

Production of loosely bound states in relativistic nuclear collisions

- ALICE, status and prospects for the coming decade
- the statistical hadronization model and (u,d,s) hadrons
- the Dashen-Ma-Bernstein S-matrix approach
- including loosely bound hadrons, light nuclei and hyper-nuclei
- from pp to Pb-Pb collisions
- flow of hyper-nuclei
- outlook

pbm
talk at UCAS
Beijing, China
Sep. 15, 2023



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work with:

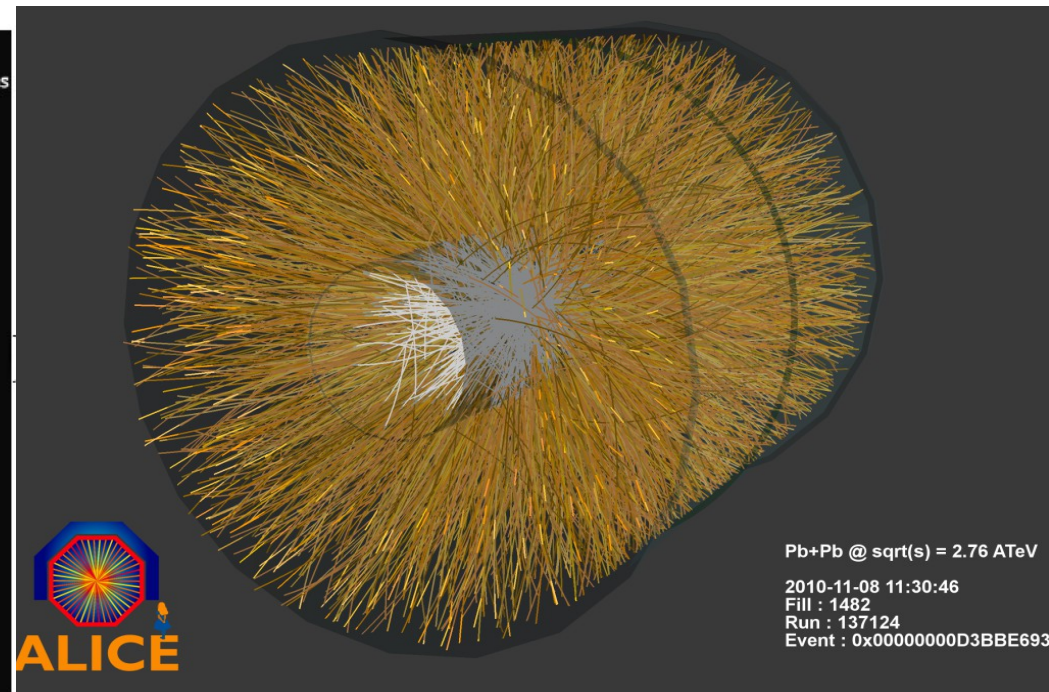
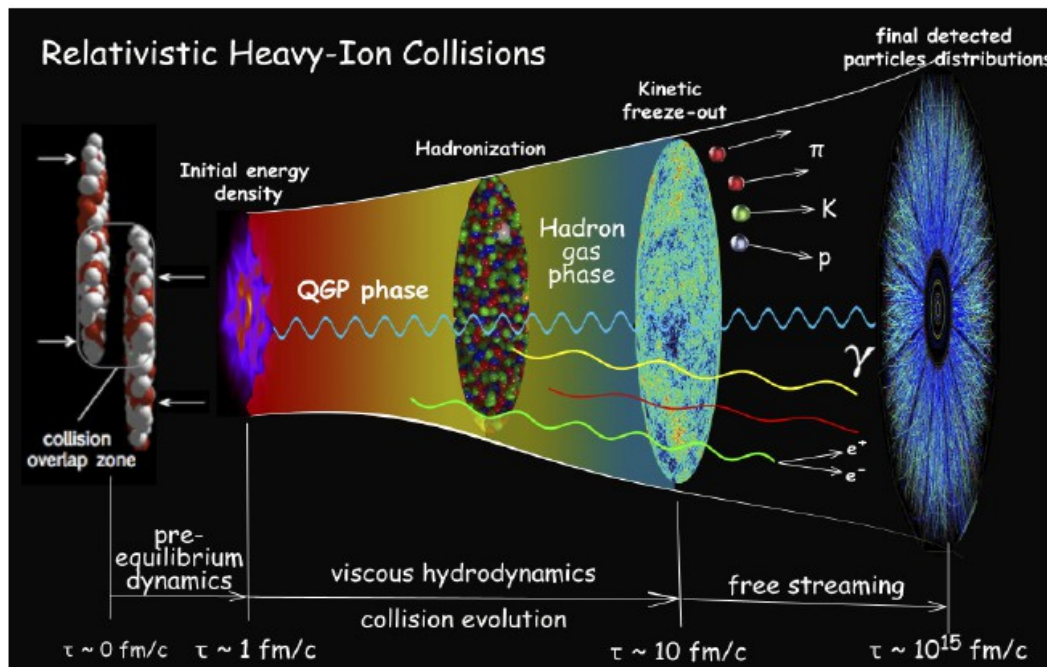
Anton Andronic, Krzysztof Redlich, Johanna Stachel

Nature 561 (2018) 7723, 321-330, 1710.09425 [nucl-th]

in this talk: newest results including those shown at QM2023@Houston



the Quark-Gluon Plasma formed in nuclear collisions at very high energy



Paul Sorensen and Chun Shen

PbPb collisions at LHC at $\sqrt{s} = 5.02$ A TeV

ALICE Run1, Run2

Run1: 3 data taking campaigns
pp, pPb, Pb—Pb
> 170 publications

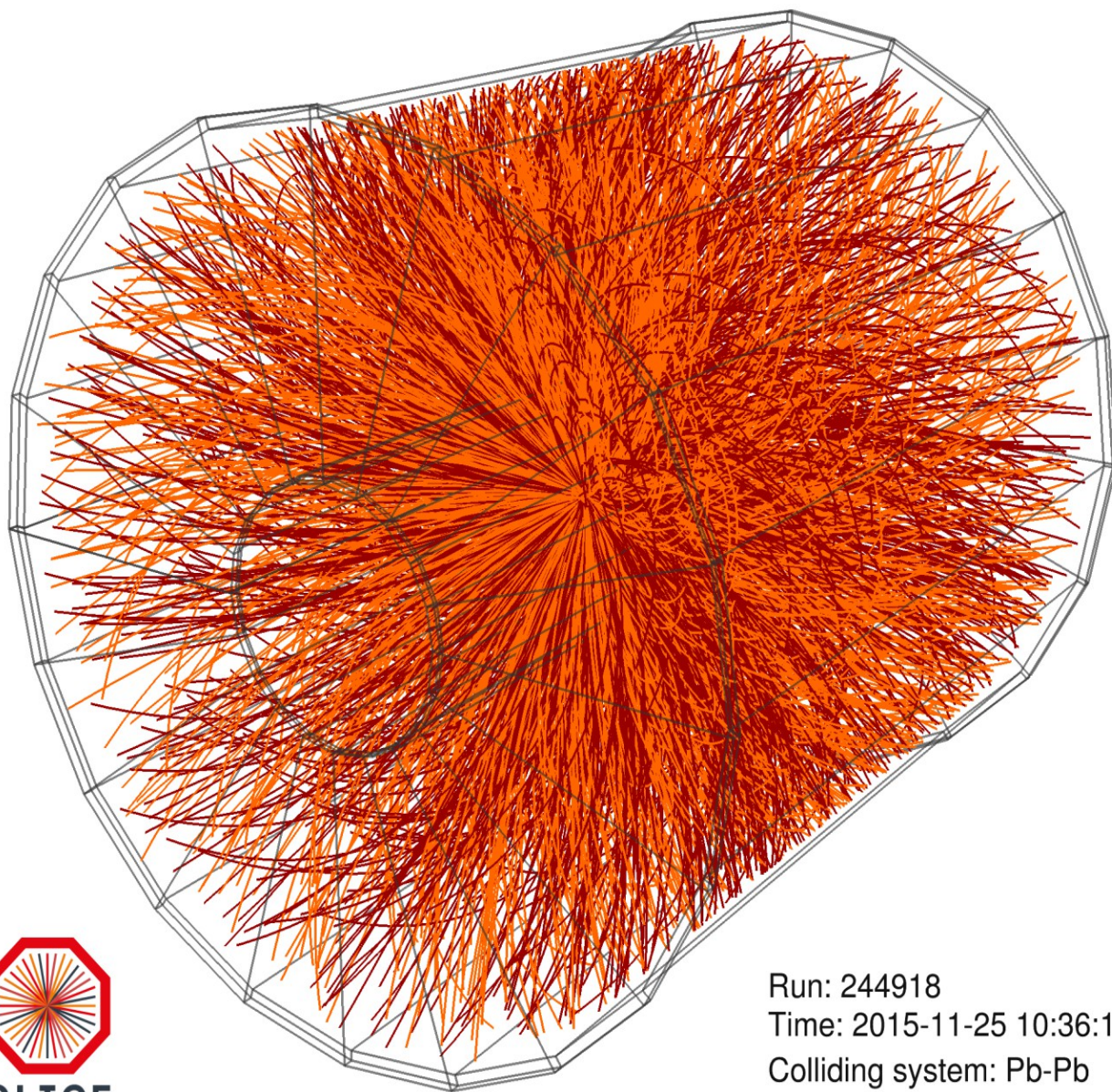
Run2 with 13 TeV pp
Pb—Pb run 5 TeV/u
p-Pb Run at 5 and 8 TeV
> 50 publications

Nov. 2018: PbPb 5 TeV/u

Snapshot taken with the ALICE
TPC

Nov. 2019: Run1 and Run2
combined: > 260 publications

central Pb-Pb collisions:
more than 32000
particles produced per collision
at top LHC energy



Run: 244918
Time: 2015-11-25 10:36:18
Colliding system: Pb-Pb
Collision energy: 5.02 TeV

ALICE plans for the coming decade 2022 – 2030

LHC Run3 and Run4

ALICE is currently being upgraded:

GEM based read-out chambers for the TPC, new inner tracker with ultra-thin Si layers, continuous read of (all) subdetectors

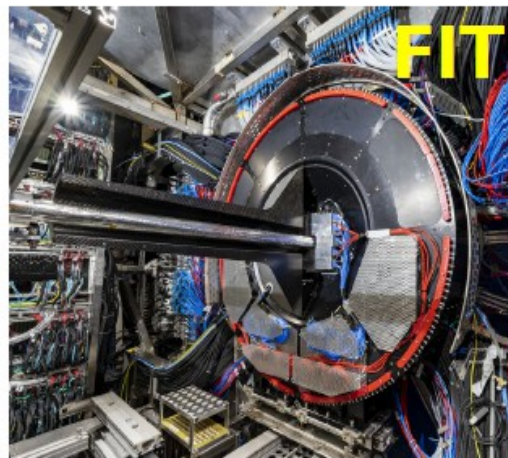
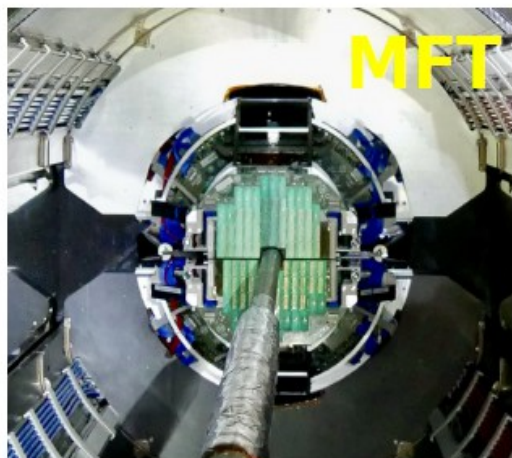
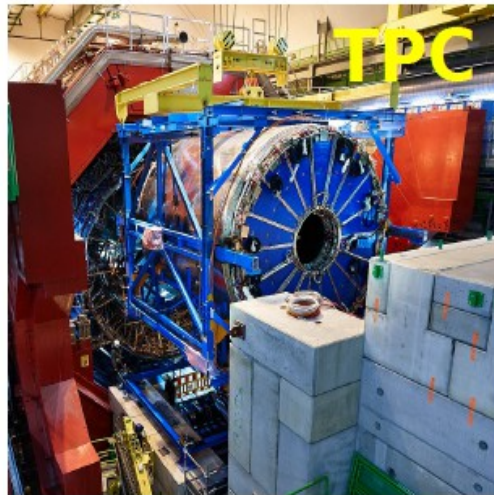
increase of data rates by factor >50

focus on rare objects, exotic quarkonia, single (and possibly double) charm hadrons to address a number of fundamental questions and issues such as:

