



Hidden-charm pentaquarks

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Interpretation of the LHCb P_c states as Hadronic Molecules and Hints of a Narrow $P_c(4380)$

Revisiting the nature of the P_c states

Prompt production of the hidden charm pentaquarks in the LHC

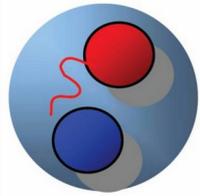
Insights into the nature of the $P_c(4459)$

Deciphering the mechanism of near-threshold J/ψ photoproduction

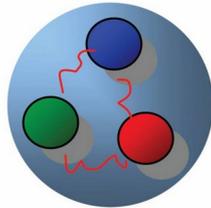
In preparation

Conventional hadrons vs. Exotic hadrons

Conv. Hadrons



meson

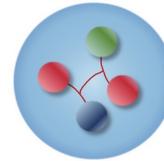


baryon

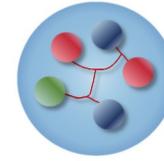
Hundreds of hadrons can be described as $q\bar{q}$ and qqq states

Exotic Hadrons

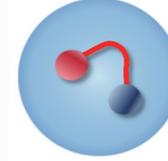
Tetraquark



Pentaquark



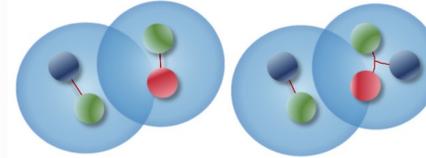
Hybrid



Glueball



Hadronic molecule



Volume 8, number 3 PHYSICS LETTERS 1 February 1964

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN
California Institute of Technology, Pasadena, California

Received 4 January 1964

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon b if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqq\bar{q})$ etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assumed that the lowest baryon configuration (qqq) gives just the representations 1, 8, and 10 that have been observed, while

21 February 1964

AN SU_3 MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

II *)

G. Zweig
CERN---Geneva

*) Version I is CERN preprint 8182/TH.401, Jan. 17, 1964.

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6) In general, we would expect that baryons are built not only from the product of three aces, AAA , but also from $\bar{A}AAAA$, $\bar{A}AAAAA$, etc., where \bar{A} denotes an anti-ace. Similarly, mesons could be formed from $\bar{A}A$, $\bar{A}AA$ etc. For the low mass mesons and baryons we will assume the simplest possibilities, $\bar{A}A$ and AAA , that is, "deuces and treys".

The multiquark states were predicted at the birth of Quark Model.

The experimental and theoretical study of such states is a key to understand QCD

Light-flavor Pentaquarks

- **$\Lambda(1405)$** $[ud\bar{s}]$

- 1959: $\bar{K}N$ molecule predicted by Dalitz-Tuan, PRL2,425
- 1961: $\Lambda(1405) \rightarrow \Sigma\pi$ observed by Alston et al., PRL6, 698
- 1995: $\bar{K}N$ dynamically generated, by Kaiser et al., NPA954, 325
- 2001: two-pole structure by $\bar{K}N - \Sigma\pi$ by Oller et al., PLB500, 263

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... on two-pole structure, eg. Meißner, Symmetry12,981(2020),
Xie et al., PRD108, L111502...

- **$\theta^+(1540)$** $[uudd\bar{s}]$

- 1997: predicted w/ chiral soliton model by Diakonov et al., ZPA359, 305
- 2003: $\theta^+(1540) \rightarrow K^+n$ by LEPS, PRL91, 012002
- 2004: appear on Review of Particle Physics (RPP) by PDG, supported by many exp.
- 2005: not supported by many high stats exp.
- 2006: removed from RPP by PDG

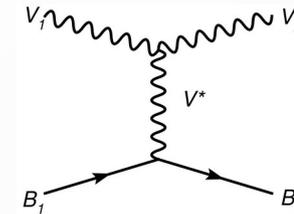
Hidden-charm Pentaquarks: Predictions

2006: SU(4)+unitarity, by Hofmann et al., NPA776,17-51

(I, S)	State	M_R [MeV]	$ g_R $
		Γ_R [MeV]	
$(\frac{1}{2}, 0)$	$\pi \Delta$	3430	0.05
	$K \Sigma$	0.50	0.04
	$\bar{D} \Sigma_c$		5.6
$(0, -1)$	$\pi \Sigma$	3538	0.04
	$K \Xi$	0.63	0.05
	$\bar{D} \Xi_c$		5.6

2010: local hidden gauge + unitarity, by J.J. Wu et al., PRL105, 232001

(I, S)	M	Γ	Γ_i				
$(1/2, 0)$			πN	ηN	$\eta' N$	$K \Sigma$	$\eta_c N$
$\bar{D} \Sigma_c$	4261	56.9	3.8	8.1	3.9	17.0	23.4
$(1/2, 0)$			ρN	ωN	$K^* \Sigma$		$J/\psi N$
$\bar{D}^* \Sigma_c$	4412	47.3	3.2	10.4	13.7		19.2



$$T = [1 - VG]^{-1}V$$

2012: One-boson-exchange model ($\pi, \eta, \rho, \omega, \sigma$) + Schrödinger Eq., by Z.C. Yang et al., CPC36, 6

$$\leftrightarrow \bar{D} \Sigma_c(1/2^-), \bar{D}^* \Sigma_c(1/2^-, 3/2^-): 0 \sim 50 \text{ MeV}$$

2013: HQSS + local hidden gauge + unitarity, by C.W. Xiao et al., PRD88, 56012

$$\leftrightarrow \bar{D} \Sigma_c(1/2^-), \bar{D} \Sigma_c^*(3/2^-), \bar{D}^* \Sigma_c(1/2^-, 3/2^-), \\ \bar{D}^* \Sigma_c^*(1/2^-, 3/2^-, 5/2^-): \text{binding energy} \sim 50 \text{ MeV}$$

Chiral quark model, W.L. Wang et al., PRC84, 015203 (2011)
 Hyperfine interaction, S.G. Yuan et al., EPJA48, 61 (2012)

Review papers:

H.X. Chen, et al., Phys. Rept. 639, 1 (2016)

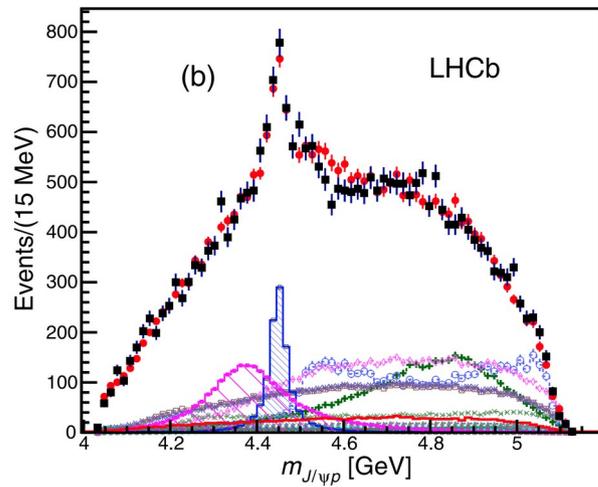
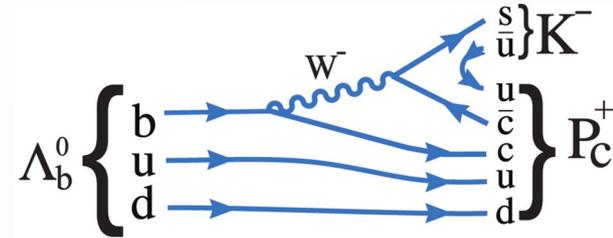
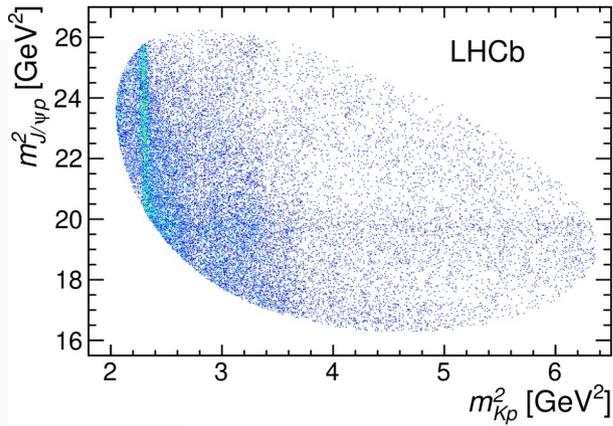
F.K. Guo, et al., Rev.Mod.Phys.90,015004(2018)

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Charmonium-pentaquark states (I)

Observation of exotic structures (P_c) in $\Lambda_b^0 \rightarrow J/\psi p K^-$

LHCb, PRL 115, 072001 (2015)



$$P_c(4380)^+ : M = 4380 \pm 8 \pm 29 \text{ MeV}$$

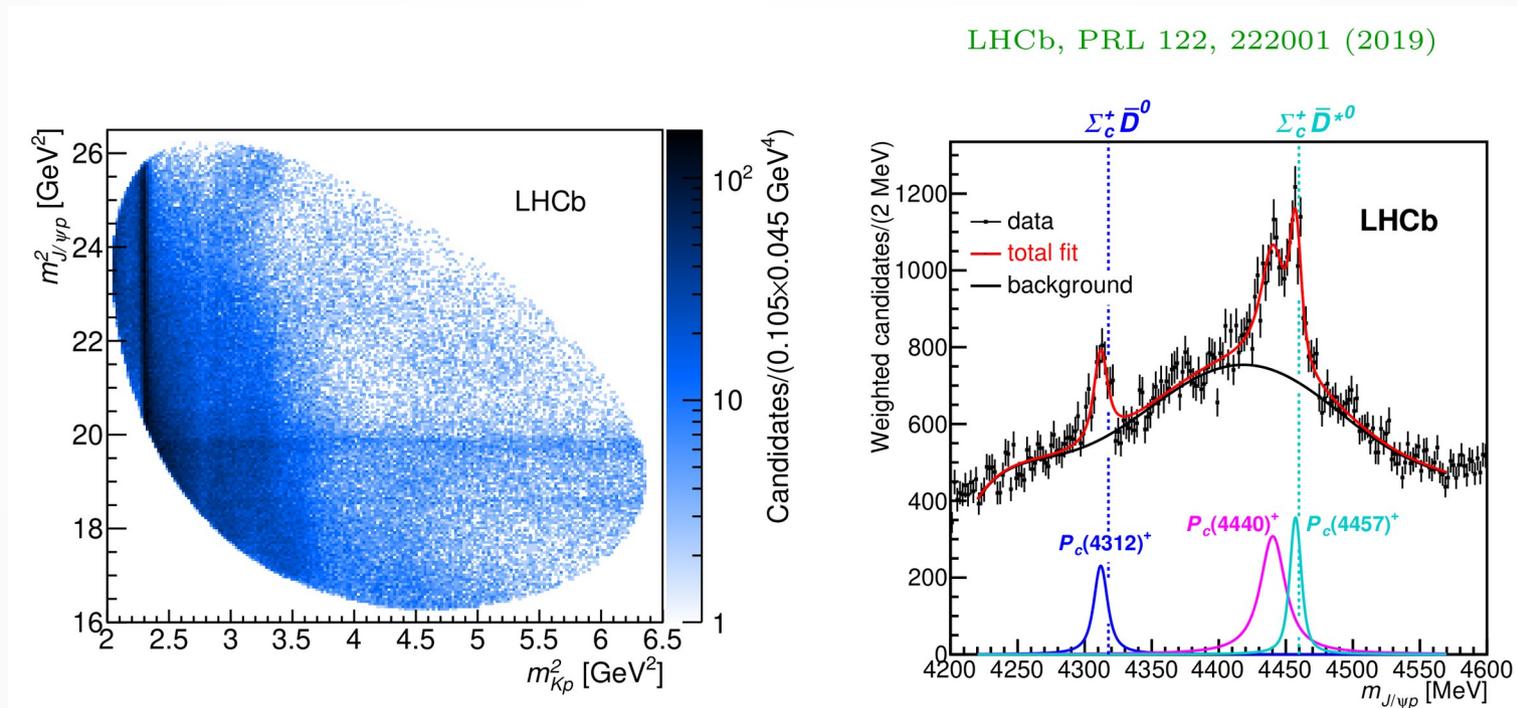
$$\Gamma = 205 \pm 18 \pm 86 \text{ MeV}$$

$$P_c(4450)^+ : M = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$$

$$\Gamma = 39 \pm 5 \pm 19 \text{ MeV}$$

Preferred Parity: Opposite

Charmonium-pentaquark states (II)

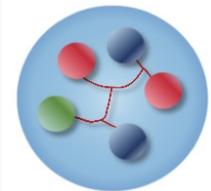


the $P_c(4440)^+$ and $P_c(4457)^+$ states. The six-dimensional amplitude analysis reported in Ref. [9], which provided evidence for the $P_c(4380)^+$ state, is also obsolete since it used the single $P_c(4450)^+$ state and it lacked the $P_c(4312)^+$ state. Therefore, the results presented in the Letter weaken the previously reported evidence for the $P_c(4380)^+$ state, but do not contradict its existence, since the present one-dimensional analysis is not sensitive to wide P_c^+ states. Only a future six-dimensional amplitude analysis of $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays that includes the $P_c(4440)^+$, $P_c(4457)^+$, and $P_c(4312)^+$ states will be able to determine if there is still evidence for the $P_c(4380)^+$ state or any other wide P_c^+ states.

