

First observation of a negative-parity doubly charmed baryon on lattice

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Doubly charmed baryons

Observation of doubly charmed baryons

- **SELEX** M. Mattson and others, Phys. Rev. Lett. 89, 112001 (2002).
- **FOCUS** S. P. Ratti, Nucl. Phys. B Proc. Suppl. 115, 33 (2003).
- **Belle** R. Chistov and others, Phys. Rev. Lett. 97, 162001 (2006).
- **BABAR** B. Aubert and others, Phys. Rev. D 74, 011103 (2006).
- **LHCb** R. Aaij and others, Phys. Rev. Lett. 119, 112001 (2017).

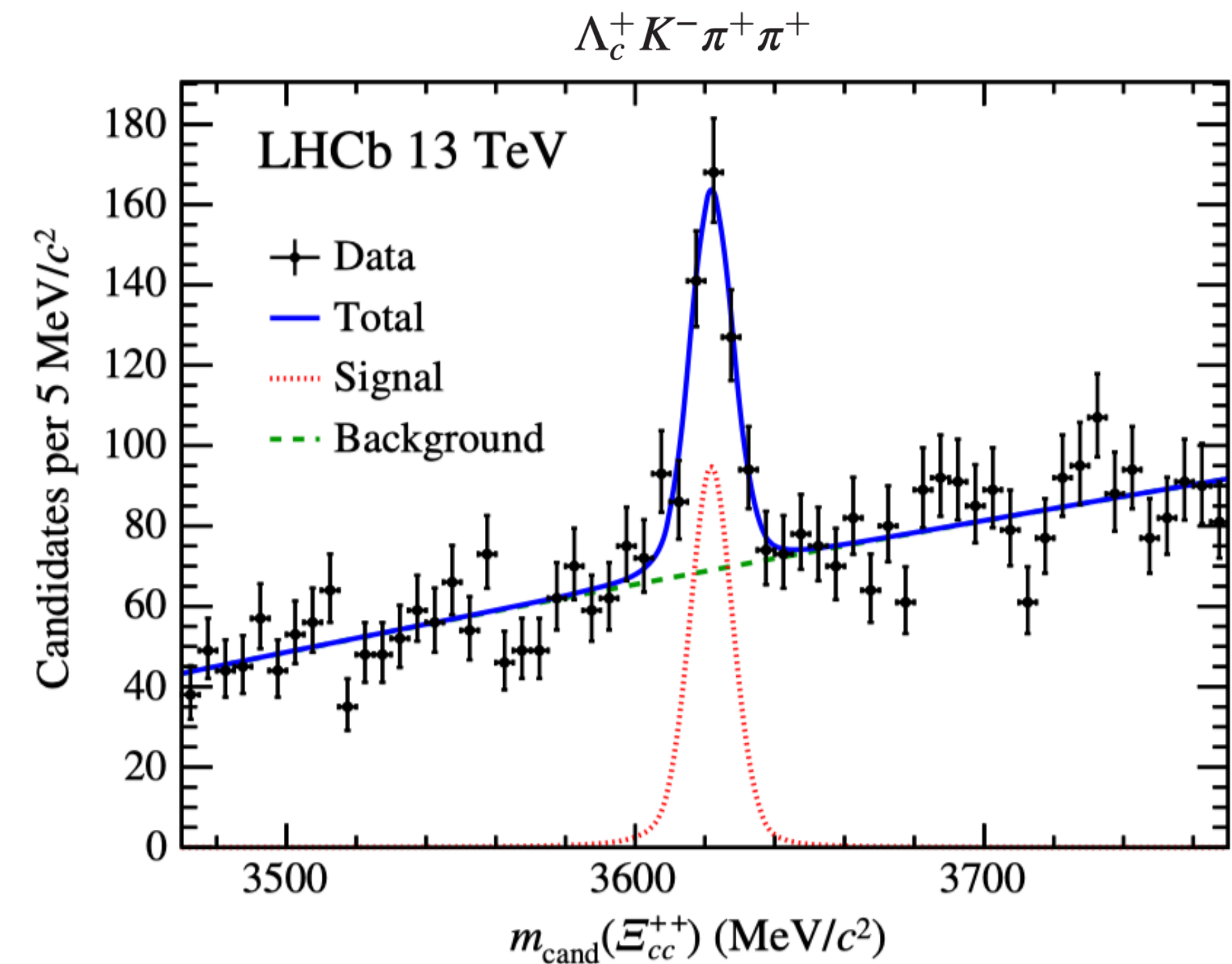
$$m_{\Xi_{cc}^{++}} = 3621.40 \pm 0.72(\text{stat.}) \pm 0.27(\text{syst.}) \pm 0.14(\Lambda_c^+) \text{ MeV}/c^2$$

Observations in other decay channels

- $\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$ R. Aaij and others, Phys. Rev. Lett. **121**, 162002 (2018).
- $\Xi_{cc}^{++} \rightarrow \Xi_c'^+ \pi^+$ R. Aaij and others, JHEP **05**, 038 (2022).
- $\Xi_{cc}^{++} \rightarrow \Xi_c^0 \pi^+ \pi^+$ R. Aaij and others, arXiv:2504.05063 [hep-ex] (2025).

More precise measurements

- Mass: R. Aaij and others, JHEP 02, 049 (2020)
- Lifetime: R. Aaij and others, Phys. Rev. Lett. **121**, 052002 (2018).
- Production cross section: R. Aaij and others, Chin. Phys. C **44**, 022001 (2020).



R. Aaij and others, Phys. Rev. Lett. 119, 112001 (2017)

Recent searches for Ξ_{cc}^+ and Ω_{cc}^+ at LHCb

- R. Aaij and others, JHEP **12**, 107 (2021).
- R. Aaij and others, Sci. China Phys. Mech. Astron. **64**, 101062 (2021).

Doubly charmed baryons

Lattice QCD calculations

Mass

- L. Liu, H.-W. Lin, K. Orginos, and A. Walker-Loud, Phys. Rev. D **81**, 094505 (2010).
- Z. S. Brown, W. Detmold, S. Meinel, and K. Orginos, Phys. Rev. D **90**, 094507 (2014).
- C. Alexandrou and C. Kallidonis, Phys. Rev. D **96**, 034511 (2017).
- S. Mondal, M. Padmanath, and N. Mathur, EPJ Web Conf. **175**, 05021 (2018).
- K. U. Can, H. Bahtiyar, G. Erkol, P. Gubler, M. Oka, and T. T. Takahashi, JPS Conf. Proc. **26**, 022028 (2019).
- N. Mathur and M. Padmanath, Phys. Rev. D **99**, 031501 (2019).
- M. Padmanath, Heavy Baryon Spectroscopy from Lattice QCD (2019).
- H. Bahtiyar, K. U. Can, G. Erkol, P. Gubler, M. Oka, and T. T. Takahashi, Phys. Rev. D **102**, 054513 (2020).
- C. Alexandrou, S. Bacchio, G. Christou, and J. Finkenrath, Phys. Rev. D **108**, 094510 (2023).

Other properties (electromagnetic form factors, radiative transitions, ...)

- K. U. Can, G. Erkol, B. Isildak, M. Oka, and T. T. Takahashi, Phys. Lett. B **726**, 703 (2013).
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- K. U. Can, Int. J. Mod. Phys. A **36**, 2130013 (2021).
- H. Bahtiyar, Phys. Rev. D **108**, 034504 (2023).
- H. Bahtiyar, K. U. Can, G. Erkol, M. Oka, and T. T. Takahashi, Phys. Rev. D **98**, 114505 (2018).
- G. Aarts, C. Allton, M. N. Anwar, R. Bignell, T. J. Burns, B. Jäger, and J.-I. Skullerud, Eur. Phys. J. A **60**, 59 (2024).

Doubly charmed baryons

Chiral perturbation theory

- Z.-H. Guo, Phys. Rev. D 96, 074004 (2017).
- Z.-F. Sun and M. J. Vicente Vacas, Phys. Rev. D 93, 094002 (2016).
- A. N. Hiller Blin, Z.-F. Sun, and M. J. Vicente Vacas, Phys. Rev. D 98, 054025 (2018).
- M.-J. Yan, X.-H. Liu, S. González-Solís, F.-K. Guo, C. Hanhart, U.-G. Meißner, and B.-S. Zou, Phys. Rev. D 98, 091502 (2018).
- M.-Z. Liu, Y. Xiao, and L.-S. Geng, Phys. Rev. D 98, 014040 (2018).
- D.-L. Yao, Phys. Rev. D 97, 034012 (2018).
- L. Meng and S.-L. Zhu, Phys. Rev. D 100, 014006 (2019).

Heavy diquark-antiquark (HDA) symmetry

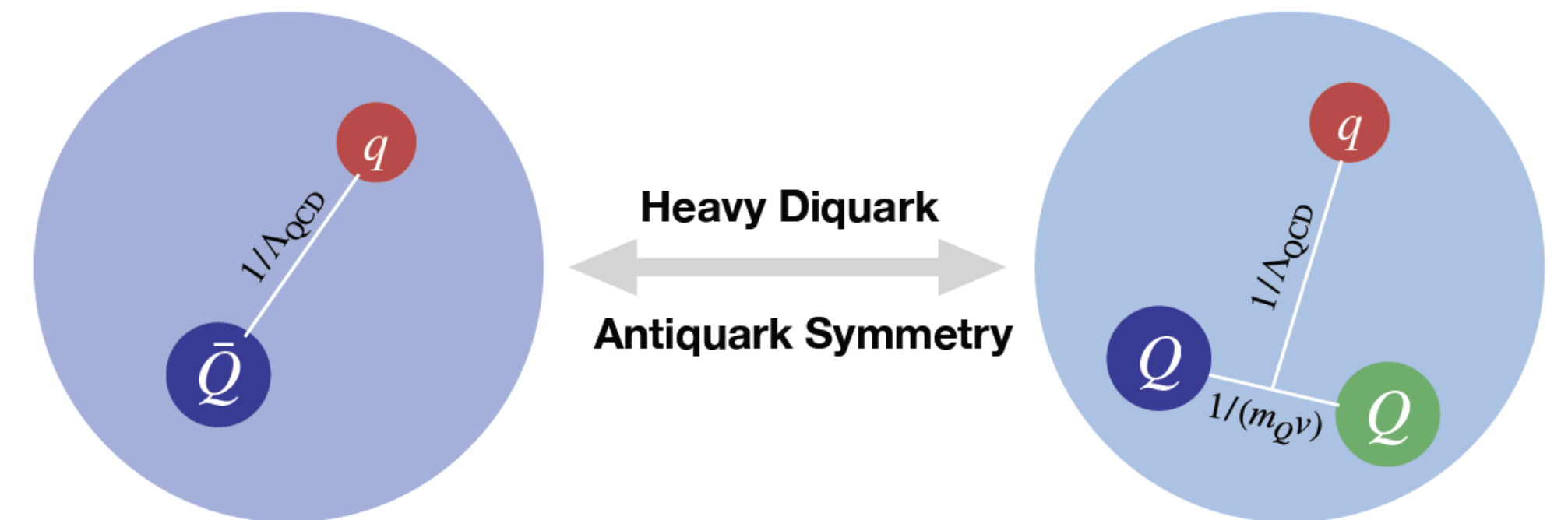
- M. J. Savage and M. B. Wise, Phys. Lett. B 248, 177 (1990).
- M.-J. Yan, X.-H. Liu, S. González-Solís, F.-K. Guo, C. Hanhart, U.-G. Meißner, and B.-S. Zou, Phys. Rev. D 98, 091502 (2018).
- L. Meng and S.-L. Zhu, Phys. Rev. D 100, 014006 (2019).
- Z.-R. Liang, P.-C. Qiu, and D.-L. Yao, JHEP 07, 124 (2023).
-

Baryon chiral perturbation theory (BChPT)

$$\mathcal{L}_{\psi\phi}^{(1)} = \bar{\psi} (i\not{D} - m) \psi + \frac{g}{2} \bar{\psi} \not{\psi} \gamma_5 \psi ,$$

$$\begin{aligned} \mathcal{L}_{\psi\phi}^{(2)} = & b_1 \bar{\psi} \langle \chi_+ \rangle \psi + b_2 \bar{\psi} \tilde{\chi}_+ \psi + b_3 \bar{\psi} u^2 \psi + b_4 \bar{\psi} \langle u^2 \rangle \psi + \frac{b_5}{m^2} \bar{\psi} (\{u^\mu, u^\nu\} D_{\mu\nu} + H.c.) \psi \\ & + \frac{b_6}{m^2} \bar{\psi} (\langle u^\mu u^\nu \rangle D_{\mu\nu} + H.c.) \psi + i b_7 \bar{\psi} [u^\mu, u^\nu] \sigma_{\mu\nu} \psi , \end{aligned}$$

$$\begin{aligned} \mathcal{L}_{\psi\phi}^{(3)} = & i c_{11} \bar{\psi} [u_\mu, h^{\mu\nu}] \gamma_\nu \psi + \frac{c_{12}}{m^2} \bar{\psi} (i [u^\mu, h^{\nu\rho}] \gamma_\mu D_{\nu\rho} + H.c.) \psi + \frac{c_{13}}{m} \bar{\psi} (i \{u^\mu, h^{\nu\rho}\} \\ & \times \sigma_{\mu\nu} D_\rho + H.c.) \psi + \frac{c_{14}}{m} \bar{\psi} (i \sigma_{\mu\nu} \langle u^\mu h^{\nu\rho} \rangle D_\rho + H.c.) \psi + c_{15} \bar{\psi} \{u^\mu, \tilde{\chi}_+\} \gamma_5 \gamma_\mu \psi \\ & + c_{16} \bar{\psi} u^\mu \gamma_5 \gamma_\mu \langle \chi_+ \rangle \psi + c_{17} \bar{\psi} \gamma_5 \gamma_\mu \langle u^\mu \tilde{\chi}_+ \rangle \psi + i c_{18} \bar{\psi} \gamma_5 \gamma_\mu [D^\mu, \tilde{\chi}_-] \psi \\ & + i c_{19} \bar{\psi} \gamma_5 \gamma_\mu \langle [D^\mu, \chi_-] \rangle \psi + c_{20} \bar{\psi} [\tilde{\chi}_-, u^\mu] \gamma_\mu \psi . \end{aligned}$$