- what is the deconfinement radius for charm quarks
- are there colorless bound states in a deconfined medium?
- are complex, light nuclei and exotic charmonia (X,Y,Z) produced as compact multi-quark bags? 
- can fluctuation measurements shed light on the mechanism of baryon production and critical behavior near the phase boundary?
- low mass dileptons and low- p_T thermal photons
- collectivity from pp to AA collisions
- nuclear and hadronic physics
 - structure of light hyper-nuclei 
 - hadron-hadron interaction from particle correlations
- ultra-peripheral and diffractive collisions

deciphering QCD in the strongly coupled regime

ALICE in Run 3 (ongoing)



- Major upgrades installed in 2019-2021
- In production since 2022
- 50x increase in readout rate
- 3 to 6x improvement in pointing resolution
- Secondary vertexing for forward muons

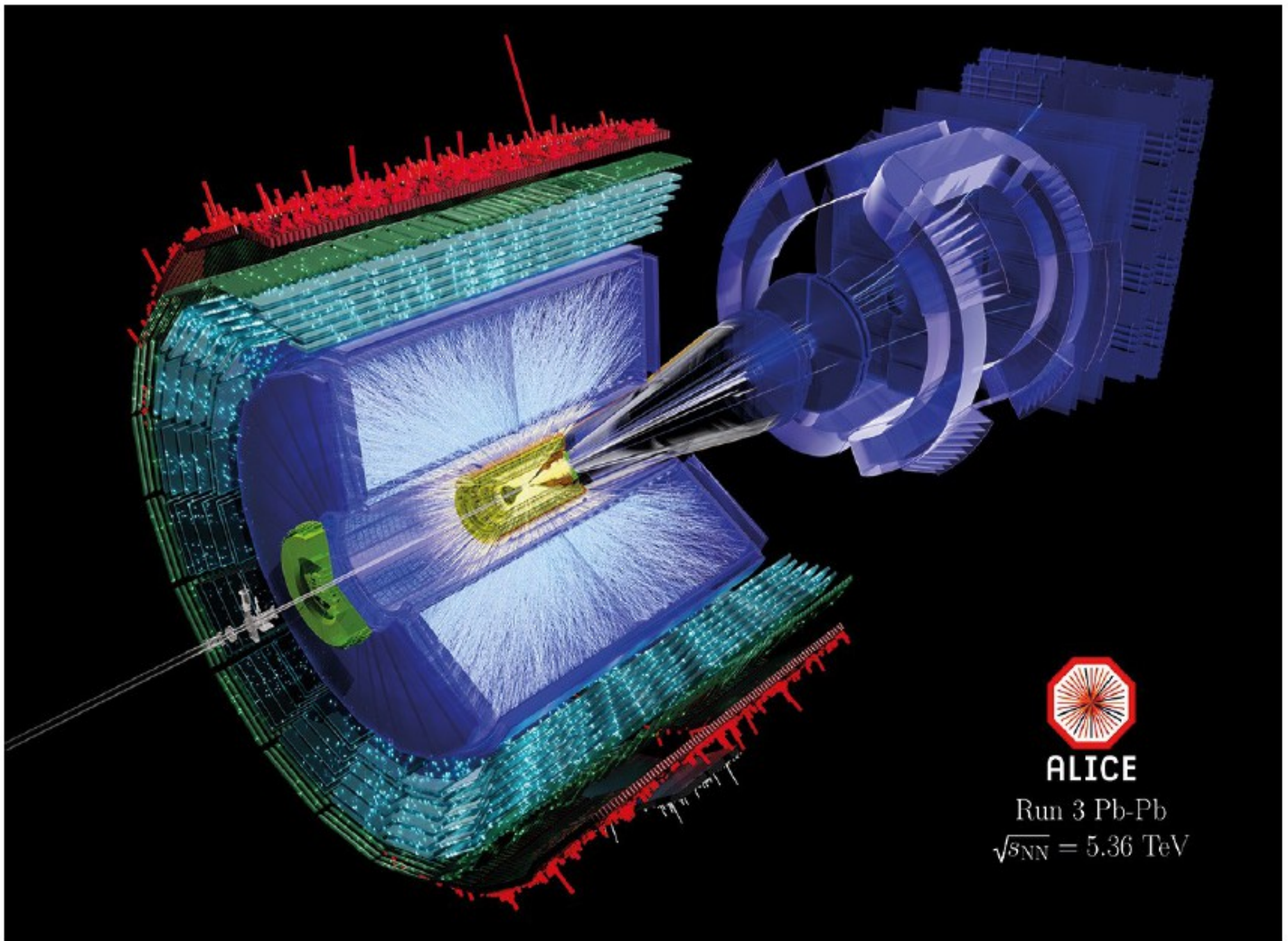
ALICE upgrades: [arXiv:2302.01238](https://arxiv.org/abs/2302.01238)

ITS: [NIM 1032\(2022\)166632](#)

TPC: [JINST 16 P03022 \(2021\)](#)

MFT: [CDS link](#)

FIT: [NIM 1039 \(2022\) 167021](#)



ALICE in 2023 Run 3

hadron production and the QCD phase boundary

measure the momenta and identity of all produced particles at all energies and look for signs of equilibration, phase transitions, regularities, etc

at the phase boundary, all quarks and gluons are converted ('hadronized') into hadrons which we measure in our detectors

main aim: establish the existence and position of the phase boundary

an important milestone also for understanding the evolution of the early universe

statistical hadronization model of particle production

partition function $Z(T,V)$ contains sum over the full hadronic mass spectrum and is fully calculable in QCD

for each particle i , the statistical operator is:

$$\ln Z_i = \frac{V g_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln[1 \pm \exp(-(E_i - \mu_i)/T)]$$

particle densities are then calculated according to:

$$n_i = N_i/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

from analysis of all available nuclear collision data we now know the energy dependence of the parameters T , μ_b , and V over an energy range from threshold to LHC energy and can confidently extrapolate to even higher energies

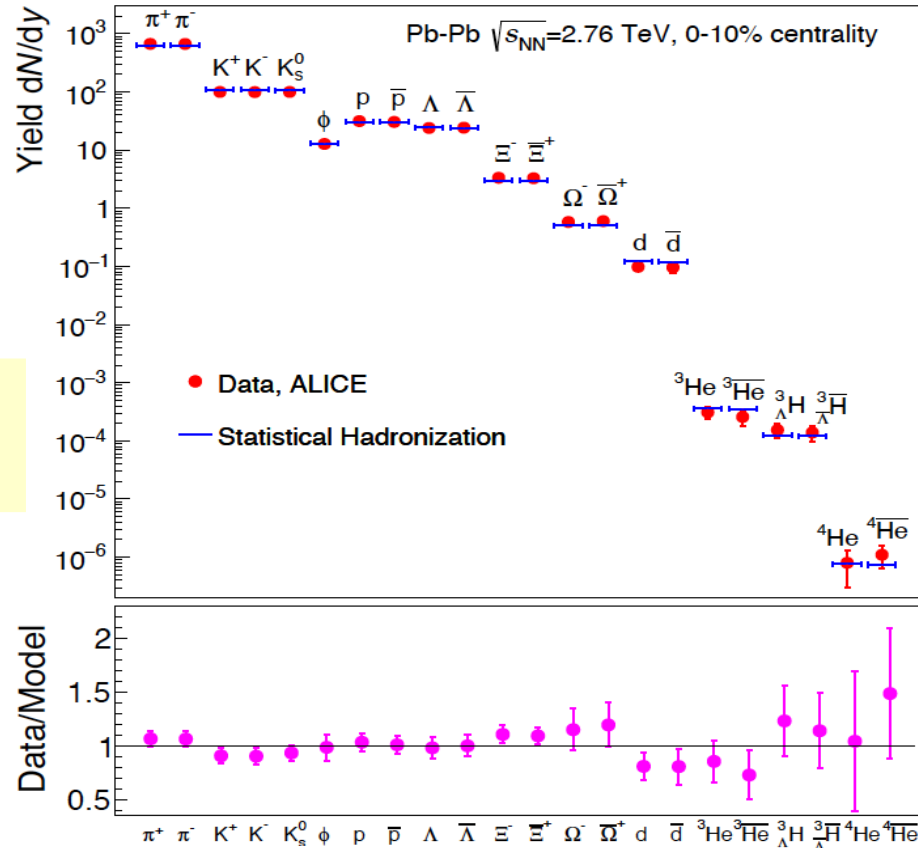
in practice, we use the full experimental hadronic mass spectrum from the PDG compilation (vacuum masses) to compute the 'primordial yield'

comparison with measured hadron yields needs evaluation of all strong decays

statistical hadronization of (u,d,s) hadrons

A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Nature 561 (2018) 321

status as of Sep. 2021



agreement over 9 orders of magnitude with QCD statistical operator prediction
(- strong decays need to be added)

- matter and antimatter formed in equal portions
- even large very fragile (hyper) nuclei follow the systematics

Best fit:

$$T_{CF} = 156.6 \pm 1.7 \text{ MeV}$$

$$\mu_B = 0.7 \pm 3.8 \text{ MeV}$$

$$V_{\Delta y=1} = 4175 \pm 380 \text{ fm}^3$$

$$\chi^2/N_{df} = 16.7/19$$

S-matrix treatment of interactions (non-strange sect.)

"proton puzzle" solved

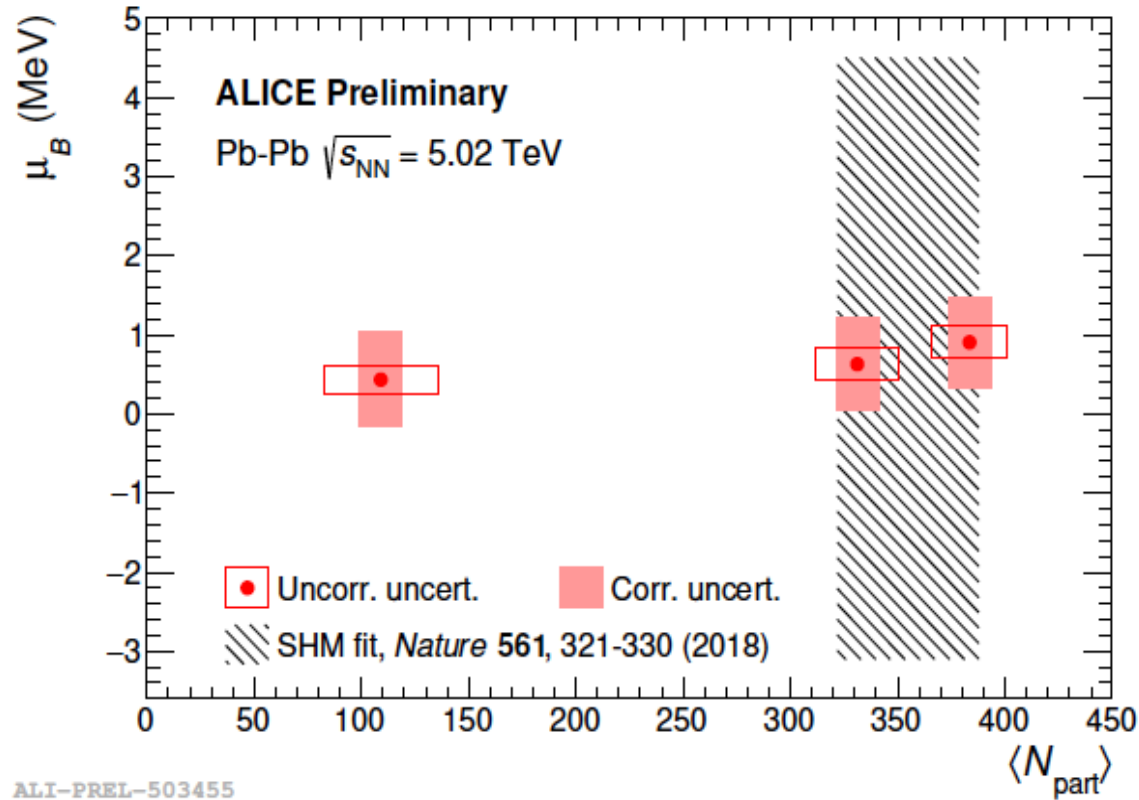
PLB 792 (2019) 304

data: ALICE coll.,
Nucl. Phys. A971 (2018) 1

similar results at lower energy,
each new energy yields a pair of
(T , μ_B) values

connection to QCD (QGP) phase
diagram

newest determination of baryon chemical potential



$$\mu_B = 0.66 \pm 0.45 \text{ MeV}$$

the proton anomaly and the Dashen, Ma, Bernstein S-matrix approach

R. Dashen, S. K. Ma, and H. J. Bernstein, Phys. Rev. **187**, 345 (1969).

The S-matrix formalism [20–24] is a systematic framework for incorporating interactions into the description of the thermal properties of a dilute medium. In this scheme, two-body interactions are, via the scattering phase shifts, included in the leading term of the S-matrix expansion of the grand canonical potential. The resulting interacting density of states is then folded into an integral over thermodynamic distribution functions, which, in turn, yields the interaction contribution to a particular thermodynamic observable.

