

# 首届喷注与重夸克物理研讨会



## Flavor effects on jet quenching

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# Flavor(mass) effects in jet shower

*g*-initiated jet

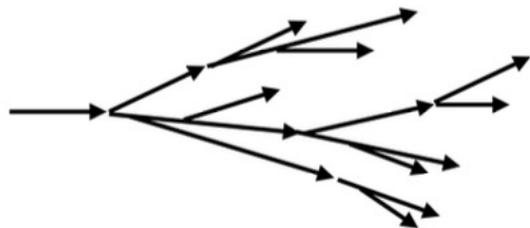
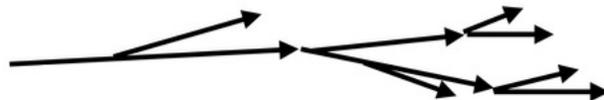


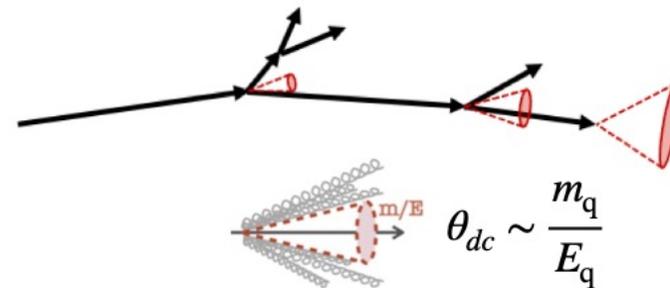
Illustration by P. Dhankher

*q*-initiated jet

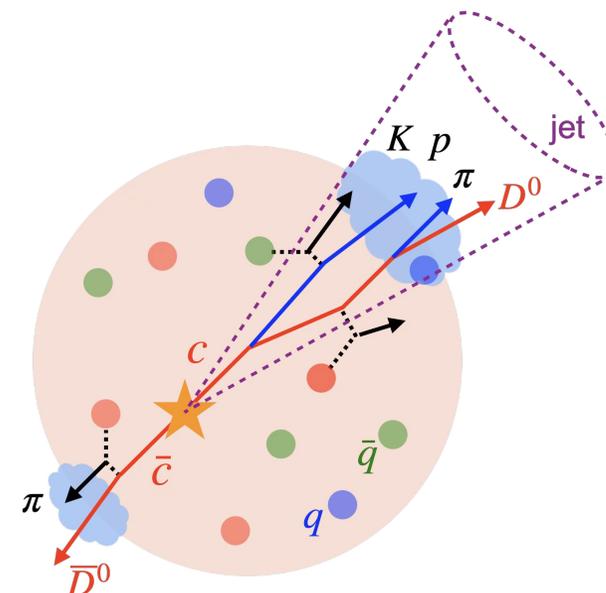


$$\frac{C_A}{C_F} = \frac{9}{4}$$

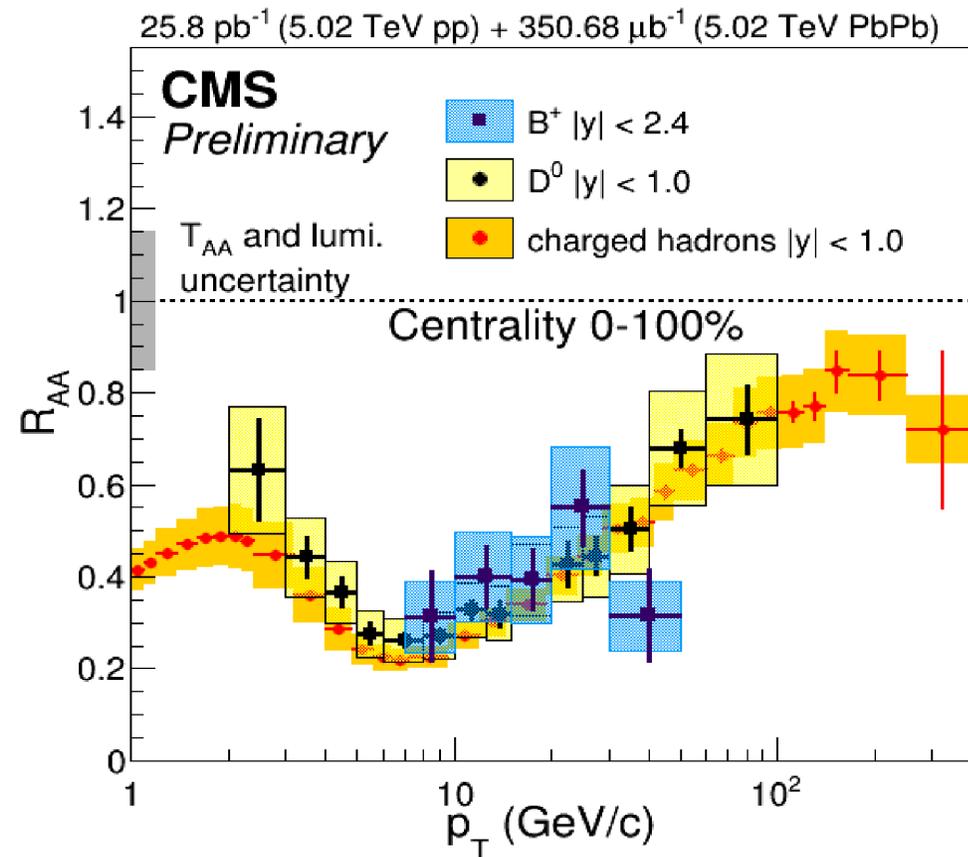
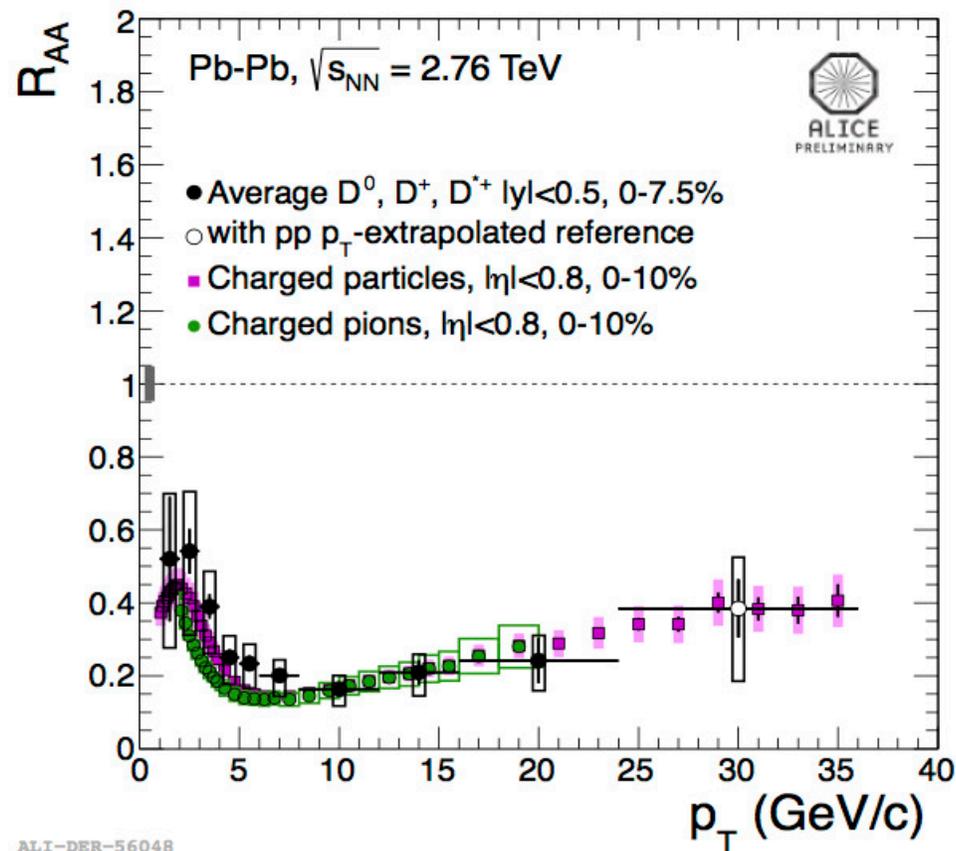
heavy-*q*-initiated jet



- **Casimir-color factors:** *g*-initiated showers have a broader and softer fragmentation profile than *q*-initiated showers.
- **Mass (Dead-cone) effect:** gluon emissions from massive quark are suppressed within a cone of  $\theta_0 \sim m_Q/E$ .
- **Heavy-quark-tagged jets serve as key tools for studying the flavor dependence of parton splitting.**



# Flavor hierarchy in single hadron $R_{AA}$

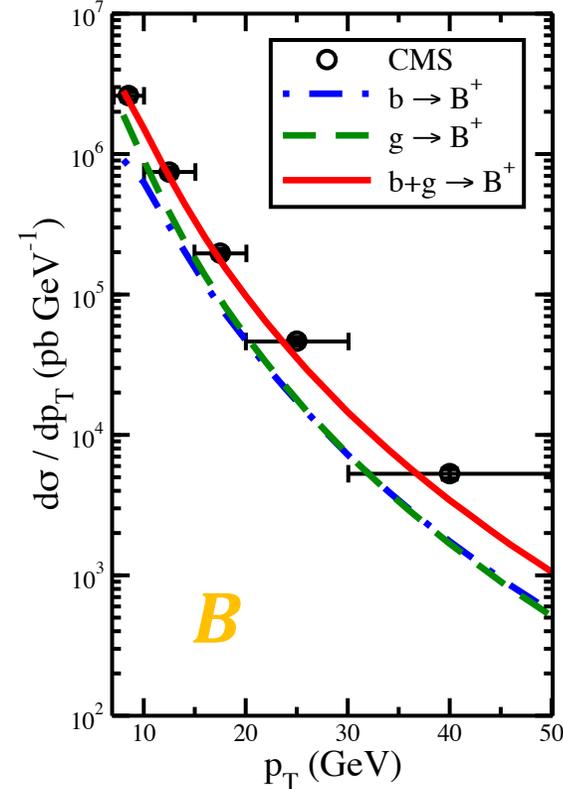
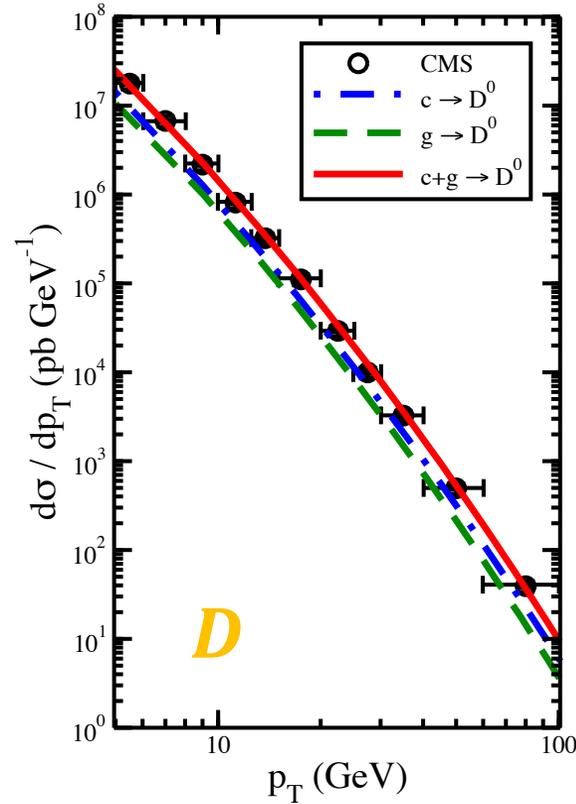
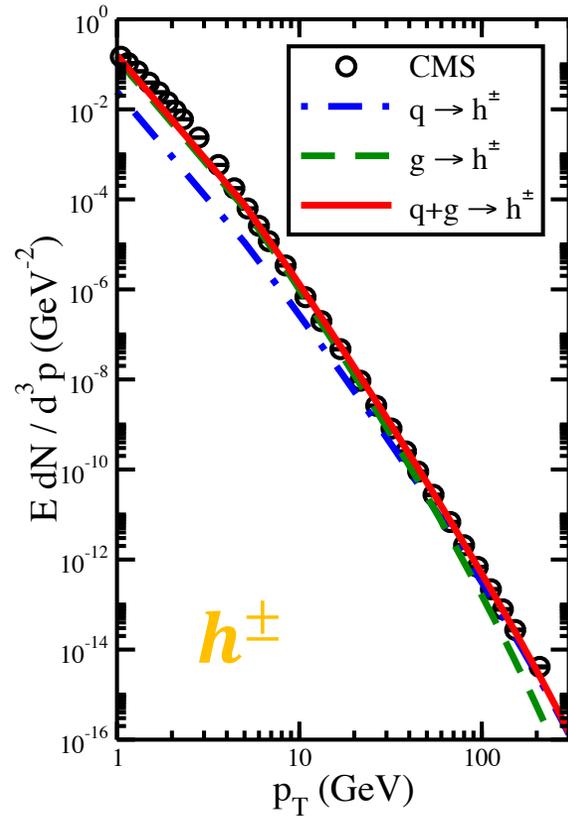


- How to explain the observation of similar  $R_{AA}$  for  $D$  and  $h^\pm$  at high  $p_T$  ?
- Constrain the flavor (mass) dependence of (leading-)parton energy loss.

# High- $p_T$ hadron production in pp @NLO

$$d\sigma_{pp \rightarrow hX} = \sum_{abc} f_a \otimes f_b \otimes d\hat{\sigma}_{ab \rightarrow c} D_{h/c}$$

【WJX, Cao, Qin, Xing, PLB 2020】



- **Essential contribution from gluon fragmentation to hadron production.**
  - dominates  $h^\pm$  production up to 50 GeV.
  - **Contributes to over 40%  $D(B)$  up to 100 GeV.**

# LBT model – elastic and inelastic scatterings

- **Boltzmann equation:**

$$p_a \cdot \partial f_a = E_a [C^{\text{el}}(f_a) + C^{\text{inel}}(f_a)]$$

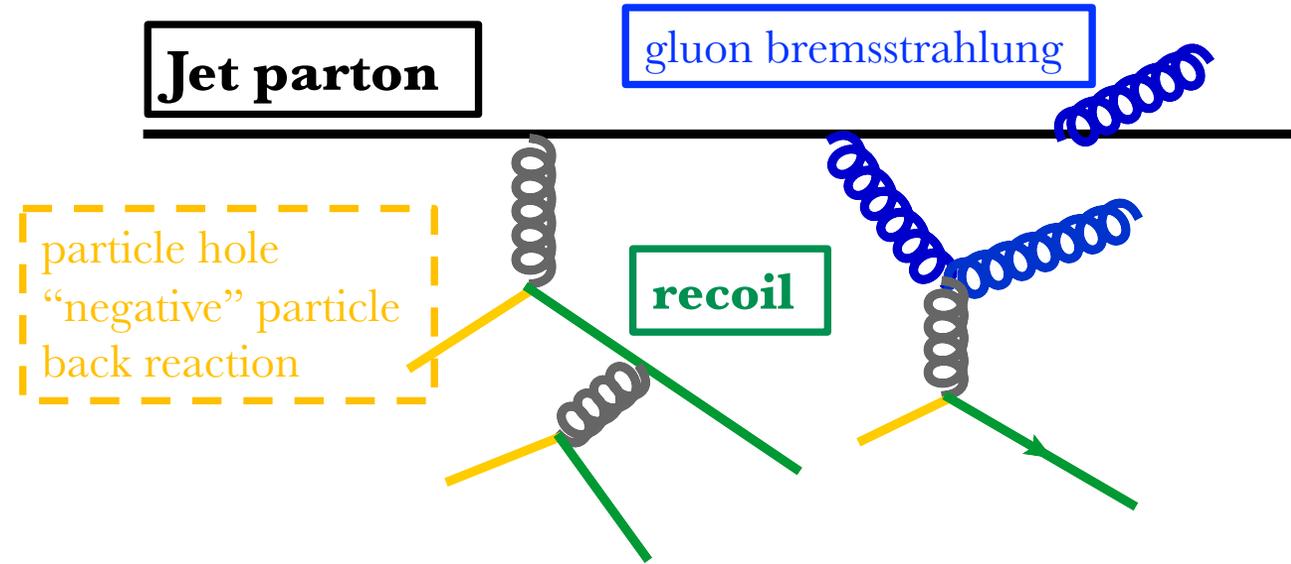
- **Elastic collisions:**

$$\Gamma_a^{\text{el}}(E_a, T) = \sum_{b,(cd)} \frac{\gamma_b}{2E_a} \int \prod_{i=b,c,d} \frac{d^3 p_i}{E_i (2\pi)^3} f_b(E_b, T) \\ \times [1 \pm f_c(E_c, T)][1 \pm f_d(E_d, T)] S_2(\hat{s}, \hat{t}, \hat{u}) \\ \times (2\pi)^4 \delta^{(4)}(p_a + p_b - p_c - p_d) |\mathcal{M}_{ab \rightarrow cd}|^2$$

