

$Z_c(3900)$ as a tetraquark

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R. Faccini, L. Maiani, F. Piccinini, AP, A.D. Polosa, V.Riquer
arXiv:1303.6857

Outline

- Charged $Z_c(3900)$
- Tetraquark hypothesis
- Decay channels
- Other models
- Conclusions

Charged $Z_c(3900)$

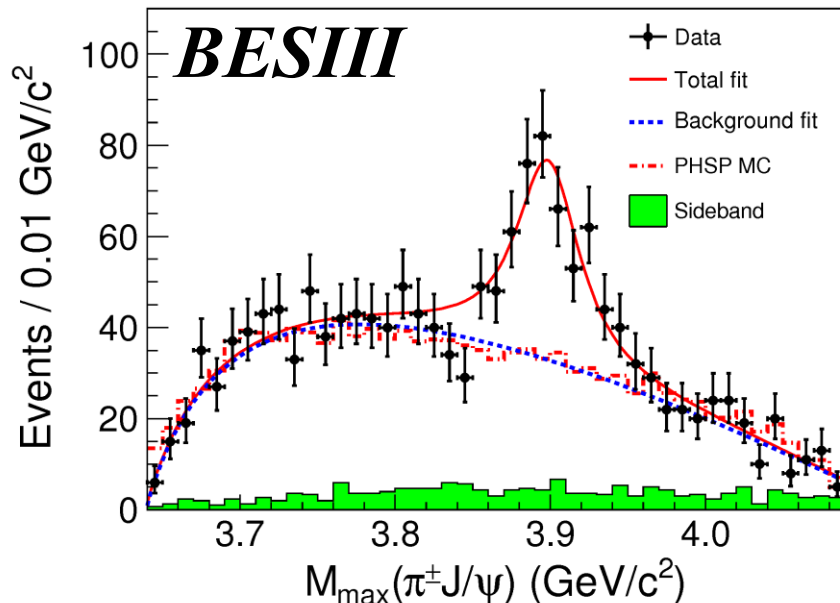
Found in $Y(4260) \rightarrow Z_c^\pm(3900) \pi^\mp \rightarrow J/\psi \pi^\pm \pi^\mp$

Exotic charged charmonium-like state!

BESIII, arXiv:1303.5949

$$M = 3899.0 \pm 3.6 \pm 4.9 \text{ MeV}$$

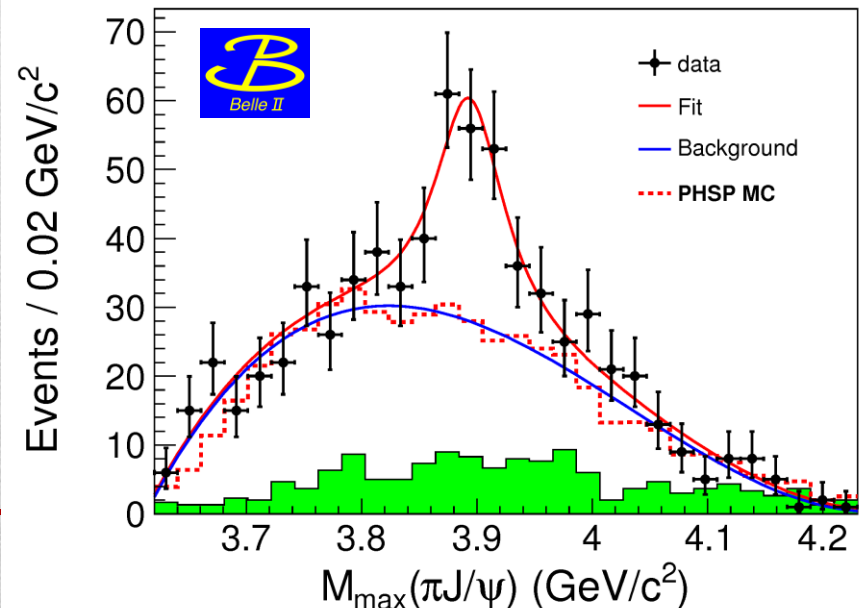
$$\Gamma = 46 \pm 10 \pm 20 \text{ MeV}$$



Belle, arXiv:1304.0121

$$M = 3894.5 \pm 6.6 \pm 4.5 \text{ MeV}$$

$$\Gamma = 63 \pm 24 \pm 26 \text{ MeV}$$



Quantum numbers

From the decay $Y \rightarrow Z_c \pi \rightarrow J/\psi \pi\pi$ we know $I^G J^P = 1^{+??}$

