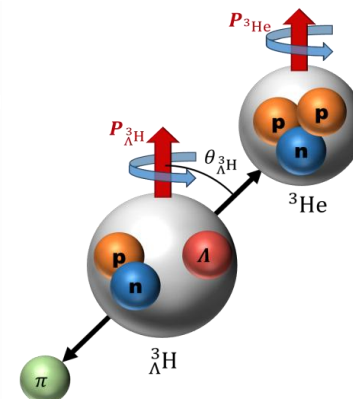
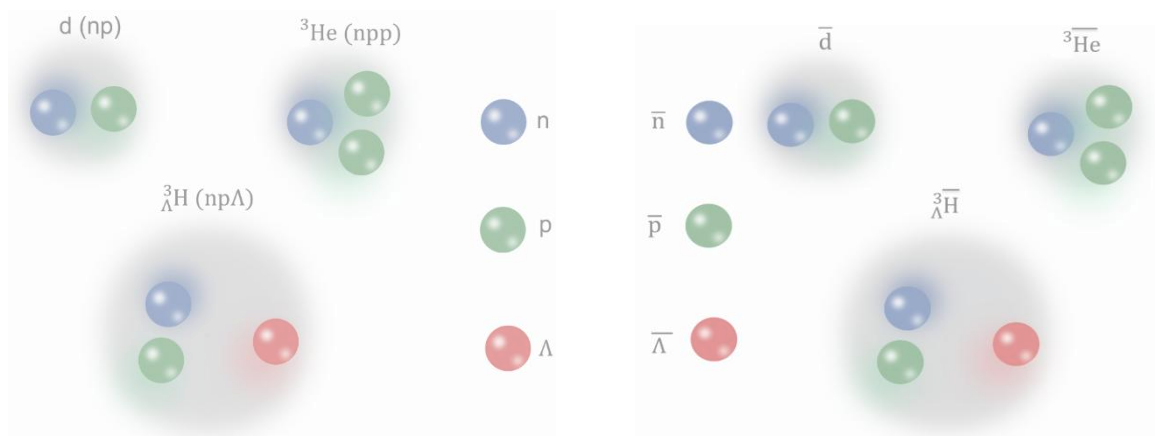
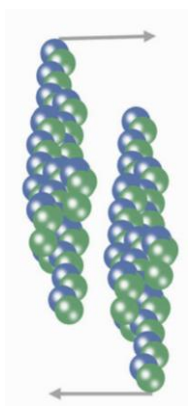


Production and Polarization of Hypernuclei in Heavy-Ion Collisions

KJ Sun, Dai-Neng Liu, Yun-Peng Zhen, Jin-Hui Chen, Che Ming Ko, Yu-Gang Ma [arXiv:2405.12015](#)



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Oct. 24, 2024



復旦大學
FUDAN UNIVERSITY

Outline

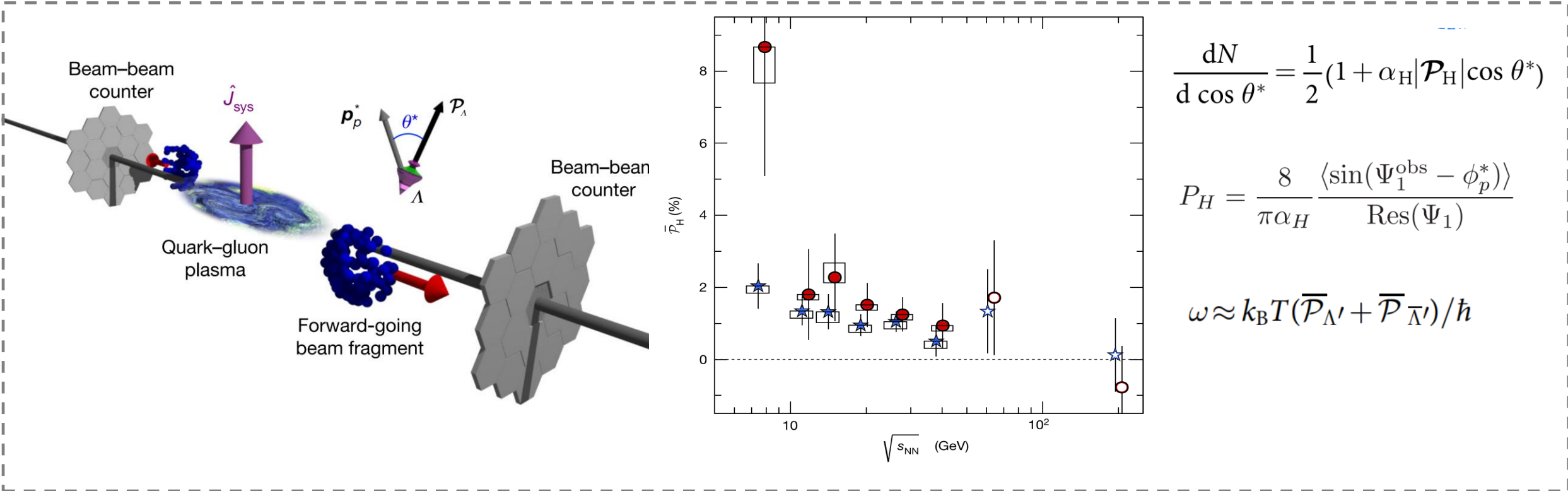
1. Polarization in heavy-ion collisions
2. The property and production of (anti-)hypertriton
3. Results: (Anti-)Hypertriton polarization and its spin structure
4. Discussions: Effects of baryon spin correlations
5. Summary and outlook

1. Polarization of hadrons in relativistic heavy-ion collisions (1)

STAR, Nature 548, 62 (2017)

Z. T. Liang and X. N. Wang PRL 94, 102301 (2005)

F. Becattini, F. Piccinini, and J. Rizzo, PRC 77, 024906 (2008)



Spin polarization of Lambda hyperon

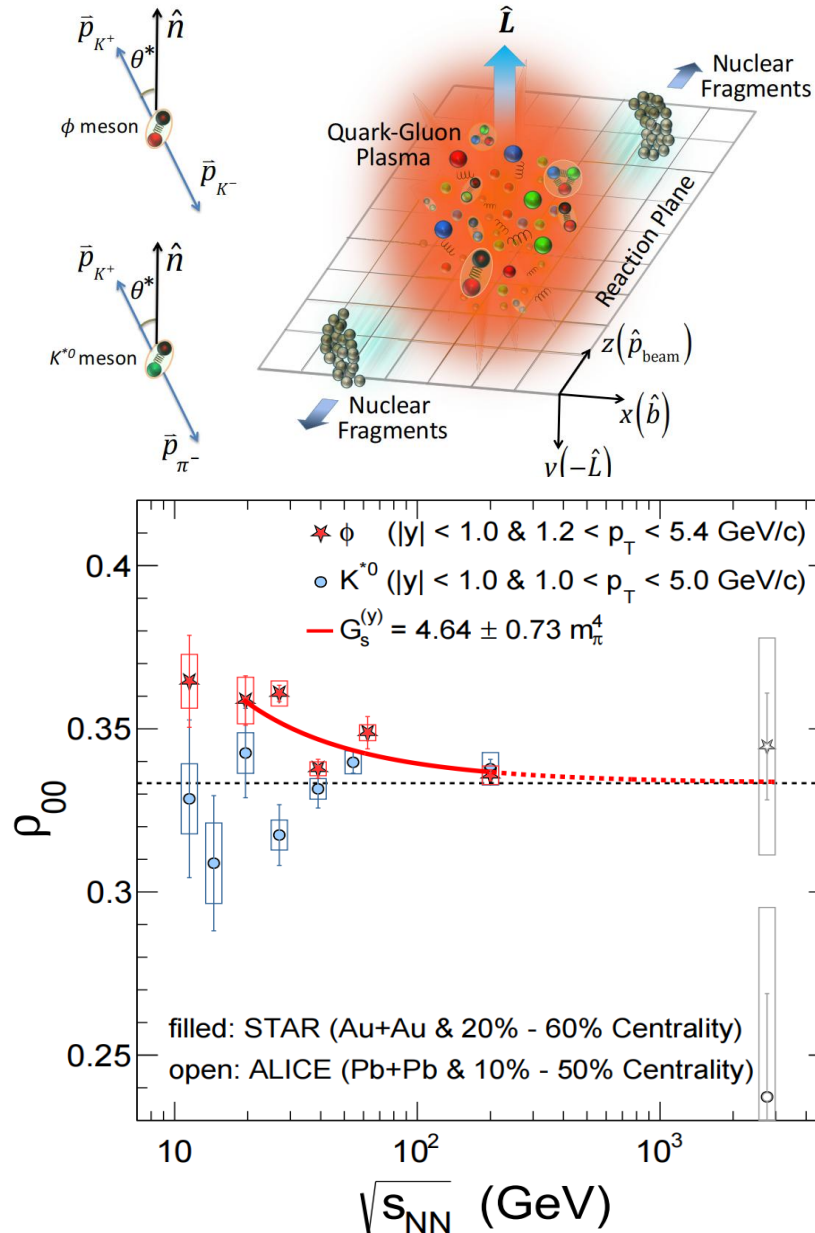


Vorticity of QGP

1. Polarization of hadrons in relativistic heavy-ion collisions

(2)

STAR, Nature 614, 7947 (2023)



Spin alignment of mesons

$$\frac{dN}{d(\cos\theta^*)} \propto (1 - \rho_{00}) + (3\rho_{00} - 1)\cos^2\theta^*$$



Fluctuation/correlation of strong force field

X. L. Sheng et al., PRL 131, 042304 (2023)

$$G_s^{(y)} \equiv g_\phi^2 \left[3\langle B_{\phi,y}^2 \rangle + \frac{\langle \mathbf{p}^2 \rangle_\phi}{m_s^2} \langle E_{\phi,y}^2 \rangle - \frac{3}{2} \langle B_{\phi,x}^2 + B_{\phi,z}^2 \rangle - \frac{\langle \mathbf{p}^2 \rangle_\phi}{2m_s^2} \langle E_{\phi,x}^2 + E_{\phi,z}^2 \rangle \right]$$

Quark-antiquark spin correlation

J. P. Lv et al., arXiv:2402.13721

Meson spectral property

F. Li and S. Liu, arXiv:2206.11890

1. Polarization of light (anti-)(hyper-)nuclei

(3)

Unstable hadrons

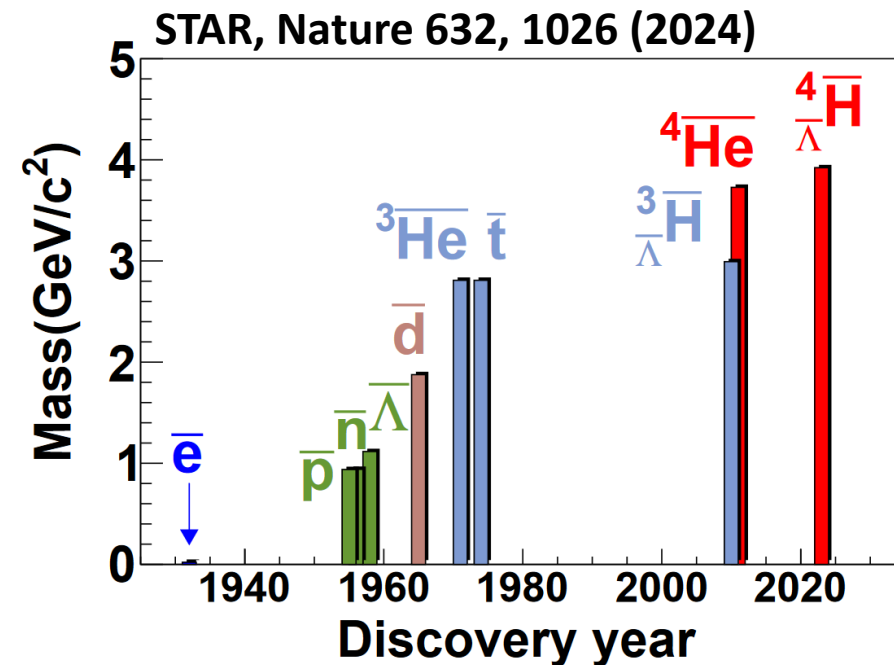
$\Lambda(uds)$ $\Xi(uss)$ $\Omega(sss)$
 $\phi(s\bar{s})$ $K^{*0}(d\bar{s})$ $\rho^+(u\bar{d})$
 $J/\psi(c\bar{c})$...

Unstable (anti-)(hyper-)nuclei

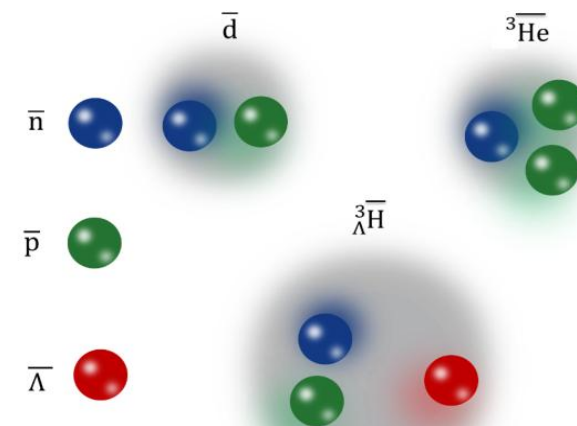
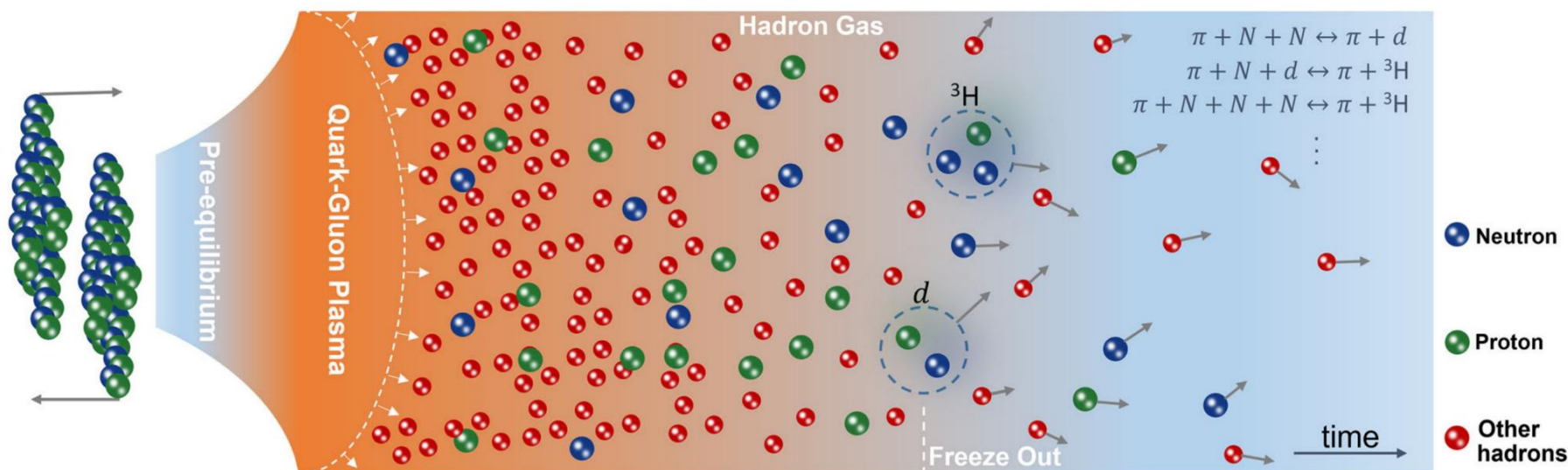
${}^3\Lambda\text{H}(np\Lambda)$ ${}^4\text{Li}(nppp)$
 ${}^3_{\Lambda}\bar{\text{H}}(\bar{n}\bar{p}\bar{\Lambda})$ ${}^4\bar{\text{Li}}(\bar{n}\bar{p}\bar{p}\bar{p})$
 ...

