

Precision measurement of CP violation and branching fractions in $B^\pm \rightarrow K_S^0 h^\pm$ ($h = \pi, K$) decays, and a search for the rare decay $B_c^\pm \rightarrow K_S^0 K^\pm$

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Outline

- Motivation and Previous measurements
- Analysis strategy
- Corrections to the asymmetry
- Systematic uncertainties
- Search for B_c decay
- Summary

Motivation

$$B^+ \rightarrow K_S^0 h^+ (h^+ = \pi^+, K^+)$$

- Dominated by gluonic penguin contributions
- Color-suppressed electroweak P'_{EW} and annihilation amplitudes are expected to be small

Theoretical predictions → Strong model dependence

$$A_{CP}(B^\pm \rightarrow K_S^0 K^\pm):$$

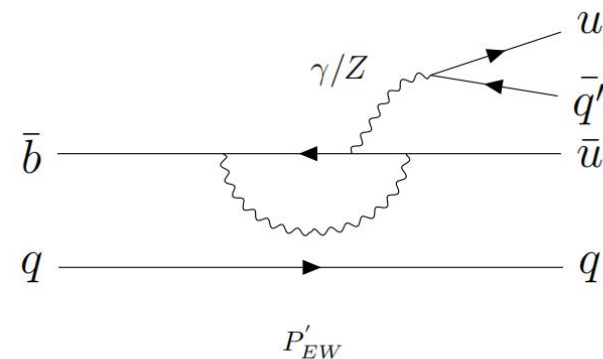
- pQCD predicts: $(1.83^{+1.94}_{-1.88})\%$ [[Chin. Phys. C 46 \(2022\) 123103](#)]
- QCDF predicts: $(-6.4^{+2.0}_{-1.9})\%$ [[Phys. Rev. D 80, 114008](#)] [[Phys. Rev. D 91, 014011](#)]

$$A_{CP}(B^\pm \rightarrow K_S^0 \pi^\pm):$$

Both predict ~ 0 , with $< 0.1\%$ uncertainty

The sign flip between models for $K_S^0 K^\pm$ implies competing contributions:

- Penguin annihilation vs. NLO QCD effects
- Needs experimental clarification



Motivation

A long-standing anomaly associated with the significant differences between direct CP-violating asymmetries observed in $B^+ \rightarrow K^+ \pi^0$ and $B_d^0 \rightarrow K^+ \pi^-$ decays.

Mode	BR[10 ⁻⁶]	A _{CP}
$B^+ \rightarrow K^+ \pi^0$	12.94 ± 0.52	0.040 ± 0.021
$B_d^0 \rightarrow K^+ \pi^-$	19.57 ± 0.53	-0.082 ± 0.006

[\[JHEP 01 \(2018\) 074\]](#)

$B \rightarrow \pi K$ Puzzle

The isospin sum rule observable $I_{K\pi}$:

[\[Phys. Rev. D 59 \(1999\) 113002\]](#)

$$I_{K\pi} = A_{K^+\pi^-} + A_{K^0\pi^+} \cdot \frac{B(K^0\pi^+)}{B(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2A_{K^+\pi^0} \cdot \frac{B(K^+\pi^0)}{B(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2A_{K^0\pi^0} \cdot \frac{B(K^0\pi^0)}{B(K^+\pi^-)} \approx 0 \text{ (SM predicts, with } \sim 1\% \text{ uncertainty)}$$

- in the limit of isospin symmetry
- assuming no electroweak penguin contributions

→ a good test of the SM

$B^+ \rightarrow K_s^0 \pi^+$ is sensitive to hadronic effects

- Useful for testing the isospin sum rule $I_{K\pi}$
- Probes EW penguin and annihilation contributions

Previous measurements



➤ LHCb 2011+2012 ($3fb^{-1}$)

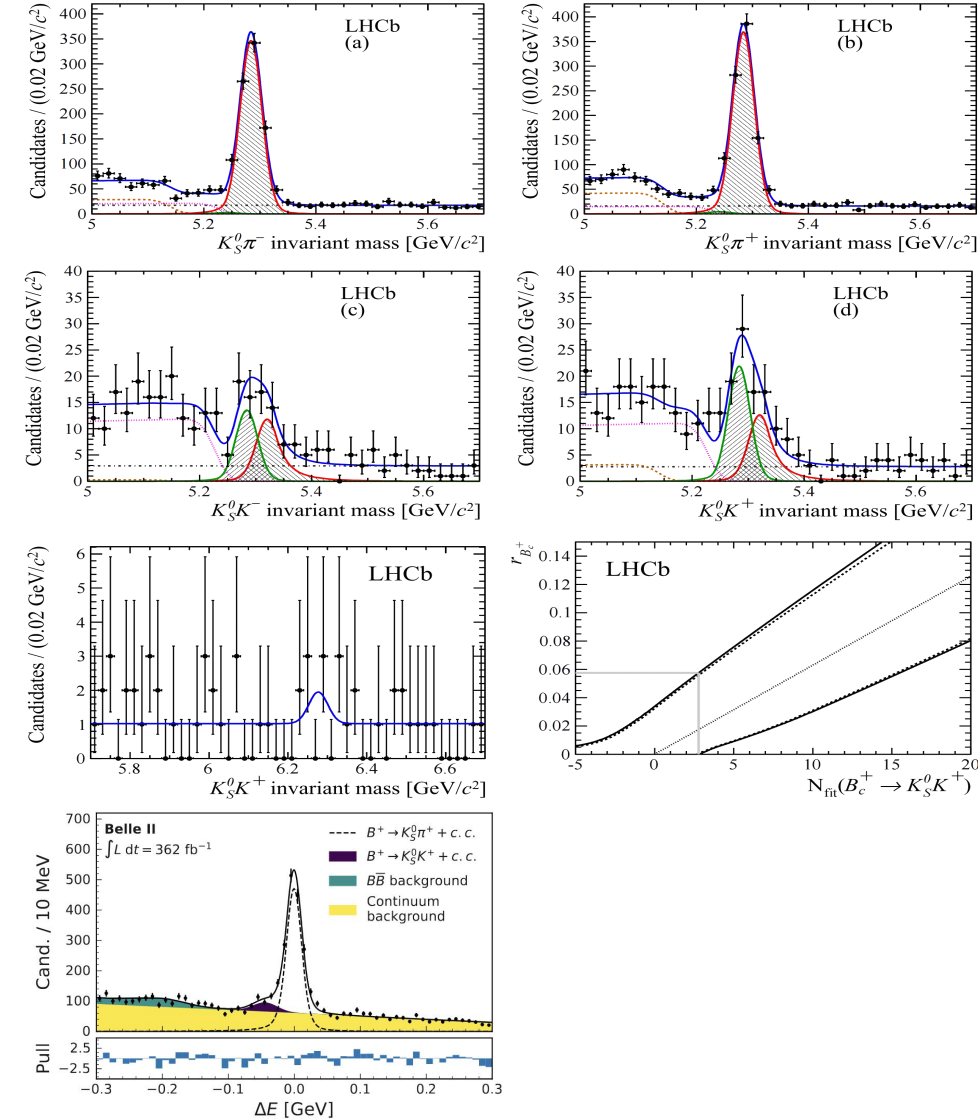
- $\mathcal{R} = \frac{\mathcal{B}(B^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)} = 0.0640 \pm 0.0038 \pm 0.0101$
- $\mathcal{A}^{CP}(B^+ \rightarrow K_S^0 K^+) = -0.21 \pm 0.14 \pm 0.01$
- $\mathcal{A}^{CP}(B^+ \rightarrow K_S^0 \pi^+) = -0.024 \pm 0.025 \pm 0.010$
- $\mathcal{R}' = \frac{f_c}{f_u} \cdot \frac{\mathcal{B}(B_c^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)} < 5.8 \times 10^{-2}$ at 90% confidence level

