}$  radius and coalescence mechanism

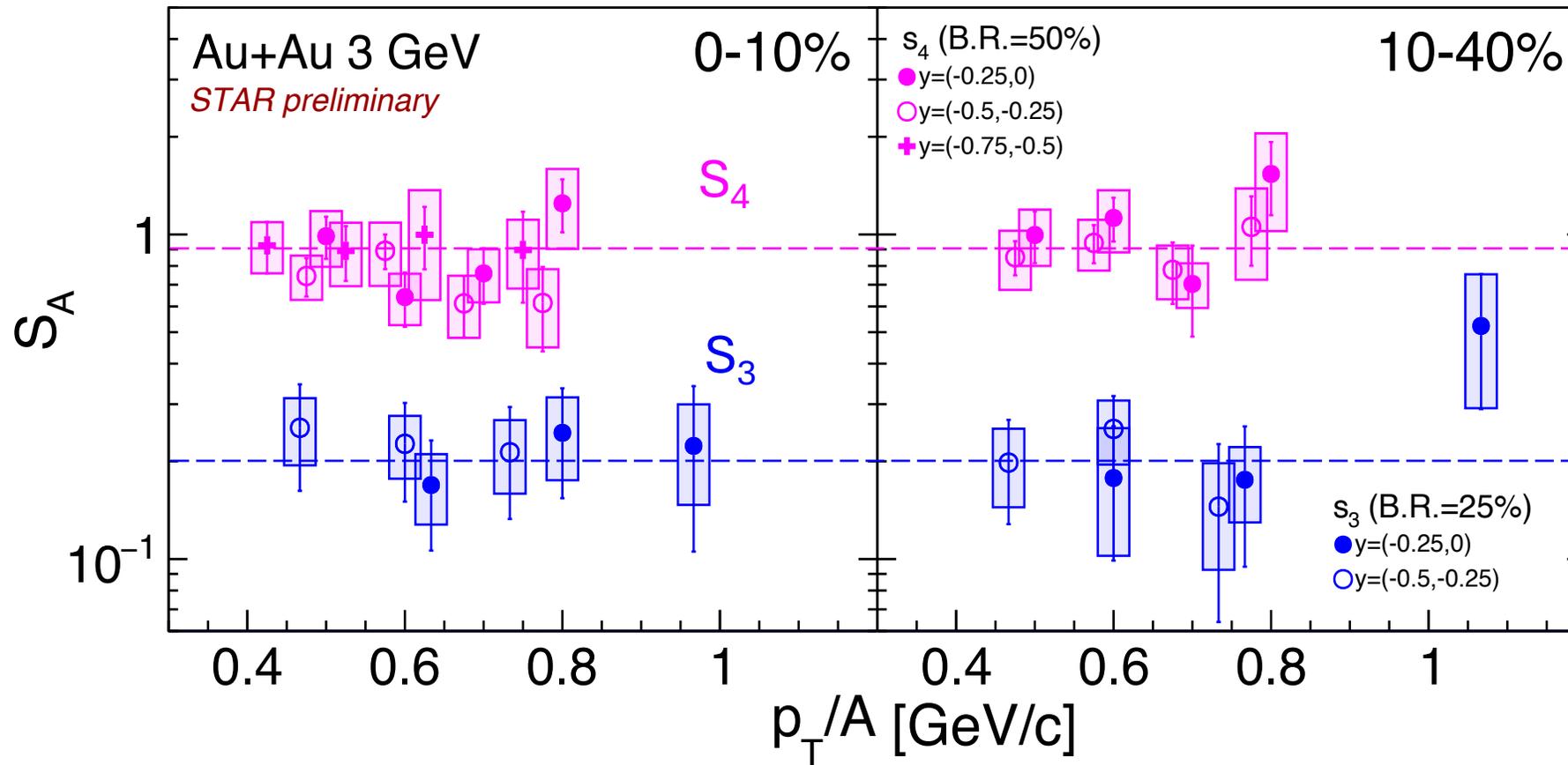
T. Reichert et al, PRC 107, 014912 (2023)



K. Jia, PLB 792 (2019) 132-137



# $S_3$ and $S_4$ in Au+Au 3 GeV



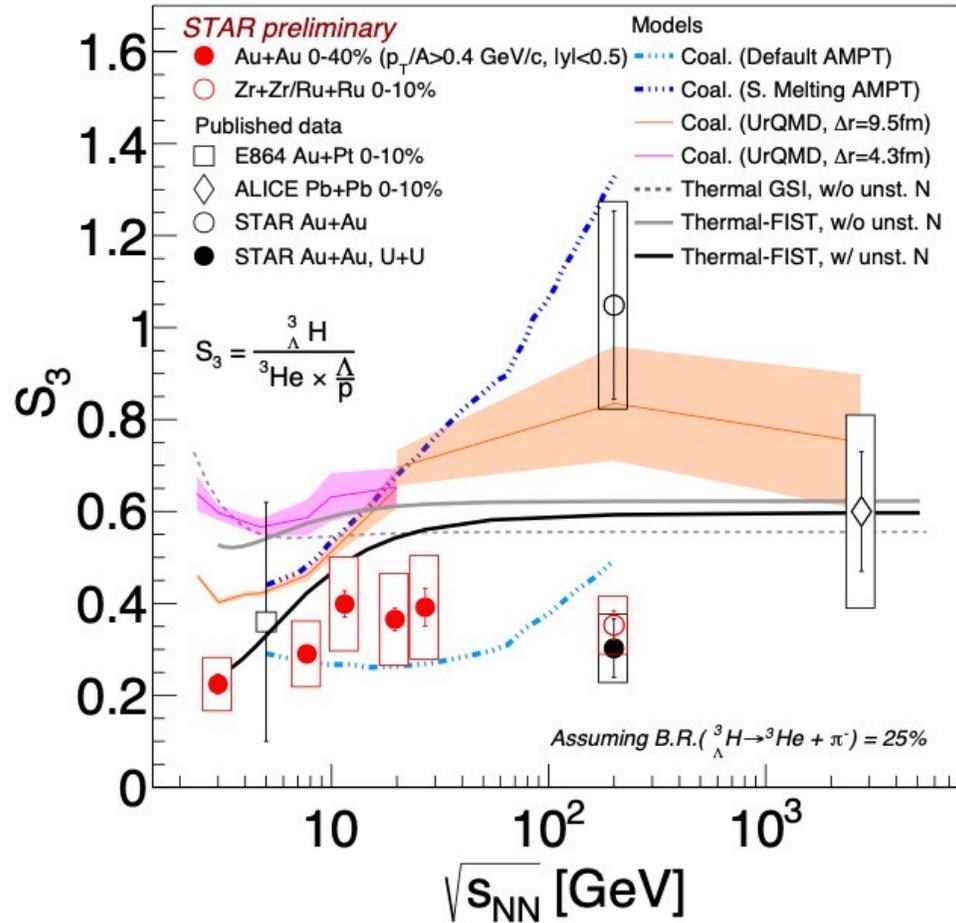
$$S_A = \frac{A_{\Lambda} H(A \times p_T)}{A_{\Lambda} He(A \times p_T) \times \frac{\Lambda}{p}}$$

$$= \frac{B_A(A_{\Lambda} H)(p_T)}{B_A(A_{He})(p_T)}$$

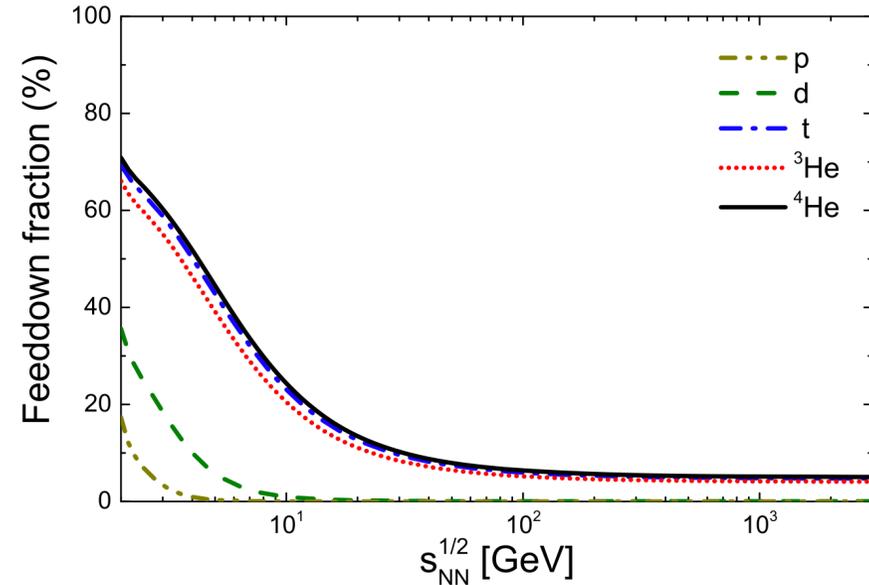
- No obvious  $p_T$ , rapidity and centrality dependence of  $S_A$  observed at 3 GeV
  - Evidence that  $B_A$  of light and hyper nuclei follow similar tendency versus  $p_T$ , rapidity and centrality

# System Size Dependence of $S_3$

STAR COL data: Yue Hang Leung, CPOD2024



$$S_A = \frac{{}^A\Lambda\text{H}(A \times p_T)}{{}^A\text{He}(A \times p_T) \times \frac{\Lambda}{p}(p_T)}$$