For a S-wave decay, $I^G J^{PC} = 1^+ 1^{+-}$

For a P-wave decay, $I^G J^{PC} = 1^+ (0,1,2)^{--}$

C is defined for the neutral Z_c^0

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Similarly to $X(3872)$ with $J^{PC} = 1^{++}$,
a signature $J^P = 1^+$ is favored by models

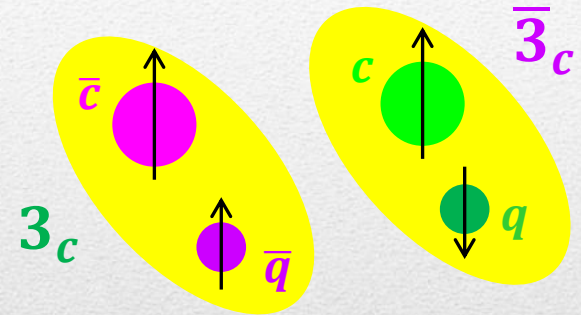
C is defined for the neutral Z_c^0

Tetraquark

One of the models for the **X(3872)** is a compact **diquark-antidiquark bound state**

$$[cq]_{s=0}[\bar{c}\bar{q}]_{s=1} + h.c.$$

Maiani *et al.* PRD71 014028



We can evaluate mass spectrum in a constituent quark model

$$H = -2 \sum_{i < j} \kappa_{ij} \vec{S}_i \cdot \vec{S}_j \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$

Tetraquark

$\kappa_{\bar{q}Q}$ from meson spectrum:

$\pi, \rho, D, D^*, \eta_c, J/\psi$

$$\kappa_{c\bar{q}} = 17.5 \text{ MeV}$$

$$\kappa_{c\bar{c}} = 15.0 \text{ MeV}$$

$$\kappa_{q\bar{q}} = 77.5 \text{ MeV}$$

κ_{qQ} from baryon spectrum:

$\Lambda_c, \Sigma_c, p, \Delta^+$

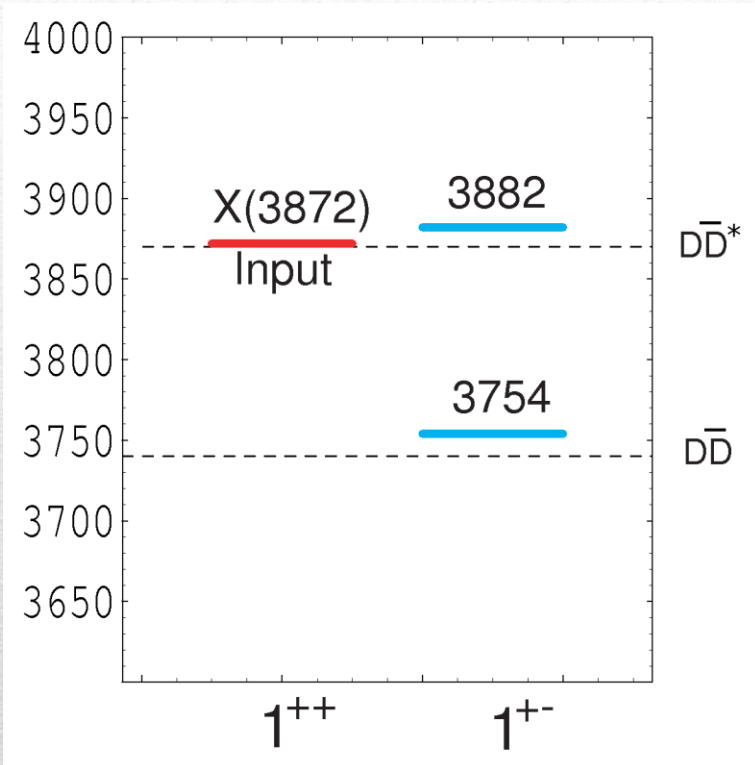
$$\kappa_{cq} = 13.5 \text{ MeV}$$

But the mass of **constituent diquark** is unknown

We impose the 1^{++} state to be the $X(3872)$

and get $m_{\mathbf{q}} = 1933 \text{ MeV}$

Tetraquark



We can combine
S=0 and S=1 diquarks
to get **3 vector states**:

$$\begin{array}{ll}
 1^{++} & \frac{1}{\sqrt{2}} (|0, 1\rangle + |1, 0\rangle) \\
 1^{+-} & \frac{1}{\sqrt{2}} (|0, 1\rangle - |1, 0\rangle) \\
 1^{+-} & |1, 1\rangle
 \end{array}
 \left. \vphantom{\begin{array}{l} 1^{++} \\ 1^{+-} \\ 1^{+-} \end{array}} \right\} \text{mix}$$