- **Inelastic collisions:**

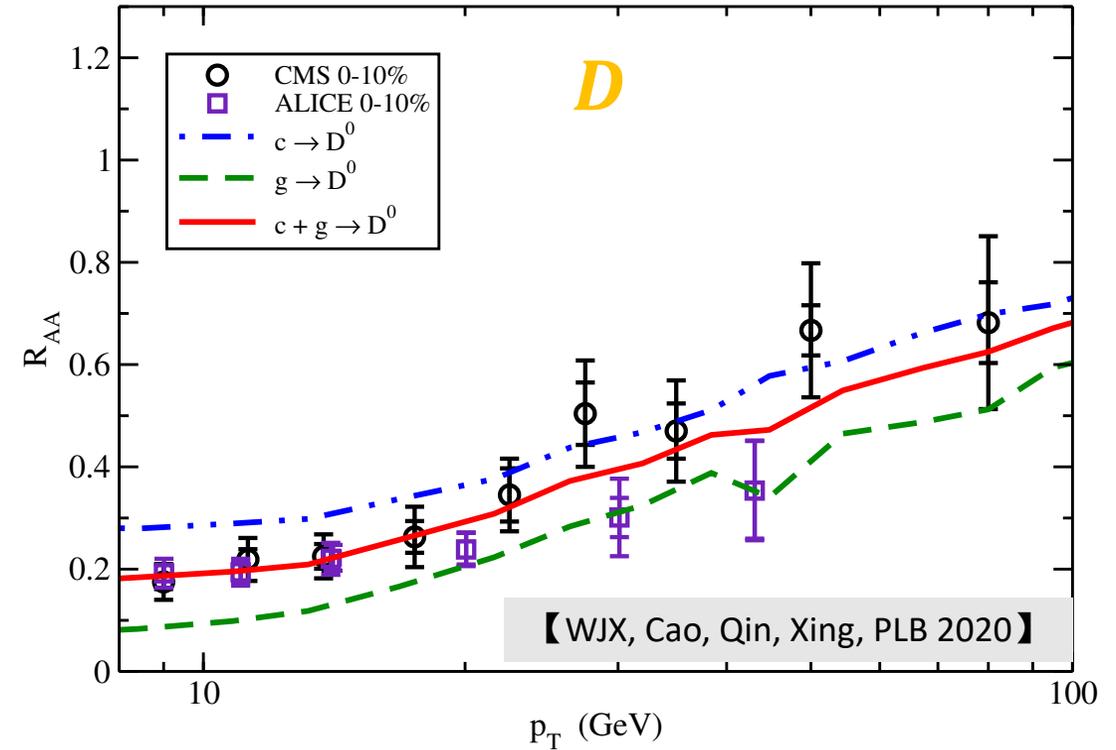
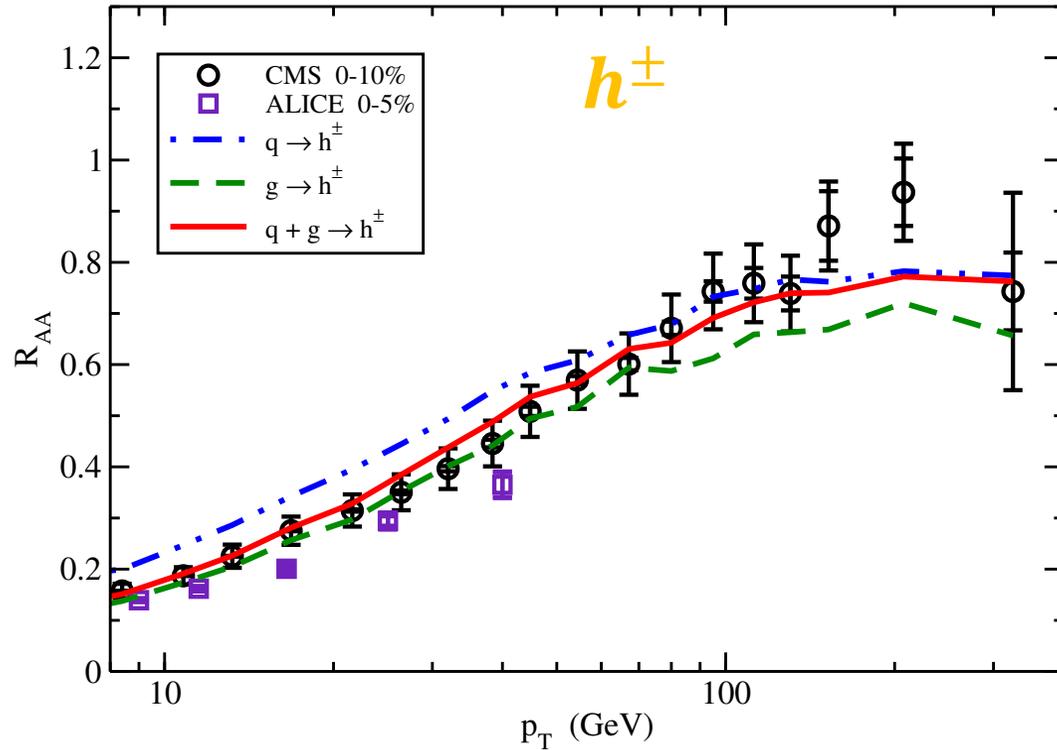
$$\Gamma_a^{\text{inel}}(E_a, T, t) = \int dz dk_{\perp}^2 \frac{1}{1 + \delta^{ag}} \frac{dN_g^a}{dz dk_{\perp}^2 dt}$$

- **Describe jet partons, radiated gluons, recoil partons and “negative” partons within the same transport framework.**



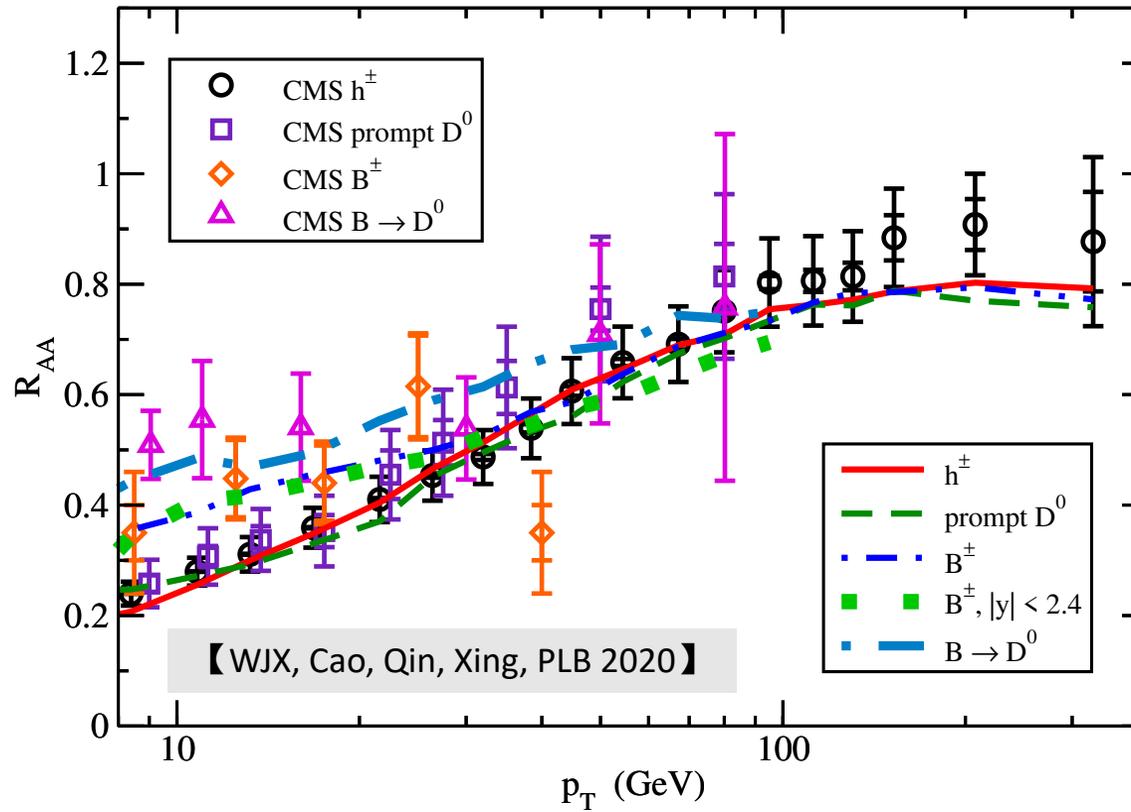
# High- $p_T$ hadron suppression in central Pb-Pb collision

- A state-of-art jet quenching framework (NLO-pQCD + LBT + Hydrodynamics)



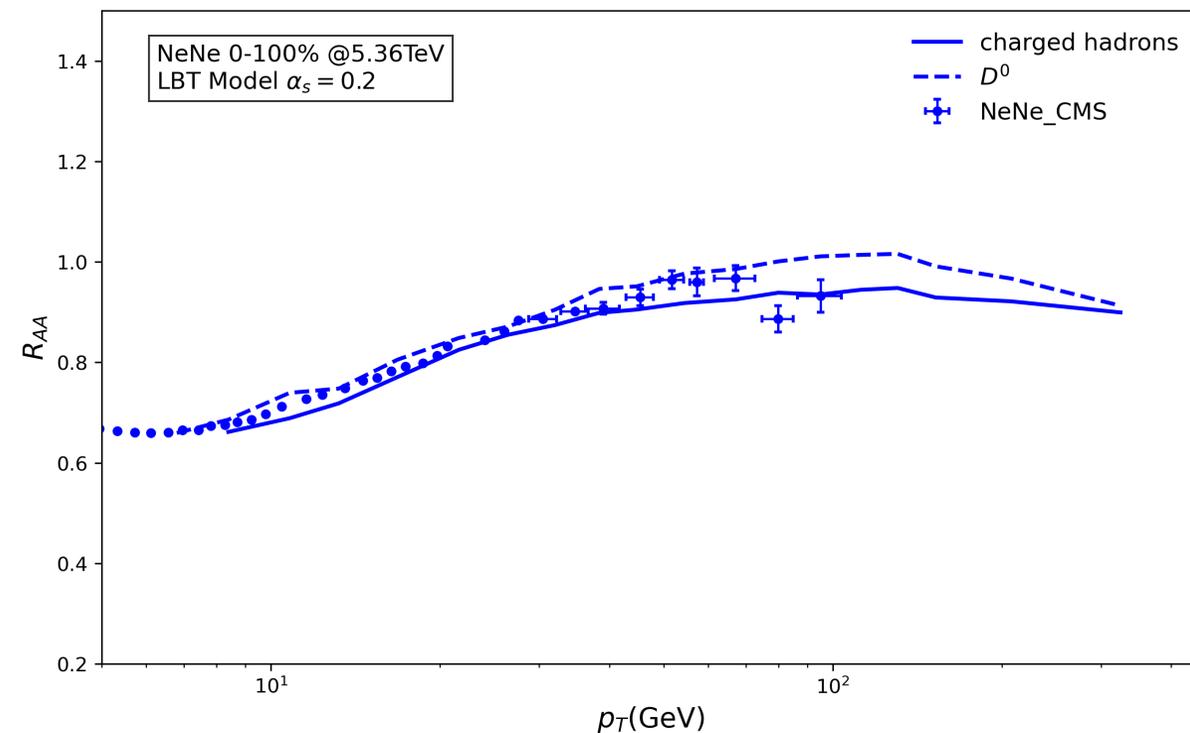
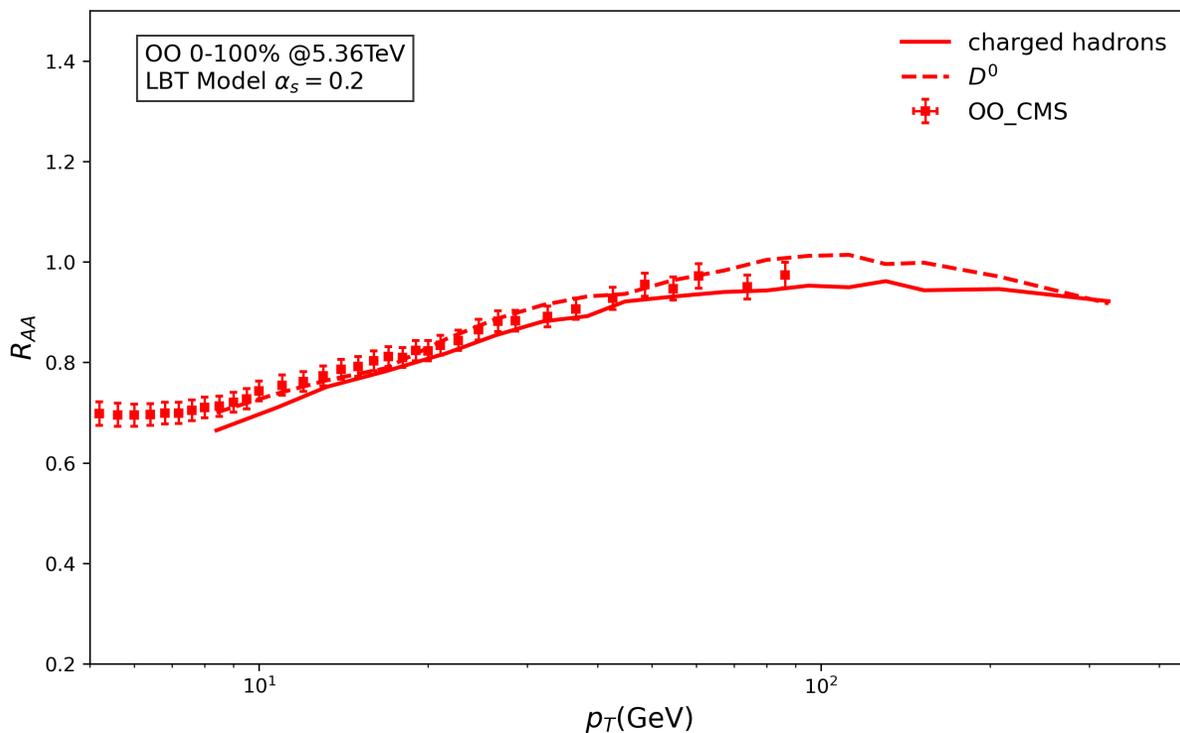
- $g$ -initiated hadron  $R_{AA} < q$ -initiated hadron  $R_{AA}$  [ $\Delta E_g > \Delta E_{q/c}$ ].
- $R_{AA}(c \rightarrow D) > R_{AA}(q \rightarrow h^\pm)$  [ $\Delta E_q > \Delta E_c$ ],  $R_{AA}(g \rightarrow D) < R_{AA}(g \rightarrow h^\pm)$  [different FFs],  
 $\Rightarrow R_{AA}(D) \approx R_{AA}(h^\pm)$ .

# High- $p_T$ hadron suppression in Pb-Pb collision



- **A simultaneous description of charged hadrons,  $D$  mesons,  $B$  mesons and  $B$ -decayed  $D$  mesons  $R_{AA}$ 's for  $p_T > 8$  GeV.**
- **Predict similar  $R_{AA}$  for  $B$  mesons compared to charged hadrons and  $D$  mesons at  $p_T > 30$ -40 GeV.**

# High- $p_T$ hadron suppression in O-O and Ne-Ne



- **LBT model can reproduce the nuclear suppression of high- $p_T$  charged hadrons in light-ion collisions.**

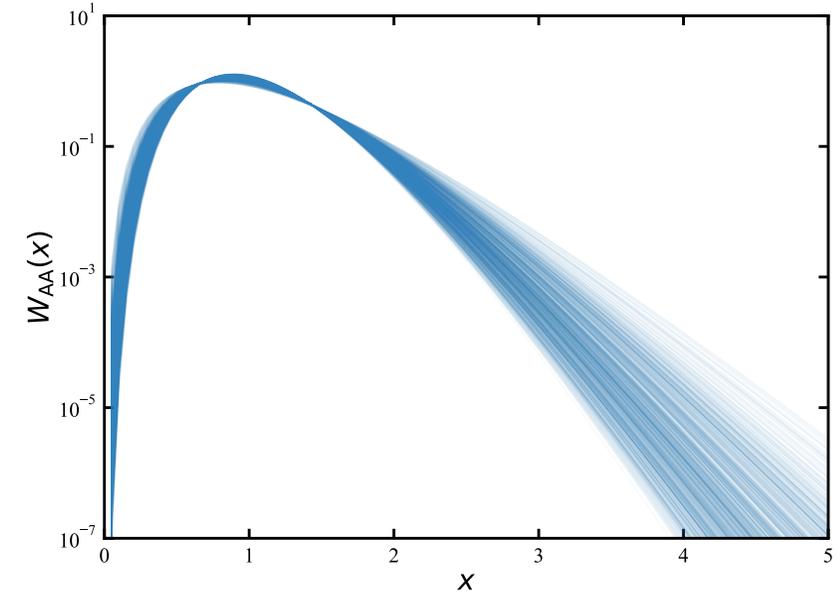
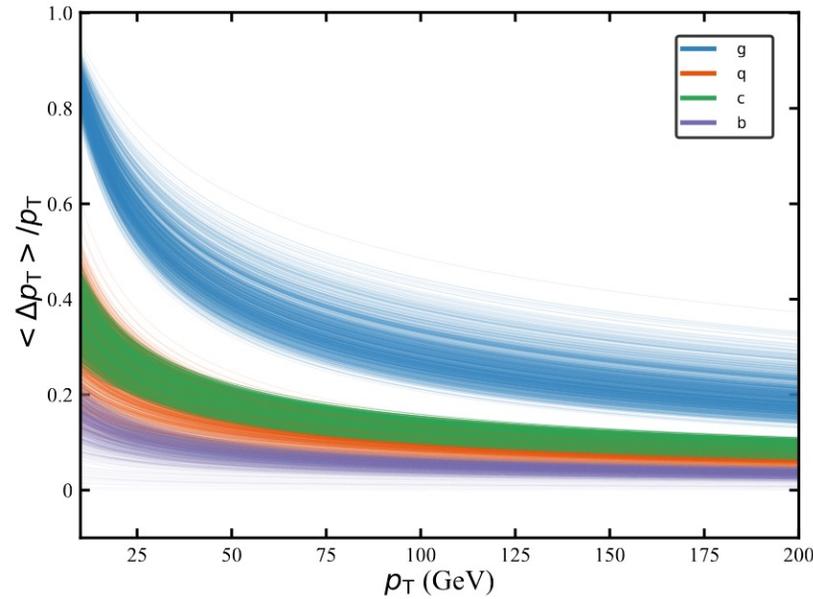
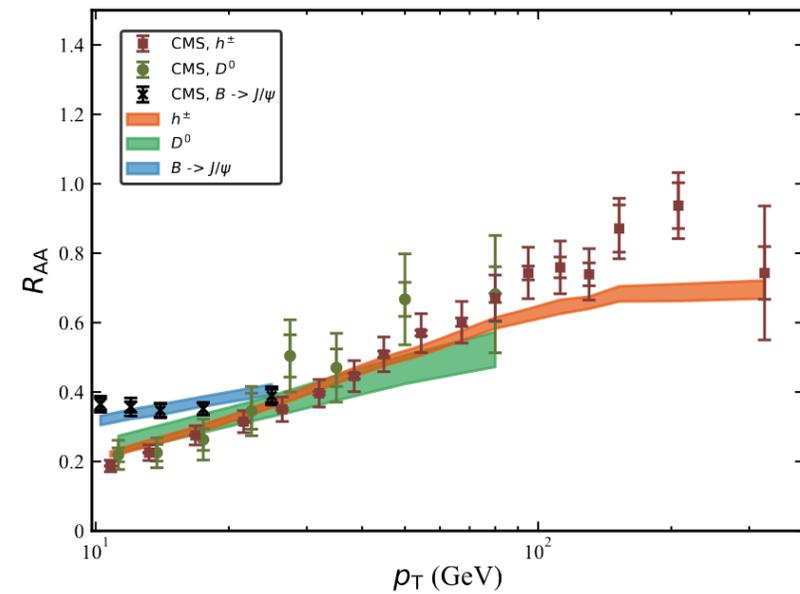
# Parton energy loss from Bayesian analysis