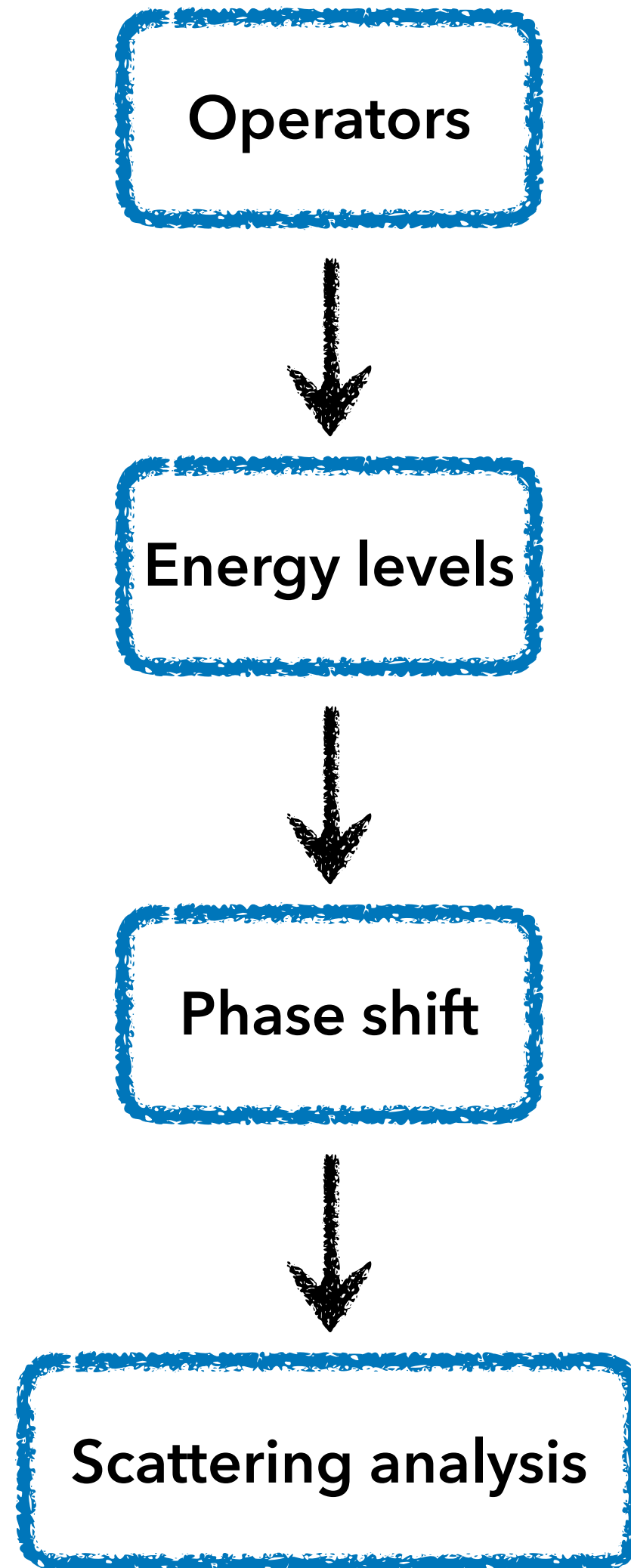
Doubly charmed baryons

(S, I)	Processes	Connected(C)/ Disconnected(D)	(S, I)	Relation to $D\phi$ scattering
$(-2, \frac{1}{2})$	$\Omega_{cc}\bar{K} \rightarrow \Omega_{cc}\bar{K}$	C	$(2, \frac{1}{2})$	$D_s K \rightarrow D_s K$
$(-1, 1)$	$\Omega_{cc}\pi \rightarrow \Omega_{cc}\pi$	C	$(1, 1)$	$D_s\pi \rightarrow D_s\pi$
	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$ $\Omega_{cc}\pi \rightarrow \Xi_{cc}\bar{K}$			$DK \rightarrow DK$ $D_s\pi \rightarrow DK$
$(-1, 0)$	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$	D	$(1, 0)$	$DK \rightarrow DK$
	$\Omega_{cc}\eta \rightarrow \Omega_{cc}\eta$ $\Xi_{cc}\bar{K} \rightarrow \Omega_{cc}\eta$			$D_s\eta \rightarrow D_s\eta$ 2317 $DK \rightarrow D_s\eta$
$(1, 0)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 0)$	$D\bar{K} \rightarrow D\bar{K}$
$(1, 1)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 1)$	$D\bar{K} \rightarrow D\bar{K}$
$(0, \frac{1}{2})$	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$	D	$(0, \frac{1}{2})$	$D\pi \rightarrow D\pi$
	$\Xi_{cc}\eta \rightarrow \Xi_{cc}\eta$			$D\eta \rightarrow D\eta$
	$\Omega_{cc}K \rightarrow \Omega_{cc}K$			$D_s\bar{K} \rightarrow D_s\bar{K}$
	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\eta$ $\Xi_{cc}\pi \rightarrow \Omega_{cc}K$ $\Xi_{cc}\eta \rightarrow \Omega_{cc}K$			$D\pi \rightarrow D\eta$ $D\pi \rightarrow D_s\bar{K}$ $D\eta \rightarrow D_s\bar{K}$
$(0, \frac{3}{2})$	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$	C	$(0, \frac{3}{2})$	$D\pi \rightarrow D\pi$

Doubly charmed baryons

(S, I)	Processes	Connected(C)/ Disconnected(D)	(S, I)	Relation to $D\phi$ scattering
$(-2, \frac{1}{2})$	$\Omega_{cc}\bar{K} \rightarrow \Omega_{cc}\bar{K}$	C	$(2, \frac{1}{2})$	$D_s K \rightarrow D_s K$
	$\Omega_{cc}\pi \rightarrow \Omega_{cc}\pi$			$D_s \pi \rightarrow D_s \pi$
$(-1, 1)$	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$	C	$(1, 1)$	$DK \rightarrow DK$
	$\Omega_{cc}\pi \rightarrow \Xi_{cc}\bar{K}$			$D_s \pi \rightarrow DK$
	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$			$DK \rightarrow DK$
$(-1, 0)$	$\Omega_{cc}\eta \rightarrow \Omega_{cc}\eta$	D	$(1, 0)$	$D_s \eta \rightarrow D_s \eta$ 2317
	$\Xi_{cc}\bar{K} \rightarrow \Omega_{cc}\eta$			$DK \rightarrow D_s \eta$
$(1, 0)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 0)$	$D\bar{K} \rightarrow D\bar{K}$
$(1, 1)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 1)$	$D\bar{K} \rightarrow D\bar{K}$
	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$			$D\pi \rightarrow D\pi$
	$\Xi_{cc}\eta \rightarrow \Xi_{cc}\eta$			$D\eta \rightarrow D\eta$
$(0, \frac{1}{2})$	$\Omega_{cc}K \rightarrow \Omega_{cc}K$	D	$(0, \frac{1}{2})$	$D_s \bar{K} \rightarrow D_s \bar{K}$ Two-pole
	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\eta$			$D\pi \rightarrow D\eta$
	$\Xi_{cc}\pi \rightarrow \Omega_{cc}K$			$D\pi \rightarrow D_s \bar{K}$
	$\Xi_{cc}\eta \rightarrow \Omega_{cc}K$			$D\eta \rightarrow D_s \bar{K}$
$(0, \frac{3}{2})$	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$	C	$(0, \frac{3}{2})$	$D\pi \rightarrow D\pi$

Simulation in lattice QCD



Two-particle operators for **S-wave** scattering $J^P = (1/2)^- \longrightarrow G_1^-$

Spectrum of two-particle system

Solve generalized eigenvalue problem (**GEVP**) and extract energy levels

$$C_{ij}(t) = \sum_{t_{src}} \langle \mathcal{O}_i(t + t_{src}) \mathcal{O}_j^\dagger(t_{src}) \rangle \quad C(t)v^n(t) = \lambda^n(t)C(t_0)v^n(t)$$

M. Luscher and U. Wolff, Nucl. Phys. B 339, 222 (1990).

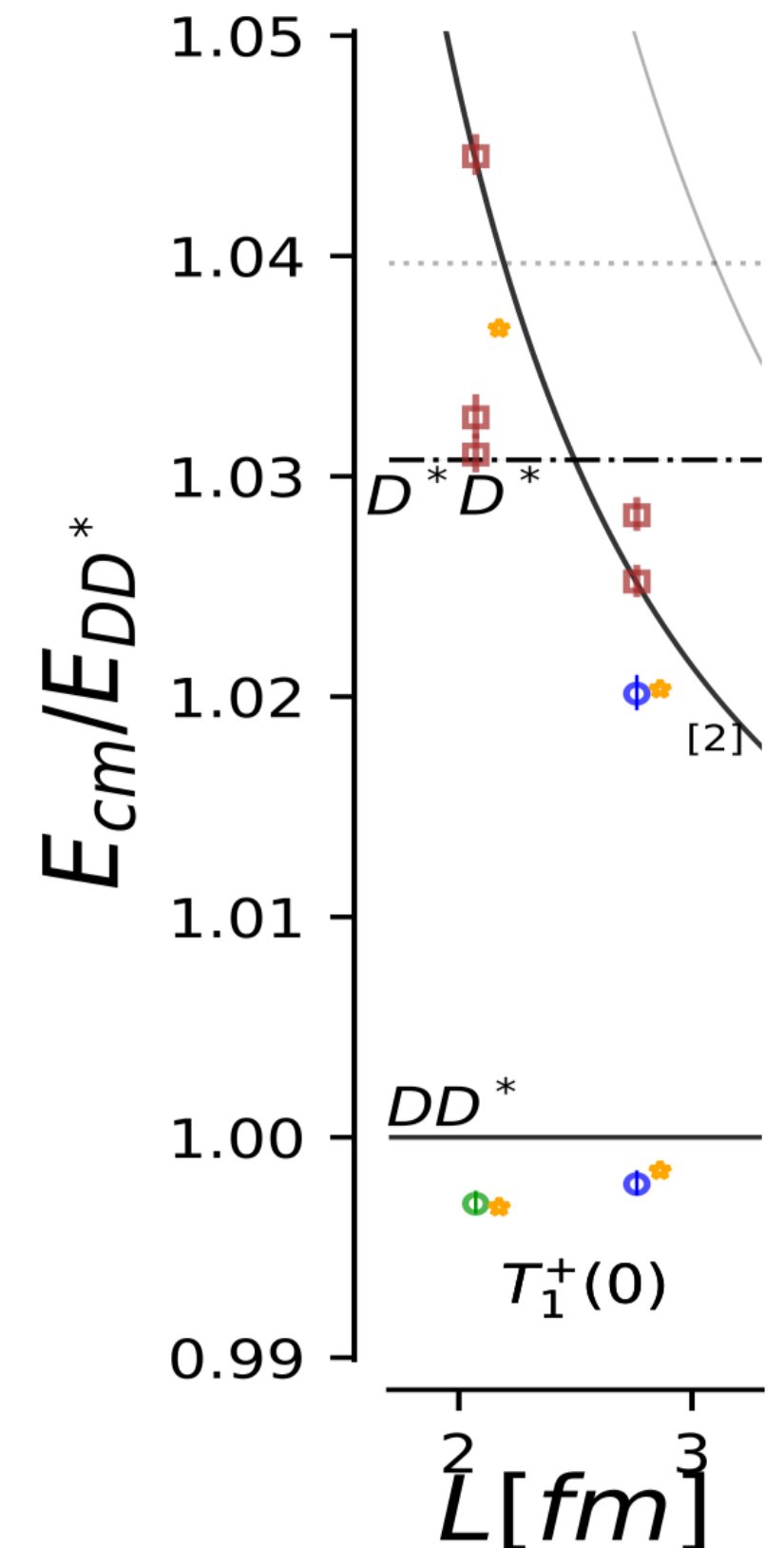
Luscher's formula for two-body scattering M. Luscher, Nucl. Phys. B 354, 531 (1991).