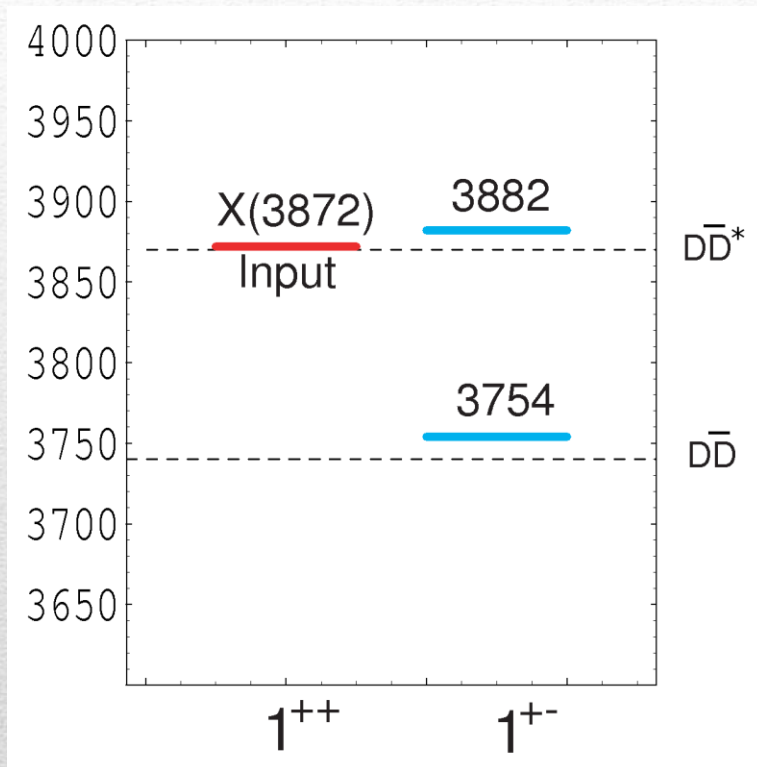
Tetraquark

1^{+-} state at 3882 MeV
compatible with $Z_c(3900)$!

Prevision for other states:

- Neutral $I^G = 1^+$ partner
~ 3900 MeV
- Neutral $I^G = 0^-$ partner
~ 3900 MeV
- Charged/neutral 1^{+-} states
~ 3755 MeV