$P_c(4450)^+$

State	M [MeV]	Γ [MeV]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$

Proposals [after 2019]



Compact Pentaquark

Chromomagnetic model, JB Cheng and YR Liu, PRD100, 054002 (2019)

$$P_c(4312), P_c(4440), P_c(4457): J^P = 3/2^-, 1/2^-, 3/2^-$$

$P_c(4380)^+, P_c(4440)^+$ and $P_c(4457)^+$ is $\frac{3}{2}^-$ R. Deng, PRD105, 116021 (2022)

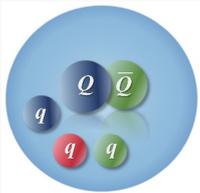
Compact diquark model, Ali et al., JHEP10, 256 (2019)

R. Zhu et al., PLB797, 134869(2019)

Giron et al., JHEP05, 061 (2019)

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$3/2^-$	4240 ± 29
$3/2^+$	4440 ± 35
$5/2^+$	4457 ± 35



Hadron-Charmonium

Compact ($\bar{Q}Q$) surrounded by light quarks

Eides et al., Mod. Phys. Lett. A 35, 2050151 (2020)

$$J^P = 1/2^+, 1/2^-, 3/2^-$$

Hadronic Molecule

Extended object

H.X. Chen et al., PRD100, 051501 (2019)

R. Chen et al., PRD100, 011502 (2019)

F.K. Guo et al., PRD99, 091501 (2019)

M.Z. Liu et al., PRL122, 242001 (2019)

Z.H. Guo et al., PLB793, 144 (2019)

L. Meng et al., PRD100, 014031(2019)

J.J. Wu et al., PRC100, 035026 (2019)

J.-Z. Wu et al., CPL41,091201(2024)

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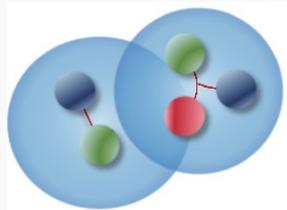
Kinematic effect

Kuang et al., EPJC80,433 (2020)

Nakamura, PRD103, L111503(2021)

Burns et al., PRD106,054029(2022)

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Heavy Quark Spin Symmetry (HQSS)

- For a heavy-quark Q (charm, bottom) with $m_Q \gg \Lambda_{\text{QCD}}$

☞ chromomag. interaction $\propto \frac{\boldsymbol{\sigma} \cdot \mathbf{B}}{m_Q} \rightarrow 0$: independent of heavy-quark spin

- For a hadron containing a heavy-quark Q : $J = s_Q + j_l$

S -wave baryon-meson system
(ground states)

$$s_Q = \frac{1}{2} \otimes \frac{1}{2} = 0 \oplus 1$$

$$j_l = \frac{1}{2} \oplus \frac{3}{2}$$

LO Contact Interaction: Only 2 LECs

Molecule	J^P	M (MeV)	Molecule	J^P	M (MeV)
A	$\bar{D}\Sigma_c$ $\frac{1}{2}^-$	4311.8 – 4313.0	B	$\bar{D}\Sigma_c$ $\frac{1}{2}^-$	4306.3 – 4307.7
A	$\bar{D}\Sigma_c^*$ $\frac{3}{2}^-$	4376.1 – 4377.0	B	$\bar{D}\Sigma_c^*$ $\frac{3}{2}^-$	4370.5 – 4371.7
A	$\bar{D}^*\Sigma_c$ $\frac{1}{2}^-$	4440.3*	B	$\bar{D}^*\Sigma_c$ $\frac{1}{2}^-$	4457.3*
A	$\bar{D}^*\Sigma_c$ $\frac{3}{2}^-$	4457.3*	B	$\bar{D}^*\Sigma_c$ $\frac{3}{2}^-$	4440.3*
A	$\bar{D}^*\Sigma_c^*$ $\frac{1}{2}^-$	4500.2 – 4501.0	B	$\bar{D}^*\Sigma_c^*$ $\frac{1}{2}^-$	4523.2 – 4523.6
A	$\bar{D}^*\Sigma_c^*$ $\frac{3}{2}^-$	4510.6 – 4510.8	B	$\bar{D}^*\Sigma_c^*$ $\frac{3}{2}^-$	4516.5 – 4516.6
A	$\bar{D}^*\Sigma_c^*$ $\frac{5}{2}^-$	4523.3 – 4523.6	B	$\bar{D}^*\Sigma_c^*$ $\frac{5}{2}^-$	4500.2 – 4501.0

7 Pc states!

Xiao et al., PRD88, 56012 (2013)

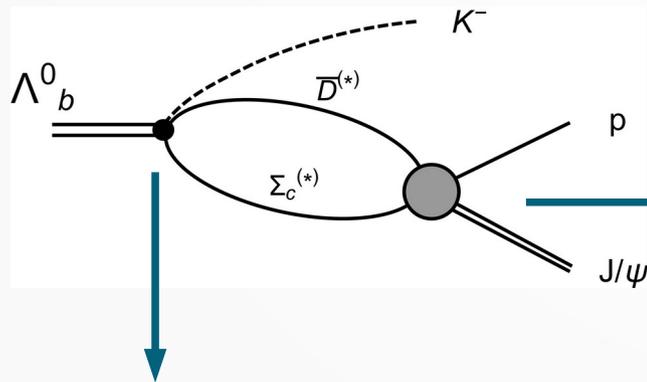
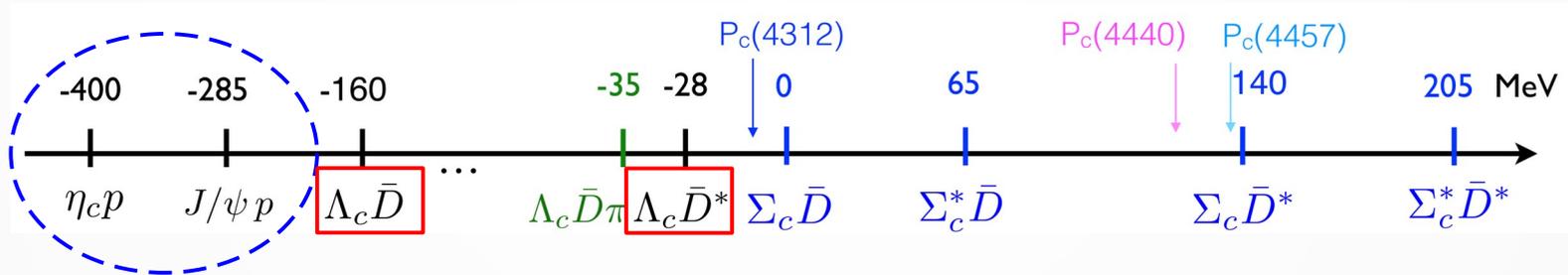
Liu et al., PRL122,242001 (2019)

Molecular Interpretation [EFT]

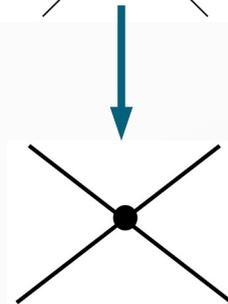
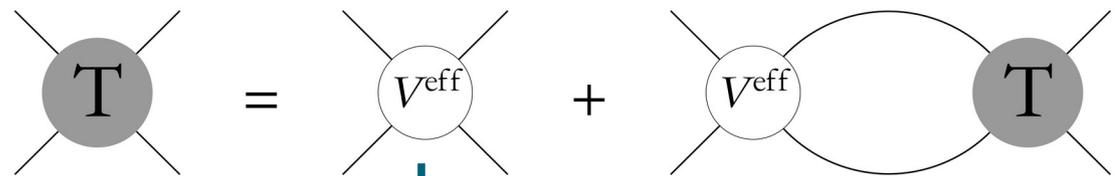
MLD et al., PRL124,072001(2020)

MLD et al., JHEP08,157 (2021)

- A coupled-channel analysis of the LHCb spectra using an EFT approach



7 LECs for contact Production



$$\bar{D}^{(*)} \Sigma_c^{(*)} \rightarrow \bar{D}^{(*)} \Sigma_c^{(*)} \quad 2 \text{ LECs}$$

$$\bar{D}^{(*)} \Sigma_c^{(*)}(S) \rightarrow J/\Psi p(S), J/\Psi p(D) \quad 2 \text{ LECs}$$

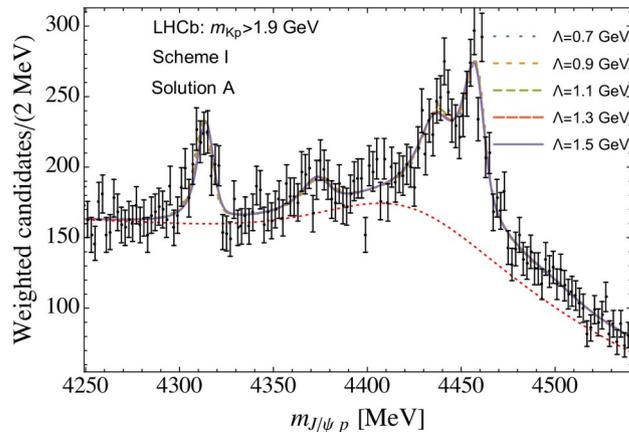
2 LECs

"Contact" Fits to the LHCb data

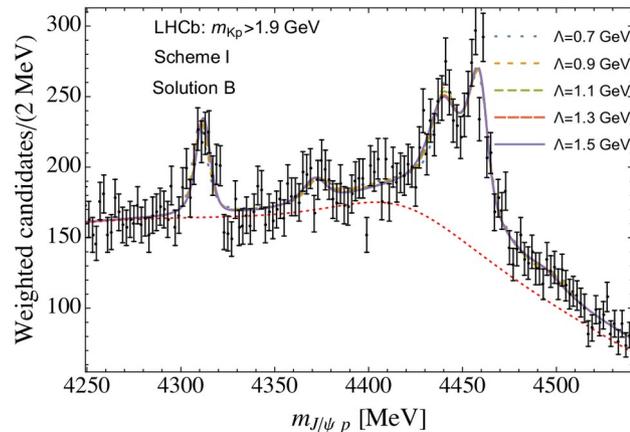
MLD et al., PRL124,072001(2020)

MLD et al., JHEP08,157 (2021)

Solution A



Solution B



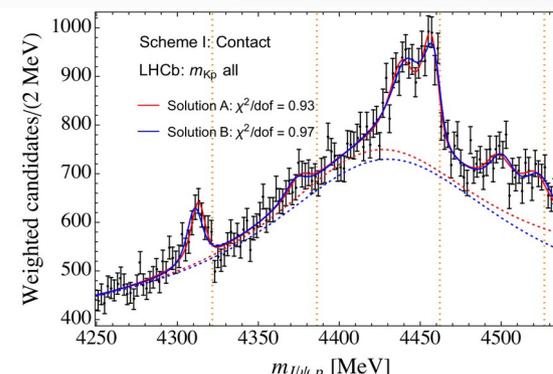
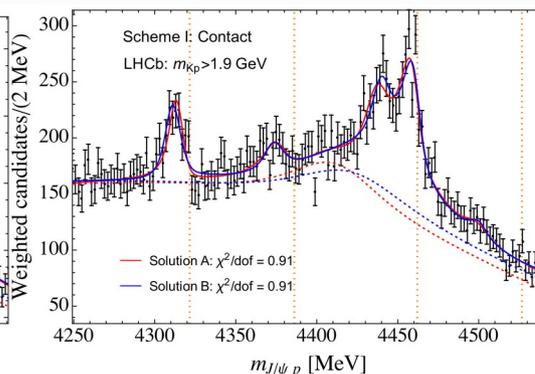
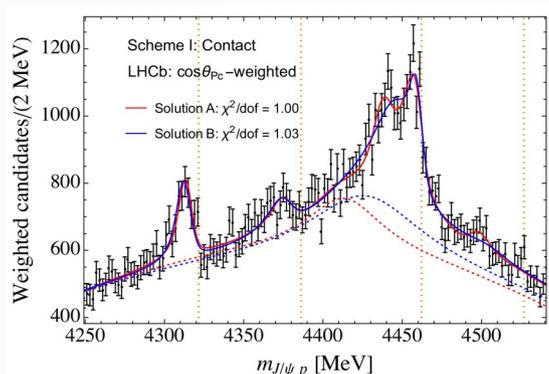
$\Lambda > \Lambda_{\text{soft}} \sim \sqrt{2\mu\delta} \sim 0.7 \text{ GeV}$

Cutoff-independent for both solution A and B

	$P_c(4440)$	$P_c(4457)$
Fit A	1	0
Fit B	0	1

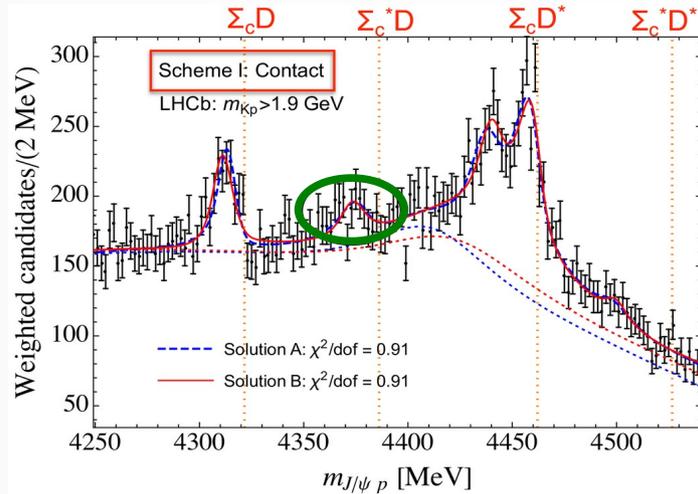
If $\Sigma_c^{(*)} \bar{D}^{(*)} \rightarrow \Lambda_c \bar{D}^{(*)}$ is included, one more LEC

No need for $\Lambda_c \bar{D}^{(*)}$ overdetermined



Line shape and Pc Poles: Contact

MLD et al., PRL124,072001(2020)
MLD et al., JHEP08,157 (2021)



- $P_c(4312)$, $P_c(4440)$, $P_c(4457)$ are well understood as $\Sigma_c D$, $\Sigma_c D^*$ and $\Sigma_c^* D^*$ quasi-bound states, respectively
- A narrow $P_c(4380)$ state predicted as a $\Sigma_c^* D$ $3/2^-$ molecule is seen in data
- $\Sigma_c^* D^*$ states are not seen yet, their production rate is suppressed ?