$$\frac{1}{\langle N_{\text{coll}} \rangle} \frac{d\sigma_{AA \rightarrow hX}}{dp_T^h} = \sum_j \int dp_T^j dx dz \frac{d\hat{\sigma}_{p'p' \rightarrow jX}}{dp_T^j}(p_T^j) W_{AA}(x) D_{j \rightarrow h}(z) \delta(p_T^h - z(p_T^j - x \langle \Delta p_T^j \rangle))$$

$$\langle \Delta p_T^j \rangle = C_j \beta_g p_T^\gamma \log(p_T),$$

$$W_{AA}(x) = \frac{\alpha^\alpha x^{\alpha-1} e^{-\alpha}}{\Gamma(\alpha)}$$

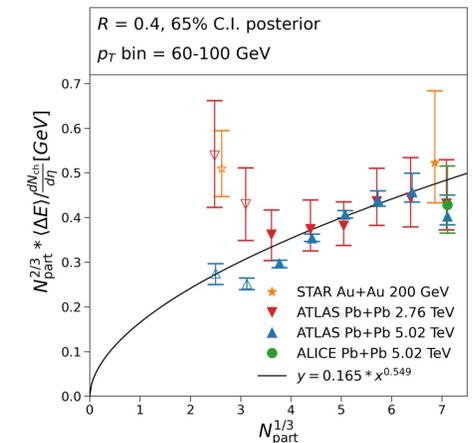
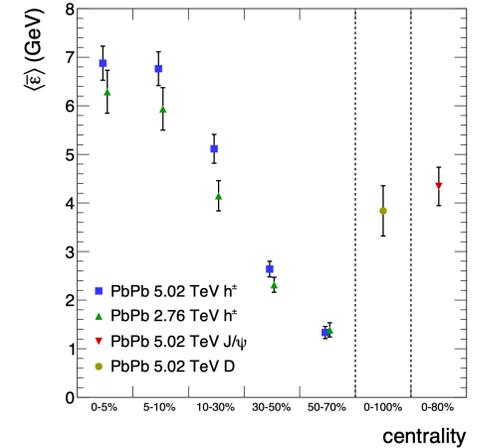
【WJX, Cao, Qin, PLB 2024】



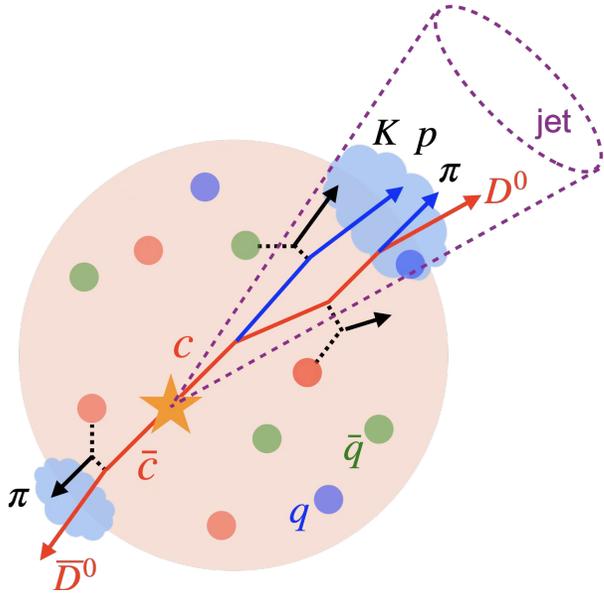
- $\langle \Delta E_g \rangle > \langle \Delta E_q \rangle \sim \langle \Delta E_c \rangle > \langle \Delta E_b \rangle$ .
- Direct extraction of flavor dependence of parton energy loss in QGP from data.
- Provides a stringent test of  $p$ QCD calculation in parton-medium interaction.

# Other works on extracting parton energy loss

- **F. Arleo, PRL 2017.**
  - Take  $W_{AA}(x)$  from BDMPS medium-induced gluon spectrum, and extract  $\langle \Delta p_T \rangle R_{AA}$  data on  $h^\pm, D, J/\psi$ .
- **He, Pang and Wang, PRL 2019.**
  - Use a general ansatz of jet  $W_{AA}(x)$ , and extract flavor-averaged jet  $\langle \Delta P_T \rangle$  and  $W_{AA}(x)$  from  $R_{AA}$  data on single inclusive &  $\gamma$ -jets.
- **Wu, Ke and Wang, PRC 2023**
  - Extract L-dependence of jet  $\langle \Delta P_T \rangle$  from  $R_{AA}$  data on single inclusive &  $\gamma$ -jets.
- **Zhang, Liao, Qin, Xing, Sci. Bull. 2023**
  - Extract gluon & charm quark  $\langle \Delta p_T \rangle$  and  $W_{AA}(x)$  from  $J/\psi$   $R_{AA}$  data.

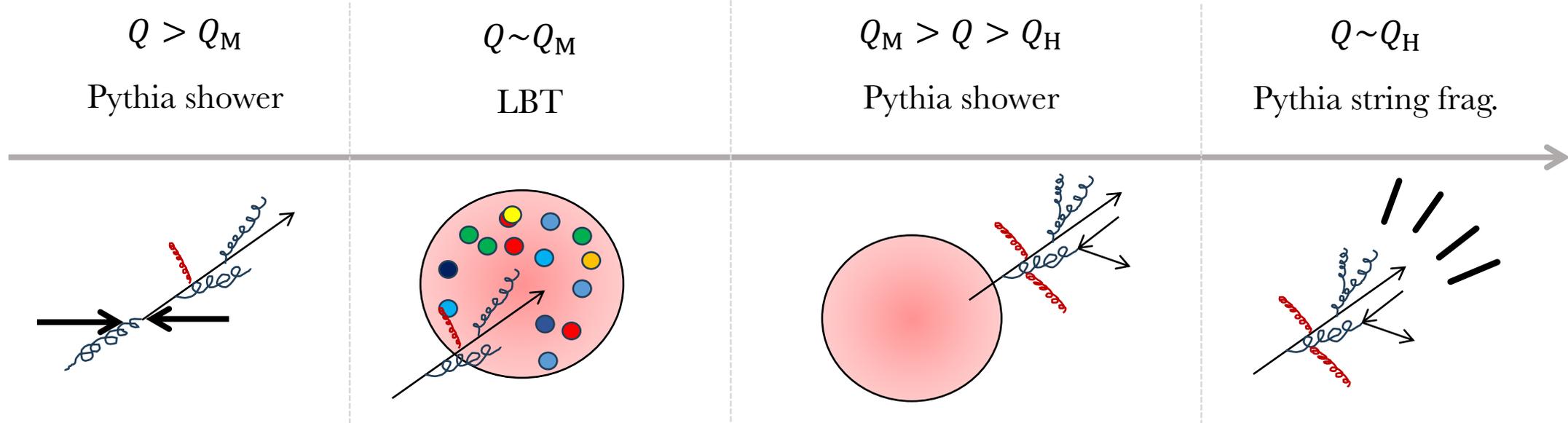


# From leading hadron to jet/jet-substructure



- **Dead-cone effect on medium-induced radiation can be indirectly studied from the flavor hierarchy of leading hadron suppression in heavy-ion collisions.**
- **What else can jet/jet substructure tell us ?**

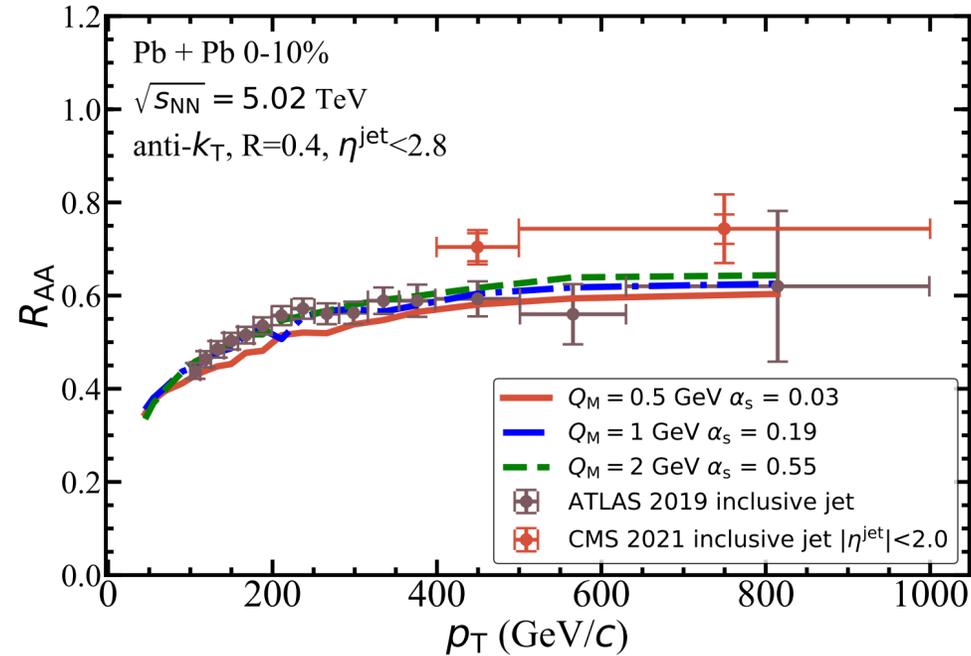
# Jet quenching framework in QGP



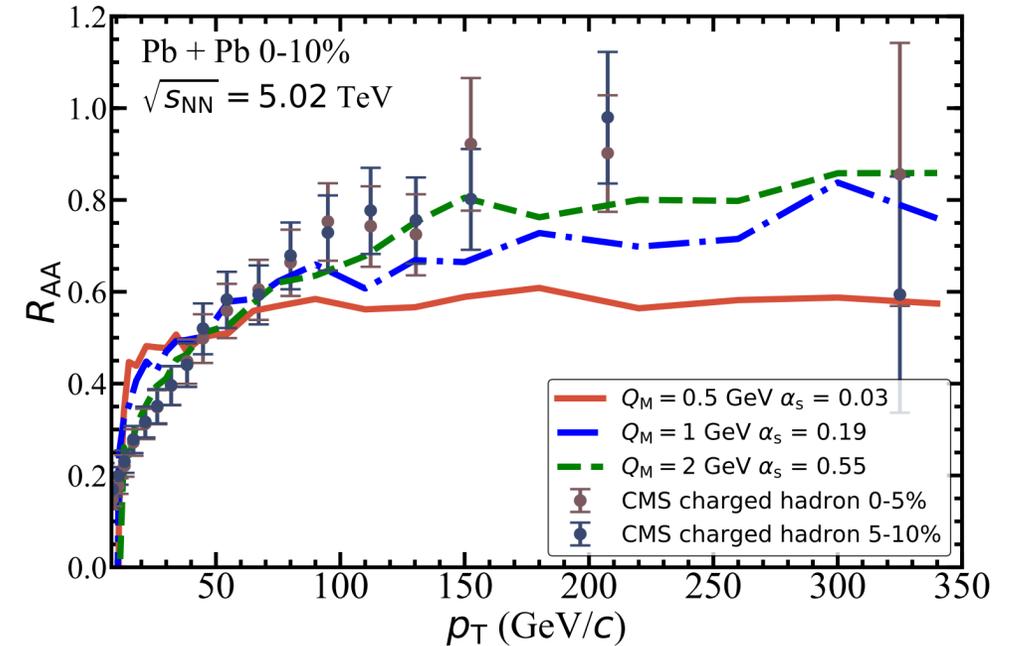
- $Q_M$ : medium evolution scale
- $Q_H$ : hadronization scale,  $\sim 0.5\text{GeV}$

# $Q_M$ (medium scale) effect on jet & hadron $R_{AA}$

## Inclusive jet :

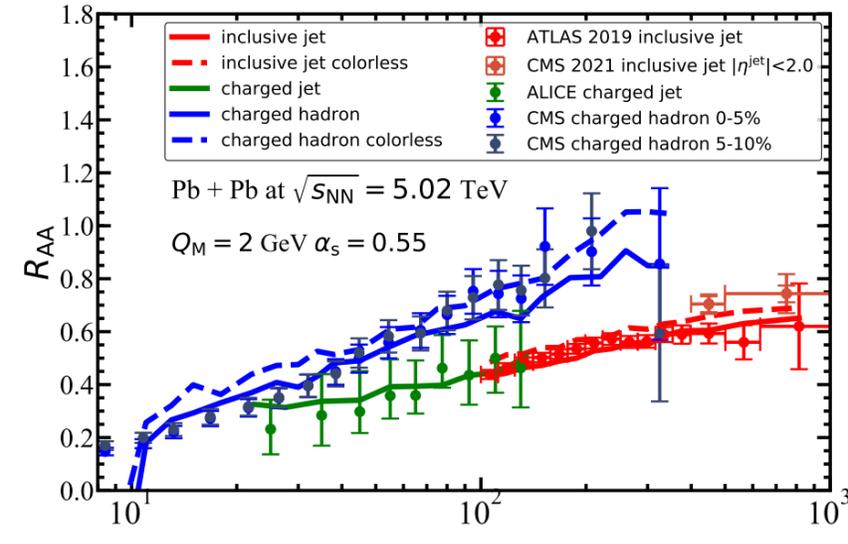


## Charged hadron :

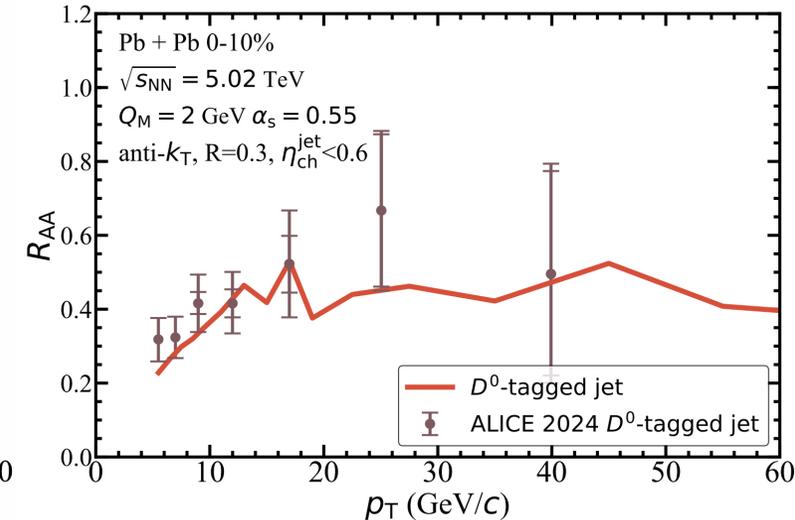
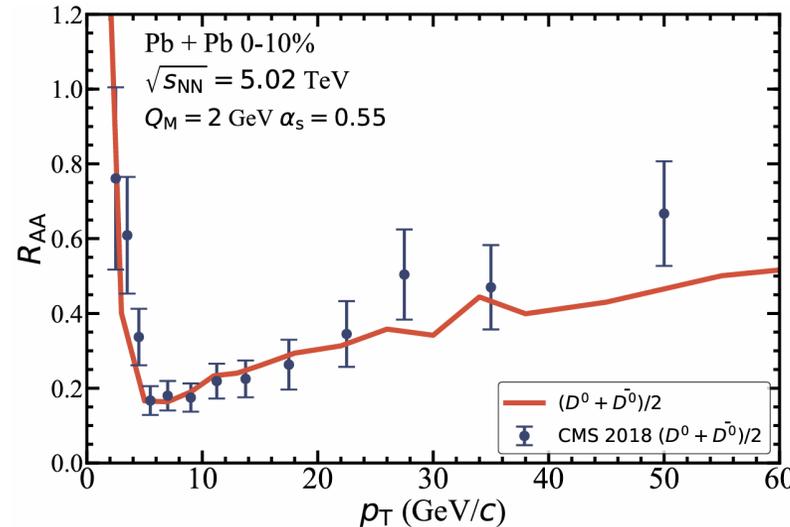


- $Q_M = 2$  GeV provides a simultaneous description of jet and hadron  $R_{AA}$ .
- Setting larger  $Q_M$  enhances the energy loss of softer partons while leaves hard partons less affected.