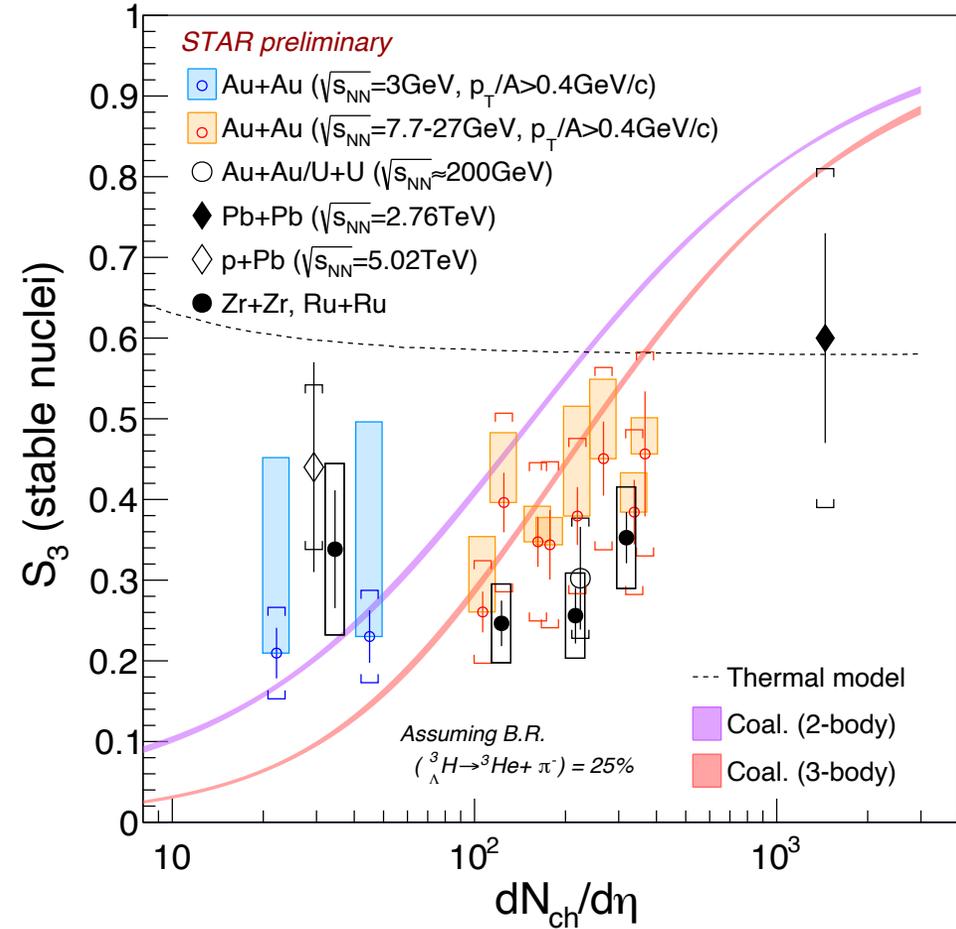
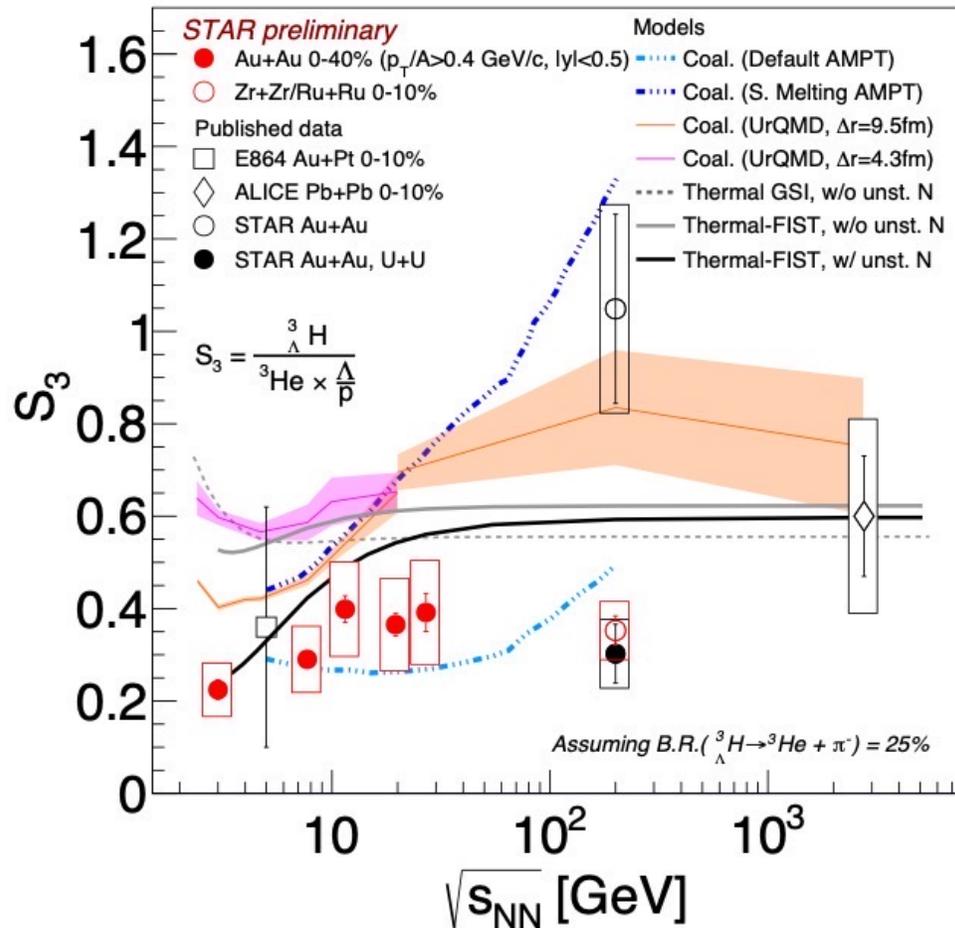


V. Vovchenko, PLB (2020) 135746

- Increasing trend observed in  $S_3$  vs collisions energy.
  - Possibly due to stronger feed down contribution in lower energies.

# System Size Dependence of $S_3$

STAR COL data: Yue Hang Leung, CPOD2024



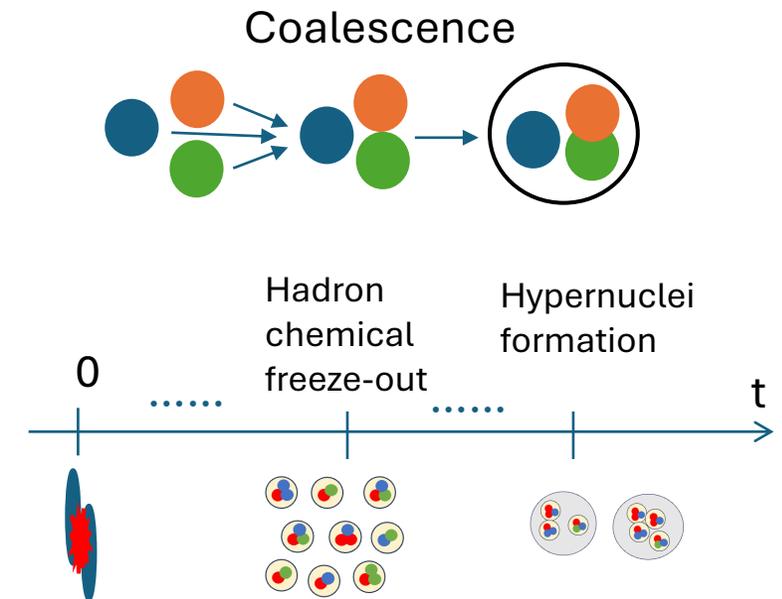
- Increasing trend observed in  $S_3$  vs collisions energy. V. Vovchenko, PLB (2020) 135746
  - Possibly due to stronger feed down contribution in lower energies.
- $S_3$  vs.  $dN_{ch}/d\eta$ : coalescence model describes the data within uncertainties.

# Summary

## New experimental data on:

- ${}^3_{\Lambda}\text{H}$  in 3.0 – 27 GeV Au+Au collisions
- ${}^4_{\Lambda}\text{H}$ ,  ${}^4_{\Lambda}\text{He}$  in 3.0 – 3.5 GeV Au+Au collisions
- ${}^3_{\Lambda}\text{H}$  in 200 GeV Zr+Zr/Ru+Ru collisions

- Experimental data support **coalescence is a dominate mechanism** of hypernuclei formation at mid-rapidity in heavy-ion collisions at RHIC.
- Hypernuclei **are not in equilibrium** at hadron chemical freeze-out at RHIC energies.

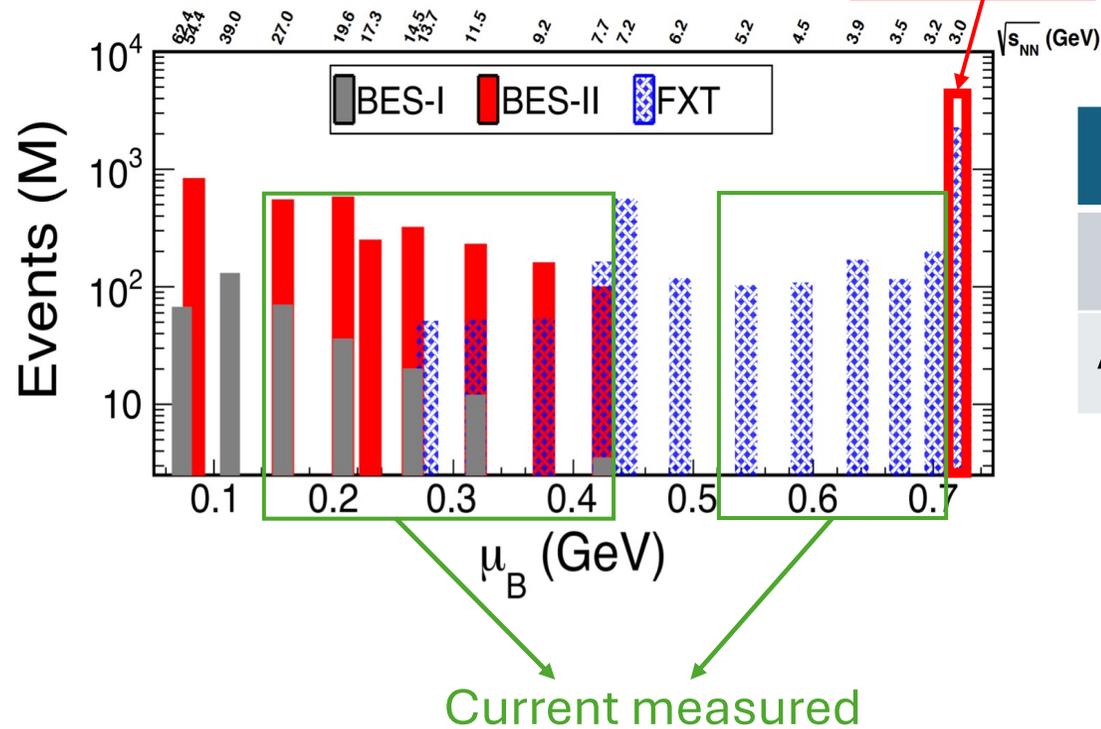


# What's Next at RHIC?

Huge datasets from BES-II and 200 GeV Au+Au collisions at RHIC.  
 - Enable measurements on both high  $\mu_B$  and  $\mu_B \rightarrow 0$  region.