thermal yield of an
(interacting) resonance
with mass M , spin J , and
isospin I

$$\langle R_{I,J} \rangle = d_J \int_{m_{th}}^{\infty} dM \int \frac{d^3p}{(2\pi)^3} \frac{1}{2\pi} B_{I,J}(M) \\ \times \frac{1}{e^{(\sqrt{p^2+M^2}-\mu)/T} + 1},$$

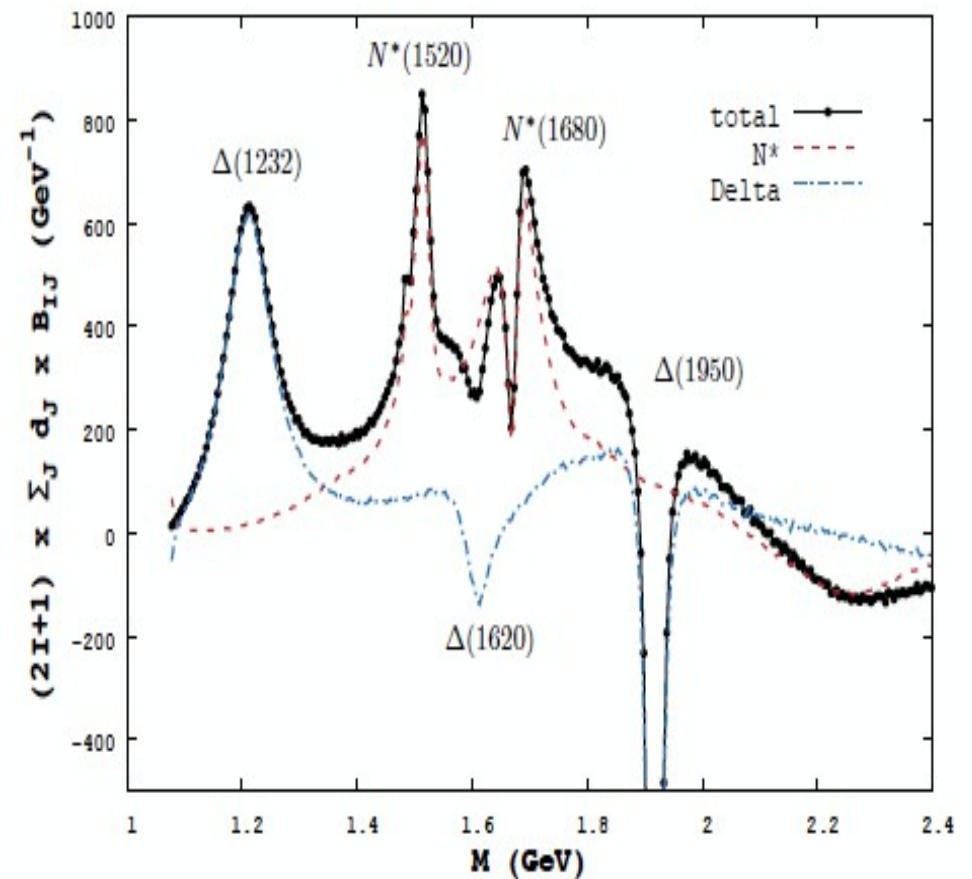
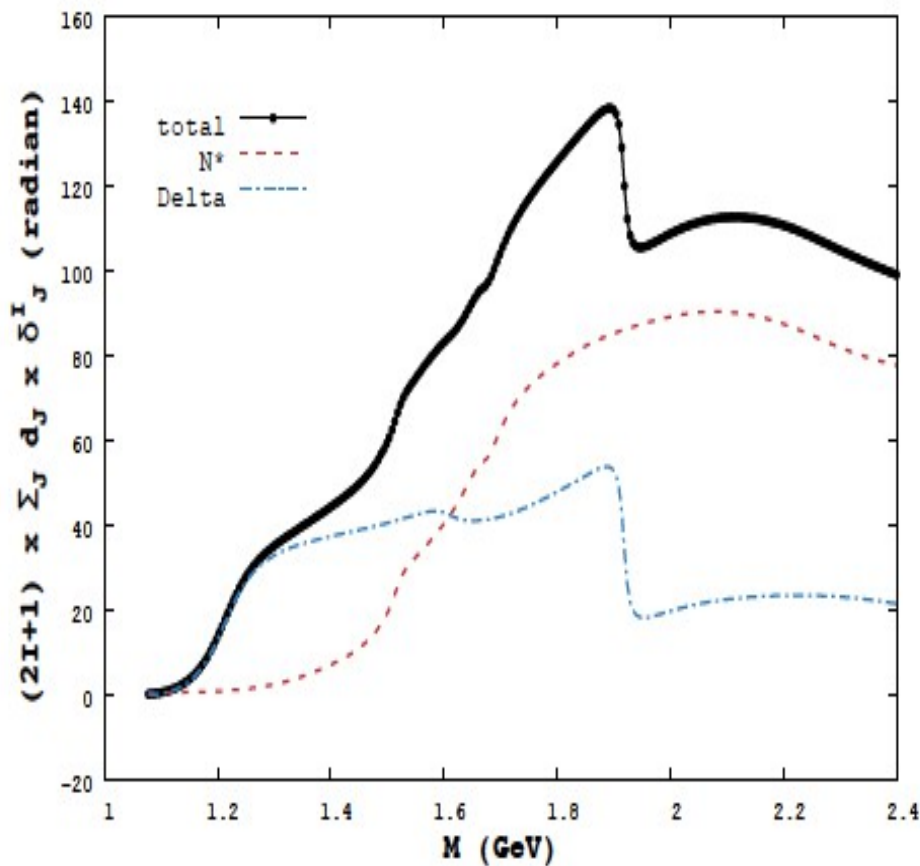
need to know derivatives
of phase shifts with
respect to invariant mass

$$B_{I,J}(M) = 2 \frac{d\delta_J^I}{dM}.$$

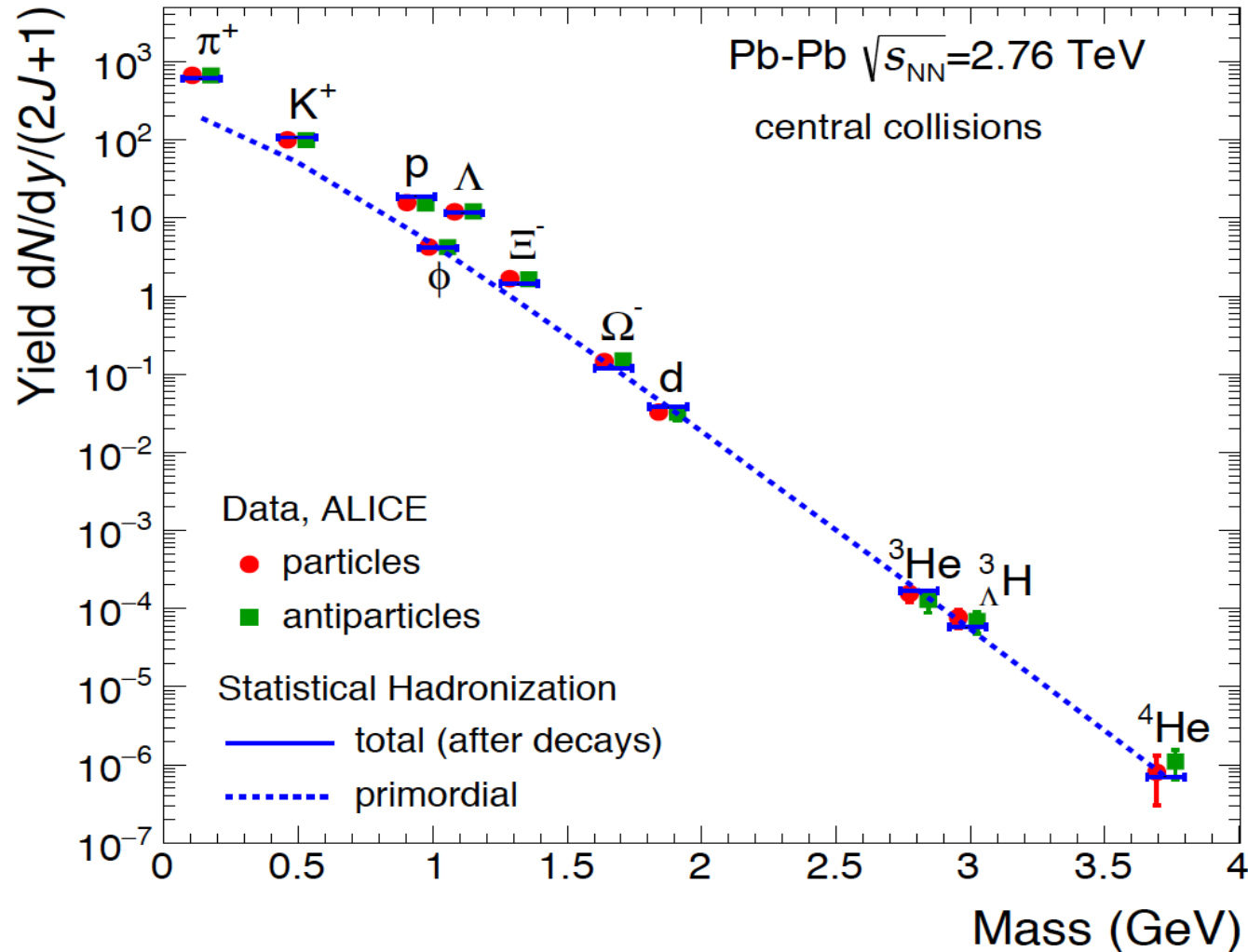
A. Andronic, pbm, B. Friman,
P.M. Lo, K. Redlich, J. Stachel,
arXiv:1808.03102,
Phys.Lett.B792 (2019)304

pion nucleon phase shifts and thermal weights for N^* and Δ resonances

GWU/SAID phase shift analysis, 15 partial waves for each isospin channel



at LHC energy, production of (u,d,s) hadrons is governed
by mass and quantum numbers only
quark content does not matter

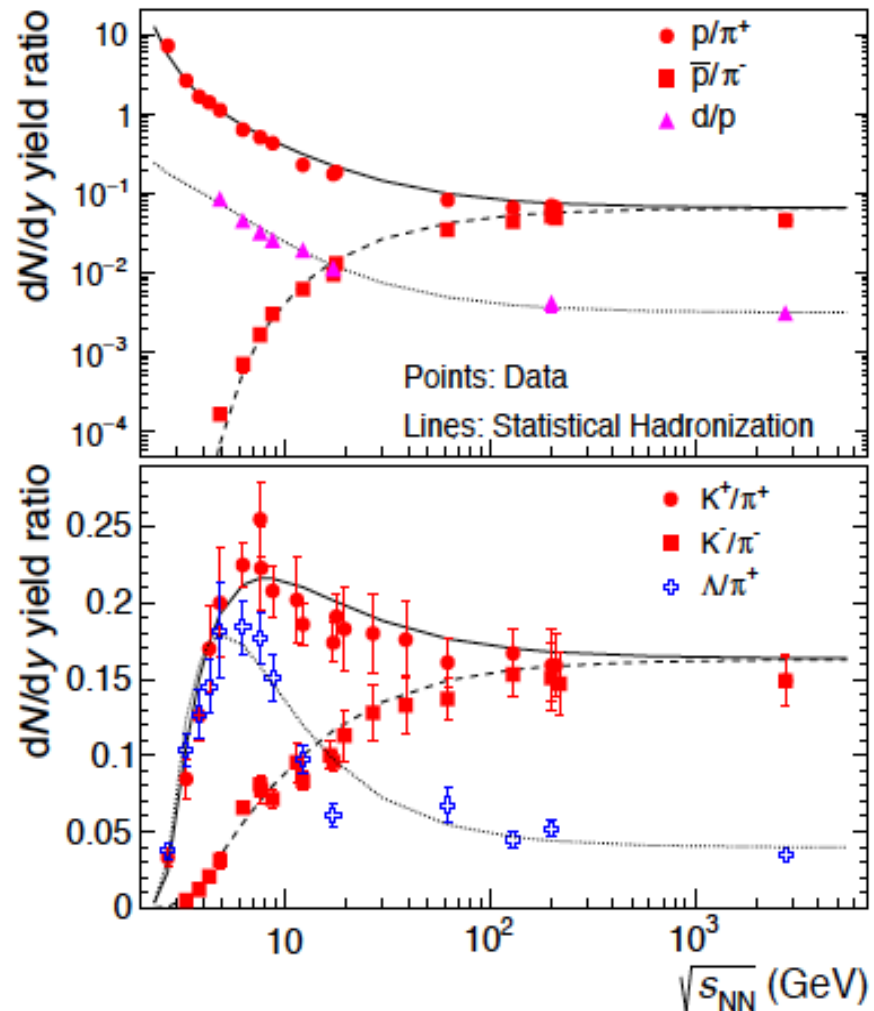
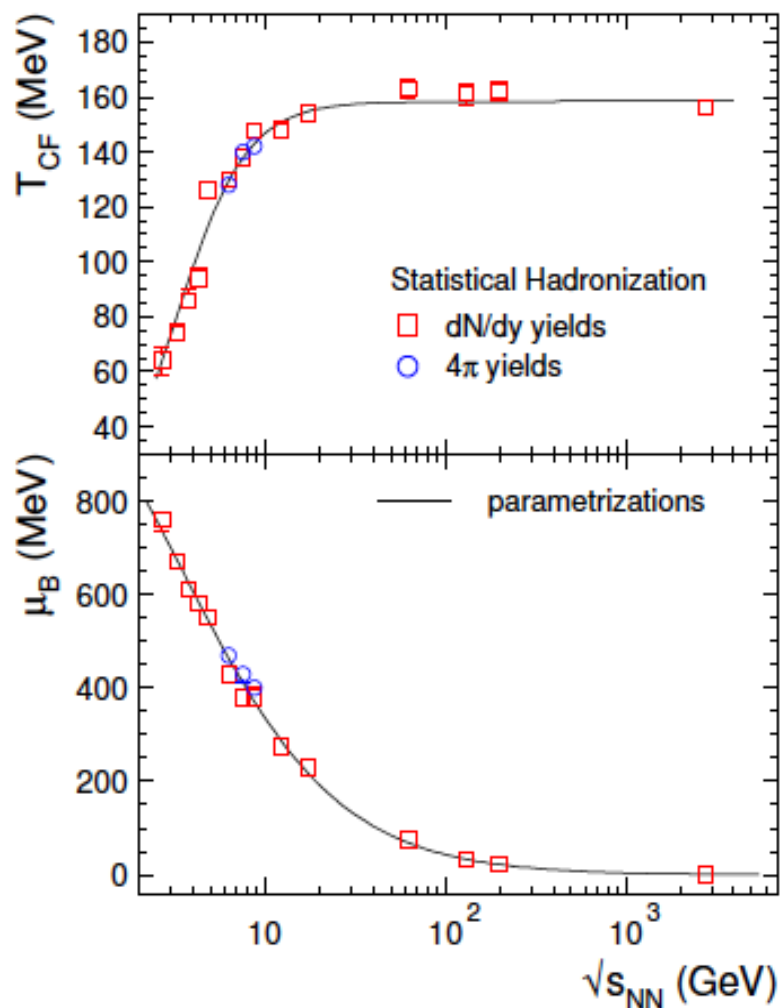