# Light and heavy flavor jet & hadron $R_{AA}$



【Dang, et al, in preparation】

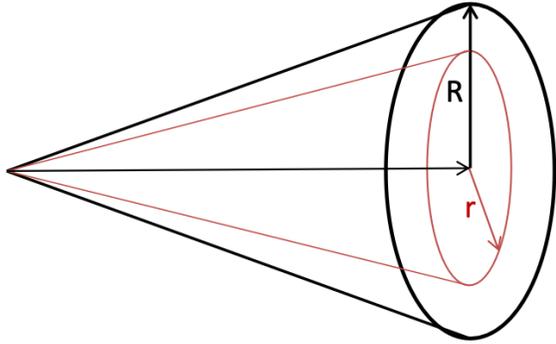


- **A simultaneous description of jet and hadron  $R_{AA}$  for both heavy and light flavors.**
- **Colorless hadronization approach — where strings are formed by connecting the particles that are closest in phase space — is used as an estimate of systematic errors.**

# Jet shape

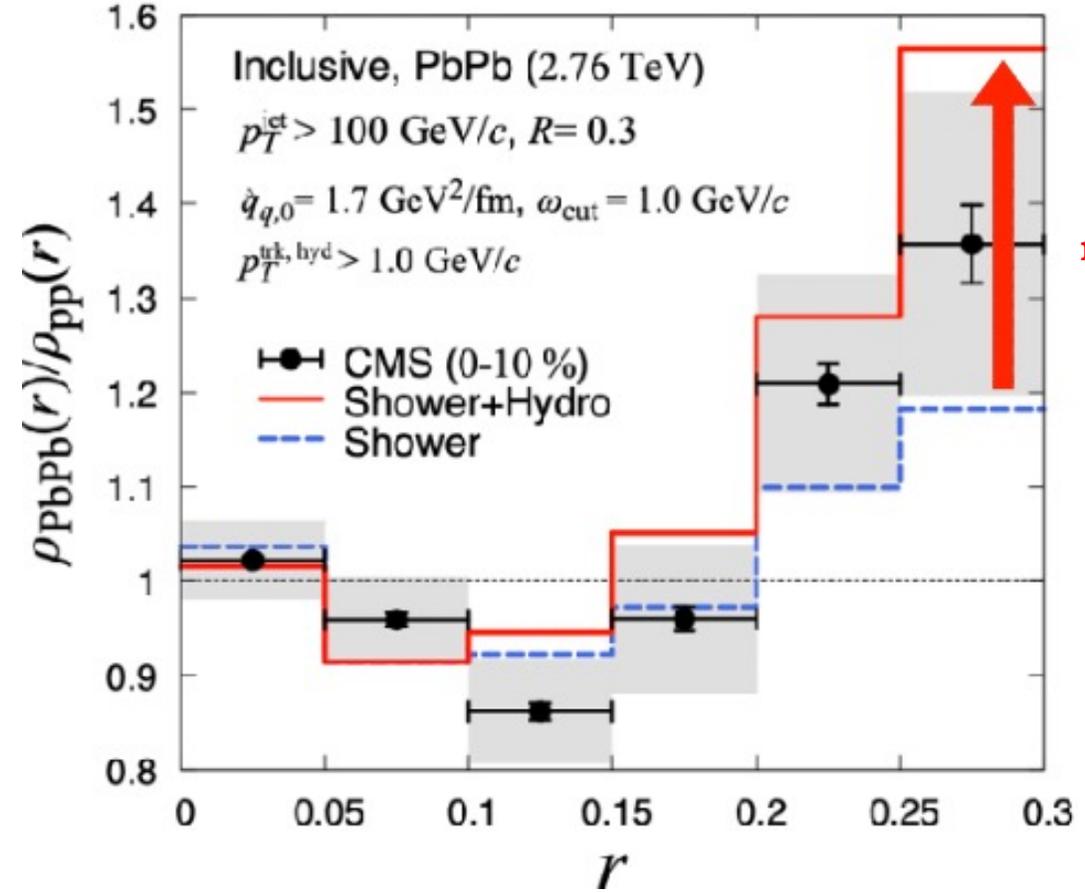
Tachibana, et al, PRC (2017)

$p_T$  distribution of jet constituents along  $r$  :



$$\rho(r) = \frac{1}{\delta r} \frac{1}{N_{\text{jet}}} \sum_{\text{jet}} \frac{\sum_{\text{trk} \in (r_a, r_b)} p_T^{\text{trk}}}{\sum_{\text{trk}} p_T^{\text{trk}}}$$

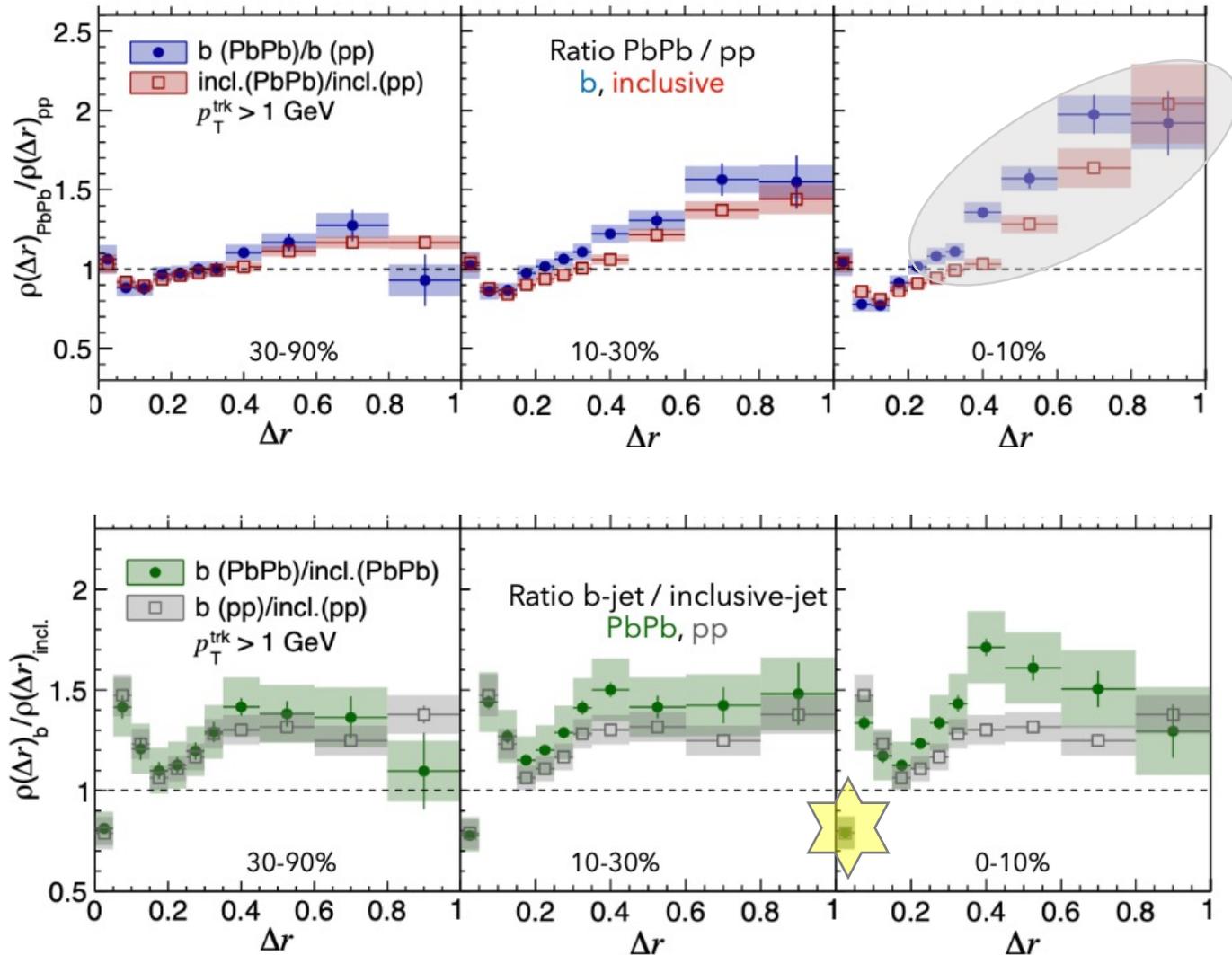
$$r = \sqrt{(\eta_{\text{trk}} - \eta_{\text{jet}})^2 + (\phi_{\text{trk}} - \phi_{\text{jet}})^2}$$



**Medium response**

- **Medium response has a significant contribution to PbPb/pp ratio of jet shape at large  $r$ .**

# Heavy and light flavor jet shape



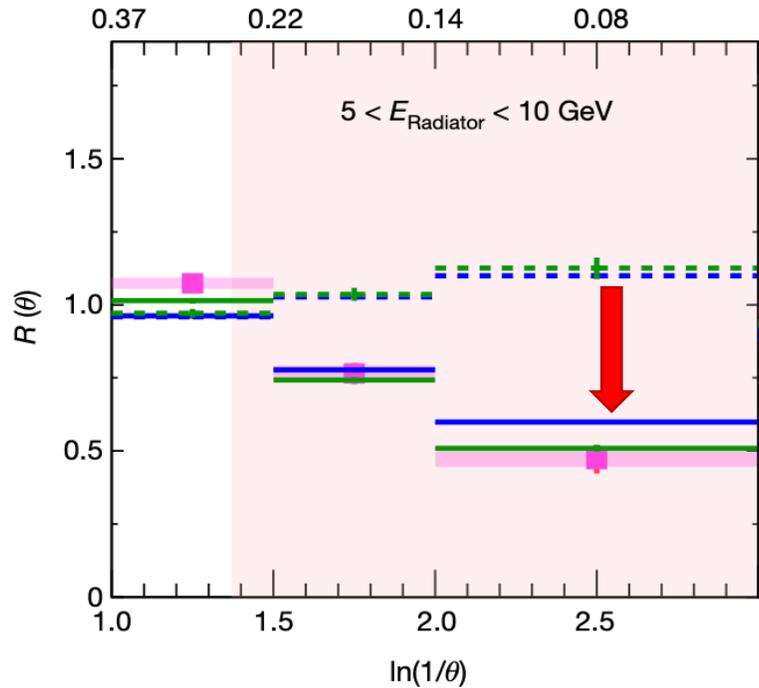
- **PbPb/pp ratio**
- **Larger PbPb/pp ratio for b jets than for inclusive jets in the large- $\Delta r$  region.**
- **b-jet/inclusive-jet ratio**
- **A depletion is observed for  $\Delta r \leq 0.05$ , which indicates the dead-cone effect.**

【CMS, PLB (2023)】

# Mass effect in parton splitting – dead-cone effect

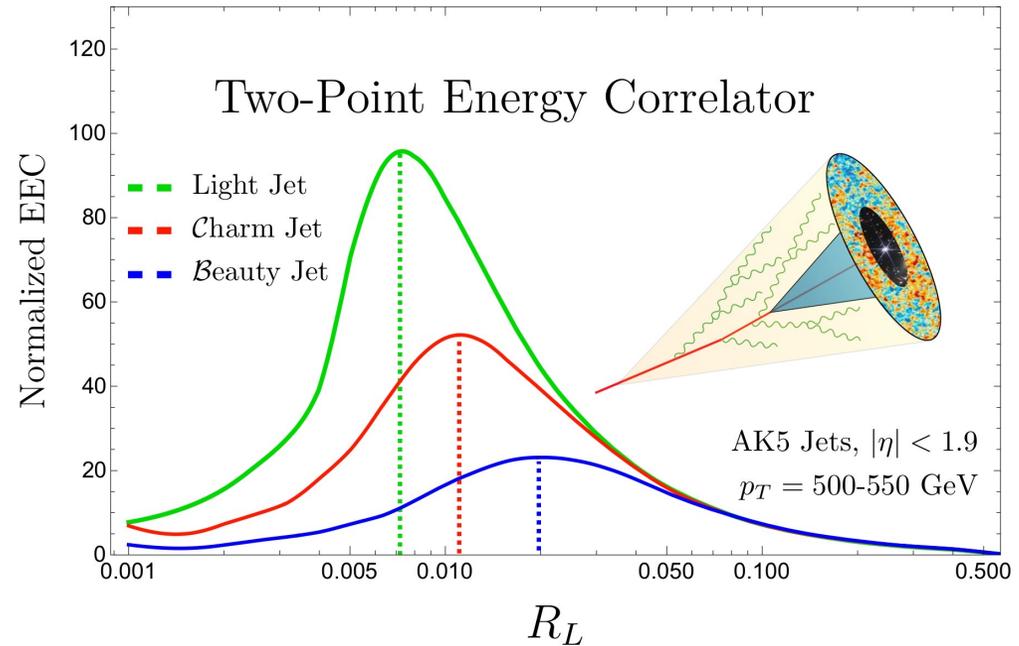
## Splitting angle distribution

$$R(\theta) = \frac{1}{N^{\text{D}^0 \text{ jets}}} \frac{dn^{\text{D}^0 \text{ jets}}}{d\ln(1/\theta)} \bigg/ \frac{1}{N^{\text{inclusive jets}}} \frac{dn^{\text{inclusive jets}}}{d\ln(1/\theta)}$$

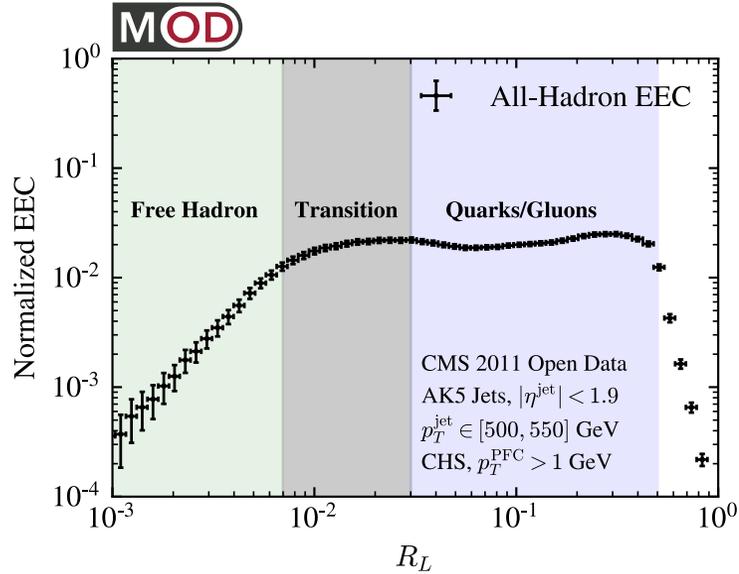


## E-weighted angular distribution

$$\frac{d\Sigma_{\text{EEC}}}{dR_L} = \int d\sigma(\Delta R_{ij}) \frac{p_{T,i} p_{T,j}}{p_{T,\text{jet}}^2} \delta(\Delta R_{ij} - R_L), \quad \Delta R_{ij} = \sqrt{\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2}$$

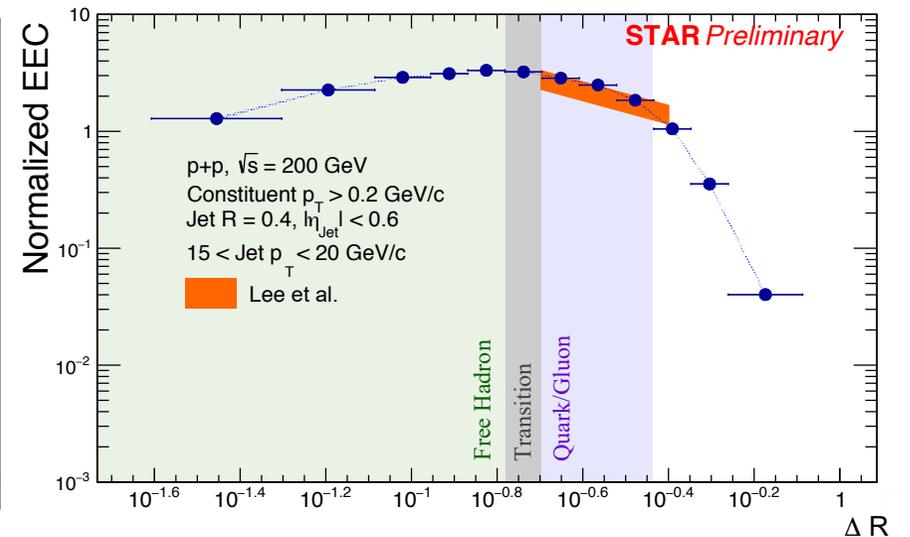
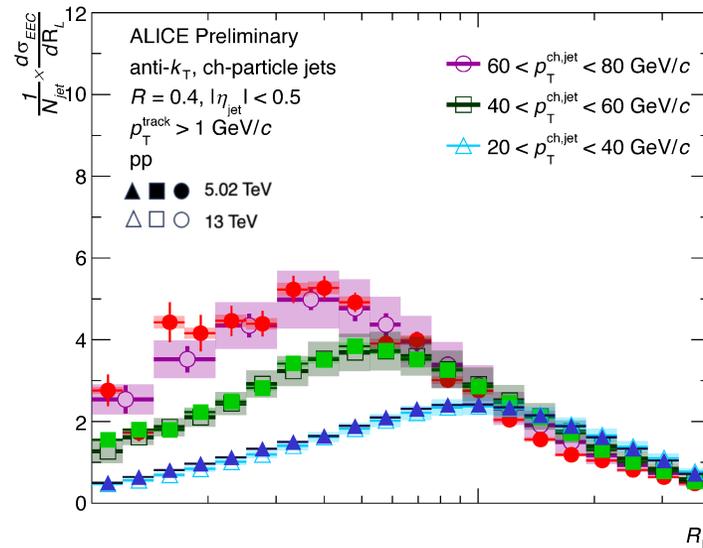
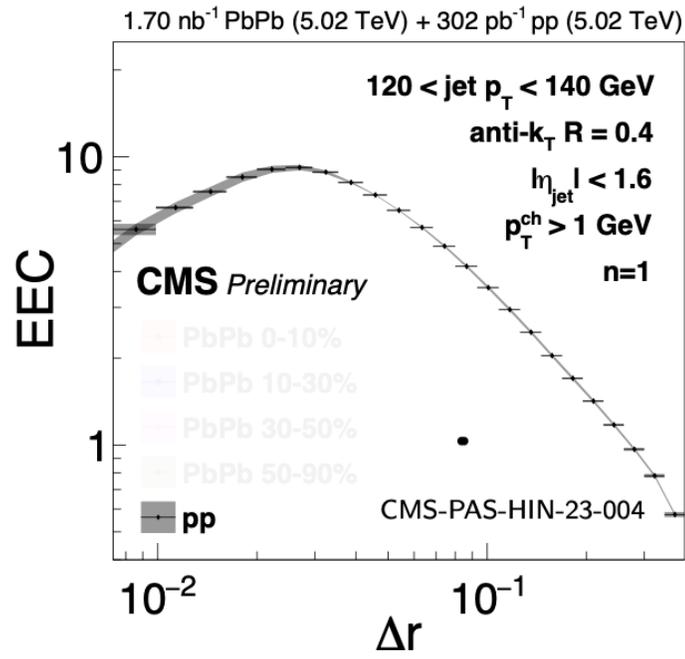


# Jet EEC in pp



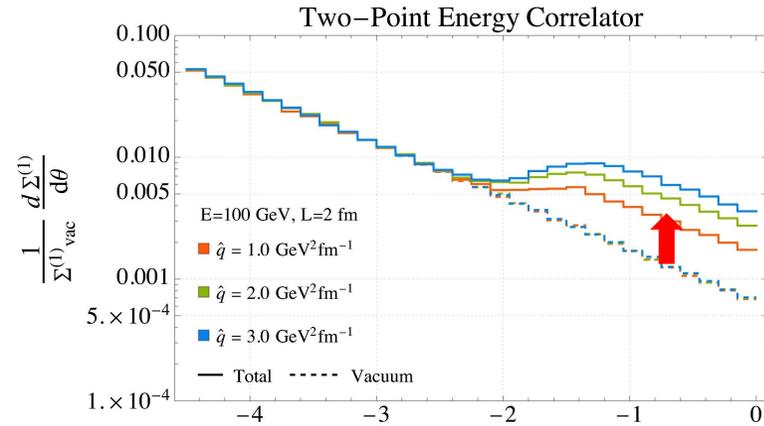
$$\frac{d\Sigma_{\text{EEC}}}{dR_L} = \int d\sigma(\Delta R_{ij}) \frac{p_{T,i} p_{T,j}}{p_{T,\text{jet}}^2} \delta(\Delta R_{ij} - R_L), \quad \Delta R_{ij} = \sqrt{\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2}$$

- Jet EEC is proposed in **PRL 130 (2023) 5, 051901**.
- Jet EEC separates pert. region and non-pert. region.
- Verified by experiments at RHIC and the LHC.

