



華中師範大學

CENTRAL CHINA NORMAL UNIVERSITY

Energy-energy correlators from large to small systems

Lin Li (李林)

Central China Normal University

Collaborators: Yan-Ru Bao, Weiyao Ke, Guang-You Qin

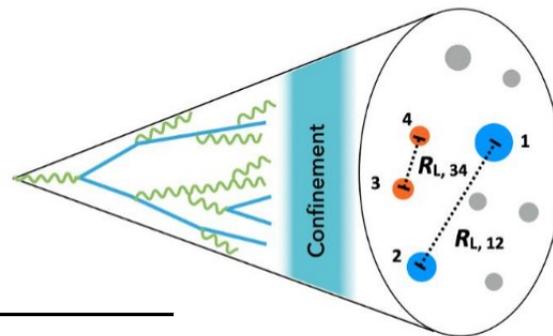


JET AND HEAVY QUARK
JUST ASK QUESTIONS



Energy-Energy Correlators

$$EEC(R_L) = \sum_{i_1, i_2 \in \text{jet}} \int dR_L \frac{p_T^{i_1} p_T^{i_2}}{p_{T, \text{jet}}^2} \delta(R_L - \Delta \hat{R}_L)$$



$$R_L = \sqrt{(\eta_{i1} - \eta_{i2})^2 + (\phi_{i1} - \phi_{i2})^2}$$

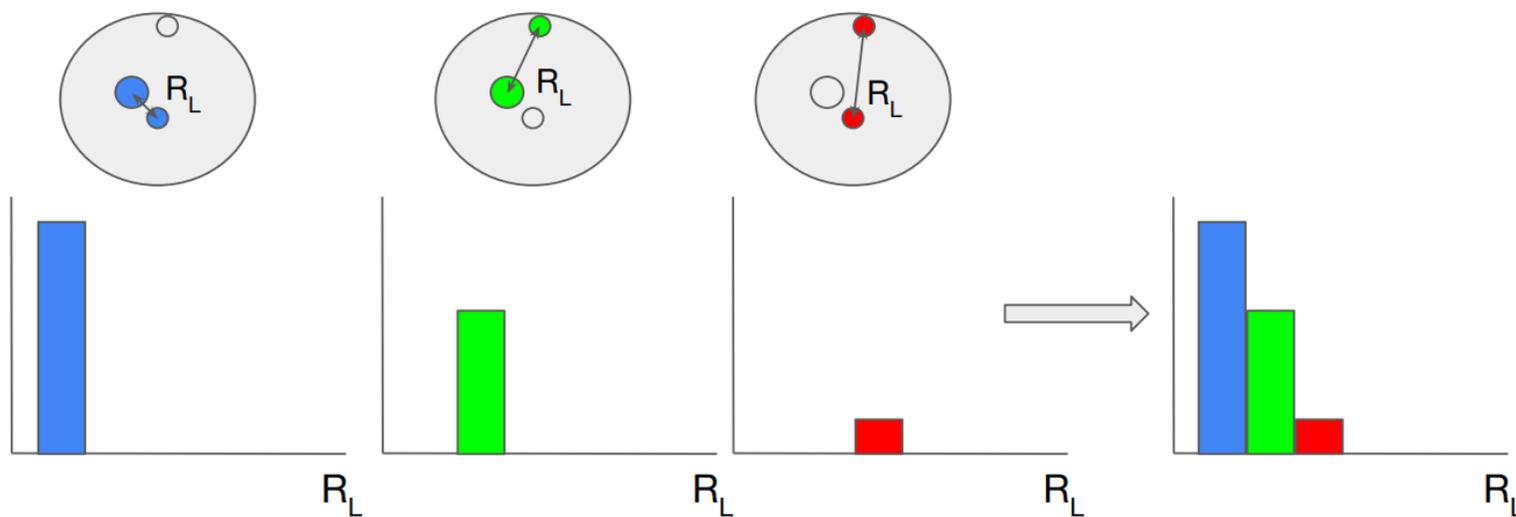
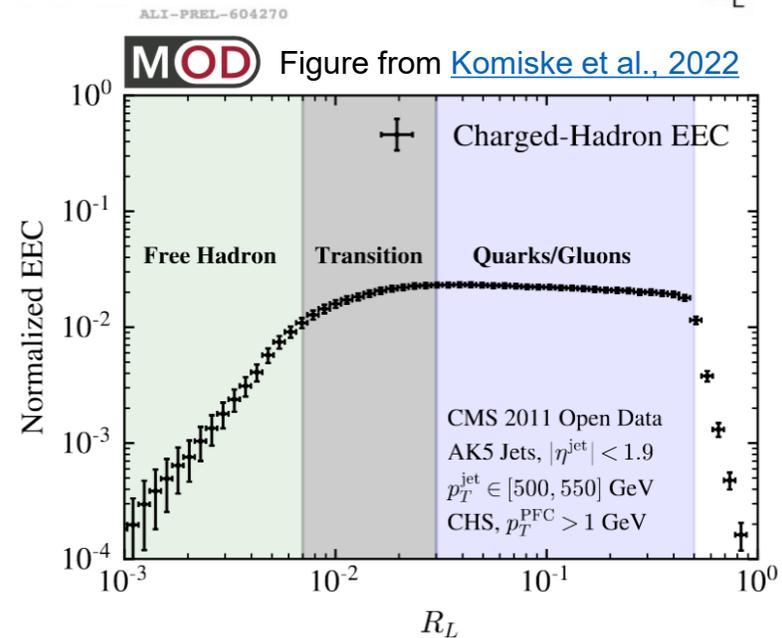
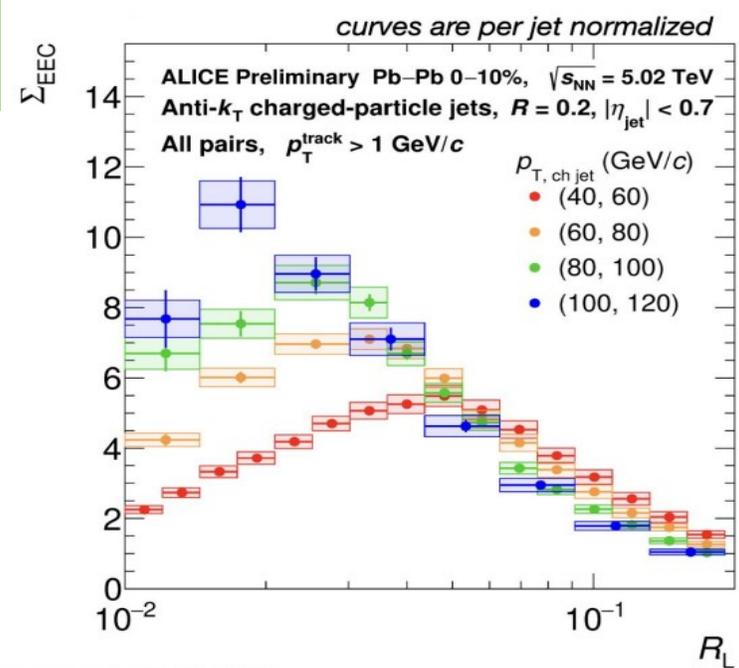


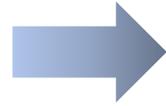
Figure from [Arjun Kudinoor \(quark matter 2025\)](#)



From Hadrons to Jets to Substructures

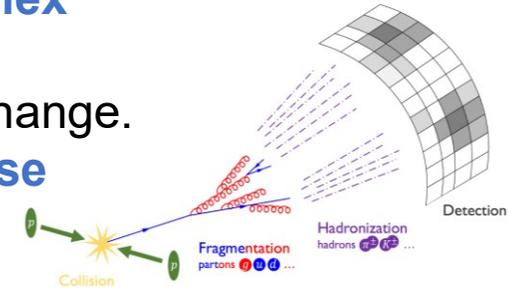
High- p_T hadrons:

- ✓ Single-particle observables show **overall energy loss**.