[LHCb-PAPER-2013-034](#)
[ArXiv:1308.1277](#)

➤ Belle II ($362fb^{-1}$)

- $\mathcal{B}(B^+ \rightarrow K^0 \pi^+) = [24.37 \pm 0.71 \pm 0.86] \times 10^{-6}$
- $\mathcal{A}^{CP}(B^+ \rightarrow K_S^0 \pi^+) = 0.046 \pm 0.029 \pm 0.007$

Belle II
[arXiv:2310.06381\(2024\)](#)
[Phys. Rev. D 109, 012001 \(2024\)](#)



- Samples: $B^+ \rightarrow K_S^0 \pi^+$, $B_{(c)}^+ \rightarrow K_S^0 K^+$ data/MC Run 2(16/17/18, $5.4 fb^{-1}$, 13TeV)
- Event Selection:
 - StrippingBu2KShLLLine
 - Offline selection, Simulated samples corrections, Multivariate selection, Mass Veto
- Mass fits: $B^+ \rightarrow K_S^0 \pi^+$ and $B^+ \rightarrow K_S^0 K^+$ are fitted simultaneously
- Corrections to the asymmetry measurement
- Systematics uncertainties
- Search for $B_c^+ \rightarrow K_S^0 K^+$ decay

PID&MVA optimization



- PID requirements follow the same strategy as Run 1
- Optimal BDTG output requirement

pion: PIDK < 3

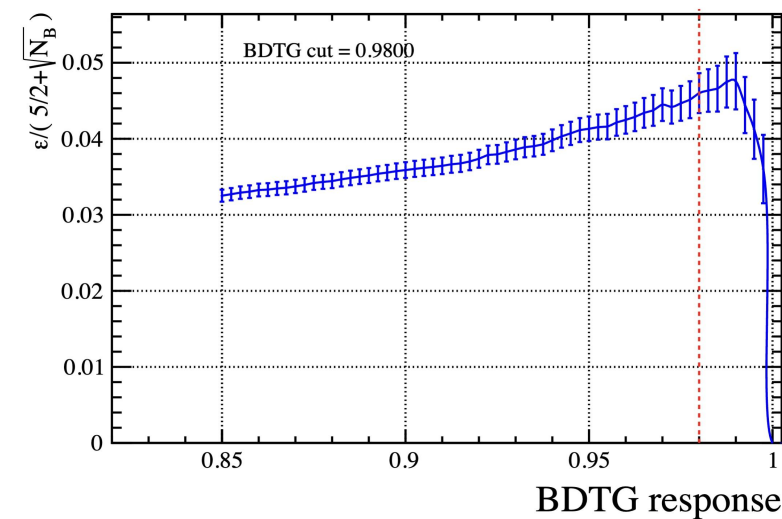
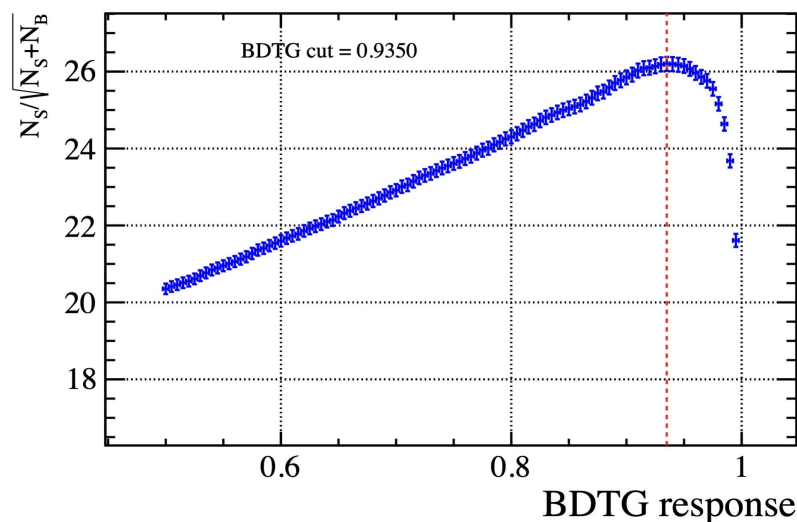
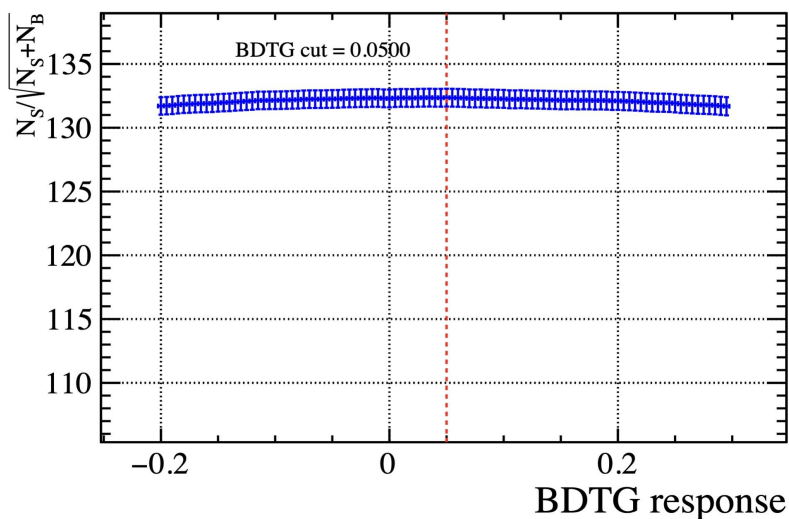
kaon: PIDK > 3

