

Tracking down the Route of GUT Breaking

EJC, Velasco-Sevilla, 2112.14483

EJC, Dutka, Jung, Nagels, Vanvlasselaer, 2305.10759

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Eung Jin Chun



Outline

- Motivation: GW probe of GUT breaking routes to SM predicting different types of topological defects and FOTP at various scales.

$$G_{\text{GUT}} \rightarrow H_1 \rightarrow H_2 \rightarrow \cdots \rightarrow G_{\text{SM}}: \pi_k(G/H) \neq I, k = 0 \text{ (DW)}, 1 \text{ (CS)}, 2 \text{ (MP)}$$

- Review: GW signals from topological defects & FOTP.
- Phenomenologically viable routes: unification, proton decay, and inflation removing dangerous defects.
- Prediction of a certain combination of GW signals may be probed.

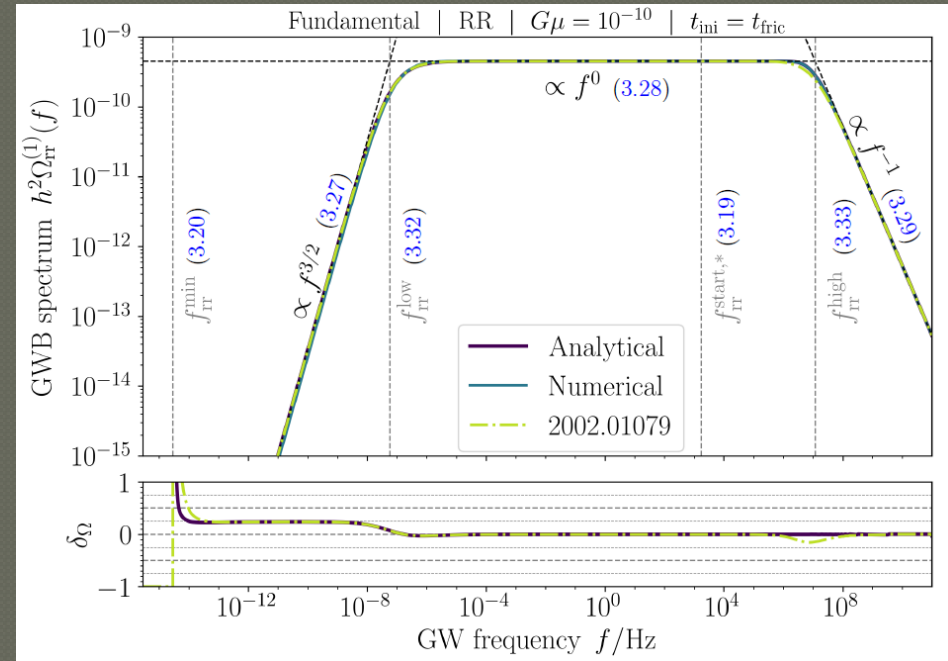
GW from Cosmic Strings

Flat spectrum from a scaling solution during radiation era

Schmitz, Schroeder, 2412.20907

$$\Omega_{\text{GW}} h^2 \sim 4.5 \times 10^{-10} \left(\frac{G\mu}{10^{-10}} \right)^{1/2} \quad \mu \approx M_{\text{CS}}^2$$

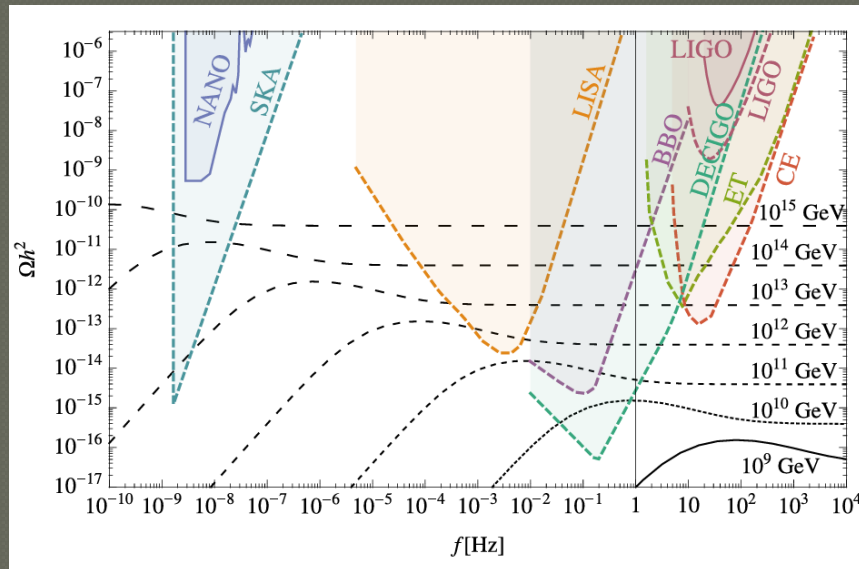
$$5.7 \times 10^{-8} \text{Hz} \left(\frac{10^{-10}}{G\mu} \right) < f < 3.5 \times 10^{10} \text{Hz}$$