Stable (anti-)nuclei

$d(np)$ ${}^3\text{He}(npp)$
 $\bar{d}(\bar{n}\bar{p})$ ${}^3\bar{\text{He}}(\bar{n}\bar{p}\bar{p})$
 ...



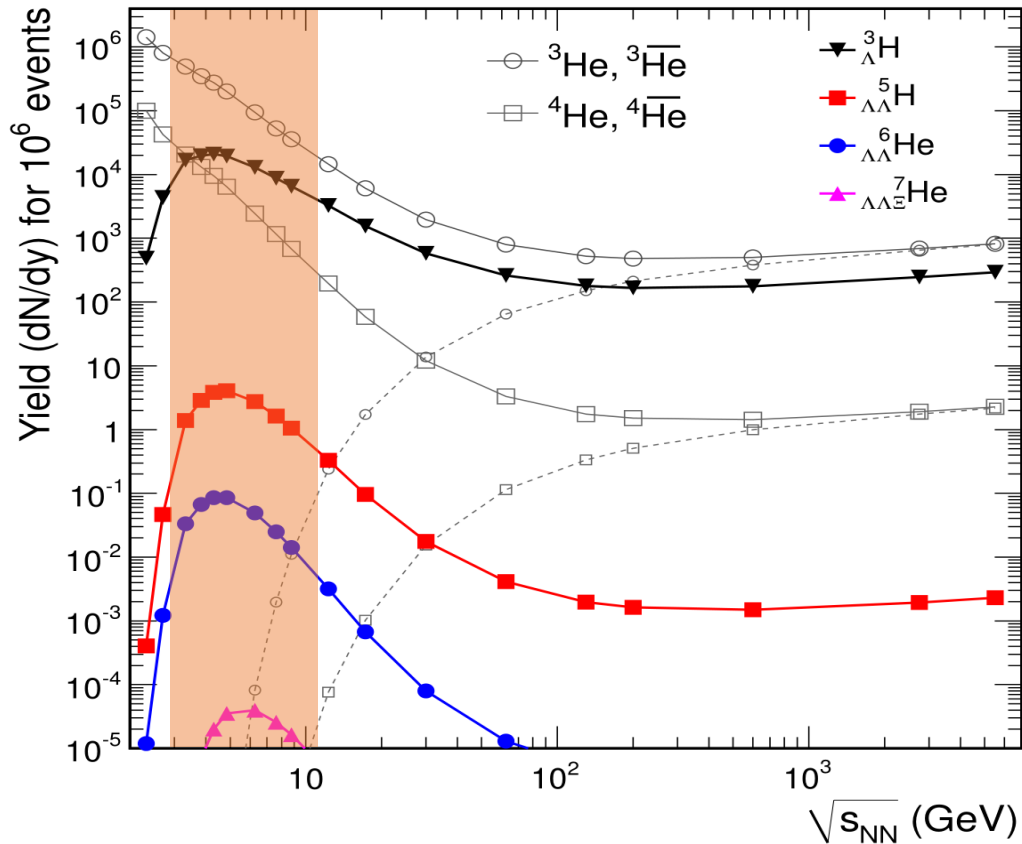
K. J. Sun, R. Wang, C. M. Ko, Y. G. Ma, C. Shen, *Nature Commun.* 15, 1074 (2024)



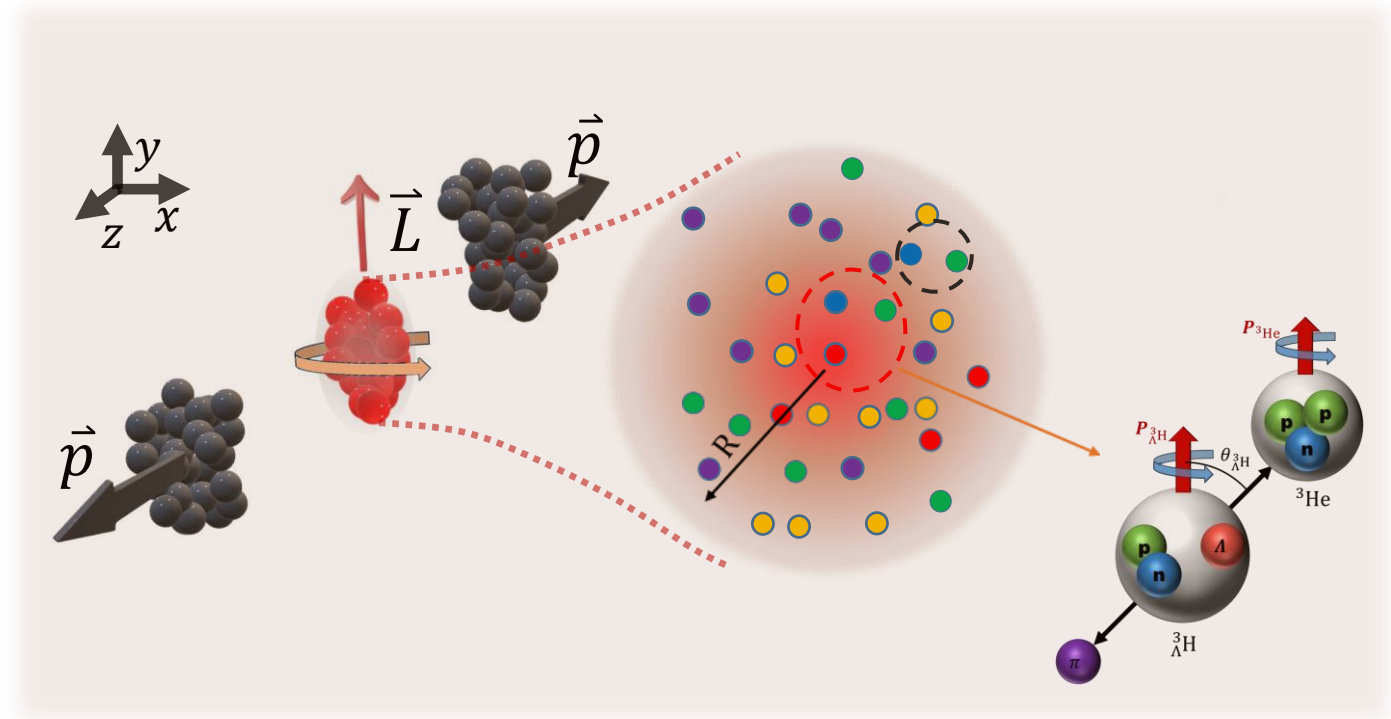
1. Polarization of light (anti-)(hyper-)nuclei

(4)

A. Andronic et al., Phys. Lett. B 697, 203-207 (2011)



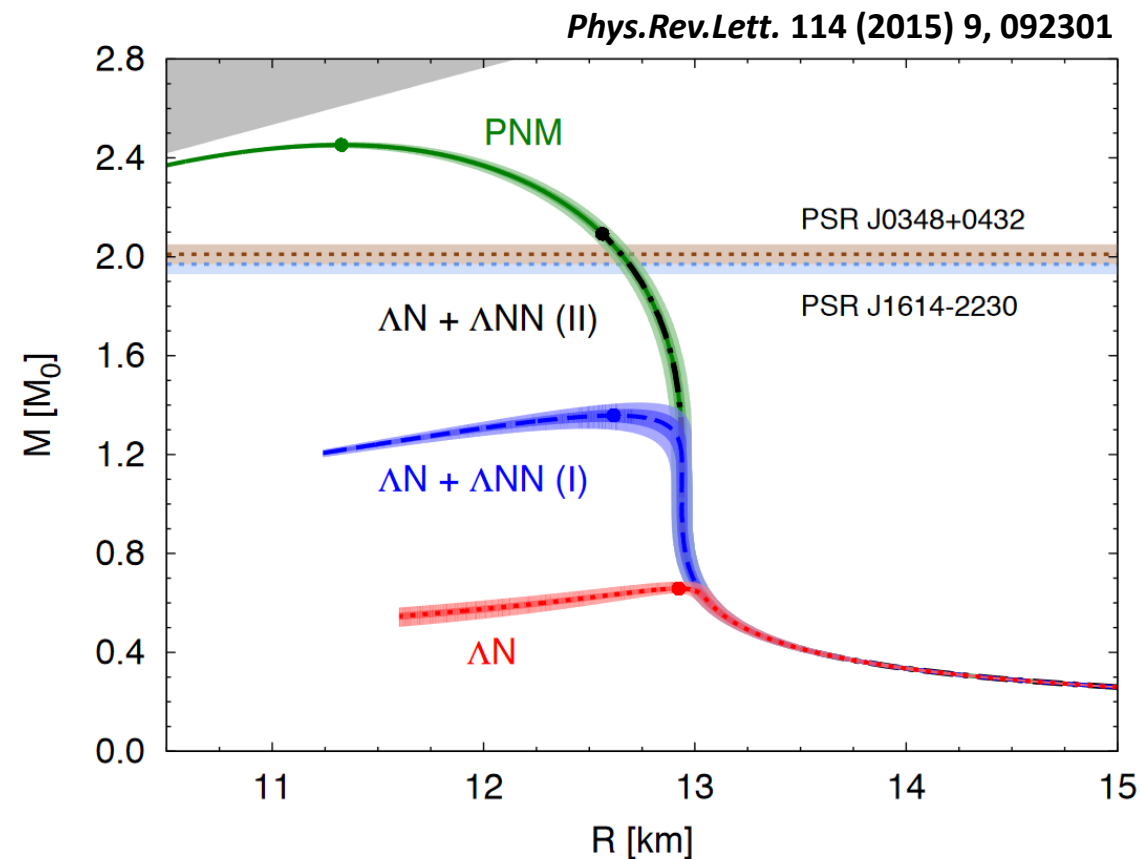
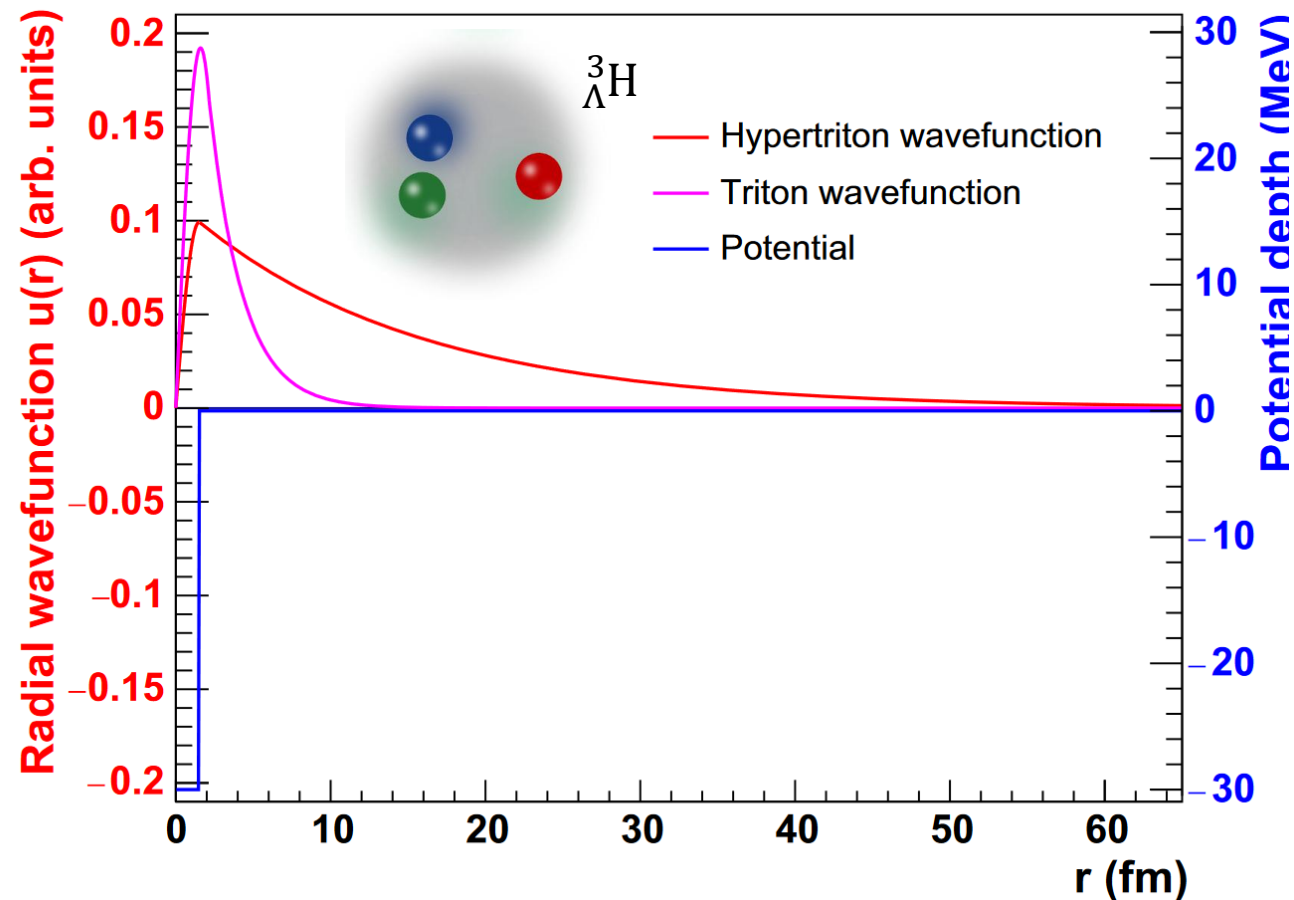
- FAIR/CBM (2.4-4.9 GeV)
- HIAF/CEE (2.1-4.5 GeV)
- NICA/MPD (4-11 GeV)



A novel tool to study the evolution of strongly-interacting matter at high-baryon density region

2. The halo-like nucleus: (anti-)hypertriton

(5)