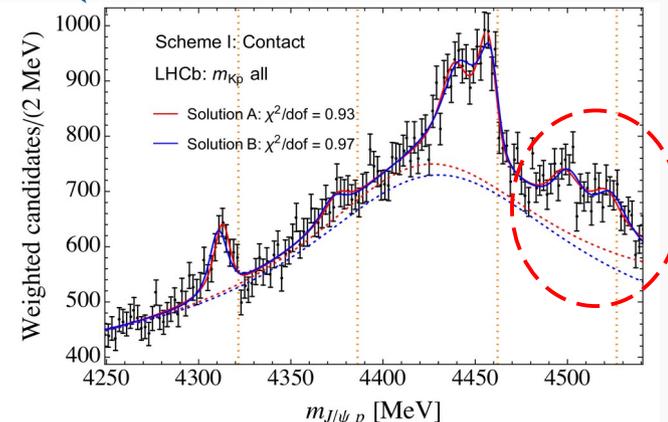
NOT the broad $P_c(4380)$
reported by LHCb in 2015

↪ prompt production in the pp collision in the LHC

Poles and quantum numbers:

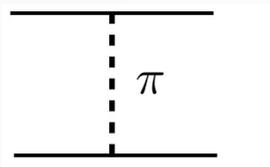
	thr. ([MeV])	solution A		solution B	
		J^P	Pole [MeV]	J^P	Pole [MeV]
$P_c(4312)$	$\Sigma_c \bar{D}$ (4321.6)	$\frac{1}{2}^-$	4314(1) - 4(1)i	$\frac{1}{2}^-$	4312(2) - 4(2)i
$P_c(4380)$	$\Sigma_c^* \bar{D}$ (4386.2)	$\frac{3}{2}^-$	4377(1) - 7(1)i	$\frac{3}{2}^-$	4375(2) - 6(1)i
$P_c(4440)$	$\Sigma_c D^*$ (4462.1)	$\frac{1}{2}^-$	4440(1) - 9(2)i	$\frac{3}{2}^-$	4441(3) - 5(2)i
$P_c(4457)$	$\Sigma_c \bar{D}^*$ (4462.1)	$\frac{3}{2}^-$	4458(2) - 3(1)i	$\frac{1}{2}^-$	4462(4) - 5(3)i
P_c	$\Sigma_c \bar{D}^*$ (4526.7)	$\frac{1}{2}^-$	4498(2) - 9(3)i	$\frac{1}{2}^-$	4526(3) - 9(2)i
P_c	$\Sigma_c^* \bar{D}^*$ (4526.7)	$\frac{3}{2}^-$	4510(2) - 14(3)i	$\frac{3}{2}^-$	4521(2) - 12(3)i
P_c	$\Sigma_c \bar{D}^*$ (4526.7)	$\frac{5}{2}^-$	4525(2) - 9(3)i	$\frac{5}{2}^-$	4501(3) - 6(4)i

P. Ling et al., EPJC81,819 (2021)



Including OPE

contact + OPE



Long range: OPE

Determined by exp. data

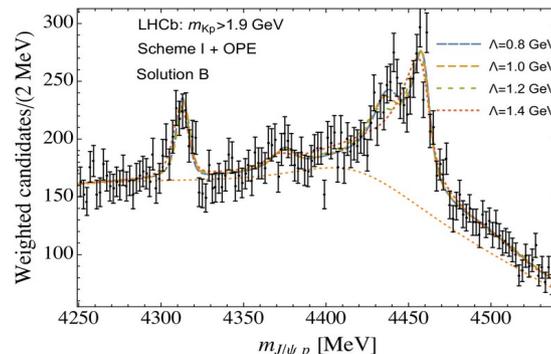
☞ No solution A

☞ Solution B:
Cut-off dependent

☞ $\Lambda_{\text{soft}} \sim 700$ MeV

MLD et al., PRL124,072001(2020)

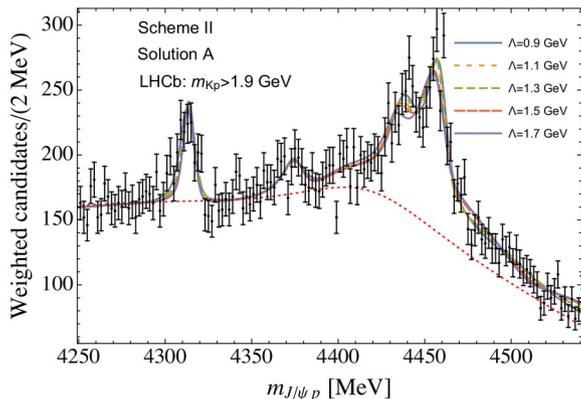
MLD et al., JHEP08,157 (2021)



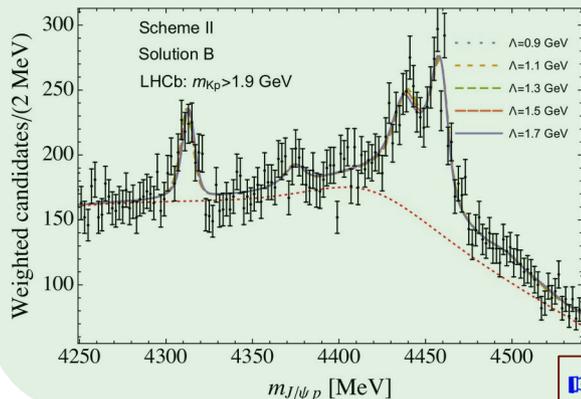
$$+ \Lambda_c \bar{D}^*$$

contact + OPE + S-D

Solution A



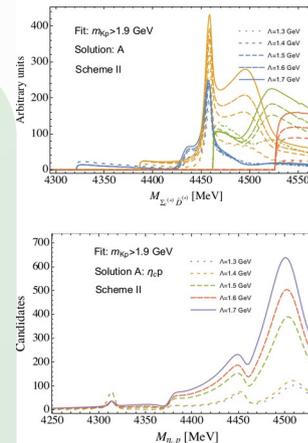
Solution B



Solution A

$\Lambda_{\text{soft}} \sim 0.7$ GeV

Solution B

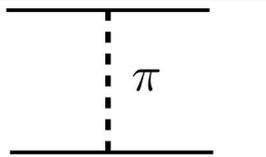


☞ Overdetermined. w/ $\Lambda_c \bar{D}^*$ $\Lambda_{\text{soft}} \sim 0.9$ GeV

☞ Cutoff-independent only for solution B

Including OPE

contact + OPE



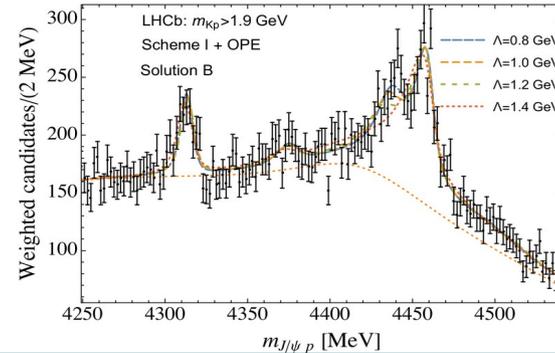
Long range: OPE

Determined by exp. data

☞ No solution A

☞ Solution B:
Cut-off dependent

☞ $\Lambda_{\text{soft}} \sim 700$ MeV



MLD et al., PRL124,072001(2020)

MLD et al., JHEP08,157 (2021)

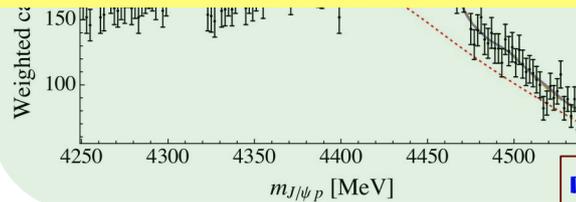
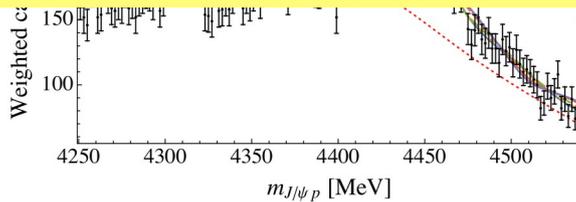
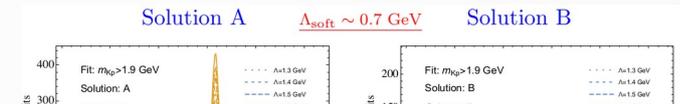
$$\Lambda_c \bar{D}^{(*)}$$

contact + OPE + S-D

Fit B shows a much more natural pattern than fit A

⇒ $P_c(4440)$ is $3/2^-$ and $P_c(4457)$ is $1/2^-$

⇒ experimentally testable via $\Lambda_b \rightarrow K \Sigma^{(*)} D^{(*)}$ and $\Lambda_b \rightarrow K \eta_c p$



☞ Overdetermined. w/ $\Lambda_c \bar{D}^{(*)}$ $\Lambda_{\text{soft}} \sim 0.9$ GeV

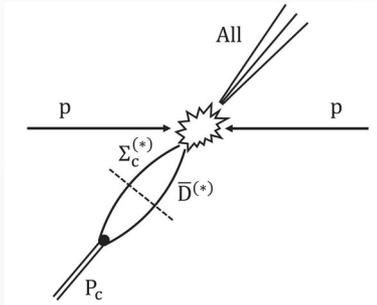
☞ Cutoff-independent only for solution B

Prompt production in the LHC

Poles and quantum numbers:

	thr. [MeV]	solution A		solution B	
		J^P	Pole [MeV]	J^P	Pole [MeV]
$P_c(4312)$	$\Sigma_c \bar{D}$ (4321.6)	$\frac{1}{2}^-$	4314(1) - 4(1) i	$\frac{1}{2}^-$	4312(2) - 4(2) i
$P_c(4380)$	$\Sigma_c^* \bar{D}$ (4386.2)	$\frac{3}{2}^-$	4377(1) - 7(1) i	$\frac{3}{2}^-$	4375(2) - 6(1) i
$P_c(4440)$	$\Sigma_c \bar{D}^*$ (4462.1)	$\frac{1}{2}^-$	4440(1) - 9(2) i	$\frac{3}{2}^-$	4441(3) - 5(2) i
$P_c(4457)$	$\Sigma_c \bar{D}^*$ (4462.1)	$\frac{3}{2}^-$	4458(2) - 3(1) i	$\frac{1}{2}^-$	4462(4) - 5(3) i
P_c	$\Sigma_c^* \bar{D}^*$ (4526.7)	$\frac{1}{2}^-$	4498(2) - 9(3) i	$\frac{1}{2}^-$	4526(3) - 9(2) i
P_c	$\Sigma_c^* \bar{D}^*$ (4526.7)	$\frac{3}{2}^-$	4510(2) - 14(3) i	$\frac{3}{2}^-$	4521(2) - 12(3) i
P_c	$\Sigma_c^* \bar{D}^*$ (4526.7)	$\frac{5}{2}^-$	4525(2) - 9(3) i	$\frac{5}{2}^-$	4501(3) - 6(4) i

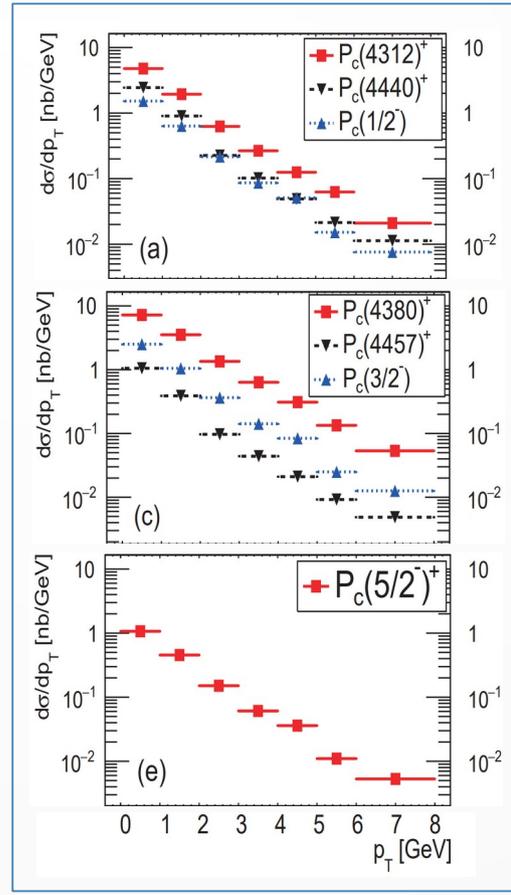
?