GW probing Seesaw/GUT

Seesaw scale of $U(1)_{B-L}$ breaking

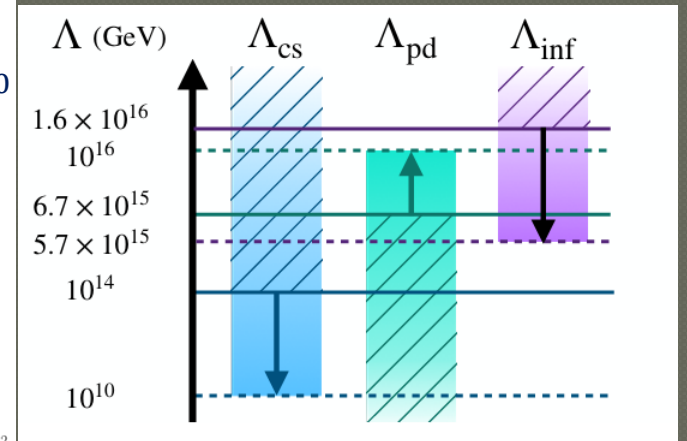
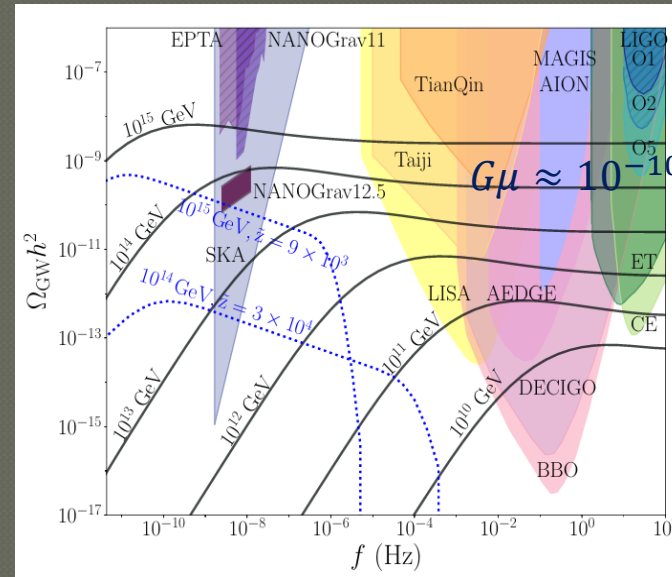
Dror, et.al., 1903.03227



SO(10) GUT with proton decay

$$SO(10) \rightarrow G_I \times U(1)_{B-L} \rightarrow \dots \rightarrow G_{SM}$$

King, Pascoli, Turner, Zhou, 2005.13549



GW from unstable Domain Walls

- Stable overclose the Universe.
- They may be diluted by inflation, or destabilized by a bias potential ΔV breaking softly the symmetry.
- GW signals are controlled by two parameters: wall tension $\sigma \sim M_{\text{DW}}^3$ and ΔV .

$$T_{\text{ann}} \approx 4 \times 10^{-2} \text{GeV} \left(\frac{\sigma}{\text{TeV}^3} \right)^{-\frac{1}{2}} \left(\frac{\Delta V}{\text{MeV}^4} \right)^{\frac{1}{2}} > 10 \text{MeV}$$

$$f_{\text{peak}} \approx \left(\frac{a_{\text{ann}}}{a_0} \right) H_{\text{ann}} \approx 10^{-9} \text{Hz} \left(\frac{T_{\text{ann}}}{10^{-2} \text{GeV}} \right)$$

$$\Omega_{\text{GW}} h^2_{\text{peak}} \approx 10^{-18} \left(\frac{\sigma}{\text{TeV}^3} \right)^2 \left(\frac{T_{\text{ann}}}{10^{-2} \text{GeV}} \right)^{-4}$$