- $B^+ \rightarrow K_s^0 h^+$: maximize signal significance

$$FoM = \frac{N_S}{\sqrt{N_S + N_B}}, \quad N_S(N_B): \text{expected signal (background) yield}$$

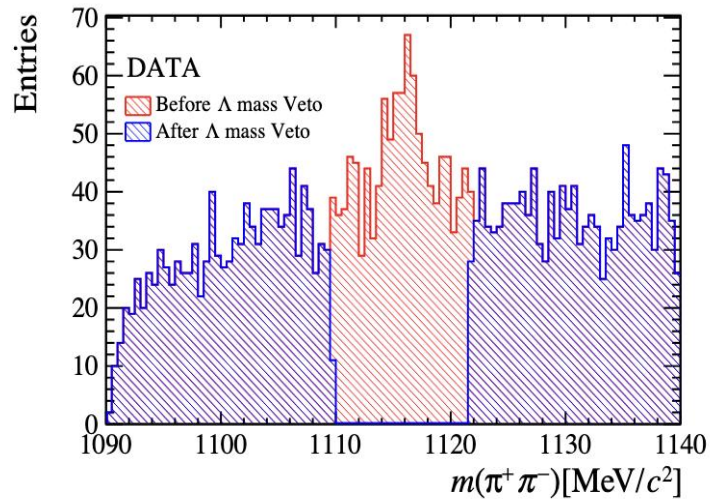
- $B_c^+ \rightarrow K_s^0 K^+$: Punzi FoM

$$FoM = \frac{\varepsilon}{\frac{a}{2} + \sqrt{N_B}}, \quad a = 5, \varepsilon: \text{signal efficiency}$$

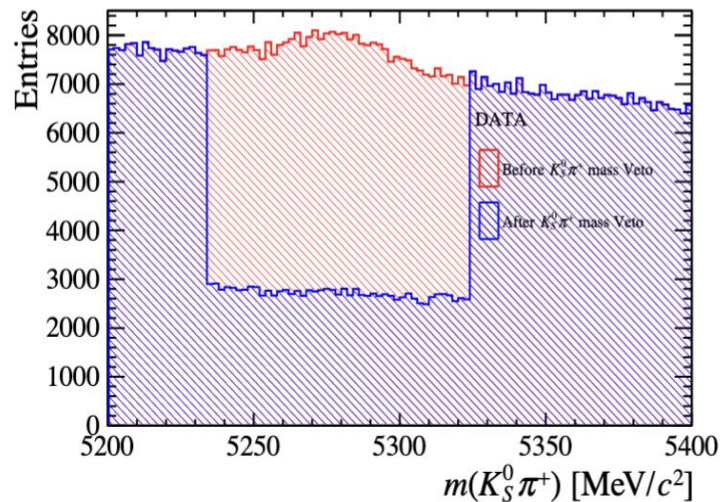


Veto Peaking background

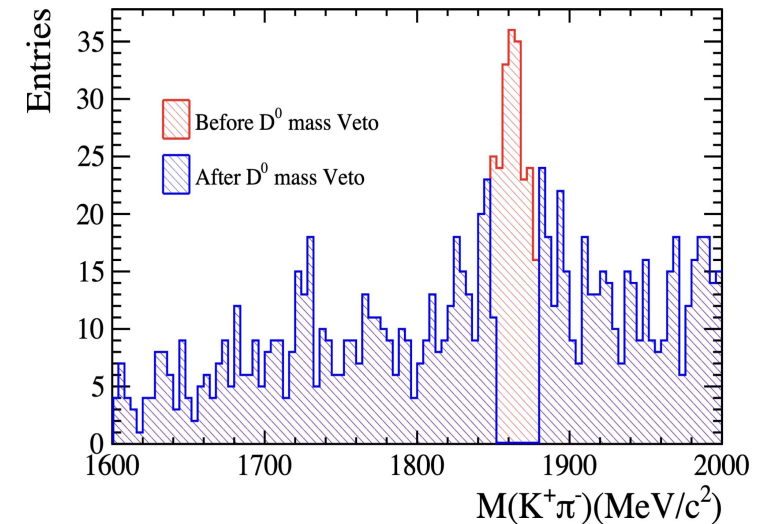
- For the $B^+ \rightarrow K_s^0 \pi^+$ mode
 - Peaking background from $\Lambda \rightarrow p \pi^-$ misidentified as $K_s^0 \rightarrow \pi^+ \pi^-$ ($p \rightarrow \pi$ mis-ID) (left plot)
- For the $B^+ \rightarrow K_s^0 K^+$ mode
 - The same Λ mass veto as in the $B^+ \rightarrow K_s^0 \pi^+$ mode is applied
 - Cross-feed from $B^+ \rightarrow K_s^0 \pi^+$ decays (middle plot)
 - The $B^+ \rightarrow D^0 \pi^+$ process, with $D^0 \rightarrow K^+ \pi^-$ decays (the bachelor kaon and an oppositely charged pion from K_s^0) (right plot)