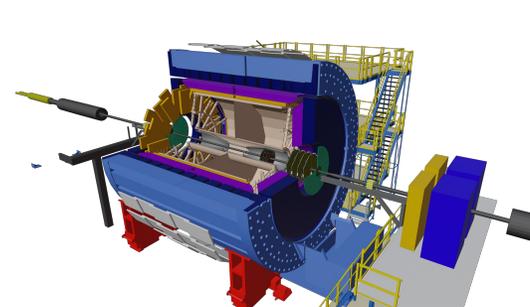
## BES II datasets

3 GeV 2B events!

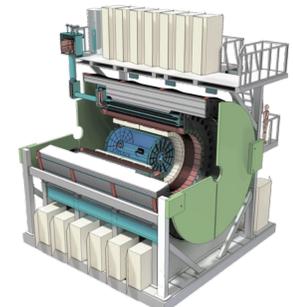


## High energy runs in 2023-2025

System	Run year	No. events/Luminosity
p+p 200 GeV	2024	235 pb <sup>-1</sup>
Au+Au 200 GeV	2023+2025	20B / 40 nb <sup>-1</sup>



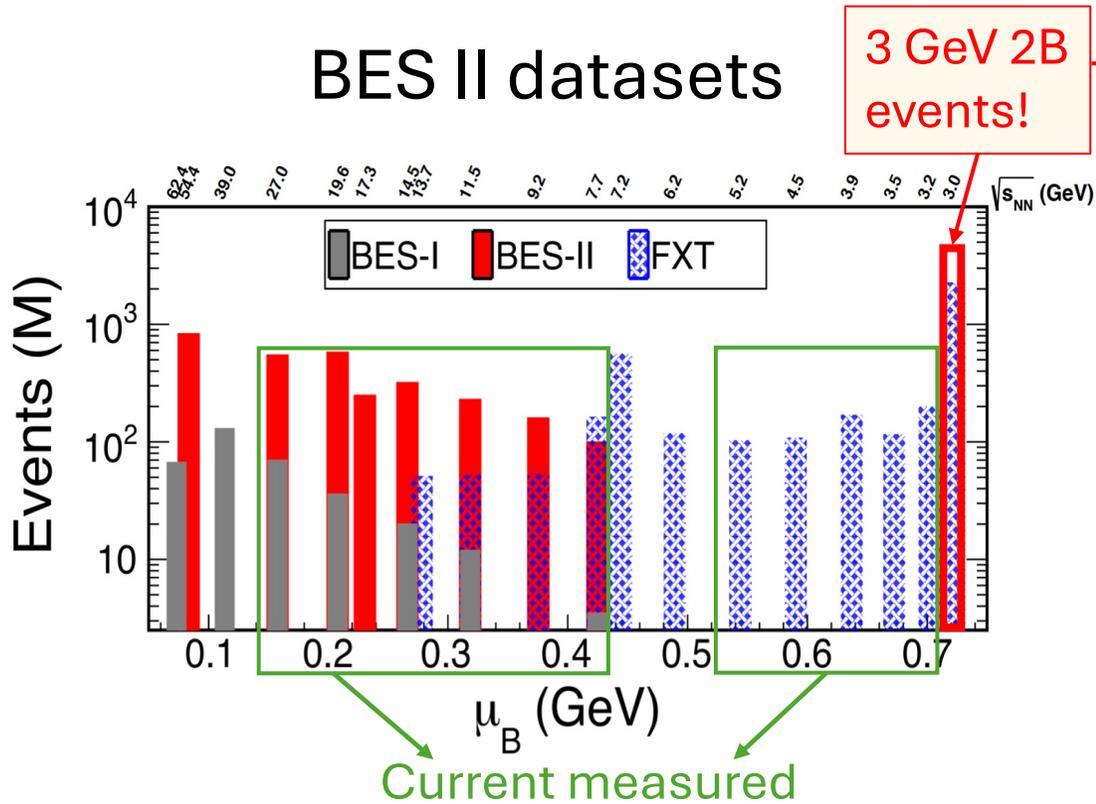
STAR



sPHENIX

# What's Next at RHIC?

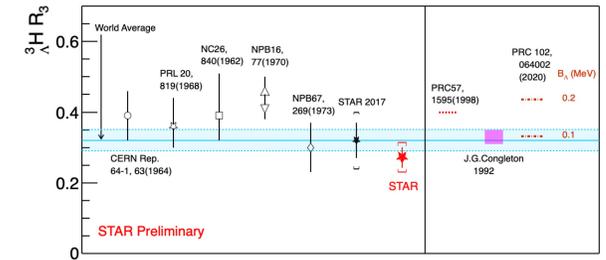
Huge datasets from BES-II and 200 GeV Au+Au collisions at RHIC.  
 - Enable measurements on both high  $\mu_B$  and  $\mu_B \rightarrow 0$  region.



**Expected total significance from BES-II:**

${}^4_\Lambda\text{H} : 60\sigma$ ;  ${}^4_\Lambda\text{He} : 40\sigma$ ;  ${}^5_\Lambda\text{He} : 10\sigma$

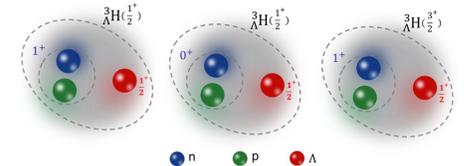
${}^3_\Lambda\text{H} R_3$



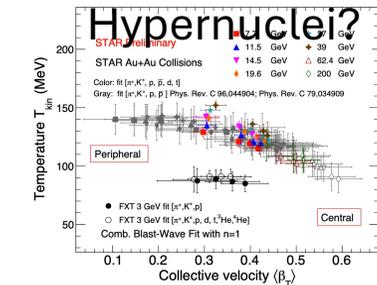
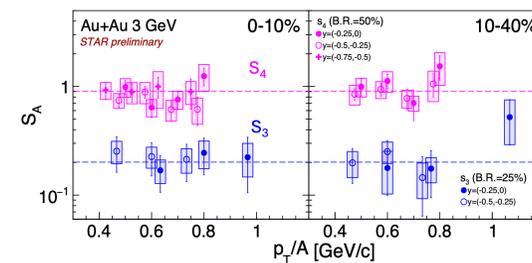
Global polarization

arXiv:2405.12015

Spin structures



Kinematics

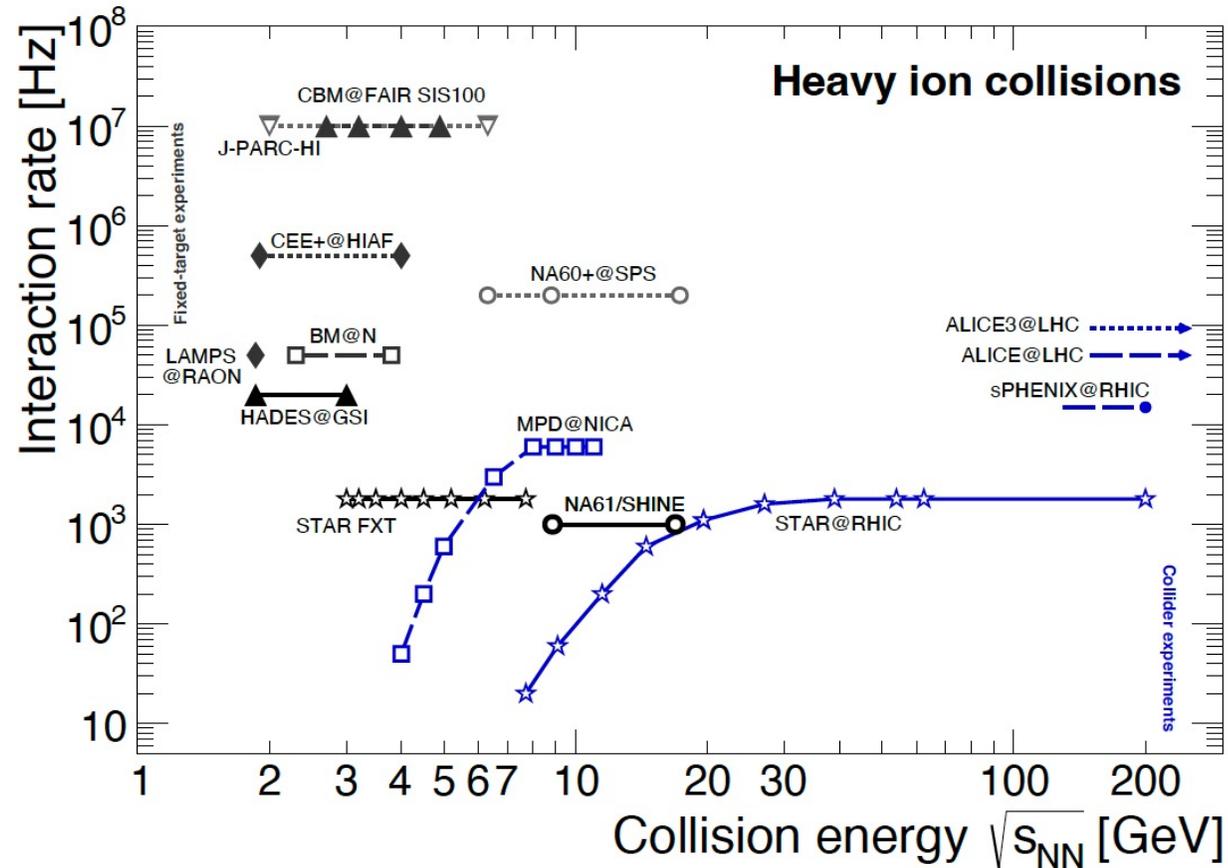


$\Xi^-$  and double- $\Lambda$  hypernuclei

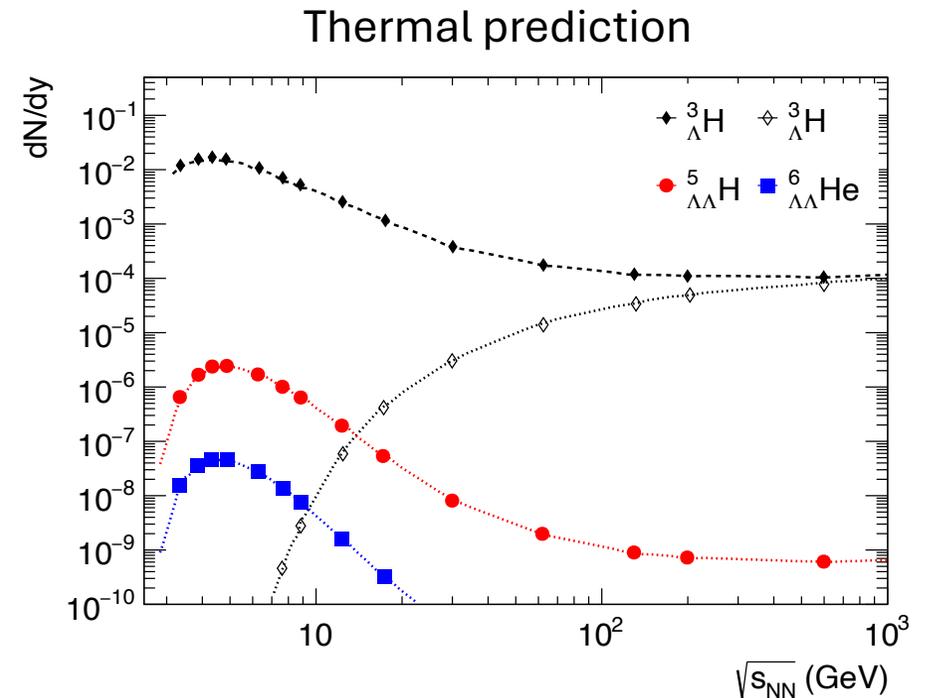
# Future Perspective

Great potential for discovering unobserved hypernuclei in heavy ion collisions.