J. Chen et al., Phys. Rep. 760, 1 (2018); P. Braun-Munzinger and B. Donigus NPA987, 144 (2019)

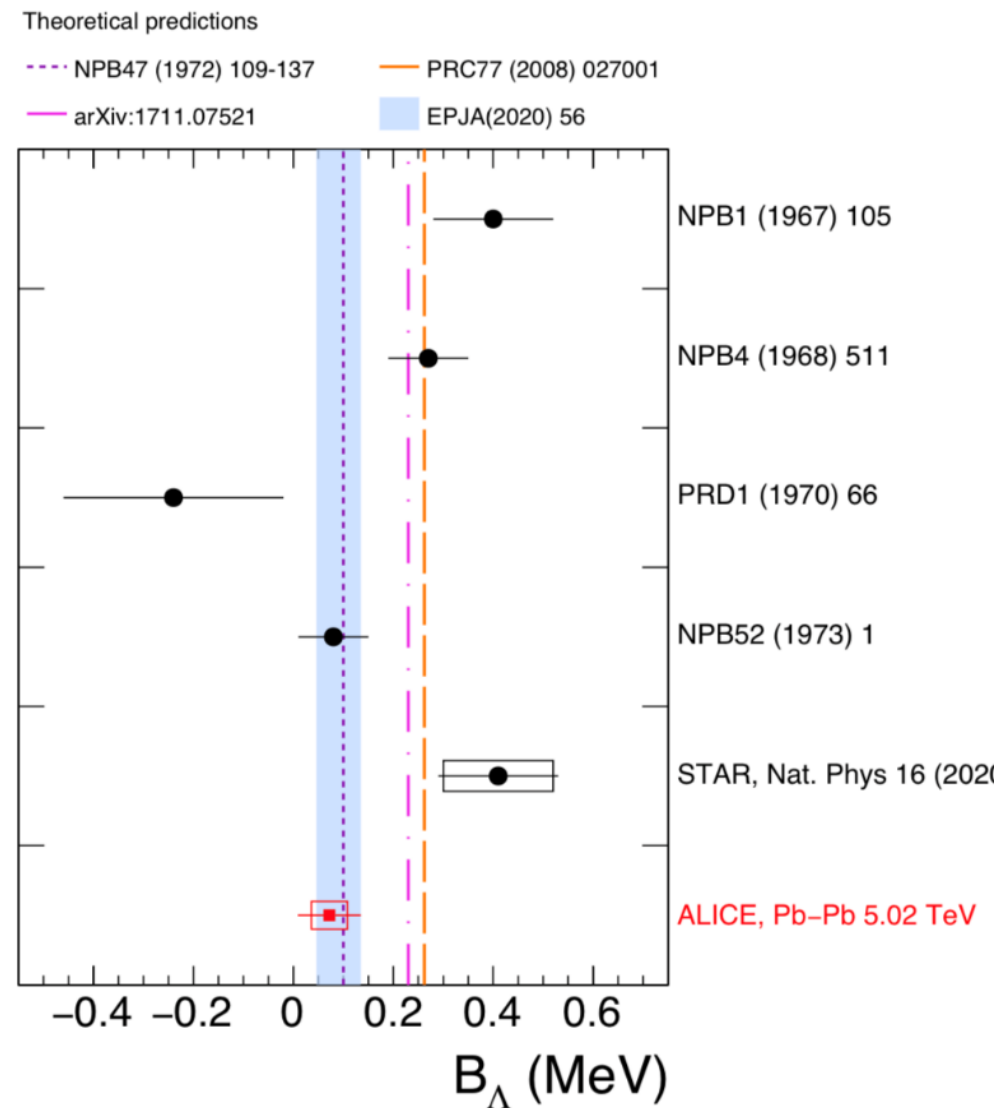
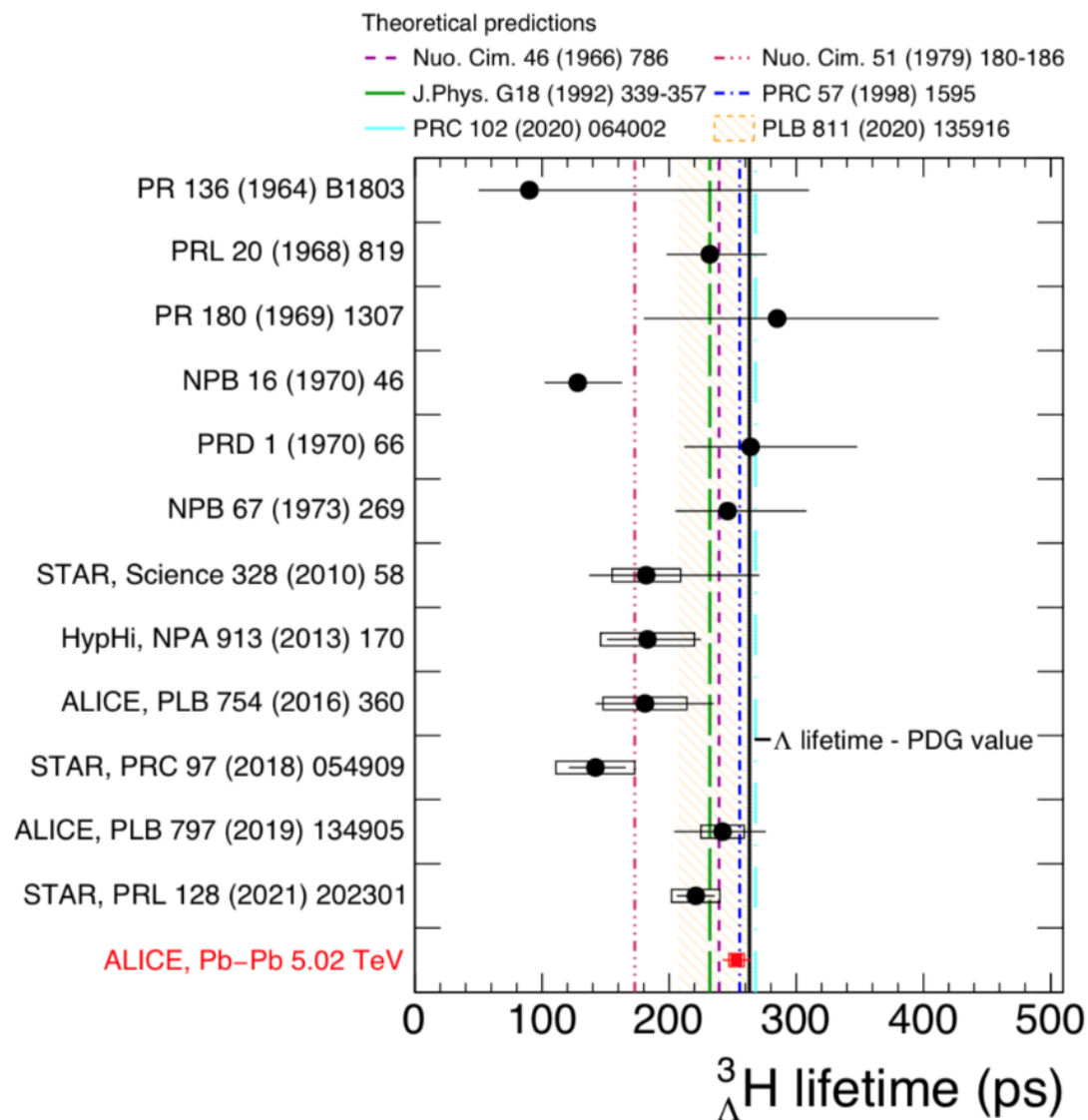
D. N. Liu et al. Phys. Lett. B 855, 138855 (2024)

2. Binding energy and lifetime

(6)

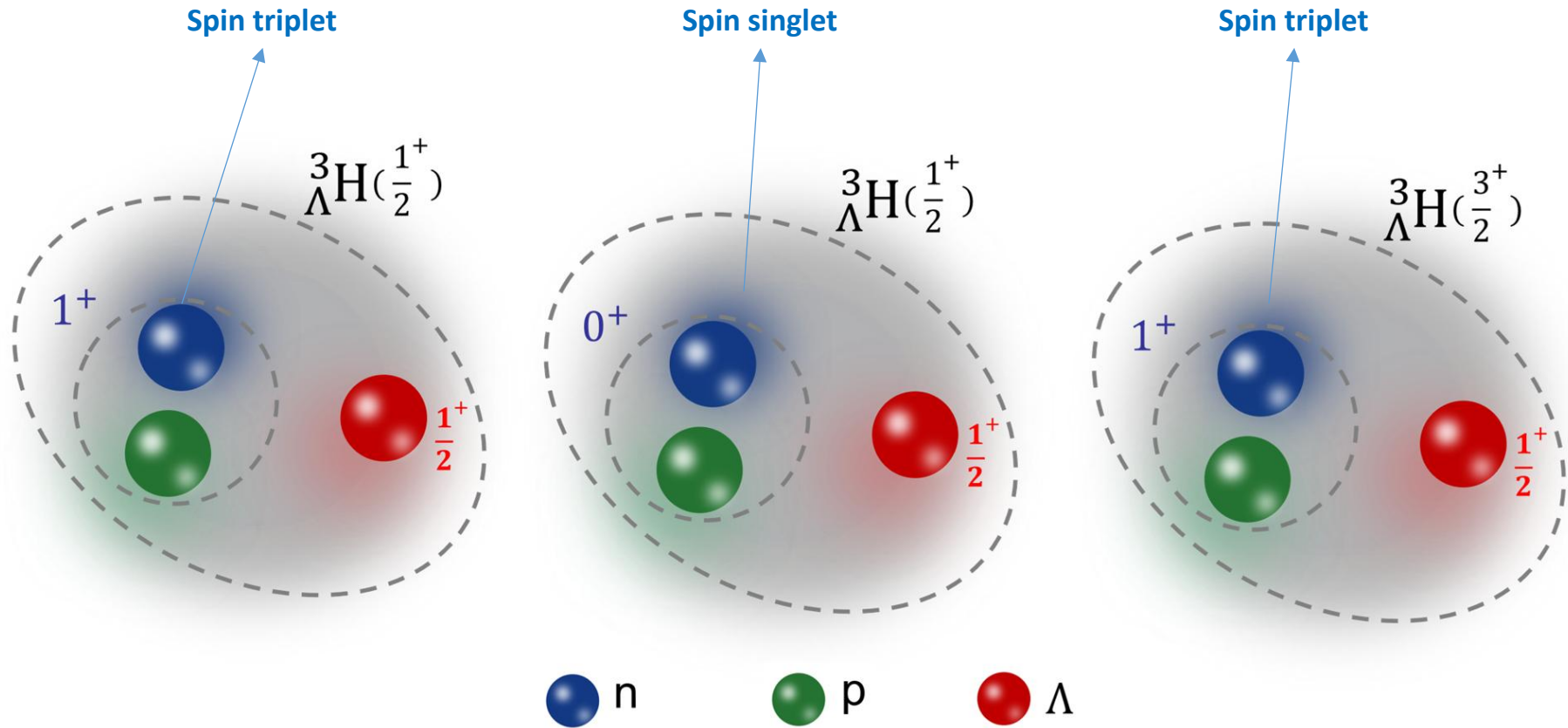
ALICE, PRL 131, 102302 (2023)

Y. G. Ma, Nucl. Sci. Tech. 3497 (2023)



2. Spin of (anti-)hypertriton ?

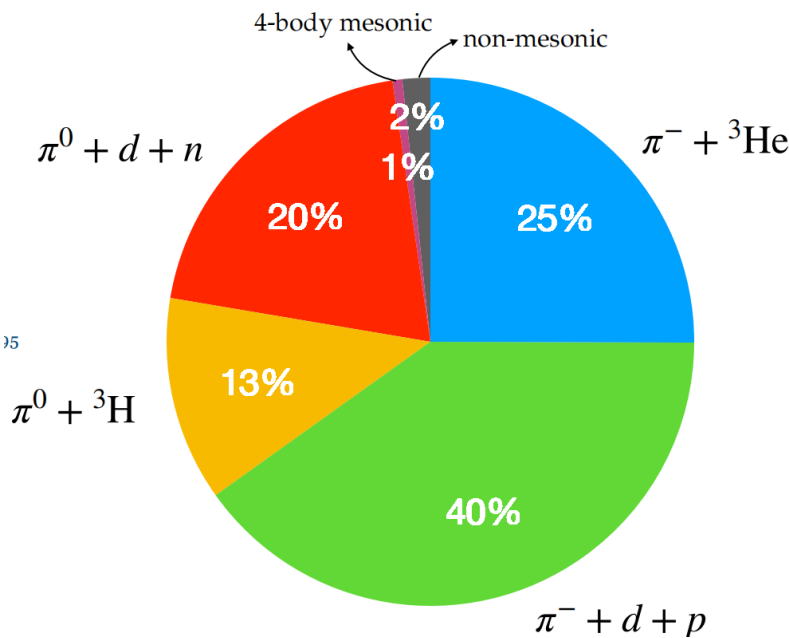
(7)



2. Spin of (anti-)hypertriton ?

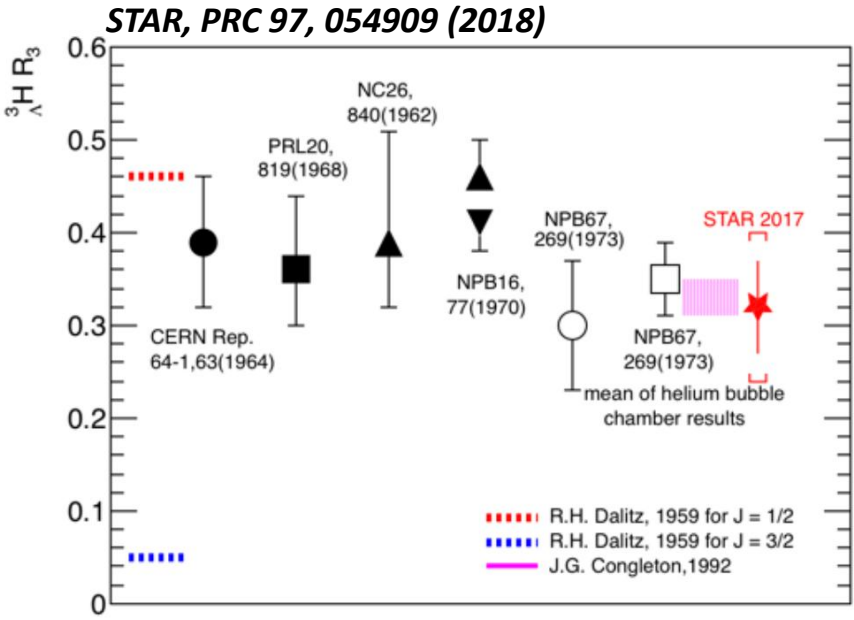
(8)

$$\begin{aligned} {}^3_{\Lambda}H &\mapsto \pi^- + {}^3\text{He}, & {}^3_{\Lambda}H &\mapsto \pi^0 + {}^3\text{H}, \\ {}^3_{\Lambda}H &\mapsto \pi^- + d + p, & {}^3_{\Lambda}H &\mapsto \pi^0 + d + n, \\ {}^3_{\Lambda}H &\mapsto \pi^- + p + n + p, & {}^3_{\Lambda}H &\mapsto \pi^0 + p + n + n. \end{aligned}$$



Relative branching ratio:

$$R_3 = \frac{\text{B.R.}({}^3_{\Lambda}H \rightarrow {}^3\text{He}\pi^-)}{\text{B.R.}({}^3_{\Lambda}H \rightarrow {}^3\text{He}\pi^-) + \text{B.R.}({}^3_{\Lambda}H \rightarrow dp\pi^-)}$$