(a) Λ mass veto

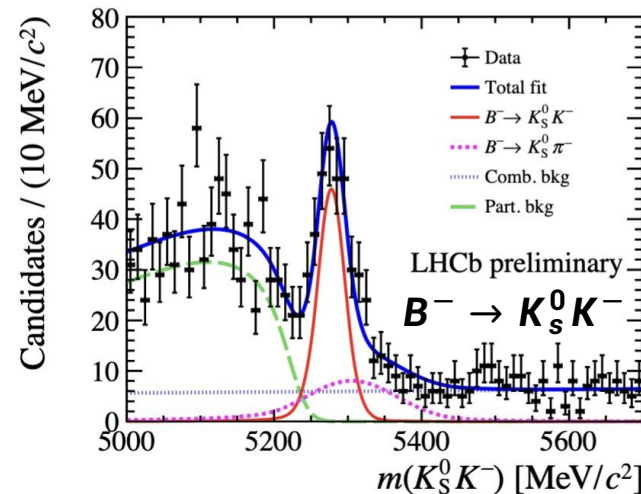
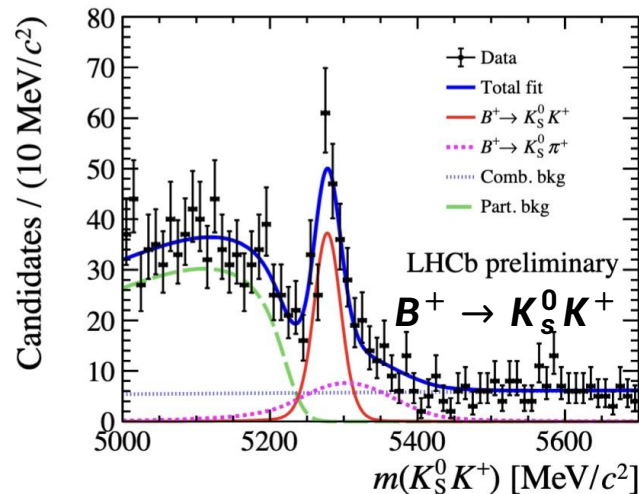
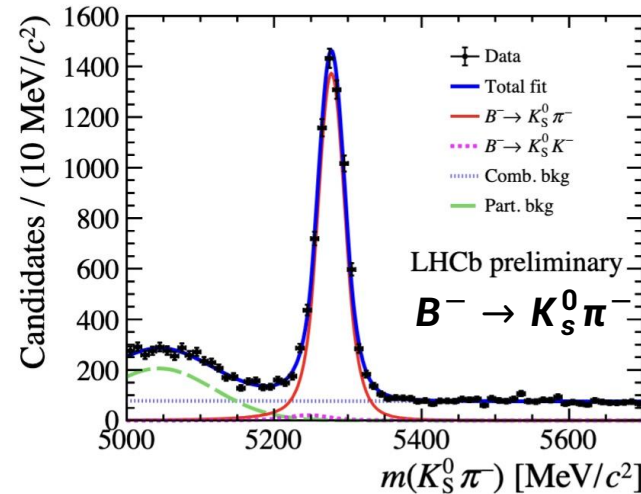
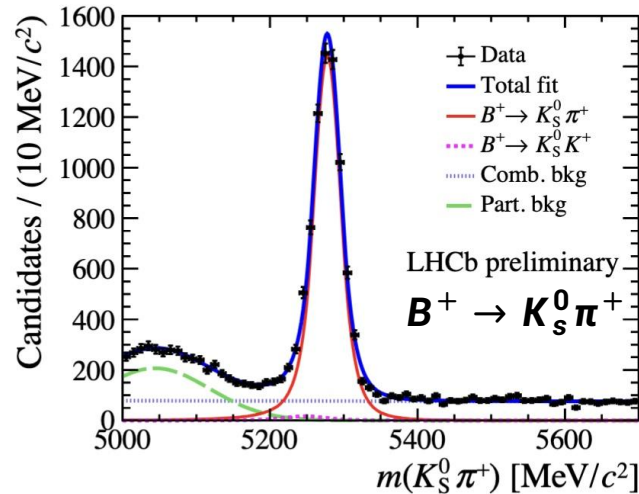


(b) $K_s^0 \pi^+$ mass veto



(c) D^0 mass veto

Simultaneous fit of $K_S^0\pi^+$ and $K_S^0K^+$



➤ Partially Reconstructed Backgrounds

- B^0 , B^+ and B_s^0 decays $\rightarrow$ open-charm final states
- smaller ones from charmless 3-body decays
- Model: Argus function $\otimes$ Gauss resolution

➤ Misidentified Backgrounds

- a DSCB function
- constrained to expected signal yields

➤ Combinatorial background: a first-order polynomial function

➤ Signal mode $B^+ \rightarrow K_S^0 \pi^+ / B^+ \rightarrow K_S^0 K^+$: a DSCB function + a Gaussian function

	$B^\pm \rightarrow K_S^0 \pi^\pm$ Run 2	$B^\pm \rightarrow K_S^0 K^\pm$ Run 2
N_{signal}	14482 ± 156	393 ± 28

Corrections to the CP asymmetry

$$\triangleright \mathcal{A}^{CP}(B^+ \rightarrow K_S^0 \pi^+) = \mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{raw} - \mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{det+prod} + \mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{K_S^0}$$

$$\triangleright \mathcal{A}^{CP}(B^+ \rightarrow K_S^0 K^+) = \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{raw} - \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} - \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{K_S^0}$$