$$\det[1 + i\rho \cdot \mathbf{t} \cdot (1 + i\mathbf{M})] = 0$$

For single-channel S-wave scattering

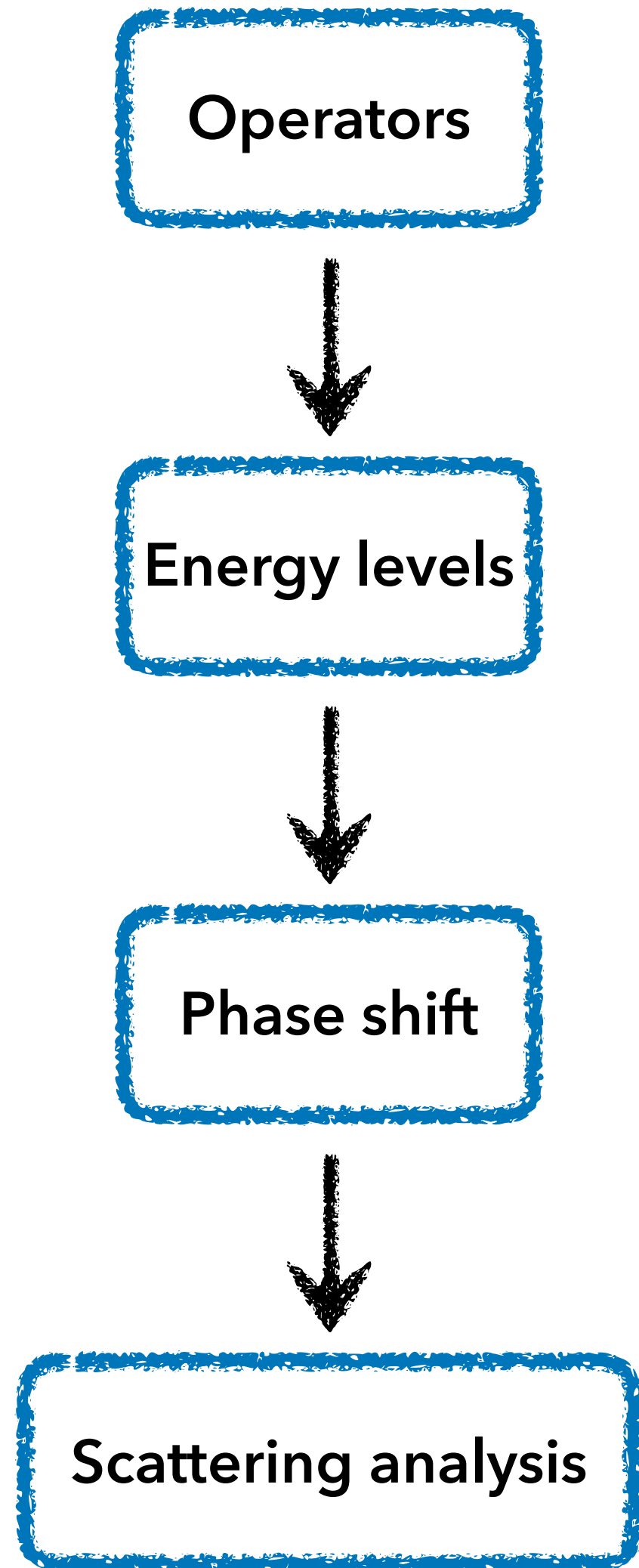
$$p \cot \delta_0(p) = \frac{2}{L\sqrt{\pi}} \mathcal{Z}_{00}(1; q^2)$$

$$E = \sqrt{m_1^2 + p^2} + \sqrt{m_2^2 + p^2} \quad q = \frac{pL}{2\pi}$$



M. Padmanath and S. Prelovsek, Phys. Rev. Lett. 129, 032002 (2022).

Simulation in lattice QCD



Effective range expansion

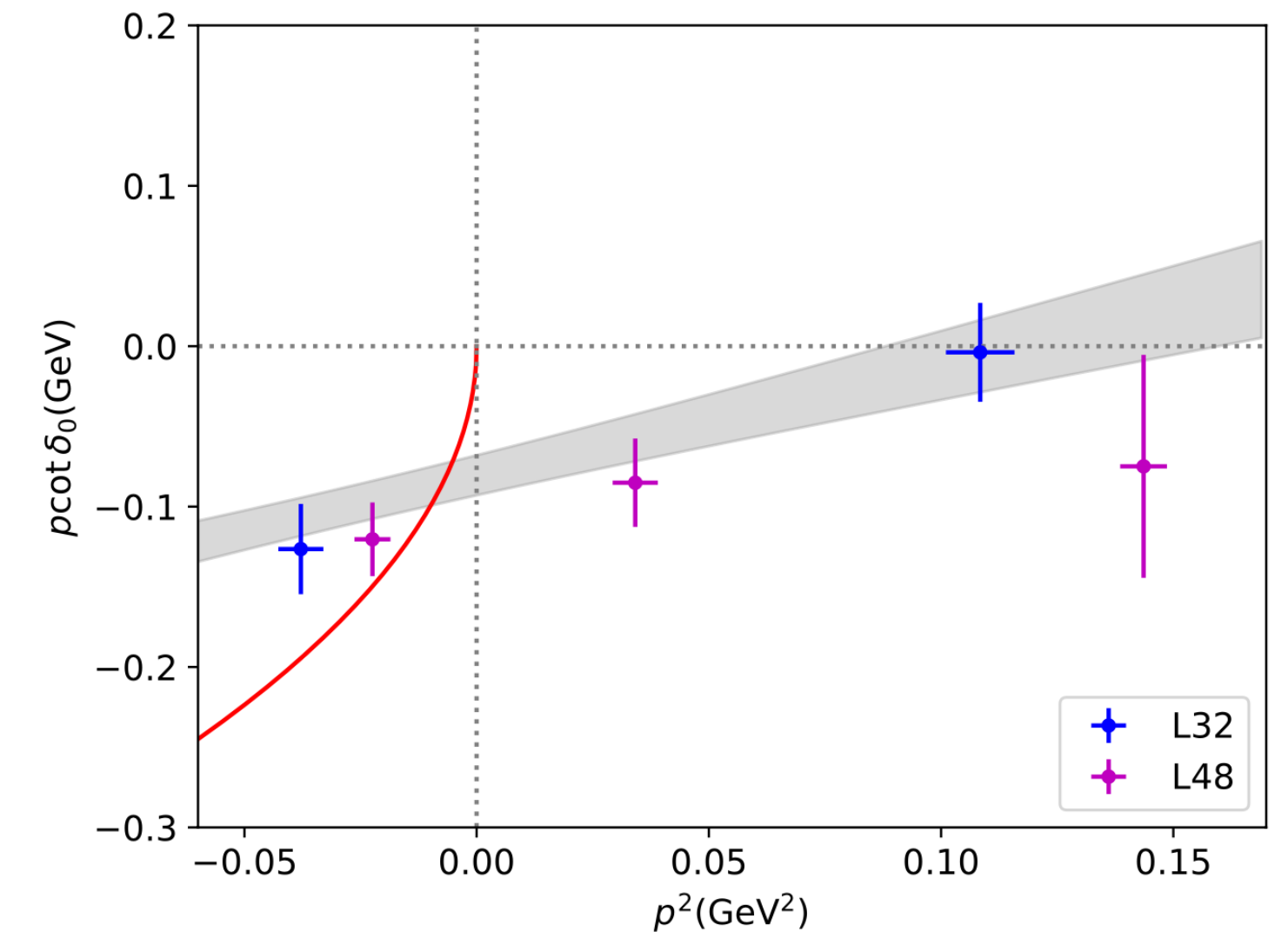
$$p \cot \delta_0 = \frac{1}{a_0} + \frac{1}{2} r_0 p^2 + \mathcal{O}(p^4)$$

Scattering amplitude

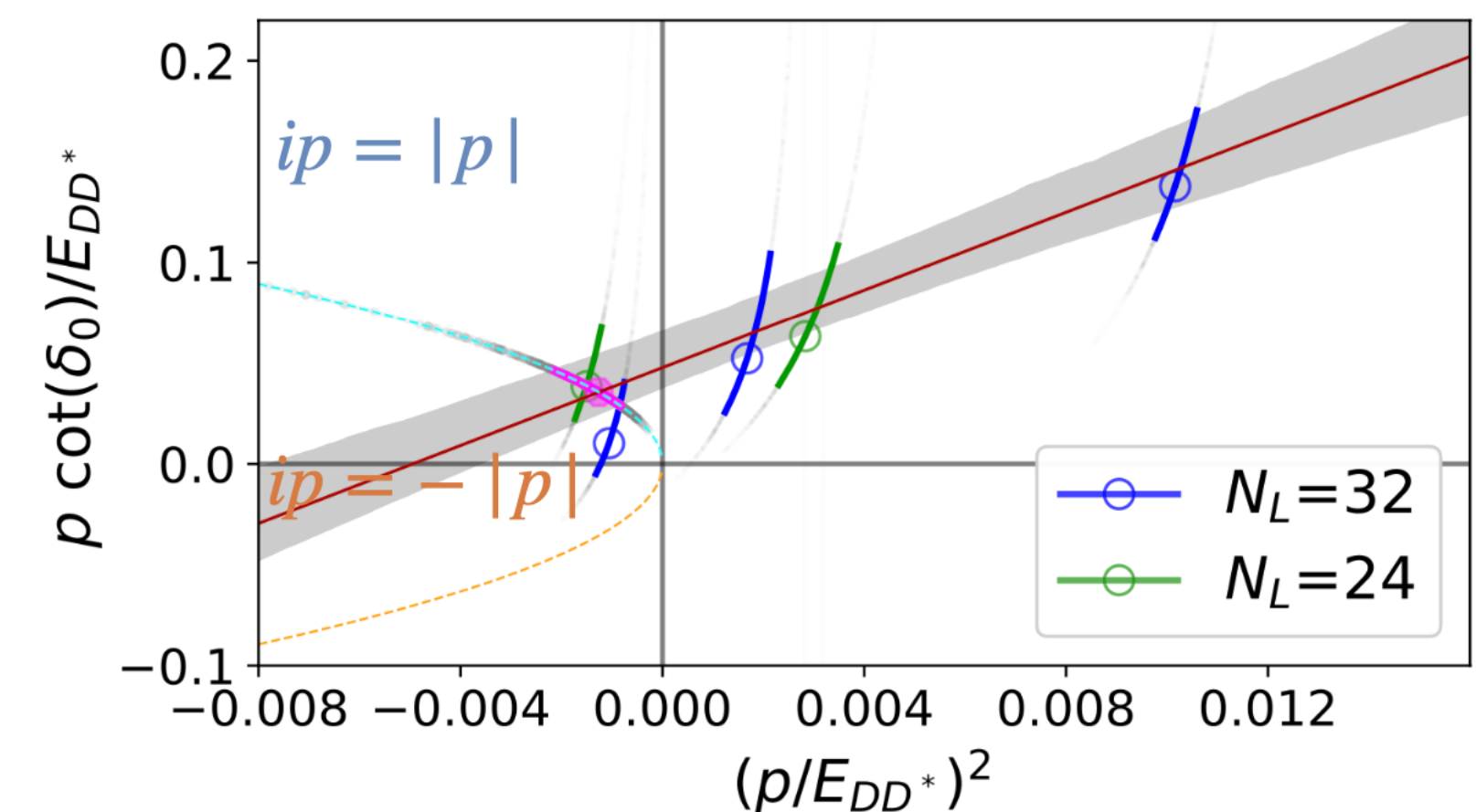
$$t_l^{(J)} \sim \frac{1}{p \cot \delta_l^{(J)} - ip}$$