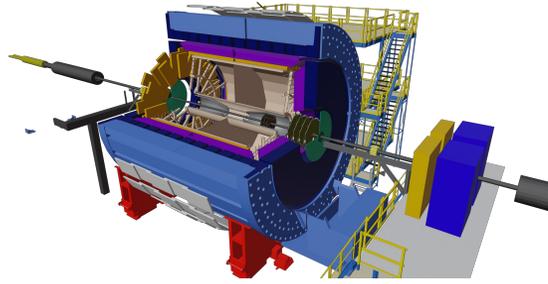
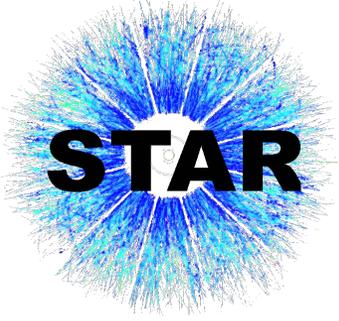
- $A \geq 5$  and  $\Xi$  hypernuclei
- Anti-hypernuclei
- Exotic strangeness states and double  $\Lambda$  hypernuclei
- etc



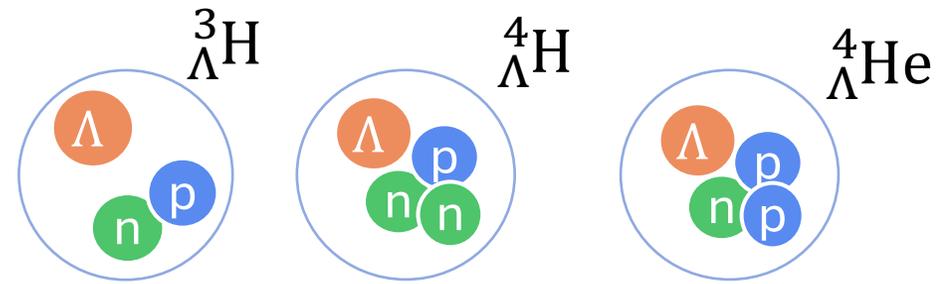
T. Galatyuk, NPA 982 (2019)

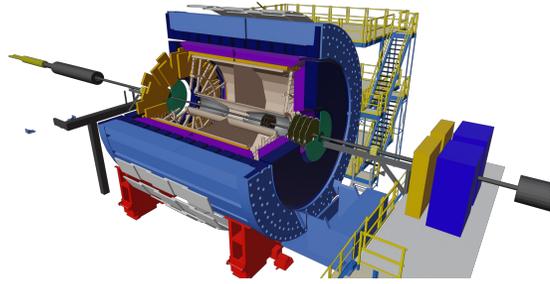
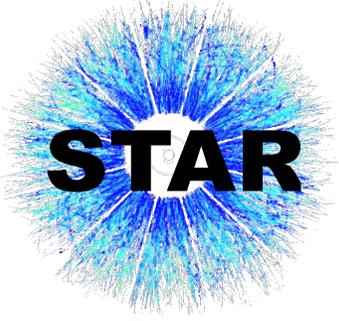


Thermal model: B. Dönigus, Eur. Phys. J. A 56:280 (2020)  
A. Andronic et al, PLB 697, 203 (2011)

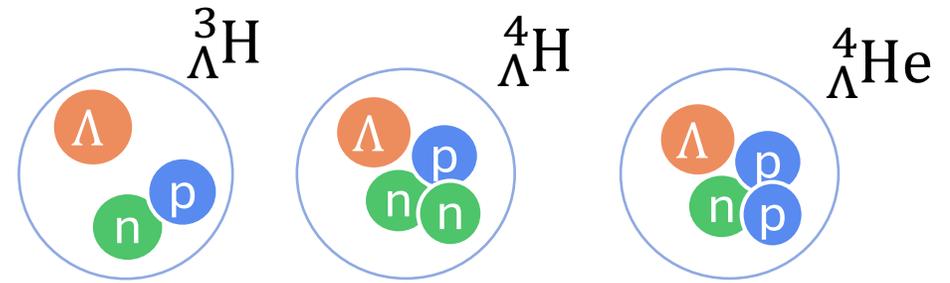


Thank you!



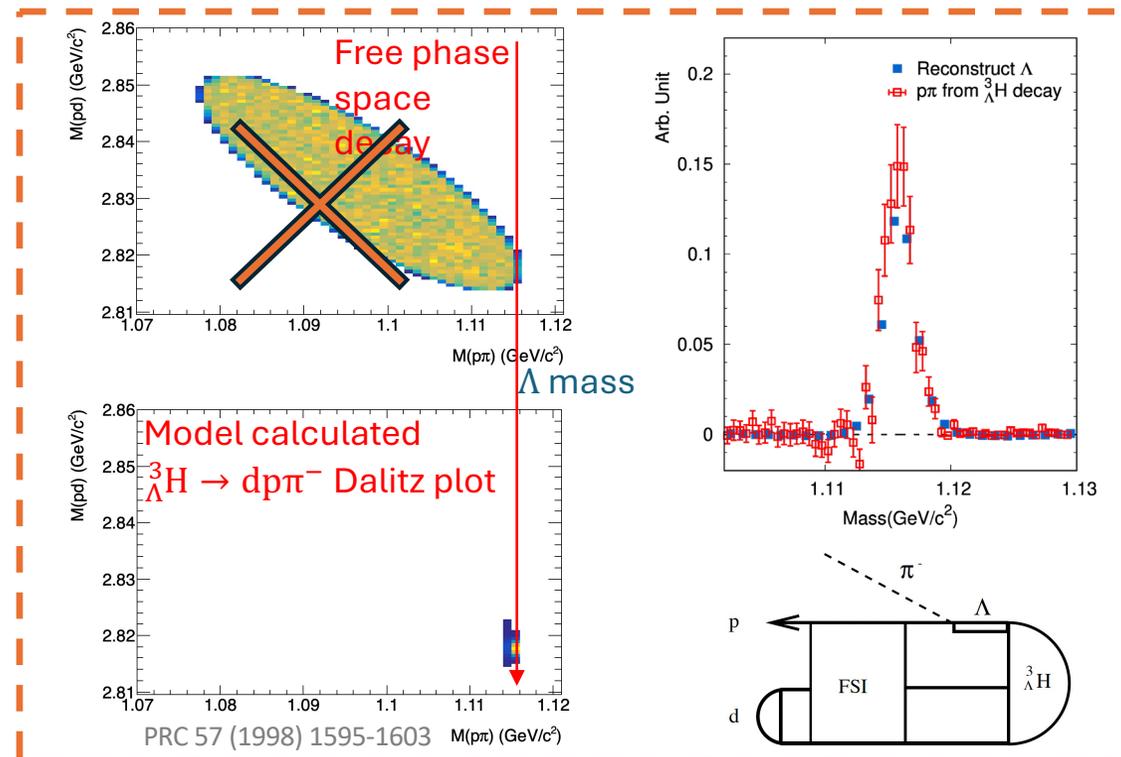
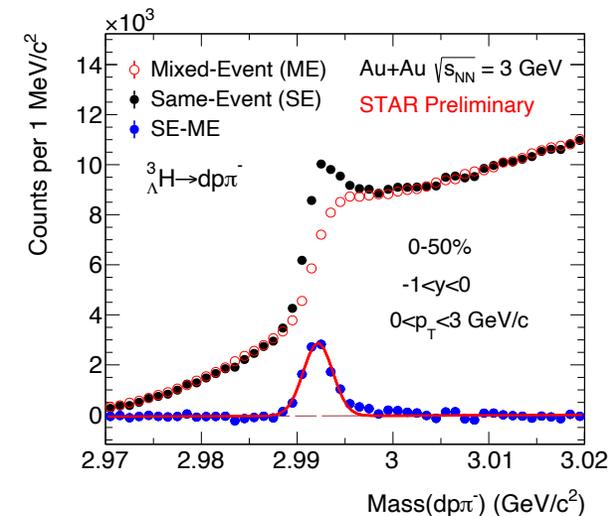
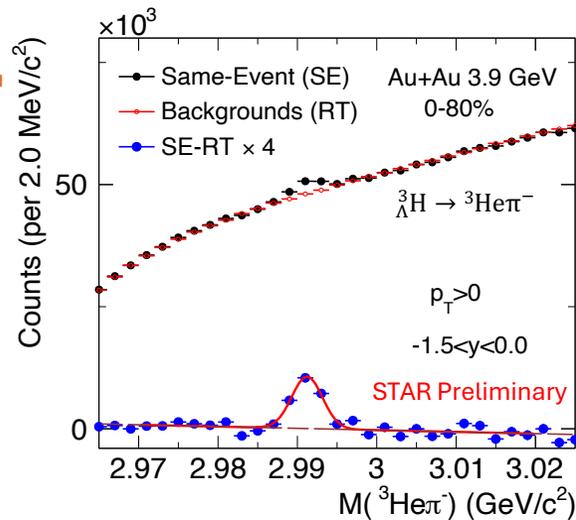
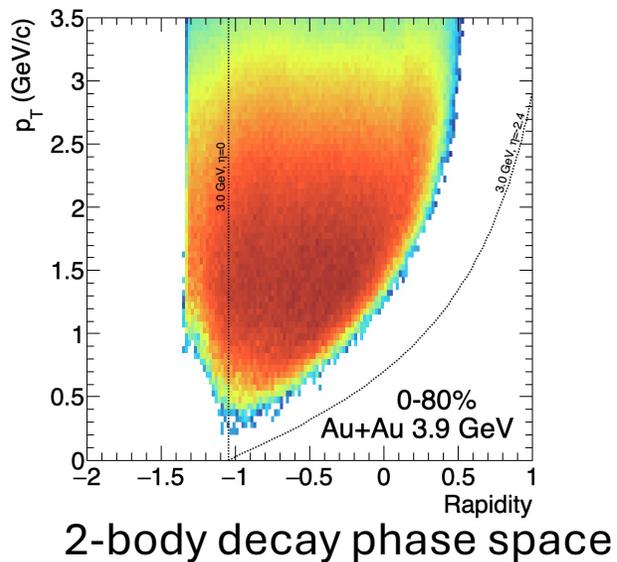
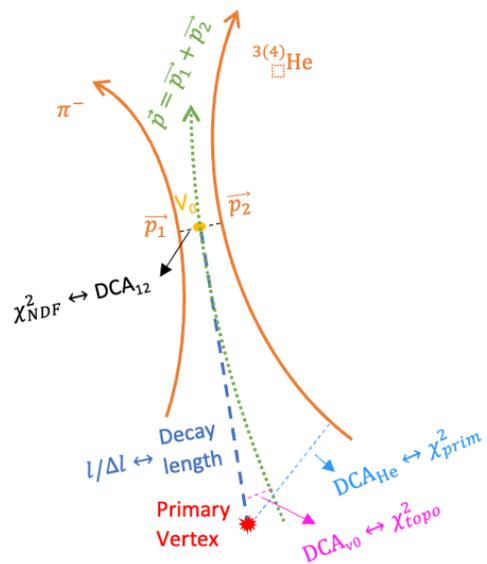


# Back ups



# ${}^3_{\Lambda}\text{H}$ reconstruction

- Decay channel:
  - ${}^3_{\Lambda}\text{H} \rightarrow {}^3\text{He} \pi^- \sim \text{B.R. } 20\text{-}25\%$ ,
  - ${}^3_{\Lambda}\text{H} \rightarrow d p \pi^- \sim \text{B.R. } \sim 40\text{-}50\%$ ,
- Backgrounds reconstructed by rotation of  ${}^3\text{He}$ .