universal hadronization

1 parameter (T)

at LHC energy, matter and anti-matter is
produced with equal yields

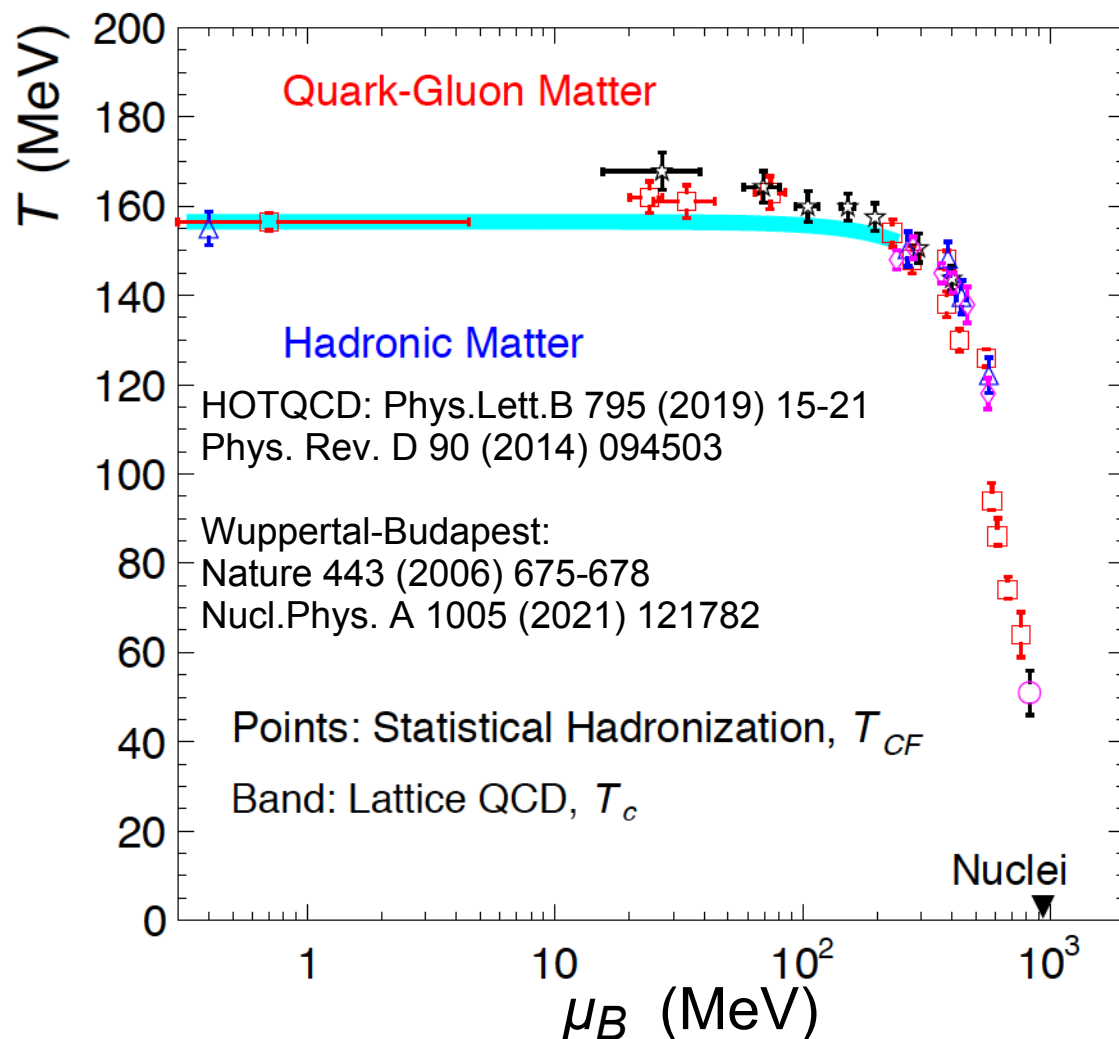
energy dependence of hadron production described quantitatively



together with known energy dependence of charged hadron production in Pb-Pb collisions we can predict yield of all hadrons at all energies with < 10% accuracy

the QGP phase diagram, LatticeQCD, and hadron production data

note: all coll. at SIS, AGS, SPS, RHIC and LHC involved in data taking
each entry is result of several years of experiments, variation of μ_B via variation of cm energy



quantitative agreement of
chemical freeze-out parameters
with most recent LQCD
predictions for baryo-chemical
potential < 300 MeV

**cross over transition at
 $\mu_B = 0$ MeV, no experimental
confirmation**

**should the transition be 1st
order for large μ_B (large net
baryon density)?**

**then there must be a critical
endpoint in the phase
diagram**

experimental determination of phase boundary at
 $T_c = 156.6 \pm 1.7$ (stat.) ± 3 (syst.) MeV and $\mu_B = 0$ MeV
Nature 561 (2018) 321

now on to very loosely bound states and their production in high energy collisions

- already the deuteron with 2.2 MeV binding energy is very loosely bound compared to the average energy of particles at the LHC (TeV)
- the hyper-triton is an even more extreme case, see below
- the quantum mechanical formation time of such states far exceeds 100 fm/c, i.e. they cannot be generated or destroyed more than once in a collision

The hyper-triton

mass = 2990 MeV, binding energy = 2.3 MeV

Lambda sep. energy = 0.13 MeV

molecular structure: $(p+n) + \text{Lambda}$

2-body threshold: $(p+p+n) + \pi^- = {}^3\text{He} + \pi^-$

rms radius = $(4 \text{ B.E. } M_{\text{red}})^{-1/2} = 10.3 \text{ fm} =$

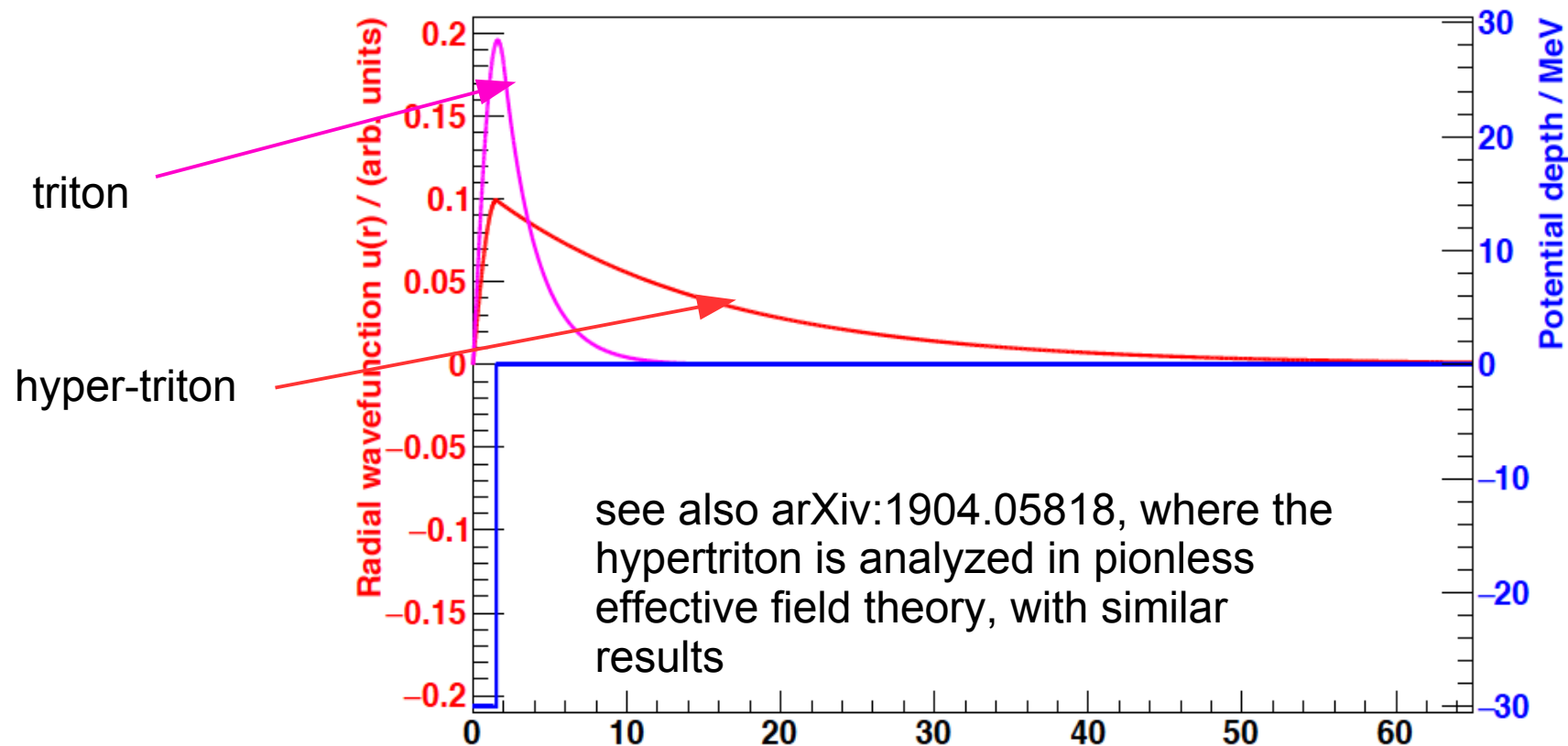
rms separation between d and Lambda

in that sense: hypertriton = $(p \ n \ \text{Lambda}) =$
 $(d \ \text{Lambda})$ is the ultimate halo state

yet production yield is fixed at 156 MeV temperature
(about 1000 x Lambda separation energy.)

wave function of the hyper-triton – schematic picture

figure by Benjamin Doenigus, August 2017



Wavefunction (red) of the hypertriton assuming a s-wave interaction for the bound state of a Λ and a deuteron. The root mean square value of the radius of this function is $\sqrt{\langle r^2 \rangle} = 10.6$ fm. In blue the corresponding square well potential is shown. In addition, the magenta curve shows a "triton" like object using a similar calculation as the hypertriton, namely a deuteron and an added nucleon, resulting in a much narrower object as the hypertriton.

now most recent results on hyper-triton structure from ALICE precision measurements