For partial wave l and total angular momentum J

- L. Liu, K. Orginos, F.-K. Guo, C. Hanhart, and U.-G. Meissner, Phys. Rev. D 87, 014508 (2013).
- Y. Lyu, S. Aoki, T. Doi, T. Hatsuda, Y. Ikeda, and J. Meng, arXiv:2302.04505 [hep-lat] (2023).
- H. Xing, J. Liang, L. Liu, P. Sun, and Y.-B. Yang, arXiv:2210.08555 [hep-lat] (2022).
- M. Padmanath and S. Prelovsek, Phys. Rev. Lett. 129, 032002 (2022).
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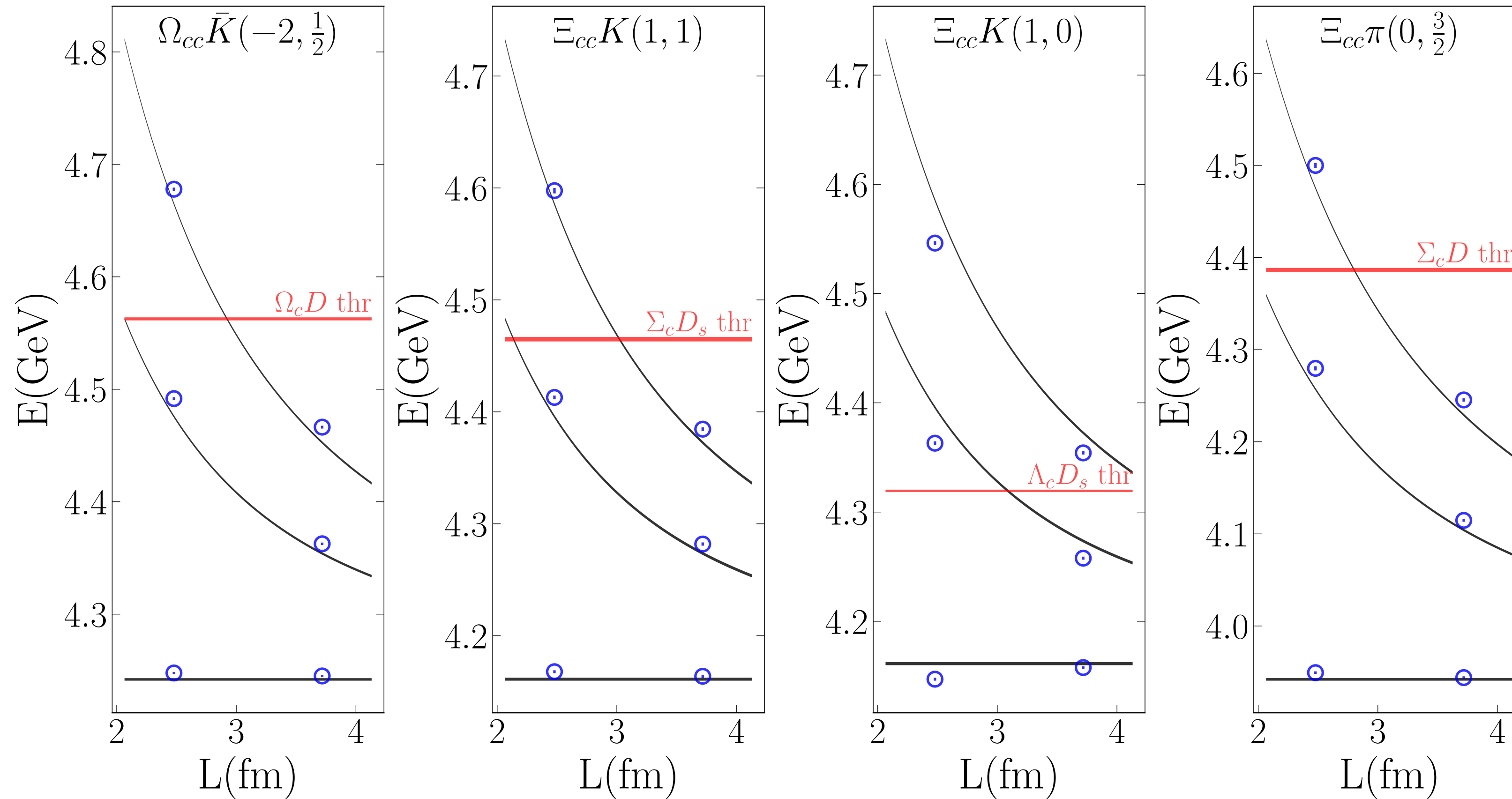


H. Xing, J. Liang, L. Liu, P. Sun, and Y.-B. Yang, arXiv:2210.08555 [hep-lat] (2022).



M. Padmanath and S. Prelovsek, Phys. Rev. Lett. 129, 032002 (2022).

Single-channel results



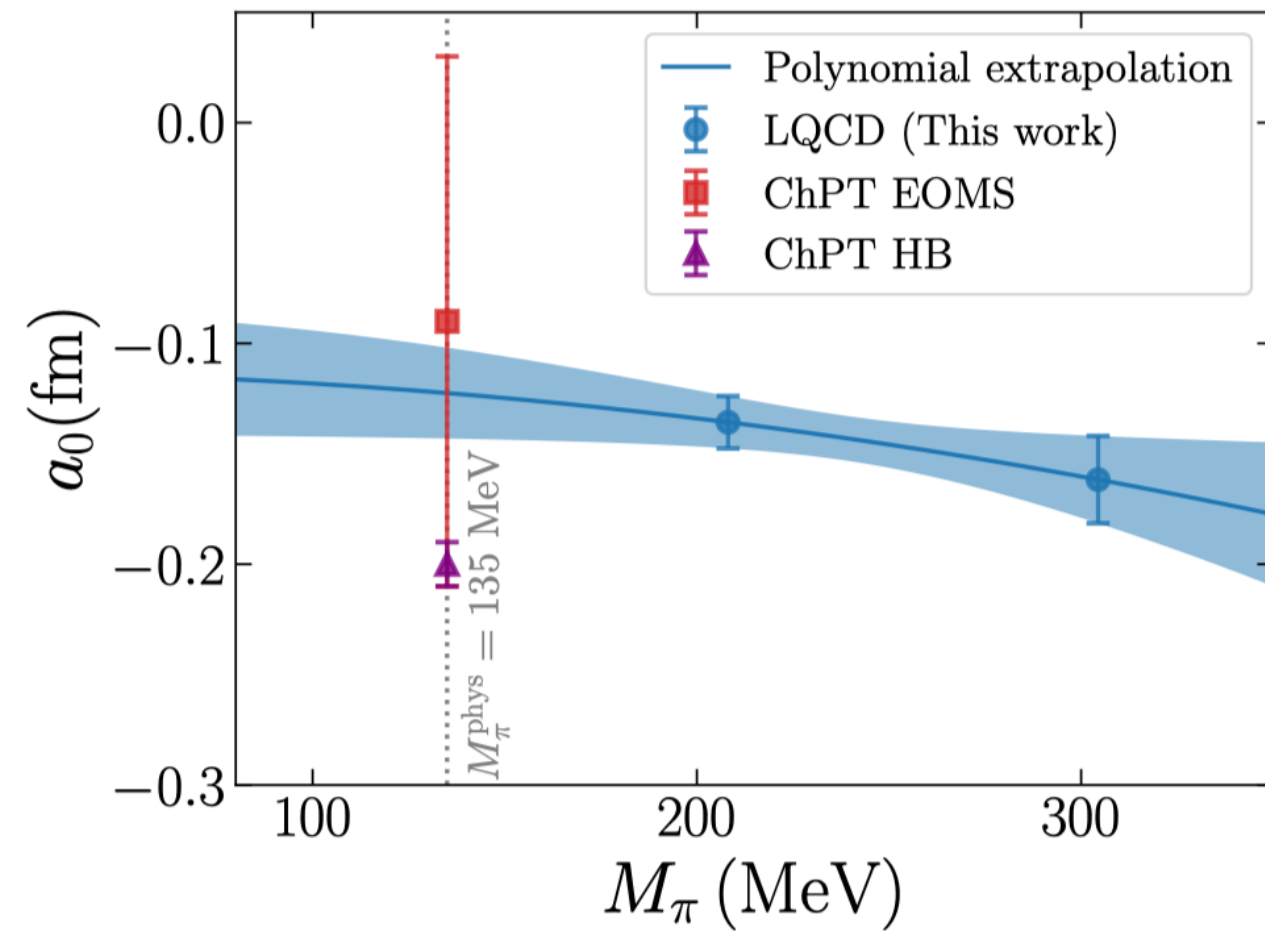
J.-Y. Yi, Z.-R. Liang, L. Liu & DLY, JHEP03(2026)

Results for four single channels

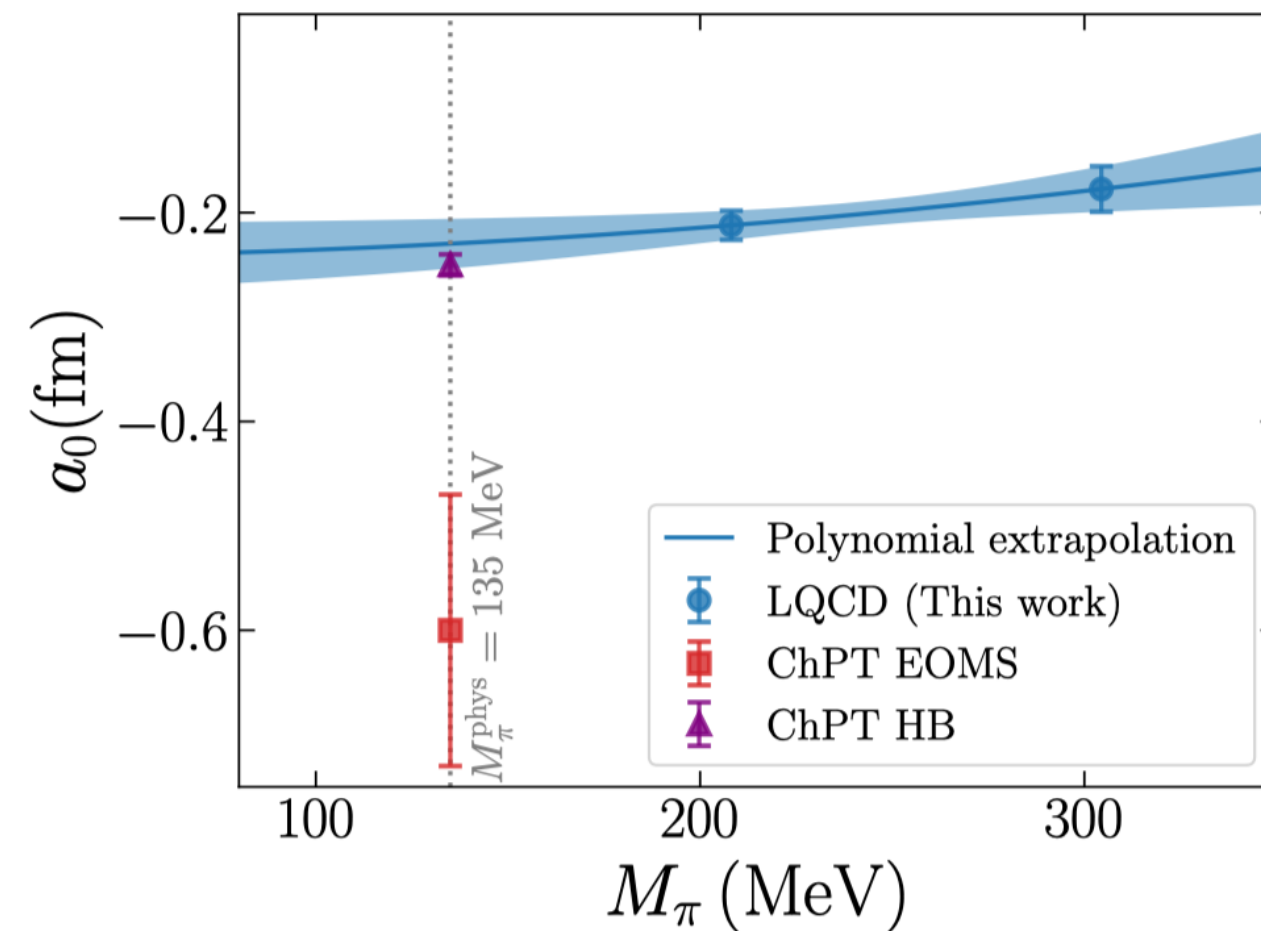
- Pion mass ~ 300 and 210 MeV.
- Lattice spacing $a = 0.07746$.
- A possible virtual state in $(S, I) = (1, 0)$ channel.