Jets:

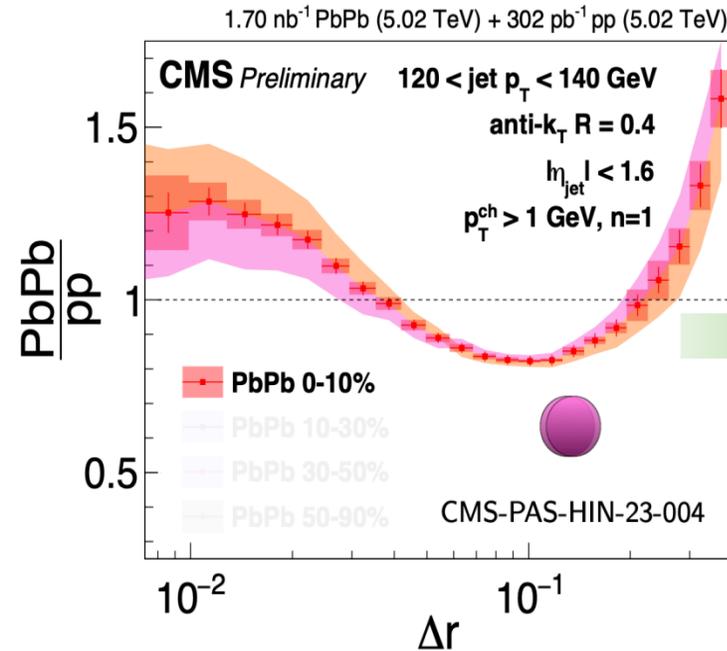
- ☉ Collections of many particles → **more complex modifications**.
- ☉ Substructure and particle composition can change.
- ☉ Traditional observables **cannot capture these details**.



EEC (Energy–Energy Correlator):

- Measures **energy correlations between particle pairs** inside a jet.
- Reveals **how energy is distributed angularly** within the jet.

CMS, arXiv: [2503.19993](https://arxiv.org/abs/2503.19993)

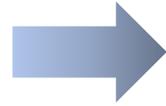


- **Large angle:**
 - Medium response
 - Medium-induced radiation
- **Small angle:**
 - Jet p_T selection bias,
 - Flavor dependence of jet
- **Intermediate angles:** Both effects contribute, but the dip is mainly due to radiation.

From Hadrons to Jets to Substructures

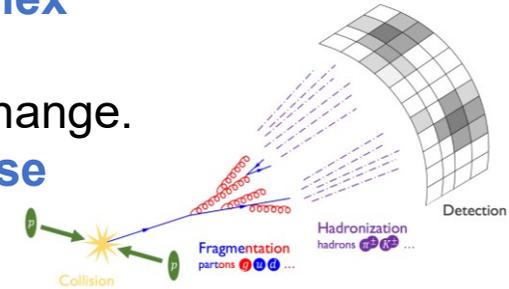
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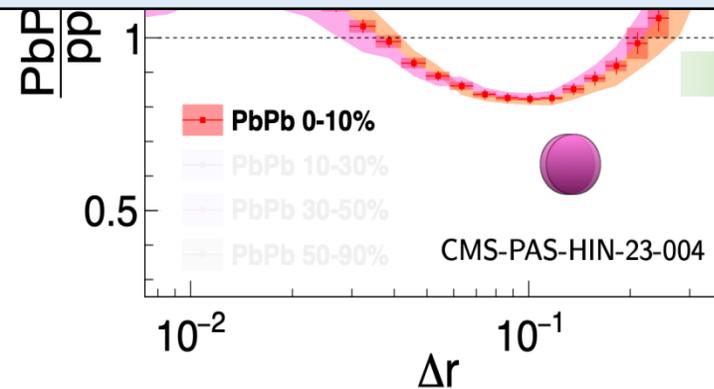


This work: employ the **LIDO partonic transport model + hydrodynamic description of QGP + linear medium response model** to study jet substructure via the EEC.

linear medium response model to study jet substructure via the EEC.

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Flavor dependence of jet

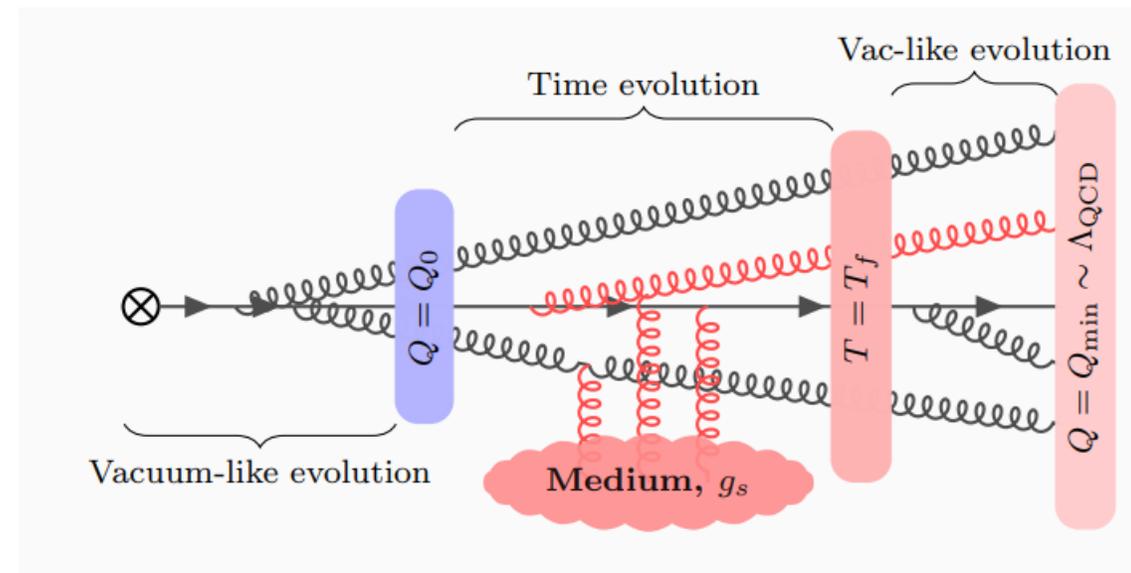
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LIDO Model: Jet Evolution Framework



Framework Components

- **PYTHIA8**: Initial jet production and Vacuum shower evolution
- **LIDO**: In-medium transport (Partons decouple below $T < T_f$)
- **PYTHIA8**: Vacuum shower + fragmentation.
- **2+1D Hydrodynamics**: QGP background evolution