Look for a $Z'_c(3760)$ about ~ 100 MeV below $Z_c(3900)$

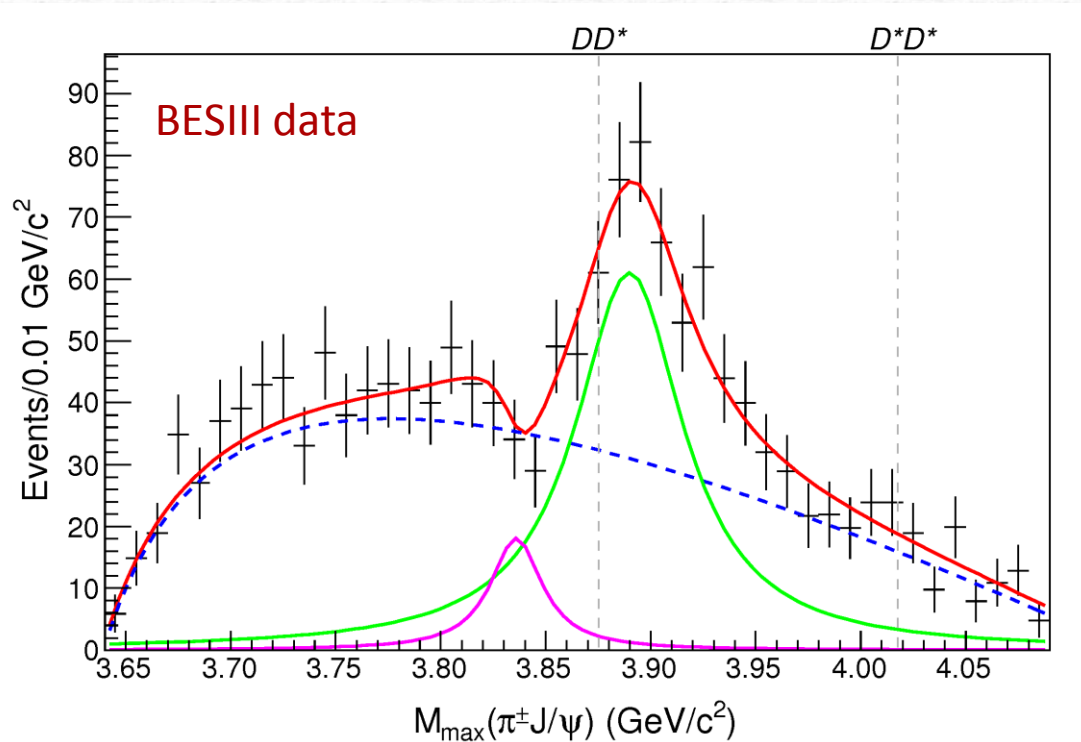


Combined BES-Belle fit

Faccini, Maiani, Piccinini, AP, Polosa,
Riquer arXiv:1303.6857

Is there room for a lighter resonance?

Combined BES-Belle fit



Faccini, Maiani, Piccinini, AP, Polosa,
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$$Z_c \quad \begin{aligned} M &= 3898 \pm 6 \text{ MeV} \\ \Gamma &= 62 \pm 12 \text{ MeV} \end{aligned}$$

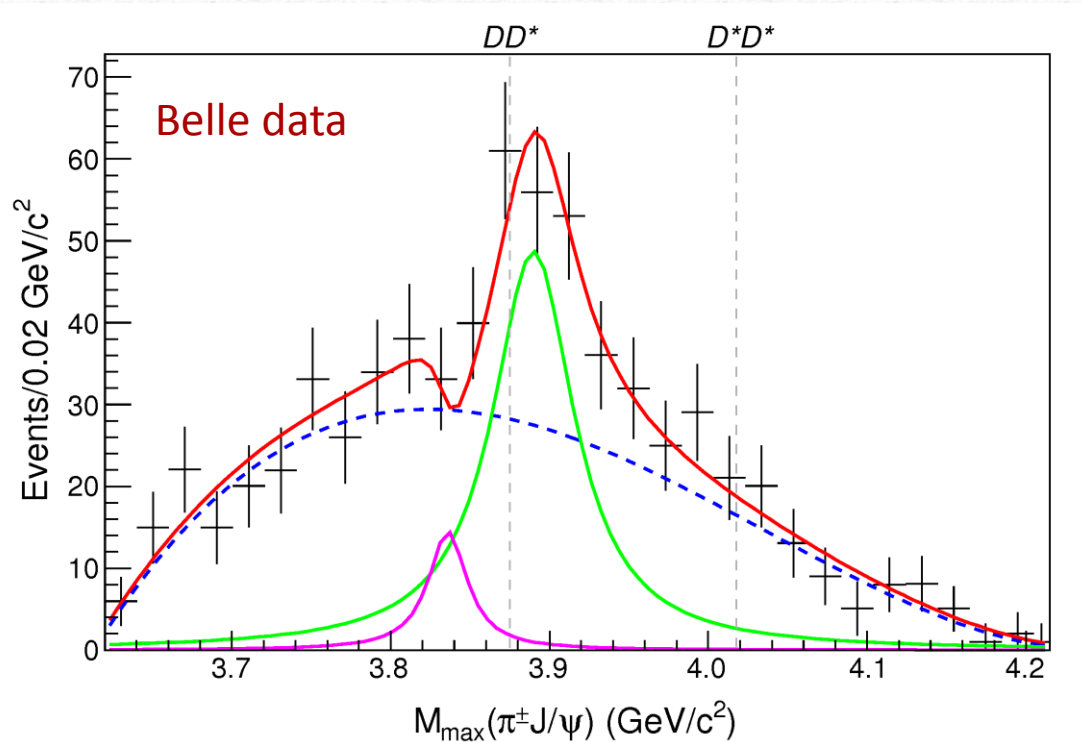
$$Z'_c \quad \begin{aligned} M' &= 3836 \pm 13 \text{ MeV} \\ \Gamma' &= 30 \pm 18 \text{ MeV} \end{aligned}$$