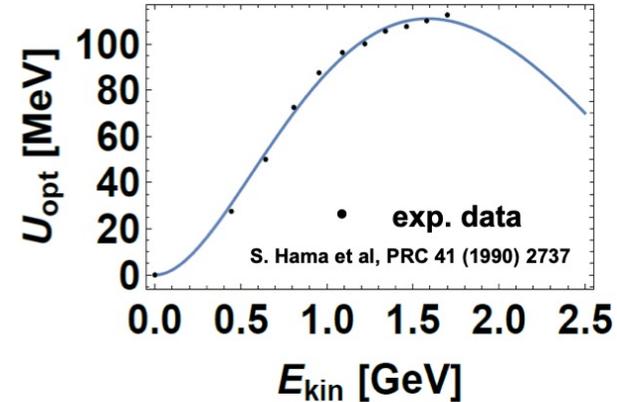
## 2) Momentum dependent potential :

$$V(\mathbf{r}_1, \mathbf{r}_2, \mathbf{p}_{01}, \mathbf{p}_{02}) = (a\Delta p + b\Delta p^2) \exp[-c\sqrt{\Delta p}] \delta(\mathbf{r}_1 - \mathbf{r}_2)$$

$$\Delta p = \sqrt{(\mathbf{p}_{01} - \mathbf{p}_{02})^2}$$

Parameters **a**, **b**, **c** are fitted to the "optical" potential (Schrödinger equivalent potential  $U_{SEP}$ )

extracted from elastic scattering data in pA:  $U_{SEQ}(p) = \frac{\int^{p_F} V(\mathbf{p} - \mathbf{p}_1) d^3p_1}{\frac{4}{3}\pi p_F^3}$



❖ In infinite matter a potential corresponds to the EoS:

$$E/A(\rho) = \frac{3}{5}E_F + V_{Skyrme\ stat}(\rho) + V_{mom}(\rho)$$

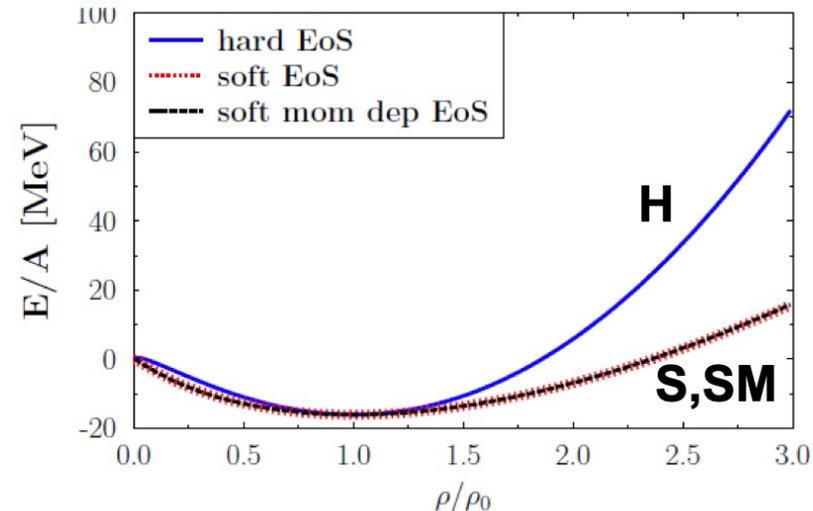
$$V_{Skyrme} = \alpha \frac{\rho}{\rho_0} + \beta \frac{\rho^\gamma}{\rho_0}$$

compression modulus **K** of nuclear matter:

$$K = -V \frac{dP}{dV} = 9\rho^2 \frac{\partial^2(E/A(\rho))}{(\partial\rho)^2} \Big|_{\rho=\rho_0}$$

E.o.S.	$\alpha$ [MeV]	$\beta$ [MeV]	$\gamma$	K [MeV]
S	-383.5	329.5	1.15	200
H	-125.3	71.0	2.0	380
SM	-478.87	413.76	1.10	200
	$a$ [MeV <sup>-1</sup> ]	$b$ [MeV <sup>-2</sup> ]	$c$ [MeV <sup>-1</sup> ]	
	236.326	-20.73	0.901	

EoS for infinite cold nuclear matter at rest

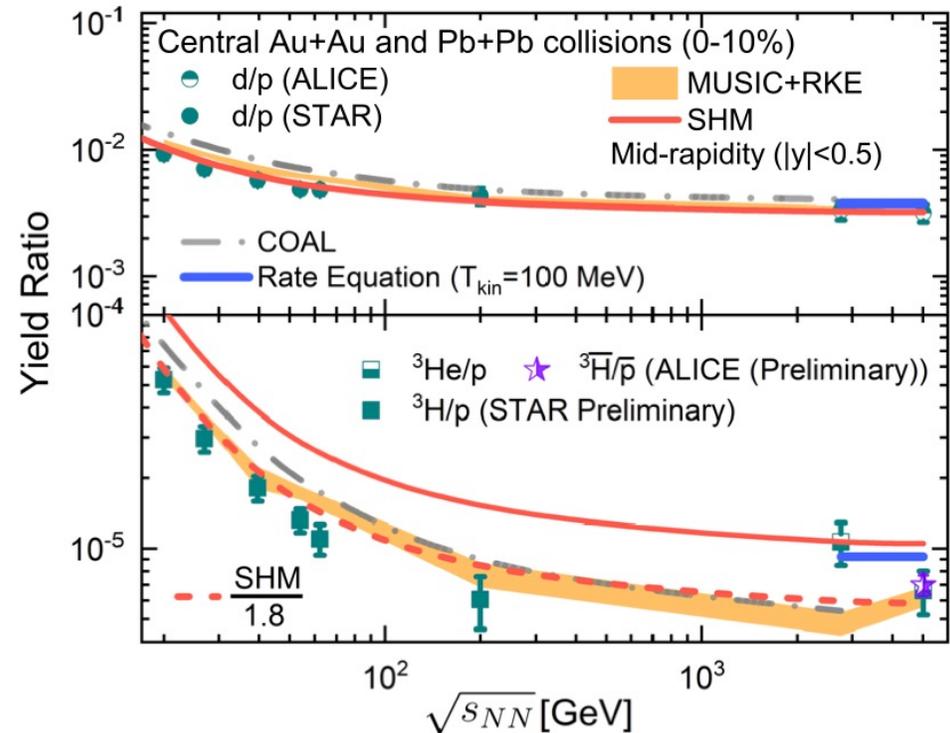
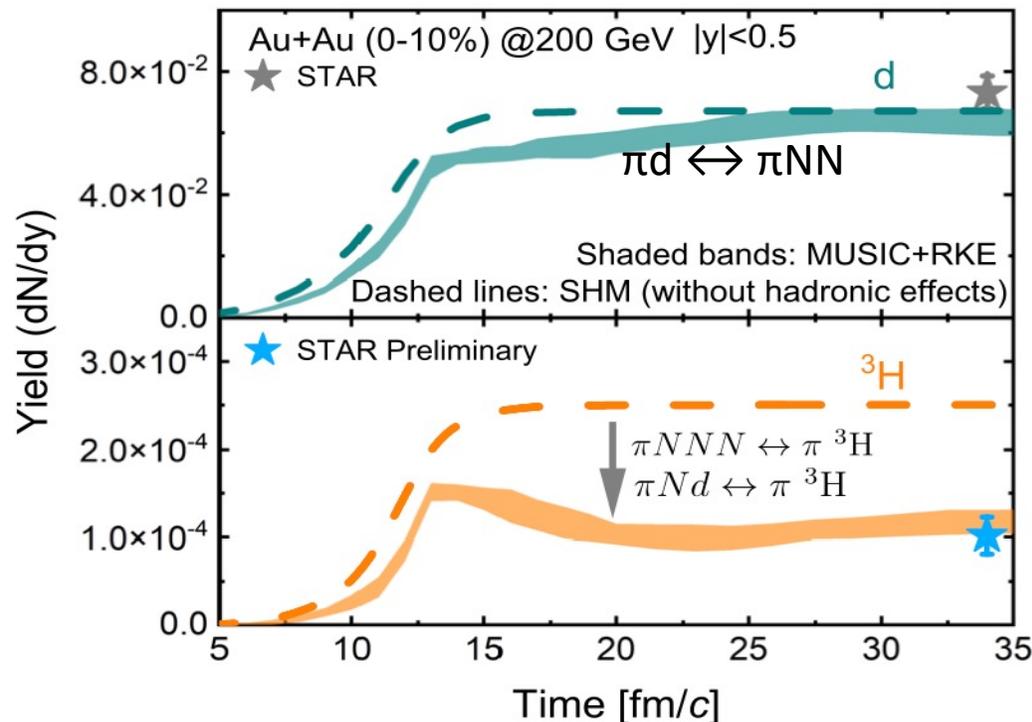