[PRC 100\(2019\)064911](#)

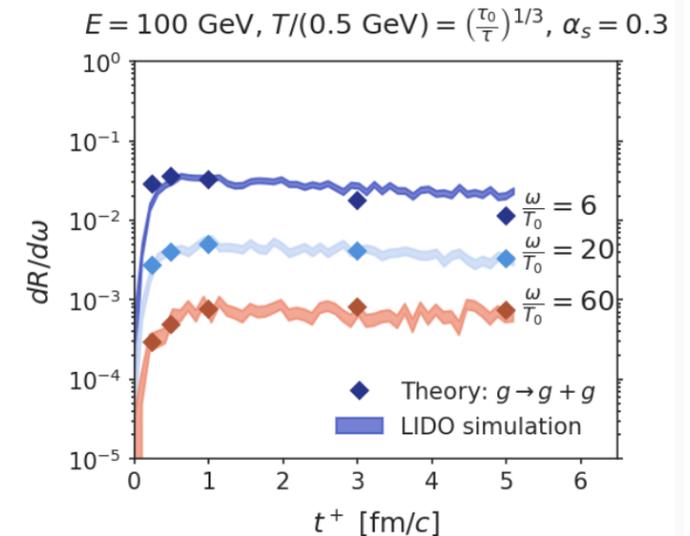
Transport Equation in the Incoherent Limit

The semiclassical transport equation for hard partons ($p \cdot u > E_{min}$) in the incoherent and independent-collision limit is:

$$p \cdot \partial [f \Theta(p \cdot u - E_{min})] = (p \cdot u) \Theta(p \cdot u - E_{min}) \{ D + C_{1 \leftrightarrow 2} + C_{2 \leftrightarrow 2} + C_{2 \leftrightarrow 3} \}$$

The distribution function of a hard parton evolves under the influence of : [PRC 82 \(2010\) 064902](#)
[PRC 58 \(1998\) 1706](#)

- Diffusion term: $D[f]$
- Large- \hat{q} elastic collisions: $C_{2 \rightarrow 2}[f]$
- Diffusion-induced small- \hat{q} parton splitting/merging: $C_{1 \rightarrow 2}[f]$
- Large- \hat{q} inelastic collisions: $C_{2 \rightarrow 3}[f]$
- $E_{min} = \theta T$, θ is a Parameter



☺ The strong coupling $\alpha_s(Q, T)$ ceases to run for momentum transfers below the thermal scale, and is given by:

$$\alpha_s(Q, T) = \frac{4\pi}{9} \cdot \frac{1}{\ln\left(\frac{\max\{Q^2, \mu_{min}^2\}}{\Lambda_{QCD}^2}\right)} \quad \mu_{min} = C_M \times \pi T$$

Linear Medium Response Model

- Energy-momentum deposition to soft sector:

$$\frac{d\delta p^\mu}{dt}(t, \mathbf{x}) = \int_p \Theta(p \cdot u < E_{\min}) p^\mu \frac{d}{dt} f_H(t, \mathbf{x}, p)$$

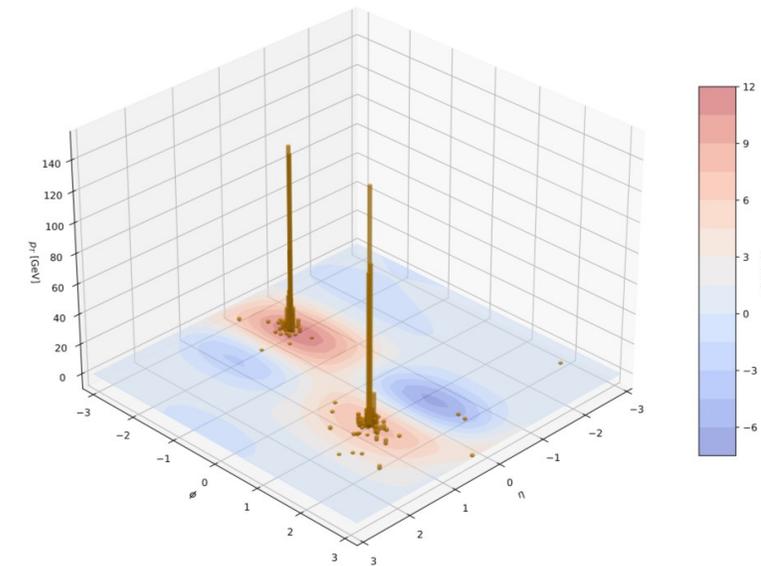
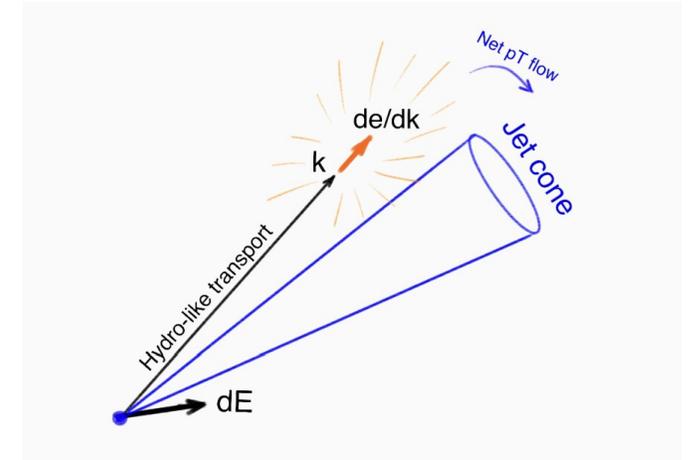
- An ideal-hydro response (no transverse flow)

$$\frac{de}{d\Omega'_k} = \frac{\delta p^0 + \hat{k}' \cdot \delta \vec{p} / c_s}{4\pi}, \quad \frac{d\vec{p}}{d\Omega'_k} = \frac{3(c_s \delta p^0 + \hat{k}' \cdot \delta \vec{p}) \hat{k}'}{4\pi}$$

- Freeze-out to massless particles under a radial transverse flow $v_\perp \Rightarrow$ corrects the momentum density in $\eta - \phi$ plane.

$$\frac{d\Delta p_T}{d\phi d\eta} = \int \frac{3}{4\pi} \frac{\frac{4}{3} \sigma u_\mu - \hat{p}_\mu}{\sigma^4} \delta p^\mu(\hat{k}) \frac{d\Omega_{\hat{k}}}{4\pi}$$

$$\sigma = \gamma_\perp [\cosh(\eta - \eta_s - \eta_{\hat{k}}) - v_\perp \cos(\phi - \phi_{\hat{k}})]$$