- binding energy
- Λ separation energy
- lifetime

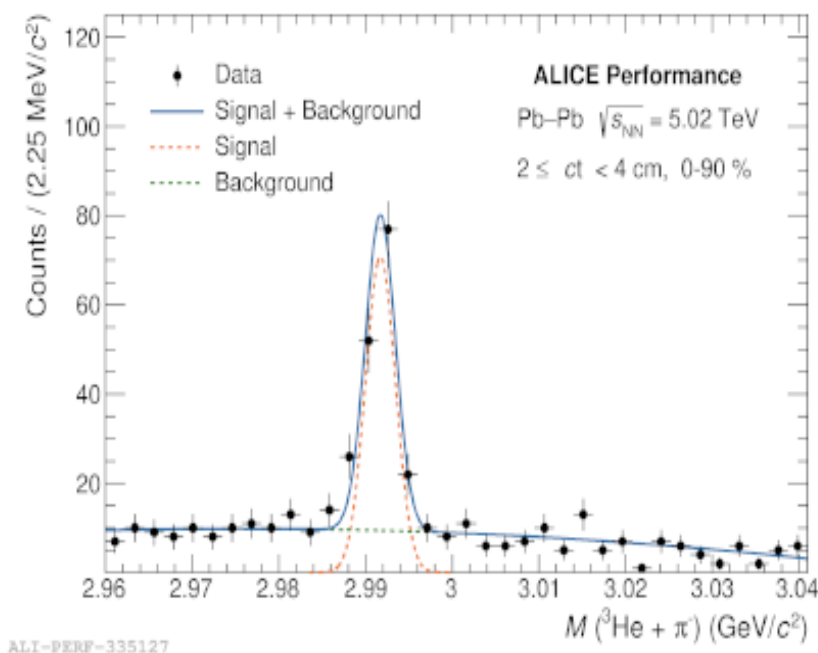
hyper-triton identification in ALICE using machine-learning techniques



BDT

for boosting the signal extraction

- Boosted Decision Trees (BDT) models trained on dedicated sample to discriminate signal and background
- State-of-the-art hyperparameter optimization
- BDT selection optimized to improve the significance of the hypertriton signal
- Signal extracted with high significance over a wide ct range



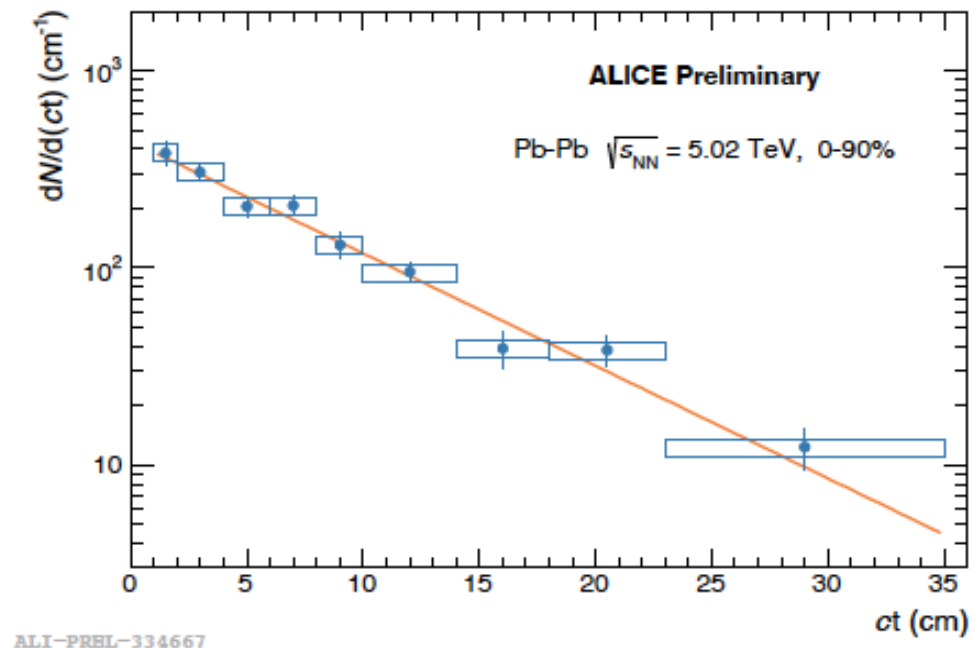
very small background contribution

newest result on lifetime measurement – needs precision determination of ALICE detector material



Lifetime measurement

- Signal extracted in a wide ct range thanks to the BDT
- Most precise hypertriton lifetime determination so far
 - 5% stat. 6% syst.
 - Statistical uncertainty lower than the world average uncertainty
- Consistent with free Λ lifetime and previous ALICE measurement

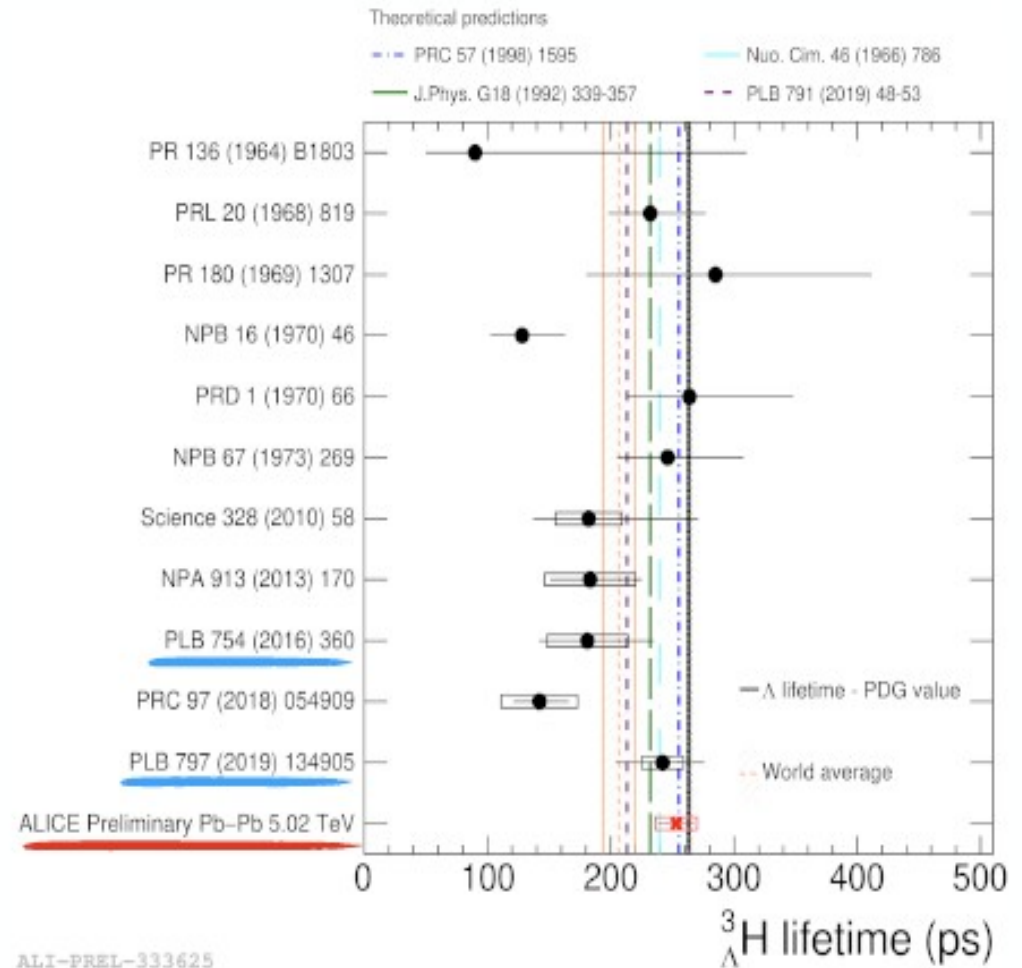


newest ALICE results strongly support loosely bound structure of hyper-triton

Lifetime measurement

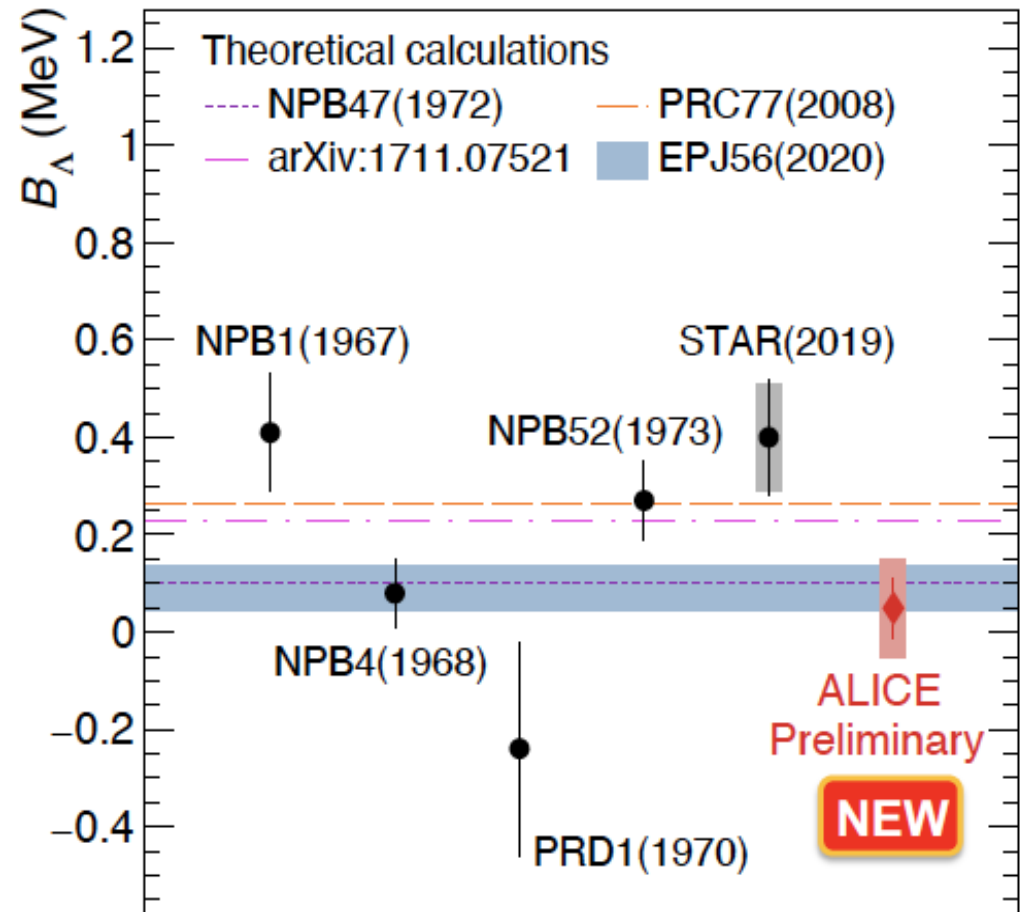


- Signal extracted in a wide ct range thanks to the BDT
- Most precise hypertriton lifetime determination so far
 - 5% stat. 6% syst.
 - Statistical uncertainty lower than the world average uncertainty
- Consistent with free Λ lifetime and previous ALICE measurement



new ALICE results on hyper-triton binding energy

- Use Machine Learning (BDTs) to identify ${}^3_{\Lambda}\text{H}$ candidates in Pb–Pb
- Most precise measurement of ${}^3_{\Lambda}\text{H}$ lifetime
 - Favors ${}^3_{\Lambda}\text{H}$ lifetime near free Λ lifetime
- Very precise measurements of ${}^3_{\Lambda}\text{H}$ mass and **binding energy**
 - Binding energy compatible with 0.
 - Support loosely bound ${}^3_{\Lambda}\text{H}$



note: measurement of B_{Λ} : 100 keV precision out of 2.99 GeV mass, $dm/m = 1/30000$