# Other possible model: kinetic approach

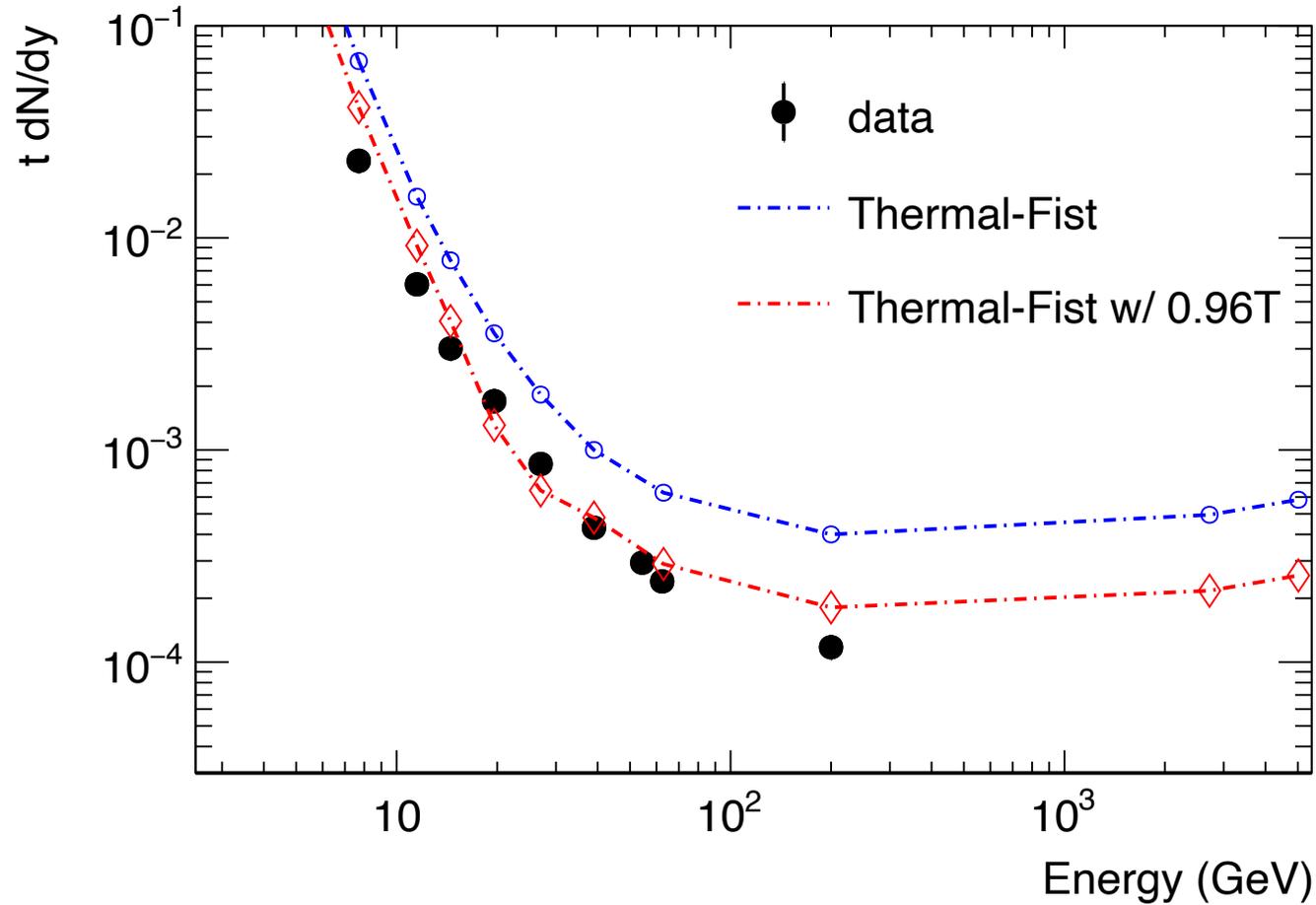
- Relativistic kinetic equation (RKE) to include hadronic re-scattering processes.
  - Close connection to Coal. via final state interaction close to kinetic freeze-out.

*P. Danielewicz et al. NPA 533 (1991) 712-748*  
*Kaijia Sun et al, Nature Commun. 15 (2024) 1, 1074*

- Evolution of QGP: MUSIC
- Hadron and light nuclei yields at QGP hadronization: SHM
- The evolution of the hadronic matter (besides the nonlocal many-body scatterings for d / t): AMPT



# Triton yields with tuned T



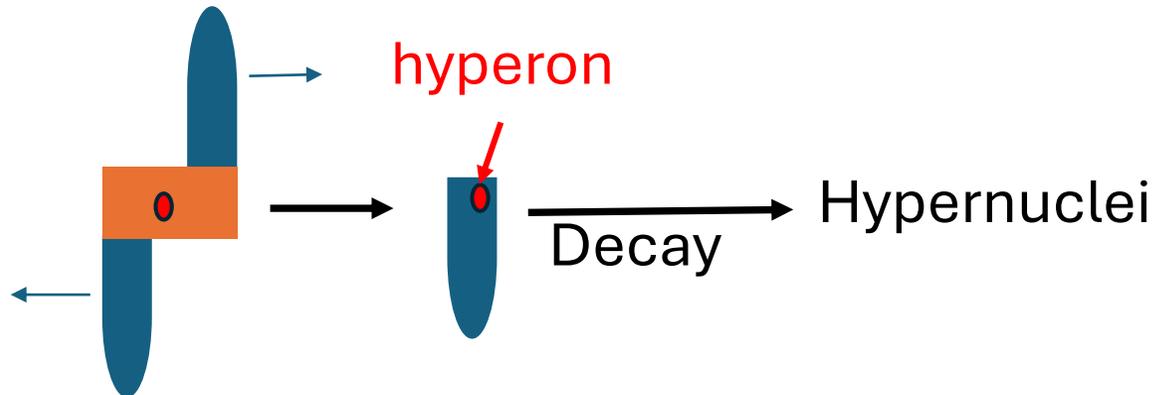
- Triton yields are closer to the data compared with default Thermal.

# Hypernuclei Production in HIC

## Other proposed mechanism

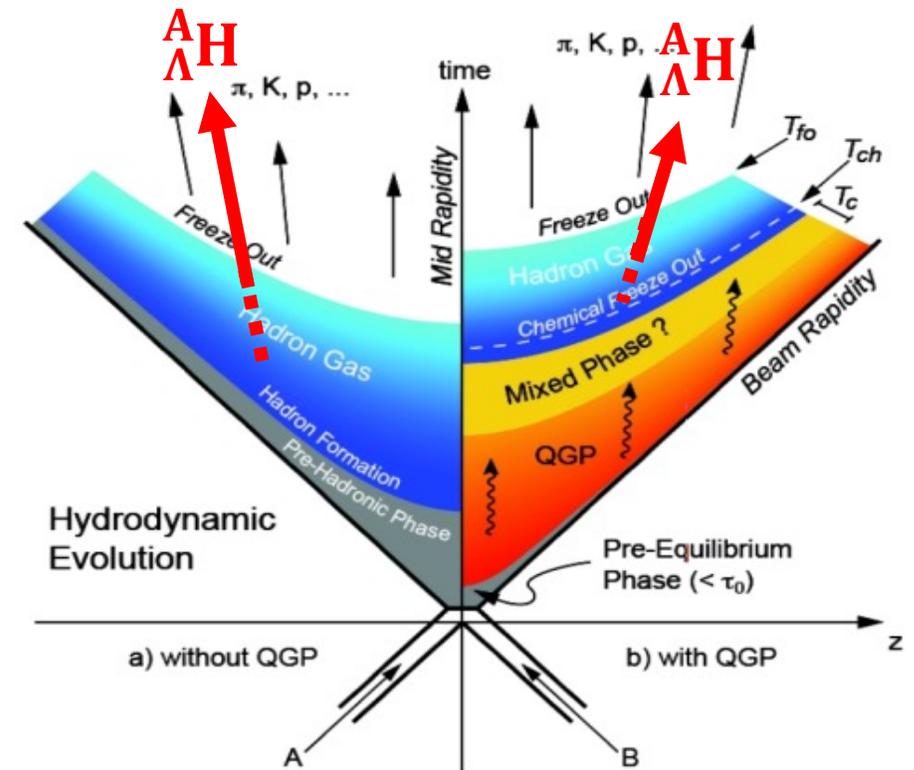
### Nuclear fragmentation of hypercluster

- Dominates at **beam rapidity**.
- Dominates for heavy hypernuclei formation.