Favors spin 1/2

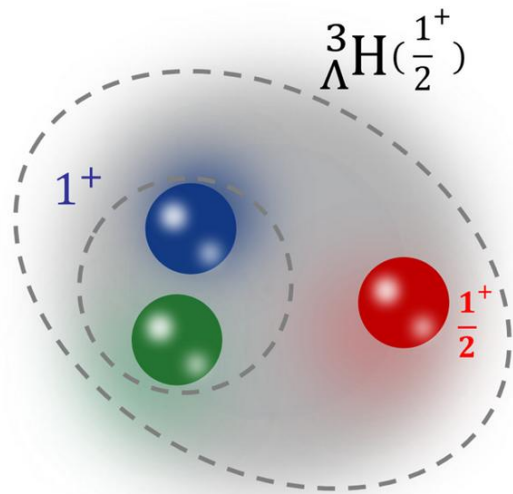
PHYSICAL REVIEW D **87**, 034506 (2013)
Light nuclei and hypernuclei from quantum chromodynamics in the limit of SU(3) flavor symmetry
S. R. Beane,¹ E. Chang,² S. D. Cohen,³ W. Detmold,^{4,5} H. W. Lin,³ T. C. Luu,⁶ K. Orginos,^{4,5}
A. Parreño,² M. J. Savage,³ and A. Walker-Loud^{7,8}

Label	A	s	I	J ^π	Local SU(3) irreps	This work
N	1	0	1/2	1/2 ⁺	8	8
Λ	1	-1	0	1/2 ⁺	8	8
Σ	1	-1	1	1/2 ⁺	8	8
Ξ	1	-2	1/2	1/2 ⁺	8	8
d	2	0	0	1 ⁺	10	10
nn	2	0	1	0 ⁺	27	27
nΛ	2	-1	1/2	0 ⁺	27	27
nΛ	2	-1	1/2	1 ⁺	8 _A , 10	-
nΣ	2	-1	3/2	0 ⁺	27	27
nΣ	2	-1	3/2	1 ⁺	10	10
nΞ	2	-2	0	1 ⁺	8 _A	8 _A
nΞ	2	-2	1	1 ⁺	8 _A , 10, 10	-
H	2	-2	0	0 ⁺	1, 27	1, 27
³ H, ³ H	3	0	1/2	1/2 ⁺	35	35
³ H(1/2 ⁺)	3	-1	0	1/2 ⁺	35	-
³ ΛH(3/2 ⁺)	3	-1	0	3/2 ⁺	10	10
³ He, ³ ΛH, nnΛ	3	-1	1	1/2 ⁺	27, 35	27, 35
³ ΣHe	3	-1	1	3/2 ⁺	27	27
⁴ He	4	0	0	0 ⁺	28	28
⁴ ΛHe, ⁴ ΛH	4	-1	1/2	0 ⁺	28	-
⁴ ΛΛHe	4	-2	1	0 ⁺	27, 28	27, 28
ΛΞ ⁰ pnn	5	-3	0	3/2 ⁺	10 + ...	10

Favors spin 3/2

3. (Anti-)hypertriton polarization and its spin structure

(9)



$$\begin{aligned}
 |\frac{1}{2}, \uparrow\rangle_{\Lambda H} &= \frac{\sqrt{6}}{3} |\frac{1}{2}, \frac{1}{2}\rangle_n |\frac{1}{2}, \frac{1}{2}\rangle_p |\frac{1}{2}, -\frac{1}{2}\rangle_{\Lambda} \\
 &\quad - \frac{\sqrt{6}}{6} (|\frac{1}{2}, \frac{1}{2}\rangle_n |\frac{1}{2}, -\frac{1}{2}\rangle_p |\frac{1}{2}, \frac{1}{2}\rangle_{\Lambda} \\
 &\quad + |\frac{1}{2}, -\frac{1}{2}\rangle_n |\frac{1}{2}, \frac{1}{2}\rangle_p |\frac{1}{2}, \frac{1}{2}\rangle_{\Lambda}), \\
 |\frac{1}{2}, \downarrow\rangle_{\Lambda H} &= -\frac{\sqrt{6}}{3} |\frac{1}{2}, -\frac{1}{2}\rangle_n |\frac{1}{2}, -\frac{1}{2}\rangle_p |\frac{1}{2}, \frac{1}{2}\rangle_{\Lambda} \\
 &\quad + \frac{\sqrt{6}}{6} (|\frac{1}{2}, \frac{1}{2}\rangle_n |\frac{1}{2}, -\frac{1}{2}\rangle_p |\frac{1}{2}, -\frac{1}{2}\rangle_{\Lambda} \\
 &\quad + |\frac{1}{2}, -\frac{1}{2}\rangle_n |\frac{1}{2}, \frac{1}{2}\rangle_p |\frac{1}{2}, -\frac{1}{2}\rangle_{\Lambda}).
 \end{aligned}$$

Coalescence model for hypertriton production (without baryon spin correlation)

$$E_i \frac{d^3 N_{i, \pm \frac{1}{2}}}{d\mathbf{p}_i^3} = \int_{\Sigma^\mu} d^3 \sigma_\mu p_i^\mu w_{i, \pm \frac{1}{2}}(\mathbf{x}_i, \mathbf{p}_i) \bar{f}_i(\mathbf{x}_i, \mathbf{p}_i)$$

$$w_{i, \pm \frac{1}{2}} = \frac{1}{2} [1 \pm \mathcal{P}_i(\mathbf{x}_i, \mathbf{p}_i)]$$

$$\hat{\rho}_i = \text{diag} \left(\frac{1+\mathcal{P}_i}{2}, \frac{1-\mathcal{P}_i}{2} \right)$$

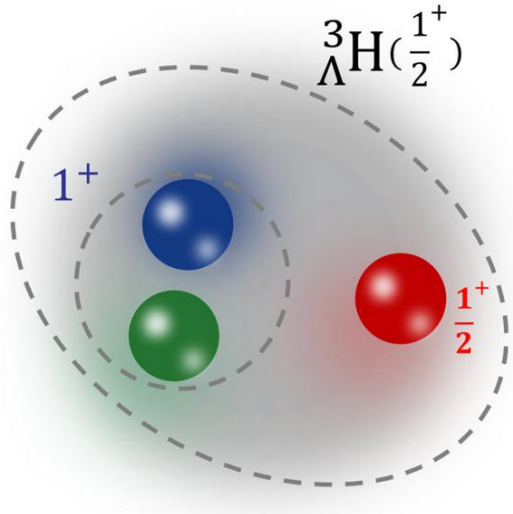
$$\bar{f}_i = \frac{g_i}{(2\pi)^3} [\exp(p_i^\mu u_\mu / T) / \xi_i + 1]^{-1}$$

$$\hat{\rho}_{np\Lambda} = \hat{\rho}_n \otimes \hat{\rho}_p \otimes \hat{\rho}_\Lambda$$

$$\begin{aligned}
 E \frac{d^3 N_{\Lambda H, \pm \frac{1}{2}}}{d\mathbf{P}^3} &= E \int \prod_{i=n,p,\Lambda} p_i^\mu d^3 \sigma_\mu \frac{d^3 p_i}{E_i} \bar{f}_i(\mathbf{x}_i, \mathbf{p}_i) \\
 &\quad \times \left(\frac{2}{3} w_{n, \pm \frac{1}{2}} w_{p, \pm \frac{1}{2}} w_{\Lambda, \mp \frac{1}{2}} + \frac{1}{6} w_{n, \pm \frac{1}{2}} w_{p, \mp \frac{1}{2}} w_{\Lambda, \pm \frac{1}{2}} \right. \\
 &\quad \left. + \frac{1}{6} w_{n, \mp \frac{1}{2}} w_{p, \pm \frac{1}{2}} w_{\Lambda, \pm \frac{1}{2}} \right) \\
 &\quad \times W_{\Lambda H}(\mathbf{x}_n, \mathbf{x}_p, \mathbf{x}_\Lambda; \mathbf{p}_n, \mathbf{p}_p, \mathbf{p}_\Lambda) \delta(\mathbf{P} - \sum_i \mathbf{p}_i)
 \end{aligned}$$

3. (Anti-)hypertriton polarization and its spin structure

(10)



$$\begin{aligned}\mathcal{P}_{\Lambda^3\text{H}} &\approx \frac{\frac{2}{3}\mathcal{P}_n + \frac{2}{3}\mathcal{P}_p - \frac{1}{3}\mathcal{P}_\Lambda - \mathcal{P}_n\mathcal{P}_p\mathcal{P}_\Lambda}{1 - \frac{2}{3}(\mathcal{P}_n + \mathcal{P}_p)\mathcal{P}_\Lambda + \frac{1}{3}\mathcal{P}_n\mathcal{P}_p} \\ &\approx \frac{2}{3}\mathcal{P}_n + \frac{2}{3}\mathcal{P}_p - \frac{1}{3}\mathcal{P}_\Lambda \\ &\approx \mathcal{P}_\Lambda\end{aligned}$$

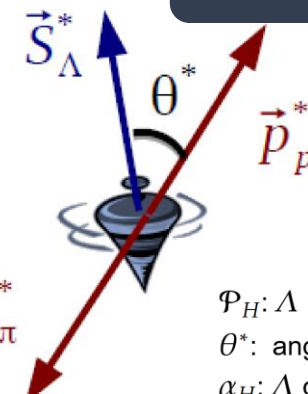
3. (Anti-)hypertriton polarization and its spin structure

(11)

K. J. Sun et al., arXiv:2405.12015(2024)

Parity-violating weak decay

Λ hyperons



$$\frac{dN}{d\cos\theta^*} = \text{Tr}[T^+ \hat{\rho} T]$$

$$\rho_\Lambda = \begin{pmatrix} \frac{1 + \mathcal{P}_\Lambda}{2} & \\ & \frac{1 - \mathcal{P}_\Lambda}{2} \end{pmatrix}$$

$\mathcal{P}_H$: Λ polarization
 θ^* : angle between proton momentum and Λ spin
 α_H : Λ decay parameter
 $\alpha_\Lambda = 2\text{Re}(T_s^* T_p) = 0.732 \pm 0.01$
 BESIII, Phys. Rev. Lett. 129, 131801 (2022)

$$\Lambda \rightarrow p + \pi^-$$

The transition matrix

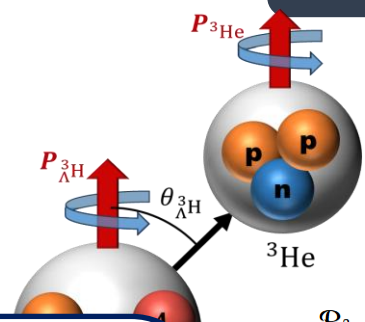
$$T(\Lambda \rightarrow \pi^- + p) = \frac{1}{\sqrt{4\pi}} \begin{pmatrix} T_s + T_p \cos\theta_p^* & T_p \sin\theta_p^* e^{-i\phi_p^*} \\ T_p \sin\theta_p^* e^{i\phi_p^*} & T_s - T_p \cos\theta_p^* \end{pmatrix}$$

The angular distribution

$$\frac{dN}{d\cos\theta^*} = \frac{1}{2} (1 + \alpha_H |\mathcal{P}_H| \cos\theta^*)$$

H denotes Λ and $\bar{\Lambda}$

Hypertriton



$$\rho_{^3\text{H}} = \begin{pmatrix} \frac{1 + \mathcal{P}_{^3\text{H}}}{2} & \\ & \frac{1 - \mathcal{P}_{^3\text{H}}}{2} \end{pmatrix}$$

$\mathcal{P}_{^3\text{H}}$: ^3H polarization
 θ^* : Angle between ^3He momentum and ^3H rest frame
 $\alpha_{^3\text{H}}$: ^3H decay parameter

$$\alpha_{^3\text{H}} \approx -\frac{1}{3T_s^2 + \frac{1}{3}T_p^2} \alpha_\Lambda$$

$$\approx -\frac{1}{2.58} \alpha_\Lambda$$

Sign flip !

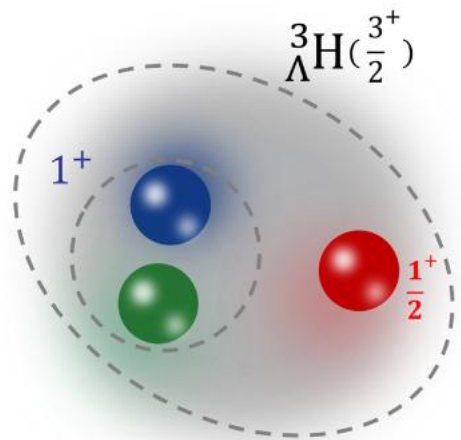
$\pi^- + ^3\text{He}$

$$\begin{pmatrix} 3T_s - T_p \cos\theta^* & -T_p \sin\theta^* e^{i\phi^*} \\ -T_p \sin\theta^* e^{-i\phi^*} & 3T_s + T_p \cos\theta^* \end{pmatrix}$$

$$\frac{dN}{d\cos\theta^*} = \frac{1}{2} \left(1 + \alpha_{^3\text{H}} \mathcal{P}_{^3\text{H}} \cos\theta^* \right)$$

3. (Anti-)hypertriton polarization and its spin structure

(12)

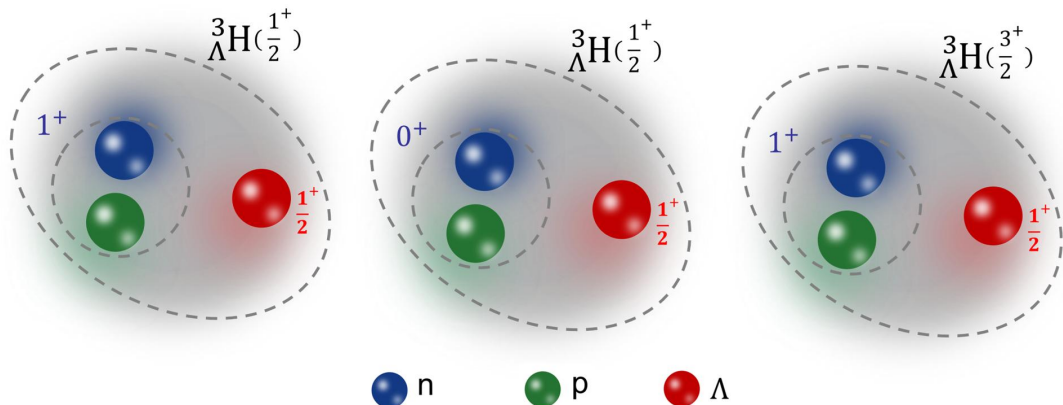


$$\hat{\rho}_{\Lambda}^3 \approx \text{diag} \left[\frac{(1 + \mathcal{P}_{\Lambda})^3}{4(1 + \mathcal{P}_{\Lambda}^2)}, \frac{(1 - \mathcal{P}_{\Lambda})(1 + \mathcal{P}_{\Lambda})^2}{4(1 + \mathcal{P}_{\Lambda}^2)}, \right. \\ \left. \frac{(1 - \mathcal{P}_{\Lambda})^2(1 + \mathcal{P}_{\Lambda})}{4(1 + \mathcal{P}_{\Lambda}^2)}, \frac{(1 - \mathcal{P}_{\Lambda})^3}{4(1 + \mathcal{P}_{\Lambda}^2)} \right]$$

$$T({}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}) = \frac{FT_p}{\sqrt{6\pi}} \begin{pmatrix} e^{i\phi^*} \sin \theta^* & 0 \\ -\frac{2}{\sqrt{3}} \cos \theta^* & \frac{e^{i\phi^*} \sin \theta^*}{\sqrt{3}} \\ -\frac{e^{-i\phi^*} \sin \theta^*}{\sqrt{3}} & -\frac{2}{\sqrt{3}} \cos \theta^* \\ 0 & -e^{-i\phi^*} \sin \theta^* \end{pmatrix}$$

$$\frac{dN}{d\cos\theta^*} = \frac{1}{2} \left[1 + \left(\hat{\rho}_{\frac{1}{2}, \frac{1}{2}} + \hat{\rho}_{-\frac{1}{2}, -\frac{1}{2}} - \frac{1}{2} \right) (3\cos^2\theta^* - 1) \right]$$

$$\hat{\rho}_{\frac{1}{2}, \frac{1}{2}} + \hat{\rho}_{-\frac{1}{2}, -\frac{1}{2}} - \frac{1}{2} \approx -\frac{\mathcal{P}_{\Lambda}^2}{1 + \mathcal{P}_{\Lambda}^2} \approx -\mathcal{P}_{\Lambda}^2$$