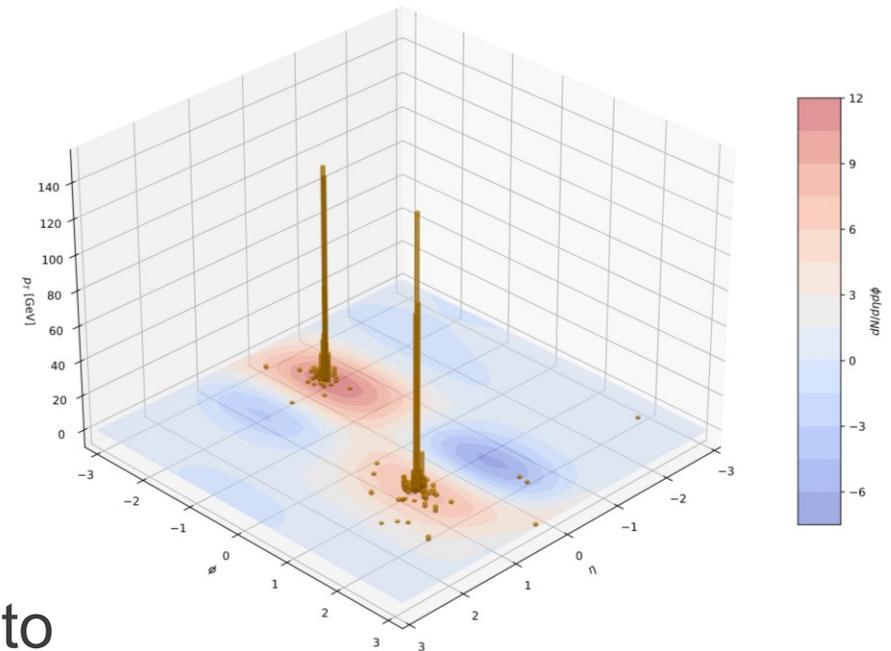


Jet Definition in LIDO with medium response

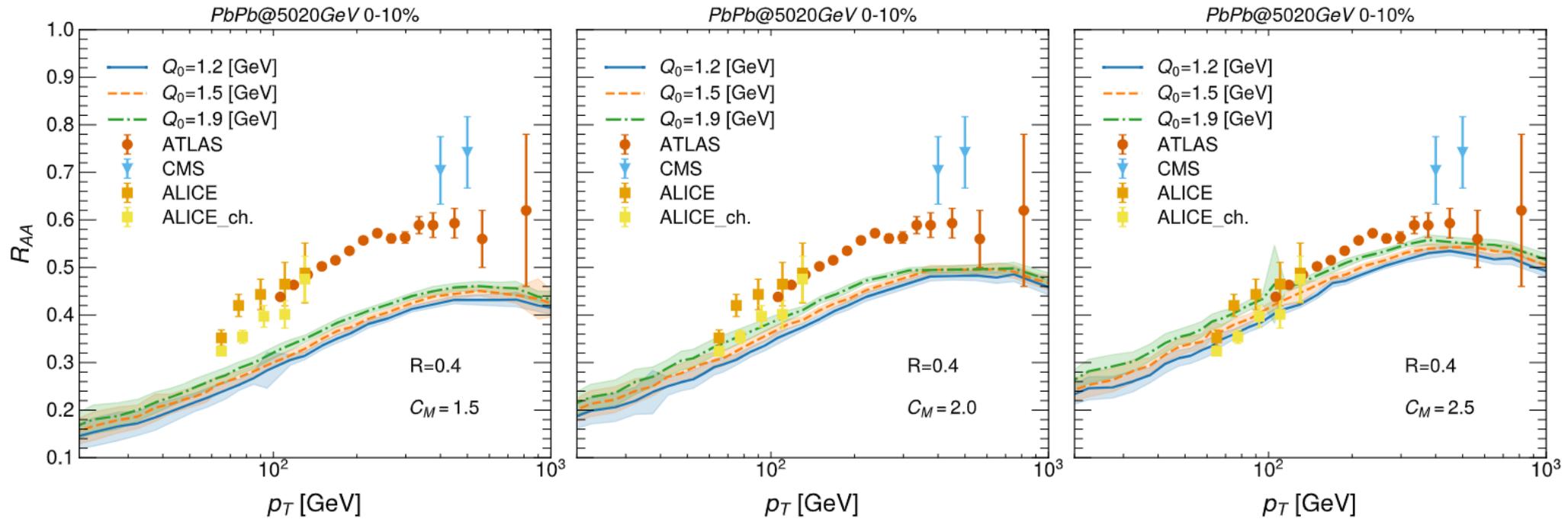
- Jets (anti- K_T) are reconstructed from energy bins $E_{T,ij}$, defined by

$$E_{T,ij} = \underbrace{\frac{d\Delta p_T}{d\phi d\eta}(\eta_i, \phi_j) \Delta\eta \Delta\phi}_{\text{from medium response}} + \underbrace{\sum_{\substack{|\eta_k - \eta_i| < \Delta\eta/2 \\ |\phi_k - \phi_j| < \Delta\phi/2}} p_{T,k}}_{\text{from parton fragmentations}}$$

- Uncorrelated medium background are assumed to be perfectly subtracted.



Parameter sensitivity: effective coupling and initialization scale



Q_0 modulates jet quenching magnitude

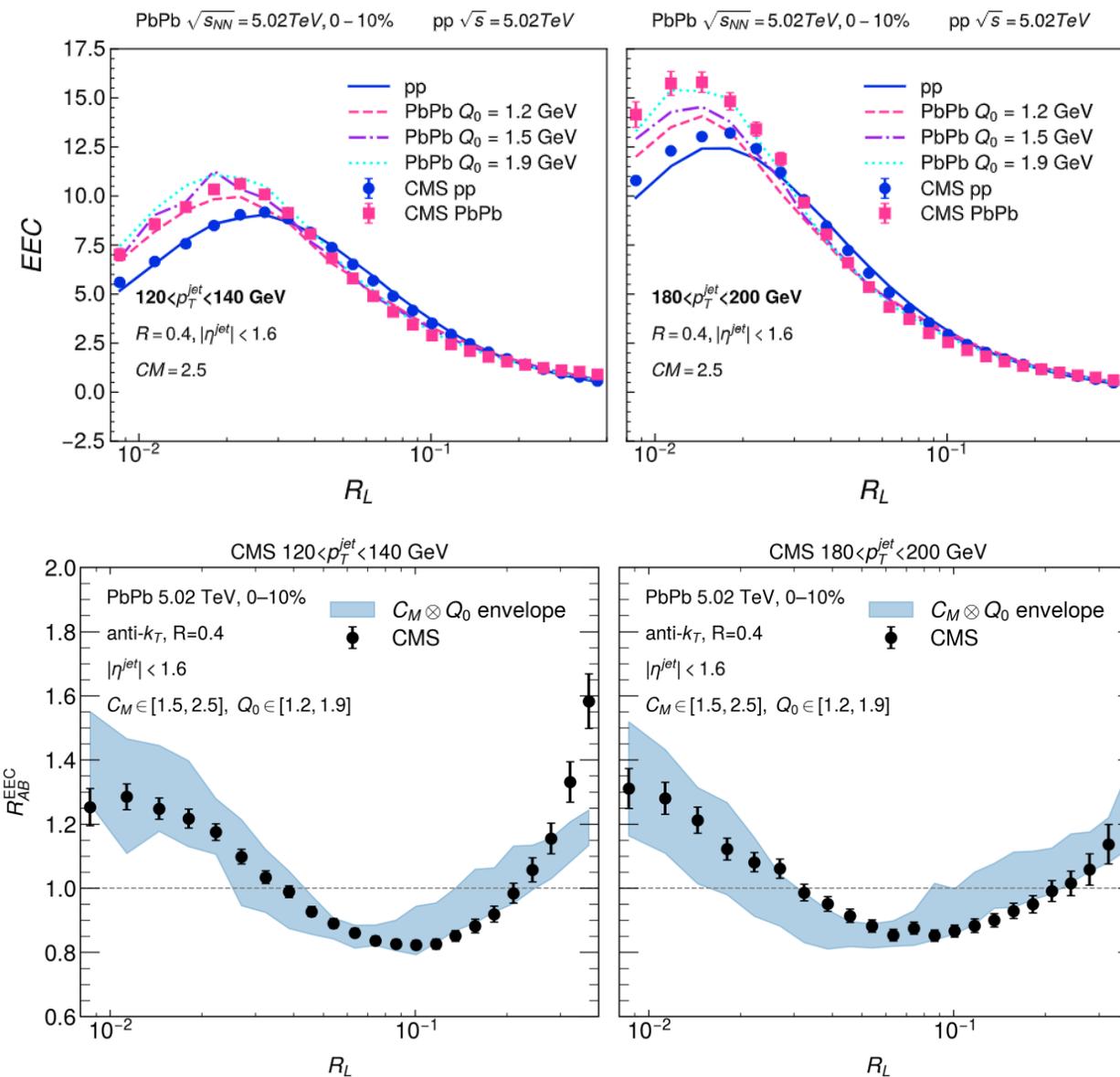
increasing $C_M \Rightarrow$ decreasing jet-medium coupling at $T \Rightarrow$ less suppression