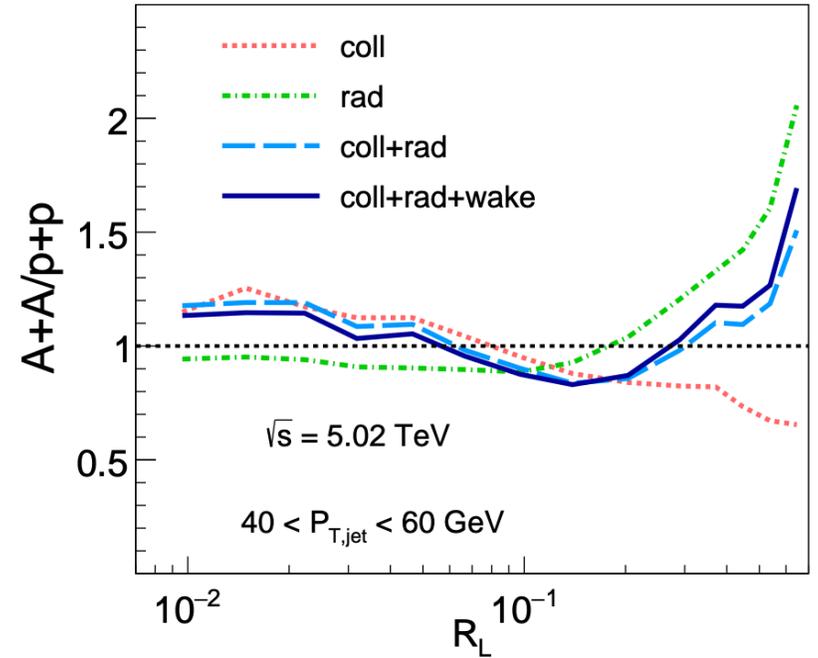
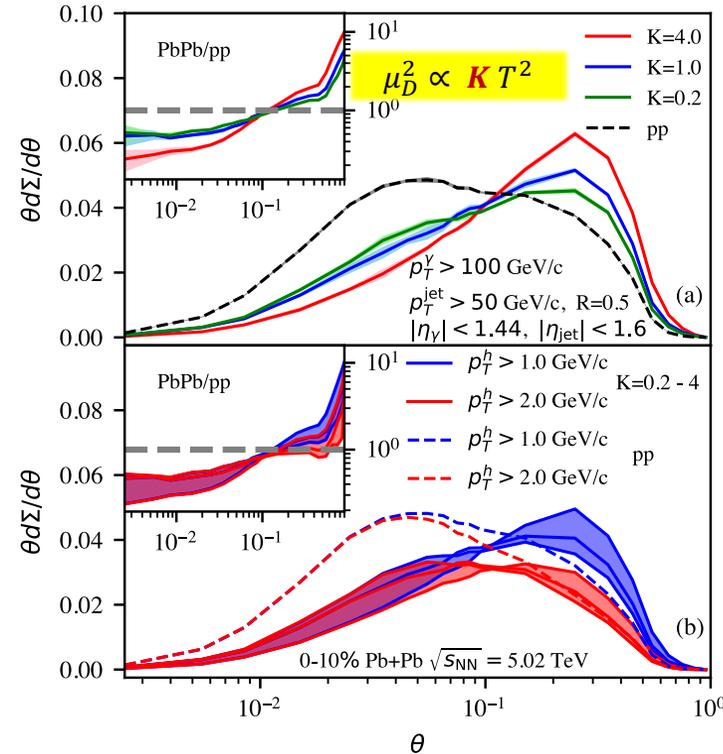


# Jet EEC in heavy-ion collisions

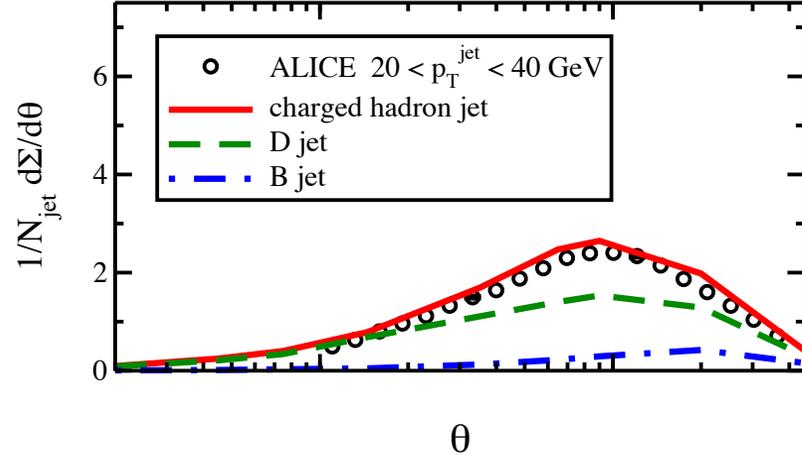
- Jet EECs imprints **the scale of medium-induced radiation**, **medium screening mass**, and **jet-medium interaction mechanism**.



【Andres, et al., in PRL (2023)】  
 【Yang, et al., PRL (2024)】  
 【Chen, et al., arXiv:2409.13996】

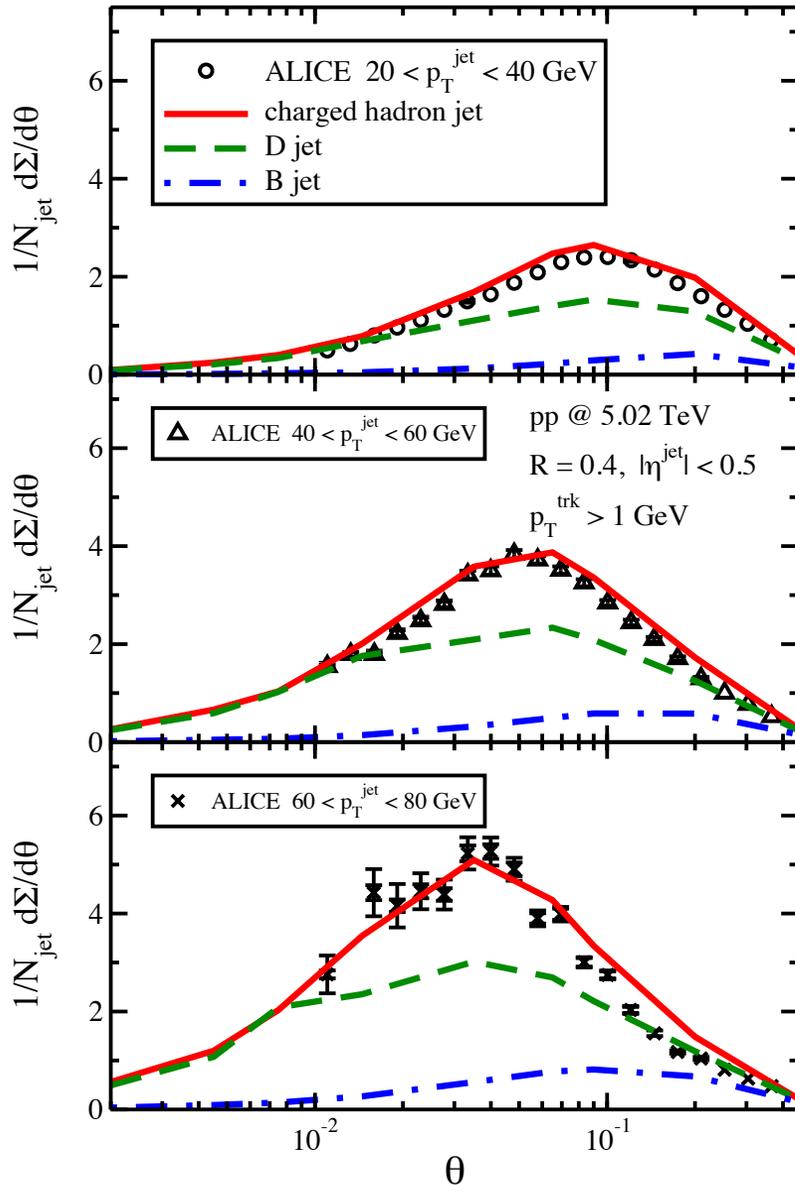


# Light vs. heavy flavor jet EEC in pp



- **Jet in pp: Pythia 8 simulation**
- **Flavor (mass) dependence:**
  - $\Sigma(\text{charged jet}) > \Sigma(\text{D jet}) > \Sigma(\text{B jet})$
  - $\theta^{\text{peak}}(\text{charged jet}) < \theta^{\text{peak}}(\text{D jet}) < \theta^{\text{peak}}(\text{B jet})$
- **Transition angle  $\theta^{\text{peak}} \sim \Lambda_{\text{QCD}}/p_T^{\text{jet}} (m_Q/p_T^{\text{jet}})$**

# Light vs. heavy flavor jet EEC in pp



- **Jet in pp: Pythia 8 simulation**

- **Flavor (mass) dependence:**

- $\Sigma(\text{charged jet}) > \Sigma(\text{D jet}) > \Sigma(\text{B jet})$

- $\theta^{\text{peak}}(\text{charged jet}) < \theta^{\text{peak}}(\text{D jet}) < \theta^{\text{peak}}(\text{B jet})$

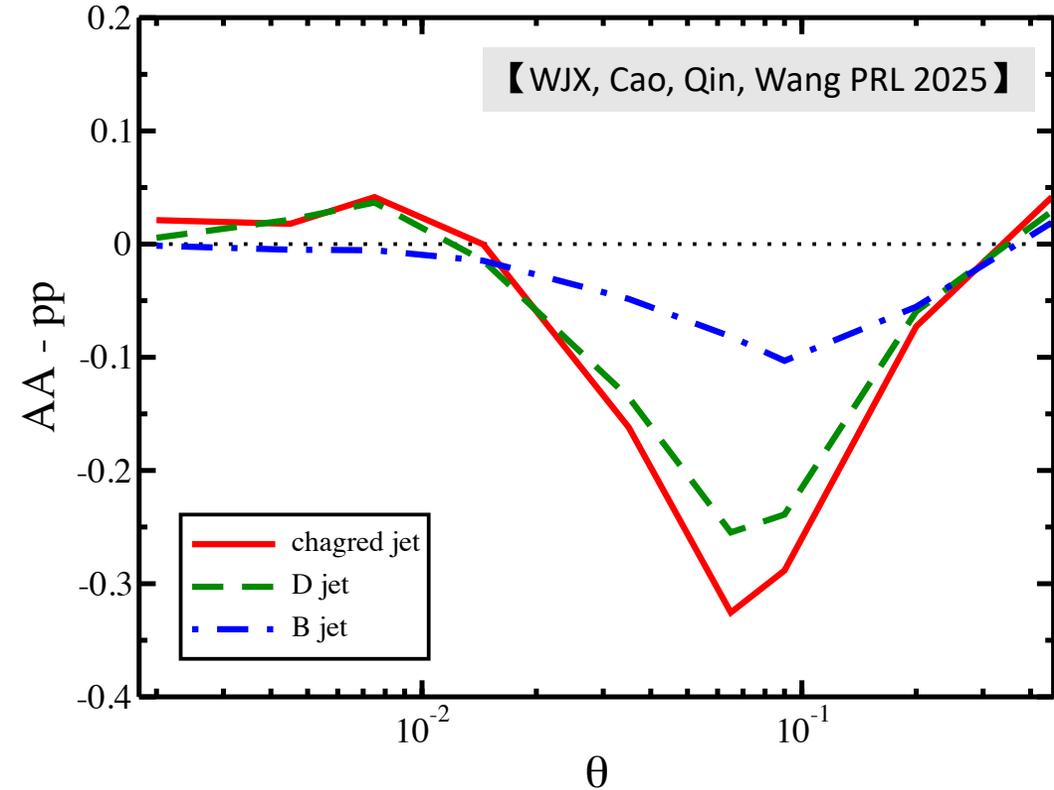
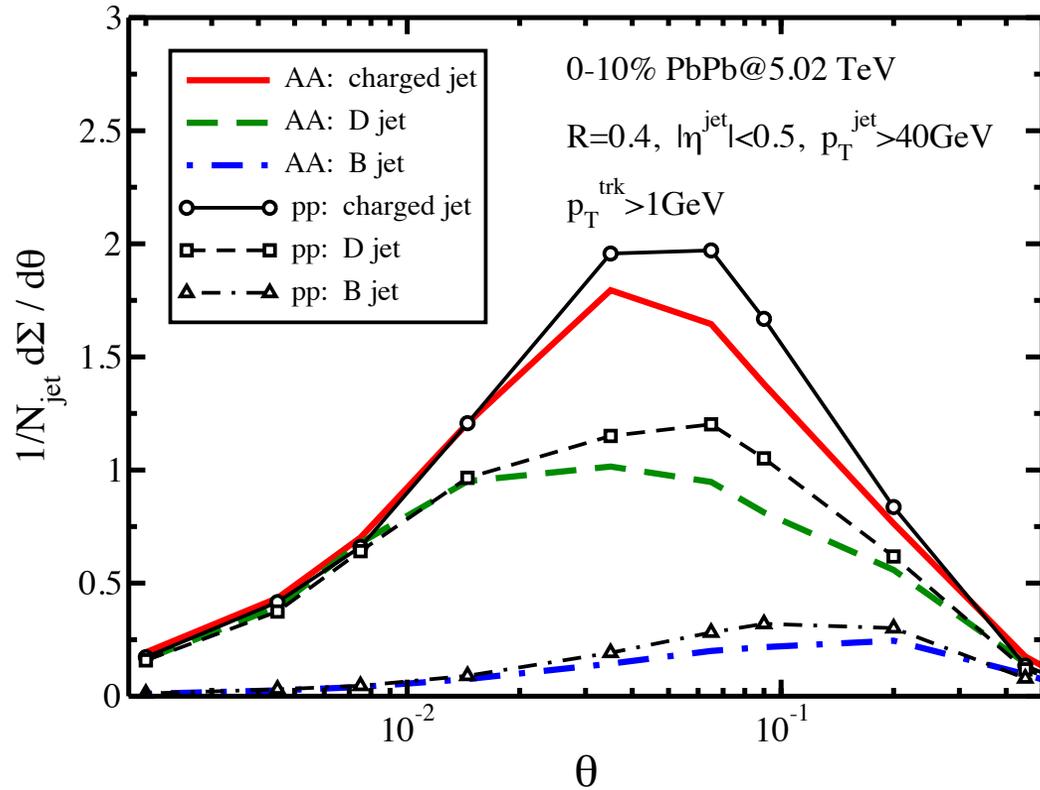
- **Transition angle  $\theta^{\text{peak}} \sim \Lambda_{\text{QCD}}/p_T^{\text{jet}} (m_Q/p_T^{\text{jet}})$**