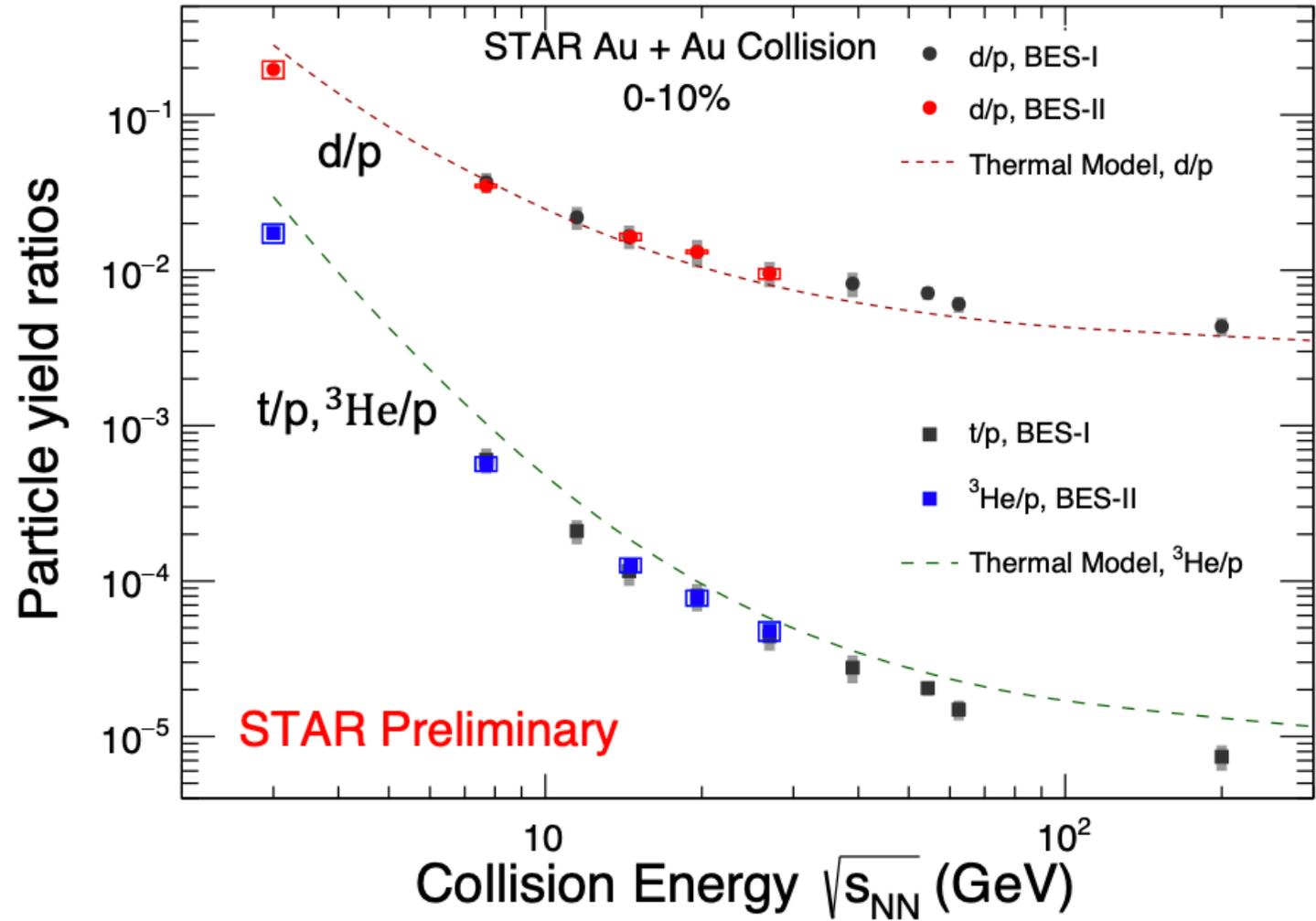


M. Wakai et al. PRC 38, 748 (1988)

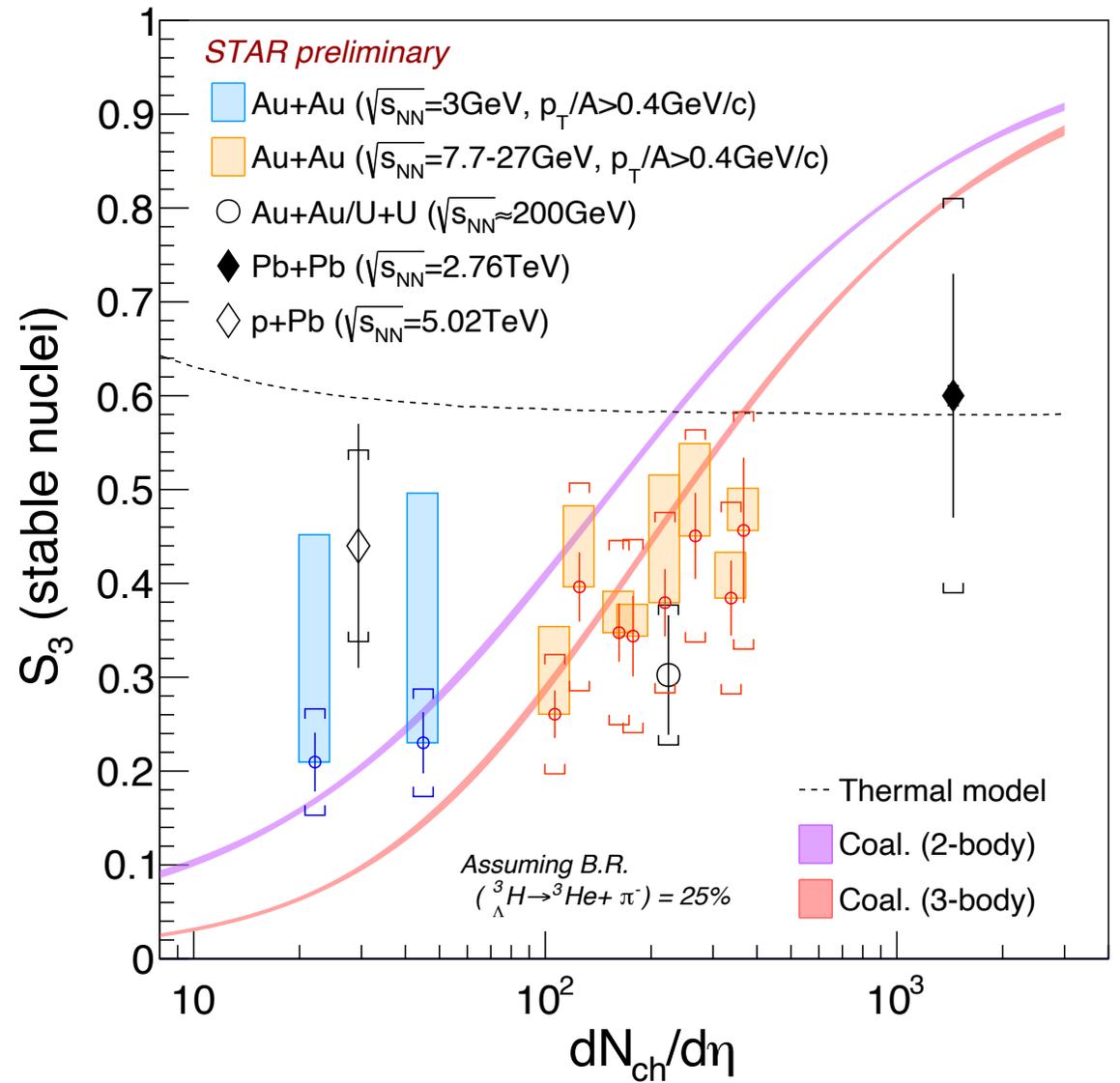
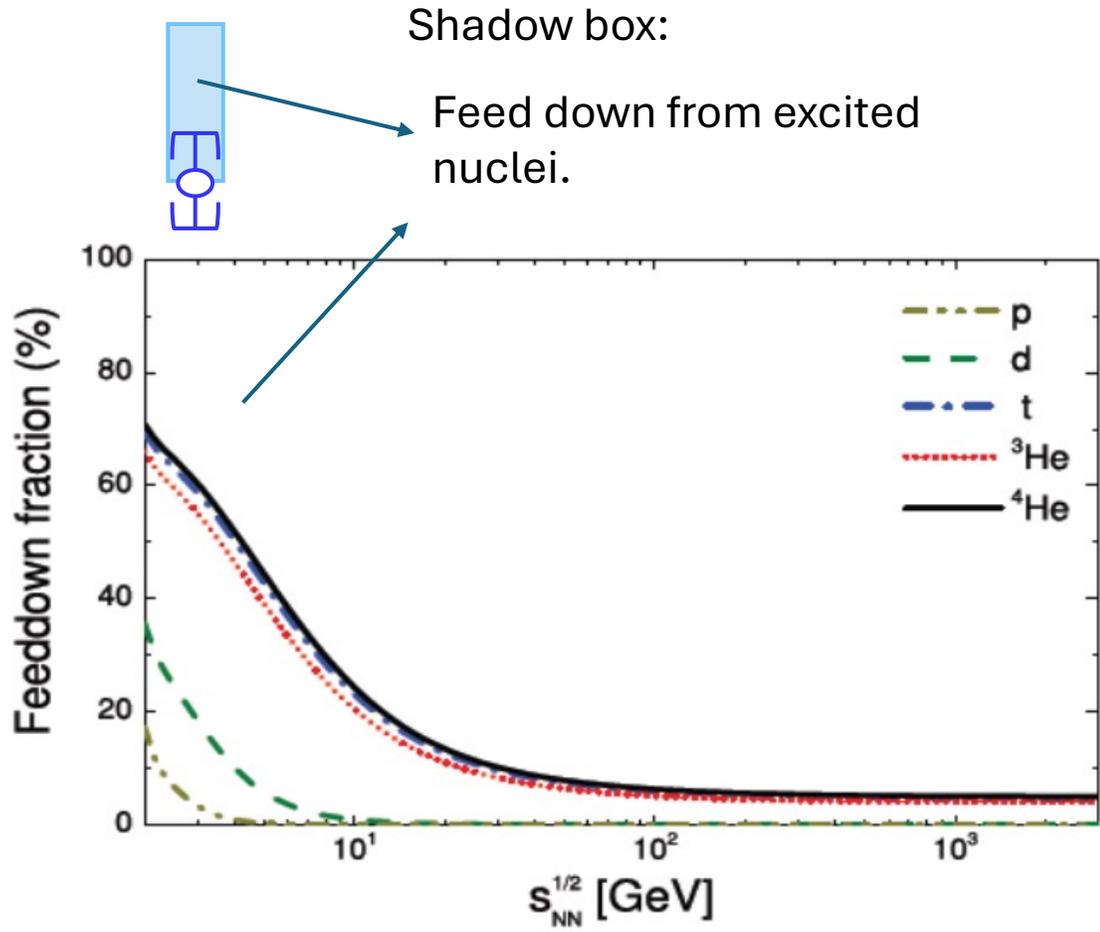
A.S. Botvina et al. PLB 742, 7-14 (2015)



# $^3\text{He}/p$ and $d/p$ from BES II



STAR, Phys. Rev. Lett. 130, 202301 (2023)