$$\alpha_s(Q, T) = \frac{4\pi}{9} \cdot \frac{1}{\ln\left(\frac{\max\{Q^2, \mu_{\min}^2\}}{\Lambda_{\text{QCD}}^2}\right)} \quad \mu_{\min} = C_M \times \pi T$$

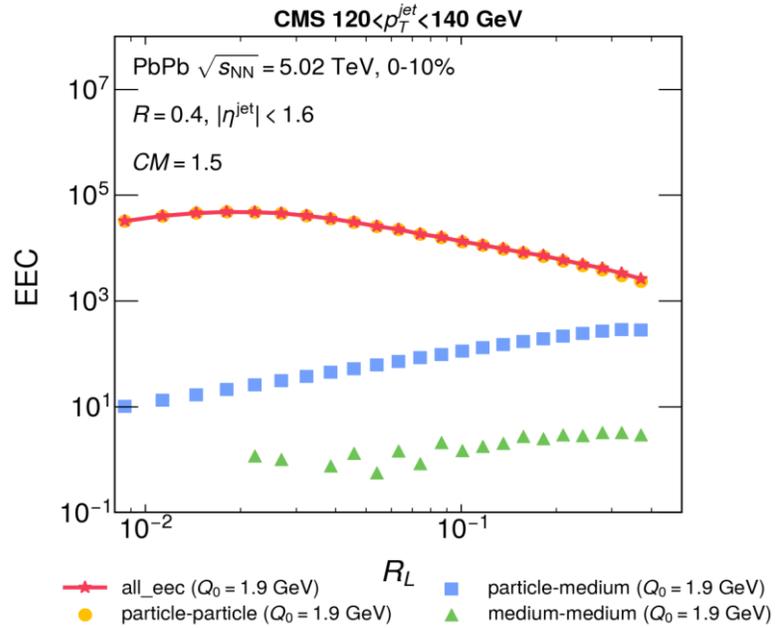
EEC in Pb-Pb: Theory vs. CMS Data

$$EEC(\Delta r) = \frac{1}{W_{pairs}} \frac{1}{\delta r} \sum_{jets \in [p_{T,1}, p_{T,2}]} \sum_{pairs \in [\Delta r_a, \Delta r_b]} (p_{T,i} p_{T,j})^n$$

- Normalize with the number of pairs W_{pairs}
- Exponent values $n = 1$ used in this analysis



The Full EEC with medium response



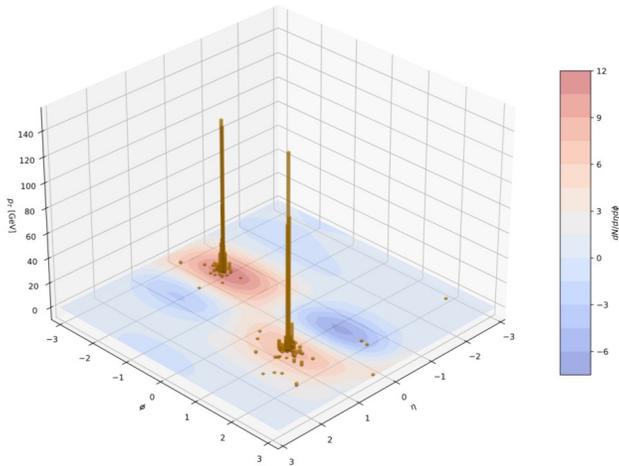
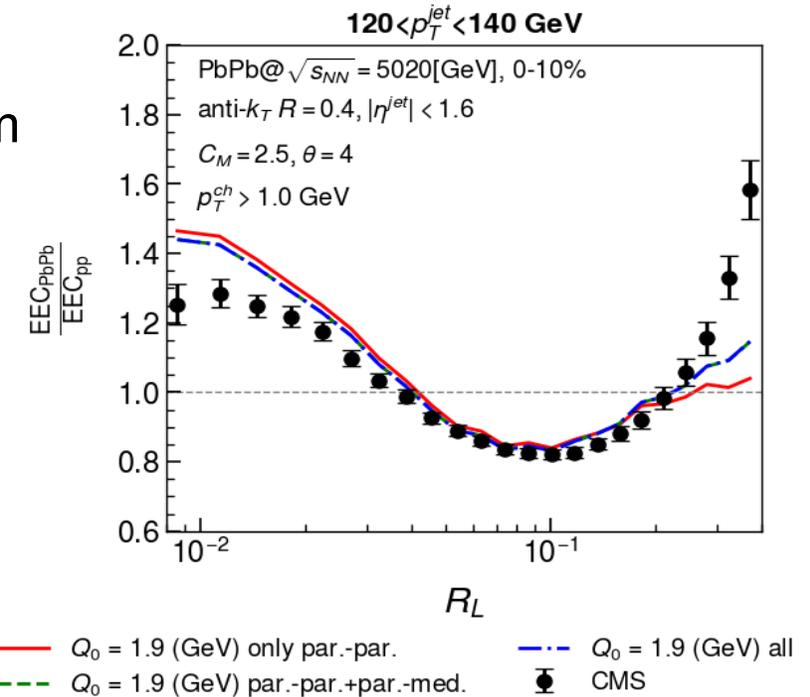
- Medium particles generated from transverse momentum density:

$$\frac{dp_T}{d\eta d\phi} \Delta\eta \Delta\phi$$

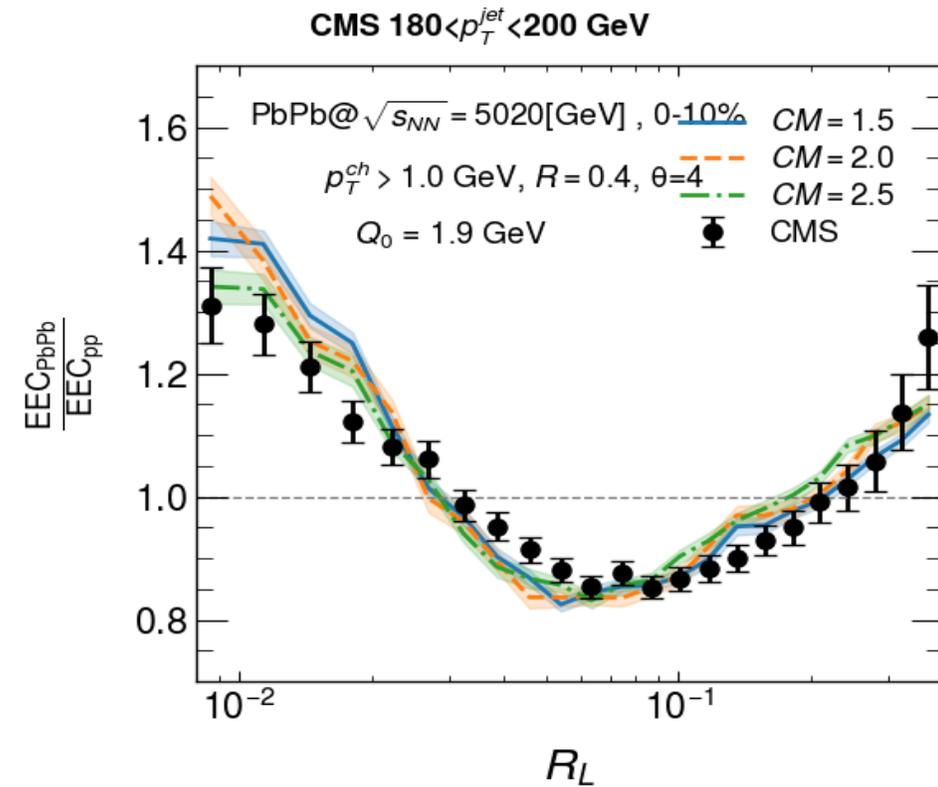
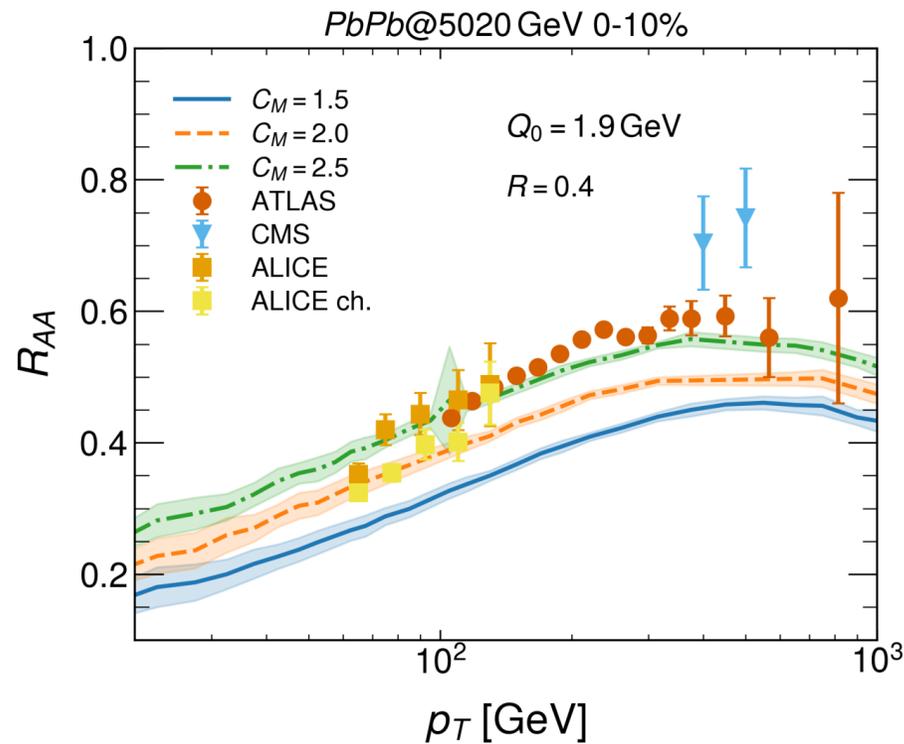
via energy-tower method

- EEC include:

- ① Hard particle – Hard particle correlations
- ② Medium response – Hard particle correlations
- ③ Medium response – Medium response correlations.



Sensitivity of EEC and Jet R_{AA} to the Jet–Medium Coupling Cutoff C_M

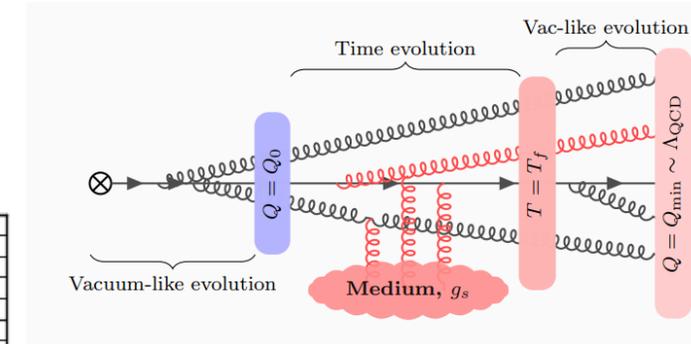
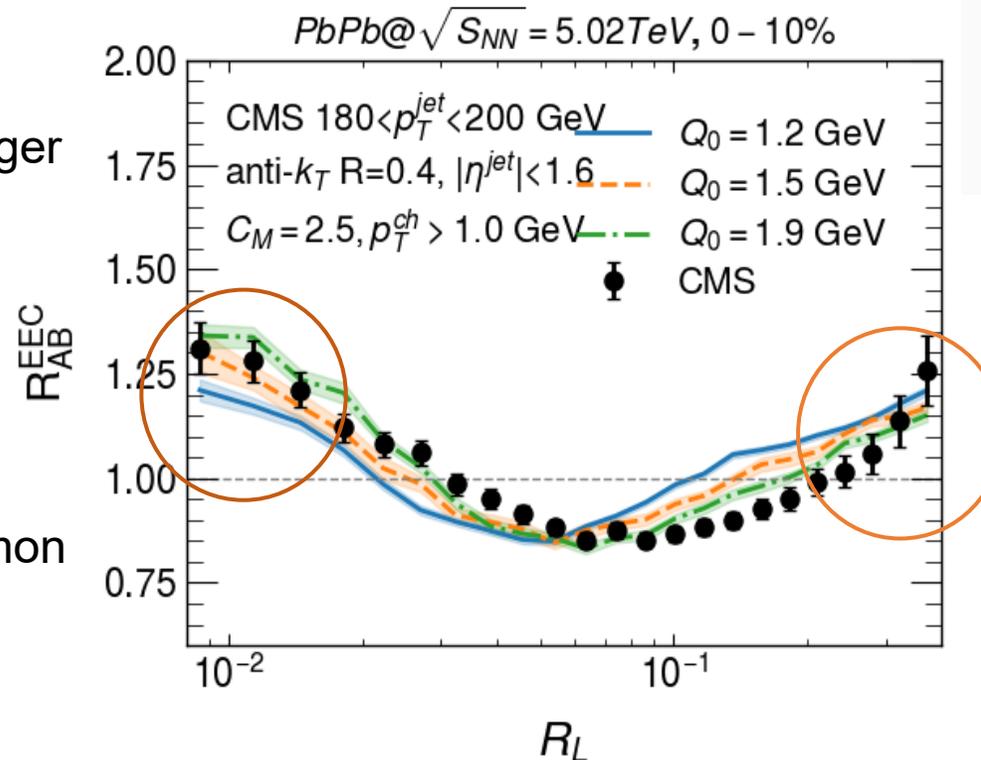