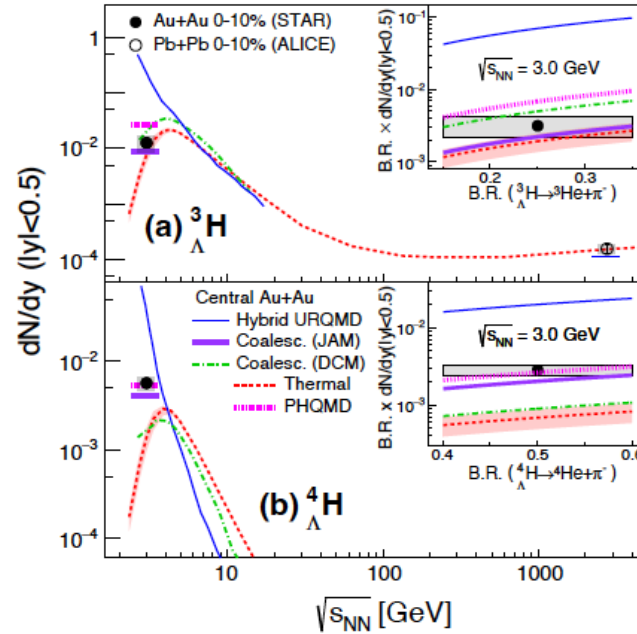
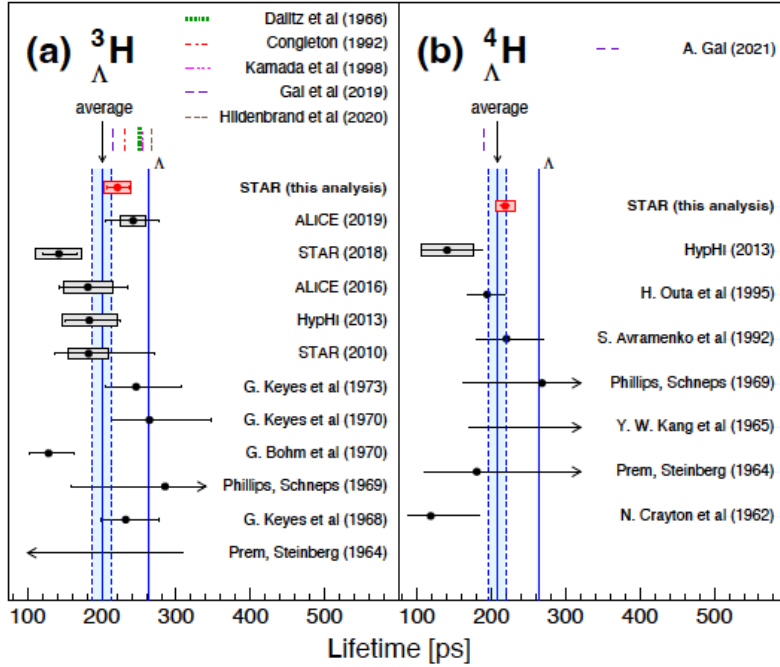
**hyper-triton is large (about 10 fm radius)
and very loosely bound**

ALICE coll., Phys.Rev.Lett. 131 (2023) 10, 102302

$$\tau = [253 \pm 11 \text{ (stat.)} \pm 6 \text{ (syst.)}] \text{ ps},$$

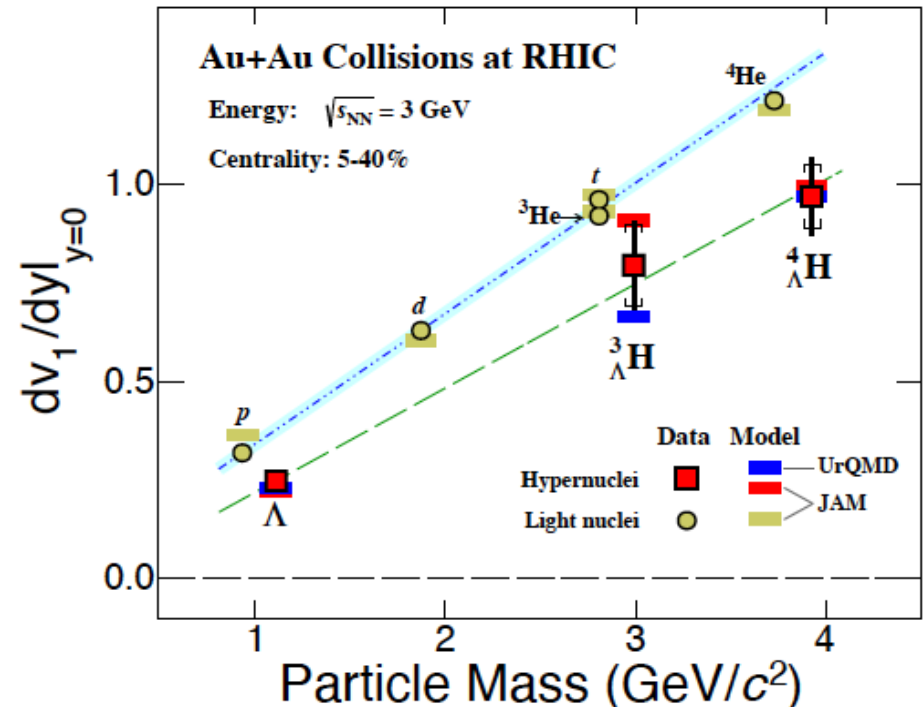
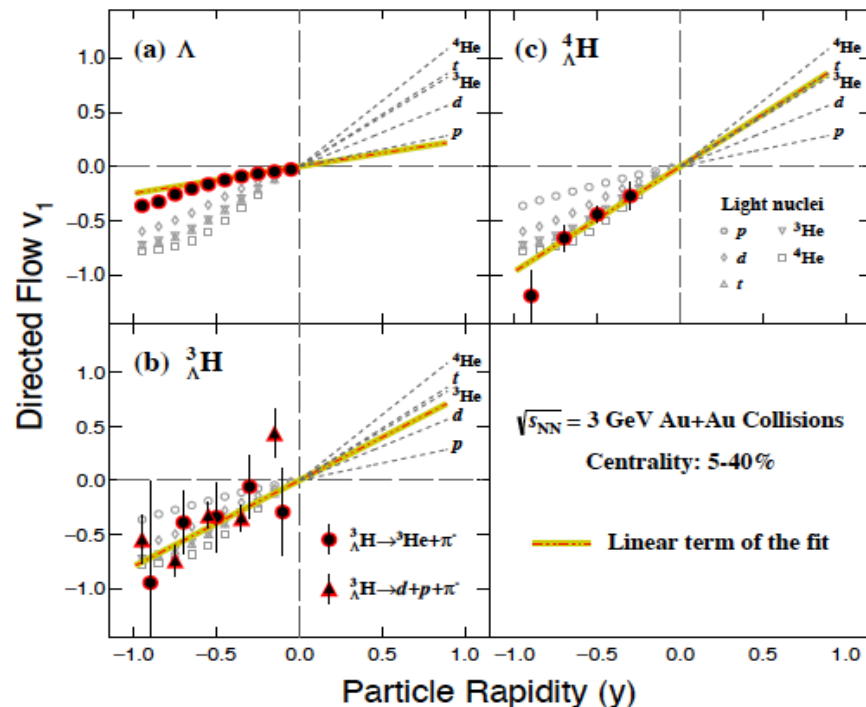
$$B_{\Lambda} = [72 \pm 63 \text{ (stat.)} \pm 36 \text{ (syst.)}] \text{ keV}.$$

in Au-Au collisions at low energy $\sqrt{s_{NN}} = 3$ GeV



results from STAR at $\sqrt{s_{NN}} = 3$ GeV,
Phys.Rev.Lett. 128 (2022) 20, 202301

flow of hyper-nuclei in Au-Au collisions at low energy $\sqrt{s_{NN}} = 3$ GeV



STAR collaboration, Phys.Rev.Lett. 130 (2023) 21, 212301

coalescence for hyper-nuclei??
or doorway production, see below

extension of SHM description to production in light systems from Pb-Pb to pPb to pp

need canonical thermodynamics and extended S-matrix approach

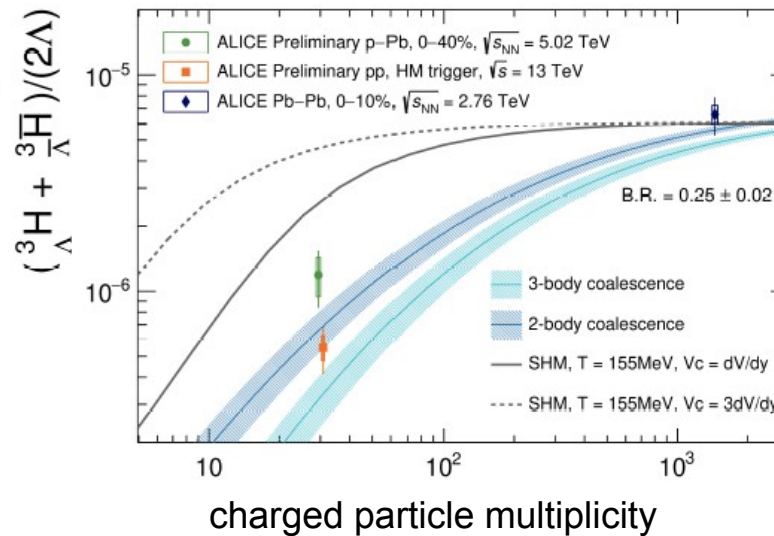
'the S-matrix calculation is based on the empirical phase shifts of πN scattering, an estimate of the $\pi\pi N$ background constrained by Lattice QCD results of baryon-charge susceptibility, and an existing coupled-channel model describing the $|S| = 1$ strange baryons. an accurate description results of the widths of resonances and the non-resonant interactions in the thermal model. this leads to a reduction of the proton yield relative to the HRG baseline (by $\approx 25\%$). including the protons from strong decays of $|S| = 1$ hyperons, which constitute $\approx 6\%$ of the total yields, does not alter this conclusion. '

adapted from:

Cleymans, Lo, Redlich, Sharma, Phys.Rev.C 103 (2021) 1, 014904, 2009.04844 [hep-ph]

hyper-triton production from pp to Pb-Pb collisions coalescence vs statistical hadronization model

- First measurements of ${}^3_{\Lambda}\text{H}$ yields in **pp** (high-multiplicity) & **p-Pb**
- Results: ${}^3_{\Lambda}\text{H}/\Lambda$ yield ratio



inconclusive: no S-matrix correction for protons

S-matrix correction for strange baryons

Cleymans, Lo, Redlich, Sharma, Phys.Rev.C 103 (2021) 1, 014904, 2009.04844 [hep-ph]

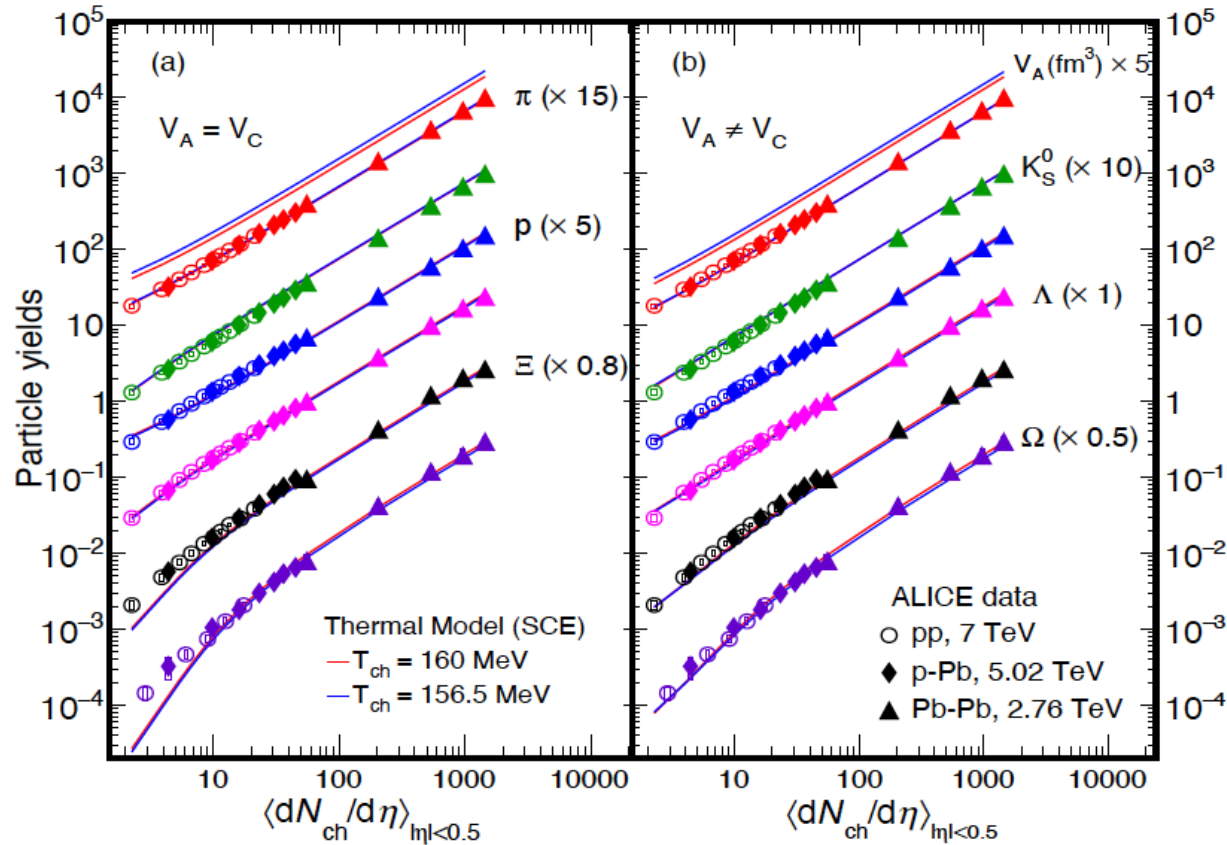
4

channel	elastic	channel	quasi-elastic	channel	unitarity
1	$\bar{K}N$	6	$\bar{K}_1^*N$	15	$\pi\pi\Lambda$
2	$\pi\Sigma$	7	$[\bar{K}_3^*N]_-$	16	$\pi\pi\Sigma$
3	$\pi\Lambda$	8	$[\bar{K}_3^*N]_+$		
4	$\eta\Lambda$	9	$[\pi\Sigma(1385)]_-$		
5	$\eta\Sigma$	10	$[\pi\Sigma(1385)]_+$		
		11	$[\bar{K}\Delta(1232)]_-$		
		12	$[\bar{K}\Delta(1232)]_+$		
		13	$[\pi\Lambda(1520)]_-$		
		14	$[\pi\Lambda(1520)]_+$		