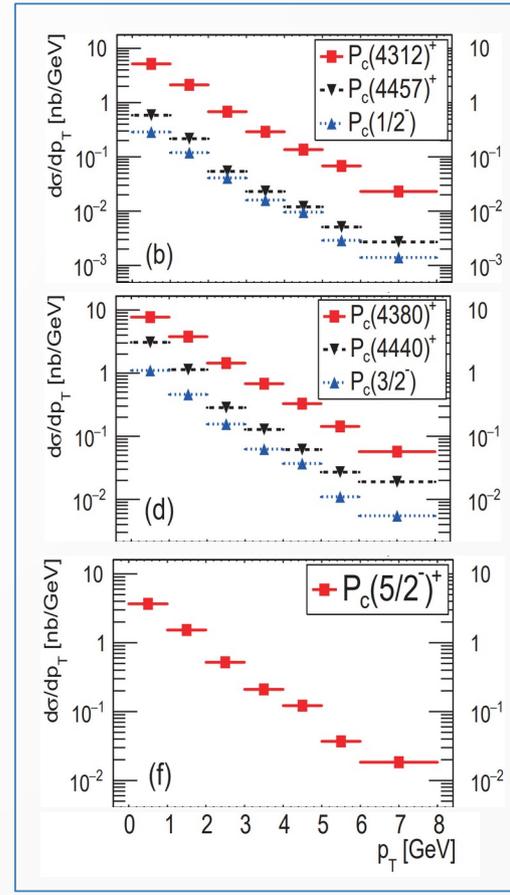
Madgraph5
+
Phythia8

$$\mathcal{M}[P_c(E)] \approx \sum_{\alpha} \int \frac{d^3 \mathbf{q}}{(2\pi)^3} \mathcal{M}[(\Sigma_c^* \bar{D}^*)^{\alpha}(\mathbf{q}) + \text{all}] \times G_{\alpha}(E, \mathbf{q}) \times T_{P_c}^{\alpha}(E),$$

P. Ling et al., Eur.Phys.J.C 81, 819 (2021)



A

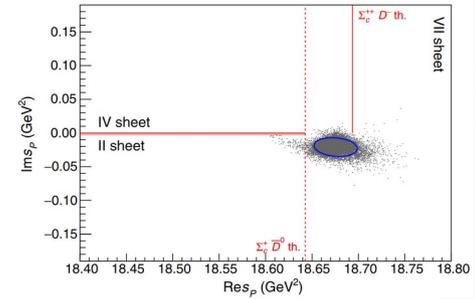
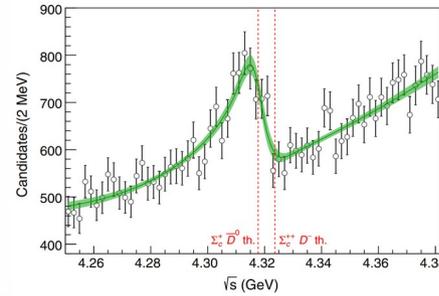


B

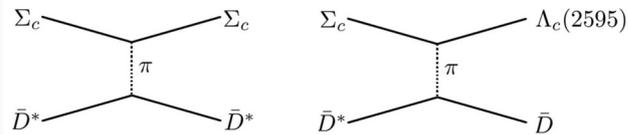
(Some) More Molecular Interpretations...

- the $P_c(4312)^+$ peak as a virtual (unbound) state

JPAC, PRL123, 092001 (2019)



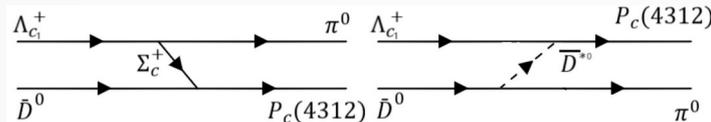
- $J^P(4457) = 1/2^+$ and $J^P(4440) = 3/2^-$



Burns et al., PRD100, 114033(2019)

FIG. 1. Elastic and inelastic t -channel pion-exchange diagrams in the $\Sigma_c \bar{D}^* - \Lambda_c(2595) \bar{D}$ system.

- $P_c(4457)$ interpreted as a $J^P = 1/2^+$ state

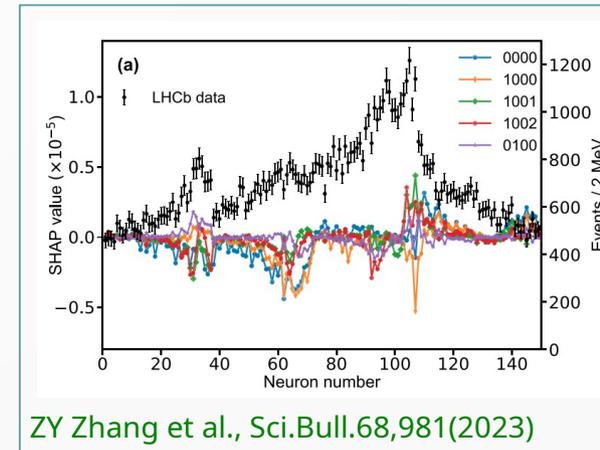


JZ Wu et al., CPL41,091202(2024)

- interpreting the $P_c(4457)$ pentaquark as a $I = \frac{3}{2}$ $\bar{D}^* \Sigma_c$ bound state (with spin $J = \frac{1}{2}$)

$$|P_c(4457)^+\rangle = \cos \theta_I |\bar{D}^{*0} \Sigma_c^+\rangle + \sin \theta_I |D^{*-} \Sigma_c^{++}\rangle$$

FZ Peng et al.,2211.09154

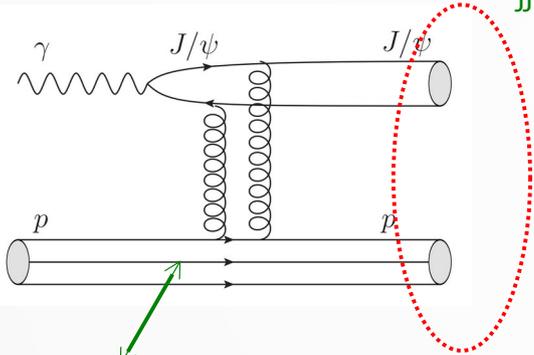


ZY Zhang et al., Sci.Bull.68,981(2023)

A look at the J/ψ photoproduction

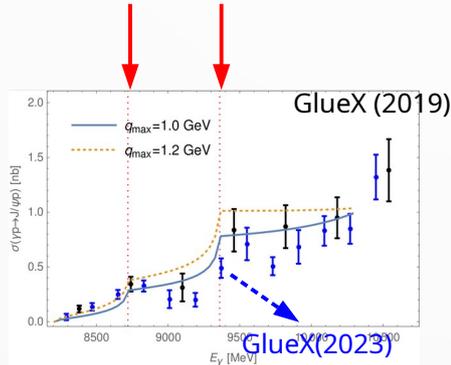
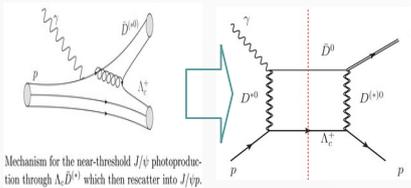
$$T_{\gamma p \rightarrow J/\psi p} = g_{\gamma\psi} T_{J/\psi p \rightarrow J/\psi p}$$

Q Wang et al., PRD92(2015)
JJ Wu et al., PRC100(2019)



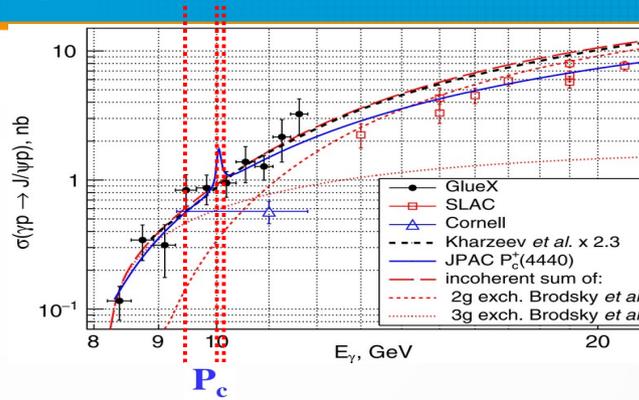
$P_c?$

$$M_N = \left\langle \frac{\beta}{2g} F^2 + \sum_f \gamma m_f \bar{\psi}_f \psi_f \right\rangle_H + \sum_f m_f \langle \bar{\psi}_f \psi_f \rangle_H$$



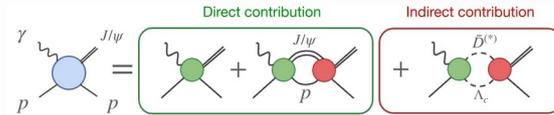
The $\Lambda_c^+ \bar{D}^0$ threshold is only 116 MeV above the $J/\psi p$ threshold, rendering the contribution from the $\Lambda_c \bar{D}$ channel potentially sizeable.

MLD et al., EPJC80,1053(2021)

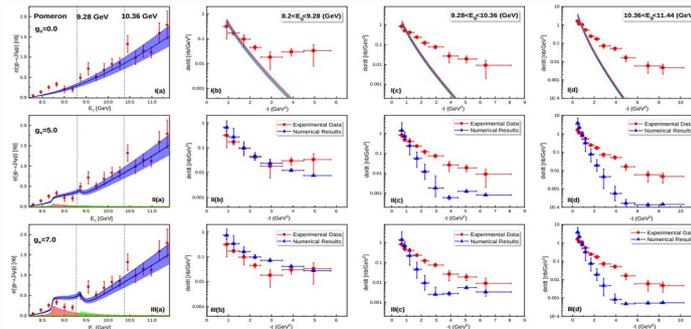
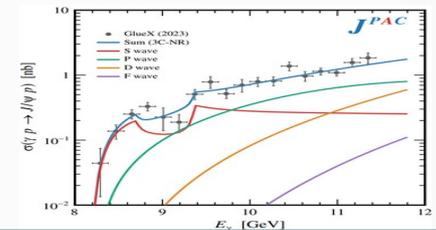


GlueX, PRL123,072001(2019)

No evidence for P_c .



JPAC, PRD108,054018(2023)



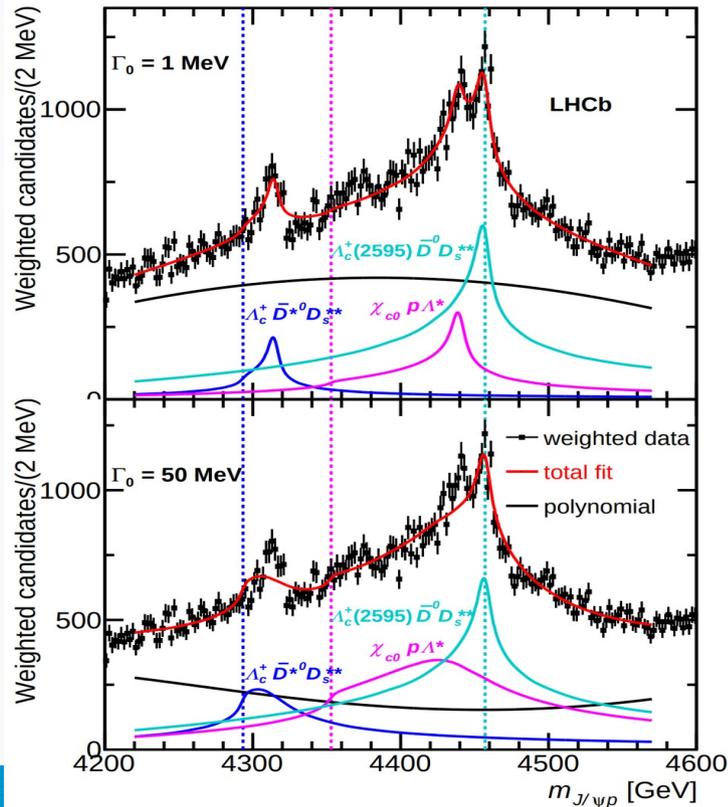
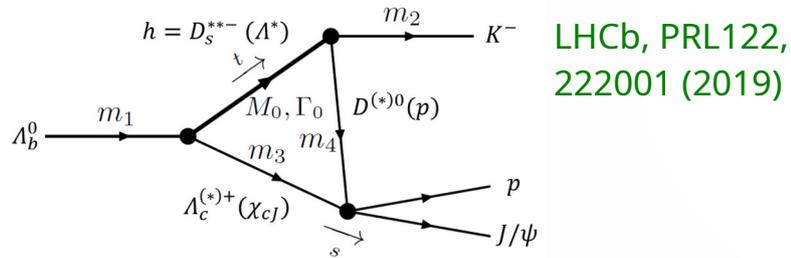
MX Duan et al., 2409.10364

The production of P_c suppressed

A similar result by X Zhang, 2410.1015

The inclusion of the open charm channels and intermediate P_c states can significantly improve the descriptions of the differential cross section data