J^P	structure	decay mode	$\frac{dN}{d\cos\theta^*}$
$\frac{1}{2}^+$	$\Lambda(\frac{1}{2}^+) - np(1^+)$	${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	$\frac{1}{2}(1 - \frac{1}{2.58}\alpha_{\Lambda}\mathcal{P}_{\Lambda}\cos\theta^*)$
$\frac{1}{2}^+$	$\Lambda(\frac{1}{2}^+) - np(0^+)$	${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	$\frac{1}{2}(1 + \alpha_{\Lambda}\mathcal{P}_{\Lambda}\cos\theta^*)$
$\frac{3}{2}^+$	$\Lambda(\frac{1}{2}^+) - np(1^+)$	${}^3_{\Lambda}\text{H} \rightarrow \pi^- + {}^3\text{He}$	$\frac{1}{2}(1 - \mathcal{P}_{\Lambda}^2(3\cos^2\theta^* - 1))$
$\frac{1}{2}^-$	$\bar{\Lambda}(\frac{1}{2}^-) - \bar{n}\bar{p}(1^-)$	${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^+ + {}^3\bar{\text{He}}$	$\frac{1}{2}(1 - \frac{1}{2.58}\alpha_{\bar{\Lambda}}\mathcal{P}_{\bar{\Lambda}}\cos\theta^*)$
$\frac{1}{2}^-$	$\bar{\Lambda}(\frac{1}{2}^-) - \bar{n}\bar{p}(0^-)$	${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^+ + {}^3\bar{\text{He}}$	$\frac{1}{2}(1 + \alpha_{\bar{\Lambda}}\mathcal{P}_{\bar{\Lambda}}\cos\theta^*)$
$\frac{3}{2}^-$	$\bar{\Lambda}(\frac{1}{2}^-) - \bar{n}\bar{p}(1^-)$	${}^3_{\Lambda}\bar{\text{H}} \rightarrow \pi^+ + {}^3\bar{\text{He}}$	$\frac{1}{2}(1 - \mathcal{P}_{\bar{\Lambda}}^2(3\cos^2\theta^* - 1))$

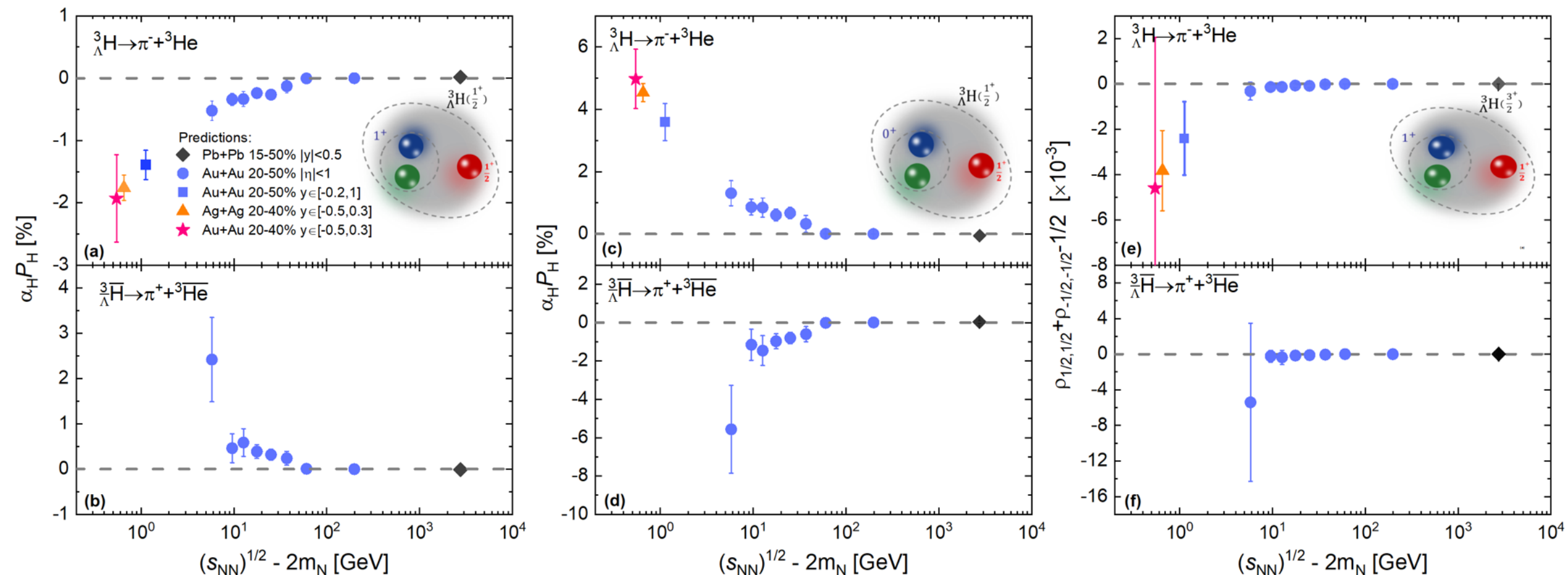
3. (Anti-)hypertriton polarization and its spin structure

(13)

The measurement of hypertriton polarization provides a novel method to uniquely determine its internal spin structure

$$\alpha_{\Lambda^3\text{H}} \approx -\frac{1}{2.58}\alpha_{\Lambda}$$

$$\alpha_{\Lambda^3\text{H}} \approx \alpha_{\Lambda}$$



4. Effects of baryon spin correlation

(14)

Z. T. Liang, Chirality 2023

$$\left| \rho_{00}^V - \frac{1}{3} \right| \gg P_A^2 \sim P_q^2 \quad \left. \begin{array}{l} \text{The STAR data show that: } \langle P_q P_{\bar{q}} \rangle \neq \langle P_q \rangle \langle P_{\bar{q}} \rangle \quad \langle P_q P_{\bar{q}} \rangle \gg \langle P_q \rangle \langle P_{\bar{q}} \rangle \\ \rho_{00}^V - \frac{1}{3} \sim \langle P_q P_{\bar{q}} \rangle \end{array} \right\}$$

By studying P_H , we study the **average** of quark polarization P_q ;
by studying ρ_{00}^V , we study the **correlation** between P_q and $P_{\bar{q}}$.

How to separate long range or local correlations

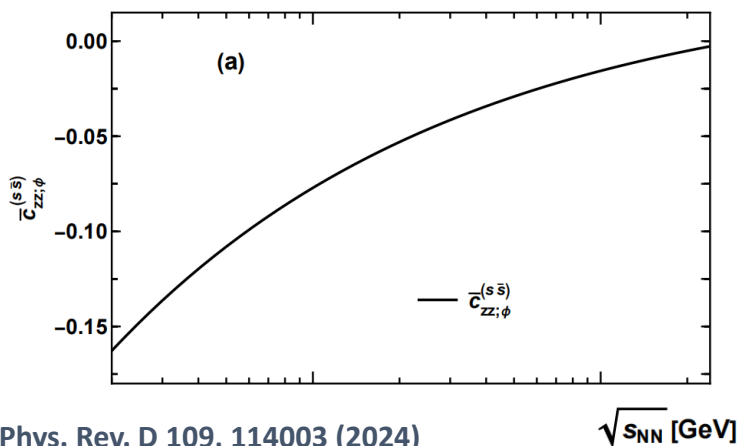
$$C_{NN}^{H_i \bar{H}_j} \equiv \frac{N_{H_i \bar{H}_j}^{\uparrow\uparrow} + N_{H_i \bar{H}_j}^{\downarrow\downarrow} - N_{H_i \bar{H}_j}^{\uparrow\downarrow} - N_{H_i \bar{H}_j}^{\downarrow\uparrow}}{N_{H_i \bar{H}_j}^{\uparrow\uparrow} + N_{H_i \bar{H}_j}^{\downarrow\downarrow} + N_{H_i \bar{H}_j}^{\uparrow\downarrow} + N_{H_i \bar{H}_j}^{\downarrow\uparrow}}$$

sensitive to the long range correlation

They should be sensitive to the local correlations.

Global quark spin correlations in relativistic heavy ion collisions

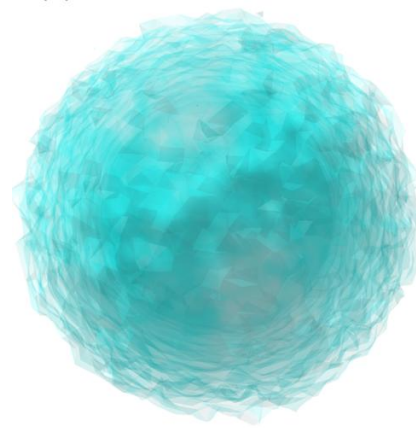
Ji-peng Lv,^{1,*} Zi-han Yu,^{1,†} Zuo-tang Liang,^{1,‡} Qun Wang,^{2,3,§} and Xin-Nian Wang^{4,¶}



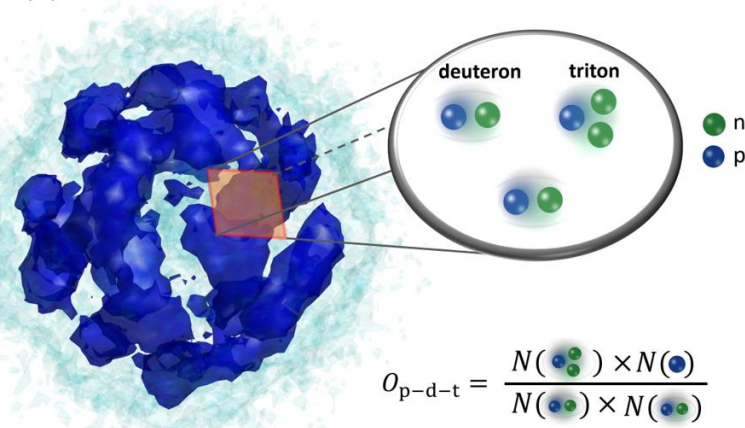
J. P. Lv et al., Phys. Rev. D 109, 114003 (2024)

C. M. Ko, NST 34, 80 (2023).

(a) Crossover



(b) First-order



$$O_{p-d-t} = \frac{N(\text{deuteron}) \times N(\text{triton})}{N(\text{proton}) \times N(\text{neutron})}$$

$$N_d \approx N_d^{(0)} (1 + C_{np}) + \frac{3}{2^{1/2}} \left(\frac{2\pi}{mT} \right)^{3/2} \times \int d^3 \mathbf{x}_1 d^3 \mathbf{x}_2 C_2(\mathbf{x}_1, \mathbf{x}_2) \frac{e^{-\frac{(\mathbf{x}_1 - \mathbf{x}_2)^2}{2\sigma_d^2}}}{(2\pi\sigma_d^2)^{3/2}}$$

$$N_t \approx \frac{3^{3/2}}{4} \left(\frac{2\pi}{mT} \right)^3 \int d^3 \mathbf{x}_1 d^3 \mathbf{x}_2 d^3 \mathbf{x}_3 \rho_{nnp}(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3) \times \frac{1}{3^{3/2}(\pi\sigma_t^2)^3} e^{-\frac{(\mathbf{x}_1 - \mathbf{x}_2)^2}{2\sigma_t^2} - \frac{(\mathbf{x}_1 + \mathbf{x}_2 - 2\mathbf{x}_3)^2}{6\sigma_t^2}},$$

$$\rho_{nnp}(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3) \approx \rho_n(\mathbf{x}_1) \rho_n(\mathbf{x}_2) \rho_p(\mathbf{x}_3) + C_2(\mathbf{x}_1, \mathbf{x}_2) \rho_p(\mathbf{x}_3) + C_2(\mathbf{x}_2, \mathbf{x}_3) \rho_n(\mathbf{x}_1) + C_2(\mathbf{x}_3, \mathbf{x}_1) \rho_n(\mathbf{x}_2) + C_3(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3)$$

$$\rho_{np}(\mathbf{x}_1, \mathbf{x}_2) = \rho_n(\mathbf{x}_1) \rho_p(\mathbf{x}_2) + C_2(\mathbf{x}_1, \mathbf{x}_2)$$

$$\frac{N_t N_p}{N_d^2} \approx \frac{1}{2\sqrt{3}} \left[1 + \Delta\rho_n + \frac{\lambda}{\sigma} G\left(\frac{\xi}{\sigma}\right) \right]$$

K. J. Sun, L. W. Chen, C. M. Ko, and Z. Xu, Phys. Lett. B 774, 103 (2017);

K. J. Sun, C. M. Ko, and F. Li, PLB 816, 136258 (2021);

4. Effects of baryon spin correlation

(15)

$$\begin{aligned}
 \hat{\rho}_{np\Lambda} &= \hat{\rho}_n \otimes \hat{\rho}_p \otimes \hat{\rho}_\Lambda + \frac{1}{2^2} (c_{np}^{\alpha\beta} \hat{\sigma}_{n,\alpha} \otimes \hat{\sigma}_{p,\beta} \otimes \hat{\rho}_\Lambda \\
 &\quad + c_{p\Lambda}^{\alpha\beta} \hat{\sigma}_{p,\alpha} \otimes \hat{\sigma}_{\Lambda,\beta} \otimes \hat{\rho}_n + c_{n\Lambda}^{\alpha\beta} \hat{\sigma}_{n,\alpha} \otimes \hat{\sigma}_{\Lambda,\beta} \otimes \hat{\rho}_p) \\
 &\quad + \frac{1}{2^3} c_{np\Lambda}^{\alpha\beta\gamma} \hat{\sigma}_{n,\alpha} \otimes \hat{\sigma}_{p,\beta} \otimes \hat{\sigma}_{\Lambda,\gamma}, \\
 \mathcal{P}_{\Lambda H}^3 &\approx \frac{\frac{2}{3}\langle \mathcal{P}_n \rangle + \frac{2}{3}\langle \mathcal{P}_p \rangle - \frac{1}{3}\langle \mathcal{P}_\Lambda \rangle - \langle \mathcal{P}_n \mathcal{P}_p \mathcal{P}_\Lambda \rangle + C_-}{1 - \frac{2}{3}(\langle (\mathcal{P}_n + \mathcal{P}_p) \mathcal{P}_\Lambda \rangle) + \frac{1}{3}\langle \mathcal{P}_n \mathcal{P}_p \rangle + C_+} \\
 C_- &= -\frac{1}{4}(\langle c_{np}^{zz} \mathcal{P}_\Lambda \rangle + \langle c_{p\Lambda}^{zz} \mathcal{P}_n \rangle + \langle c_{n\Lambda}^{zz} \mathcal{P}_p \rangle) - \frac{1}{4}\langle c_{np\Lambda}^{zzz} \rangle, \\
 C_+ &= \frac{1}{12}(\langle c_{np}^{zz} \rangle - 2\langle c_{p\Lambda}^{zz} \rangle - 2\langle c_{n\Lambda}^{zz} \rangle).
 \end{aligned}$$