TABLE I. The list of interaction channels included in the coupled-channel PWA describing the $|S| = 1$ hyperon system by the Joint Physics Analysis Center (JPAC) Collaboration [70]. Note that $\bar{K}^*$ is spin one and together with a nucleon can couple to spin 1/2 (denoted $\bar{K}_1^*N$) and spin 3/2 (denoted $\bar{K}_3^*N$). Subindices $\pm$ represent the higher and lower orbital angular momentum states which couple to a given partial wave.

no phase shift measurements available, use plane wave coupled channel approach instead

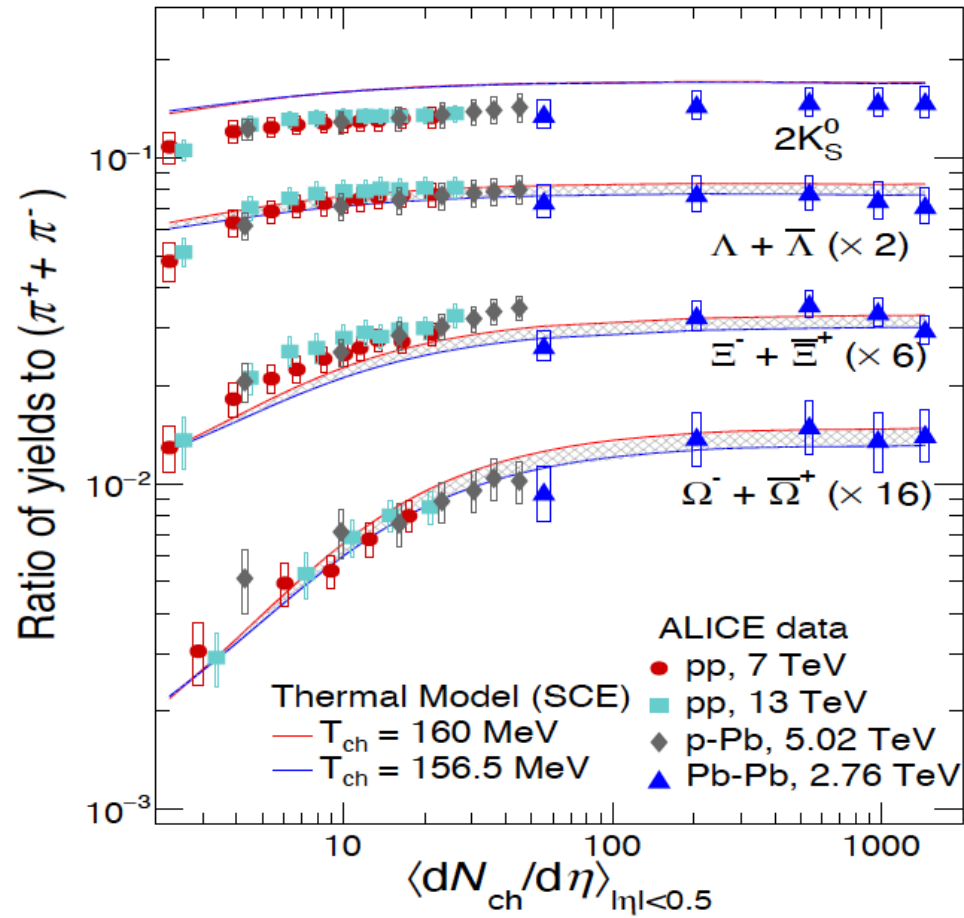
correlation volume dependence of canonical approach



Cleymans, Lo, Redlich, Sharma, Phys.Rev.C 103 (2021) 1, 014904, 2009.04844 [hep-ph]

excellent description of ALICE data from Pb-Pb to pp collisions with enlarged canonical volume

ratio of yields to pions

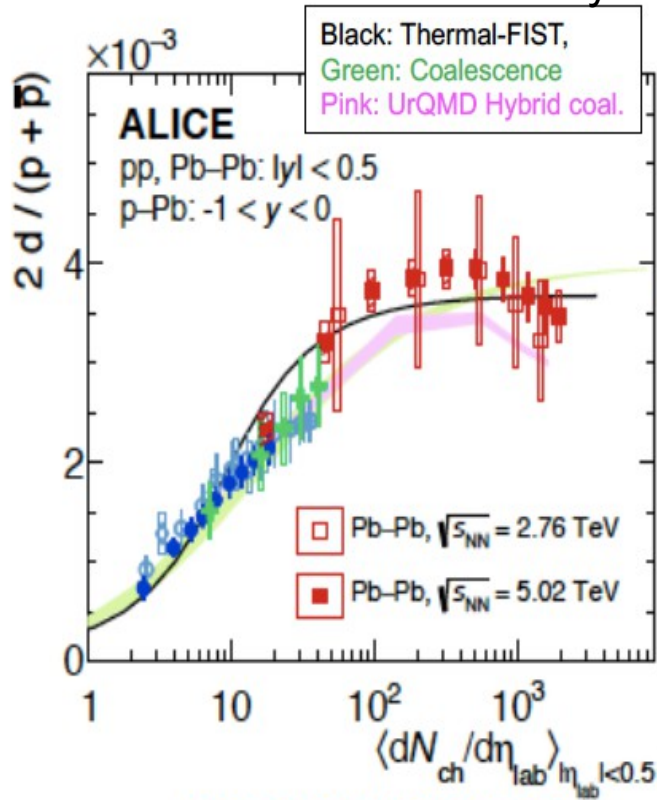


Cleymans, Lo, Redlich, Sharma, Phys.Rev.C 103 (2021) 1, 014904, 2009.04844 [hep-ph]

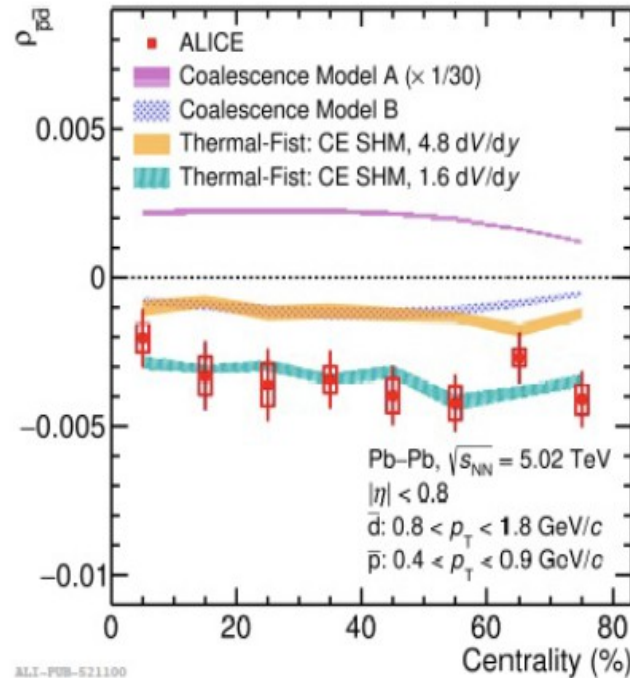
coalescence vs statistical hadronization (SHM)

for deuteron production, both work equally well in Pb-Pb collisions, but no wave function info is needed in SHM

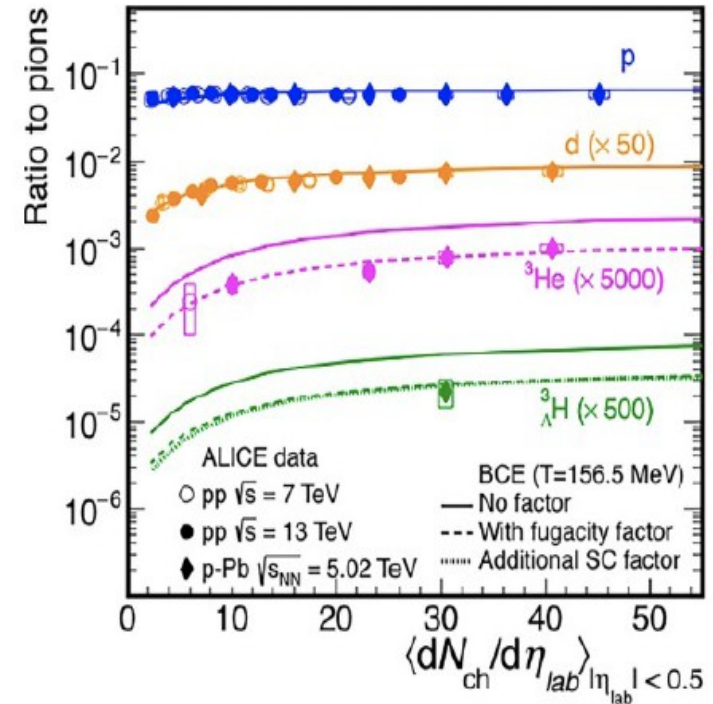
for ^3He and hyper-triton, an additional fugacity factor is needed for the description of results from small systems in SHM



ALICE, PRC 107, 064904 (2023)



ALICE, PRL 131, (2023) 041901



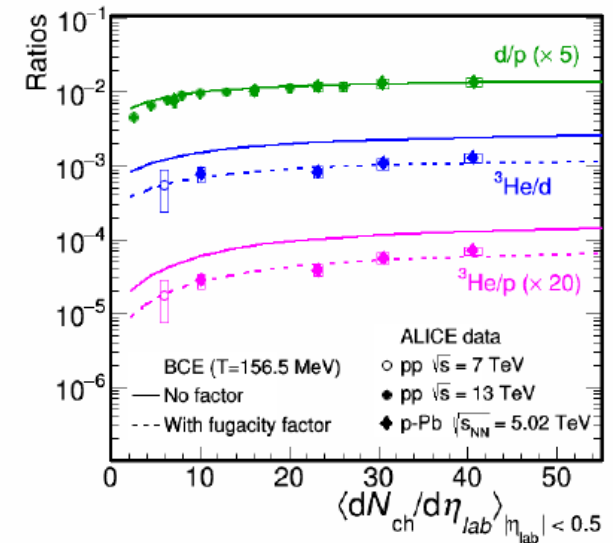
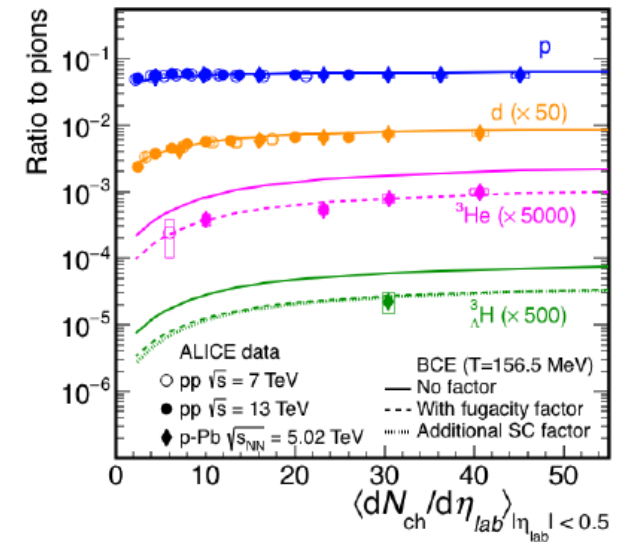
N. Sharma, K. Redlich et al., PRC107, 054903 (2023)