Triangle Diagrams

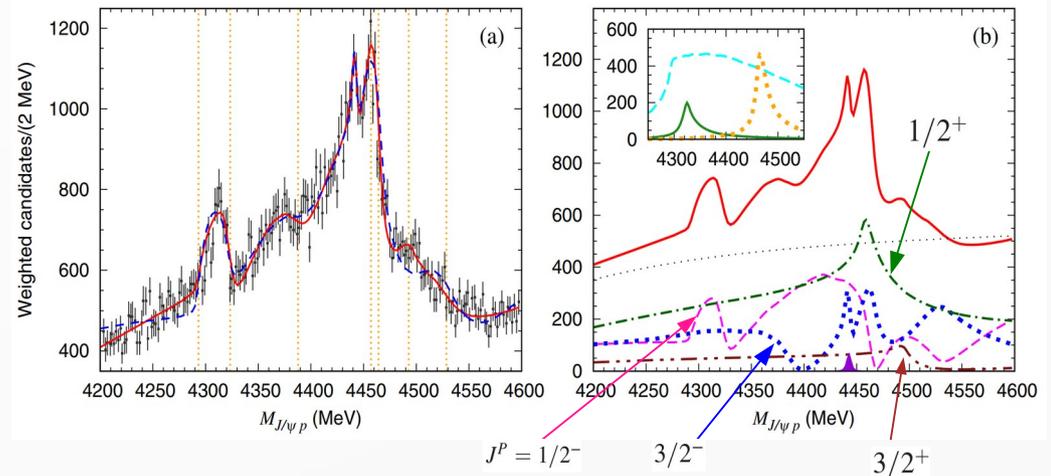
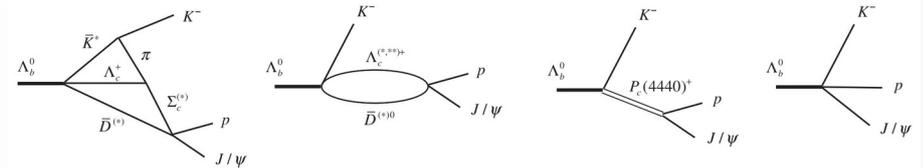


Nakamura, PRD103,L111503 (2021)

$P_c(4312)^+$, $P_c(4380)^+$, and $P_c(4457)^+$ as double triangle cusps

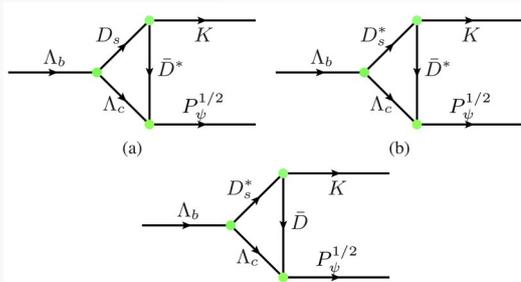
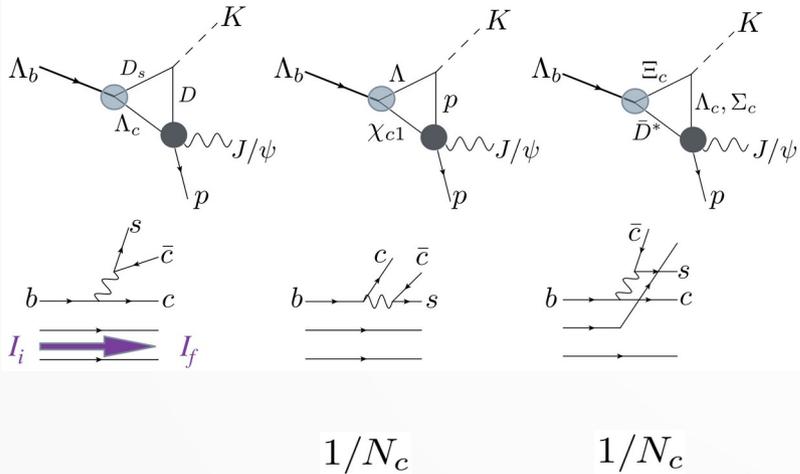
double triangle amplitudes reproduce the peak structures of $P_c(4312)^+$, $P_c(4380)^+$, and $P_c(4457)^+$

Only the $P_c(4440)^+$ peak is due to a resonance



A Production/Rescattering Model

Burns et al., PRD106,054029 (2022)



ZW Liu et al., PRD108,114022 (2023)

$1/2^-$:

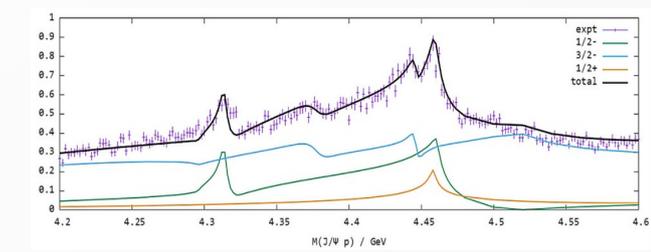
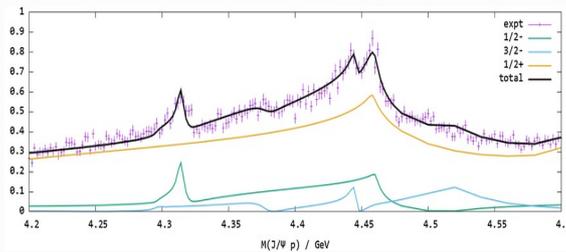
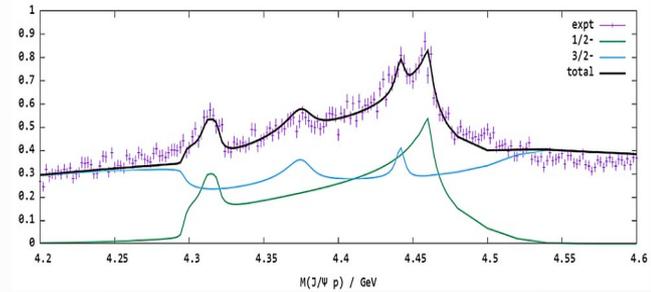
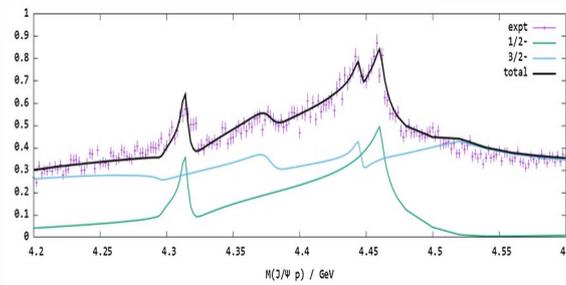
$3/2^-$:

$1/2^+$:

$\Lambda_c \bar{D}, \Lambda_c \bar{D}^*, \Sigma_c \bar{D}, \Sigma_c \bar{D}^*, \Sigma_c^* \bar{D}^*, NJ/\psi, N\eta_c$

$\Lambda_c \bar{D}^*, \Sigma_c^* \bar{D}, \Sigma_c \bar{D}^*, \Sigma_c^* \bar{D}^*, NJ/\psi$

$\Lambda_c(2595) \bar{D}, \Lambda_c(2595) \bar{D}^*, \Lambda_c(2625) \bar{D}^*, NJ/\psi(^2P_{1/2}), NJ/\psi(^4P_{1/2}), N\eta_c(^2P_{1/2})$

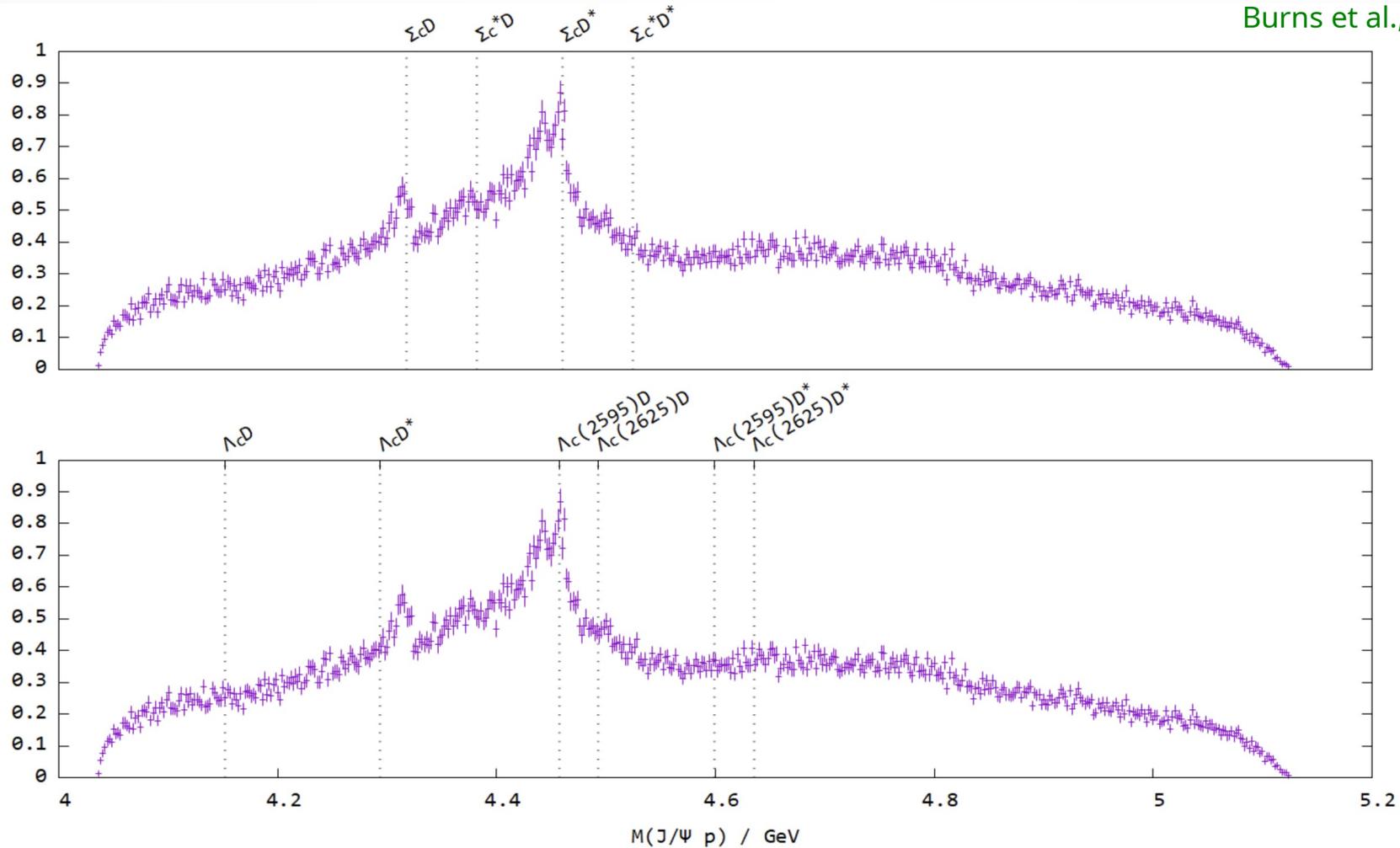


● Weakly bound $\Sigma_c^{(*)} D^{(*)}$ resonances are required:

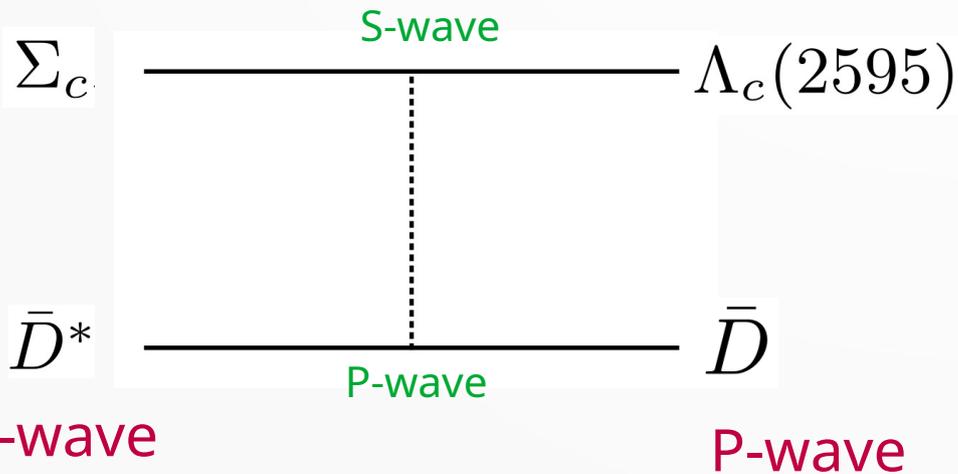
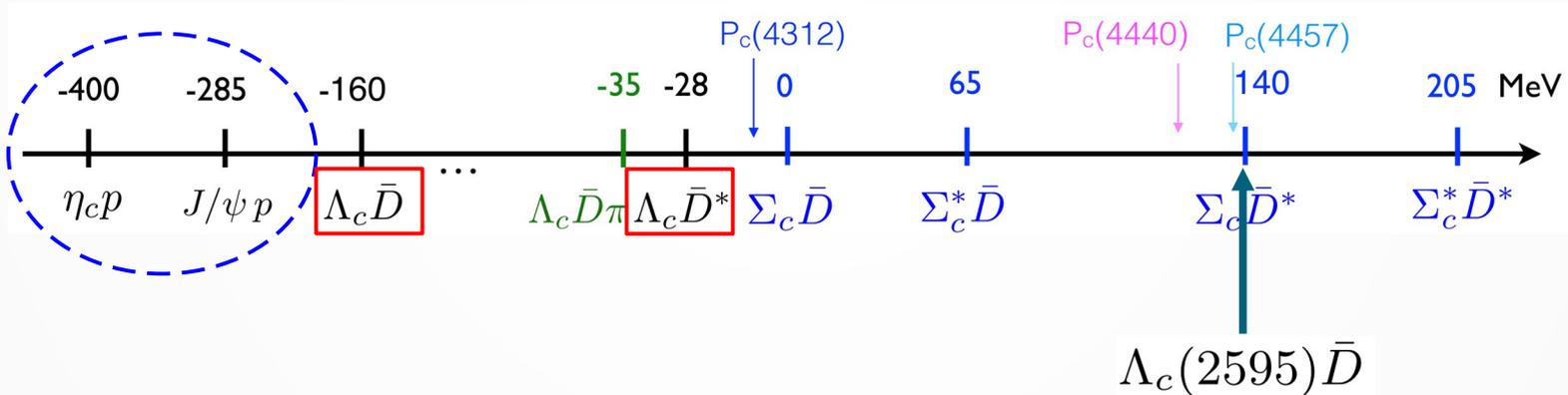
- 4312 ($\Sigma_c D$, $1/2^-$)
- 4380 ($\Sigma_c^* D$, $3/2^-$)
- 4440 ($\Sigma_c D^*$, $3/2^-$)
- 4457 ($1/2^-$ - $\Sigma_c D^*$ threshold cusp / $1/2^+$ triangle)