Saikawa, 1703.02576

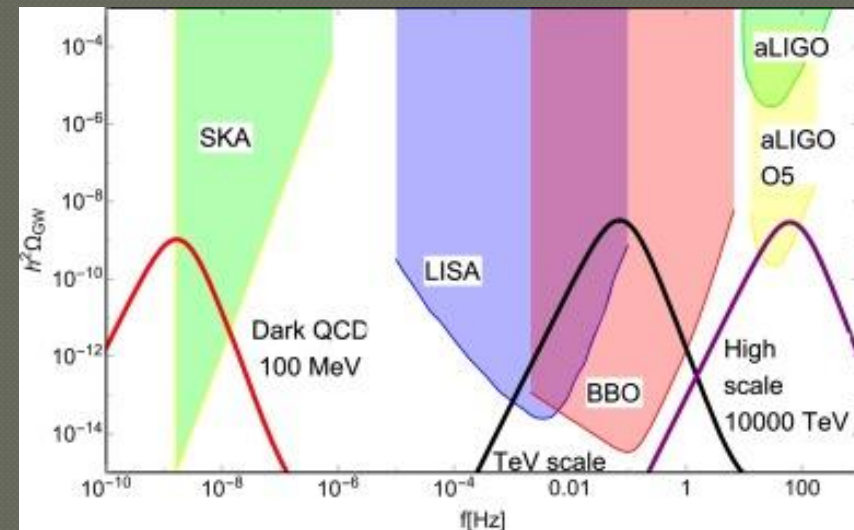
GW from FOPT

- FOPT characterized by nucleation temperature T_* , burble wall velocity v_w , latent heat $\alpha = \Delta\rho/\rho_R$, change of burble nucleation rate β/H_* , which control GW signals:

Caprini, et.al., 1512.06239 (LISA)

$$f_{\text{peak}}^{\text{SW}} \approx 2 \times 10^{-5} \text{Hz} \frac{1}{v_w} \left(\frac{\beta}{H_*} \right) \left(\frac{T_*}{100 \text{GeV}} \right)$$

$$\Omega_{\text{GW}}^{\text{SW}} h^2_{\text{peak}} \approx 2.7 \times 10^{-6} v_w \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{SW}} \alpha}{1 + \alpha} \right)^2$$



Huang, Zhang, 1701.04338 (3-3-1 model)

GUT breaking routes

- ◉ We consider SUSY SO(10) GUT.
- ◉ For a given breaking pattern, intermediate breaking scales are to be fixed consistently with gauge unification and proton decay constraints depending on matter content.
- ◉ Multiple topological defects and FOPT appear, which may be probed by GW detection.

Phenomenological consideration

Observables:

Parameter	Experimental/Lattice values used		
	Current Value	Projected Bound	3σ Discovery
$M_Z(M_Z)$	91.1876 (21) GeV		
$\alpha_S(M_Z)$	0.1179(10)		
$\alpha_{e.m.}(M_Z)$	1/127.9		
$\sin^2 \theta_W(M_Z)$	0.23121(4)		
$m_t(m_t)$	172.5 ± 0.7		
$\langle \pi^0 (ud)_R u_L p \rangle$	$-0.131(4)(13)$ [67]		
$\langle \pi^0 (ud)_L u_L p \rangle$	$0.134(5)(16)$ [67]		
$\tau(p \rightarrow \pi^0 e^+)$	$> 1.6 \times 10^{34}$ yrs [67] [68] 95% C.L.	7.8×10^{34} yrs 90% C.L. [HK[63]]	6.3×10^{34} yrs [HK[63]]
$\tau(p \rightarrow K^+ \bar{\nu})$	$> 6.6 \times 10^{33}$ yrs 95% C.L.	5×10^{34} yrs [DUNE [62]] 3.2×10^{34} yrs 90% C.L. [HK[63]]	2×10^{34} yrs [HK[63]]

Common outputs: $M_{GUT} \approx (8.9 - 1.6) \times 10^{16}$ GeV

$$\tau(p \rightarrow K^+ \bar{\nu}) \sim 4 \times 10^{33} \left(\frac{M_S}{10 \text{ TeV}} \right)^2 \left(\frac{M_{HC}}{10^{16} \text{ GeV}} \right)^2 \text{ yr}$$

Standard routes

Intermediate steps of breaking and the corresponding Higgs multiplets

Appearance of **FOPT** and topological defects: **2(MP)**, **1(CS)**, **0(DW)**

$$\begin{aligned}
 \text{SO}(10) & \xrightarrow[126 (2)]{M_{\text{GUT}}} \text{SU}(5) \times \text{U}(1)_V \xrightarrow[45 (2)]{M_R} \text{SU}(3)_C \times \text{SU}(2)_L \times \text{U}(1)_V \times \text{U}(1)_Z, \xrightarrow[45 (1)]{M_{B-L}} G_{\text{SM}} \times \mathbb{Z}_2 \\
 & \xrightarrow[10]{M_{\text{EW}}} \text{SU}(3)_C \times \text{U}(1)_Y \times \mathbb{Z}_2, \\
 \text{SO}(10) & \xrightarrow[45 (2)]{M_{\text{GUT}}} \text{SU}(3)_C \times \text{SU}(2)_L \times \text{SU}(2)_R \times \text{U}(1)_{B-L} \xrightarrow[126 (1,\text{pt})]{M_{B-L}} G_{\text{SM}} \times \mathbb{Z}_2 \\
 & \xrightarrow[10]{M_{\text{EW}}} \text{SU}(3)_C \times \text{U}(1)_Y \times \mathbb{Z}_2, \\
 \text{SO}(10) & \xrightarrow[210 (2,1)]{M_{\text{GUT}}} \text{SU}(3)_C \times \text{SU}(2)_L \times \text{SU}(2)_R \times \text{U}(1)_{B-L} \times D \xrightarrow[45 (0)]{M_D} \\
 & \text{SU}(3)_C \times \text{SU}(2)_L \times \text{SU}(2)_R \times \text{U}(1)_{B-L} \xrightarrow[126 (1)]{M_{B-L}} G_{\text{SM}} \times \mathbb{Z}_2 \\
 & \xrightarrow[10]{M_{\text{EW}}} \text{SU}(3)_C \times \text{U}(1)_Y \times \mathbb{Z}_2.
 \end{aligned}$$