- Raw asymmetry $\mathcal{A}^{raw} = \frac{N(B^-) - N(B^+)}{N(B^-) + N(B^+)}$

- Production and detection asymmetry

Control channel: $B^+ \rightarrow J/\psi K^+$

- $\mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} = \mathcal{A}_{B^+ \rightarrow J/\psi K^+}^{det+prod} = \mathcal{A}_{B^+ \rightarrow J/\psi K^+}^{raw} - \mathcal{A}^{CP}(B^+ \rightarrow J/\psi K^+)$ from PDG [Phys. Rev. D110372 \(2024\) 030001](#)

- $\mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{det+prod} = \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} - \mathcal{A}^{K^+ \pi^-} = \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} - (\mathcal{A}^{K^+ \pi^-} + \mathcal{A}^{K^0}) + \mathcal{A}^{K^0}$

[LHCb-PUB-2018-004](#)

- Neutral kaon asymmetry $\mathcal{A}^{K^0}$

CP violation in the decay $K_S^0 \rightarrow \pi^+ \pi^-$ and interaction of the K^0 with the detector material

[arXiv:1110.3790](#)

[Phys. Rev. D84 \(2011\)](#)

Systematic Uncertainties

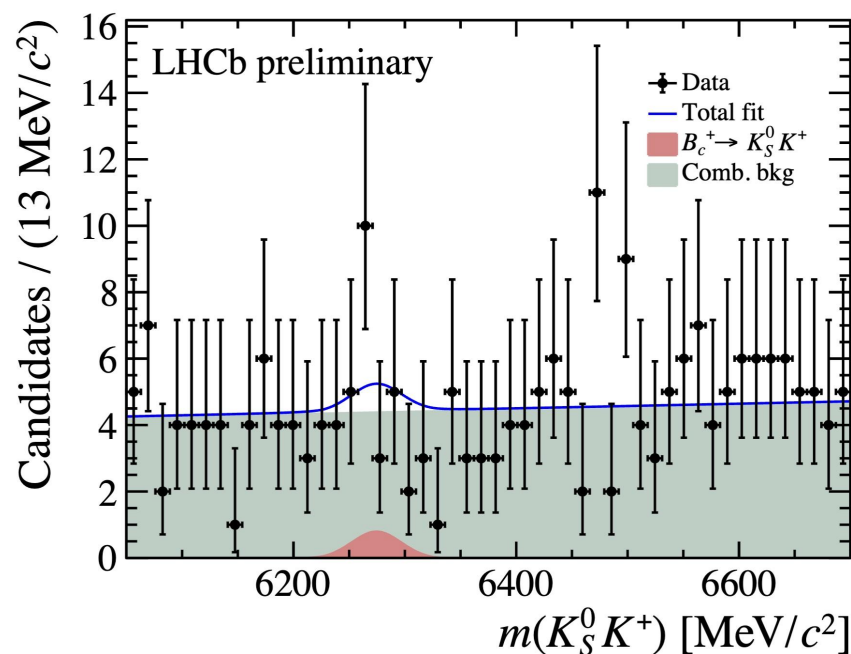


	CP asymmetry (%)		$\mathcal{R}$ (%)
	$B^+ \rightarrow K_S^0 \pi^+$	$B^+ \rightarrow K_S^0 K^+$	
Fit model	0.15	1.29	1.92
PID weighting	0.01	0.01	0.44
$\mathcal{A}^{\text{det+prod}}$	0.32	0.32	—
$(\mathcal{A}^{K^+ \pi^-} + \mathcal{A}^{K^0})$	—	0.01	—
$\mathcal{A}^{K^0}$	0.01	0.01	—
Trigger	0.70	0.74	0.23
Tracking efficiency	—	—	0.01
K/π interaction	—	—	0.30
BDTG selection	0.41	2.56	—
Mass veto selection	0.10	0.88	3.31
Simulation sample size	—	—	0.87
Total	0.89	3.11	3.97

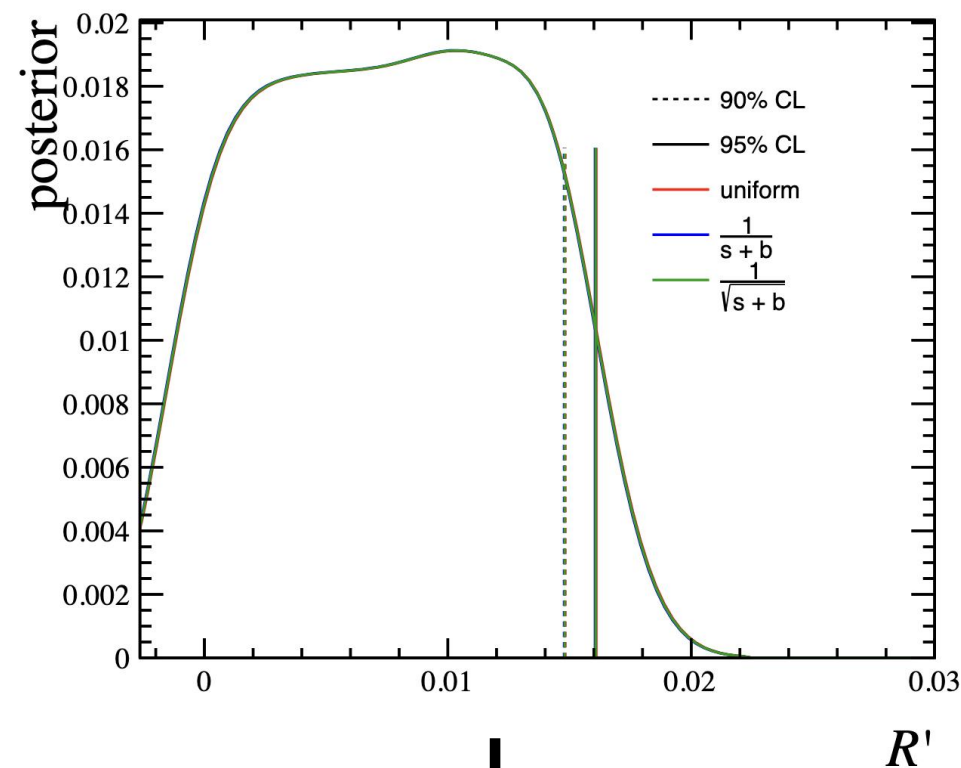
Absolute uncertainties for $\mathcal{A}^{CP}$, relative uncertainties for $\mathcal{R} = \frac{\mathcal{B}(B^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)}$

Search for $B_c^+ \rightarrow K_S^0 K^+$ decay

- **Combinatorial background:** a first-order polynomial function
- **Signal model:** a DSCB function, tail parameters and σ fixed from MC, μ fixed from PDG.