A look at the data

Burns et al., PRD106,054029 (2022)



Including $\Lambda_c(2595)D$



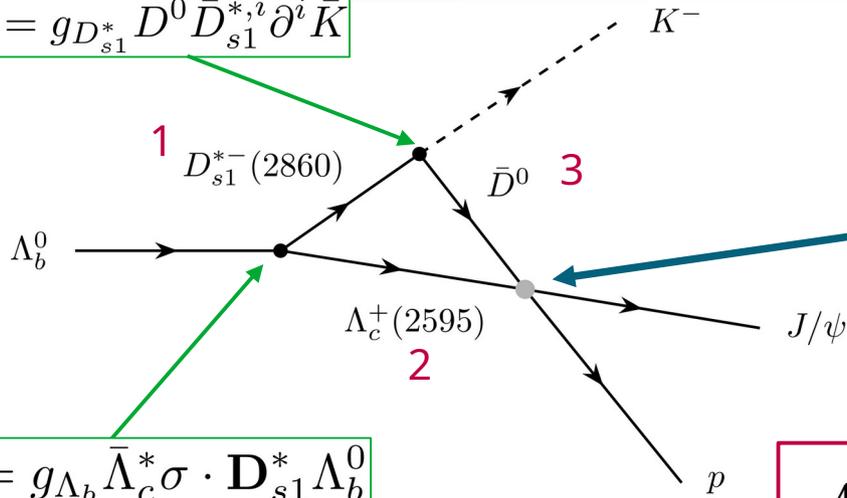
$\Lambda_c(2595)^+$ DECAY MODES

$\Lambda_c^+ \pi \pi$ and its submode $\Sigma_c(2455) \pi$ – the latter just barely – are the only strong decays allowed to an excited Λ_c^+ having this mass; and the submode seems to dominate.

ode		Fraction (Γ_i / Γ)	Scale Factor/ Conf. Level P(MeV/c)
Γ_1	$\Lambda_c^+ \pi^+ \pi^-$	^[1]	117 \downarrow
Γ_2	$\Sigma_c(2455)^{++} \pi^-$	$(24 \pm 7)\%$	3 \downarrow
Γ_3	$\Sigma_c(2455)^0 \pi^+$	$(24 \pm 7)\%$	3 \downarrow
Γ_4	$\Lambda_c^+ \pi^+ \pi^-$ 3-body	$(18 \pm 10)\%$	117 \downarrow
Γ_5	$\Lambda_c^+ \pi^0$	^[2] not seen	258 \downarrow
Γ_6	$\Lambda_c^+ \gamma$	not seen	288 \downarrow

Production of the LHCb Pc states

$$\mathcal{L}_{D_{s1}^*} = g_{D_{s1}^*} D^0 \bar{D}_{s1}^{*,i} \partial^i \bar{K}$$



$$\mathcal{L}_b = g_{\Lambda_b} \bar{\Lambda}_c^* \sigma \cdot \mathbf{D}_{s1}^* \Lambda_b^0$$

$$T^J(E) = [1 - V^J(E) \cdot G(E)]^{-1} \cdot V^J(E)$$

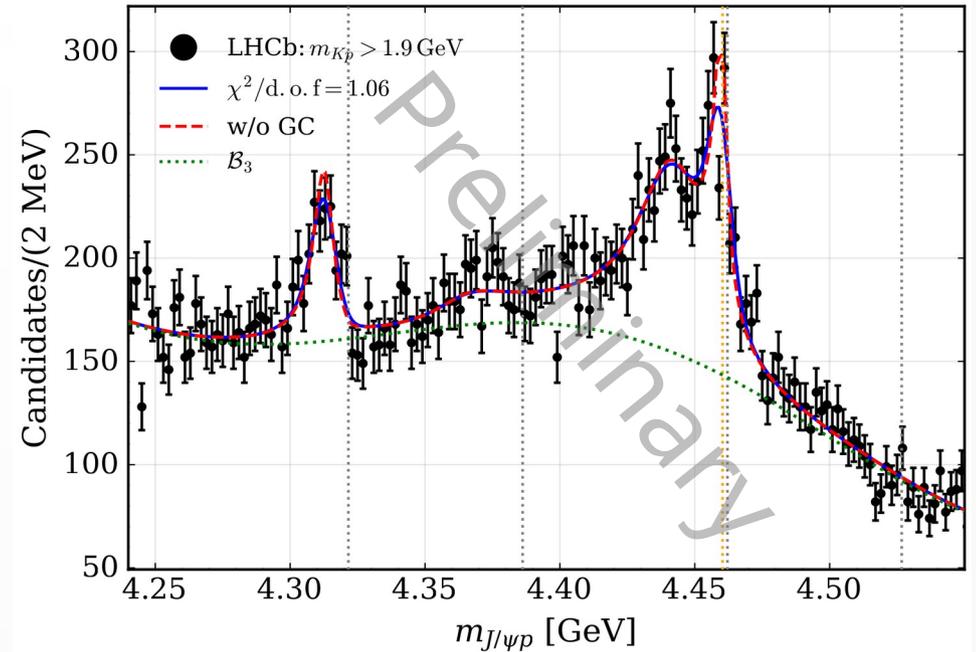
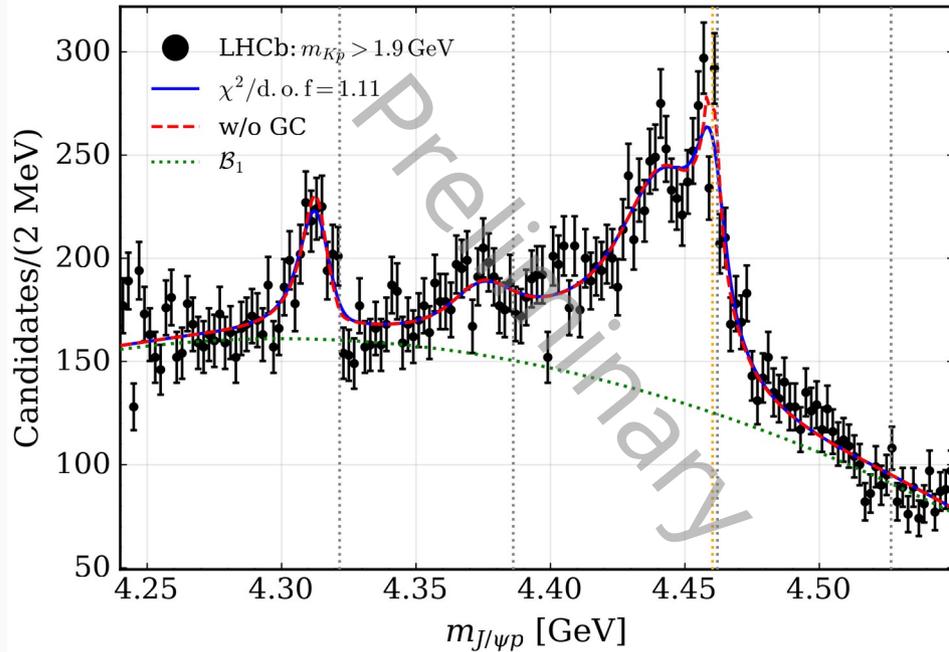
$$T_{4i}^J(E) = \sum_{\alpha=1}^3 T_{4\alpha}^J(E) G_{\alpha}(E) \mathcal{V}_{\alpha i}^J$$

$$\mathcal{A}^J(E) = g(I^{(1)}(p_K) - I(p_K)) p_K^2 T_{4i}^J(E)$$

$$I(q) \equiv i \int \frac{d^4 l}{(2\pi)^4} \frac{1}{(l^2 - m_1^2) ((P-l)^2 - m_2^2) ((l-q)^2 - m_3^2)},$$

$$q^i I^{(1)}(q) \equiv i \int \frac{d^4 l}{(2\pi)^4} \frac{l^i}{(l^2 - m_1^2) ((P-l)^2 - m_2^2) ((l-q)^2 - m_3^2)}.$$

Production of the LHCb Pc states



$$\mathcal{B}_1(E) = b_0 + b_1 E^2 + b_2 E^4$$

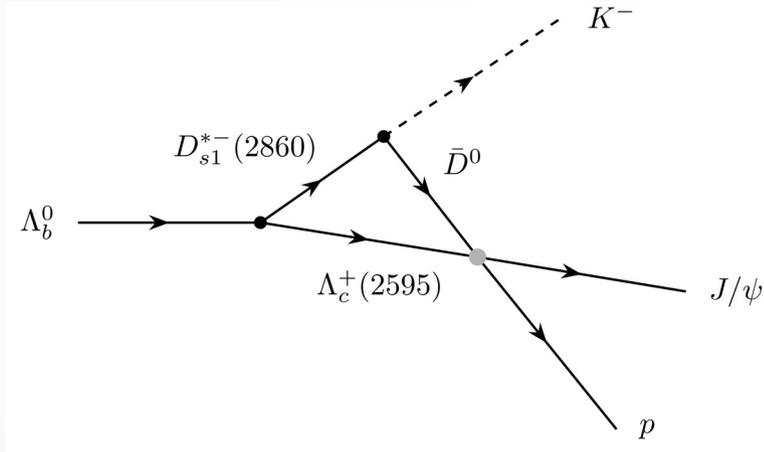
$$\mathcal{B}_3(E) = b_0 + b_1 E^2 + b_2 E^4 + \frac{b_3^2}{(E - b_4)^2 + b_5^2}$$

Solution B! ⇒ **P_c(4440) is 3/2⁻ and P_c(4457) is 1/2⁻**

$\Lambda_c(2595)\bar{D}$ not significant!

consistent with [Yalikul et al., PRD104,094039\(2021\)](#)

Production of the LHCb Pc states



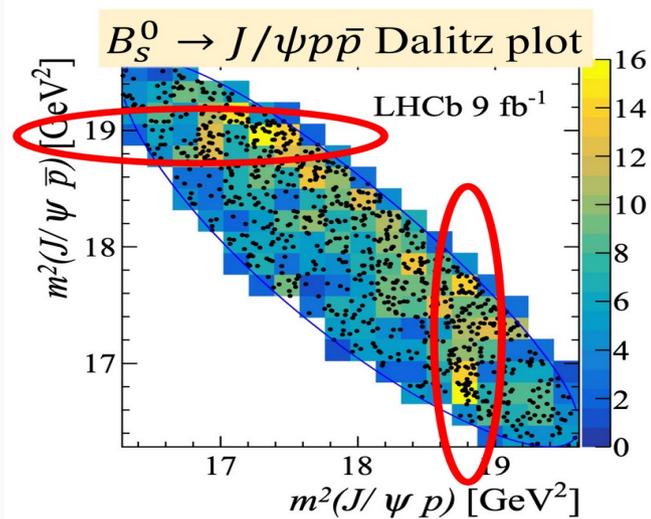
$$R = \frac{\Gamma(\Lambda_b^0 \rightarrow P_c^+ K^- \rightarrow J/\psi p K^-)}{\Lambda_b^0 \rightarrow D_{s1}^{*-} (2860) \Lambda_c (2595)} \approx 5\%$$

	J^P	Pole [MeV]	DC (threshold [MeV])	g_{DC}	RS
$P_c(4312)$	$\frac{1}{2}^-$	$4313(2) - 6(2)i$	$\Sigma_c \bar{D} (4321.6)$	$2.83(23) + 0.40(22)i$	RS ₊₊₊₊
$P_c(4380)$	$\frac{3}{2}^-$	$4373(9) - 16(3)i$	$\Sigma_c^* \bar{D} (4386.2)$	$3.13(40) + 0.48(23)i$	RS ₊₊₊₊
$P_c(4440)$	$\frac{3}{2}^-$	$4442(4) - 18(7)i$	$\Sigma_c \bar{D}^* (4462.1)$	$3.28(63) + 0.47(42)i$	RS ₋₊₊₊
$P_c(4457)$	$\frac{1}{2}^-$	$4465(8) - 5(4)i$	$\Sigma_c \bar{D}^* (4462.1)$	$2.01(34) + 0.95(57)i$	RS ₋₊₊₋
P_c	$\frac{1}{2}^-$	$4535(11) - 10(4)i$	$\Sigma_c^* \bar{D}^* (4526.7)$	$1.83(43) + 1.88(95)i$	RS ₋₋₋₊
P_c	$\frac{3}{2}^-$	$4533(18) - 22(8)i$	$\Sigma_c^* \bar{D}^* (4526.7)$	$2.61(39) + 1.75(85)i$	RS ₋₋₋₊
P_c	$\frac{5}{2}^-$	$4491(13) - 28(6)i$	$\Sigma_c^* \bar{D}^* (4526.7)$	$4.52(51) + 0.60(18)i$	RS ₊

Charmonium-pentaquark states (III)