‘genuine’ correlation terms

Induced correlations

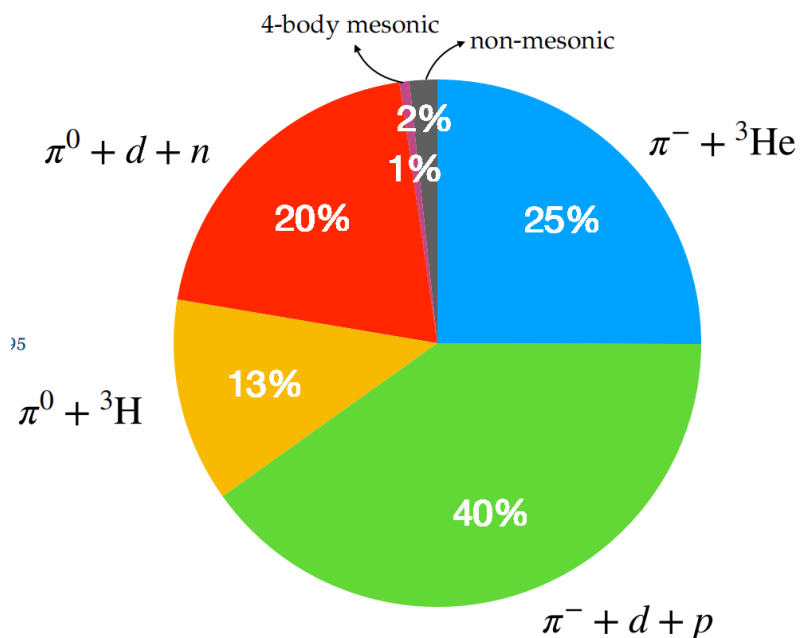
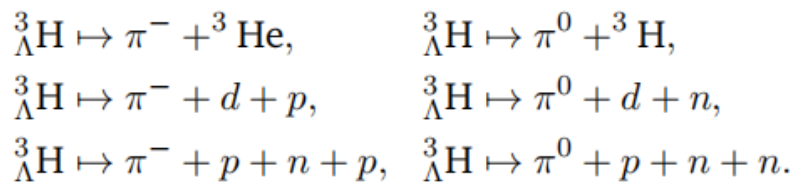
We can express the polarization of a particle as $\mathcal{P} = \langle \mathcal{P} \rangle + \delta\mathcal{P}$ with $\delta\mathcal{P}$ denoting its space and momentum dependent fluctuations, which leads to the relations $\langle \mathcal{P}_n \mathcal{P}_p \rangle = \langle \mathcal{P}_n \rangle \langle \mathcal{P}_p \rangle + \langle \delta\mathcal{P}_n \delta\mathcal{P}_p \rangle$ and $\langle \mathcal{P}_n \mathcal{P}_p \mathcal{P}_\Lambda \rangle = \langle \mathcal{P}_n \rangle \langle \mathcal{P}_p \rangle \langle \mathcal{P}_\Lambda \rangle + \langle \delta\mathcal{P}_n \delta\mathcal{P}_p \rangle \langle \mathcal{P}_\Lambda \rangle + \langle \delta\mathcal{P}_n \delta\mathcal{P}_\Lambda \rangle \langle \mathcal{P}_p \rangle + \langle \delta\mathcal{P}_p \delta\mathcal{P}_\Lambda \rangle \langle \mathcal{P}_n \rangle + \langle \delta\mathcal{P}_n \delta\mathcal{P}_p \delta\mathcal{P}_\Lambda \rangle$. Assuming again $\langle \mathcal{P}_n \rangle \approx \langle \mathcal{P}_p \rangle \approx \langle \mathcal{P}_\Lambda \rangle$ and neglecting the three-body correlation, we then have

$$\mathcal{P}_{\Lambda H}^3 \approx (1 - \langle \delta\mathcal{P}_n \delta\mathcal{P}_p \rangle - \langle \delta\mathcal{P}_p \delta\mathcal{P}_\Lambda \rangle - \langle \delta\mathcal{P}_n \delta\mathcal{P}_\Lambda \rangle) \langle \mathcal{P}_\Lambda \rangle.$$

This result suggests that it is possible to extract the information on the spin-spin correlations among nucleons and Λ hyperons from the measurement of hypertriton polarization in heavy-ion collisions, although it is non-trivial in practice.

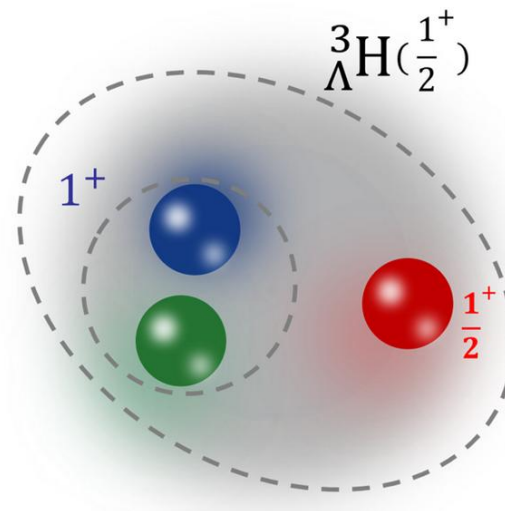
4. Three-body decay

(16)

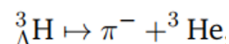


Relative branching ratio:

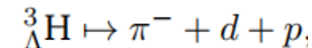
$$R_3 = \frac{\text{B.R.}({}^3_{\Lambda}\text{H} \rightarrow {}^3\text{He}\pi^-)}{\text{B.R.}({}^3_{\Lambda}\text{H} \rightarrow {}^3\text{He}\pi^-) + \text{B.R.}({}^3_{\Lambda}\text{H} \rightarrow \text{dp}\pi^-)}$$



$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} \left(1 + \alpha_{{}^3_{\Lambda}\text{H}} \mathcal{P}_{{}^3_{\Lambda}\text{H}} \cos \theta^* \right)$$



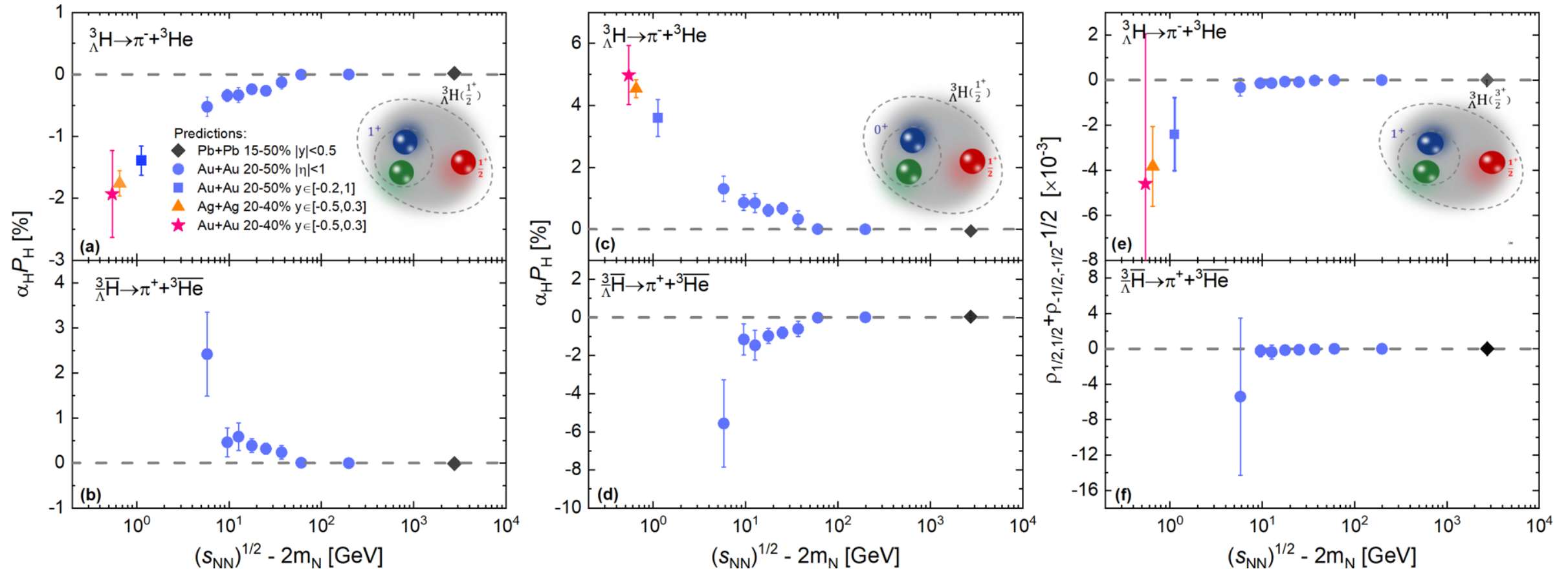
$$\begin{aligned} \alpha_{{}^3_{\Lambda}\text{H}} &\approx -\frac{1}{3T_s^2 + \frac{1}{3}T_p^2} \alpha_{\Lambda} \\ &\approx -\frac{1}{2.58} \alpha_{\Lambda} \end{aligned}$$



$$\alpha_{{}^3_{\Lambda}\text{H}} \approx -\frac{1}{3.2} \alpha_{\Lambda}$$

with $R_3 = 0.25$

1. (Anti-)hypertriton is globally polarized in non-central heavy-ion collisions.
2. (Anti-)hypertriton polarization and its decay pattern provide a novel method to uniquely determine the spin structure of its wavefunction.

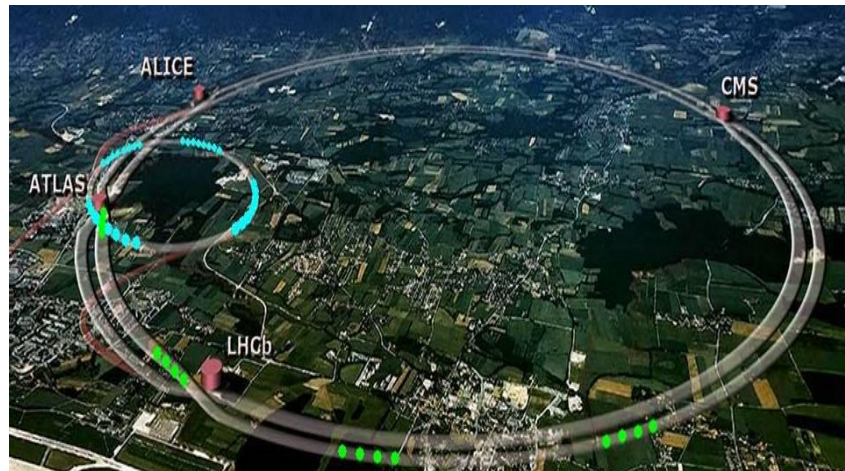
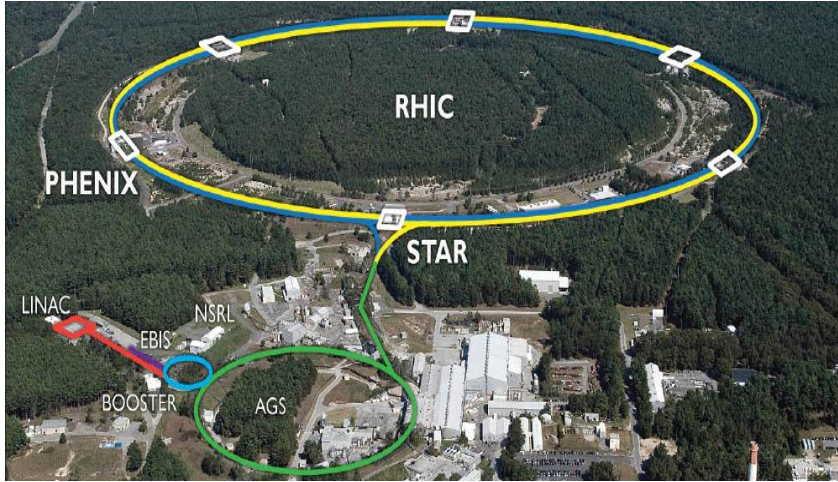


Backup

Little Bang Nucleosynthesis

(2)

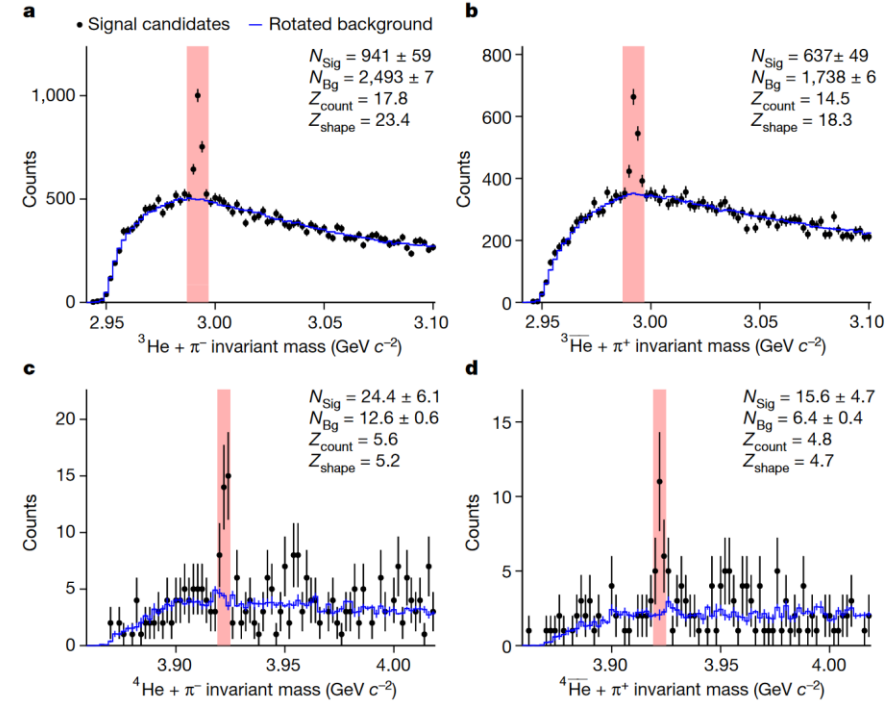
Antimatter factory



Observation of the antimatter hypernucleus ${}^4_{\Lambda}\bar{\text{H}}$

[STAR Collaboration](#)