- Smeared profile likelihood curve



$$\mathcal{R}' = \frac{f_c}{f_u} \times \frac{\mathcal{B}(B_c^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)} < 0.015(0.016) \text{ at } 90\%(95\%) \text{ CL}$$

➤ Results

- $\mathcal{A}^{CP}(B^+ \rightarrow K_S^0 \pi^+) = -0.028 \pm 0.009(\text{stat}) \pm 0.009(\text{syst})$
- $\mathcal{A}^{CP}(B^+ \rightarrow K_S^0 K^+) = 0.118 \pm 0.062(\text{stat}) \pm 0.031(\text{syst})$
- $\mathcal{R} = \frac{\mathcal{B}(B^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)} = 0.055 \pm 0.004(\text{stat}) \pm 0.002(\text{syst})$
→ All results are statistically dominated.
- $\mathcal{R}' = \frac{f_c}{f_u} \times \frac{\mathcal{B}(B_c^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)} < 0.015(0.016) \text{ at } 90\%(95\%) \text{ CL}$

➤ Conclusion and Outlook

- Improved precision compared to previous LHCb measurement
- All measurements are consistent with SM predictions, while offering improved constraints for flavor physics and searches for physics beyond the SM
- With the increased statistics from LHCb Run 3, future analyses will further enhance the sensitivity to potential deviations from the SM

Thanks for listening!

Back up

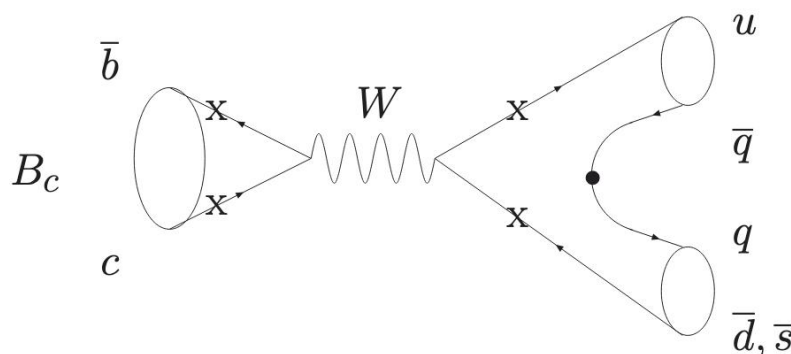
At tree level, only annihilation diagrams contribute to $B_c^+ \rightarrow K_s^0 K^+$

Offers clean test of QCD annihilation via $b - c$ annihilation mediated by W^+ boson.

Theoretical prediction:

- Branching fraction $\rightarrow 10^{-6}$ to 9×10^{-8} [\[Phys. Rev. D 80 \(2009\) 114031\]](#)

If observed, this decay would offer a unique test ground for annihilation dynamics in heavy meson decays



Generic diagram for the non-leptonic charmless B_c decays [\[arXiv:0907.2256v1\]](#)

➤ Trigger

- L0: Hadron TOS || DiMuon TIS || Muon TIS || Electron TIS || MuonEW TIS || Hadron TIS || JetElectron TIS || JetPhysics TIS
- HLT1: TrackMVA TOS || TwoTrackMVA TOS
- HLT2: Topo(2,3)Body(Simple) TOS

➤ Further offline selection

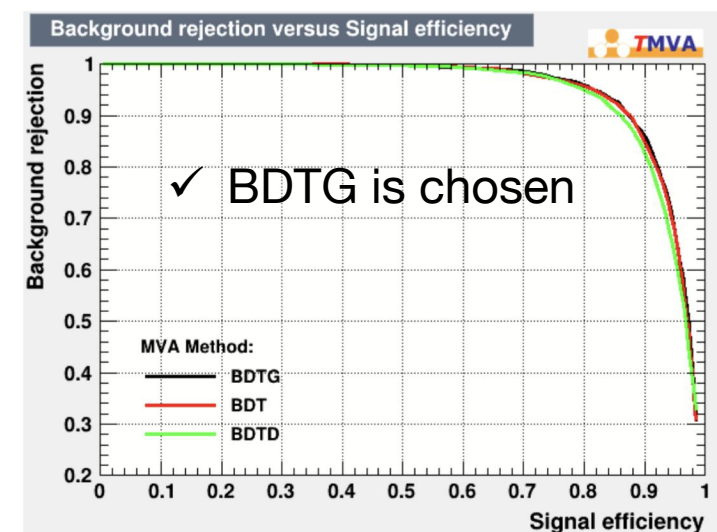
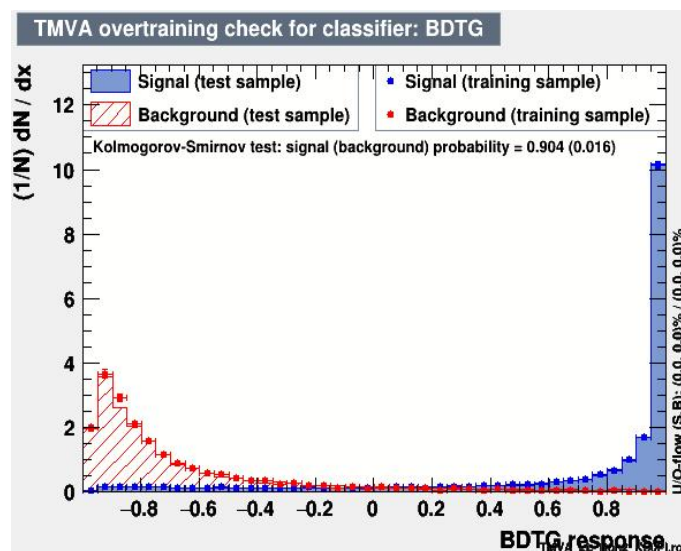
Particle	Variable	Cut
K_S^0	$(z(K_S^0) - z(B)) / \sqrt{\sigma_z^2(K_S^0) + \sigma_z^2(B)}$	> 2
Bachelor h	χ_{IP}^2	> 16
Bachelor h	p	$< 300 \text{ GeV}$
Bachelor h	hasRich	true
track	hasMuon && isMuon	false
B	χ^2 of the B^+ vertex fit	< 20
Fiducial cut	n / a	$ p_x > 0.267 \times p - 1400 $ $-0.00285 \times p + 818 < p_x < 0.01034 \times p + 818$