P_c state in $B_s^0 \rightarrow J/\psi p \bar{p}$

LHCb, PRL128,062001(2022)



- New pentaquark candidate: $P_c(4337)^+ \rightarrow J/\psi p > 3\sigma$

$$M = 4337_{-4}^{+7}(\text{stat})_{-2}^{+2}(\text{syst}) \text{ MeV}, \Gamma = 29_{-12}^{+26}(\text{stat})_{-14}^{+14}(\text{syst}) \text{ MeV}$$

- No evidence of P_c^+ states observed in $\Lambda_b^0 \rightarrow J/\psi p K^-$

$P_c(4312) ?$

Proposals

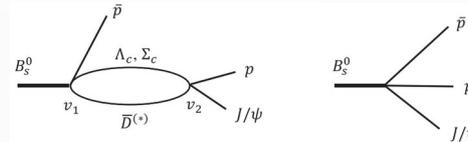
Compact pentaquark

C.R. Deng, PRD105, 116021 (2022)

Hadroncharmonium: $\chi_{c0}(1S)p$ bound state

Ferretti et al., Sci.Bull.67,1209(2022)

$P_c(4312)^+$ and $P_c(4337)^+$ as interfering $\Sigma_c \bar{D}$ and $\Lambda_c \bar{D}^*$ threshold cusps



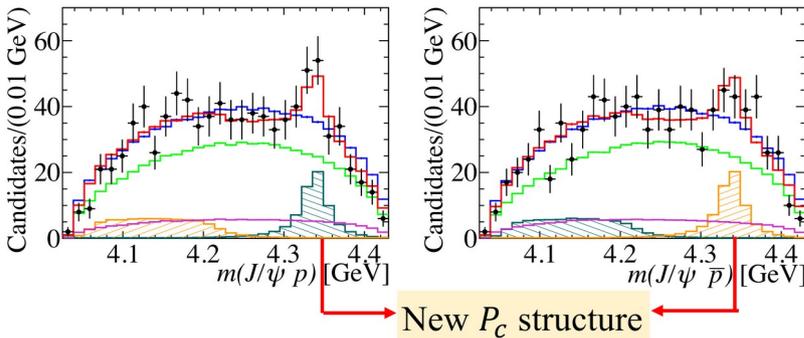
Nakamura et al., PRD104, L091503(2021)

A few of possibilities are reviewed, including $\bar{D}^* \Lambda_c$ and $\bar{D} \Sigma_c$ states

$\bar{D}^* \Lambda_c - \bar{D} \Sigma_c$ and $\bar{D}^* \Lambda_c - \bar{D} \Sigma_c^*$

MJ Yan et al., EPJC82,574 (2022)

.....



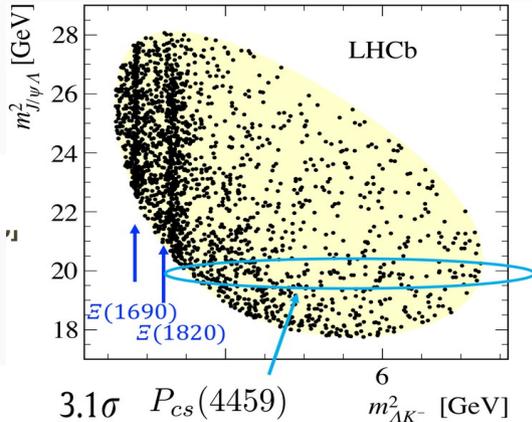
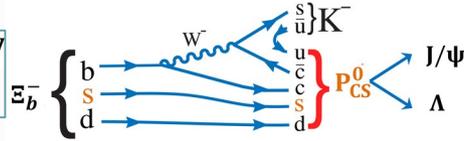
Hidden-charm Pentaquarks with strangeness (I)

- SU(3) partner P_{CS} is predicted, and suggested to search for in $\Xi_b^- \rightarrow J/\psi \Lambda K^-$

JJ Wu et al., PRL105, 232001(2010);
HX Chen et al., PRC93,065203(2016) ...

LHCb, Sci.Bull.66,1278 (2021)

$4458.8 \pm 2.9^{+4.7}_{-1.1}$ MeV
 $17.3 \pm 6.5^{+8.0}_{-5.7}$ MeV



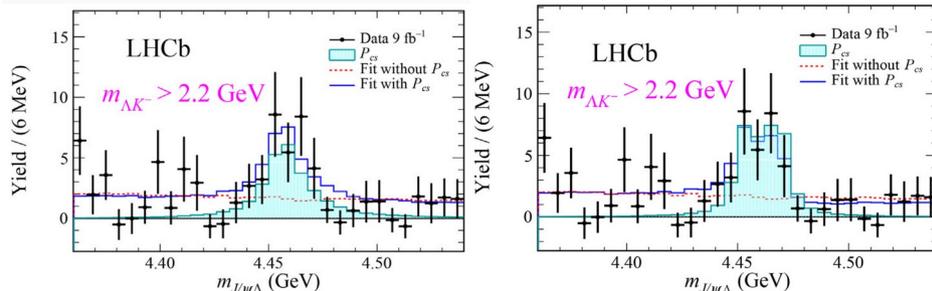
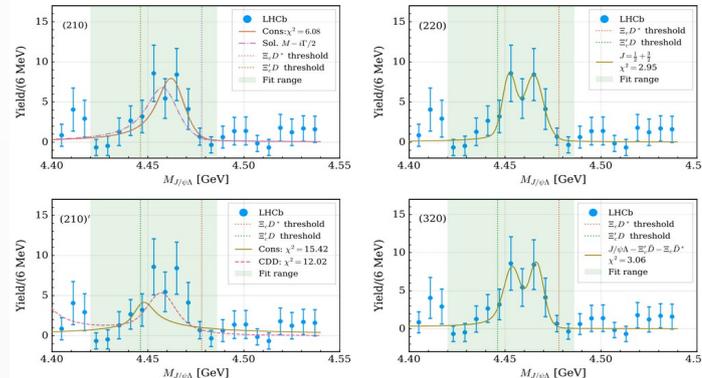
Molecular Interpretation

B. Wang et al., PRD101,034018(2020)

System	$[\Xi_c \bar{D}]_{\frac{1}{2}}$	$[\Xi_c' \bar{D}^*]_{\frac{1}{2}}$	$[\Xi_c \bar{D}^*]_{\frac{3}{2}}$	$[\Xi_c' \bar{D}]_{\frac{3}{2}}$	$[\Xi_c^* \bar{D}^*]_{\frac{1}{2}}$	$[\Xi_c^* \bar{D}^*]_{\frac{3}{2}}$	$[\Xi_c \bar{D}^*]_{\frac{1}{2}}^{\#}$	$[\Xi_c \bar{D}]_{\frac{1}{2}}$	$[\Xi_c \bar{D}^*]_{\frac{1}{2}}$	$[\Xi_c \bar{D}^*]_{\frac{3}{2}}$
ΔE	$-18.5^{+6.4}_{-6.8}$	$-15.6^{+6.4}_{-7.2}$	$-2.0^{+1.8}_{-3.3}$	$-7.5^{+4.2}_{-5.3}$	$-17.0^{+6.7}_{-7.5}$	$-8.0^{+4.5}_{-5.6}$	$-0.7^{+0.7}_{-2.2}$	$-13.3^{+2.8}_{-3.0}$	$-17.8^{+3.2}_{-3.3}$	$-11.8^{+2.8}_{-3.0}$
M	$4423.7^{+6.4}_{-6.8}$	$4568.7^{+6.4}_{-7.2}$	$4582.3^{+1.8}_{-3.3}$	$4502.9^{+4.2}_{-5.3}$	$4635.4^{+6.7}_{-7.5}$	$4644.4^{+4.5}_{-5.6}$	$4651.7^{+0.7}_{-2.2}$	$4319.4^{+2.8}_{-3.0}$	$4456.9^{+3.2}_{-3.3}$	$4463.0^{+2.8}_{-3.0}$

MLD et al., PRD104, 114034(2021)

Our different analyses clearly indicate the molecular nature of the P_{CS} (4459) with a clear $\Xi_c \bar{D}^*$ dominant component.



See review papers:

An updated review of the new hadron states, HX Chen et al., Rept.Prog.Phys.86,026201(2023)

ChPT for heavy hadrons and ChEFT for heavy hadronic molecules, L.

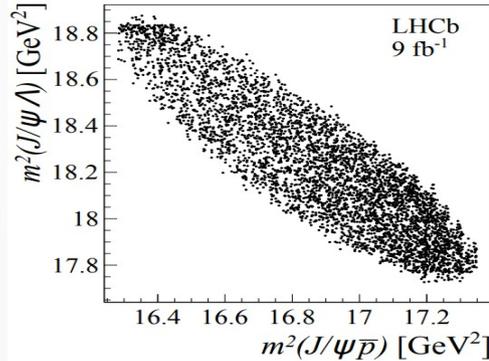
Meng et al., Phys. Rept.1019,1(2023)

Hidden-charm Pentaquarks with strangeness (II)

$$B^- \rightarrow J/\psi \Lambda \bar{p}$$

(Some) Proposals

- $P_{\psi S}^\Lambda(4338)^0$ is likely to be a $1/2^-$ compact P_{CS} pentaquark framework of MIT bag model [WX Zhang et al., PRD109,114037 \(2024\)](#)
- HQSS+local hidden gauge [Feijoo et al., PLB839, 137760\(2023\)](#)



$$J^P = \frac{1}{2}^-$$

$P_{CS}(4459)$

Poles	$\eta_c \Lambda$	$\bar{D}_s \Lambda_c$	$\bar{D} \Xi_c$	$\bar{D} \Xi'_c$	
4198.94 + i0.11	g_i $g_i G_i^{II}$	0.12 - i0.00 -0.35 + i1.01	3.01 - i0.01 -19.24 + i0.05	4.85 + i0.01 -20.35 - i0.07	0.01 - i0.03 -0.03 + i0.09
4422.79 + i7.75	g_i $g_i G_i^{II}$	0.71 - i0.08 1.14 + i10.71	0.05 + i0.00 0.76 + i1.82	-0.06 + i0.04 -0.43 - i1.53	2.79 - i0.35 -26.54 + i0.64

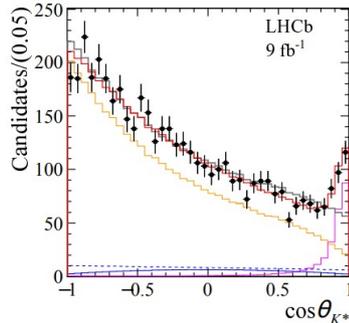
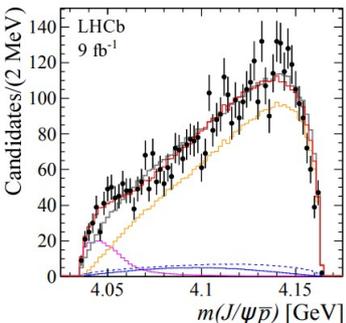
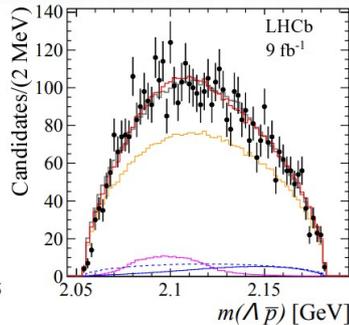
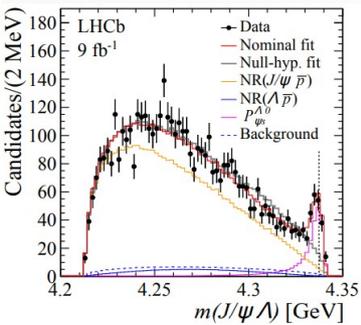
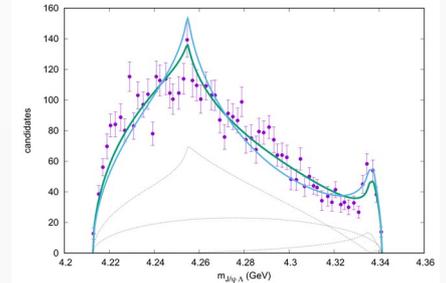
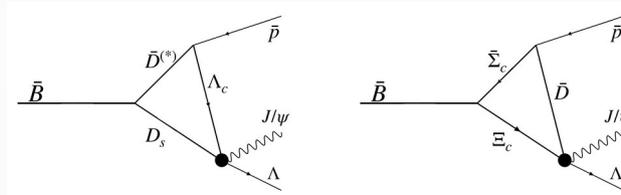
$$J^P = \frac{1}{2}^-, \frac{3}{2}^-$$

$P_{\psi S}^\Lambda(4338)$

Poles	$J/\psi \Lambda$	$\bar{D}_s^* \Lambda_c$	$\bar{D}^* \Xi_c$	$\bar{D}^* \Xi'_c$	
4337.98 + i0.12	g_i $g_i G_i^{II}$	0.11 - i0.00 -0.13 + i1.07	3.17 - i0.01 -18.57 + i0.06	5.07 + i0.01 -19.94 - i0.07	0.00 - i0.04 -0.01 + i0.10
4565.73 + i15.58	g_i $g_i G_i^{II}$	0.70 - i0.16 6.24 + i21.04	0.09 - i0.03 2.07 + i3.40	-0.10 + i0.09 -1.37 - i2.81	2.84 - i0.72 -26.31 + i1.15

[Burns et al., PLB838,137715 \(2023\)](#)