[Nature \(2024\)](#) | [Cite this ar](#)



PHYSICAL REVIEW C **93**, 064909 (2016)

Antimatter ${}^4_{\Lambda}\bar{\text{H}}$ hypernucleus production and the ${}^3_{\Lambda}\bar{\text{H}}/{}^3\text{He}$ puzzle in relativistic heavy-ion collisions

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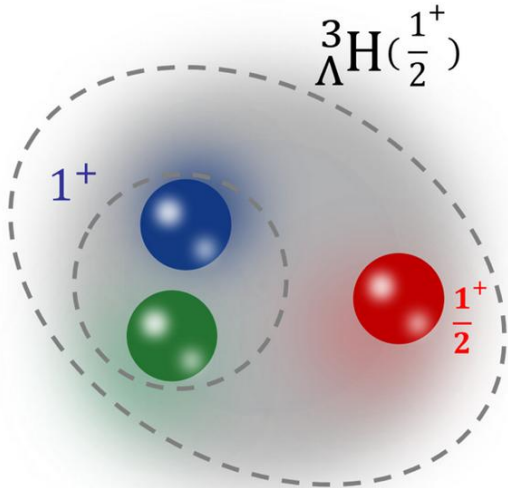
We show that the measured yield ratio ${}^3_{\Lambda}\bar{\text{H}}/{}^3\text{He}$ (${}^3_{\Lambda}\bar{\text{H}}/{}^3\text{He}$) in Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV and in Pb + Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV can be understood within a covariant coalescence model if (anti-)Λ particles freeze out earlier than (anti-)nucleons but their relative freeze-out time is closer at $\sqrt{s_{NN}} = 2.76$ TeV than at $\sqrt{s_{NN}} = 200$ GeV. The earlier (anti-)Λ freeze-out can significantly enhance the yield of (anti)hypernucleus ${}^4_{\Lambda}\bar{\text{H}}$ (${}^4_{\Lambda}\bar{\text{H}}$), leading to that ${}^4_{\Lambda}\bar{\text{H}}$ has a comparable abundance with ${}^4\bar{\text{He}}$ and thus provides an easily measured antimatter candidate heavier than ${}^4\bar{\text{He}}$. The future measurement on ${}^4_{\Lambda}\bar{\text{H}}$ (${}^4_{\Lambda}\bar{\text{H}}$) would be very useful to understand the (anti-)Λ freeze-out dynamics and the production mechanism of (anti)hypernuclei in relativistic heavy-ion collisions.

(Anti-)hypertriton polarization and its spin structure

Parity-violating weak decay:

$$T(\Lambda \rightarrow \pi^- + p) = \frac{1}{\sqrt{4\pi}} \begin{pmatrix} T_s + T_p \cos \theta_p^* & T_p \sin \theta_p^* e^{i\phi_p^*} \\ T_p \sin \theta_p^* e^{-i\phi_p^*} & T_s - T_p \cos \theta_p^* \end{pmatrix}$$

$$T({}^3_\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He}) = \frac{F}{6\sqrt{\pi}} \begin{pmatrix} 3T_s - T_p \cos \theta^* & -T_p \sin \theta^* e^{i\phi^*} \\ -T_p \sin \theta^* e^{-i\phi^*} & 3T_s + T_p \cos \theta^* \end{pmatrix}$$



The normalized angular distribution of the ${}^3\text{He}$ in the decay ${}^3_\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He}$ is given by

$$\frac{dN}{d\cos\theta^*} = \text{Tr}[T^+ \hat{\rho} T] = \frac{1}{2}(1 + \alpha_{{}^3_\Lambda\text{H}} \mathcal{P}_{{}^3_\Lambda\text{H}} \cos \theta^*), \quad (7)$$

in terms of the hypertriton decay parameter $\alpha_{{}^3_\Lambda\text{H}} \approx -\frac{1}{3T_s^2 + \frac{1}{3}T_p^2} \alpha_\Lambda \approx -\frac{1}{2.58} \alpha_\Lambda$. The angular distribution of ${}^3\text{He}$ in the decay ${}^3_\Lambda\text{H} \rightarrow \pi^- + {}^3\text{He}$ can thus be further expressed as

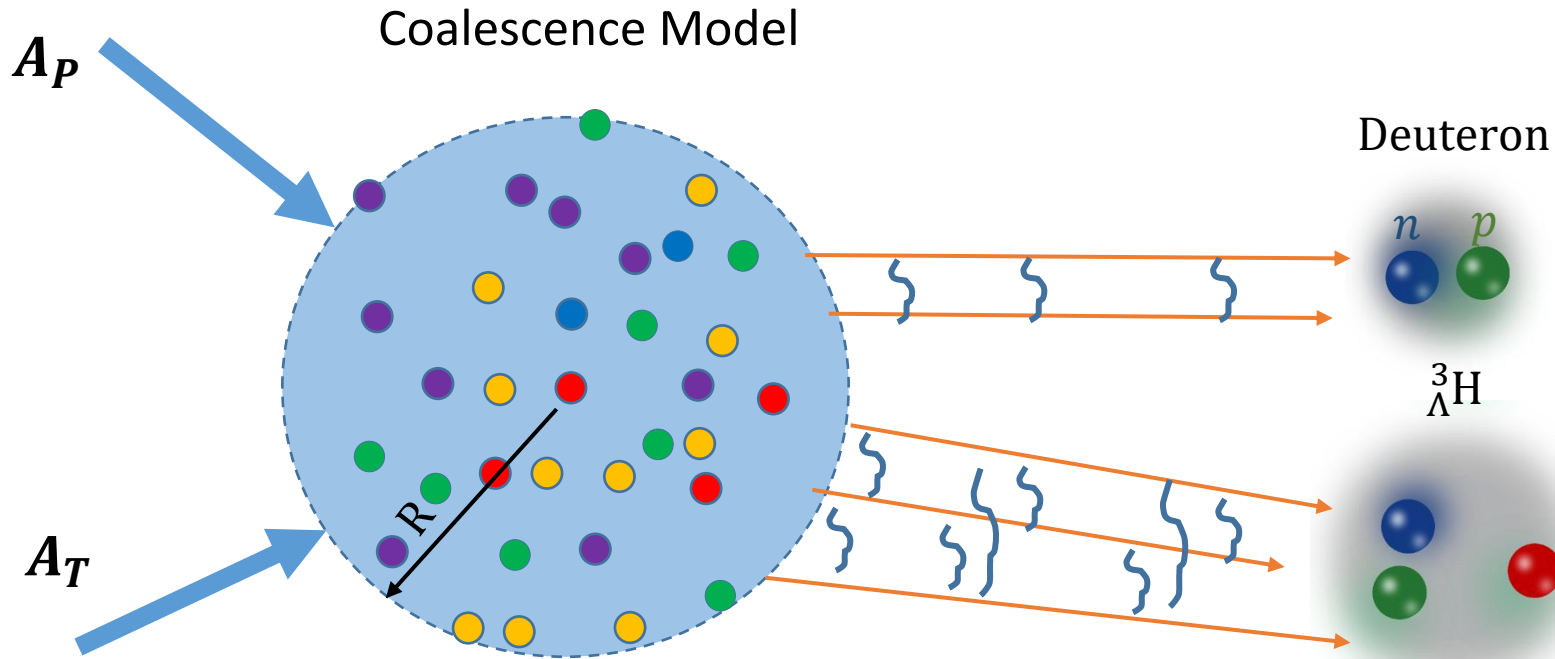
$$\frac{dN}{d\cos\theta^*} \approx \frac{1}{2} \left(1 - \frac{1}{2.58} \alpha_\Lambda \mathcal{P}_\Lambda \cos \theta^* \right). \quad (8)$$

Compared to the angular distribution of the proton in the Λ decay, which has the form

Sign flip !

$$\frac{dN}{d\cos\theta_p^*} = \frac{1}{2} (1 + \alpha_\Lambda \mathcal{P}_\Lambda \cos \theta_p^*), \quad (9)$$

the ${}^3\text{He}$ in ${}^3_\Lambda\text{H}$ decay has an opposite sign in its angular dependence.



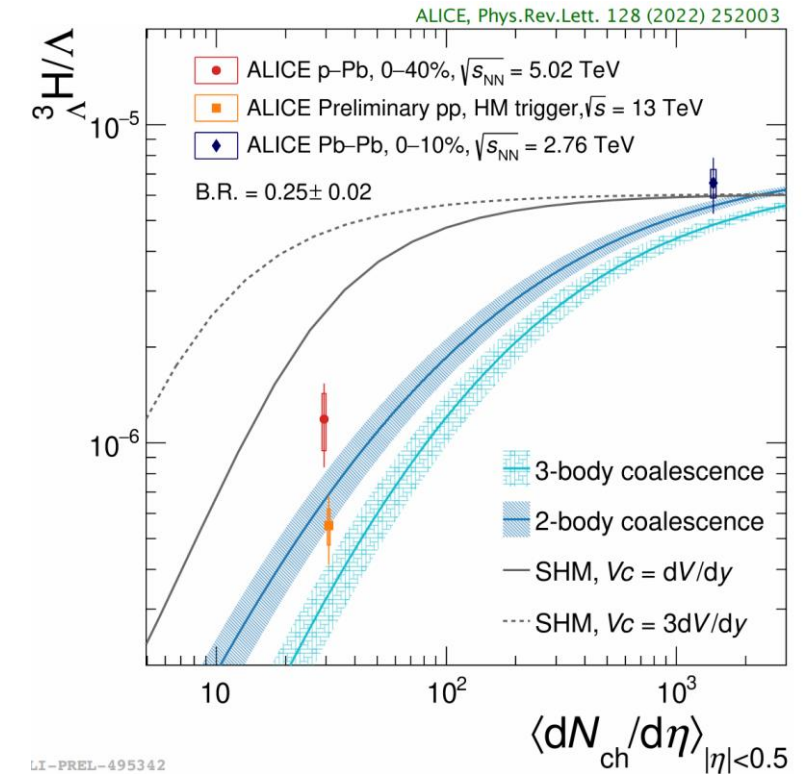
Density Matrix Formulation
(sudden approximation)

$$N_A = \text{Tr}(\hat{\rho}_s \hat{\rho}_A)$$

$$= g_c \int d\Gamma \rho_s(\{x_i, p_i\}) \times W_A(\{x_i, p_i\})$$

Wigner function of light cluster

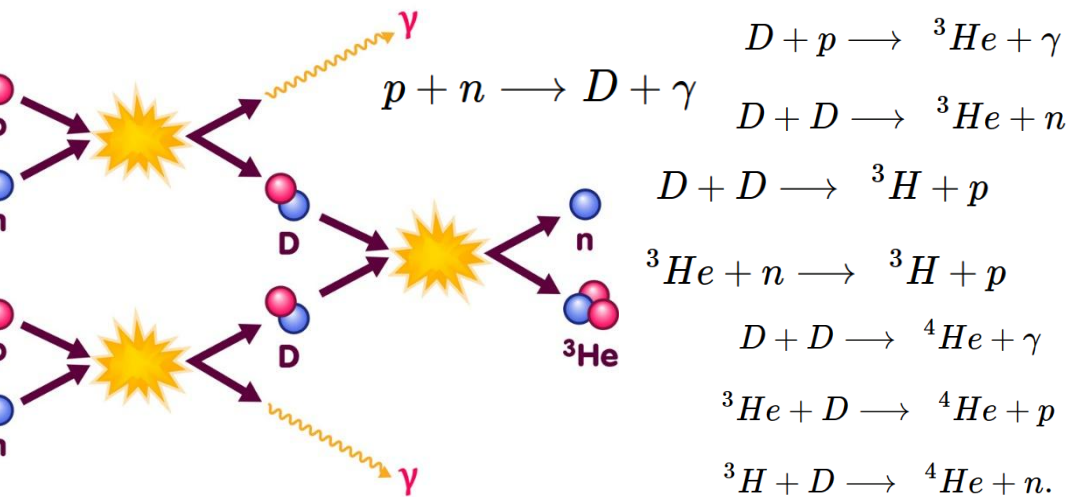
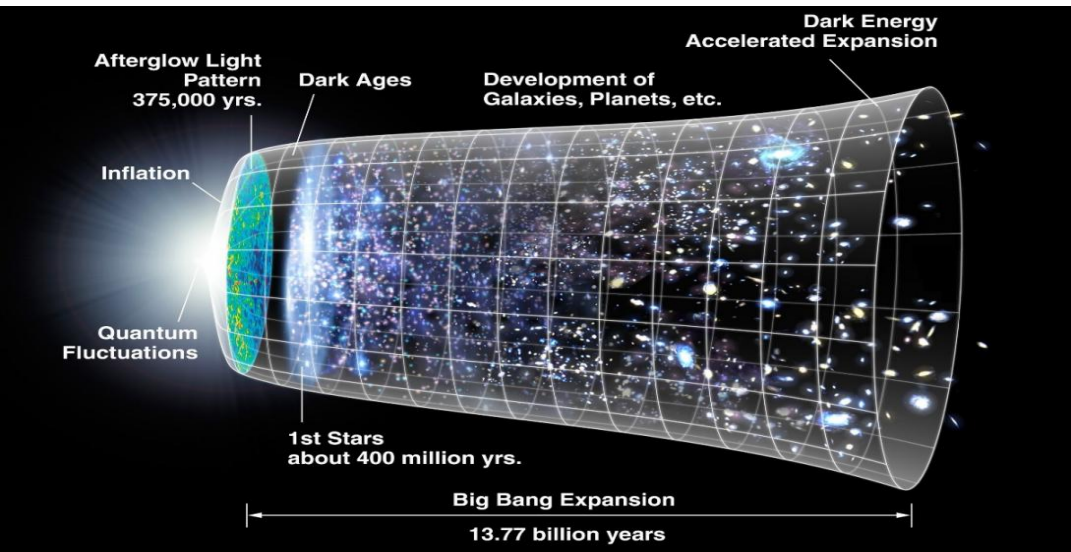
Overlap between source distribution function and Wigner function of light nuclei