Single-channel results

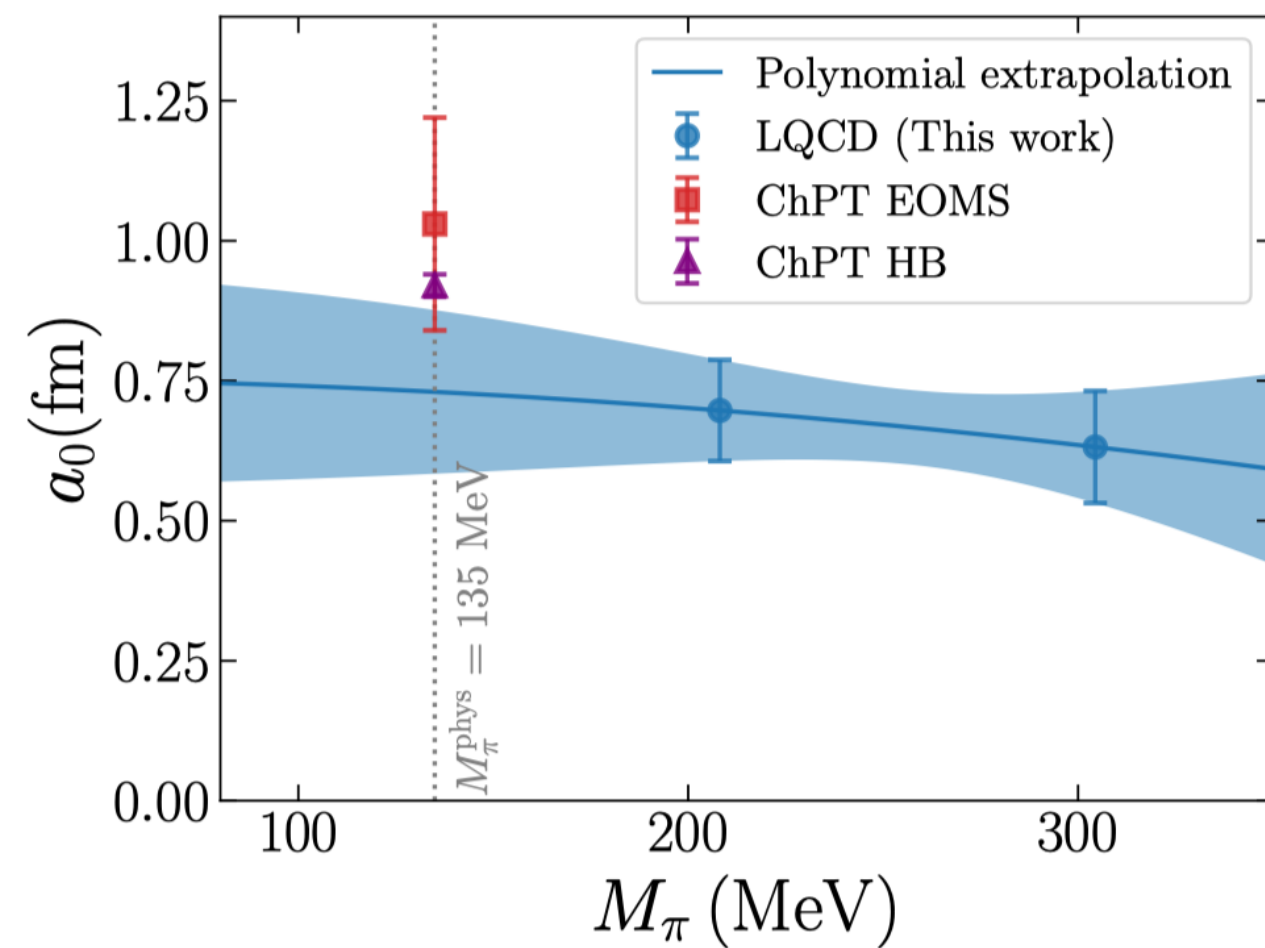
Extrapolation of S-wave scattering length a_0 to the physical pion mass



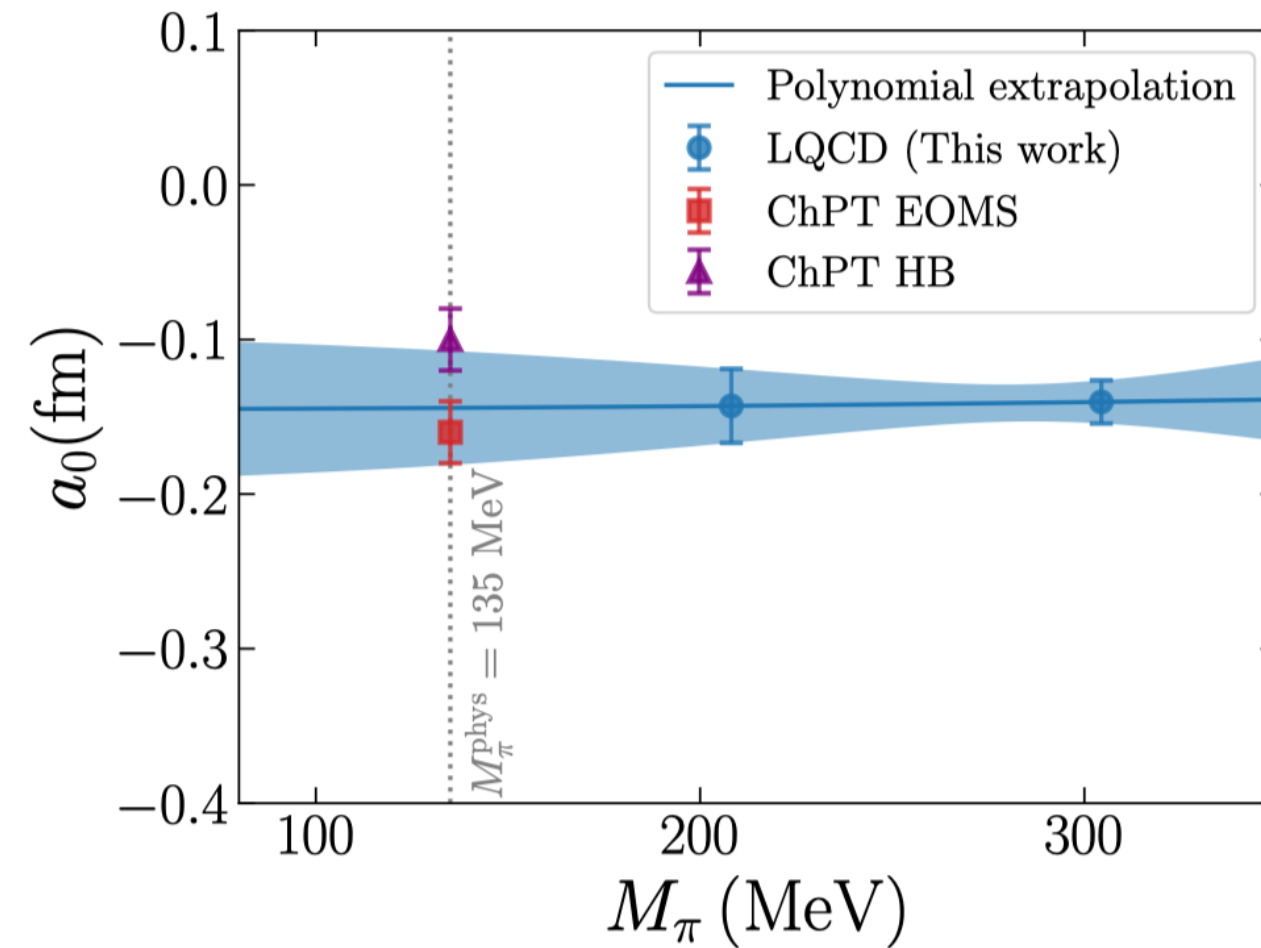
(a) $\Omega_{cc}\bar{K}(-2, \frac{1}{2})$



(b) $\Xi_{cc}K(1, 1)$



(c) $\Xi_{cc}K(1, 0)$



(d) $\Xi_{cc}\pi(0, \frac{3}{2})$

(S, I)	Processes	Connected(C)/ Disconnected(D)	(S, I)	Relation to $D\phi$ scattering
✓ $(-2, \frac{1}{2})$	$\Omega_{cc}\bar{K} \rightarrow \Omega_{cc}\bar{K}$	C	$(2, \frac{1}{2})$	$D_s K \rightarrow D_s K$
	$\Omega_{cc}\pi \rightarrow \Omega_{cc}\pi$			$D_s \pi \rightarrow D_s \pi$
$(-1, 1)$	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$	C	$(1, 1)$	$DK \rightarrow DK$
	$\Omega_{cc}\pi \rightarrow \Xi_{cc}\bar{K}$			$D_s \pi \rightarrow DK$
$(-1, 0)$	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$			$DK \rightarrow DK$
	$\Omega_{cc}\eta \rightarrow \Omega_{cc}\eta$	D	$(1, 0)$	$D_s \eta \rightarrow D_s \eta$
	$\Xi_{cc}\bar{K} \rightarrow \Omega_{cc}\eta$			$DK \rightarrow D_s \eta$
✓ $(1, 0)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 0)$	$D\bar{K} \rightarrow D\bar{K}$
✓ $(1, 1)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 1)$	$D\bar{K} \rightarrow D\bar{K}$
	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$			$D\pi \rightarrow D\pi$
	$\Xi_{cc}\eta \rightarrow \Xi_{cc}\eta$			$D\eta \rightarrow D\eta$
$(0, \frac{1}{2})$	$\Omega_{cc}K \rightarrow \Omega_{cc}K$	D	$(0, \frac{1}{2})$	$D_s \bar{K} \rightarrow D_s \bar{K}$
	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\eta$			$D\pi \rightarrow D\eta$
	$\Xi_{cc}\pi \rightarrow \Omega_{cc}K$			$D\pi \rightarrow D_s \bar{K}$
	$\Xi_{cc}\eta \rightarrow \Omega_{cc}K$			$D\eta \rightarrow D_s \bar{K}$
✓ $(0, \frac{3}{2})$	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$	C	$(0, \frac{3}{2})$	$D\pi \rightarrow D\pi$

Lattice setup & operators

Lattice setup Gauge configurations from CLQCD

	C48P14	F32P30	F48P30	F32P21	F48P21	H48P32
β	6.20		6.41			6.72
$a(\text{fm})$	0.10530(18)		0.07746(18)			0.05187(26)
am_l	-0.2825	-0.2295	-0.2295	-0.2320	-0.2320	-0.1850
am_s	-0.2310	-0.2050	-0.2050	-0.2050	-0.2050	-0.1700
$M_\pi(\text{MeV})$	135.5(1.6)	303.9(0.6)	304.9(0.4)	208.1(1.9)	207.4(0.7)	317.2(0.9)
$M_\pi L$	3.471(41)	3.8180(75)	5.7458(75)	2.614(24)	3.908(13)	4.003(11)
$L^3 \times T$	$48^3 \times 96$	$32^3 \times 96$	$48^3 \times 96$	$32^3 \times 64$	$48^3 \times 96$	$48^3 \times 144$
$N_{\text{cfgs.}}$	-	750	359	459	222	-

Operators

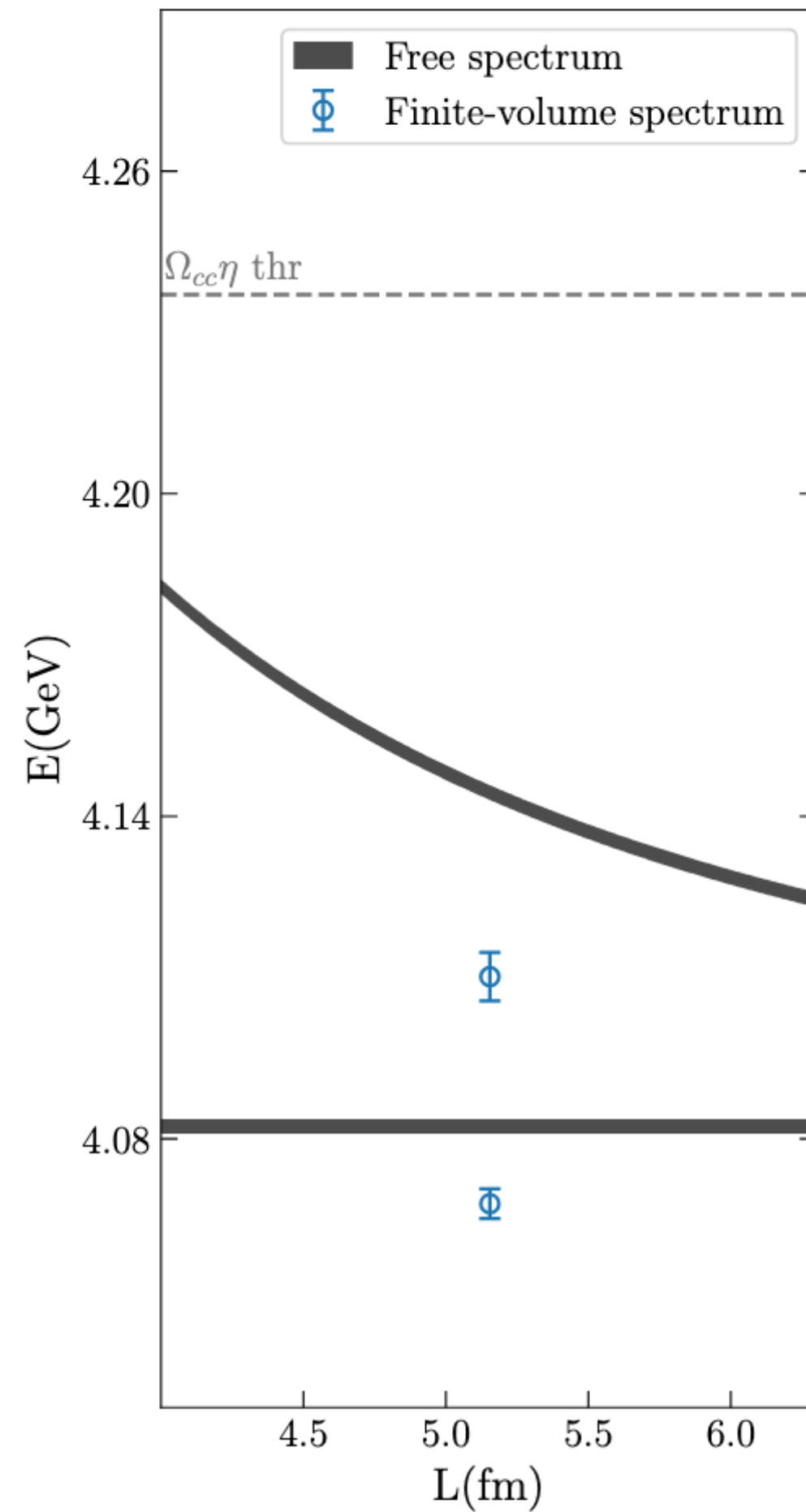
$$\mathcal{O}_p^{\Xi_{cc}\bar{K}} = \frac{1}{\sqrt{2}} \sum_{\alpha, \mathbf{p}_1, \mathbf{p}_2} C_{\alpha, \mathbf{p}_1, \mathbf{p}_2} \left(\mathcal{O}_{\Xi_{cc}^{++}, \alpha}(\mathbf{p}_1) \mathcal{O}_{K^-}(\mathbf{p}_2) - \mathcal{O}_{\Xi_{cc}^+, \alpha}(\mathbf{p}_1) \mathcal{O}_{\bar{K}^0}(\mathbf{p}_2) \right)$$

$$\mathcal{O}_{ccs}(x) = \epsilon^{ijk} P_- [c^{iT}(x) C \gamma_5 s^j(x)] c^k(x)$$