- **Training samples** ($B^+ \rightarrow K_S^0 \pi^+$ and $B^+ \rightarrow K_S^0 K^+$ are trained separately)
 - Signal: $B^+ \rightarrow K_S^0 h^+$ full simulated sample (reweighted)
 - Background: candidates in high sideband $m(K_S^0 h^+) \in (5600, 6000) \text{ MeV}$

➤ Training variables

Particle	Variable
B	p_T asymmetry in a cone of 1 rad
B	p_T
B	χ_{IP}^2
B	$\chi_{\text{vtx}}^2 / \text{ndf}$
bachelor π	χ_{IP}^2
K_S^0	χ_{IP}^2
K_S^0	$(z(K_S^0) - z(B)) / \sqrt{\sigma_z^2(K_S^0) + \sigma_z^2(B)}$
B	DIRA
B	DecayTreeFitter (DTF) χ^2 / ndf
B	$c\tau$

➤ Algorithms



Selection	$B^+ \rightarrow K_S^0 \pi^+$	$B^+ \rightarrow K_S^0 K^+$	$B_c^+ \rightarrow K_S^0 K^+$
Acceptance(%)	25.98 ± 0.05	18.48 ± 0.03	24.81 ± 0.04
MC Match(%)	96.70 ± 0.14	96.97 ± 0.15	99.80 ± 0.08
Preselection(%)	1.15 ± 0.01	1.58 ± 0.01	1.03 ± 0.01
Trigger(%)	44.00 ± 0.23	42.25 ± 0.20	32.07 ± 0.23
LooseSelection(%)	97.46 ± 0.11	-	-
Veto(%)	95.48 ± 0.20	76.35 ± 0.36	-
PID(%)	97.46 ± 0.14	78.11 ± 0.30	75.96 ± 0.37
BDTG(%)	85.64 ± 0.31	71.08 ± 0.37	39.61 ± 0.49
Track(%)	99.88 ± 0.00	99.87 ± 0.00	99.64 ± 0.00
Total(10^{-4})	10.27 ± 0.10	5.41 ± 0.06	2.45 ± 0.04

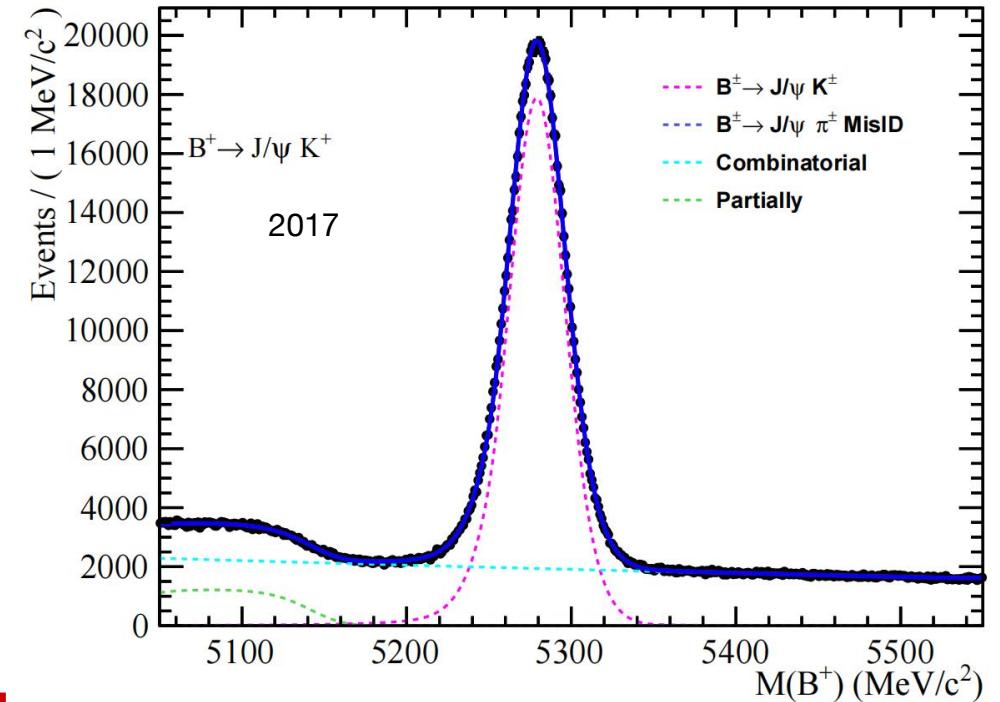
Production and detection asymmetry($\mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod}$)



Control channel: $B^+ \rightarrow J/\psi K^+$

Stripping line: FullDSTDimuonJpsi2MuMuDetachedLine

Particle	Variable	Cut
J/ψ	invariant mass $\chi^2_{\text{vtx}}/\text{ndf}$	[3048, 3139] < 10
K	p_T momentum $\chi^2_{\text{track}}/\text{ndf}$ PID	> 1000.0 MeV < 300000 MeV < 16 > 3
fiducial cut	n / a	$ h_{PX} > 0.267 h_P - 1400 $ $-0.00385h_P + 818 < h_{PX} < 0.01034h_P + 818$
trigger	L0	L0Muon TOS L0DiMuon TOS
trigger	HLT1	Hlt1TrackMuon TOS Hlt1DiMuonHighMass TOS
trigger	HLT2	Topo(2,3)Body(Simple) TOS



$$\mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} = \mathcal{A}_{B^+ \rightarrow J/\psi K^+}^{det+prod} = \boxed{\mathcal{A}_{B^+ \rightarrow J/\psi K^+}^{raw}} - \boxed{\mathcal{A}^{CP}(B^+ \rightarrow J/\psi K^+)}$$