SHM and small systems – nuclei and hypernuclei

N. Sharma et al.,
Phys. Rev.C 107 (2023) 5, 054903

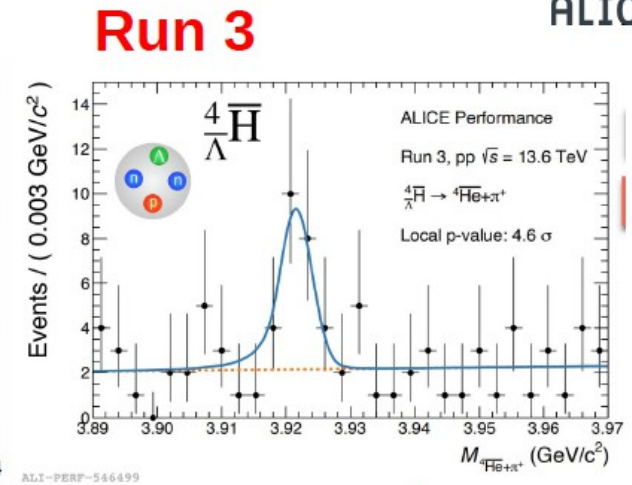
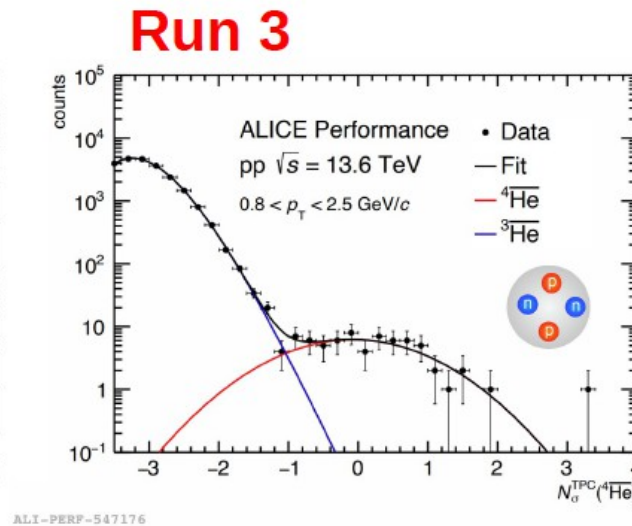
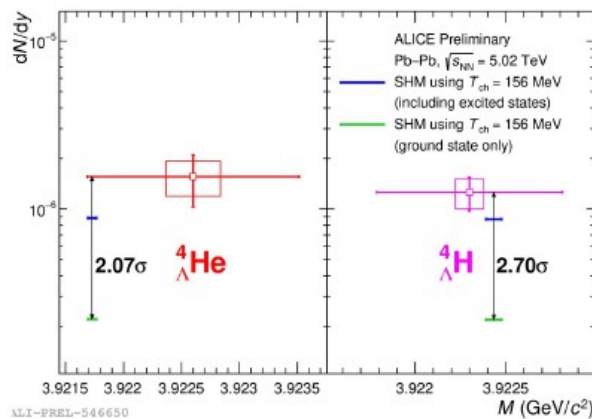
for ${}^3\text{He}$ and t production and $dN_{\text{ch}}/d\eta < 50$ a
fugacity $\lambda = 0.45 \pm 0.03$ is required,
independent of the exact value of $dN_{\text{ch}}/d\eta$

is this an indication of chemical non-
equilibration?



new results from ALICE reported at the Quark Matter 2023 conference

(Anti-)(hyper-)nuclei measurements

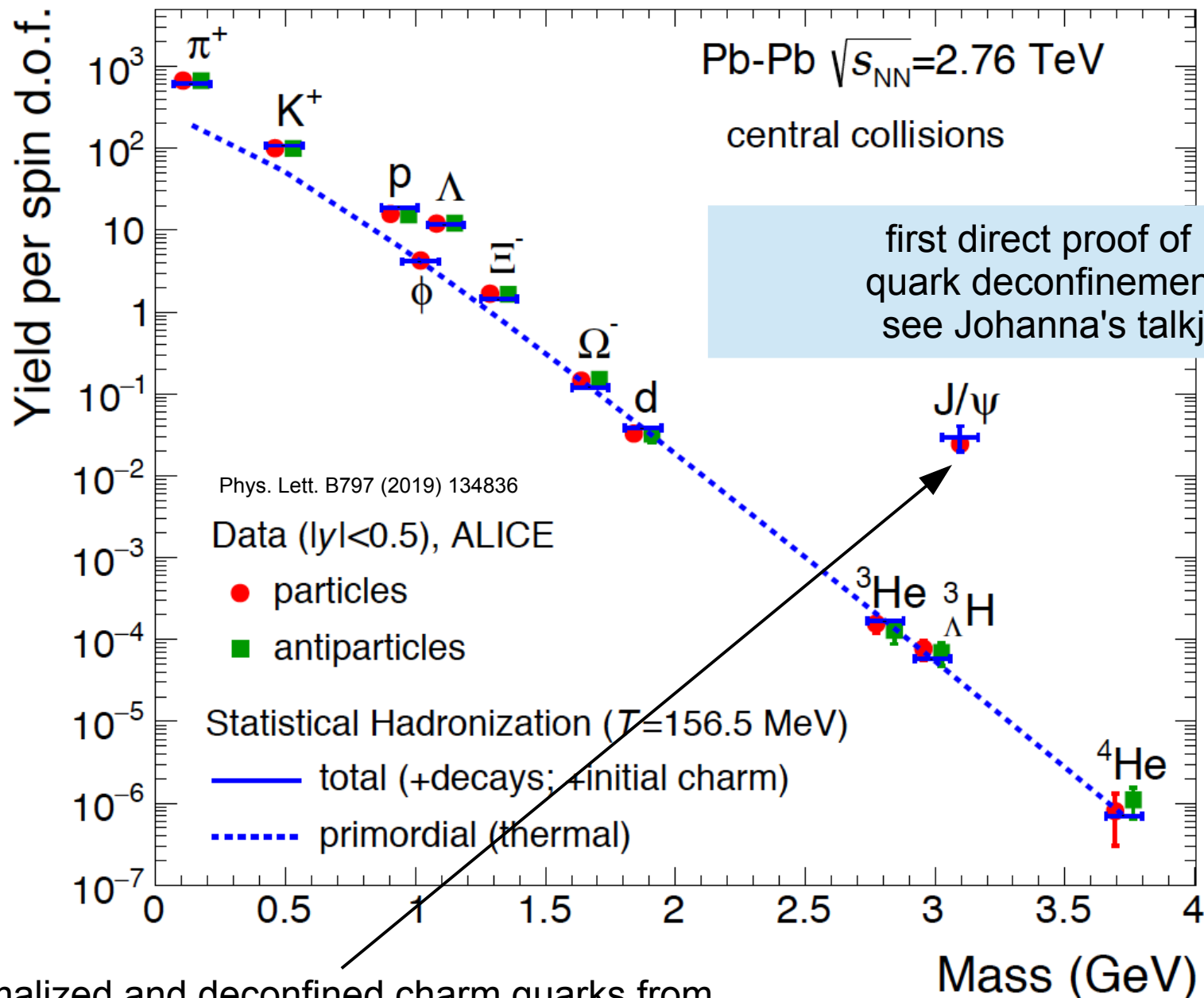


yields of $A = 4$ hypernuclei in Pb-Pb collisions very well reproduced in SHM
once excited states are taken into account

some considerations on bound state formation in relativistic nuclear collisions

- in general, bound states have finite formation time t_F
- bound state formation is a quantum mechanical process
- $t_F = 1/E_B$ as guideline
- for deuteron production, $E_B = 2.2$ MeV and $t_F = 90$ fm $\gg$ collision time
- for hyper-triton, use 'molecular structure' d- Λ
 $t_F = 1/0.13$ MeV = 1500 fm
- sudden approximation as used in coalescence models inappropriate
- loosely bound state cannot be described in multiple collision models, see
e.g. Oliinychenko et al.,
Phys.Rev.C 103 (2021) 3, 034913, 2009.01915 [hep-ph]

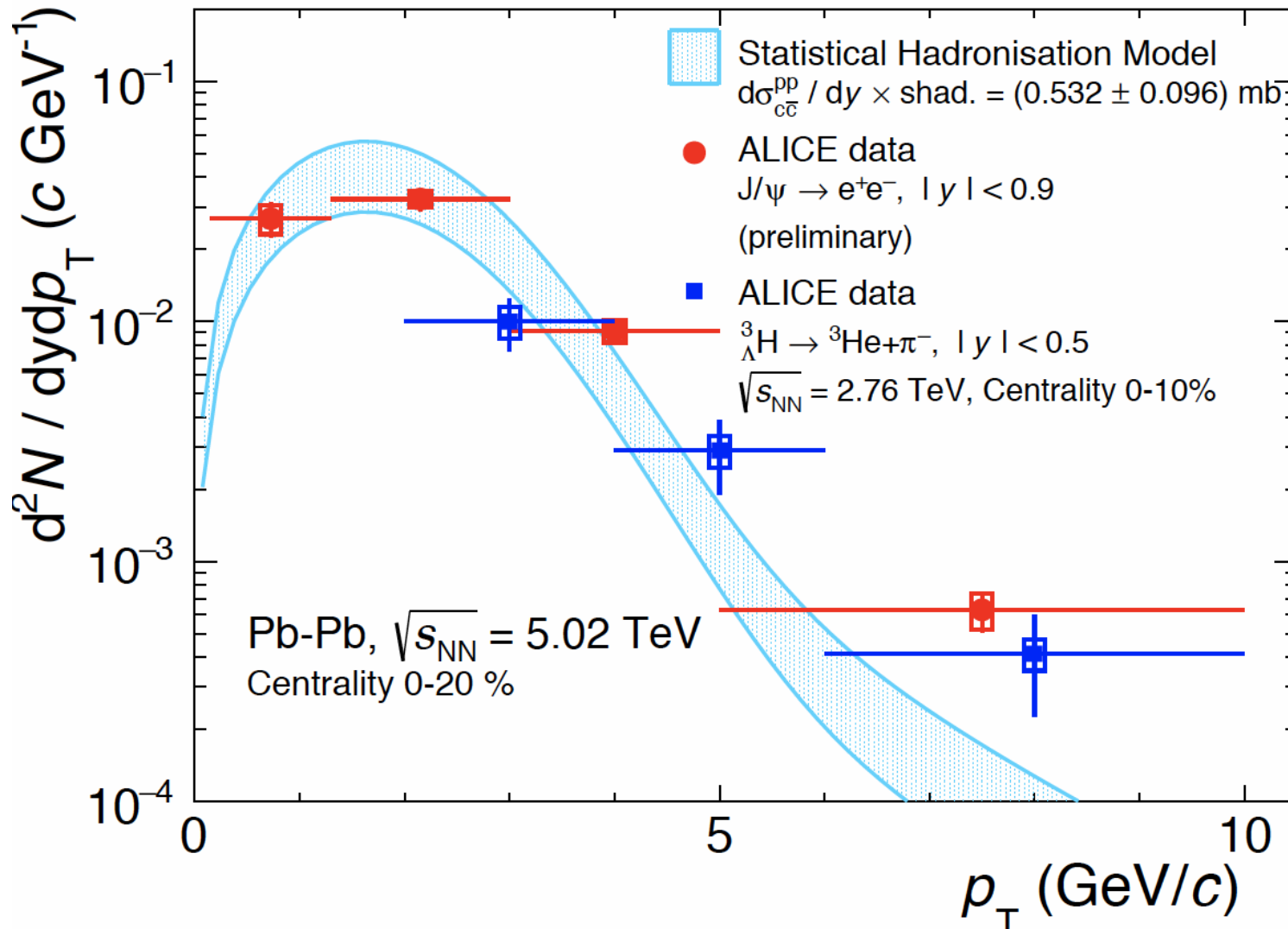
**an unexpected surprise:
production yields and spectra of loosely bound and strongly
bound objects simultaneously described in the SHM**



with thermalized and deconfined charm quarks from
initial hard scattering

Andronic, pbm, Koehler, Redlich, Stachel,
Phys. Lett B797 (2019) 134836

J/ψ and hyper-triton yields described with the same flow parameters in the statistical hadronization model



binding energies:
 J/ψ 600 MeV
 hypertriton 2.2 MeV
 Lambda S.E. 0.13 MeV

from review: hypernuclei and other loosely bound objects produced in nuclear collisions at the LHC,
 pbm and Benjamin Doenigus,
 Nucl. Phys. A987 (2019) 144, arXiv:1809.04681

**how are loosely bound states produced in
high energy nuclear collisions?**

**doorway state hypothesis:
all nuclei and hyper-nuclei, penta-quark and T,X,Y,Z states
are formed as virtual, compact multi-quark states at the
phase boundary. Then slow time evolution into hadronic
representation. Excitation energy about 20 MeV, time
evolution about 10 fm/c**

Andronic, pbm, Redlich, Stachel
Nature 561 (2018) 321, arXiv :1710.09425

how can this be tested?

precision measurement of spectra and flow pattern for light
nuclei and hyper-nuclei, multi-charm hadrons, penta-quark and
X,Y,Z states from pp via pPb to Pb-Pb

**a major new opportunity for ALICE Run3/4
and beyond 2030 for X,Y,Z, T_{cc} and penta-quark states**

**also new opportunities for
GSI/FAIR and JINR/NICA
experiments**

summary and outlook

quantitative description of hadron production including loosely bound states
in Pb-Pb and Au-Au collisions with SHM

all hadrons are produced very close to the QCD phase boundary

universal hadronization at temperature $T = T_{\text{chem}}$ with T_{chem} as single parameter

for composite hadrons, SHM and coalescence approach works well
provided that excited states are included in the description, details of wave functions
important for coalescence approach

for production from small systems (pp, pPb, ...) SHM with canonical thermodynamics is
needed, correlation volume is under investigation

much new information expected with upgraded detectors in LHC Run 3 and Run 4