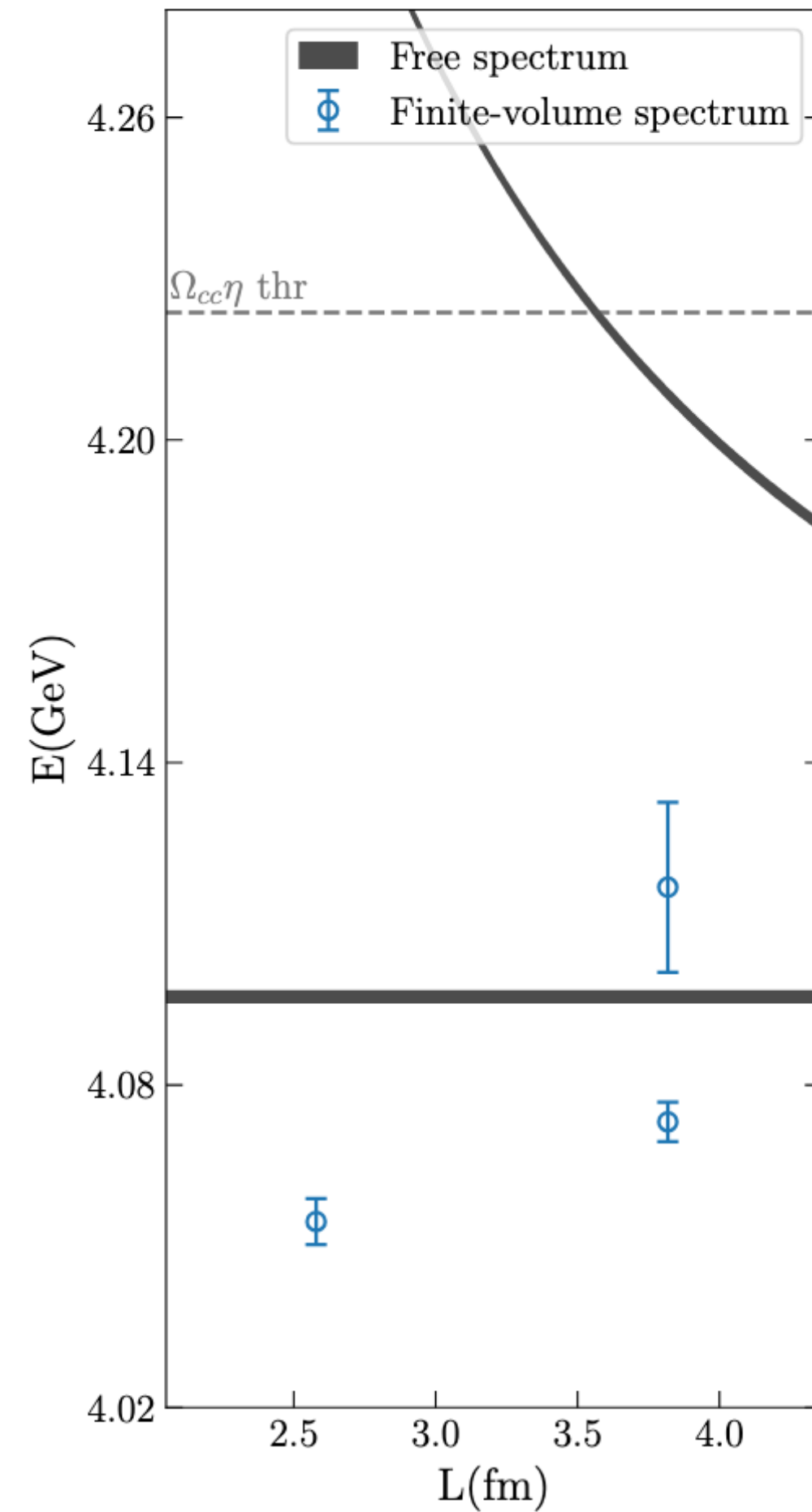
- **Four pion masses** (~140-320 MeV).
- **Three lattice spacings** (~ 0.05-0.11 fm).
- Six ensembles of gauge configurations with **2+1** dynamical quark flavors.
- tree-level Symanzik-improved gauge action.
- Shekholeslami-Wohlert fermion action with tree-level tadpole improvement.
- **Distillation** quark smearing.
- Charm quark mass determined by physical J/ψ .

Preliminary results for $\Xi_{cc}\bar{K}$ ($I = 0$)

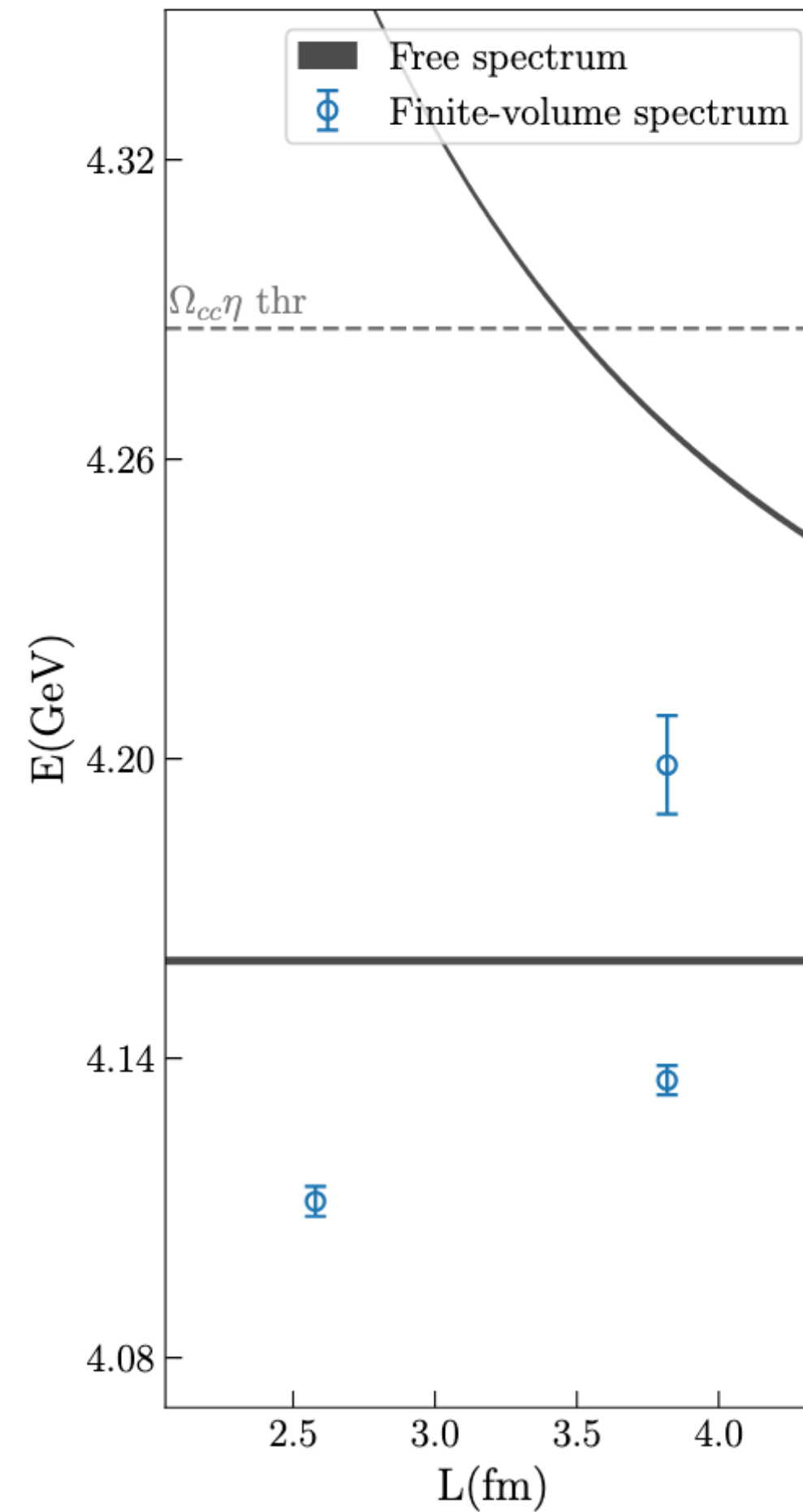
Energy levels



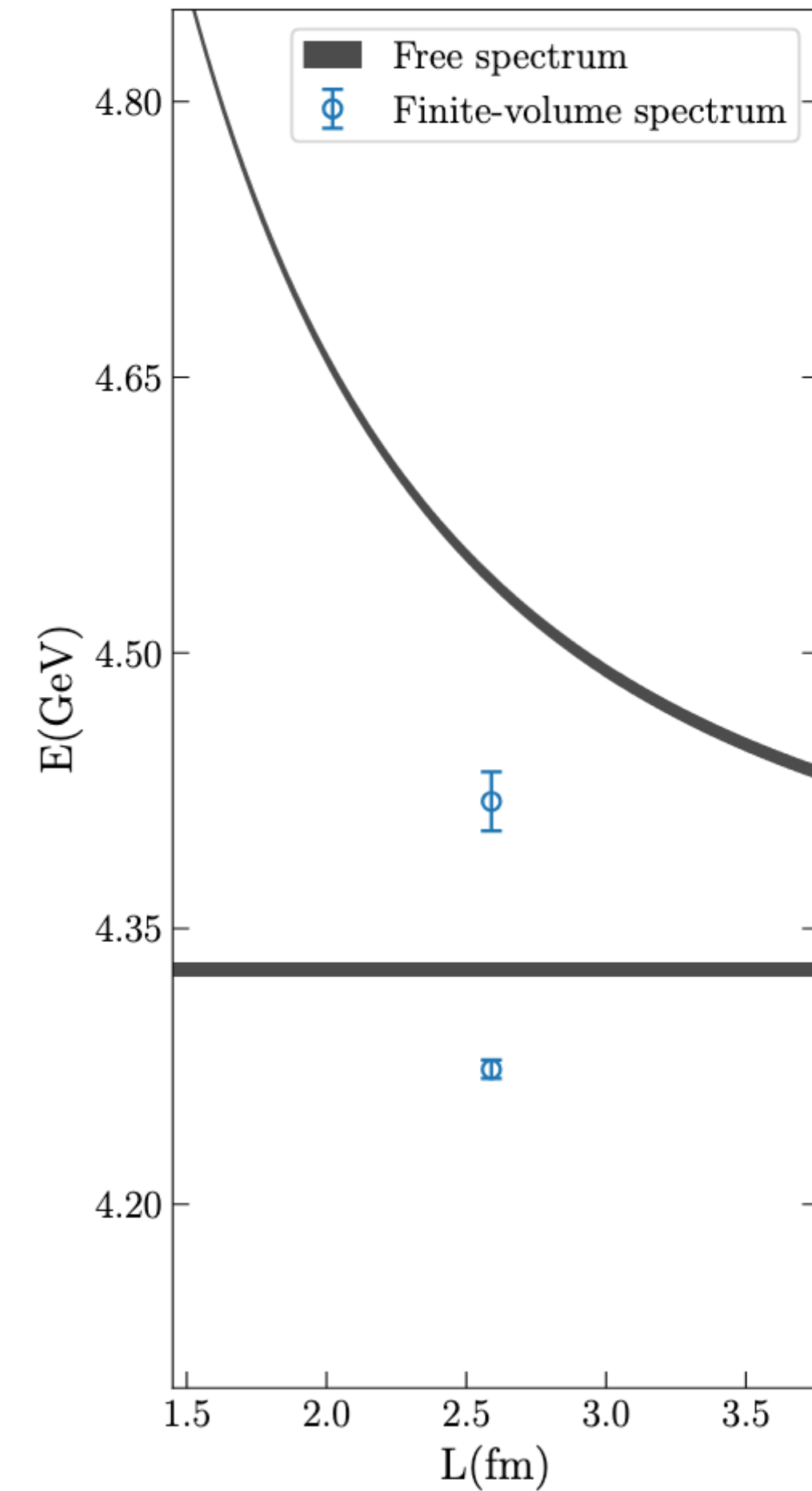
(a) $M_\pi \approx 140$ MeV,
 $a = 0.10530$ fm ($L = 48$)