First Second

$$\mathcal{A}_{B^+ \rightarrow J/\psi K^+}^{raw} = \frac{N^{B^- \rightarrow J/\psi K^-} - N^{B^+ \rightarrow J/\psi K^+}}{N^{B^- \rightarrow J/\psi K^-} + N^{B^+ \rightarrow J/\psi K^+}}$$

$(0.18 \pm 0.30)\%$ From PDG 2025

Production and detection asymmetry($\mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{det+prod}$)



$$\mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{det+prod} = \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} - \mathcal{A}^{K^+ \pi^-} = \mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{det+prod} - (\mathcal{A}^{K^+ \pi^-} + \mathcal{A}^{K^0}) + \mathcal{A}^{K^0}$$

depends on momentum(P)

Bin	p(K^-) GeV/c	$\mathcal{A}^{det}(K^- \pi^+) + \mathcal{A}(K^0)[\%]$
1	3 - 5	-1.81 ± 0.11
2	5 - 10	-1.15 ± 0.05
3	10 - 15	-0.97 ± 0.04
4	15 - 20	-0.79 ± 0.06
5	20 - 25	-0.68 ± 0.07
6	25 - 40	-0.64 ± 0.07
7	40 - 60	-0.46 ± 0.14
8	60 - 80	-0.37 ± 0.17

$$\longrightarrow N_{eff} = \frac{(\sum_{j=1}^N w_i)^2}{\sum_{j=1}^N w_i^2}$$

$$\mathcal{A}^{K^+ \pi^-} + \mathcal{A}^{K^0} = (-0.64 \pm 0.01)\%$$

[LHCb-PUB-2018-004](#)

Systematic Uncertainties



1. Mass fit
2. PID efficiency and PID asymmetry
 - Binning scheme of PID efficiencies → [the PID efficiency maps](#)
 - Statistics of PID calibration sample
 - Kernel density PDFs used in the PID efficiency study
 - Statistics of signal simulation sample
3. L0 Trigger efficiency and L0 Trigger asymmetry $\varepsilon_{L0trigger}^{weighted} = \frac{\sum_{i=1} w_{GB,i}}{\sum_{i=1} w_{GB,i}/\varepsilon_i} \rightarrow$ [L0 hadron efficiency tables](#)
4. Selection efficiency
 - MVA selection efficiency
 - Veto selection efficiency
5. Other uncertainties

Asymmetry: Det+Prod asymmetry, $A^{K^+\pi^-} + A^{K^0}$, neutral kaon asymmetry

Branching-fraction ratio:

- Tracking efficiency correction → based on the momentum (p) and pseudorapidity (η)
- K/ π interaction → Limitations in the description of the detector material → [Tracking systematics for hadrons](#)
- MC Sample statistics

CP asymmetry and Branch fraction ratio

- $\mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{\text{raw}} = -0.030 \pm 0.009(\text{stat})$ $\mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{\text{raw}} = -0.109 \pm 0.062(\text{stat})$
- $\mathcal{A}_{B^+ \rightarrow K_S^0 K^+}^{\text{det+prod}} = (-1.02 \pm 0.32)\%$ $\mathcal{A}_{B^+ \rightarrow K_S^0 \pi^+}^{\text{det+prod}} = (-0.31 \pm 0.32)\%$
- $\mathcal{A}^{K^+ \pi^-} + \mathcal{A}^{K^0} = (-0.64 \pm 0.01)\%$ $\mathcal{A}_{B^+ \rightarrow K_S^0 h^+}^{K_S^0} = (-0.07 \pm 0.01)\%$
- $\mathcal{A}^{\text{CP}}(B^+ \rightarrow K_S^0 \pi^+) = -0.030 \pm 0.009(\text{stat}) \pm 0.009(\text{syst})$
- $\mathcal{A}^{\text{CP}}(B^+ \rightarrow K_S^0 K^+) = 0.118 \pm 0.062(\text{stat}) \pm 0.031(\text{syst})$
- $\mathcal{R} = \frac{\mathcal{B}(B^+ \rightarrow K_S^0 K^+)}{\mathcal{B}(B^+ \rightarrow K_S^0 \pi^+)} = \frac{N(B^+ \rightarrow K_S^0 K^+)}{N(B^+ \rightarrow K_S^0 \pi^+)} \times \frac{\varepsilon(B^+ \rightarrow K_S^0 \pi^+)}{\varepsilon(B^+ \rightarrow K_S^0 K^+)} = 0.055 \pm 0.004(\text{stat}) \pm 0.002(\text{syst})$

Search for $B_c^+ \rightarrow K_s^0 K^+$



Upper limit

- The method of profile likelihood $L(x|R', \theta)$ scan is employed to calculate the upper limit on the branching fraction of $B_c^+ \rightarrow K_s^0 K^+$

profile likelihood ratio $\lambda(R')$:

$$\lambda_0(\mathcal{R}') = \frac{L(x|\mathcal{R}', \hat{\theta})}{L(x|\hat{\mathcal{R}}', \hat{\theta})}$$

- Toy MC samples are generated under the "background" only hypothesis.
- The high-mass sideband region (6400-6700 MeV) is fitted using a first-order polynomial function.

Signal Estimation:

- Signal yield is extrapolated from the mass sideband to the search region (6050-6700 MeV).
- Toy MC samples are randomly generated with the assumption of a first-order polynomial slope and a given yield.
- Assuming a flat prior PDF for R' from 0 to 100%, the Bayesian upper limit on R' is calculated at 90%(95%) confidence level

$$\int_0^{\mathcal{R}'_{up}} \lambda(\mathcal{R}') d\mathcal{R}' = 90\%(95\%) \times \int_0^1 \lambda(\mathcal{R}') d\mathcal{R}'$$