SU(5) route

$$SO(10) \Rightarrow SU(5) \times U(1)_V \Rightarrow SU(3)_C \times SU(2)_L \times U(1)_Z \times U(1)_V \Rightarrow G_{SM} \times Z_2$$

$$M_{GUT} \approx 10^{16} \text{ GeV}$$

MP

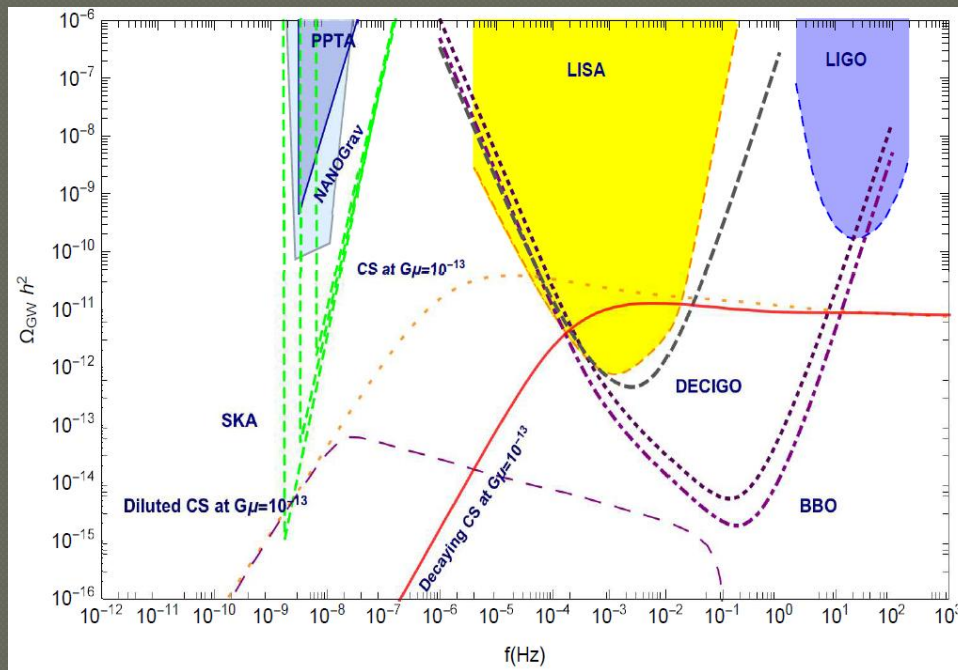
$$M_R > 10^{14} \text{ GeV}$$

MP

$$T_{RH}$$

$$M_{B-L} \approx 10^{14} \text{ GeV}$$

CS



Diluted CS

Regeneration after inflation

Cui, Levicki, Morrissey, 1912.08832

Decaying CS

Strings connecting MP-antiMP

$$\frac{\Gamma_{\text{dec}}}{\mu} = \frac{1}{2\pi} e^{-M_R^2/\mu}$$

Martin, Vilenkin, 9606022

LR route

$$SO(10) \Rightarrow SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \Rightarrow G_{SM} \times Z_2$$