- **Jet energy dependence:**

- **Higher  $p_T$  jet peaks at smaller angle.**

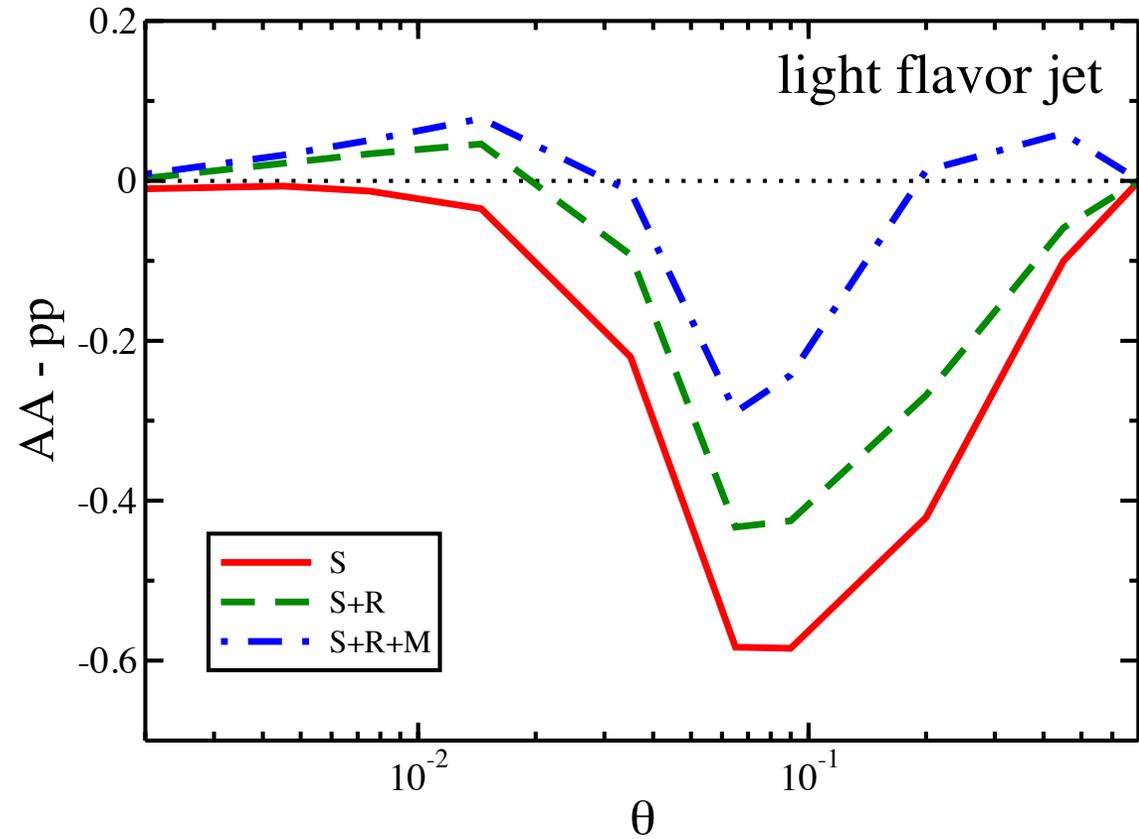
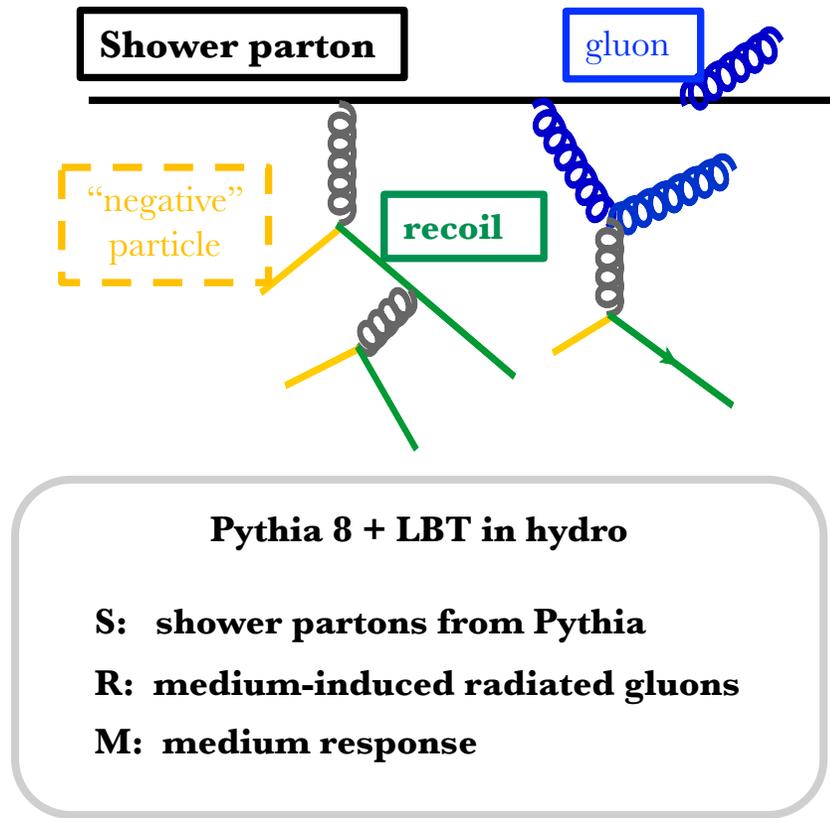
【WJX, Cao, Qin, Wang PRL 2025】

# Light vs. heavy flavor jet EEC in Pb-Pb



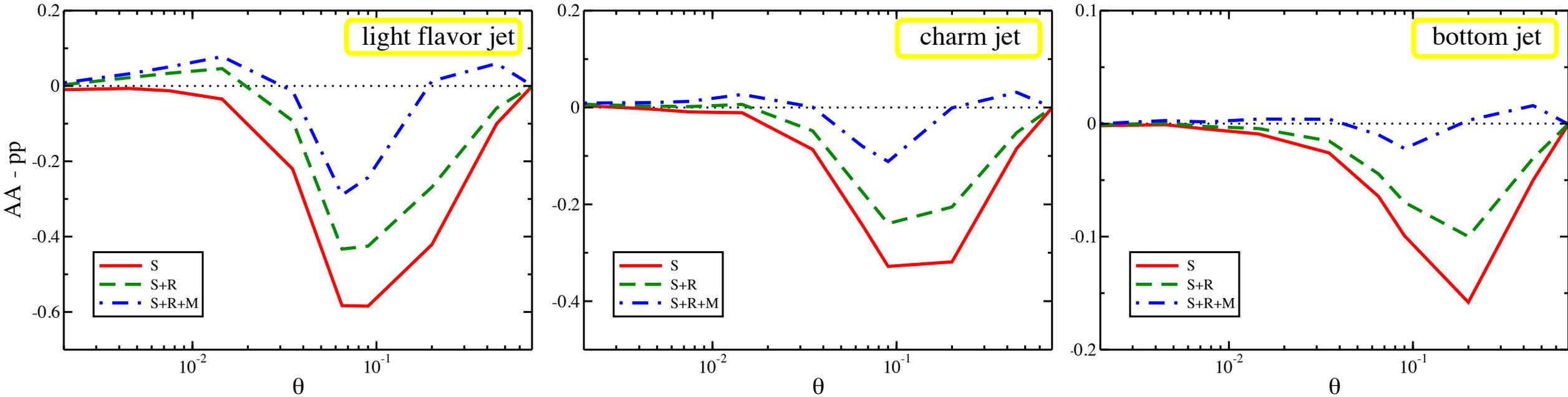
- **Flavor hierarchy of jet EEC preserves in AA.**
- **General feature of nuclear modification (AA-pp): suppression at intermediate  $\theta$ , enhancement at small  $\theta$  (except for B-jet) and large  $\theta$ .**

# Different contributions to medium modification on EEC



- **Jet energy loss causes suppression over entire  $\theta$  region.**
- **Medium-induced gluon radiation enhances EEC at small  $\theta$ .**
- **Medium response enhances EEC at large  $\theta$ .**

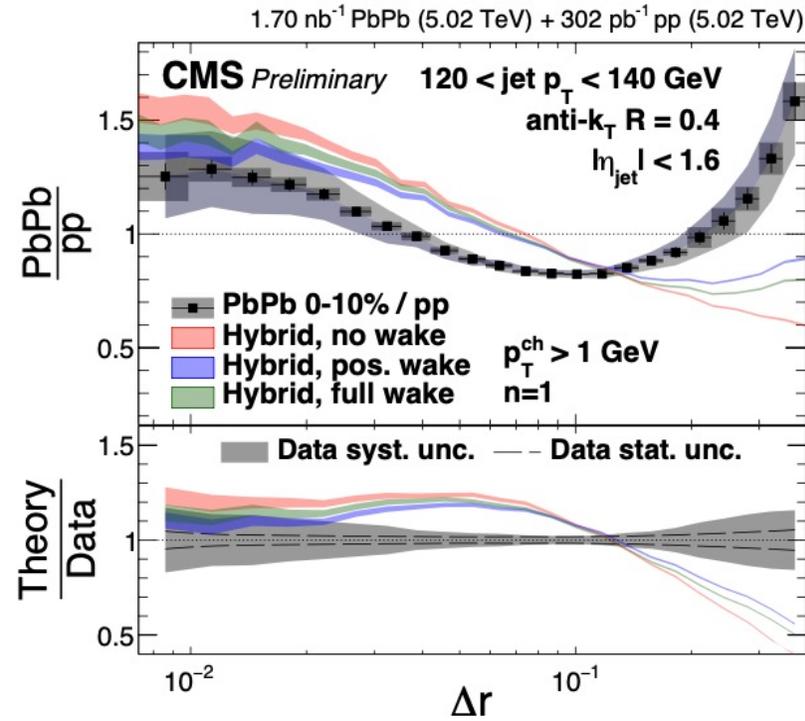
# Mass effect on jet EEC modification



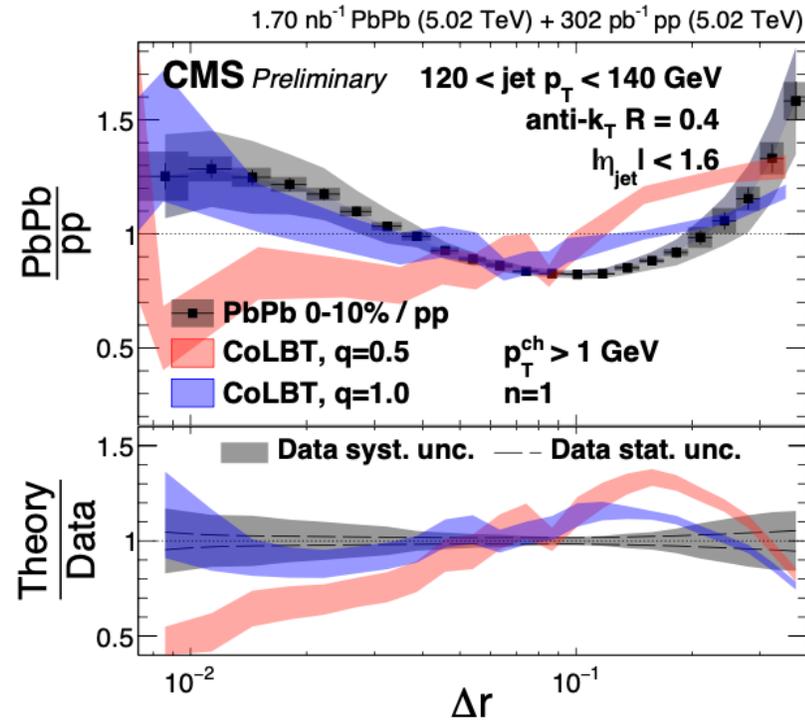
- **For heavy-quarks-tagged jets, both suppression and enhancement of EEC becomes weaker.**

# Jet EEC: model comparison with PbPb/pp ratio

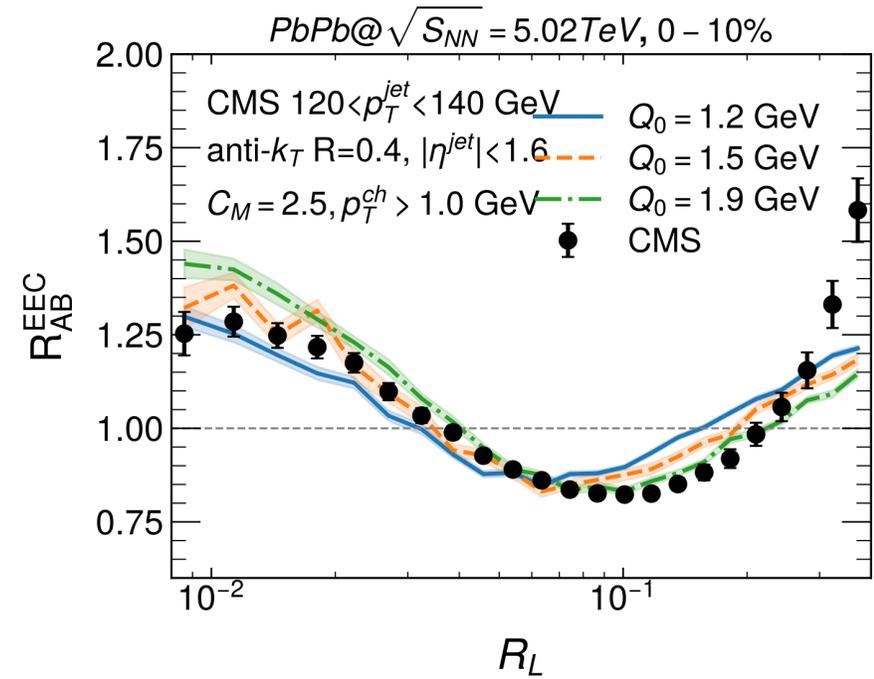
## Hybrid model



## CoLBT model

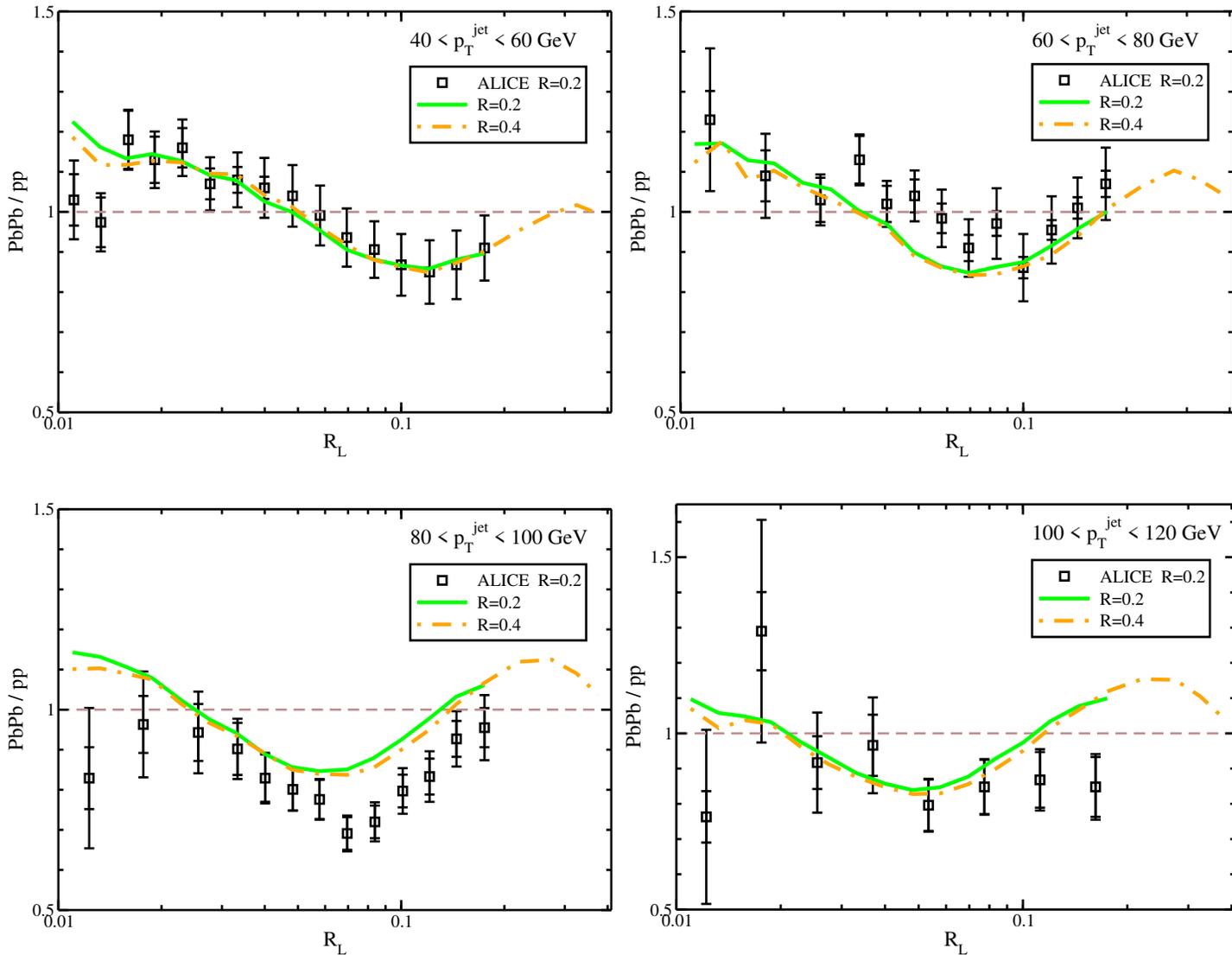


## LIDO model



- Hybrid model does not predict enough enhancement at large  $\Delta r$ .
- CoLBT and LIDO can reproduce the structure of PbPb/pp ratio.