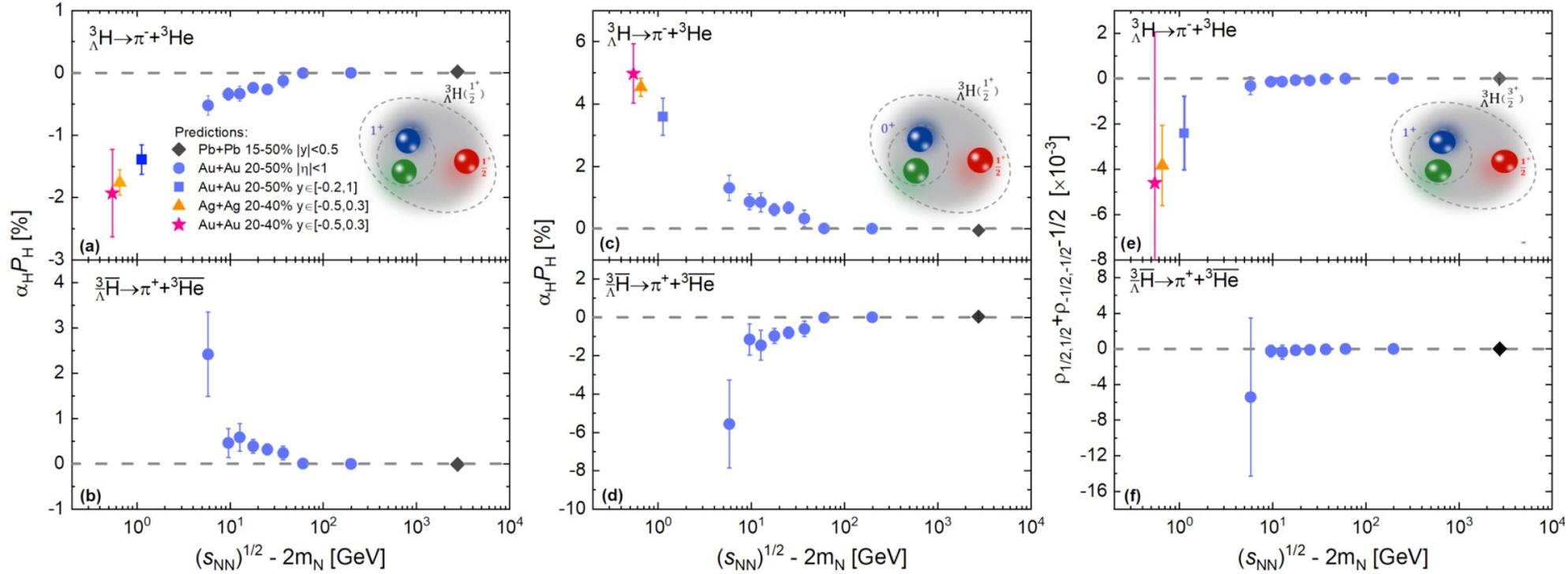
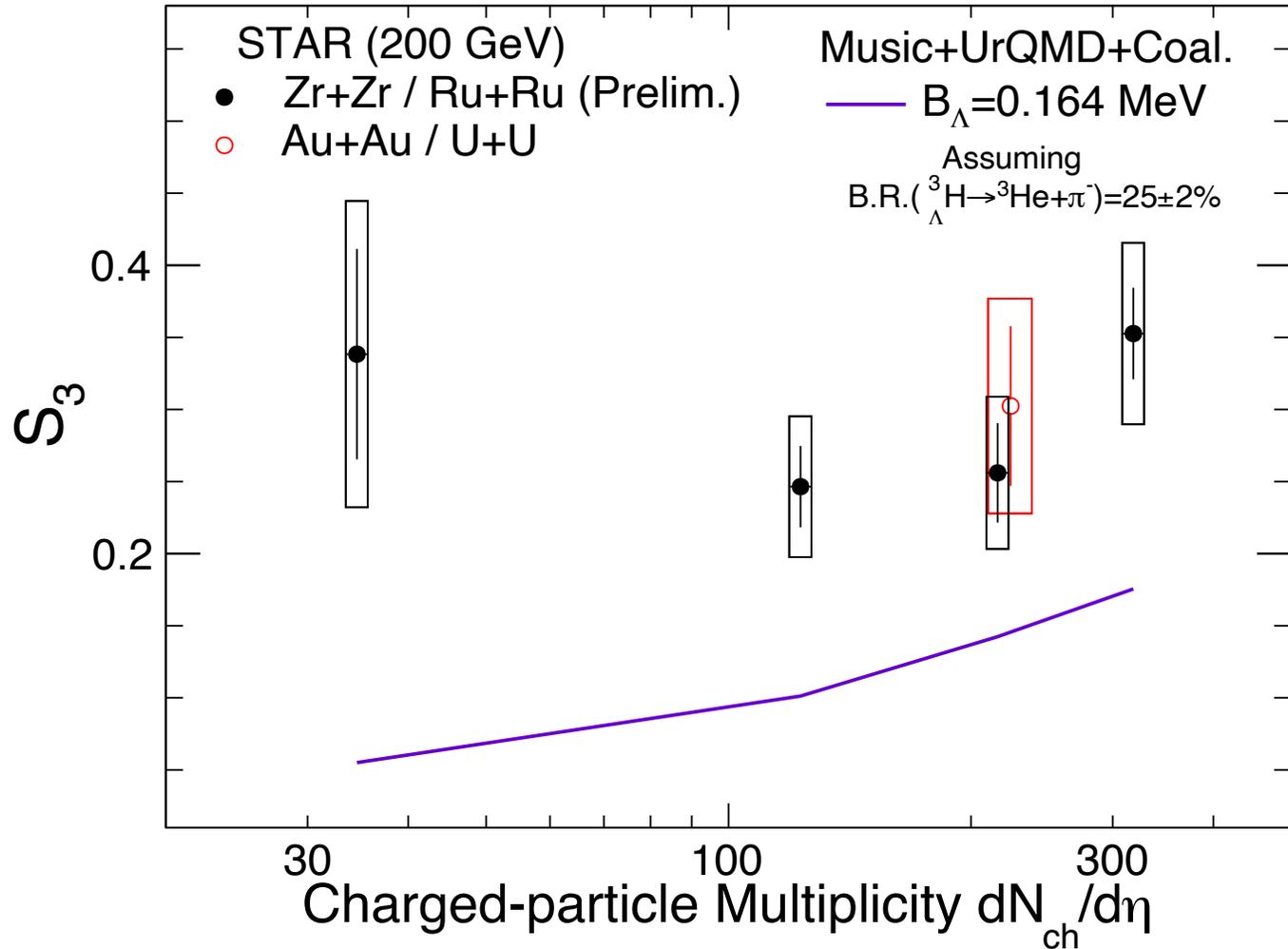


FIG. 2. Collision energy dependence of (anti-)hypertriton polarization predicted from the decay channel  ${}^3_{\Lambda}\text{H} \rightarrow \pi^{-} + {}^3\text{He}$  (upper panels) and  ${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^{+} + {}^3\bar{\text{He}}$  (lower panels) based on the  $\Lambda$  polarization data from the STAR [51], ALICE [52], and HADES [53] Collaborations. Panels (a) and (b) depict results for  ${}^3_{\Lambda}\text{H}(\frac{1}{2}^{+})$  and  ${}^3_{\Lambda}\bar{\text{H}}(\frac{1}{2}^{-})$ , respectively, assuming the two nucleons inside the (anti-)hypertriton are in a spin-triplet state, while results shown in panels (c) and (d) are for the case that the two nucleons are in a spin-singlet state. Panels (e) and (f) depict results for the combined spin density matrix element  $\hat{\rho}_{\frac{1}{2},\frac{1}{2}} + \hat{\rho}_{-\frac{1}{2},-\frac{1}{2}} - \frac{1}{2}$  for  ${}^3_{\Lambda}\text{H}(\frac{3}{2}^{+})$  and  ${}^3_{\Lambda}\bar{\text{H}}(\frac{3}{2}^{-})$ , respectively.

# Multiplicity Dependence of $S_3$ at $\mu_B \rightarrow 0$

Dongsheng Li, SQM 2024

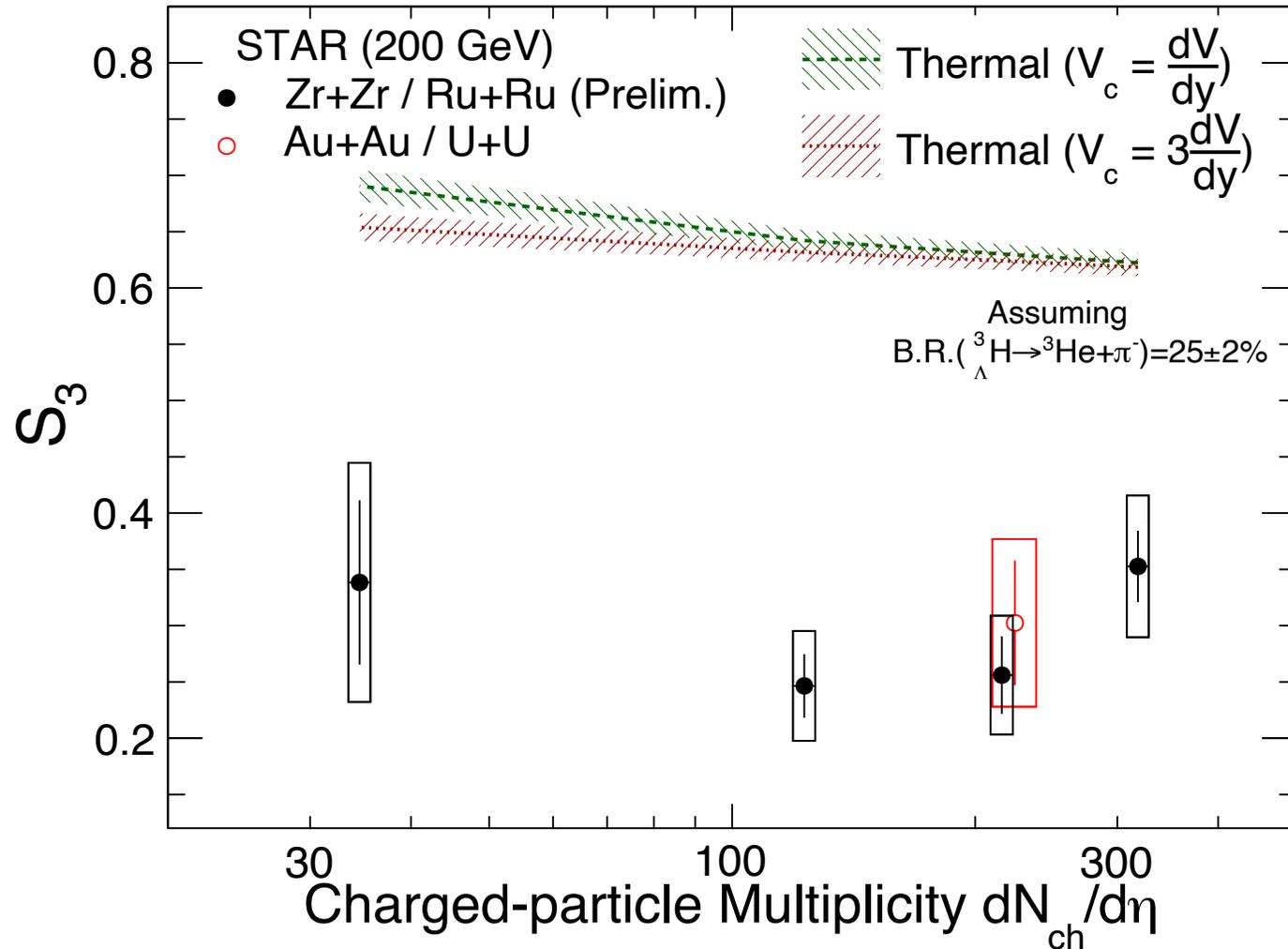


- No obvious multiplicity dependence within uncertainties
- Within uncertainties, coalescence calculations are consistent with the measured data
  - More precise data needed

STAR: arXiv:2310.12674; Science 328, 58-62 (2010)  
MUSIC + UrQMD + Coal.: arXiv:2404.02701

# Multiplicity Dependence of $S_3$ at $\mu_B \rightarrow 0$

Dongsheng Li, SQM 2024



- Thermal-FIST with canonical ensemble fails to describe the data trend
  - Ratios have already canceled volume size and strangeness suppression factor

STAR: arXiv:2310.12674; Science 328, 58-62 (2010)  
 Thermal-FIST: Com. Phys. Comm. 244, 295 (2019)  
 PLB 785, 171 (2018)

T and  $\mu_B$  from  $\pi/K/p$  spectra