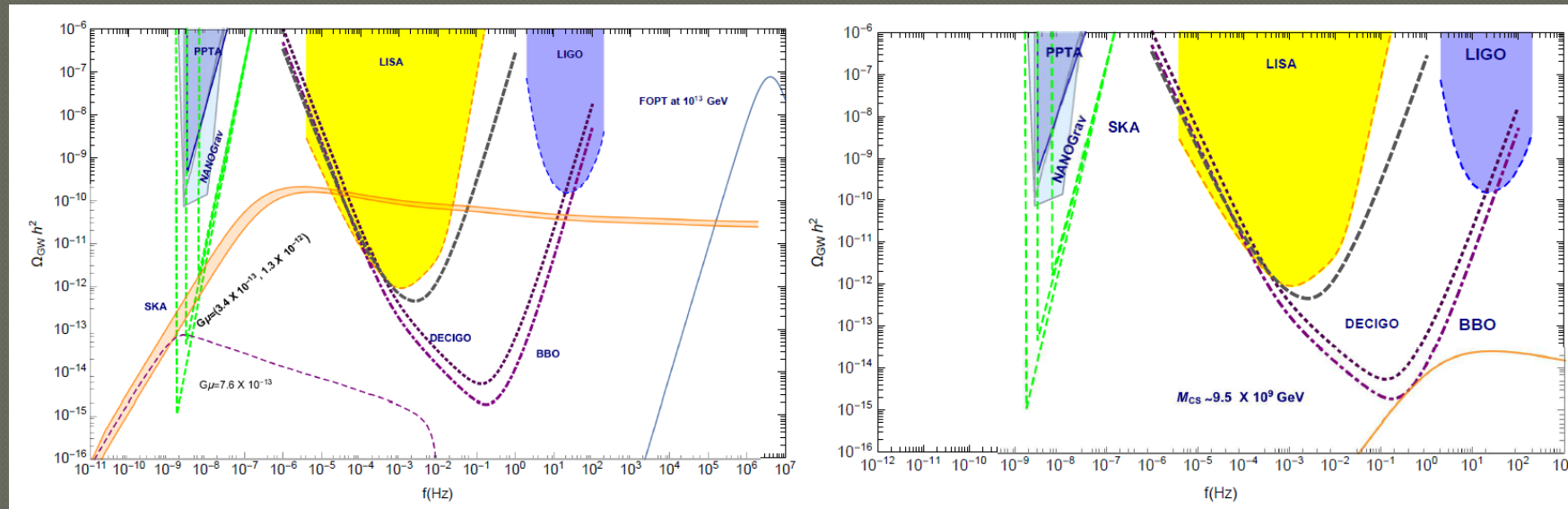
$$M_{GUT} \approx 10^{16} \text{ GeV}$$

MP

$$T_{RH}$$

$$M_{B-L} \approx 3 \times 10^{13} \text{ GeV}$$

CS, FOPT



SUSY

non-SUSY

LR route with D-parity

$$SO(10) \Rightarrow SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times D$$

$$M_{GUT} \approx 10^{16} \text{ GeV}$$

MP, CS

 T_{RH}

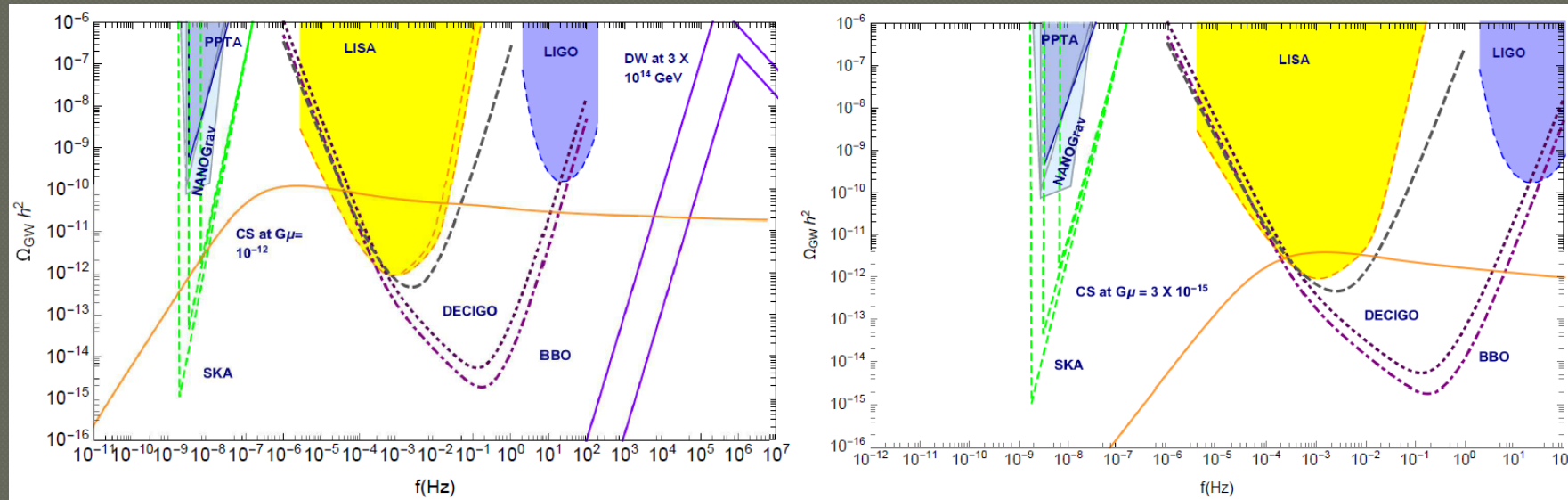
$$\Rightarrow SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \Rightarrow G_{SM} \times Z_2$$