# LBT vs. ALICE data



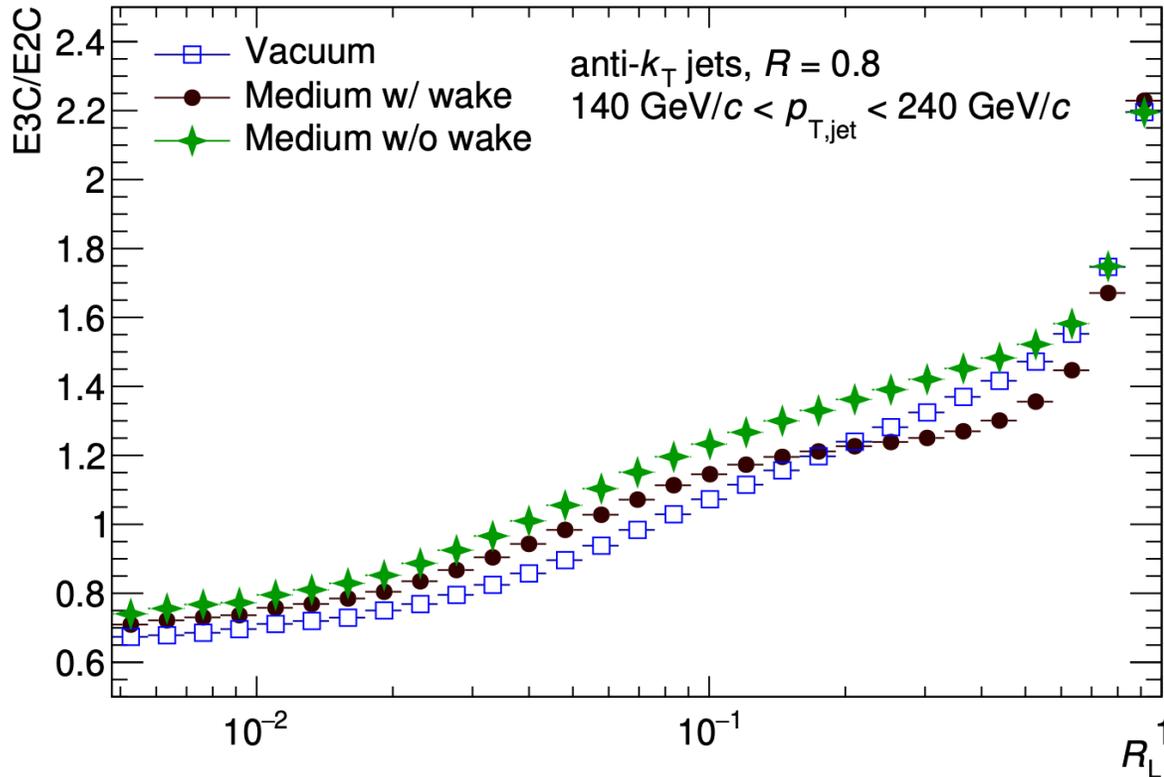
- **LBT describes the PbPb/pp ratio of jet EEC.**

- **LBT predicts a weak dependence of PbPb/pp ratio on jet cone size  $R$ .**

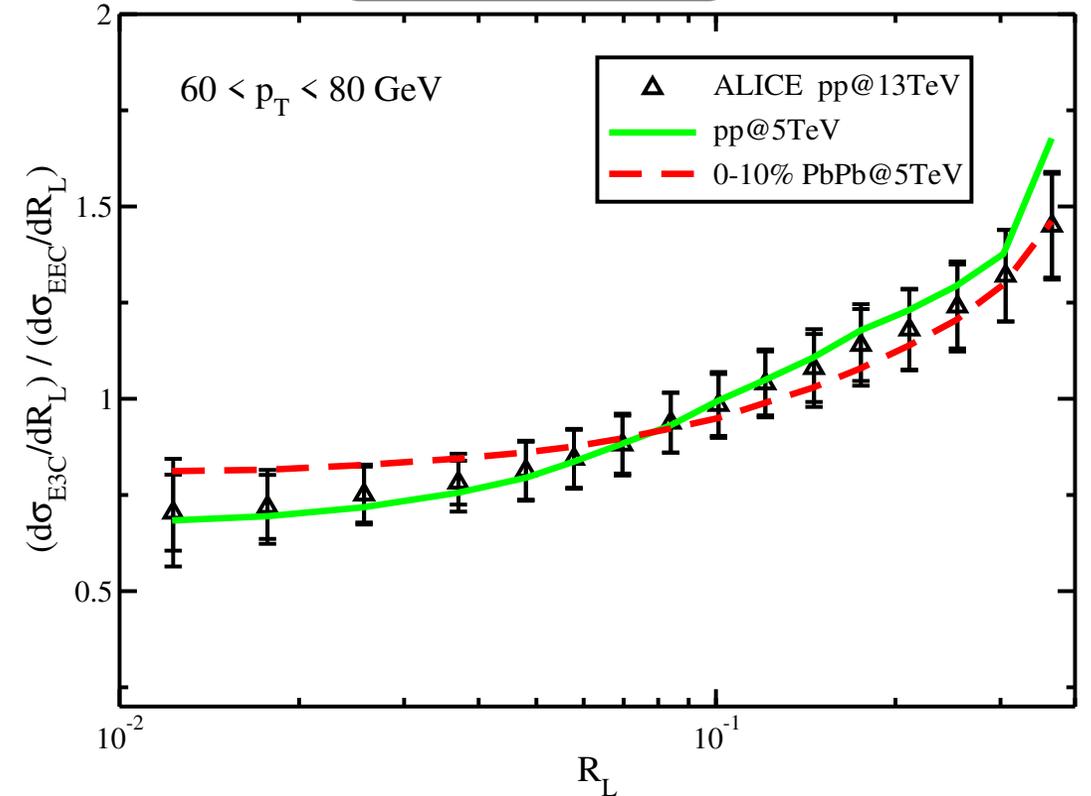
【ALICE: ALI-PREL-557542】

# Extension to E3C/E2C

Hybrid model



LBT model



- **With medium response, both Hybrid and LBT model predict E3C/E2C get suppressed at large  $R_L$ .**
- **Can we use multi-particle correlation to probe dead-cone effect in medium?**

# Summary

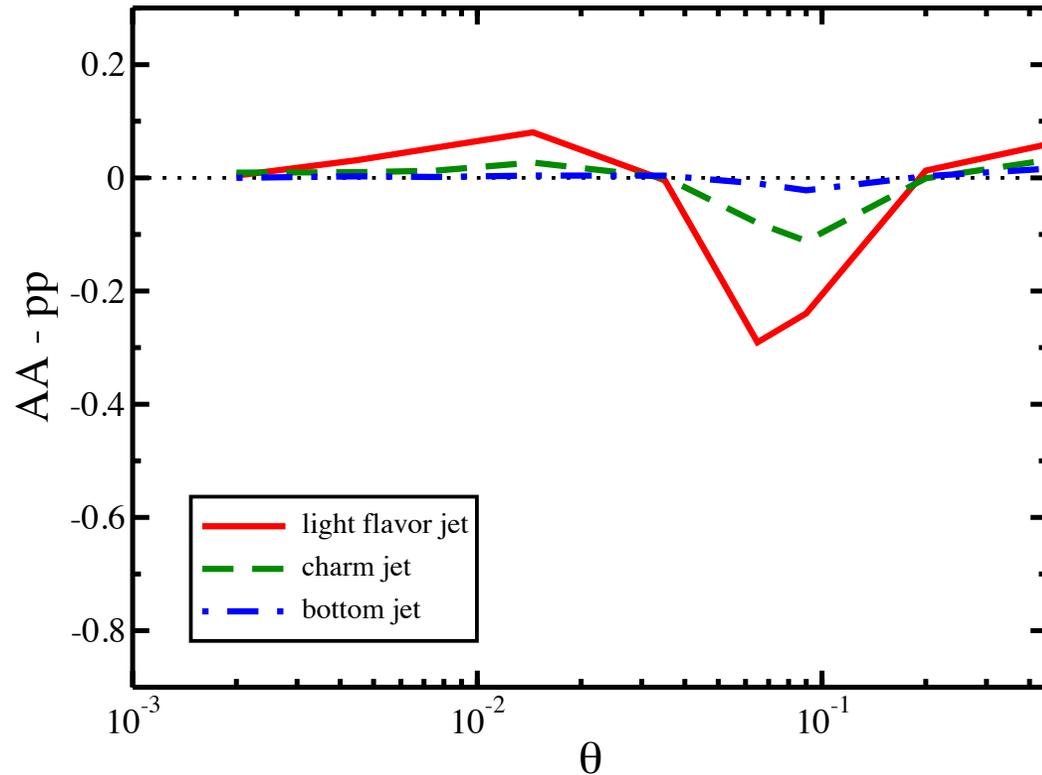
- ❑ **Mass effect on the nuclear modification of single hadrons:**
  - ❑ **By using a pQCD-based jet quenching model, we obtain a simultaneous description of  $R_{AA}$  for different flavor hadrons at  $p_T$  region in both heavy-ion and light-ion collisions.**
  - ❑ **Through a Bayesian analysis, we can extract averaged parton energy loss and the energy loss functions.**
- ❑ **Mass effect on the nuclear modification of jet and jet substructure:**
  - ❑ **A simultaneous description of jet and hadron  $R_{AA}$  for both heavy and light flavors.**
  - ❑ **The medium modification of inclusive jet EEC exhibits rich structure: suppression at intermediate angles, and enhancement at small and large angles, which can be explained by the interplay of mass effect, energy loss, medium-induced radiation and medium response.**
  - ❑ **The explorations on jet E3C is on-going ...**

***Thank You !***

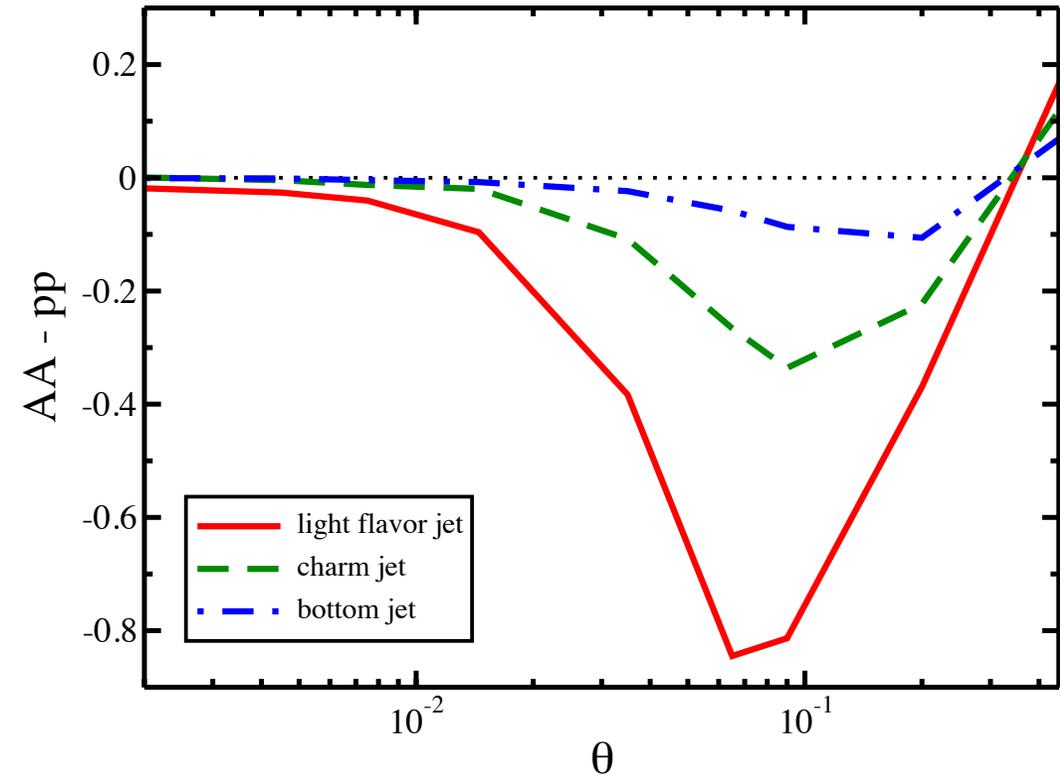


# Effect of selection bias on jet EEC

$p_T$  trigger in both pp and AA



$p_T$  trigger only in pp  
(no trigger bias in AA)



- **Selection bias contributes the enhancement of inclusive jet EEC: high energy jets tend to radiate more gluons, which facilitates the enhancement of EEC at small angle.**

# Low to intermediate $p_T$ heavy quark

- Use a parametrized Cornell-type potential to describe perturbative and non-perturbative interactions between HQs and QGP.

$$V(r) = V_Y(r) + V_S(r) = -\frac{4}{3}\alpha_s \frac{e^{-m_d r}}{r} - \frac{\sigma e^{-m_s r}}{m_s}$$

$$V(\vec{q}) = -\frac{4\pi\alpha_s C_F}{m_d^2 + |\vec{q}|^2} - \frac{8\pi\sigma}{(m_s^2 + |\vec{q}|^2)^2} \quad \begin{array}{l} \alpha_s = 0.27, \sigma = 0.45 \text{ GeV}^2 \\ m_d = 2T + 0.2 \text{ GeV} \\ m_s = \sqrt{0.1 \text{ GeV} \times T} \end{array}$$

$$\begin{aligned} i\mathcal{M} &= \mathcal{M}_Y + \mathcal{M}_S \\ &= \bar{u}(p')\gamma^\mu u(p)V_Y(\vec{q})\bar{u}(k')\gamma^\nu u(k) \\ &\quad + \bar{u}(p')u(p)V_S(\vec{q})\bar{u}(k')u(k), \end{aligned}$$

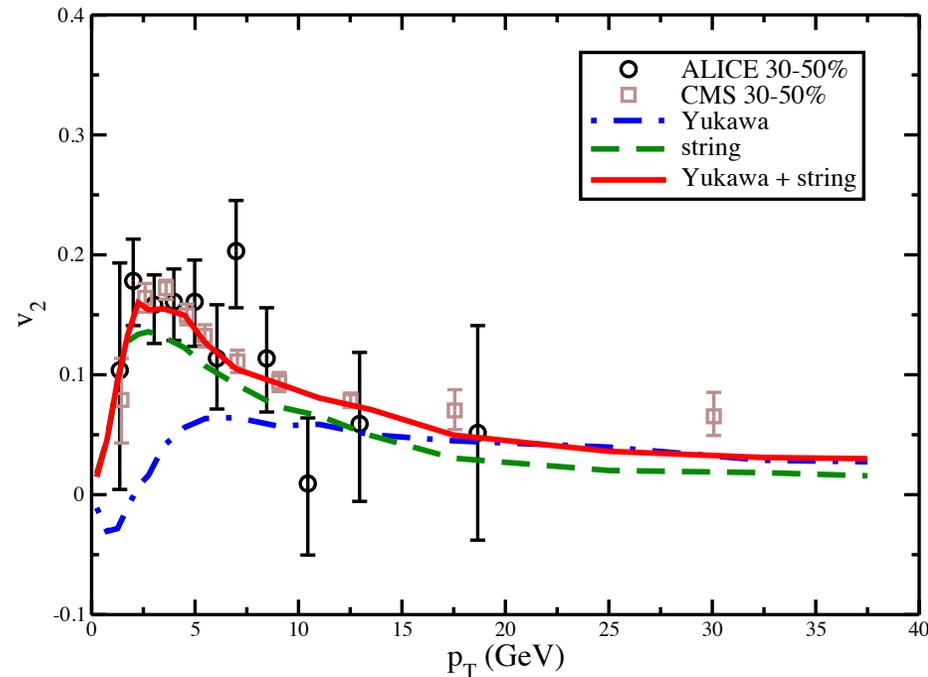
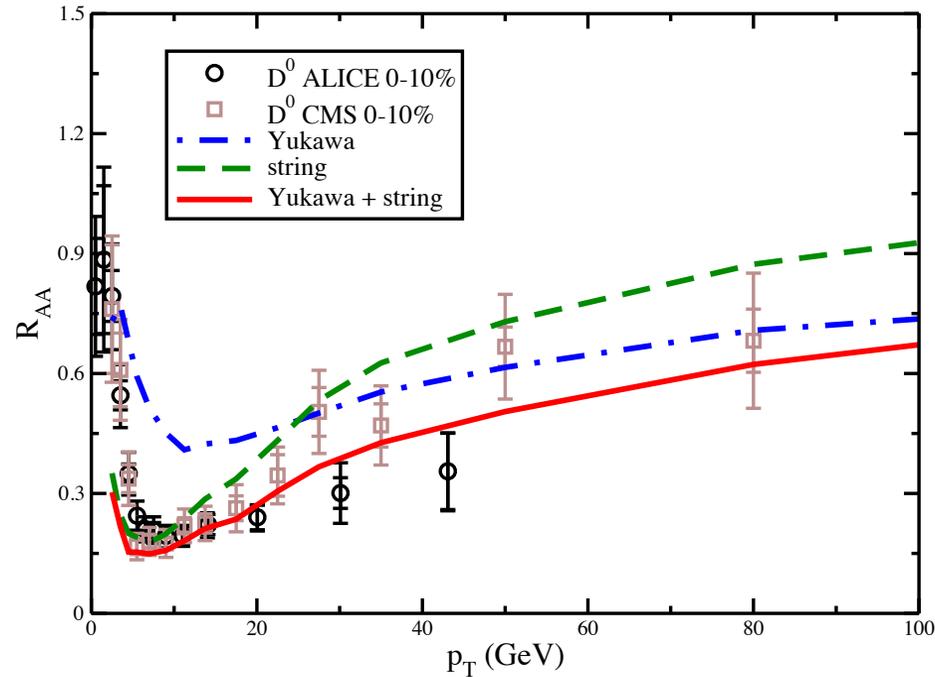
HQ dynamics at low energy & close to  $T_c$  is highly non-perturbative. Include the contributions from long-range confining potential & short-range Yukawa potential.