- **R_{AA}** : Governed by total energy loss → Strongly affected by soft interactions
→ Stronger sensitivity
- **EEC**: Probes relative angular structure in jets → Normalized & energy-weighted → weak sensitivity

Sensitivity of EEC to the Vacuum–Medium Transition Scale Q_0

Q_0 (Scale separating vacuum & medium shower) \uparrow : fewer partons in the shower, interacting earlier with the medium.

- **Small angles:** Larger $Q_0 \rightarrow$ stronger enhancement.
- **Large angles:** Smaller $Q_0 \rightarrow$ steeper slope.
- **Intermediate angles:** Curves for different Q_0 intersect near a common point.

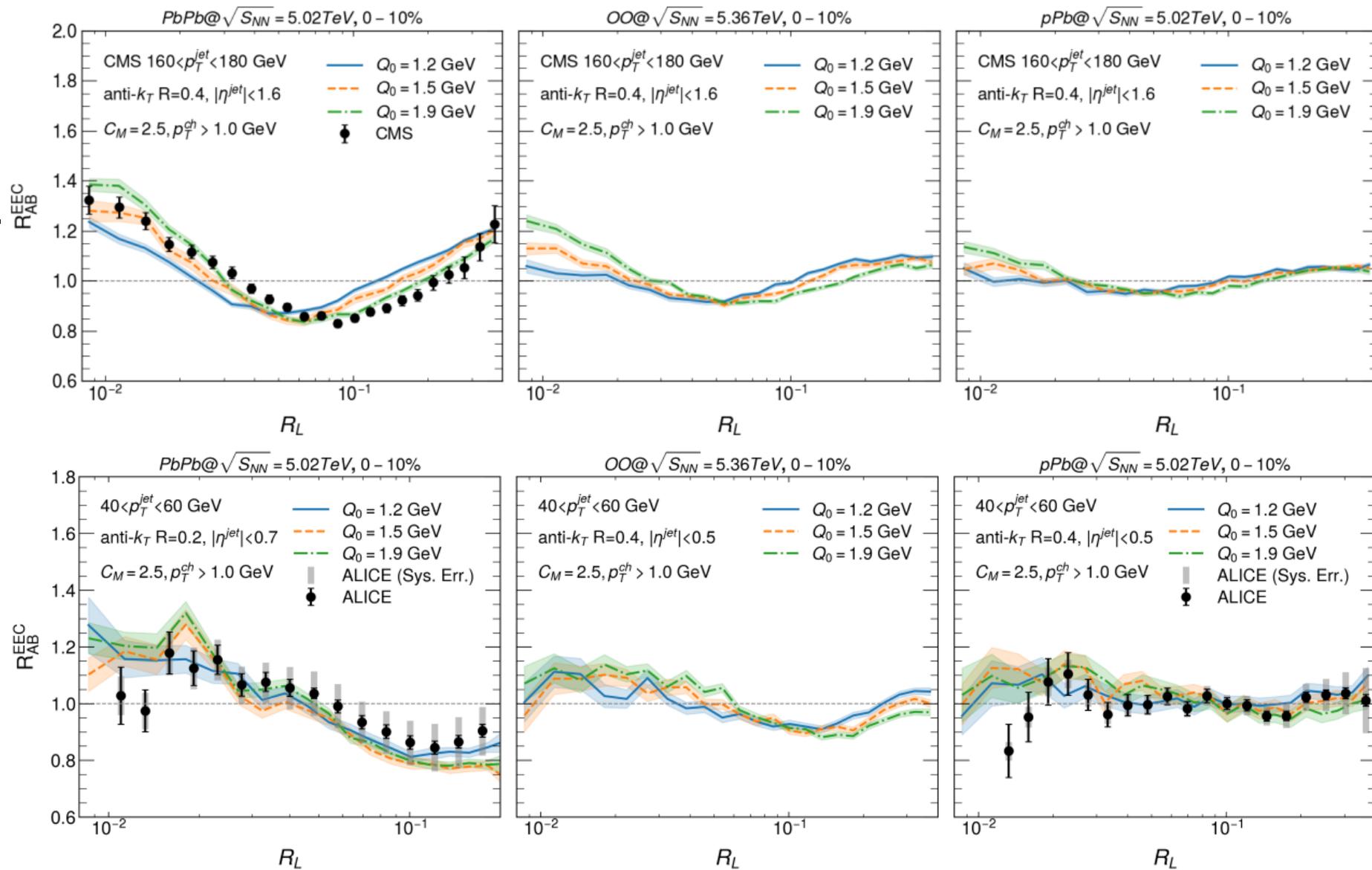


- At small angles, a smaller Q_0 leads to a richer vacuum shower reduces the quark-gluon energy-loss difference thereby suppressing their selection bias.
- At large angles, a smaller Q_0 leads to more shower particles, resulting in stronger medium-induced radiation.