$$M_R \approx 3 \times 10^{14} \text{ GeV}$$

DW

$$M_{B-L} \approx 4 \times 10^{13} \text{ GeV}$$

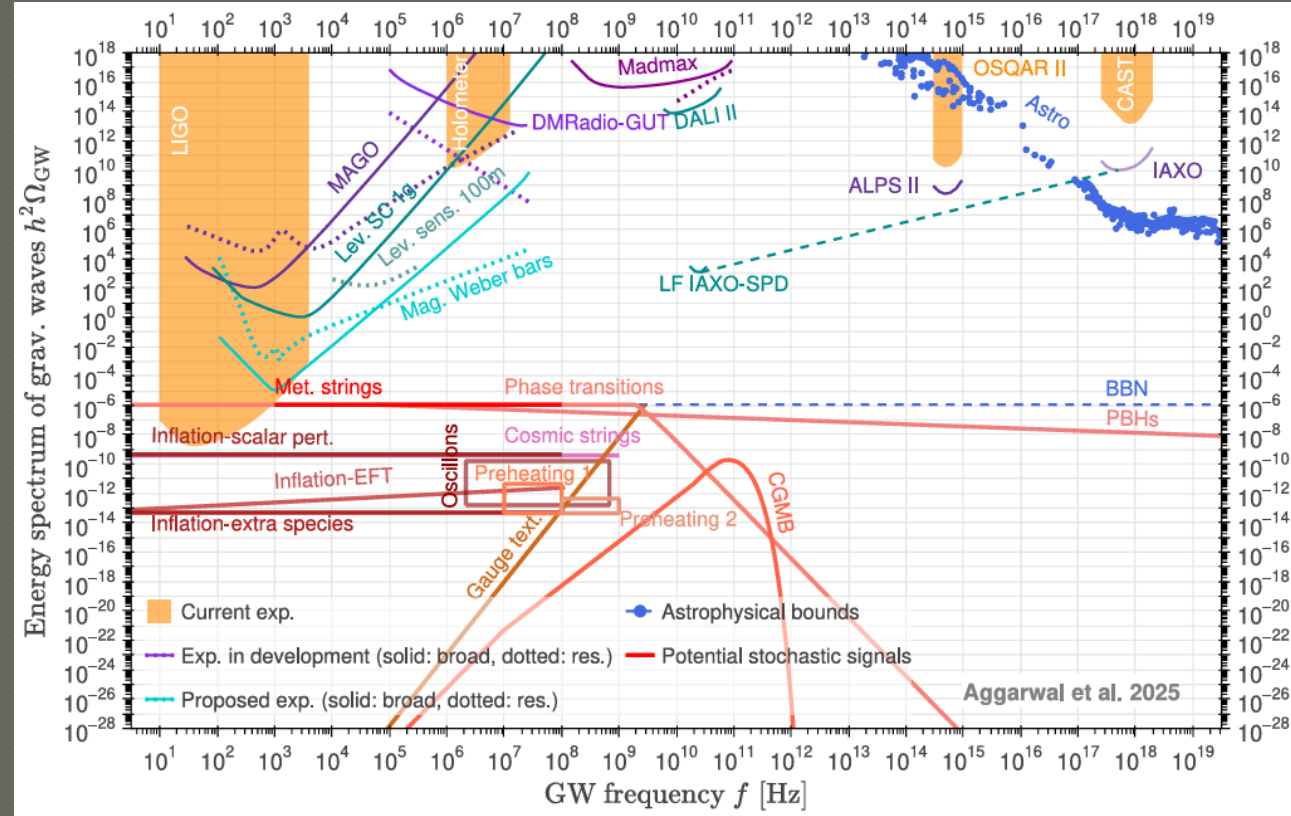
CS



SUSY

non-SUSY

HFGW detection



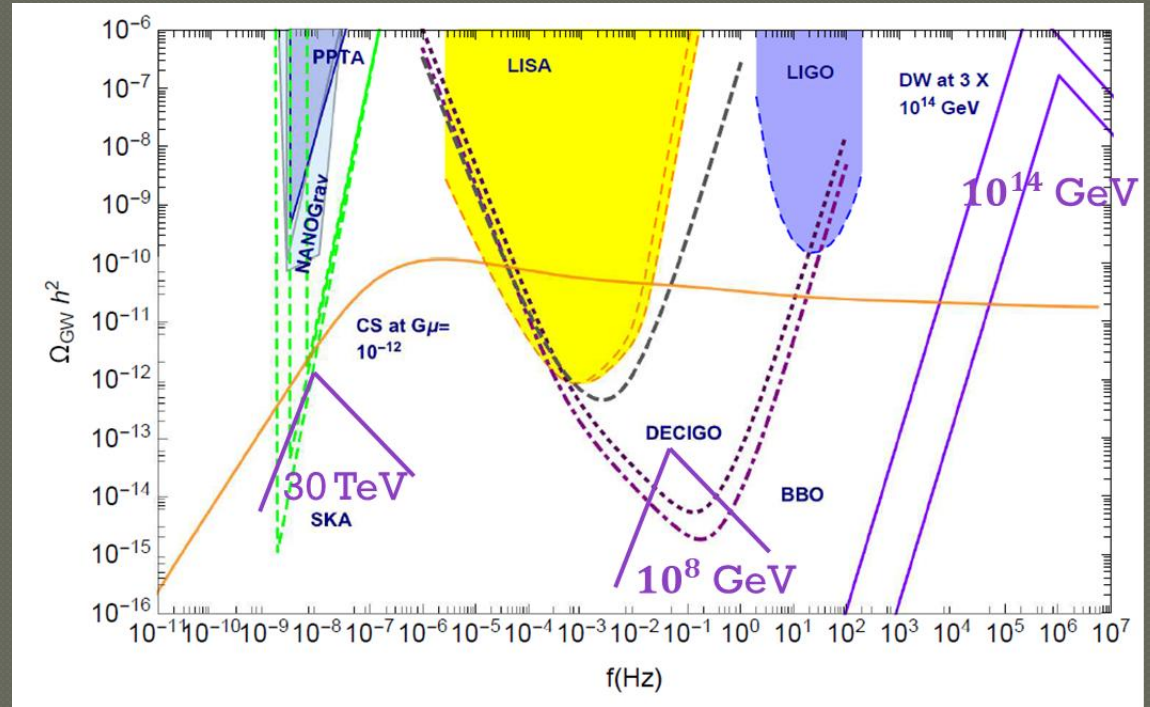
2501.11723

DW at lower scale?

Consistent Z_2 breaking with an additional Higgs?

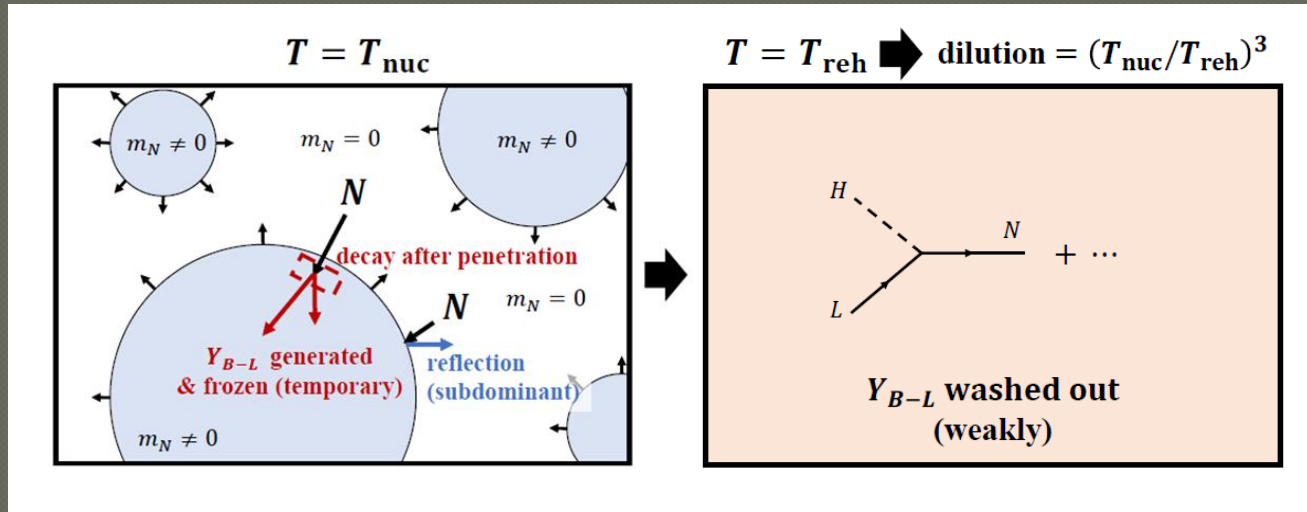
$$f_{\text{peak}} \approx \left(\frac{a_{\text{ann}}}{a_0} \right) H_{\text{ann}} \approx 10^{-9} \text{Hz} \left(\frac{T_{\text{ann}}}{10^{-2} \text{GeV}} \right)$$

$$\Omega_{\text{GW}} h^2_{\text{peak}} \approx 10^{-18} \left(\frac{\sigma}{\text{TeV}^3} \right)^2 \left(\frac{T_{\text{ann}}}{10^{-2} \text{GeV}} \right)^{-4}$$