$$\Delta\phi = (109 \pm 30)^\circ$$

$$\chi^2/\text{DOF}=41/65, CL = 99.0\%$$

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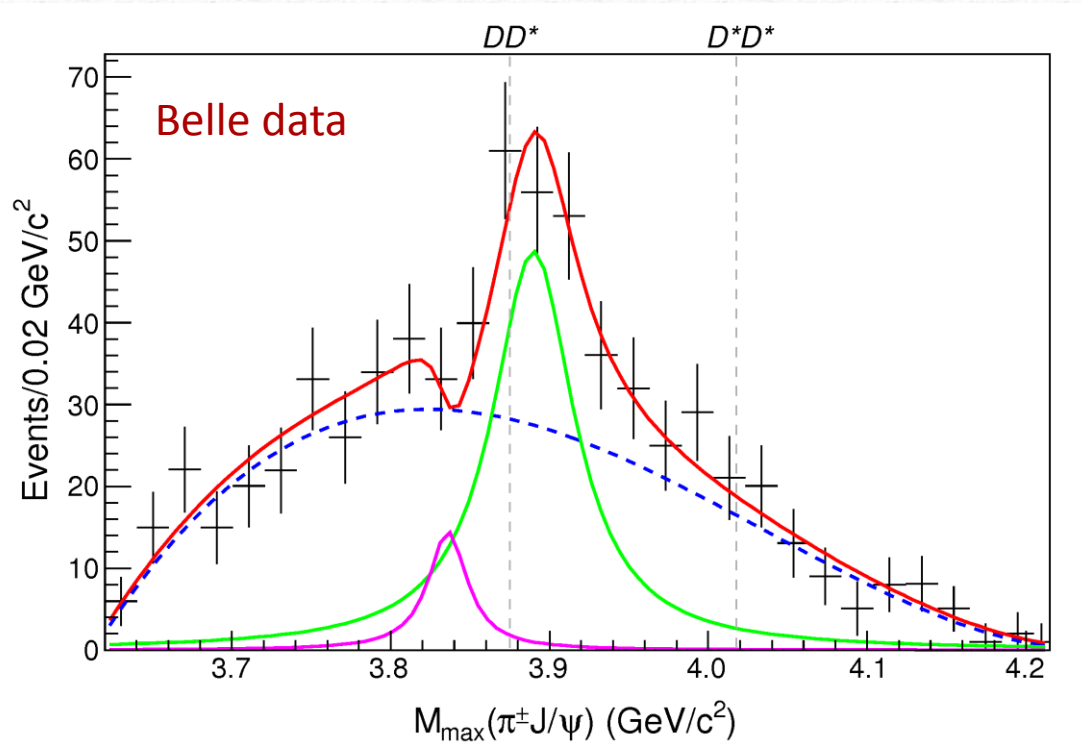
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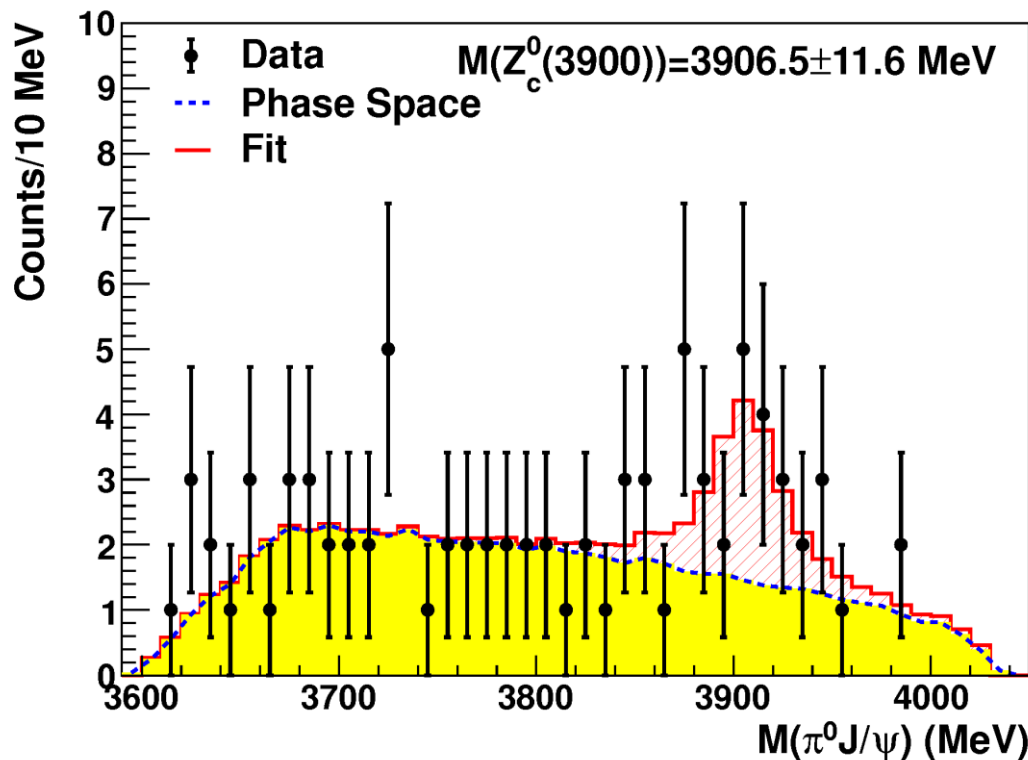
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Just a hint, but... could it be the $Z'_c(3760)$?