$$|\mathcal{M}_{Qq}|^2 = \frac{64\pi^2\alpha_s^2}{9} \frac{(s - m_Q^2)^2 + (m_Q^2 - u)^2 + 2m_Q^2 t}{(t - m_d^2)^2} + \frac{(8\pi\sigma)^2}{N_c^2 - 1} \frac{t^2 - 4m_Q^2 t}{(t - m_s^2)^4},$$

$$\begin{aligned} |\mathcal{M}_{Qg}|^2 &= \frac{64\pi^2\alpha_s^2}{9} \frac{(s - m_Q^2)(m_Q^2 - u) + 2m_Q^2(s + m_Q^2)}{(s - m_Q^2)^2} \\ &\quad + \frac{64\pi^2\alpha_s^2}{9} \frac{(s - m_Q^2)(m_Q^2 - u) + 2m_Q^2(u + m_Q^2)}{(u - m_Q^2)^2} \\ &\quad + 8\pi^2\alpha_s^2 \frac{5m_Q^4 + 3m_Q^2 t - 10m_Q^2 u + 4t^2 + 5tu + 5u^2}{(t - m_d^2)^2} \\ &\quad + 8\pi^2\alpha_s^2 \frac{(m_Q^2 - s)(m_Q^2 - u)}{(t - m_d^2)^2} \\ &\quad + 16\pi^2\alpha_s^2 \frac{3m_Q^4 - 3m_Q^2 s - m_Q^2 u + s^2}{(s - m_Q^2)(t - m_d^2)} \\ &\quad + \frac{16\pi^2\alpha_s^2}{9} \frac{m_Q^2(4m_Q^2 - t)}{(s - m_Q^2)(m_Q^2 - u)} \\ &\quad + 16\pi^2\alpha_s^2 \frac{3m_Q^4 - m_Q^2 s - 3m_Q^2 u + u^2}{(t - m_d^2)(u - m_Q^2)} + \frac{C_A}{C_F} \frac{(8\pi\sigma)^2}{N_c^2 - 1} \frac{t^2 - 4m_Q^2 t}{(t - m_s^2)^4}. \end{aligned}$$

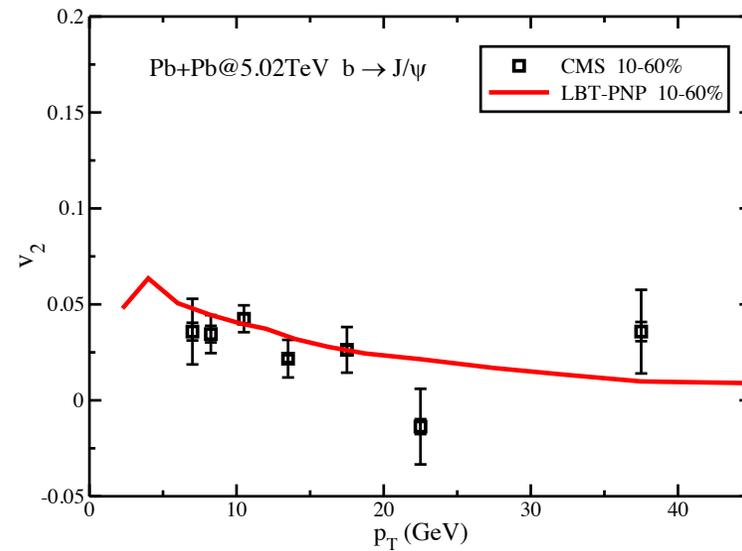
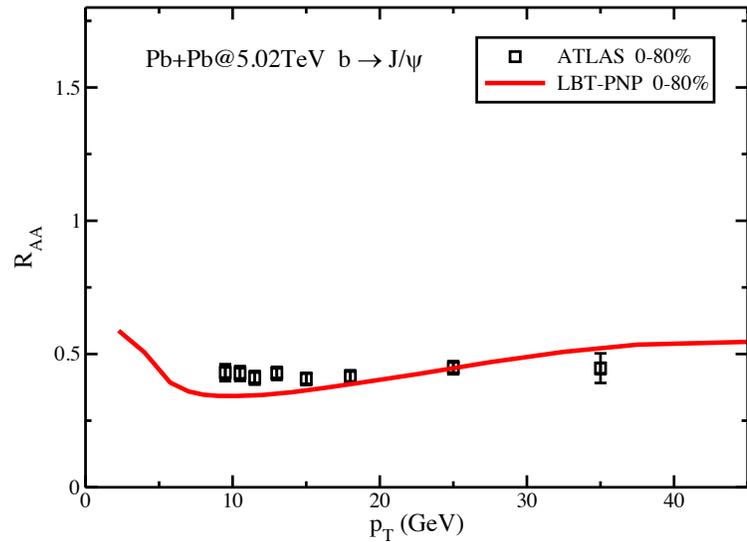
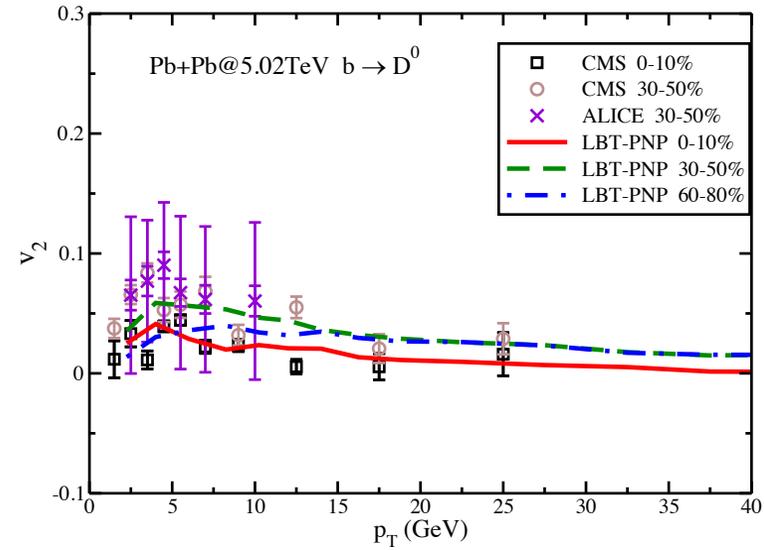
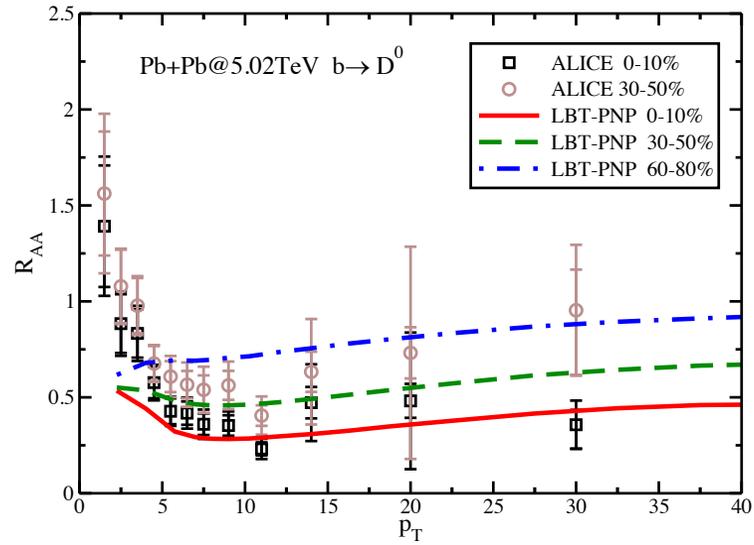
# Implementation of color potential interaction in LBT

- FONLL + LBT-PNP + hydrodynamics

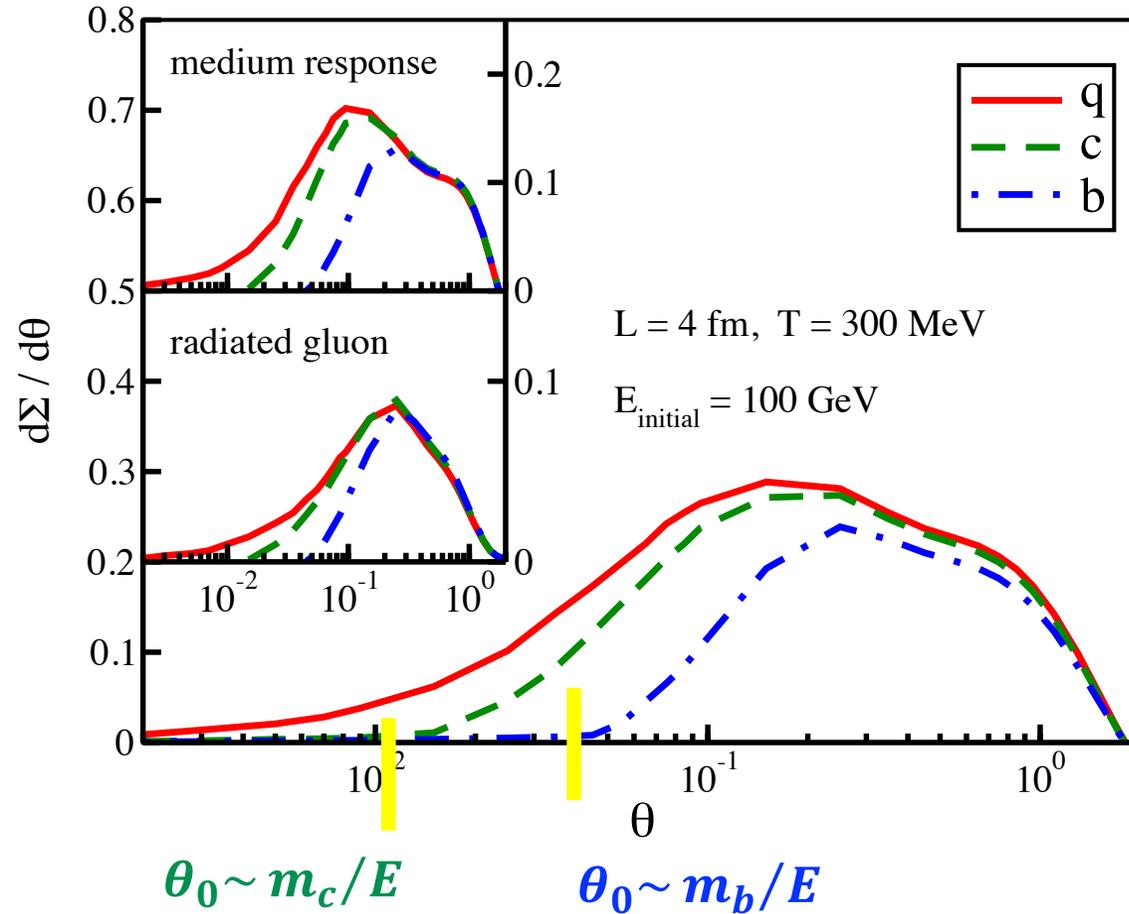


- **LBT-PNP model can simultaneously describe D meson  $R_{AA}$  &  $v_2$  at RHIC & the LHC.**
- **Perturbative interaction dominates D meson  $R_{AA}$  and  $v_2$  at high  $p_T$ , while non-perturbative interaction dominates at low  $p_T$ .**

# Bottom quark dynamics within LBT-PNP

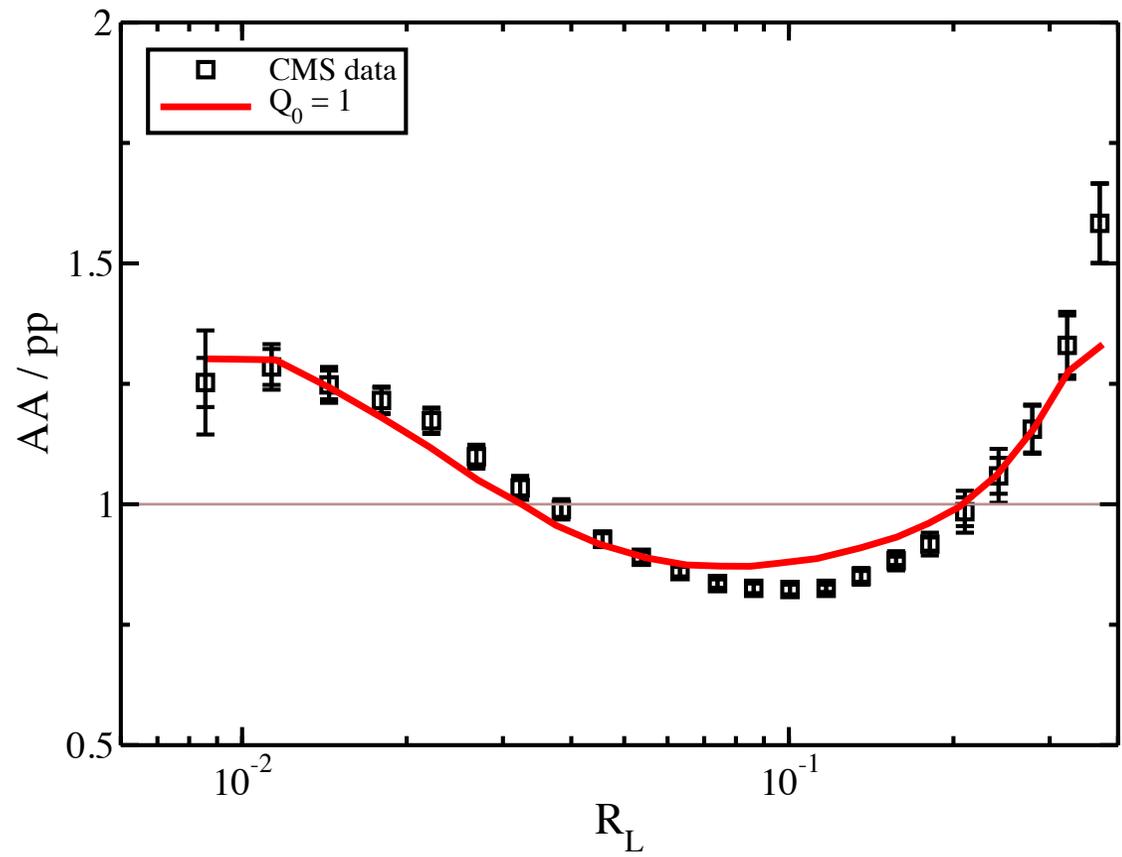


# Medium response and medium-induced radiation to jet EEC



## Flavor (mass) hierarchy in quark-jet EEC:

- $\Sigma(\text{light jet}) > \Sigma(\text{charm jet}) > \Sigma(\text{bottom jet})$ , this hierarchy maintains in the contribution from medium response and medium-induced radiation.

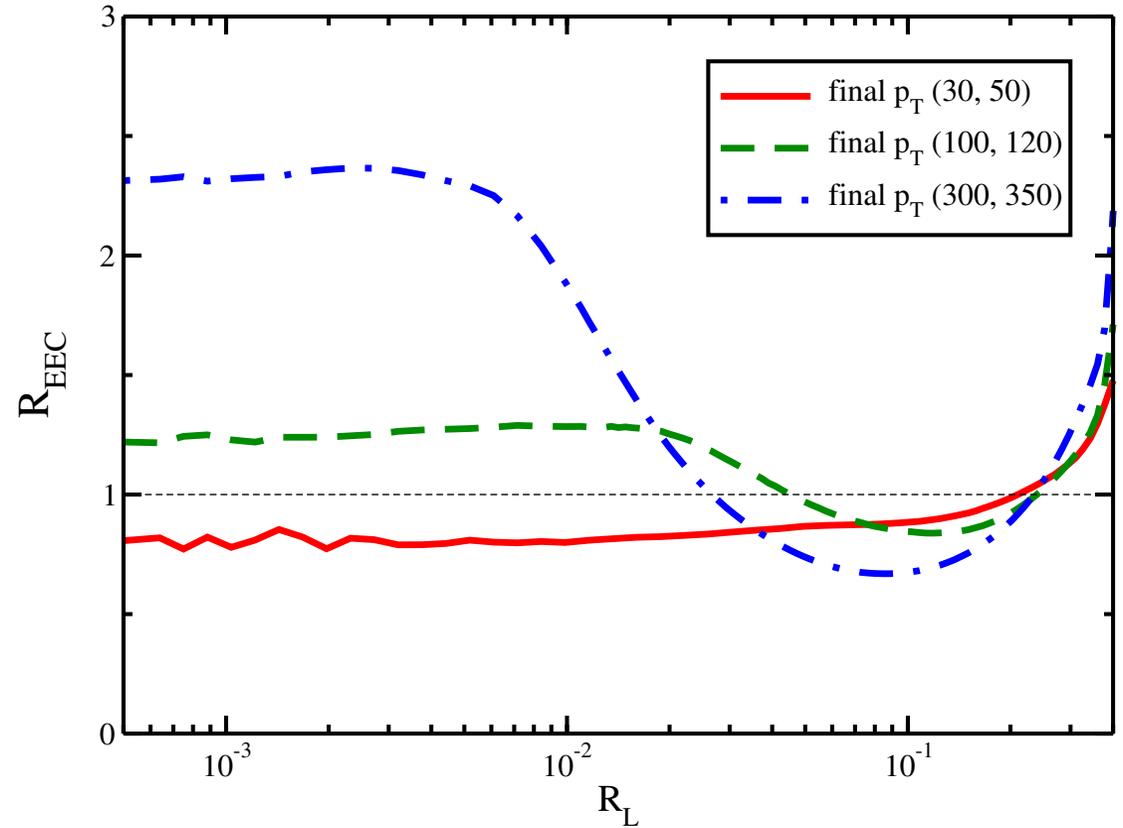


# Genuine particle correlation in jets

$$\frac{d\langle\text{EEC}\rangle_{\text{full}}}{d^2\theta} = \frac{1}{N_{\text{jet}}} \sum_{\text{jets}J} \sum_{i \neq j \in J} \frac{E_i E_j}{E_J^2} \delta^{(2)}(\vec{\theta} - (\vec{\theta}_i - \vec{\theta}_j))$$

$$\frac{d\langle\text{EEC}\rangle_{\text{trivial}}}{d^2\theta} = N_{\text{trivial}} \int d^2\theta_1 d^2\theta_2 \frac{d\langle E(\theta_1)\rangle}{d^2\theta_1} \frac{d\langle E(\theta_2)\rangle}{d^2\theta_2} \delta^{(2)}(\vec{\theta} - (\vec{\theta}_1 - \vec{\theta}_2))$$

$$\mathcal{R} = \frac{d\langle\text{EEC}(\theta)\rangle_{\text{full}}}{d^2\theta} / \frac{d\langle\text{EEC}(\theta)\rangle_{\text{trivial}}}{d^2\theta}$$



# Genuine particle correlation in jets