A route with Bubble Leptogenesis

EJC, Dutka, Jung, Nagels, Vanvlasselaer, 2305.10759

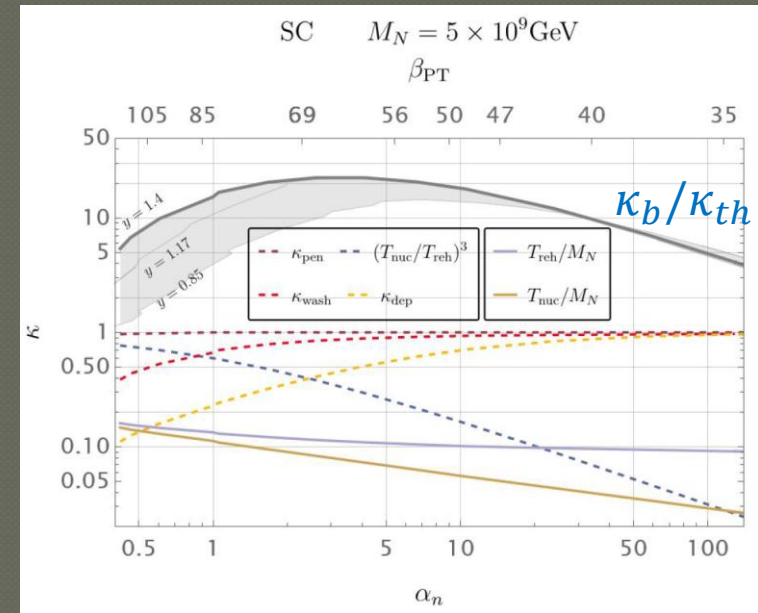


Penetration

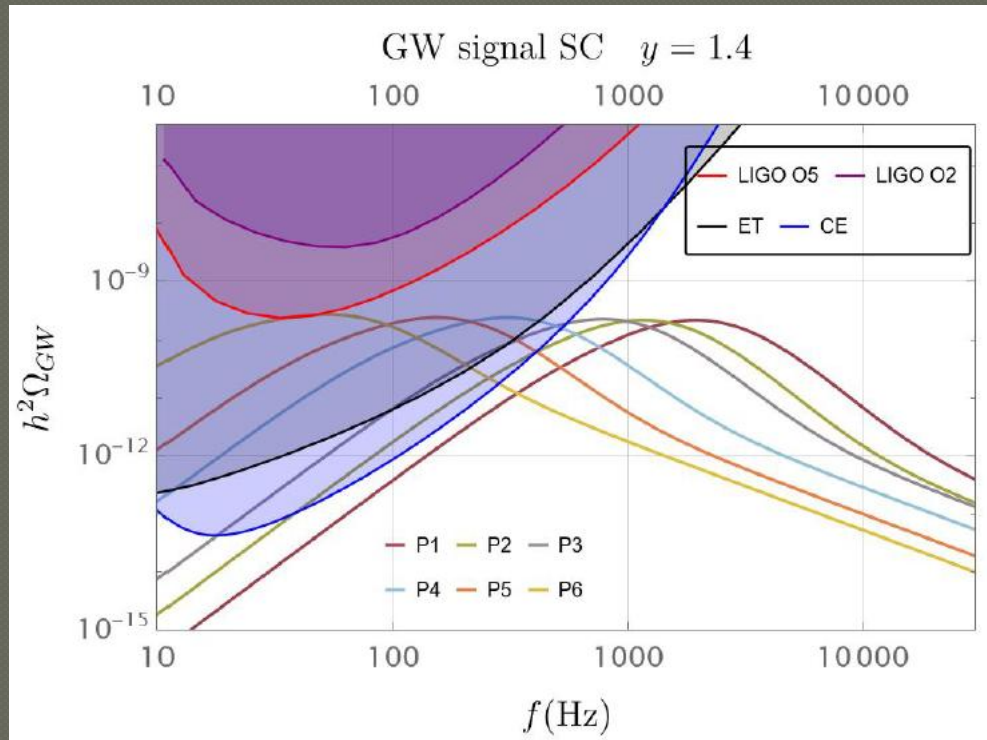
Depletion

$$\Gamma(NN \rightarrow \phi\phi) \sim y^4 \left(\frac{T}{M_N}\right)^4 M_N$$

$$Y_B = Y_N^{\text{eq}} \epsilon_{\text{CP}} \kappa_{\text{sph}} \kappa_{\text{wash}} \kappa_{\text{pen}} \kappa_{\text{dep}} \left(\frac{T_{\text{nuc}}}{T_{\text{reh}}}\right)^3$$



FOPT at lower scale?



$$M_{B-L} = 10^{8-9} \text{GeV}$$

	SC		
	$M_N/10^8 \text{GeV}$	$\frac{n_B^{FOPT}}{n_B^{\text{thermal}}}$	α_n
P1	62	26	4.4
P2	34	21	6
P3	26	18	6.
P4	10	12	10
P5	4.2	8	25
P6	1.4	3.5	25

Conclusion

- To track a route from $SO(10)$ down to SM using GW signals, we identified appropriate intermediate breaking scales consistently with gauge unification and proton decay.
- SUSY models can be different from non-SUSY models.
- Typically appear observable CS signals and very high frequency GW from DW and FOPT.
- Desirable to explore the possibility of DW/FOPT formation at low scales.