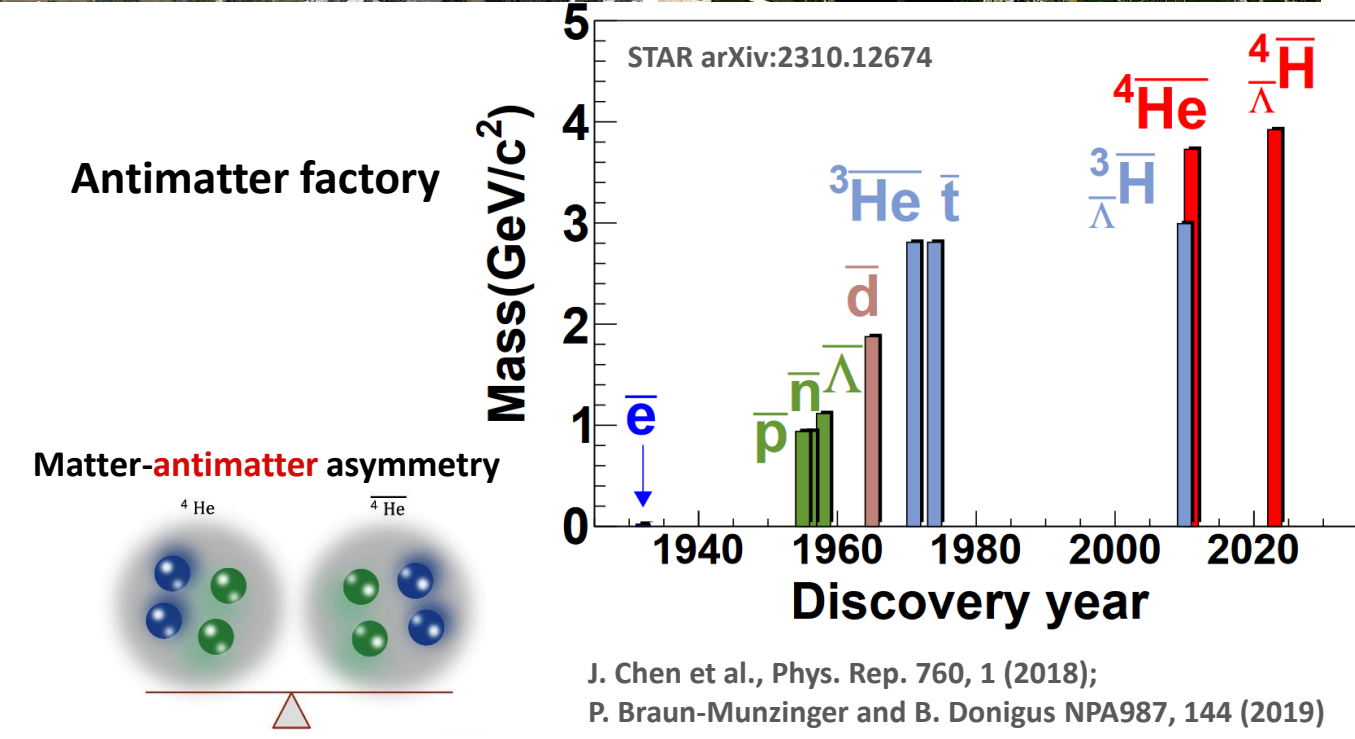
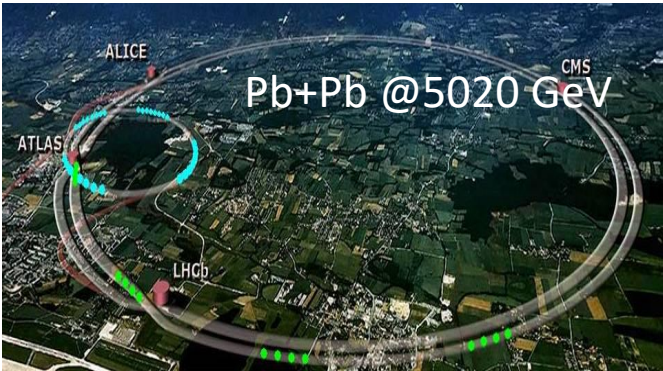
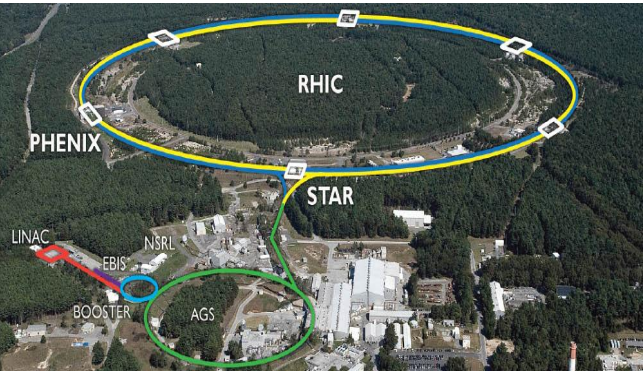
Little Bang Nucleosynthesis

Big-bang nucleosynthesis is responsible for the formation of light nuclei in our Universe.
 $t \sim 100\text{ s}, kT < 1\text{ MeV}$

K. A. Olive et al., Phys. Rept. 333, 389–407 (2000);
 《The First Three Minutes》 S. Weinberg

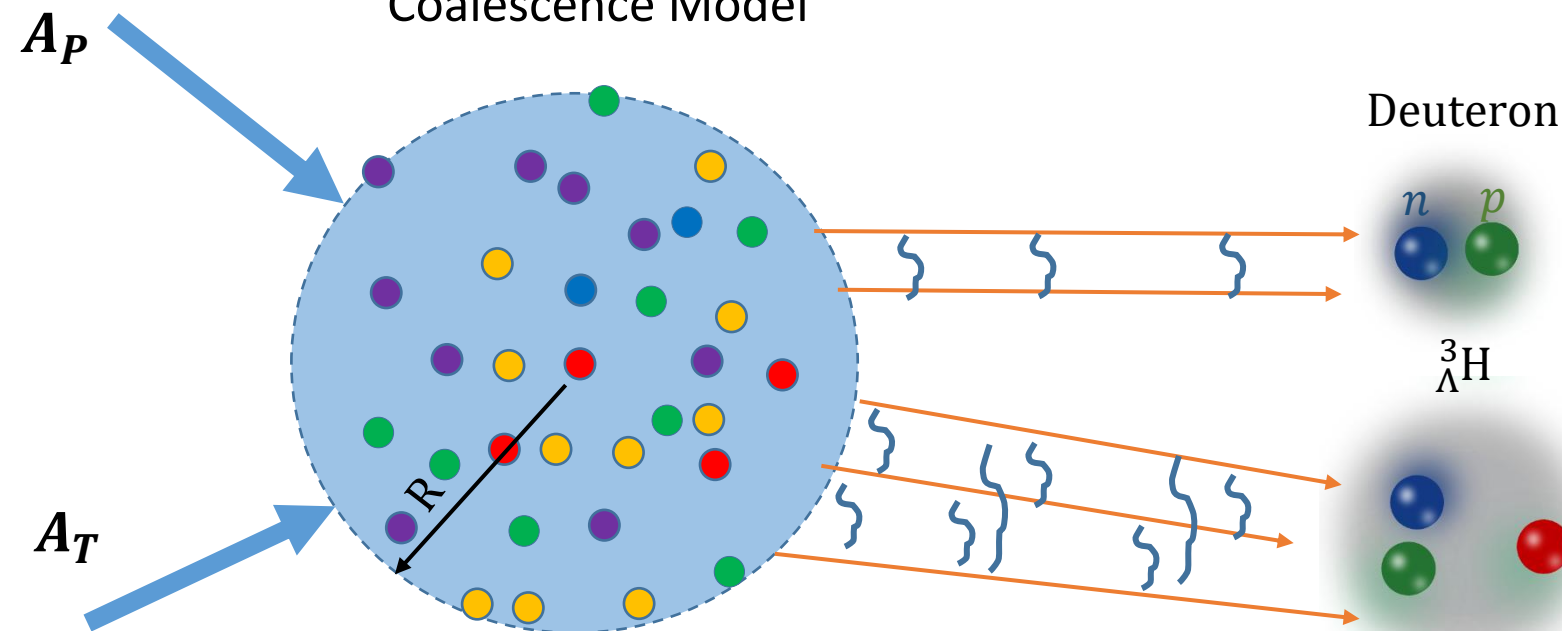


Synthesis of **antimatter** nuclei in little bangs of relativistic heavy-ion collisions
 $t \sim 10^{-22}\text{ s}, kT \sim 100\text{ MeV}$



Final-state coalescence

Coalescence Model



Density Matrix Formulation (sudden approximation)

$$N_A = \text{Tr}(\hat{\rho}_s \hat{\rho}_A)$$

$$= g_c \int d\Gamma \rho_s(\{x_i, p_i\}) \times W_A(\{x_i, p_i\})$$

Wigner function of light cluster

**Overlap between source
distribution function and Wigner
function of light nuclei**

Two-body coalescence $a + b \rightarrow c$:

$$N_c = \frac{2J_c + 1}{(2J_a + 1)(2J_b + 1)} \int \frac{dx_a dk_a}{(2\pi)^3} \frac{dx_b dk_b}{(2\pi)^3} f_a(x_a, k_a) f_b(x_b, k_b) W_c(x, k)$$

$$\approx \frac{2J_c + 1}{(2J_a + 1)(2J_b + 1)} \frac{N_a N_b}{\left(\frac{m_a m_b T}{m_a + m_b} (R_a^2 + R_b^2)\right)^{3/2}} \times \boxed{\frac{1}{\left(1 + \frac{\sigma^2}{R_a^2 + R_b^2}\right)^{3/2}}}$$

$$f_a = \frac{N_a}{(m_a T R_a^2)^{3/2}} e^{-\frac{k_a^2}{2m_a T} - \frac{x_a^2}{2R_a^2}}$$

$$W_c = 8e^{-x^2/\sigma^2 - \sigma^2 k^2}$$

$$N_a = \int \frac{dx_a dk_a}{(2\pi)^3} f_a(x_a, k_a) \quad 1 = \int \frac{dx dk}{(2\pi)^3} W_c(x, k)$$

"Quantum mechanical correction"

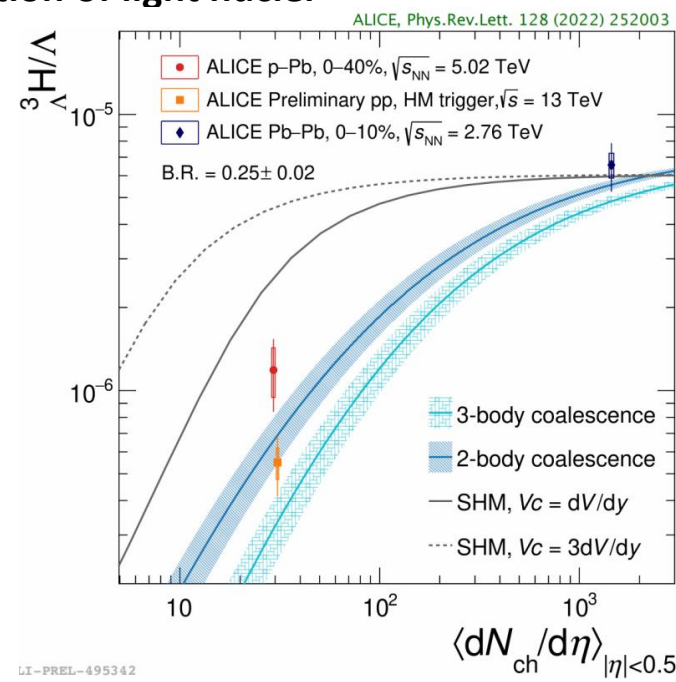
$$N_d \propto \frac{1}{\left[1 + \left(\frac{2r_d^2}{3R^2}\right)\right]^{\frac{3}{2}}}$$

Production

$$N_{{}^3_\Lambda\text{H}} \propto \frac{1}{\left[1 + \left(\frac{r_{{}^3_\Lambda\text{H}}^2}{2R^2}\right)\right]^3}$$

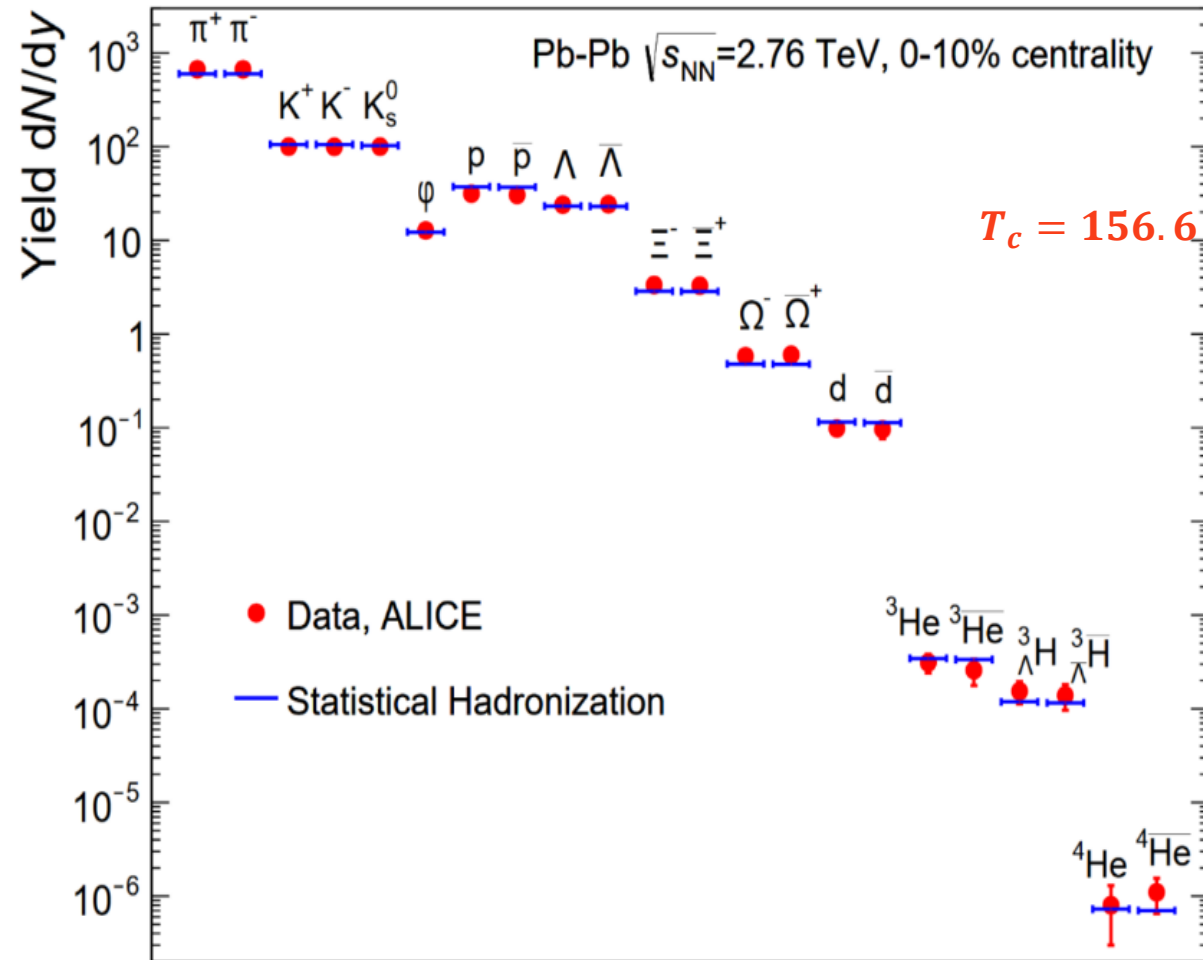
Structure

can be inferred from Femtoscopy



Statistical hadronization

Andronic, Braun-Munzinger, Redlich, Stachel, Nature 561, 321 (2018)



$$N_h \approx \frac{g_h V_C}{2\pi^2} m_h^2 T_C K_2\left(\frac{m_h}{T_C}\right)$$

$$\approx g_h V_C \left(\frac{m_h T_C}{2\pi}\right)^{3/2} e^{-m_h/T_C}$$

T_C : Chemical freeze-out temperature, which is close to the chiral transition temperature (LQCD)

All (stable) particles including light (hyper)nuclei are produced at the QCD phase boundary and share a common chemical freeze-out

Compact multi-quark states

loosely bound states