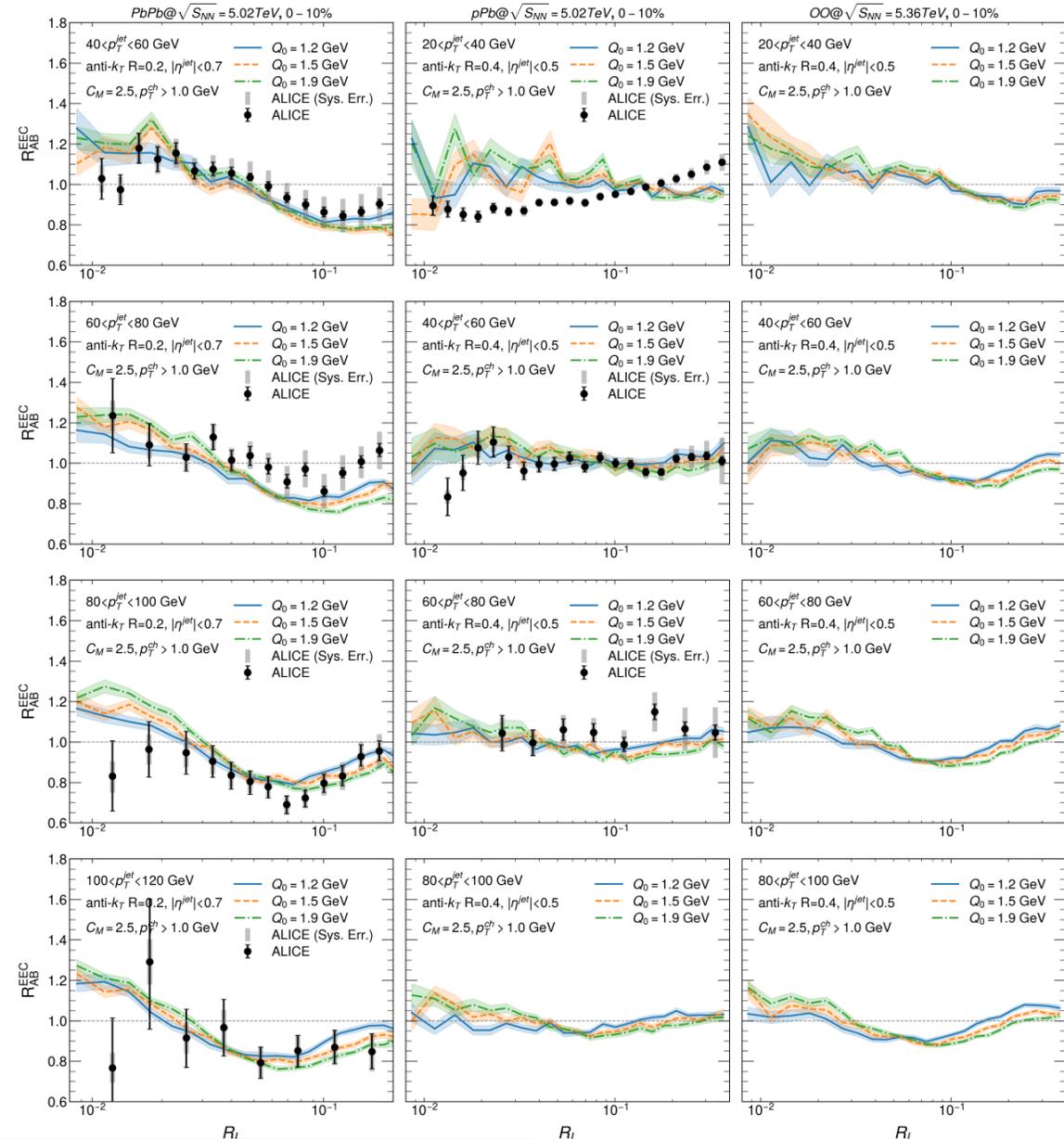
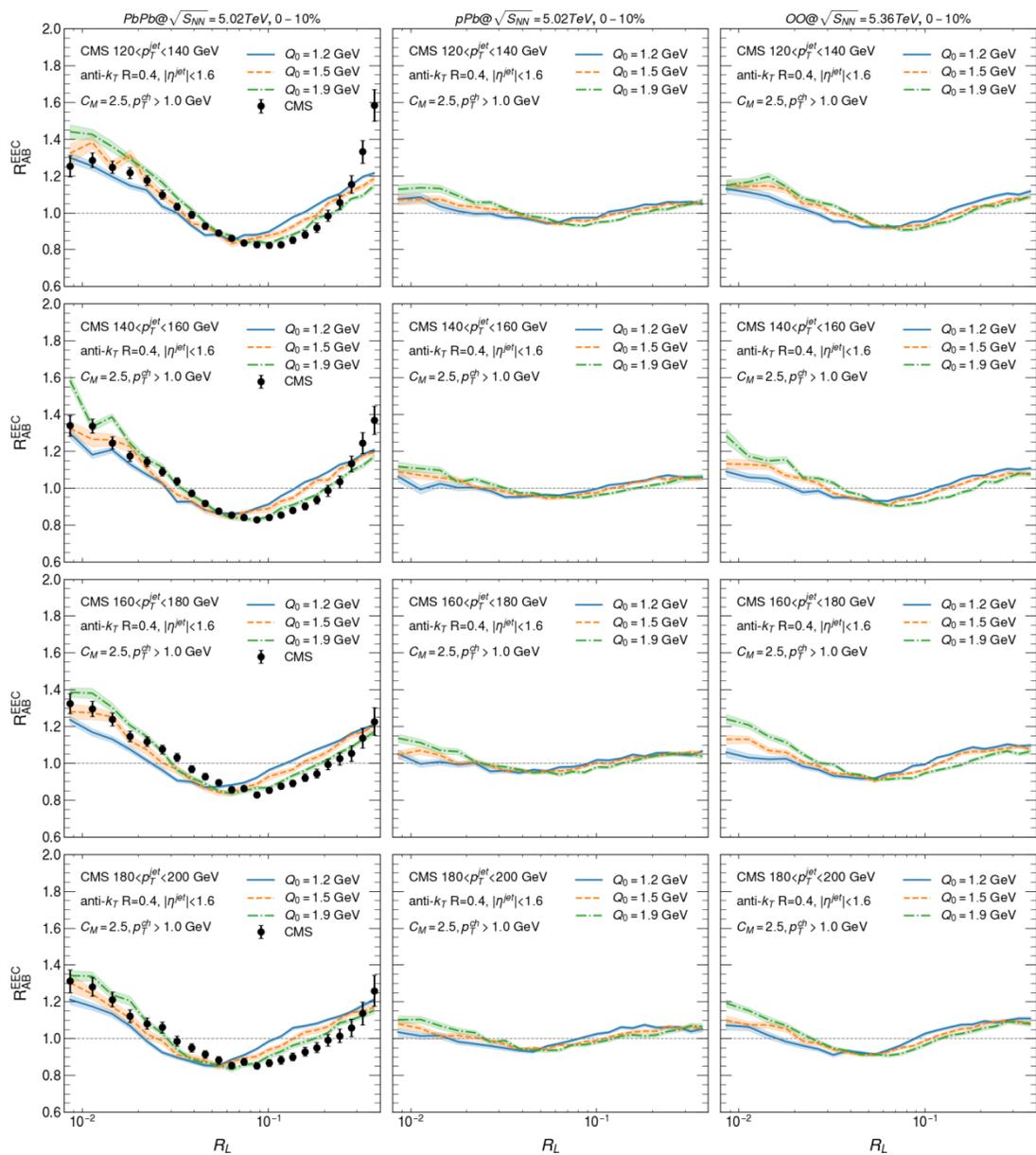
EEC from large to small systems: Pb-Pb, O-O and p-Pb

- O--O : Similar structure but smaller magnitude than Pb-Pb.
- p--Pb : Even smaller than O-O

⇒ The shape of the EEC ratio is the similar across systems, with only an overall change in magnitude.



Pb-Pb, p-Pb, O-O EEC: vs. Experiment



- The EEC is a sensitive probe of the vacuum–medium transition scale Q_0 .
- **A smaller Q_0 suppresses small-angle enhancement and enhances large-angle medium-induced correlations.**
- The EEC modification shows a similar trend across Pb–Pb, p–Pb, and O–O systems, with only an overall change in magnitude.
- Our model describes CMS and ALICE data at high p_T and provides predictions for O–O collisions