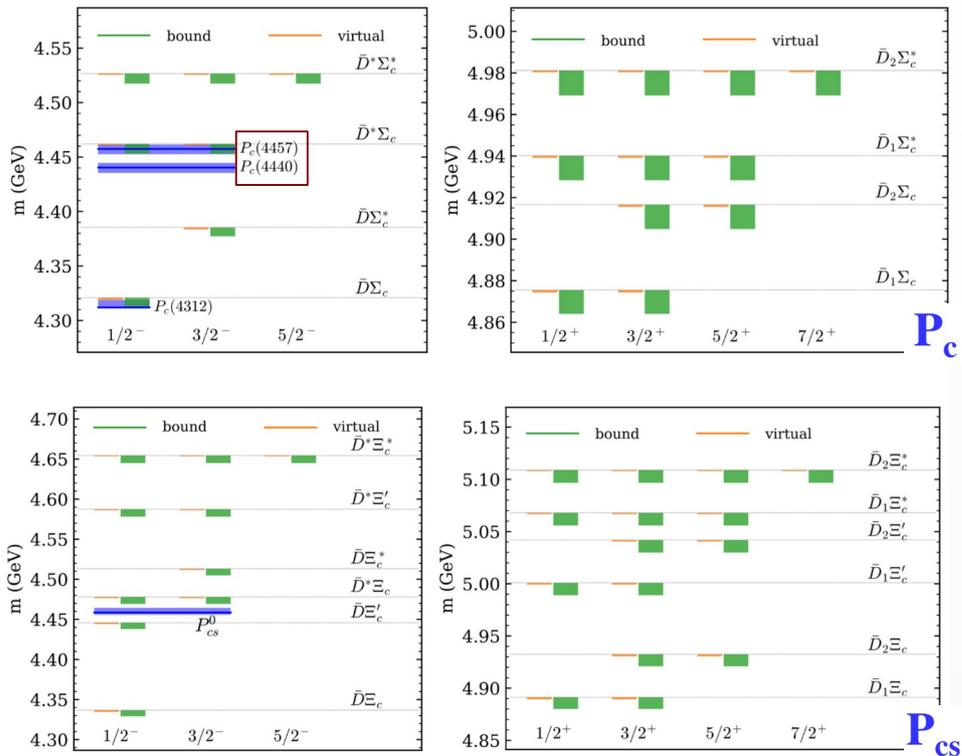
- The LHCb state $P_{\psi S}^\Lambda(4338)$ as a triangle singularity



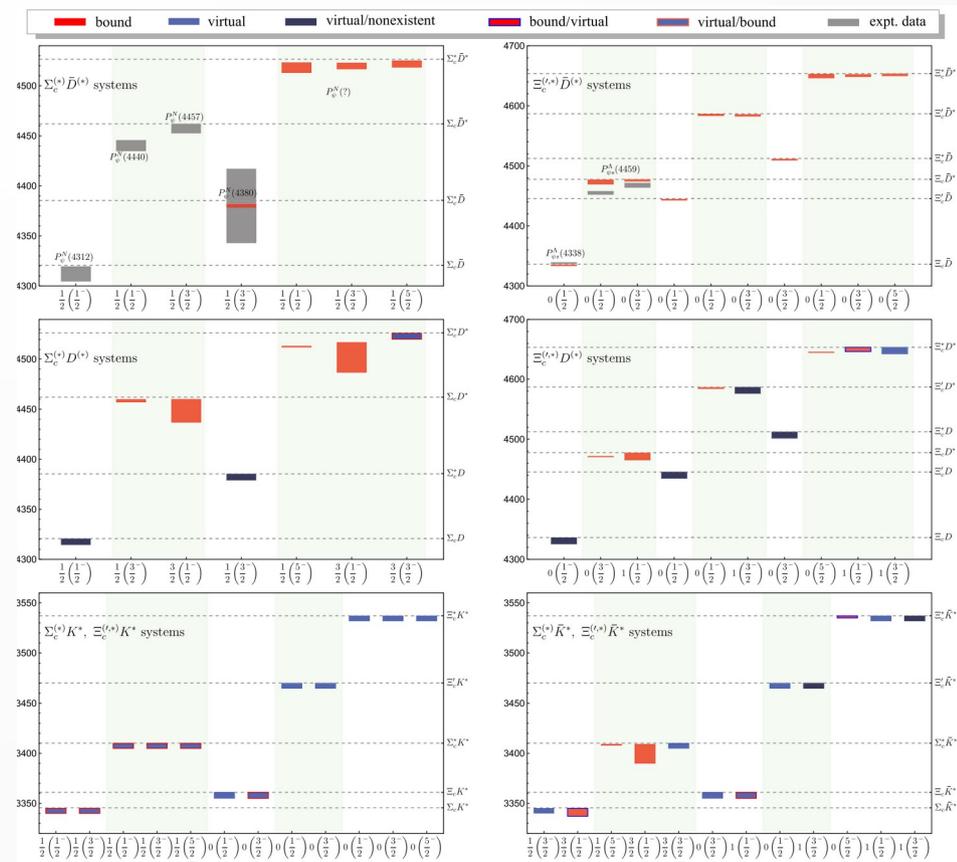
and much more works ...

More Pentaquarks ...

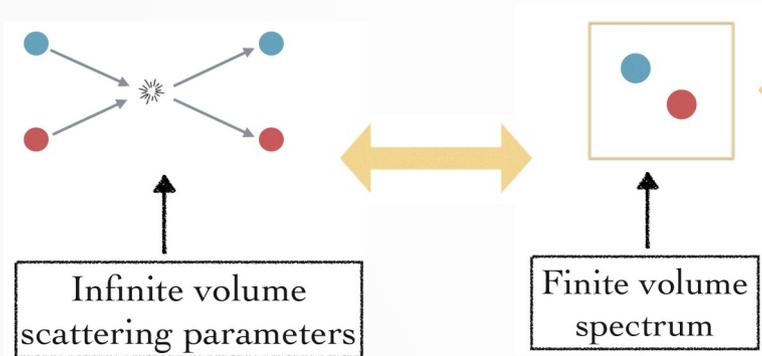
XK Dong et al., Progr.Phys.41,65(2021)



B Wang et al., PRD109,074035(2024)



Lattice QCD study of the Pc states



$\Sigma_c \bar{D}$ and $\Sigma_c \bar{D}^*$ scattering ($J^P = \frac{1}{2}^-$)

◆ Five operators:

$\mathcal{O}_1 = \Sigma_c(\mathbf{p}) \bar{D}(-\mathbf{p})$ ($|\mathbf{p}| = 0$)

$\mathcal{O}_2 = \Sigma_c(\mathbf{p}) \bar{D}(-\mathbf{p})$ ($|\mathbf{p}| = 1$)

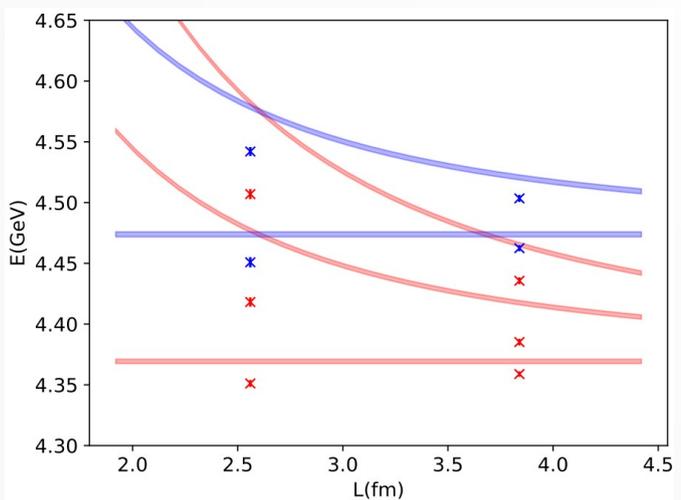
$\mathcal{O}_3 = \Sigma_c(\mathbf{p}) \bar{D}(-\mathbf{p})$ ($|\mathbf{p}| = \sqrt{2}$)

$\mathcal{O}_4 = \Sigma_c(\mathbf{p}) \bar{D}^*(-\mathbf{p})$ ($|\mathbf{p}| = 0$)

$\mathcal{O}_5 = \Sigma_c(\mathbf{p}) \bar{D}^*(-\mathbf{p})$ ($|\mathbf{p}| = 1$)

HY Xing et al., 2210.08555

Single-Channel

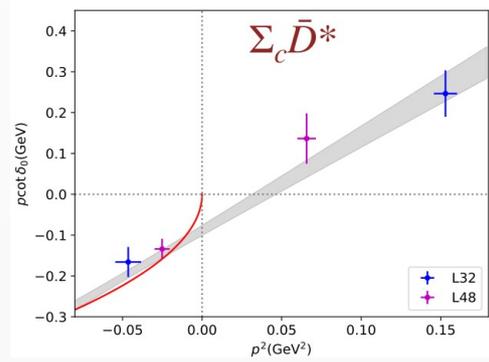
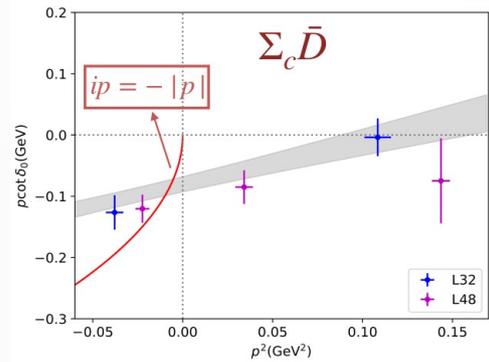


$\Sigma_c \bar{D} : P_c(4312) ?$
 $a_0 = -2.0(3)(5) \text{ fm}$
 $E_B = 6(2)(2) \text{ MeV}$

$\Sigma_c \bar{D}^* : P_c(4440)/P_c(4457) ?$
 $a_0 = -2.3(5)(1) \text{ fm}$
 $E_B = 7(3)(1) \text{ MeV}$

◆ The finite-volume energies lie below the free energies, indicating rather strong attractive interactions.

Coupled-Channel still going!

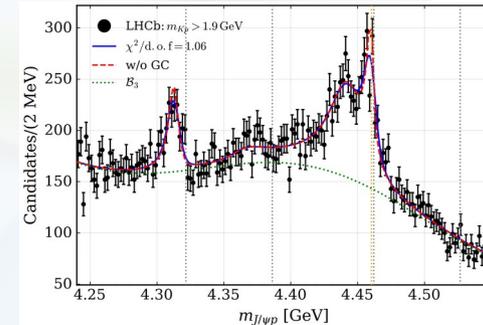


Conclusions and Propects

Conclusions

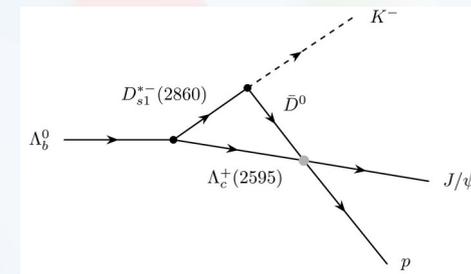
- Molecular interpretation of the Pc's and 7 Pc's are predicted from HQSS
- A narrow Pc(4380), different from the broad one reported by LHCb in 2015
- Production through the triangle diagram
- The missing Pc's from HQSS in LHCb is naturally explained

$$R = \frac{\Gamma(\Lambda_b^0 \rightarrow P_c^+ K^- \rightarrow J/\psi p K^-)}{\Lambda_b^0 \rightarrow D_{s1}^* (2860) \Lambda_c (2595)} \approx 5\%$$



Propects

- The missing Pc's from HQSS, Pc's with strangeness
- Lattice simulations
- STCF: charmonium-like, clearly defined IS&FS properties, full event reconstruction



Pc: $e^+e^- \rightarrow p\bar{p}J/\psi, \Lambda_c\bar{D}^{(*)}\bar{p}, \Sigma_c^{(*)}\bar{D}^{(*)}\bar{p}$ **Pcs(s):** $e^+e^- \rightarrow \Lambda\bar{\Lambda}J/\psi, \Sigma\bar{\Sigma}J/\psi, \text{ and } \Xi\bar{\Xi}J/\psi$ **Pcsss:** $e^+e^- \rightarrow \Omega\bar{\Omega}J/\psi$

Thank you very much for your attention!

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backup

$$\Lambda_b^0 \quad I(J^P) = 0(1/2^+)$$

Γ_{46}	$\Sigma_c(2455)^{++} D^- K^-$	$(6.0 \pm 0.8) \times 10^{-4}$	1448
Γ_{47}	$\Sigma_c(2455)^{++} D^{*-} K^-$	$(1.36 \pm 0.22) \times 10^{-3}$	1324
Γ_{48}	$\Sigma_c(2520)^{++} D^- K^-$	$(2.8 \pm 0.5) \times 10^{-4}$	1392
Γ_{49}	$\Sigma_c(2520)^{++} D^{*-} K^-$	$(5.4 \pm 1.1) \times 10^{-4}$	1262

Γ_{36}	$\Lambda_c^+ D^-$	$(4.6 \pm 0.6) \times 10^{-4}$	1886
Γ_{37}	$\Lambda_c^+ D_s^-$	$(1.10 \pm 0.10) \%$	1833
Γ_{38}	$\Lambda_c^+ D_s^{*-}$	$(1.83 \pm 0.18) \%$	1748
Γ_{39}	$\Lambda_c^+ \bar{D}^0 K^-$	$(2.13 \pm 0.20) \times 10^{-3}$	1581
Γ_{40}	$\Lambda_c^+ \bar{D}^{*0} K^-$	$(6.6 \pm 0.7) \times 10^{-3}$	1471