(b) $M_\pi \approx 210$ MeV,
 $a = 0.07746$ fm ($L = 32, 48$)



(c) $M_\pi \approx 300$ MeV,
 $a = 0.07746$ fm ($L = 32, 48$)



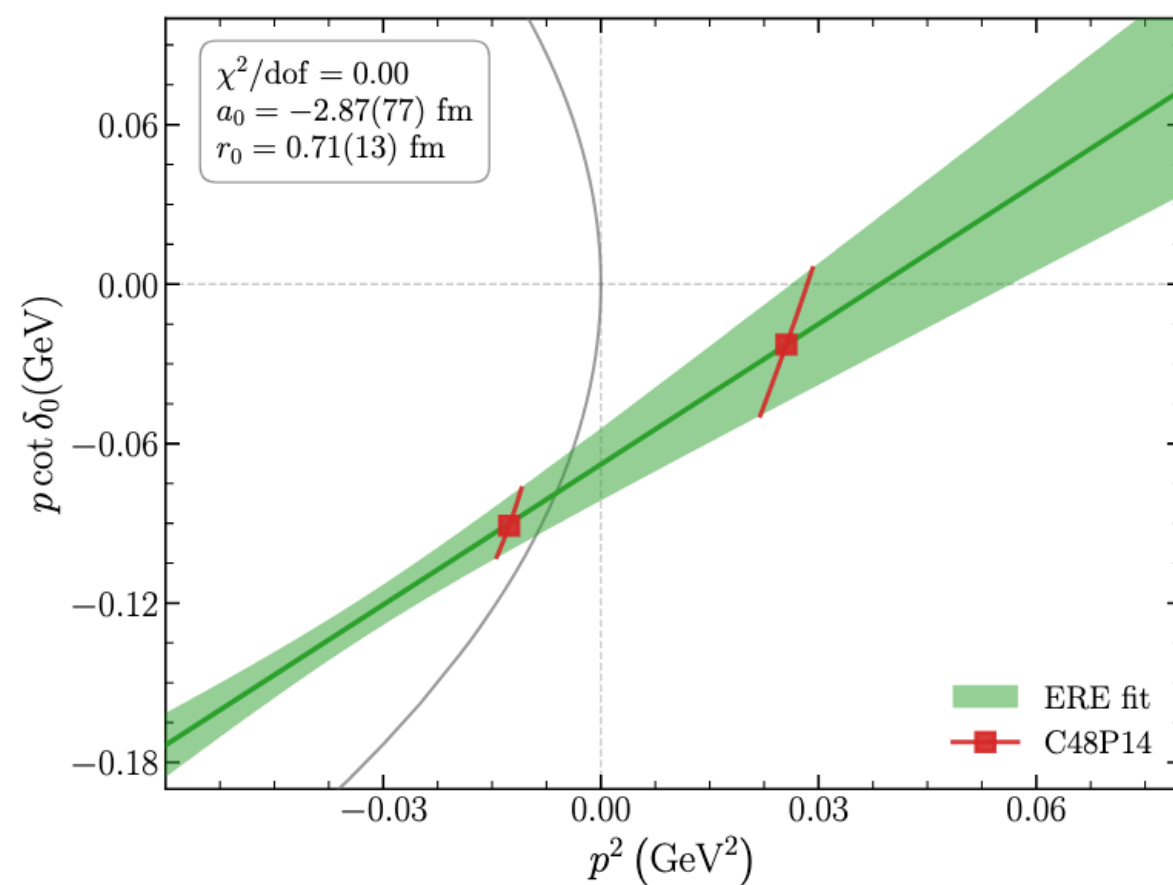
(d) $M_\pi \approx 320$ MeV,
 $a = 0.05187$ fm ($L = 48$)

Preliminary results for $\Xi_{cc}\bar{K}$ ($I = 0$)

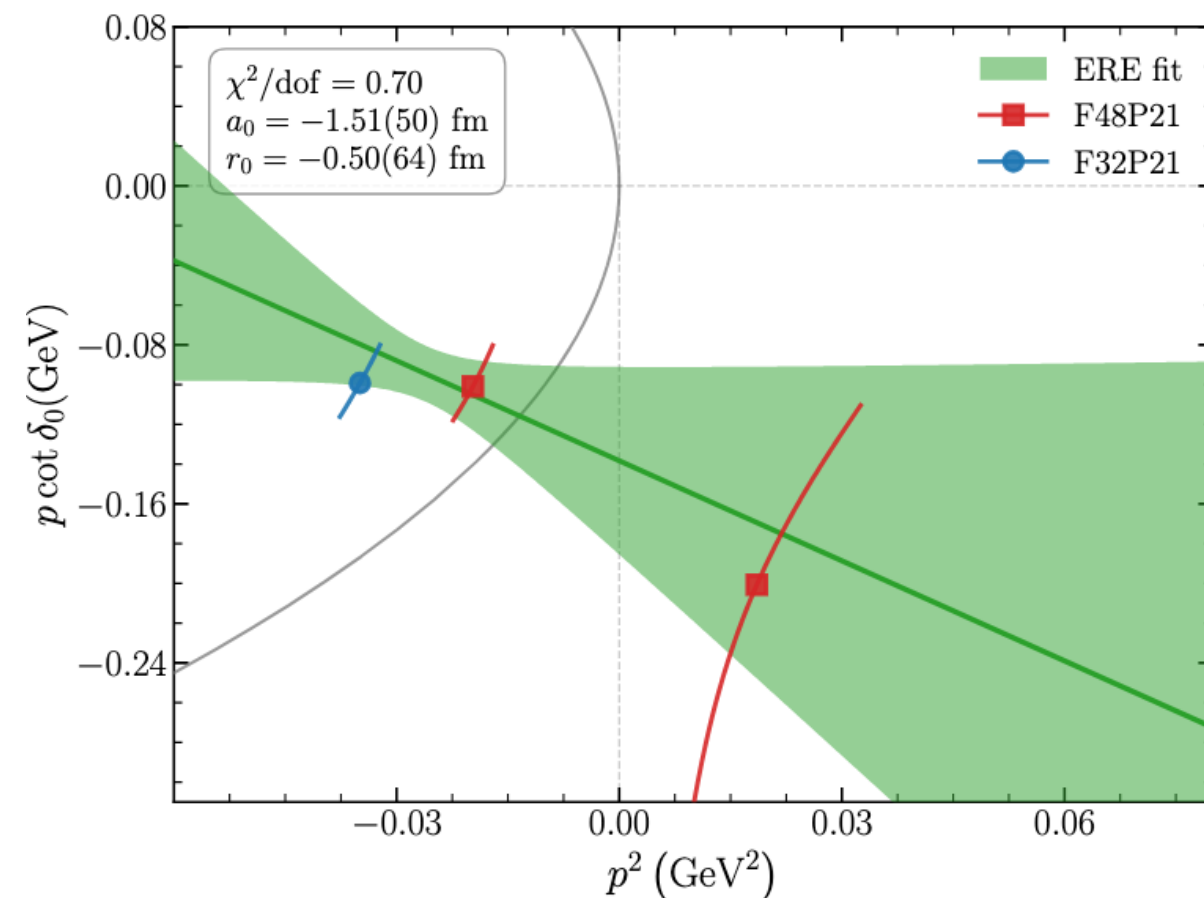
Scattering analysis

$$p \cot \delta_0 = \frac{1}{a_0} + \frac{1}{2}r_0 p^2 + \mathcal{O}(p^4) \quad t_l^{(J)} \sim \frac{1}{p \cot \delta_l^{(J)} - ip}$$

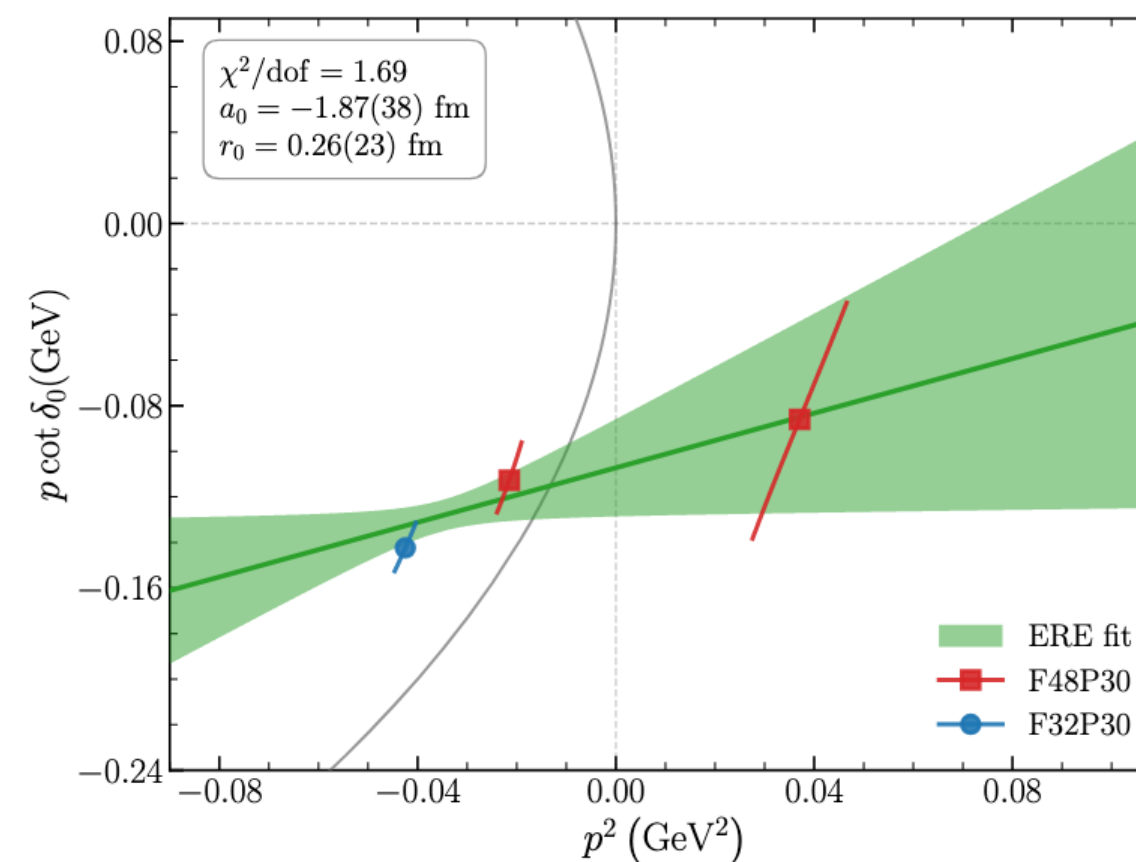
Ensemble Group	a_0 (fm)	r_0 (fm)	p_B^2 (GeV ²)	E_B (MeV)	χ^2/dof
$M_\pi \approx 140$ MeV, $a = 0.105$ fm ($L = 48$)	-2.87(77)	0.71(13)	-0.0064(23)	7.3(2.6)	0.00
$M_\pi \approx 210$ MeV, $a = 0.077$ fm ($L = 32, 48$)	-1.51(50)	-0.50(64)	-0.0131(38)	15.4(4.5)	0.70
$M_\pi \approx 300$ MeV, $a = 0.077$ fm ($L = 32, 48$)	-1.87(38)	0.26(23)	-0.0130(36)	14.4(4.0)	1.69
$M_\pi \approx 320$ MeV, $a = 0.052$ fm ($L = 48$)	-1.35(24)	0.21(14)	-0.0256(65)	27.7(7.1)	0.00