$Z_c^0(3900)$ at CLEO?

A reanalysis of CLEO data shows a 3σ neutral resonance in

$$\psi(4160) \rightarrow \pi^0 Z_c^0 \rightarrow J/\psi \pi^0 \pi^0$$



Xiao et al.
arXiv:1304.3036

$$M = 3907 \pm 12 \text{ MeV}$$
$$\Gamma = 34 \pm 29 \text{ MeV}$$

Isospin violation?
Look for $Z_c^0 \rightarrow J/\psi \eta$

Decay channels

Two questions:

- What can $Z_c(3900)$ decay into?
- Why is $Z_c(3900)$ much broader than $X(3872)$?

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- $J/\psi \pi^+$
- $\psi(2S)\pi^+$
- $D^+ \overline{D^{*0}}, D^{*+} \overline{D^0}$
- $\eta_c \rho^+$
- $h_c \pi^+$ in P-wave
- Radiative decays

Allowed by HQSS if $Z_c(3900)$
contains a $S = 0 \ c\bar{c}$ component

} suppressed

Decay channels

Two questions:

- What can $Z_c(3900)$ decay into?
 - Why is $Z_c(3900)$ much broader than $X(3872)$?
- $J/\psi \pi^+$
 - $\psi(2S)\pi^+$
 - $D^+ \overline{D^{*0}}, D^{*+} \overline{D^0} \sim 4 \text{ MeV}$
 - $\eta_c \rho^+$
 - $h_c \pi^+$ in P-wave
 - Radiative decays

We suppose

$$g_{DD^*X(3872)} = g_{DD^*Z(3900)}$$

Decay channels

Two questions:

- What can $Z_c(3900)$ decay into?
- Why is $Z_c(3900)$ much broader than $X(3872)$?

- $J/\psi \pi^+ \sim 29 \text{ MeV}$
- $\psi(2S)\pi^+ \sim 6 \text{ MeV}$
- $D^+ \overline{D^{*0}}, D^{*+} \overline{D^0} \sim 4 \text{ MeV}$
- $\eta_c \rho^+ \sim 19 \text{ MeV}$
- $h_c \pi^+$ in P-wave
- Radiative decays

No grounds for other couplings

We only suppose

$$g = M_{Z_c}$$

Some agreement with QCD sum rules

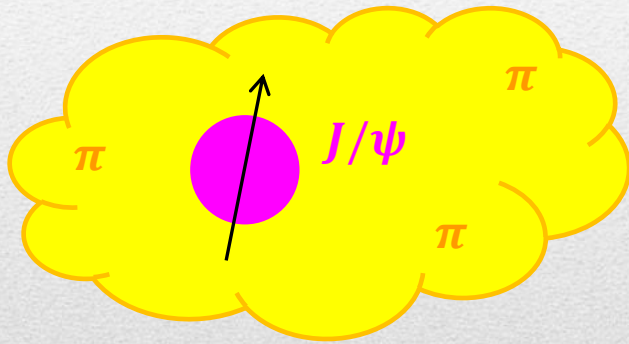
Dias *et al.* arXiv:1304.6433

$\Gamma \sim 60 \text{ MeV}$, agrees with experimental value

Other models

Hadro-charmonium

Voloshin arXiv:1304.0380



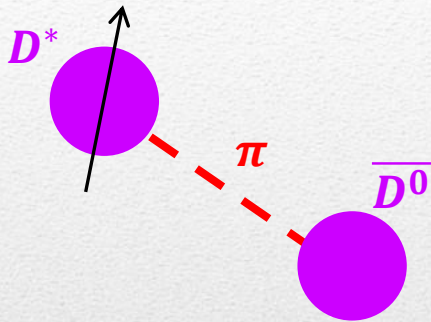
A $c\bar{c}$ state surrounded by light matter