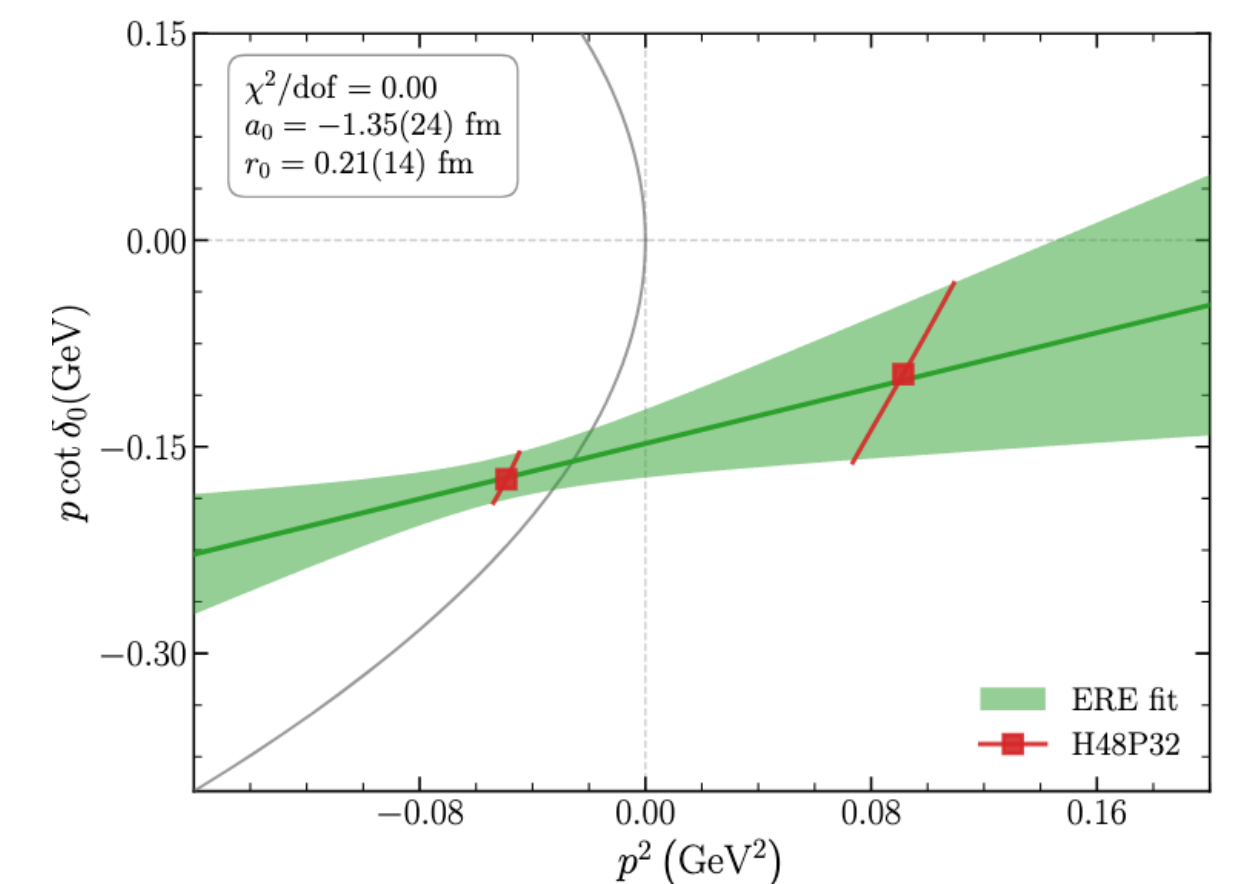
(a) $M_\pi \approx 140$ MeV, $a = 0.105$ fm ($L = 48$)



(b) $M_\pi \approx 210$ MeV, $a = 0.077$ fm ($L = 32, 48$)

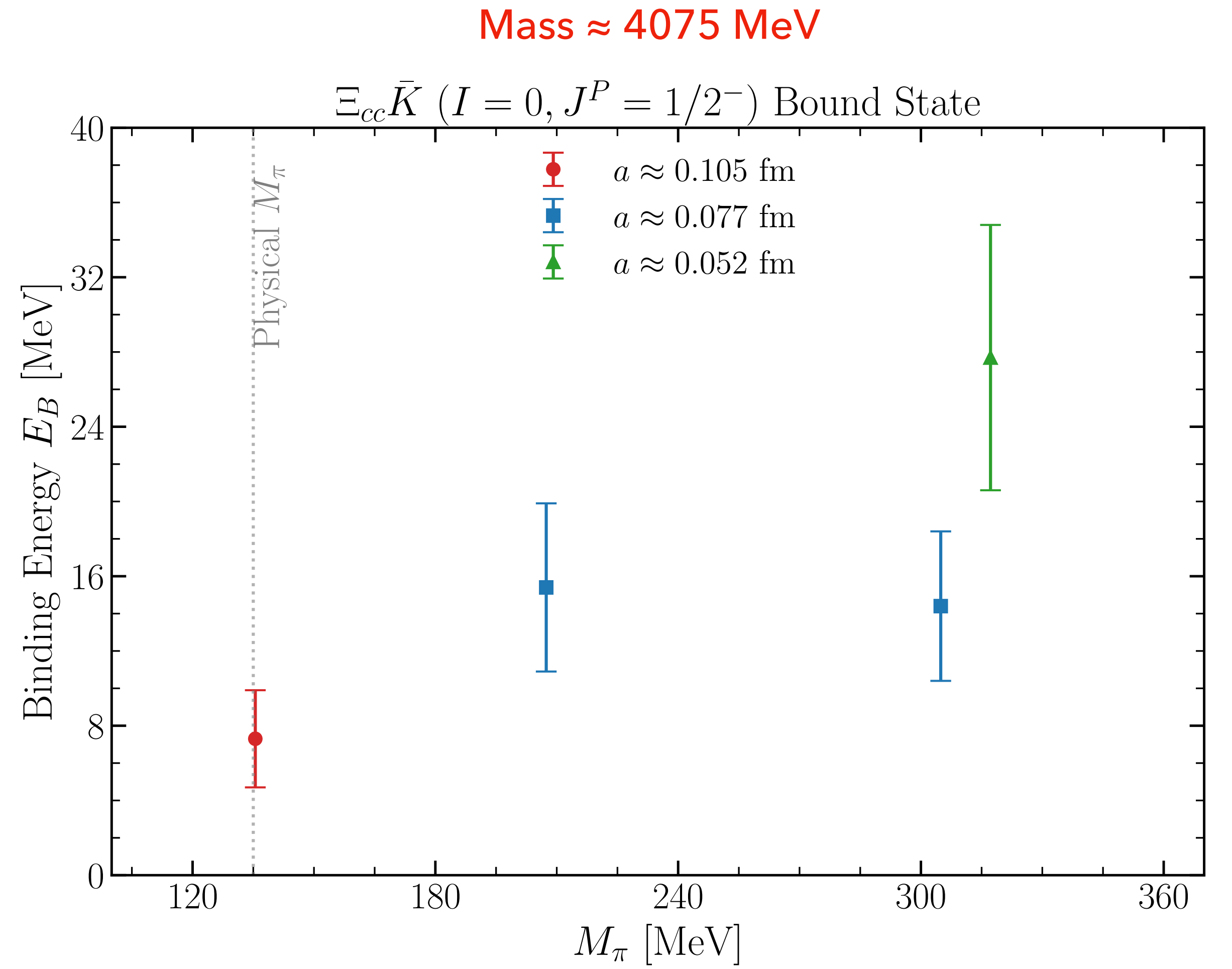
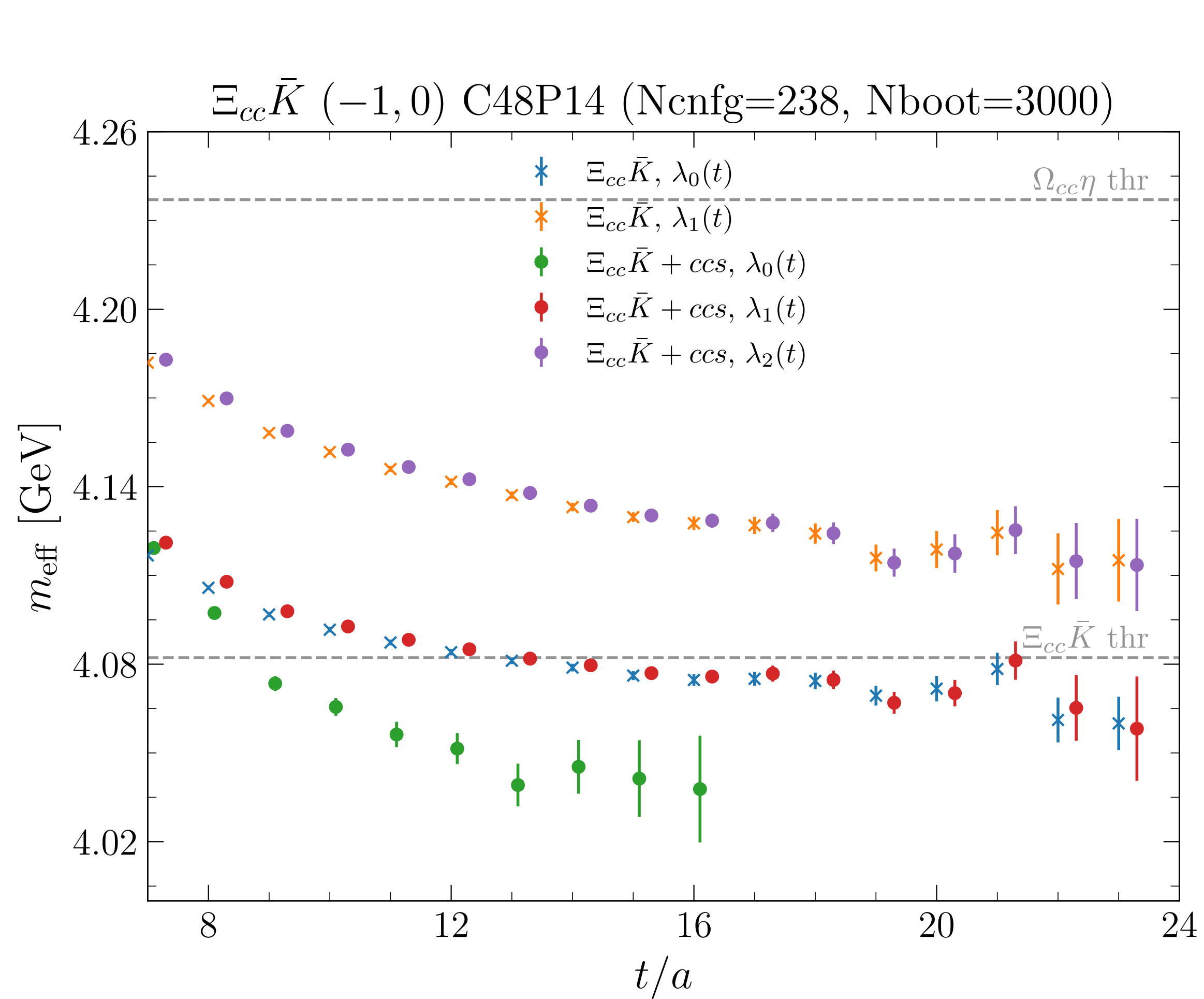


(c) $M_\pi \approx 300$ MeV, $a = 0.077$ fm ($L = 32, 48$)



(d) $M_\pi \approx 320$ MeV, $a = 0.052$ fm ($L = 48$)

Preliminary results for $\Xi_{cc}\bar{K}$ ($I = 0$)



Summary

(S, I)	Processes	Connected(C)/ Disconnected(D)	(S, I)	Relation to $D\phi$ scattering
✓ $(-2, \frac{1}{2})$	$\Omega_{cc}\bar{K} \rightarrow \Omega_{cc}\bar{K}$	C	$(2, \frac{1}{2})$	$D_s K \rightarrow D_s K$
$(-1, 1)$	$\Omega_{cc}\pi \rightarrow \Omega_{cc}\pi$	C	$(1, 1)$	$D_s\pi \rightarrow D_s\pi$
	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$			$DK \rightarrow DK$
	$\Omega_{cc}\pi \rightarrow \Xi_{cc}\bar{K}$			$D_s\pi \rightarrow DK$
✓ $(-1, 0)$	$\Xi_{cc}\bar{K} \rightarrow \Xi_{cc}\bar{K}$	D	$(1, 0)$	$DK \rightarrow DK$
	$\Omega_{cc}\eta \rightarrow \Omega_{cc}\eta$			$D_s\eta \rightarrow D_s\eta$
	$\Xi_{cc}\bar{K} \rightarrow \Omega_{cc}\eta$			$DK \rightarrow D_s\eta$
✓ $(1, 0)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 0)$	$D\bar{K} \rightarrow D\bar{K}$
✓ $(1, 1)$	$\Xi_{cc}K \rightarrow \Xi_{cc}K$	C	$(-1, 1)$	$D\bar{K} \rightarrow D\bar{K}$
$(0, \frac{1}{2})$	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$	D	$(0, \frac{1}{2})$	$D\pi \rightarrow D\pi$
	$\Xi_{cc}\eta \rightarrow \Xi_{cc}\eta$			$D\eta \rightarrow D\eta$
	$\Omega_{cc}K \rightarrow \Omega_{cc}K$			$D_s\bar{K} \rightarrow D_s\bar{K}$
	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\eta$			$D\pi \rightarrow D\eta$
	$\Xi_{cc}\pi \rightarrow \Omega_{cc}K$			$D\pi \rightarrow D_s\bar{K}$
	$\Xi_{cc}\eta \rightarrow \Omega_{cc}K$			$D\eta \rightarrow D_s\bar{K}$
✓ $(0, \frac{3}{2})$	$\Xi_{cc}\pi \rightarrow \Xi_{cc}\pi$	C	$(0, \frac{3}{2})$	$D\pi \rightarrow D\pi$

- **S-wave scattering lengths.**
- **A virtual state** in $(S, I) = (1, 0)$ channel.
- **A bound state** in $(S, I) = (-1, 0)$ channel.
- Examination of the validity of HDA symmetry.
- Determination of LECs in BChPT.
- Better understanding of double-heavy baryon spectroscopy.

Thank you!