Decay into $\eta_c \rho$ forbidden by HQSS

A light $Z'_c(3785)$ expected with $I^G J^{PC} = 1^- 0^{++}$
(not visible in $J/\psi \pi$ channel)

Other models

Molecule



Wang *et al.* arXiv:1303.6355

DD^* loosely bound molecule

$1-\pi$ exchange attractive in $I^C = 1^-$ channel,
although less than in $I^C = 0^+$ ($X(3872)$)

Tornqvist Z.Phys. C61 525-537

A molecule decays mostly **into its constituents**
(long range decay)

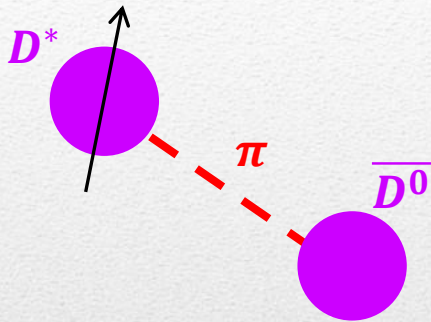
Decays into **charmonium + light mesons**
suppressed by $1/a$ (short range decay)

Braaten *et al.* PRD69, 074005

e.g. $BR(X(3872) \rightarrow DD^*) \sim 70\%$, $BR(X(3872) \rightarrow J/\psi \rho) \sim 5\%$

Other models

Molecule



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$1-\pi$ exchange attractive in $I^C = 1^-$ channel,
although less than in $I^C = 0^+$ ($X(3872)$)

Tornqvist Z.Phys. C61 525-537

Expected with $\text{BR}(Z_c \rightarrow DD^*) \sim 70\text{-}80\%$

But we estimated $\Gamma(Z_c \rightarrow DD^*) \sim 4 \text{ MeV}$,

How to reach $\Gamma = 40 \text{ MeV}$?

A light $Z'_c(3760)$ expected with $I^G J^{PC} = 1^- 0^{++}$

A heavy $Z''_c(4020)$ expected at $D^* D^*$ threshold

Voloshin

PRD 84, 031502

Other models

Molecule

$Z_c^0(3900)$ could violate isospin just like $X(3872)$

A $Y(4260) \rightarrow Z_c^0 \pi^0 \rightarrow J/\psi \eta \pi^0$ could occur

If so, it cannot be accommodated into molecular picture:

In $X(3872)$ isospin violation is due to

$$\Delta = M(D^+ D^{*-}) - M(D^0 D^{0*}) \sim 8 \text{ MeV}$$

Hanhart *et al.* PRD85 011501

Z_c^0 is above both thresholds, and $\Delta \ll \Gamma$

In molecular picture Z_c^0 should be a pure isovector

Conclusions

A $Z_c(3900)$ with $I^G J^{PC} = 1^+ 1^{+-}$ is compatible
with different models (tetraquark, molecule, hadro- $c\bar{c}$)

Conclusions

A $Z_c(3900)$ with $I^G J^{PC} = 1^+ 1^{+-}$ is compatible with different models (tetraquark, molecule, hadro- $c\bar{c}$)

To establish its nature, we need:

- Quantum numbers
- Decay channels (DD^* , $J/\psi \eta$, $\eta_c \rho$)
- Looking for a lighter partner 3750-3850 MeV in both $G = \pm$ channels
- Looking for a heavier partner at ~ 4020 MeV

Thank you

BACKUP

Strong couplings

How do we evaluate $g_{DD^*X(3872)}$?

$$g_{DD^*X(3872)}^2 = BR(X \rightarrow DD^*) \Gamma_X \left(\frac{p^*}{8\pi M_X^2} \overline{|M(X \rightarrow DD^*)|^2} \right)^{-1}$$

But if $M_X < M_D + M_{D^*}$ the decay momentum p^* is undefined

We average over a random set $(M_X)_i$, distributed as a Breit-Wigner, centered at $M_X = 3872$ MeV and with a width $\Gamma_X = 1.2$ MeV respecting the kinematical limits

$$M_D + M_{D^*} < (M_X)_i < M_B - M_K$$

We get $g_{DD^*X(3872)} = 2.5 \text{ GeV}$

Strong couplings

The matrix element can be evaluated in an effective theory

$$\langle D(p) D^*(\eta, q) | X(\lambda, P) \rangle = g_{DD^*X} \eta \cdot \lambda$$
$$\frac{1}{3} \sum_{\text{pol}} |\langle D(p) D^*(\eta, q) | X(\lambda, P) \rangle|^2 = \frac{1}{3} g_{DD^*X}^2 \left(3 + \frac{p^{*2}}{M_X^2} \right)$$

The D-wave component is negligible with respect to the S-wave one

We get $g_{DD^*X(3872)} = 2.5 \text{ GeV}$

Strong couplings

What about other couplings?

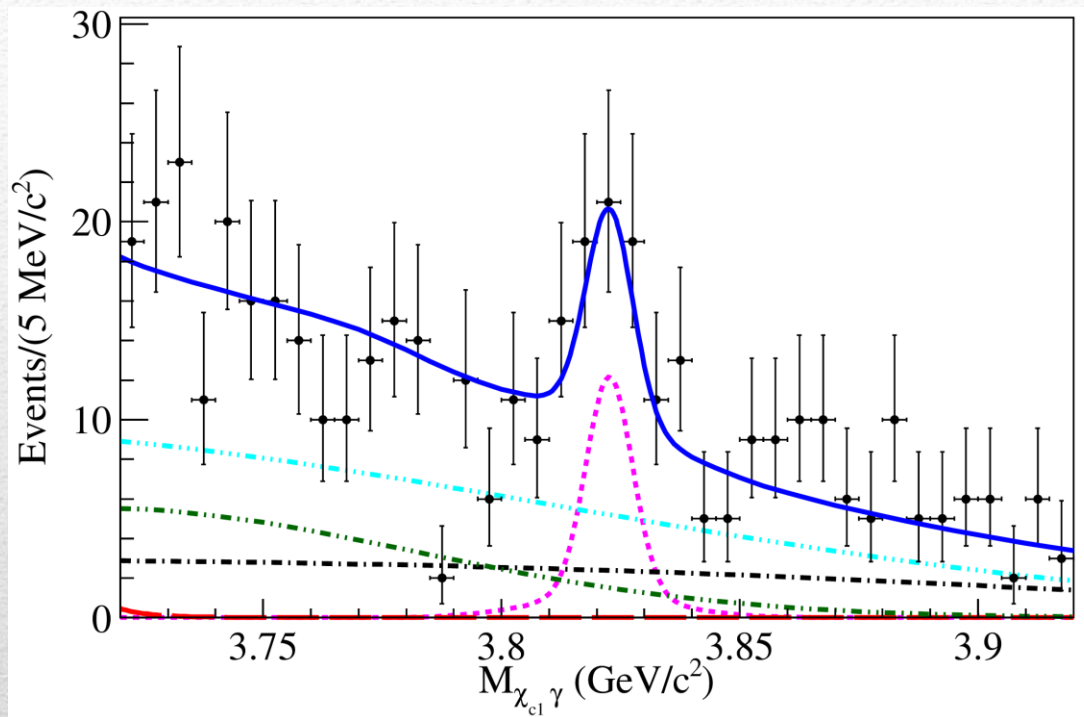
We cannot relate $g_{X\psi\rho}$ to $g_{Z_c\psi\pi}$
(no chiral symmetry or HQSS)

But we are talking about **S-wave decays**
and we need couplings with the **dimension of a mass**

The main **mass scale** is the **mass of the $Z_c(3900)$**
So we estimate

$$g \sim M_{Z_c} \sim 3900 \text{ MeV}$$

$$Z'_c \rightarrow \chi_{c1} \gamma?$$



Belle arXiv:1304.3975

$$M = 3823.1 \pm 1.8 \pm 0.7 \text{ MeV}$$

$$\Gamma < 24 \text{ MeV}$$

Proposed a 2^{--} signature (identified as $\psi_2(1D)$),
but **could be** 1^{+-} if the decay is in P-wave

Could be the neutral partner of Z'_c ?